

# Partial branching fractions and extraction of $|V_{ub}|$ from inclusive semileptonic B decays

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# $|V_{ub}|$ Determination

Limiting factor in CKM precision tests; known much less well than  $|V_{cb}|$

CKM suppressed  $V_{ub} \sim 0.1 \times V_{cb}$  - therefore harder to measure

$V_{ub}$ : @**8%** precision, dominated by theoretical uncertainties

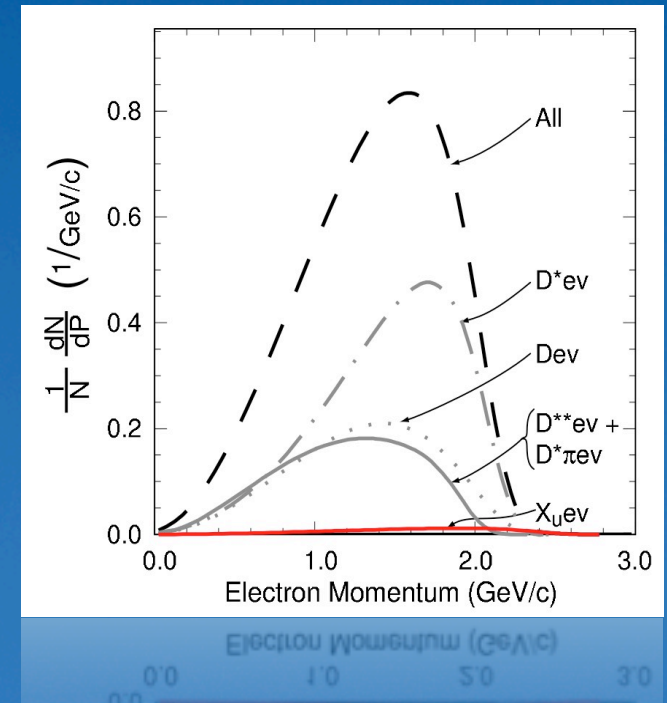
$$\Gamma(b \rightarrow ul\bar{\nu}) = \frac{G_F^2}{192\pi^2} |V_{ub}|^2 m_b^5 \left(1 + \text{補正項}\right)$$

The problem:  $b \rightarrow cl\bar{\nu}$  decay

$$\frac{\Gamma(b \rightarrow ul\bar{\nu})}{\Gamma(b \rightarrow cl\bar{\nu})} \approx \frac{|V_{ub}|^2}{|V_{cb}|^2} \approx \frac{1}{50}$$

How can we suppress 50× larger background?

How can we reach 4% precision on  $|V_{ub}|$ ?



# $|V_{ub}|$ Measurement

- Cut away  $b \rightarrow clv$  Lose a part of the  $b \rightarrow ulv$  signal

- We measure

$$\Gamma(B \rightarrow X_u \ell \nu) \times f_C = |V_{ub}|^2 \zeta_C$$

Total  $b \rightarrow ulv$  rate

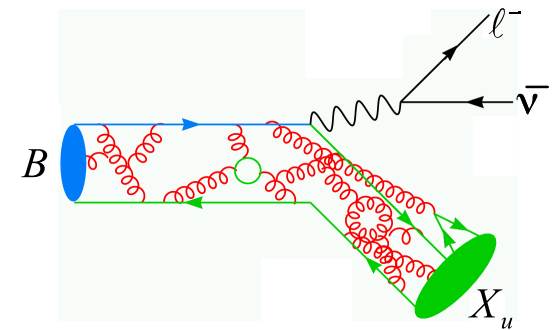
Fraction of the signal that pass the cut

Requires the knowledge of the  $b$  quark's motion inside the  $B$  meson

Cut-dependent constant predicted by theory

- Must be corrected for QCD

$$\Gamma(B \rightarrow X_u \ell \nu) = \frac{G_F^2 |V_{ub}|^2 m_b^5}{192\pi^3} \left[ 1 - \mathcal{O}\left(\frac{\alpha_s}{\pi}\right) - \frac{9\lambda_2 - \lambda_1}{2m_b^2} + \dots \right]$$



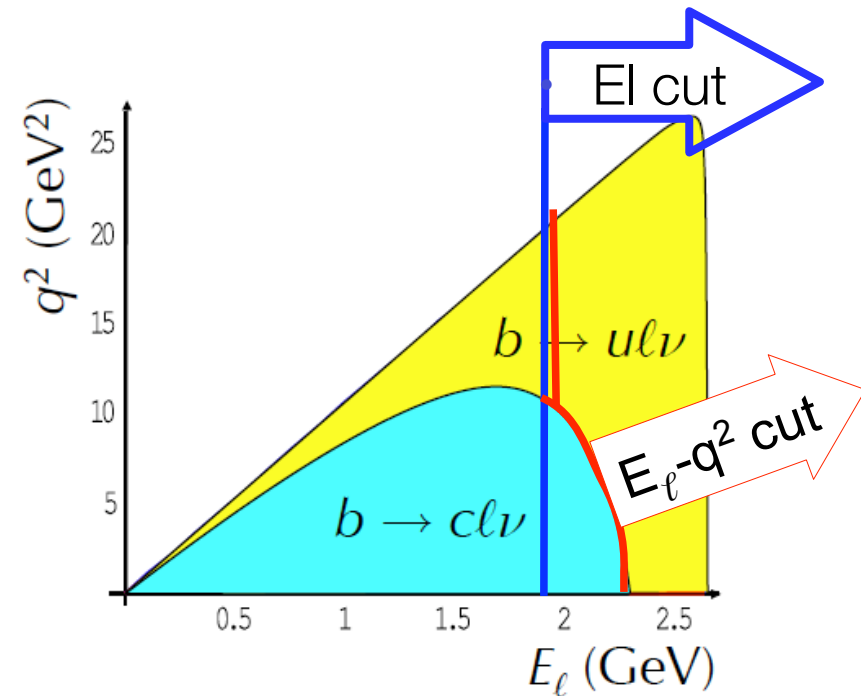
- Main uncertainty ( $\pm 5\%$ ) from  $m_b^5 \rightarrow \pm 2.5\%$  on  $|V_{ub}|$ , correlated between all measurements/experiments!

- But we need the **reasonable fraction** (e.g.,  $E_\ell > 2$  GeV) of the rate.

# Detecting $b \rightarrow ul\nu$

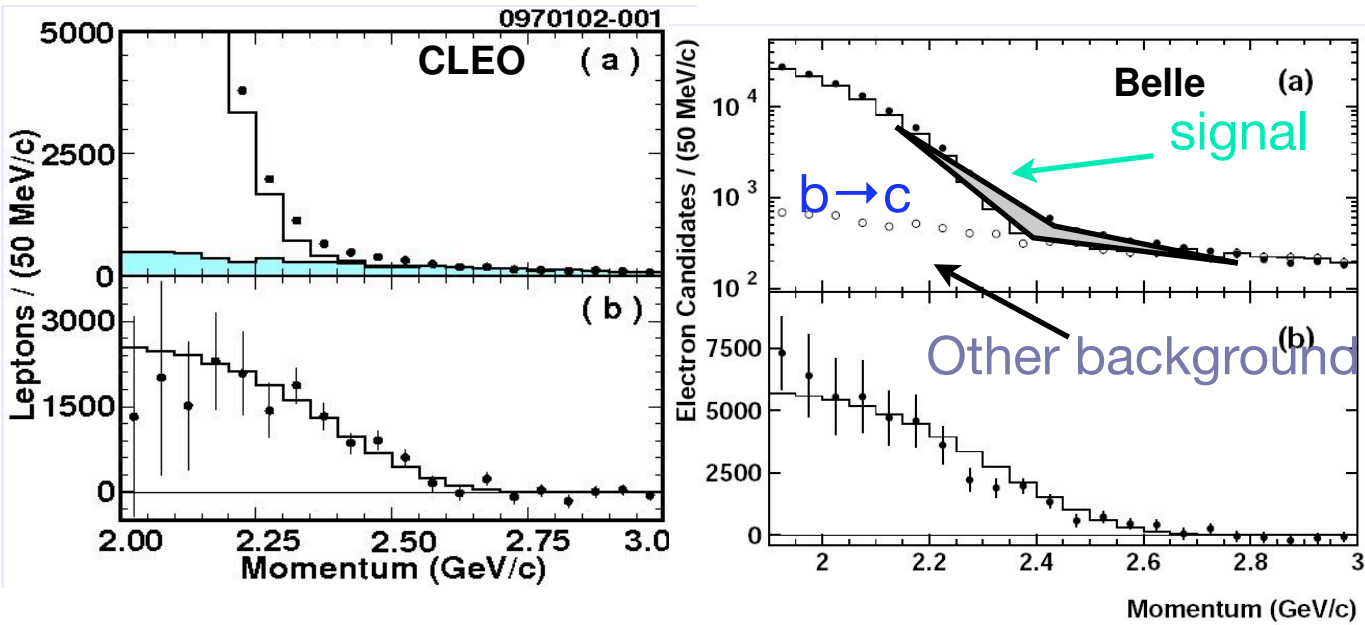
**Inclusive:** Use  $m_u \ll m_c$  difference in kinematics

- Maximum lepton energy **2.64** vs. **2.31** GeV
- First observations (1990) used this technique
- Only 6% of signal accessible
- Small theory error requires low  $E_{\text{lepton}}$  cut
- **Small BG uncertainty requires high  $E_{\text{lepton}}$  cut**
- Measure partial BR in a region where S/N is acceptable and that the width is reliably calculable.



- Many techniques used:
- Endpoint, Improved Endpoint, Simulated Annealing, SF factorisation, Full Reconstruction tagging etc.

# Endpoint method



Subtract offpeak data scaled to onpeak luminosity bin-by-bin.

