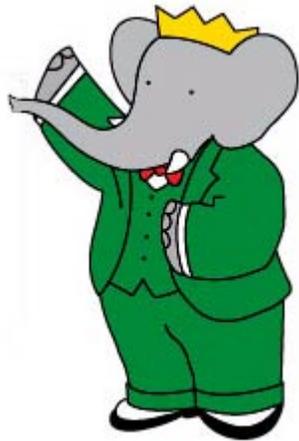


# $\alpha(\varphi_2)$ from a time-dependent analysis of $B^0 \rightarrow (\rho\pi)^0$ Dalitz-plot



Gagan Mohanty

University of Warwick

From BABAR Collaboration



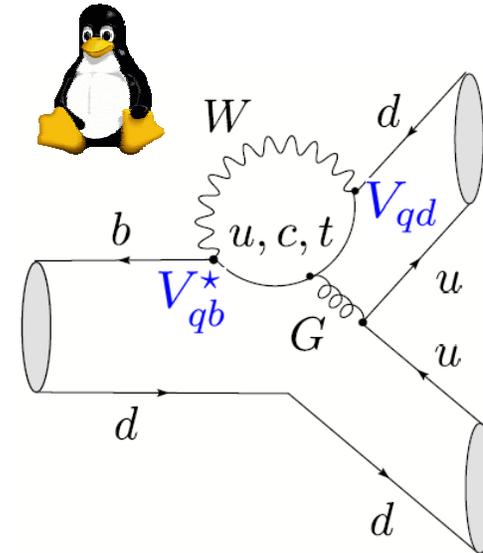
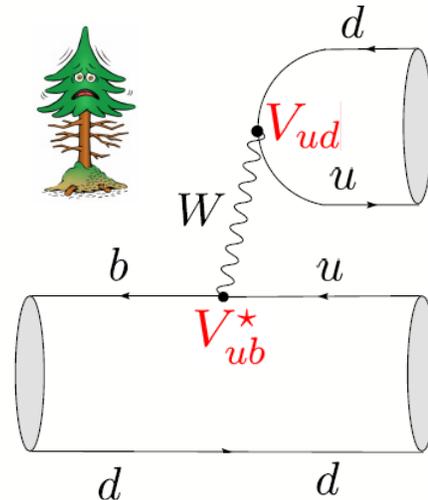


# Outline of the Talk

- Introduction
- Signal Model
- Reconstruction Effects
- Backgrounds
- Dalitz-plot Fit Results
- Q2B Interpretation
- Constraint on Angle  $\alpha$
- Conclusions and Outlook



# Introduction



Issues in hand:

- Not a  $CP$  eigenstate
- Has four isospin (0, 1, 2) amplitudes
  - 12 unknowns in the isospin pentagon

Snyder-Quinn Approach: **PRD 48 (1993) 2139**

- Time-dependent Dalitz plot analysis (TDPA) to constrain  $\alpha$  without any discrete ambiguity
  - Variation of strong phase of interfering  $\rho$  resonances over the DP



# TDPA Formulation

Three-body differential decay rate:

$$d\Gamma [B^0(\bar{B}^0) \rightarrow \pi^+ \pi^- \pi^0] = \frac{1}{(2\pi)^3} \frac{|A_{3\pi}|^2}{32m_{B^0}^3} dm_+^2 dm_-^2$$

Decay amplitude

DP variables

For a decay tagged as  $B^0(+)$  or  $\bar{B}^0(-)$ :

$$|A_{3\pi}^\pm|^2 \propto \left[ 1 \mp \frac{|A_{3\pi}|^2 - |\bar{A}_{3\pi}|^2}{|A_{3\pi}|^2 + |\bar{A}_{3\pi}|^2} \cos(\Delta m_d \Delta t) \pm \frac{2 \operatorname{Im}(\frac{q}{p} A_{3\pi}^* \bar{A}_{3\pi})}{|A_{3\pi}|^2 + |\bar{A}_{3\pi}|^2} \sin(\Delta m_d \Delta t) \right]$$



$$A_{3\pi}(m_+^2, m_-^2) = \sum_{\kappa} f_{\kappa}(m_+^2, m_-^2) A_{\kappa}$$

27 Bilinear coefficients ( $U, I$ ) – determine from the data fit:

$$|A_{3\pi}|^2 \pm |\bar{A}_{3\pi}|^2 = \sum_{\kappa \in \{+, -, 0\}} |f_{\kappa}|^2 U_{\kappa}^{\pm} + 2 \sum_{\kappa < \sigma \in \{+, -, 0\}} (\operatorname{Re}[f_{\kappa} f_{\sigma}^*] U_{\kappa\sigma}^{\pm, \operatorname{Re}} - \operatorname{Im}[f_{\kappa} f_{\sigma}^*] U_{\kappa\sigma}^{\pm, \operatorname{Im}})$$

