

# Patterns of flavor signals in supersymmetric models

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## Introduction

Flavor physics: probe for new physics.

- Heavy particles and their interactions contribute in various ways.
- ⇒ Plays a complementary role with direct measurements (@LHC).
  - ▷ SM:  $b \rightarrow s, d$  (flavor)  $\oplus m_t$  (direct)  $\Rightarrow V_{td}, V_{ts}$ .
  - ▷ Similar case will occur in the study of physics beyond the SM.
    - \*  $b \rightarrow s, d \oplus m_{\tilde{q}} \Rightarrow q_i - \tilde{q}_j - \tilde{g}$  coupling.

Experimental improvements expected.

- LHCb:  $S_{CP}(B_s \rightarrow J/\psi\phi), \dots$
- MEG: search for  $\mu \rightarrow e\gamma$  with b.r. down to  $10^{-13}$ .
  - ▷ current upper limit:  $B(\mu \rightarrow e\gamma) < 1.1 \times 10^{-11}$ .
- Super B factories (under discussion) with  $\int \mathcal{L} = 50 - 75 \text{ab}^{-1}$ :
  - ⇒ uncertainties reduced by  $\sim \frac{1}{7}$  ( $\int \mathcal{L}(\text{KEKB} + \text{PEPII}) \approx 1.3 \text{ab}^{-1}$ ).

In this work, we study quark/lepton flavor signals:

- LFV ( $\mu \rightarrow e \gamma$ ,  $\tau \rightarrow \mu \gamma$ ,  $\tau \rightarrow e \gamma$ ),
- CP Asymmetries in  $B$  decays,
  - ▷  $S_{\text{CP}}(B_d \rightarrow K^* \gamma)$ ,  $S_{\text{CP}}(B_d \rightarrow \rho \gamma)$
  - ▷  $S_{\text{CP}}(B_d \rightarrow \phi K_S)$
  - ▷  $S_{\text{CP}}(B_s \rightarrow J/\psi \phi)$

in SUSY models with typical flavor structures:

- mSUGRA,
- MSSM with  $\nu_R$ 's,
- SU(5) SUSY GUT with  $\nu_R$ 's,
- U(2) Flavor Symmetry model.

We show the pattern of flavor signals varies depending on the model.

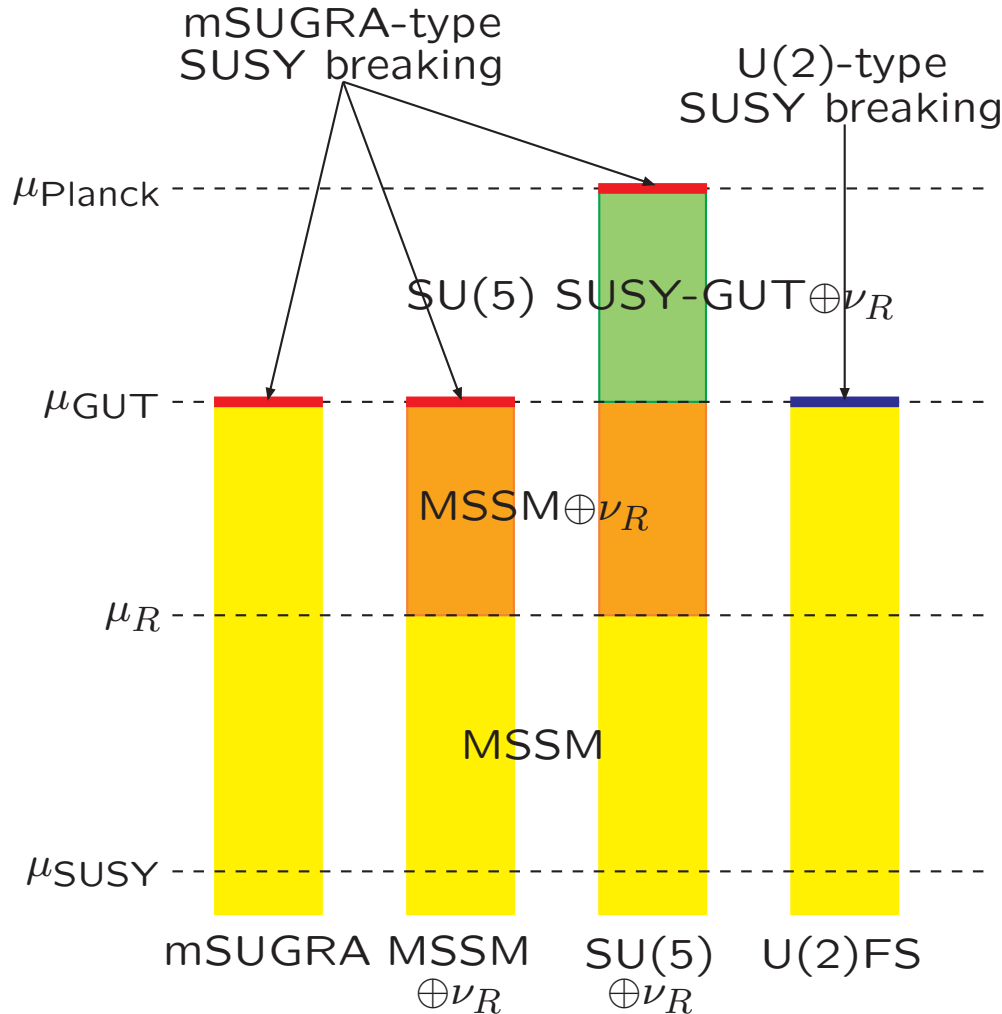
⇒ Flavor measurements are useful to distinguish models.

## Contents:

- Models
- Numerical results
- Summary

# Models: Minimal Supersymmetric Standard Model + $\alpha$

“+ $\alpha$ ”: mechanism which controls flavor mixing in SUSY breaking.



- mSUGRA:  $Y_{U,D}$  ( $V_{\text{CKM}}$ ) only.
  - ▷ Flavor-blind SUSY breaking
  - $m_0, m_{1/2}, A_0$ .
- MSSM  $\oplus \nu_R$ :  $Y_\nu$  affects running.
  - ▷ SUSY breaking = mSUGRA.
  - ▷ GUT: quark  $\leftrightarrow$  lepton.
- U(2) flavor symmetry:
  - ▷  $Y_{U,D} \sim \begin{bmatrix} \epsilon' & & \\ \epsilon' & \epsilon & \epsilon \\ & \epsilon & 1 \end{bmatrix}$ ,  
 ( $\epsilon \sim V_{cb}, \epsilon'/\epsilon \sim V_{us}$ ).
  - ▷  $m_{Q,U,D}^2 \sim m_0^2 \begin{bmatrix} 1 & & \\ & 1 & \epsilon \\ & \epsilon & O(1) \end{bmatrix}$ ,

## Flavor mixing/CPV source

- $V_{CKM}$  (all cases)  $\Rightarrow \tilde{q}_L$  mixing (running).
  - ▷ Significant in  $B(b \rightarrow s \gamma)$ ; small in others.
  - ▷ GUT  $\Rightarrow \tilde{\ell}_R$  mixing (Barbieri-Hall).  $\mathbf{10} = \{q_L, (u_R)^c, (e_R)^c\}$ .
- $Y_\nu$  (cases with  $\nu_R$ 's)  $\Rightarrow \tilde{\ell}_L$  mixing (running above  $\mu_R$ ).
  - ▷ GUT  $\Rightarrow \tilde{d}_R$  mixing (Moroi)  $\bar{\mathbf{5}} = \{(d_R)^c, \ell_L\}$ .
- $m_{Q,U,D}^2(\mu_{GUT})$  (U(2)FS).
  - ▷ U(2) structure neglected in (s)lepton sector.
- SUSY CPV phases ( $\phi_A, \phi_\mu, \dots$ ).
  - ▷ Affect CP asymmetries in  $b$  decays, EDMs ( $e, n, \text{Hg}$ ).

