



Gravitational wave astronomy

past, present and future

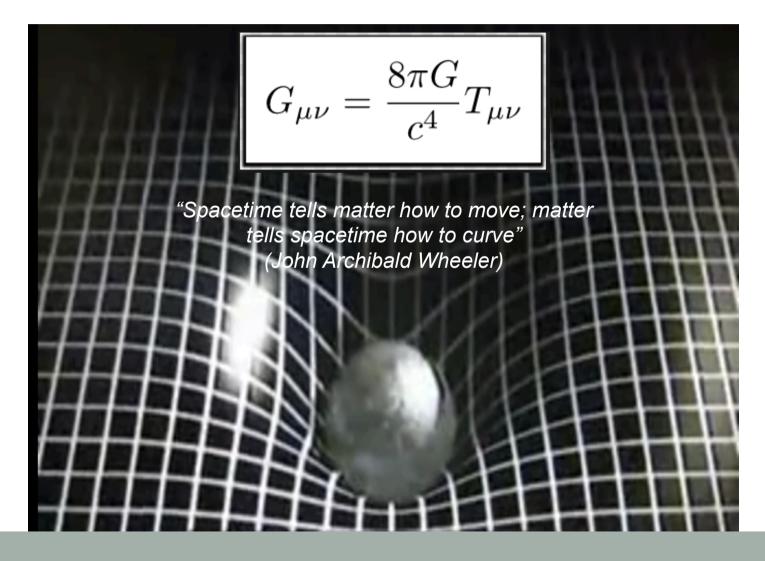
Eugenio Coccia Gran Sasso Science Institute and INFN

SciNeGHE 2016 High-energy gamma-ray experiments at the dawn of gravitational wave astronomy Pisa,18 October 2016





Gravity is a manifestation of spacetime curvature induced by mass-energy



1916

Über Gravitationswellen.

Von A. EINSTEIN.

Die wichtige Frage, wie die Ausbreitung der Gravitationsfelder erfolgt, ist schon vor anderthalb Jahren in einer Akademiearbeit von mir behandelt worden¹. Da aber meine damalige Darstellung des Gegenstandes nicht genügend durchsichtig und außerdem durch einen bedauerlichen Rechenfehler verunstaltet ist, muß ich hier nochmals auf die Angelegenheit zurückkommen.

Wie damals beschränke ich mich auch hier auf den Fall, daß las betrachtete zeiträumliche Kontinuum sich von einem •galileischen • nur sehr wenig unterscheidet. Um für alle Indizes

$$\gamma_{\mu\nu} = -\delta_{\mu\nu} + \gamma_{\mu\nu}$$

(1)

(1)

setzen zu können, wählen wir, wie es in der speziellen Relativitätstheorie üblich ist, die Zeitvariable x_4 rein imaginär, indem wir

 $x_4 = it$

setzen, wobei t die "Lichtzeit" bedeutet. In (1) ist $\delta_{\mu\nu} = 1$ bzw. $\delta_{\mu\nu} = 0$, je nachdem $\mu = \nu$ oder $\mu \pm \nu$ ist. Die $\gamma_{\mu\nu}$ sind gegen 1 kleine Größen, welche die Abweichung des Kontinuums vom feldfreien darstellen; sie bilden einen Tensor vom zweiten Range gegenüber LORENTZ-Transformationen.

§ 1. Lösung der Näherungsgleichungen des Gravitationsfeldes durch retardierte Potentiale.

Wir gehen aus von den für ein beliebiges Koordinatensystem gültigen² Feldgleichungen

$$-\sum_{\alpha} \frac{\partial}{\partial x_{\alpha}} { \binom{\mu\nu}{\alpha} } + \sum_{\alpha} \frac{\partial}{\partial x_{\nu}} { \binom{\mu\alpha}{\alpha} } + \sum_{\alpha,\beta} { \binom{\mu\alpha}{\beta} } { \binom{\nu\beta}{\beta} } - \sum_{\alpha\beta} { \binom{\mu\nu}{\alpha} } { \binom{\alpha\beta}{\beta} }$$

$$= -\varkappa \left(T_{a\nu} - \frac{1}{2} g_{a\nu} T \right) \cdot$$

$$(2)$$

¹ Diese Sitzungsber. 1916, S. 688 ff.

² Von der Einführung des «2-Gliedes» (vgl. diese Sitzungsber. 1917, S. 142) ist dabei Abstand genommen.

Sitzungsberichte 1918.

La prima pagina di un lavoro di Albert Einstein del 1918 in cui per la prima volta vengono dedotte le equazioni della propagazione ondosa del campo gravitazionale.

Weak field approximation

$$g_{\mu\nu} = g_{\mu\nu}^{o} + h_{\mu\nu}$$
$$\left|h_{\mu\nu}\right| <<1$$

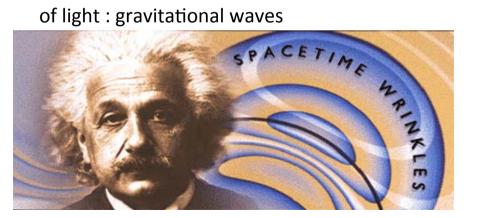
The Einstein equation in vacuum becomes

$$(\nabla^2 - \frac{1}{c^2} \frac{\partial^2}{\partial t^2})h_{\mu\nu} = 0$$

Having solutions

$$h_{\mu\nu}(t-x/c)$$

Spacetime perturbations, propagating in vacuum like waves, at the speed of light : gravitational waves



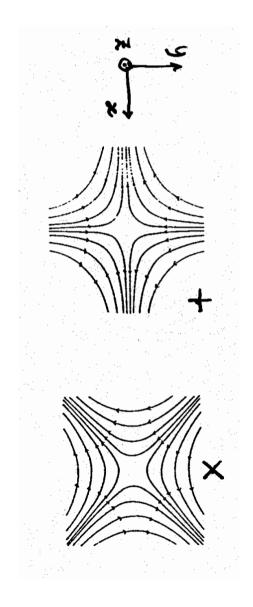
Gravitational waves are strain in space propagating with the speed of light

Main features

- 2 transversal polarization states
- Associated with massless, spin 2 particles (gravitons)
- Emitted by time-varying quadrupole mass moment no dipole radiation because of conservation laws

$$-\frac{dE}{dt} = \frac{2G}{3e^{3}} \left(\dot{d} \right)^2 + \frac{G}{45c^5} \left(\ddot{Q} \right)^2 + \dots$$
$$\dot{d} = \sum_i m_i \dot{x}_i \Rightarrow \ddot{d} = 0 \qquad Q_{ij} = \int \rho x_i x_j d^3 x_j$$

$$h_{ij}(t) = \frac{2G}{rc^4} \ddot{Q}_{ij}(t - r/c)$$



No laboratory equivalent of Hertz experiments for production of GWs

Luminosity due to a mass M and size R oscillating at frequency o~ v/R:

$$L = \frac{2G}{5c^5} \left\langle \ddot{Q}^2 \right\rangle \approx \frac{GM^2 v^6}{R^2 c^5} \qquad Q \approx MR^2 \sin\omega t$$

M=1000 tons, steel rotor, $f = 4 \text{ Hz} \implies L = 10^{-30} \text{ W}$ Einstein: "... a pratically vanishing value..."

Collapse to neutron star 1.4 M_o \implies L = 10⁵² W

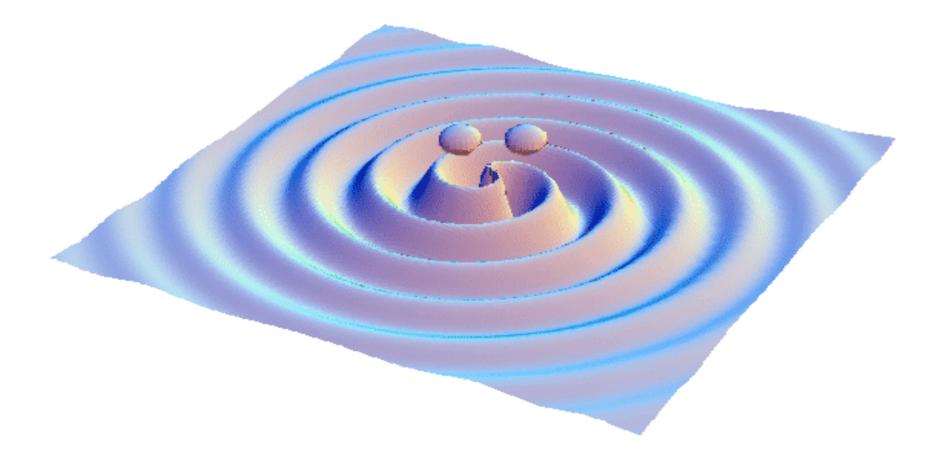
 $h \sim W^{1/2}d^{-1}$; source in the Galaxy $h \sim 10^{-18}$, in VIRGO cluster $h \sim 10^{-21}$ Fairbank: "...a challenge for contemporary experimental physics.."

$$A = \frac{\varkappa}{24\pi} \sum_{\alpha\beta} \left(\frac{\partial^3 J_{\alpha\beta}}{\partial t^3} \right)^2$$
(21)

Würde man die Zeit in Sekunden, die Energie in Erg messen, so würde zu diesem Ausdruck der Zahlenfaktor $\frac{1}{c^4}$ hinzutreten. Berücksichtigt man außerdem, daß $\varkappa = 1.87 \cdot 10^{-27}$, so sieht man, daß A in allen nur denkbaren Fällen einen praktisch verschwindenden Wert haben muß.

> ".....in any case one can think of A will have a practically vanishing value."

