



# Gravitational wave astronomy

# past, present and future

## **Eugenio Coccia** *Gran Sasso Science Institute and INFN*

SciNeGHE 2016 High-energy gamma-ray experiments at the dawn of gravitational wave astronomy Pisa,18 October 2016





Gravity is a manifestation of spacetime curvature induced by mass-energy



### **1916**

#### Über Gravitationswellen.

Von A. EINSTEIN.

Die wichtige Frage, wie die Ausbreitung der Gravitationsfelder erfolgt, ist schon vor anderthalb Jahren in einer Akademiearbeit von mir behandelt worden<sup>1</sup>. Da aber meine damalige Darstellung des Gegenstandes nicht genügend durchsichtig und außerdem durch einen bedauerlichen Rechenfehler verunstaltet ist, muß ich hier nochmals auf die Angelegenheit zurückkommen.

Wie damals beschränke ich mich auch hier auf den Fall, daß las betrachtete zeiträumliche Kontinuum sich von einem »galileischen« nur sehr wenig unterscheidet. Um für alle Indizes

$$
g_{\mu\nu} = -\delta_{\mu\nu} + \gamma_{\mu\nu}
$$

 $(1)$ 

 $(1)$ 

setzen zu können, wählen wir, wie es in der speziellen Relativitätstheorie üblich ist, die Zeitvariable x, rein imaginär, indem wir

$$
x_i = it
$$

setzen, wobei t die »Lichtzeit« bedeutet. In (1) ist  $\delta_{xx} = 1$  bzw.  $\delta_{xy} = 0$ , je nachdem  $\mu = v$  oder  $\mu \pm v$  ist. Die  $\gamma_w$  sind gegen 1 kleine Größen, welche die Abweichung des Kontinuums vom feldfreien darstellen; sie bilden einen Tensor vom zweiten Range gegenüber Lorenrz-Transformationen.

#### § 1. Lösung der Näherungsgleichungen des Gravitationsfeldes durch retardierte Potentiale.

Wir gehen aus von den für ein beliebiges Koordinatensystem gültigen<sup>2</sup> Feldgleichungen

$$
-\sum_{\alpha} \frac{\partial}{\partial x_{\alpha}} \left\{ \frac{\mu v}{\alpha} \right\} + \sum_{\alpha} \frac{\partial}{\partial x_{\alpha}} \left\{ \frac{\mu \alpha}{\alpha} \right\} + \sum_{\alpha, \beta} \left\{ \frac{\mu \alpha}{\beta} \right\} \left\{ \frac{v \beta}{\alpha} \right\} - \sum_{\alpha, \beta} \left\{ \frac{\mu v}{\alpha} \right\} \left\{ \frac{\alpha \beta}{\beta} \right\}
$$

$$
= -\kappa \left( T_{\alpha} - \frac{1}{2} g_{\alpha} T \right).
$$

<sup>1</sup> Diese Sitzungsber. 1916, S. 688 ff.

<sup>2</sup> Von der Einführung des »2-Gliedes« (vgl. diese Sitzungsber. 1917, S. 142) ist dabei Abstand genommen.

Sitzungsberichte 1918.

La prima pagina di un lavoro di Albert Einstein del 1918 in cui per la prima volta vengono dedotte le equazioni della propagazione ondosa del campo gravitazionale.

Weak field approximation

$$
g_{\mu\nu} = g_{\mu\nu}^o + h_{\mu\nu}
$$

$$
h_{\mu\nu} < 1
$$

The Einstein equation in vacuum becomes

$$
(\nabla^2 - \frac{1}{c^2} \frac{\partial^2}{\partial t^2}) h_{\mu\nu} = 0
$$

Having solutions

$$
h_{\mu\nu}(t-x/c)
$$

Spacetime perturbations, propagating of light : gravitational waves



### *Gravitational waves are strain in space propagating with the speed of light*

## **Main features**

- • **2 transversal polarization states**
- • **Associated with massless, spin 2 particles (gravitons)**
- • **Emitted by time-varying quadrupole mass moment** *no dipole radiation because of conservation laws*

