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**New observables in $\bar{B}_d \rightarrow \bar{K}^*(K\pi)\ell^+\ell^-$
and their sensitivity to new physics**

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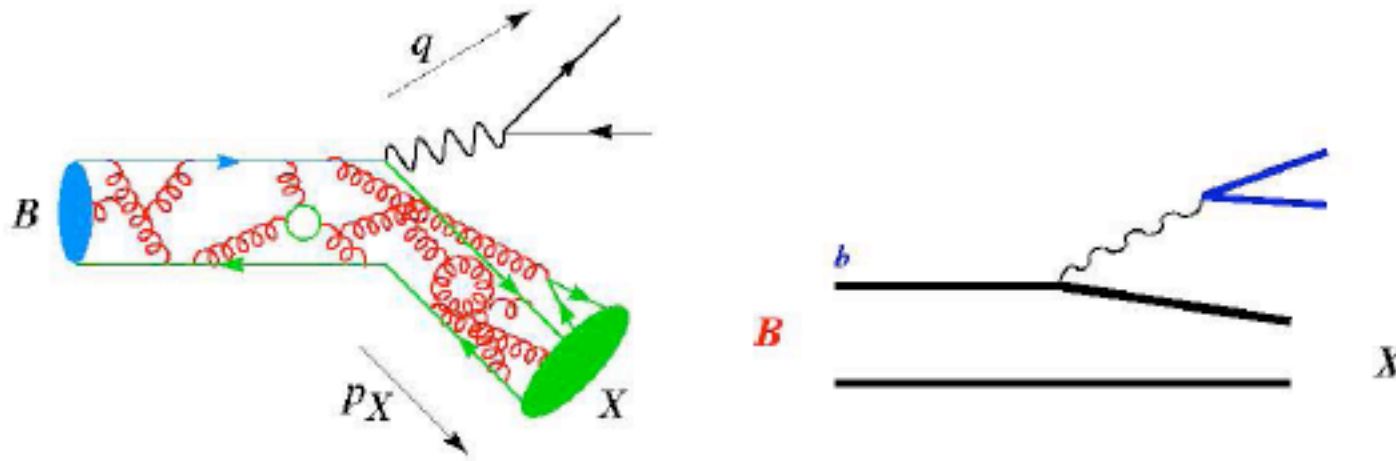
[arXiv:0807.2589 \[hep-ph\]](https://arxiv.org/abs/0807.2589)

CKM workshop, Rome, September 2008

Plan of the Talk

New observables in $\bar{B}_d \rightarrow \bar{K}^*(K\pi)\ell^+\ell^-$ and their sensitivity to new physics

- Motivation
- Angular distributions in $B \rightarrow K^*(\rightarrow K\pi)\ell^+\ell^-$
- Symmetries of angular distributions
- Theoretical framework, SCET formfactors
- Phenomenological discussion of new observables
 - Theoretical uncertainties
 - New physics sensitivity
 - Experimental sensitivity at LHCb



Crucial problem: Separation of new physics effects and hadronic uncertainties!
 Focus on theoretically clean observables is mandatory

Three strategies:

- focus on inclusive modes: operator product expansion (OPE)

$$\Gamma(B \rightarrow X_s \gamma) \xrightarrow{m_b \rightarrow \infty} \Gamma(b \rightarrow X_s^{\text{parton}} \gamma), \quad \Delta^{\text{nonpert.}} \sim \Lambda_{QCD}^2 / m_b^2$$

No linear term Λ_{QCD}/m_b (perturbatively calculable contribution dominant)

In general restricted to e^+e^- machines

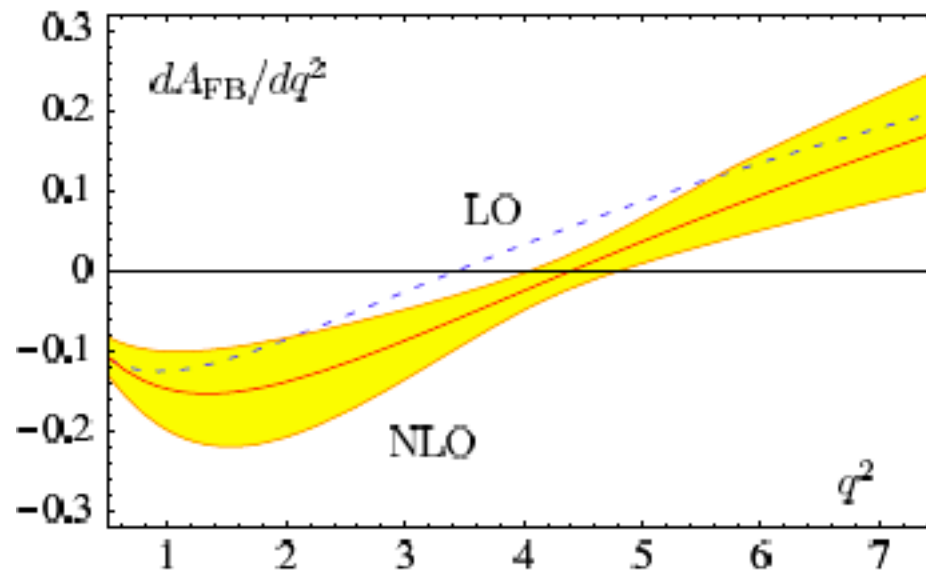
- focus on ratios of exclusive modes like asymmetries
 (hadronic uncertainties partially cancel out)

General strategy followed at LHCb

- focus on specific decays like $K \rightarrow \pi \nu \bar{\nu}$
 (hadronic matrix elements known from experiment)

LHCb Strategy: Focus on ratios of exclusive modes

Well-known example: Forward-Backward-Charge-Asymmetry in $B \rightarrow K^* \ell^+ \ell^-$



- In contrast to the branching ratio the zero of the FBA is almost insensitive to hadronic uncertainties. At LO the zero depends on the short-distance Wilson coefficients only:

$$q_0^2 = q_0^2(C_7, C_9), \quad q_0^2 = (3.4 + 0.6 - 0.5) GeV^2 \quad (LO)$$

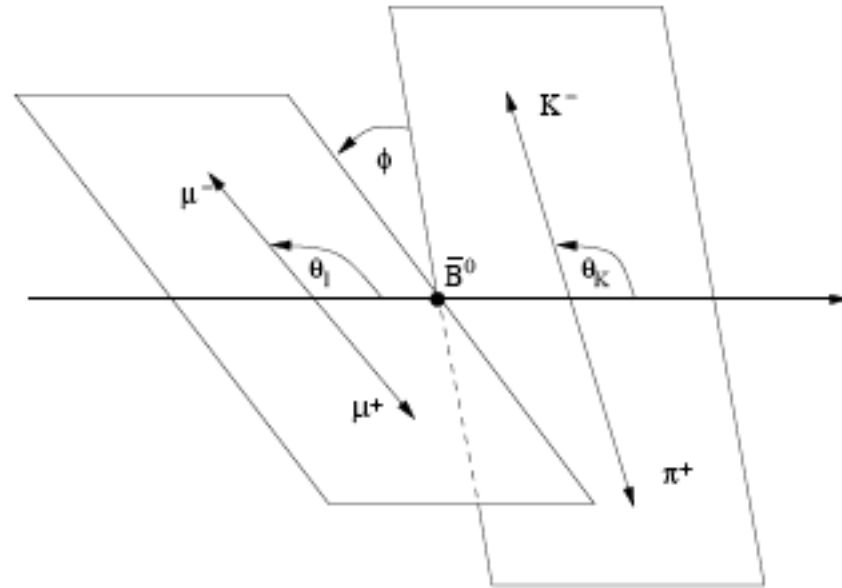
- NLO contribution calculated within QCD factorization approach leads to a large 30%-shift: (Beneke, Feldmann, Seidel 2001)

$$q_0^2 = (4.39 + 0.38 - 0.35) GeV^2 \quad (NLO)$$

- However: Issue of unknown power corrections (Λ/m_b) !

