

The many roles of QCD in the exploration of fundamental interactions



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CERN, Theory Department
19 December, 2016

Foreward

- The known fundamental particles and interactions play a double role
 1. they are objects of study, to measure their properties, to test our understanding of the dynamics, and to test the compatibility with existing predictions
 2. they are tools for the discovery of the unknown
- The depth of knowledge we can acquire from (1) defines the strength and power of these tools to accomplish (2)

EW interactions hold the secret of the most puzzling aspects of the SM: *symmetry breaking* and *flavour*

$$\mathcal{L}_{EW} = -\frac{1}{4g^2} W_a^{\mu\nu} W_{\mu\nu}^a - \frac{1}{4g'^2} B^{\mu\nu} B_{\mu\nu} + i \sum_F \bar{F} \gamma_\mu D^\mu F + |D_\mu H|^2$$

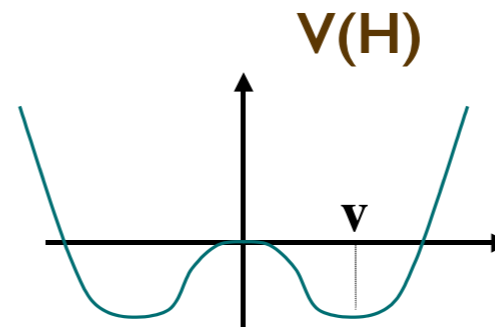
$$- V(H) - Y_u^{ij} \bar{Q}_i H^* u_j^c - Y_d^{ij} \bar{Q}_i H d_j^c - Y_\ell^{ij} \bar{L}_i H \ell_j^c$$

who ordered those ?? *the answer is worth a Nobel prize*

Given the EW lagrangian, however, the study of its dynamics is “straightforward”.

In particular, finding the ground state is a high-school exercise:

$$V_{SM}(H) = -\mu^2 |H|^2 + \lambda |H|^4$$



$$\frac{\partial V_{SM}(H)}{\partial H} \Big|_{H=v} = 0 \quad \text{and} \quad m_H^2 = \frac{\partial^2 V_{SM}(H)}{\partial H \partial H^*} \Big|_{H=v} \Rightarrow$$

$$\begin{aligned} \mu &= m_H \\ \lambda &= \frac{m_H^2}{2v^2} \end{aligned}$$

QCD, in comparison, is conceptually rather dull:

$$\mathcal{L}_{QCD} = -\frac{1}{4g^2} G_{\mu\nu}^a G_a^{\mu\nu} + i \sum_f \bar{q}_f D_\mu \gamma^\mu q_f$$

Its perturbative dynamics is controlled by the scale evolution of the coupling

$$\frac{\partial \alpha_s(\mu^2)}{\partial \log \mu^2} = \beta(\alpha_s)$$

$$\alpha_s = \frac{g^2}{4\pi}$$

$$\langle (gG)^2 \rangle \stackrel{\text{def}}{=} \langle g^2 G_{\mu\nu} G^{\mu\nu} \rangle \simeq 0.5 \text{ GeV}^4$$

$$\langle \bar{\psi}\psi \rangle \simeq (-0.23)^3 \text{ GeV}^3$$

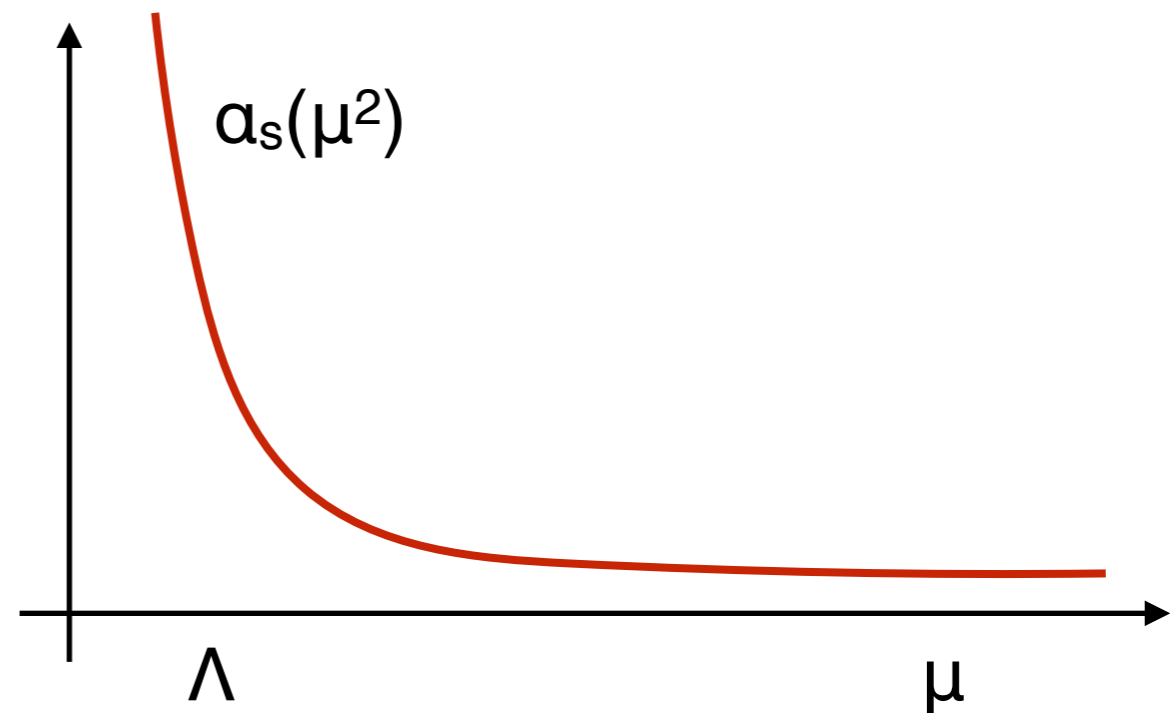
$$\langle (gG)^4 \rangle \simeq 5 : 10 \langle (gG)^2 \rangle^2$$

At the lowest order,

$$\beta(\alpha_s) = -b_0 \alpha_s^2, \quad b_0 = \frac{33 - 2n_f}{12\pi}$$

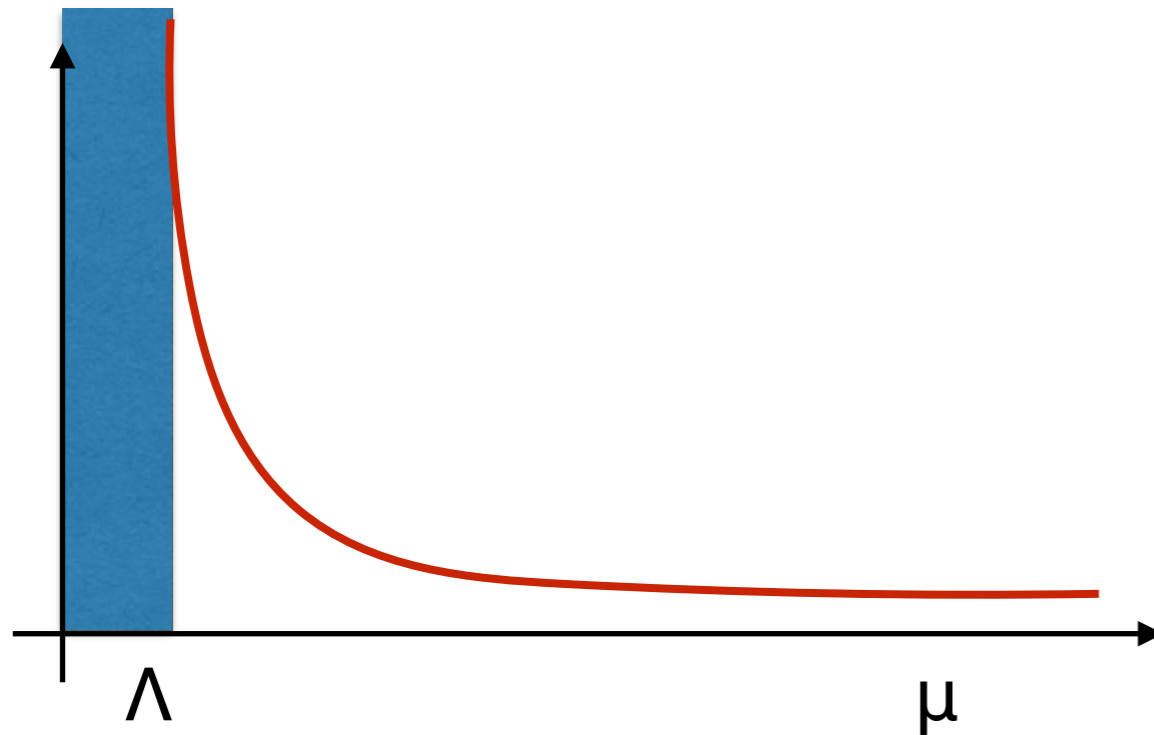
and

$$\alpha_s(\mu^2) = \frac{1}{b_0 \log(\mu^2/\Lambda^2)}$$



See G. Altarelli,
http://pos.sissa.it/archive/conferences/177/002/Corfu2012_002.pdf

The problem is that the “real” world sits in the deep infrared, at $\mu < \Lambda$!!



The identification of the QCD **vacuum state** and the formal proof of its properties (mass gap, confinement, chiral symmetry breaking) is one of the outstanding “millennium” problems, worth a Nobel prize (and loads of money from the Clay foundation*)

* <http://www.claymath.org/sites/default/files/yangmills.pdf>

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What makes QCD highly non-trivial, therefore, is the challenge (intellectual and technical) to develop frameworks that allow up to make quantitative, and precise, predictions for hadronic phenomena, in spite of our limited control from first principles of the vacuum and the spectrum

QCD in the non-PT regime: phenomenological issues interesting “per se”

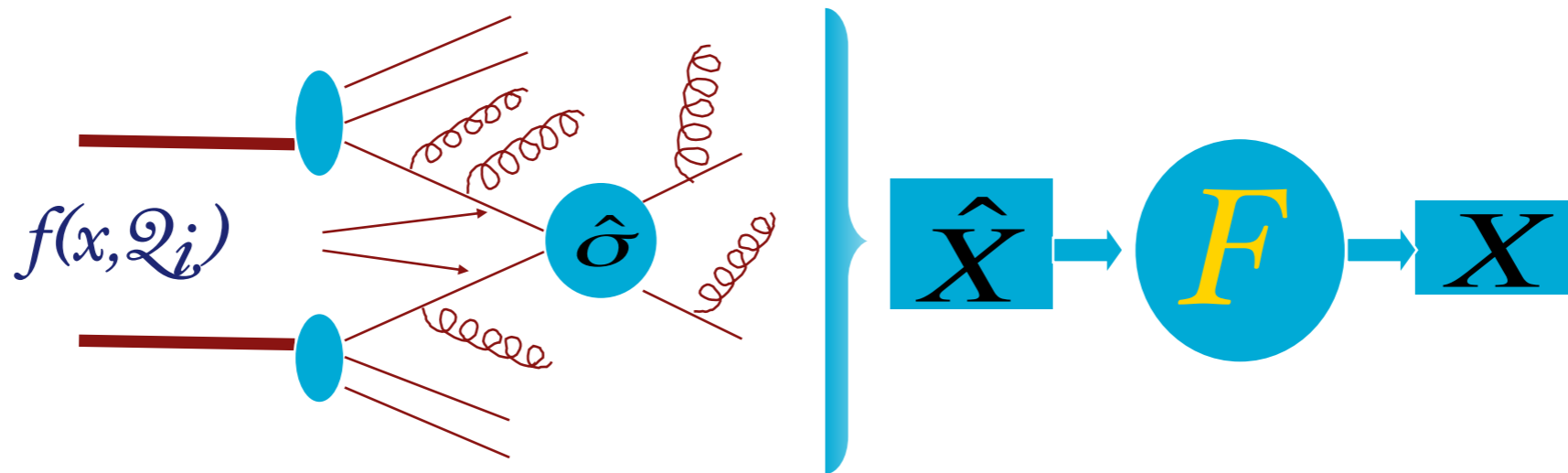
- Issues that used to be classified as “chemistry”, have become exciting fields of research, addressed also using powerful theoretical frameworks such as AdS/CFT or supersymmetry
- They may not be relevant for applications of QCD as a tool to explore the puzzles of the SM, but testify to the richness of the dynamics emerging from QCD
- Examples:
 - Exotic states in the hadronic spectrum: tetra- and pentaquarks, glueballs, ...
 - The phase diagram at finite density and temperature: deconfinement, the quark-gluon plasma, strange matter, the equation of state of neutron stars, ...
 - ...

QCD in the non-PT regime: role in the exploration of the SM and its limits

- Quark flavour physics: extraction of CKM parameters and CP violation, rare decays and FCNC transitions, heavy meson decay dynamics, etc etc: crucial role of non-PT QCD => lattice QCD, HQET, sum rules, ...
- $(g-2)_\mu$: role of light hadrons in the evolution of α_{QED} , light-by-light scattering
- Measurement of α_s and its evolution from
 - hadronic τ decays
 - quarkonium spectroscopy
 - jet shapes in $e^+e^- \rightarrow$ hadrons
- LHC physics => proton structure
- ...

Factorization in hadronic collisions

$$\frac{d\sigma}{dX} = \sum_{j,k} \int_{\hat{X}} f_j(x_1, Q_i) f_k(x_2, Q_i) \frac{d\hat{\sigma}_{jk}(Q_i, Q_f)}{d\hat{X}} F(\hat{X} \rightarrow X; Q_i, Q_f)$$



$f_j(x, Q)$ Parton distribution functions (PDF)

$F(\hat{X} \rightarrow X; Q_i, Q_f)$

- sum over all initial state histories leading, at the scale Q , to:

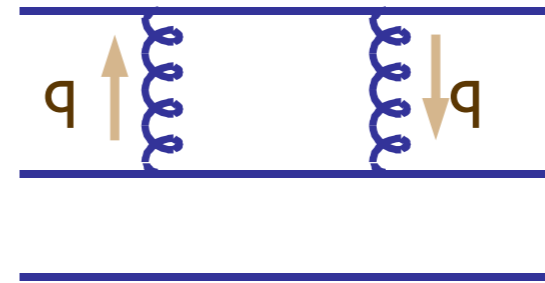
$$\vec{p}_j = x \vec{P}_{proton}$$

- transition from partonic final state to the hadronic observable (hadronization, fragm. function, jet definition, etc)
- Sum over all histories with X in them

Universality of parton densities and factorization, an intuitive picture

Universality of parton densities and factorization, an intuitive picture

- 1) Exchange of **hard gluons** among quarks inside the proton is suppressed by powers of $(m_p/Q)^2$



The diagram shows a proton represented by three horizontal blue lines. Two quarks are shown as vertical lines between the top two blue lines. The left quark has an upward-pointing arrow and is labeled 'q'. The right quark has a downward-pointing arrow and is labeled 'q'. A blue wavy line representing a gluon connects the two quarks. To the right of the diagram, the text $q \gg Q$ is written in red, followed by a red tilde symbol \sim , then the integral $\int_Q^\infty \frac{d^4 q}{q^6}$ in red, another red tilde symbol \sim , and finally $\frac{1}{Q^2}$ in red.

$$q \gg Q \sim \int_Q^\infty \frac{d^4 q}{q^6} \sim \frac{1}{Q^2}$$

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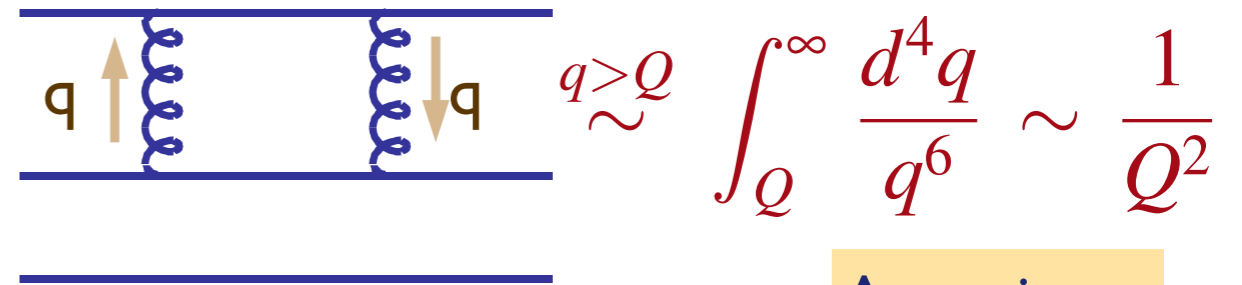


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Assuming asymptotic freedom!

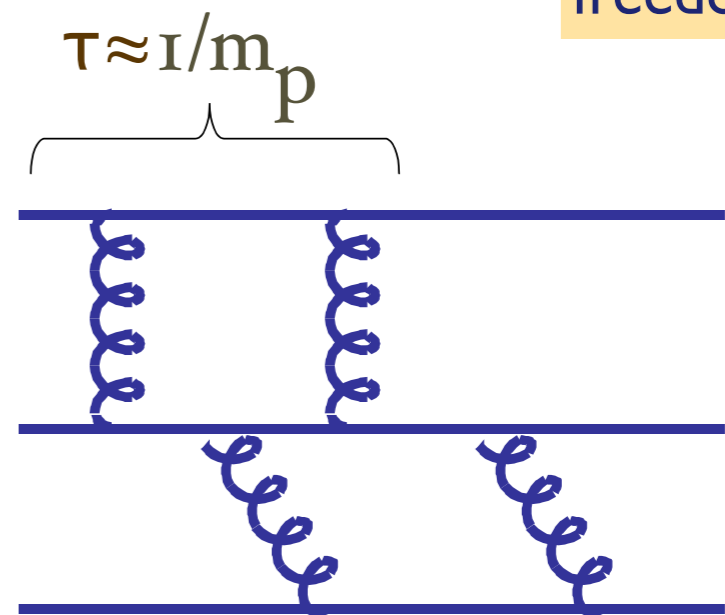
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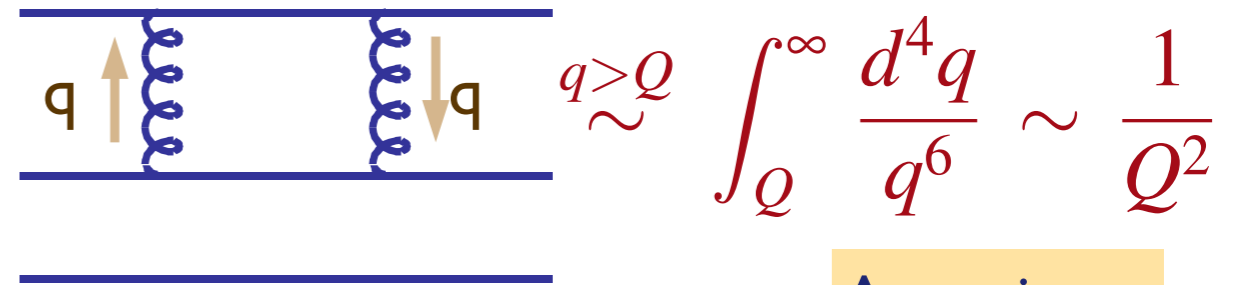
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- 2) Typical time-scale of interactions binding the proton is therefore of $O(1/m_p)$ (in a frame in which the proton has energy E , $\tau = \gamma/m_p = E/m_p^2$)



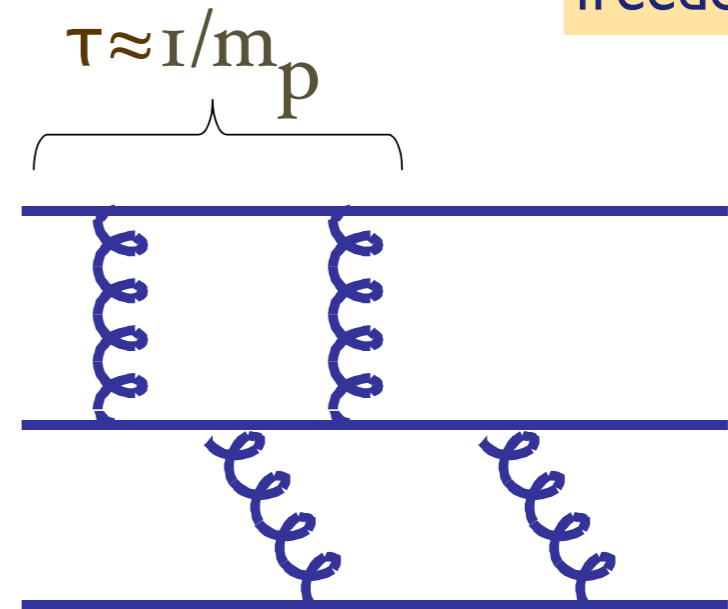
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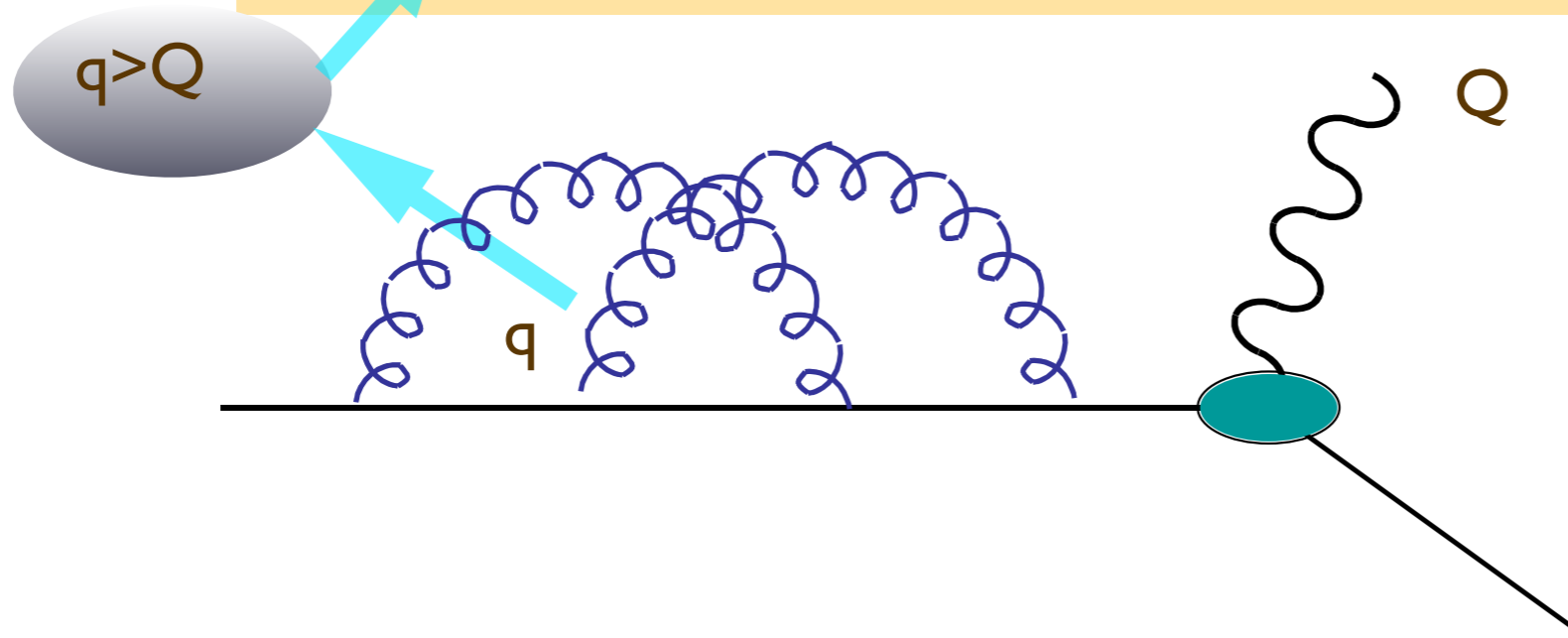
- 3) If a hard probe ($Q \gg m_p$) hits the proton, on a time scale $= 1/Q$, there is no time for quarks to negotiate a coherent response. The struck quark receives no feedback from its pals, and acts as a free particle

As a result, to study inclusive processes at large Q it is sufficient to consider the interactions between the external probe and a single parton:



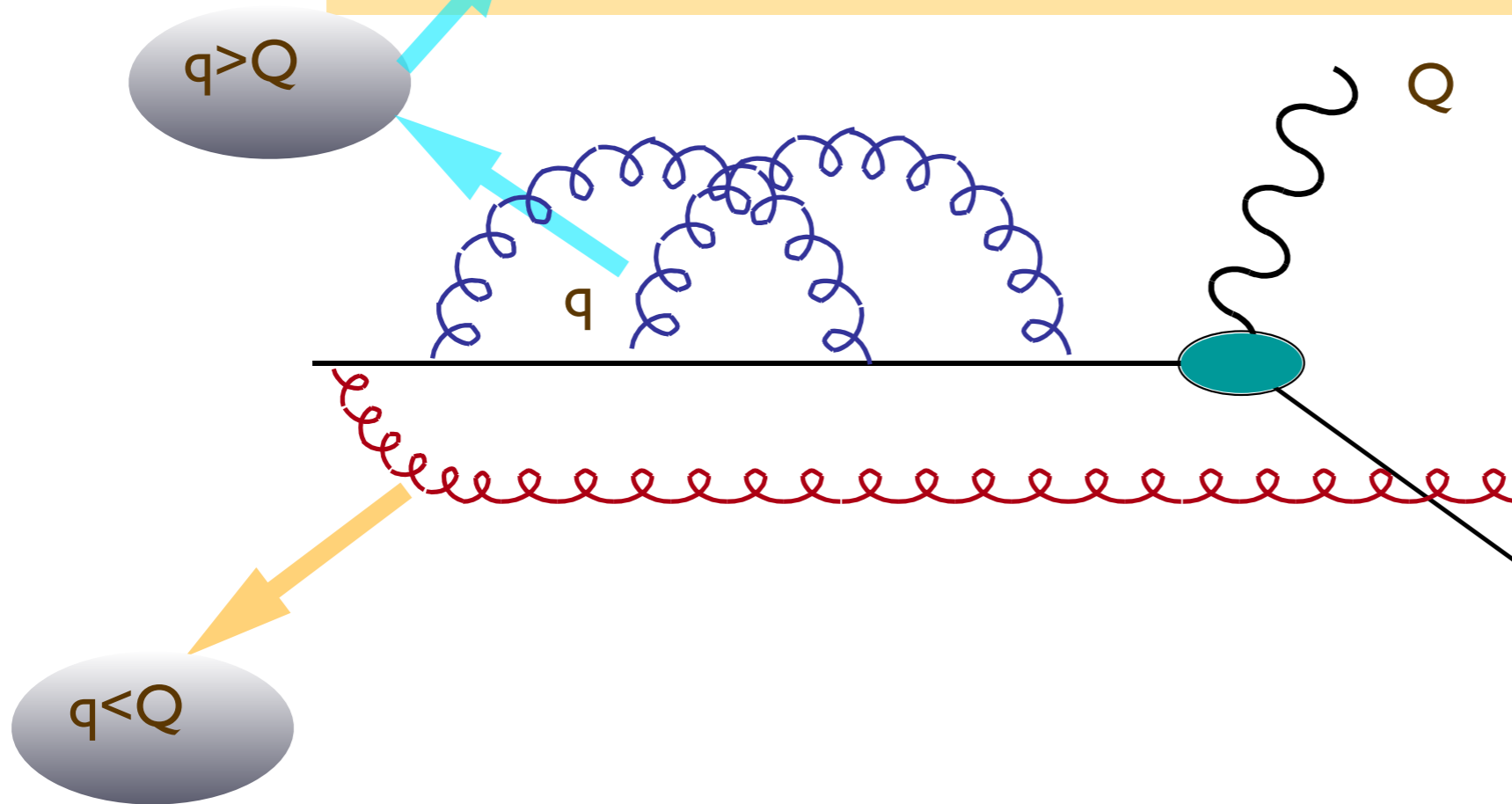
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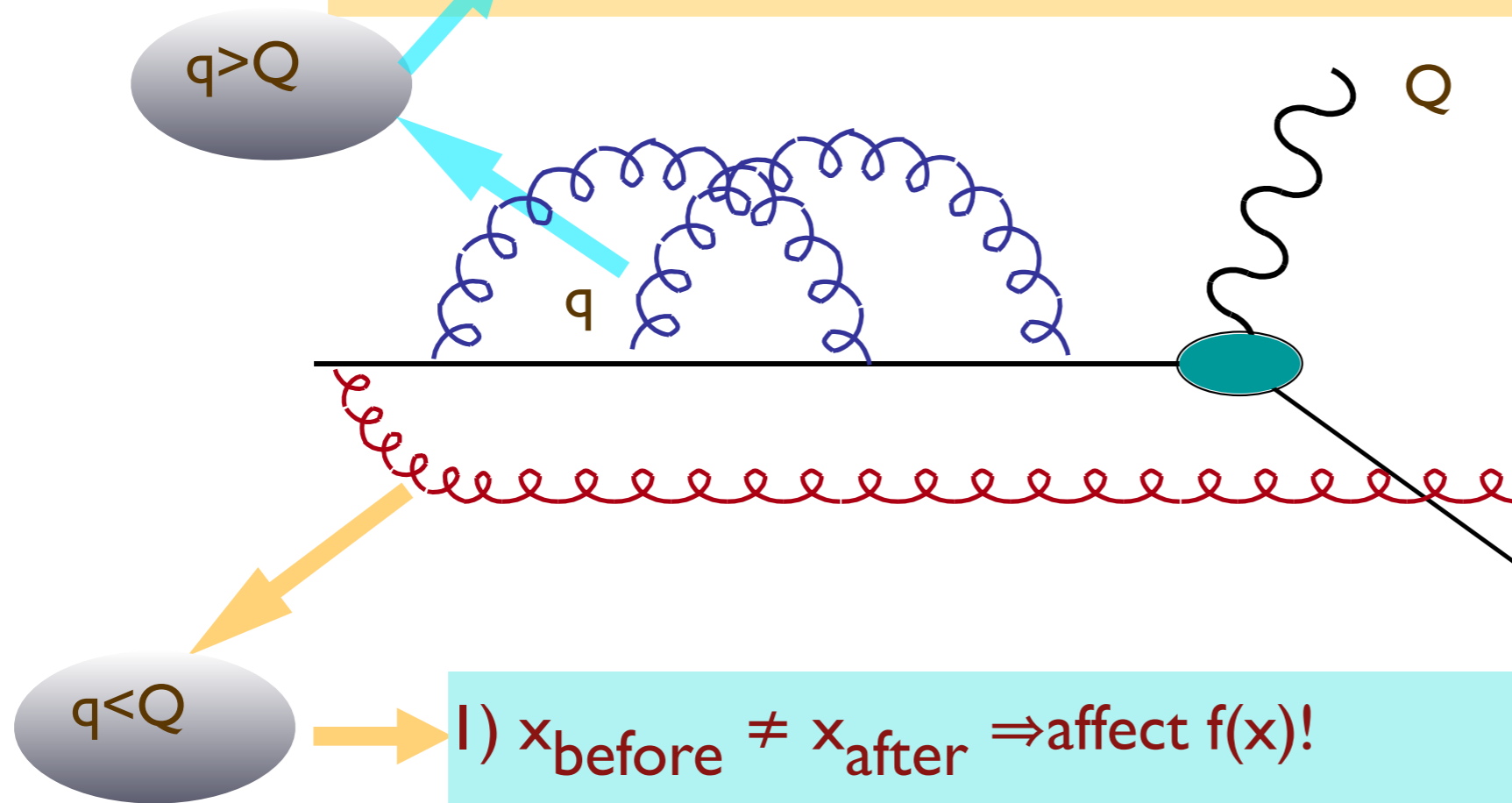
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This gluon cannot be reabsorbed because the quark is gone

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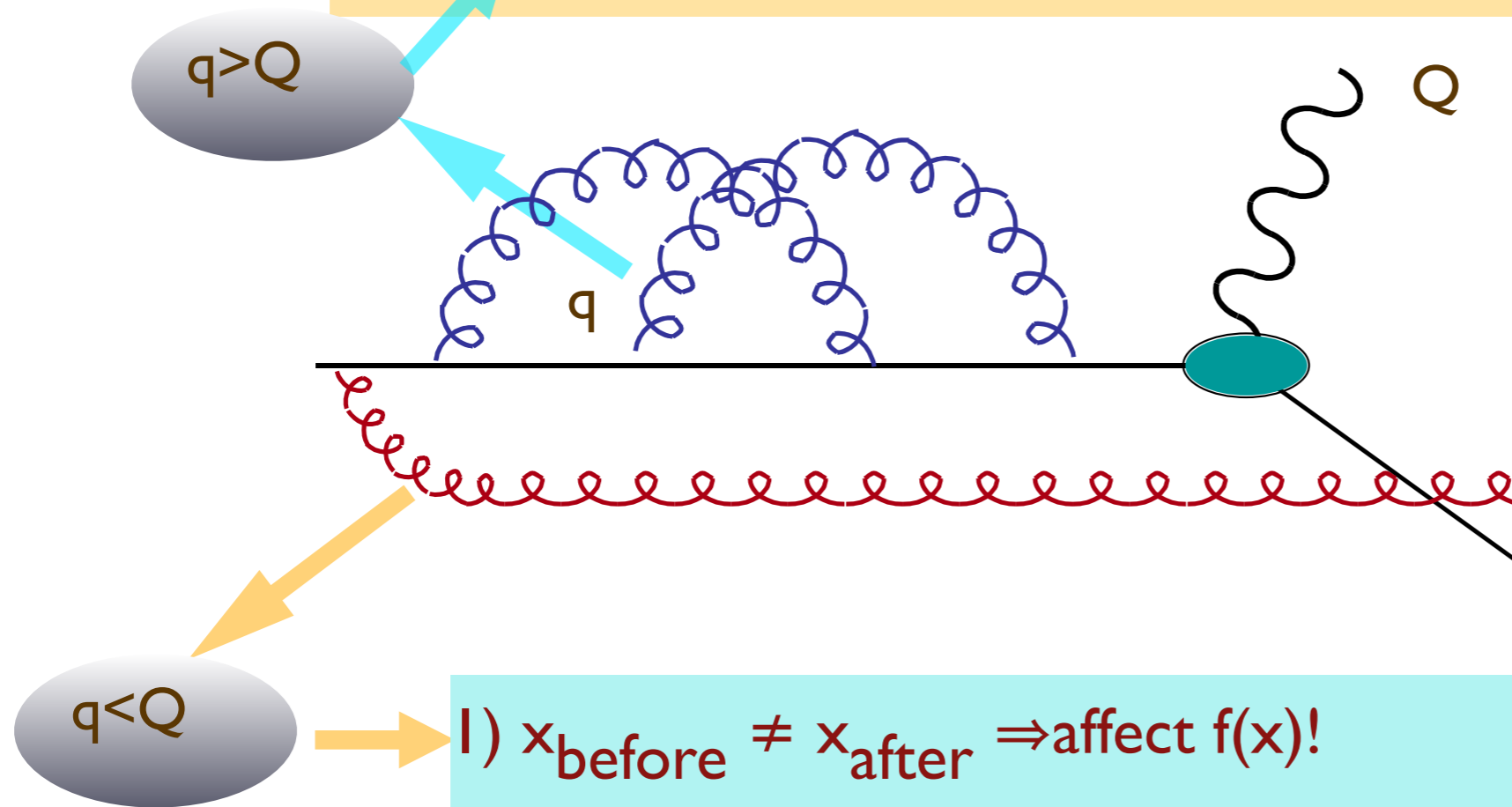


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- 1) $x_{\text{before}} \neq x_{\text{after}} \Rightarrow$ affect $f(x)$!
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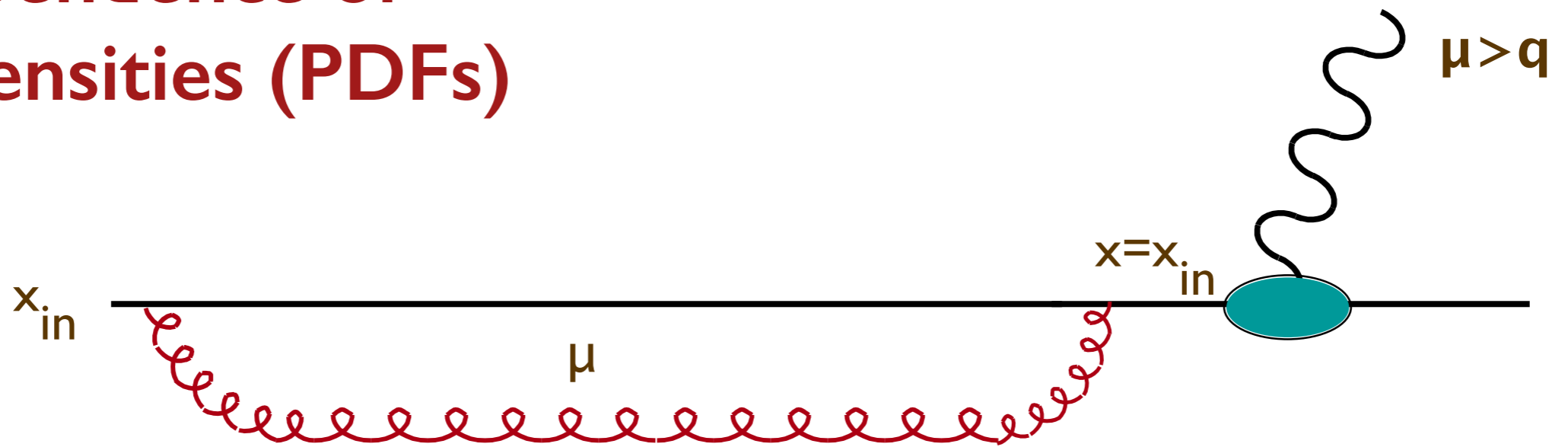
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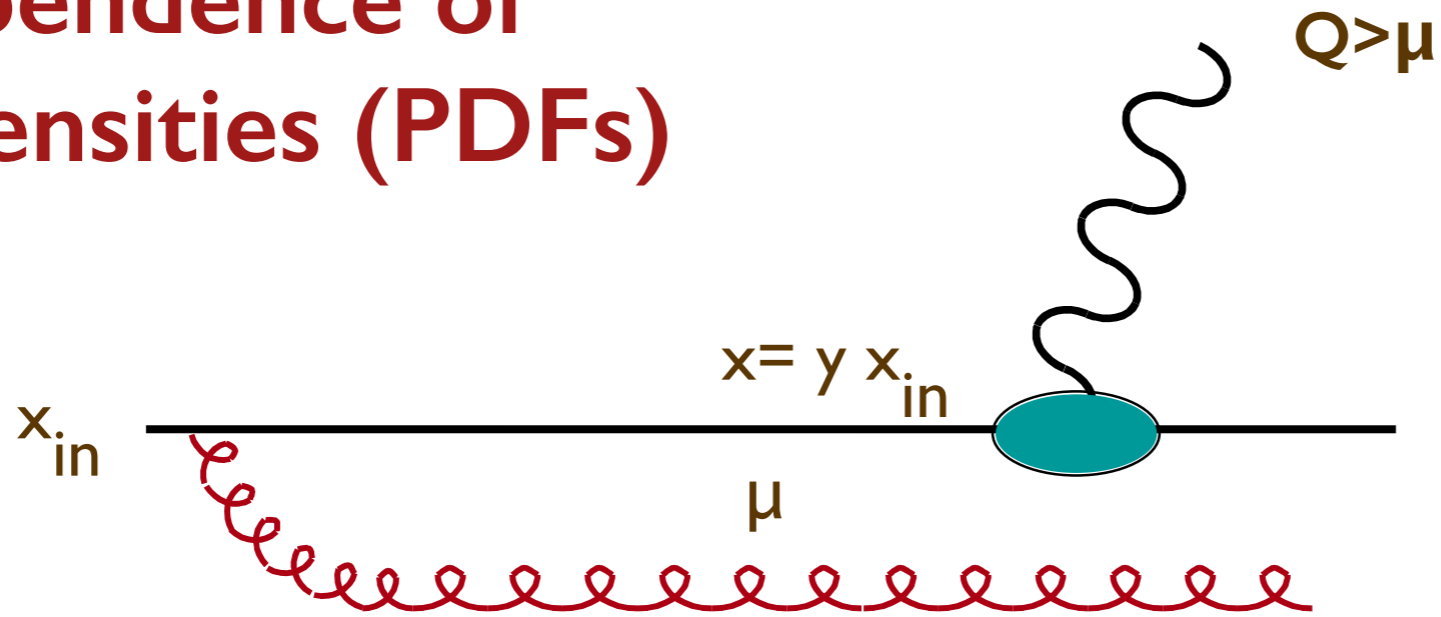
However, since $\tau(q \approx 1 \text{ GeV}) \gg 1/Q$, the emission of low-virtuality gluons will take place long before the hard collision, and therefore cannot depend on the detailed nature of the hard probe. While it is not calculable in pQCD, $f(q \ll Q)$ can be measured using a reference probe, and used elsewhere