## Structure of the neutrino mass matrices ( $\text{MSSM} \oplus \nu_R$ , $\text{SU}(5) \oplus \nu_R$ )

**Light:**  $|\Delta m_{32}^2|(\text{atm}) \gg \Delta m_{21}^2(\text{sol})$

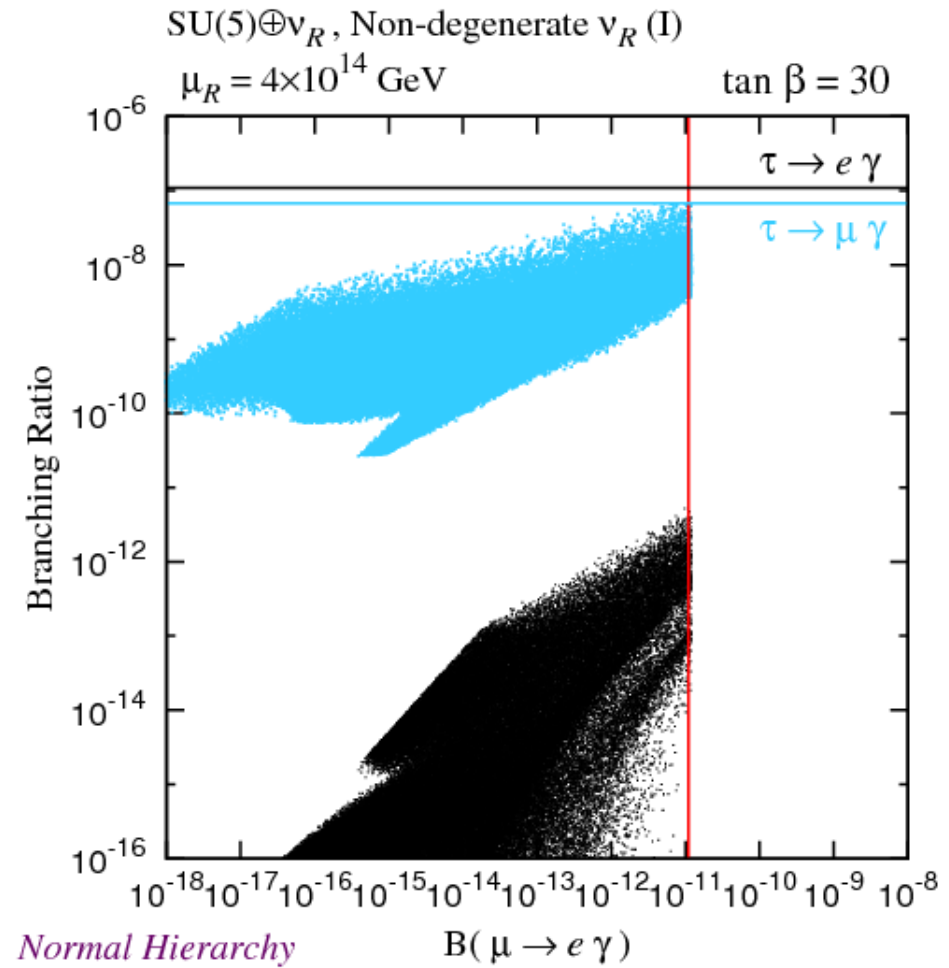
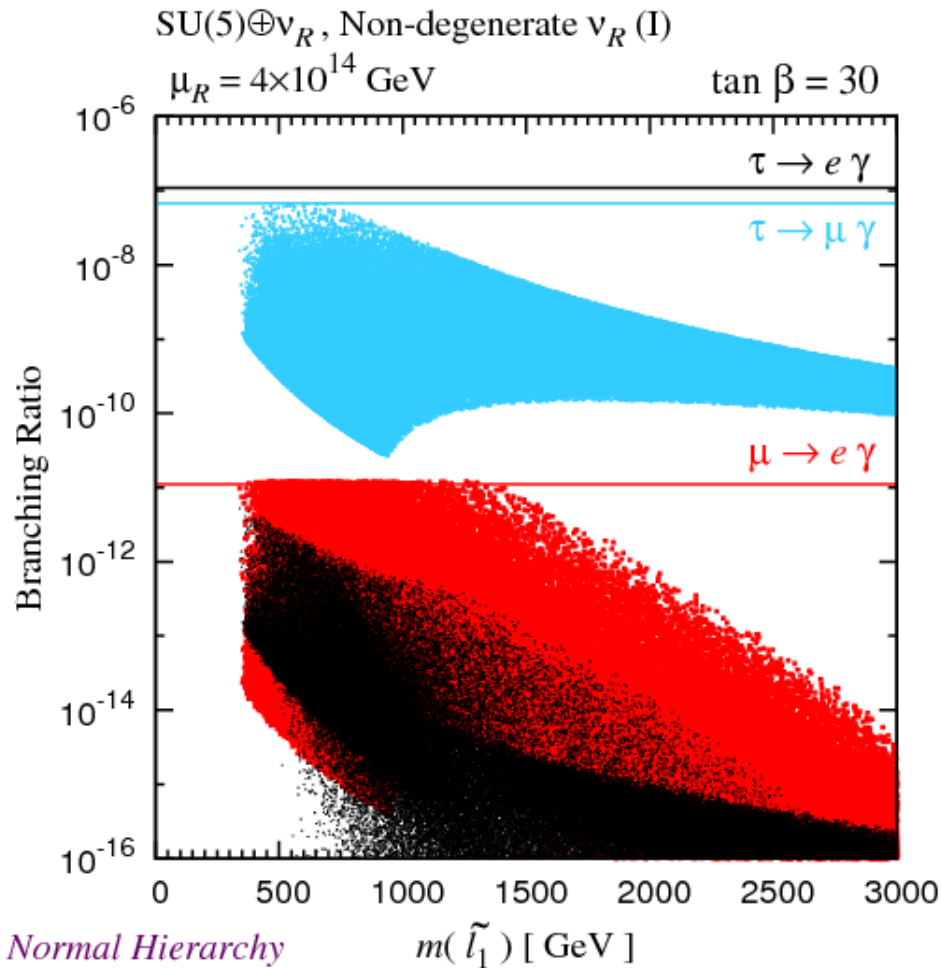
- Normal Hierarchy
  - ▷  $m_3 \gg m_2 \gg m_1 = 0.003\text{eV}$ .  
( $\Delta m_{21}^2 \gg m_1^2$ )
- Inverted Hierarchy
  - ▷  $m_2 > m_1 \gg m_3$ .
- Degenerate
  - ▷  $m_3 > m_2 > m_1$ ,  
 $m_1^2 = (0.1\text{eV})^2 \gg |\Delta m_{32}^2|$ .

**Heavy ( $\nu_R$ ):**

- Degenerate  $\nu_R$ :  $M_{\nu_R} \propto \mathbf{1}$ .
    - ▷  $\mu \rightarrow e \gamma$  enhanced.
  - Non-Degenerate  $\nu_R$ :  $M_{\nu_R} \not\propto \mathbf{1}$ .
    - ▷ More free parameters in  $Y_\nu$ .
    - ▷  $\mu \rightarrow e \gamma$  suppression possible.
- (I)  $(Y_\nu)_{12} = (Y_\nu)_{21} = 0$ ,  
 $(Y_\nu)_{13} = (Y_\nu)_{31} = 0$ .
- (II)  $(Y_\nu)_{12} = (Y_\nu)_{21} = 0$ ,  
 $(Y_\nu)_{23} = (Y_\nu)_{32} = 0$ .

**LFV:**  $\mu \rightarrow e \gamma$ ,  $\tau \rightarrow \mu \gamma$ ,  $\tau \rightarrow e \gamma$

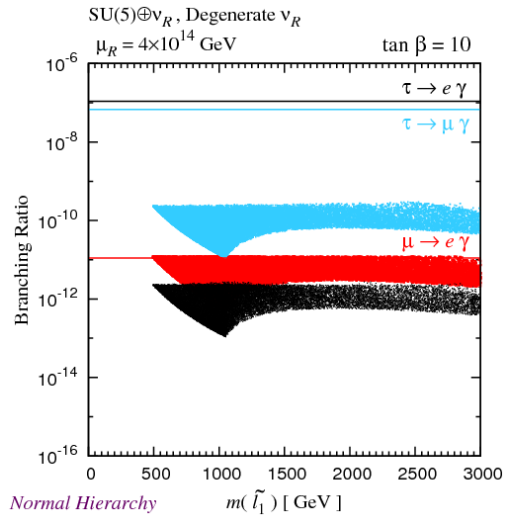
$SU(5) \oplus \nu_R$ , Non-degenerate  $\nu_R$  (I), Normal Hierarchy



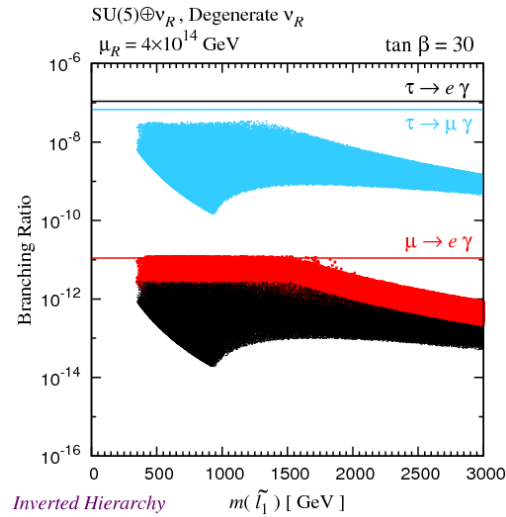
$m_{1/2}(\mu_G) \leq 1.5 \text{ TeV}$ ,  $m_0(\mu_P) \leq 4 \text{ TeV}$  scanned.