More opportunities in $B \rightarrow K^*(K\pi)\ell^+\ell^-$: angular distributions

Assuming the \bar{K}^* to be on the mass shell, the decay $\bar{B}^0 \rightarrow \bar{K}^{*0}(\rightarrow K^-\pi^+)\ell^+\ell^-$ described by the lepton-pair invariant mass, s , and the three angles θ_l , θ_{K^*} , ϕ .



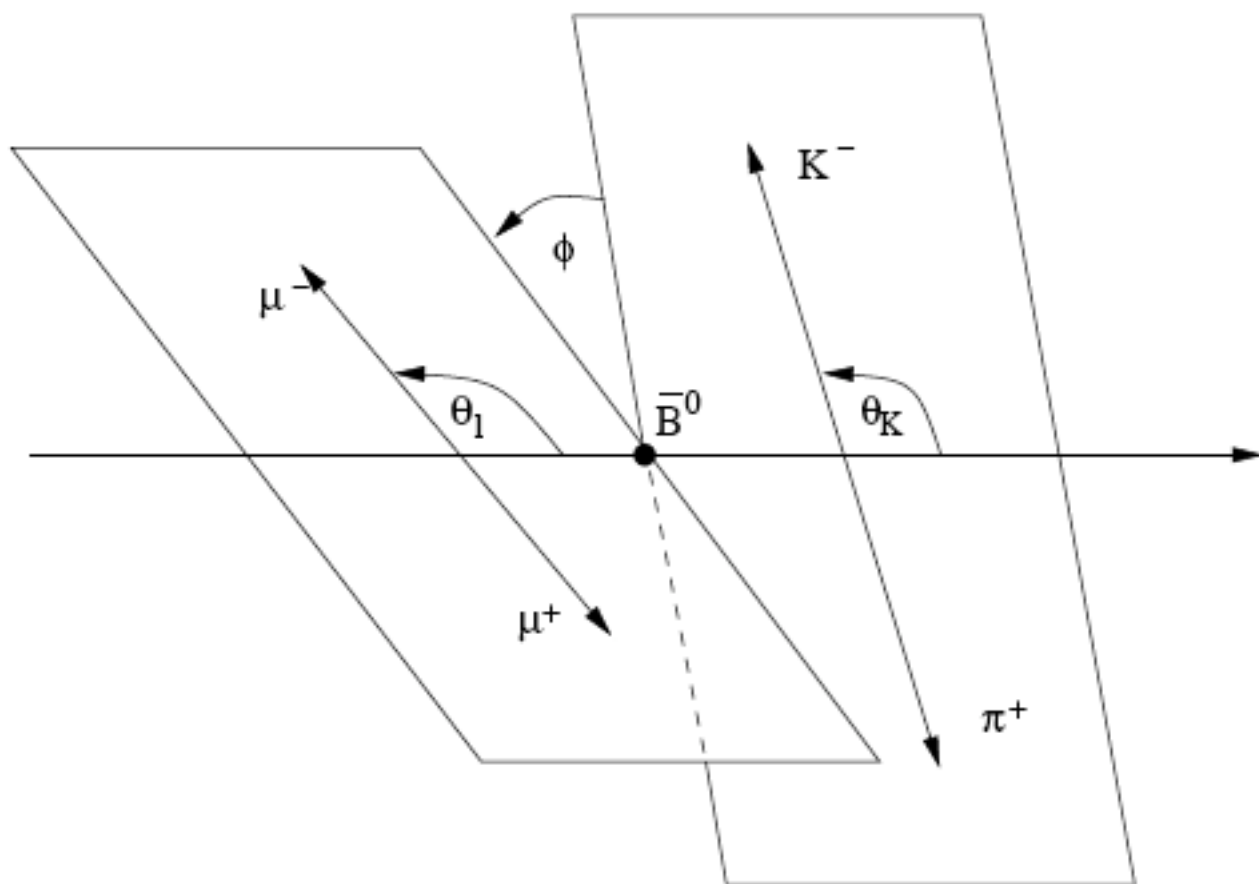
After summing over the spins of the final particles:

$$\frac{d^4\Gamma_{\bar{B}_d}}{dq^2 d\theta_l d\theta_K d\phi} = \frac{9}{32\pi} I(q^2, \theta_l, \theta_K, \phi) \sin\theta_l \sin\theta_K$$

$$I = I_1 + I_2 \cos 2\theta_l + I_3 \sin^2 \theta_l \cos 2\phi + I_4 \sin 2\theta_l \cos \phi + I_5 \sin \theta_l \cos \phi + I_6 \cos \theta_l \\ + I_7 \sin \theta_l \sin \phi + I_8 \sin 2\theta_l \sin \phi + I_9 \sin^2 \theta_l \sin 2\phi.$$

LHCb statistics ($10fb^{-1}$, $\succ 2fb^{-1}$) allows for a full angular fit!

More on kinematics:



z axis: Direction of anti- K^{*0} in rest frame of anti- B_d

θ_l : Angle between μ^- and z axis in $\mu\mu$ rest frame

θ_K : Angle between K^- and z axis in anti- K^* rest frame

ϕ : Angle between the anti- K^* and $\mu\mu$ decay planes

$$\mathbf{e}_z = \frac{\mathbf{p}_{K^-} + \mathbf{p}_{\pi^+}}{|\mathbf{p}_{K^-} + \mathbf{p}_{\pi^+}|}, \quad \mathbf{e}_l = \frac{\mathbf{p}_{\mu^-} \times \mathbf{p}_{\mu^+}}{|\mathbf{p}_{\mu^-} \times \mathbf{p}_{\mu^+}|}, \quad \mathbf{e}_K = \frac{\mathbf{p}_{K^-} \times \mathbf{p}_{\pi^+}}{|\mathbf{p}_{K^-} \times \mathbf{p}_{\pi^+}|}$$

$$\cos \theta_l = \frac{\mathbf{q}_{\mu^-} \cdot \mathbf{e}_z}{|\mathbf{q}_{\mu^-}|}, \quad \cos \theta_K = \frac{\mathbf{r}_{K^-} \cdot \mathbf{e}_z}{|\mathbf{r}_{K^-}|}, \quad \sin \phi = (\mathbf{e}_l \times \mathbf{e}_K) \cdot \mathbf{e}_z, \quad \cos \phi = \mathbf{e}_K \cdot \mathbf{e}_l$$

Angular distributions functions depend on the 6 complex K^* spin amplitudes

$$I_i = I_i(A_{\perp L/R}, A_{\parallel L/R}, A_{0L/R}) \quad (\text{limit } m_{\text{lepton}} = 0)$$

