



Characterisation and Comparison of Event Generators for Pair Conversion: *A Crucial Step for Future Low Energy Gamma Telescopes*

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- Motivation
- Conversion kinematics
- exact 5D generator validation
- Comparison of generators
 - Angular resolution
 - Polarimetry
- Conclusions



Telescope projects



C	Ciliana	
Gaseous	Silicon	Emulsion
<u> </u>	<u> </u>	

HARPO e-ASTROGAM GRAINE

AdEPT ComPair

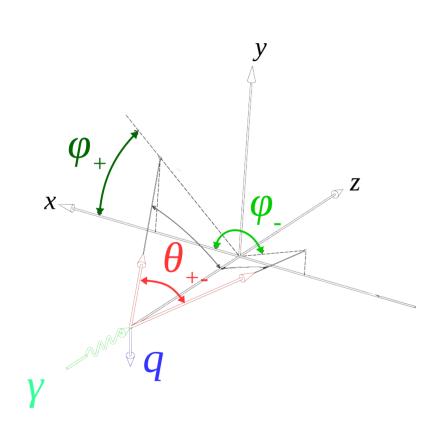
PANGU

- Improvement on angular resolution of tracks
 - Light (low scattering) + (very) fine point resolution
 - Better angular resolution for photon
 - Access to polarisation



Kinematics





- *q* recoil momentum
- θ_{+} opening angle

$$\bullet \ \chi_{+} = E_{+}/E_{\gamma}$$

•
$$\phi = (\phi_{-} + \phi_{+})/2$$
 azimuthal angle



5D exact generator

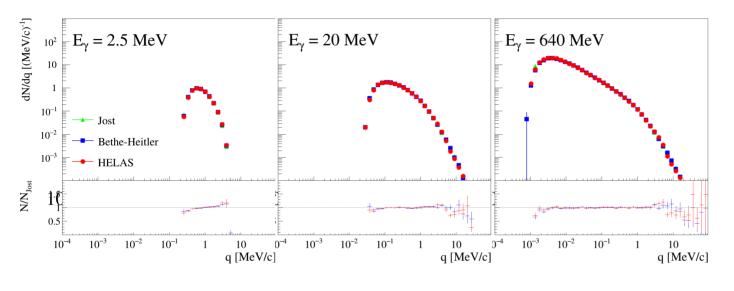


- Home made generator (D. Bernard)
- Models of 5D cross-section:
 - full Feynman diagram calculation with HELAS
 - Bethe-Heitler formula
- P.d.f. generation with SPRING/BASE