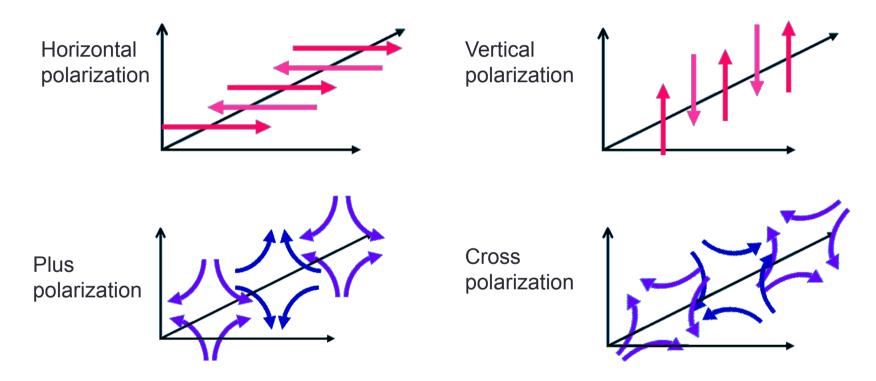
Gravitational Waves



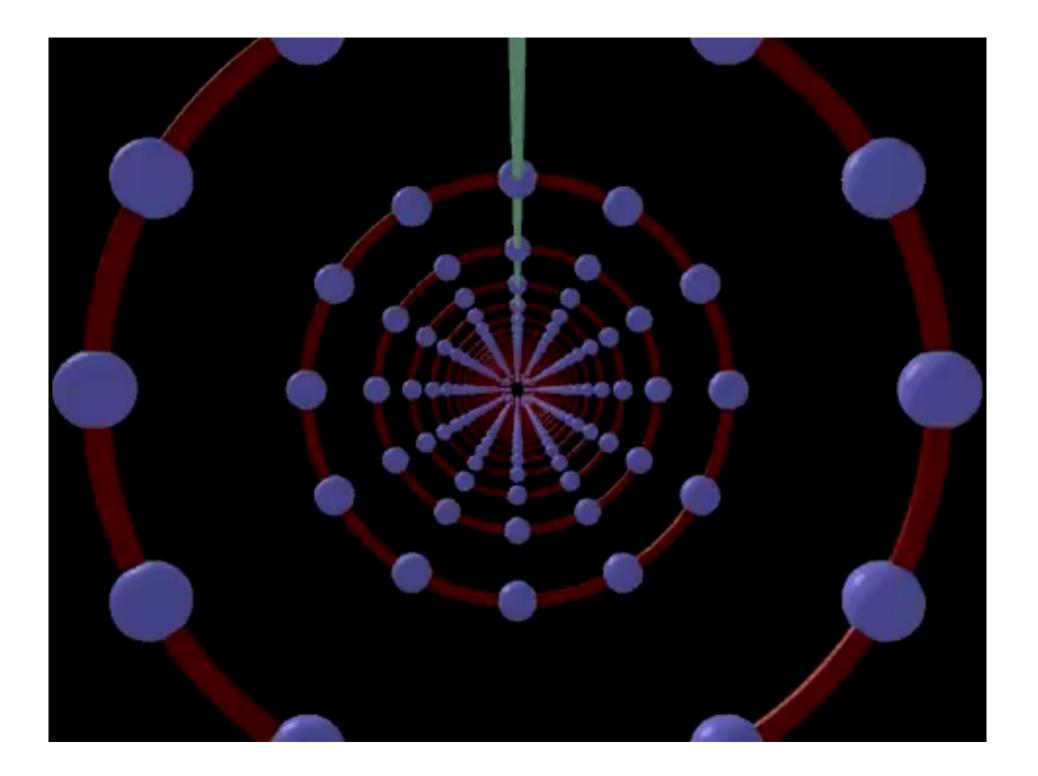


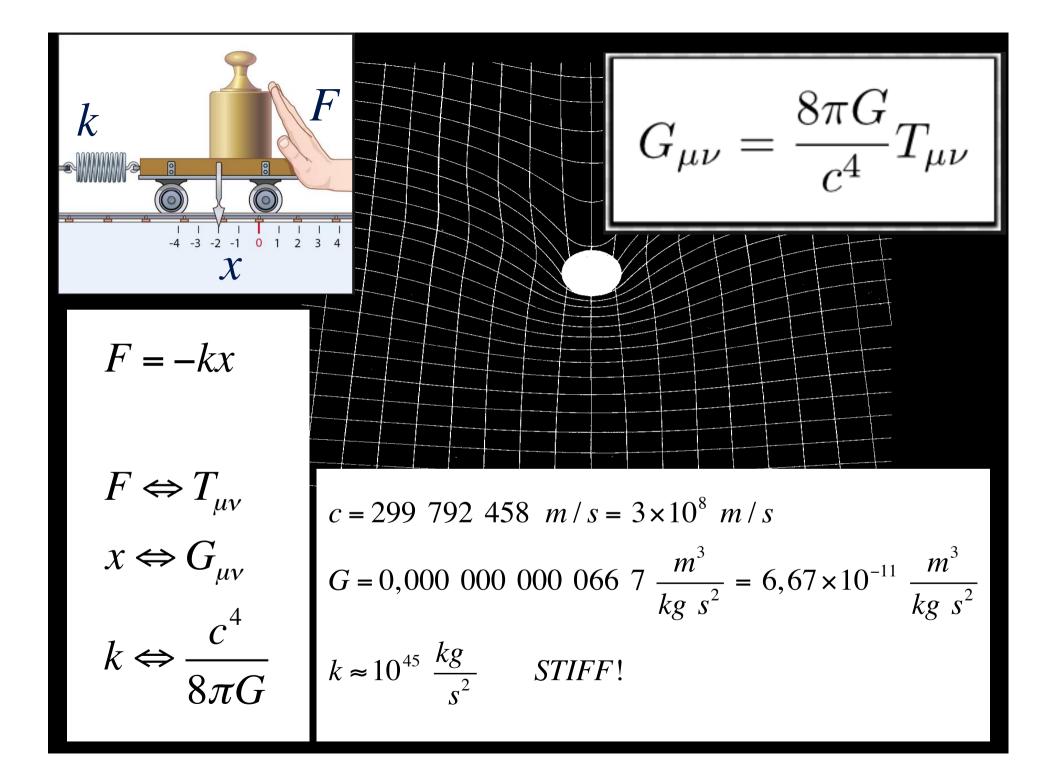


Comparison with electromagnetic waves



The so-called "electromagnetic theory of light" has not helped us hitherto . . it seems to me that it is rather a backward step . . . the one thing about it that seems intelligible to me, I do not think is admissible . . That there should be an electric displacement perpendicular to the line of propagation' Lord Kelvin





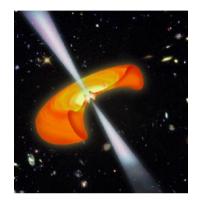
GW OBJECTIVES

FIRST DETECTION test Einstein prediction

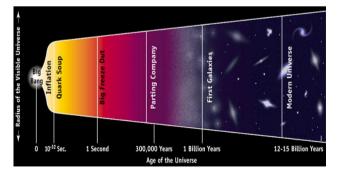
$$\mathbf{G} = \frac{8\pi G}{c^4} \mathbf{T}$$

ASTRONOMY & ASTROPHYSICS

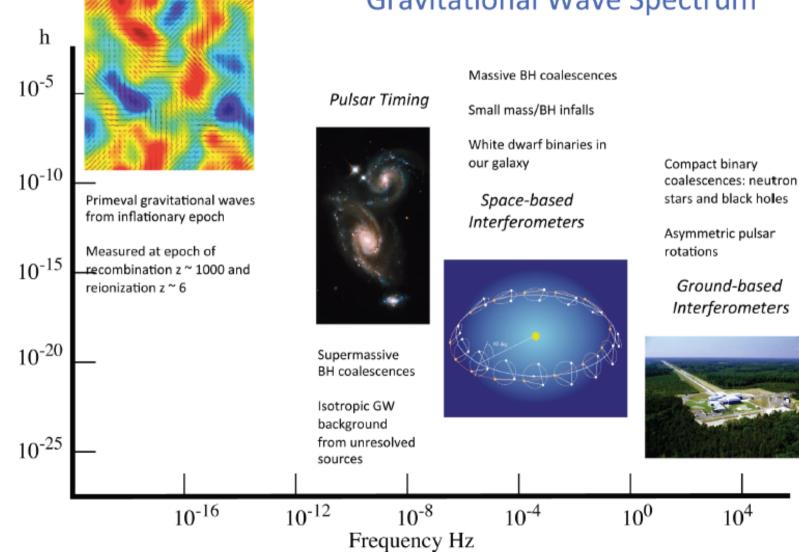
look beyond the visible, understand Black Holes, Neutron Stars and supernovae understand GRB



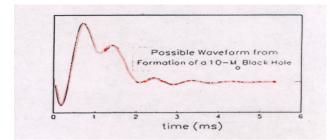
COSMOLOGY the Planck time: look as back in time as theorist can conceive



Cosmic Microwave Background Polarization B Modes



Gravitational Wave Spectrum

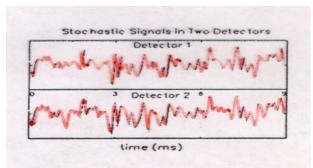


SUPERNOVAE.

If the collapse core is non-symmetrical, the event can give off considerable radiation in a millisecond timescale.

Pulsor Waveform 0.00 0.05 0.10 0.15 0.20 0.25 time (s)

Chirp Waveform from Two 10-M_Black Holes



SPINNING NEUTRON STARS.

Pulsars are rapidly spinning neutron stars. If they have an irregular shape, they give off a signal at constant frequency (prec./Dpl.)

COALESCING BINARIES.

Two compact objects (NS or BH) spiraling together from a binary orbit give a chirp signal, whose shape identifies the masses and the distance

STOCHASTIC BACKGROUND.

Random background, relic of the early universe and depending on unknown particle physics. It will look like noise in any one detector, but two detectors will be correlated.