PRD 62 (2000) 054002

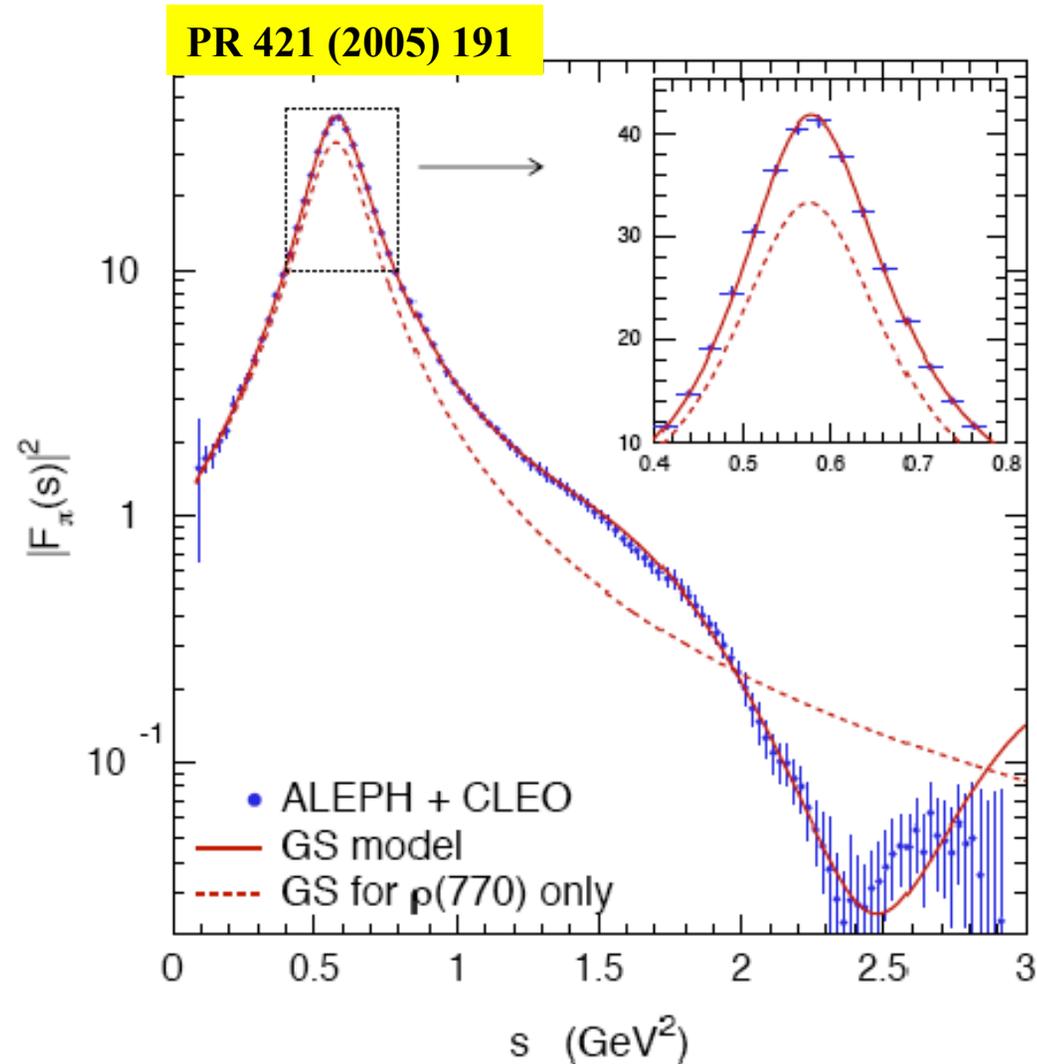
$$\operatorname{Im} \left( \frac{q}{p} A_{3\pi}^* \bar{A}_{3\pi} \right) = \sum_{\kappa \in \{+, -, 0\}} |f_{\kappa}|^2 I_{\kappa} + \sum_{\kappa < \sigma \in \{+, -, 0\}} (\operatorname{Re}[f_{\kappa} f_{\sigma}^*] I_{\kappa\sigma}^{\operatorname{Im}} + \operatorname{Im}[f_{\kappa} f_{\sigma}^*] I_{\kappa\sigma}^{\operatorname{Re}})$$



# Nominal Signal Model

Isobar Approach:

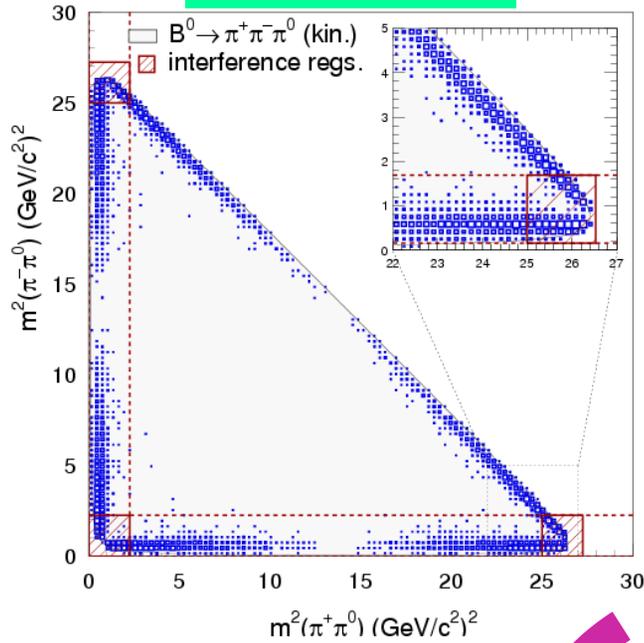
- $\rho$  dominated:  
 $\rho^0(770)$ ,  $\rho^0(1450)$   
and  $\rho^0(1700)$
- Gounaris-Sakurai  
(GS) lineshape for  
broad  $P$ -waves  
**PRL 21 (1968) 224**
- Other resonances as  
a part of systematic
  - ❖ scalar, e.g.  $f_0(980)$
  - ❖ tensor  $f_2(1270)$