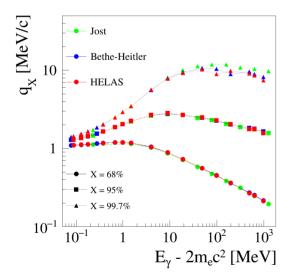


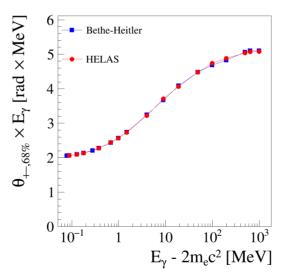
Cross-Validation

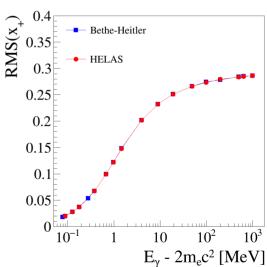




q distributions compared to analytic formula by Jost



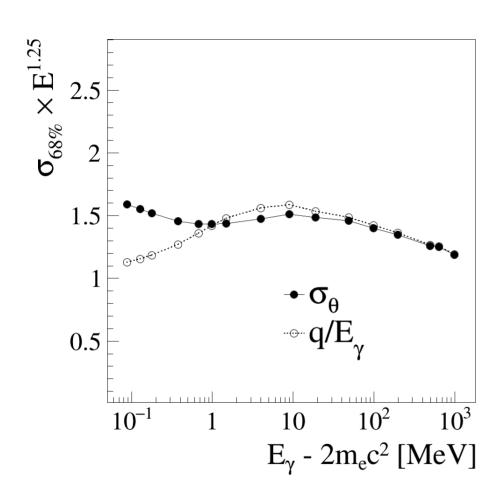






Remark: Angular resolution vs q





- High energy approximation
 - tranverse recoil
 - small angles

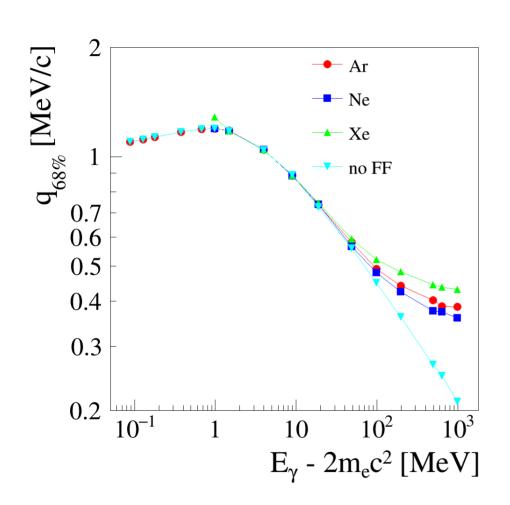
$$\theta = q/E$$

Valid within 10% above 1 MeV



Form factors





- Nature of conversion nuclei taken into account with form factors
- Negligible at low E
- Clear above 100 MeV



Available generators



- EGS5 (v1.0.6)
 - IPRDST=0 $\theta_{+} = \theta_{-} = m/E$
 - IPRDST=2
 θ₊,θ₋ independent
 (Schiff)

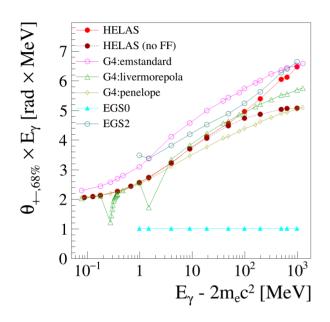
 no conservation of energy-momentum

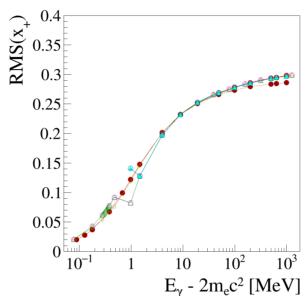
- Geant4 (v10.02.01)
 - emstandard G4BetheHeitler coplanar $(\phi_- \phi_+ = \pi)$
 - penelope G4PenelopeGammaConversion $\theta_{+,}\theta_{-}$ independent (no conservation of E-p)
 - livermorepola
 G4LivermorePolarizedGammaConversion
 high energy approximation
 from Depaola, polarised

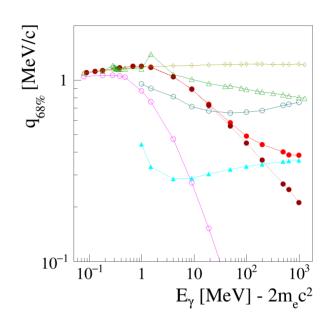


Comparison







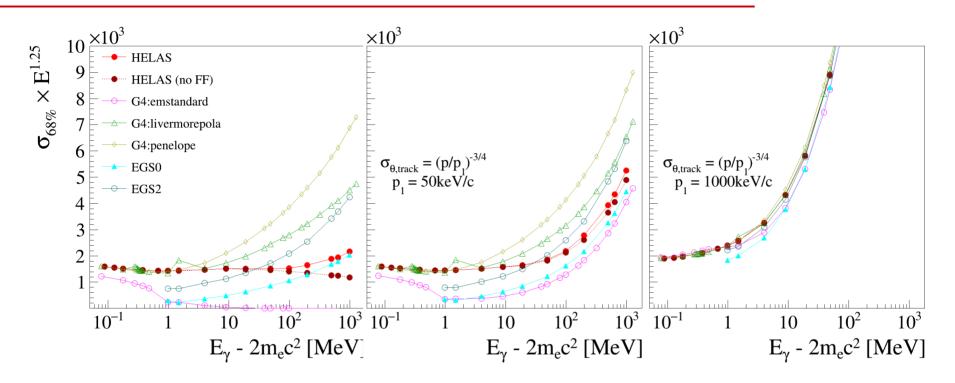


- The distribution vary between models
 - especially *q*, and therefore the angular resolution
 - EGSO and emstandard are most inaccurate, as expected
 - regime changes around 200keV and 1MeV for livermorepola



