

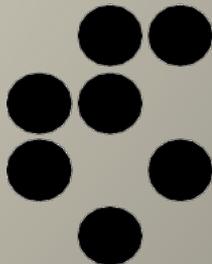
Electric field, mobility and trapping in Si detectors irradiated with neutrons and protons up to $10^{17} n_{eq}/cm^2$

**M.Mikuž, G.Kramberger, V.Cindro, I.Mandić,
M.Zavrtanik**

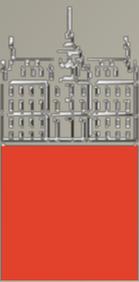
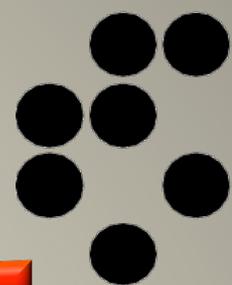
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RD50 Workshop

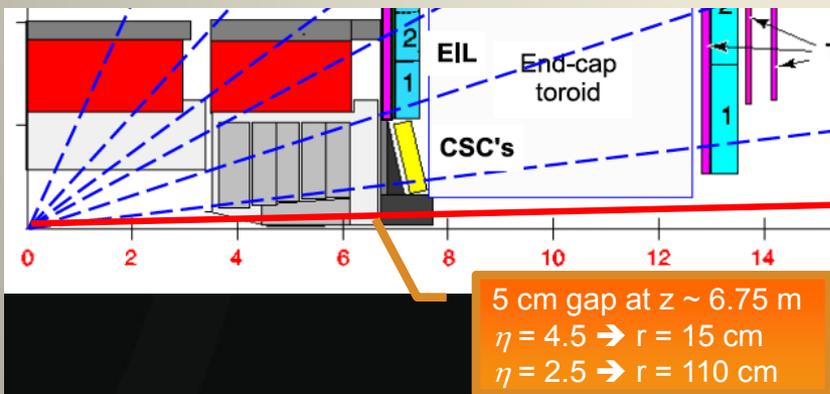
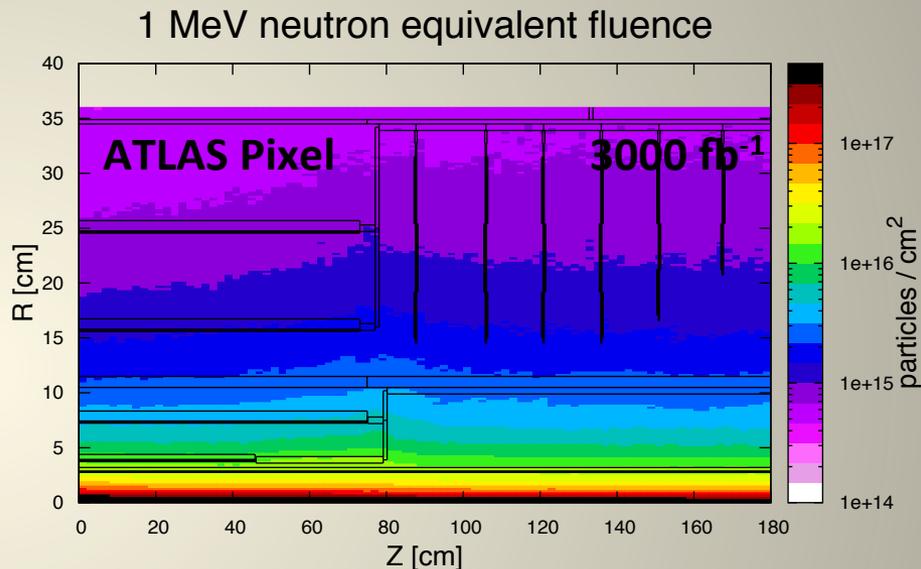
Torino, June 8th, 2016



Why the 10^{17} Ballpark ?

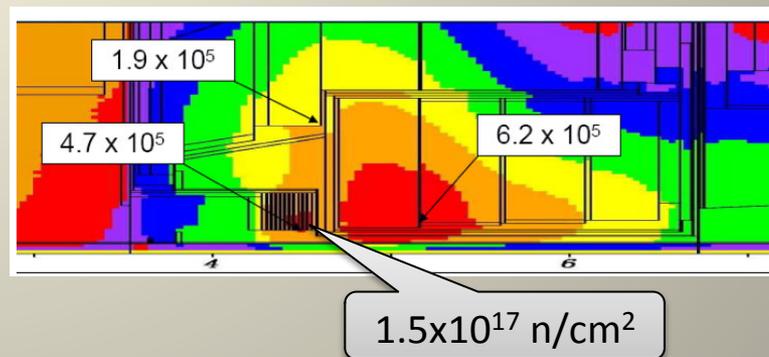


- Run1 at LHC finished, 2 under way
 - LHC trackers designed for 730 fb^{-1} of 14 TeV pp collisions, $\sim 35 \text{ fb}^{-1}$ up to now
 - Will probably get $\sim 1/2$ of planned
- HL-LHC in advanced planning
 - 3000 fb^{-1} i.e. $\sim 10 \times \text{LHC}$
 - $\sim 10^{15} \text{ n}_{\text{eq}}/\text{cm}^2$ for strips (neutrons&pions)
 - $\sim 10^{16} \text{ n}_{\text{eq}}/\text{cm}^2$ for pixels (pions)
 - $n \times 10^{16} \text{ n}_{\text{eq}}/\text{cm}^2$ for vFW pixels (π & n)
 - $\sim 10^{17} \text{ n}_{\text{eq}}/\text{cm}^2$ for FCAL (neutrons)
- Can (tracking) sensors survive in these extreme environments ?



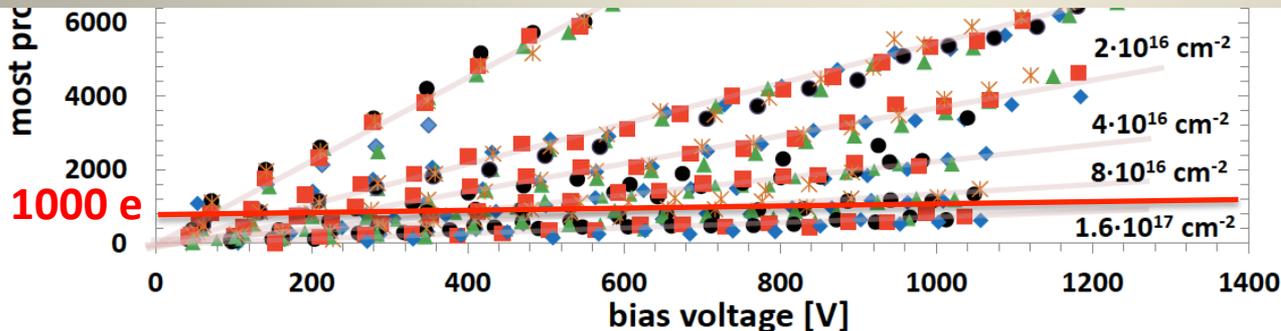
ATLAS FCAL

3000 fb^{-1}



Expectations for $10^{17} n_{eq}/\text{cm}^2$

- Linear extrapolation from low fluence data
 - Current: $I_{leak} = 4 \text{ A/cm}^3 @ 20^\circ\text{C}$
 - 2 mA for 300 μm thick 1 cm^2 detector @ -20°C
 - Depletion: $N_{eff} \approx 1.5 \times 10^{15} \text{ cm}^{-3}$
 - $FDV \approx 100 \text{ kV}$
 - Trapping $\tau_{eff} \approx 1/40 \text{ ns} = 25 \text{ ps}$
 - $Q \approx Q_0/d v_{sat} \tau_{eff} \approx 80 \text{ e}/\mu\text{m} \cdot 200 \mu\text{m}/\text{ns} \cdot 1/40 \text{ ns} = 400 \text{ e}$ in very high electric field ($\gg 1 \text{ V}/\mu\text{m}$)
- Observed signal not at all compatible with expectations

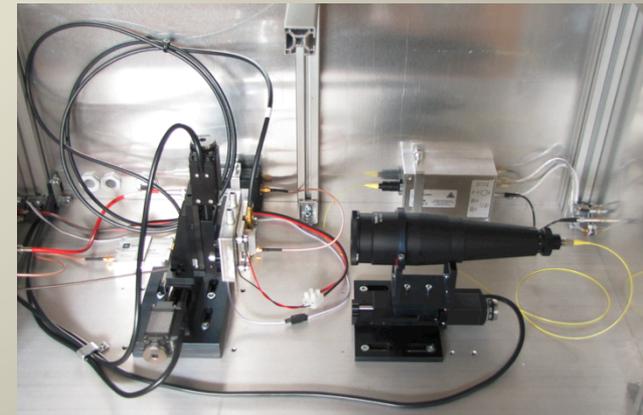
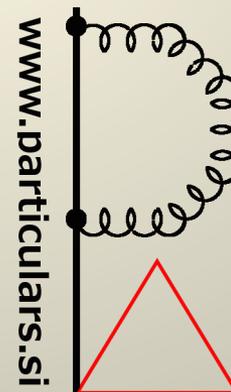
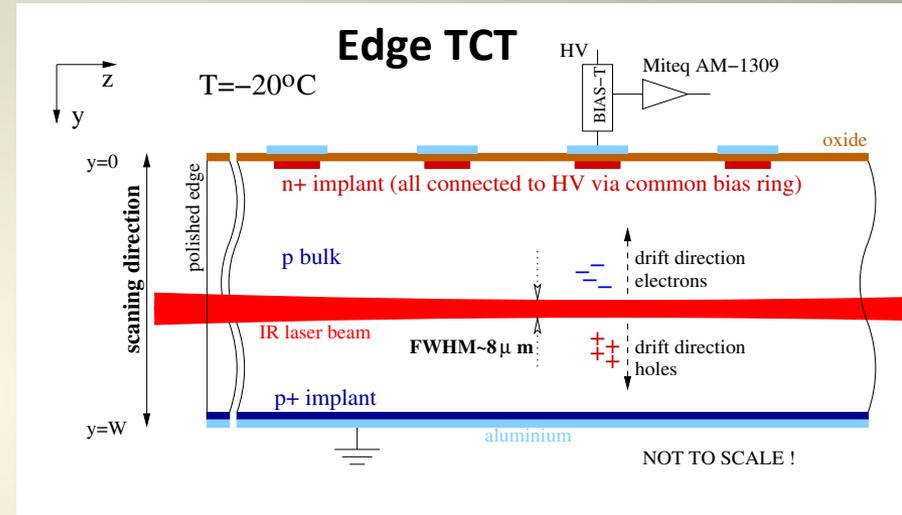


From:
**G. Kramberger et al.,
*JINST 8 P08004 (2013).***

Edge TCT

Edge-TCT

- Generate charges by edge-on IR laser perpendicular to strips, detector edge polished
- Focus laser under the strip to be measured, move detector to scan
- Measure induced signal with fast amplifier with sub-ns rise-time (Transient Current Technique)
- Laser beam width $8\ \mu\text{m}$ FWHM under the chosen strip, fast (40 ps) and powerful laser
 - Caveat – injecting charge under all strips effectively results in constant weighting (albeit not electric !) field

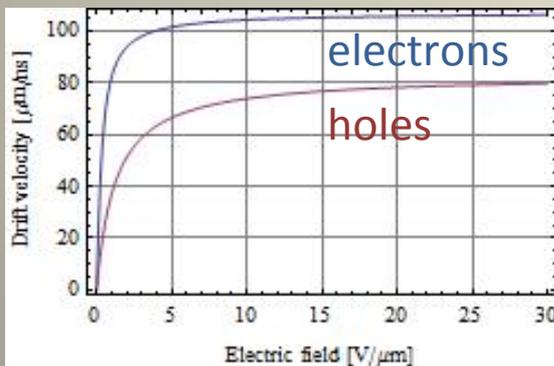


Electric Field Measurement

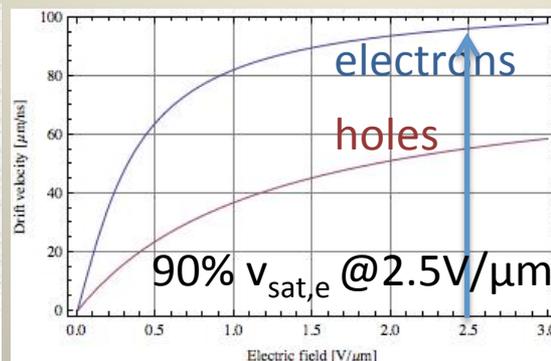


- Initial signal proportional to velocity sum at given detector depth
- Caveats for field extraction
 - Transfer function of electronics smears out signal, snapshot taken at ~ 600 ps
 - Problematic with heavy trapping
 - Electrons with v_{sat} hit electrode in 500 ps
 - Mobility depends on E
 - v saturates for $E \gg 1V/\mu m$