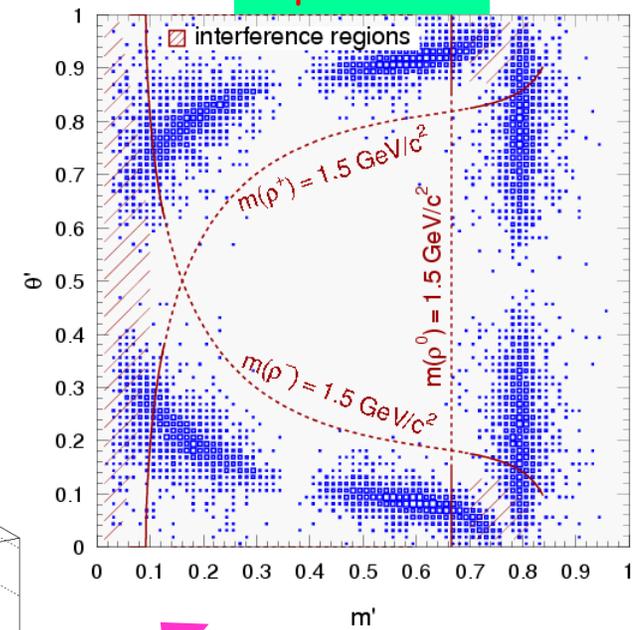


# Square Dalitz Plot

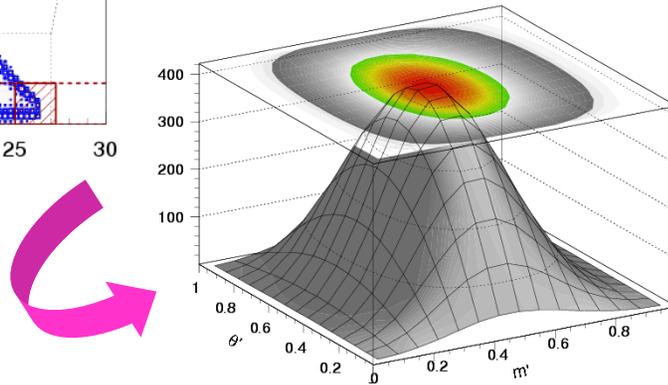
Traditional DP



Square DP



- Square DP zooms in regions of interest
- Plots from simulated signal events



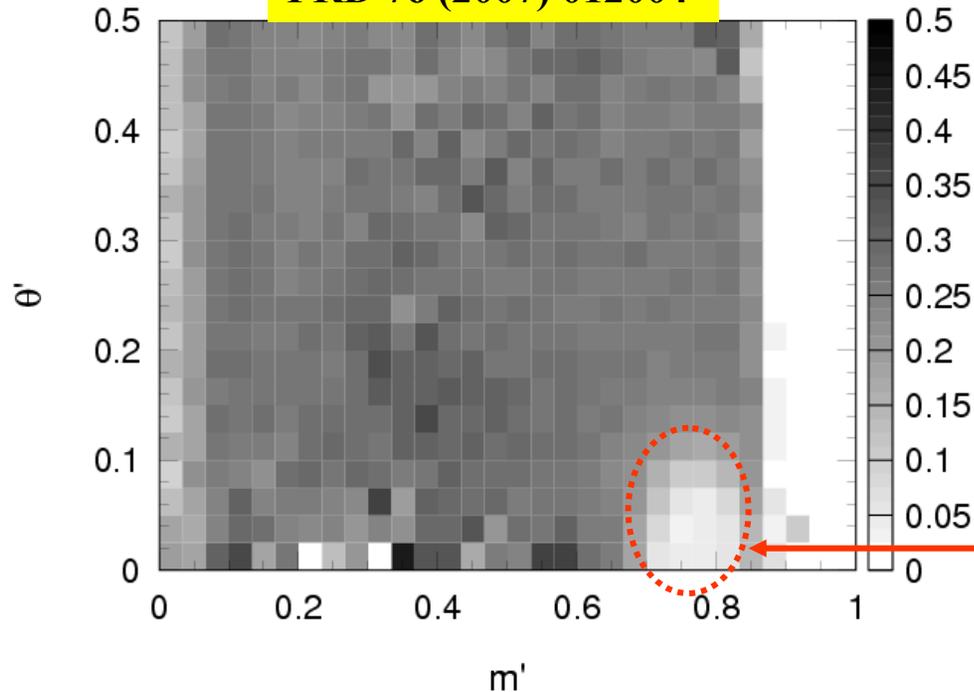
$$m' \equiv \frac{1}{\pi} \arccos \left( 2 \frac{m_0 - m_0^{\min}}{m_0^{\max} - m_0^{\min}} - 1 \right)$$

$$\theta' \equiv \frac{1}{\pi} \theta_0$$



# Reconstruction Effects

PRD 76 (2007) 012004



## Efficiency variation over DP

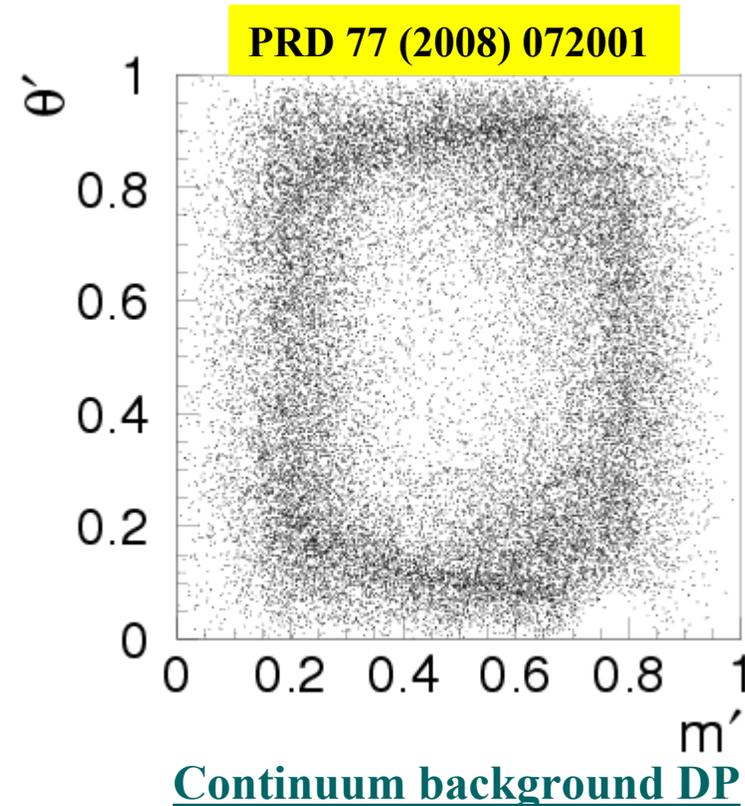
- Smooth across major part of the DP
- Inefficiency because of low momentum tracks

- Explicit treatment of misreconstructed (SCF) events
  - ❑ BABAR: 22%  $\rho^+\pi^-$ , 13%  $\rho^0\pi^0$  and 6% nonresonant
  - ❑ Belle: about 6% charged- and 14% neutral-type SCF
- Swapping of a track or neutral cluster with the tagged  $B$