Angular resolution



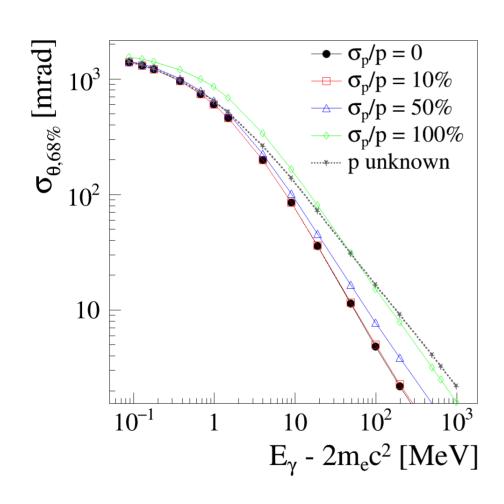


- Tracking resolution from multiple scattering
 - approximation of homogeneous tracker $\sigma = (p/p_1)^{-3/4}$
 - model differences disappear for p_1 =1MeV (~Fermi-LAT)
 - accurate models necessary for high resolution (e.g. gaseous tracker)



Momentum resolution



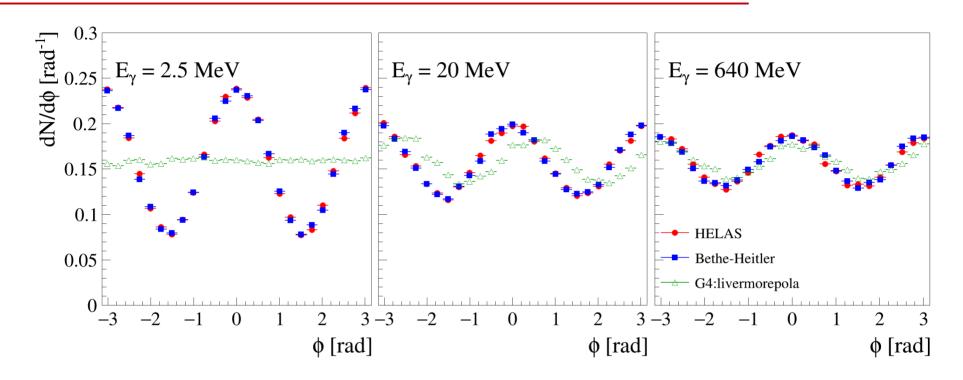


- Track momentum used in estimation of photon direction
- Bisector gives worse resolution at high energy (factor 3 at 100MeV)
- Rough momentum estimation (<50%) recovers most of it



Polarimetry



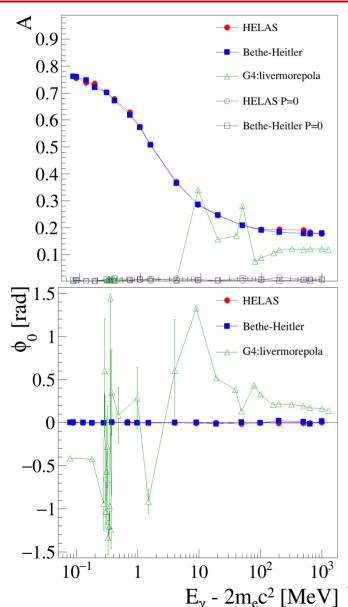


- Azimuthal angle distributions
 - Apparently consistent at high energy
 - No asymmetry in *livermorepola* at low energy



Polarimetry





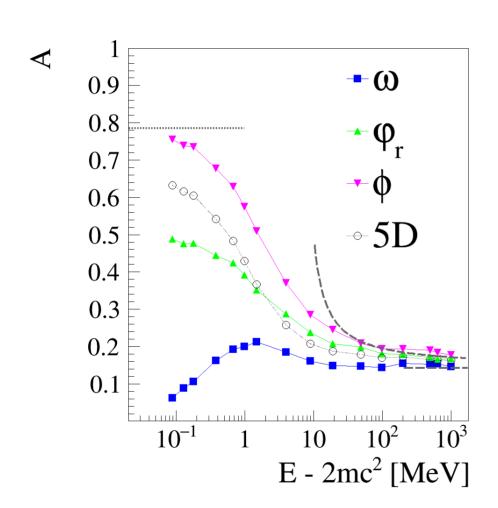
$dN/d\phi \propto 1 + A\cos(2(\phi - \phi_0))$