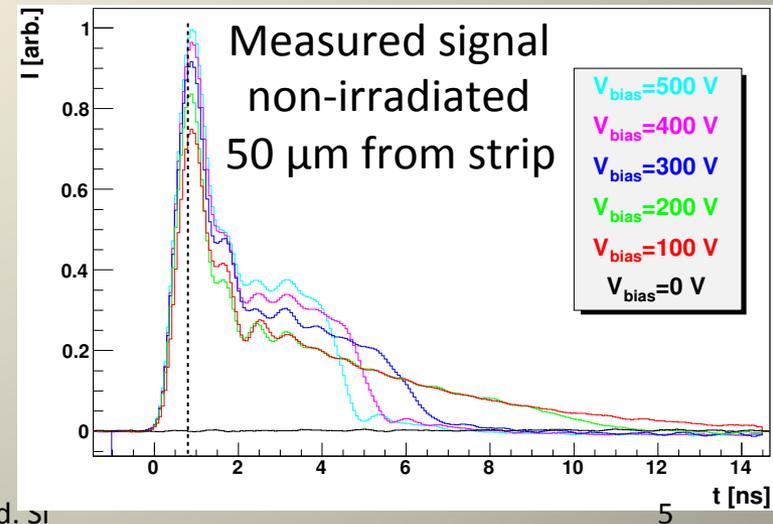
$$\begin{aligned}
 I(t=0) &= q \cdot \vec{v} \cdot \vec{E}_w = \\
 &= N_{e-h} e_0 \cdot (v_e + v_h) / d = \\
 &= N_{e-h} e_0 \cdot (\mu_e + \mu_h) \cdot E(x) / d
 \end{aligned}$$



RD50, Torino, June 8, 2016

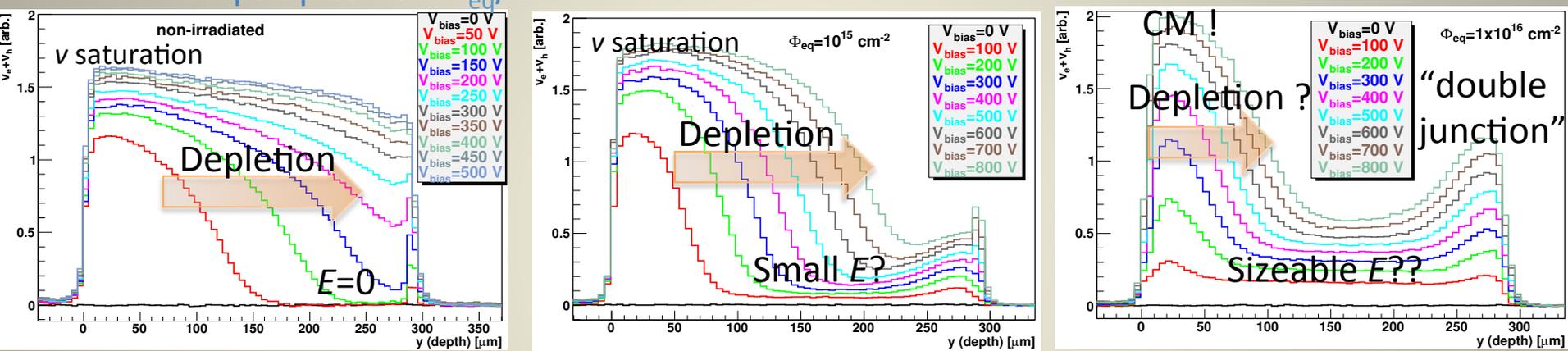


Marko Mikuž: E , μ and τ in irradi. Si



Selected Results from Neutrons

- Hamamatsu ATL07 n⁺ mini-strip, FZ p-type, neutron irradiated at JSI TRIGA reactor
 - In steps up to 10¹⁶ n_{eq}/cm²



- Very instructive regarding qualitative electric field shape
 - Non-irradiated “by the book” for abrupt junction n⁺p diode
 - SCR and ENB nicely separated, small double junction near backplane
 - Medium fluence ($\Phi=10^{15}$ neutrons): some surprise
 - Smaller space charge than expected in SCR, some field in “ENB”
 - Large fluence ($\Phi=10^{16}$): full of surprises
 - Still lower space charge, sizeable field in “ENB”
 - Charge multiplication (CM) additional trouble for interpretation at large V
- Nice, but let’s get *quantitative* !

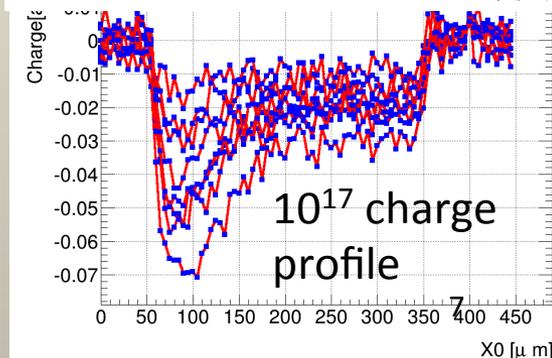
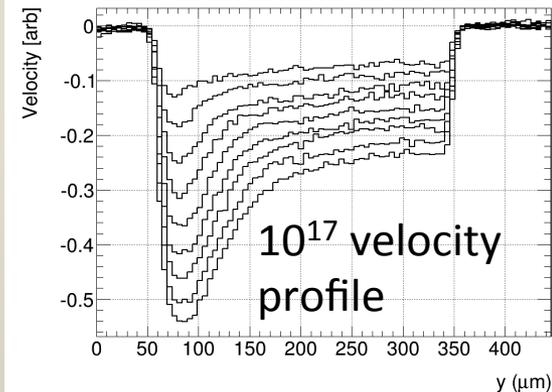
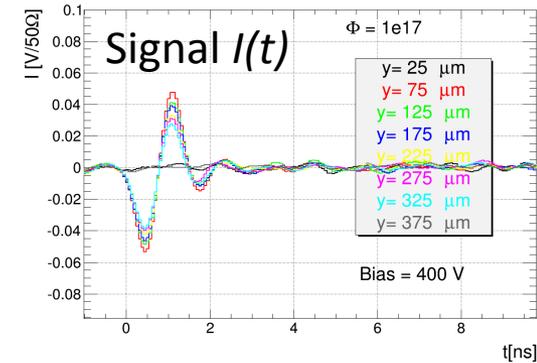
Published in :
**G. Kramberger et al.,
 JINST 9 P10016(2014).**

Extending the Reach

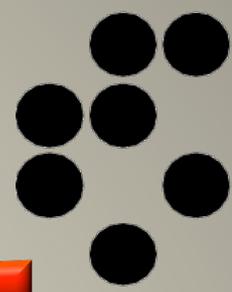
- In 2014 added 5×10^{16} and 10^{17} n_{eq}/cm^2 measurements of the same detector
 - 10^{16} of this fluence fully annealed, the rest 80 min @ $60^\circ C$
- Intrinsic feature – signal oscillations
 - period $\sim 5/4$ ns
 - LRC ($C \sim 2$ pf $\Rightarrow L \sim 20$ nH ~ 1 cm of wire)
 - velocity (slope) and charge (integral) yield consistent results
 - should be, as $Q \approx Q_0 v_{sum} \tau_{eff} / d$

☹ Cannot use $I(t)$ to measure trapping...

☑ ... shall be revised



Absolute Field Measurement



- Solution: *concurrent* forward bias v_{sum} measurements
 - Ohmic behaviour with some linear (field) dependence

- constant (positive) space charge

– can use $\int E(y) dy = \bar{E}d = V$ to pin down field scale

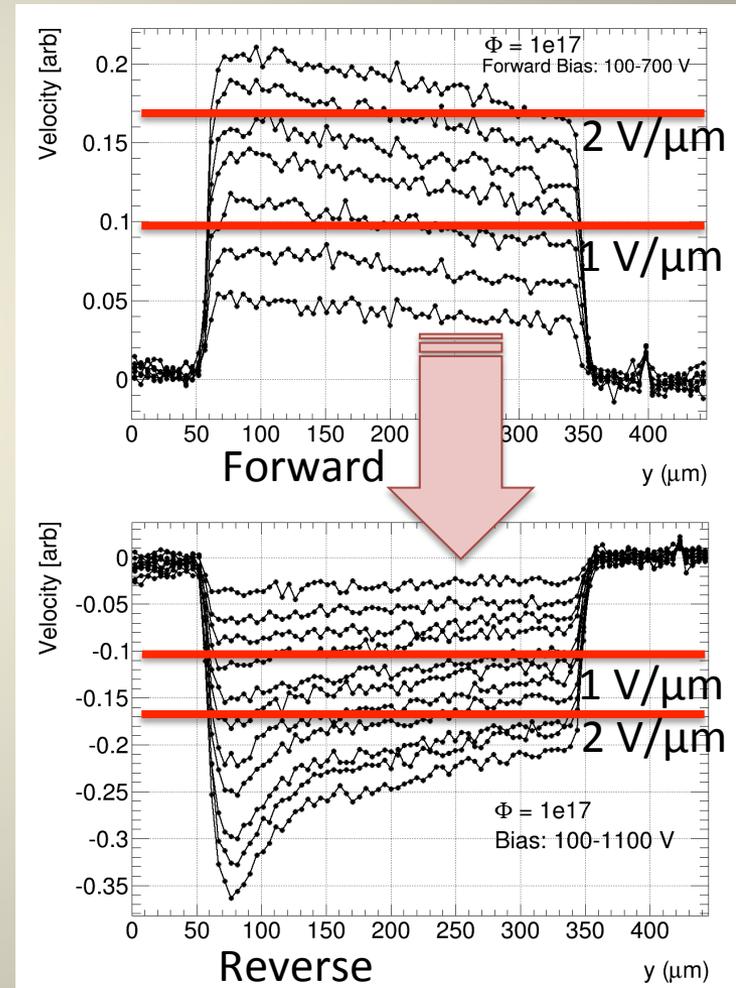
- corrections from $v(E)$ non-linearity small

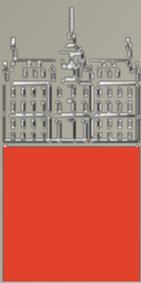
- Use same scale for reverse bias!

