

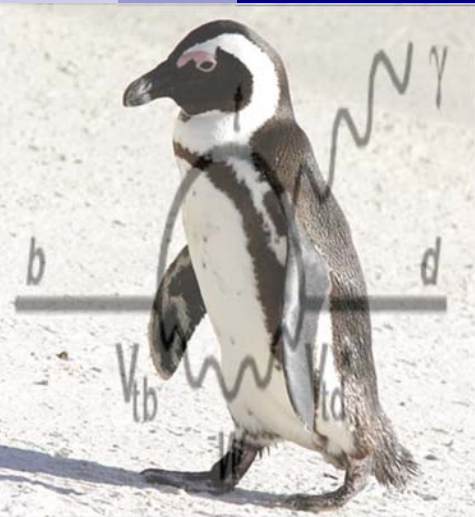


# CKM 2008: 5<sup>th</sup> International Workshop on the CKM Unitarity Triangle

Rome, Italy, September 9-13, 2008



## New Results on $|V_{td}/V_{ts}|$ from Radiative Decays



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**for the BaBar and Belle Collaborations**



- Motivation

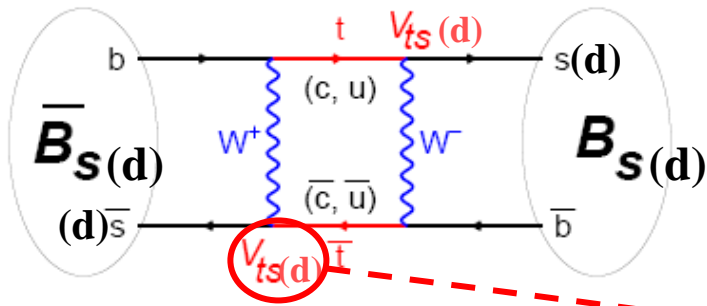
- $B \rightarrow (\rho, \omega) \gamma$  (“Standard” Approach)



- $B \rightarrow X_d$  (“Semi-Inclusive” Approach)

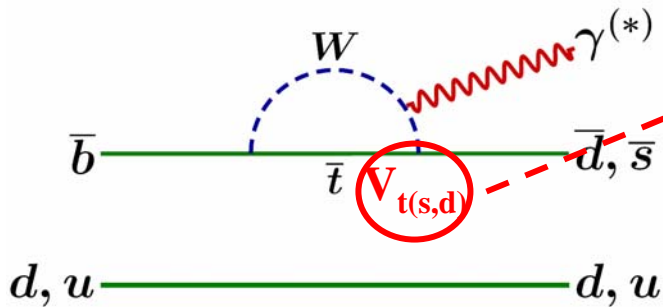
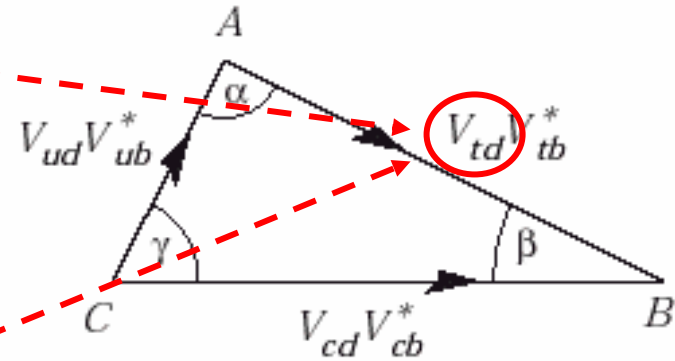


- Status of  $|V_{td}/V_{ts}|$  and Conclusions



B Mixing

Two independent diagrams provide sensitivity to CKM parameter  $V_{td}$



Radiative Penguins

Note: In both cases, hadronic uncertainties minimized by comparing to corresponding  $V_{ts}$  process ( $B_s$  mixing,  $b \rightarrow s\gamma$ )

→ Observable is  $|V_{td}/V_{ts}|$

# $|V_{td}/V_{ts}|$ from Penguins: Motivation



ICHEP '08 B Mixing Results [Farrington(CDF), Moulik(D0), averaged by DeLodovico(BaBar)]:

$$|V_{td}|/|V_{ts}| = 0.207 \pm 0.001_{\text{exp}} \pm 0.006_{\text{theo}}$$

How do penguins fit into the picture?