- Asymmetry A is underestimated in livermorepola, especially below 50MeV (regime change)
- Phase ϕ_0 varies below 50MeV; strange offset above



Remark on Azimuthal angle





- Azimuthal angle ill defined
 - recoil angle ϕ_r
 - pair plane angle ω
 - pair bisector ϕ
- Angle ω used in previous publications underestimates A at low energy
- ϕ appears in Bethe-Heitler formula, agrees with asymptotic values



Conclusion



- Exact 5D generator fully validated
- Detailed kinematics of pair conversion poorly described by available generators
- Important for new generation telescopes with fine resolution/low multiple scattering (gas, Si only or emulsions)
- Polarisation rarely taken into account
 - only Geant4, but poorly described < 50MeV

Be careful which generator you use!



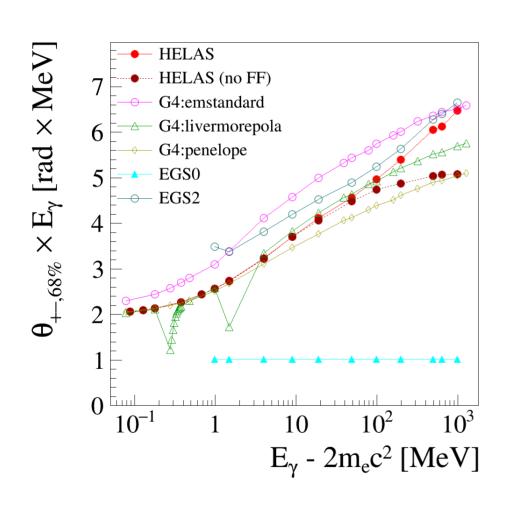


Backup



Comparison θ_{+}



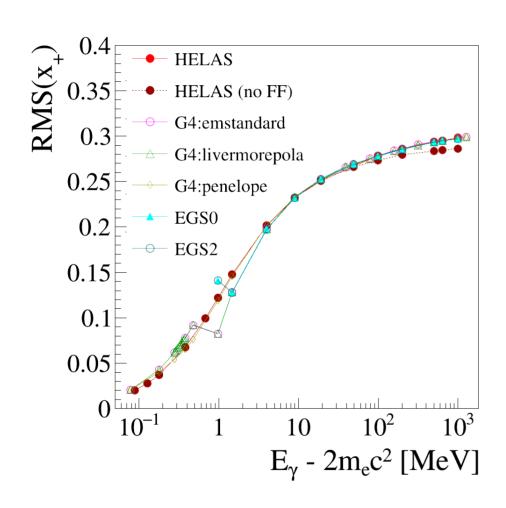


- EGS0 with fixed value $\theta_+ E = 2m$
- Other models qualitatively similar
- 2 regime changes in *livermorepola*



Comparison X_{+}



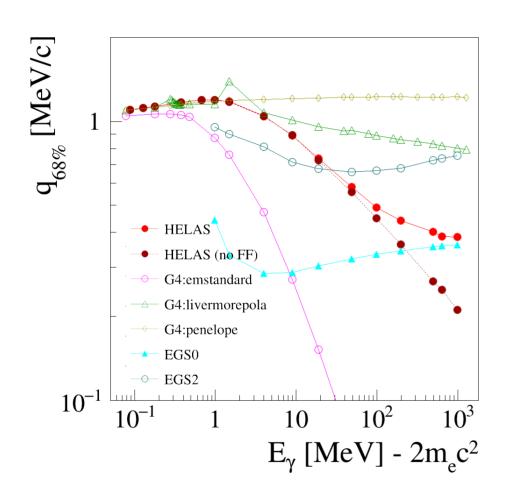


- All models consistent
- small offset around 1MeV for emstandard and livermorepola models



Comparison q





- Very different results from generators
- No FF in Geant4 and EGS5
- *EGS* (*IPRDST*=0) and *emstandard* inappropriate