- FW measurements up to 700 V

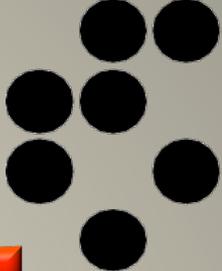
– know E scale up to $2.33 \text{ V}/\mu\text{m}$

– can reveal $v(E)$ dependence



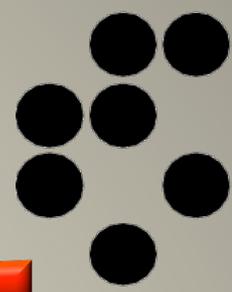


Proton Irradiations



- 5 sample pairs of ATL12 mini-strips irradiated at CERN PS during summer 2015
 - got 0.5, 1.0, 2.9, 11, 28e15 protons/cm²
 - NIEL hardness factor 0.62
 - thanks to CERN IRRAD team
- Covers HL-LHC tracker range well
- Samples back in September 15, 2 per fluence investigated by E-TCT for all fluences
 - concurrent forward and reverse bias measurements

Mobility Considerations FW bias

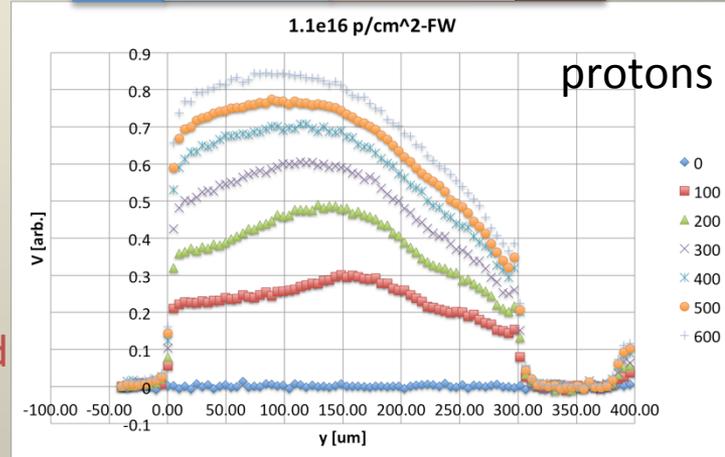
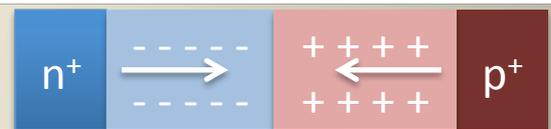
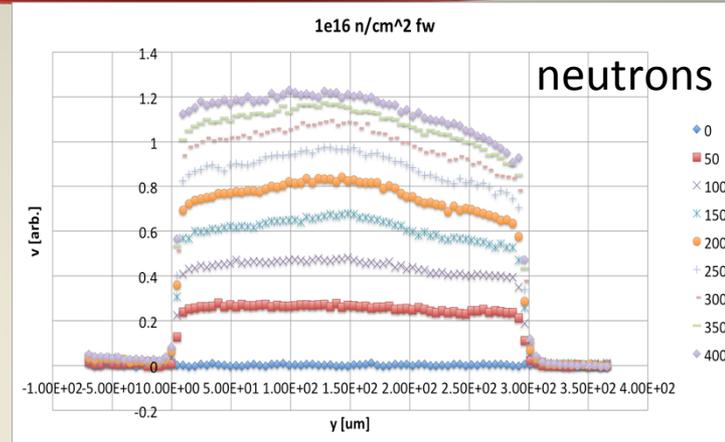


- For forward bias can extract $v(E)$ up to a scale factor
- Observe less saturation than predicted
- Model with

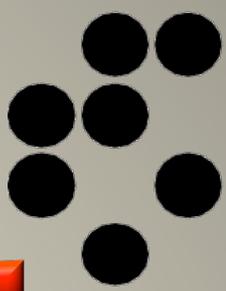
$$v_{sum}(E) = \frac{\mu_{0,e}E}{1 + \frac{\mu_{0,e}E}{v_{e,sat}}} + \frac{\mu_{0,h}E}{1 + \frac{\mu_{0,h}E}{v_{h,sat}}}$$

- keep saturation velocities at nominal values @-20°C ($v_{e,sat} = 107 \mu\text{m/ns}$; $v_{h,sat} = 83 \mu\text{m/ns}$)
- float (common) zero field mobility degradation
- fit $v(E)$ for $\phi_n \geq 5 \times 10^{15}$ and $\phi_p \geq 3 \times 10^{15}$

n.b. FW profiles less uniform for lower fluences and for protons, but departures from average field still small

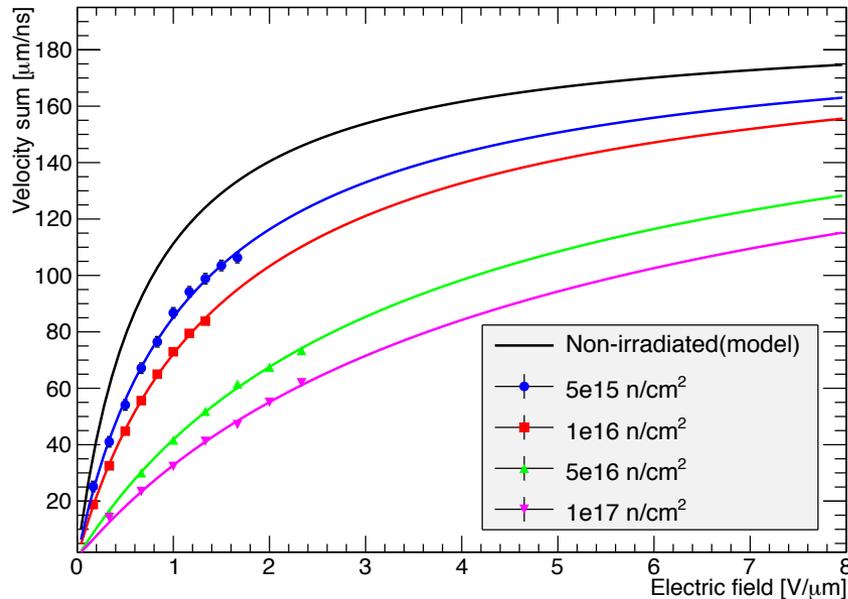


Mobility Fits

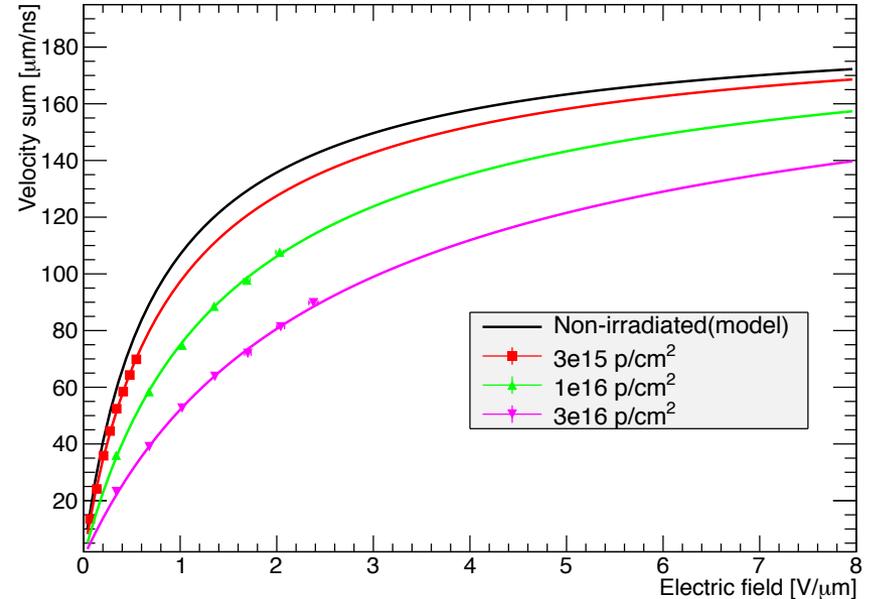


- Data follow the model perfectly
 - μ_0 degradation the only free parameter, scale fixed by $v_{sum,sat}$
 - although E range limited, $v_{sum,max}$ still $> 1/3$ of $v_{sum,sat}$

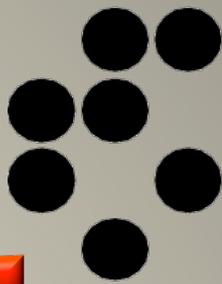
Mobility neutrons



Mobility protons



Mobility Results



- Fit to $v_e + v_h$ with common mobility degradation factor
 - factor of **2** at $10^{16} n_{eq}/cm^2$
 - factor of **6** at $10^{17} n_{eq}/cm^2$
 - need **2x/6x** higher E to saturate v !

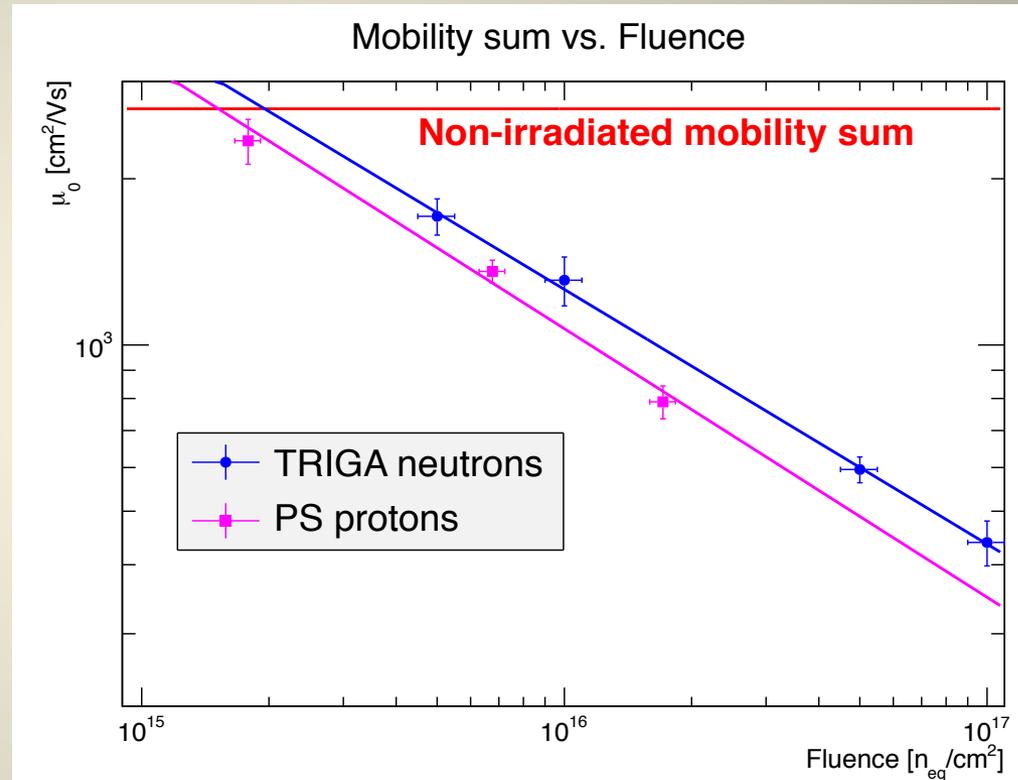
Φ_n	$\mu_{0,sum}$	Φ_p	$\mu_{0,sum}$
[$10^{15} n_{eq}/cm^2$]	[cm^2/Vs]	[$10^{15} n_{eq}/cm^2$]	[cm^2/Vs]
non-irr (model)		2680	
5	1661 ± 134	1.8	2165 ± 212
10	1238 ± 131	6.8	1319 ± 67
50	555 ± 32	17	750 ± 54
100	407 ± 40	T=-20°C	

Mobility Analysis

- Fit mobility dependence on fluence with a power law

$$\mu_{0,sum}(\Phi) = C\Phi^a$$

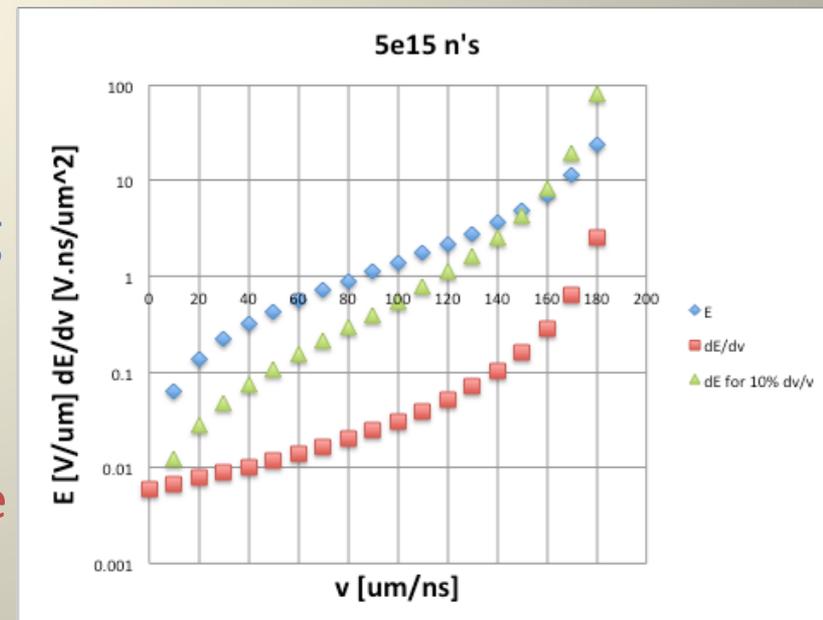
- Fits perfectly with $a \approx -1/2$ indicating a single scattering process in this fluence range
 - ~same a for neutrons and protons
- Below $\sim 10^{15} n_{eq}/cm^2$ the process gets obscured by acoustic phonon scattering
- At same equivalent fluence, mobility decrease $\sim 20\%$ worse for protons
 - NIEL violation
- Is $a \approx -1/2$ accidental?