Mixing:  $x_d = \Delta m_B / \Gamma_B \sim 1 \rightarrow \Delta m_B \sim \Gamma_B$

Penguins:  $\text{Br}(b \rightarrow d\gamma) \sim 10^{-5} \rightarrow \Gamma_{d\gamma} \sim 10^{-5} \Gamma_B$

SM effects suppressed by  $10^{-5}$  relative to mixing

Furthermore (Ali, Asatrian, Greub, Phys. Lett B **429**, 87):

*“These  $[b \rightarrow d\gamma]$  vertices are CKM-suppressed in the standard model, but new physics contributions may not follow the CKM pattern in flavor-changing-neutral-current transitions and hence new physics effects may become more easily discernible in  $B \rightarrow X_d + \gamma$  (and its charge conjugate) than in the corresponding CKM-allowed vertices  $b \rightarrow s\gamma$  and  $b \rightarrow sg$ ”*

**With  $|V_{td}/V_{ts}|$  precisely constrained by mixing,  $b \rightarrow d\gamma$  is a compelling testbed for new physics.**





“Traditional” Approach: measure exclusive rate  $\text{Br}(B \rightarrow \rho(\omega) \gamma)$ ; normalize with  $\text{Br}(B \rightarrow K^* \gamma)$

$$\frac{\mathcal{B}(B \rightarrow \rho \gamma)}{\mathcal{B}(B \rightarrow K^* \gamma)} = S_\rho \left| \frac{V_{td}}{V_{ts}} \right|^2 \left( \frac{1 - m_\rho^2/M_B^2}{1 - m_{K^*}^2/M_B^2} \right)^3 \zeta^2 [1 + \Delta R]$$

isopin factor: 1(.5) for  $\rho^\pm(\rho^0)$ (and  $\omega$ )      form factor ratio

well measured      annihilation amplitude corrections

Annihilation Diagram

Values of  $\zeta^2$  and  $\Delta R$  are state ( $\rho^+, \rho^0, \omega$ ) dependent and are available from

Ali, Parkhomenko, arXiv:hep-ph/0610149

Ball, Zwicky, J. High. Energy Phys. 0604, 046 (2006); Ball, Jones, Zwicky, Phys. Rev. D 75 054004 (2007)

at approximately **8%** overall accuracy.



# Measurement of $B(B \rightarrow \rho(\omega) \gamma)$

Belle: New result this Spring

351 fb<sup>-1</sup> (2006) → 598 fb<sup>-1</sup> (April 2008)

BaBar: New (preliminary) result this Summer

316 fb<sup>-1</sup> (April 2007) → 423 fb<sup>-1</sup> (July 2008)

Challenge: BRs are small ( $<10^{-6}$ ); backgrounds are high

- continuum [Neural Net with event shape, B tagging information, ...]
- $B \rightarrow K^* \gamma; K^* \rightarrow K \pi$  [particle ID]
- $B \rightarrow (\rho^{\pm,0}, \omega)(\pi^0, \eta)$  [veto if  $\gamma$  found such that  $M_{\gamma\gamma} \sim M_{(\pi, \eta)}$ ]



# Measurement of $B(B \rightarrow \rho(\omega) \gamma)$ (continued)

Remaining separation achieved by two-dimensional fit to the largely independent kinematic variables

$$M_{ES} = \sqrt{(E_{beam}^* - p_B^*)^2}$$

“Energy-substituted mass”; since  $E_{beam} \sim M_B$ , largely a measurement of momentum balance

$$\Delta E^* = E_B^* - E_{beam}^*$$

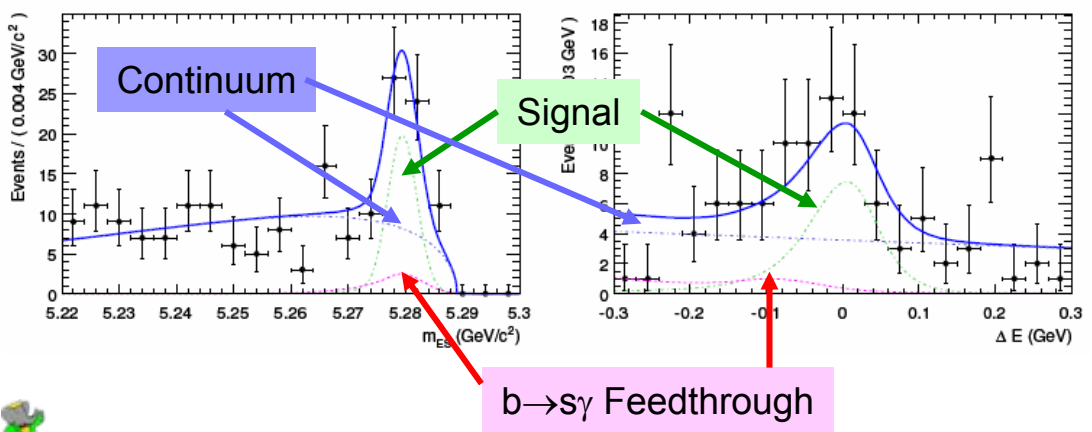
$E_B = E_{beam}$  for properly reconstructed candidate; total energy measurement