➔ **Universality of $f(x)$**

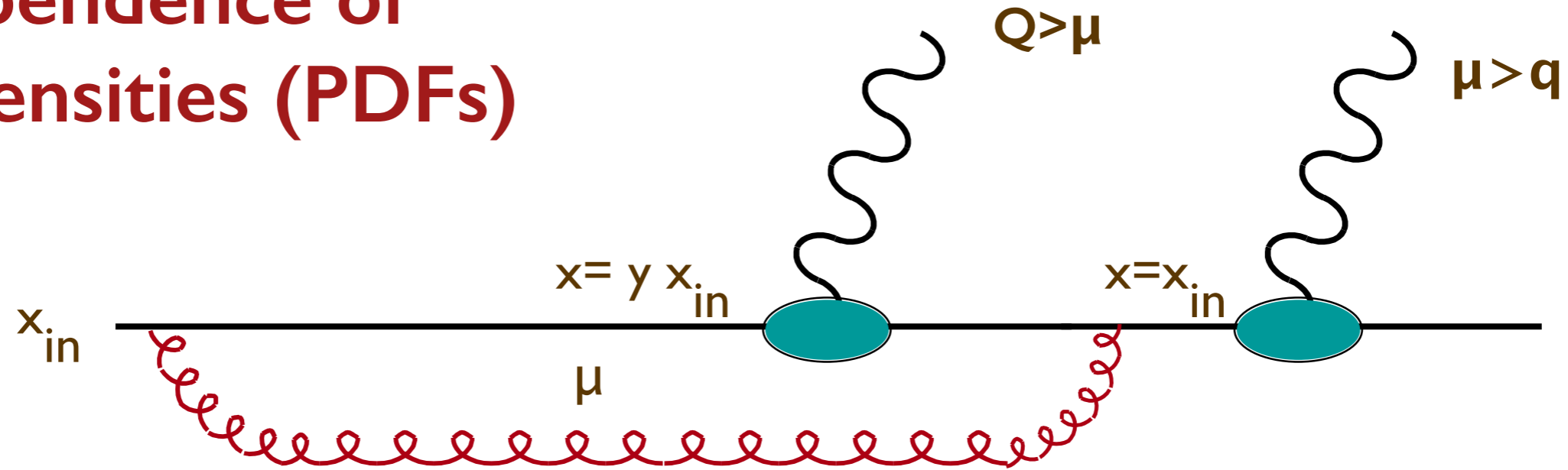
Q dependence of parton densities (PDFs)



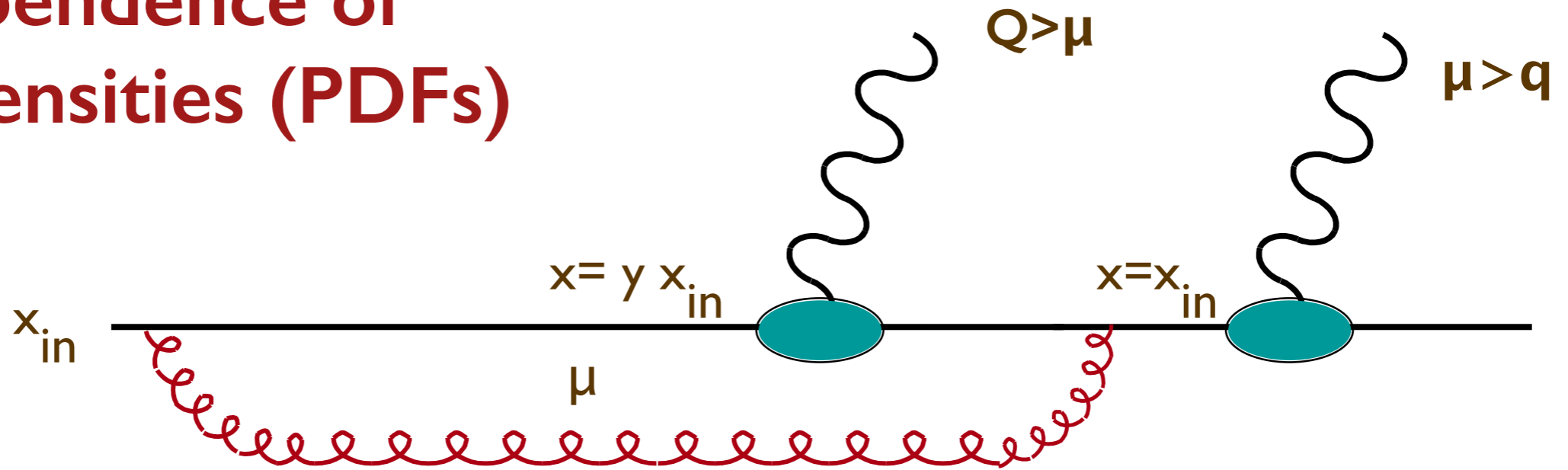
Q dependence of parton densities (PDFs)



Q dependence of parton densities (PDFs)



Q dependence of parton densities (PDFs)



The larger is Q , the more gluons will **not** have time to be reabsorbed

PDF's depend on Q !

$$f(x, Q) = f(x, \mu) + \int_x^1 dx_{in} f(x_{in}, \mu) \int_{\mu}^Q dq^2 \int_0^1 dy P(y, q^2) \delta(x - yx_{in})$$

$$f(x, Q) = f(x, \mu) + \int_x^1 dx_{in} f(x_{in}, \mu) \int_{\mu}^Q dq^2 \int_0^1 dy P(y, q^2) \delta(x - yx_{in})$$

$f(x, Q)$ should be independent of the intermediate scale μ considered:

$$\frac{df(x, Q)}{d\mu^2} = 0 \quad \Rightarrow \quad \frac{df(x, \mu)}{d\mu^2} = \int_x^1 \frac{dy}{y} f(y, \mu) P(x/y, \mu^2)$$

One can prove that:

$$P(x, Q^2) = \frac{\alpha_s}{2\pi} \frac{1}{Q^2} P(x)$$

calculable in pQCD

and finally (Dokshitzer-Gribov-Lipatov-Altarelli-Parisi DGLAP equation):

$$\frac{df(x, \mu)}{d \log \mu^2} = \frac{\alpha_s}{2\pi} \int_x^1 \frac{dy}{y} f(y, \mu) P(x/y)$$

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ASYMPTOTIC FREEDOM IN PARTON LANGUAGE

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G. PARISI ***

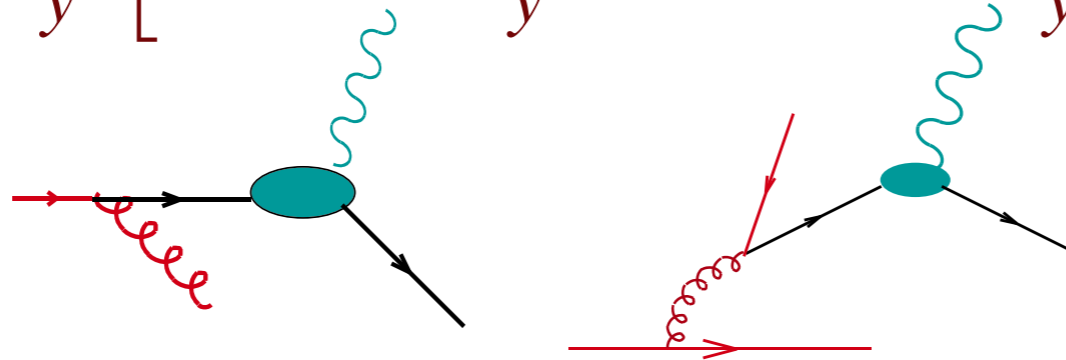
Institut des Hautes Etudes Scientifiques, Bures-sur-Yvette, France

Received 12 April 1977

More in general, one should consider additional processes which lead to the evolution of partons at high Q ($t = \log Q^2$):

$$[g(x)]_+ : \int_0^1 dx f(x) g(x)_+ \equiv \int_0^1 [f(x) - f(1)] g(x) dx$$

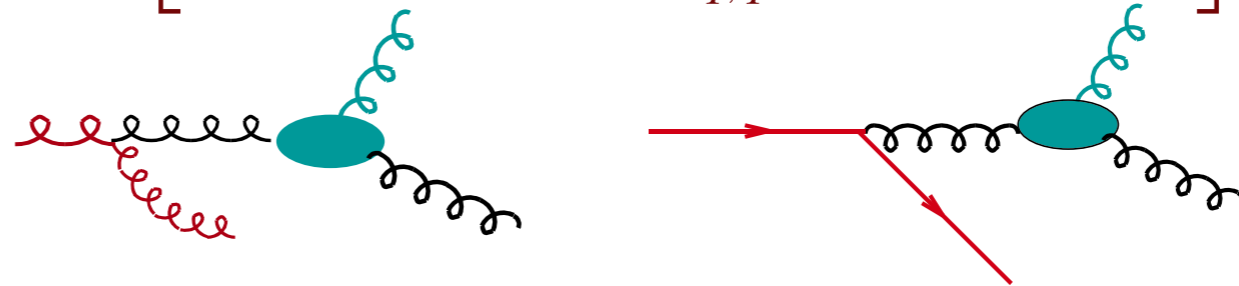
$$\frac{dq(x, Q)}{dt} = \frac{\alpha_s}{2\pi} \int_x^1 \frac{dy}{y} \left[q(y, Q) P_{qq}\left(\frac{x}{y}\right) + g(y, Q) P_{qg}\left(\frac{x}{y}\right) \right]$$



$$P_{qq}(x) = C_F \left(\frac{1+x^2}{1-x} \right)_+$$

$$P_{qg}(x) = \frac{1}{2} [x^2 + (1-x)^2]$$

$$\frac{dg(x, Q)}{dt} = \frac{\alpha_s}{2\pi} \int_x^1 \frac{dy}{y} \left[g(y, Q) P_{gg}\left(\frac{x}{y}\right) + \sum_{q, \bar{q}} q(y, Q) P_{gq}\left(\frac{x}{y}\right) \right]$$



$$P_{gq}(x) = C_F \left(\frac{1 + (1-x)^2}{x} \right)$$

$$P_{gg}(x) = 2N_c \left[\frac{x}{(1-x)_+} + \frac{1-x}{x} + x(1-x) \right] + \delta(1-x) \left(\frac{11N_c - 2n_f}{6} \right)$$

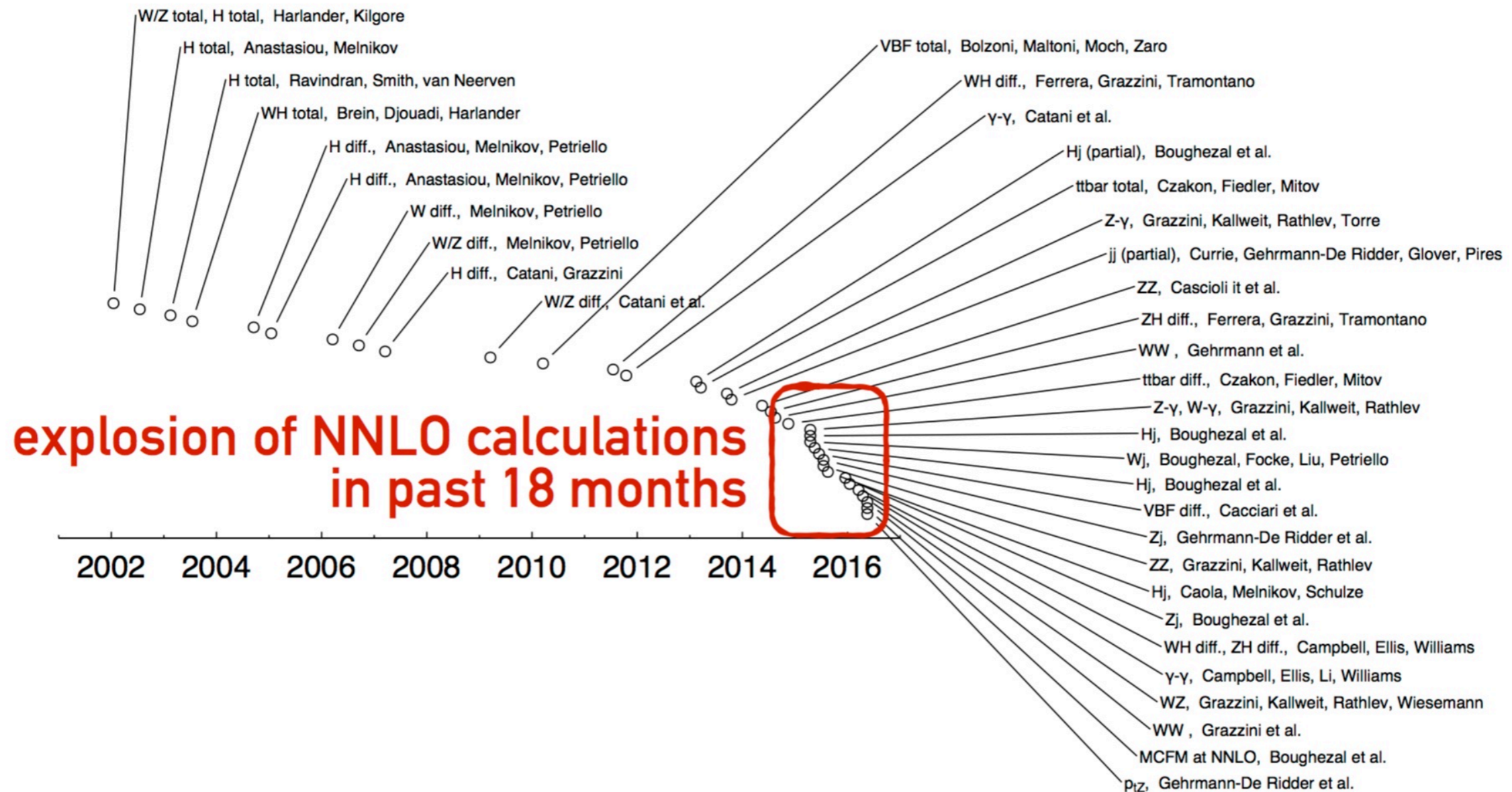
Directions for progress

- Improve the determination of the PDFs, using LHC data
- Improve the calculations of partonic matrix elements (N^nLO)
- Improve the description of the full final state:
 - higher-order corrections to the matrix element (resummation, parton shower)
 - transition from partons to hadrons
 - modeling the interaction of the proton fragments
- Validate the theoretical progress against data, test validity/limitations of factorization

TH is rapidly making progress

NNLO hadron-collider calculations v. time

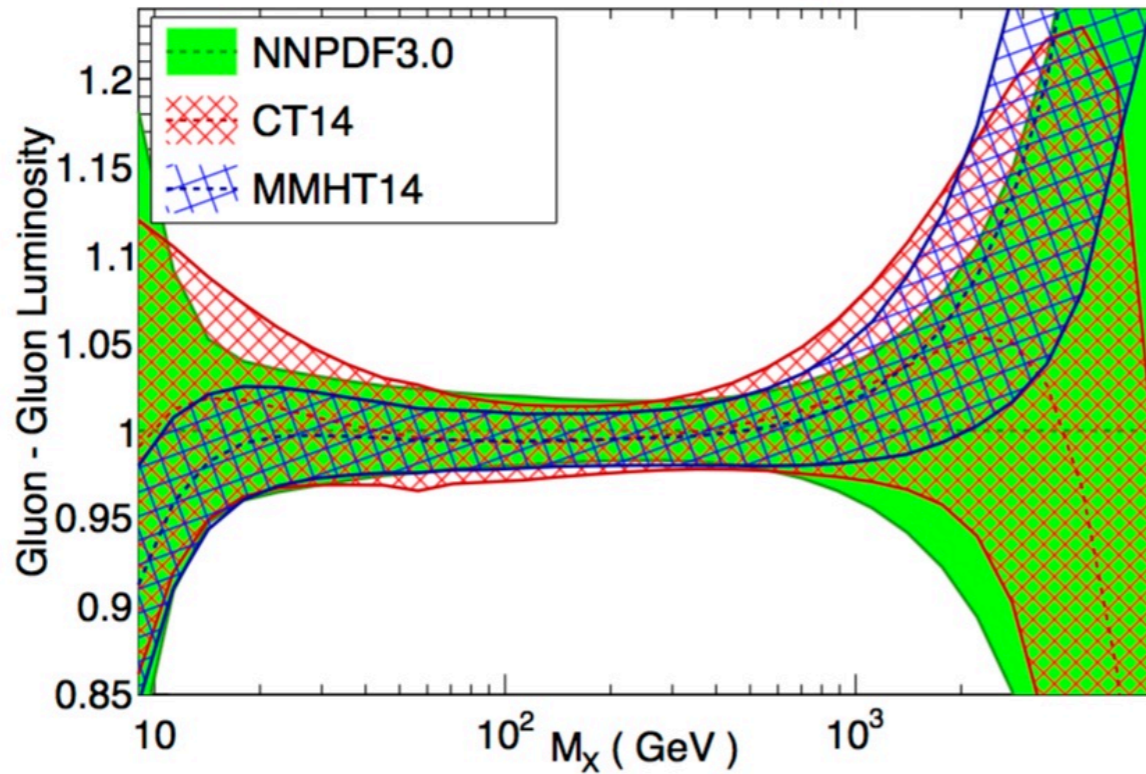
as of mid June



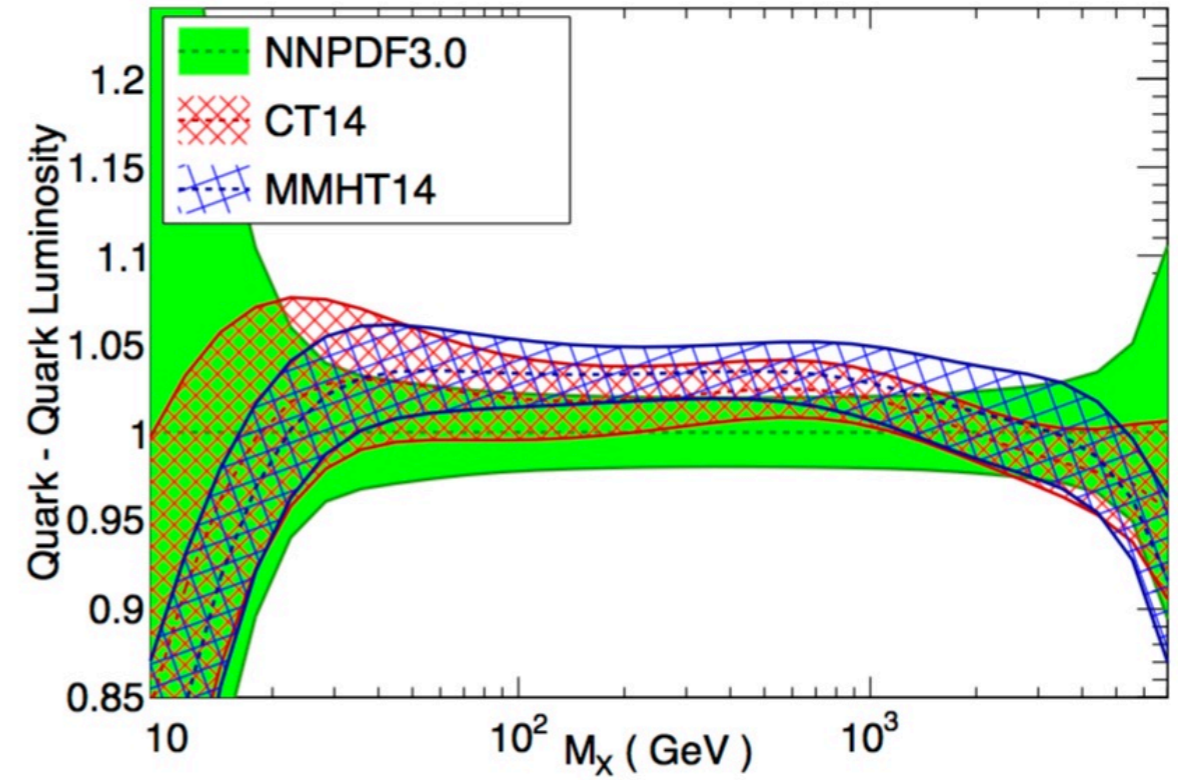
Status of PDF luminosity uncertainties

$$\frac{dL_{ij}}{d\tau} \equiv \frac{1}{1 + \delta_{ij}} \int \frac{dx}{x} [f_i(x) f_j(\frac{\tau}{x}) + f_j(x) f_i(\frac{\tau}{x})] \quad \tau = M^2/S$$

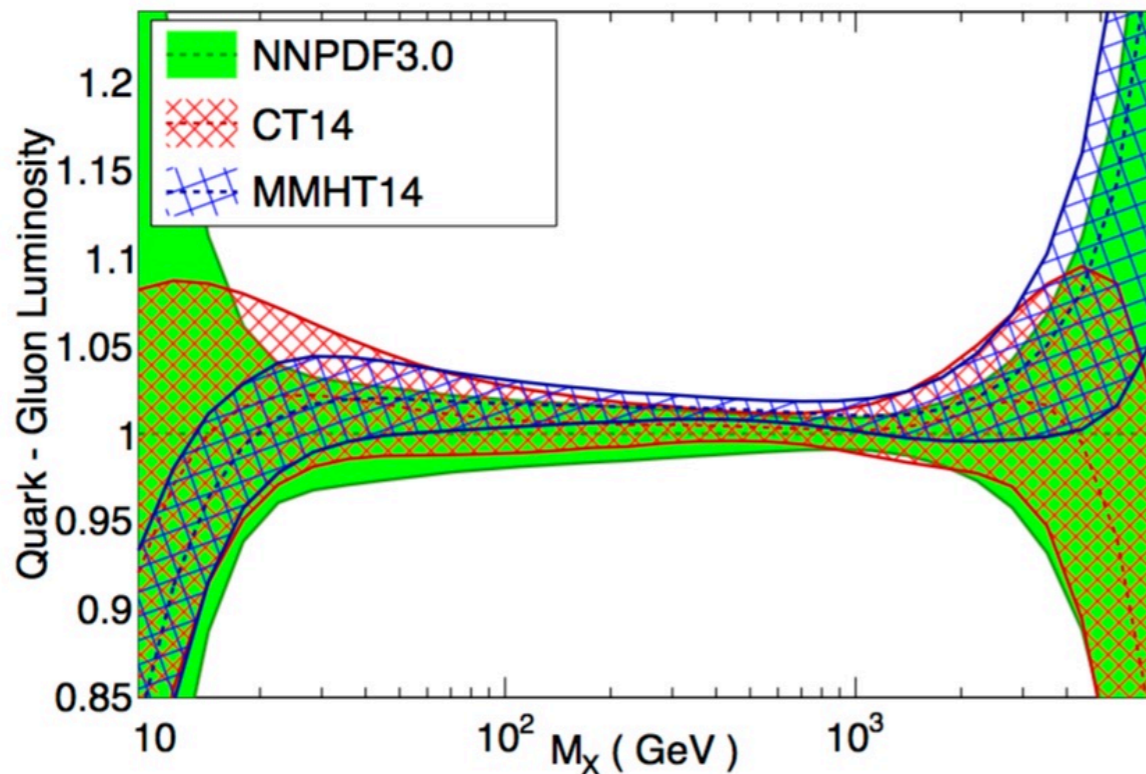
LHC 13 TeV, NNLO, $\alpha_s(M_Z)=0.118$



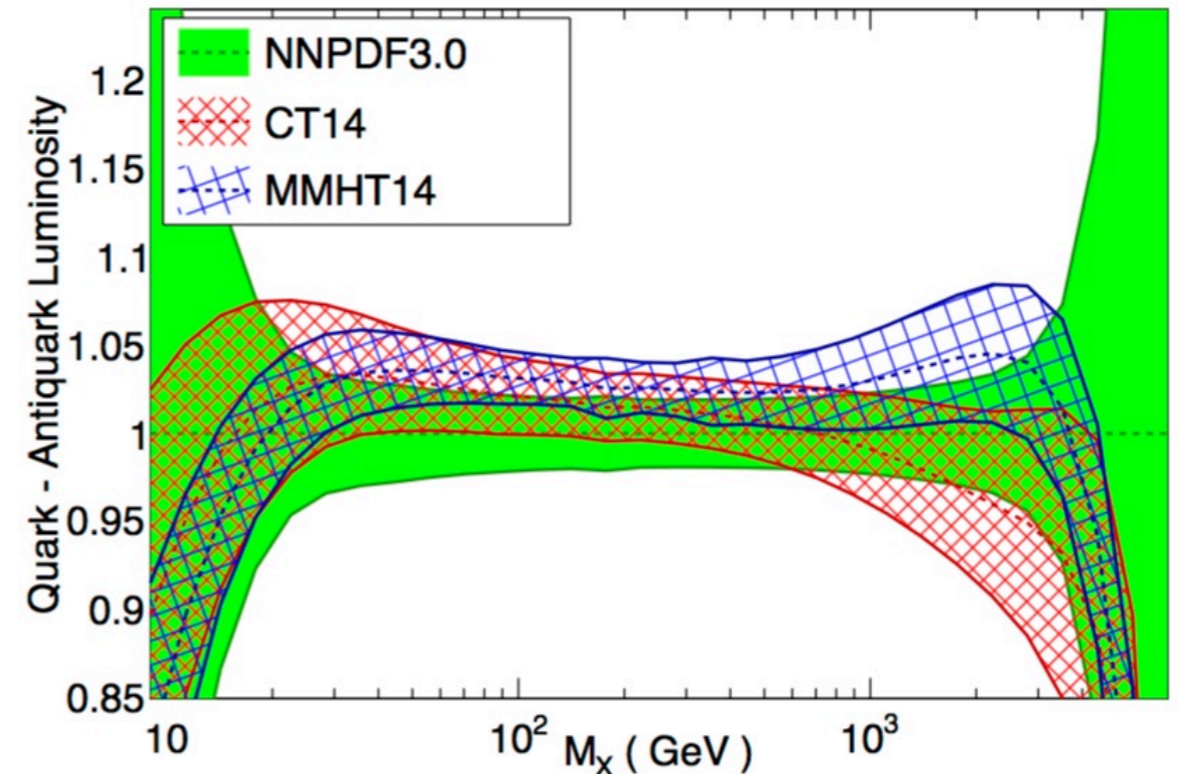
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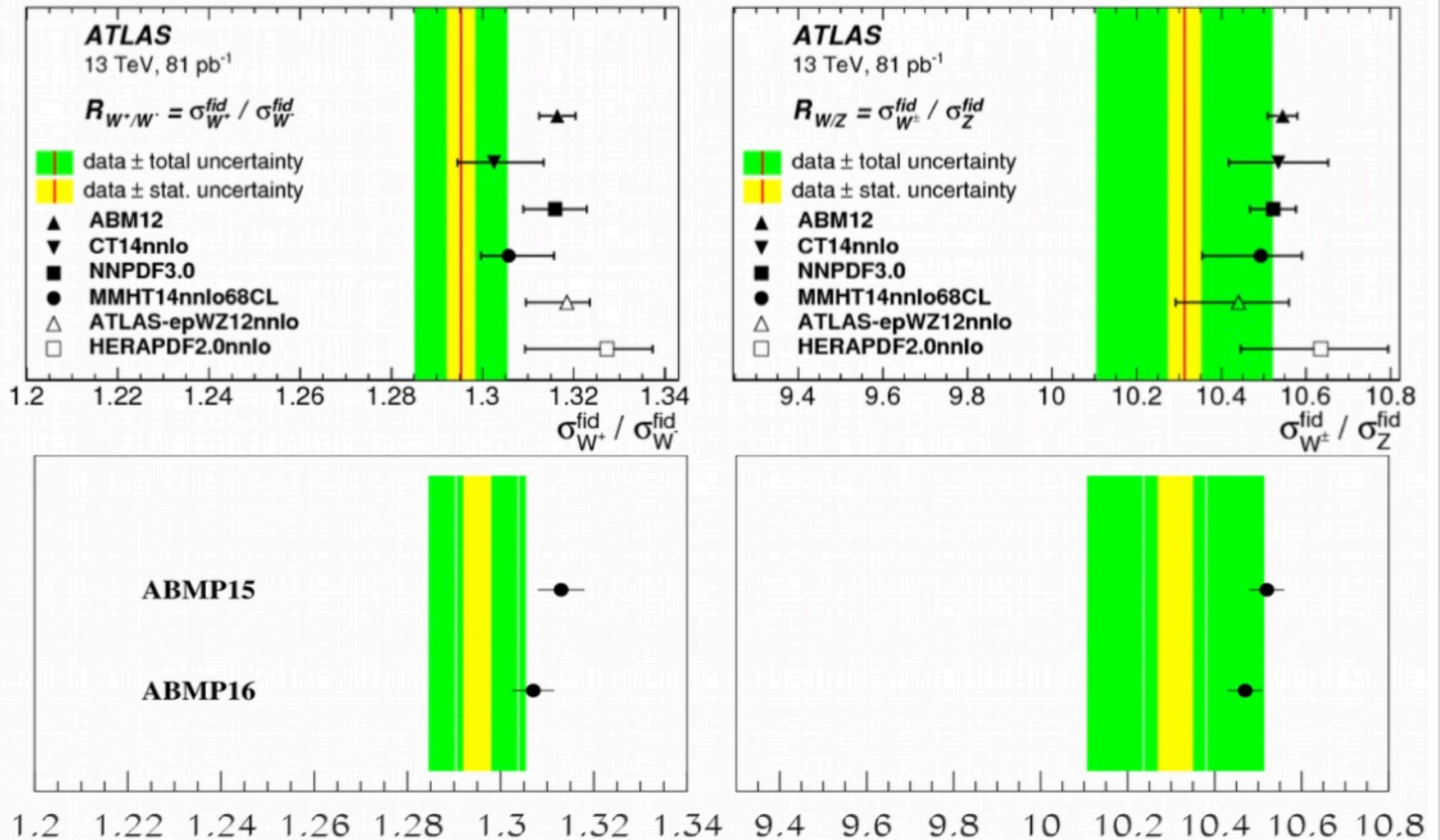


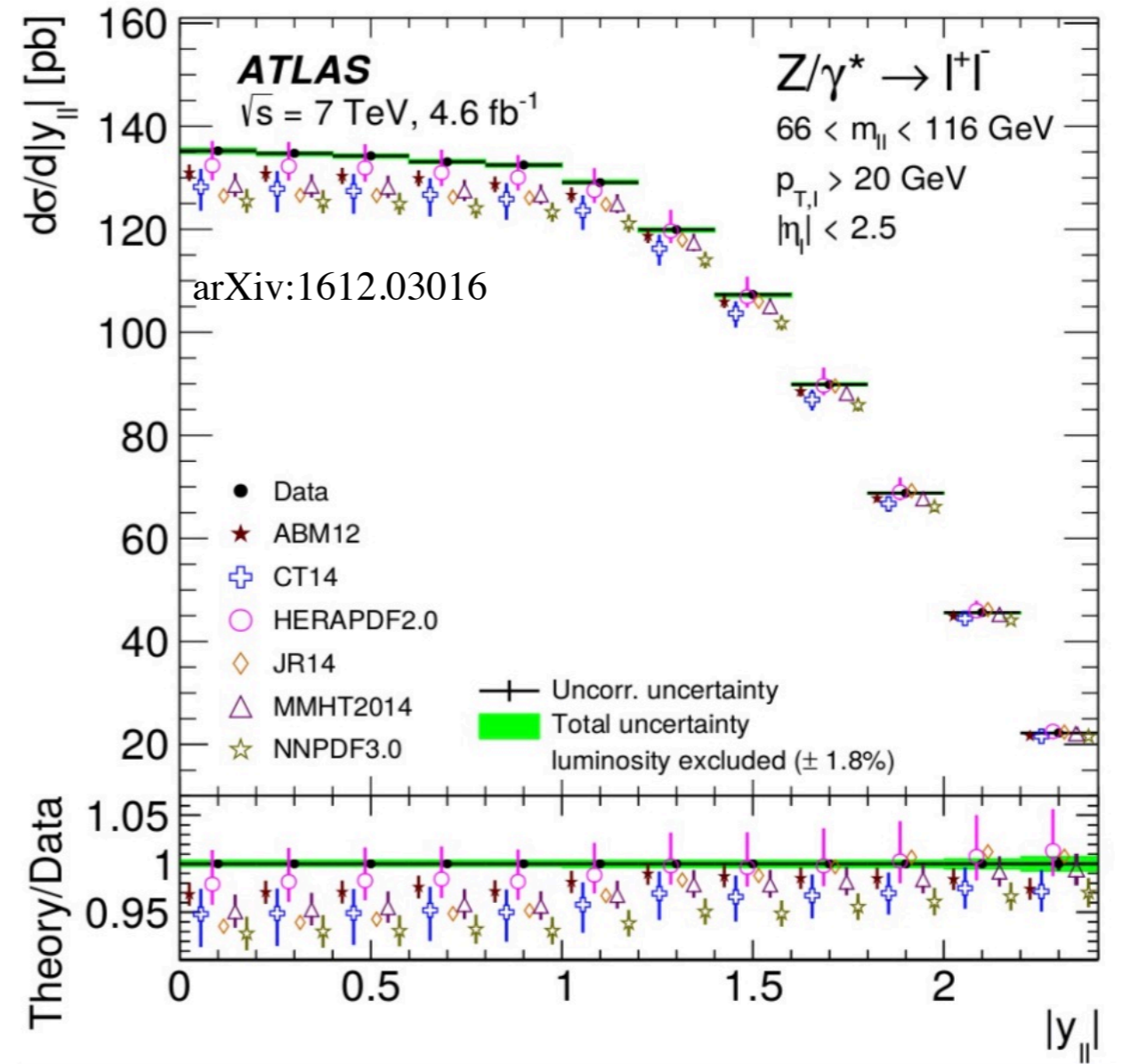
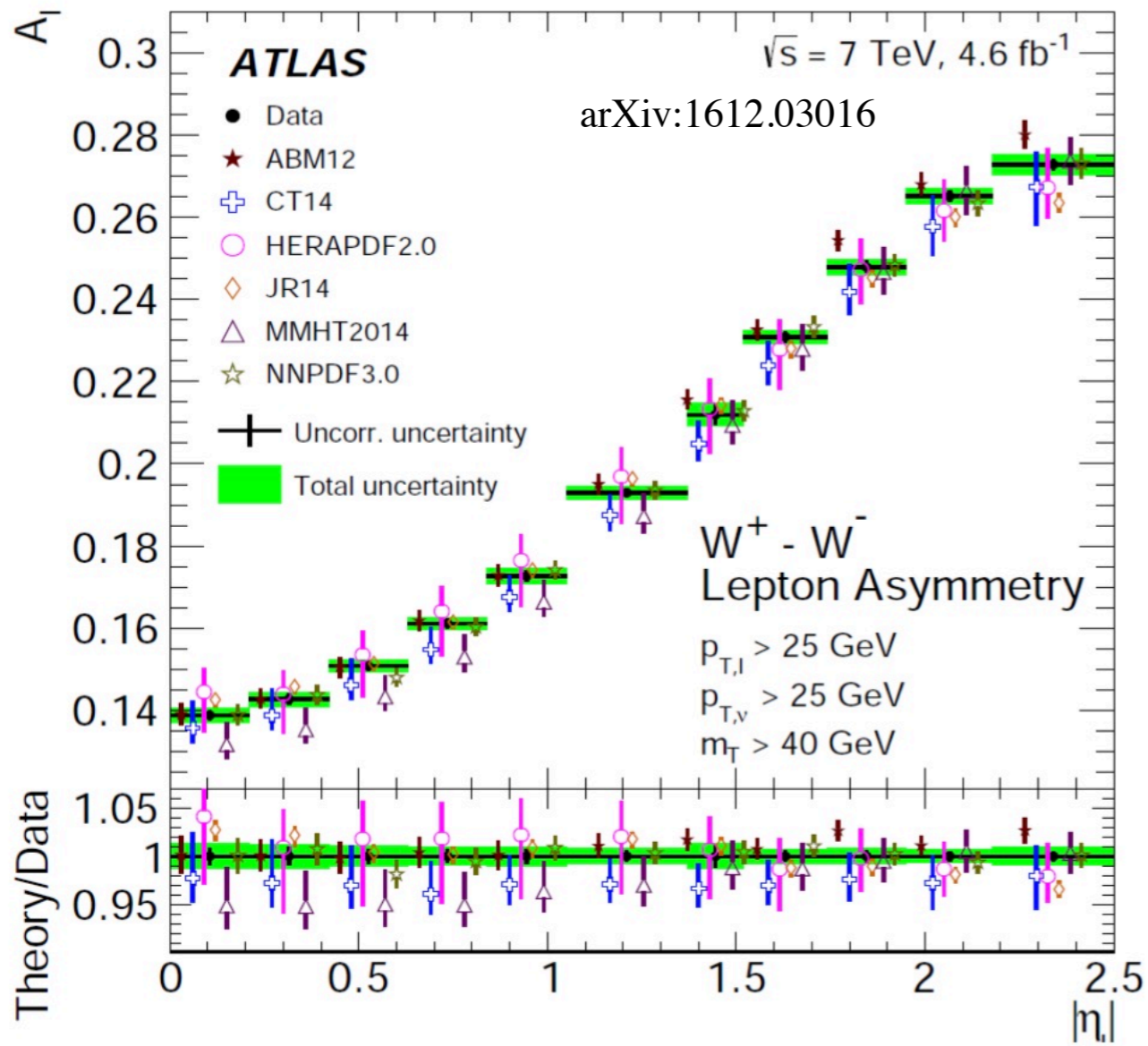
LHC 13 TeV, NNLO, $\alpha_s(M_Z)=0.118$