$$
-\frac{dE}{dt} = \frac{2G}{3e^3} \left(\frac{7}{d}\right)^2 + \frac{G}{45c^5} \left(\frac{7}{d}\right)^2 + \dots
$$

$$
\dot{d} = \sum_i m_i \dot{x}_i \Rightarrow \ddot{d} = 0 \qquad Q_{ij} = \int \rho x_i x_j d^3x
$$

$$
h_{ij}(t) = \frac{2G}{rc^4}\ddot{Q}_{ij}(t-r/c)
$$



. No laboratory equivalent of Hertz experiments for production of GWs

Luminosity due to a mass M and size R oscillating at frequency  $\omega \sim v/R$ :

$$
L = \frac{2G}{5c^5} \langle \ddot{Q}^2 \rangle \approx \frac{GM^2v^6}{R^2c^5} \qquad Q \approx MR^2 \text{sin}\omega t
$$

M=1000 tons, steel rotor,  $f = 4$  Hz  $\implies L = 10^{-30}$  W Einstein: " .. a pratically vanishing value..."

Collapse to neutron star 1.4 M<sub>o</sub>  $\longrightarrow$  L = 10<sup>52</sup> W

 $h \sim W^{1/2} d^{-1}$ ; source in the Galaxy  $h \sim 10^{-18}$ , in VIRGO cluster  $h \sim 10^{-21}$ Fairbank: "...a challenge for contemporary experimental physics.."

$$
A = \frac{\kappa}{24\pi} \sum_{\alpha\beta} \left( \frac{\partial^3 J_{\alpha\beta}}{\partial t^3} \right)^2.
$$
 (21)

Würde man die Zeit in Sekunden, die Energie in Erg messen, so würde zu diesem Ausdruck der Zahlenfaktor  $\frac{1}{c^4}$  hinzutreten. Berücksichtigt man außerdem, daß  $x = 1.87 \cdot 10^{-27}$ , so sieht man, daß A in allen nur denkbaren Fällen einen praktisch verschwindenden Wert haben muß.

> ".....in any case one can think of A will have a practically vanishing value."

# Gravitational Waves







## Comparison with electromagnetic waves



The so-called "electromagnetic theory of light" has not helped us hitherto . . it seems to me that it is rather a backward step . . . the one thing about it that seems intelligible to me, I do not think is admissible . . That there should be an electric displacement perpendicular to the line of propagation' **Lord Kelvin** 





# GW OBJECTIVES

### **FIRST DETECTION**  test Einstein prediction

$$
G = \frac{8\pi G}{c^4}T
$$

### **ASTRONOMY & ASTROPHYSICS**

look beyond the visible, understand Black Holes, Neutron Stars and supernovae understand GRB



**COSMOLOGY**  the Planck time: look as back in time as theorist can conceive



#### Cosmic Microwave Background **Polarization B Modes**



## **Gravitational Wave Spectrum**



### SUPERNOVAE.

 If the collapse core is non-symmetrical, the event can give off considerable radiation in a millisecond timescale.

# Pulsar Waveform  $time(e)$

### SPINNING NEUTRON STARS.

Pulsars are rapidly spinning neutron stars. If they have an irregular shape, they give off a signal at constant frequency (prec./Dpl.)

## Chirp Waveform from Two 10-M Black Holes  $0.02$



 $time(s)$ 

### COALESCING BINARIES.

Two compact objects (NS or BH) spiraling together from a binary orbit give a chirp signal, whose shape identifies the masses and the distance

#### STOCHASTIC BACKGROUND.

Random background, relic of the early universe and depending on unknown particle physics. It will look like noise in any one detector, but two detectors will be correlated.