\*In  $e^+e^-$  CMS frame

Example: BaBar  $B^0 \rightarrow \rho^0 \gamma$



**PRELIMINARY**



- “self-calibrating” continuum background subtraction
- efficiencies (~5-15%) estimated with control samples

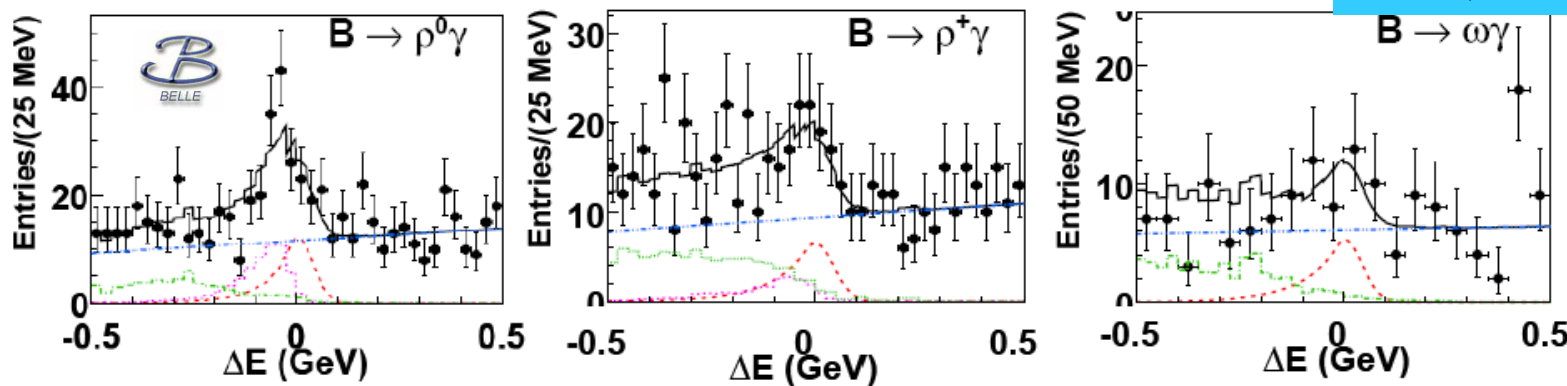


# Belle's April Update of $B \rightarrow \rho(\omega) \gamma$



- Increase sample from 351 fb<sup>-1</sup> to 598 fb<sup>-1</sup>
- Continuum: Fischer Discriminant with Fox-Wolfram moments, B flight information, vertex information
- Include photons from endcap calorimeter

Ji Lin, ICHEP '08



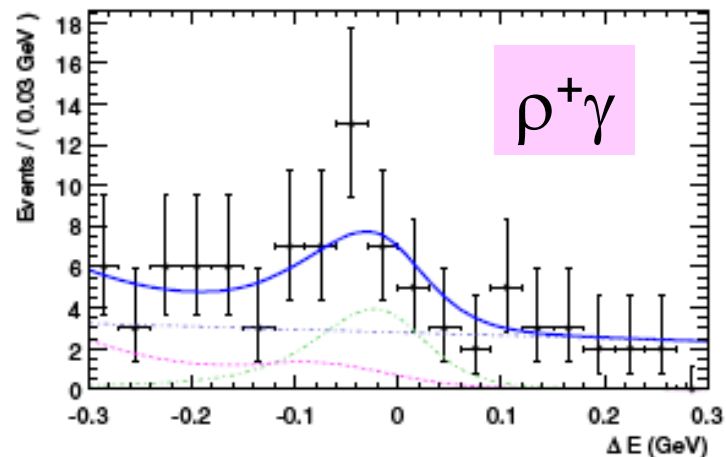
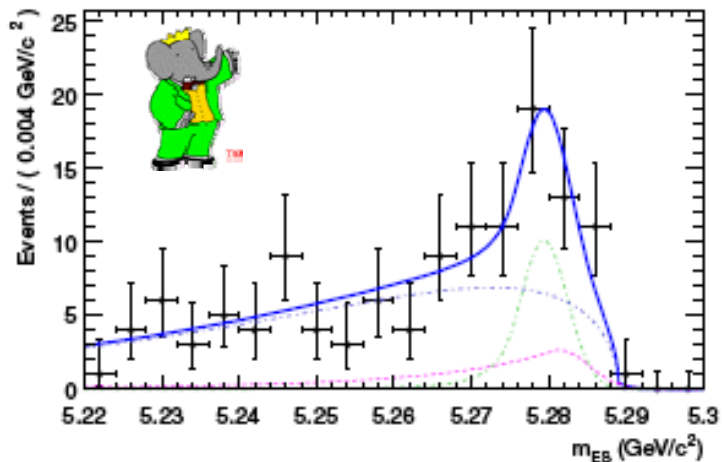
Mode	Belle '06 (x10 <sup>-7</sup> )	Belle '08 (x10 <sup>-7</sup> )
$\rho^+ \gamma$	$5.5^{+4.2 +0.9}_{-3.6 -0.8}$	$8.7^{+2.9 +0.9}_{-2.7 -1.1}$
$\rho^0 \gamma$	$12.5^{+3.7 +0.7}_{-3.3 -0.6}$	$7.8^{+1.7 +0.9}_{-1.6 -1.0}$
$\omega \gamma$	$5.6^{+3.4 +0.5}_{-2.7 -1.0}$	$4.0^{+1.9}_{-1.7} \pm 1.3$