Helicity amplitudes: $A_{\perp, \parallel} = (H_{+1} \mp H_{-1})/\sqrt{2}, \quad A_0 = H_0,$

$$I_1 = \frac{3}{4} (|A_{\perp L}|^2 + |A_{\parallel L}|^2 + (L \rightarrow R)) \sin^2 \theta_K + (|A_{0L}|^2 + |A_{0R}|^2) \cos^2 \theta_K$$

$$\equiv a \sin^2 \theta_K + b \cos^2 \theta_K,$$

$$I_2 = \frac{1}{4} (|A_{\perp L}|^2 + |A_{\parallel L}|^2) \sin^2 \theta_K - |A_{0L}|^2 \cos^2 \theta_K + (L \rightarrow R)$$

$$\equiv c \sin^2 \theta_K + d \cos^2 \theta_K,$$

$$I_3 = \frac{1}{2} \left[(|A_{\perp L}|^2 - |A_{\parallel L}|^2) \sin^2 \theta_K + (L \rightarrow R) \right] \equiv e \sin^2 \theta_K,$$

$$I_4 = \frac{1}{\sqrt{2}} \left[\text{Re}(A_{0L} A_{\parallel L}^*) \sin 2\theta_K + (L \rightarrow R) \right] \equiv f \sin 2\theta_K,$$

$$I_5 = \sqrt{2} \left[\text{Re}(A_{0L} A_{\perp L}^*) \sin 2\theta_K - (L \rightarrow R) \right] \equiv g \sin 2\theta_K,$$

$$I_6 = 2 \left[\text{Re}(A_{\parallel L} A_{\perp L}^*) \sin^2 \theta_K - (L \rightarrow R) \right] \equiv h \sin^2 \theta_K,$$

$$I_7 = \sqrt{2} \left[\text{Im}(A_{0L} A_{\parallel L}^*) \sin 2\theta_K - (L \rightarrow R) \right] \equiv j \sin 2\theta_K,$$

$$I_8 = \frac{1}{\sqrt{2}} \left[\text{Im}(A_{0L} A_{\perp L}^*) \sin 2\theta_K + (L \rightarrow R) \right] \equiv k \sin 2\theta_K,$$

$$I_9 = \left[\text{Im}(A_{\parallel L}^* A_{\perp L}) \sin^2 \theta_K + (L \rightarrow R) \right] \equiv m \sin^2 \theta_K.$$

11 coefficients to be fixed in the full angular fit, but $a = 3c$ and $b = -d$

?

12 theoretical independent amplitudes $A_j \Leftrightarrow$ 9 independent coefficient functions in I

Symmetries of the angular distribution functions $I_i = I_i(A_{\perp L/R}, A_{\parallel L/R}, A_{0L/R})$

(angular distribution spin averaged)

- Global phase transformation of the L amplitudes

$$A'_{\perp L} = e^{i\phi_L} A_{\perp L}, \quad A'_{\parallel L} = e^{i\phi_L} A_{\parallel L}, \quad A'_{0L} = e^{i\phi_L} A_{0L}$$

- Global phase transformations of the R amplitudes

$$A'_{\perp R} = e^{i\phi_R} A_{\perp R}, \quad A'_{\parallel R} = e^{i\phi_R} A_{\parallel R}, \quad A'_{0R} = e^{i\phi_R} A_{0R}$$

- Continuous L - R rotation

$$A'_{\perp L} = +\cos(\theta)A_{\perp L} - \sin(\theta)A_{\perp R}^*$$

$$A'_{\perp R} = +\sin(\theta)A_{\perp L} + \cos(\theta)A_{\perp R}^*$$

$$A'_{0L} = +\cos(\theta)A_{0L} - \sin(\theta)A_{0R}^*$$

$$A'_{0R} = +\sin(\theta)A_{0L} + \cos(\theta)A_{0R}^*$$

$$A'_{\parallel L} = +\cos(\theta)A_{\parallel L} + \sin(\theta)A_{\parallel R}^*$$

$$A'_{\parallel R} = -\sin(\theta)A_{\parallel L} + \cos(\theta)A_{\parallel R}^*$$

Only 9 amplitudes A_j are independent in respect to the angular distribution

Observables as $F(I_i)$ are also invariant under the 3 symmetries !

Standard theoretical framework

- Effective Hamiltonian describing the quark transition $b \rightarrow sl^+\ell^-$:

$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}}V_{tb}V_{ts}^* \sum_{i=1}^{10} [C_i(\mu)\mathcal{O}_i(\mu) + C'_i(\mu)\mathcal{O}'_i(\mu)]$$

We focus on magnetic and semi-leptonic operators and their chiral partners

$$\mathcal{O}_7 = \frac{e}{16\pi^2}m_b(\bar{s}\sigma_{\mu\nu}P_Rb)F^{\mu\nu}, \quad \mathcal{O}'_7 = \frac{e}{16\pi^2}m_b(\bar{s}\sigma_{\mu\nu}P_Lb)F^{\mu\nu}$$

$$\mathcal{O}_9 = \frac{e^2}{16\pi^2}(\bar{s}\gamma_\mu P_Lb)(\bar{\ell}\gamma^\mu\ell), \quad \mathcal{O}_{10} = \frac{e^2}{16\pi^2}(\bar{s}\gamma_\mu P_Lb)(\bar{\ell}\gamma^\mu\gamma_5\ell),$$

- Matrix element for the decay $\bar{B}_d \rightarrow \bar{K}^{*0}(\rightarrow K^-\pi^+)\ell^+\ell^-$:

$$\mathcal{M} = \frac{G_F\alpha}{\sqrt{2}\pi}V_{tb}V_{ts}^* \left\{ \left[C_9^{\text{eff}} \langle K\pi | (\bar{s}\gamma^\mu P_Lb) | B \rangle - \frac{2m_b}{q^2} \langle K\pi | \bar{s}i\sigma^{\mu\nu}q_\nu (C_7^{\text{eff}} P_R + C_7^{\text{eff}'} P_L)b | B \rangle \right] (\bar{\ell}\gamma_\mu\ell) \right. \\ \left. + C_{10} \langle K\pi | (\bar{s}\gamma^\mu P_Lb) | B \rangle (\bar{\ell}\gamma_\mu\gamma_5\ell) \right\}$$

- Hadronic matrix element parametrized in terms of $B \rightarrow K^*$ form factors:

$$\langle K^*(p_{K^*}) | \bar{s} \gamma_\mu P_{L,R} b | B(p) \rangle = i \epsilon_{\mu\nu\alpha\beta} \epsilon^{\nu*} p^\alpha q^\beta \frac{V(s)}{m_B + m_{K^*}} \mp \frac{1}{2} \left\{ \epsilon_\mu^* (m_B + m_{K^*}) A_1(s) \right. \\ \left. - (\epsilon^* \cdot q)(2p - q)_\mu \frac{A_2(s)}{m_B + m_{K^*}} - \frac{2m_{K^*}}{s} (\epsilon^* \cdot q) [A_3(s) - A_0(s)] q_\mu \right\}$$

$$\langle K^*(p_{K^*}) | \bar{s} i \sigma_{\mu\nu} q^\nu P_{R,L} b | B(p) \rangle = -i \epsilon_{\mu\nu\alpha\beta} \epsilon^{\nu*} p^\alpha q^\beta T_1(s) \pm \frac{1}{2} \left\{ [\epsilon_\mu^* (m_B^2 - m_{K^*}^2) \right. \\ \left. - (\epsilon^* \cdot q)(2p - q)_\mu] T_2(s) + (\epsilon^* \cdot q) \left[q_\mu - \frac{s}{m_B^2 - m_{K^*}^2} (2p - q)_\mu \right] T_3(s) \right\}$$

- Heavy-light form factors by means of QCD sum rules lead to uncertainties of 30% on the branching fractions

(Ali, Ball, Handoko, Hiller 2000)

Crucial theoretical input

- In the $m_B \rightarrow \infty$ and $E_{K^*} \rightarrow \infty$ limit

7 form factors ($A_i(s)/T_i(s)/V(s)$) reduce to 2 universal form factors ($\xi_{\perp}, \xi_{\parallel}$)