#### **Information**

Inner detailed dynamics of supernova See NS and BH being formed Nuclear physics at high density

#### **Information**

Neutron star locations near the Earth Neutron star Physics Pulsar evolution

#### **Information**

Masses of the objects BH identification Distance to the system Hubble constant Test of strong-field general relativity

#### **Information**

Confirmation of Big Bang, and inflation Unique probe to the Planck epoch Existence of cosmic strings



Chapter 14 Measurement of Classical Gravitation Fields Felix Pirani

Because of the principle of equivalence, one cannot ascribe a direct physical interpretation to the gravitational field insofar as it is characterized by Christoffel symbols  $\Gamma^{\mu}_{\nu\rho}$ . One can, however, give an invariant interpretation to the variations of the gravitational field. These variations are described by the Riemann tensor; therefore, measurements of the relative acceleration of neighboring free particles, which yield information about the variation of the field, will also yield information about the Riemann tensor.

Now the relative motion of free particles is given by the equation of geodesic deviation

$$
\frac{\partial^2 \eta^{\mu}}{\partial \tau^2} + R^{\mu}_{\nu\rho\sigma} v^{\nu} \eta^{\rho} v^{\sigma} = 0 \quad (\mu, \nu, \rho, \sigma = 1, 2, 3, 4)
$$
 (14.1)

Here  $\eta^{\mu}$  is the infinitesimal orthogonal displacement from the (geodesic) worldline  $\zeta$  of a free particle to that of a neighboring similar particle.  $v^V$  is the 4-velocity of the first particle, and  $\tau$  the proper time along  $\zeta$ . If now one introduces an orthonormal frame on  $\zeta$ ,  $\nu^{\mu}$  being the timelike vector of the frame, and assumes that the frame is parallelly propagated along  $\zeta$  (which insures that an observer using this frame will see things in as Newtonian a way as possible) then the equation of geodesic deviation  $(14.1)$  becomes

$$
\frac{\partial^2 \eta^a}{\partial \tau^2} + R^a_{0b0} \eta^b = 0 \quad (a, b = 1, 2, 3, ) \tag{14.2}
$$

Here  $\eta^a$  are the physical components of the infinitesimal displacement and  $R_{0b0}^{a}$  some of the physical components of the Riemann tensor, referred to the orthonormal frame.

By measurements of the relative accelerations of several different pairs of particles, one may obtain full details about the Riemann tensor. One

can thus very easily imagine an experiment for measuring the physical components of the Riemann tensor.

Now the Newtonian equation corresponding to (14.2) is

$$
\frac{\partial^2 \eta^a}{\partial \tau^2} + \frac{\partial^2 v}{\partial x^a \partial x^b} \eta^b = 0
$$
 (14.3)

It is interesting that the empty-space field equations in the Newtonian and general relativity theories take the same form when one recognizes the correspondence  $R_{0b0}^a \sim \frac{\partial^2 v}{\partial x^a \partial x^b}$  between equations (14.2) and (14.3), for the respective empty-space equations may be written  $R_{0a0}^a = 0$  and  $\frac{\partial^2 v}{\partial x^a \partial x^b} = 0$ . (Details of this work are in the course of publication in Acta Physica Polonica.)

BONDI: Can one construct in this way an absorber for gravitational energy by inserting a  $\frac{d\eta}{d\tau}$  term, to learn what part of the Riemann tensor would be the energy producing one, because it is that part that we want to isolate to study gravitational waves?

PIRANI: I have not put in an absorption term, but I have put in a "spring." You can invent a system with such a term quite easily.

LICHNEROWICZ: Is it possible to study stability problems for  $\eta$ ?

PIRANI: It is the same as the stability problem in classical mechanics, but I haven't tried to see for which kind of Riemann tensor it would blow up.



The main point of this presentation was that it is relative accelerations of neighboring free particles that are the physically meaningful (i.e.,measurable) ways to observe gravitational effects. Pirani points out the transparent connection between the equation of geodesic deviation and Newton's Second Law, as long as one identifies  $\mathbf{R}_{\text{a0bo}}$  with the second derivative of the Newtonian potential (i.e., as the tidal field.)