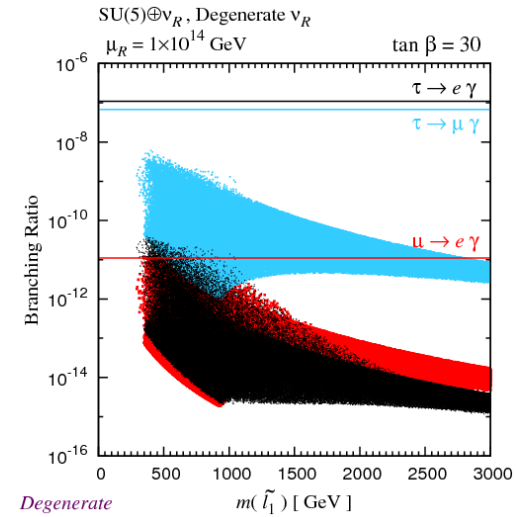
$\mu \rightarrow e \gamma, \tau \rightarrow \mu \gamma, \tau \rightarrow e \gamma$ :  $SU(5) \oplus \nu_R$  ( $Y_\nu$  &  $\mu_P \leftrightarrow \mu_G$  running)



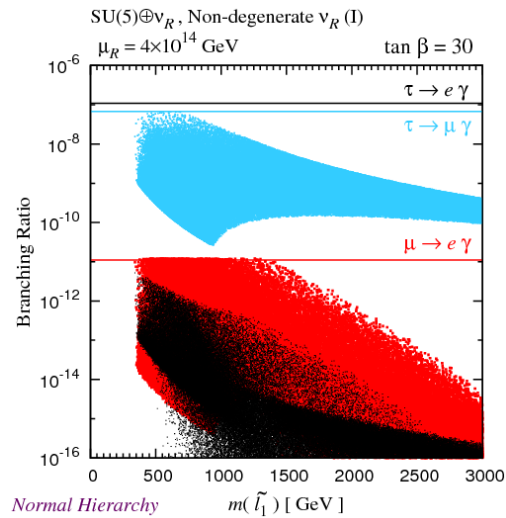
$D\nu_R$ -NH



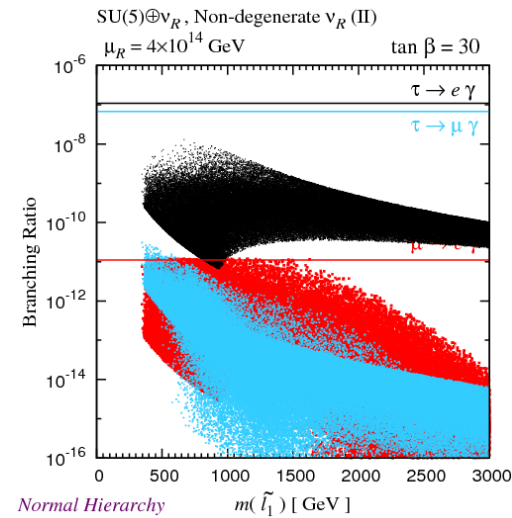
$D\nu_R$ -IH



$D\nu_R$ -D

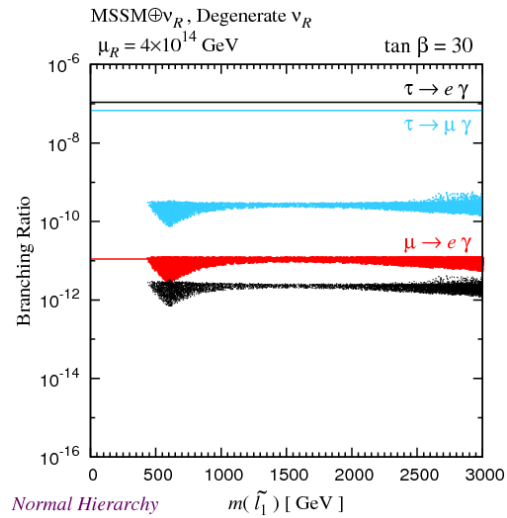


$ND\nu_R$ (I)-NH

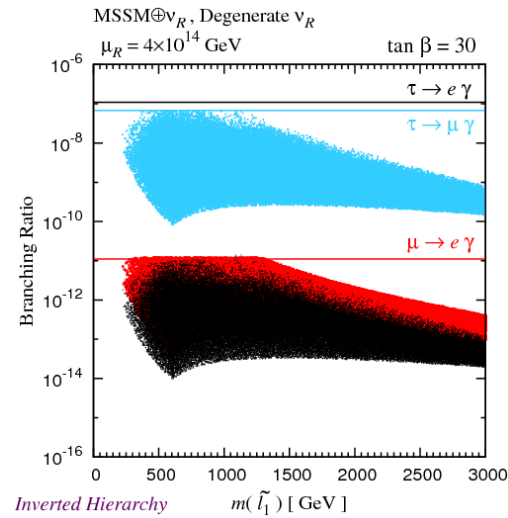


$ND\nu_R$ (II)-NH

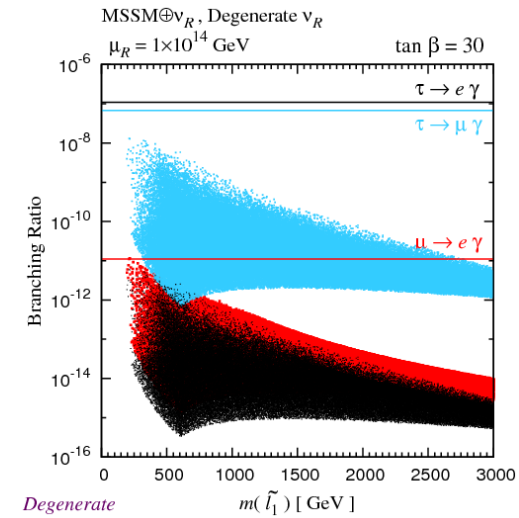
# $\mu \rightarrow e \gamma, \tau \rightarrow \mu \gamma, \tau \rightarrow e \gamma$ : $\text{MSSM} \oplus \nu_R$ ( $Y_\nu$ only)



