

# Update on intra-nuclear cascade models

[Mostly on the new eta production in INCLXX]

**Jean-Christophe David**



# Plan

- ❑ A few words about Binary Cascade and Bertini Cascade
- ❑  $\eta(\omega)$  in INCL++

# Binary Cascade

**From Gunter Folger**

For Binary Cascade and Binary Light Ion Cascade,  
there has been no development in the last year.

**Geant 4**

21st Collaboration Meeting  
12-16 September 2016  
Ferrara, Italy

Update on intra-nuclear cascade models

# Updates and Plans for Bertini Cascade

- For 10.3
  - complete extension of kaon interactions from  $\sim 5$  to  $\sim 15$  GeV
    - required the addition of 8- and 9-body final state partial cross sections, and inclusion of data up to 32 GeV to get correct behavior
    - reactions enabled:  $K^+$ ,  $K^-$ ,  $K^0$ ,  $K^0_{\text{bar}}$  on  $p$ ,  $n$
  - no longer do filtering of low energy gamma-nuclear final states by default: too time-consuming
- For 10.4
  - re-tune gamma-nuclear with larger data set
  - re-examine giant dipole physics
  - examine de-excitation code for possible bug: may be the cause of observed over-production of low energy neutrons



## Plan (2)

- A few words about Binary Cascade and Bertini Cascade
  
- $\eta(\omega)$  in INCL++
  - Introduction
  - Motivations
  - Inputs:
    - $\sigma_R$  (production, scattering, absorption)
    - features of the reaction products (particles, E,  $\theta$ )
    - in-medium Potential
    - Decay
  - Results

# Introduction

## INCL++ (INCLXX)

- a reaction code in Geant4
  - INC ( $\sim 10$  MeV  $\rightarrow$  10-15 GeV)
  - followed by a de-excitation code
  
  - until 2010-2011  $\rightarrow$  2-3 GeV
  - Then, with Multipion channels  $\rightarrow$  10-15 GeV
  
  - However other particles are produced
    - $\eta, \omega, \dots$       2016
    - K, Y                2017
- $\rightarrow$  Minor roles, but New Physics

# Motivations

## Why $\eta$ , $\omega$ ?

- a necessary step toward K, Y
- what's the role in  $\pi$  production? (decay product)
- source of dileptons (= clean information of nuclear matter)
- to study rare decays violating a conservation law

# Inputs

- Inputs:
  - $\sigma_R$  (production, scattering, absorption)
  - features of the reaction products (particles, E,  $\theta$ )
  - in-medium Potential
  - Decay

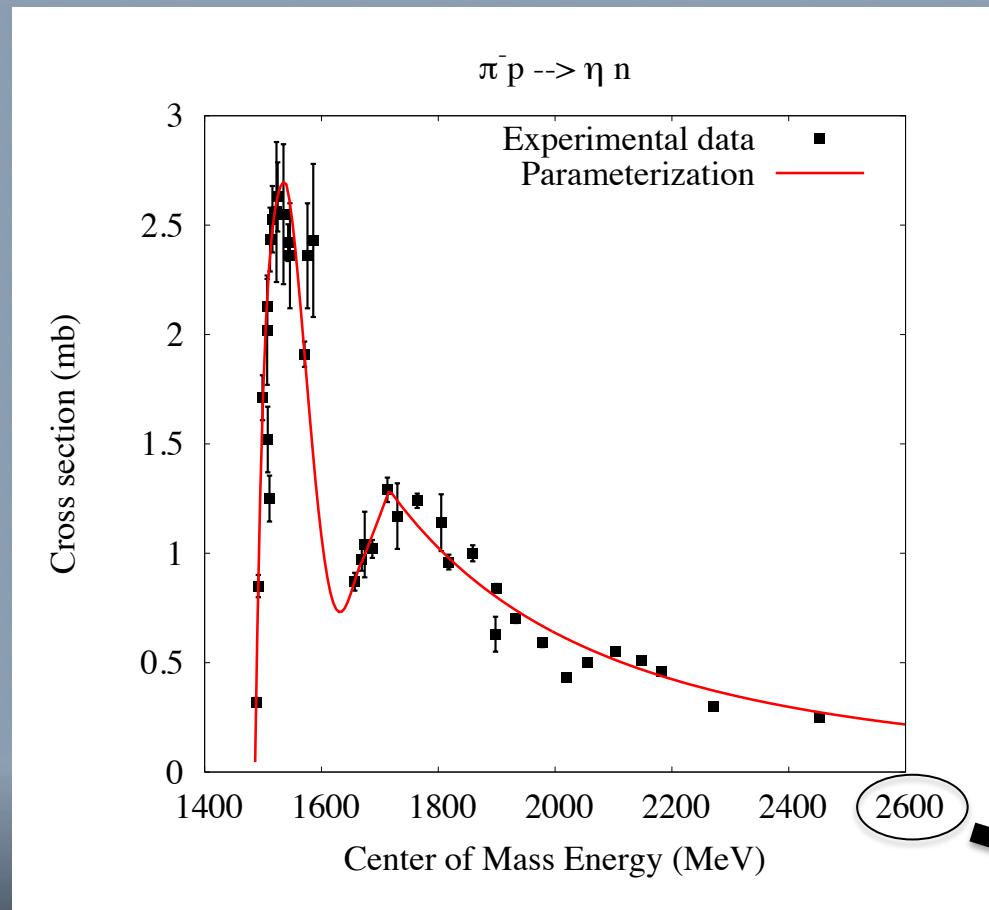
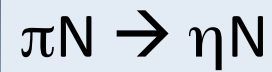


## Inputs

$$\pi N \rightarrow \eta N$$

$$NN \rightarrow \eta + X$$

## Inputs

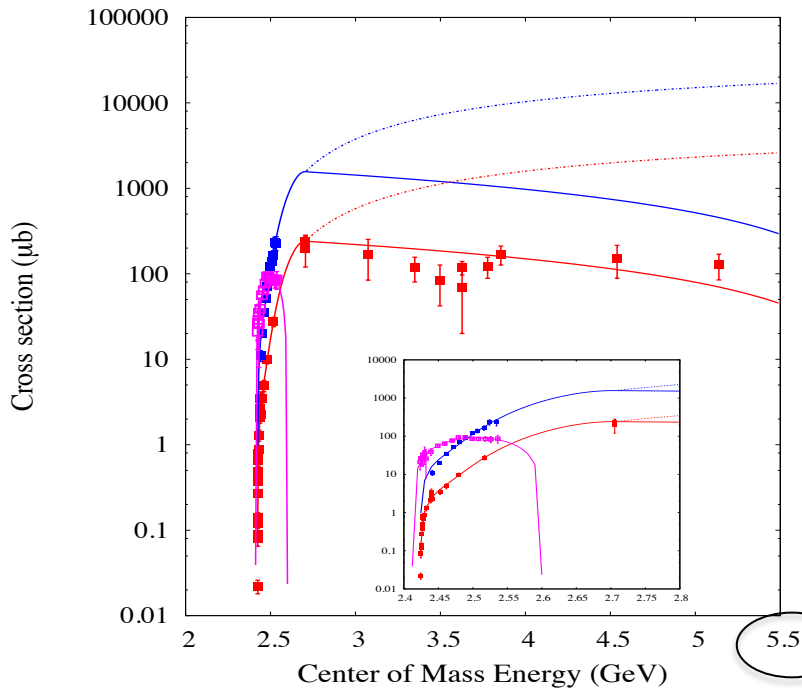


Fit on exp. data

## Inputs

NN  $\rightarrow$   $\eta$  + X

pp  $\rightarrow$  pp $\eta$  - Experimental data ■  
                   Parameterization —  
 pn  $\rightarrow$  pn $\eta$  - Experimental data ■  
                   Parameterization —  
 pn  $\rightarrow$  d $\eta$  - Experimental data □  
                   Parameterization —  
 pp  $\rightarrow$   $\eta$  + X - Parameterization ⋯  
 pn  $\rightarrow$   $\eta$  + X - Parameterization ⋯



exclusive (NN $\rightarrow$  NN $\eta$ ): Fit on exp.data

inclusive (NN $\rightarrow$   $\eta$  + X): parameterization from Sibirtsev - Z. Phys. A 358, 357 (1997).

case of pn!!!