Information

Inner detailed dynamics of supernova See NS and BH being formed Nuclear physics at high density

Information

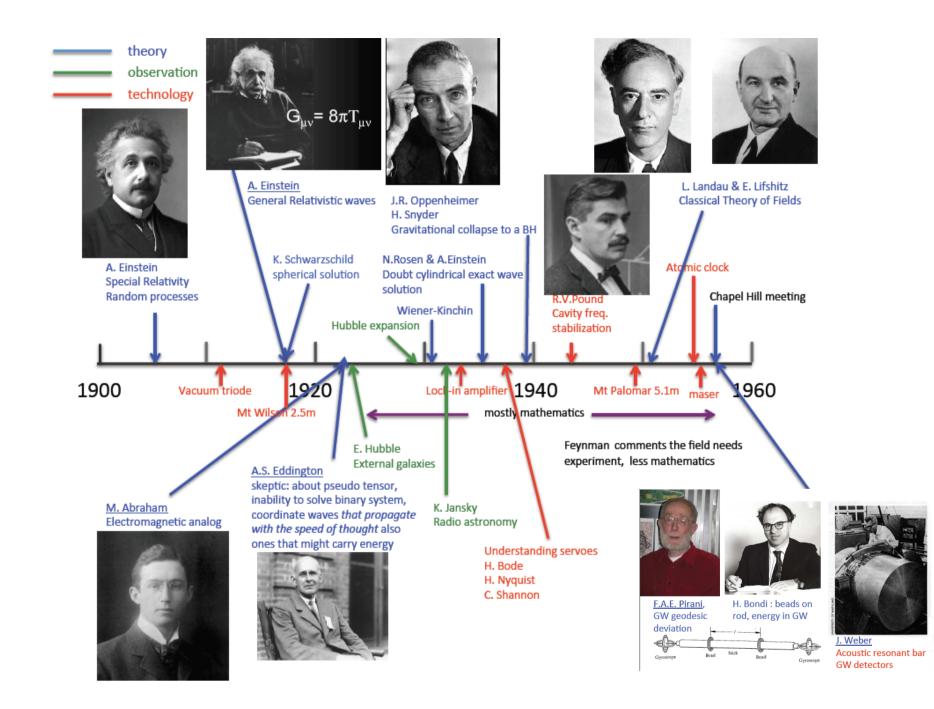
Neutron star locations near the Earth Neutron star Physics Pulsar evolution

Information

Masses of the objects BH identification Distance to the system Hubble constant Test of strong-field general relativity

Information

Confirmation of Big Bang, and inflation Unique probe to the Planck epoch Existence of cosmic strings



Chapter 14 Measurement of Classical Gravitation Fields Felix Pirani

Because of the principle of equivalence, one cannot ascribe a direct physical interpretation to the gravitational field insofar as it is characterized by Christoffel symbols $\Gamma^{\mu}_{\nu\rho}$. One can, however, give an invariant interpretation to the variations of the gravitational field. These variations are described by the Riemann tensor; therefore, measurements of the relative acceleration of neighboring free particles, which yield information about the variation of the field, will also yield information about the Riemann tensor.

Now the relative motion of free particles is given by the equation of geodesic deviation

$$\frac{\partial^2 \eta^{\mu}}{\partial \tau^2} + R^{\mu}_{\nu\rho\sigma} v^{\nu} \eta^{\rho} v^{\sigma} = 0 \quad (\mu, \nu, \rho, \sigma = 1, 2, 3, 4)$$
(14.1)

Here η^{μ} is the infinitesimal orthogonal displacement from the (geodesic) worldline ζ of a free particle to that of a neighboring similar particle. v^{ν} is the 4-velocity of the first particle, and τ the proper time along ζ . If now one introduces an orthonormal frame on ζ , v^{μ} being the timelike vector of the frame, and assumes that the frame is parallelly propagated along ζ (which insures that an observer using this frame will see things in as Newtonian a way as possible) then the equation of geodesic deviation (14.1) becomes

$$\frac{\partial^2 \eta^a}{\partial \tau^2} + R^a_{0b0} \eta^b = 0 \quad (a, b = 1, 2, 3,)$$
(14.2)

Here η^a are the physical components of the infinitesimal displacement and R^a_{0b0} some of the physical components of the Riemann tensor, referred to the orthonormal frame.

By measurements of the relative accelerations of several different pairs of particles, one may obtain full details about the Riemann tensor. One can thus very easily imagine an experiment for measuring the physical components of the Riemann tensor.

Now the Newtonian equation corresponding to (14.2) is

$$\frac{\partial^2 \eta^a}{\partial \tau^2} + \frac{\partial^2 v}{\partial x^a \partial x^b} \eta^b = 0 \tag{14.3}$$

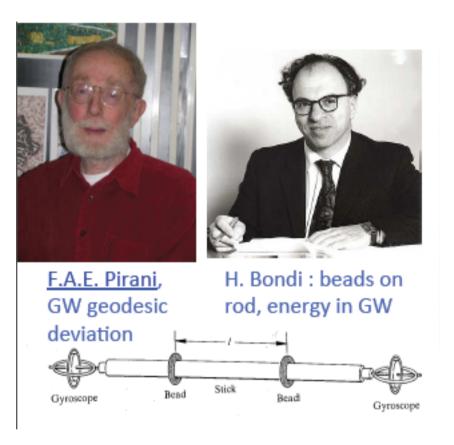
It is interesting that the empty-space field equations in the Newtonian and general relativity theories take the same form when one recognizes the correspondence $R^a_{0b0} \sim \frac{\partial^2 v}{\partial x^a \partial x^b}$ between equations (14.2) and (14.3), for the respective empty-space equations may be written $R^a_{0a0} = 0$ and $\frac{\partial^2 v}{\partial x^a \partial x^b} = 0$. (Details of this work are in the course of publication in Acta Physica Polonica.)

BONDI: Can one construct in this way an absorber for gravitational energy by inserting a $\frac{d\eta}{d\tau}$ term, to learn what part of the Riemann tensor would be the energy producing one, because it is that part that we want to isolate to study gravitational waves?

PIRANI: I have not put in an absorption term, but I have put in a "spring." You can invent a system with such a term quite easily.

LICHNEROWICZ: Is it possible to study stability problems for η ?

PIRANI: It is the same as the stability problem in classical mechanics, but I haven't tried to see for which kind of Riemann tensor it would blow up.



The main point of this presentation was that it is relative accelerations of neighboring free particles that are the physically meaningful (i.e.,measurable) ways to observe gravitational effects. Pirani points out the transparent connection between the equation of geodesic deviation and Newton's Second Law, as long as one identifies \mathbf{R}_{a0b0} with the second derivative of the Newtonian potential (i.e., as the tidal field.)

To make sure everyone sees how important and simple this is, he remarks, "By measurements of the relative accelerations of several different pairs of particles, one may obtain full details about the Riemann tensor. One can thus very easily imagine an experiment for measuring the physical components of the Riemann tensor".

from: P. Saulson, Gen Relativ Gravit (2011) 43:3289–3299

Joe Weber at Chapel Hill



Joe Weber, co-inventor of the maser, was a U Md professor, on sabbatical in 1956 -57 with John Wheeler at Princeton.

At the Chapel Hill conference in Jan 1957, they heard the key talk by Pirani that clarified that GW's were real, because they could (in principle) be detected.

GWs are detectable in principle

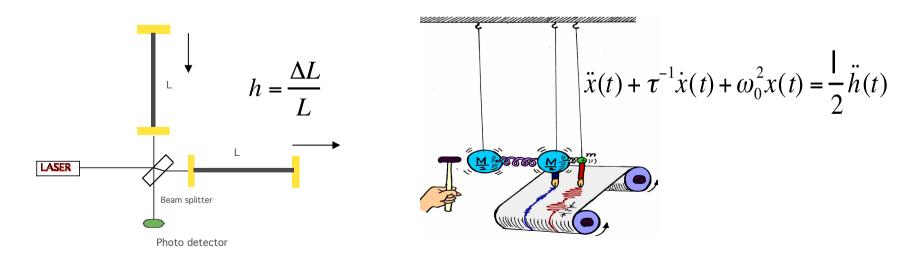
The equation for geodetic deviation is the basis for all experimental attempts to detect GWs:

$$\frac{d^2 \delta l^{j}}{dt^2} = -R_{joko} l^k = \frac{1}{2} \frac{\partial^2 h_{jk}}{\partial t^2} l^k$$

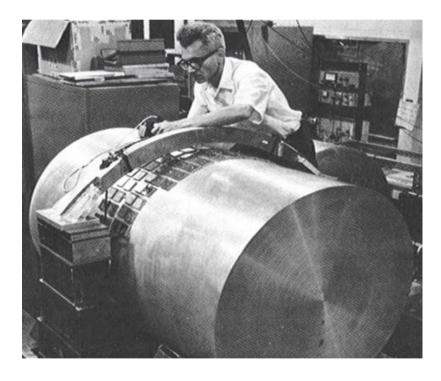
• GWs change (δI) the distance (I) between freely-moving particles in empty space.

They change the proper time taken by light to pass to and fro fixed points in space

In a system of particles linked by non gravitational (ex.: elastic) forces, GWs perform work and deposit energy in the system



Weber's bar



Weber's detector embodied Pirani's gedankenexperiment. It was a cylinder of aluminum, each end of which is like a test mass, while the center is like a spring. PZT's around the midline absorb energy to send to an electrical amplifier.

Weber invented us from scratch

It was an act of genius (and/or madness) to transform a *gendankenexperiment* into a working apparatus and an observing program.

Along the way, Weber developed:

- Sensitivity calculation and noise analysis
- Thermal noise minimization by high *Q*
- Seismic isolation
- Coincidence for background rejection
- Time slides for background estimation
- Inverse False Alarm Rate detection statistic

Weber started seeing things

In 1969, Weber made his first of many announcements that he was seeing coincident excitations of two detectors.