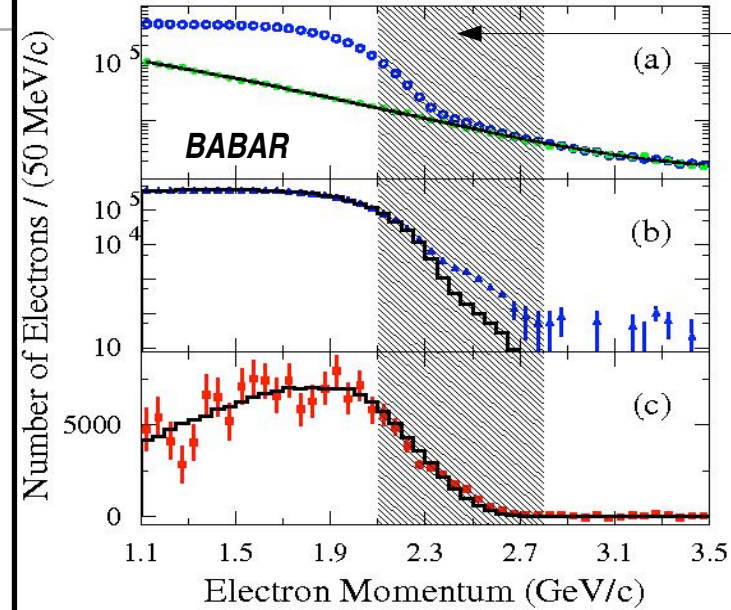
Fit MC to data in low energy region to constrain  $B \rightarrow X_c l \nu$  from data.

$B \rightarrow X_u l \nu$ ,  $B \rightarrow D l \nu + B \rightarrow D^* l \nu$  (ratio fixed)

$B \rightarrow X_u l \nu$ ,  $B \rightarrow D l \nu + B \rightarrow D^* l \nu$  ( $D/D^*$  fixed)

$B \rightarrow D^{**} l \nu$ ,  $B \rightarrow D^{(*)} \pi l \nu$  (Goity & Roberts)

$B \rightarrow D^{**} l \nu$   $D^{**}/D + D^*$  fitted ( $(D_1 + D_2)/D^{**}$  fixed)



Simultaneous fit for non- $B\bar{B}$ ,  $B \rightarrow X_u l \nu$ ,  $B \rightarrow D l \nu$

$B \rightarrow D^* l \nu$ ,  $B \rightarrow D^{**} l \nu$ ,  $B \rightarrow D^{(*)} \pi l \nu$ , other BG

		$\Delta BR \times 10^{-4}$	$ V_{ub}  \times 10^{-3}$ % $\Delta$ (exp -the. + the.)
(PRL 88, 231803, 2002)	Belle $27\text{fb}^{-1}: E_e > 1.9 \text{ GeV}$	$8.47 \pm 0.37_{\text{stat}} \pm 1.53_{\text{sys}}$	$4.61(\pm 9.3 + 5.0 - 6.7)$
(PLB621, 28, 2005)	BaBar: $E_e > 2.0 \text{ GeV}$	$5.72 \pm 0.41_{\text{(stat)}} \pm 0.65_{\text{(syst)}}$	$4.13(\pm 5.6 + 5.6 - 8.2)$
((PRD 73, 012006, 2006)	CLEO: $E_e > 2.0 \text{ GeV}$	$4.22 \pm 0.33_{\text{stat}} \pm 1.78_{\text{sys}}$	$3.77(\pm 12. + 6.9 - 10.)$

CKM Workthop, Rome Sept 2008

Phillip Urquijo

~25 % acceptance

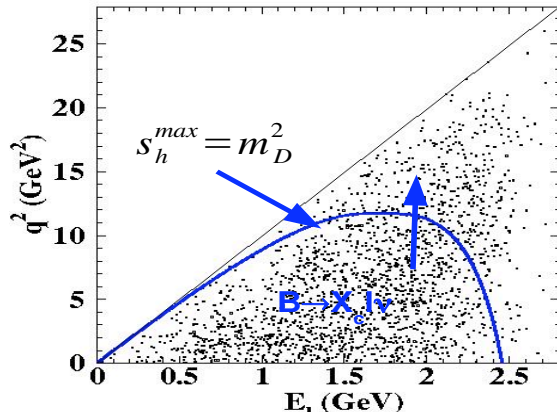


# Improved Endpoint method

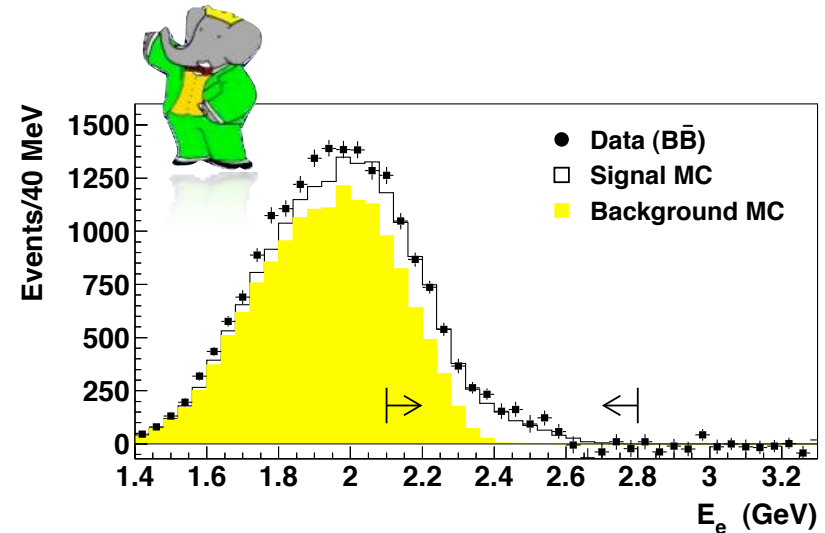
Maximally allowed hadronic mass for given  $E_l$  &  $q^2$  can be determined:

$$s_h^{\max} = m_B^2 + q^2 - 2m_B(E_l \eta_- + q^2 \eta_+ / 4 E_e), \quad \pm 2 E_e > \pm \sqrt{q^2} \eta_{\pm} \quad \eta_{\pm} = \sqrt{(1 \pm \beta)/(1 \mp \beta)}$$

$$s_h^{\max} = m_B^2 + q^2 - 2m_B \sqrt{q^2}, \quad \text{otherwise} \quad \beta \approx 0.06$$



BaBar (PRL 95, 111801, 2005  
PRL 97, 019903 (2006) Err.)



## Principal ingredients (BABAR):

1)  $p_\nu = p_{miss} = (E_{miss}, \vec{p}_{miss}) \rightarrow (|\vec{p}_{miss}|, \vec{p}_{miss})$

## 2) \* track & neutral selection

\* Only one high energetic lepton

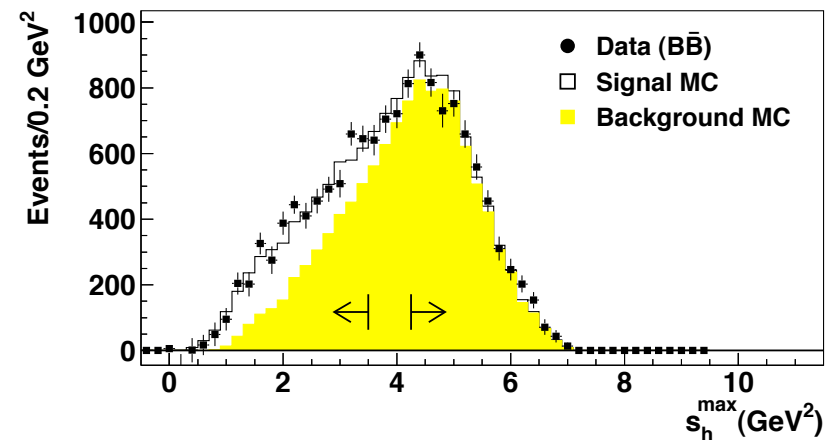
\*  $|\vec{p}_{miss}|, E_{miss} - |\vec{p}_{miss}|, \cos \theta_{miss}, \cos \theta_{thrust, e}$

## 3) Signal region: $E_l^*$ & $s_h^{\max} \Rightarrow B \rightarrow X_c l \nu$ suppression

core  $|\vec{p}_{miss}|/q^2$  - resolution: 0.32 GeV/2.5 GeV<sup>2</sup>

\* dominated by particle losses

\* complicated by  $K_L$ , split-offs, etc.



# Summary of Endpoint methods

$\Delta BR$

Errors in %

Method		EI cut	Integrated Luminosities (fb-1)		Uncertainties on BF (%)			
			onpeak	offpeak	EI > 2.1 GeV		EI > 2.3 GeV	
					Stat	Sys	Stat	Sys
<b>EI</b>	CLEO (PRL 88, 231803, 2002)	2.0	9.1	4.3	7.0	22.3	7.0	9.1
	Belle (PLB621, 28, 2005)	1.9	27	8.8	5.3	12.7	8.5	5.9
	BaBar (PRD 73, 012006, 2006)	2.1	80	9.5	5.7	9.4	4.1	6.9
<b>EI-q2</b>	BaBar (PRL 95, 111801, 2005 PRL 97, 019903 (2006) Err.)	2.0	81	9.6	9.3 (>2.0 GeV)	9.6 (>2.0 GeV)		

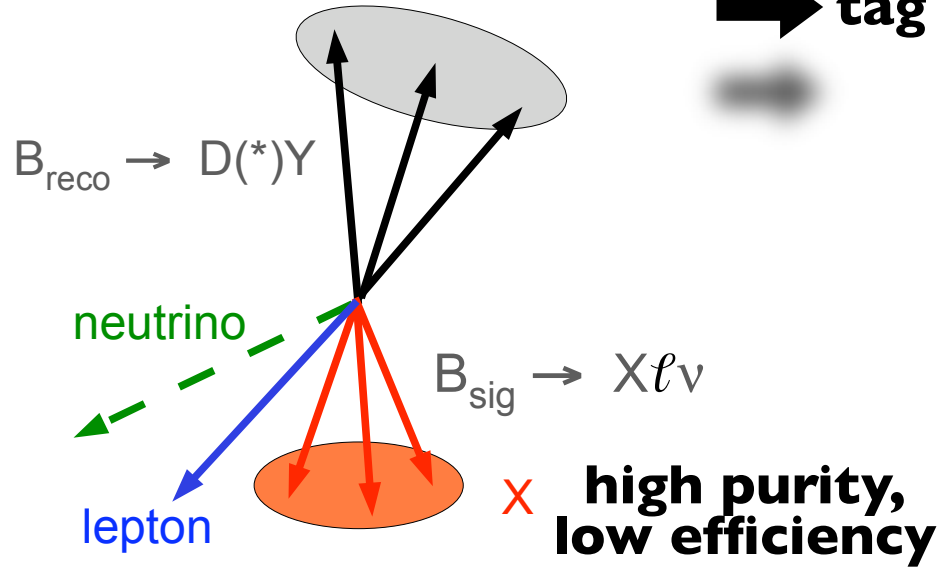
Systematics	Select	non-BB	FSR/Brem	KL	Neutral	B → Xu l v	D → Xs l nu		B → cl v	
							D → e, mu	D → KL	FF	Excl BR
<b>EI</b>	6.8	2.4	1.0	-	1.1	<0.5	-	2.4	2.8	
<b>EI-q2</b>	-	-	3.8	2.0	3.4	4.4	2.1	4.5	0.3	2.0

- ▶ Current data sets from Belle and BaBar have low offpeak/onpeak ratios.
- ▶ Prospect for stat. error <2.5% by relaxing continuum suppression techniques.
- ▶ B → Xc l v systematics have improved significantly over 5 years.