. Exclusive

At low E

pn = 6.5 pp

At high E

hyp. : same factor

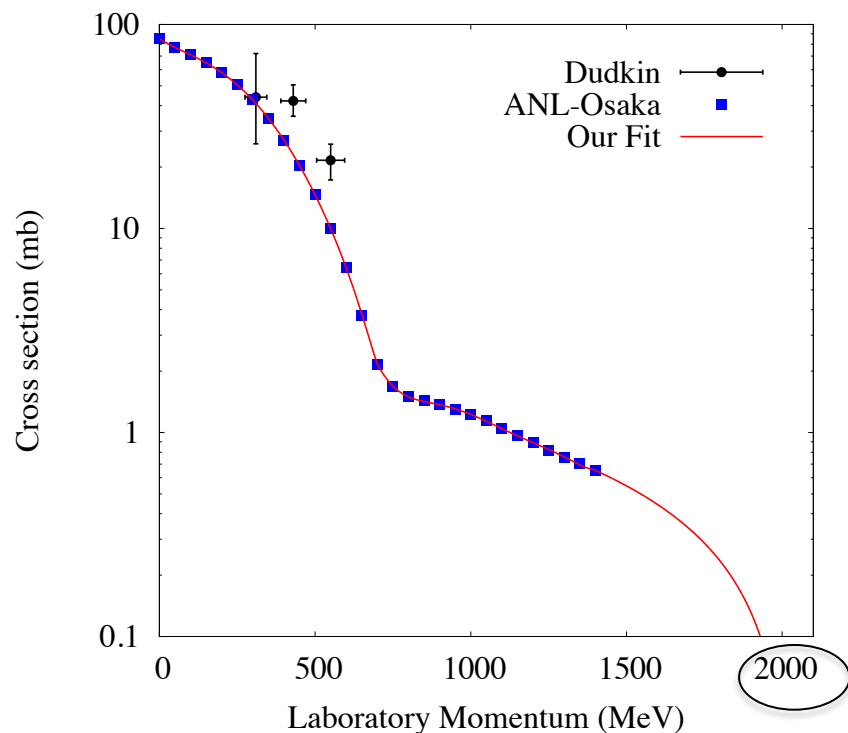
. Inclusive

Same hypothesis...

. pn  $\rightarrow$  d $\eta$  considered as pn  $\rightarrow$  pn $\eta$

$T_p \approx 14$  GeV

## Inputs

 $\eta N \rightarrow \eta N$  $\eta p \rightarrow \eta p$ 

Fit of ANL-Osaka model result

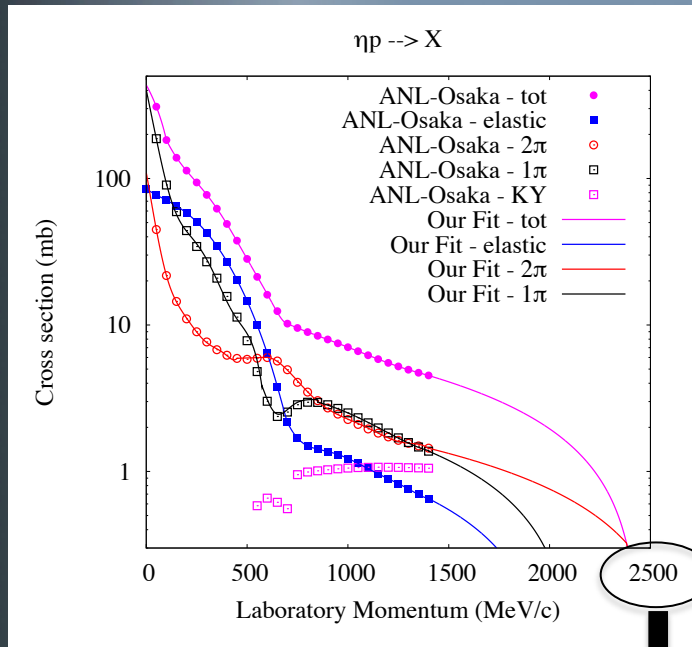
Courtesy of H. Kamano

ANL-Osaka model - PRC 88, 035209 (2013)

a Dynamical Coupled-Channel model  
based on Lagrangians $T_\eta \approx 1.5$   
GeV



## Inputs

 $\eta N \rightarrow X$  $T_\eta \approx 2 \text{ GeV}$ 

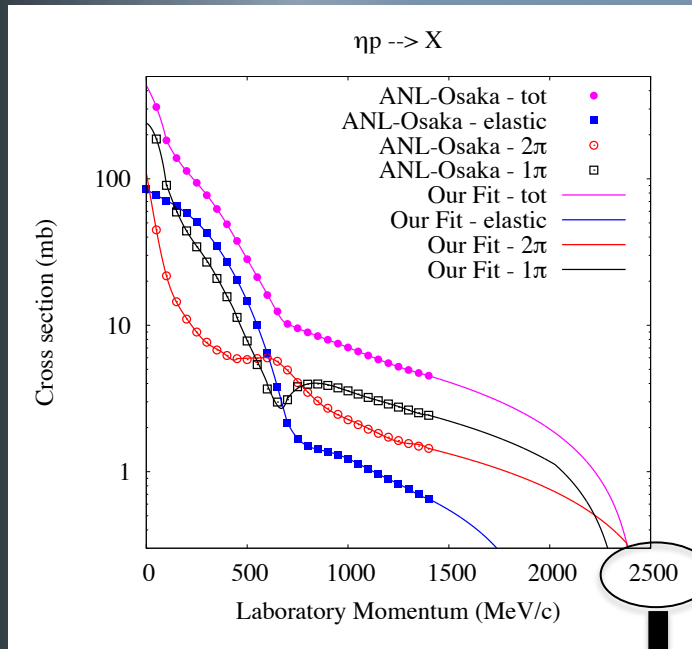
Fit of ANL-Osaka model results  
 Courtesy of H. Kamano

- $\eta N \rightarrow \eta N$  (elastic)
- $\eta N \rightarrow \pi N$
- $\eta N \rightarrow \pi\pi N$

- $\eta N \rightarrow KY$  ( $Y = \Lambda$  or  $\Sigma$ )

up to now no KY in INCL++,  
 so used later

## Inputs

 $\eta N \rightarrow X$  $T_\eta \approx 2 \text{ GeV}$ 

Fit of ANL-Osaka model result  
 Courtesy of H. Kamano

- $\eta N \rightarrow \eta N$  (elastic)
- $\eta N \rightarrow \pi N$
- $\eta N \rightarrow \pi\pi N$

BUT THE RESULTS WILL BE SHOWN  
 WITH

$$\pi N = \text{Tot} - \text{elastic} - \pi\pi N$$

# Inputs

- Inputs:
  - $\sigma_R$  (production, scattering, absorption)
  - **features of the reaction products (particles, E,  $\theta$ )**
  - in-medium Potential
  - Decay

## Inputs

Final products  
 $p - \theta$



- Type of C and D  $\rightarrow$  Obvious or via Clebsch-Gordan
- E  $\rightarrow$  given by the center-of-mass energy and masses
- $\theta \rightarrow$ 
  - No information: Isotropy or Phase-Space
  - Information: Fit on exp.data or Model results



- Type of C,D,...  $\rightarrow$  Clebsch-Gordan or model
- E,  $\theta \rightarrow$  Phase-Space