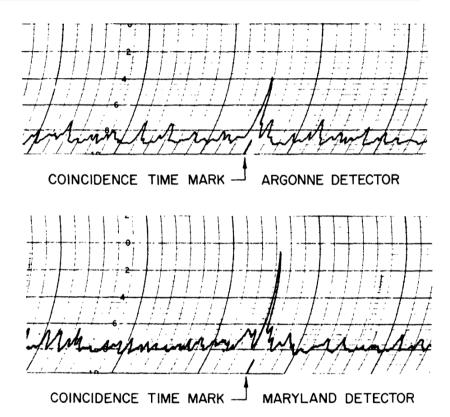


FIG. 2. Argonne National Laboratory and University of Maryland detector coincidence.

Detection Workshop, IPTA@Banff, 27 June 2014

Acoustic bar GW Detector groups







W. Fairbank



G. Pizzella, E. Amaldi

1965-1975 Room T bars

Bell Labs Frascati Glasgow IBM Rochester Max Planck Rome



A. Tyson

1975-1990+ Cryogenic bars

> Frascati Louisiana Moscow Perth Rochester Stanford



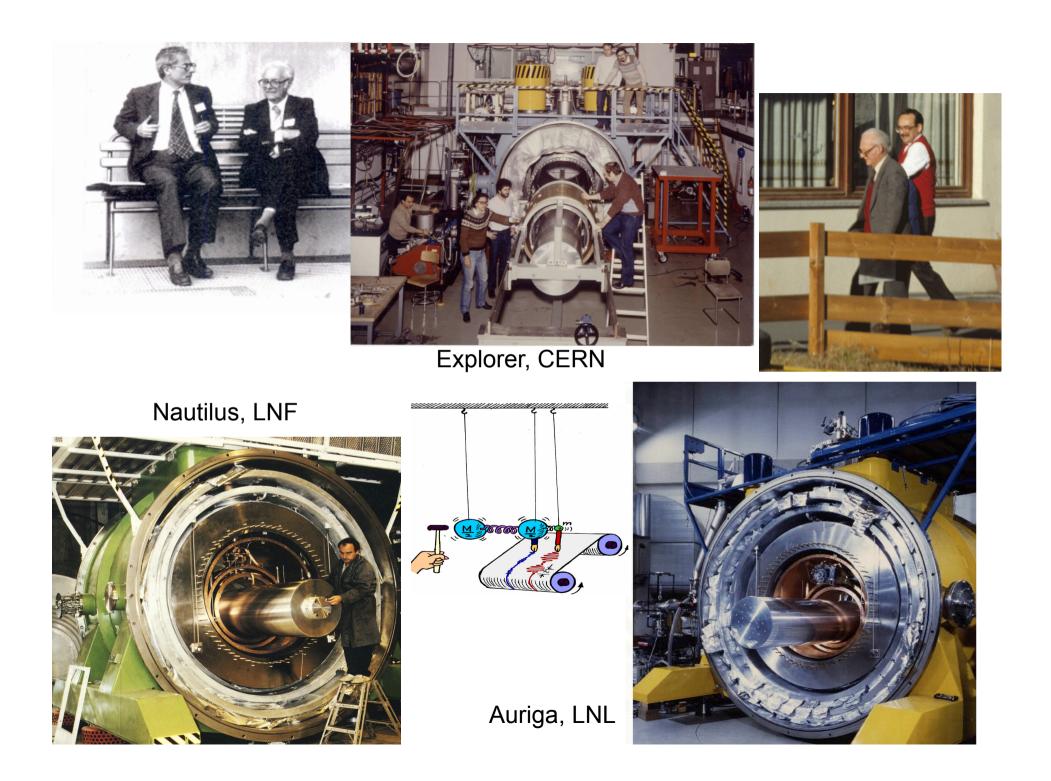
W. Hamilton

2000 -> Spherical cryogenic detectors

> Brazil Netherlands



P. Michelson



Some perspective: 50 years of attempts at detection:



60': Joe Weber pioneering work Since the pioneering work of Joseph Weber in the '60, the search for Gravitational Waves has never stopped, with an increasing effort of manpower and ingenuity:



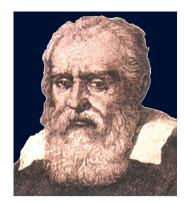
1997: GWIC was formed

GWIC thesis prize named after Stefano Braccini





2000' - : Large Interferometers



Experimental gravitational physicists are heirs to several great traditions:

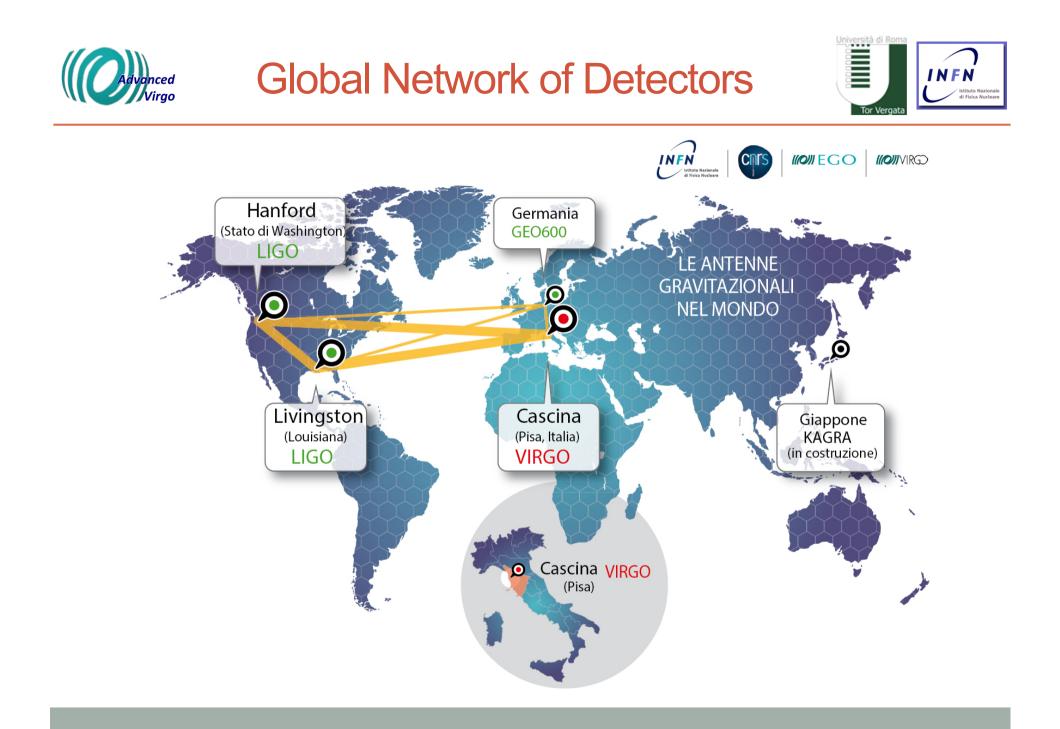
- High precision mechanical experiments (Cavendish, Eotvos, Dicke..) detection of weak forces applied on mechanical test bodies
- High precision optical measurements (Michelson, laser developers...)
- Operation of ultraprecise e-m measurement systems (microwave pioneers of World War II)
- Low temperature physics (K. Onnes) superfluids and superconductors technology