(Charles, Le Yaouanc, Oliver, Pène, Raynal 1999)

$$A_1(s) = \frac{2E_{K^*}}{m_B + m_{K^*}} \xi_{\perp}(E_{K^*}),$$

$$A_2(s) = \frac{m_B}{m_B - m_{K^*}} \left[\xi_{\perp}(E_{K^*}) - \xi_{\parallel}(E_{K^*}) \right],$$

$$A_0(s) = \frac{E_{K^*}}{m_{K^*}} \xi_{\parallel}(E_{K^*}),$$

$$V(s) = \frac{m_B + m_{K^*}}{m_B} \xi_{\perp}(E_{K^*}),$$

$$T_1(s) = \xi_{\perp}(E_{K^*}),$$

$$T_2(s) = \frac{2E_{K^*}}{m_B} \xi_{\perp}(E_{K^*}),$$

$$T_3(s) = \xi_{\perp}(E_{K^*}) - \xi_{\parallel}(E_{K^*}).$$

- Form factor relations broken by α_s and Λ/m_b corrections

- Large Energy Effective Theory \Rightarrow QCD factorization/Soft Collinear Effective Theory (IR structure of QCD)

Formal factorization formula for heavy-light formfactors within SCET approach (Beneke,Feldmann;Becher,Hill,Lange,Neubert;Bauer,Pirjol,Stewart)

- Factorizable and Non-factorizable α_s corrections have been calculated (NLO) (Beneke,Feldmann,Seidel 2001)
- Caveat: unknown Λ/m_b corrections to the factorization formula

- Above results are valid in the kinematic region in which

$$E_{K^*} \simeq \frac{m_B}{2} \left(1 - \frac{s}{m_B^2} + \frac{m_{K^*}^2}{m_B^2} \right) \quad \text{is large.}$$

We restrict our analysis to the dilepton mass region $s \in [1\text{GeV}^2, 6\text{GeV}^2]$

K^* spin amplitudes in the heavy quark and large energy limit

$$A_{\perp,\parallel} = (H_{+1} \mp H_{-1})/\sqrt{2}, \quad A_0 = H_0$$

$$A_{\perp L,R} = N\sqrt{2}\lambda^{1/2} \left[(C_9^{\text{eff}} \mp C_{10}) \frac{V(s)}{m_B + m_{K^*}} + \frac{2m_b}{s} (C_7^{\text{eff}} + C_7^{\text{eff}'}) T_1(s) \right]$$

$$A_{\parallel L,R} = -N\sqrt{2}(m_B^2 - m_{K^*}^2) \left[(C_9^{\text{eff}} \mp C_{10}) \frac{A_1(s)}{m_B - m_{K^*}} + \frac{2m_b}{s} (C_7^{\text{eff}} - C_7^{\text{eff}'}) T_2(s) \right]$$

$$A_{0L,R} = -\frac{N}{2m_{K^*}\sqrt{s}} \left[(C_9^{\text{eff}} \mp C_{10}) \left\{ (m_B^2 - m_{K^*}^2 - s)(m_B + m_{K^*}) A_1(s) - \lambda \frac{A_2(s)}{m_B + m_{K^*}} \right\} \right. \\ \left. + 2m_b(C_7^{\text{eff}} - C_7^{\text{eff}'}) \left\{ (m_B^2 + 3m_{K^*}^2 - s) T_2(s) - \frac{\lambda}{m_B^2 - m_{K^*}^2} T_3(s) \right\} \right]$$

$$A_{\perp L,R} = +\sqrt{2}N m_B (1 - \hat{s}) \left[(C_9^{\text{eff}} \mp C_{10}) + \frac{2\hat{m}_b}{\hat{s}} (C_7^{\text{eff}} + C_7^{\text{eff}'}) \right] \xi_{\perp}(E_{K^*})$$

$$A_{\parallel L,R} = -\sqrt{2}N m_B (1 - \hat{s}) \left[(C_9^{\text{eff}} \mp C_{10}) + \frac{2\hat{m}_b}{\hat{s}} (C_7^{\text{eff}} - C_7^{\text{eff}'}) \right] \xi_{\perp}(E_{K^*})$$

$$A_{0L,R} = -\frac{N m_B}{2\hat{m}_{K^*}\sqrt{\hat{s}}} (1 - \hat{s})^2 \left[(C_9^{\text{eff}} \mp C_{10}) + 2\hat{m}_b (C_7^{\text{eff}} - C_7^{\text{eff}'}) \right] \xi_{\parallel}(E_{K^*})$$

In the SM ($C_7^{\text{eff}'} = 0$) we recover naive quark model prediction $A_{\perp} = -A_{\parallel}$

($H_+ = 0$) in the $m_B \rightarrow \infty$ and $E_{K^*} \rightarrow \infty$ limit.

Careful construction of observables

- Observables have to respect all symmetries of the angular distribution
- Good sensitivity to NP contributions, i.e. to $C_7^{eff'}$
- Small theoretical uncertainties
 - Dependence of soft form factors, ξ_{\perp} and ξ_{\parallel} , to be minimized !
form factors should cancel out exactly at LO, best for all s
 - unknown Λ/m_b power corrections
 - $A_{\perp,\parallel,0} = A_{\perp,\parallel,0}^0 (1 + c_{\perp,\parallel,0})$ vary c_i in a range of $\pm 10\%$ and also of $\pm 5\%$
 - Scale dependence of NLO result
 - Input parameters
- Good experimental resolution

Interesting observables

- Forward-backward asymmetry

$$A_{\text{FB}} \equiv \frac{1}{d\Gamma/dq^2} \left(\int_0^1 d(\cos\theta) \frac{d^2\Gamma[\bar{B} \rightarrow \bar{K}^* \ell^+ \ell^-]}{dq^2 d\cos\theta} - \int_{-1}^0 d(\cos\theta) \frac{d^2\Gamma[\bar{B} \rightarrow \bar{K}^* \ell^+ \ell^-]}{dq^2 d\cos\theta} \right)$$

$$A_{\text{FB}} = \frac{3 \operatorname{Re}(A_{\parallel L} A_{\perp L}^*) - \operatorname{Re}(A_{\parallel R} A_{\perp R}^*)}{2 (|A_0|^2 + |A_{\parallel}|^2 + |A_{\perp}|^2)}$$

Form factors cancel out at LO only for Zero.

- Longitudinal polarisation of K^*

$$F_L(s) = \frac{|A_0|^2}{|A_0|^2 + |A_{\parallel}|^2 + |A_{\perp}|^2}$$

Form factors do not cancel at LO (\rightarrow larger hadronic uncertainties)

- Transversity amplitude A_T^2 (Krüger, Matias 2005)

$$A_T^{(2)} = \frac{|A_{\perp}|^2 - |A_{\parallel}|^2}{|A_{\perp}|^2 + |A_{\parallel}|^2}$$

Sensitive to right-handed currents (in LO directly $\sim C_7^{eff'}$)

Formfactor cancel out at LO for all s

$$A_i A_j^* \equiv A_{iL}(q^2) A_{jL}^*(q^2) + A_{iR}(q^2) A_{jR}^*(q^2) \quad (i, j = 0, \parallel, \perp)$$

Projection fit possible for $A_T^{(2)}$, F_L , A_{FB}

$$\frac{d\Gamma'}{d\phi} = \frac{\Gamma'}{2\pi} \left(1 + \frac{1}{2}(1 - F_L)A_T^{(2)} \cos 2\phi + A_{\text{Im}} \sin 2\phi \right), \quad \Gamma' = \frac{d\Gamma}{dq^2}$$

$$\frac{d\Gamma'}{d\theta_l} = \Gamma' \left(\frac{3}{4}F_L \sin^2 \theta_l + \frac{3}{8}(1 - F_L)(1 + \cos^2 \theta_l) + A_{\text{FB}} \cos \theta_l \right) \sin \theta_l,$$

$$\frac{d\Gamma'}{d\theta_K} = \frac{3\Gamma'}{4} \sin \theta_K (2F_L \cos^2 \theta_K + (1 - F_L) \sin^2 \theta_K),$$