**Geant 4**



Final products  
 $p - \theta$

Inputs

$\eta$

$\pi N \rightarrow \eta N$

Fit data

$NN \rightarrow \eta + X$

Phase space

$\eta N \rightarrow \eta N$

Fit Model

$\eta N \rightarrow \pi N$

Fit Model

$\eta N \rightarrow \pi\pi N$

Phase space

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Final products  
 $p - \theta$

Inputs

$\eta$

$\pi N \rightarrow \eta N$

Fit data

$NN \rightarrow \eta + X$

Phase space

$\eta N \rightarrow \eta N$

Fit Model

$\eta N \rightarrow \pi N$

Fit Model

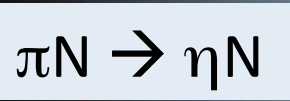
$\eta N \rightarrow \pi\pi N$

Phase space

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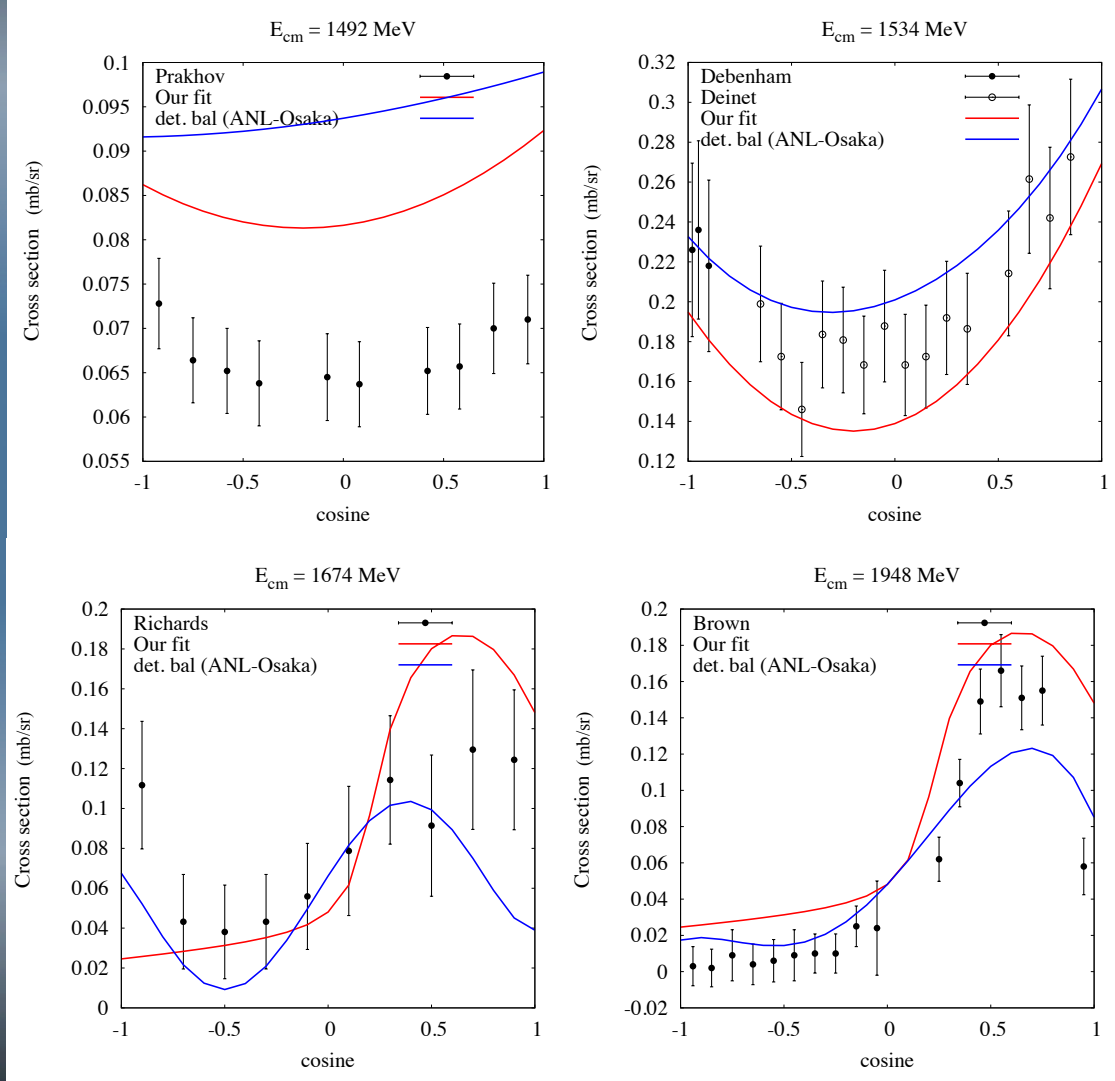
# Inputs

Fit on exp.



Reminder:  
Only the shape is important!

NB: ANL-Osaka model could be used also



Fit on model

Inputs

Final products  
 $p - \theta$

$\eta N \rightarrow \eta N$

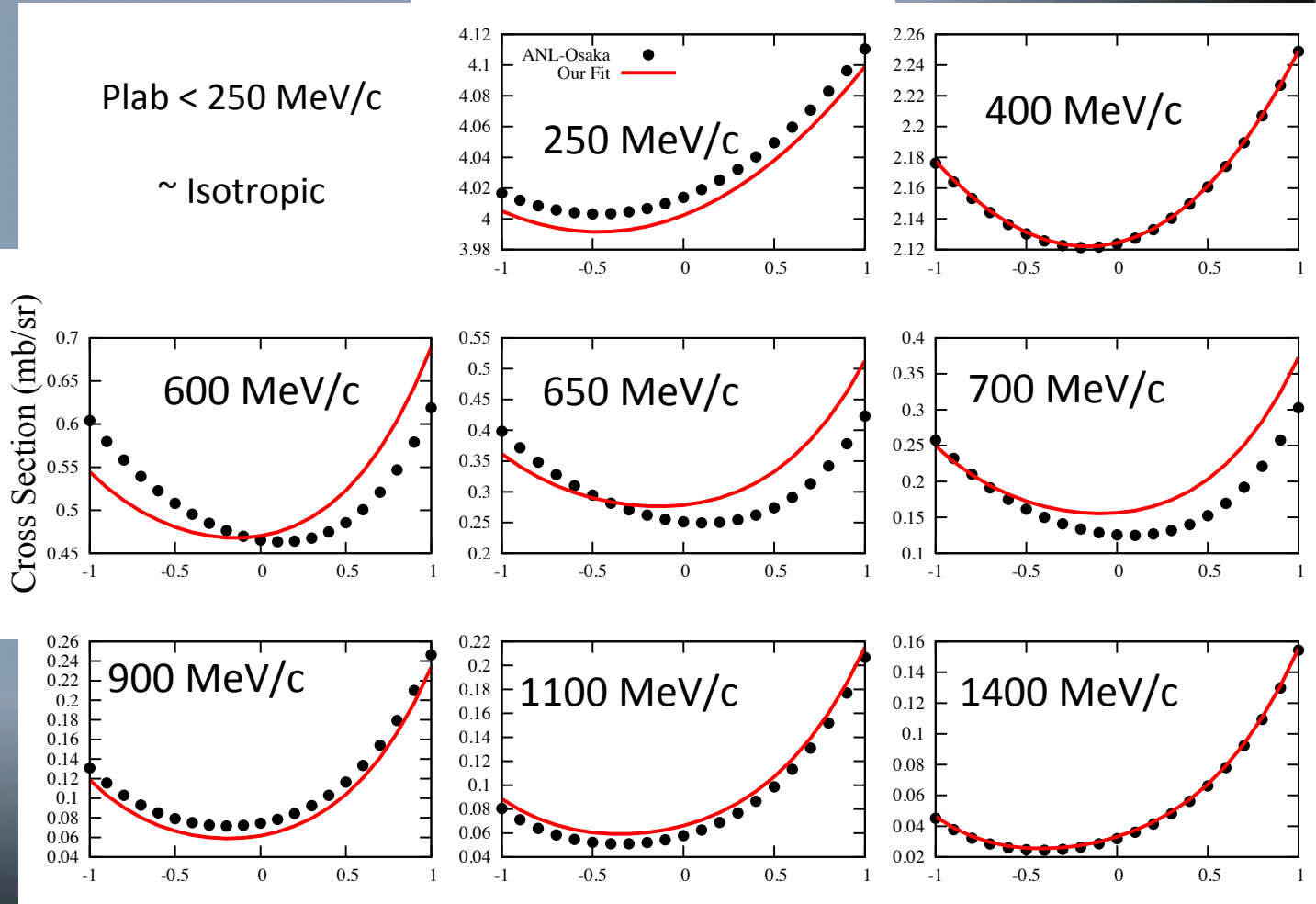
$P_{lab} > 250 \text{ MeV}/c$

Fit with polynomials  
( $p, \theta$ ) of  $d\sigma/d\Omega$   
from ANL-Osaka Model