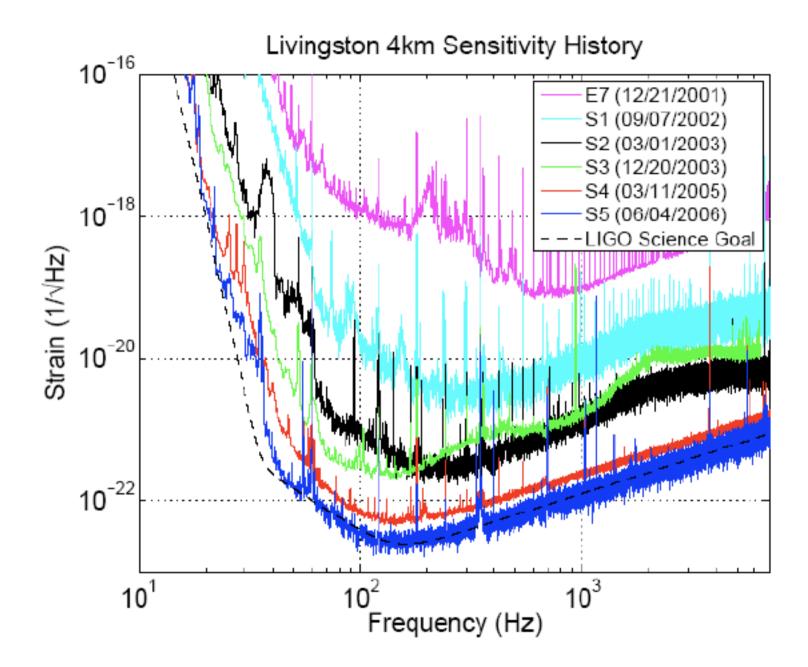


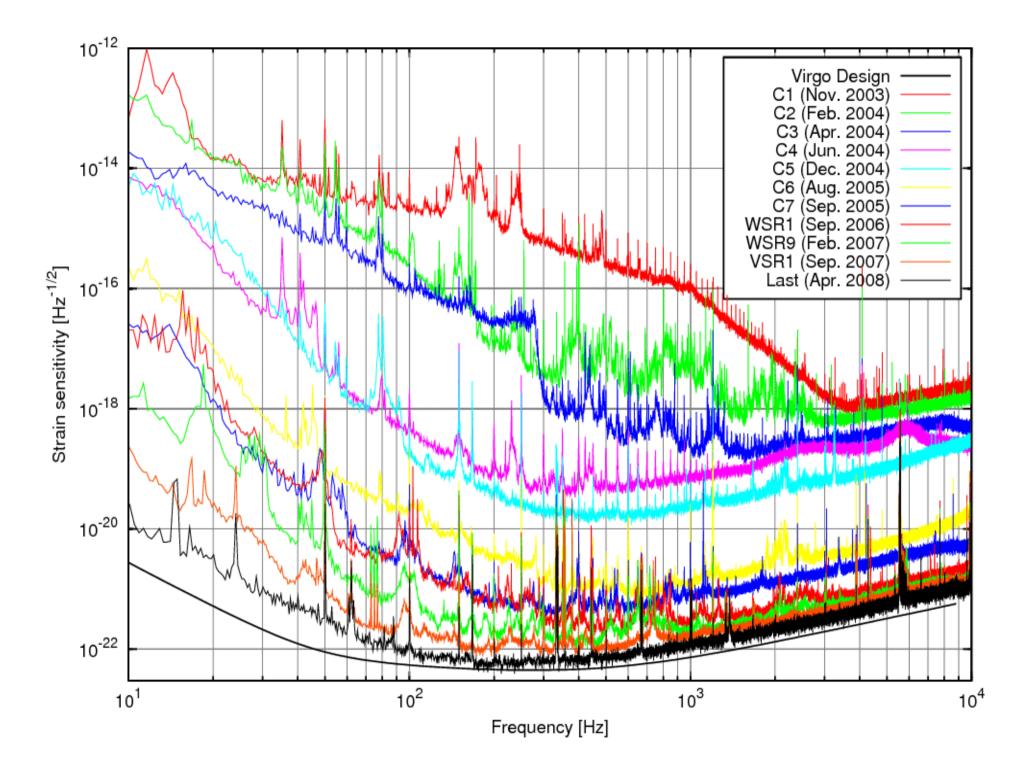


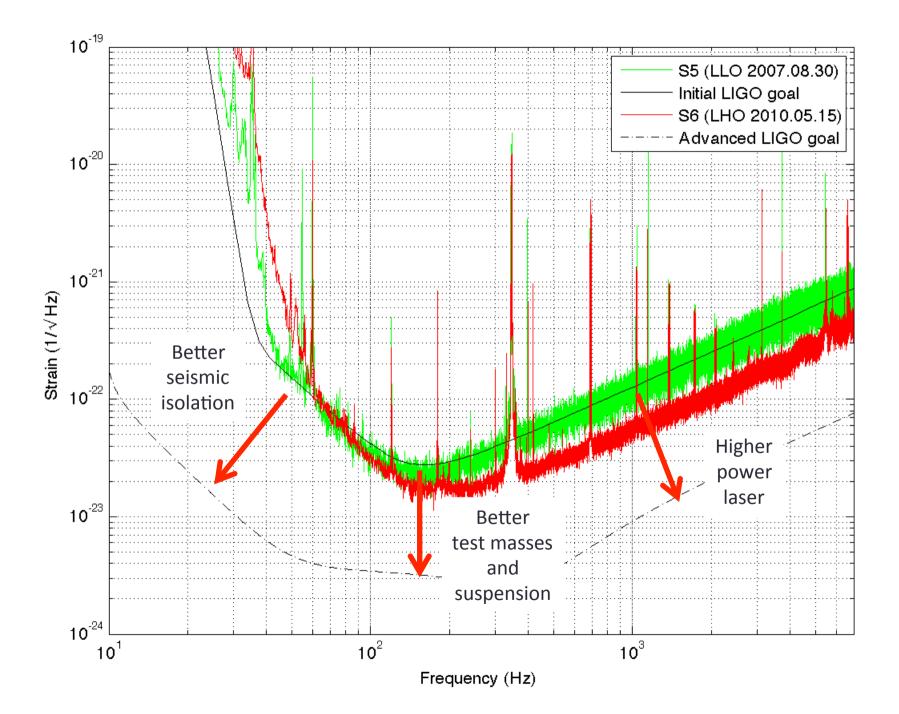


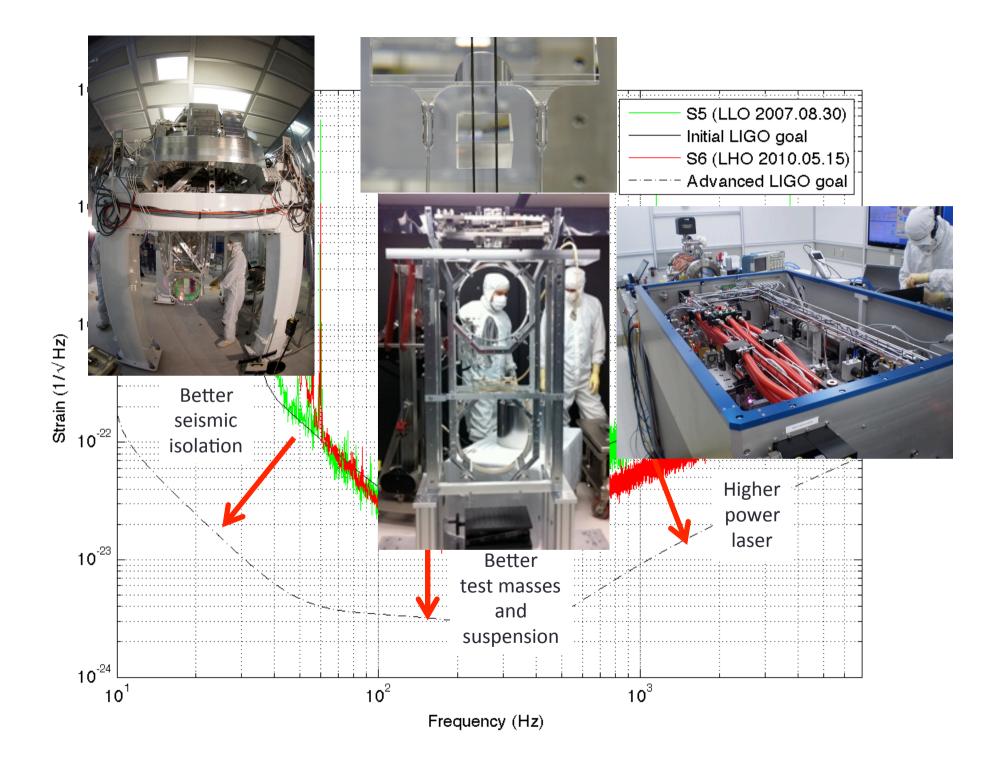


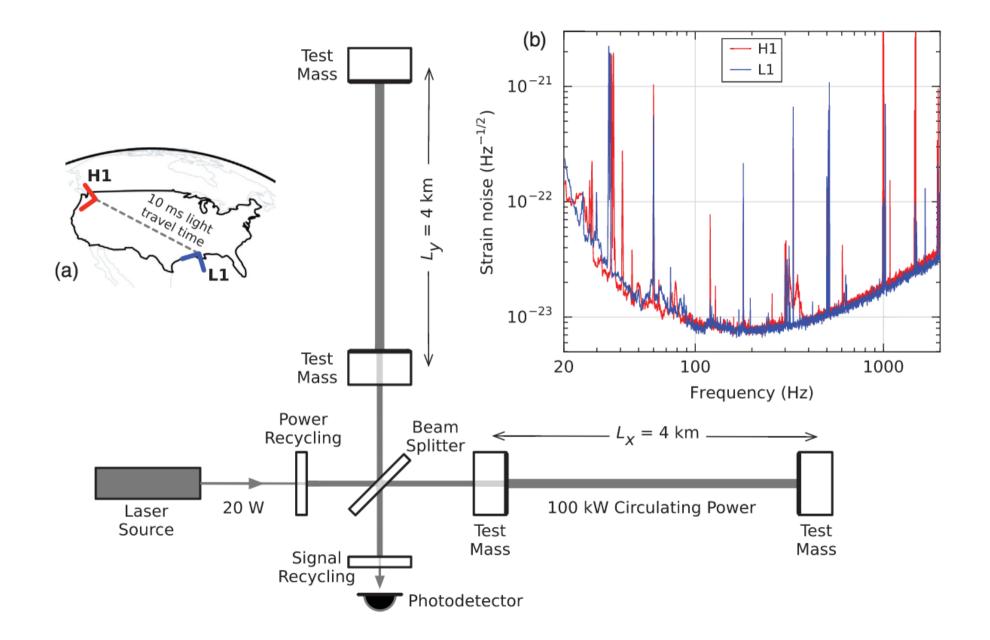








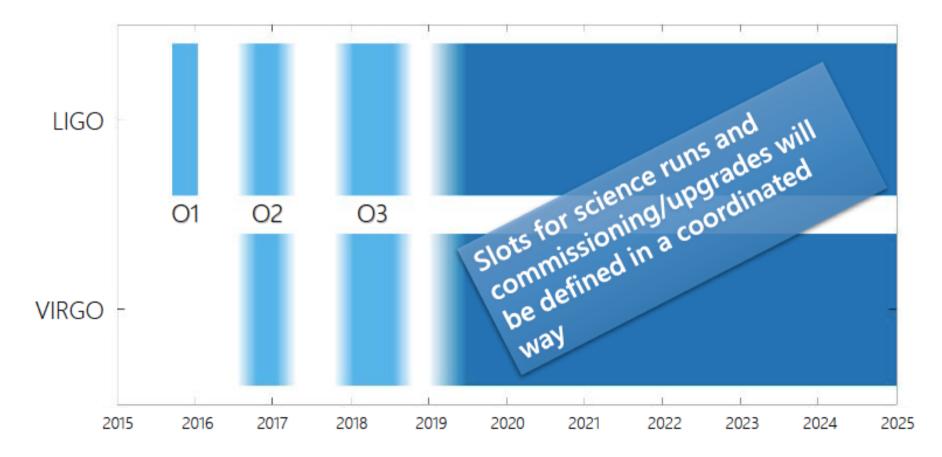






ADVANCED DETECTORS TIMELINE

foreseen at the end of 2015



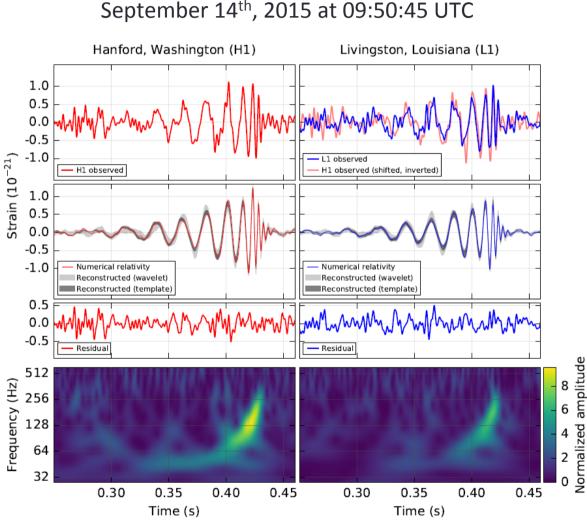
Riunione Direttori 28/04/2016

Gianluca Gemme





- Top row left Hanford
- Top row right Livingston
- Time difference ~ 6.9 ms with Livingston first
- Second row calculated • GW strain using Numerical Relativity Waveforms for quoted parameters compared to reconstructed waveforms (Shaded)
- Third Row –residuals
- Bottom row time ٠ frequency plot showing frequency increases with time (chirp)