ATLAS W&Z at 13 TeV

ATLAS, hep-ex/1603.09222





Heavy quarks and PDFs

Nuclear Physics B308 (1988) 724–752
North-Holland, Amsterdam

TOTAL CROSS SECTIONS FOR HEAVY FLAVOUR PRODUCTION IN HADRONIC COLLISIONS AND QCD

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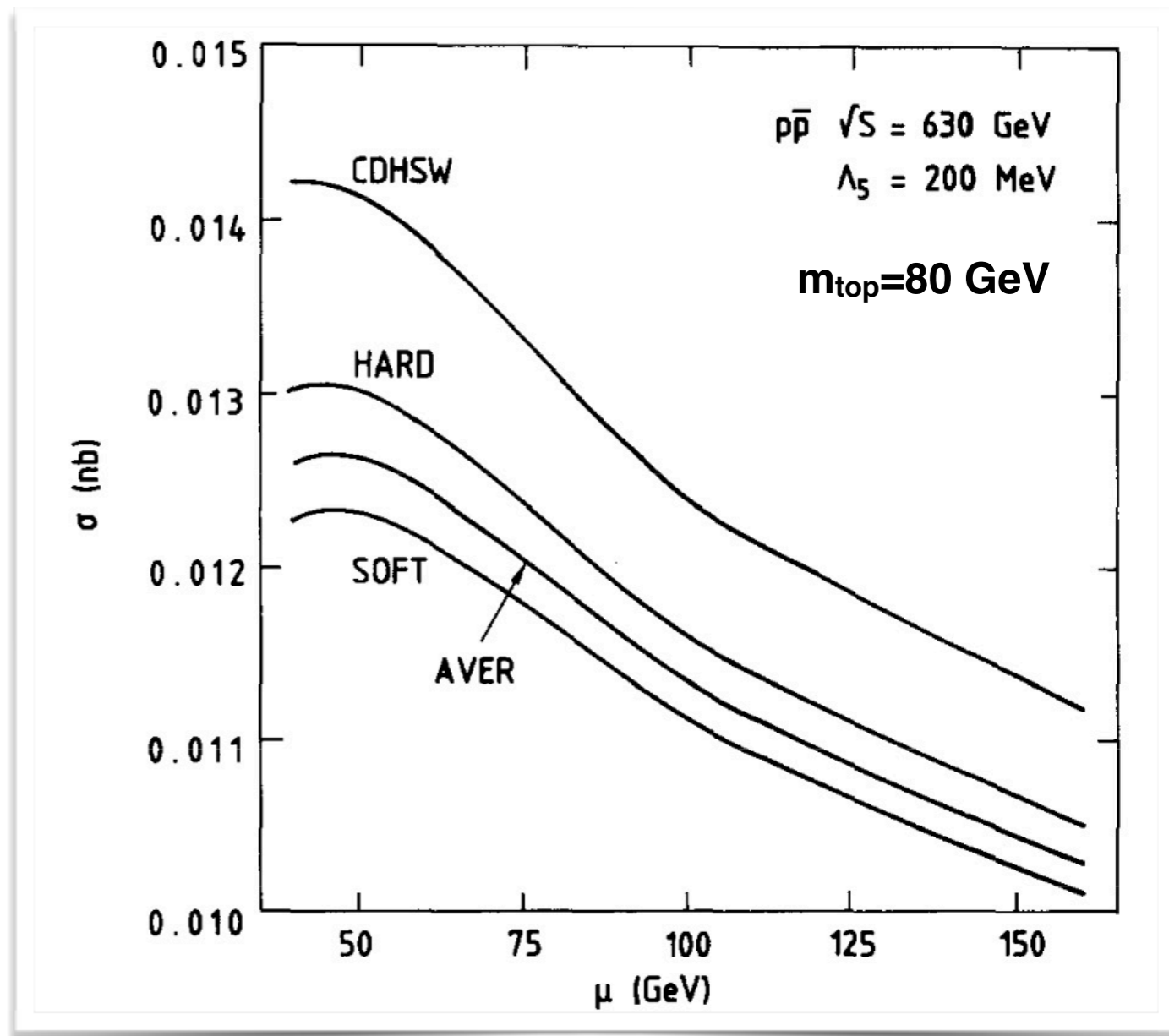
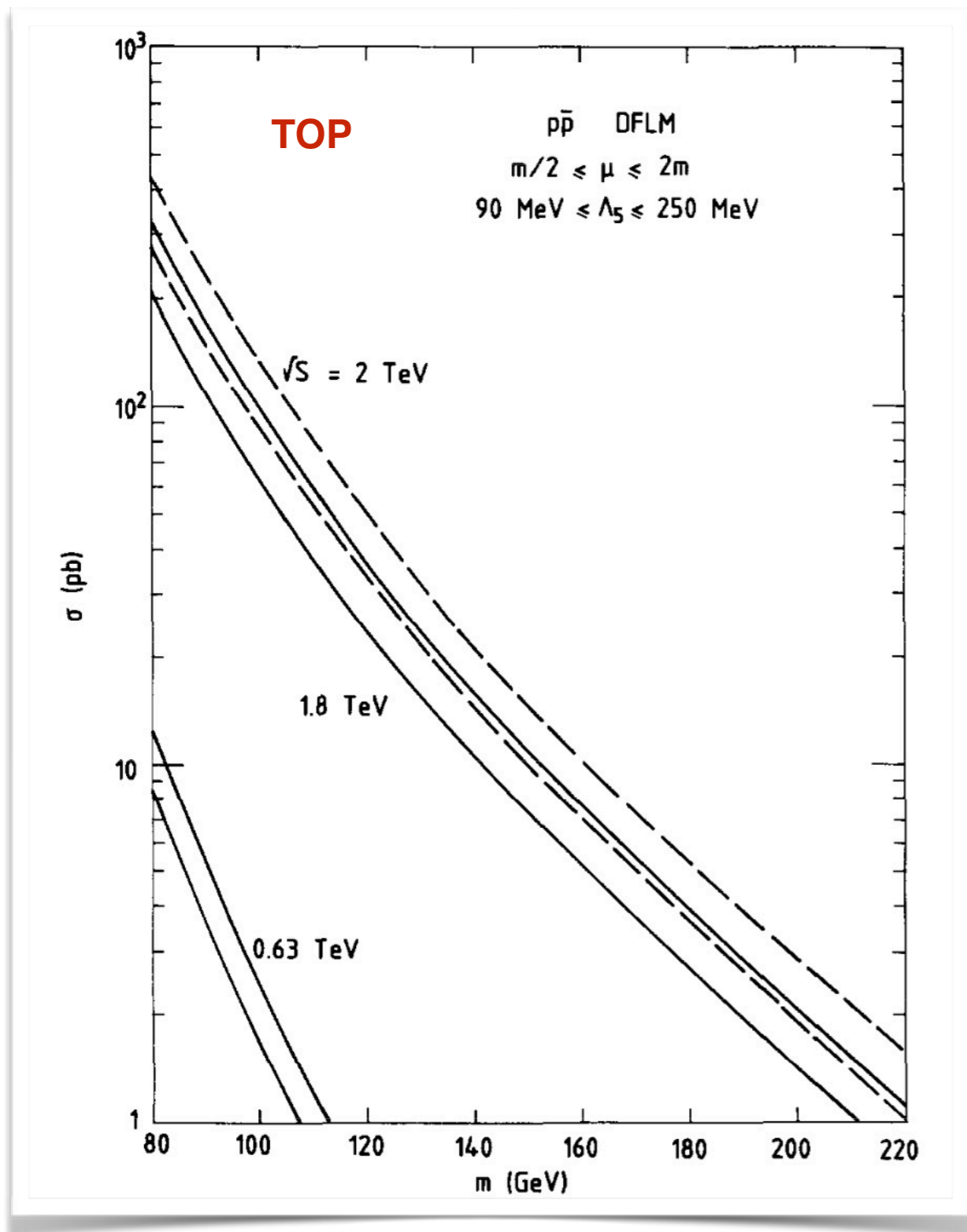
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Received 5 April 1988



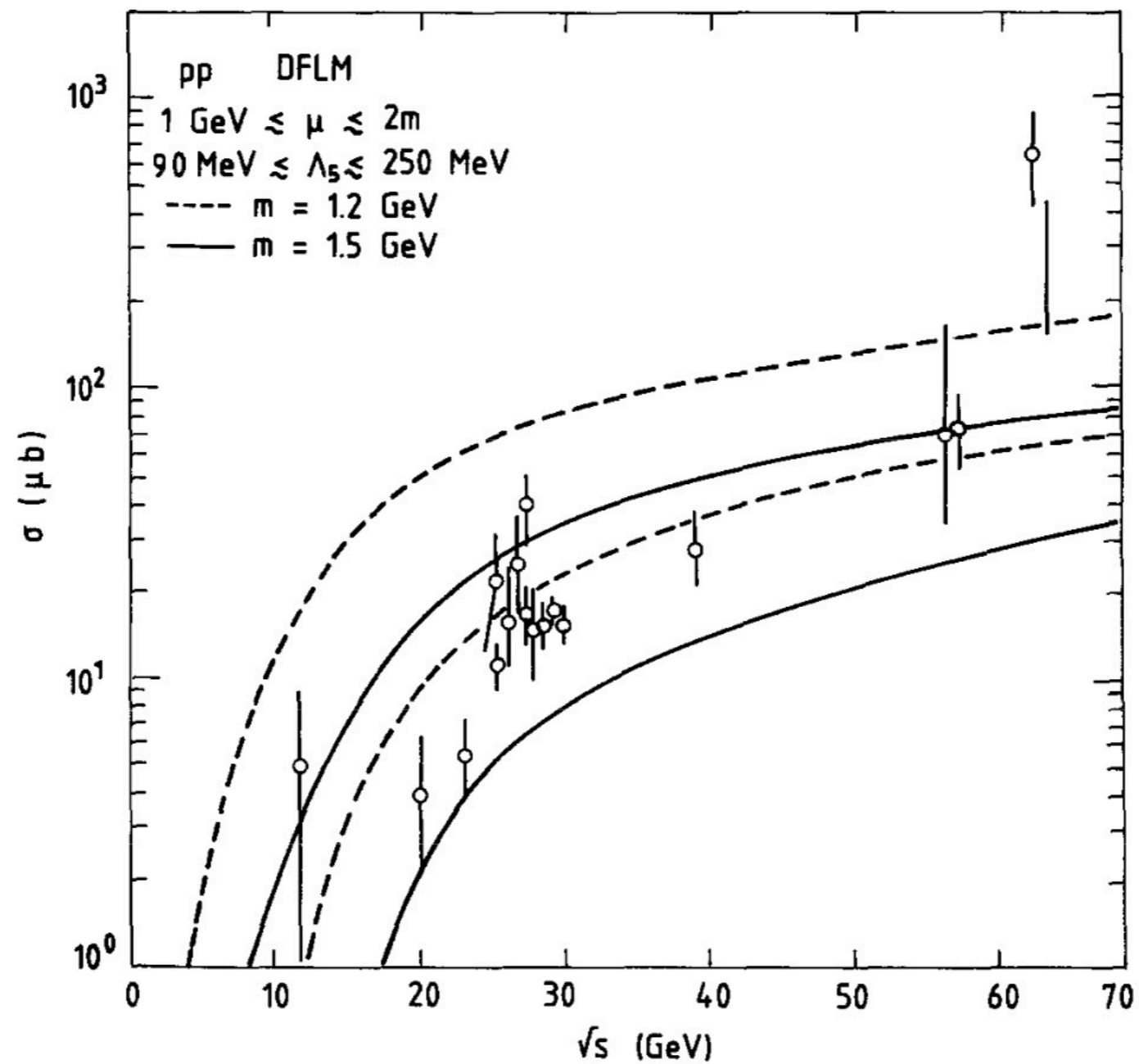
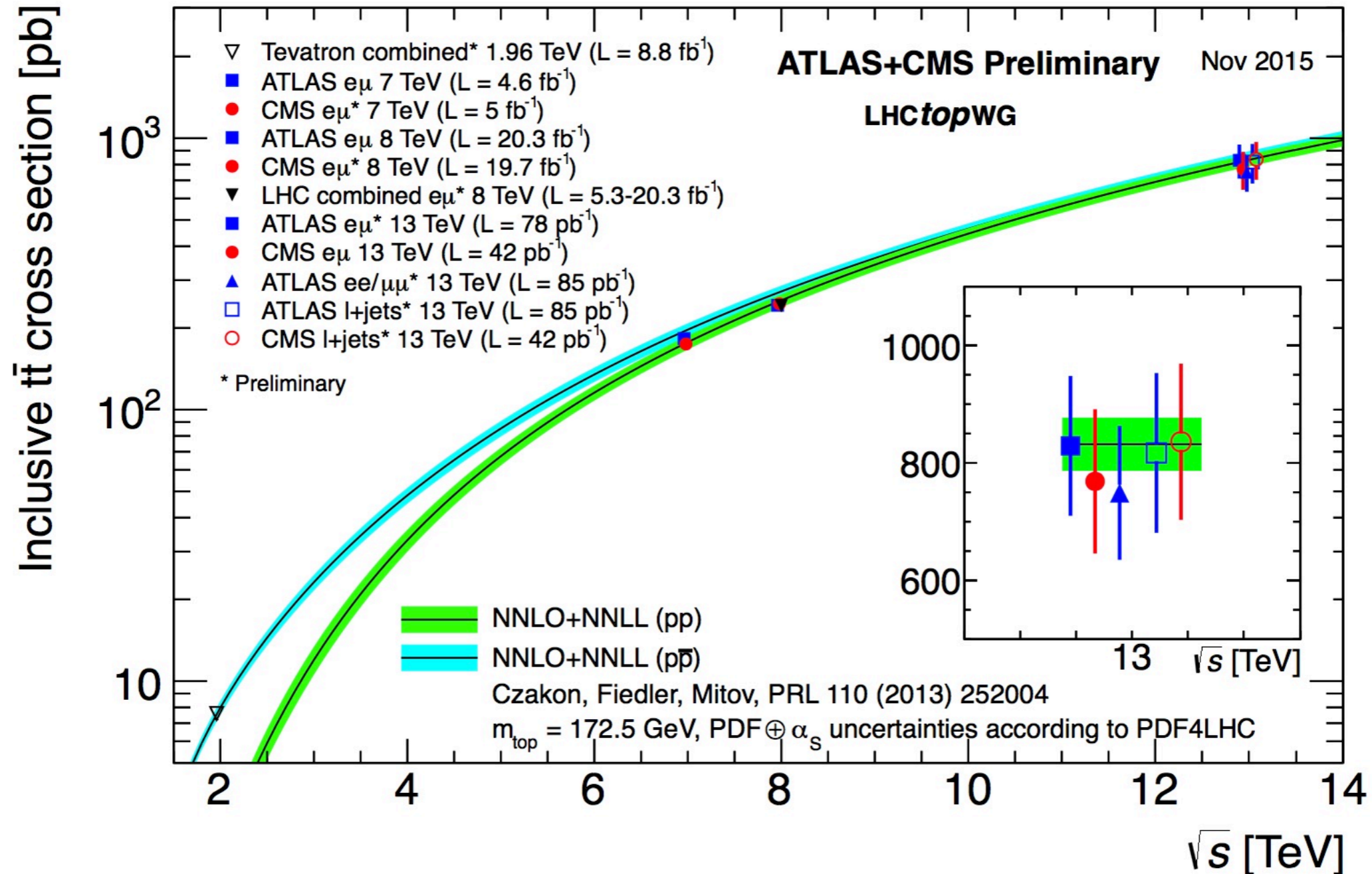
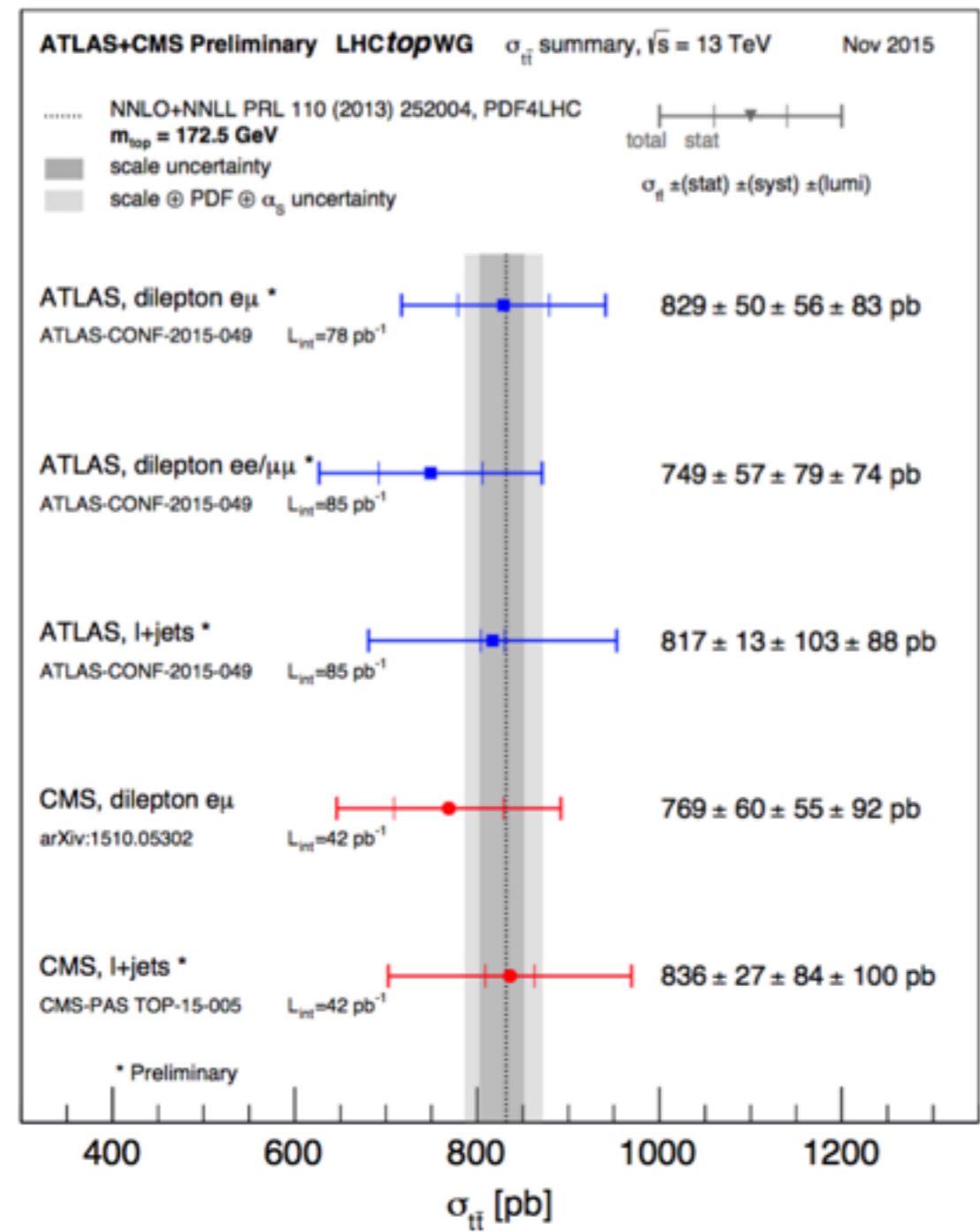
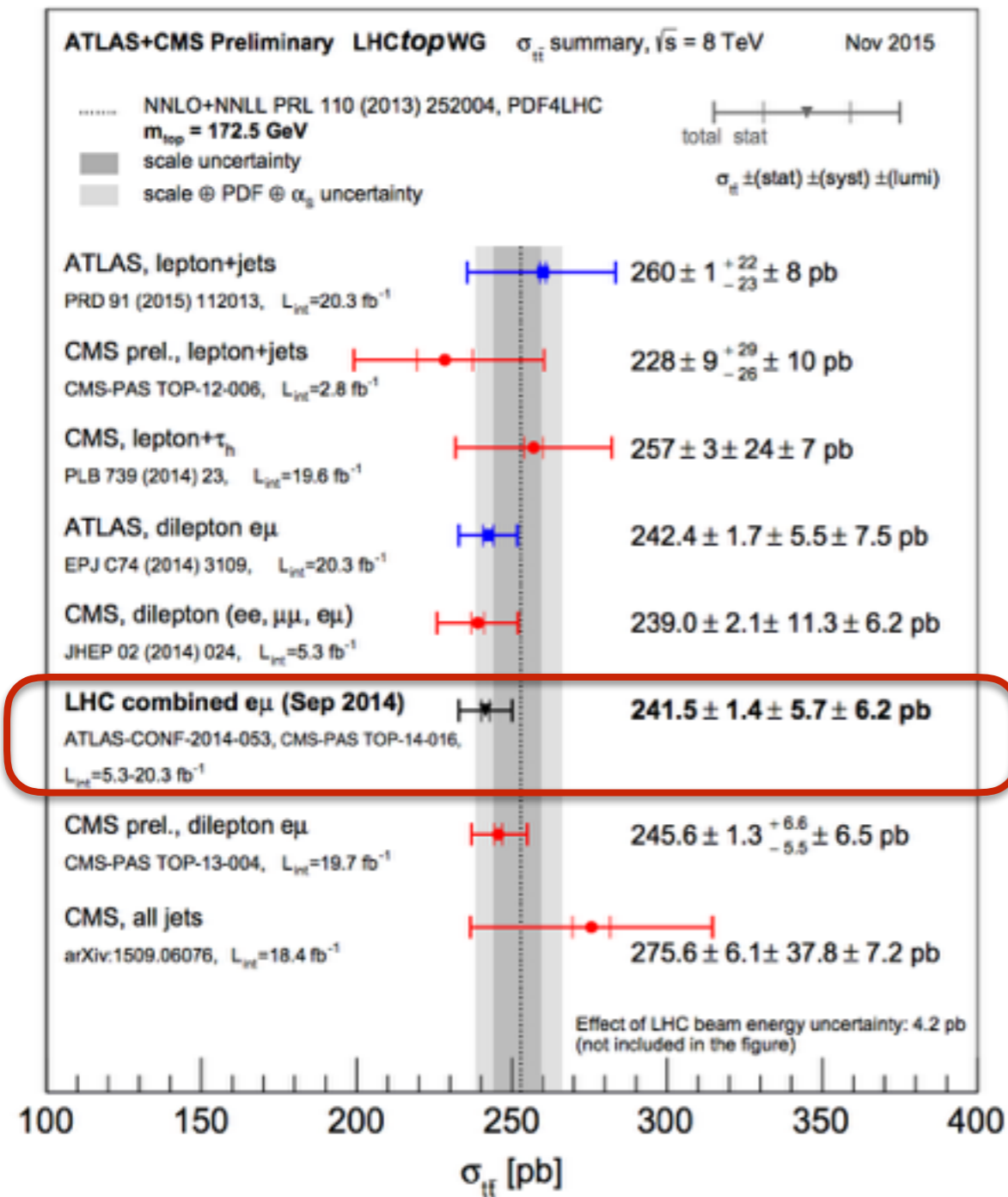
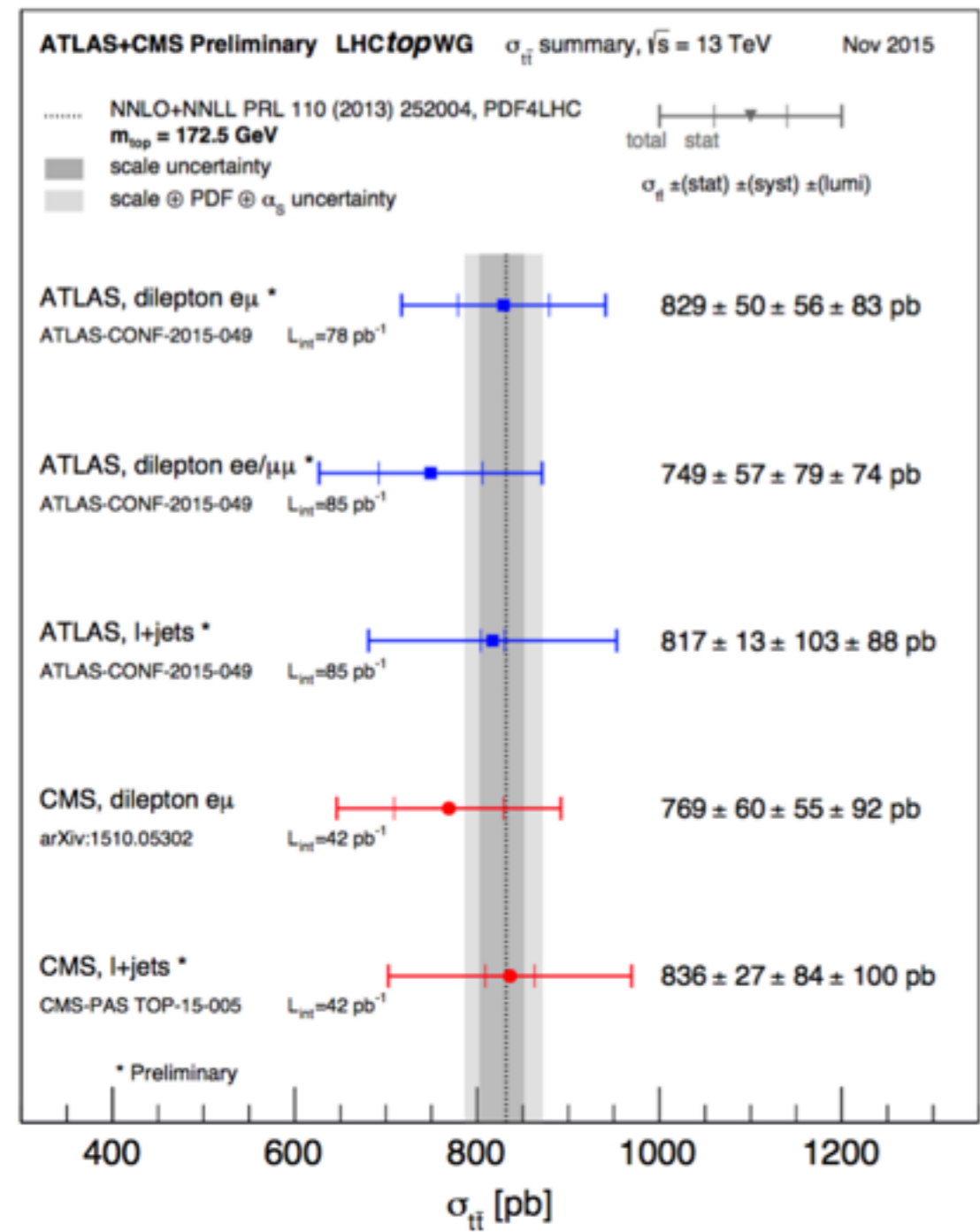
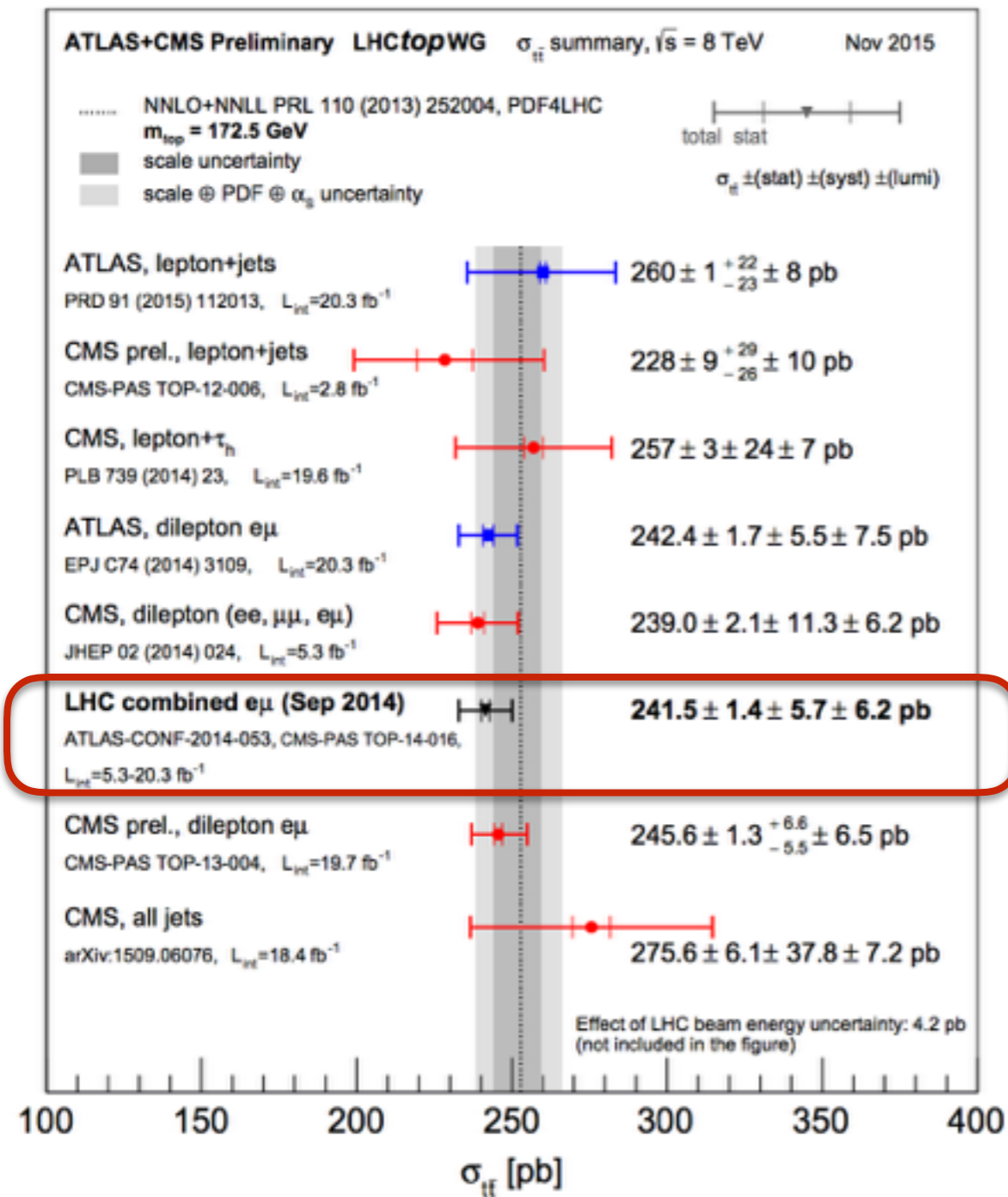


Fig. 18. Total cross section for charm production in pp collisions. The data compilation is taken from ref. [38]. The solid (dashed) curves determine the band, obtained for $m_c = 1.5 \text{ GeV}$ (1.2 GeV), by combining the theoretical uncertainties deriving from independent variations of μ and Λ_5 in the given ranges (added in quadrature).

Top quark production at LHC

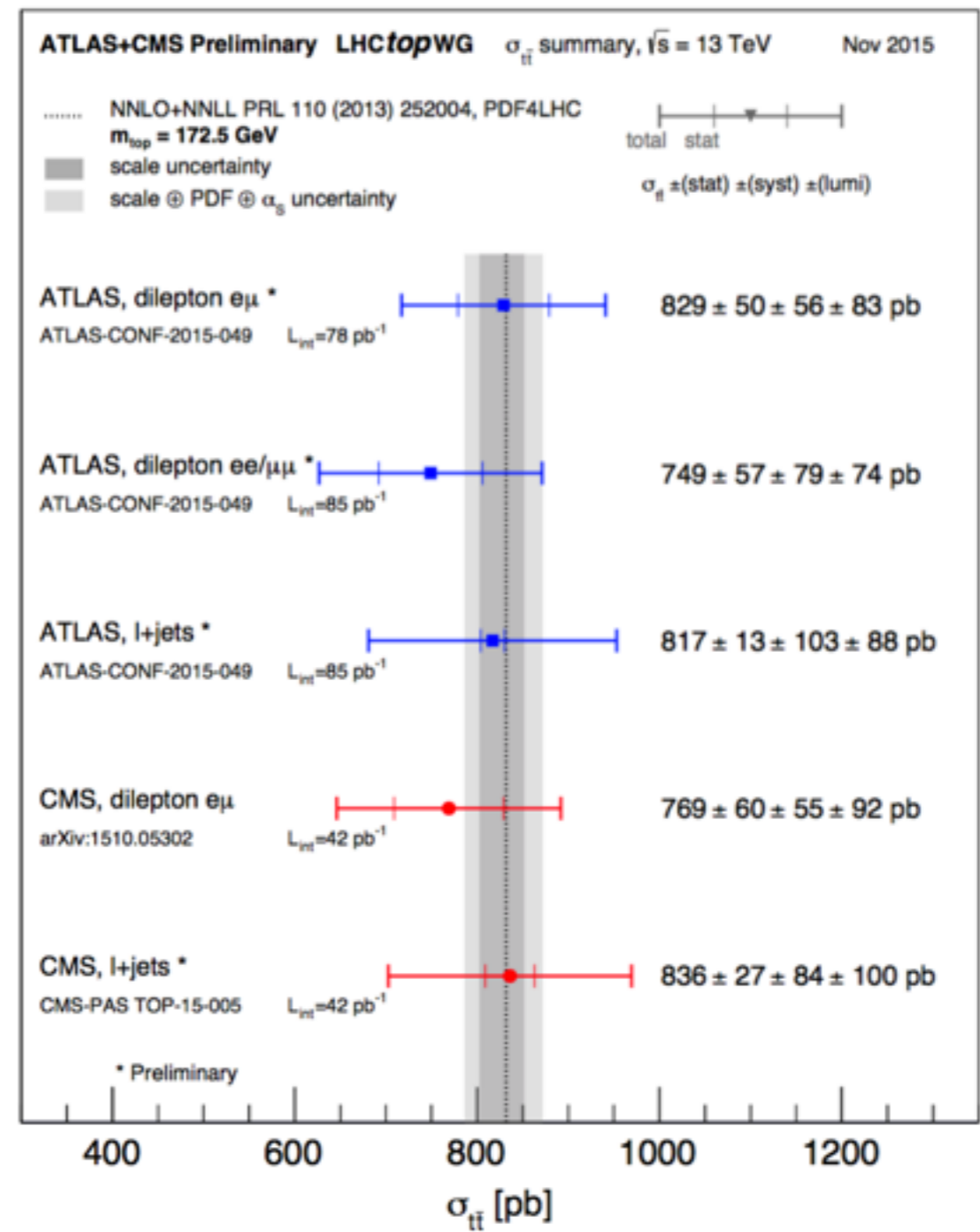
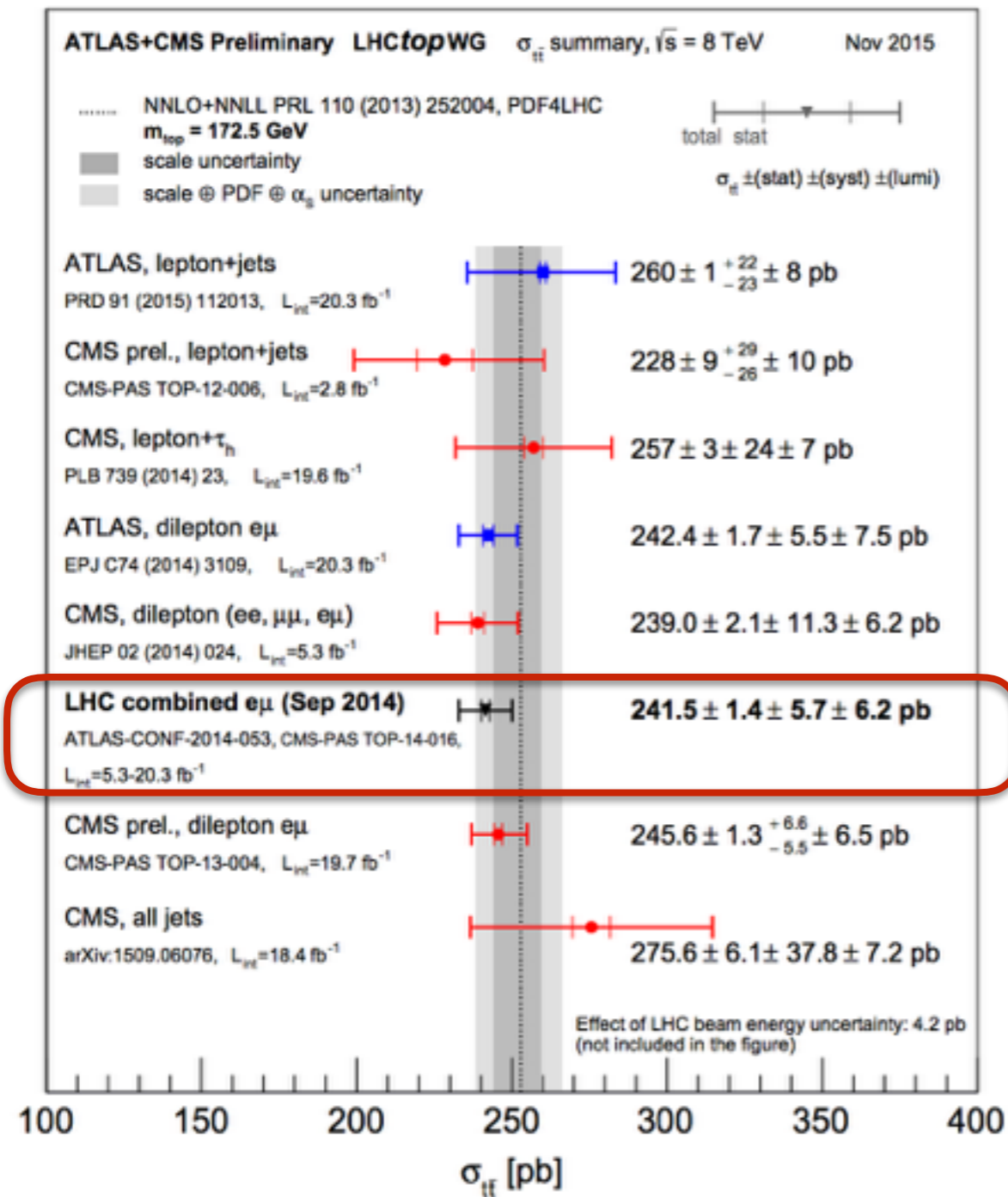






(pb)	$\sigma(172.5 \text{ GeV})$	δ_{scale}	$\delta_{\text{PDF}+\alpha_s}$	$\delta_{m_{top}}$
8 TeV	253	+6 -9	± 12	± 7.5
13 TeV	832	+20 -29	± 35	± 23