# Backgrounds

- Dominant background from  $q\bar{q}$  continuum events
- Topological variables are combined into
  - ❖ Neural network, NN (BABAR)
  - ❖ Likelihood ratio (LR) for Belle



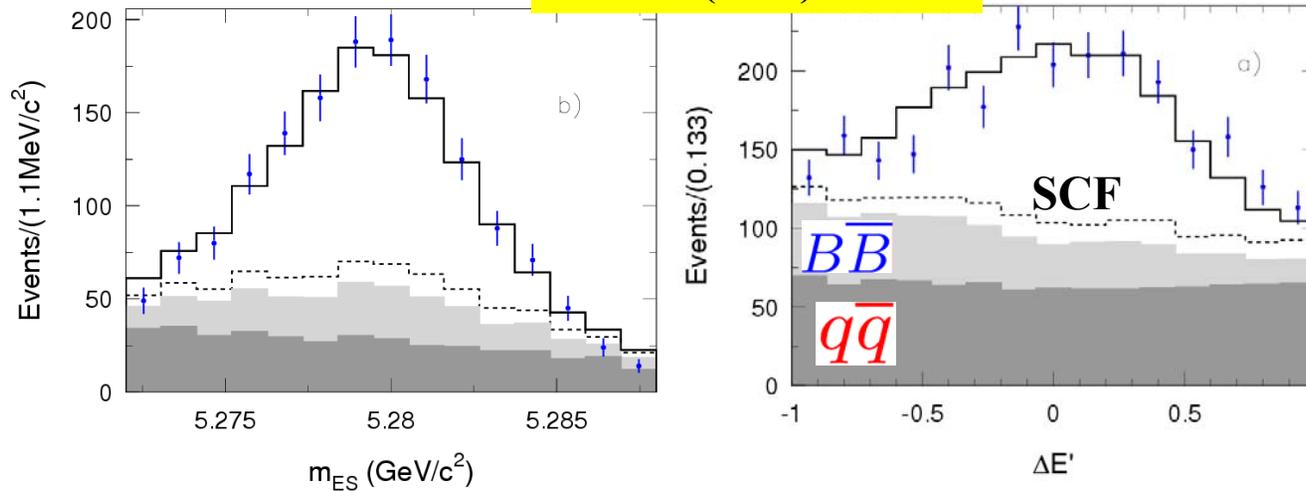
- $B$ -backgrounds mainly from:
  - ❑ Charmed  $B$  decays, such as  $B^0 \rightarrow D^-(\rightarrow \pi^-\pi^0)\pi^+$
  - ❑ Three-body final state ( $K^+\pi^-\pi^0$ ) and its Q2B decays



# Signal Yield



PRD 76 (2007) 012004



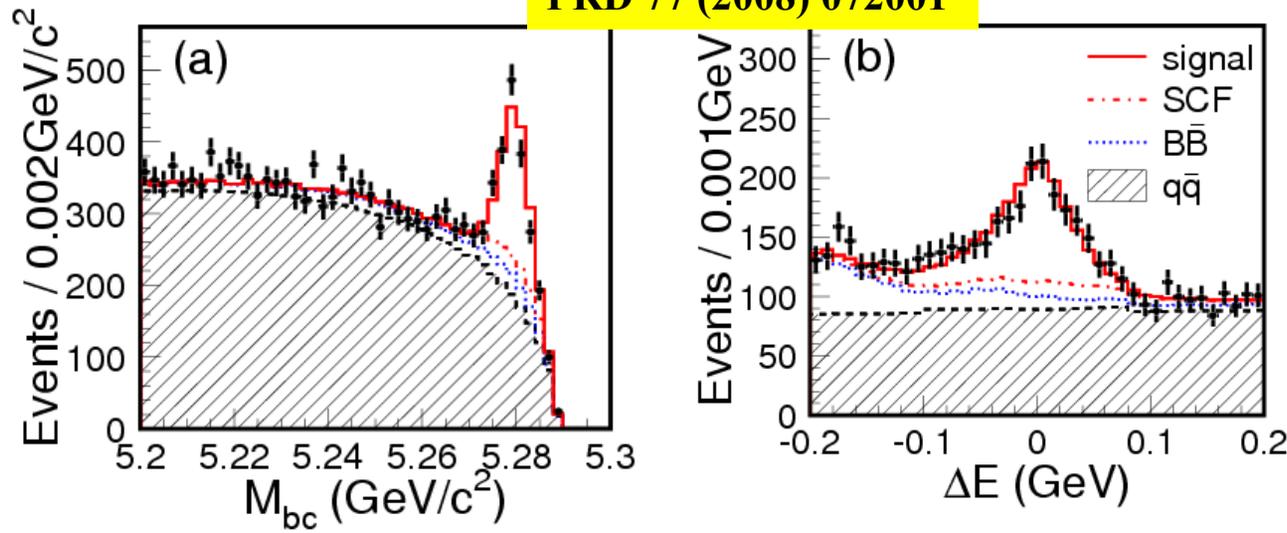
BABAR

$$N_{B\bar{B}} = 375 \times 10^6$$

$$N_{3\pi} = 2067 \pm 86$$

- $\Delta E \rightarrow \Delta E'$  (remove dependence on the  $\pi^0$  momentum)
- NN is a part of the ML fit