GW150914: Estimated Strain Amplitude



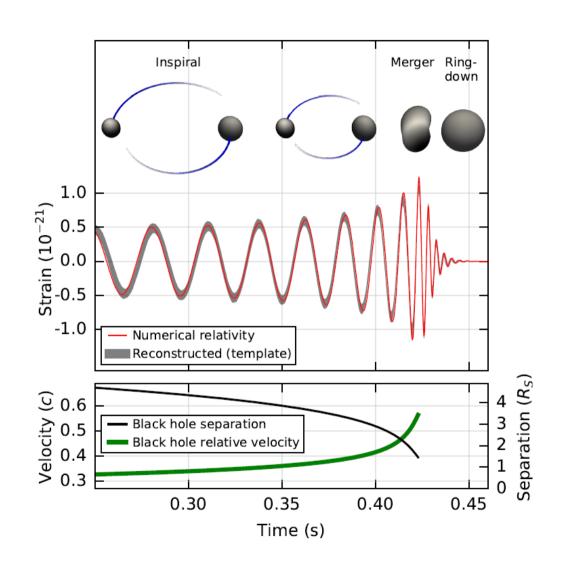
$$\mathcal{M} = \frac{(m_1 m_2)^{3/5}}{(m_1 + m_2)^{1/5}} = \frac{c^3}{G} \left[\frac{5}{96} \pi^{-8/3} f^{-11/3} \dot{f} \right]^{3/5}$$

- Numerical relativity models of black hole horizons during coalescence
- Effective black hole separation in units of Schwarzschild radius $(R_s=2GM_{tot}/c^2=210km);$ and effective relative velocities given by post-Newtonian parameter v/c = $(GM_{tot}\pi f_{GW}/c^3)^{1/3}$

Binary Black Hole System

- M1 = 36 +5/-4 M_{sol}
- M2 = 29 +/- 4 M_{sol}

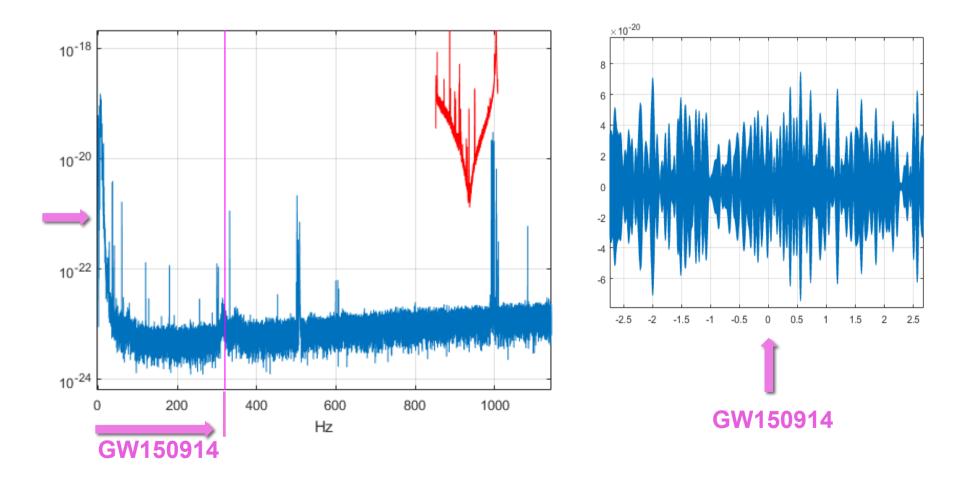
 distance=410 +160/-180 MPc (redshift z = 0.09)







Nautilus - September 14, 2015

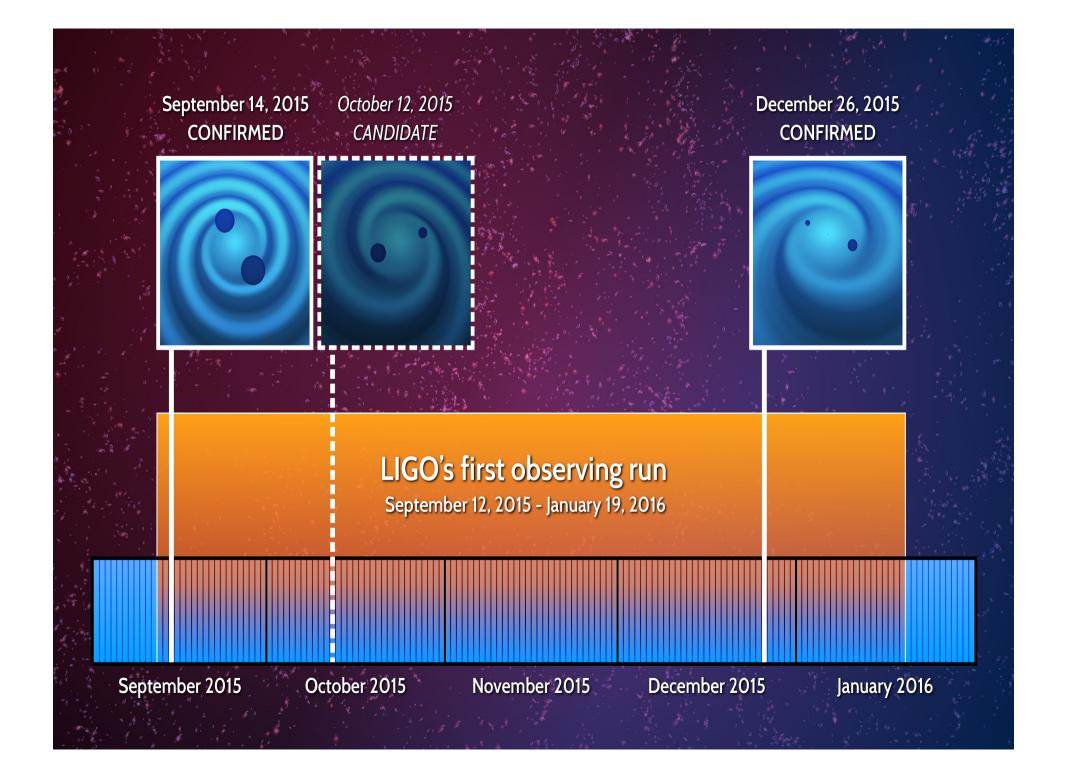


E. Coccia

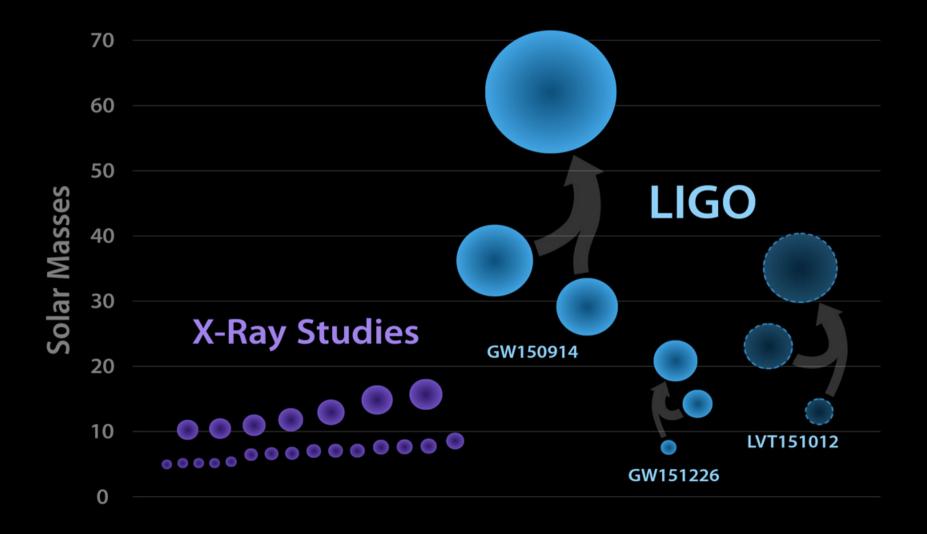


Use numerical simulations fits of black hole merger to determine parameters, we determine total energy radiated in gravitational waves is $3.0\pm0.5 \text{ M}_{\odot} \text{ c}^2$. The system reached a peak ~ 3.6×10^{56} erg, and the spin of the final black hole < 0.7