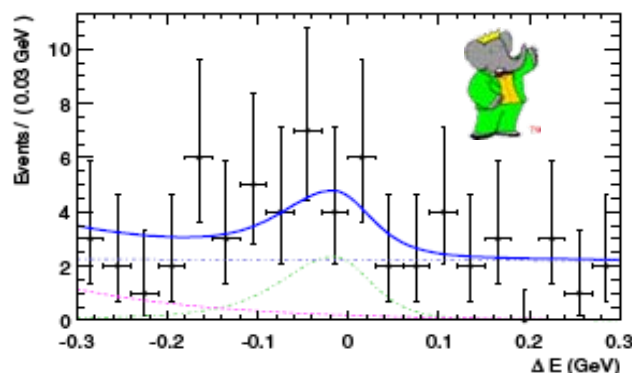
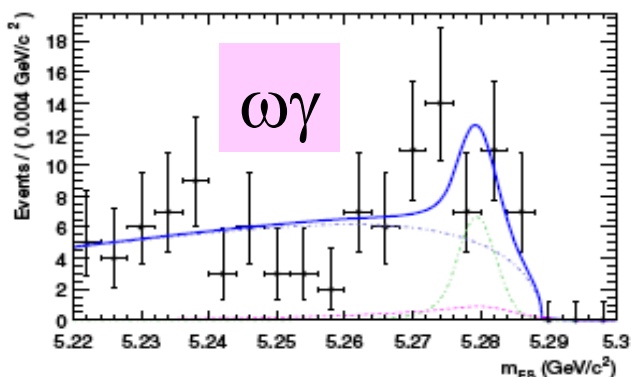
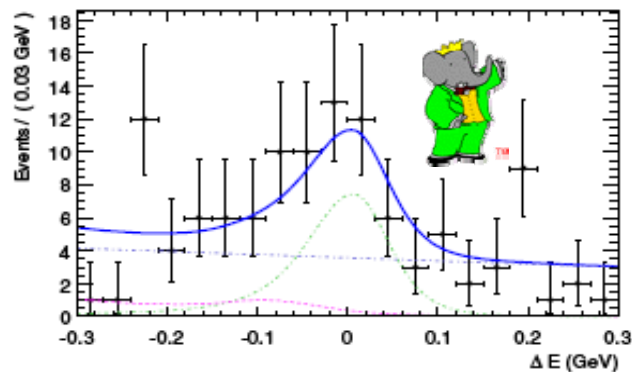
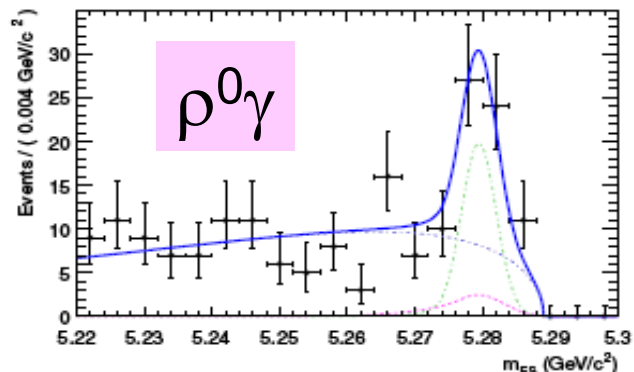
- Increase sample from  $316 \text{ fb}^{-1}$  to  $423 \text{ fb}^{-1}$  (final data set)
  - Strategy: Focus on unconfirmed  $B \rightarrow \omega \gamma$  mode
  - Continuum suppression: “Bagged Decision Tree” with 60 input event variables
- ➔ Relatively good signal-to-noise