PRD 77 (2008) 072001



Belle

$$N_{B\bar{B}} = 449 \times 10^6$$

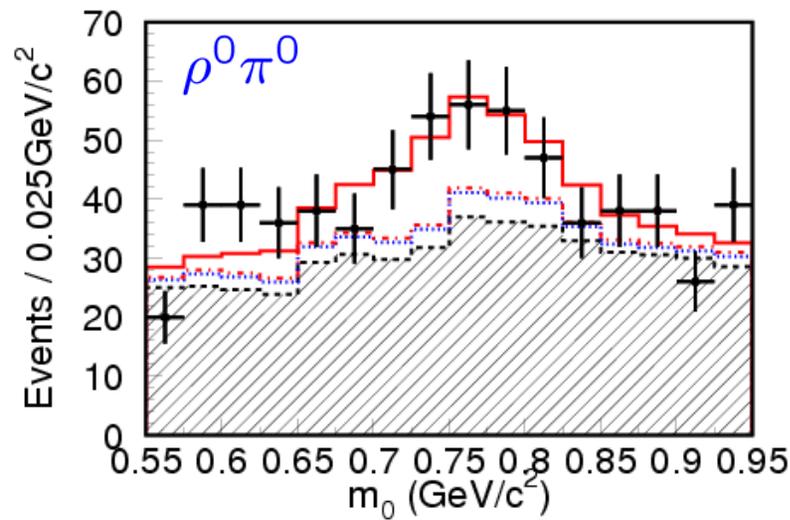
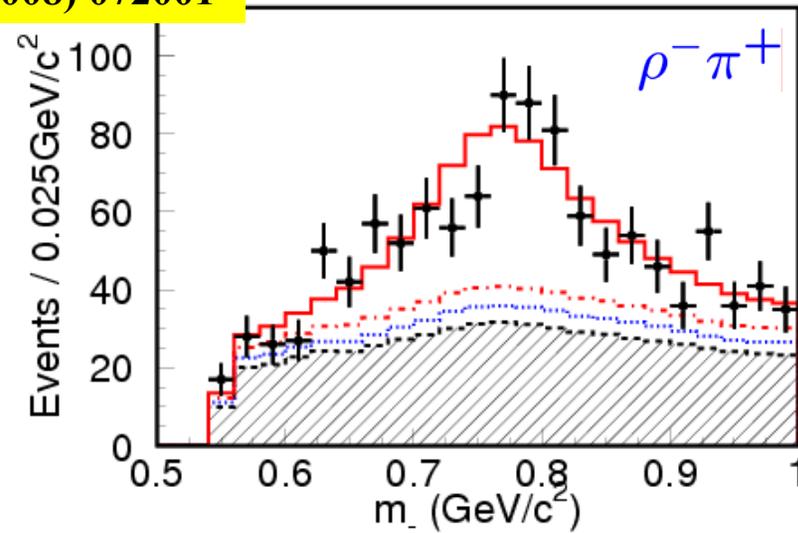
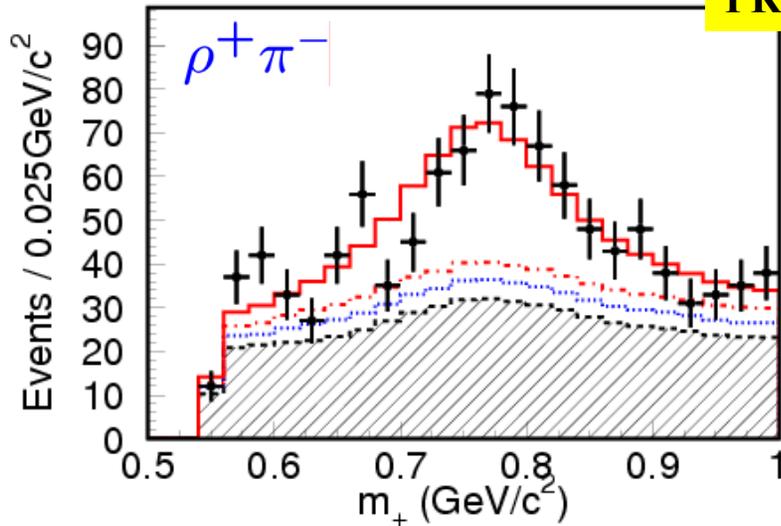
$$N_{3\pi} = 971 \pm 42$$