# B meson "beam" method

Best access to kinematics with **B meson "beam"**

➔ **tag - charge - momentum**



$E_l$  = lepton energy (in B rest frame)

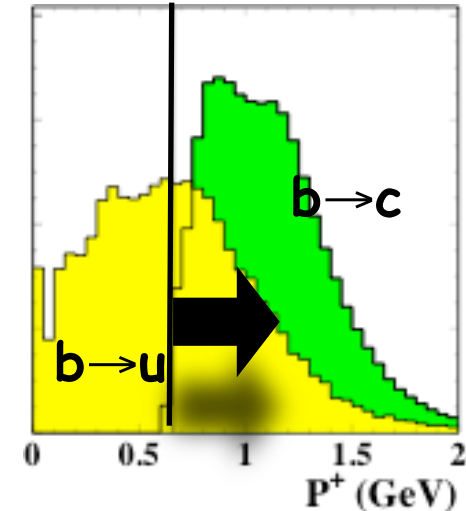
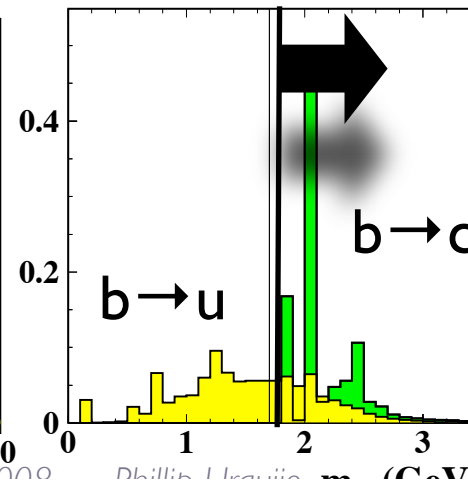
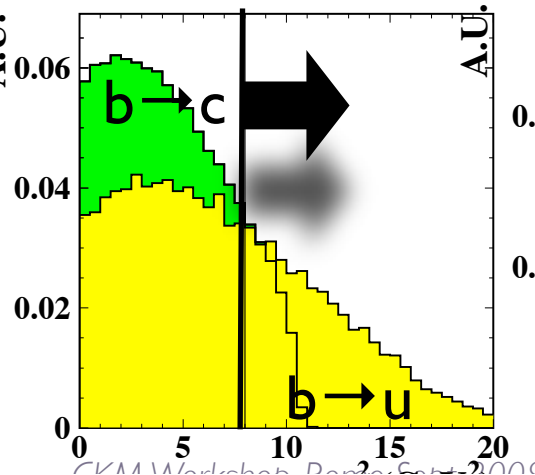
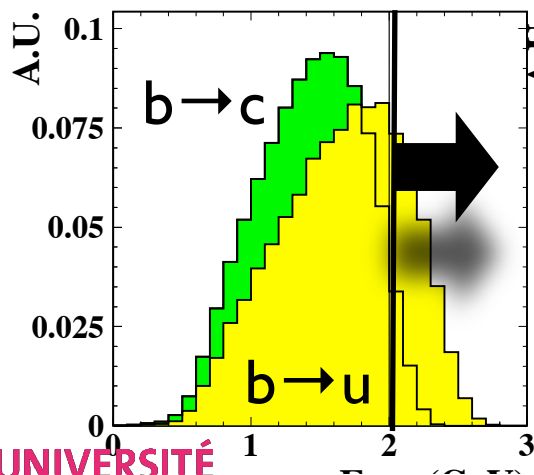
$q^2$  = lepton-neutrino mass squared

$m_X$  = hadron system mass (all remaining particles)

$P^+ = E_X - |P_X|$  ( $P_X = p_{\text{beam}} - p_{\text{Btag}} - p_l - p_\nu$ )

Signal events have smaller  $M_X$  and  $P_+ \rightarrow$  Larger  $E_l$  and  $q^2$

Not to scale!





# Measurement technique

## I. Signal side

Reconstruct high momentum lepton

$$p_{\text{lep}}^{\text{CMS}} > 1 \text{ GeV}/c$$

No strangeness

$$N(K^\pm, K^0_S) = 0 \text{ (KL cut used by Belle 2005)}$$

## 2. Event Level

$$\Sigma Q = 0,$$

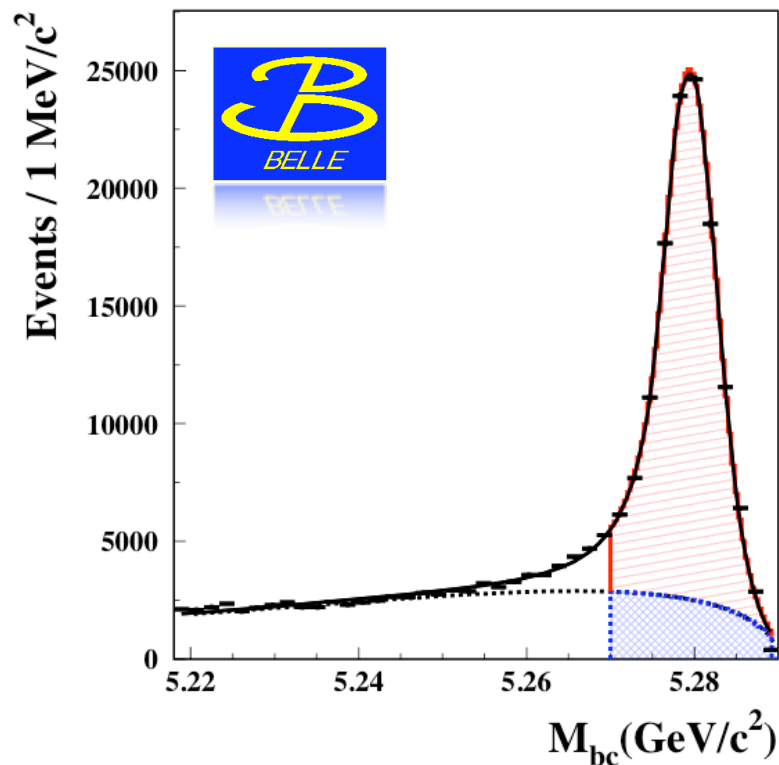
$$Q(B_{\text{reco}}^+) \times Q(\text{lep}) = -1$$

$M_{\text{miss}}$ , etc.

## 3. Fit $M_{bc}$ in bins of $P_+$ , $M_x$ , $q^2$

4. Fit to  $P_+$ ,  $M_x$ ,  $q^2$  with various background and signal floated to determine background yield.

5. Measure relative BR to control systematics



e.g.  
Belle

Number of excess events

Unfolding factor F

PDG

$$\frac{\Delta \text{Br}(X_u 1\nu)}{\text{Br}(X 1\nu)} = \frac{N_{b \rightarrow u}}{N_{sl}} \cdot \frac{F}{\epsilon_{\text{sel}}}$$

$$F = \frac{\epsilon_{\text{frec}}^{b \rightarrow u} \epsilon_l^{b \rightarrow u}}{\epsilon_{\text{frec}}^{sl} \epsilon_l^{sl}}$$

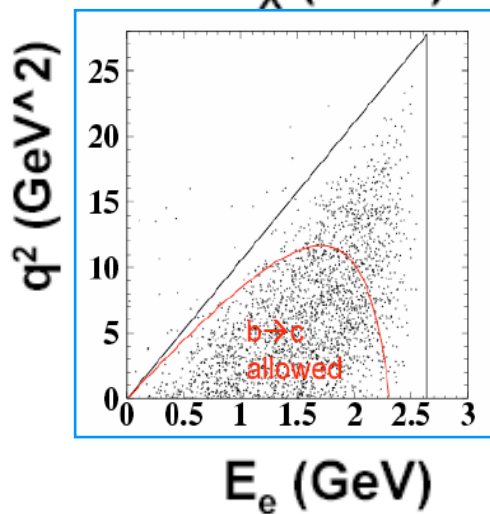
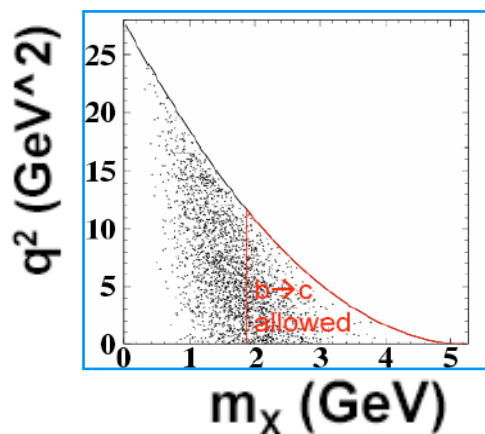
Number of semileptonic events