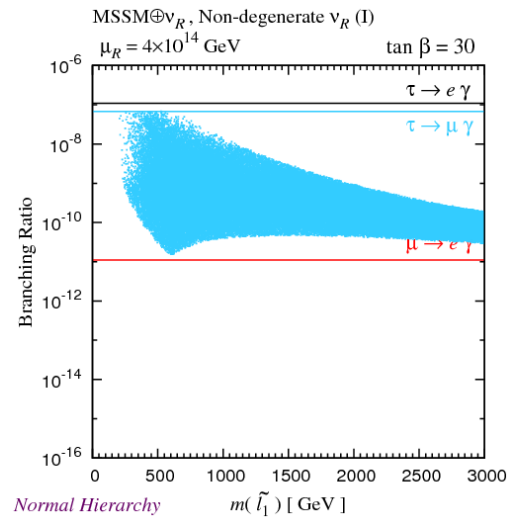
$D\nu_R$ -NH



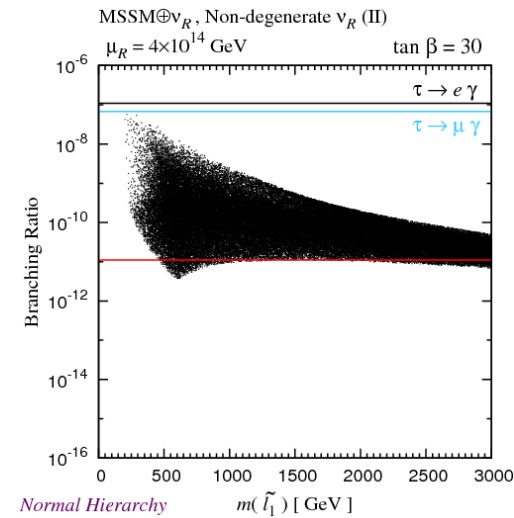
$D\nu_R$ -IH



$D\nu_R$ -D



$ND\nu_R$ (I)-NH



$ND\nu_R$ (II)-NH

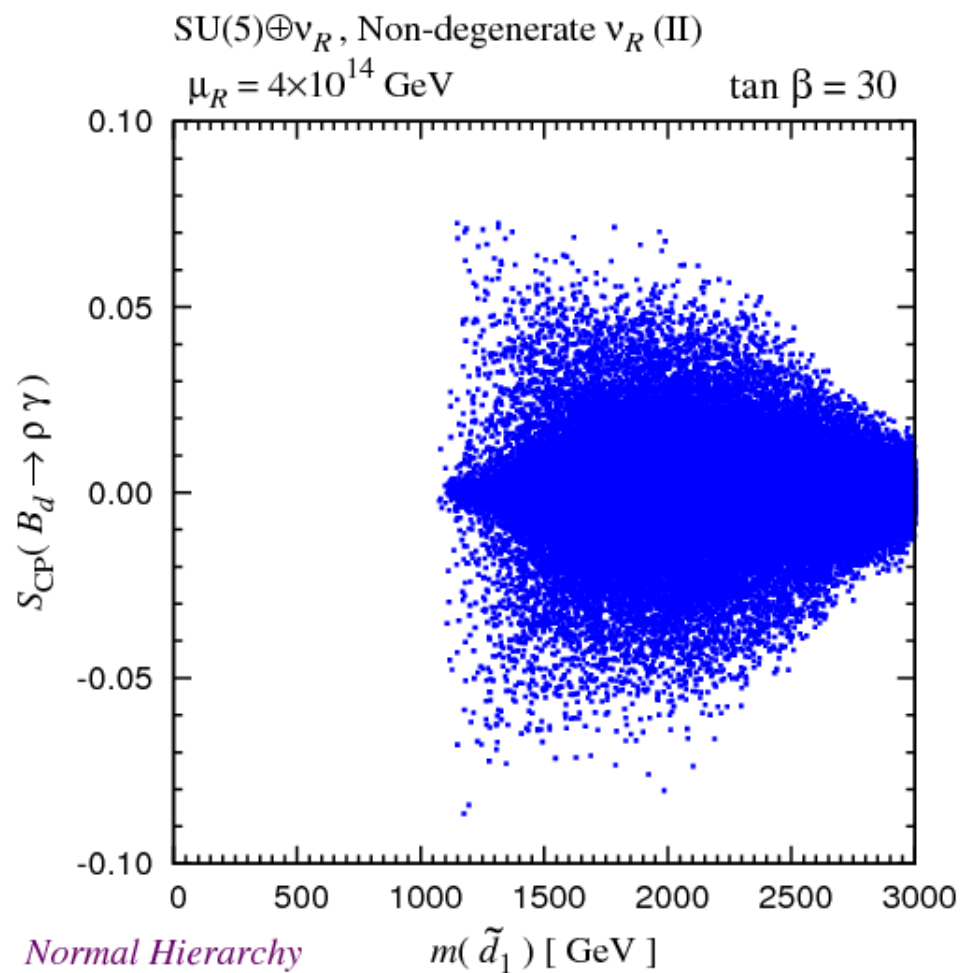
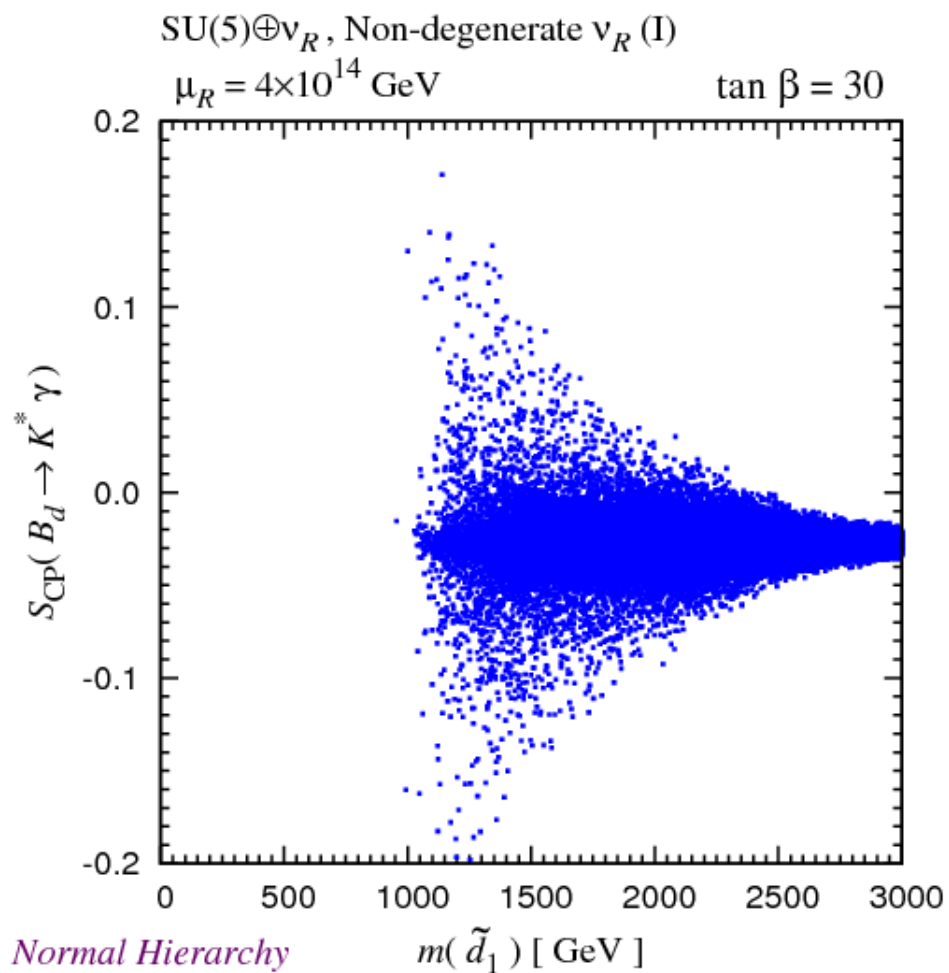
## Time-dependent CP asymmetries in $b \rightarrow s/b \rightarrow d$ decays

- $S_{\text{CP}}(B_d \rightarrow K^* \gamma), S_{\text{CP}}(B_d \rightarrow \rho \gamma)$ 
  - ▷  $B_d - \bar{B}_d$  mixing  $\otimes$   $b \rightarrow s(d) \gamma$  decay.
  - ▷ Interference between  $b_R \rightarrow s(d)_L \gamma_L$  and  $(\bar{b}_L) \rightarrow (\overline{s(d)_R}) \gamma_L$ ; suppressed by  $m_{s,d}/m_b$  in SM (Atwood-Gronau-Soni).
- $S_{\text{CP}}(B_d \rightarrow \phi K_S)$ 
  - ▷  $B_d - \bar{B}_d$  mixing  $\otimes$   $b \rightarrow s s \bar{s}$  decay.
  - ▷ Differs from  $S_{\text{CP}}(B_d \rightarrow J/\psi K_S)$  if new phase exists in  $b \rightarrow s$  penguin amplitude.
- $S_{\text{CP}}(B_s \rightarrow J/\psi \phi)$ 
  - ▷  $B_s - \bar{B}_s$  mixing  $\otimes$   $b \rightarrow s c \bar{c}$  decay.
  - ▷ Small in SM; enhanced if new phase exists in  $B_s - \bar{B}_s$  mixing.

$\Rightarrow \tilde{d}_R$  mixing can contribute to all.

- Significant in  $\text{SU}(5) \text{ SUSY-GUT} \oplus \nu_R$  and  $\text{U}(2)\text{FS}$ .