- Cut on LR and  $(M_{bc}, \Delta E)$  in the ML fit

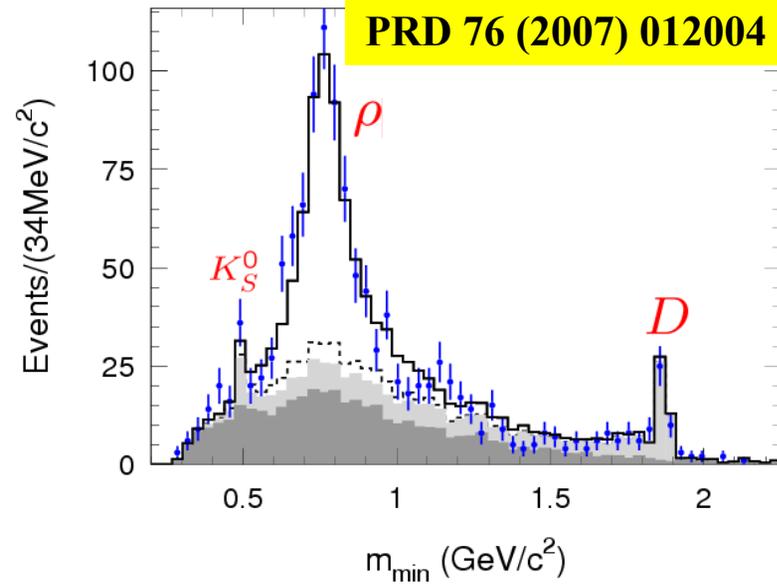


# Mass Distributions

PRD 77 (2008) 072001



PRD 76 (2007) 012004





# Fit Results



□ Overall normalization fixed  $[U_+^+ = 1.0]$

□ Excellent agreement between two expts:  
 $\chi^2=19.0$  for 26 dof

**From HFAG**

□ We translate these seemingly complex bilinear coefficients to Q2B parameters

➤ Easy to interpret

Parameter	BABAR	Belle
$U_+^+$	$+1.32 \pm 0.12 \pm 0.05$	$+1.27 \pm 0.13 \pm 0.09$
$U_0^+$	$+0.28 \pm 0.07 \pm 0.04$	$+0.29 \pm 0.05 \pm 0.04$
$U_+^-$	$+0.54 \pm 0.15 \pm 0.05$	$+0.23 \pm 0.15 \pm 0.07$
$U_-^-$	$-0.32 \pm 0.14 \pm 0.05$	$-0.62 \pm 0.16 \pm 0.08$
$U_0^-$	$-0.03 \pm 0.11 \pm 0.09$	$+0.15 \pm 0.11 \pm 0.08$
$I_+$	$-0.02 \pm 0.10 \pm 0.03$	$-0.01 \pm 0.11 \pm 0.04$
$I_-$	$-0.01 \pm 0.10 \pm 0.02$	$+0.09 \pm 0.10 \pm 0.04$
$I_0$	$+0.01 \pm 0.06 \pm 0.01$	$+0.02 \pm 0.09 \pm 0.05$
$U_{+-}^{+,Re}$	$+0.17 \pm 0.49 \pm 0.31$	$+0.49 \pm 0.86 \pm 0.52$
$U_{+-}^{+,Im}$	$-0.07 \pm 0.71 \pm 0.73$	$+1.18 \pm 0.86 \pm 0.34$
$U_{+-}^{-,Re}$	$+2.23 \pm 1.00 \pm 0.43$	$-1.18 \pm 1.61 \pm 0.72$
$U_{+-}^{-,Im}$	$-0.38 \pm 1.06 \pm 0.36$	$-2.32 \pm 1.74 \pm 0.91$
$U_{+0}^{+,Re}$	$-1.08 \pm 0.48 \pm 0.20$	$+0.29 \pm 0.50 \pm 0.35$
$U_{+0}^{+,Im}$	$-0.16 \pm 0.57 \pm 0.14$	$-0.57 \pm 0.35 \pm 0.51$
$U_{+0}^{-,Re}$	$-0.18 \pm 0.88 \pm 0.35$	$-2.37 \pm 1.36 \pm 0.60$
$U_{+0}^{-,Im}$	$-1.66 \pm 0.94 \pm 0.25$	$-0.41 \pm 1.00 \pm 0.47$
$U_{-0}^{+,Re}$	$-0.36 \pm 0.38 \pm 0.08$	$+0.25 \pm 0.60 \pm 0.33$
$U_{-0}^{+,Im}$	$-0.17 \pm 0.50 \pm 0.23$	$-1.34 \pm 0.60 \pm 0.47$
$U_{-0}^{-,Re}$	$-0.63 \pm 0.72 \pm 0.32$	$-0.53 \pm 1.44 \pm 0.65$
$U_{-0}^{-,Im}$	$+0.12 \pm 0.75 \pm 0.22$	$-0.02 \pm 1.31 \pm 0.83$
$I_{+-}^{Re}$	$+1.90 \pm 2.03 \pm 0.65$	$+1.21 \pm 2.59 \pm 0.98$
$I_{+-}^{Im}$	$-1.99 \pm 1.25 \pm 0.34$	$-1.93 \pm 2.39 \pm 0.89$
$I_{+0}^{Re}$	$+0.41 \pm 1.30 \pm 0.41$	$+1.15 \pm 2.26 \pm 0.92$
$I_{+0}^{Im}$	$-0.21 \pm 1.06 \pm 0.25$	$-0.40 \pm 1.86 \pm 0.85$
$I_{-0}^{Re}$	$+0.41 \pm 1.30 \pm 0.21$	$-0.92 \pm 1.34 \pm 0.80$
$I_{-0}^{Im}$	$+1.23 \pm 1.07 \pm 0.29$	$-2.03 \pm 1.62 \pm 0.81$



# Q2B Parameters

- Time- and flavor-integrated  $CP$  asymmetry:

$$A_{\rho\pi}^{CP} = \frac{U_+^+ - U_-^+}{U_+^+ + U_-^+}$$

- Flavor-dependent direct  $CP$  violation (cos term):

$$C = \frac{1}{2} \left( \frac{U_+^-}{U_+^+} + \frac{U_-^-}{U_-^+} \right)$$

- Mixing-induced indirect  $CP$  violation (sine term):

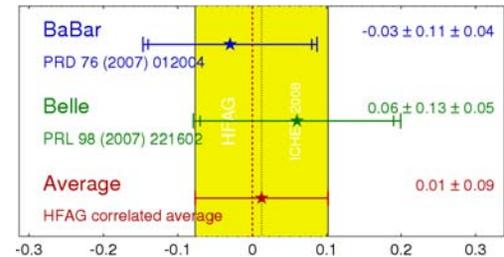
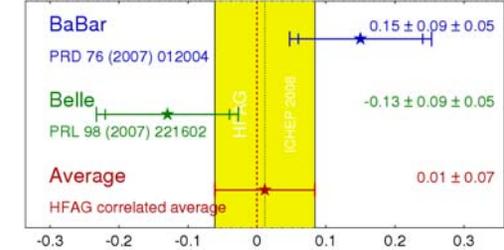
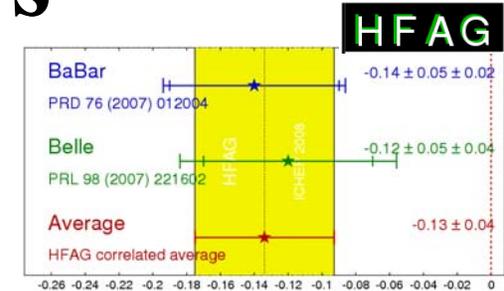
$$S = \left( \frac{I_+}{U_+^+} + \frac{I_-}{U_-^+} \right)$$