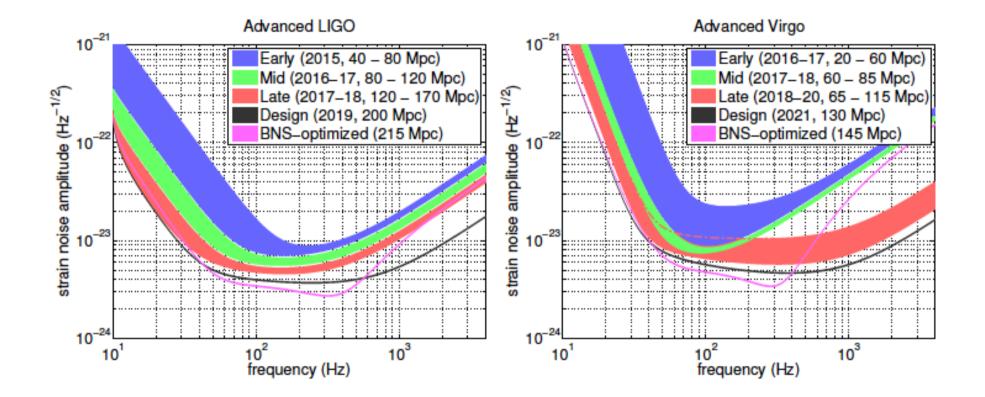
Primary black hole mass	$36^{+5}_{-4}{\rm M}_{\odot}$
Secondary black hole mass	$29^{+4}_{-4}{\rm M}_{\odot}$
Final black hole mass	$62^{+4}_{-4}{\rm M}_{\odot}$
Final black hole spin	$0.67\substack{+0.05\\-0.07}$
Luminosity distance	$410^{+160}_{-180}\mathrm{Mpc}$
Source redshift, z	$0.09^{+0.03}_{-0.04}$



Black Holes of Known Mass



Plausible scenario for the operation of the LIGO-Virgo network over the next decade



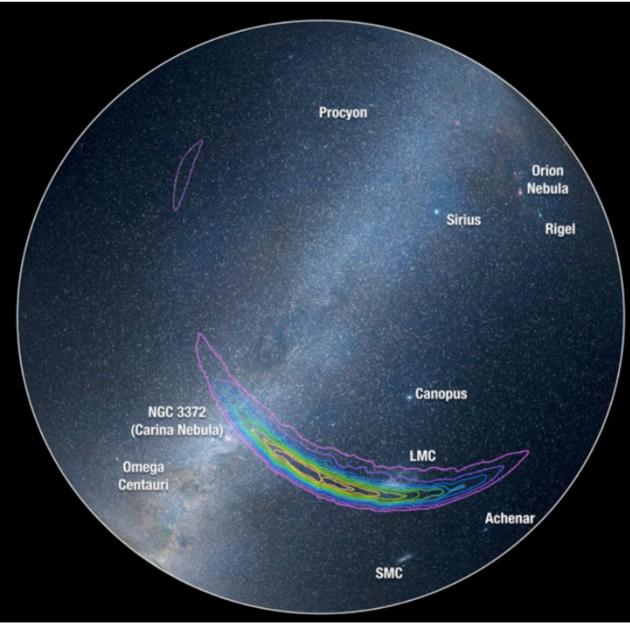
	Estimated	$E_{\rm GW} = 10^{-2} M_{\odot} c^2$			Number	% BNS Localized		
	Run	Burst Range (Mpc)		BNS Range (Mpc)		of BNS	within	
Epoch	Duration	LIGO	Virgo	LIGO	Virgo	Detections	$5 deg^2$	20deg^2
2015	3 months	40 - 60	_	40 - 80	_	0.0004 - 3	_	_
2016 - 17	6 months	60 - 75	20 - 40	80 - 120	20 - 60	0.006 - 20	2	5 - 12
2017-18	9 months	75 - 90	40 - 50	120 - 170	60 - 85	0.04 - 100	1 - 2	10 - 12
2019+	(per year)	105	40 - 80	200	65 - 130	0.2 - 200	3 - 8	8 - 28
2022 + (India)	(per year)	105	80	200	130	0.4 - 400	17	48

Gravitational-Wave Sky Posteriors

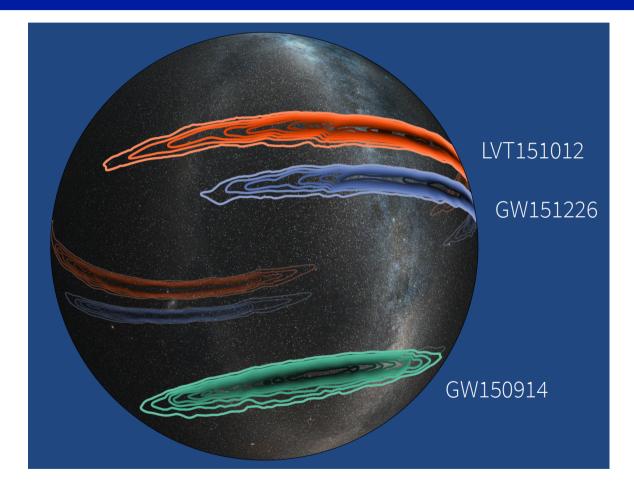
Sky areas broadly consistent with simply triangulation, and mostly crossconsistent

Triangulation ring consistent with time delay of about ~7 ms

Search area: 620 sq. degrees to cover:



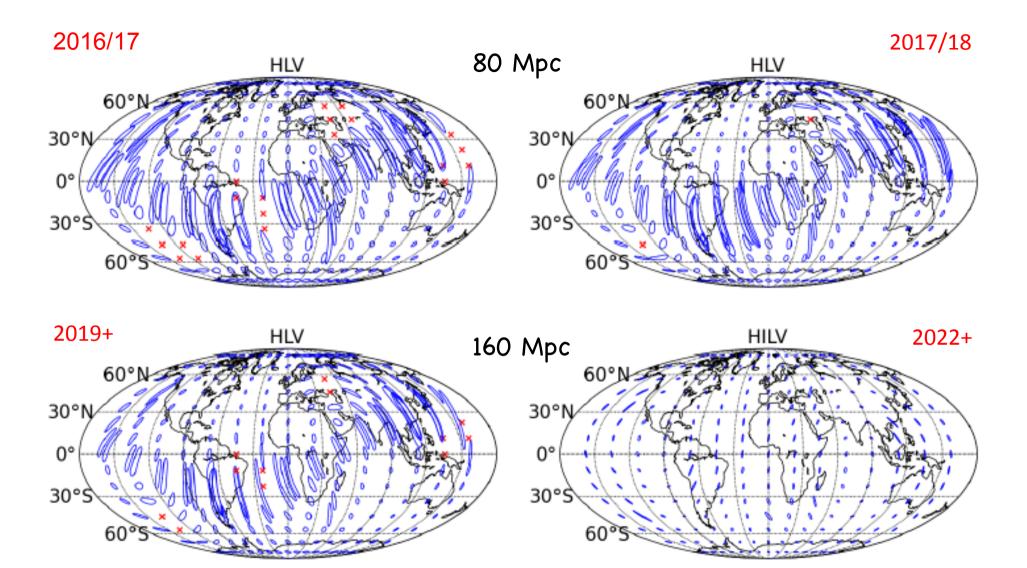
Sky Locations of Gravitational-wave Events GW150914, GW151226 and Candidate LVT151012



Università di Rom

Simulated Sky Locations of O1 Events and Candidate Including the Virgo Interferometer