Observables appear linearly, fits performed on data binned in q^2

First experimental measurements with limited accuracy is possible

But: $A_T^{(2)}$ suppressed by $1 - F_L$

Full angular fit is superior, once the data set is large enough ($\gtrsim 2fb^{-1}$)

much better resolution (factor 3 even in $A_T^{(2)}$)

New observables are available

Unbinned analysis, q^2 dependence parametrised by polynomial

New observables

By inspection of the K^* spin amplitudes in terms of Wilson coefficients and SCET form factors one identifies further observables

- sensitive to $C_7^{eff'}$
- invariant under 3 $R-L$ symmetries
- theoretical clean
- with high experimental resolution

$$A_T^{(3)} = \frac{|A_{0L}A_{\parallel L}^* - A_{0R}^*A_{\parallel R}|}{\sqrt{|A_0|^2|A_{\perp}|^2}} \quad A_T^{(4)} = \frac{|A_{0L}A_{\perp L}^* - A_{0R}^*A_{\perp R}|}{|A_{0L}^*A_{\parallel L} + A_{0R}A_{\parallel R}^*|}$$

Next step: design of observables sensitive to other new physics operators

- Transversity amplitude A_T^1

Defining the helicity distributions Γ_{\pm} as $\Gamma_{\pm} = |H_{\pm 1}^L|^2 + |H_{\pm 1}^R|^2$

one can define (Melikhov, Nikitin, Simula 1998)

$$A_T^{(1)} = \frac{\Gamma_- - \Gamma_+}{\Gamma_- + \Gamma_+} \quad A_T^{(1)} = \frac{-2\text{Re}(A_{\parallel} A_{\perp}^*)}{|A_{\perp}|^2 + |A_{\parallel}|^2}$$

Very sensitive to right-handed currents (Lunghi, Matias 2006)

Very insensitive to Λ/m_b corrections

Formfactor cancel out at LO for all s

Big surprise:

$A_T^{(1)}$ is not invariant under the symmetries of the angular distribution

- $A_T^{(1)}$ cannot be extracted from the full angular distribution
- LHCb: practically not possible to measure the helicity of the final states on a event-by-event basis (neither as statistical distribution)
- Not a principal problem, but $A_T^{(1)}$ not an observable at LHCb or at Super B (measure three-momentum and charge)

Phenomenological analysis

Analysis of SM and models with additional right handed currents ($C_7^{eff'}$)

Specific model:

MSSM with non-minimal flavour violation in the down squark sector

4 benchmark points

Diagonal: $\mu = M_1 = M_2 = M_{H^+} = m_{\tilde{u}_R} = 1 \text{ TeV}$ $\tan \beta = 5$

- **Scenario A:** $m_{\tilde{g}} = 1 \text{ TeV}$ and $m_{\tilde{d}} \in [200, 1000] \text{ GeV}$

$$-0.1 \leq (\delta_{LR}^d)_{32} \leq 0.1$$

a) $m_{\tilde{g}}/m_{\tilde{d}} = 2.5$, $(\delta_{LR}^d)_{32} = 0.016$

b) $m_{\tilde{g}}/m_{\tilde{d}} = 4$, $(\delta_{LR}^d)_{32} = 0.036$.

- **Scenario B:** $m_{\tilde{d}} = 1 \text{ TeV}$ and $m_{\tilde{g}} \in [200, 800] \text{ GeV}$
mass insertion as in Scenario A.

c) $m_{\tilde{g}}/m_{\tilde{d}} = 0.7$, $(\delta_{LR}^d)_{32} = -0.004$

d) $m_{\tilde{g}}/m_{\tilde{d}} = 0.6$, $(\delta_{LR}^d)_{32} = -0.006$.

Check of compatibility with other constraints (B physics, ρ parameter, Higgs mass, particle searches, vacuum stability constraints)

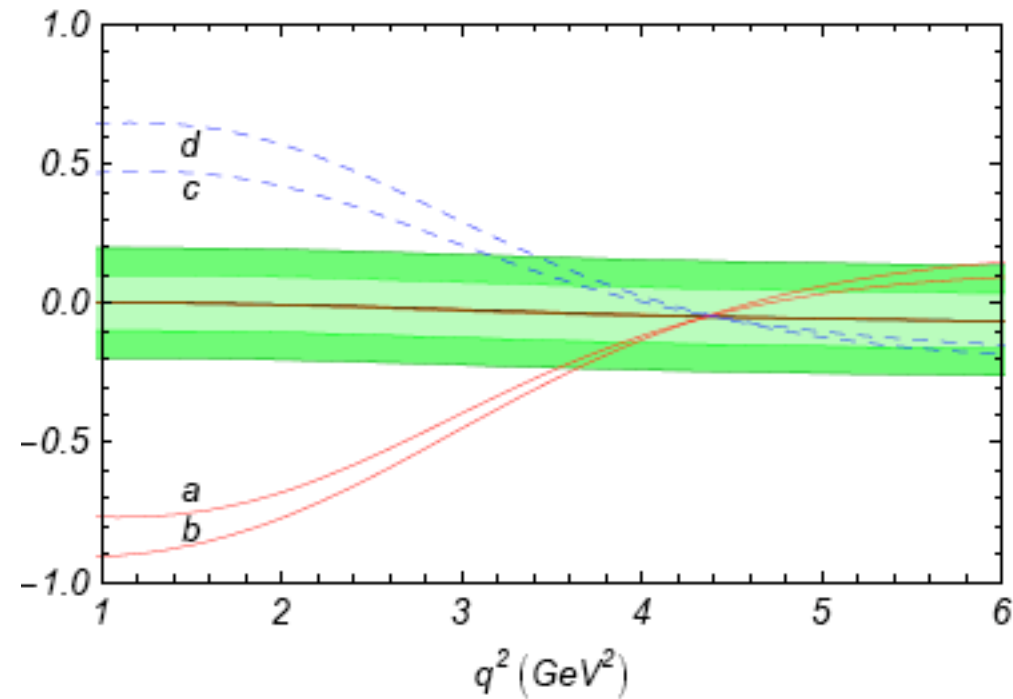
- NLO corrections included
- Λ/m_b corrections estimated for each amplitude as $\pm 10\%$ and $\pm 5\%$
this uncertainty fully dominant
- Input parameters:

m_B	$5.27950 \pm 0.00033 \text{ GeV}$	λ	0.2262 ± 0.0014
m_K	$0.896 \pm 0.040 \text{ GeV}$	A	0.815 ± 0.013
M_W	$80.403 \pm 0.029 \text{ GeV}$	$\bar{\rho}$	0.235 ± 0.031
M_Z	$91.1876 \pm 0.0021 \text{ GeV}$	$\bar{\eta}$	0.349 ± 0.020
$\hat{m}_t(\hat{m}_t)$	$172.5 \pm 2.7 \text{ GeV}$	$\Lambda_{\text{QCD}}^{(n_f=5)}$	$220 \pm 40 \text{ MeV}$
$m_{b,\text{PS}}(2 \text{ GeV})$	$4.6 \pm 0.1 \text{ GeV}$	$\alpha_s(M_Z)$	0.1176 ± 0.0002
m_c	$1.4 \pm 0.2 \text{ GeV}$	α_{em}	$1/137.035999679$
f_B	$200 \pm 30 \text{ MeV}$	$a_1(K^*)_{\perp, \parallel}$	0.20 ± 0.05
$f_{K^*,\perp}(1 \text{ GeV})$	$185 \pm 10 \text{ MeV}$	$a_2(K^*)_{\perp}$	0.06 ± 0.06
$f_{K^*,\parallel}$	$218 \pm 4 \text{ MeV}$	$a_2(K^*)_{\parallel}$	0.04 ± 0.04
$\xi_{K^*,\parallel}(0)$	0.16 ± 0.03	$\lambda_{B,+}(1.5 \text{ GeV})$	$0.485 \pm 0.115 \text{ GeV}$
$\xi_{K^*,\perp}(0)^{\text{¶}}$	0.26 ± 0.02		

$\xi_{K^*,\perp}(0)$ has been determined from experimental data.

