

# *Ab initio* many-body calculations of single-nucleon transfer reactions with deuteron projectile

[arXiv:1602.04404, accepted on PRC]

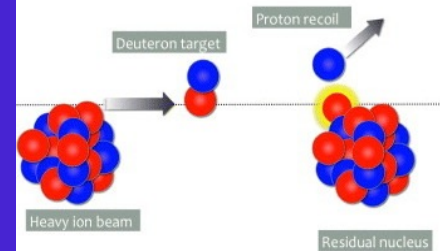


**Francesco Raimondi (University of Surrey)**

In collaboration with:  
G. Hupin (CEA, DAM),  
P. Navrátil (TRIUMF),  
S. Quaglioni (LLNL).



Figure 1 from Kate L. Jones 2013 Phys. Scr. 2013 014020

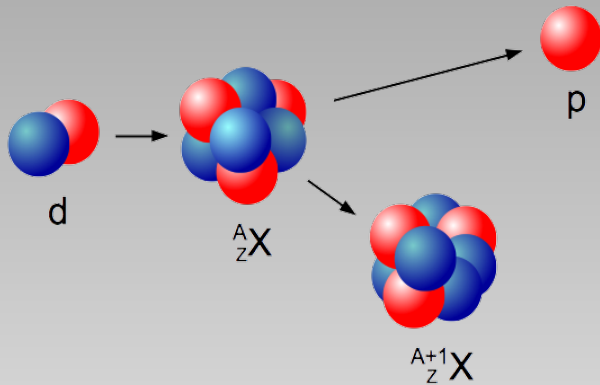


# Outline

- Motivations for the study of transfer reactions and interest in  ${}^7\text{Li}(d,p){}^8\text{Li}$  reaction
- The No-Core Shell Model with Resonating Group Method (NCSM/RGM) and with continuum (NCSMC)
- Results on  ${}^7\text{Li}(d,p){}^8\text{Li}$  reactions and resonances of  ${}^9\text{Be}$  above  $d$ - ${}^7\text{Li}$  threshold:
  - (Eigen)phase shifts
  - Cross sections
- Conclusions & perspectives

# Deuteron-nucleus reaction: experimental motivations

Intense experimental activity (direct and inverse kinematics):



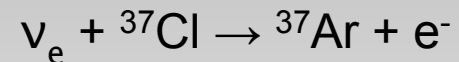
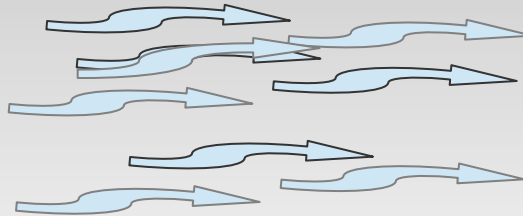
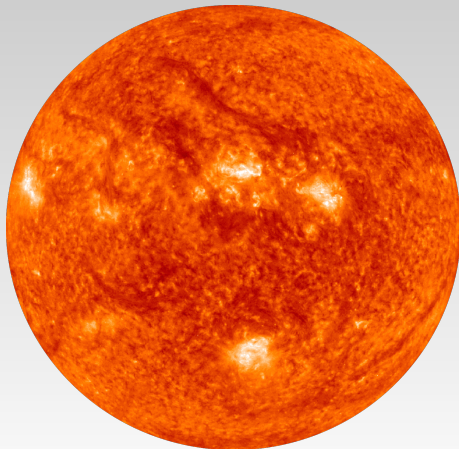
(d,p) reaction  
in direct  
kinematics

- Structure and spectroscopy of nuclei
- Nucleosynthesis and nuclear fusion applications ( $^3\text{H}(d,n)^4\text{He}$  reaction)
- Surrogate for (p/n) capture reactions
- Calibration reaction for measurement of processes of interest

# ${}^7\text{Li}(d,p){}^8\text{Li}$ transfer reaction

◆ Calibration reaction for astrophysical process:  ${}^7\text{Li}(d,p){}^8\text{Li}$  as target calibration for  ${}^7\text{Be}(p,\gamma){}^8\text{B}$

Solar neutrino problem:



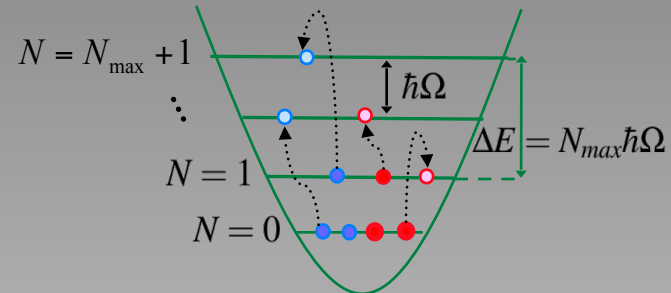
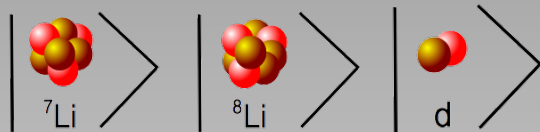
R. Davis Jr takes a dip  
At Homestake Mine (1971)



# No-core shell model combined with the resonating group method (NCSM-RGM) and NCSM with continuum (NCSMC)

## No-core shell model (NCSM):

- A-nucleon wave function expansion in the harmonic-oscillator (HO) basis
- Short- and medium-range correlations
- No continuum

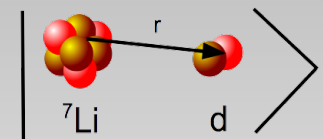
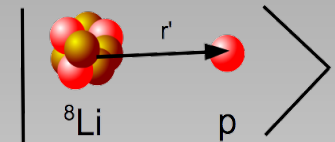


P. Navrátil et al. PRL **84**, 5728 (2000)

## NCSM+Resonating group method (NCSM-RGM):

- Microscopic approach to describe the scattering of clusters
- Long range correlations (relative motion of clusters)