# BaBar's July Update of $B \rightarrow \rho(\omega) \gamma$ continued



PRELIMINARY



Mode	BaBar '07 ( $\times 10^{-7}$ )	BaBar '08 ( $\times 10^{-7}$ )
$\rho^+ \gamma$	$11.0^{+3.7}_{-3.3} \pm 0.9$	$12.0^{+4.2}_{-3.7} \pm 2.0$
$\rho^0 \gamma$	$7.9^{+2.2}_{-2.0} \pm 0.6$	$9.7^{+2.4}_{-2.2} \pm 0.6$
$\omega \gamma$	$4.0^{+2.4}_{-2.0} \pm 0.5$	$5.0^{+2.7}_{-2.3} \pm 0.9$

PRELIMINARY





# Isospin-Averaged Branching Fractions

Assuming  $SU_3(F)$  symmetry [ $B(B \rightarrow \rho^0 \gamma) \sim B(B \rightarrow \omega \gamma)$ ] and

$$|\rho^0\rangle = \frac{1}{\sqrt{2}}(|u\bar{u}\rangle - |d\bar{d}\rangle) \quad |\omega\rangle = \frac{1}{\sqrt{2}}(|u\bar{u}\rangle + |d\bar{d}\rangle)$$

(approximately true by static quark model) we can write

$$\Gamma(B^+ \rightarrow \rho^+ \gamma) = 2\Gamma(B^0 \rightarrow \rho^0 \gamma) = 2\Gamma(B^0 \rightarrow \omega \gamma)$$

from which it follows

$$B[B \rightarrow (\rho, \omega)\gamma] \equiv \frac{1}{2} \left\{ B(B^+ \rightarrow \rho^+ \gamma) + \frac{\tau_{B^+}}{\tau_{B^0}} [B(B^0 \rightarrow \rho^0 \gamma) + B(B^0 \rightarrow \omega \gamma)] \right\}$$

→ Can combine  $\rho^+$ ,  $\rho^0$ ,  $\omega$  results to derive  $|V_{td}/V_{ts}|$  from

$$\frac{B(B \rightarrow (\rho, \omega)\gamma)}{B(B \rightarrow K^* \gamma)} = \left| \frac{V_{td}}{V_{ts}} \right|^2 \left( \frac{1 - m_\rho^2 / M_B^2}{1 - m_{K^*}^2 / M_B^2} \right) \zeta^2 [1 + \Delta R]$$



# $|V_{td}/V_{ts}|$ from Exclusive $(\rho, \omega)$ Decays

BELLE:

$$B(B \rightarrow (\rho, \omega)\gamma) = (11.4 \pm 2.0_{-1.2}^{+1.0}) \times 10^{-7} \quad \text{yielding}$$

$$|V_{td}/V_{ts}| = 0.195_{-0.019}^{+0.020} \pm 0.015$$



BaBar:

$$B(B \rightarrow (\rho, \omega)\gamma) = (16.3_{-2.8}^{+3.0} \pm 1.6) \times 10^{-7} \quad \text{yielding}$$

$$|V_{td}/V_{ts}| = 0.233_{-0.024}^{+0.025} \pm 0.022_{-0.021}$$



**PRELIMINARY**

assuming the world-average  $B(B \rightarrow K^* \gamma) = (4.16 \pm 0.17) \times 10^{-5}$

Combining, for exclusive radiative decay overall:

$$|V_{td}/V_{ts}| = 0.210 \pm 0.015 \pm 0.018$$



# Semi-Inclusive Approach: $B \rightarrow X_d \gamma$ (Preliminary)



“New” Approach (BaBar): Reconstruct seven exclusive final states  $X_d \gamma$  in range  $0.6 \text{ GeV}/c^2 < M_{X_d} < 1.8 \text{ GeV}/c^2$



iType	$X_s$	$X_d$
1	$K^+ \pi^- \gamma$	$\pi^+ \pi^- \gamma$
2	$K^+ \pi^0 \gamma$	$\pi^+ \pi^0 \gamma$
3	$K^+ \pi^- \pi^+ \gamma$	$\pi^+ \pi^- \pi^+ \gamma$
4	$K^+ \pi^- \pi^0 \gamma$	$\pi^+ \pi^- \pi^0 \gamma$
6	$K^+ \pi^- \pi^+ \pi^- \gamma$	$\pi^+ \pi^- \pi^+ \pi^- \gamma$
7	$K^+ \pi^- \pi^+ \pi^0 \gamma$	$\pi^+ \pi^- \pi^+ \pi^0 \gamma$
9	$K^+ \eta^0 \gamma$	$\pi^+ \eta^0 \gamma$