Czakov, Fiedler, Mitov,
 arXiv:1303.6254



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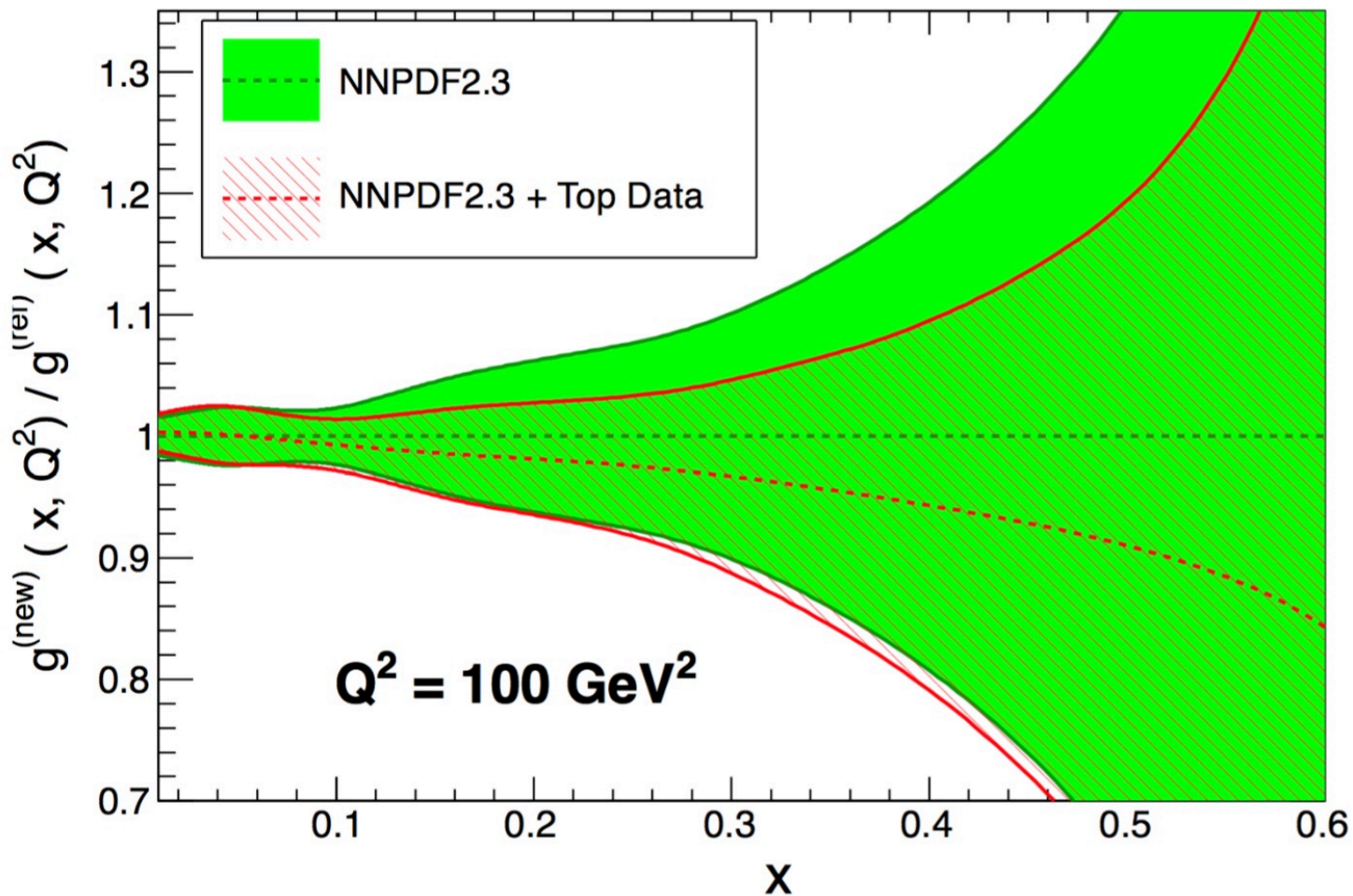
Czakoń, Fiedler, Mitov,
 arXiv:1303.6254

Pinning down PDF and parametric uncertainties is becoming more important than dealing with uncertainties from higher-order corrections

Some applications

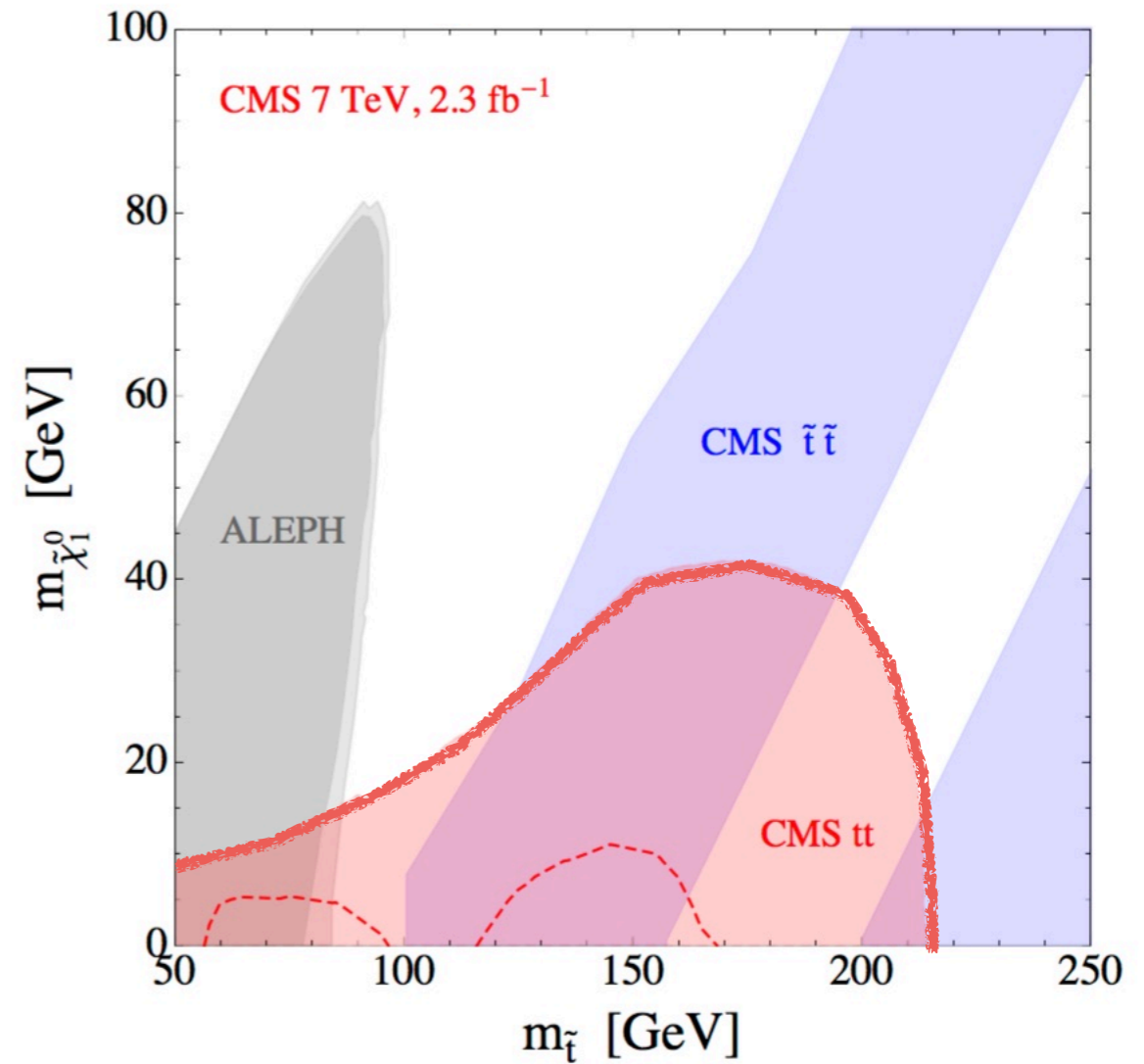
Improved determination of gluon density

Ratio to NNPDF2.3 NNLO, $\alpha_s = 0.118$



Czakon, et al
arXiv:1407.1043

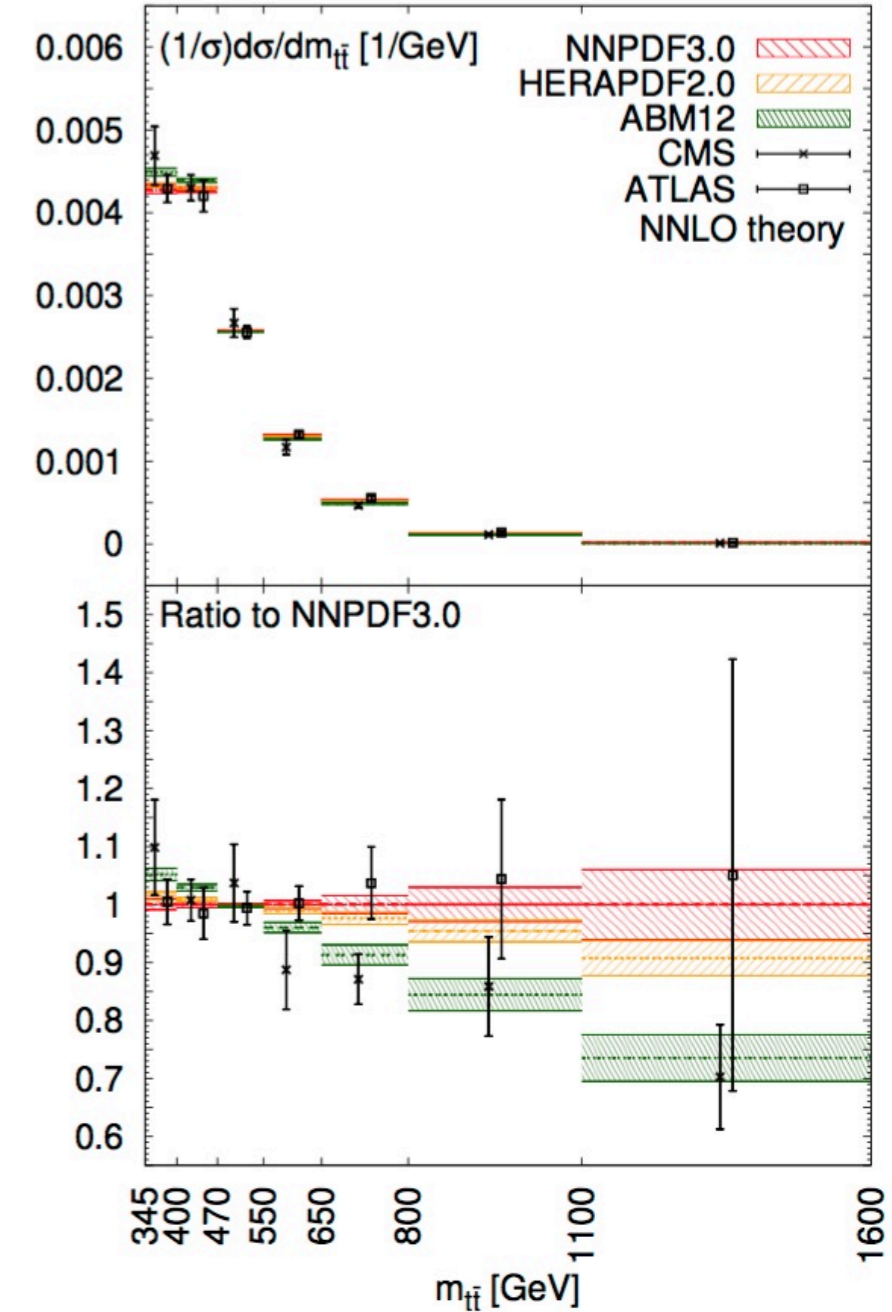
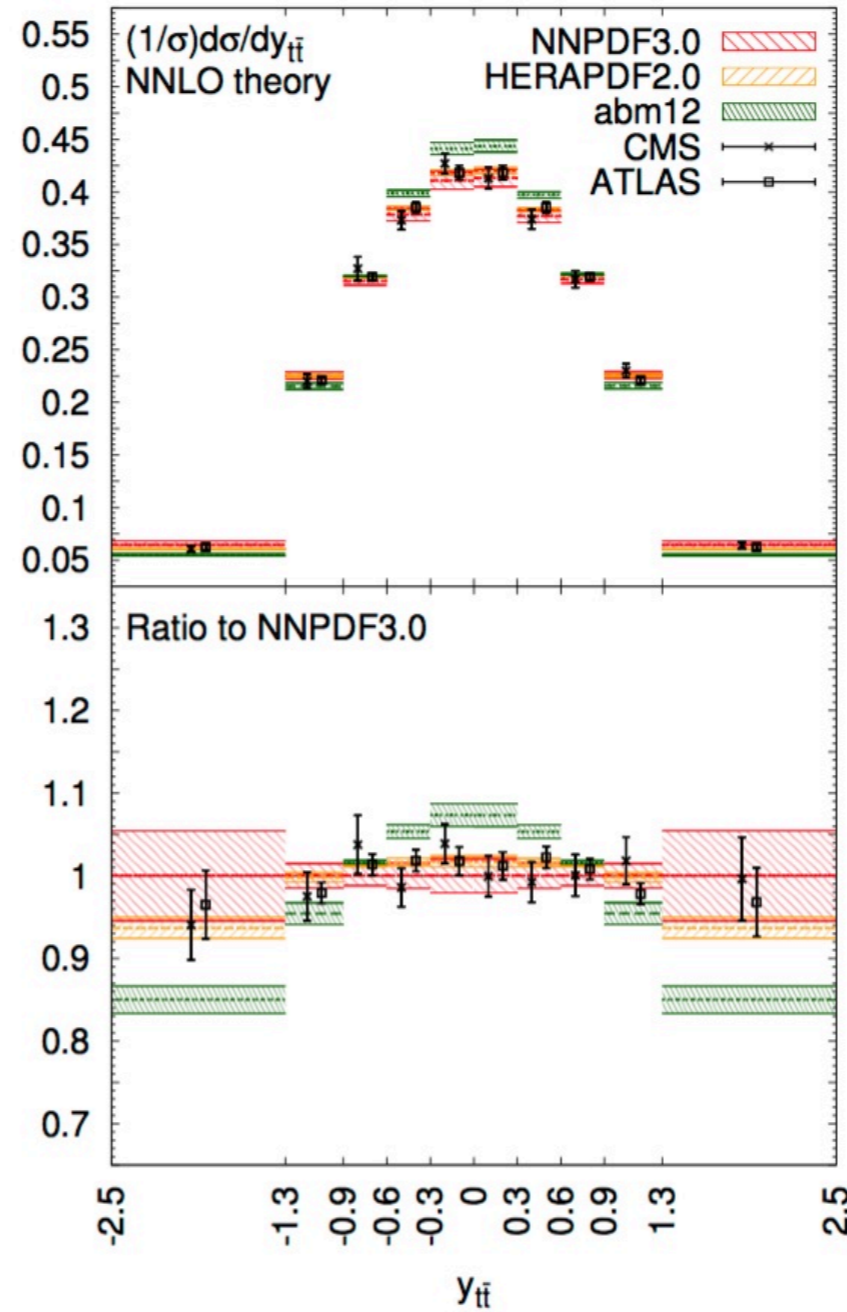
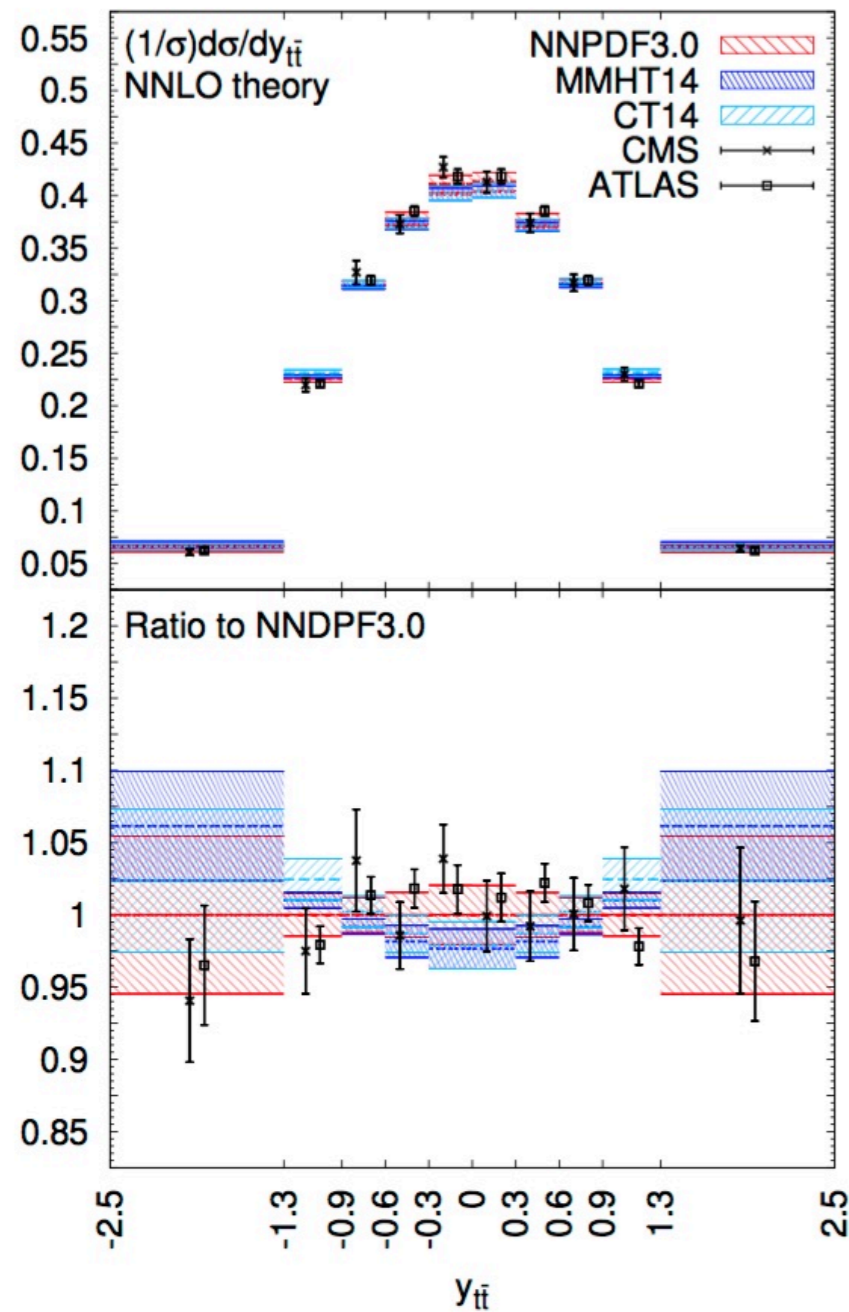
Limits on stop from $\sigma_{\text{TH}}(t\bar{t})$ vs $\sigma_{\text{exp}}(t\bar{t})$



Czakon, Papucci Mitov Rudermann Weiler,
arXiv:1407.1043

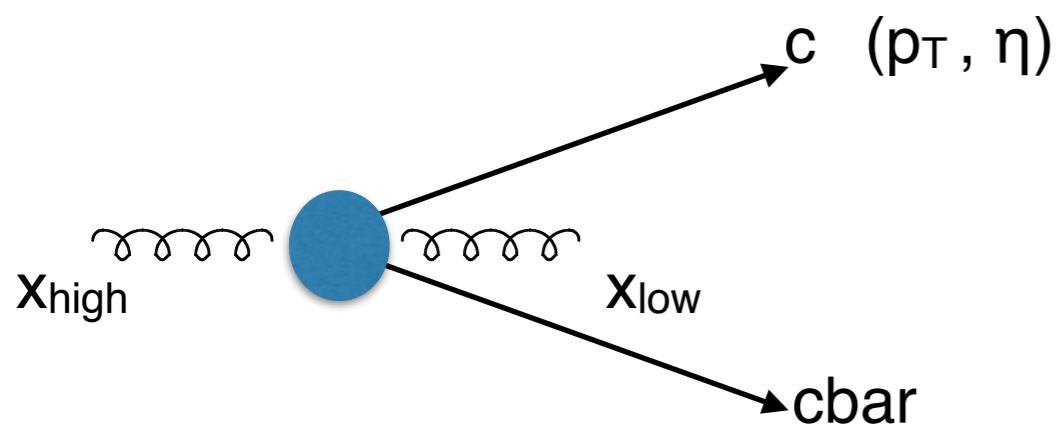
Top quark spectra @ NNLO vs PDF fits

M.Czakon et al, arXiv:1611.08609

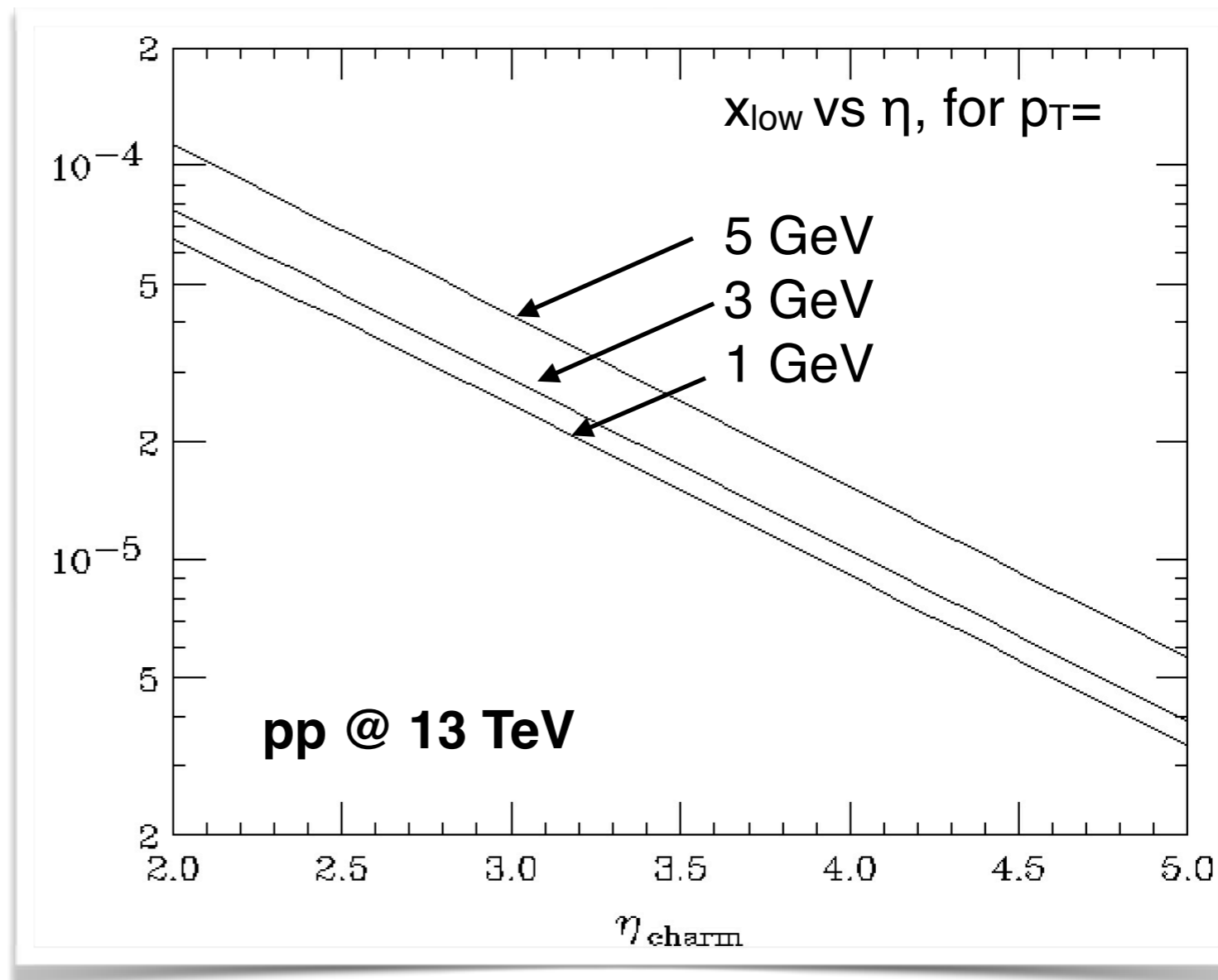


The sensitivity of measurements and TH has reached the few-% level also for complex processes like t-tbar production.
The measurement of distributions complement the total XS info, in sorting out PDF effects vs possible new physics effects

Forward charm as a probe of small-x gluons

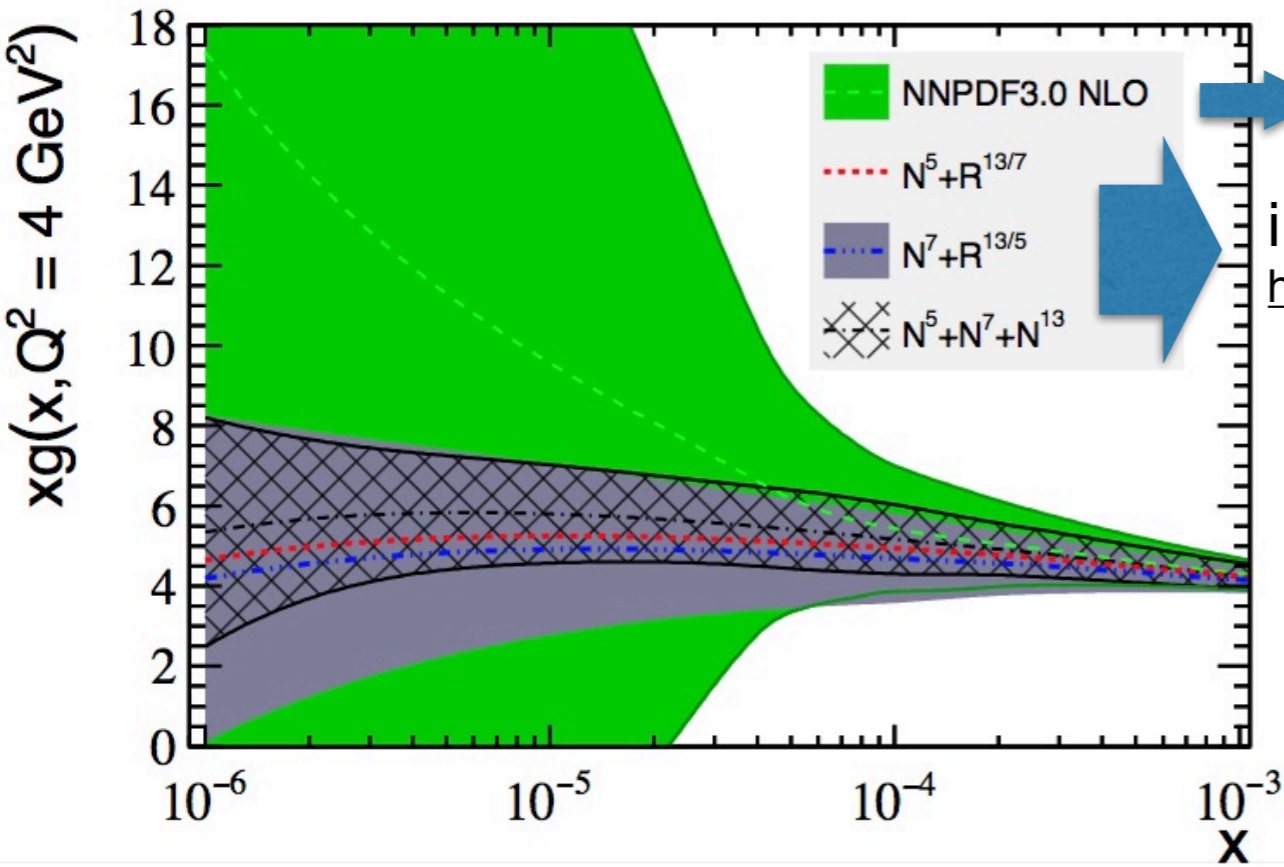


The **LHCb** experiment, with coverage for $2.5 < \eta < 5$, has a reach in the 10^{-6} range



Forward charm production at LHCb, implications for cosmic ray physics

Gauld, Rojo: <http://arxiv.org/abs/arXiv:1610.09373>



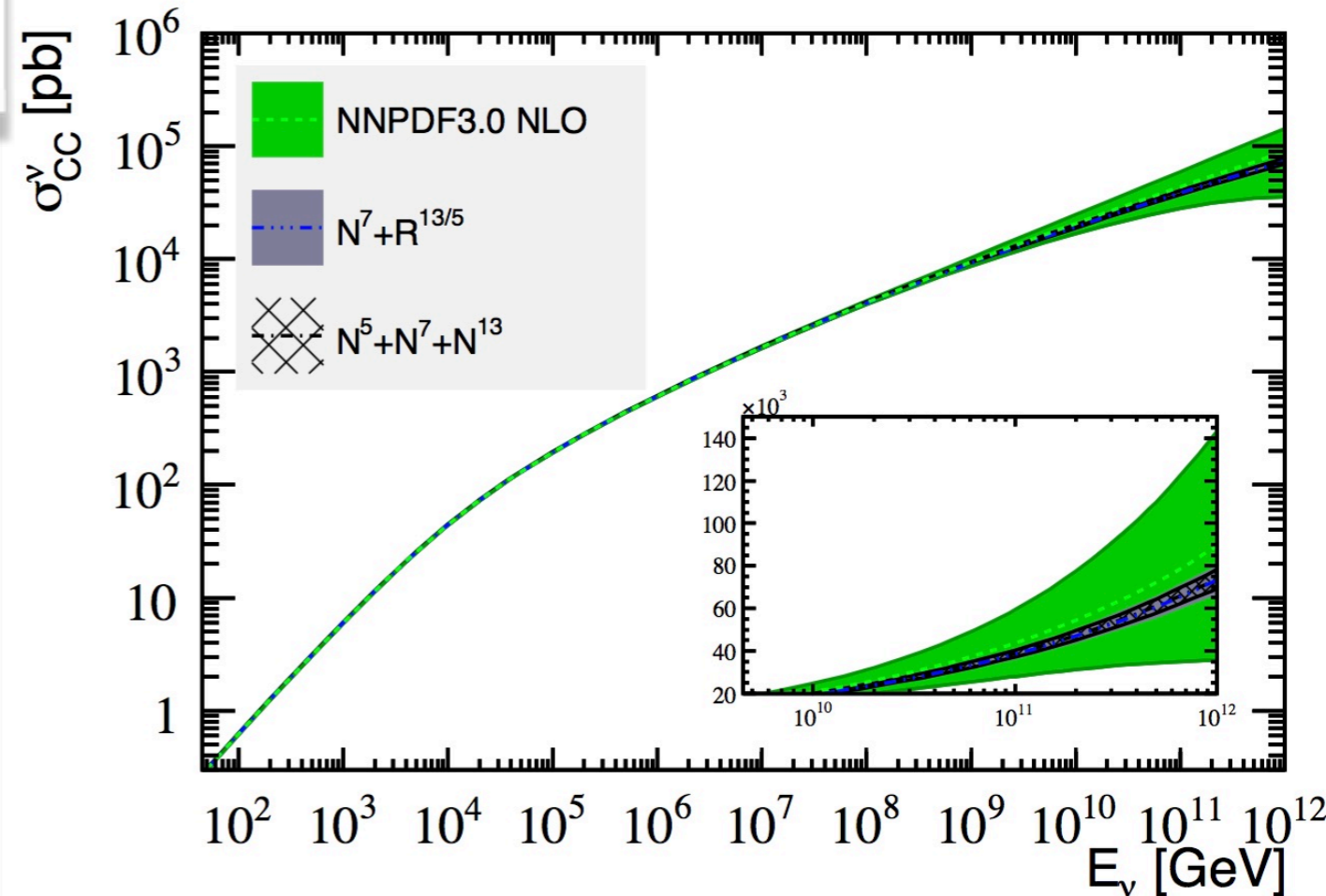
only HERA small-x data

inclusion of LHCb charm data in the fits
<http://arxiv.org/abs/arXiv:1610.02230>

$$N_X^{ij} = \frac{d^2\sigma(X \text{ TeV})}{dy_i^D d(p_T^D)_j} \bigg/ \frac{d^2\sigma(X \text{ TeV})}{dy_{\text{ref}}^D d(p_T^D)_j},$$

$$R_{13/X}^{ij} = \frac{d^2\sigma(13 \text{ TeV})}{dy_i^D d(p_T^D)_j} \bigg/ \frac{d^2\sigma(X \text{ TeV})}{dy_i^D d(p_T^D)_j},$$

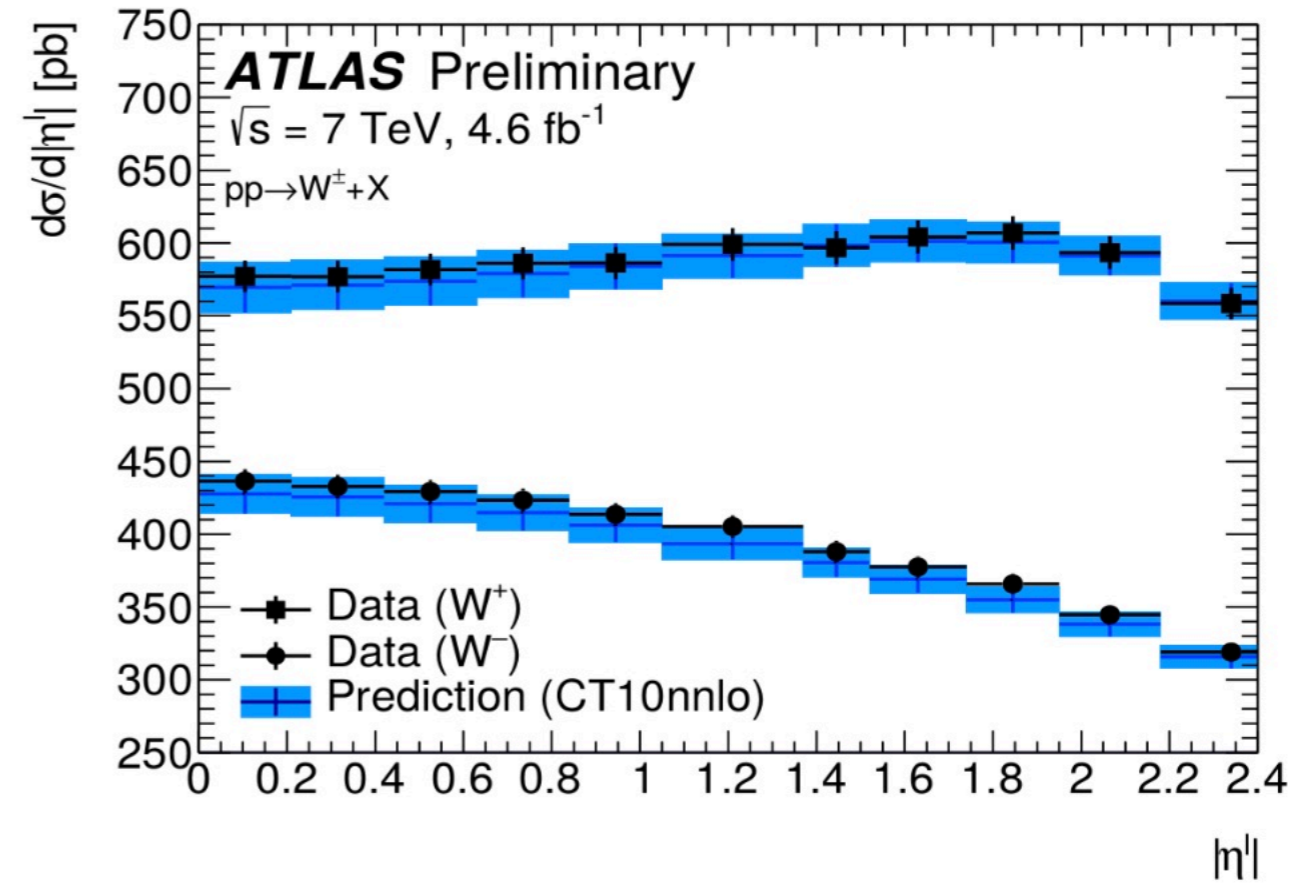
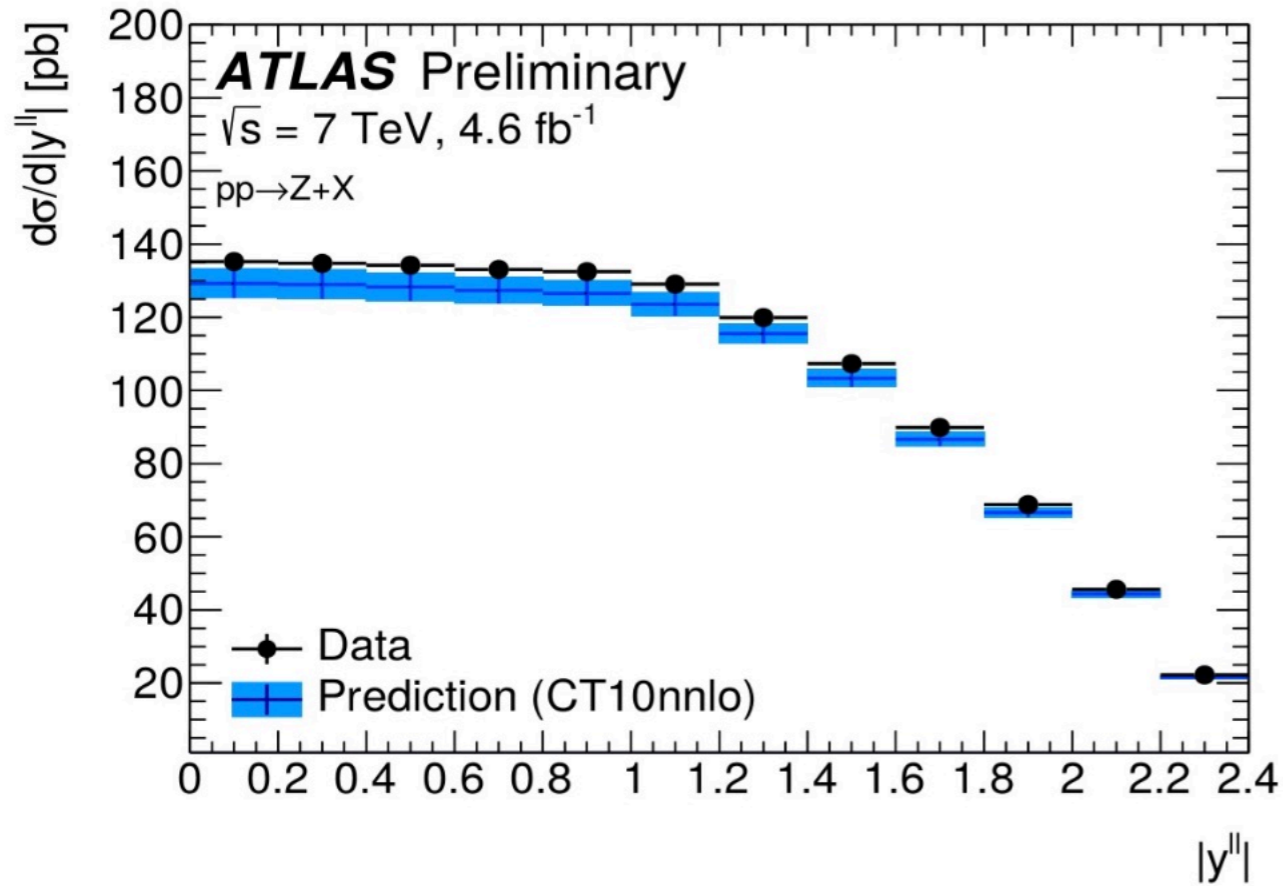
The reduction in small-x gluon PDF uncertainty leads to a reduction in systematics for the calculation of the cross sections of cosmic high-energy neutrinos