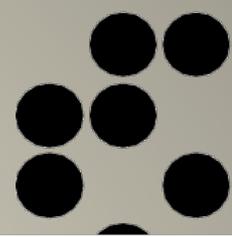
Irradiation particle	a	σ_a
Reactor neutrons	-0.46	0.04
PS protons	-0.49	0.05

Velocity and Field Profiles

- Knowing $v(E)$ can set scale to velocity profiles
 - assumption: same scale on FW and reverse bias
 - protons: for 5×10^{14} and 10^{15} use same scale, fixed by average field for 5×10^{14} at 1100 V (no good FW data)
- Invert $E(v)$ to get electric field profiles
 - big errors when approaching v_{sat} i.e. at high E
 - exaggerated by CM in high field regions
 - $v > v_{sat}$ not physical, but can be faked by CM



Velocity Profiles Neutrons



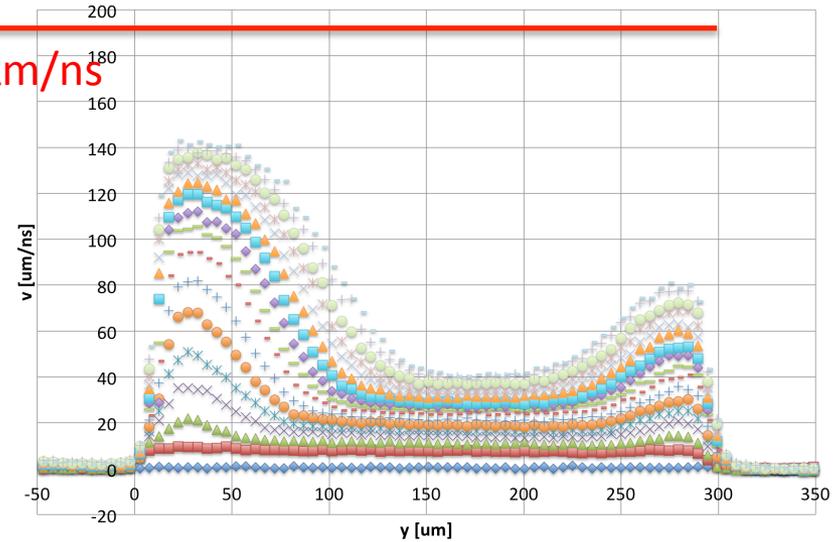
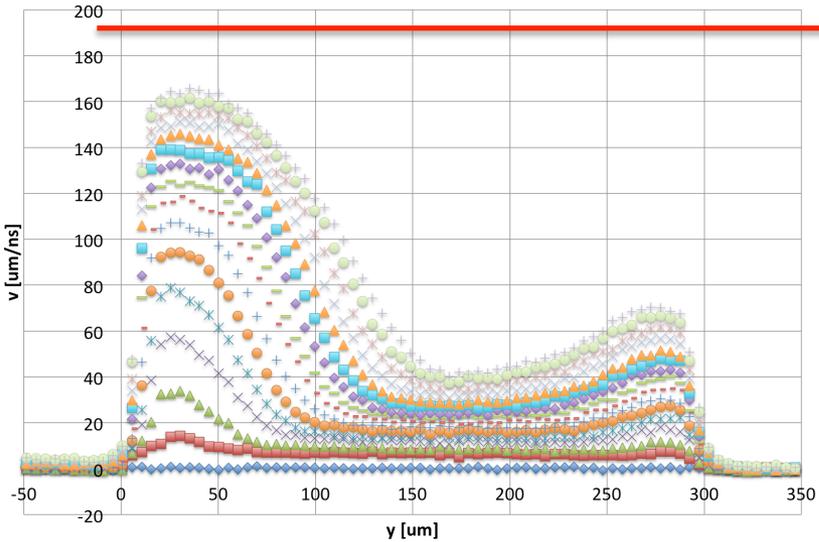
Velocity profile 5e15

Velocity profile 1e16

$v_{50} = 190 \mu\text{m/ns}$

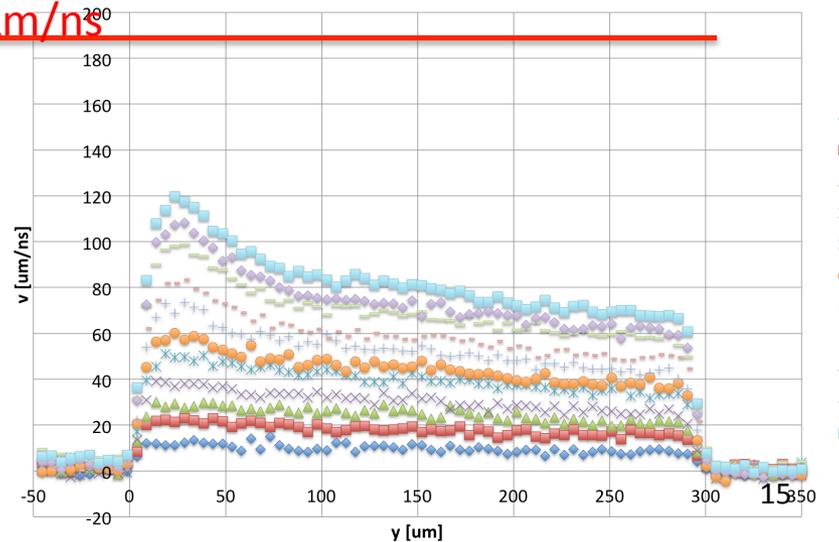
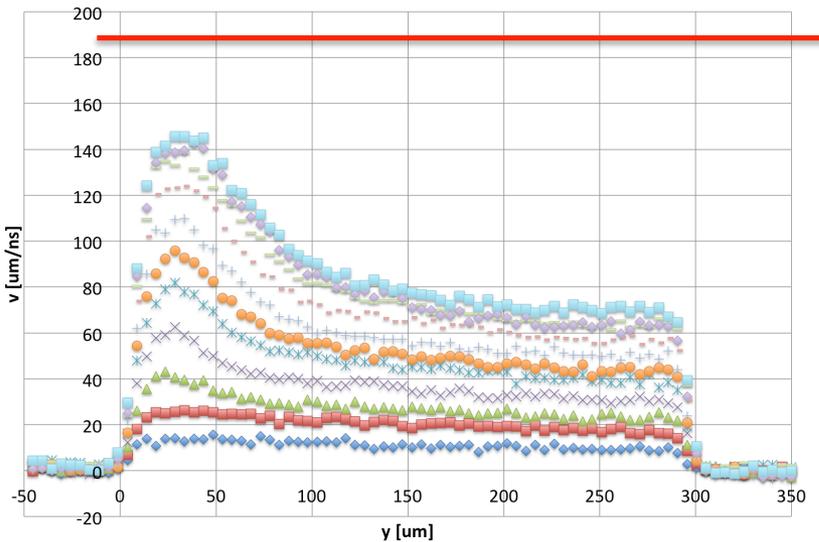
$v = 190 \mu\text{m/ns}$