Ratio of efficiencies for  $b \rightarrow u$  and  $sl$

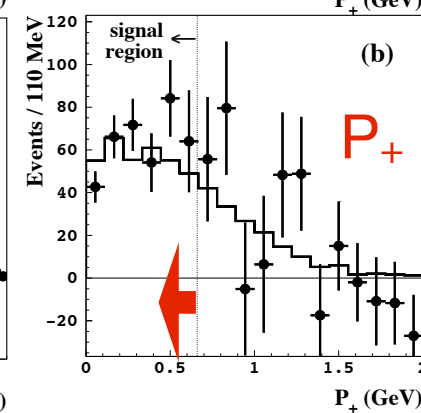
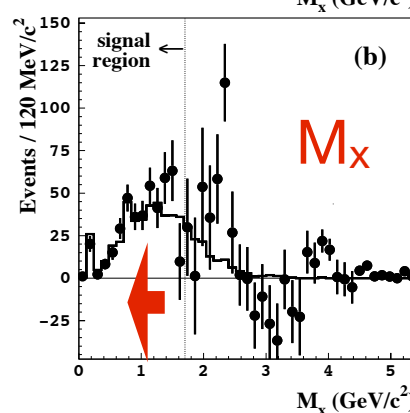
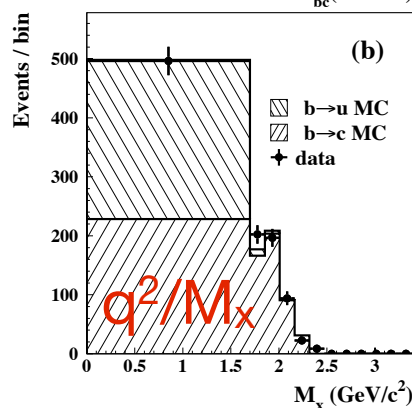
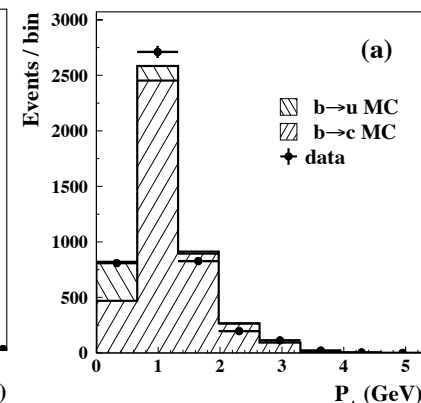
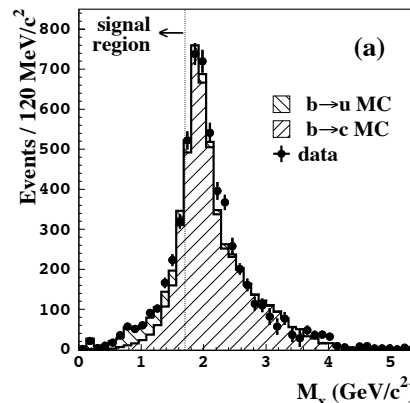
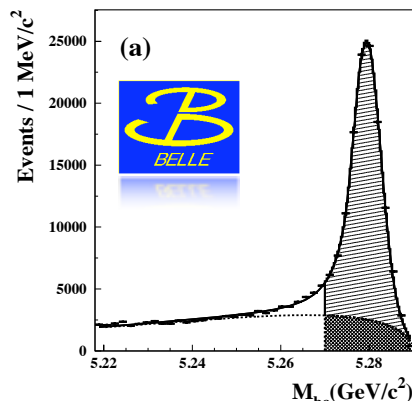
selection efficiency

# Belle tagged method

PRL .95:241801 (2005)



253 fb<sup>-1</sup>



	$ V_{ub}  \times 10^{-3}$ BLNP %Δ( stat. sys. sf. th. )	$\Delta V_{ub} $
$m_x < 1.7$	4.70( $\pm 5.1 \pm 6.0 \pm 4.2 \pm 5.1$ )	10%
$m_x < 1.7, q^2 > 8$	4.09( $\pm 4.6 \pm 4.9 \pm 4.4 \pm 3.7$ )	9%
$P_+ < 0.66$	4.19( $\pm 4.8 \pm 7.2 \pm 5.7 \pm 3.3$ )	11%

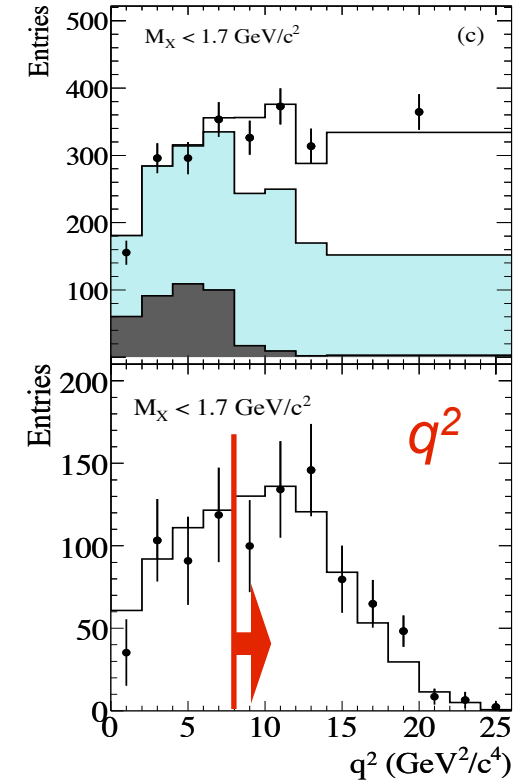
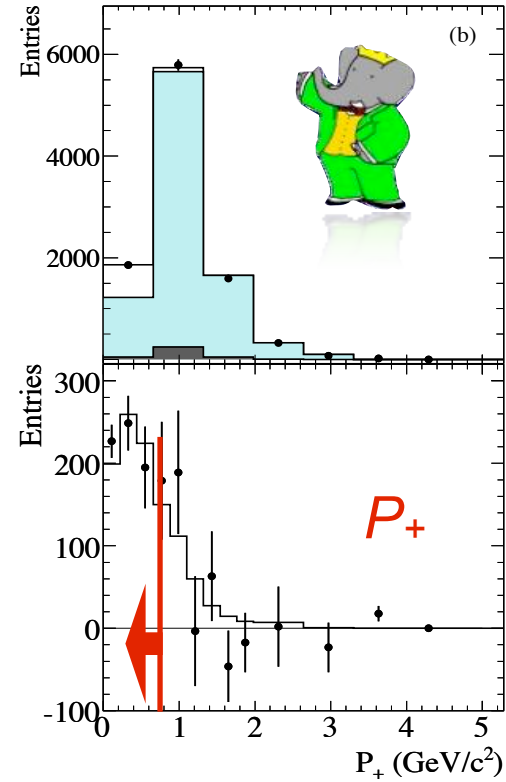
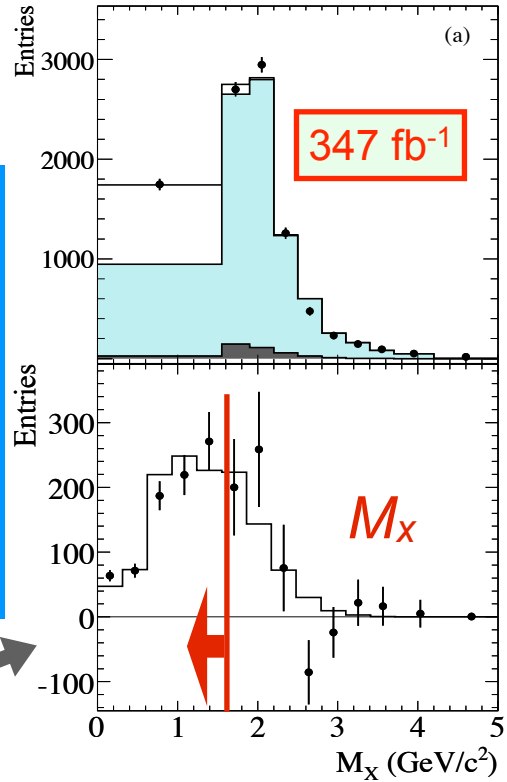
~40-60 % acceptance

# Babar tagged method

PRL 100, 171802 (2008)

- $B \rightarrow X_u l \nu$
- $B \rightarrow X_c l \nu$   
(bkgd)
- $B \rightarrow X_u l \nu$   
(outside selected region)

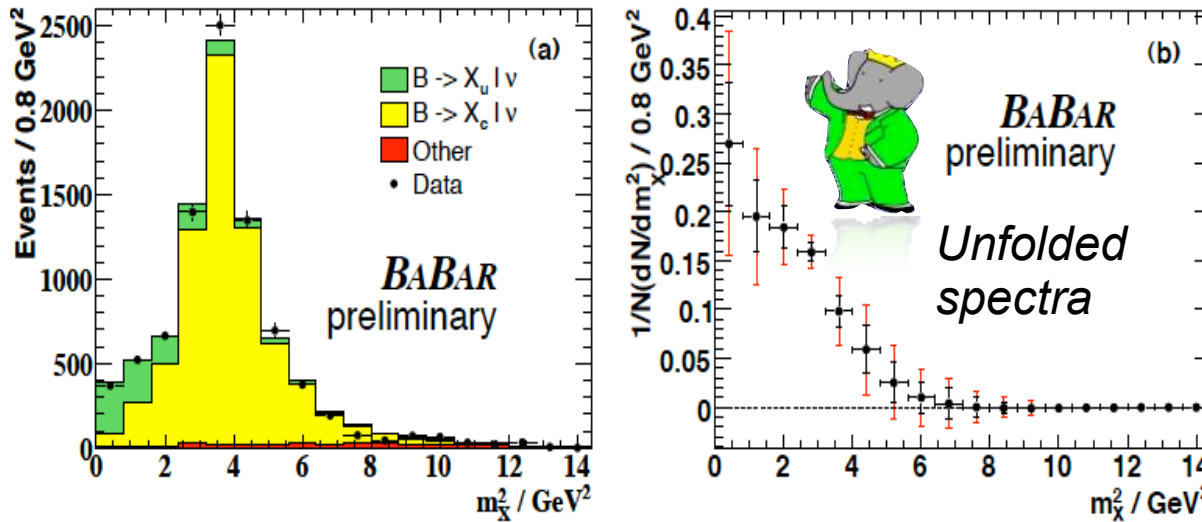
Background subtracted



Kinematic Region	$B(B \rightarrow X_{u/l} \nu) \times 10^{-3}$			$ V_{ub}  (10^{-3})$			Theory
	$\Delta$ ( stat. )	sys. )	th. )	% $\Delta$ ( stat. )	sys. )	th. )	
$M_X < 1.55 \text{ GeV}/c^2$	$1.18 \pm 0.09 \pm 0.07 \pm 0.01$			$4.27 (\pm 3.7 \pm 3.0 \pm 7.0)$			BLNP
				$4.56 (\pm 3.7 \pm 3.0 \pm 7.0)$			DGE
$P_+ < 0.66 \text{ GeV}/c^2$	$0.95 \pm 0.10 \pm 0.08 \pm 0.01$			$3.88 (\pm 4.9 \pm 4.1 \pm 7.2)$			BLNP
				$3.99 (\pm 4.9 \pm 4.1 \pm 6.0)$			DGE
$M_X < 1.7 \text{ GeV}/c^2$ & $q^2 > 8.0 \text{ GeV}^2/c^4$	$0.81 \pm 0.08 \pm 0.07 \pm 0.02$			$4.57 (\pm 5.0 \pm 4.2 \pm 4.6)$			BLNP
				$4.64 (\pm 5.0 \pm 4.2 \pm 5.4)$			DGE
				$4.93 (\pm 5.0 \pm 4.2 \pm 7.3)$			BLL