$|V_{td}/V_{ts}|^2$  related to  $\Gamma(b \rightarrow d \gamma)/\Gamma(b \rightarrow s \gamma)$  with  $\sim 1\%$  theoretical uncertainty [Ali, Asatrian, Greub, Phys. Lett. B 429, 87 (1998)]

**However, must correct for unmeasured regions:**

- Higher-multiplicity final states
- Higher-mass hadronic component (i.e.  $M_{X_d} > 1.8 \text{ GeV}/c^2$ )

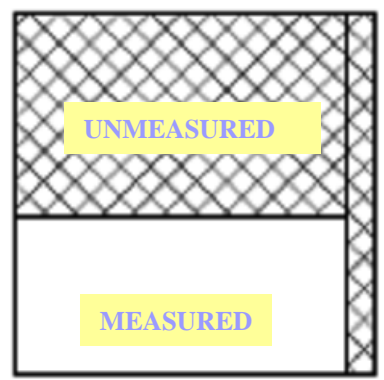
# Measured Regions for $B \rightarrow X_{d(s)} \gamma$



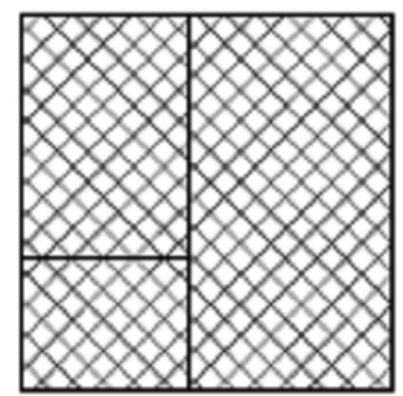
$X_{S}\gamma$



$(\rho, \omega, K^*)$

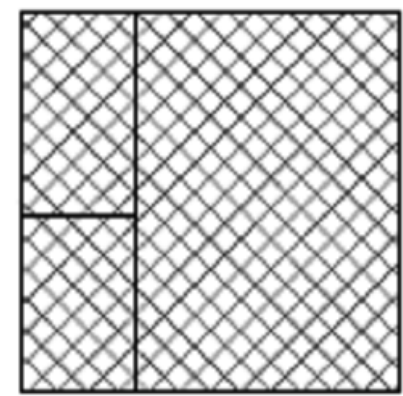
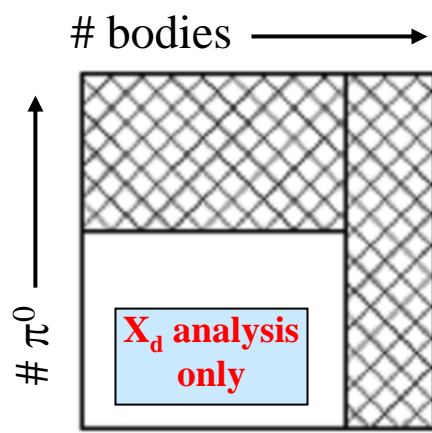
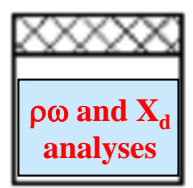