Results

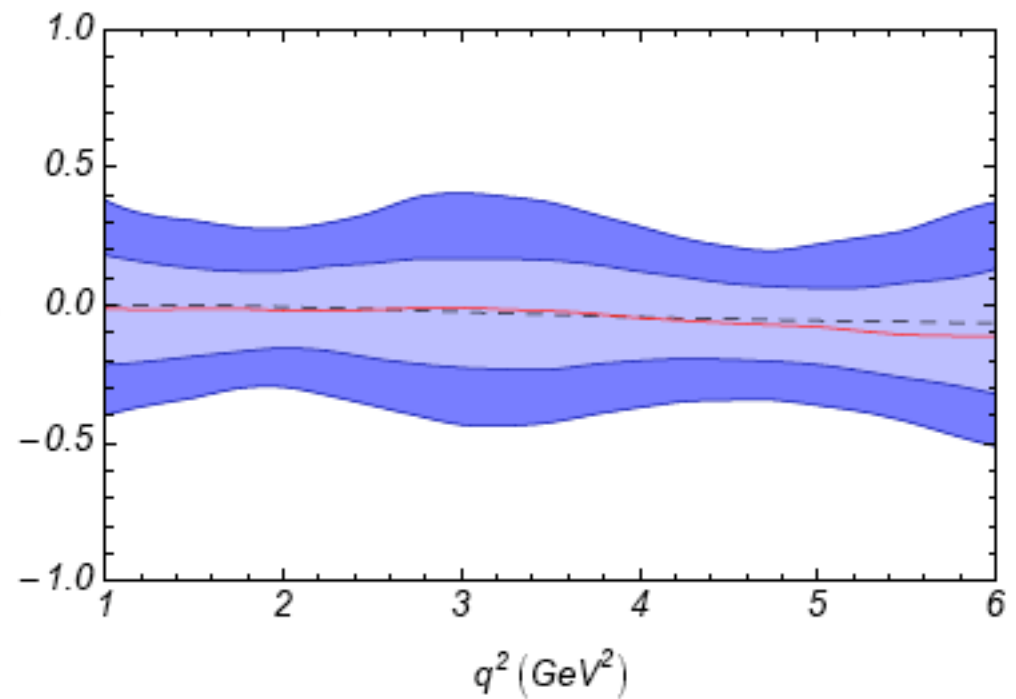
$$A_T^{(2)} = \frac{|A_\perp|^2 - |A_\parallel|^2}{|A_\perp|^2 + |A_\parallel|^2}$$



Theoretical sensitivity

light green $\pm 5\% \Lambda/m_b$

dark green $\pm 10\% \Lambda/m_b$

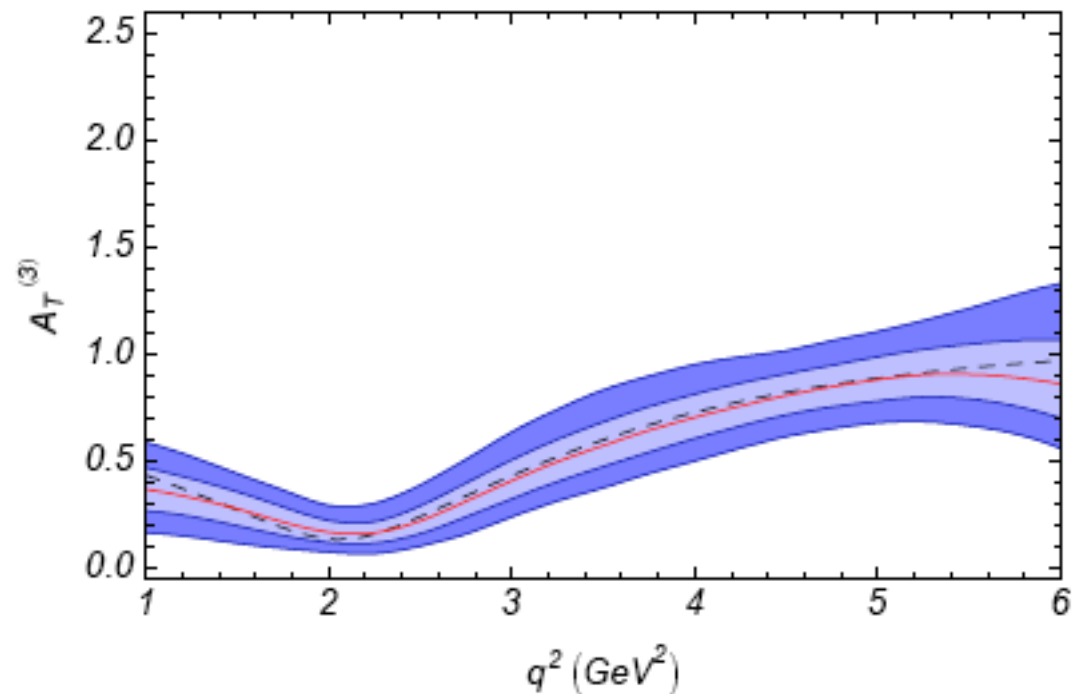
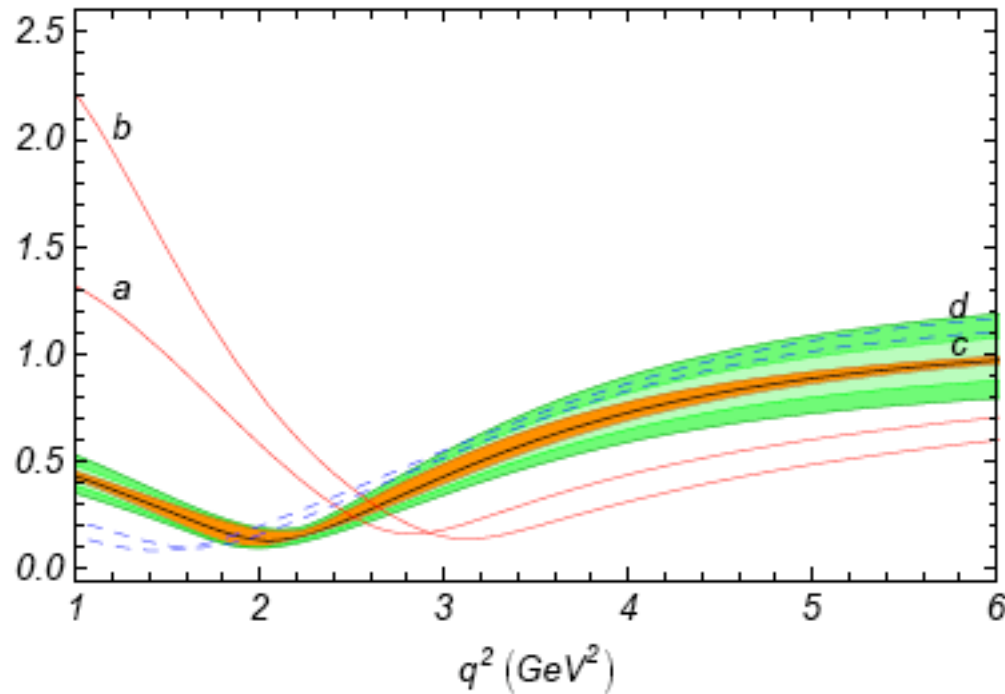