K. Wildermuth, Y.C. Tang A unified theory of the nucleus 1977



## NCSM with continuum (NCSMC):

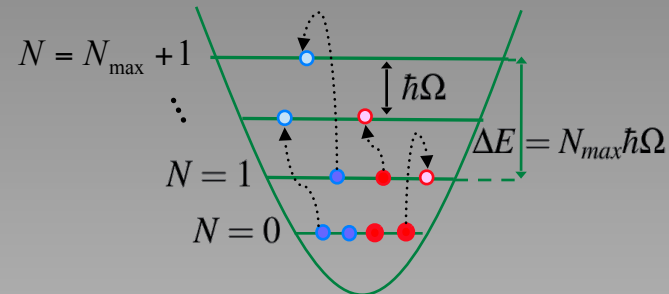
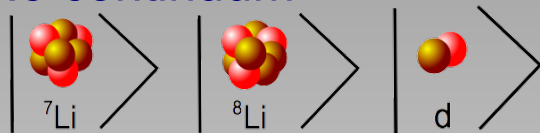
S. Baroni, P. Navrátil, and S. Quaglioni, PRL 110, 022505 (2013); PRC 87, 034326 (2013)

$$|\Psi_A^{J^\pi T}\rangle = \sum_{\lambda} c_{\lambda} |{}^9\text{Be}\rangle + \sum_{\tilde{\nu}} \int dr r^2 \frac{g_{\tilde{\nu}}^{J^\pi T}(r)}{r} \hat{A}_{\tilde{\nu}} |{}^7\text{Li} \text{ } d\rangle + \sum_{\tilde{\nu}'} \int dr' r'^2 \frac{g_{\tilde{\nu}'}^{J^\pi T}(r')}{r'} \hat{A}_{\tilde{\nu}'} |{}^8\text{Li} \text{ } p\rangle$$

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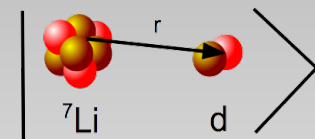
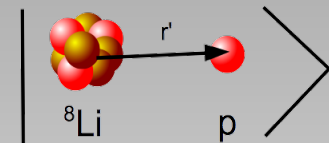


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Variational amplitudes  
(unknowns of the many-body problem)

# NCSM-RGM and NCSMC equations

$$\mathcal{H} = T_{\text{rel}}(r) + \mathcal{V}_{\text{rel}} + \bar{V}_C(r) + H_{(A-a)} + H_{(a)} \quad \text{Internal A-nucleon microscopic Hamiltonian}$$

Coupled-channel equations solved for the amplitude  $c_\lambda$  and  $g_{\tilde{\nu}}$

$$\begin{pmatrix} E_\lambda \delta_{\lambda\lambda'} & \langle {}^9\text{Be} | \mathcal{H} \mathcal{A}_{\tilde{\nu}} | {}^8\text{Li} \text{ p } {}^7\text{Li} \text{ d} \rangle \\ \langle {}^7\text{Li} \text{ d } {}^8\text{Li} \text{ p } | \mathcal{A}_{\tilde{\nu}'} \mathcal{H} | {}^9\text{Be} \rangle & \langle {}^7\text{Li} \text{ d } {}^8\text{Li} \text{ p } | \mathcal{A}_{\tilde{\nu}'} \mathcal{H} \mathcal{A}_{\tilde{\nu}} | {}^8\text{Li} \text{ p } {}^7\text{Li} \text{ d} \rangle \end{pmatrix} \begin{pmatrix} c_\lambda \\ g_{\tilde{\nu}, \tilde{\nu}'} \end{pmatrix} =$$

$$E \begin{pmatrix} \delta_{\lambda\lambda'} & \langle {}^9\text{Be} | \mathcal{A}_{\tilde{\nu}} | {}^8\text{Li} \text{ p } {}^7\text{Li} \text{ d} \rangle \\ \langle {}^7\text{Li} \text{ d } {}^8\text{Li} \text{ p } | \mathcal{A}_{\tilde{\nu}'} | {}^9\text{Be} \rangle & \langle {}^7\text{Li} \text{ d } {}^8\text{Li} \text{ p } | \mathcal{A}_{\tilde{\nu}'} \mathcal{A}_{\tilde{\nu}} | {}^8\text{Li} \text{ p } {}^7\text{Li} \text{ d} \rangle \end{pmatrix} \begin{pmatrix} c_\lambda \\ g_{\tilde{\nu}, \tilde{\nu}'} \end{pmatrix} =$$

Coupled-channel microscopic **R-matrix method** on Lagrange mesh provides **Scattering matrix** and **Asymptotic Normalization Coefficients** by matching internal solution to known asymptotic

M. Hesse, J.M. Sparenberg, F. Van Raemdonck, and D. Baye, Nucl Phys. A 640, 37 (1988)

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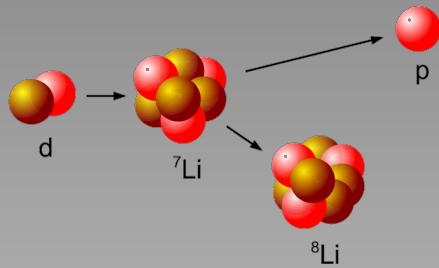
$$\begin{pmatrix} \langle \text{Diagram 1} | \mathcal{H} | \text{Diagram 2} \rangle \\ \langle \text{Diagram 3} | \mathcal{H} | \text{Diagram 4} \rangle \end{pmatrix} \begin{pmatrix} c_\lambda \\ g_{\tilde{\nu}, \tilde{\nu}'} \end{pmatrix} = \begin{pmatrix} \langle \text{Diagram 5} | \mathcal{H} | \text{Diagram 6} \rangle \\ \langle \text{Diagram 7} | \mathcal{H} | \text{Diagram 8} \rangle \end{pmatrix} \begin{pmatrix} c_\lambda \\ g_{\tilde{\nu}, \tilde{\nu}'} \end{pmatrix}$$

The diagrams represent various nuclear configurations and transitions, including  ${}^7\text{Li}$ ,  ${}^8\text{Li}$ ,  ${}^9\text{Be}$ ,  ${}^9\text{B}$ ,  ${}^8\text{Li}$ ,  ${}^7\text{Li}$ ,  ${}^6\text{Li}$ ,  ${}^5\text{He}$ ,  ${}^4\text{He}$ ,  ${}^3\text{He}$ ,  ${}^2\text{He}$ ,  ${}^1\text{H}$ , and  ${}^0$ . The equations are crossed out with large X's.