- $CP$ -conserving part of cos and sine terms:

$$\Delta C = \frac{1}{2} \left( \frac{U_+^-}{U_+^+} - \frac{U_-^-}{U_-^+} \right)$$

$$\Delta S = \left( \frac{I_+}{U_+^+} - \frac{I_-}{U_-^+} \right)$$

- Q2B parameters for the  $\rho^0\pi^0$  mode also obtained



BABAR:  $+0.39 \pm 0.09 \pm 0.09$

Belle:  $+0.36 \pm 0.10 \pm 0.05$

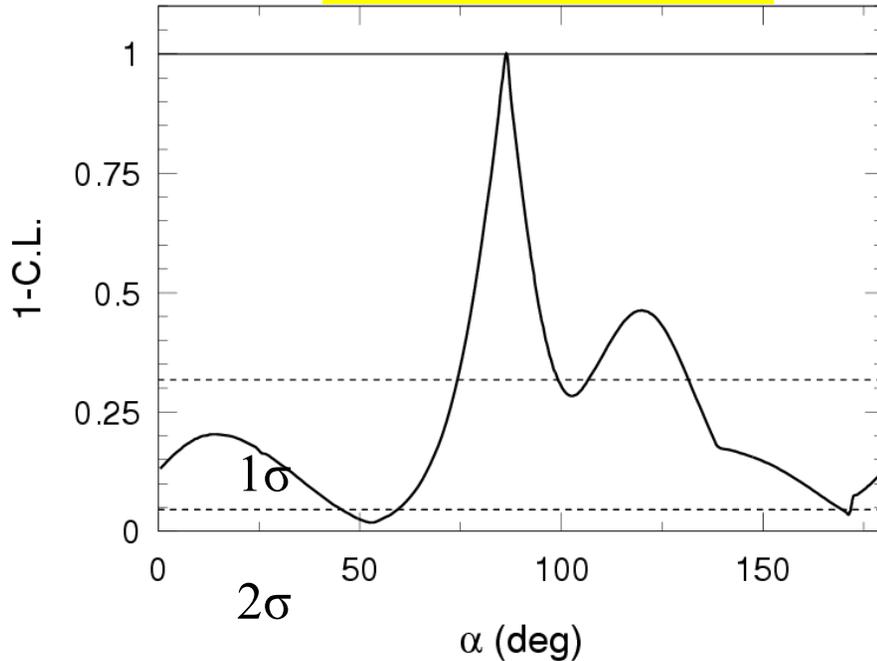
BABAR:  $-0.01 \pm 0.14 \pm 0.06$

Belle:  $-0.08 \pm 0.13 \pm 0.05$



# Constraint on Angle $\alpha$

PRD 76 (2007) 012004



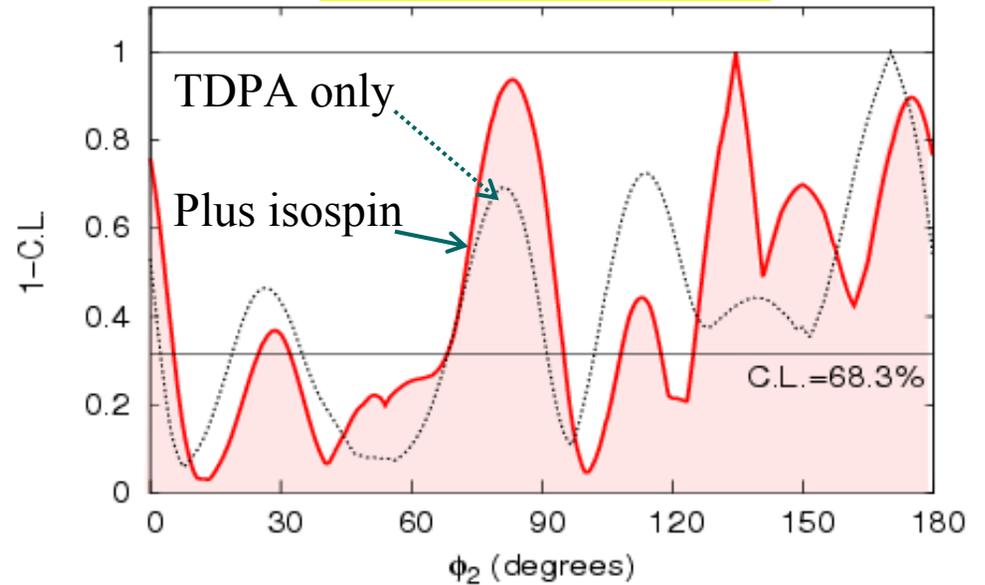
BABAR measures:

$$\alpha = (87^{+45}_{-13})^\circ$$

$$\delta = (37 \pm 37)^\circ$$

$$\delta = \arg(A^{-*}A^+)$$

PRD 77 (2008) 072001



For Belle:

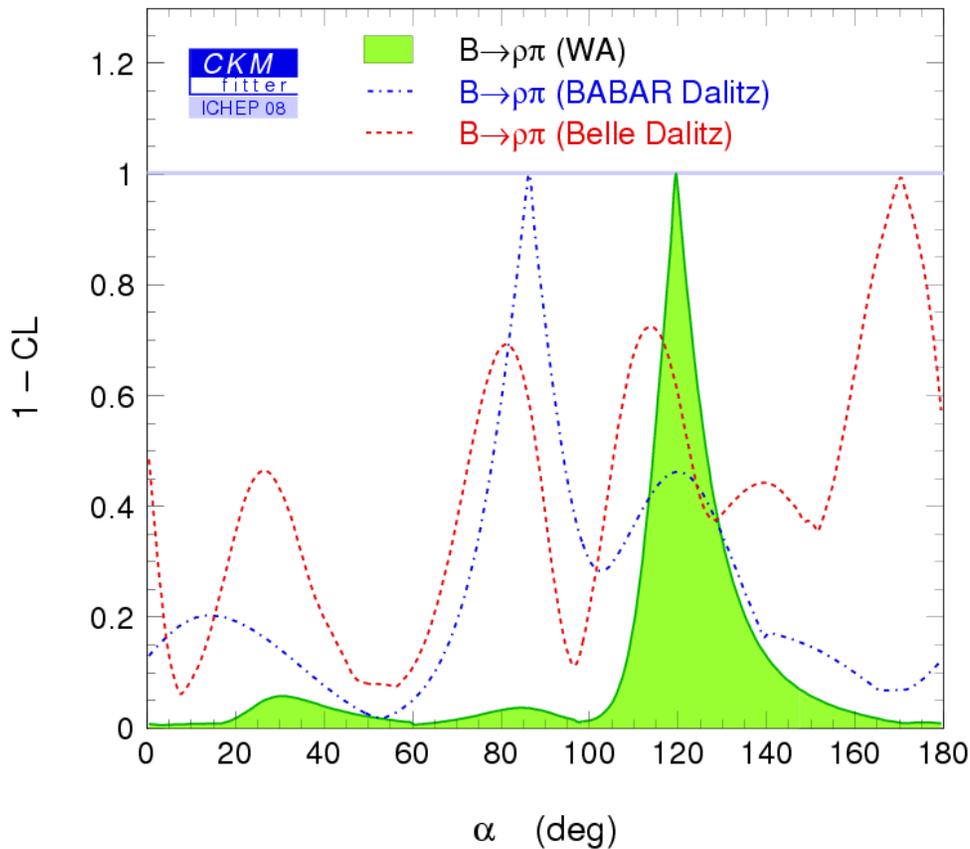
$$\square \quad 68^\circ < \phi_2 < 95^\circ \text{ at } 68.3\% \text{ C.L.}$$