Experimental sensitivity $(10fb^{-1})$

light green 1σ

dark green 2σ

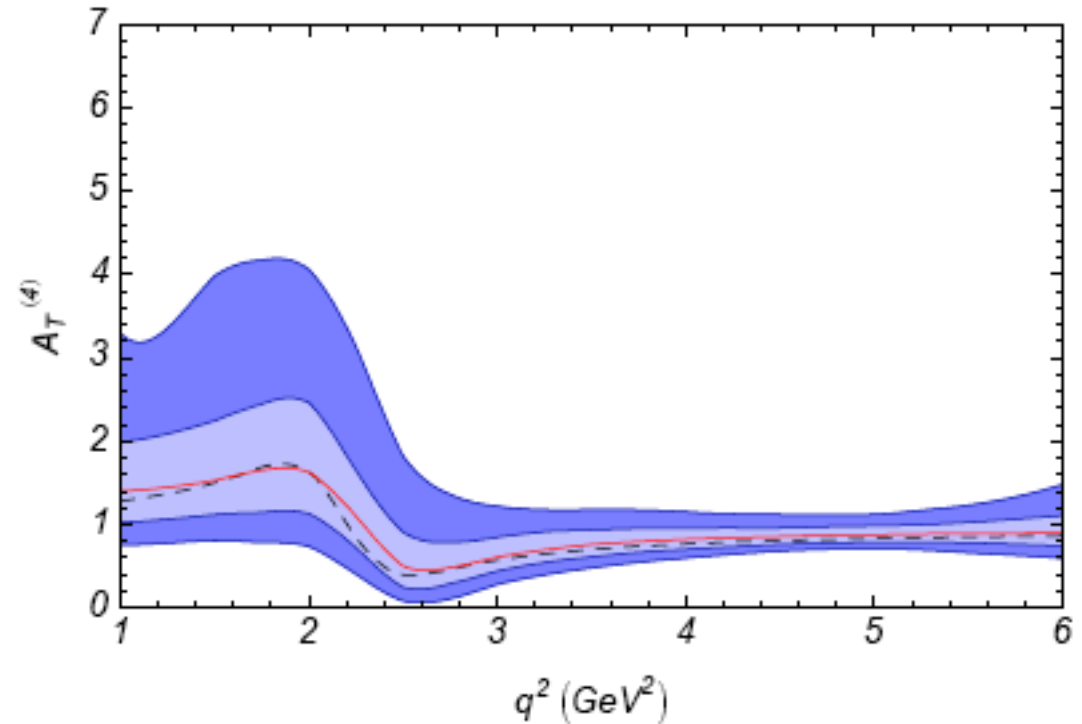
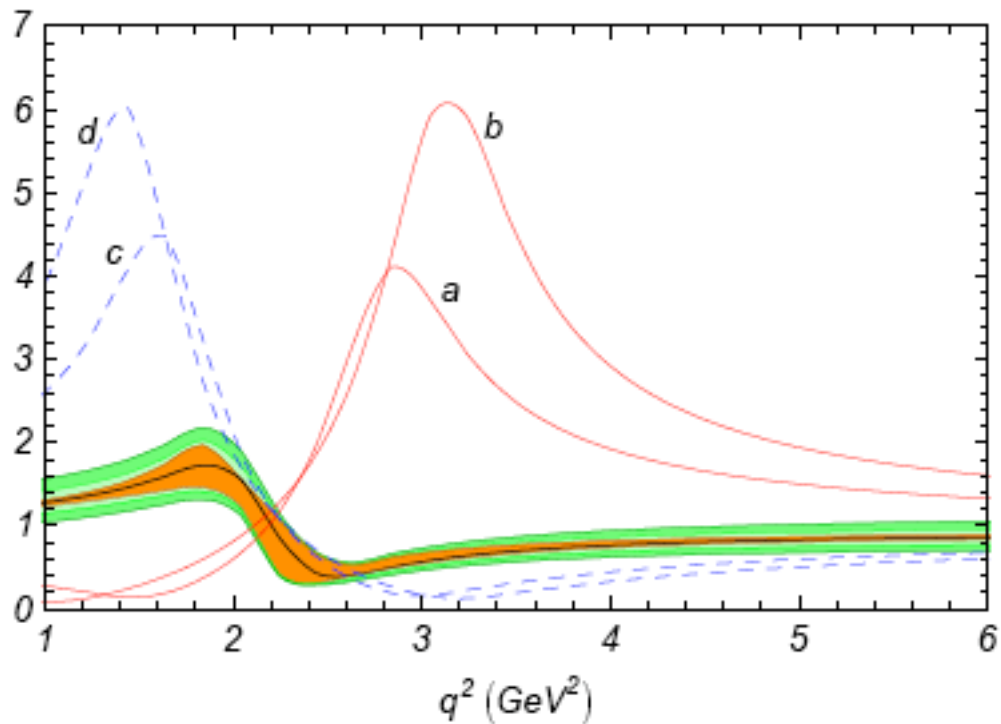
$$A_T^{(3)} = \left| \frac{A_{0L}A_{\parallel L}^* - A_{0R}^*A_{\parallel R}}{\sqrt{|A_0|^2 \times |A_{\perp}|^2}} \right|$$



New observables allow crosschecks

Different sensibility to $C_7^{eff'}$ via A_0 in $A_T^{(3)}$

$$A_T^{(4)} = \frac{|A_{0L}A_{\perp L}^* - A_{0R}^*A_{\perp R}|}{|A_{0L}^*A_{\parallel L} + A_{0R}A_{\parallel R}^*|}$$



Agreement between the central values extracted from the fit and the theoretical input is reasonable