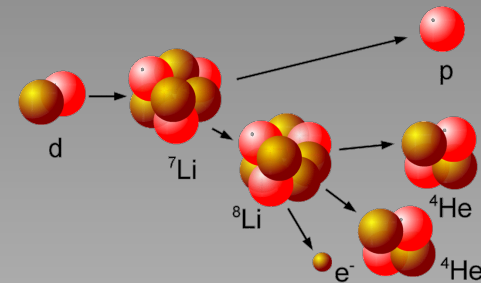
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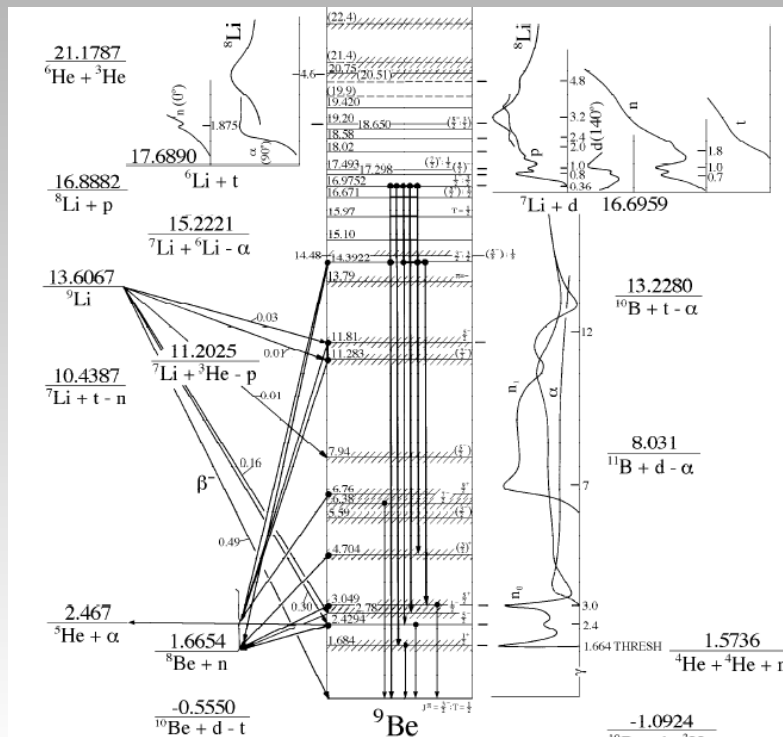
# ${}^7\text{Li}(d,p){}^8\text{Li}$ reaction and structure of ${}^9\text{Be}$



"Model space" reaction

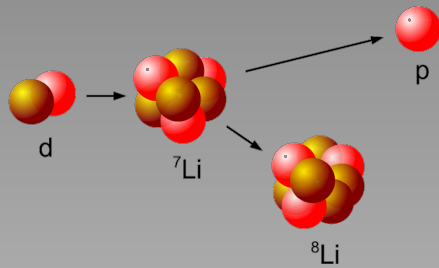


"Real world" reaction

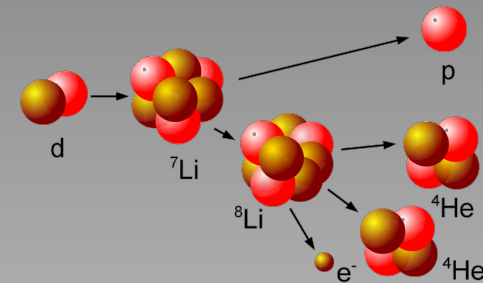


${}^9\text{Be}$  ground state is stable  
All excited states are unbound

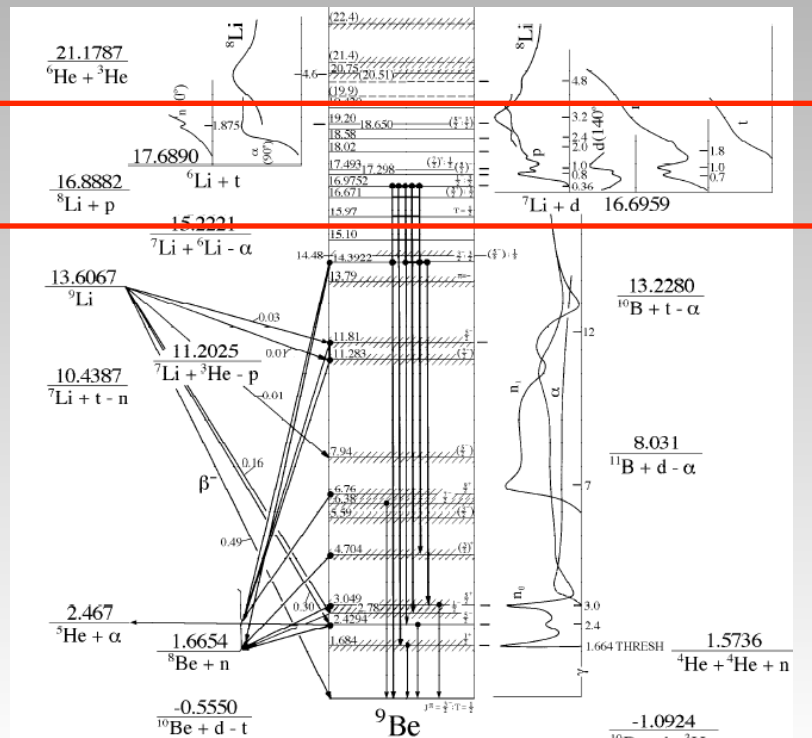
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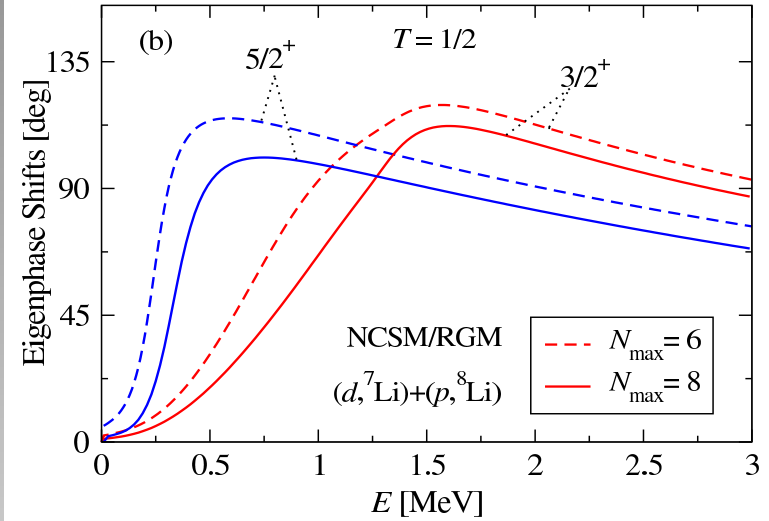
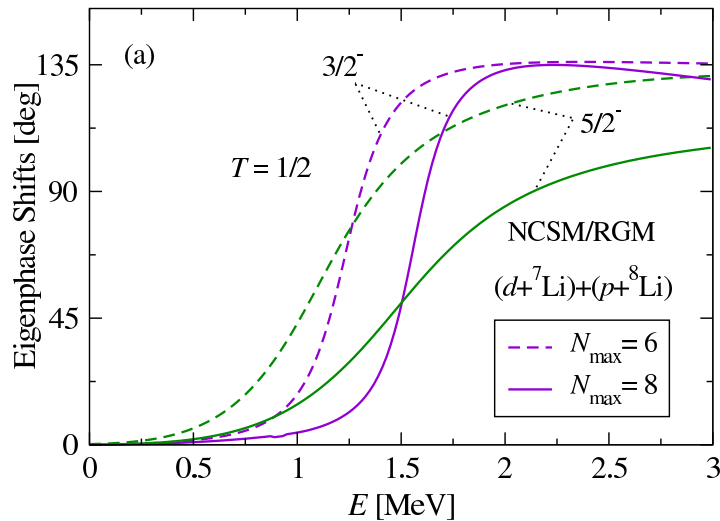
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Inclusion of the continuum:

- Low-energy spectrum:  $n$ - ${}^8\text{Be}$  ( $n$ - $\alpha$ - $\alpha$ )
- High-energy spectrum:  $d$ - ${}^7\text{Li}$  ,  $p$ - ${}^8\text{Li}$



# $(d, {}^7\text{Li}) + (p, {}^8\text{Li})$ coupled NCSM-RGM calculation Eigenphase shifts



Model space ( $N_{\text{max}}=6,8$   $\hbar\Omega=20$  MeV):

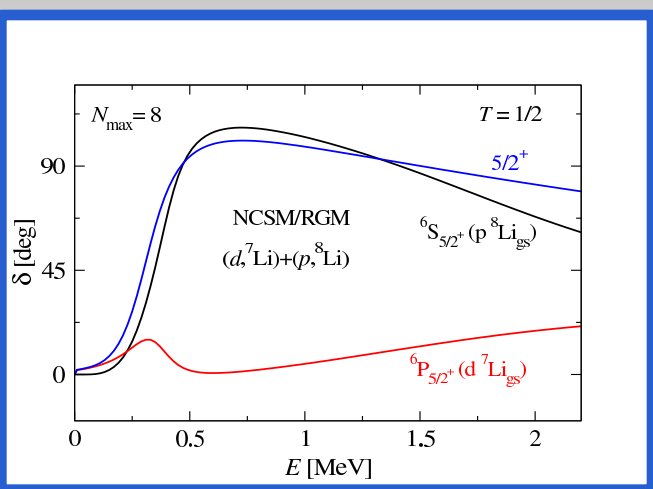
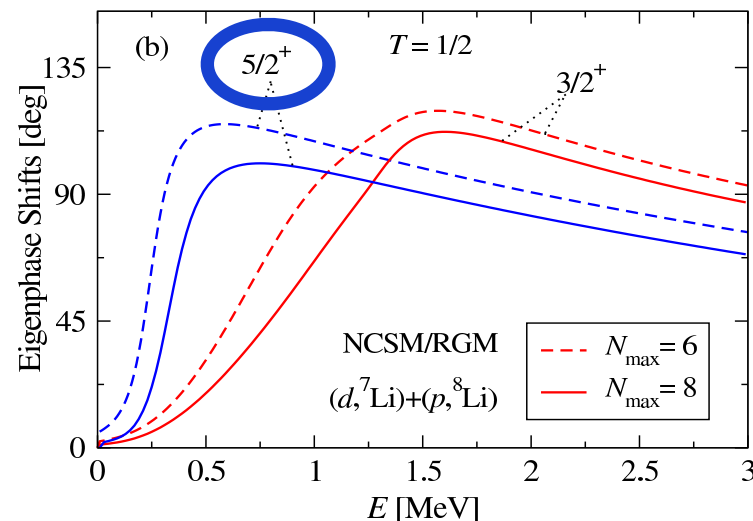
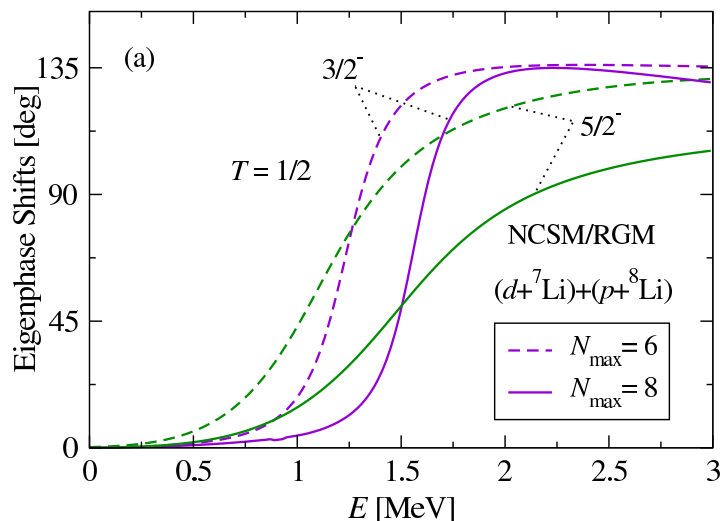
$$|d(d^*)+{}^7\text{Li}_{\text{gs}}\rangle + |d(d^*)+{}^7\text{Li}_{1\text{ex}}\rangle + |p+{}^8\text{Li}_{\text{gs}}\rangle + |p+{}^8\text{Li}_{1\text{ex}}\rangle + |p+{}^8\text{Li}_{2\text{ex}}\rangle + |p+{}^8\text{Li}_{3\text{ex}}\rangle$$