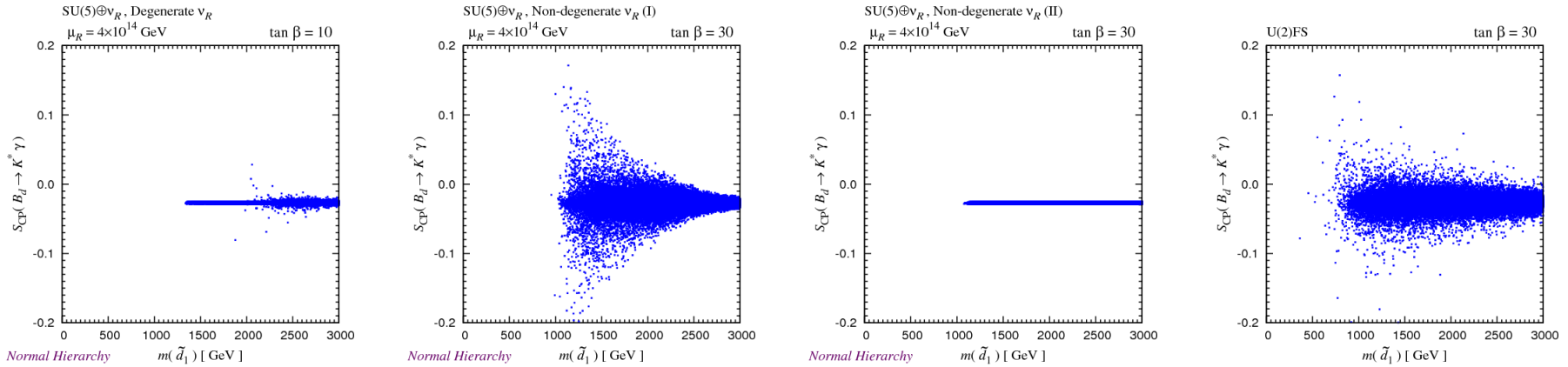
$S_{\text{CP}}(B_d \rightarrow K^* \gamma) [b \rightarrow s], S_{\text{CP}}(B_d \rightarrow \rho \gamma) [b \rightarrow d]$



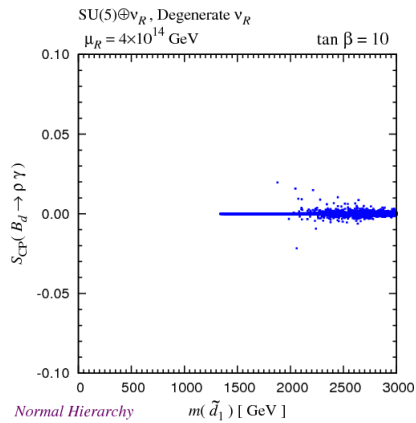
# $S_{CP}(B_d \rightarrow K^* \gamma)$ [ $b \rightarrow s$ ], $S_{CP}(B_d \rightarrow \rho \gamma)$ [ $b \rightarrow d$ ]

Significant in  $SU(5) \oplus \nu_R$ ,  $U(2)FS$ ; small in mSUGRA,  $MSSM \oplus \nu_R$ .

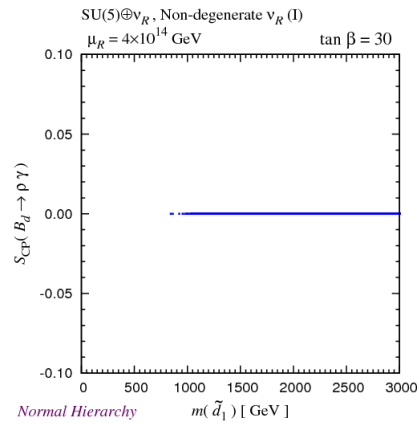
## $S_{CP}(B_d \rightarrow K^* \gamma)$ vs. $m(\tilde{d}_1)$



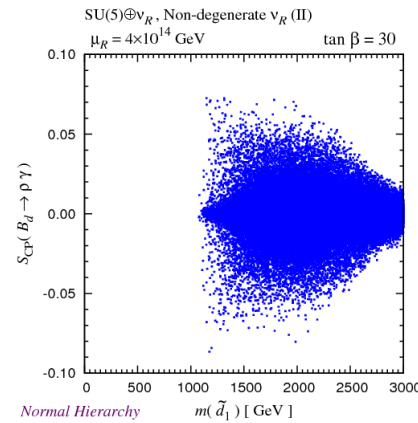
## $D\nu_R$ -NH



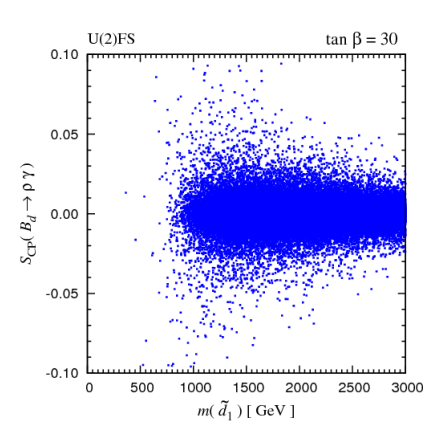
## $ND\nu_R$ (I)-NH



## $ND\nu_R$ (II)-NH



## $U(2)FS$

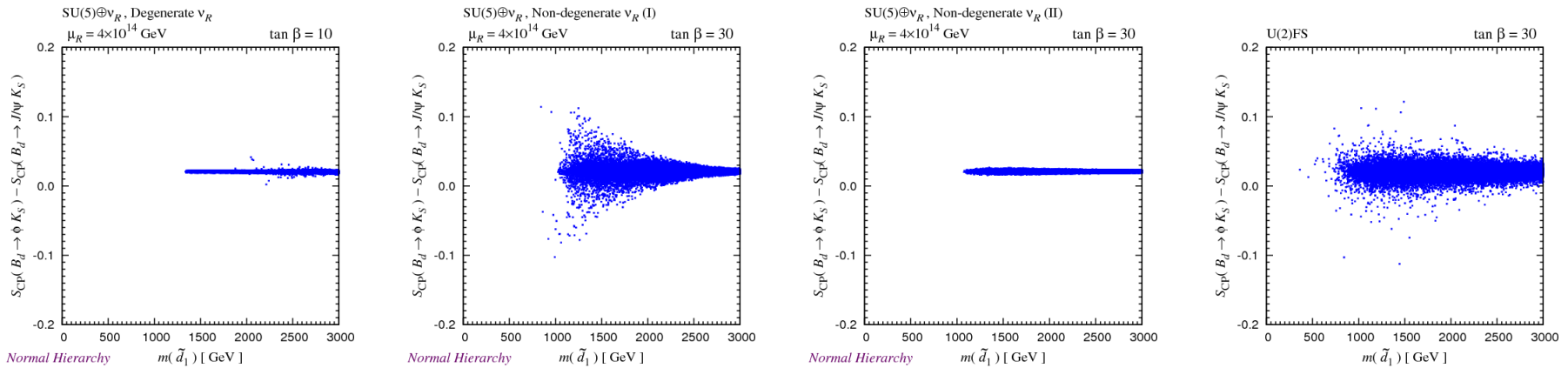


## $S_{CP}(B_d \rightarrow \rho \gamma)$ vs. $m(\tilde{d}_1)$

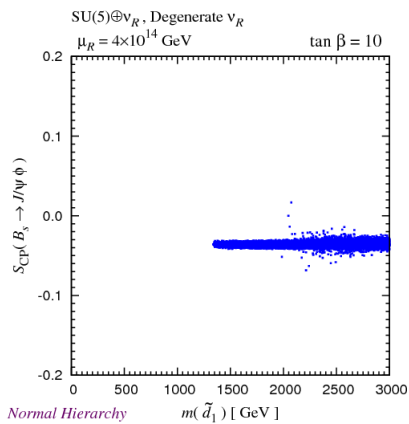
# $S_{CP}(B_d \rightarrow \phi K_S), S_{CP}(B_s \rightarrow J/\psi\phi)$ [ $b \rightarrow s$ ]

Significant in  $SU(5) \oplus \nu_R$ ,  $U(2)FS$ ; small in mSUGRA,  $MSSM \oplus \nu_R$ .