To make sure everyone sees how important and simple this is, he remarks, "By measurements of the relative accelerations of several different pairs of particles, one may obtain full details about the Riemann tensor. One can thus very easily imagine an experiment for measuring the physical components of the Riemann tensor".

*from: P. Saulson, Gen Relativ Gravit (2011) 43:3289–3299*

# Joe Weber at Chapel Hill



Joe Weber, co-inventor of the maser, was a U Md professor, on sabbatical in 1956 -57 with John Wheeler at Princeton. At the Chapel Hill conference in Jan 1957, they heard the key talk by Pirani that clarified that GW's were real, because they could (in principle) be detected.

### • **GWs are detectable in principle**

 The equation for geodetic deviation is the basis for all experimental attempts to detect GWs:

$$
\frac{d^2\delta l^j}{dt^2} = -R_{joko}l^k = \frac{1}{2}\frac{\partial^2 h_{jk}}{\partial t^2}l^k
$$

• **GWs change (**δ**l) the distance (l) between freely-moving particles in empty space.** 

 They change the proper time taken by light to pass to and fro fixed points in space

 In a system of particles linked by non gravitational (ex.: elastic) forces, GWs perform work and deposit energy in the system



# Weber's bar



 Weber's detector embodied Pirani's *gedankenexperiment.*  It was a cylinder of aluminum, each end of which is like a test mass, while the center is like a spring. PZT's around the midline absorb energy to send to an electrical amplifier.

Weber invented us from scratch

 It was an act of genius (and/or madness) to transform a *gendankenexperiment* into a working apparatus and an observing program.

Along the way, Weber developed:

- Sensitivity calculation and noise analysis
- Thermal noise minimization by high *Q*
- Seismic isolation
- Coincidence for background rejection
- Time slides for background estimation
- Inverse False Alarm Rate detection statistic

# Weber started seeing things

 In 1969, Weber made his first of many announcements that he was seeing coincident excitations of two detectors.



FIG. 2. Argonne National Laboratory and University of Maryland detector coincidence.

**LIGO-G1400715v2 Detection Workshop, IPTA@Banff, 27 June 2014** 

### **Acoustic bar GW** Detector groups



R. Garwin



W. Fairbank



G. Pizzella, E. Amaldi

### 1965-1975 Room T bars

**Bell Labs** Frascati Glasgow **IBM** Rochester **Max Planck** Rome



A. Tyson

1975-1990+ Cryogenic bars

> Frascati Louisiana **Moscow** Perth Rochester **Stanford**



W. Hamilton

 $2000 - >$ Spherical cryogenic detectors

> **Brazil Netherlands**



P. Michelson



## Some perspective: 50 years of attempts at detection:



60': Joe Weber pioneering work

Since the pioneering work of Joseph Weber in the '60, the search for Gravitational Waves has never stopped, with an increasing effort of manpower and ingenuity:



90': Cryogenic Bars

## 1997: GWIC was formed

GWIC thesis prize named after Stefano Braccini





2000' - : Large Interferometers



Experimental gravitational physicists are heirs to several great traditions:

- High precision mechanical experiments (Cavendish, Eotvos, Dicke..) *detection of weak forces applied on mechanical test bodies*
- High precision optical measurements (Michelson, laser developers…)
- Operation of ultraprecise e-m measurement systems (microwave pioneers of World War II)
- Low temperature physics (K. Onnes) *superfluids and superconductors technology*























# ADVANCED DETECTORS **TIMELINE**

## foreseen at the end of 2015



Riunione Direttori 28/04/2016

Gianluca Gemme





- Top row left  $-$  Hanford
- Top row right Livingston
- Time difference  $\sim$  6.9 ms with Livingston first
- Second row  $-$  calculated GW strain using **Numerical Relativity** Waveforms for quoted parameters compared to reconstructed waveforms (Shaded)
- Third Row residuals
- Bottom row  $-$  time frequency plot showing frequency increases with time (chirp) |