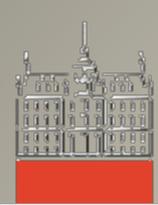
: E, μan



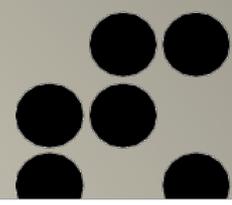
Velocity profile 5e16

Velocity profile 1e17

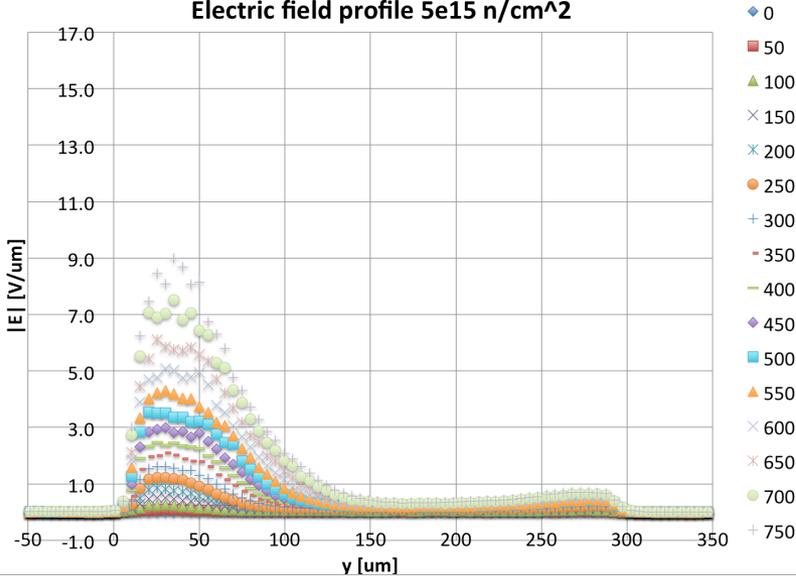




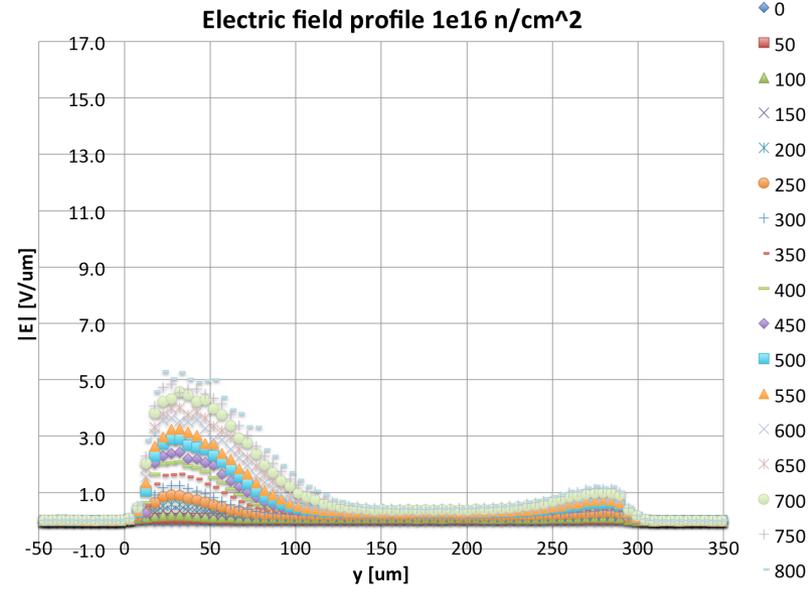
Field Profiles Neutrons



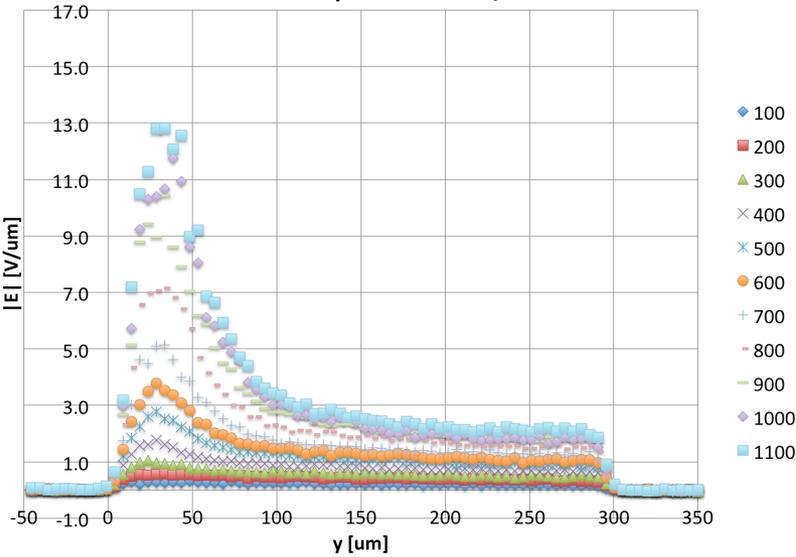
Electric field profile 5e15 n/cm²



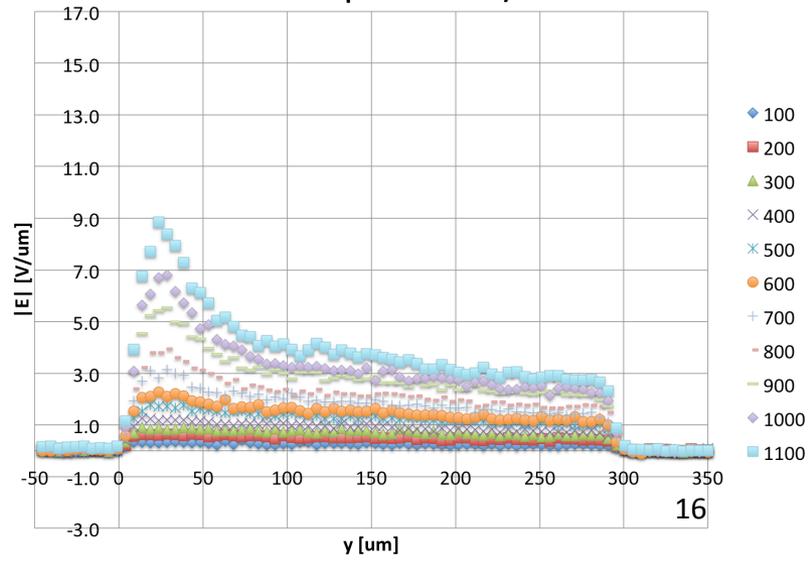
Electric field profile 1e16 n/cm²



Electric field profile 5e16 n/cm²



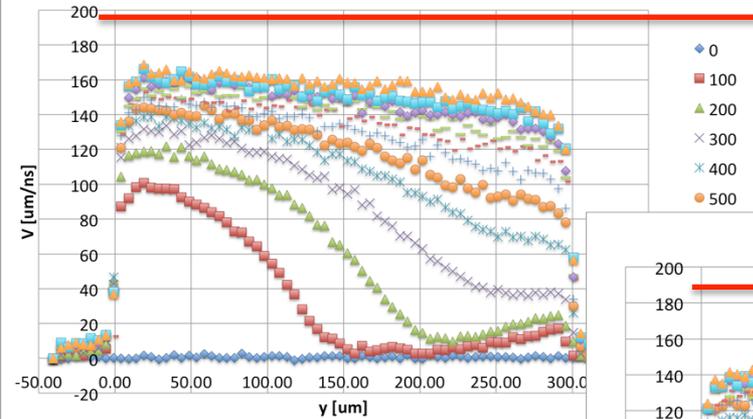
Electric field profile 1e17 n/cm²



Mikuž: E, μ and τ in i

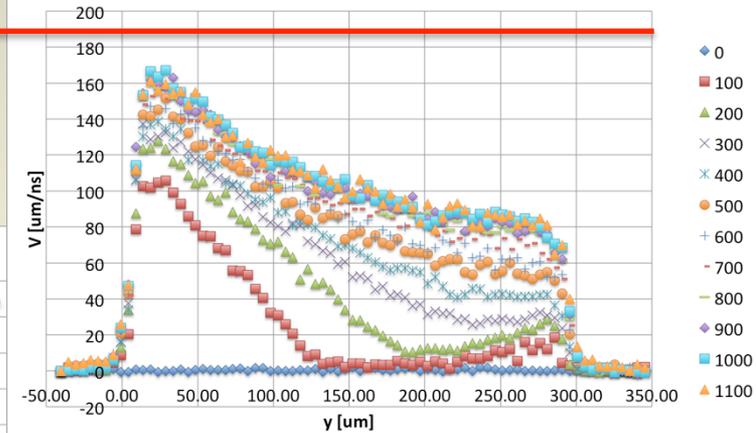
Velocity Profiles Protons

Velocity profile 5e14 p/cm²

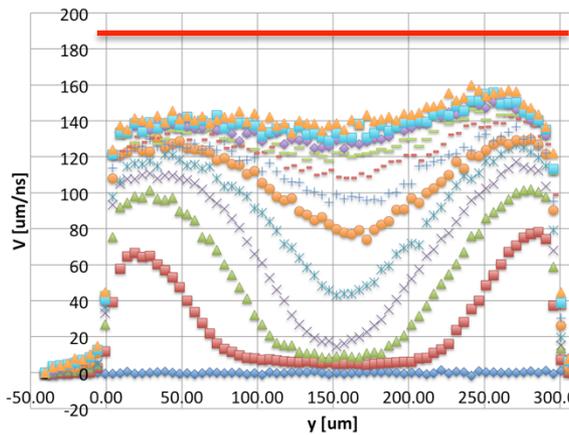


$v = 190 \mu\text{m/ns}$

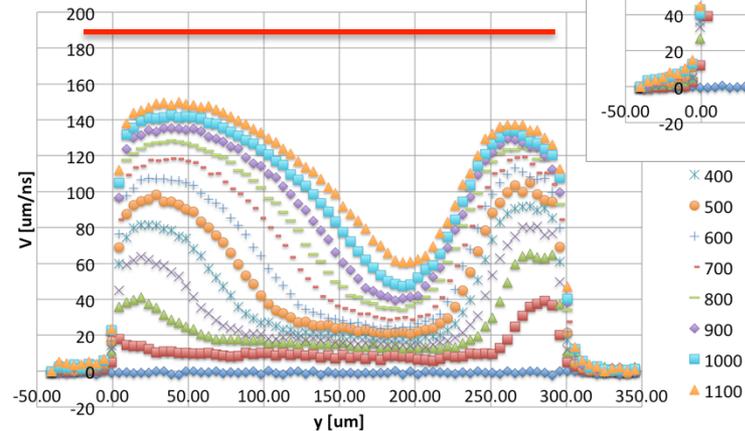
Velocity profile 1e15 p/cm²



Velocity profile 2.9e15 p/cm²

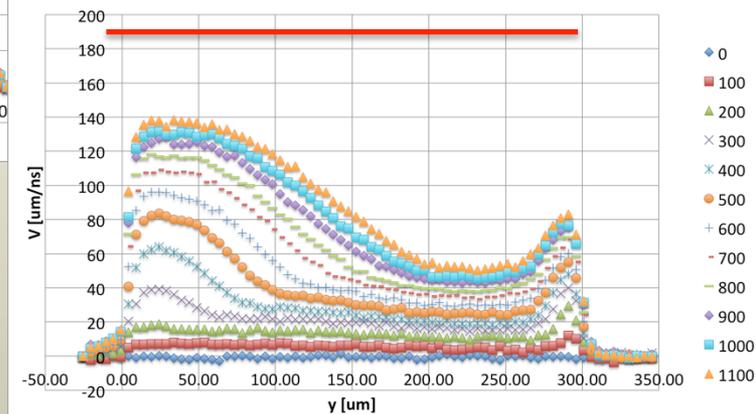


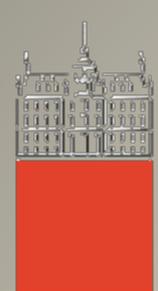
Velocity profile 1.1e16 p/cm²



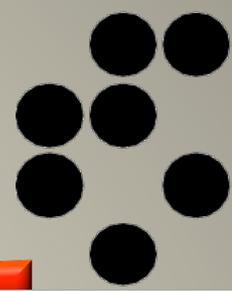
Same scale as for neutrons

Velocity profile 2.8e16 p/cm²

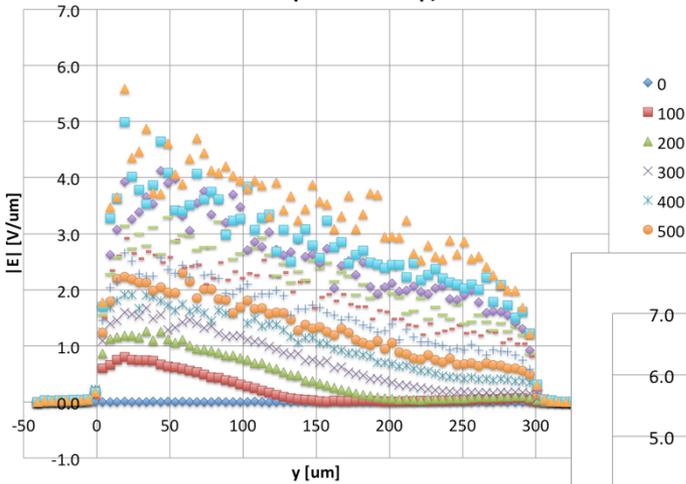




Field Profiles Protons

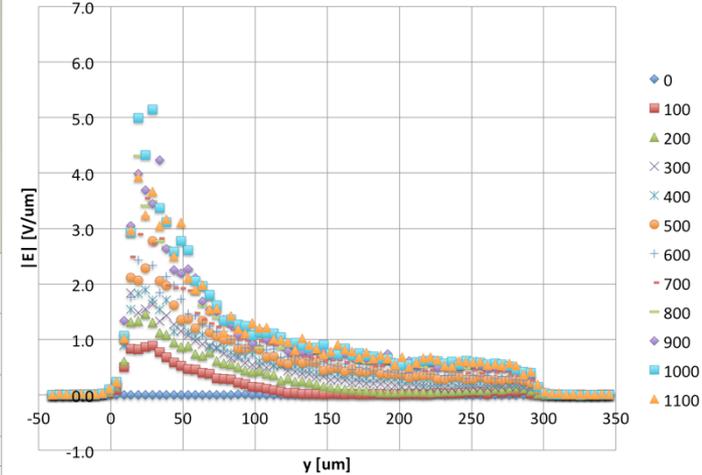


Electric field profile $5e14 \text{ p/cm}^2$

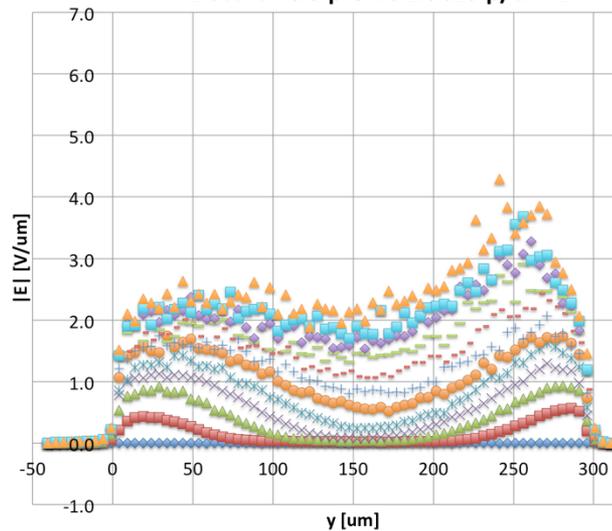


Smaller peak fields
than for neutrons
Scale 0-7 V/ μm

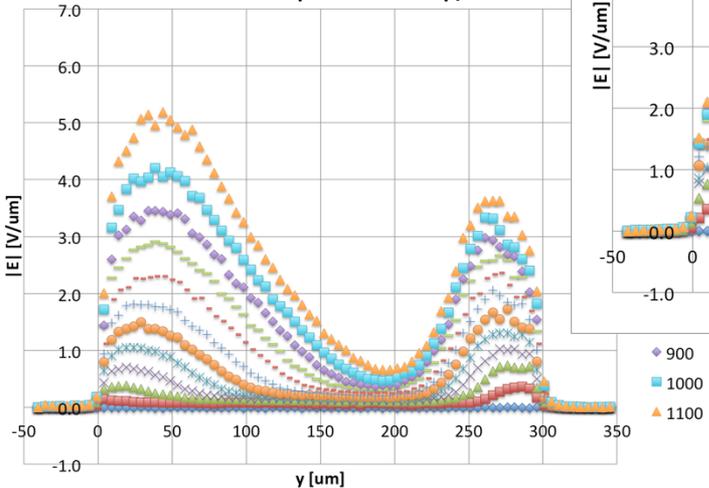
Electric field profile $1e15 \text{ p/cm}^2$