Virtual breakup of the deuteron: 4 pseudostates

Chiral nuclear interaction:

Entem-Machleidt SRG-evolved ( $\Lambda=2.02$  fm $^{-1}$ ) NN force at N<sup>3</sup>LO (cutoff 500 MeV)

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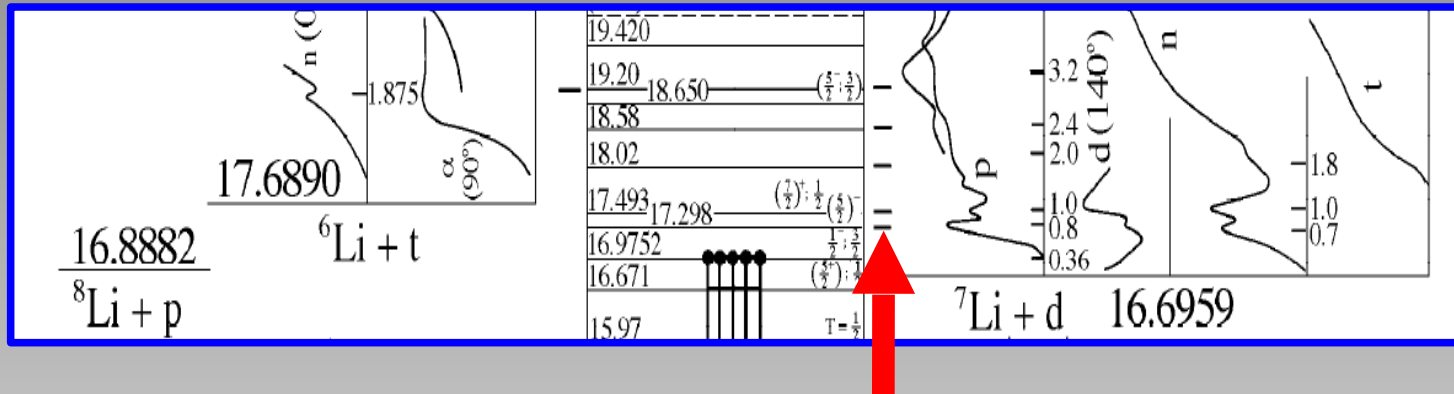
Dominant partial waves above  
 $p + {}^8\text{Li}$  threshold:  $3/2^{-,+}$ ,  $5/2^{-,+}$

Main phase shifts for  $5/2^+$ :

- P-wave in  $(d, {}^7\text{Li})$
- Resonant S-wave in  $(p, {}^8\text{Li})$

# Spin-parity assignment of 0.78 MeV resonance of $^9\text{Be}$

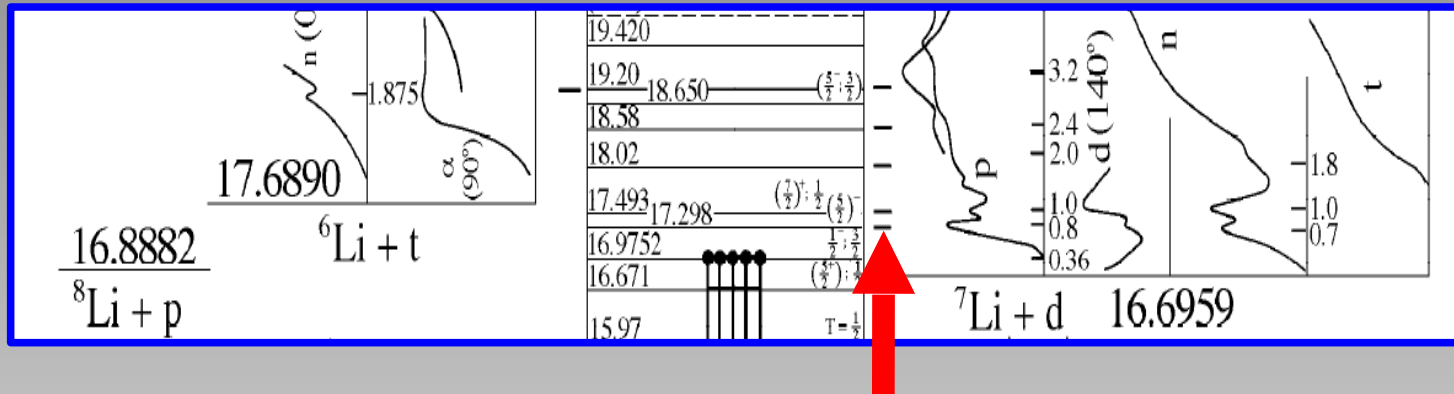
$^9\text{Be}$  spectrum above  $d$ - $^7\text{Li}$  threshold