Examples of PDF-sensitive precision measurements of SM parameters

W mass

ATLAS-CONF-2016-113



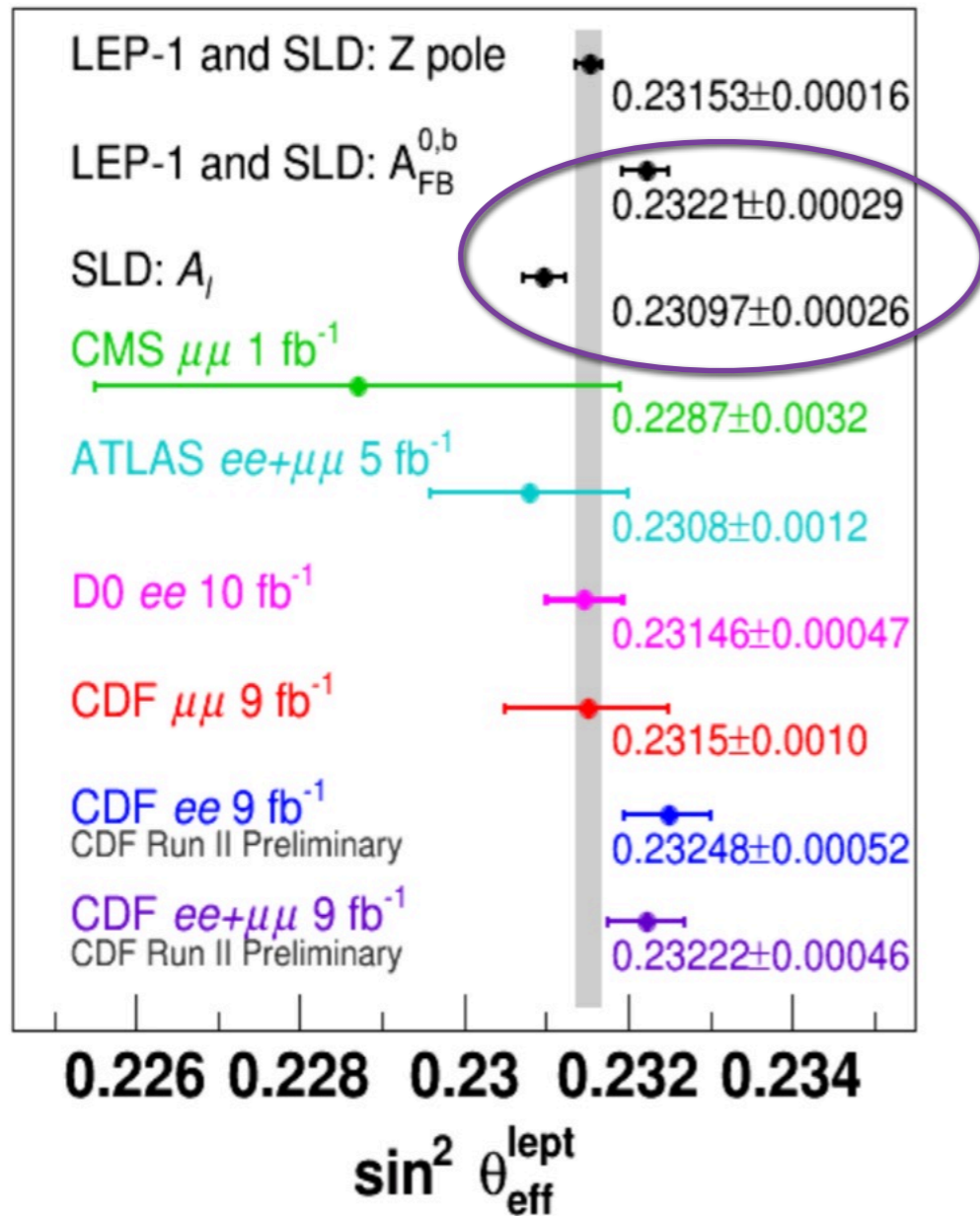
W-boson charge Kinematic distribution	W^+		W^-		Combined	
	p_T^ℓ	m_T	p_T^ℓ	m_T	p_T^ℓ	m_T
δm_W [MeV]						
Fixed-order PDF uncertainty	13.1	14.9	12.0	14.2	8.0	8.7
AZ tune	3.0	3.4	3.0	3.4	3.0	3.4
Charm-quark mass	1.2	1.5	1.2	1.5	1.2	1.5
Parton shower μ_F with heavy-flavour decorrelation	5.0	6.9	5.0	6.9	5.0	6.9
Parton shower PDF uncertainty	3.6	4.0	2.6	2.4	1.0	1.6
Angular coefficients	5.8	5.3	5.8	5.3	5.8	5.3
Total	15.9	18.1	14.8	17.2	11.6	12.9

$$m_W = 80.370 \pm 0.007 \text{ (stat.)} \pm 0.011 \text{ (exp.syst.)} \pm 0.014 \text{ (mod.syst.) GeV}$$

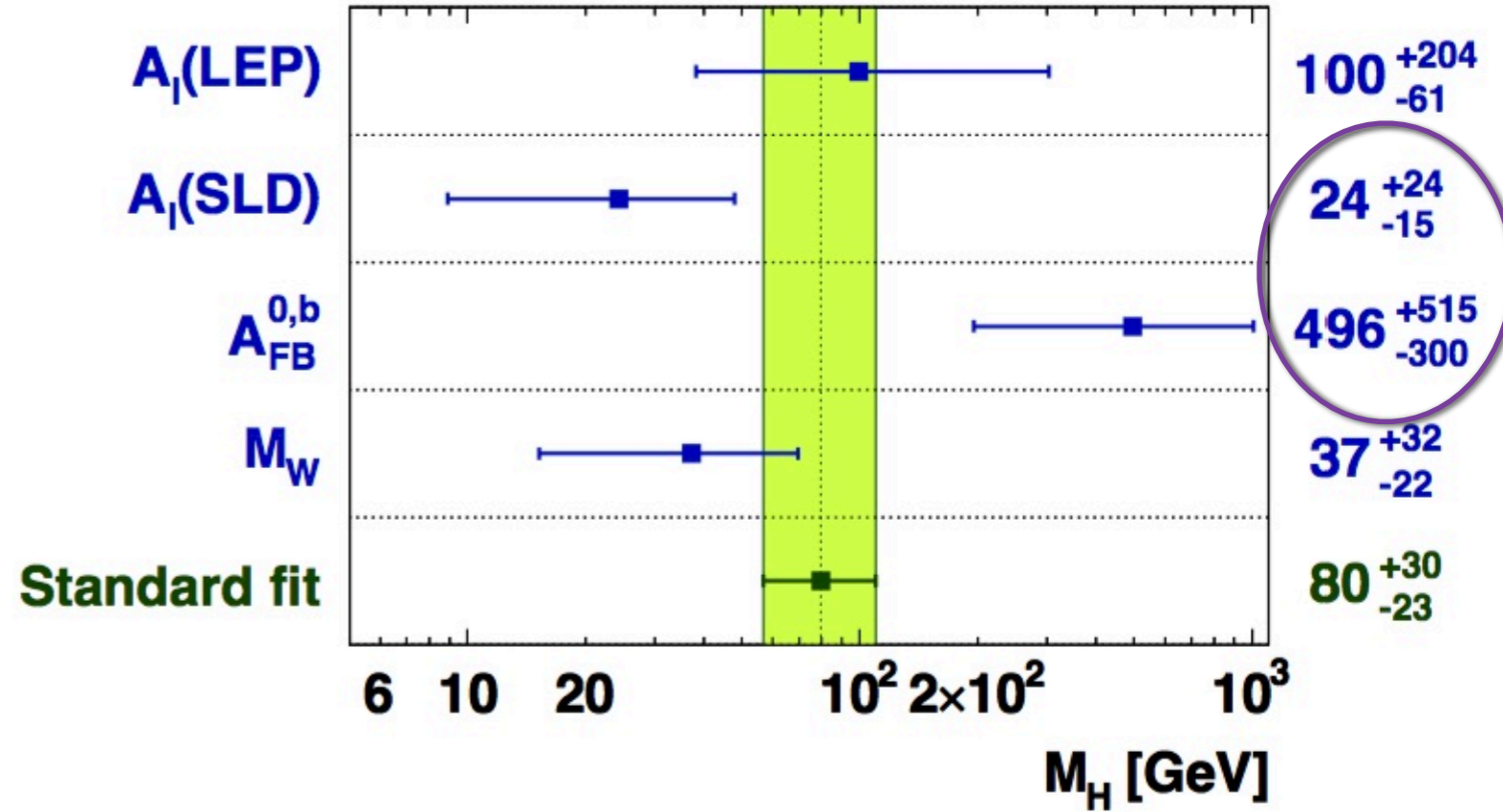
$$= \underline{80.370 \pm 0.019 \text{ GeV}}$$

$\sin^2\theta_w$

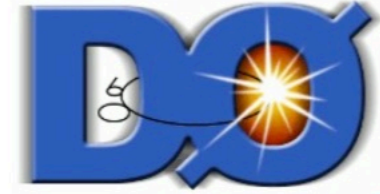
$\Delta = 0.00123 \pm 0.00040$
 $\Rightarrow \sim 3 \sigma$



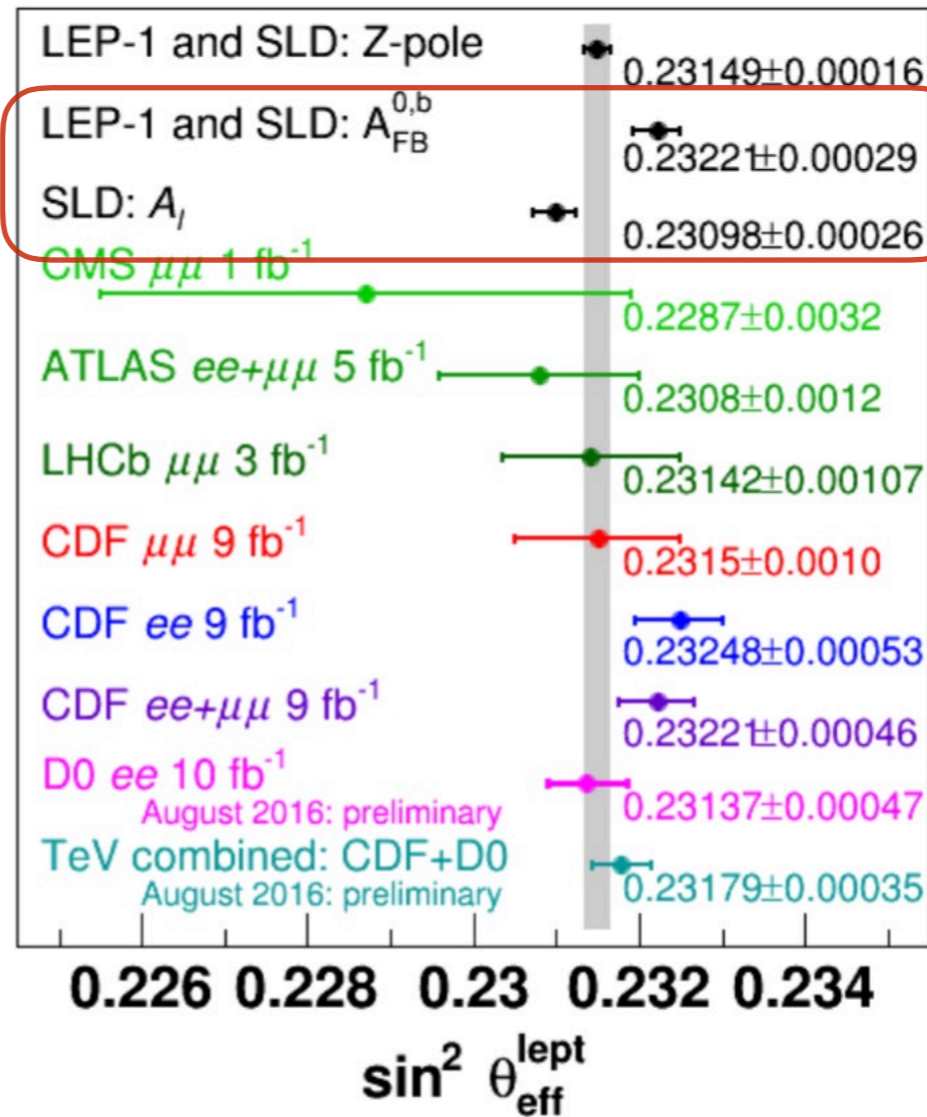
Gfitter, arXiv:0811.0009



$\sin^2\theta_w$ at the Tevatron



$\Delta = 0.00123 \pm 0.00040$
 $\Rightarrow \sim 3 \sigma$



Phys. Rep. 427, 257 (2006)
 Phys. Rep. 532, 119 (2013)

Phys. Rev. D84, 11202 (2011)

J. High Energy Phys. 09 (2015) 049

J. High Energy Phys. 11 (2015) 190

Phys. Rev. D89, 072005 (2014)

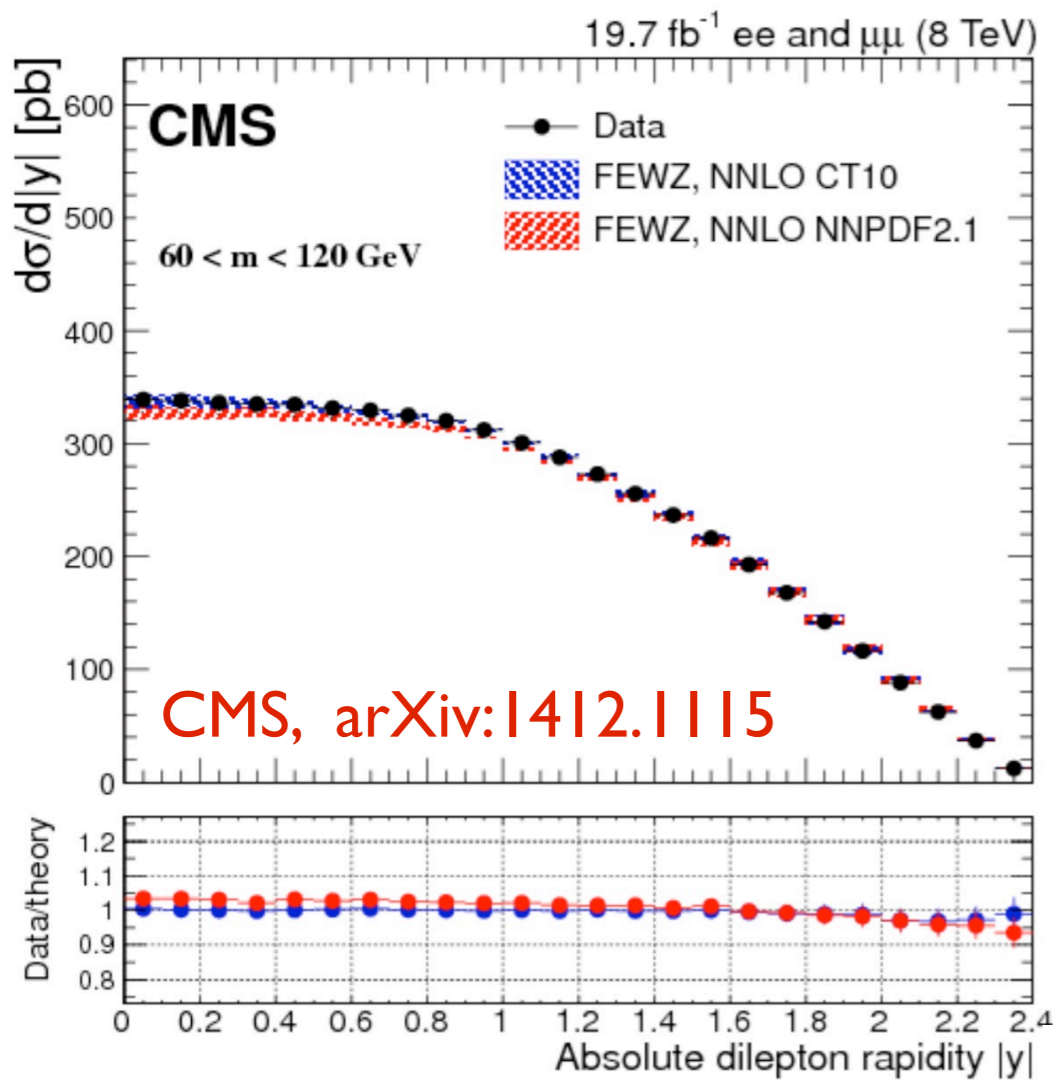
Phys. Rev. D93, 112016 (2016)

ICHEP preliminary: this talk

Willis Sakumoto
 University of Rochester

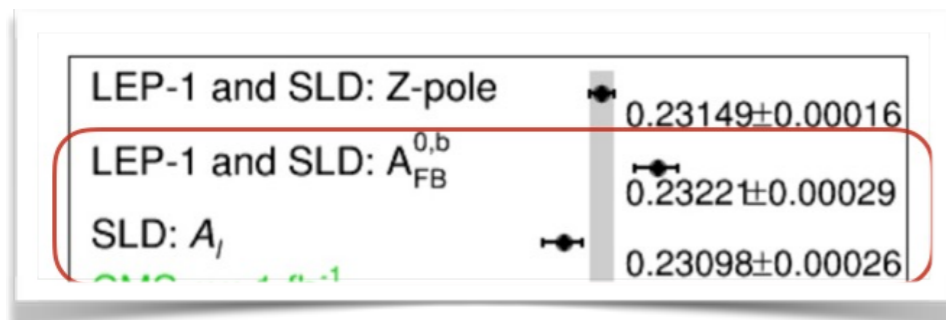
for the CDF and D0 Collaborations

$\sin^2\theta_W$ at the LHC ?



⇒ opens prospects for a precise measurement of $\sin\theta_W$ from FB lepton asymmetry in Z^0 decays at large y

CMS like detector Energy data sample	20 fb^{-1} 8 TeV current	$\approx 200 fb^{-1}$ 13-14 TeV future
Number of reconstructed events	8.2M $\mu^+\mu^-$ 6.8M e^+e^-	$\approx 120M \mu^+\mu^-$
$\Delta \sin^2 \theta_W$ CT10 PDF error	± 0.00090	± 0.00090
$\Delta \sin^2 \theta_W$ NNPDF3.0 NNLO error	± 0.00050	± 0.00050
$\Delta \sin^2 \theta_W$ χ^2 Weighted PDF error	± 0.00022	± 0.00014
$\Delta \sin^2 \theta_W$ statistical error	± 0.00034	± 0.00011
Stat+ χ^2 weighted PDF error	± 0.00040	± 0.00018

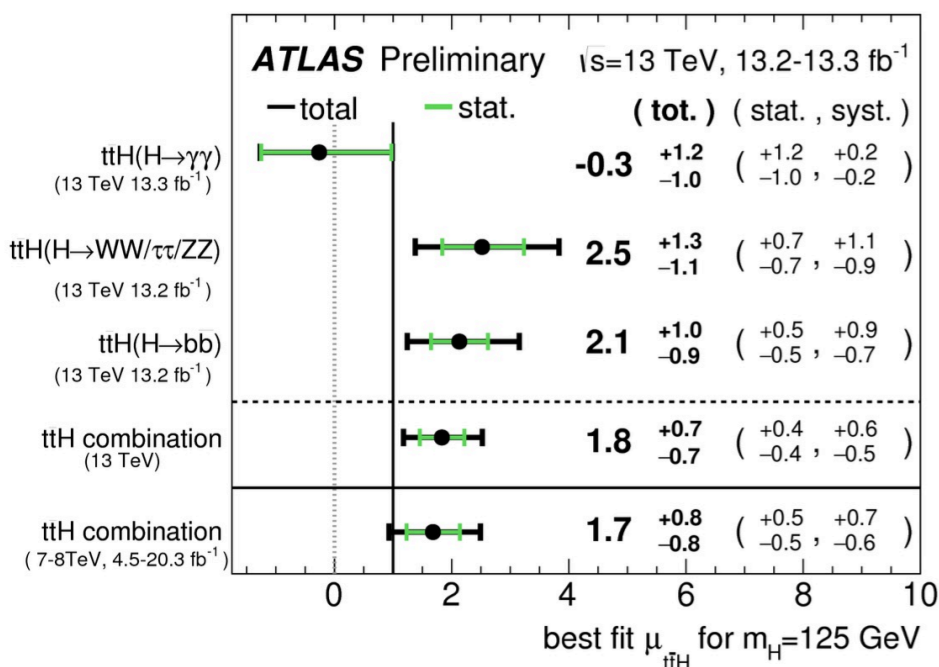


Bodek, Han, Khukhunaishvili, Sakumoto,
arXiv:1507.02470

QCD and progress in the measurement of the Higgs boson properties

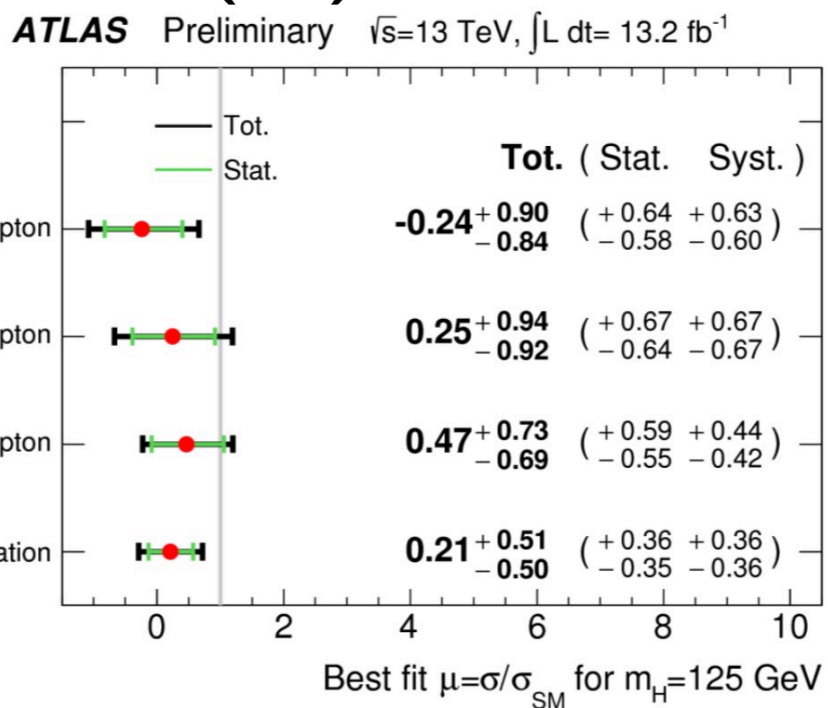
Highlights of 2015-16 Higgs measurements

ttH



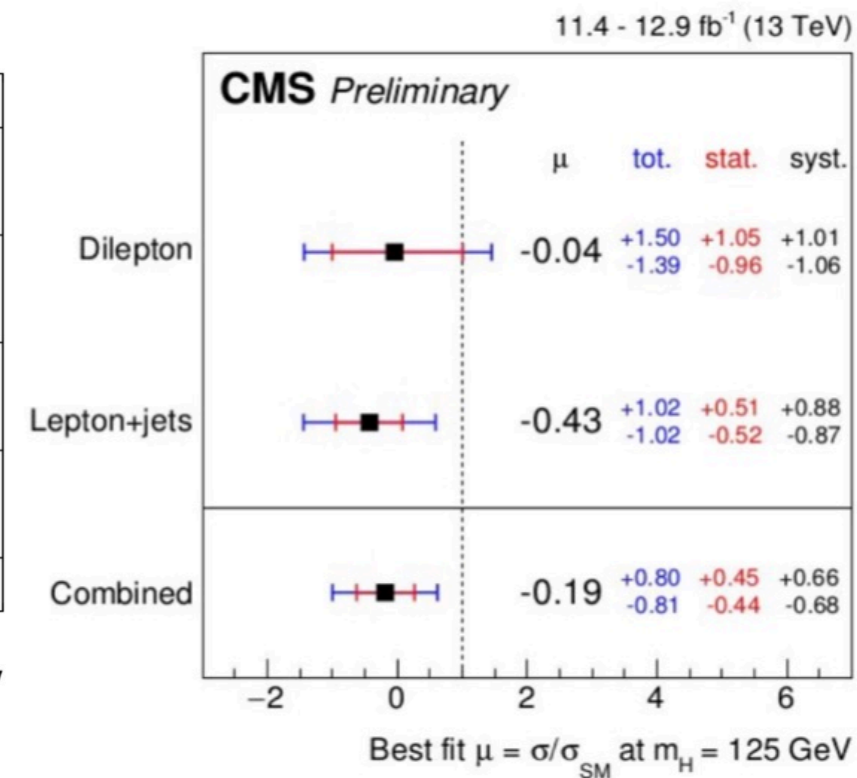
too much

VH(bb)



too little

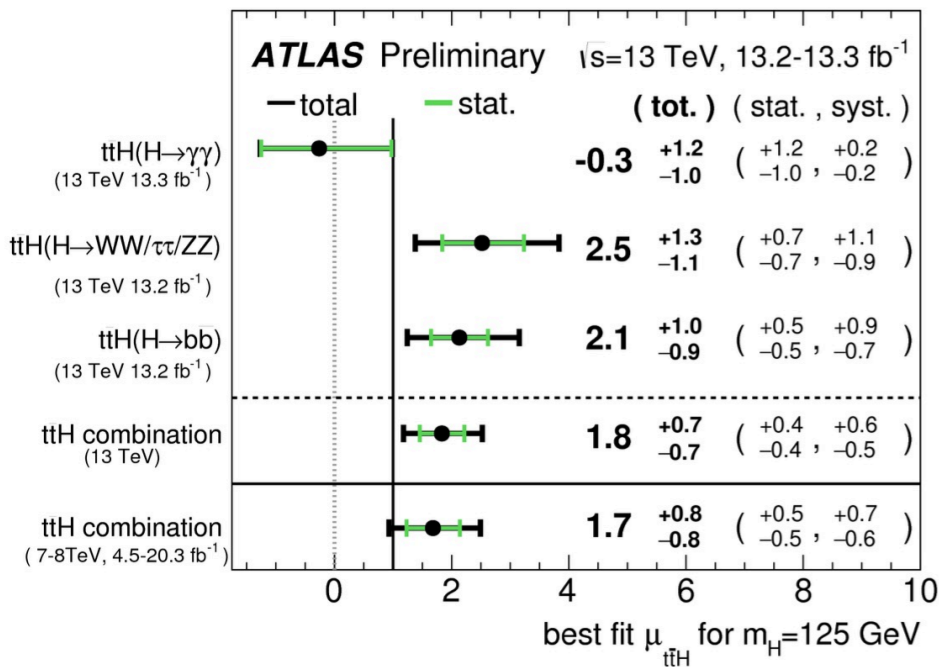
ttH ($\rightarrow bb$)



....

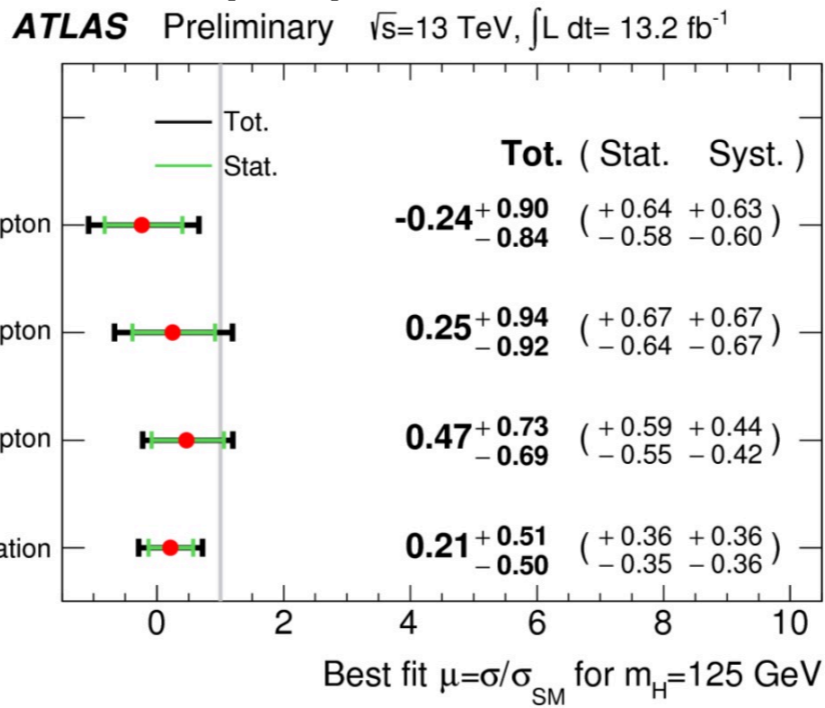
Highlights of 2015-16 Higgs measurements

ttH



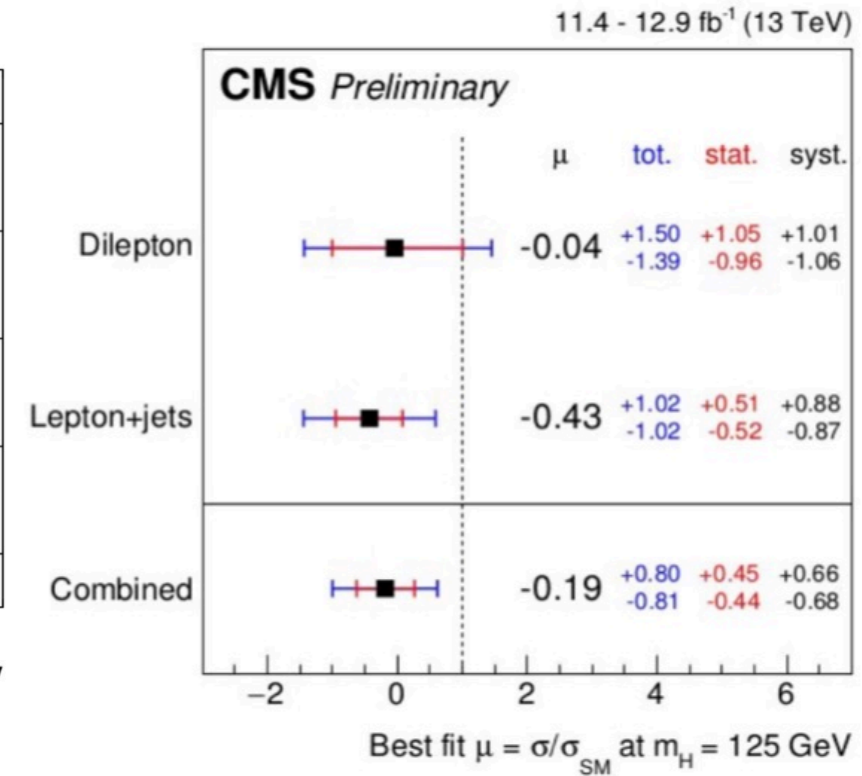
too much

VH(bb)

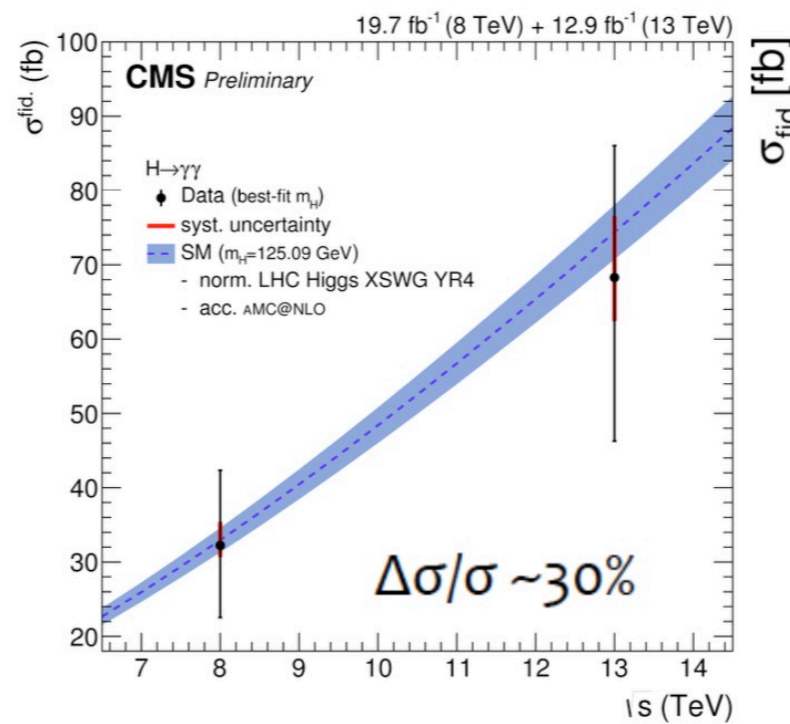
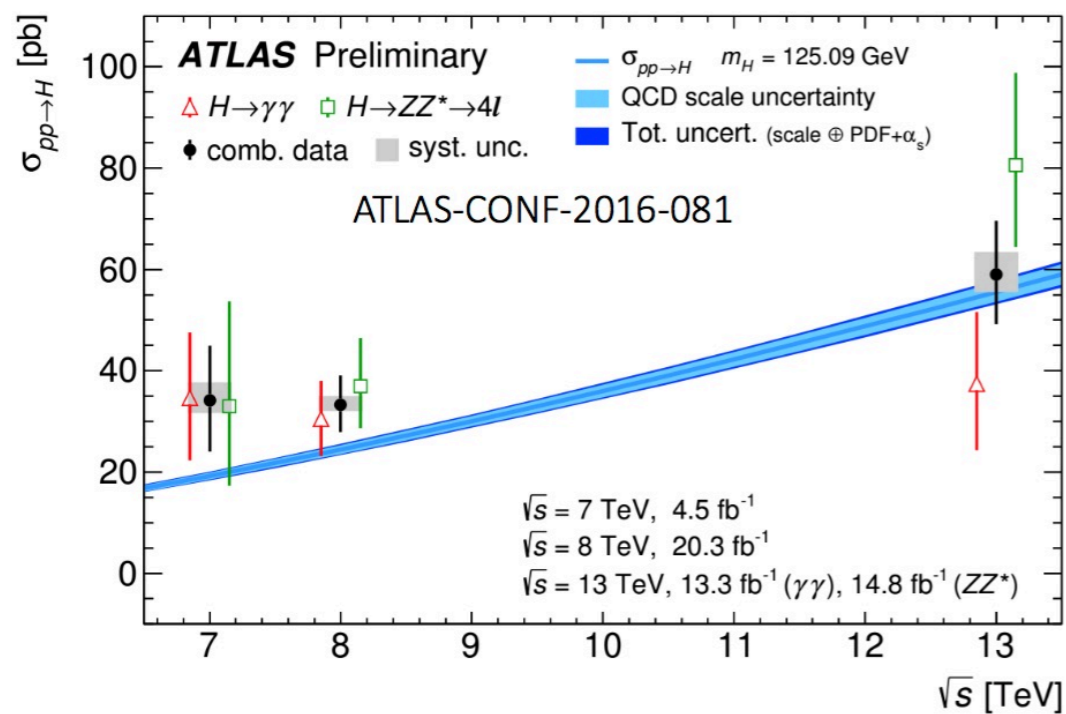


too little

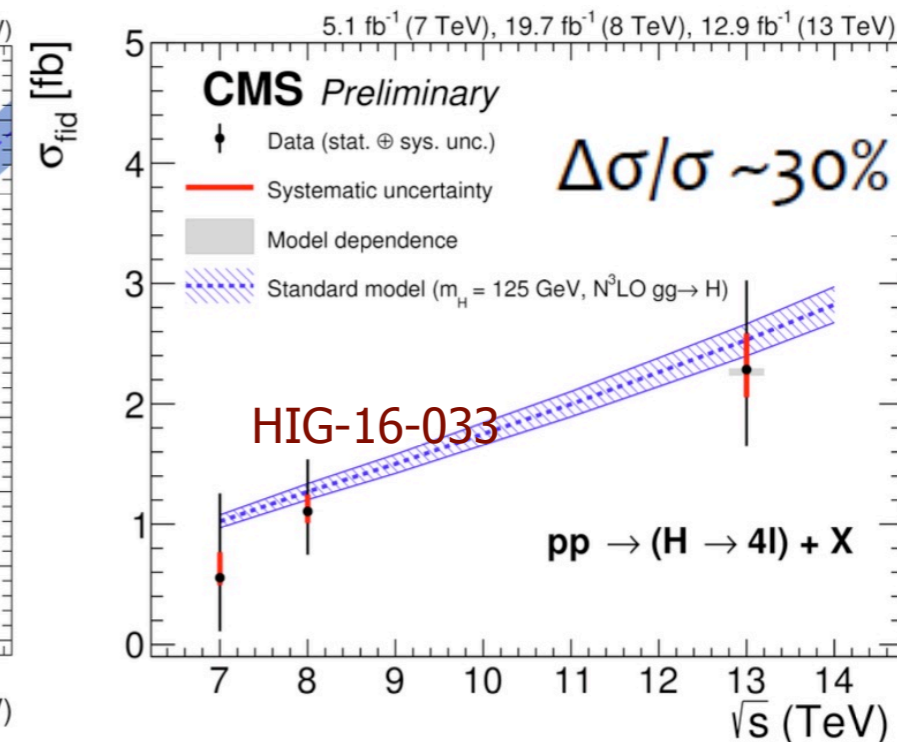
ttH (\rightarrow bb)



....



just about right ...