# Extension: Hadronic mass Moments

Measure hadronic mass spectrum over full  $M_X$  range  
 Mass moments related to  $m_b$ , with  $m_X^2 < 6.4 \text{ GeV}^2$



ArXiv: 0801.2985[hep-ex]

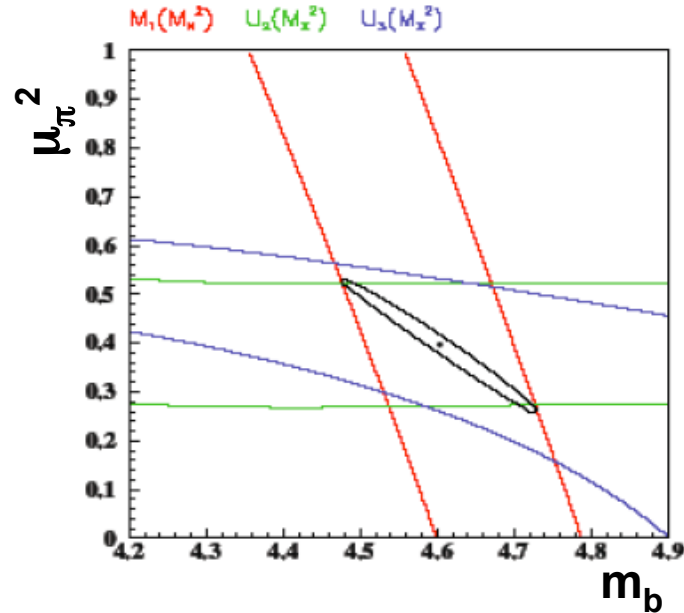
Mom	Stat.	Syst.	
<b>M1</b>	<b>1.96 ± 0.34</b>	<b>± 0.53</b>	<b>GeV<sup>2</sup></b>
<b>U2</b>	<b>1.92 ± 0.59</b>	<b>± 0.87</b>	<b>GeV<sup>4</sup></b>
<b>U3</b>	<b>1.79 ± 0.62</b>	<b>± 0.78</b>	<b>GeV<sup>6</sup></b>

Calculations of Gambino, Ossola, Uraltsev  
 JHEP09(2005)010

*First measurement of  $m_b$  in  $B \rightarrow X_u \ell \nu$  decays (in the Kinetic scheme)*

**$m_b = 4.604 \pm 0.250 \text{ GeV}$**

*compatible with Global Fit*



# Belle Multivariate analysis (NEW @ CKM2008) 1/2

The irreducible uncertainties in the measurements to date are related to limited phase space.

Solution: exploit the many non-linear correlations between kinematic and event variables available in B-beam sample that separate  $b \rightarrow u$  and  $b \rightarrow c$ .

Boosted decision tree based selection, use  $\sim 20$  event parameters from the full reconstruction sample.

**No need to place stringent, hard cuts that result in zero efficiency!**

1. Signal side: Reconstruct high momentum lepton:  $p_{\text{lep}}^{B^*} > 1 \text{ GeV}/c$

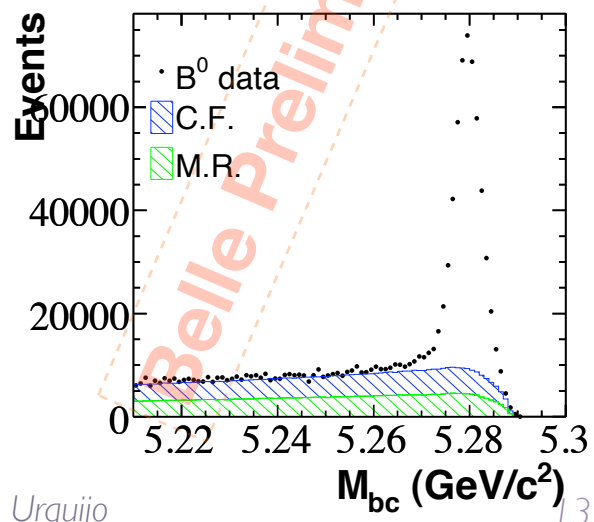
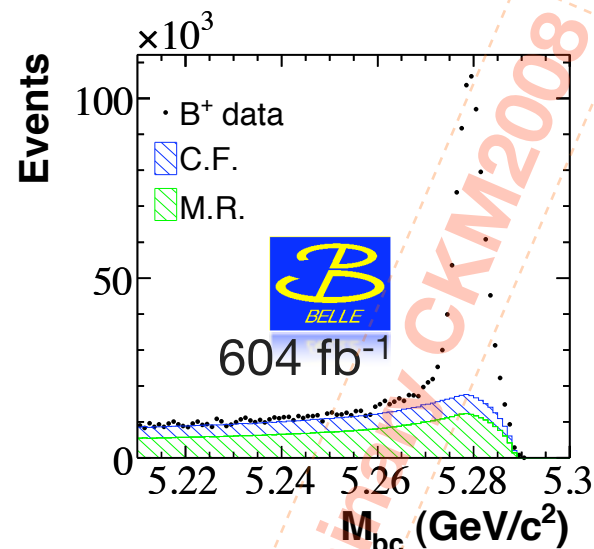
2. Event Level:  $Q(B_{\text{reco}}^+) \times Q(\text{lep}) = -1$

3. BDT cut with many input par's:  $M_{\text{miss}}^2$ ,  $dZ$ ,  $dr$ ,  $Q_{\text{total}}$ ,  $Q_{\text{lepton}}$ ,  $N_{\text{lepton}}$ ,  $Q(B)$ ,  $D^*$  partial reco etc.....

4. Combinatorial estimated from MC, normalisation from sideband region. (same approach as Vcb moments analyses)

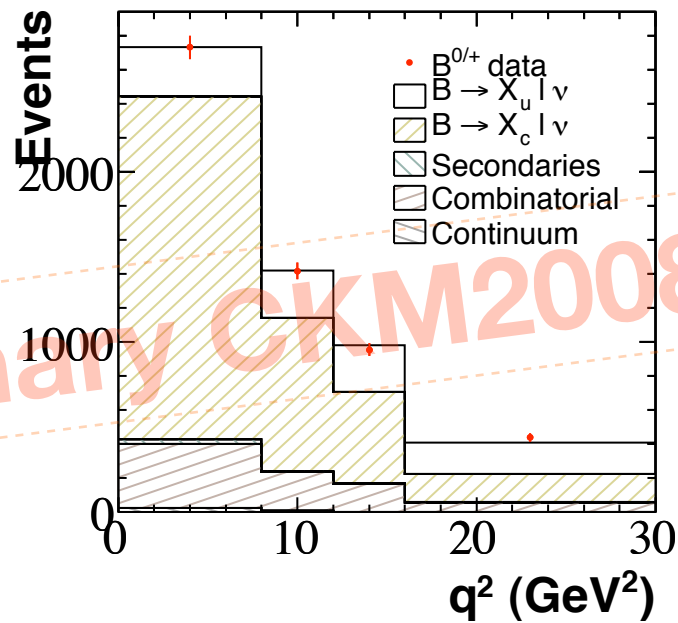
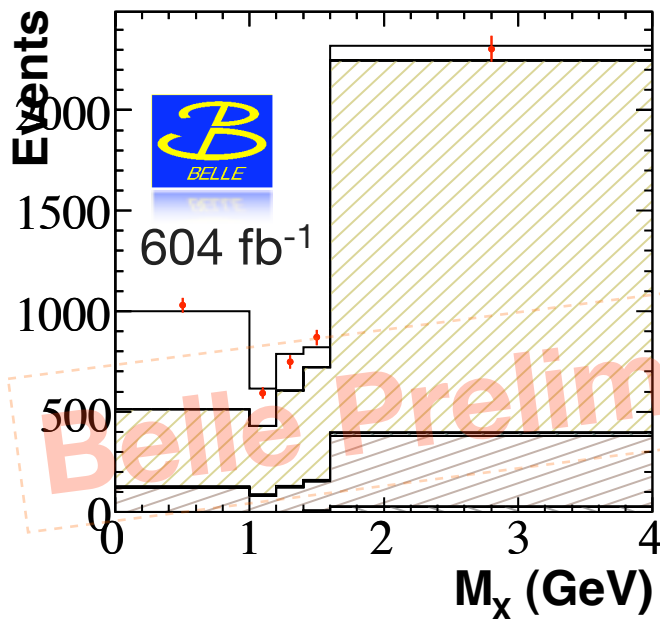
5. 2D fit to  $M_x, q^2$  with backgrounds and signal floated to determine background yield.