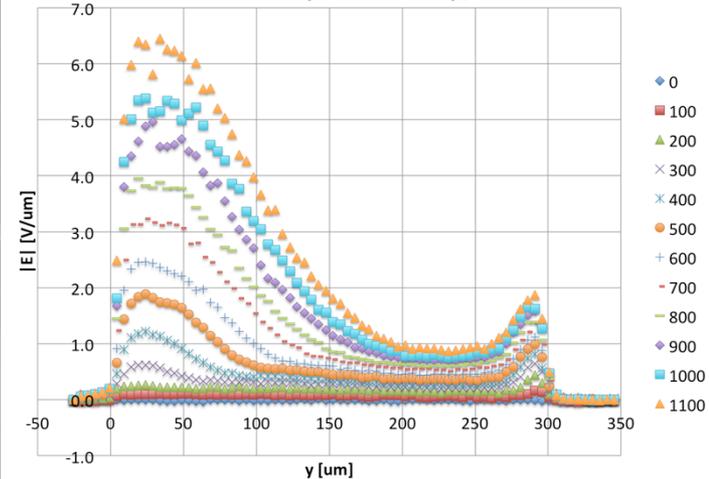
Electric field profile $2.9e15 \text{ p/cm}^2$



Electric field profile $1.1e16 \text{ p/cm}^2$

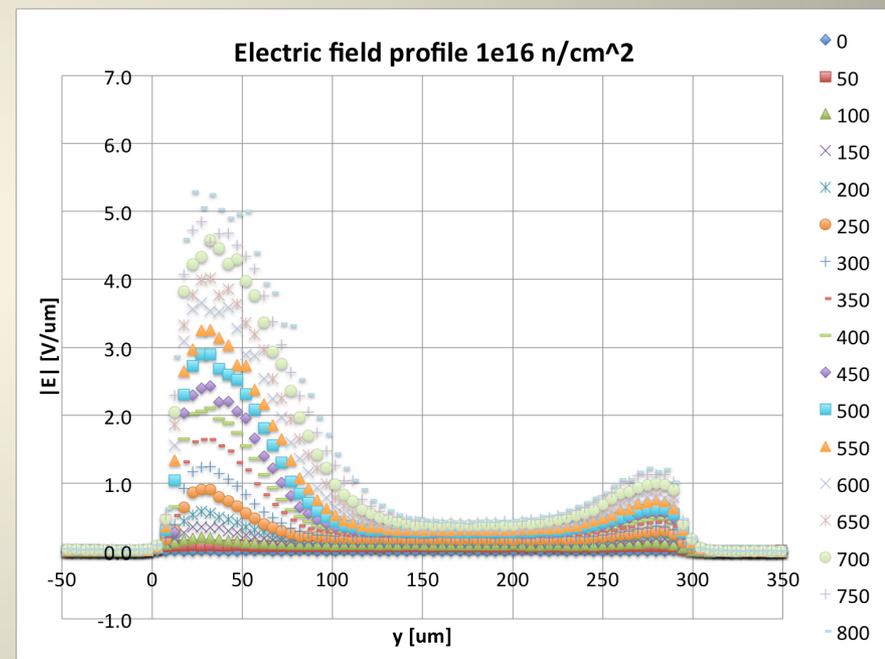
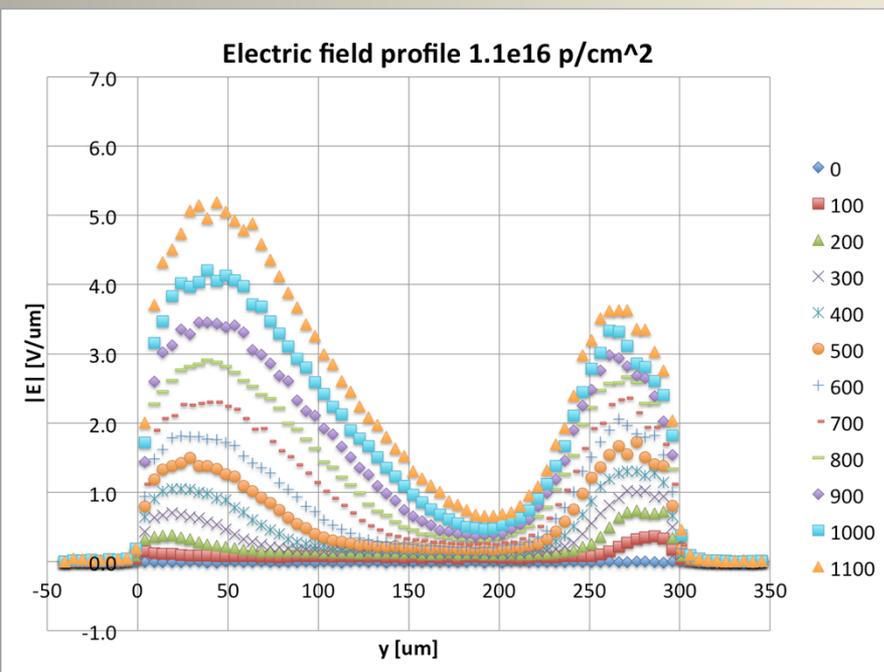


Electric field profile $2.8e16 \text{ p/cm}^2$

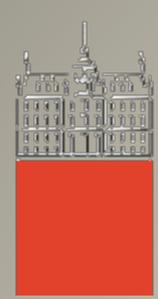


Protons \leftrightarrow Neutrons $\sim 10^{16}$

- Field profiles compared



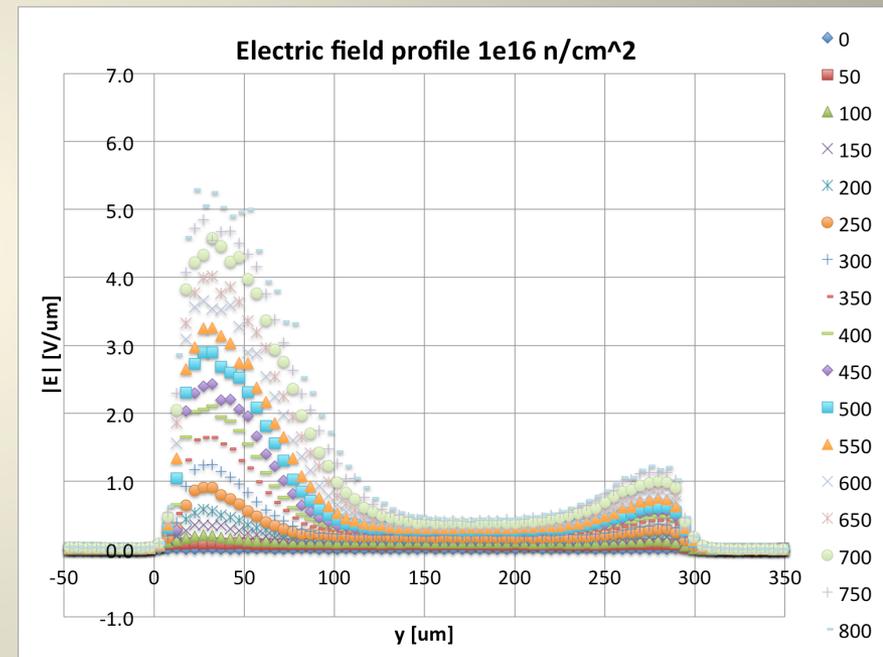
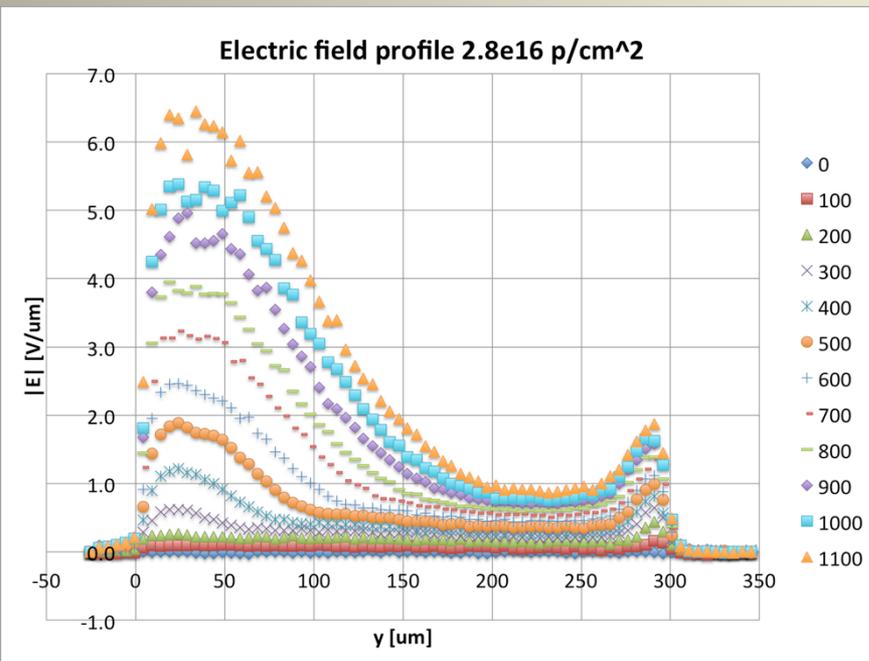
- Protons with more “double junction”, flatter field, less peaked at junction



Protons 2.8×10^{16} p/cm²



- Field profile, compared to 10^{16} neutrons



- Looks more neutron-like, with deeper SCR

Trapping Considerations

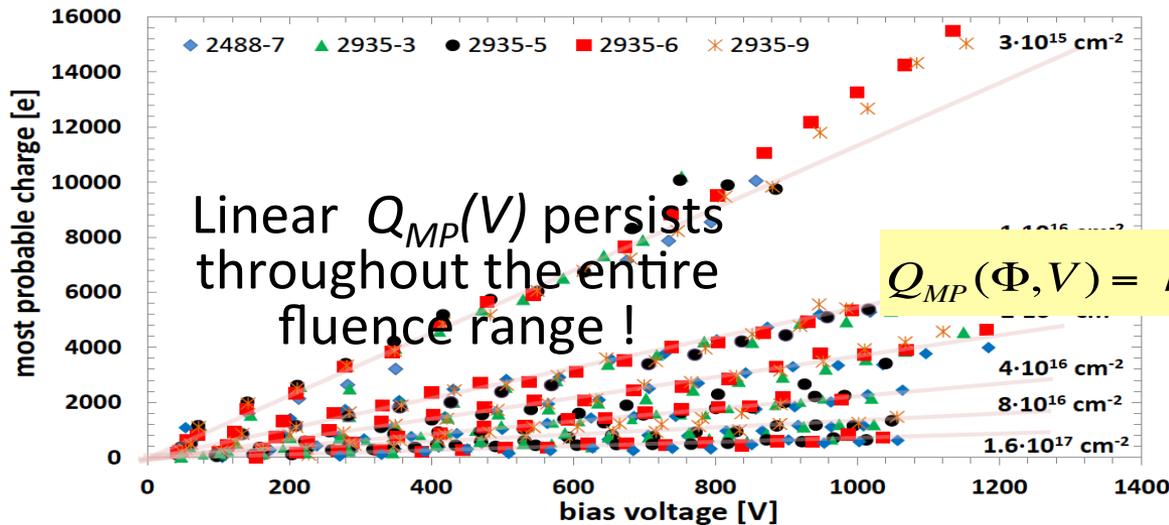
- Extrapolation from low fluence data with $\beta_{e,h}(-20^\circ\text{C})=4.4,5.8 \times 10^{-16} \text{ cm}^2/\text{ns}$; $1/\tau=\beta\Phi$

Φ [1e15]	5	10	50	100
τ [ps]	400	200	40	20
$mfp@v_{sat}$ [μm]	95	48	9.5	4.8
MPV [e_0]	7600	3800	760	380
$MPV@1000 \text{ V}$	8900	5500	1800	1150
$CCD_{1000 \text{ V}}$ [μm]	110	70	23	14

From "magic formula"
JINST 9 P10016(2014)