Future evolution of Higgs statistics

July '16
End '18
End '23
~ 2035

\mathcal{L} [fb ⁻¹]	All	$H \rightarrow \gamma\gamma$	$H \rightarrow ZZ \rightarrow 4l$	$H \rightarrow WW^* \rightarrow l\nu l\nu$
13.3	0.75M	600	20	400
120	7M	6,000	200	4,000
300	17M	14,000	500	10,000
3000	170M	140,000	5,000	100,000

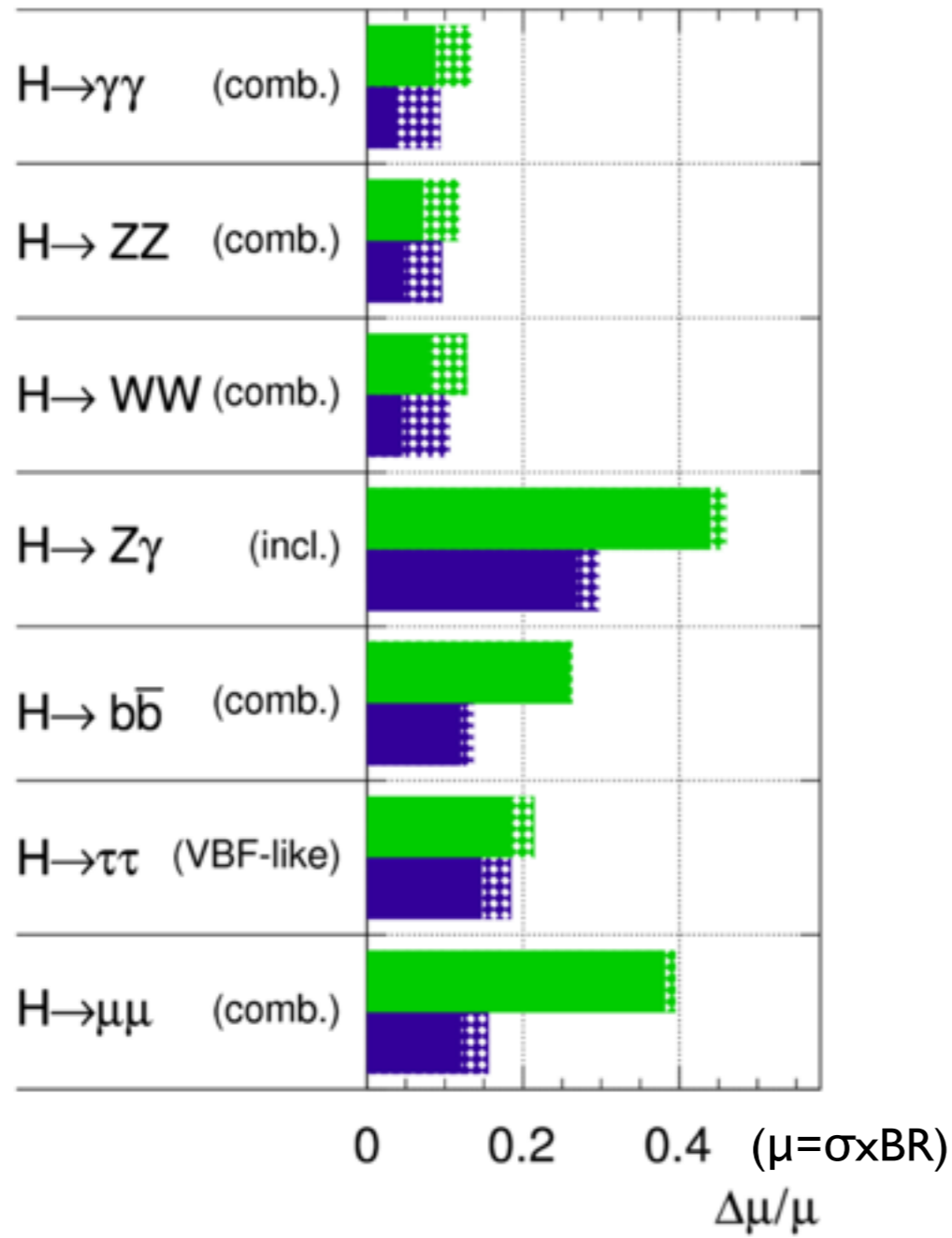
include estimates of analysis cuts and efficiencies

Projected precision on H couplings

ATL-PHYS-PUB-2014-016

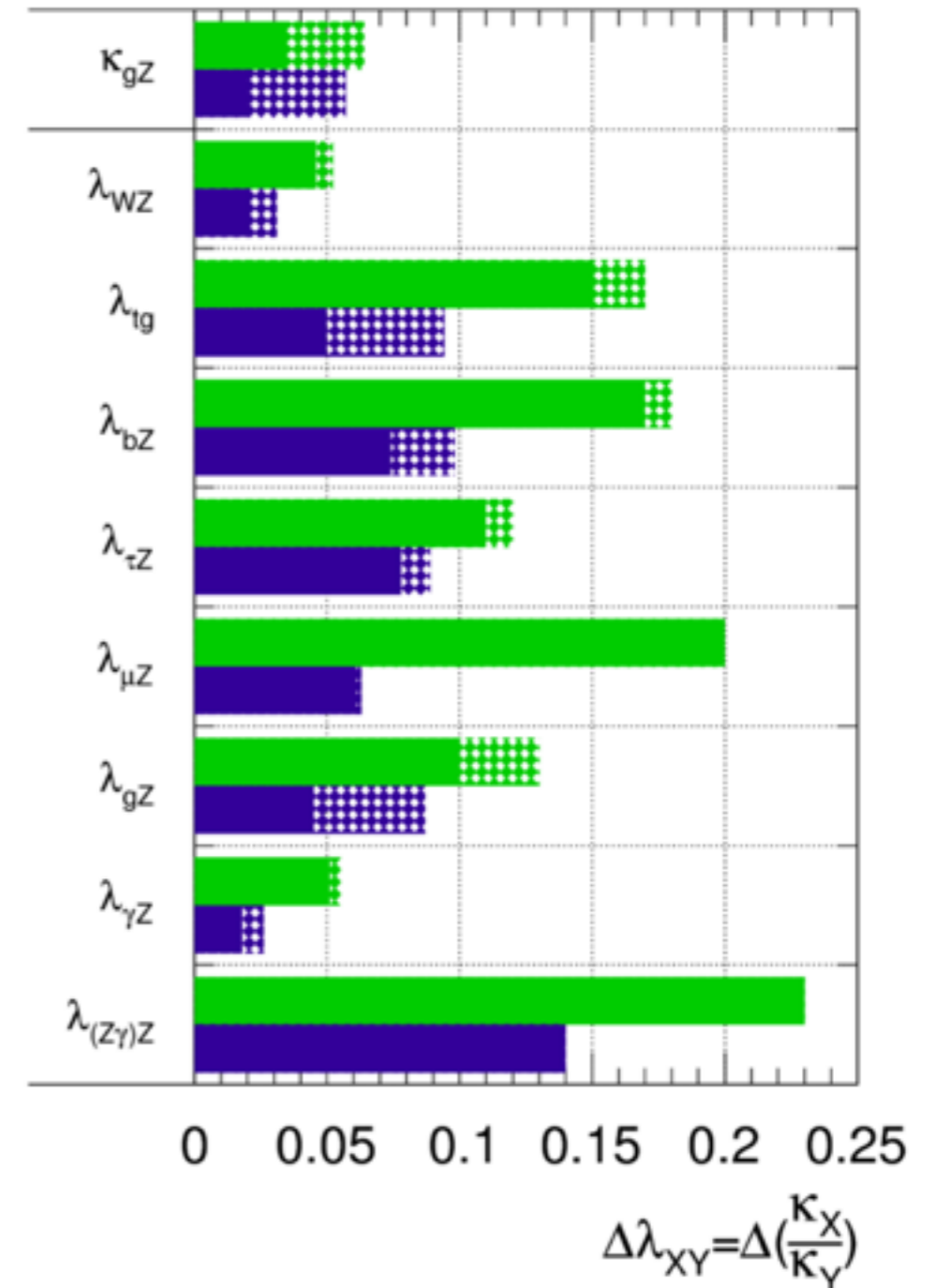
ATLAS Simulation Preliminary

$\sqrt{s} = 14 \text{ TeV}$: $\int \mathcal{L} dt = 300 \text{ fb}^{-1}$; $\int \mathcal{L} dt = 3000 \text{ fb}^{-1}$



ATLAS Simulation Preliminary

$\sqrt{s} = 14 \text{ TeV}$: $\int \mathcal{L} dt = 300 \text{ fb}^{-1}$; $\int \mathcal{L} dt = 3000 \text{ fb}^{-1}$



solid areas: no TH systematics
shaded areas: with TH systematics

On theory uncertainties

ATLAS Simulation Preliminary

$\sqrt{s} = 14$ TeV: $\int L dt = 300 \text{ fb}^{-1}$; $\int L dt = 3000 \text{ fb}^{-1}$

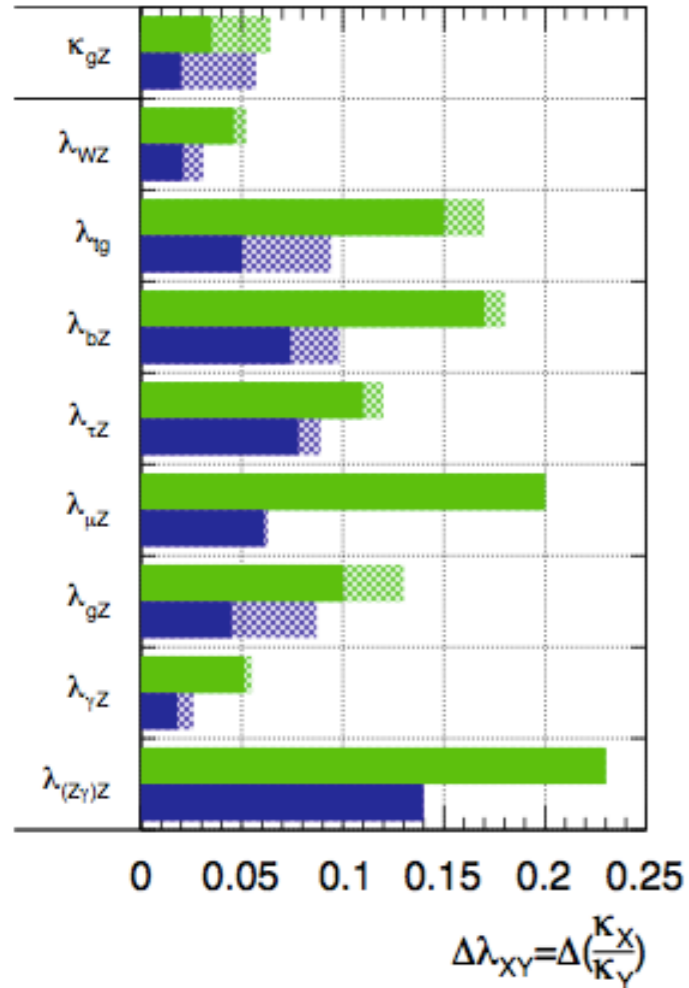


Figure 3: Relative uncertainty expected for the determination of coupling scale factor ratios λ_{XY} in a generic fit without assumptions, assuming a SM Higgs boson with a mass of 125 GeV and with 300 fb^{-1} or 3000 fb^{-1} of 14 TeV LHC data. The hashed areas indicate the increase of the estimated error due to current theory systematic uncertainties.

Scenario	Status 2014	Deduced size of uncertainty to increase total uncertainty by $\lesssim 10\%$							
		for 300 fb^{-1}			for 3000 fb^{-1}				
Theory uncertainty (%)	[10–12]	κ_{gZ}	λ_{gZ}	$\lambda_{\gamma Z}$	κ_{gZ}	$\lambda_{\gamma Z}$	λ_{gZ}	$\lambda_{\tau Z}$	λ_{ig}
<i>gg</i> → <i>H</i>									
PDF	8	2	-	-	1.3	-	-	-	-
incl. QCD scale (MHOU)	7	2	-	-	1.1	-	-	-	-
p_T shape and $0j \rightarrow 1j$ mig.	10–20	-	3.5–7	-	-	1.5–3	-	-	-
$1j \rightarrow 2j$ mig.	13–28	-	-	6.5–14	-	3.3–7	-	-	-
$1j \rightarrow \text{VBF } 2j$ mig.	18–58	-	-	-	-	-	6–19	-	-
VBF $2j \rightarrow \text{VBF } 3j$ mig.	12–38	-	-	-	-	-	-	6–19	-
VBF									
PDF	3.3	-	-	-	-	-	2.8	-	-
<i>t</i> \bar{t} <i>H</i>									
PDF	9	-	-	-	-	-	-	-	3
incl. QCD scale (MHOU)	8	-	-	-	-	-	-	-	2

Table 6: Estimation of the deduced size of theory uncertainties, in percent (%), for different Higgs coupling measurements in the generic Model 15 from Table 5, requiring that each source of theory systematic uncertainty affects the measurement by less than 30% of the total experimental uncertainty and hence increase the total uncertainty by less than 10%. A dash “-” indicates that the theory uncertainty from existing calculations [10–12] is already sufficiently small to fulfill the condition above for some measurements. The same applies to theory uncertainties not mentioned in the table for any measurement. The impact of the jet-bin and p_T related uncertainties in $gg \rightarrow H$ depends on analysis selections and hence no single number can be quoted. Therefore the range of uncertainty values used in the different analysis is shown.

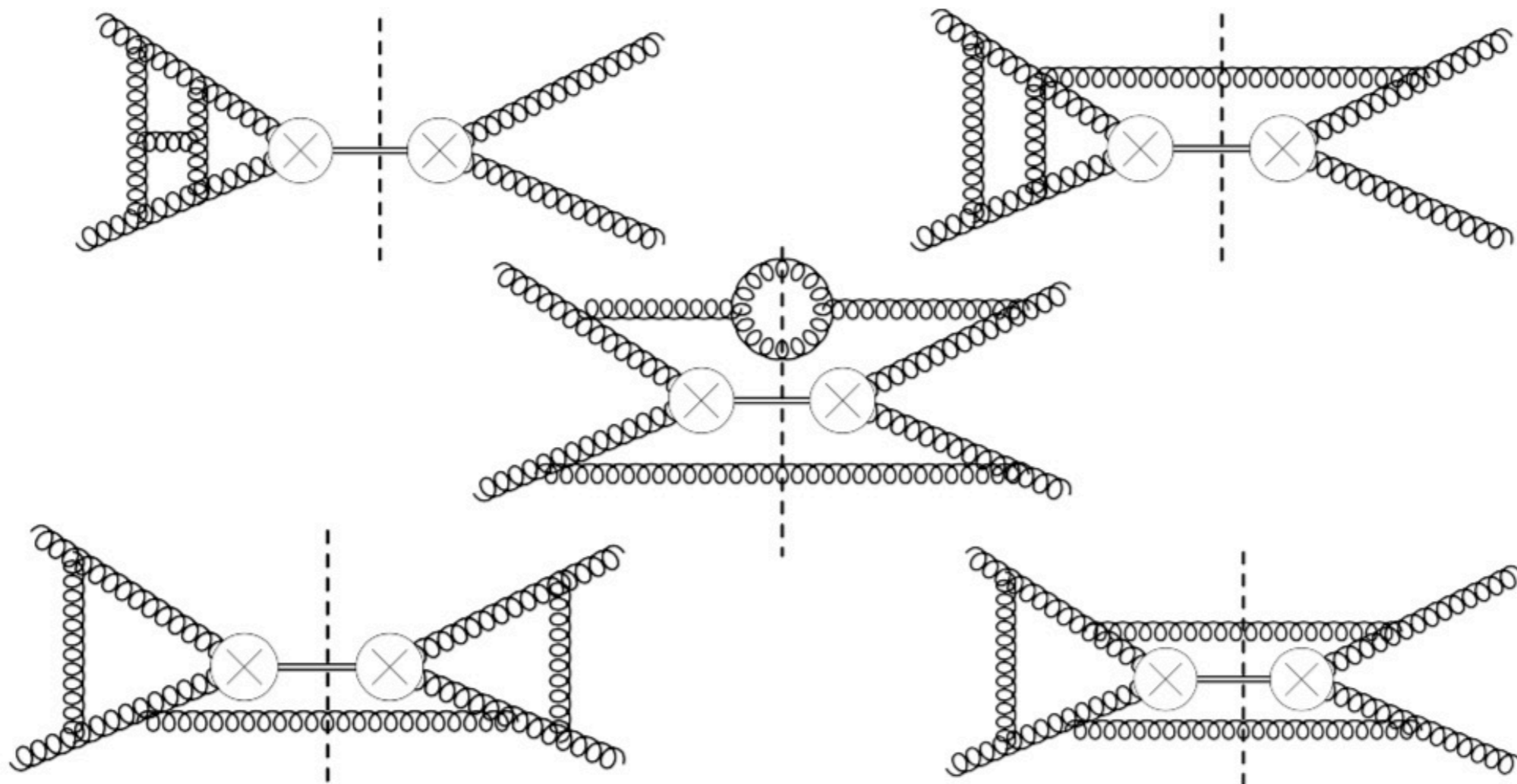
dominated by modeling

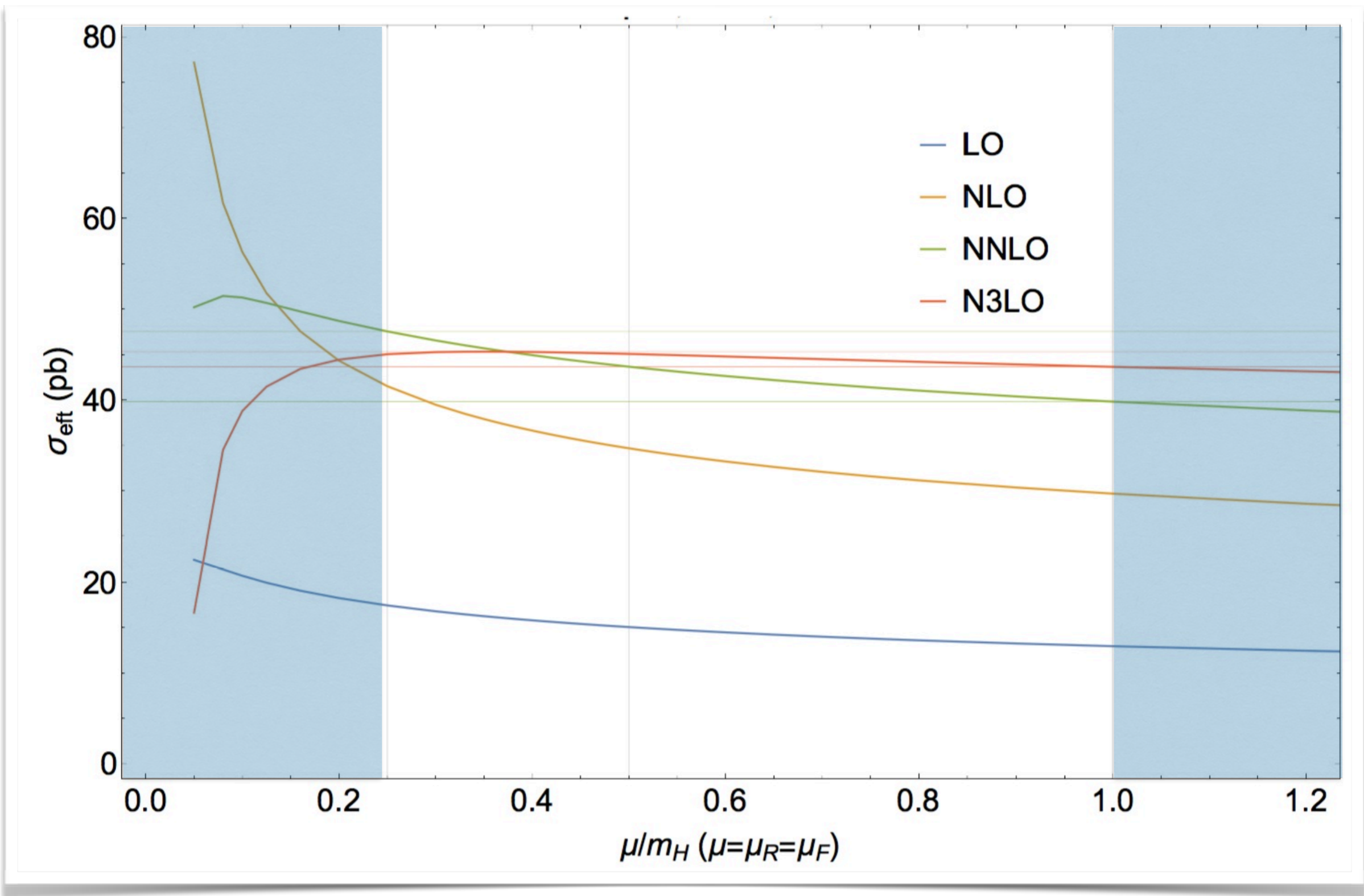
Example in TH progress: $pp \rightarrow \text{Higgs}$, via gg fusion, at $N^3\text{LO}$

High precision determination of the gluon fusion
Higgs boson cross-section at the LHC

Charalampos Anastasiou^a, Claude Duhr^{b,c*}, Falko Dulat^a, Elisabetta Furlan^a, Thomas Gehrmann^e, Franz Herzog^f, Achilles Lazopoulos^a, Bernhard Mistlberger^b

[arXiv:1602.00695](https://arxiv.org/abs/1602.00695)





NB $\sigma(\text{gg} \rightarrow \text{H}) \propto y_t^2 \implies \delta y_t / y_t \propto 0.5 \delta \sigma_{\text{TH}} / \sigma_{\text{TH}}$

48.58 pb =	16.00 pb	(+32.9%)	(LO, rEFT)
	+ 20.84 pb	(+42.9%)	(NLO, rEFT)
	- 2.05 pb	(-4.2%)	((t, b, c), exact NLO)
	+ 9.56 pb	(+19.7%)	(NNLO, rEFT)
	+ 0.34 pb	(+0.7%)	(NNLO, 1/m _t)
	+ 2.40 pb	(+4.9%)	(EW, QCD-EW)
	+ 1.49 pb	(+3.1%)	(N ³ LO, rEFT)

Lack of
NNNLO in
PDF evolution

Higher-order EW and mt
corrections

PDF fits
syst's

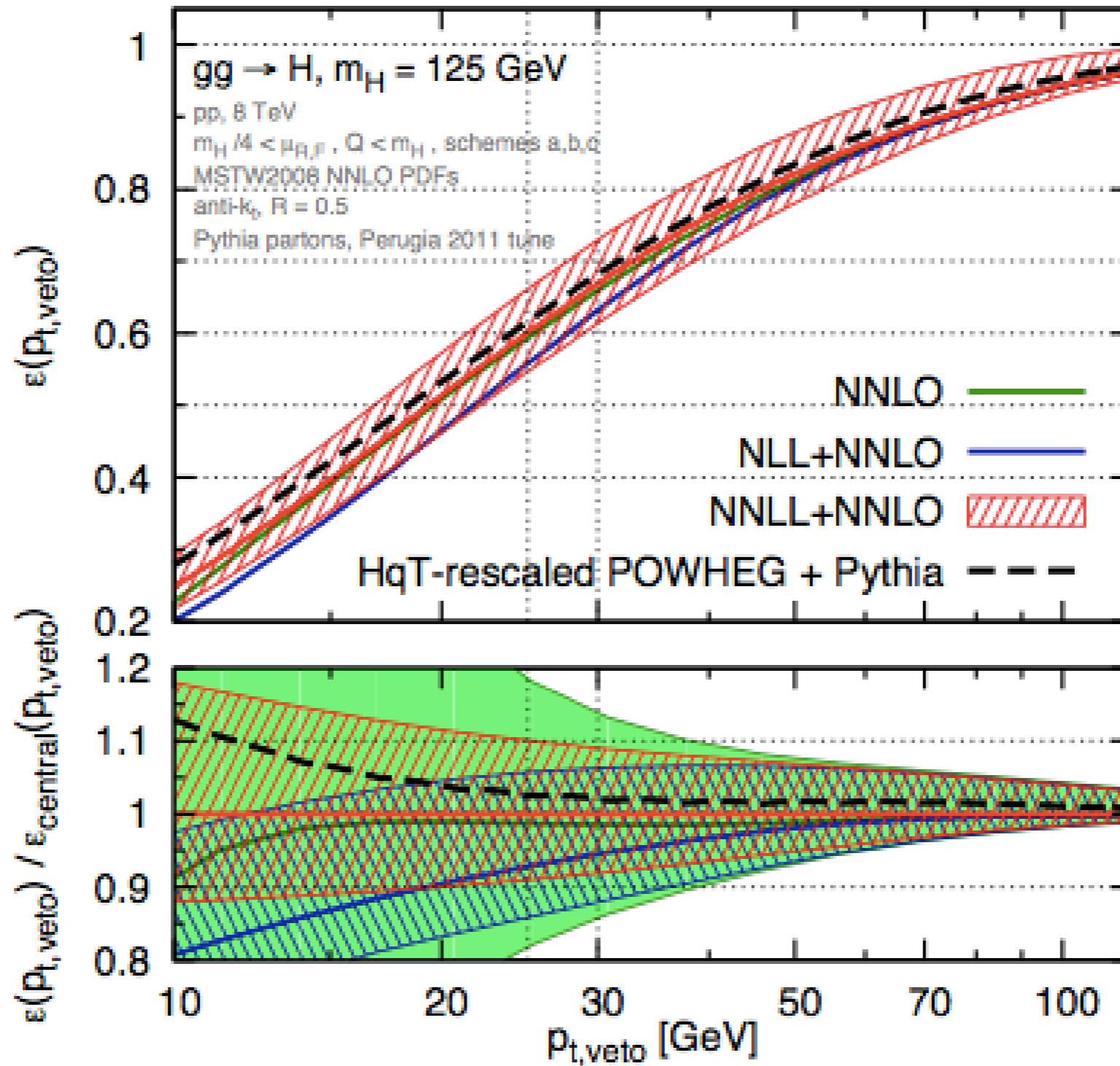
α_s
S_{syst}'s

δ(scale)	δ(trunc)	δ(PDF-TH)	δ(EW)	δ(t, b, c)	δ(1/m _t)	δ(PDF)	δ(α _s)
+0.10 pb -1.15 pb	±0.18 pb	±0.56 pb	±0.49 pb	±0.40 pb	±0.49 pb	±0.90 pb	+1.27pb -1.25pb
+0.21% -2.37%	±0.37%	±1.16%	±1%	±0.83%	±1%	±1.86%	+2.61% -2.58%

E_{CM}	σ	δ(theory)	δ(PDF)	δ(α _s)
13 TeV	48.58 pb	+2.22pb (+4.56%) -3.27pb (-6.72%)	± 0.90 pb (± 1.86%)	+1.27pb (+2.61%) -1.25pb (-2.58%)

Example of theoretical modeling systematics in the interpretation of Higgs measurements: jet vetoes

Jet veto required to reduce $t\bar{t}b\bar{g}$'s to $H \rightarrow WW^*$



Digression: the importance of EW bosons' p_T distributions in hadronic collisions

Nuclear Physics B246 (1984) 12–44
© North-Holland Publishing Company

VECTOR BOSON PRODUCTION AT COLLIDERS: A THEORETICAL REAPPRAISAL

G. ALTARELLI

*CERN, Geneva, Switzerland and Dipartimento di Fisica, Università “La Sapienza”, Roma, Italy
INFN, Sezione di Roma, Italy*

R.K. ELLIS*

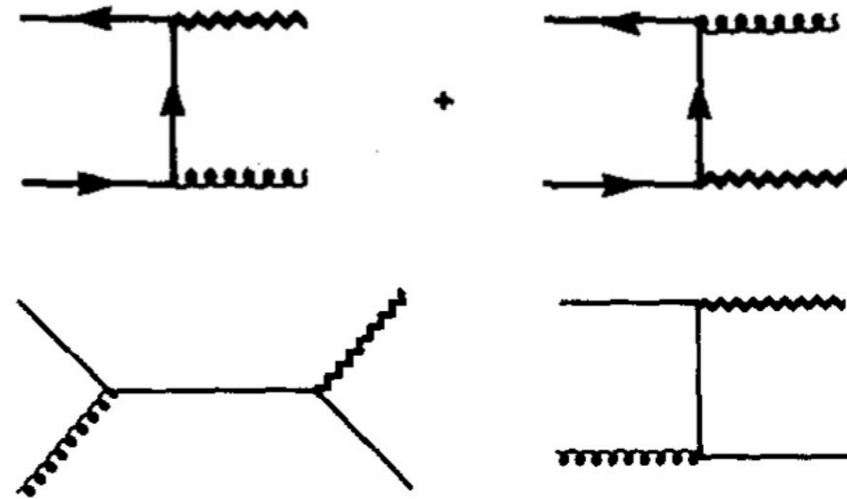
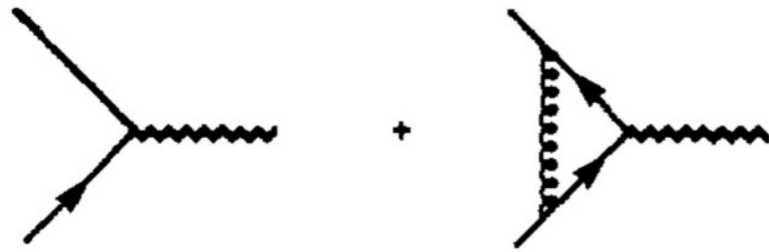
INFN, Sezione di Roma, Italy

M. GRECO and G. MARTINELLI

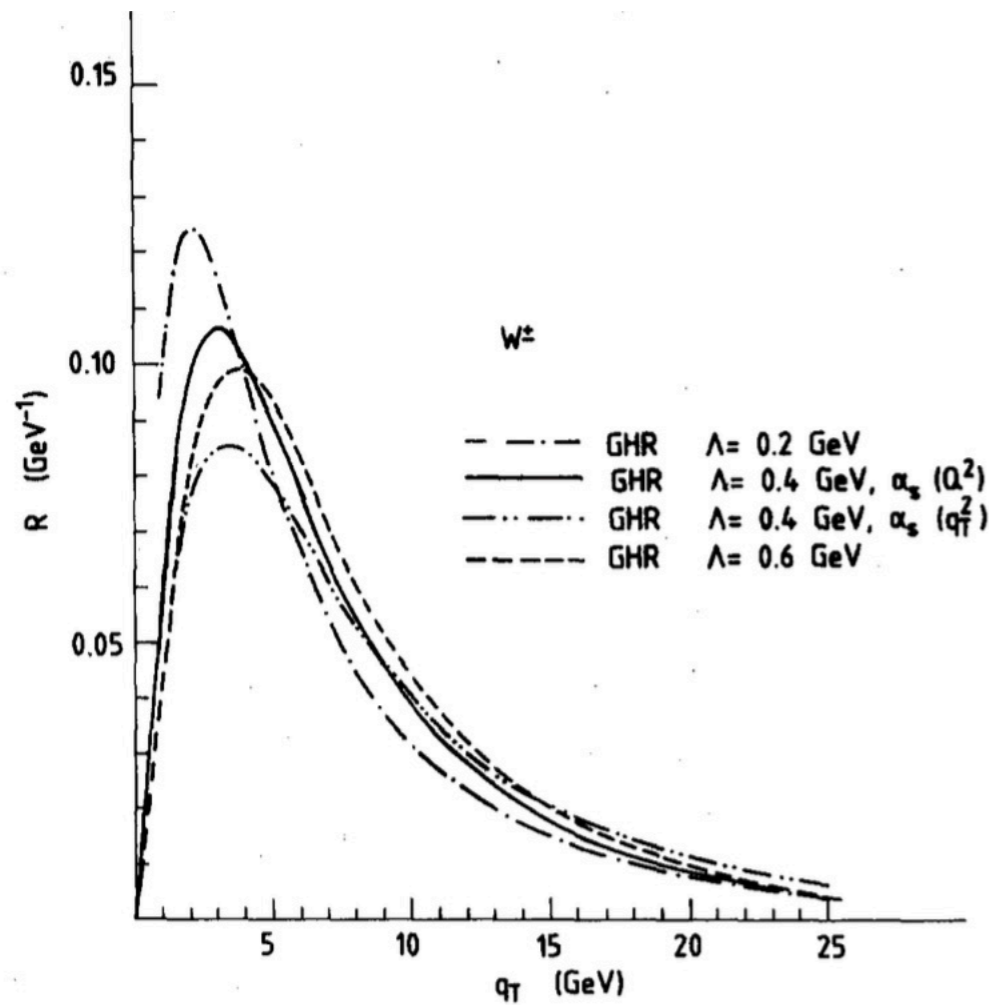
INFN, Laboratori Nazionali di Frascati, Italy

Received 2 May 1984
(Revised 13 June 1984)

$p_T(W)$ spectrum at LO



The theoretical systematics



... the comparison with data

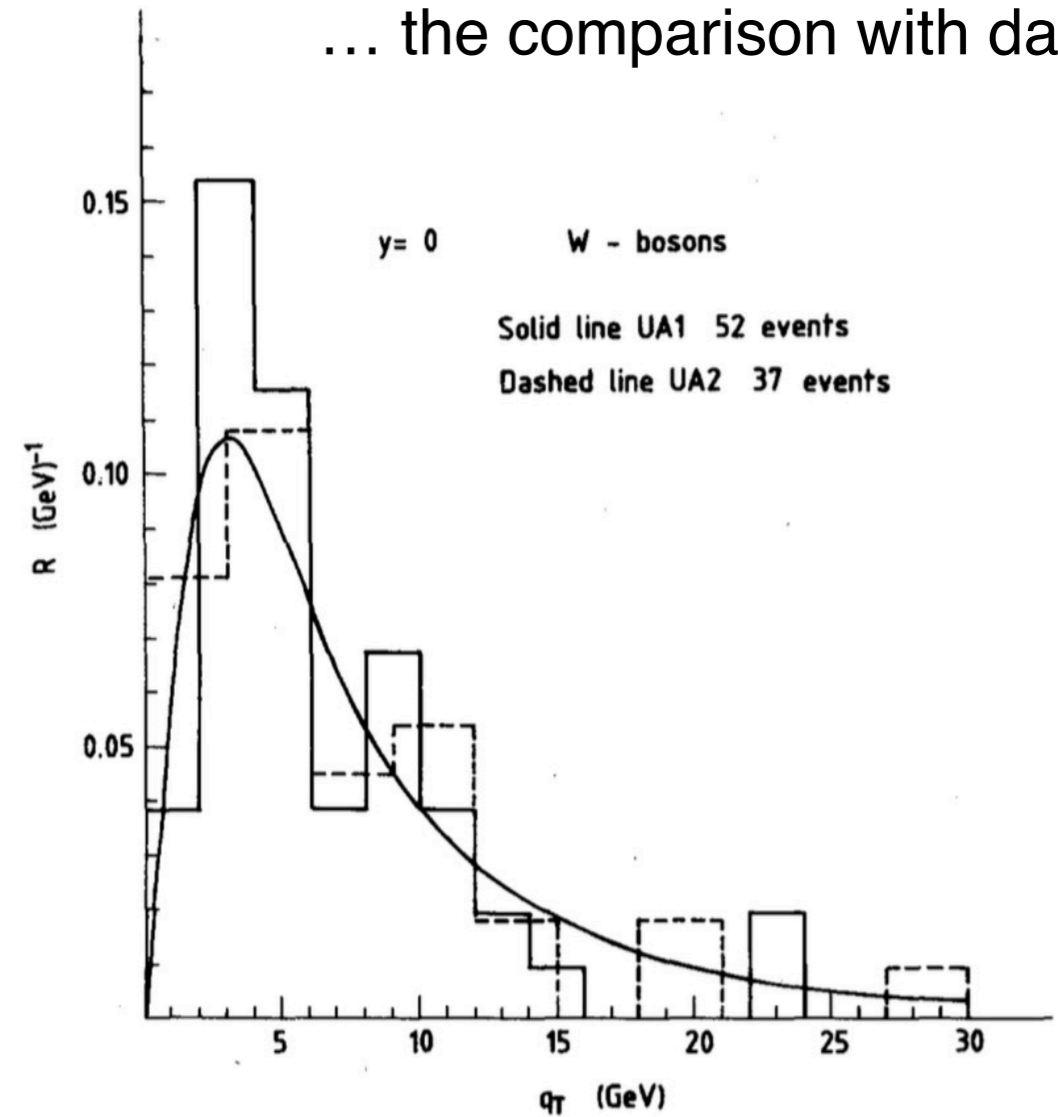
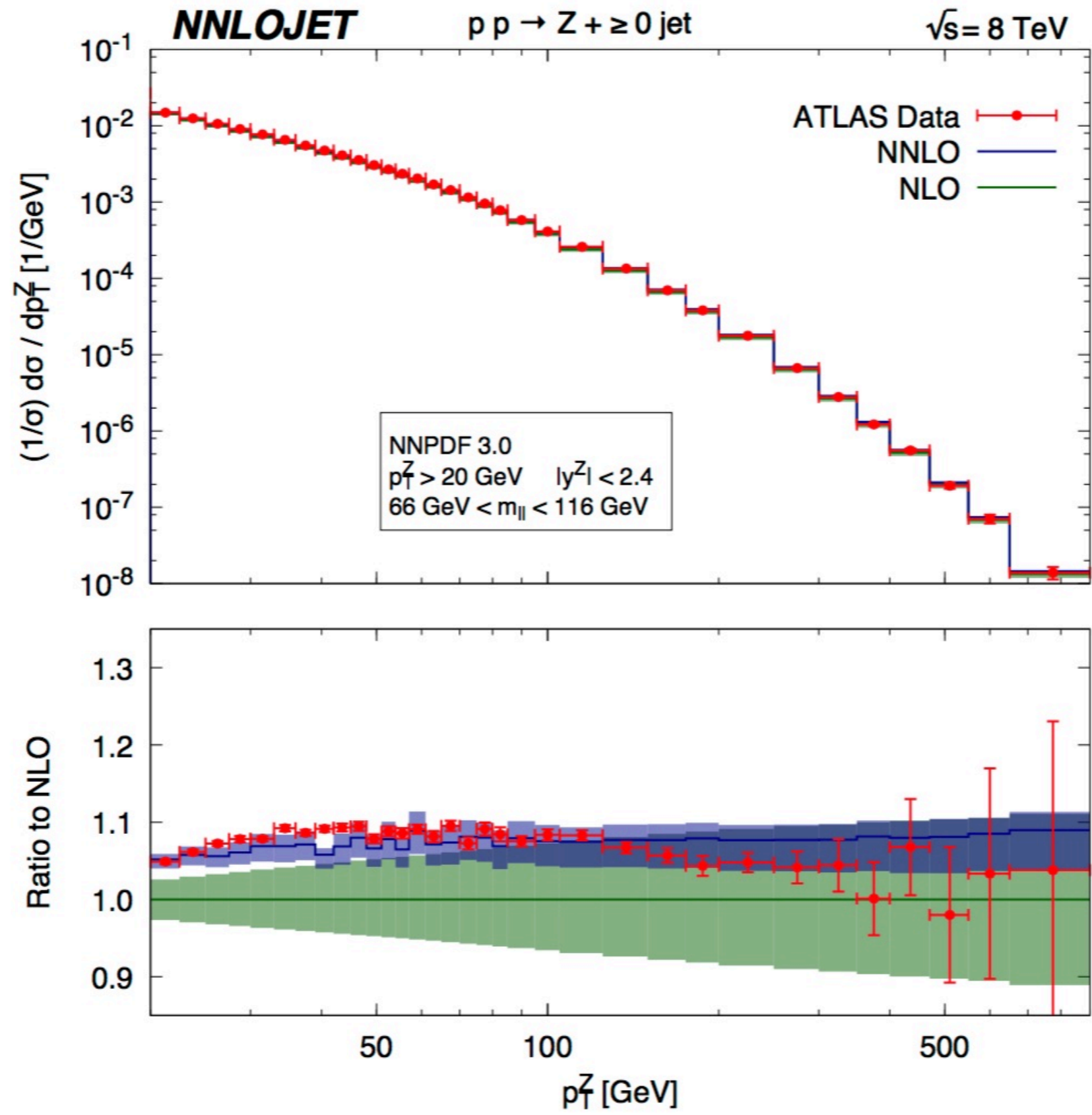


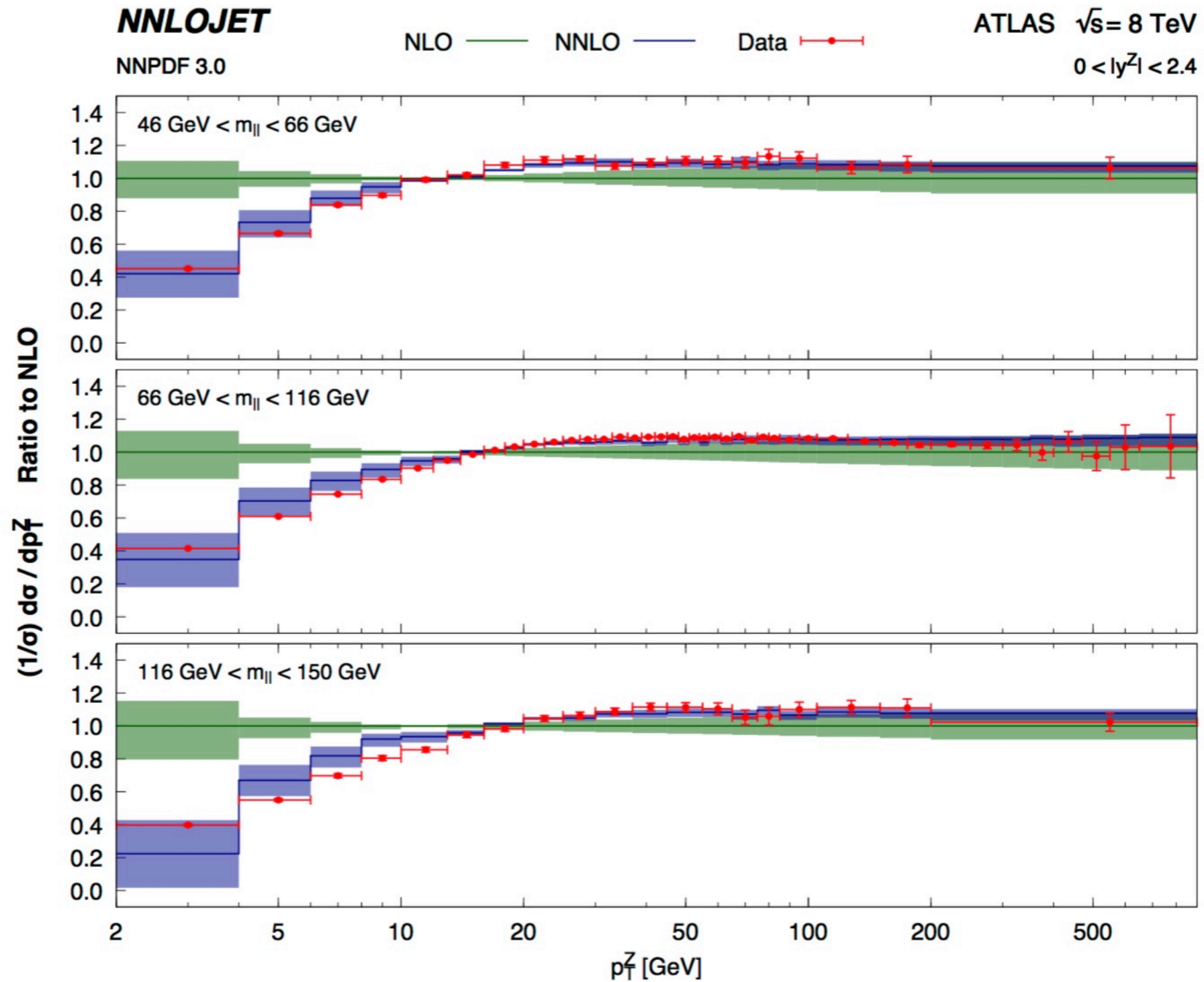
Fig. 4. The ratio $R = (d\sigma/dq_T dy)/(d\sigma/dy)$ at rapidity $y = 0$ using the densities of GHR. The two curves with $\Lambda = 0.4 \text{ GeV}$ differ by the choice of scale in terms of order α_s which is taken either as Q^2 or q_T^2 (other values of Λ correspond to the choice Q^2).