6. Measure absolute rate.





# Belle Multivariate analysis (NEW @ CKM2008) 2/2



~1035 Evts

2D fit in  $q^2$   $m_x$ . (projections shown)

Kinematic Region	$B(B \rightarrow X_u l \nu) \times 10^{-3}$		$m_b$	$ V_{ub} $ (10 <sup>-3</sup> ) % error	Theory
	$\Delta$ (stat.)	sys.)			
$P_{lepton} > 1.0$ GeV	1.96 x (1 ± 0.088 ± 0.076)		(kinetic) 4.613 GeV, $m_{upl} = 0.440$ GeV <sup>2</sup>	4.42 (± 3.1 ± 5.1)	GGOU (thanks P. Giordano)
			(MSbar) 4.243 GeV	4.47 (± 6.7)	DGE (thanks E. Gardi)

~90<sup>+</sup> % total phase space, thus theory error less correlated to other  $V_{ub}$  determinations

# Tagged method Uncertainty Breakdown

$\Delta$ BR      Errors in %

		$\Delta$ BR		Errors in %								
		stat	sys.	MC stat	detector/other		B $\rightarrow$ Xu l v			B $\rightarrow$ cl v		
	P <sub>D</sub> >1.0 GeV				Det.	M <sub>bc</sub> /ES	SF	Excl	ss	Inc.	FF	Excl BR
<b>PRL 100, 171802 (2008)</b>	M <sub>X</sub> /q <sup>2</sup>	8.0	7	4.3	3.8	5.2	2.4	2.7	1.0	1.2	0.6	0.8
	M <sub>X</sub>	9.0	7	3.2	1.9	3.7	0.9	2.1	1.6	0.9	0.2	0.4
	P <sub>+</sub>	10.0	8	4.6	3.9	4.0	1.3	2.2	1.5	2.8	0.4	0.7
<b>Phys.Rev.Lett. 95:241801 (2005)</b>	M <sub>X</sub> /q <sup>2</sup>	10.0	8.9		8.9		6.2			5.3		
	M <sub>X</sub>	9.1	7.1		7.1		6.1			2.2		
	P <sub>+</sub>	9.4	9.3		9.3		6.4			8.7		
<b>Belle Preliminary CKM2008</b>	BDT	8.8	7.6		4.8		3.6	4.0	1.5	1.7		

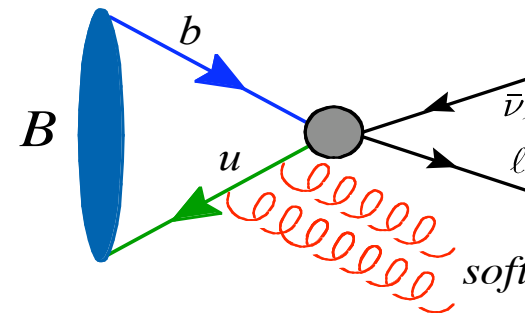
- Detector effects are better understood and no longer dominate.
- Selection often involves complex fitting techniques (m<sub>ES</sub>)
  - more data improves fit convergence in m<sub>ES</sub> method.
  - more data will mean more detail in q<sup>2</sup>/M<sub>X</sub>/P<sub>+</sub> to account for!
- Dominant systematics are in the modelling of signal and background contributions
  - b  $\rightarrow$  u l v (resonances, non-resonant contributions)
  - b  $\rightarrow$  c l v (D, D\*, D\*\* very small)
  - Continuum error large in q<sup>2</sup>/M<sub>X</sub>/P<sub>+</sub> analyses.

KL cut powerful (used in Belle M<sub>X</sub>/P<sub>+</sub>/q<sup>2</sup> analysis) but modelling/understanding needs huge improvements.



# Weak Annihilation

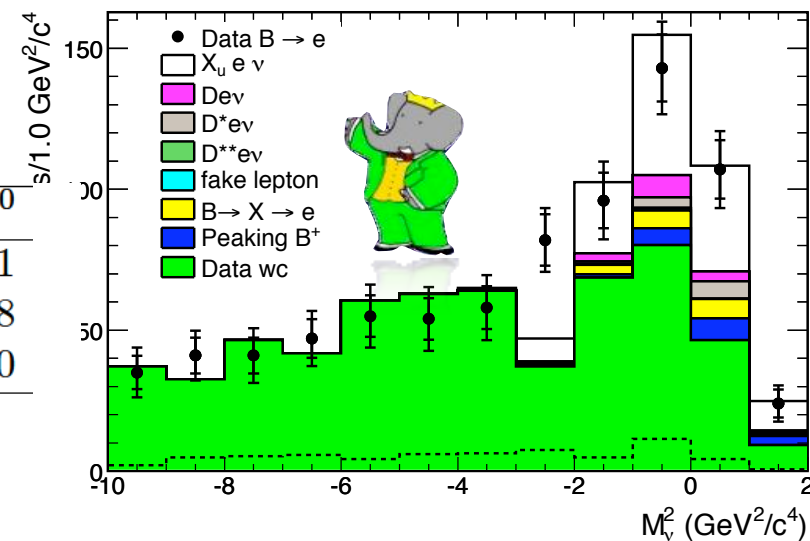
- Small contribution to  $B \rightarrow Xu l \nu$  decays
- Introduces difference between  $B^0$  and  $B^+$  decays.
- Tag with partial reconstructed  $B^0 \rightarrow D^{*+} l \nu$
- Neutrino mass from  $m_\nu^2 = (P_B - P_D - P_l)^2$
- Compare  $B^0$  partial rate to  $B^+$  averaged rate over large  $PI$  region (to enhance the WA contribution) PRD73, 012006 (2006)



$$\frac{|\Gamma_{WA}|}{\Gamma_u} < 7.4\% \text{ at } 90\% C.L. \quad \text{CLEO, studying the } q^2 \text{ spectra} \\ \text{PRL96,121801 (2006)}$$

$\Delta p$	$\Delta\mathcal{B}(B) \cdot 10^4 [8]$	$\Delta\mathcal{B}(B^0) \cdot 10^4$	$A^{+/0}$
2.2 – 2.6 GeV/c	$2.31 \pm 0.10 \pm 0.18$	$2.62 \pm 0.33 \pm 0.16$	$-0.17 \pm 0.15 \pm 0.11$
2.3 – 2.6 GeV/c	$1.46 \pm 0.06 \pm 0.10$	$1.30 \pm 0.21 \pm 0.07$	$0.08 \pm 0.15 \pm 0.08$
2.4 – 2.6 GeV/c	$0.75 \pm 0.04 \pm 0.06$	$0.76 \pm 0.15 \pm 0.05$	$-0.05 \pm 0.20 \pm 0.10$

$$\frac{|\Gamma_{WA}|}{\Gamma_u} < \frac{3.8\%}{f_{WA}(2.3 - 2.6)} \text{ at } 90\% C.L.$$



arXiv: 0708.1753 383 M BB

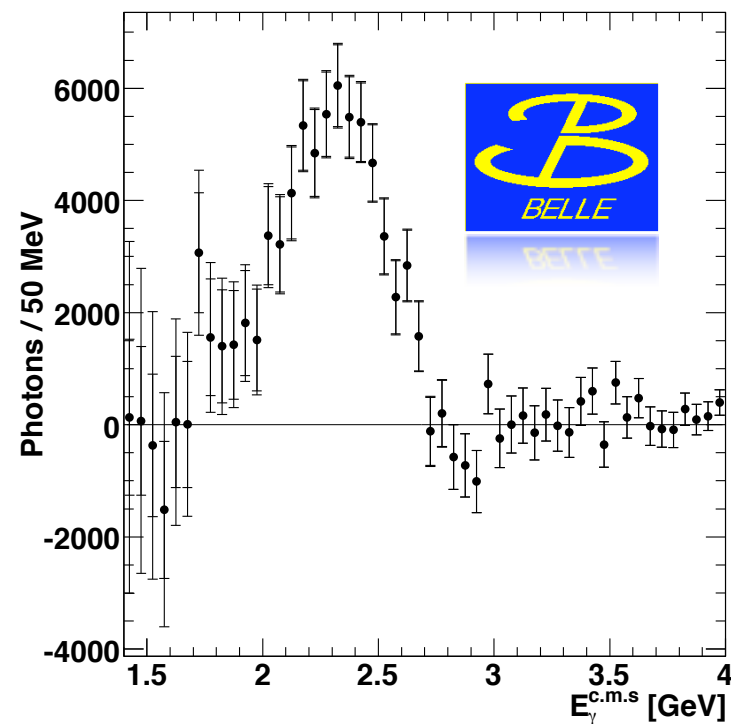
# Shape Function

Theory doesn't work everywhere in the phase space →  
re-sum turn non-perturbative terms

We can determine mean and width of shape function.

- Fit the  $b \rightarrow s\gamma$  spectrum to constrain the shape function
- b-quark: mass and kinetic energy from  $b \rightarrow clv$  and  $b \rightarrow s\gamma$  decays
- Plug the SF into the  $b \rightarrow ulv$  spectrum calculations
- Ready to extract  $|V_{ub}|$

Theory calculation for SF  $\geq$  2-loop.



Shape Function needs to be determined from experimental data.

alternatives: cut out SF region, or factorise out the SF

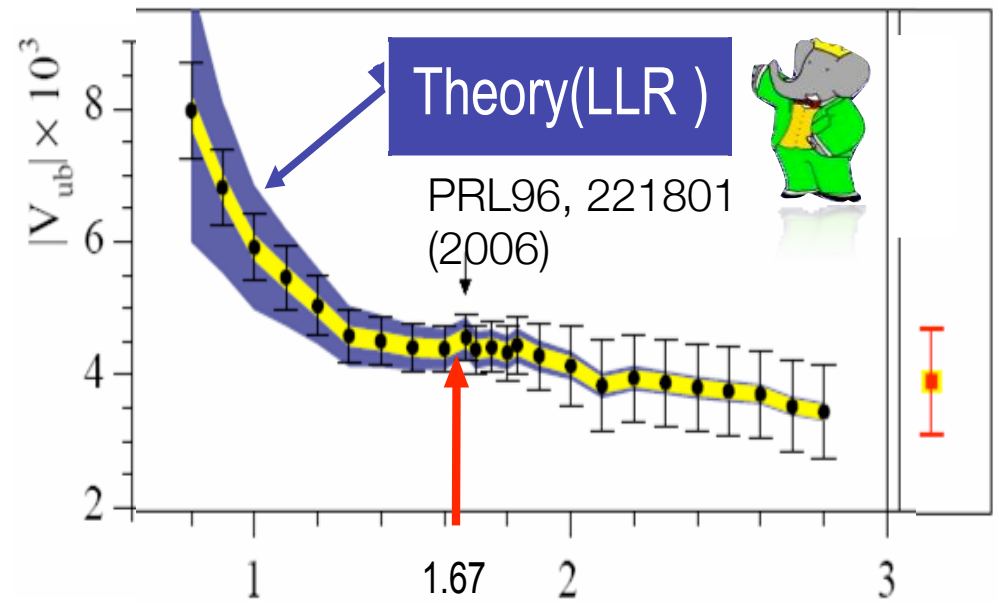
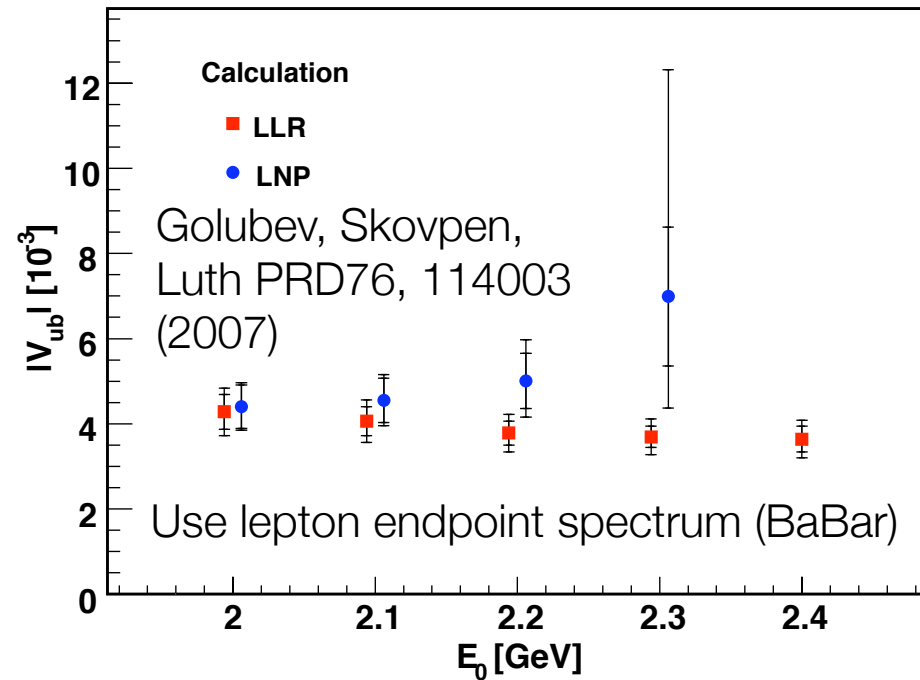
# SF independent analyses