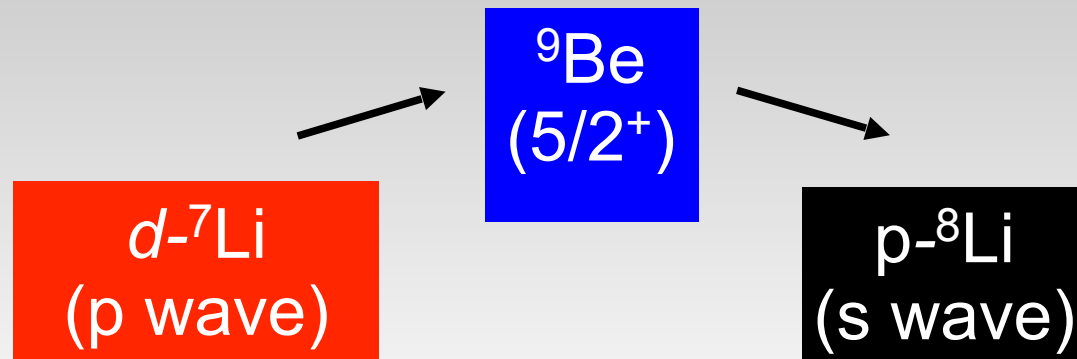
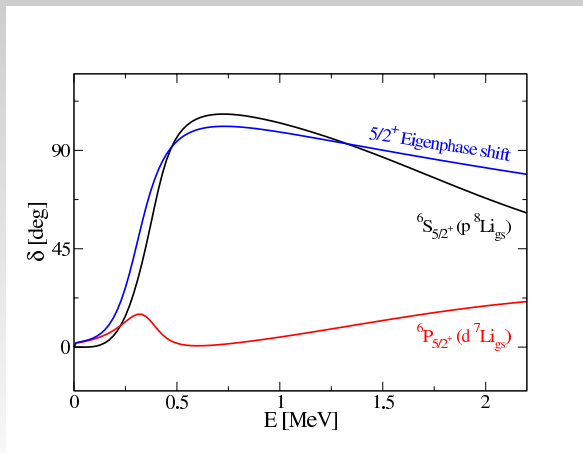
Low peak in the experimental total cross section:  
 $E(5/2^-) \sim 0.78 \text{ MeV}$  above the threshold  
 (Uncertain spin-parity assignment)

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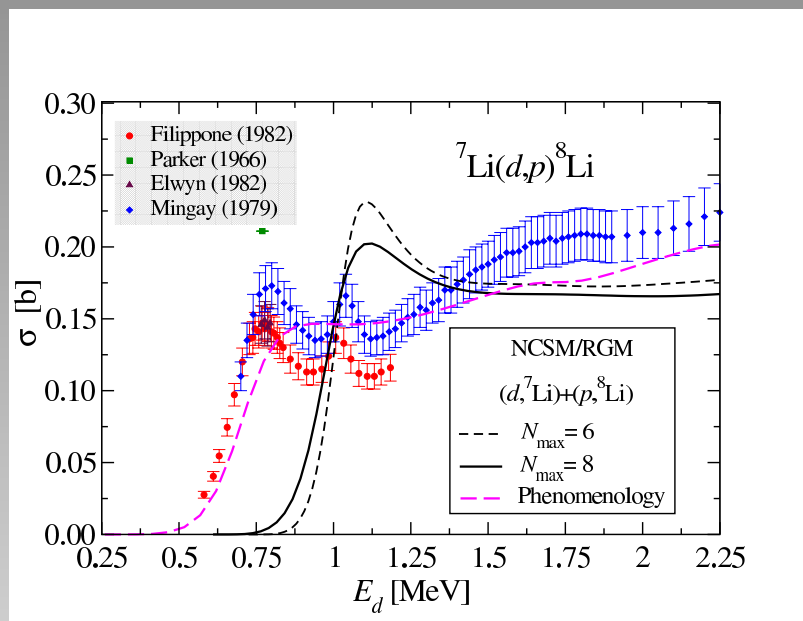
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# ${}^7\text{Li}(d,p){}^8\text{Li}$ total cross section

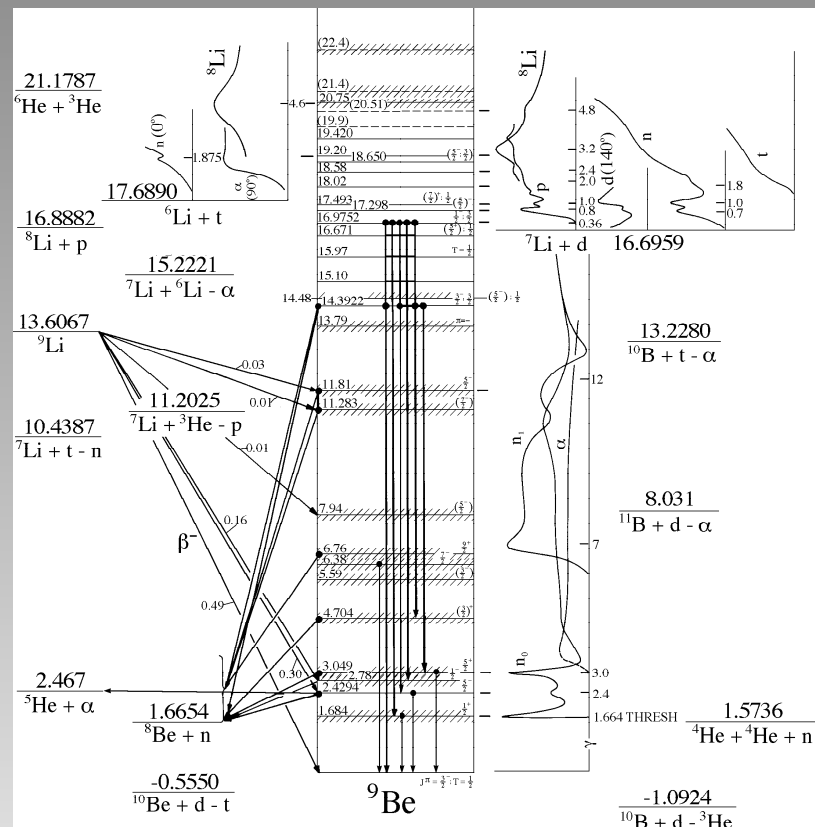


Included channels:

- (1)  $p, {}^8\text{Li}$  (2)  $d, {}^7\text{Li}$  (3) coupling  $(d,p)$
- (4) virtual breakup of  $d$