Courtesy of H. Kamano

Inputs

ANL-Osaka ●  
Our Fit —





Fit on model

Inputs

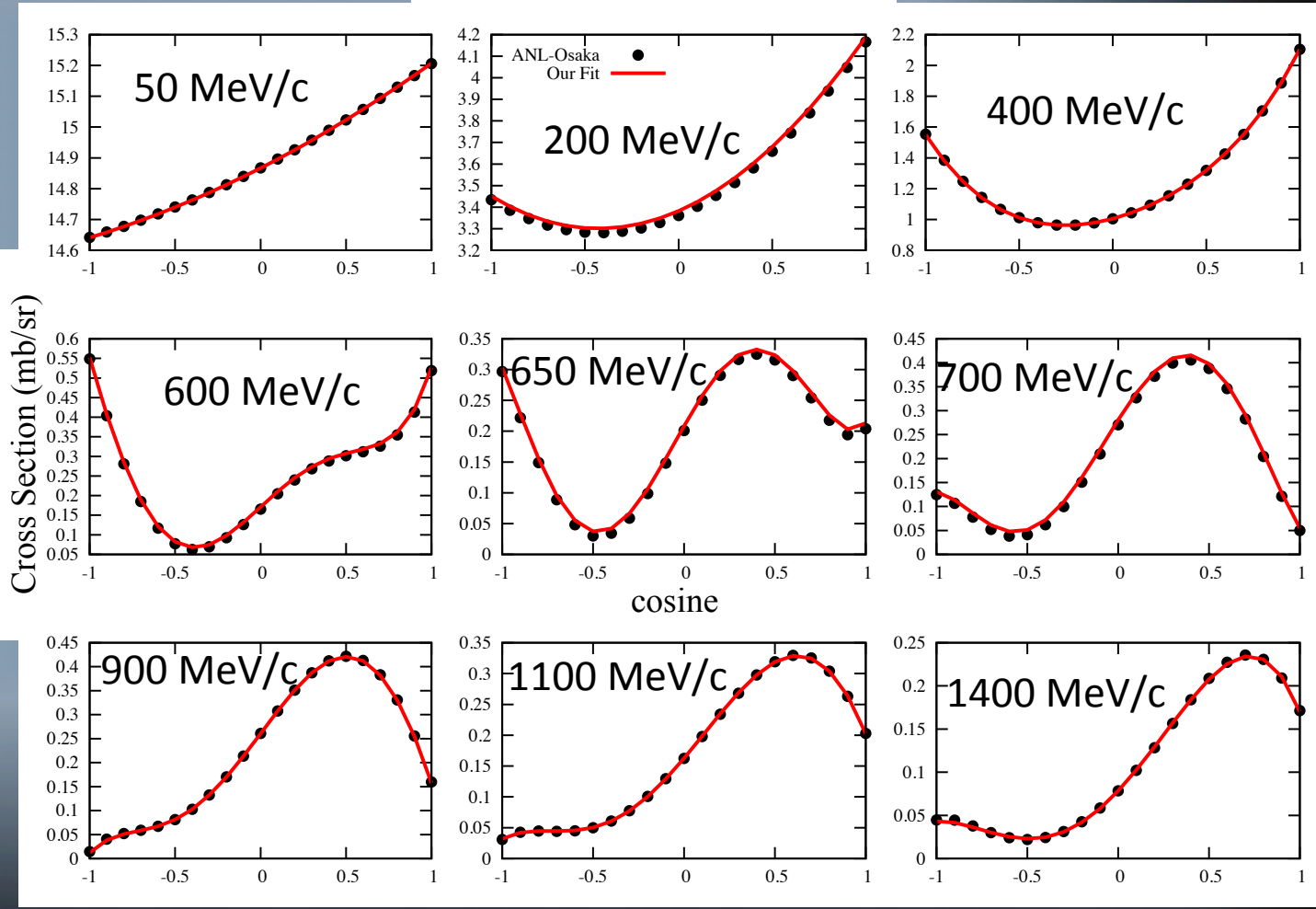
Final products  
 $p - \theta$

$\eta N \rightarrow \pi N$

Fit with polynomials  
( $p, \theta$ ) of  $d\sigma/d\Omega$   
from ANL-Osaka Model

Courtesy of H. Kamano

ANL-Osaka ●  
Our Fit —

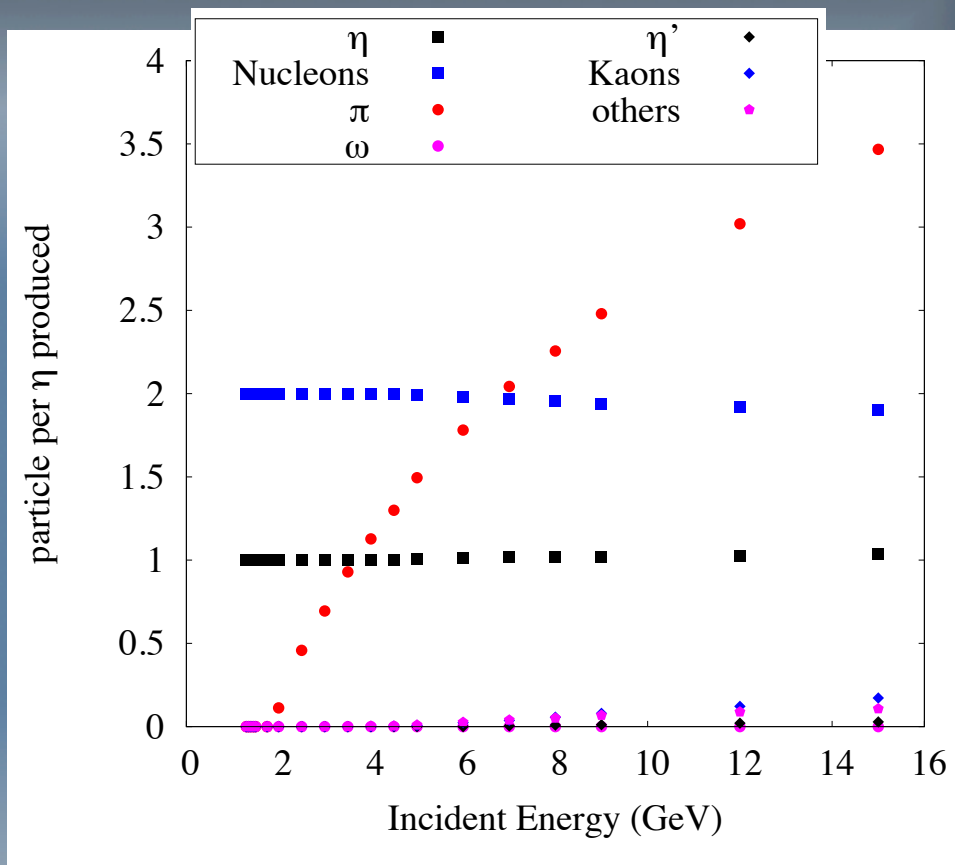


## Inputs

$NN \rightarrow \eta + X$

When 1  $\eta$

2 nucleons  
up to 3-4  $\pi$



From Fritiof (geant4 10.1-p02)