$1.0 < M_{had} < 1.8$



$1.8 < M_{had}$

$X_{d}\gamma$

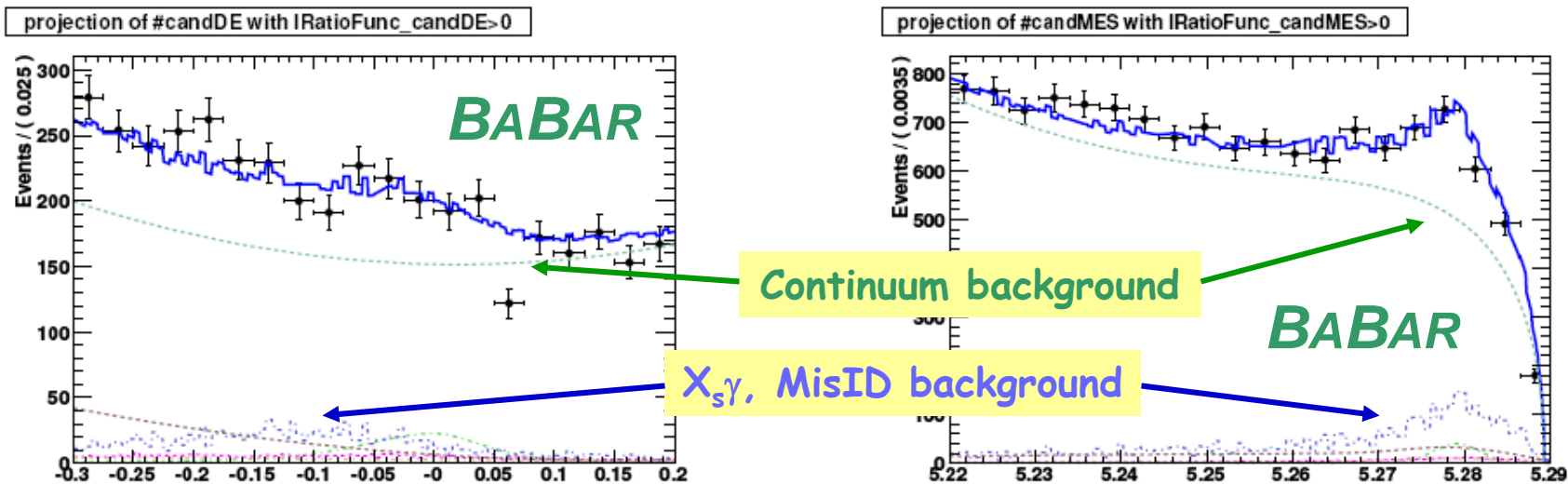


$M_{had} (M_{X_d})$  →



# $B \rightarrow X_{(s,d)} \gamma$ Partial Branching Fraction Results

Fit in high-mass  $X_d \gamma$  region (first time measured):



Yields and partial branching fractions:

**PRELIMINARY**

Mode	Mass Range	Yield	Efficiency	Partial B. F. ( $\times 10^{-6}$ )
$b \rightarrow s \gamma$	$0.6 < M_{X_s} < 1.0$	$1543 \pm 46$	8.5%	$23.7 \pm 0.7 \pm 1.7$
$b \rightarrow s \gamma$	$1.0 < M_{X_s} < 1.8$	$2279 \pm 75$	6.1%	$48.7 \pm 1.6 \pm 4.1$
$b \rightarrow d \gamma$	$0.6 < M_{X_d} < 1.0$	$66 \pm 26$	7.0%	$1.2 \pm 0.5 \pm 0.1$
$b \rightarrow d \gamma$	$1.0 < M_{X_d} < 1.8$	$107 \pm 47$	5.2%	$2.7 \pm 1.2 \pm 0.4$

High-mass  
 $b \rightarrow X_d \gamma$



# Correction for Missing Modes

- Dominant systematic error for  $1.0 < M_X < 1.8 \text{ GeV}/c^2$
- Most difficult for  $B \rightarrow X_d \gamma$  (not constrained by data)
- Can improve with statistics (internal constraints)

Try several models:

- $M_X$  given by “KN Model” Kagan & Neubert, Phys. Rev. D 58, 094012 (1998), with phase-space fragmentation
- As above, but with 50% replaced by mix of resonances
- Fix to measured  $b \rightarrow s\gamma$  fragmentation

Errors: Statistical  $\pm$  Experimental Systematic

**BABAR**

Mass Range ( $\text{GeV}/c^2$ )	$B(b \rightarrow s\gamma) (\times 10^{-6})$	$B(b \rightarrow d\gamma) (\times 10^{-6})$	$B(b \rightarrow d\gamma)/B(b \rightarrow s\gamma)$
$0.6 < M_{X(s,d)} < 1.0$	$1.2 \pm 0.5 \pm 0.1$	$47 \pm 1 \pm 3$	$0.026 \pm 0.011 \pm 0.002$
$1.0 < M_{X(s,d)} < 1.8$	$6.0 \pm 2.6 \pm 2.3$	$168 \pm 14 \pm 33$	$0.036 \pm 0.015 \pm 0.009$
$0.6 < M_{X(s,d)} < 1.8$	$7.2 \pm 2.7 \pm 2.3$	$215 \pm 14 \pm 33$	<b><math>0.033 \pm 0.013 \pm 0.009</math></b>

**Primary experimental result**

**PRELIMINARY**





# Ratio of Total Widths and $|V_{td}/V_{ts}|$



Precise ( $\sim 1\%$ ) expression for  $|V_{td}/V_{ts}|$  [Ali, Asatrian, Greub] is based on ratio of full widths  $\Gamma(b \rightarrow d\gamma)/\Gamma(b \rightarrow s\gamma)$

Measured region  $0.6 < M_x < 1.8$  is  $\sim 50\%$  of width

Extrapolate to full mass region via “KN Model”; KN calculation suggests negligible difference and uncertainty in extrapolation of the ratio (because  $m_s, m_d \ll 1.8 \text{ GeV}/c^2$ ?)

This remains a bit of a caveat...