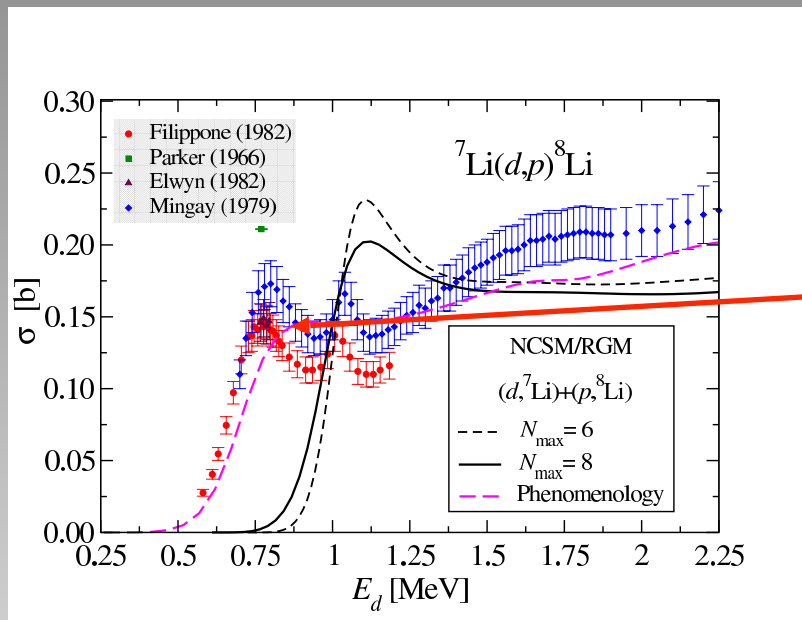
Not-included channels:

- (1)  ${}^8\text{Be}, n$  (2)  ${}^6\text{Li}, t$



Channel	Exp. thresh. [MeV]	Theo. thresh. [MeV]
$d, {}^7\text{Li}$	-41.470	-40.124
$p, {}^8\text{Li}$	-41.278	-39.659
Q-value	-0.193	-0.465

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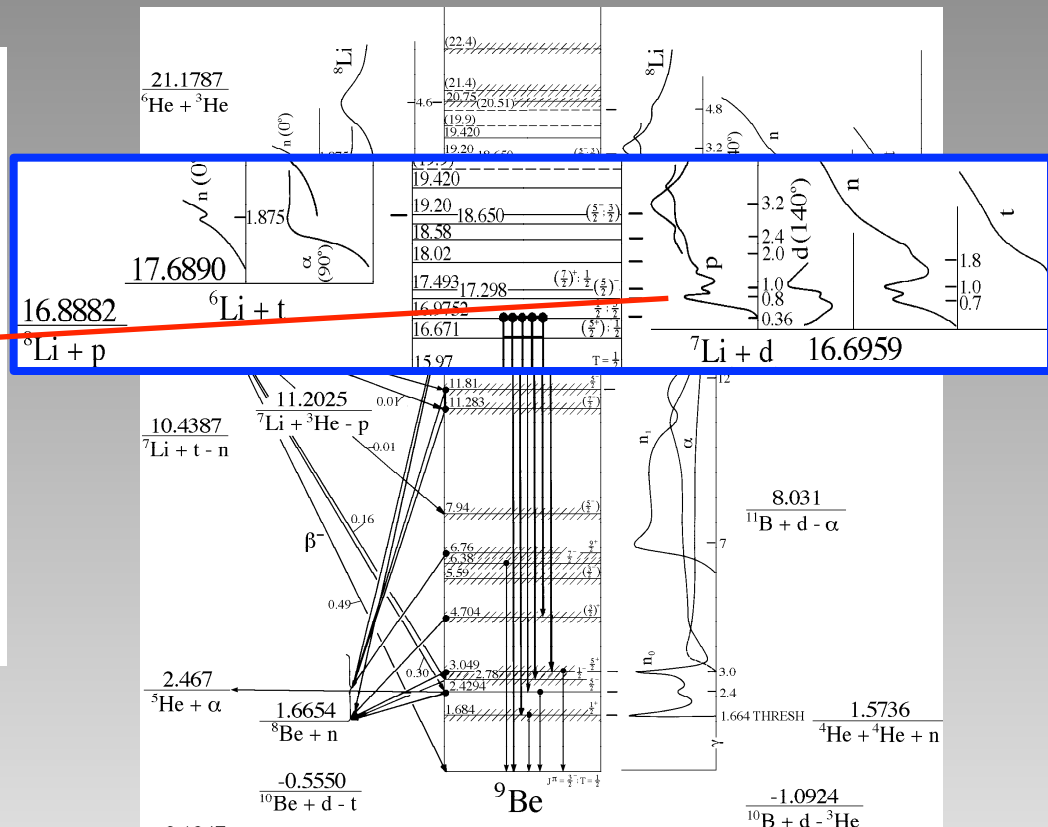


Included channels:

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- (4) virtual breakup of d

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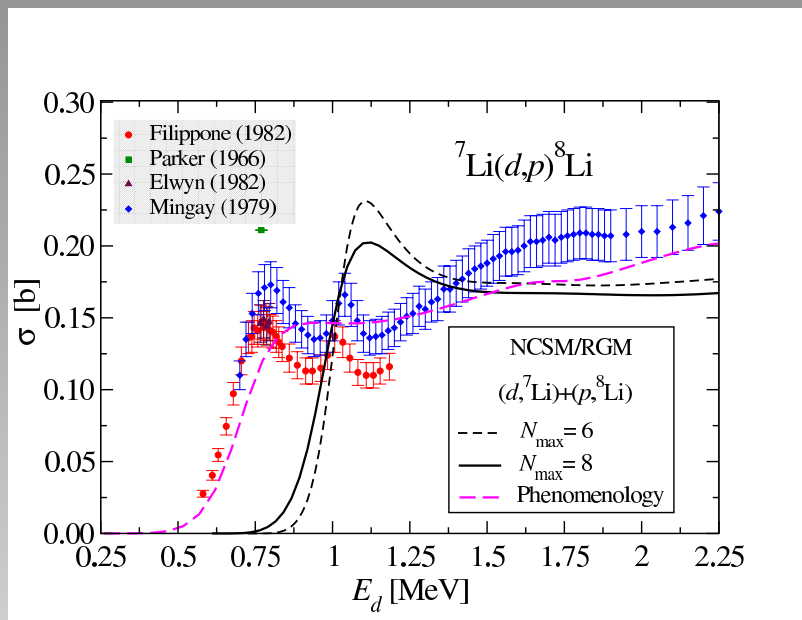


Experimental recommended value  
 $0.147 \pm 0.011$  b ( $\Gamma \approx 0.2$  MeV) at 0.78 MeV  
 of deuteron kinetic energy

Calibration peak for  
 ${}^7\text{Be}(p,\gamma){}^8\text{B}$  radiative capture reaction



# ${}^7\text{Li}(d,p){}^8\text{Li}$ total cross section



- Position of the first resonant peak overestimated by  $\sim 0.33$  MeV (see Q-value)
- Peak at 17.493 MeV ( ${}^9\text{Be}$  spectrum) not reproduced (missing  ${}^8\text{Be}(\alpha-\alpha)-n?$  3N forces?)