# Inputs

# Final products $p - \theta$

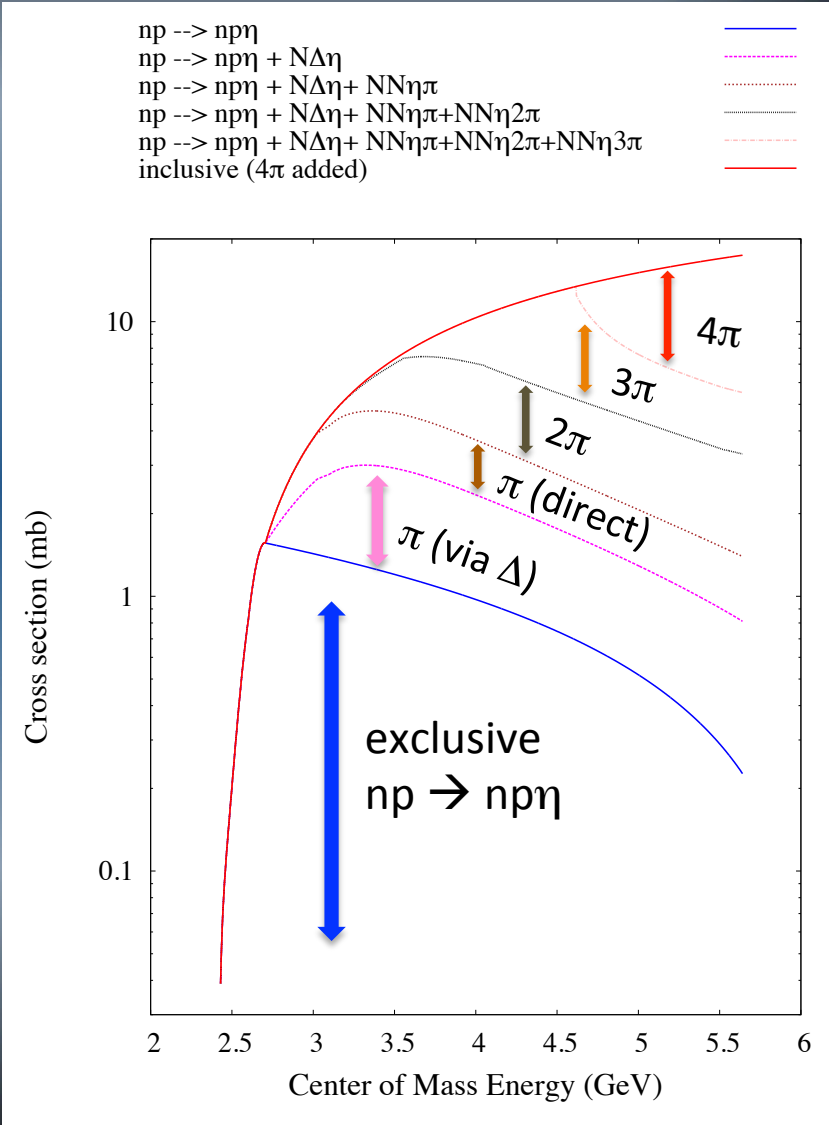
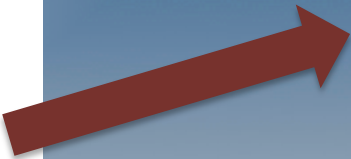
$NN \rightarrow \eta + X$

When 1  $\eta$

2 nucleons  
up to 3-4

So multipion applied

$NN \rightarrow NN\eta + x\pi$   
(from  $NN \rightarrow NN + x\pi$ )



# Inputs

- Inputs:
  - $\sigma_R$  (production, scattering, absorption)
  - features of the reaction products (particles, E,  $\theta$ )
  - **in-medium Potential**
  - Decay

## Inputs

 $\eta$ 

Few information

3 values tested

- $V = 1.5 V_{\pi 0}$
- $V = V_{\pi 0}$
- **$V = 0$**



# Inputs

- Inputs:
  - $\sigma_R$  (production, scattering, absorption)
  - features of the reaction products (particles, E,  $\theta$ )
  - in-medium Potential
  - **Decay**

## Inputs

 $\eta$ 

- $2\gamma$       39.72 %
- $3\pi^0$       32.93 %
- $\pi^+\pi^-\pi^0$     23.10 %
- $\pi^+\pi^-\gamma$       4.25 %

→  $\eta$  decays only after being emitted

→ Decay can be switched off (option using a time threshold)

# Results

## $\eta$ production

- $\pi^+(680 \text{ MeV}/c) + X$  (Ye. S. Golubeva et al, NPA 562 (1993) 389)
  - ❖  $\sigma_{\eta\text{-production}}$  with several targets
  - ❖  $T_{\eta}$  spectrum ( $X = {}^{12}\text{C}$ )
- $p(1 \text{ GeV}) + X$  (Ye. S. Golubeva et al, NPA 562 (1993) 389)
  - ❖  $\sigma_{\eta\text{-production}}$  with several targets
  - ❖  $T_{\eta}$  spectrum ( $X = {}^{11}\text{B}$ )
- $p(3.5 \text{ GeV}) + \text{Nb}$  (G. Agakishiev et al., PRC 88, 024904 (2013))
  - ❖ transverse momentum distribution