## E. Coccia  $\mathbf{G}$ W150914: Estimated Strain Amplitude  $\mathbf{\Xi}$



$$
\mathcal{M} = \frac{(m_1 m_2)^{3/5}}{(m_1 + m_2)^{1/5}} = \frac{c^3}{G} \left[ \frac{5}{96} \pi^{-8/3} f^{-11/3} \dot{f} \right]^{3/5}
$$

- Numerical relativity models of black hole horizons during coalescence
- $\cdot$  Fffective black hole separation in units of Schwarzschild radius  $(R_s = 2GM_{tot}/c^2 = 210km);$ and effective relative velocities given by post-Newtonian parameter  $v/c =$  $(GM_{\text{tot}}\pi f_{\text{GW}}/c^3)^{1/3}$

Binary Black Hole System

- $M1 = 36 + 5/4$  Msol
- $M2 = 29 +14$  M<sub>sol</sub>
- Final Mass =  $62 +/- 4$  M<sub>sol</sub>
- distance=410 +160/-180 MPc (redshift  $z = 0.09$ )







# **Nautilus** - September 14, 2015



E. Coccia



Use numerical simulations fits of black hole merger to determine parameters, we determine total energy radiated in gravitational waves is  $3.0\pm0.5$  M<sub>o</sub>  $c^2$ . The system reached a peak  $\sim$ 3.6 x10<sup>56</sup> erg, and the spin of the final black hole < 0.7





## **Black Holes of Known Mass**



### **Plausible scenario** for the operation of the LIGO-Virgo network over the next decade





## **Gravitational-Wave Sky Posteriors**

15

Sky areas broadly consistent with simply triangulation, and mostly Crossconsistent

Triangulation ring consistent with time delay of about  $-7$  ms

**Search area:** 620 sq. degrees to cover:



## Sky Locations of Gravitational-wave Events GW150914, GW151226 and Candidate LVT151012



<u>Università di l</u>

tuto Nazionale<br>fisica Nucleare

# Simulated Sky Locations of O1 Events and Candidate Including the Virgo Interferometer

E. Coccia





### **Localization expected for a BNS system**

The ellipses show 90% confidence localization areas, and the red crosses show regions of the sky where the signal would not be condently detected.

# Multi-Messenger Astronomy: Gravitational Wave + Electromagnetic +Neutrinos







![](_page_47_Picture_0.jpeg)

# **EINSTEIN TELESCOPE**

- √Design study of ET funded by the European Commission under FP7
	- interest primarily focused on the Infrastructure rather than on the detector and its technologies
	- The infrastructure should no limit the sensitivity of the future hosted detectors
		- $\cdot$  Size
		- Environmental noises (seismic and NN)
	- ET absorbed and developed many concepts in GW detectors:
		- Underground and cryo-compatible facility, pioneered in Japan by CLIO and KAGRA
		- Triangular geometry,<br>concept used in LISA
		- Xylophone configuration

![](_page_47_Figure_11.jpeg)

![](_page_48_Figure_0.jpeg)

## THE GLOBAL PLAN

- Advanced Detectors (LIGO, VIRGO) will initiate gravitational wave astronomy through the detection of the most luminous sources - compact binary mergers.
- Third Generation Detectors (ET and others) will expand detection horizons and provide new tools for extending knowledge of fundamental physics, cosmology and relativistic astrophysics.
- Observation of low frequency gravitational wave with eLISA will probe the role of super-massive black holes in galaxy formation and evolution

![](_page_49_Picture_4.jpeg)

![](_page_49_Picture_5.jpeg)

## Every newly opened astronomical window has found unexpected results

![](_page_50_Picture_71.jpeg)