Exploit the assumption that the leading shape functions are the same for all  $b \rightarrow q$  transitions.

**LNP** Lange, Neuber, Paz  
JHEP0510:084 (2005)

**LLR** Leibovich, Low, Rothstein  
PRD61,053006(2000)  
PLB513,83 (2001)

$$\int_0^{m_{max}} \frac{d\Gamma(b \rightarrow u)}{dm_X} dm_X \longleftrightarrow \int_{E_{min}}^{m_B/2} \frac{d\Gamma(b \rightarrow s\gamma)}{dE_\gamma} W(E_\gamma, E_{min}) dE_\gamma$$



Measure  $M_x$  in Breco sample (89 MBB)

$$|V_{ub}| = (4.43 \pm 0.30_{\text{stat}} \pm 0.25_{\text{syst}} \pm 0.29_{\text{theo}}) \times 10^{-3}$$

Uncertainties due to non-perturbative power corrections increase rapidly near the kinematic end point (not included in LLR).

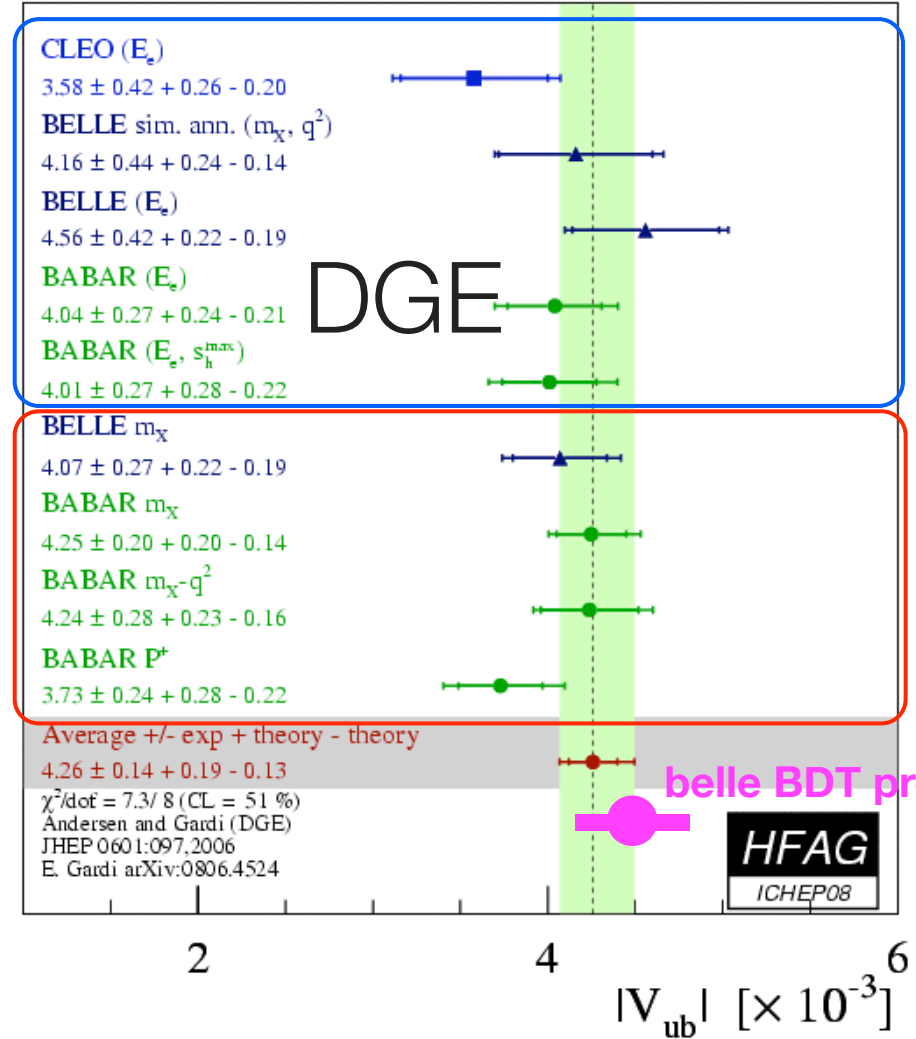
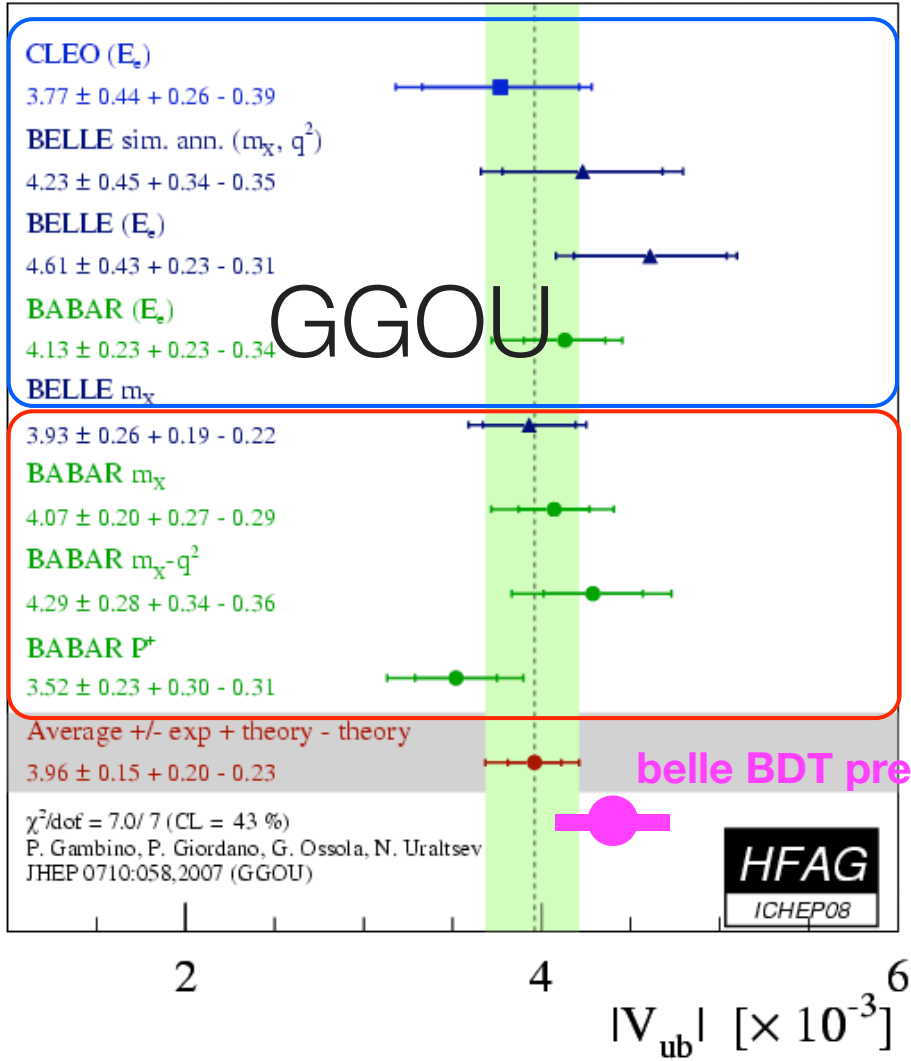
The results agree with analyses that rely on an assumed shape function form.



# Inclusive $|V_{ub}|$

$m_b(\text{kin}) = 4.601 \pm 0.034 \text{ GeV}$  **HFAG**

$m_b(\text{MSbar}) = 4.243 \pm 0.042 \text{ GeV}$  **HFAG**



no systematic difference between **tagged** and **untagged** results

# Inclusive $|V_{ub}|$ Error Breakdown

*what can improve?*

More data ( $ab^{-1}$ ) for better background suppression, more off-res in endpoint.

B Beam

Reduced significantly in tagged meas.

Exclusive  $B \rightarrow \rho/\omega/\eta$  lv recently dominate

HQE/ $|V_{cb}|$  fits/ $Y(1S)$  (hit theory and expt. wall!)

Most theory uncertainties can be reduced significantly if we increase the measured phase space.

The power dependence of  $m_b$  and related theoretical uncertainties scale inversely with phase space coverage.