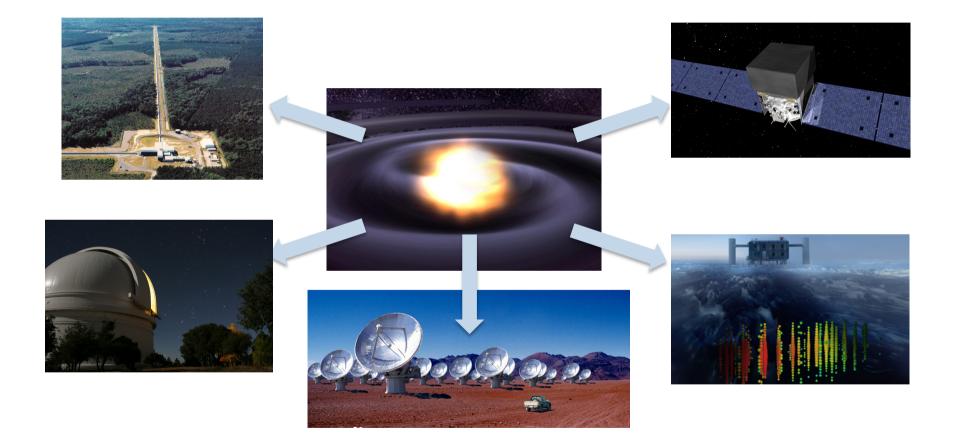


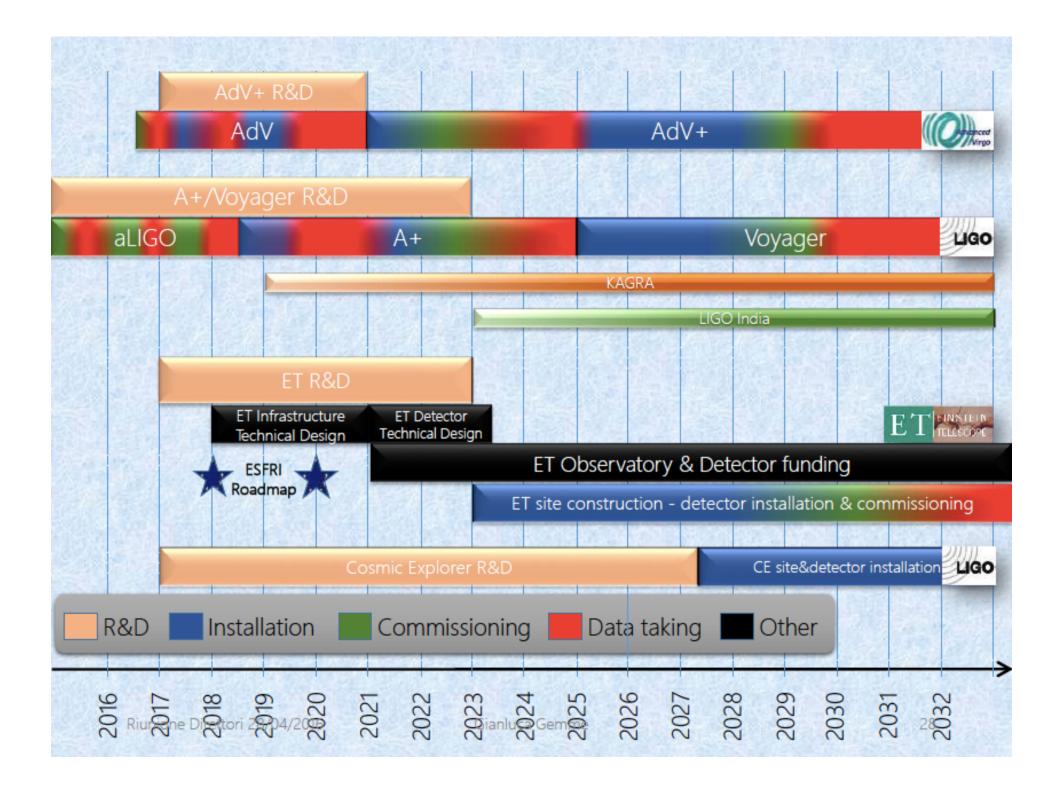


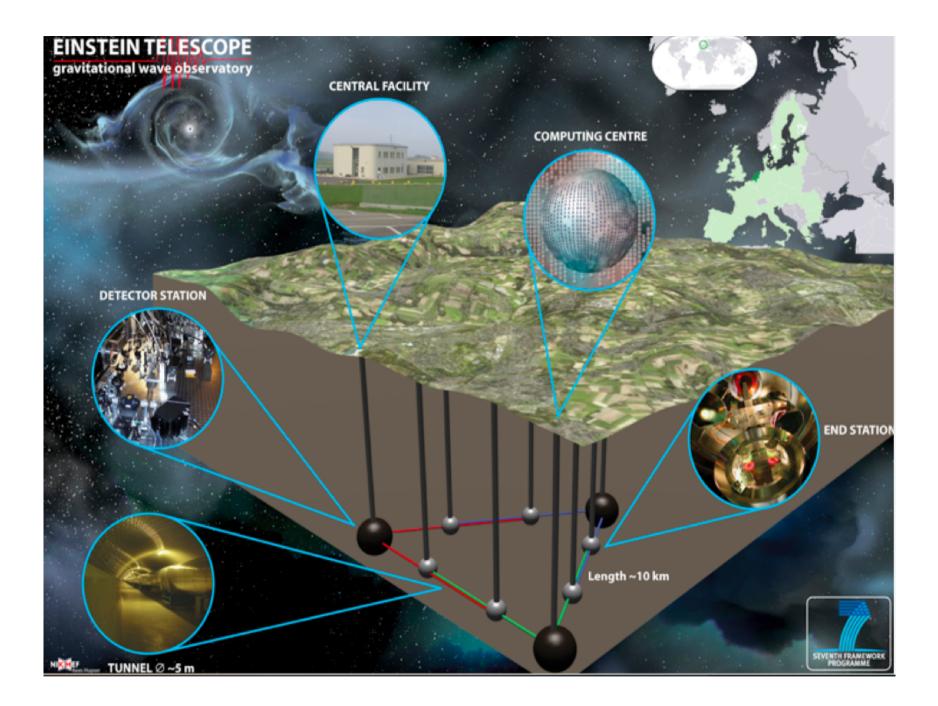
Localization expected for a BNS system

The ellipses show 90% confidence localization areas, and the red crosses show regions of the sky where the signal would not be condently detected.

Multi-Messenger Astronomy: Gravitational Wave + Electromagnetic +Neutrinos



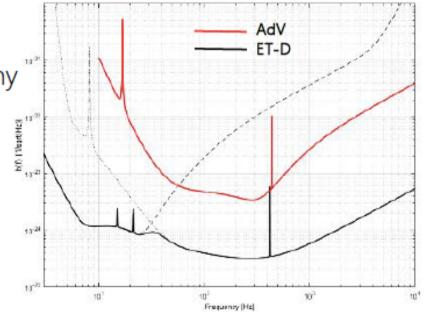


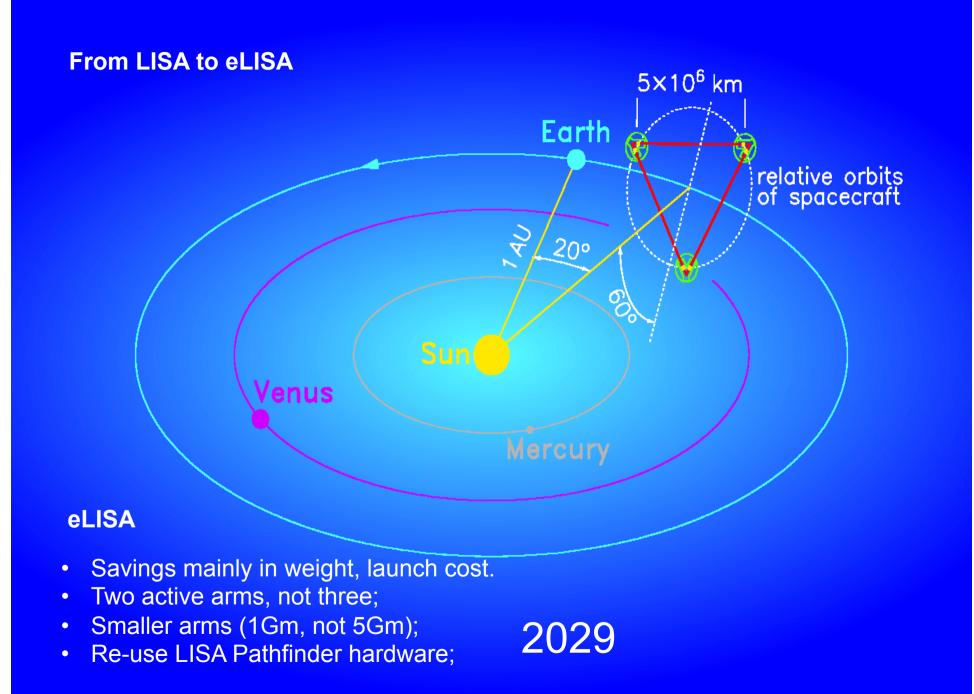




EINSTEIN TELESCOPE

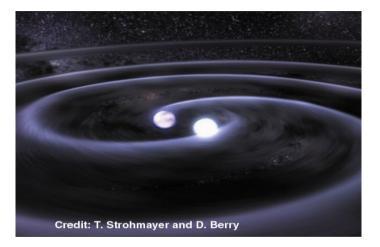
- ✓ Design study of ET funded by the European Commission under FP7
 - interest primarily focused on the Infrastructure rather than on the detector and its technologies
 - The infrastructure should no limit the sensitivity of the future hosted detectors
 - Size
 - Environmental noises (seismic and NN)
 - ET absorbed and developed many concepts in GW detectors:
 - Underground and cryo-compatible facility, pioneered in Japan by CLIO and KAGRA
 - Triangular geometry, concept used in LISA
 - Xylophone configuration

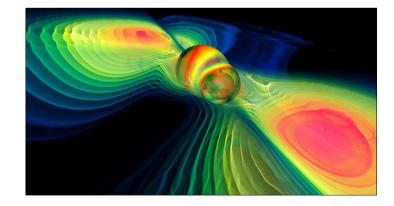




THE GLOBAL PLAN

- Advanced Detectors (LIGO, VIRGO) will initiate gravitational wave astronomy through the detection of the most luminous sources - compact binary mergers.
- Third Generation Detectors (ET and others) will expand detection horizons and provide new tools for extending knowledge of fundamental physics, cosmology and relativistic astrophysics.
- Observation of low frequency gravitational wave with eLISA will probe the role of super-massive black holes in galaxy formation and evolution





Every newly opened astronomical window has found unexpected results

Window	Opened	1 st Surprise	Year
Optical	1609 Galilei	Jupiter's moons	1610
Cosmic Rays	1912	Muon	1930s
Radio	1930s	Giant Radio Galaxies CMB Pulsars	1950s 1964 1967
X - ray	1948	Sco X-1 X-ray binaries	1962 1969 Uhuru
γ - ray	1961	GRBs	Late 1960s+ Vela
GW	2015	Binary BH mergers	2016

1610 Die 25. July: Somme more Efelds rempet in Jeach Gie Sommer Patous prinan Georgeani Fe Somiries Patous prinan George Lande Medica on enterly about on hic optim PHYSICAL Review 0.8. + + 0 prox 2 all all of the area of t ETTERS Articles published week ending 12 FEBRUARY 2016 Member Subscription Copy Library or Other Institutional Use Prohibited Until 2017 trop It post there is conucting fuit. d. 2. Secto H. 7. * 0 * * * . Hr. F. 7: Propey and as in hay off; clarift ser. D. 20. 0 ** B. 12. * 07 * * B. 12. * 6 * 0 * 6.3. H.S. * 0 + 6 * 4 + D. q. H.s. * 0 * * (0.14 * 0 * * * * media outy i 3 1.20 1/2 10 Bor attilleby! Q. 6. H.s * * 0 Dr. H. s. * * 0.00 H. T. * * * 0.0000000 orien: talig practula & Bor. oferelot? 3-25 O * * * 1. 31. 1× 1× 10 × D.T. upterno: * 0 * 3 * 8.9. H.s. * 12 * 0 ** 3. 25. 864 + + 6.0 + + 10. 4. 964. + 3. - + , 0. 0.10. H. 4. * ~ * ~ 0 + * ~ * + 1.5. × 8 × 0 8 6-13. H-3. 70. ** ** 0. Secula ~ 4. 880: 1 + 20 , stallebotur. 10. 14. H nochi . * * * 0 *. Ho.g. maining y, counce hege. Ho.g. 1/2 + + + O mering millort or 3 ~ auto Sechrane 1-15. H.S. '* * 0 * * acros conspicebout? 10.18. H.r. * 0 * 0.14. H. 3. 20. * * . . Q D.y. * 07. * 6. 19. H. 3. 20. O * * * J Legue 3. physics Published by American Physical Society[™] Volume 116, Number 6 8. 20. H. S. 2 . O * Foculty attillist b. 24. 3 - + 0 + *