Die 25. July, promoto Cf CHO rumped  $1610$  $\frac{46 i \mu_0}{x} \frac{d}{dx} \frac{h}{dx} \frac{d}{dx} \frac{g}{g} \frac{g}{g} \frac{g}{g} \frac{g}{g}$ <br> $\frac{f}{g} \frac{g}{g} \frac{g}{g} \frac{g}{g} \frac{g}{g} \frac{g}{g} \frac{g}{g}$ <br> $\frac{f}{g} \frac{g}{g} \frac{g}{g} \frac{g}{g}$ P HYSICAL REVIEW D. S. Aug! \* O \* 7 mill  $\begin{array}{ccccc} \hline 0.3 & \frac{1}{2} & \frac{2}{3} & 0 & \frac{3}{2} \\ \hline \hline 0 & 0.1 & \frac{2}{3} & \frac{1}{2} & \frac{1}{2} \\ \hline \end{array}$ L ETTERS® 1.30. \* 5 20 F Originally Articles published week ending 12 FEBRUARY 2016 **Member Subscription Copy**<br>ibrary or Other Institutional Use Prohibited Until 2017 trop # post ther. I considers fuit.  $0.17.$   $\frac{2}{\pi}$   $\frac{20.2}{\pi}$  $\frac{1}{\sqrt{1+2\sqrt{2}\epsilon\epsilon\epsilon^2}}\frac{1}{\sqrt{1+2\sqrt{2}}}\frac{1}{\sqrt{1+2\sqrt{2}}}\frac{1}{\sqrt{1+2\sqrt{2}}}\frac{1}{\sqrt{1+2\sqrt{2}}}\frac{1}{\sqrt{1+2\sqrt{2}}}\frac{1}{\sqrt{1+2\sqrt{2}}}\frac{1}{\sqrt{1+2\sqrt{2}}}\frac{1}{\sqrt{1+2\sqrt{2}}}\frac{1}{\sqrt{1+2\sqrt{2}}}\frac{1}{\sqrt{1+2\sqrt{2}}}\frac{1}{\sqrt{1+2\sqrt{2}}}\frac{1}{\sqrt{1+2\sqrt{2}}}\frac{1$  $0.20.0.*$  $1.3.11.5.7$  $0.21.4$  $C^*$  0  $0.22 *$  $0.4.4.5.$   $\frac{20}{10}$   $\frac{1}{5}$  $\frac{1}{3}$   $\frac{1}{10}$   $\frac{1}{10}$   $\frac{1}{10}$   $\frac{1}{10}$   $\frac{1}{10}$   $\frac{1}{10}$   $\frac{1}{10}$   $\frac{1}{10}$  $0.6.$  H.s \* \* 0 or. H. s. \* \* 0  $2.25 \frac{1}{2}$  $H.7.$   $\frac{1}{2}$   $\frac{1}{2}$   $\frac{1}{2}$   $\frac{1}{2}$   $\frac{1}{2}$  O. or to one of one  $\frac{1}{7}$   $\frac{1}{7}$   $\frac{1}{7}$   $\frac{1}{7}$  $0.31.4$ D. T. septemb: \* 0 \* 8 \*  $4.7564$ <br>  $4.4564$ <br>  $4.7564$ <br>  $4.7664$ <br>  $4.7664$ <br>  $4.76$  $9.9.$  H.S. \*  $\overbrace{0.40. H.4. *_{\mathscr{O}}^{\mathscr{C}}}^{\mathscr{C}} \times \overbrace{0.4}^{\mathscr{C}} \times \overbrace{0.4}^{\mathscr{C}} \times \overbrace{0.4}^{\mathscr{C}}$  $\sqrt[n]{12. H. g. x}$  $6-17.$  H . 7. 76.  $\overline{**}$   $\overline{**}$  O. Scala ~ 4. 880. 1.18.11.5.12 FOF 4 ward Ho. q. mainores y. counch sugs.  $\frac{1004}$  und mortgage. Sunt put the boot' is  $\frac{1}{2}$  $4.4.4.3.76. * 7.76.$  $7.9.477$ **Published by APS**<br>physics Volume 116, Number 6 **American Physical Society** ™ V. 20. H. s. 24 O A.J. outy attillist  $\frac{1}{2}$ . 24.  $\frac{2}{3}$   $\frac{1}{3}$   $\frac{1}{2}$   $\frac{1}{3}$   $\frac{1}{4}$