$d, {}^7\text{Li}, {}^8\text{Li}$  NCSM energies adjusted to reproduce the experimental Q-value of the reaction

position of first peak slightly overestimated

Included channels:

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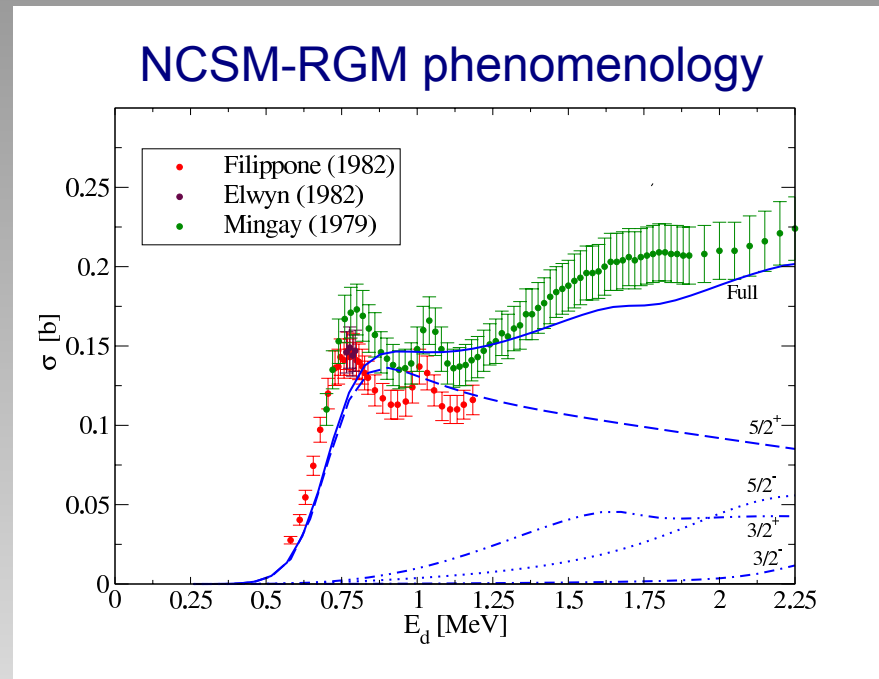
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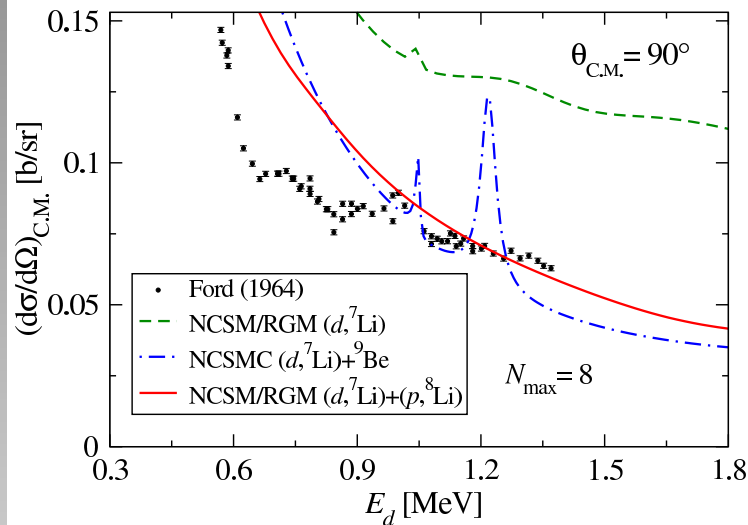
# Impact of different partial waves on NCSM-RGM total cross section

${}^7\text{Li}(d,p){}^8\text{Li}$  cross section



- Confirmed dominant role played by  $5/2^+$  partial wave
- Below  $\sim 2$  MeV the cross section is dominated by positive-parity partial waves
- Increasing trend up to deuteron break-up fairly well reproduced (contribution from  $5/2^-$  and  $3/2^+$  partial wave)

# ${}^7\text{Li}(d,d){}^7\text{Li}$ cross section (NCSMC)



Experimental resonant peaks  
at 0.8 MeV (S-wave)  
and 1.0 MeV (P-wave)  
(‘elastic’ process not ideal probe  
for the  ${}^9\text{Be}$  resonant states)

- Peak structure (1 MeV and 1.2 MeV) in uncoupled calculations (J=7/2<sup>-</sup> in D-wave and 5/2<sup>+</sup> in P-wave). ...shifted at higher energy (missing bare 3N? SRG parameter dependence? )
- Effect of the short-range correlations in NCSMC calculation:  
Increased lifetime of the resonance too narrow peaks (lack of p- ${}^8\text{Li}$  decay channel. other mass partition?)
- Qualitative trend of the data reproduced by NCSMC and coupled NCSM-RGM calculations ...still not-converged calculation at  $N_{\text{max}}=8$

# Conclusions & Perspectives

First application of the NCSM-RGM for deuteron-projectile and p-shell nucleus as target

Study of the  ${}^7\text{Li}(d,p){}^8\text{Li}$  transfer reaction and of the  ${}^9\text{Be}$  resonances above  $d$ - ${}^7\text{Li}$  threshold:

- Discussion of the spin-parity assignment of  $E_d=0.78$  MeV resonance

To be done:

- Complete the calculation of the  ${}^7\text{Li}(d,p){}^8\text{Li}$  transfer reaction in the NCSMC framework
- Include 3N force also for p-shell nuclei