The data for W^\pm boson production suitably normalized and plotted against q_T . Also shown is our prediction for GHR, $\Lambda = 0.4 \text{ GeV}$, $y = 0$, $\alpha_s(Q^2)$.

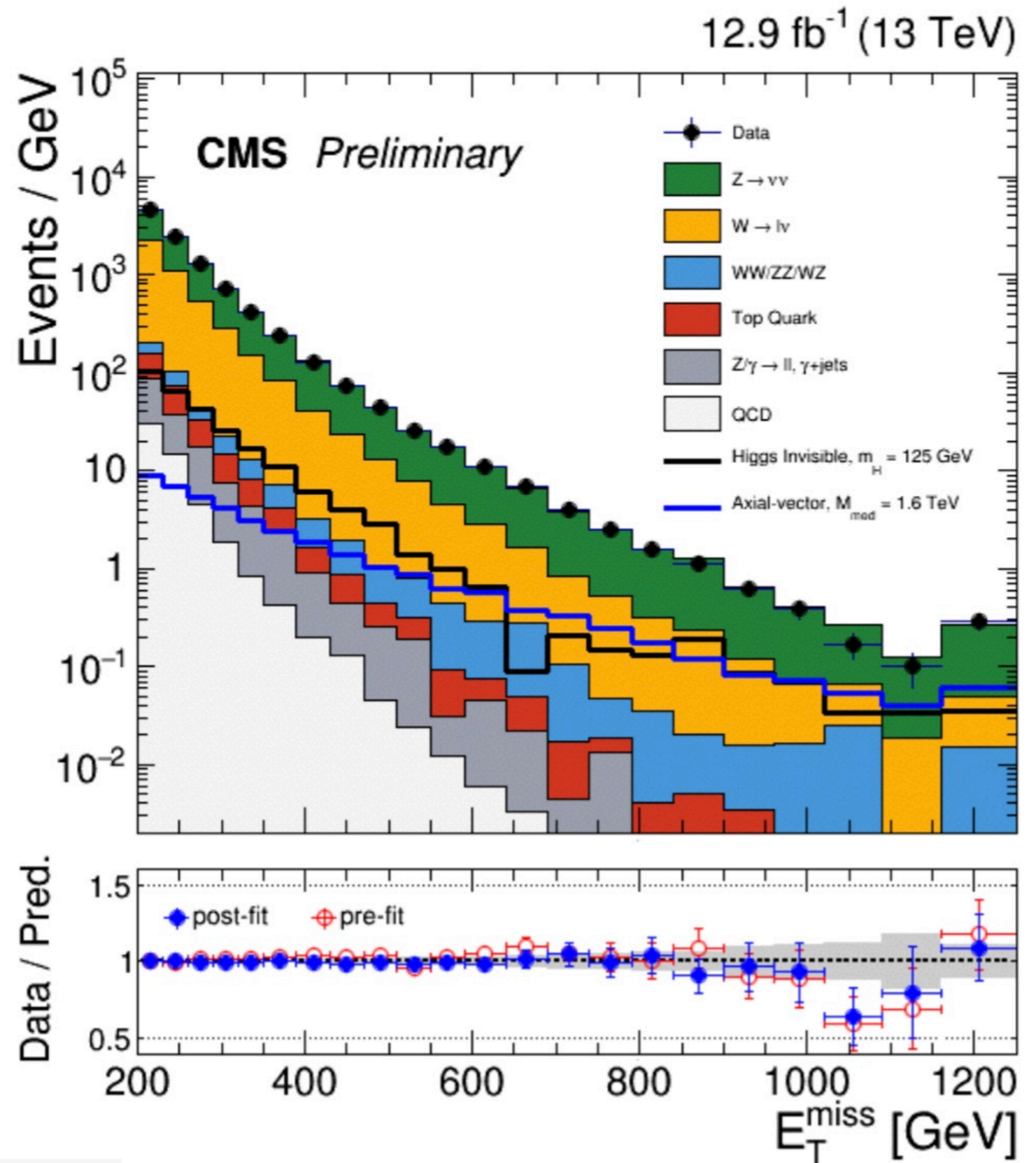
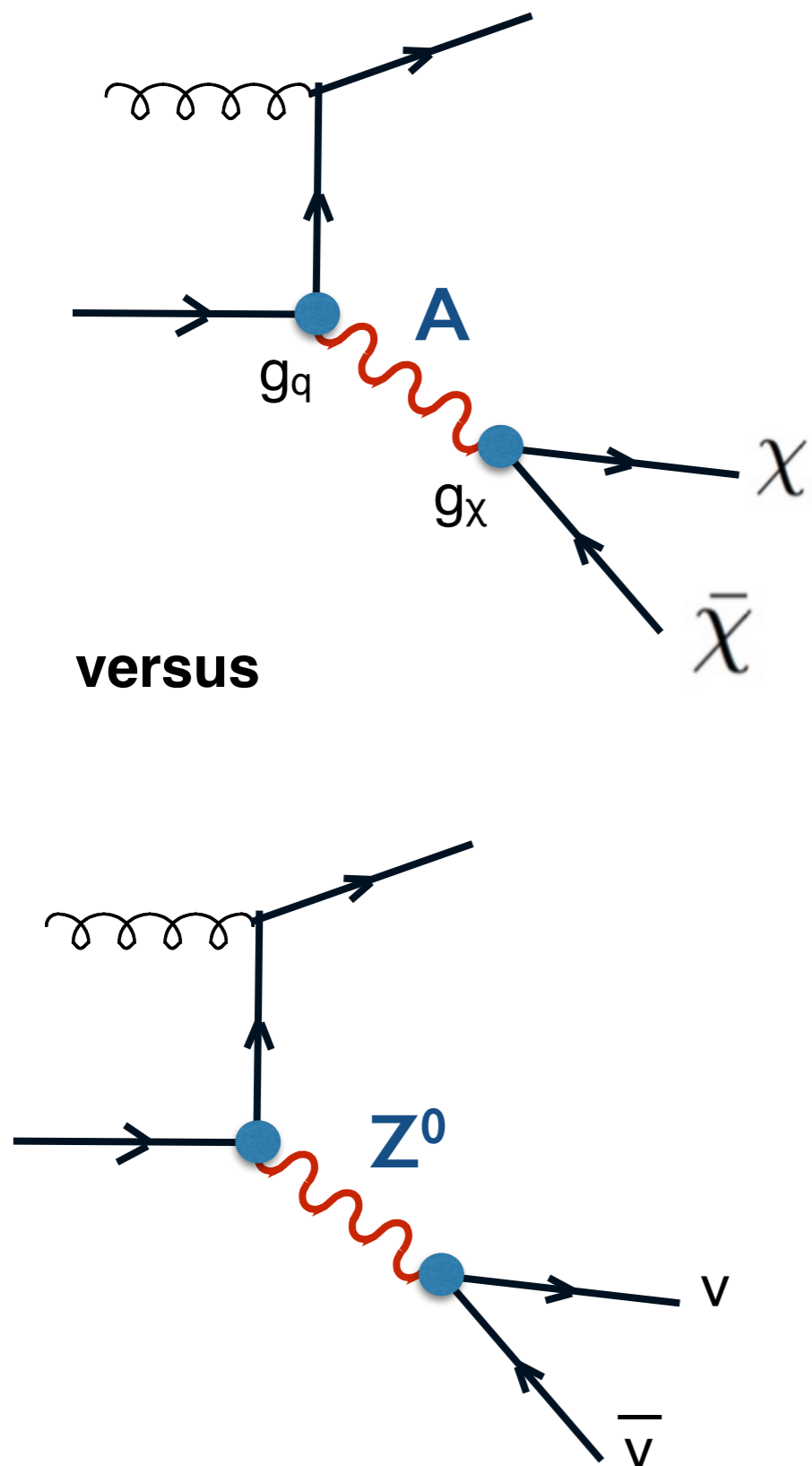
$p_T(Z)$ spectrum at NNLO



Gehrmann–De Ridder, Gehrmann, Glover, Huss, Morgan, [arxiv:1610.01843](https://arxiv.org/abs/1610.01843)

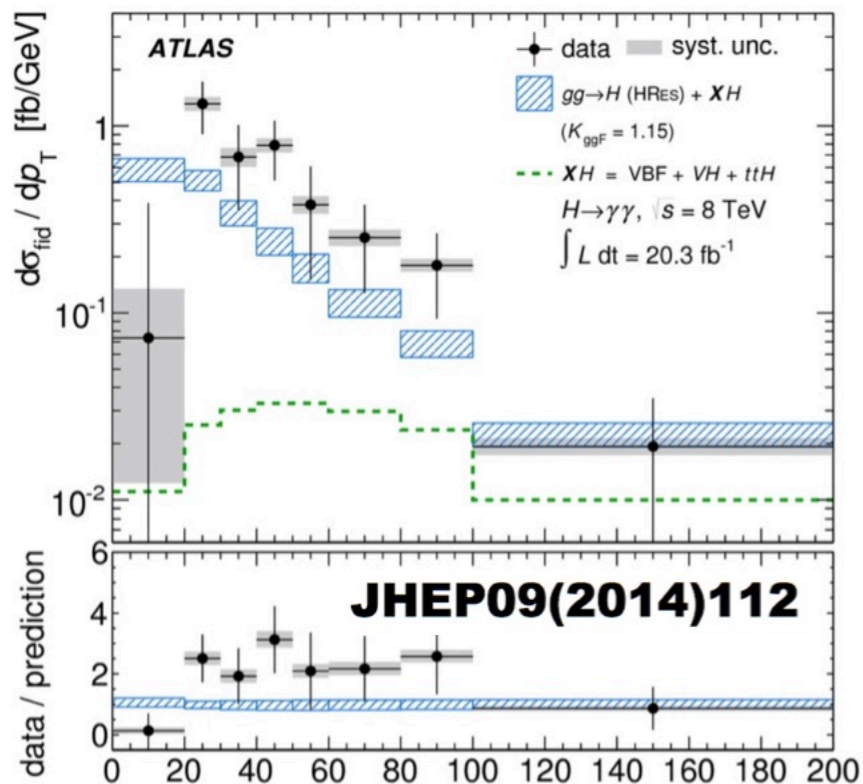


Understanding the p_T of gauge bosons in the search for DM signatures

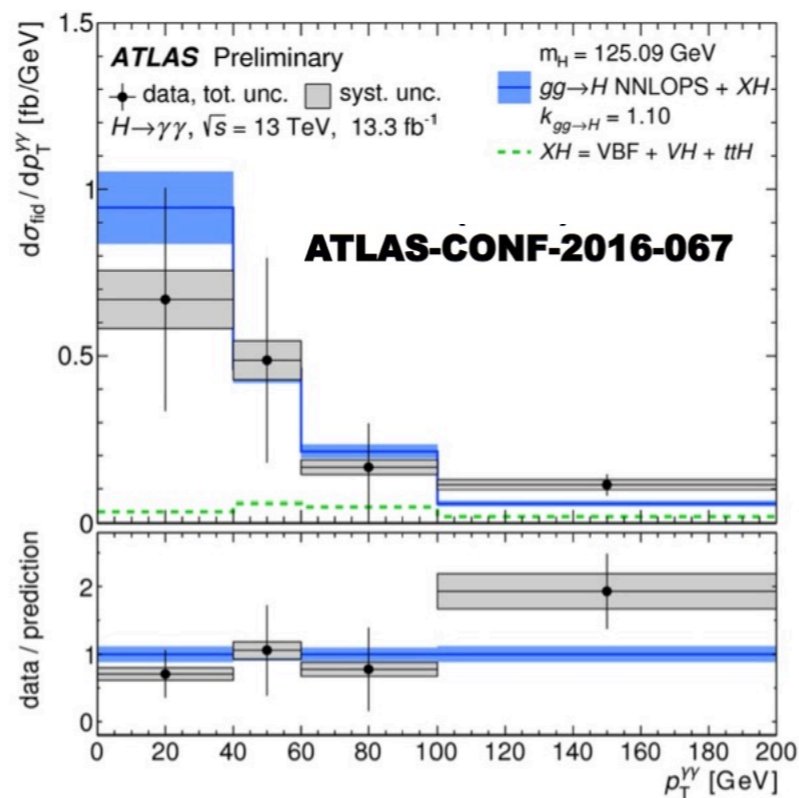


back to the Higgs: first probes of production dynamics, $p_T(H)$ spectrum

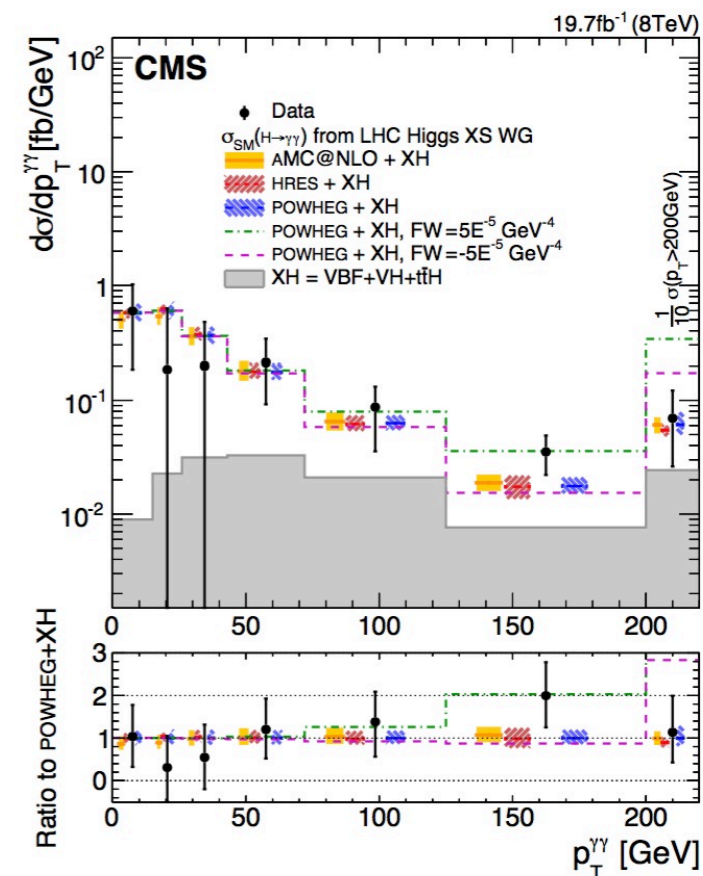
ATLAS $\gamma\gamma$ run 1



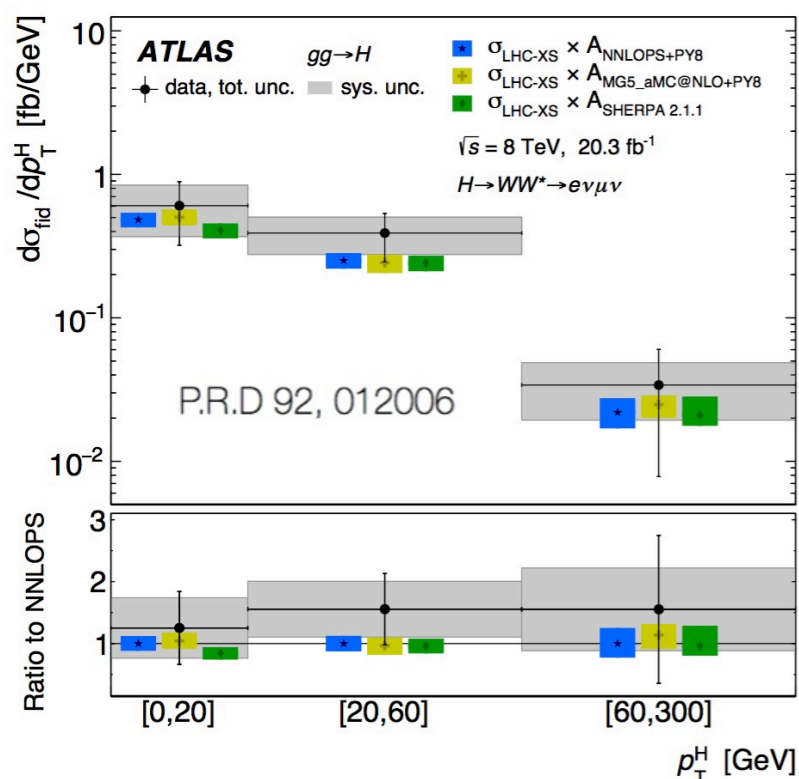
ATLAS $\gamma\gamma$ run 2



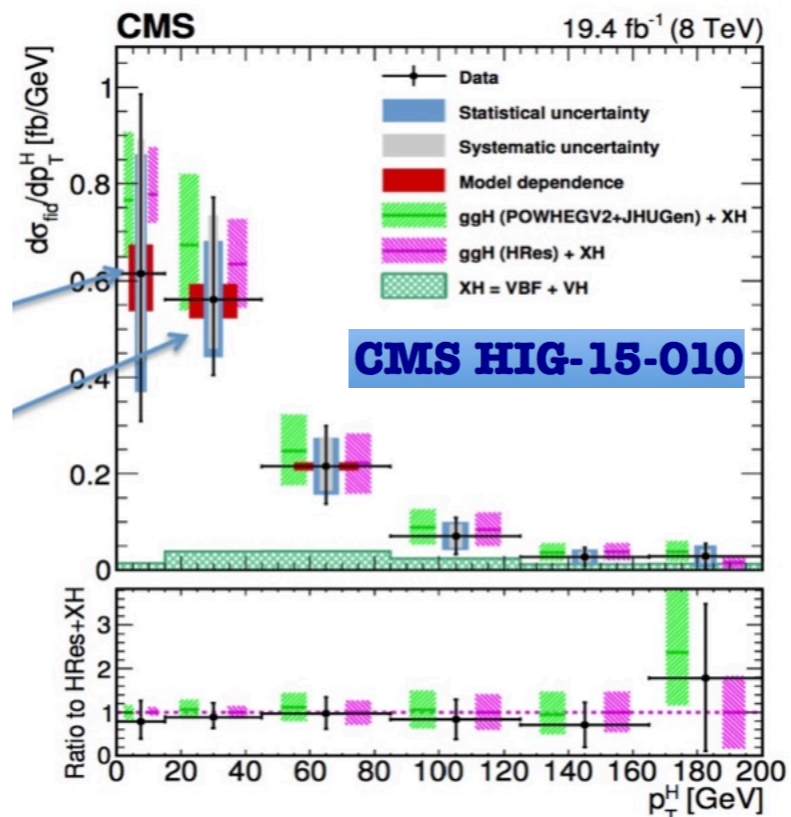
CMS $\gamma\gamma$ run 1



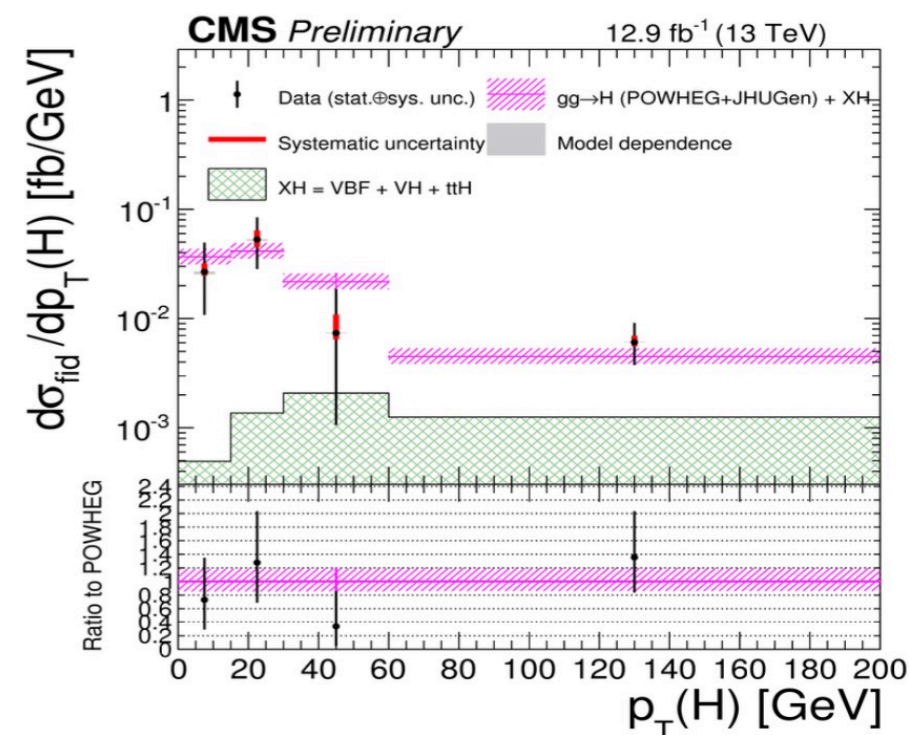
ATLAS 2l2v run 1

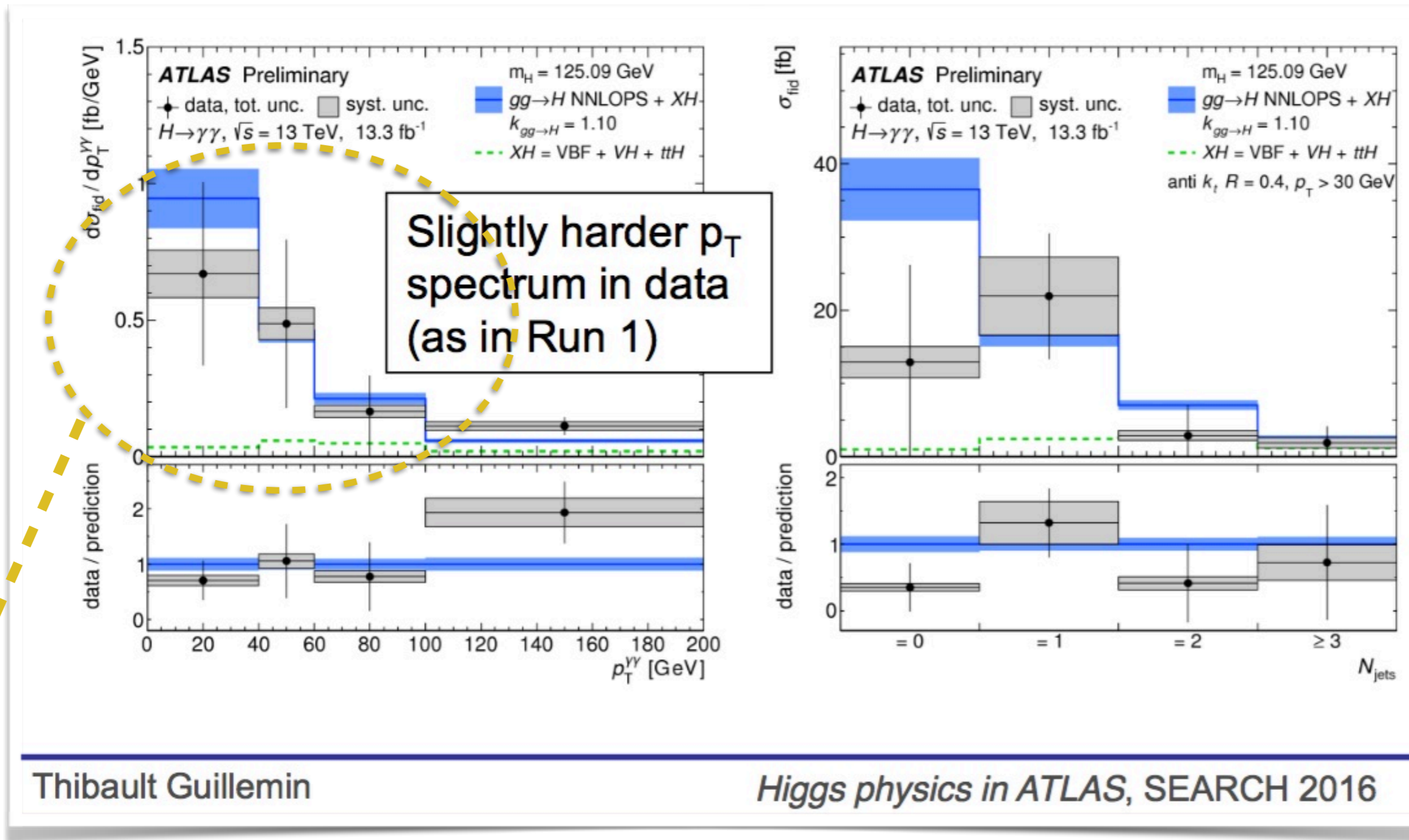


CMS 2l2v run 1



CMS 4l run 2





- $\delta_{\text{stat}} \sim 5 \delta_{\text{exp}} \Rightarrow \sim 25 \times L \sim 300 \text{fb}^{-1}$ to equalize exp&stat uncert'y
- $\mathcal{O}(\text{ab}^{-1})$ will provide an accurate, purely exptl determination of $p_T(H)$ in the theoretically delicate region 0-50 GeV, and strongly reduce/suppress th'l modeling systematics affecting other measurements (e.g. WW*)
- More in general, a global programme of higher-order calculations, data validation, MC improvements, PDF determinations, etc, will push further the TH precision....

Indirect Higgs probes of new physics at large statistics

- Higher statistics shifts the balance between systematic and statistical uncertainties. It can be exploited to define different signal regions, with better S/B, better systematics, pushing the potential for better measurements beyond the “systematics wall” of low-stat measurements.
- We often talk about “**precise**” Higgs measurements. What we actually aim at, is “**sensitive**” tests of the Higgs properties, where *sensitive* refers to the ability to reveal BSM behaviours.
- **Sensitivity** may not require extreme precision
- Going after “sensitivity”, rather than *just* precision, opens itself new opportunities ...

Higgs as a BSM probe: precision vs dynamic reach

$$L = L_{SM} + \frac{1}{\Lambda^2} \sum_k \mathcal{O}_k + \dots$$

$$O = | \langle f | L | i \rangle |^2 = O_{SM} [1 + O(\mu^2 / \Lambda^2) + \dots]$$

Higgs as a BSM probe: precision vs dynamic reach

$$L = L_{SM} + \frac{1}{\Lambda^2} \sum_k \mathcal{O}_k + \dots$$

$$O = | \langle f | L | i \rangle |^2 = O_{SM} [1 + O(\mu^2/\Lambda^2) + \dots]$$

For H decays, or inclusive production, $\mu \sim O(v, m_H)$

$$\delta O \sim \left(\frac{v}{\Lambda}\right)^2 \sim 6\% \left(\frac{\text{TeV}}{\Lambda}\right)^2 \quad \Rightarrow \text{precision probes large } \Lambda$$

e.g. $\delta O = 1\% \Rightarrow \Lambda \sim 2.5 \text{ TeV}$

Higgs as a BSM probe: precision vs dynamic reach

$$L = L_{SM} + \frac{1}{\Lambda^2} \sum_k \mathcal{O}_k + \dots$$

$$O = | \langle f | L | i \rangle |^2 = O_{SM} [1 + O(\mu^2/\Lambda^2) + \dots]$$

For H decays, or inclusive production, $\mu \sim O(v, m_H)$

$$\delta O \sim \left(\frac{v}{\Lambda}\right)^2 \sim 6\% \left(\frac{\text{TeV}}{\Lambda}\right)^2 \Rightarrow \text{precision probes large } \Lambda$$

$$\text{e.g. } \delta O = 1\% \Rightarrow \Lambda \sim 2.5 \text{ TeV}$$

For H production off-shell or with large momentum transfer Q , $\mu \sim O(Q)$

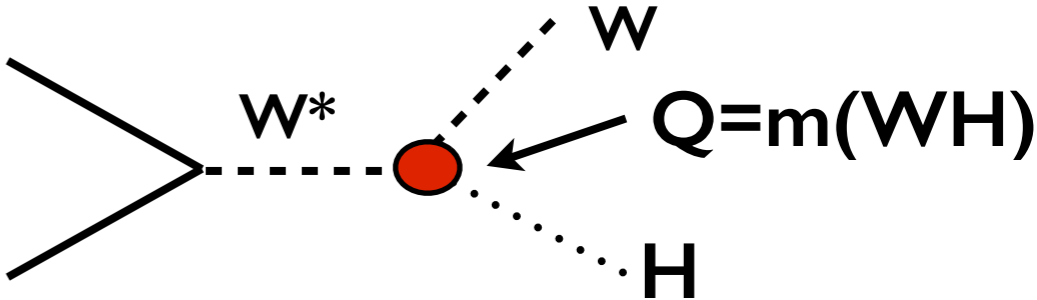
$$\delta O_Q \sim \left(\frac{Q}{\Lambda}\right)^2$$

\Rightarrow **kinematic reach** probes large Λ even if precision is low

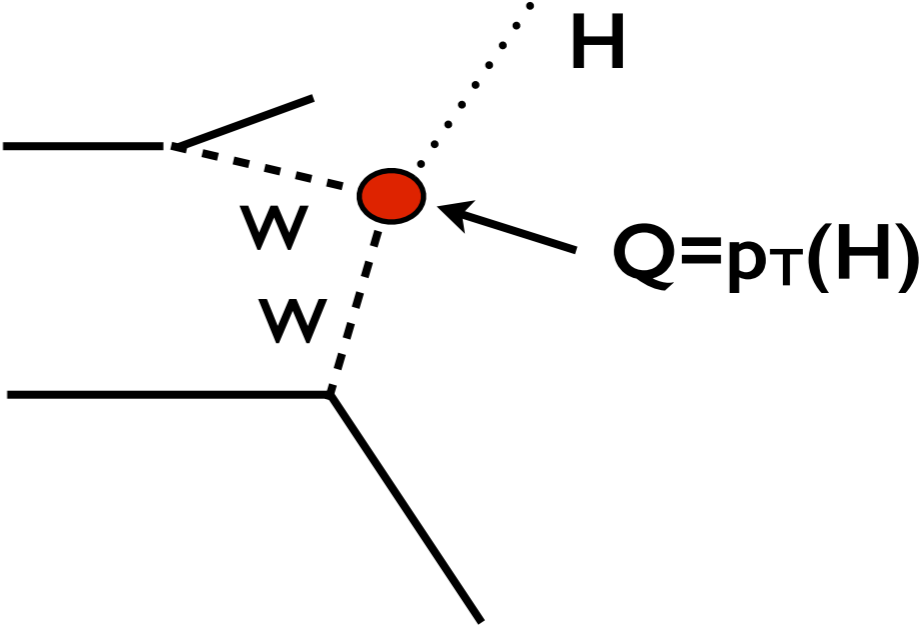
$$\text{e.g. } \delta O_Q = 10\% \text{ at } Q = 750 \text{ GeV} \Rightarrow \Lambda \sim 2.5 \text{ TeV}$$

Examples

$\delta\text{BR}(H \rightarrow WW^*)$

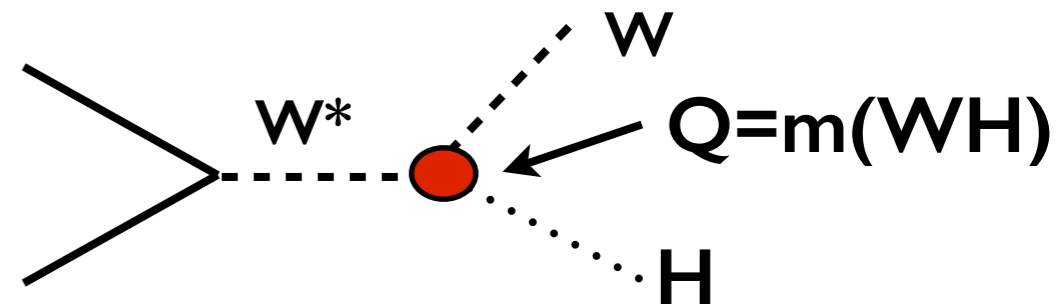
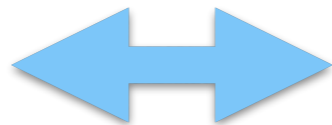


or

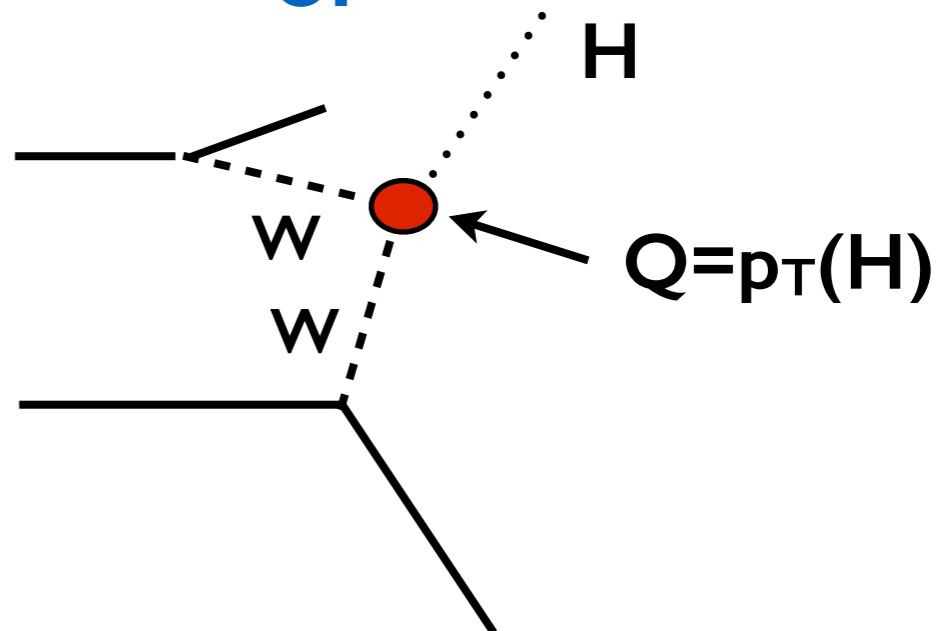


Examples

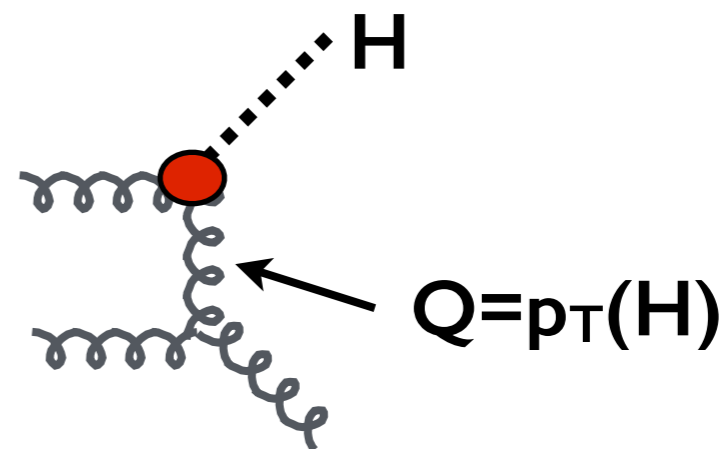
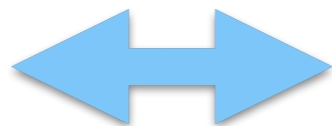
$\delta\text{BR}(H \rightarrow WW^*)$