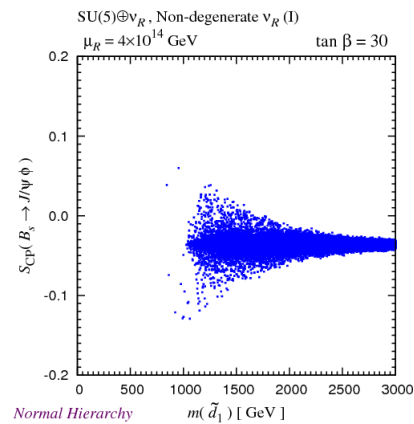
## $S_{CP}(B_d \rightarrow \phi K_S) - S_{CP}(B_d \rightarrow J/\psi K_S)$ vs. $m(\tilde{d}_1)$



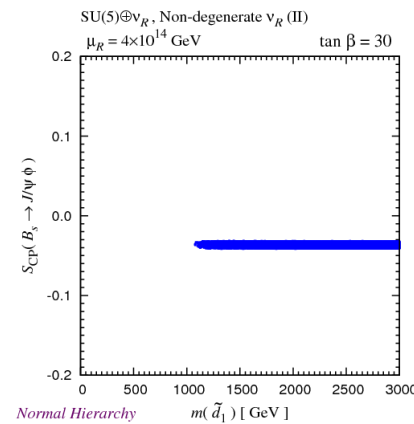
## $D\nu_R$ -NH



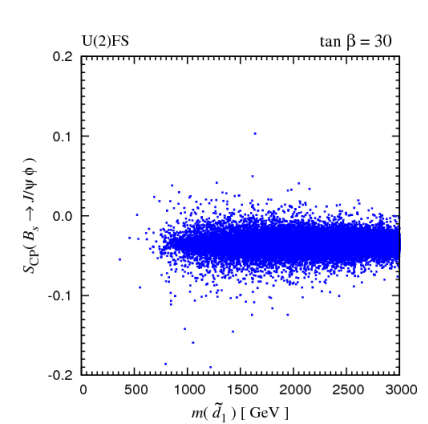
## $ND\nu_R$ (I)-NH



## $ND\nu_R$ (II)-NH



## $U(2)FS$



## $S_{CP}(B_s \rightarrow J/\psi\phi)$ vs. $m(\tilde{d}_1)$

## Summary: LFV

Model	$\mu \rightarrow e\gamma$	$\tau \rightarrow \mu\gamma$	$\tau \rightarrow e\gamma$
<b>MSSM <math>\oplus \nu_R</math></b>			
Degenerate $\nu_R$ , NH	✓		
Degenerate $\nu_R$ , IH	✓	✓	
Degenerate $\nu_R$ , D	✓	✓	
Non-degen. $\nu_R$ (I), NH		✓	
Non-degen. $\nu_R$ (II), NH			✓
<b>SU(5) <math>\oplus \nu_R</math></b>			
Degenerate $\nu_R$ , NH	✓		
Degenerate $\nu_R$ , IH	✓	✓	
Degenerate $\nu_R$ , D	✓	✓	
Non-degen. $\nu_R$ (I), NH	✓	✓	
Non-degen. $\nu_R$ (II), NH	✓		✓
Exp. sensitivity	$10^{-13}$ MEG	$2 - 8 \times 10^{-9}$ SuperB@50 – 75ab <sup>-1</sup>	

✓:  $B(\mu \rightarrow e\gamma) \sim 10^{-11}$ ,  $B(\tau \rightarrow \mu(e)\gamma) \sim 10^{-8}$  possible.

## Summary: Time-dependent CPV in $b \rightarrow s(d)$

	$S_{\text{CP}}(K^*\gamma)$	$S_{\text{CP}}(\rho\gamma)$	$\Delta S_{\text{CP}}(\phi K_S)$	$S_{\text{CP}}(B_s \rightarrow J/\psi\phi)$
SU(5) $\oplus\nu_R$				
D $\nu_R$ , NH	$\sim 0.01$	$\sim 0.01$	$\sim 0.01$	$\sim 0.01$
D $\nu_R$ , IH	$\sim 0.2$	$\sim 0.02$	$\sim 0.2$	$\sim 0.1$
D $\nu_R$ , D	$\sim 0.01$	$\sim 0.01$	$\sim 0.01$	$\sim 0.01$
ND $\nu_R$ (I), NH	$\sim 0.2$		$\sim 0.1$	$\sim 0.1$
ND $\nu_R$ (II), NH		$\sim 0.1$		
U(2)FS	$\sim 0.2$	$\sim 0.1$	$\sim 0.1$	$\sim 0.1$
Exp. precision	0.02 – 0.03	0.08 – 0.12	0.02 – 0.03	$\sim 0.01$
		SuperB@50 – 75ab $^{-1}$		LHCb@10fb $^{-1}$

- Small in mSUGRA, MSSM $\oplus\nu_R$ .

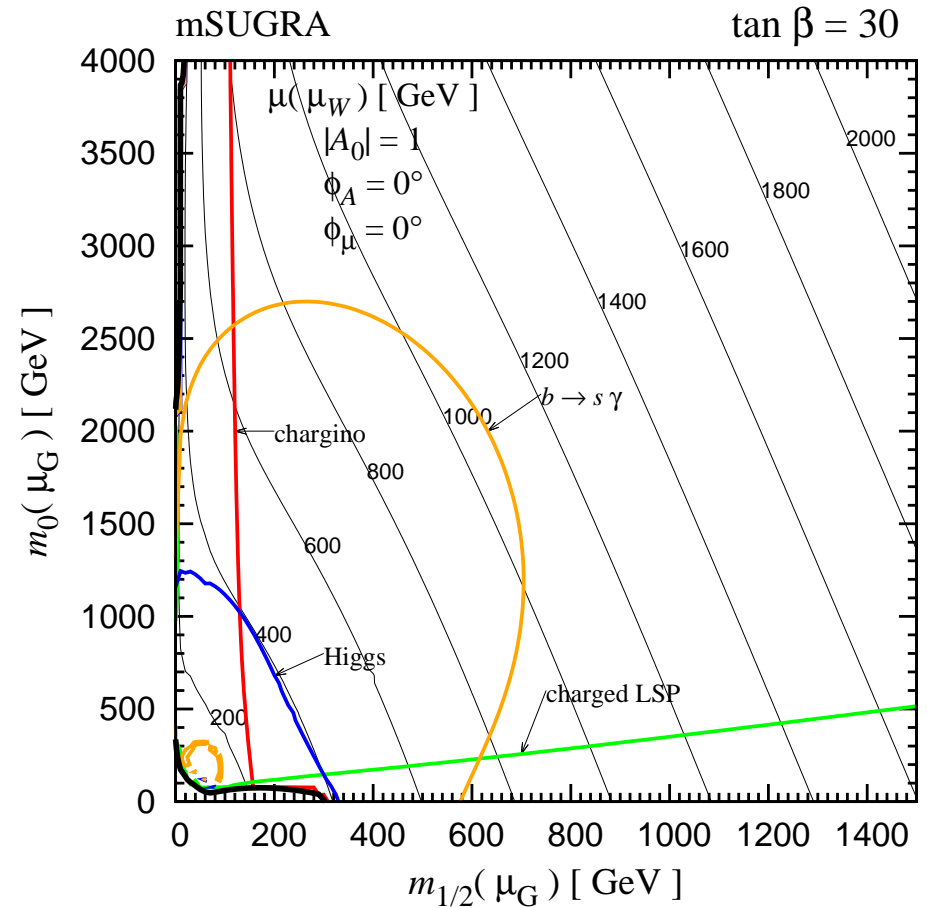
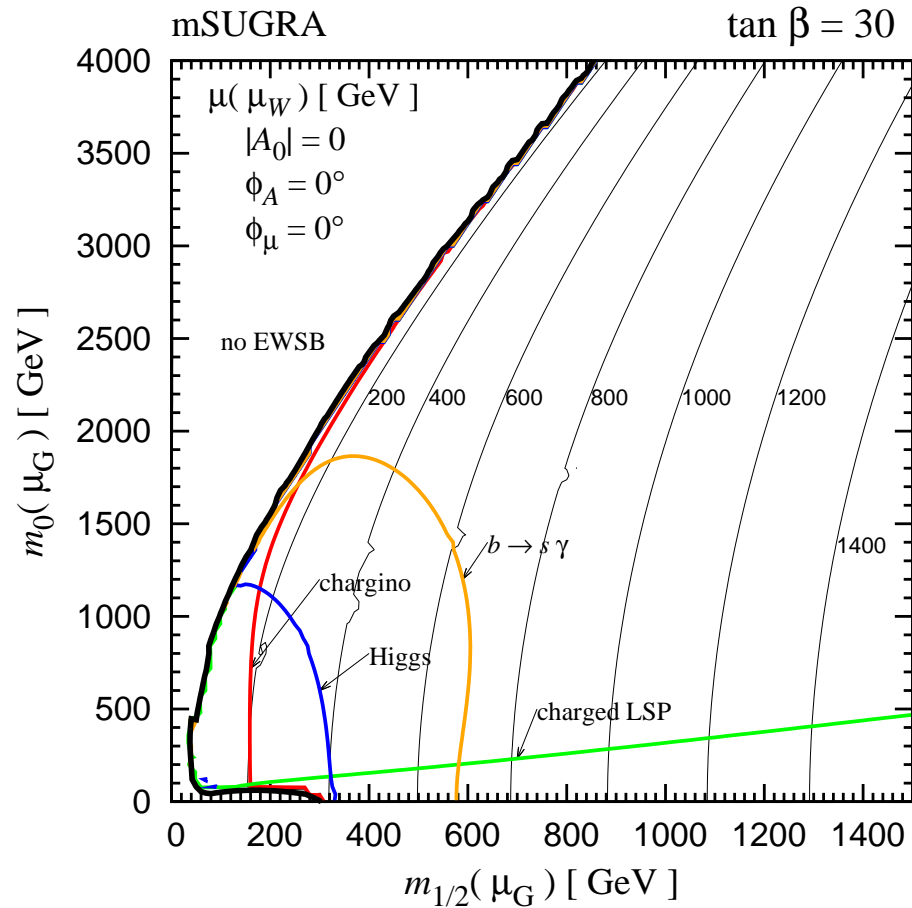