- Measured data exceeds (by far) linear extrapolation of trapping
 - n.b.1: $E \sim 3 \text{ V}/\mu\text{m}$ by far not enough to saturate velocity
 - n.b.2: little sign of CM at highest fluence

Magic revisited

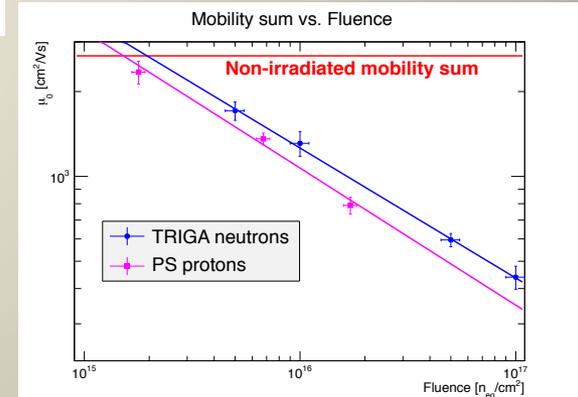


$$Q_{MP}(\Phi, V) = k \cdot (\Phi / 10^{15} \text{ n}_{eq}/\text{cm}^2)^b \cdot V$$

$$k = 26.4 \text{ e}_0 / \text{V}$$

$$b = -0.683$$

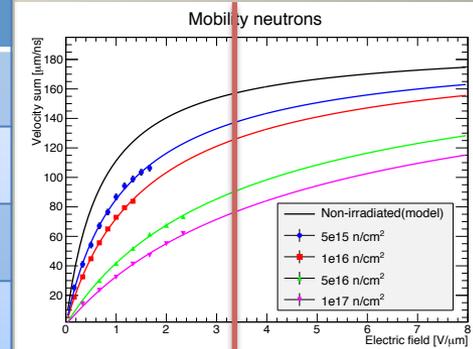
- $Q=k \cdot V$ most natural when linear $v(E)$
 - not to $E \sim 3 \text{ V}/\mu\text{m}$, especially at low Φ
 - far from saturation, too
- Fluence dependence as $\Phi^{-2/3}$
 - but mobility already decreases as $\Phi^{-1/2}$
- Small margin left for trapping increase, certainly not linear



More Considerations

- More realistic: take v_{sum} at average $E = 3.3 \text{ V}/\mu\text{m}$

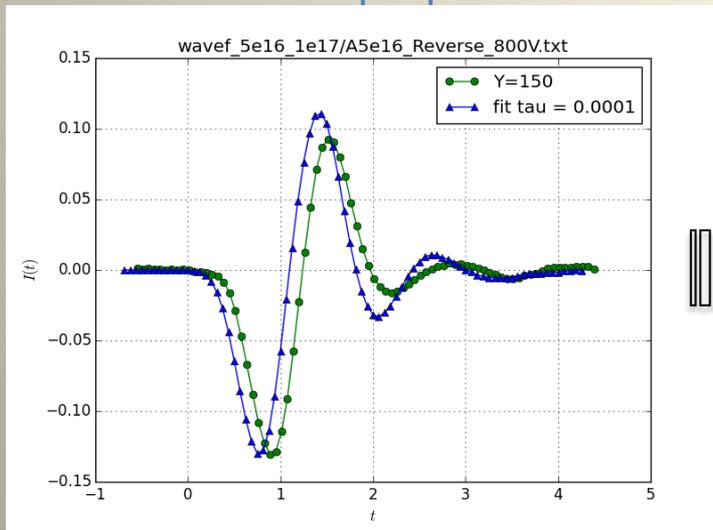
Φ [1e15]	5	10	50	100
$v_{sum}(3.3 \text{ V}/\mu\text{m})$	137	126	90	77
$CCD_{1000 \text{ V}} [\mu\text{m}]$	110	70	23	14
$\tau \approx CCD/v$ [ps]	800	560	260	180
τ_{ext} [ps]	400	200	40	20



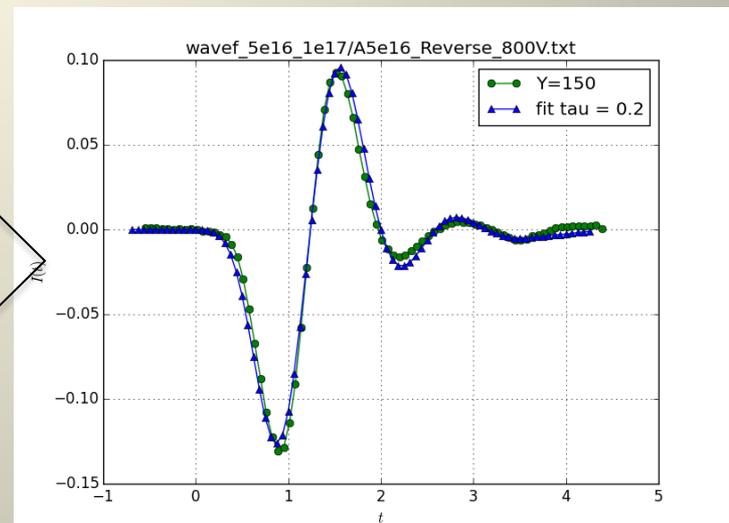
- Implies factor of 6-9 less trapping at highest fluences
 - lowest fluence still x2 from extrapolation
 - weak dependence on fluence as anticipated by “-1/6” power law
 - not good when large E variations (damped by $v(E)$)
 - not good when $CCD \approx$ thickness (less signal at same τ)

Exploiting TCT Waveforms

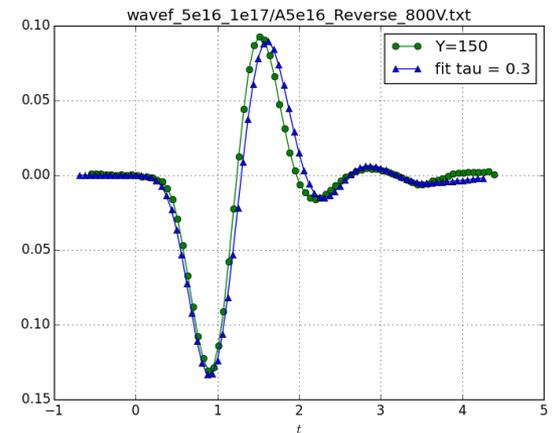
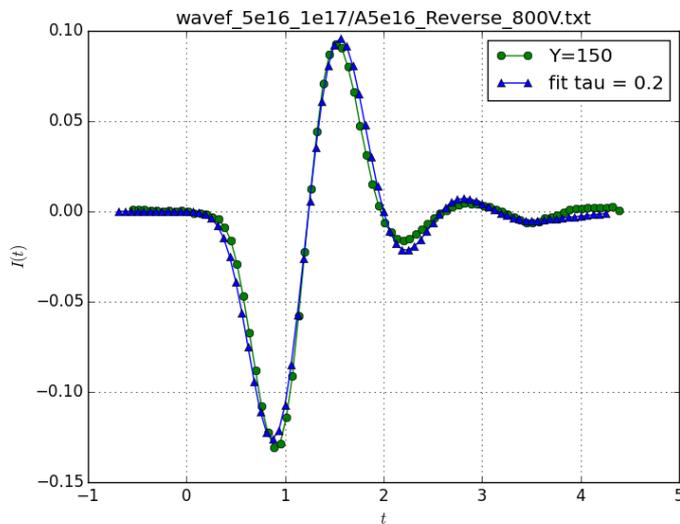
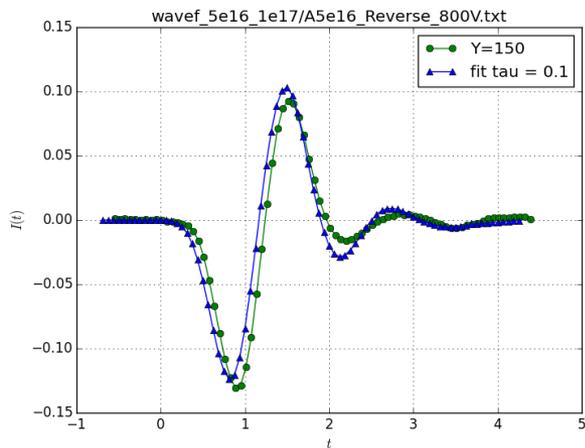
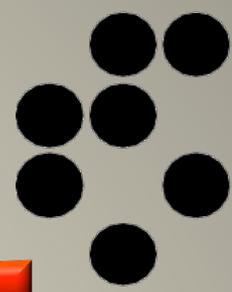
- Waveforms at $y=100 \mu\text{m}$, 800 V, 5×10^{16} and 10^{17}
 - $E \approx 3 \text{ V}/\mu\text{m}$, CCD/2 implies signal within $\sim 10 \mu\text{m}$ or $< 0.2 \text{ ns}$
 - the rest you see is the transfer function of the system
- Still distinct signals from the two fluences
 - treat 10^{17} waveform as transfer function of the system
 - convolute with $e^{-t/\tau}$ to match 5×10^{16} response
 - $\tau = 0.2 \text{ ns}$ provides a good match
- In fact, measure $\Delta\tau$, as “transfer” already convoluted with $e^{-t/\tau(1e17)}$!
 - Should do proper Fourier analysis, on the way...



$\tau = 0.2 \text{ ns}$



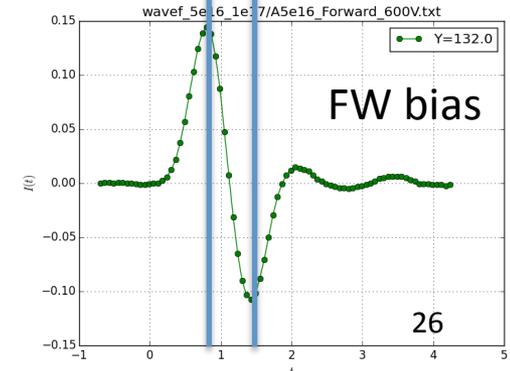
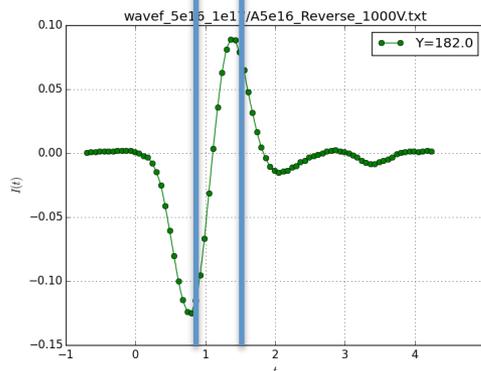
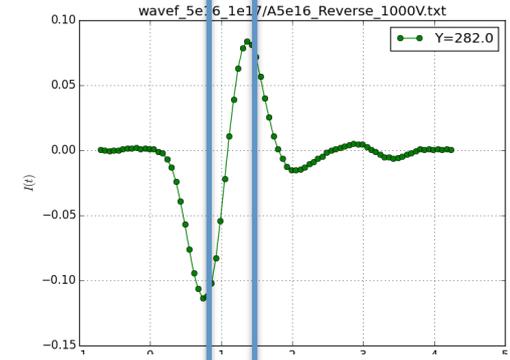
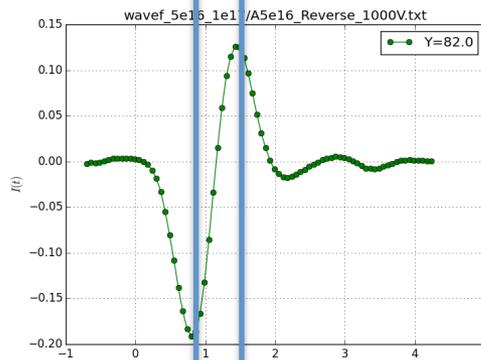
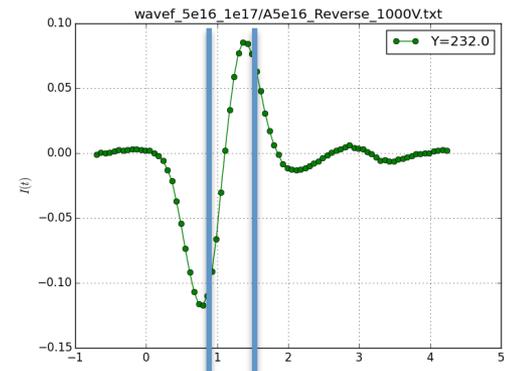
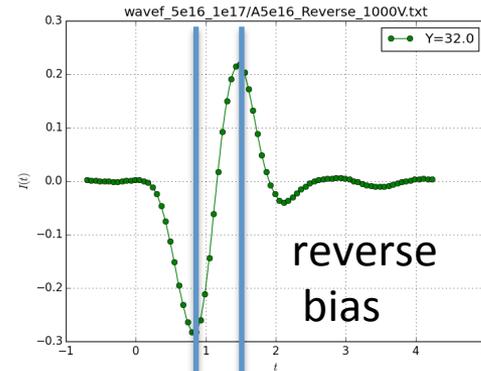
Waveforms: How sensitive ?