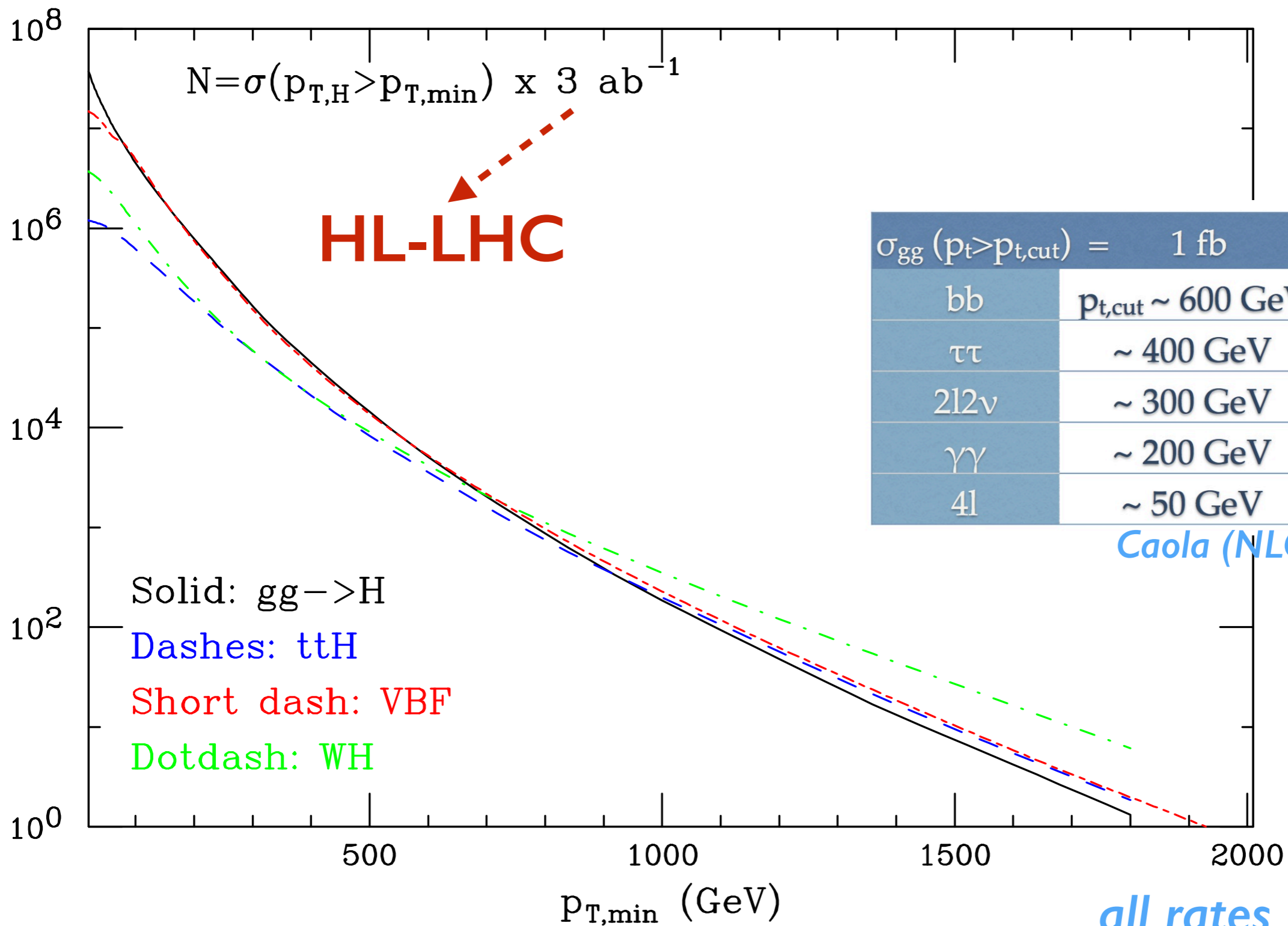
or



$\delta\text{BR}(H \rightarrow gg)$



Probing large Q: Higgs production at large p_T

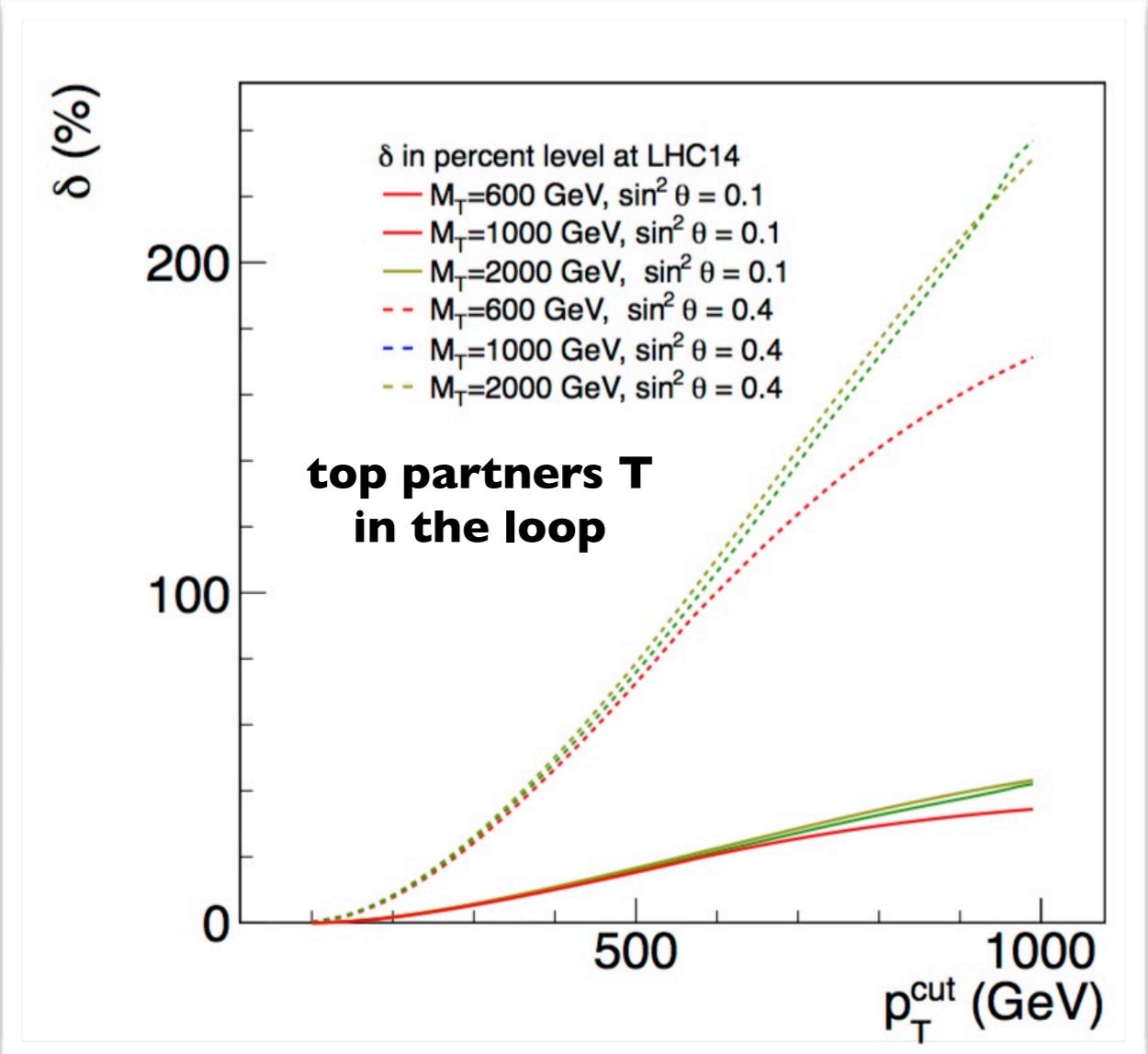


$\sigma_{gg}(p_t > p_{t,cut}) =$	1 fb	1 ab
bb	$p_{t,cut} \sim 600 \text{ GeV}$	$p_{t,cut} \sim 1.5 \text{ TeV}$
$\tau\tau$	$\sim 400 \text{ GeV}$	$\sim 1.2 \text{ TeV}$
$2l2\nu$	$\sim 300 \text{ GeV}$	$\sim 1 \text{ TeV}$
$\gamma\gamma$	$\sim 200 \text{ GeV}$	$\sim 750 \text{ GeV}$
$4l$	$\sim 50 \text{ GeV}$	$\sim 450 \text{ GeV}$

Caola (NLO rates for $gg \rightarrow H$)

Examples: $gg \rightarrow H$ at large p_T

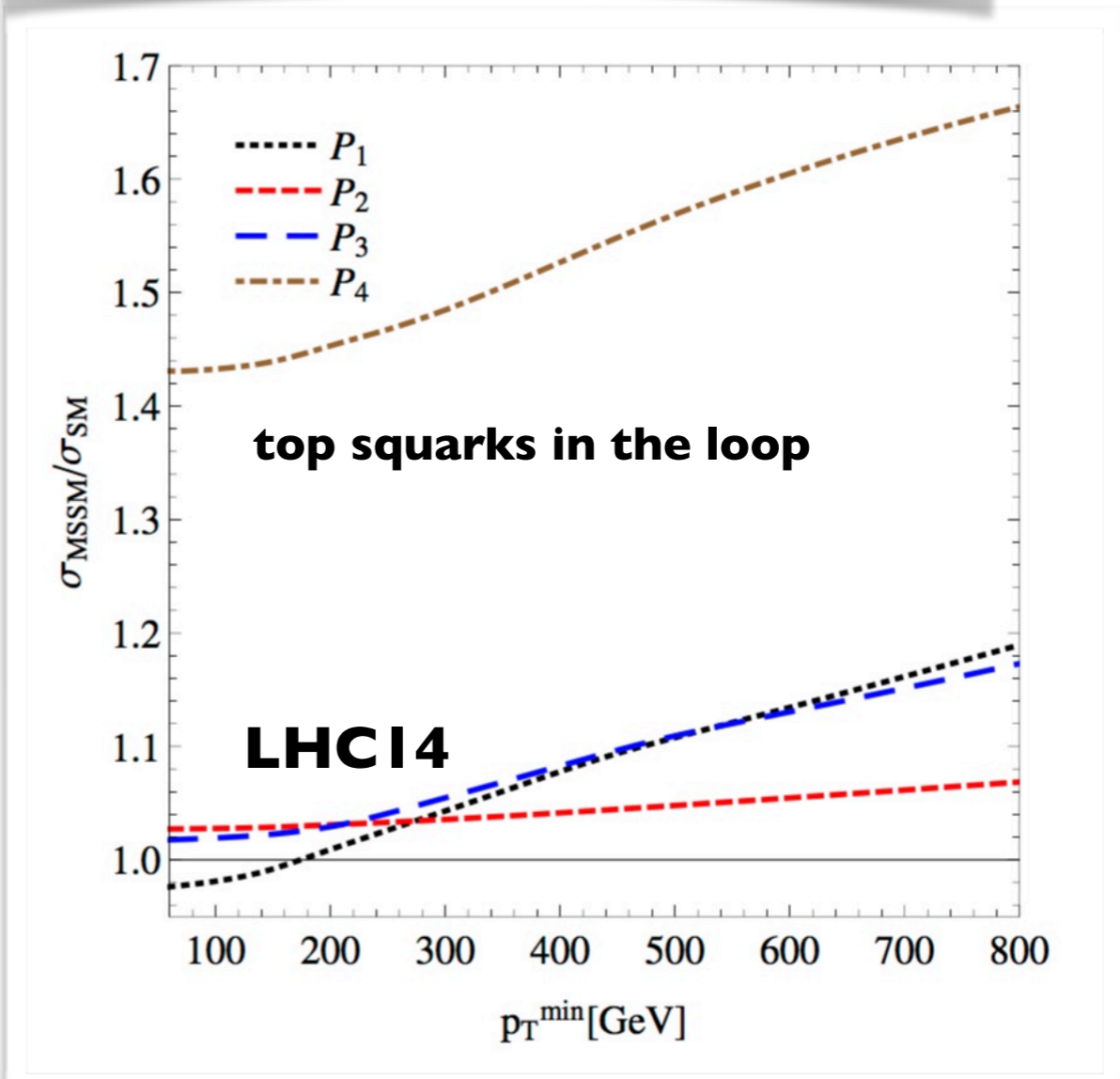
(See also Azatov and Paul [arXiv:1309.5273v3](https://arxiv.org/abs/1309.5273v3))



Banfi Martin Sanz, [arXiv:1308.4771](https://arxiv.org/abs/1308.4771)

Table 3: The benchmark points shown in Fig. 7. We set $\tan \beta = 10$, $M_{A_0} = 500$ GeV, $M_2 = 1000$ GeV, $\mu = 200$ GeV and all trilinear couplings to a common value A_t . The remaining sfermion masses were set to 1 TeV and the mass of the lightest CP -even Higgs was set to 125 GeV.

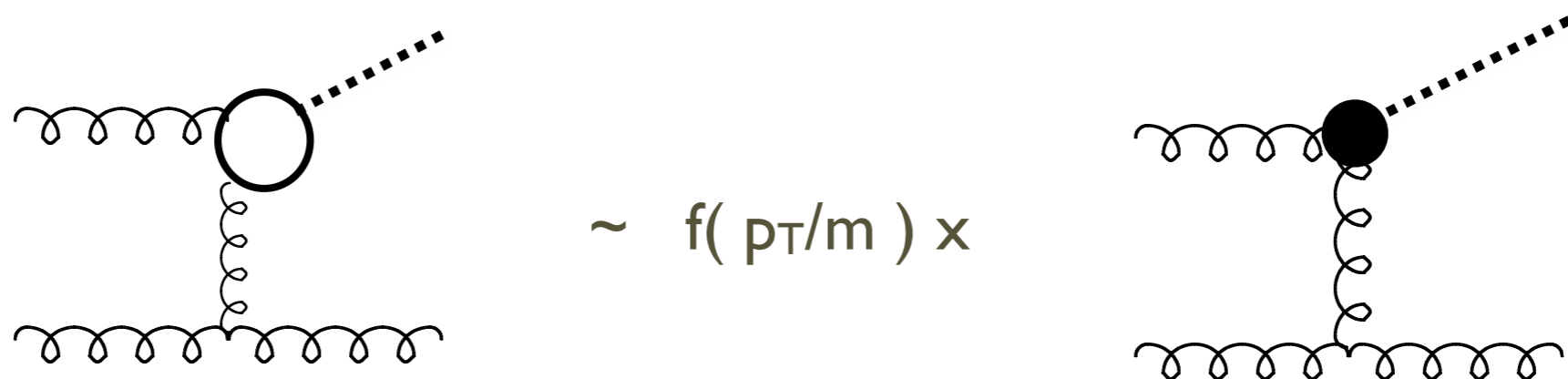
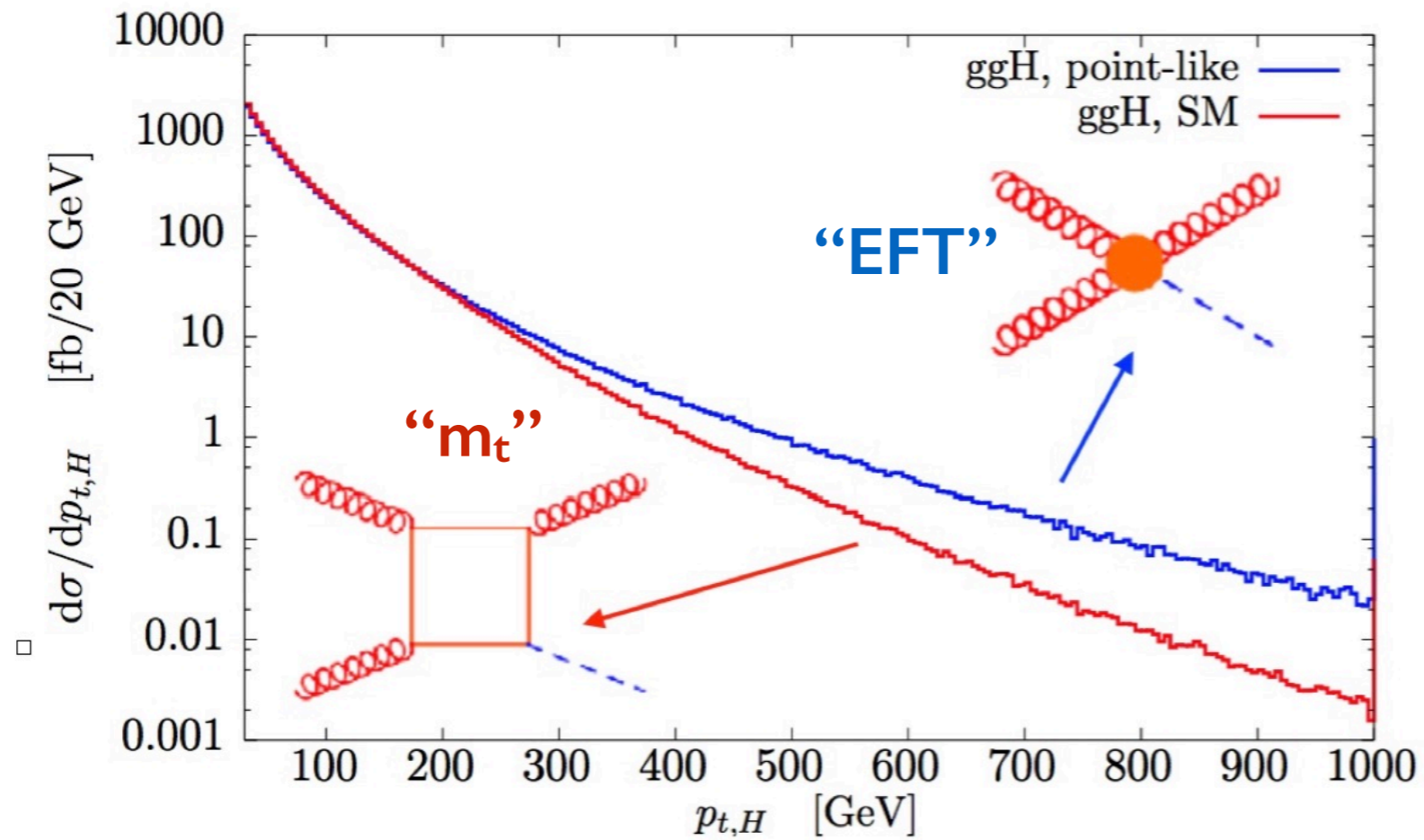
Point	$m_{\tilde{t}_1}$ [GeV]	$m_{\tilde{t}_2}$ [GeV]	A_t [GeV]	Δ_t
P_1	171	440	490	0.0026
P_2	192	1224	1220	0.013
P_3	226	484	532	0.015
P_4	226	484	0	0.18



Grojean, Salvioni, Schläffer, Weiler [arXiv:1312.3317](https://arxiv.org/abs/1312.3317)

10% sensitivity at $p_T(H) \sim 1$ TeV is compatible with 3ab^{-1} rates in previous page

TH syst's at large p_{T^H}

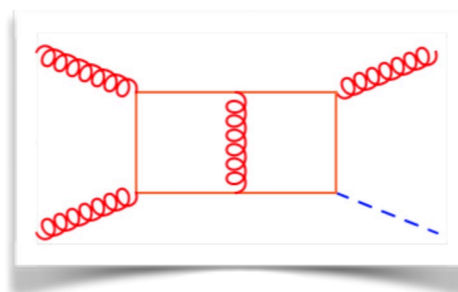


$$f \sim \frac{4m^2}{4m^2 + p_T^2} \quad \begin{array}{l} \rightarrow 1 \text{ for } p_T \ll m \\ \rightarrow 1/p_T^2 \text{ for } m \ll p_T \end{array}$$

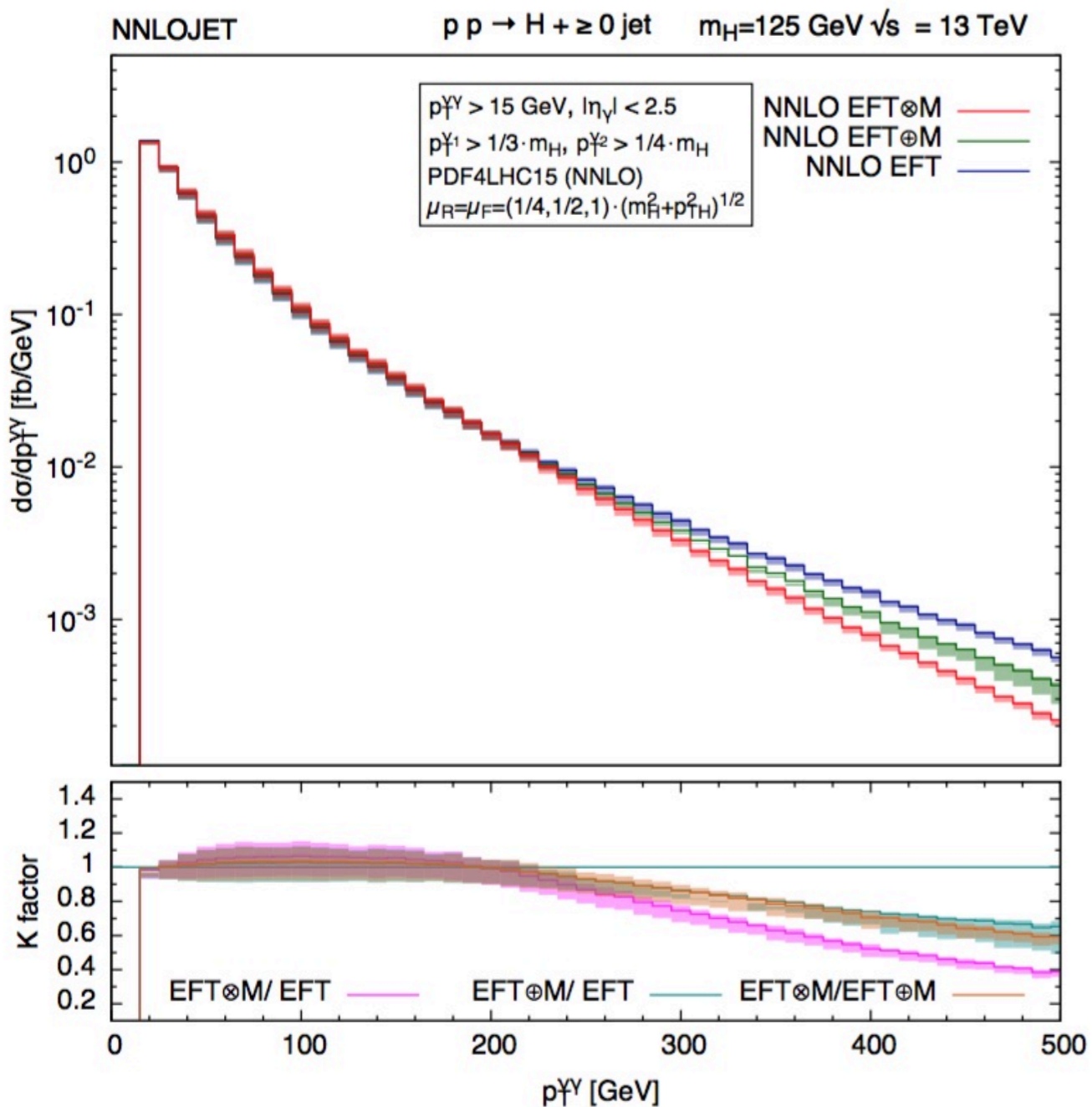
NNLO p_T spectrum available in EFT...

Chen, Cruz-Martinez, Gehrmann, Glover, Jaquier,
<https://arxiv.org/pdf/1607.08817v2>

... but for finite m_{top} , not even at NLO



- NLO at high momentum transfer: 2-loop amplitudes with several external (s , p_T , m_h) and internal (m_t) mass scales
 → significantly more complicated than any amplitude computed so far

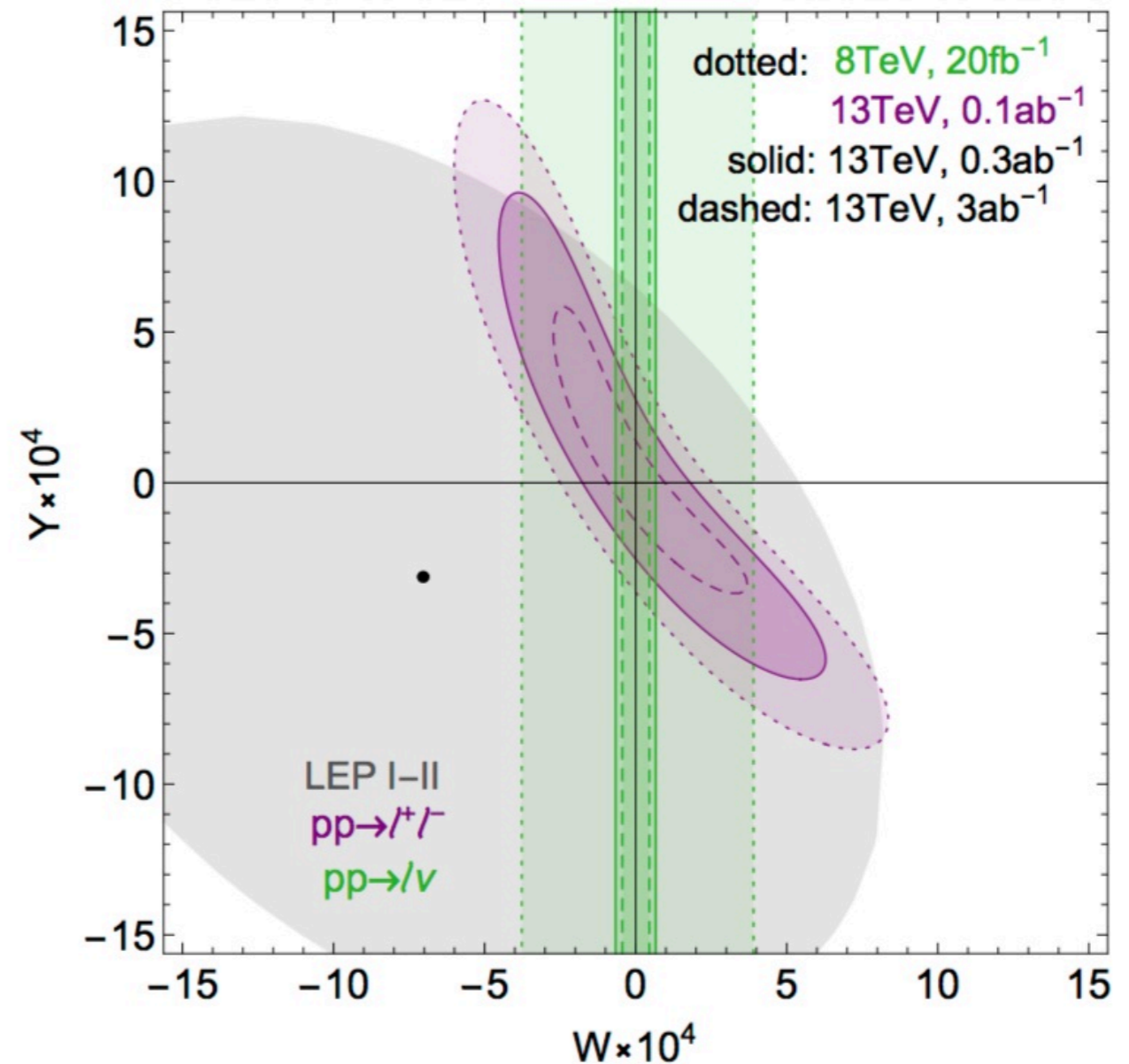
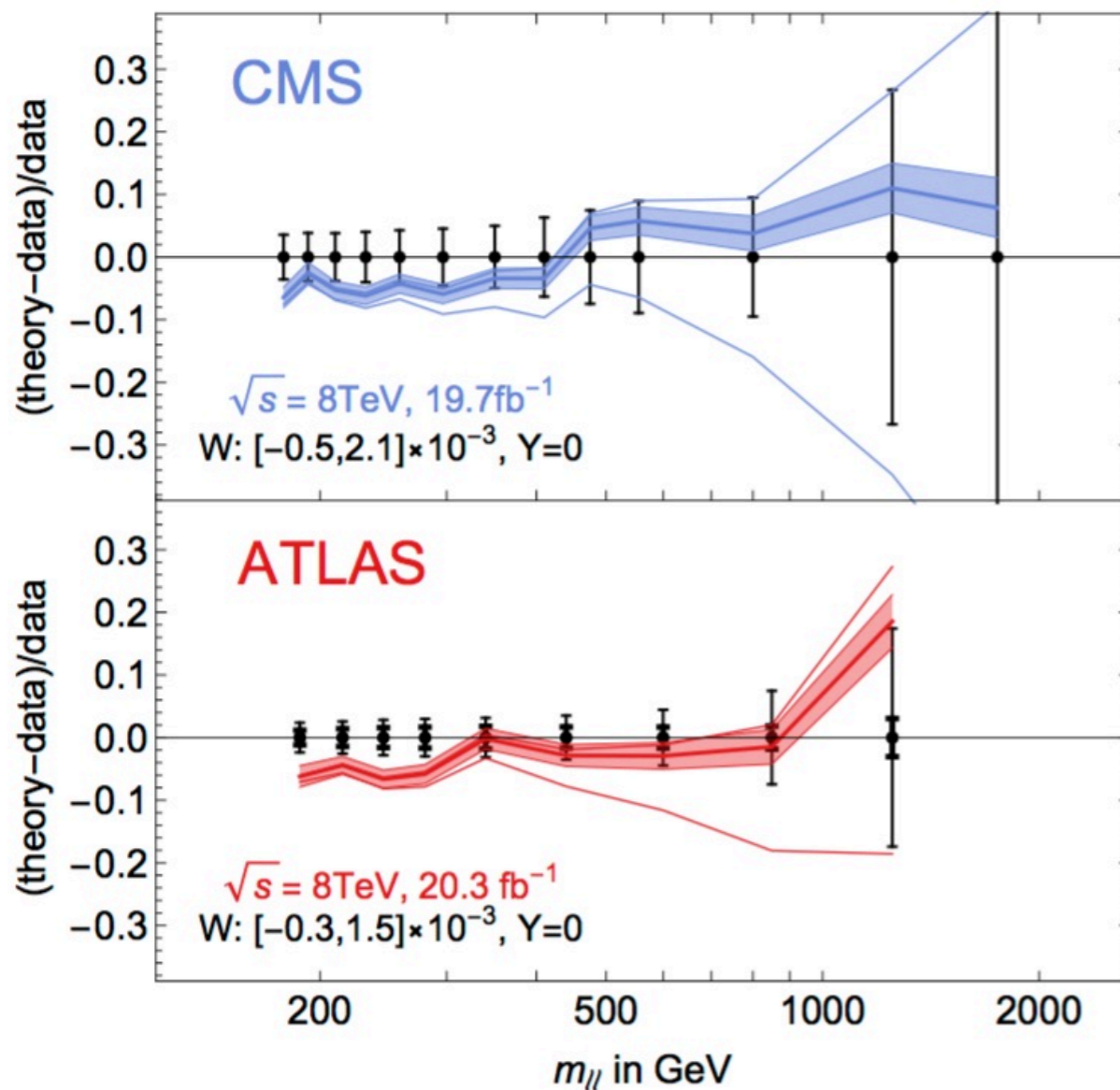


=> important systematics due to finite m_{top} effects at large p_T

Ex: Probes of dim-6 op's with high-mass DY

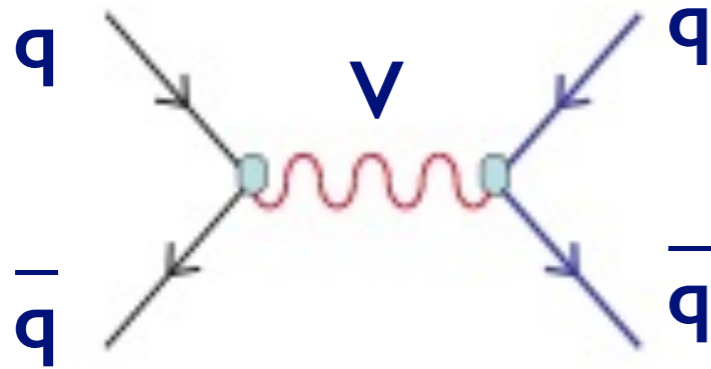
M.Farina et al, arXiv:1609.08157

	universal form factor (\mathcal{L})
W	$-\frac{W}{4m_W^2} (D_\rho W_{\mu\nu}^a)^2$
Y	$-\frac{Y}{4m_W^2} (\partial_\rho B_{\mu\nu})^2$



Physics with hadronic $W/Z(H)$ decays ?

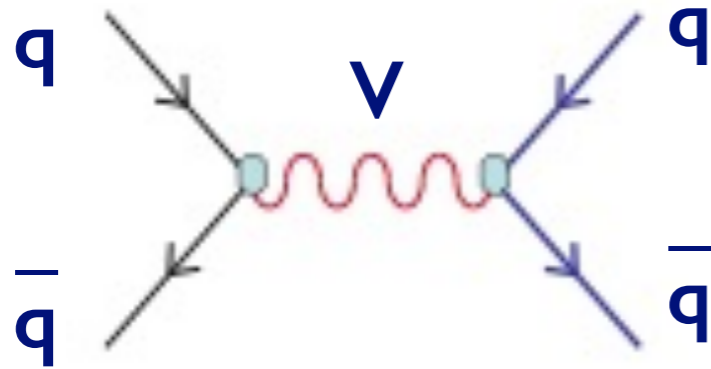
Example: search for low-mass resonances $V \rightarrow 2$ jets



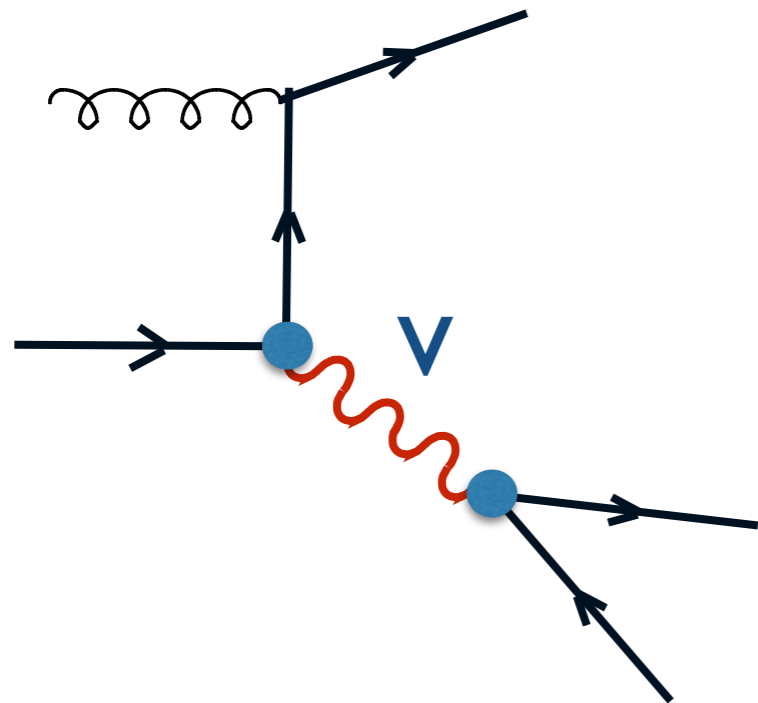
search impossible at masses below
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bg's and trigger thresholds

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At large p_T

- S/B improves (qg initial state dominates both S and B)
- use boosted techniques to differentiate $V \rightarrow qq$ vs QCD dijets
- $\epsilon_{\text{trig}} \sim 100\%$

Example: search for low-mass dijet resonances



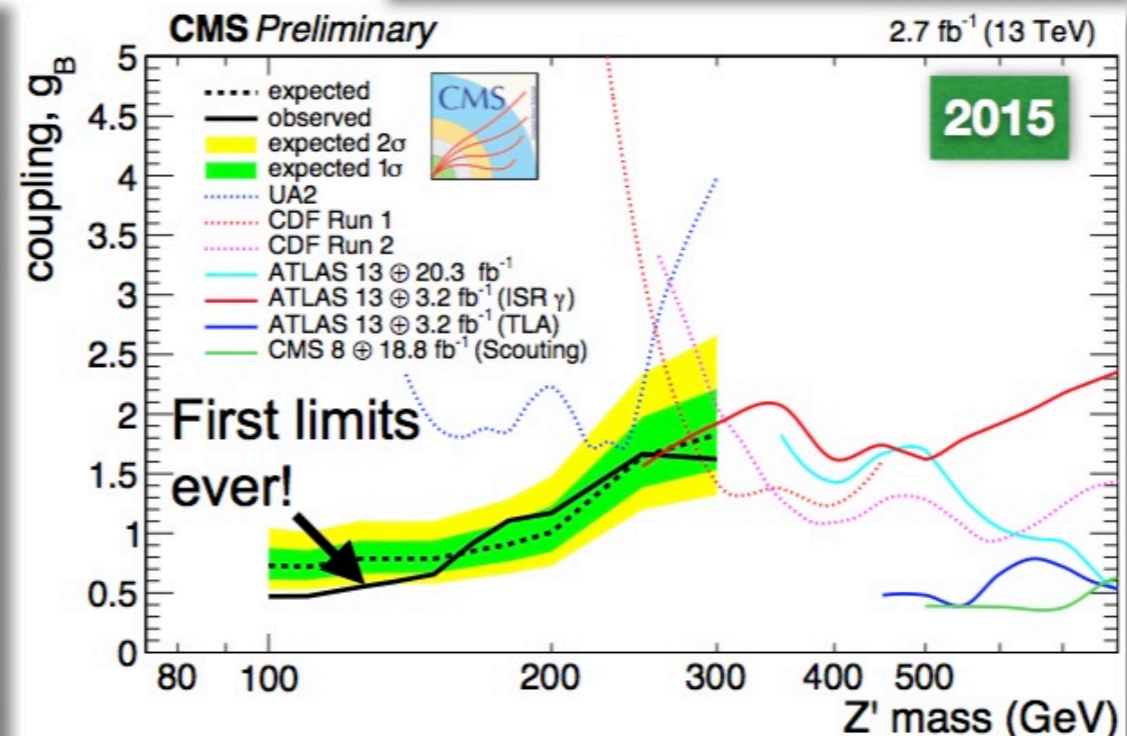
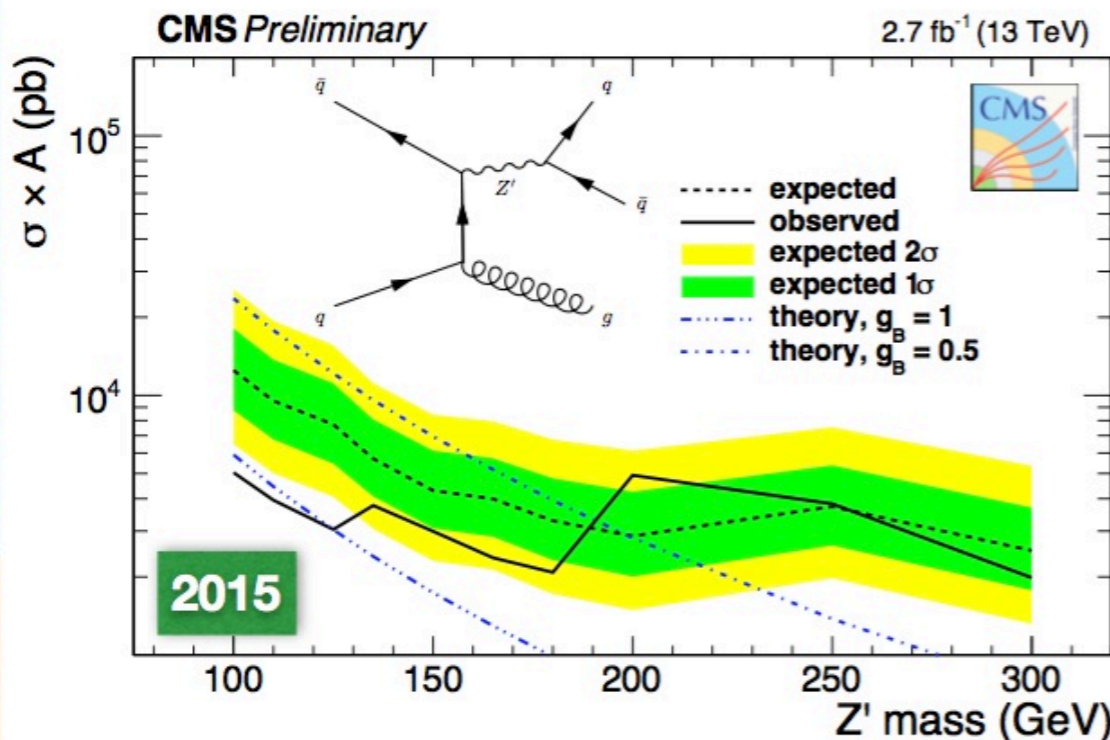
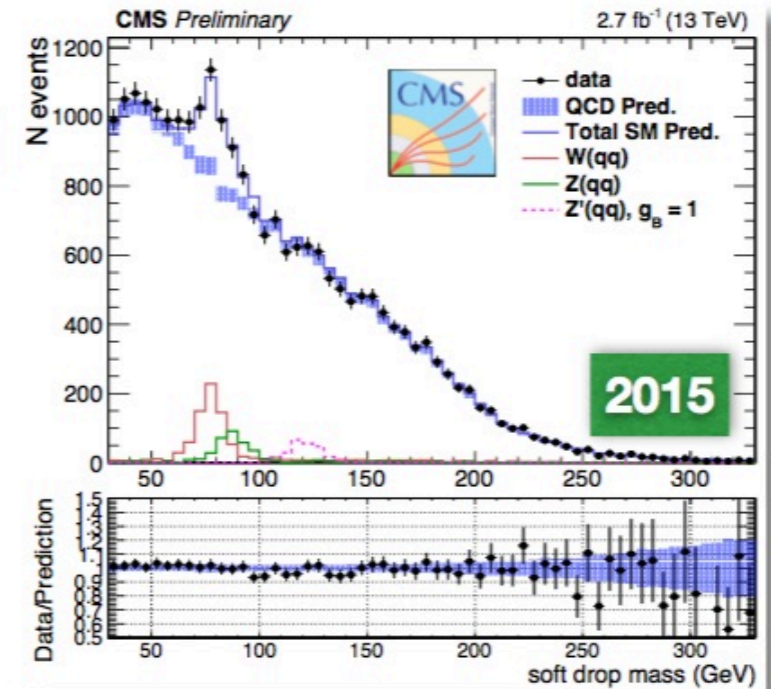
BROWN

Trijets as Dijet Proxy

Slide 30 Greg Landsberg - CMS Exotica Searches - SEARCH 2016 - Oxford

- Another way to go to low-mass dijets is to use 500 GeV ISR to aid triggering and jet substructure to reconstruct boosted Z'
- Allows to lower the dijet mass reach to 100 GeV, as demonstrated with the W/Z peak

CMS PAS EXO-16-030



Final remarks

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In either case, if new physics is there to be found, better understanding and control of QCD will play a crucial role in revealing it, and studying its properties

While we wait for the discoveries, improving our knowledge of QCD via calculations and measurements remains greatly challenging and rewarding