Threshold

and

Subthreshold

Reactions

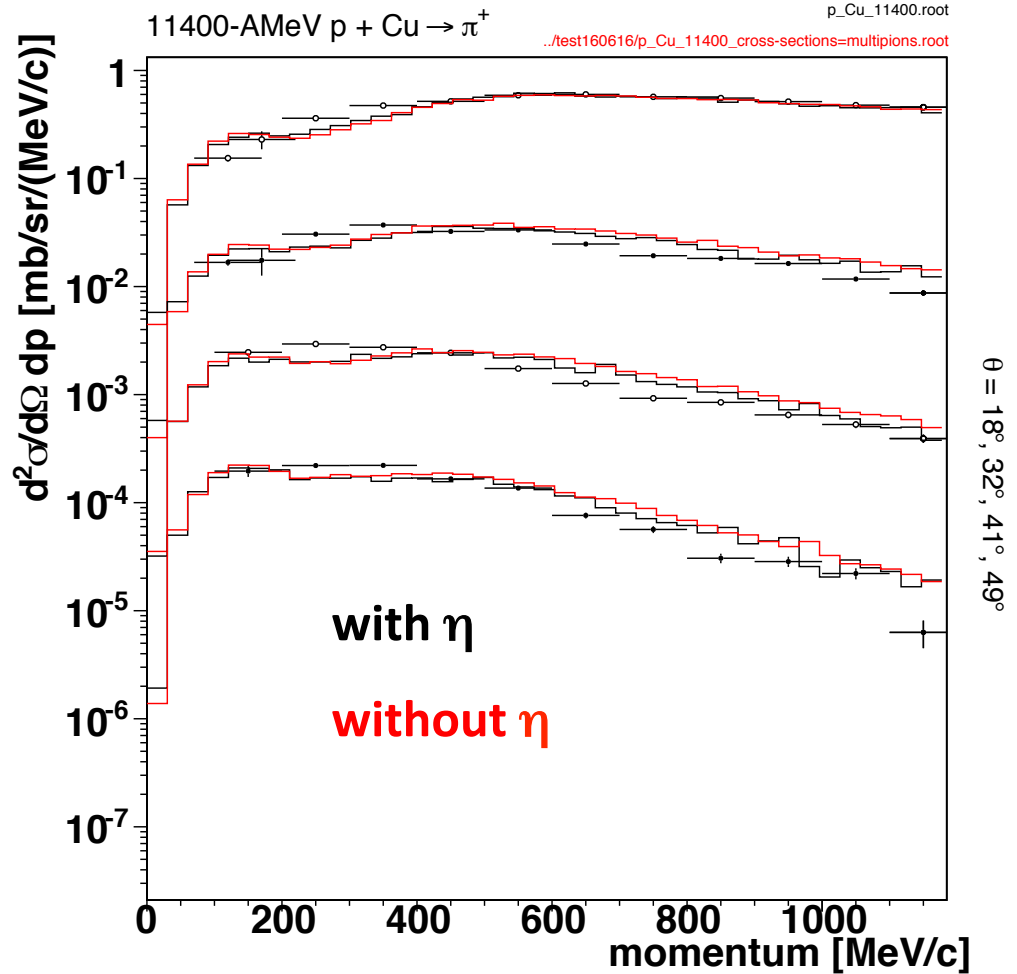
**Geant 4**

# Results

## $\pi$ production

HARP experiment

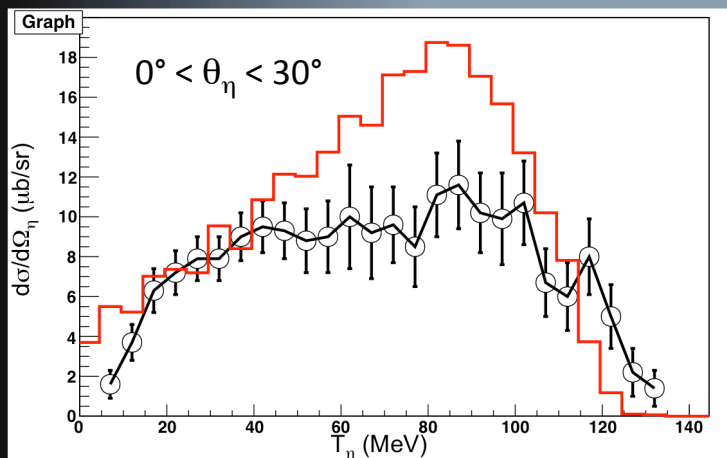
$\eta$ : no effect on  $\pi$  production



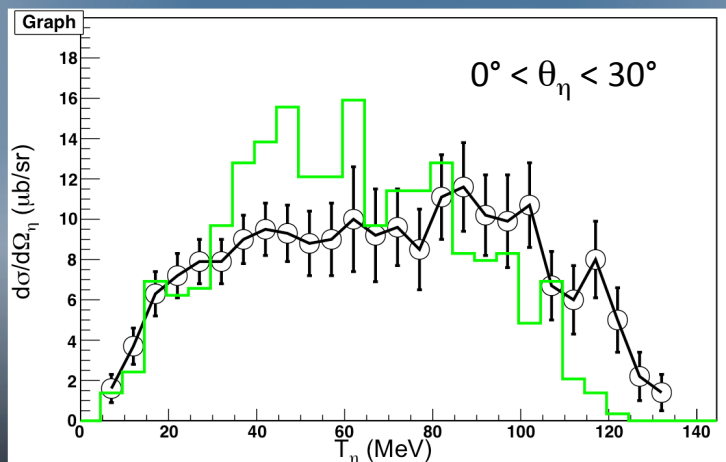
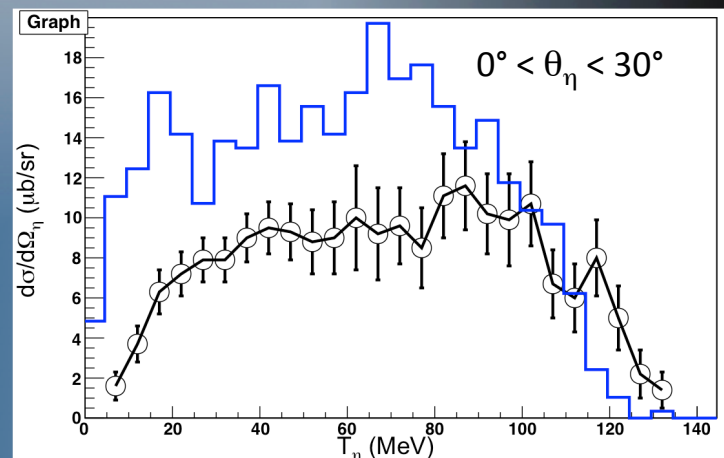
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# Results

$\pi^+(680 \text{ MeV}/c) + {}^{12}\text{C}$   
( $\eta$  Spectrum)



$V_\eta \sim 50 \text{ MeV}$   
 $V_\eta \sim 33 \text{ MeV}$   
 $V_\eta = 0 \text{ MeV}$



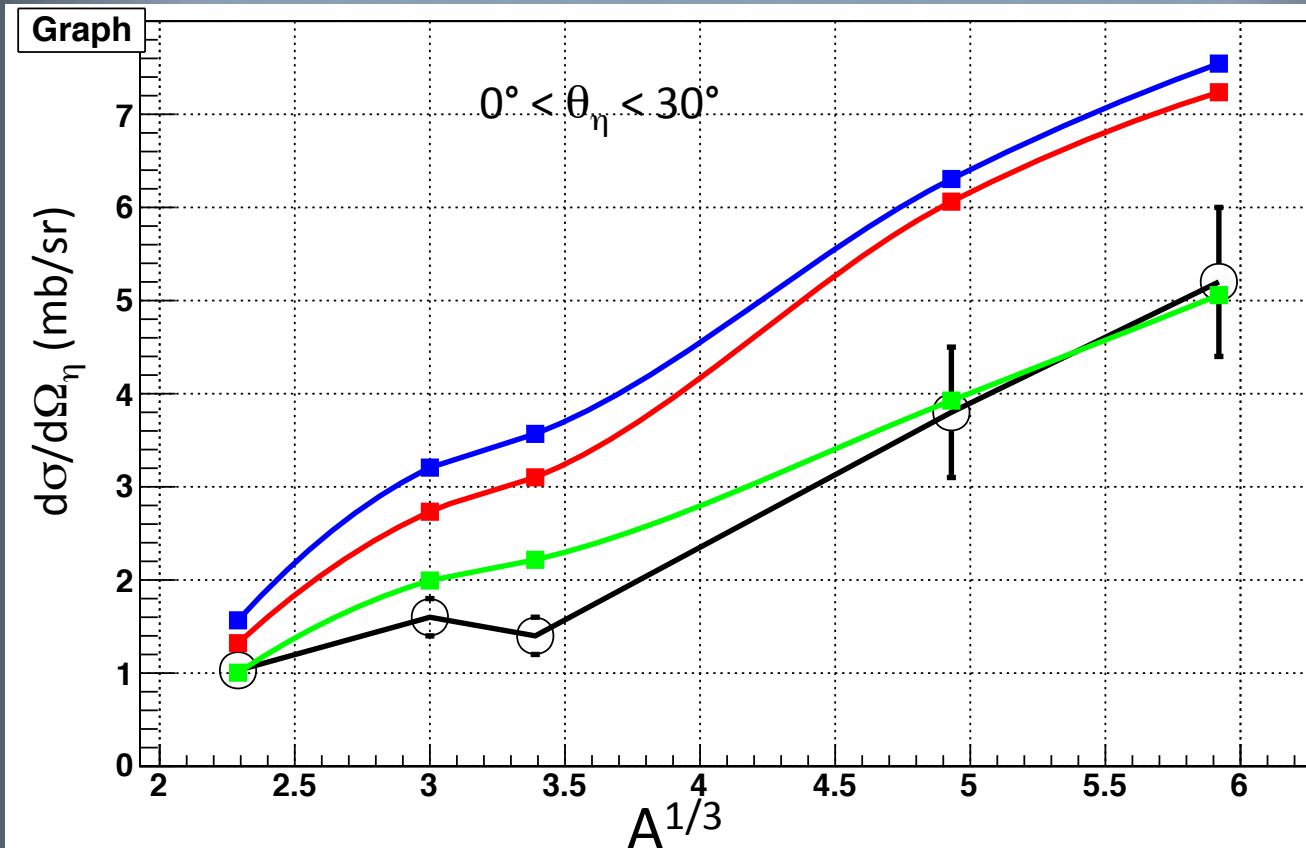
Better Results with  $V=0$ !