	BLNP	DGE	GGOU
	+8.2 -7.2	+5.7 -4.7	+6.3 - 7.0
<b>Statistical</b>	2.1	2.2	2.2
<b>Experimental Systematics</b>	2.3	2.1	2.2
<b>b-&gt;c   v model</b>	1.3	1.2	1.3
<b>b-&gt;u   v model</b>	1.4	1.3	1.5
<b>HQ parameters/non. pert</b>	5.7	+4.0 - 2.7	3.9
<b>SF + Sub. SF</b>	2.4		
<b>matching</b>	3.7		
<b>Weak Annihilation</b>	1.6	1.5	+0.0 -3.1
<b>DGE theory</b>		+1.2 -0.5	
<b><math>R_{cut}</math></b>		+0.7 -0.3	
<b>q2 tail model</b>			2.6
<b>Higher order parameters</b>			+1.3 -0.6

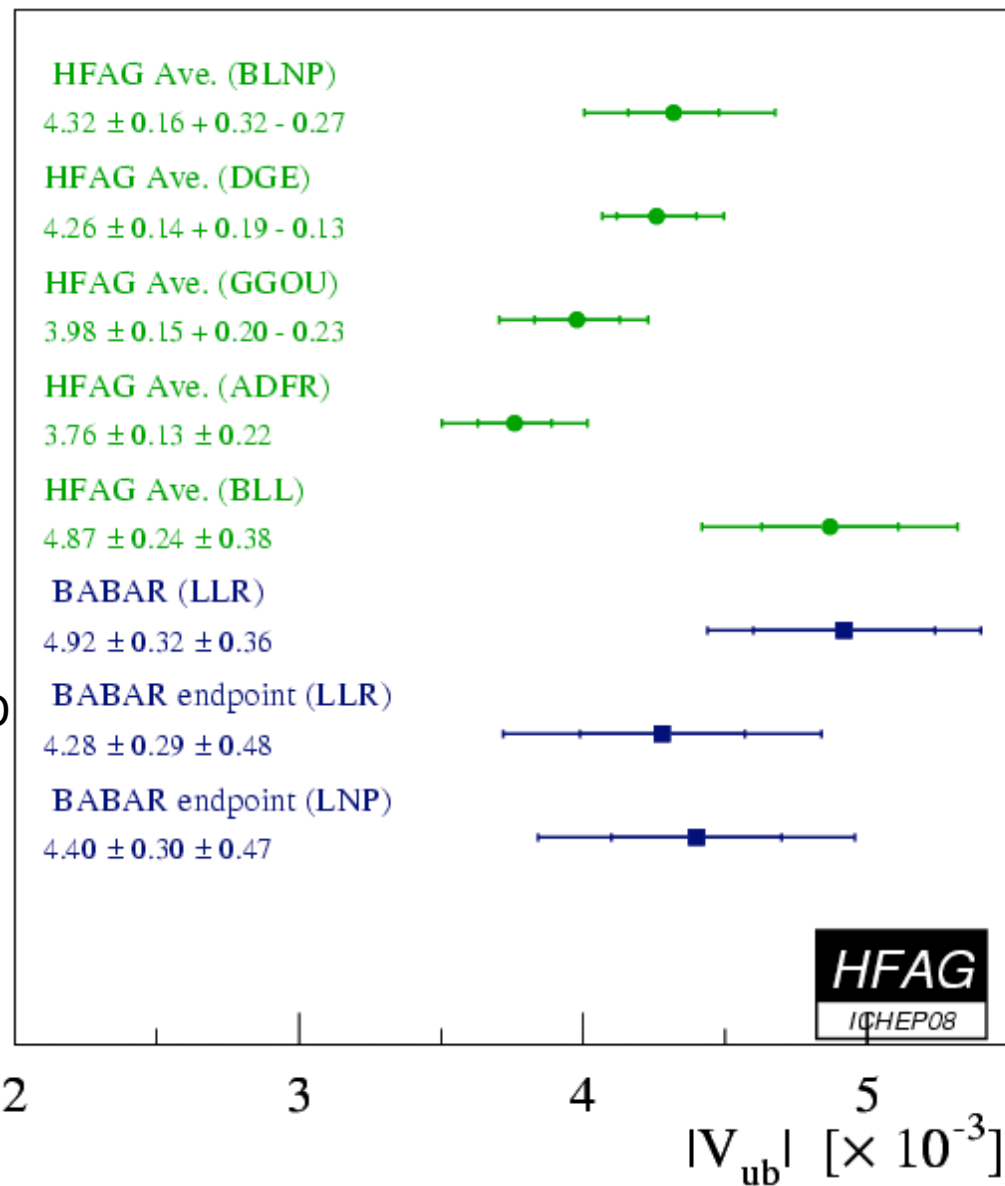
# Comparison of $|V_{ub}|$ extraction

## OPE based + SF

- ▶ **BLNP**: HQE with systematic introduction of SF  
*PRD71:073006 (2005)*
- ▶ **BLL**: phase space in  $m_X - q^2$  with reduced SF  
*PRD64:113004 (2001)*
- ▶ **GGOU**: kinetic scheme  
*JHEP 10(2007) 058*
- ▶ **LNP (LLR)**:  $b \rightarrow s \gamma$  directly related to  $b \rightarrow u \ell \nu$   
*JHEP 0510:084 (PLB 486:86)*

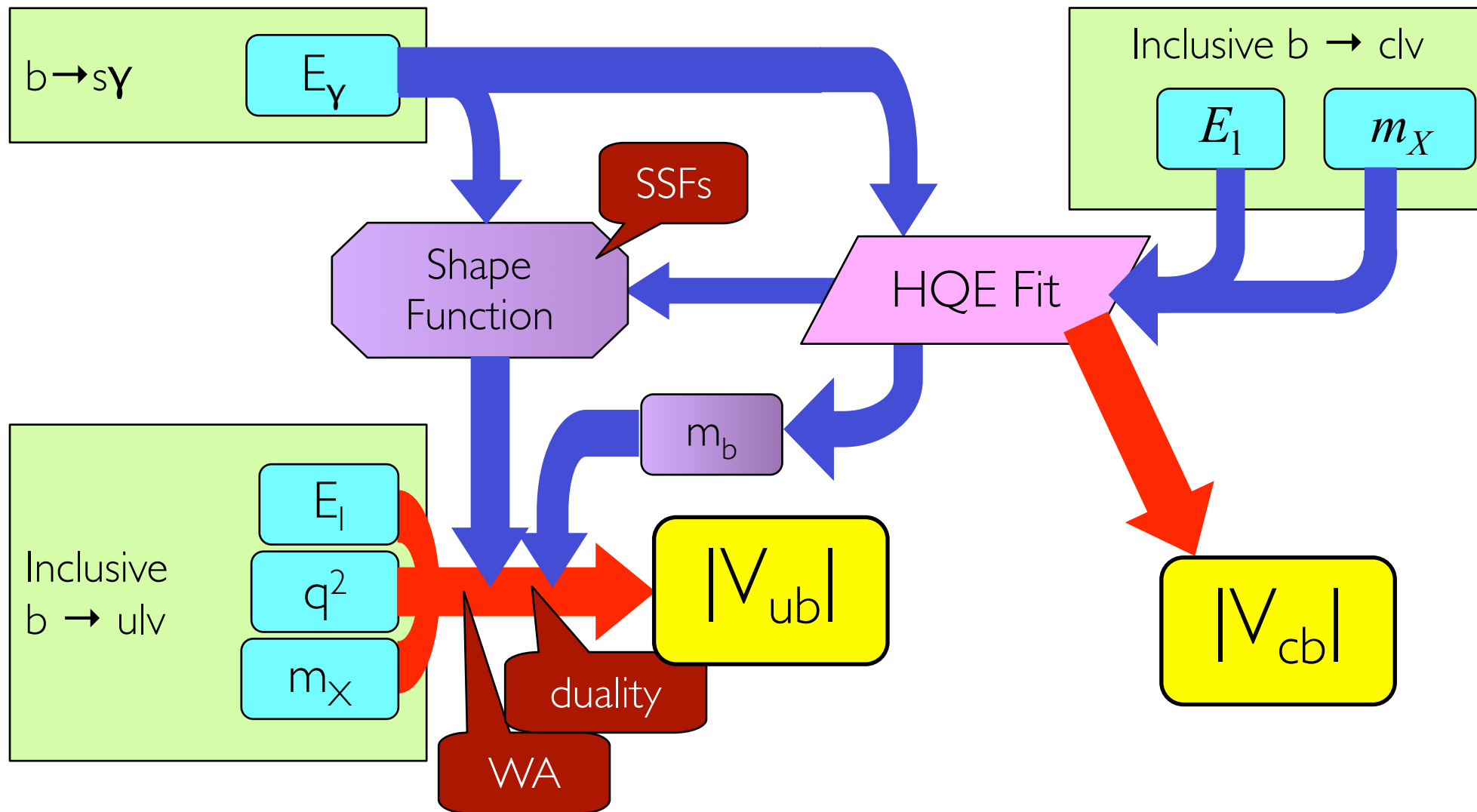
## No SF introduced $\Rightarrow$ model non-perturbative QCD

- ▶ **DGE**: Dressed Gluon Exponentiation  
*JHEP 0601:097 (2006)*
- ▶ **ADFR**: Analytic coupling  
*PRD74:03400(4,5,6) (2006)*

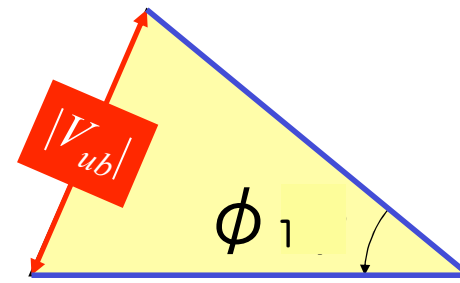


# How Things Mesh Together

AKA: M. Morii's HQE plumbing diagram



# Conclusions



## Untagged methods

### Endpoint:

Goal: lower lepton energy cut to reduce theoretical uncertainty

Will require improved knowledge of charmed semileptonic background.

Stat. error will be relatively small if we have enough off-resonance data.

### Improved Endpoint:

Prospects for reducing systematics, phase space cuts can be relaxed

Gain from relaxing  $S_h^{\max}$ , however, there is fast BG increase

## Tagged Methods

### Full Reconstruction:

Better knowledge of exclusive states crucial.

Data has become quite sensitive to the underlying hybrid model MC (though HQ parameters have become better known with charmed semileptonic decays).

Novel BDT approach by Belle promises to reduce phase space dependent uncertainties.

## Overall

Novel approaches eliminating SF dependence agree with SF, and QCD Model results.

WA tied down.

Inclusive  $V_{ub}$   $\sim 8\%$  error shared between theoretical and experimental. Static in the past 2 years.

Why?  $|V_{ub}|$  theory errors are highly correlated.