## Conclusion

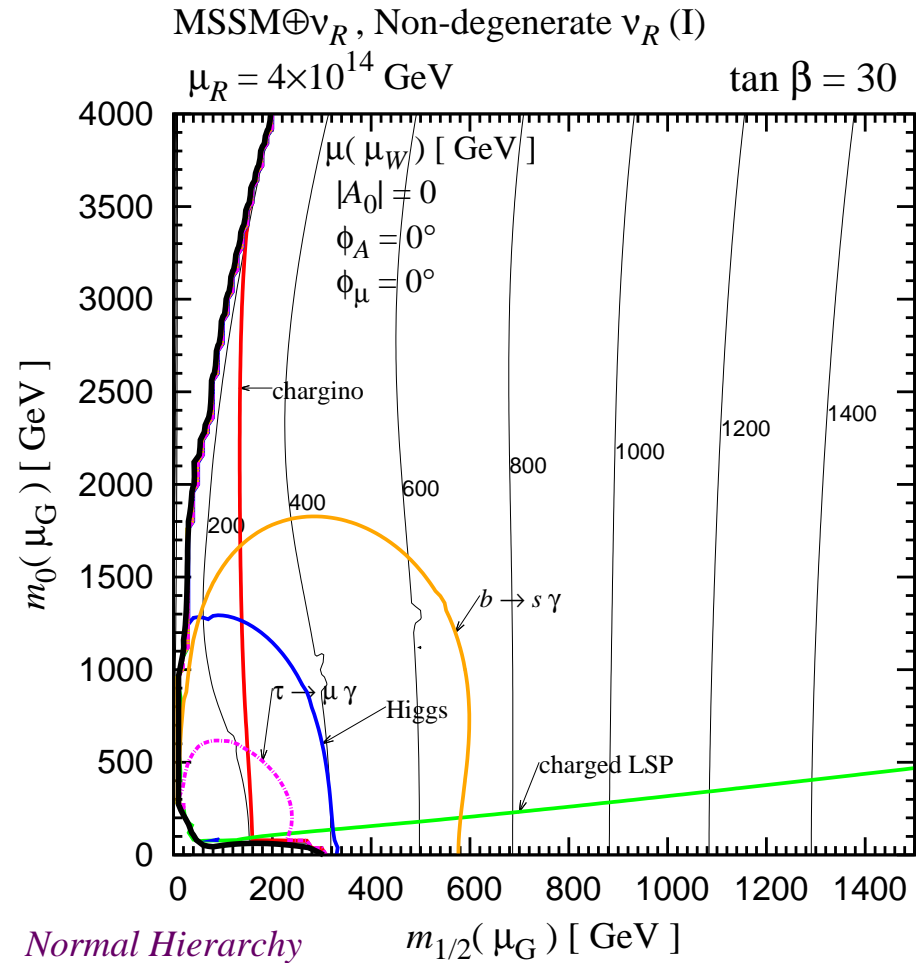
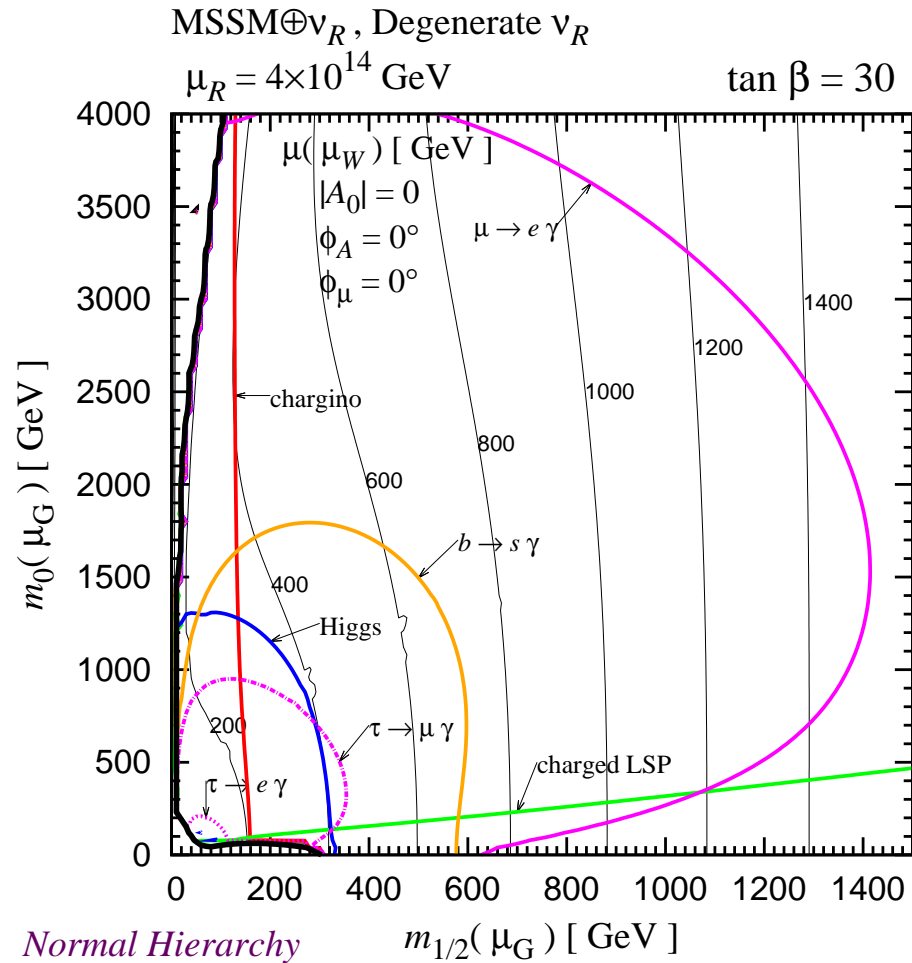
- Quark and lepton flavor signals are studied for SUSY models with various flavor structures.
- Each model gives different pattern of signals in  $b \rightarrow s$ ,  $b \rightarrow d$  and LFV processes.
- Measuring many processes is important to explore flavor structure of new physics beyond the SM.
- Reducing theoretical (hadronic) uncertainties in SM predictions to  $O(\%)$  level is important.