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# Results

$\pi^+(680 \text{ MeV}/c) + X$   
( $\eta$  Production)



Good Results  
with  $V=0$

Whatever the  
target

Geant 4

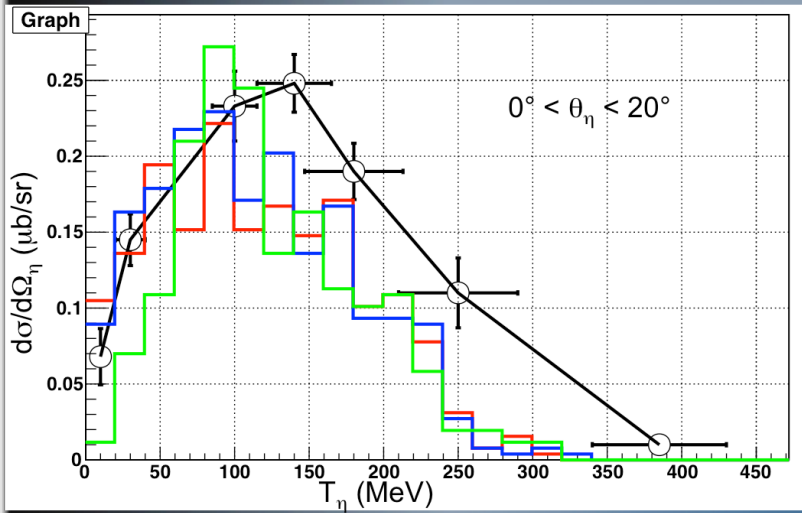
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$V_\eta \sim 50 \text{ MeV}$   
 $V_\eta \sim 33 \text{ MeV}$   
 $V_\eta = 0 \text{ MeV}$

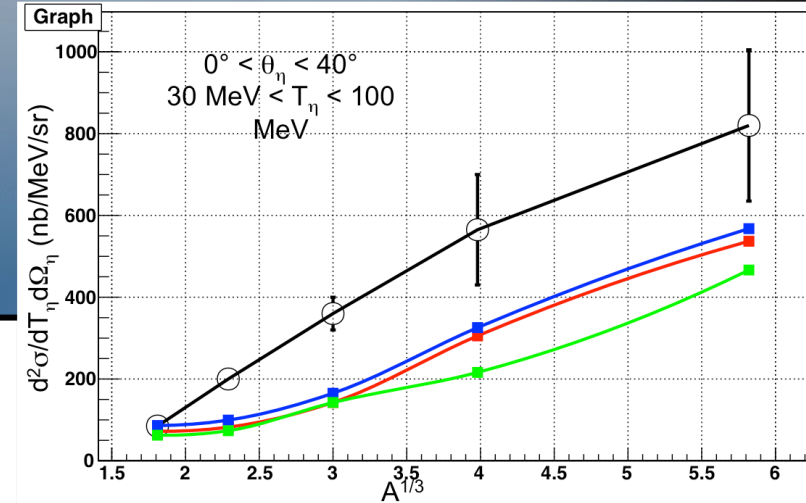
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# Results

p(1 GeV) +  $^{11}\text{B}$



p(1 GeV) + X



$V=0$ , not better not worse...

BUT subthreshold reaction  $\rightarrow$  more tricky (momentum distribution of the Ns...)

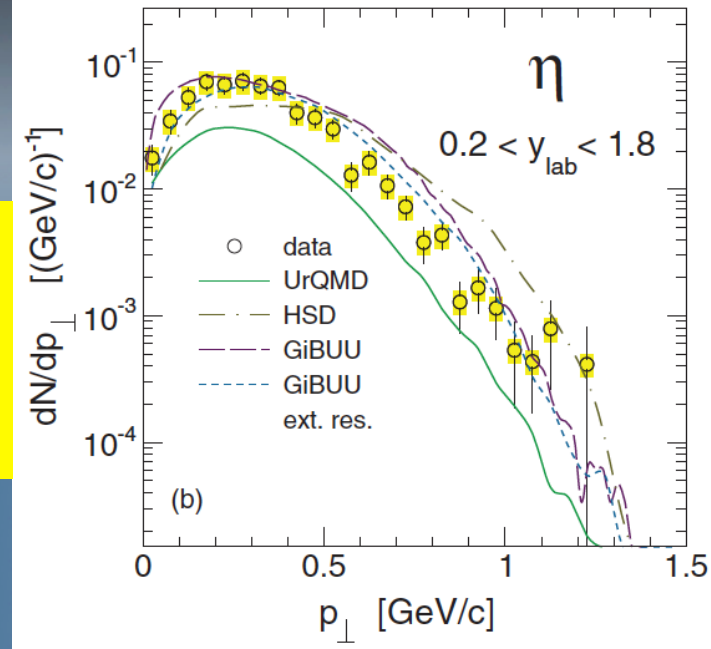
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# Results

Phys.Rev. C 88, 024904 (2013)

p(3.5 GeV) + Nb

data:  
HADES  
collaboration

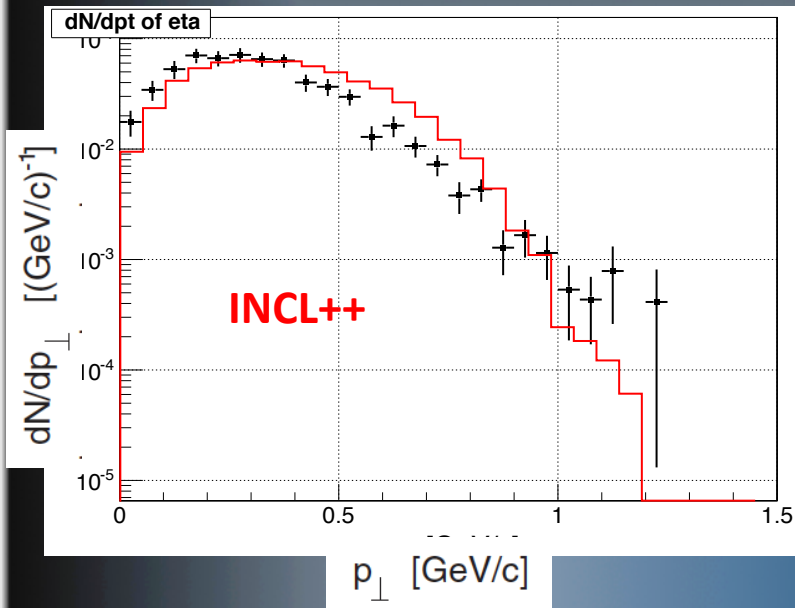


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Thanks to  
R. Holzmann and B. Ramstein  
(exp. data)