$$\square \quad \text{Using BF and } A_{CP} \text{ values of } B^+ \rightarrow \rho^0 \pi^+ \text{ and } \rho^+ \pi^0$$



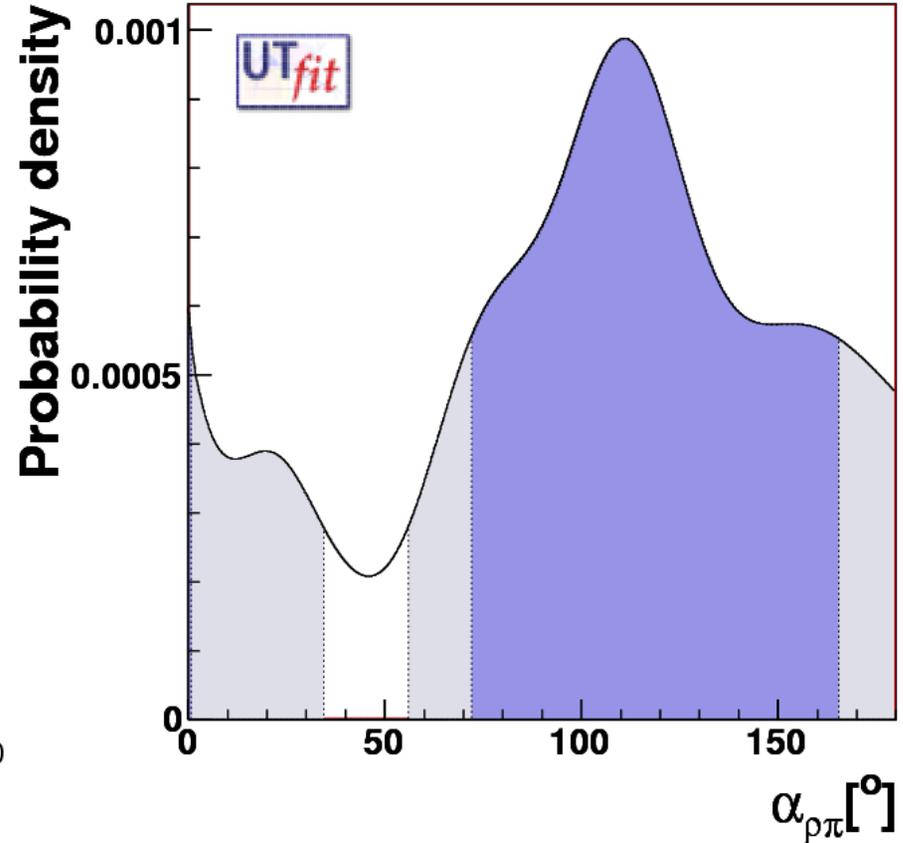
# Global Picture

➤ Two statistical (frequentist vs. Bayesian) interpretations agree quite well



CKMfitter Group (J. Charles et al.)  
Eur. Phys. J C41 (2005) 1-131

See, <http://ckmfitter.in2p3.fr>



UTFit Collab. (M. Ciuchini et al.)  
JHEP 0107 (2001) 013

See, <http://www.utfit.org>



# Conclusions and Outlook

- Time-dependent Dalitz plot analysis performed by both BABAR and Belle
  - Model  $\rho$  mesons in an isobar approach
  - Interference effect correctly modeled
  - Extract strong and weak phases without any ambiguity
- Precision limited due to statistics at present
  - Look forward to updated results from both expts ( $\sim 70\%$  more  $N_{B\bar{B}}$ )
- Charged mode ( $B^+ \rightarrow \pi^+ \pi^+ \pi^-$ ) would help to reduce model uncertainties
- Ignoring mirror solution
  - $\alpha$  is close to  $90^\circ$  (almost no constraint at  $2\sigma$ )
- LHCb is projected to give a competitive limit (about  $7^\circ$  in  $2 fb^{-1}$ )
- Super flavor factory would really pin it down

LHCb-2007-046



# Appendix



# Event Selection

- Track selection and  $\pi^0$  reconstruction
  - ❑ Interaction point, track momentum, and particle ID
  - ❑ Photon energy,  $\pi^0$  momentum and invariant mass
  
- Background suppression (mostly topology)
  
- Kinematic selection:  $m_{ES}$  and  $\Delta E$ 
  - ❑ Signal region, where TDPA is performed
  - ❑ Sidebands – parameterize background shape
  
- Best  $B$  candidate selection
  - ❑  $\pi^0$  mass (and likelihood ratio – Belle)



# Source of Systematic Error

- Dalitz plot model:
  - toyMC: Generate with alternative models:
    - Nonresonant (uniform) component
    - Scalar  $\pi^+\pi^-$  component
      - » [low mass scalar,  $f_0(980), f_2(1270)$ ]
- $\rho$  lineshape
  - Check relative amplitude assumption
  - Vary mass and width
- B-background
  - Assumption on CP contents
- And more
  - Fit bias (negligible)
  - Parameters other PDF (background Dalitz,  $f_{SCF}$ )

*Relevant for  
interference  
parameters*

*Relevant for  
Q-2b  
parameters*