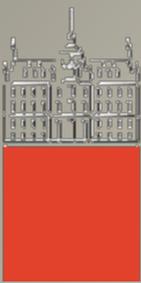


- $\Delta\tau = 0.2$ ns certainly best fit, 0.1 too narrow, 0.3 too broad
- precision ~ 50 ps

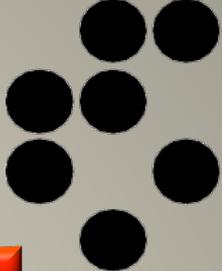
Trapping – position dependence ?

- Waveforms plotted every 50 μm in detector depth for reverse bias at 1000 V
- Forward bias in middle of detector added at 600 V
- Very little, if any, wf dependence on position observed
- Trapping not position dependent !?





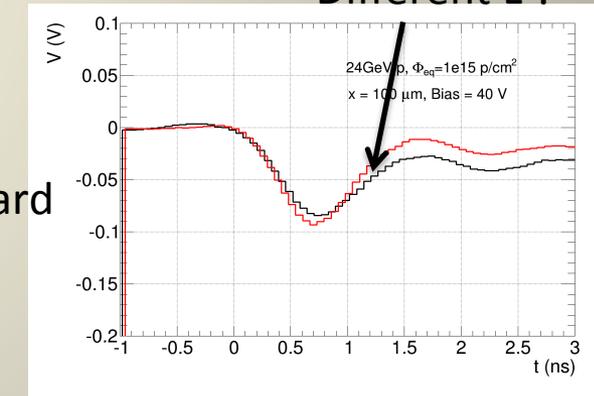
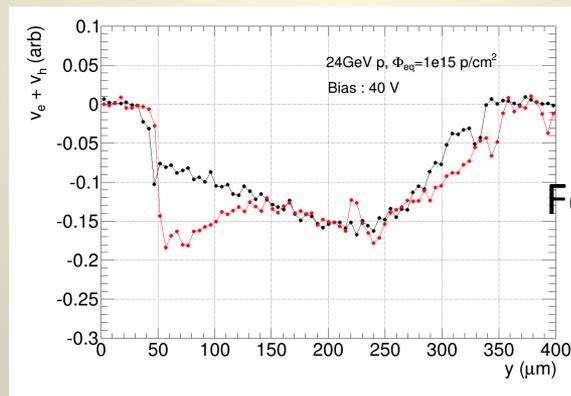
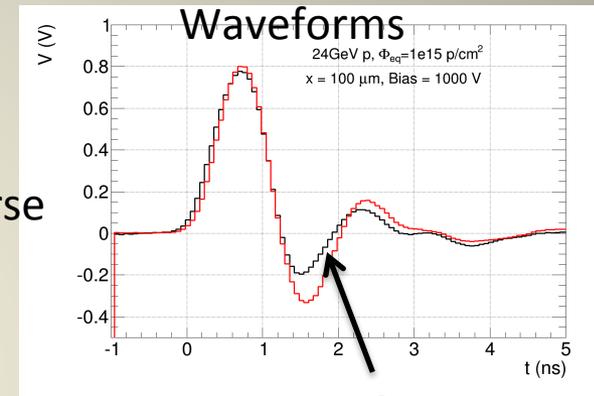
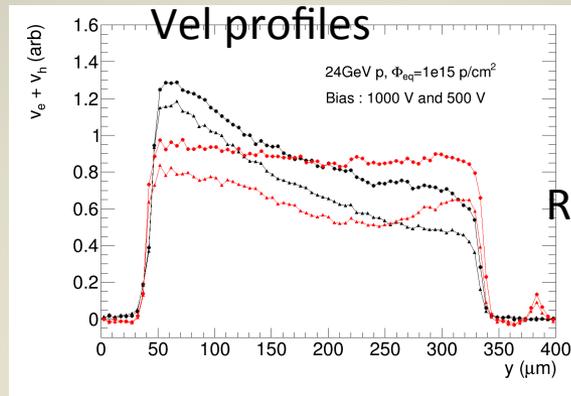
Do's and Don'ts



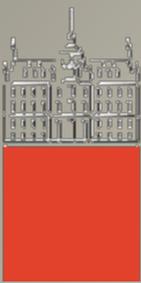
- As a rule: never repeat an experiment that looks ok'ish, just publish
 - But if you have to spend millions, you better do
 - What are the error bars associated to the measurements shown ?
 - for p's we have 2 samples at each fluence
 - comparison should tell us a lot
- ...and it does !

Worst Case ?

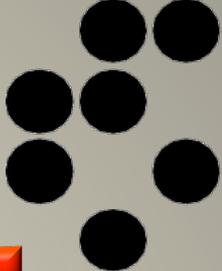
- $1e15$ p's
 - both samples irradiated in parallel
 - measured in the same setup, by the same person
- Should look the same...
- ...they definitely *don't*, even not *qualitatively* !



- Preliminary, let's hope we find the cause...
- Hard to claim errors with such discrepancy

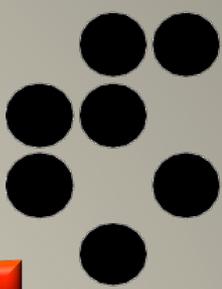


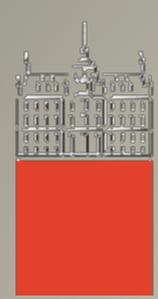
Summary



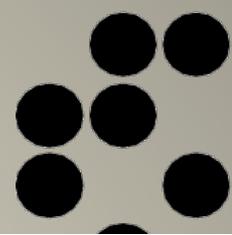
- Velocity profiling performed for Si detectors irradiated
 - with neutrons from 10^{15} to 10^{17} $n_{\text{eq}}/\text{cm}^2$
 - with protons from 5×10^{14} to 3×10^{16} p/cm^2
- Velocity vs. electric field fluence impact observed and interpreted as reduction of zero field mobility
 - Zero field mobility follows power law with $a \approx -1/2$
 - Protons degrade mobility by $\sim 20\%$ more
- Absolute velocities and field maps provided
 - With caveats at high electric fields
- Trapping estimates for very high neutron fluences
 - from charge collection
 - from waveforms
 - all estimates point to severe non-linearity of trapping with fluence
- To do:
 - CCE for protons
 - Reproducibility ?!
 - Sensible error estimates

Backup Slides

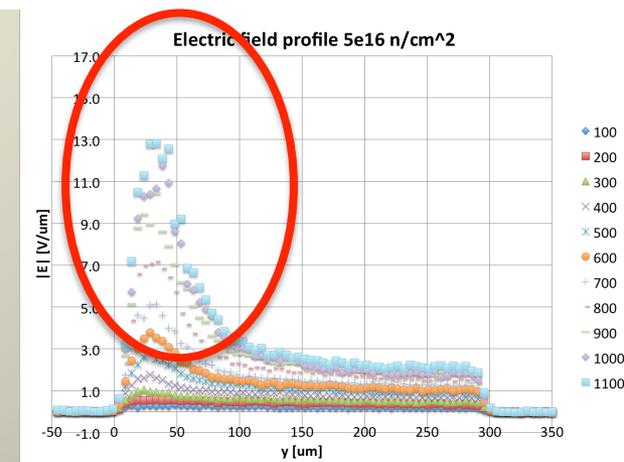
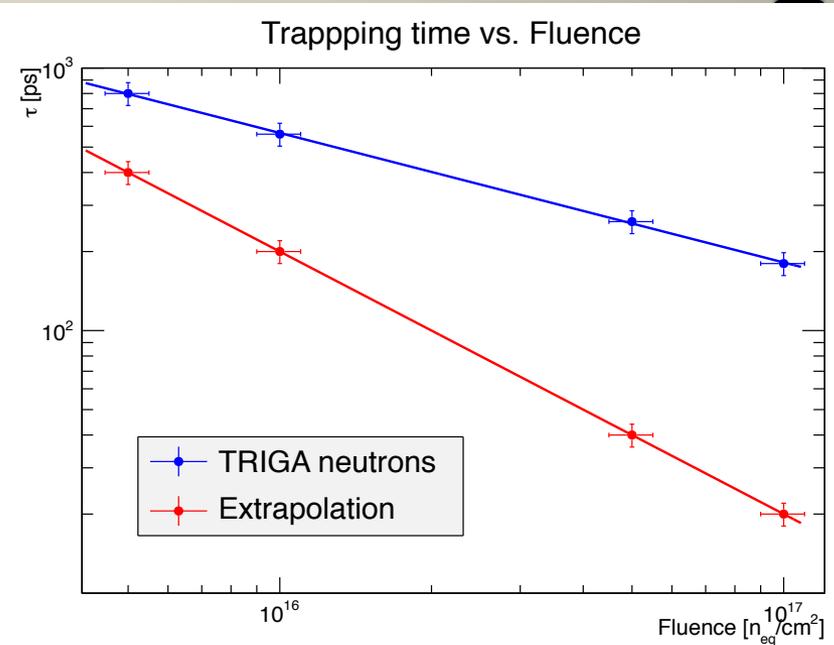




Result ?

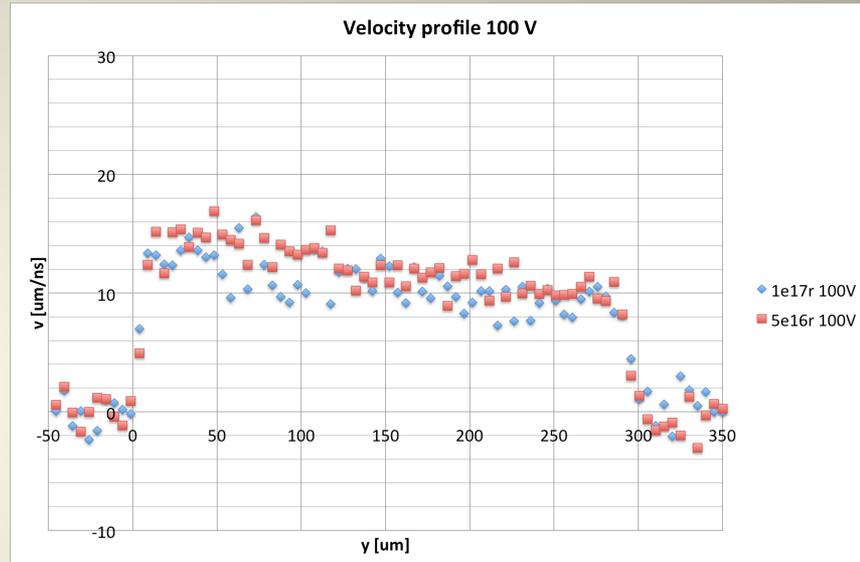


- Victory ? Wrong... two effects
 - saturating $v(E)$ -> less signal, effectively more trapping
 - charge multiplication -> more signal, less trapping
- Old story revisited, no handle on 1st few 10 microns where a lot can happen



Another try

- Focus on cases with small and linear $v(E) \rightarrow v(\bar{E}) = \bar{v}$
 - 100 V at 5×10^{16} and 10^{17} look promising – flat field
 - also the integral of $E(x)$ yields 63/100 and 76/100 V
- Can assume linear $v(E)$ in whole detector
 - assume same ratio as for low fluences
 - less trapping compared to linear extrapolation by factors of 3.2 and 5.4



Φ	τ_e [ps]	τ_h [ps]
5e16	147	81
1e17	81	62