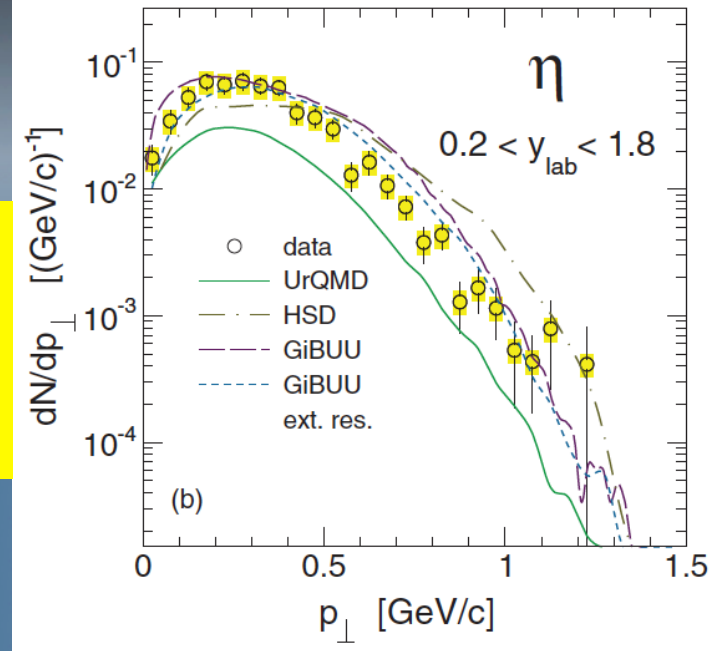
## Results

Phys.Rev. C 88, 024904 (2013)



p(3.5 GeV) + Nb

data:  
HADES  
collaboration



**Pretty good result**  
compared to  
experiment and other models

Geant 4

## Conclusions

- $\eta$  is in INCL++ and gives good results
- A first implementation in Geant4 works
- Some (minor) changes until the *official* version
- $\omega$  is almost in INCL++ and soon in Geant4  
(unfortunately no data to test it)
- See you next year for the strangeness (PhD - Jason Hirtz)



*Thank you!*

*Grazie!*

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Update on intra-nuclear cascade models

# backup

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Update on intra-nuclear cascade models

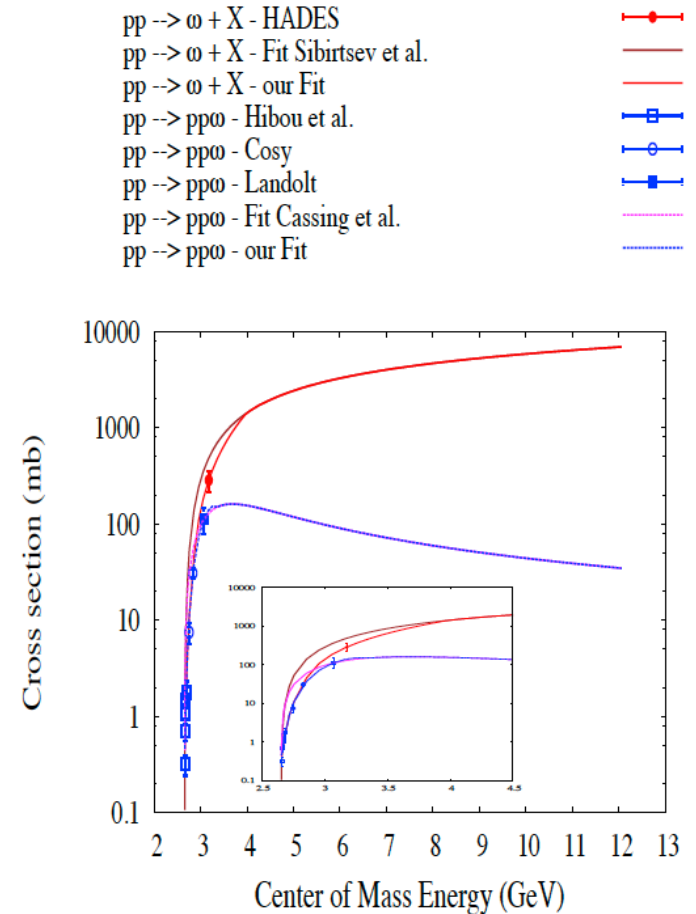
## Inputs

$$NN \rightarrow \omega + X$$

exclusive ( $NN \rightarrow NN\eta$ ):  
 parameterization from Cassing  
 - NPA 604, 455-465 (1996)  
 modified (low energies)

inclusive ( $NN \rightarrow \eta + X$ ):  
 parameterization from Sibirtsev  
 modified (recent datum from  
 HADES - A. Rustamov *et al.*, AIP  
 Conference Proceedings, 1257,  
 736 (2010))

case of pn  
 factor 3



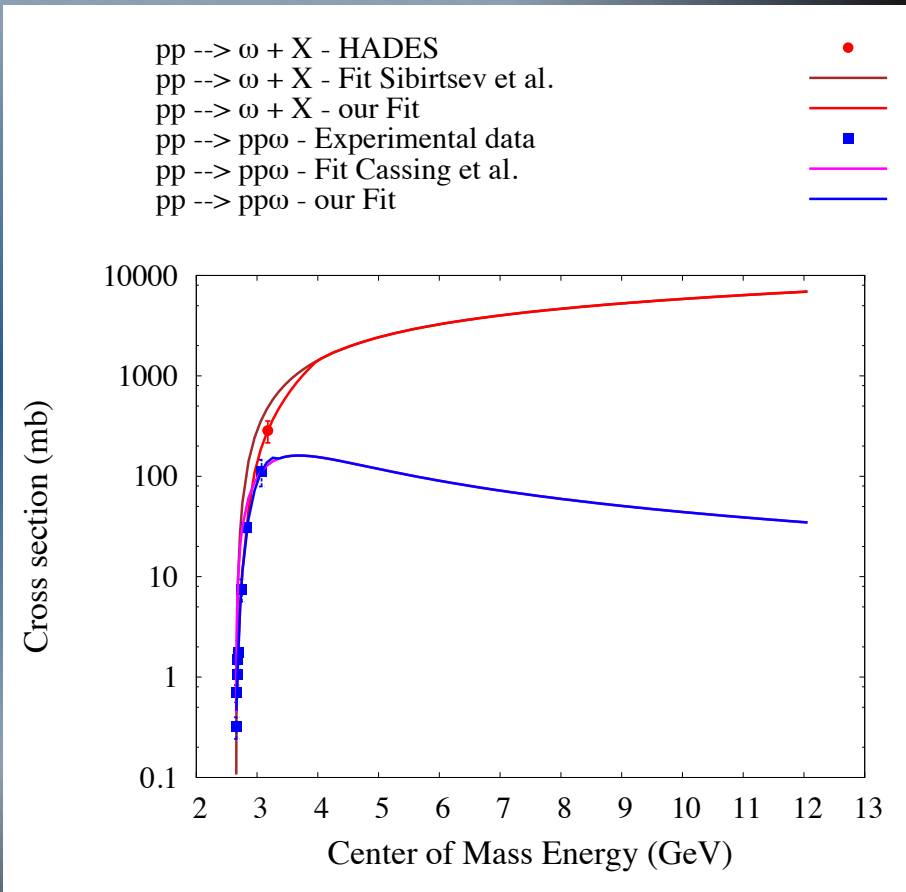
## Inputs

$$NN \rightarrow \omega + X$$

exclusive ( $NN \rightarrow NN\eta$ ):  
 parameterization from Cassing  
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 parameterization from Sibirtsev  
 modified (recent datum from  
 HADES - A. Rustamov *et al.*, AIP  
 Conference Proceedings, 1257,  
 736 (2010))

case of pn  
 factor 3



## Inputs

 $\omega N \rightarrow \omega N$ 

$$\sigma(\omega N \rightarrow \omega N) = 5.4 + 10.^{-0.6} p_{Lab}$$

Lykasov - EPJ A 6, 71 (1999)



## Inputs

 $\omega N \rightarrow \pi N$ 

detailed balance

 $\omega N \rightarrow \pi\pi N$  $\pi\pi N = \text{Inelastic} - \pi N$ 

$$\sigma_{\omega N}^{inelastic} = 20. + 4./p_{Lab}$$

Lykasov - EPJ A 6, 71 (1999)

## Inputs

 $\eta$ 

- $2\gamma$  39.72 %
- $3\pi^0$  32.93 %
- $\pi^+\pi^-\pi^0$  23.10 %
- $\pi^+\pi^-\gamma$  4.25 %

 $\omega$ 

- $\pi^+\pi^-\pi^0$  90.09 %
- $\pi^0\gamma$  8.36 %
- $\pi^+\pi^-$  1.55 %

→ 2 particles: Isotropy --- 3 particles: Phase-Space

→  $\eta$  decays only after being emitted

→ Decay can be switched off (option using a time threshold)