**BABAR**

$$\frac{\Gamma(b \rightarrow d\gamma)}{\Gamma(b \rightarrow s\gamma)} =$$

$$0.033 \pm 0.013 \pm 0.009$$

**PRELIMINARY**

arXiv:0807.4975 [hep-ex]; submitted to PRL

**Ali**  
**Asatrian**  
**Greub**

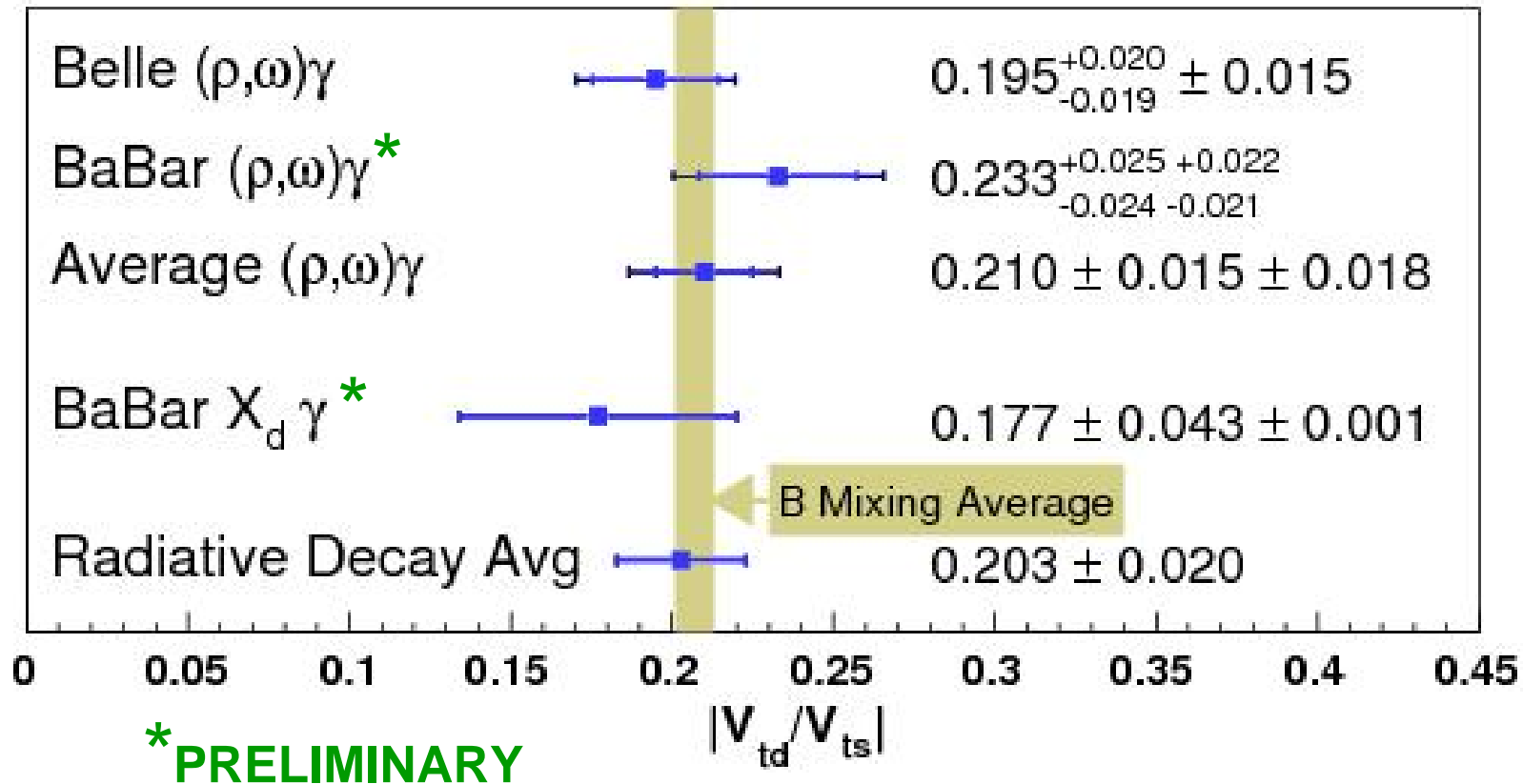
**BABAR PRELIMINARY**

$$|V_{td}/V_{ts}| =$$

$$0.177 \pm 0.043 \pm 0.001$$

Expt. Theory





No evidence for non-Standard Model contribution to the decay width.



- Radiative measurements of  $|V_{td}/V_{ts}|$  are becoming precise:

$$|V_{td}/V_{ts}|_{\text{rad}} = 0.203 \pm 0.020$$

- Semi-inclusive approach works, and is independent of exclusive approach, with small theoretical uncertainty
- Agreement with SM (as constrained by B mixing) is good

In principle, the severe SM suppression of this radiative process ( $\times 10^{-6}$  of B mixing) should make it very sensitive to new physics contributions.

Have we fully thought through the meaning of this constraint?