# Backups

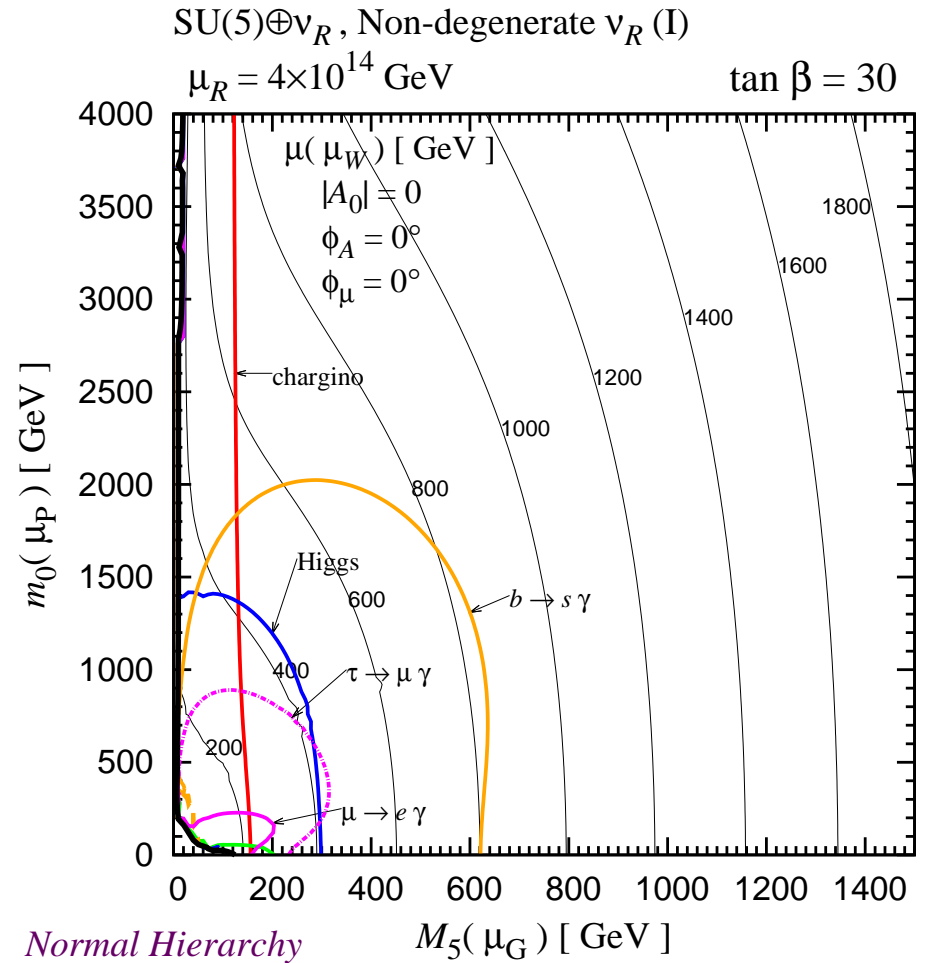
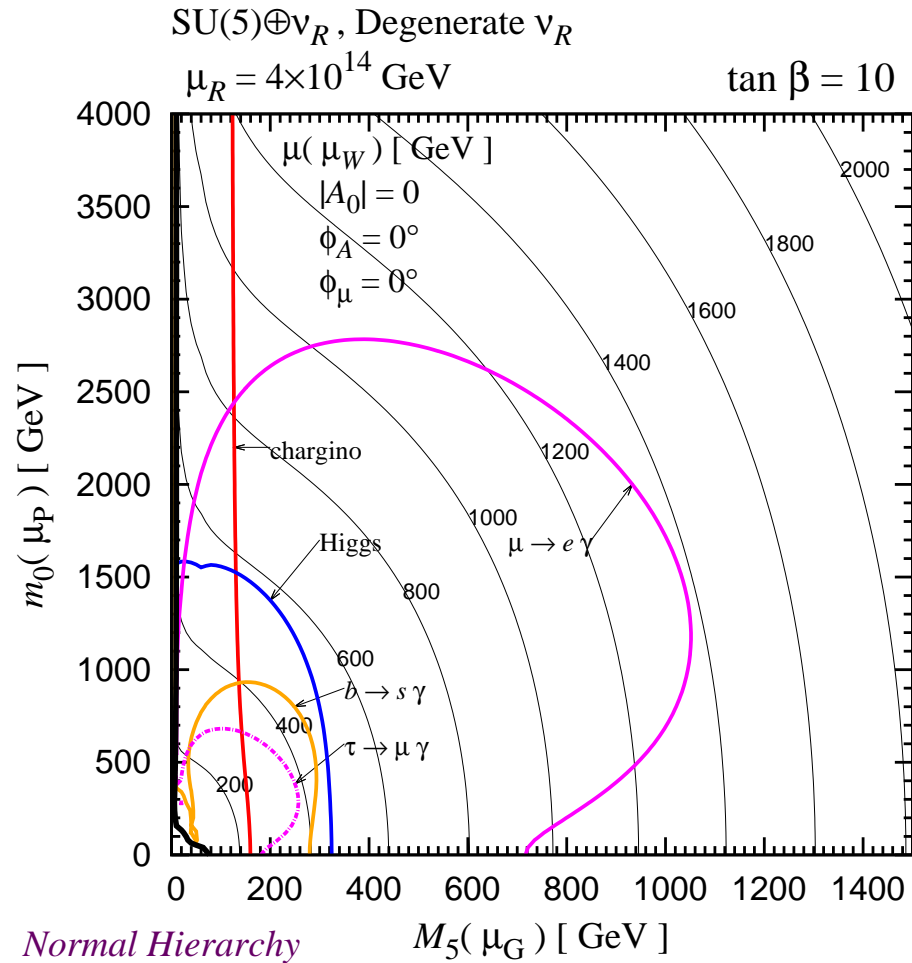
# Allowed parameter space: mSUGRA



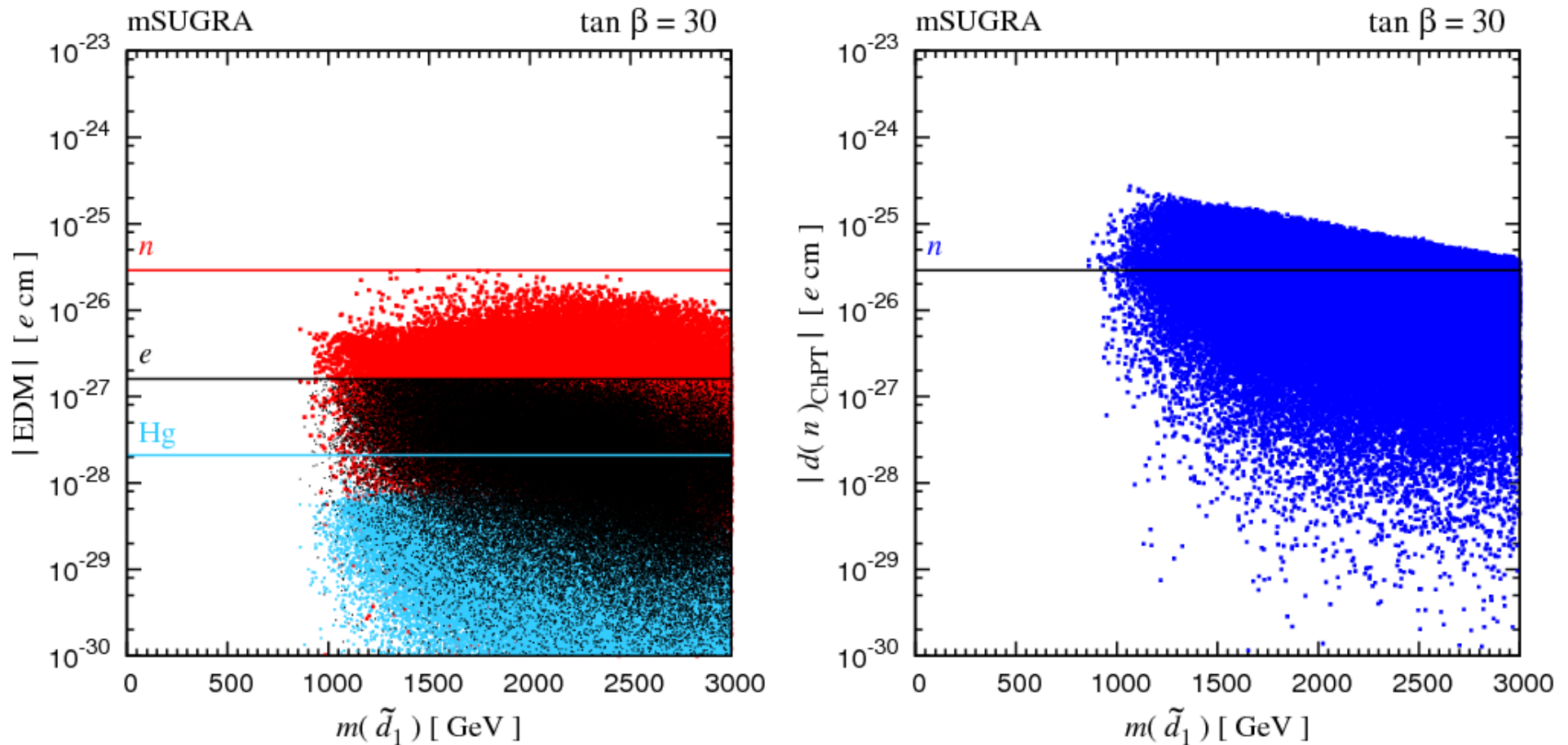
# Allowed parameter space: $MSSM \otimes \nu_R$



# Allowed parameter space: $SU(5) \otimes \nu_R$



# Neutron EDM: naive quark model vs. chiral perturbation theory



- Source:  $\phi_A$ .
- Large uncertainty in  $s$  quark contributions.