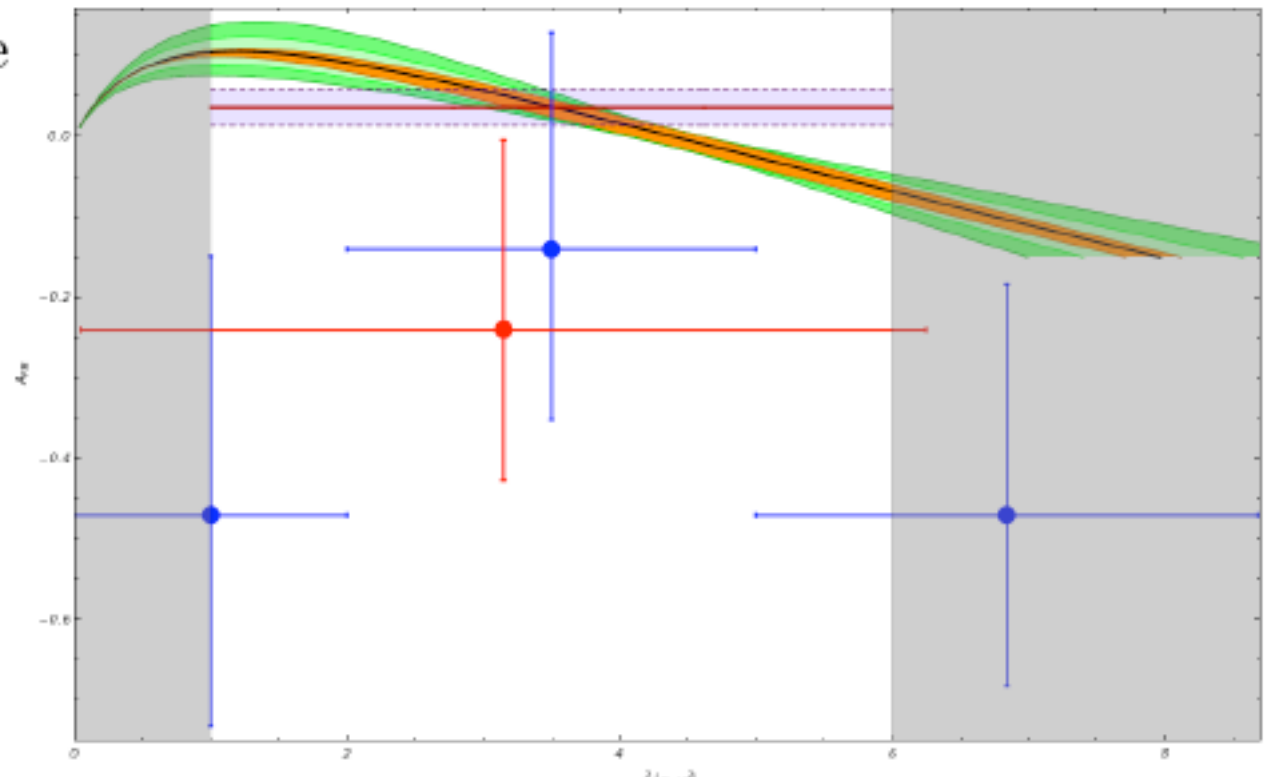
Polynomial of higher degree in fit needed in case of $100fb^{-1}$

old observables : data available

Babar FPCP 2008

Belle ICHEP 2008

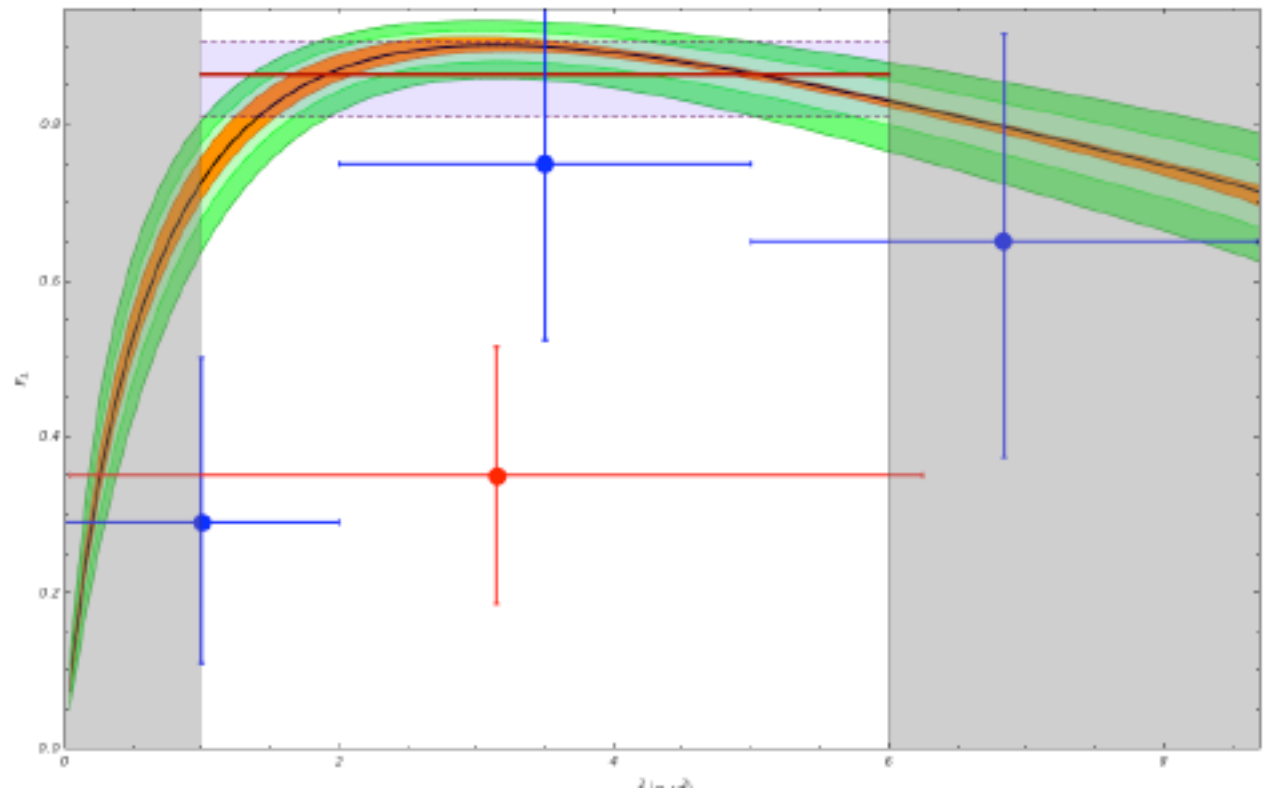
$$A_{FB} = \frac{3 \operatorname{Re}(A_{\parallel L} A_{\perp L}^*) - \operatorname{Re}(A_{\parallel R} A_{\perp R}^*)}{2 (|A_0|^2 + |A_{\parallel}|^2 + |A_{\perp}|^2)}$$



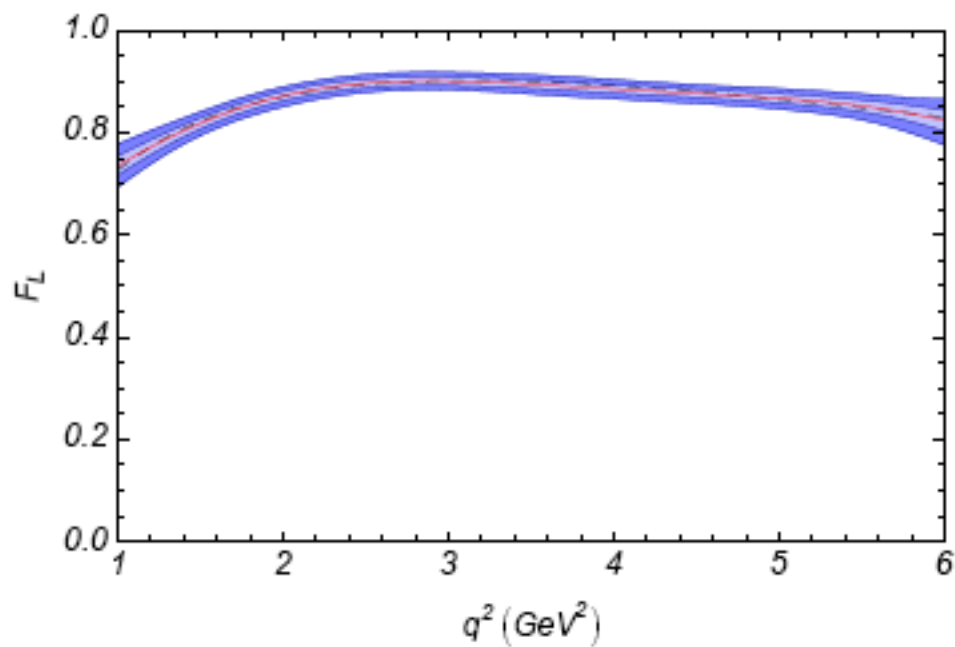
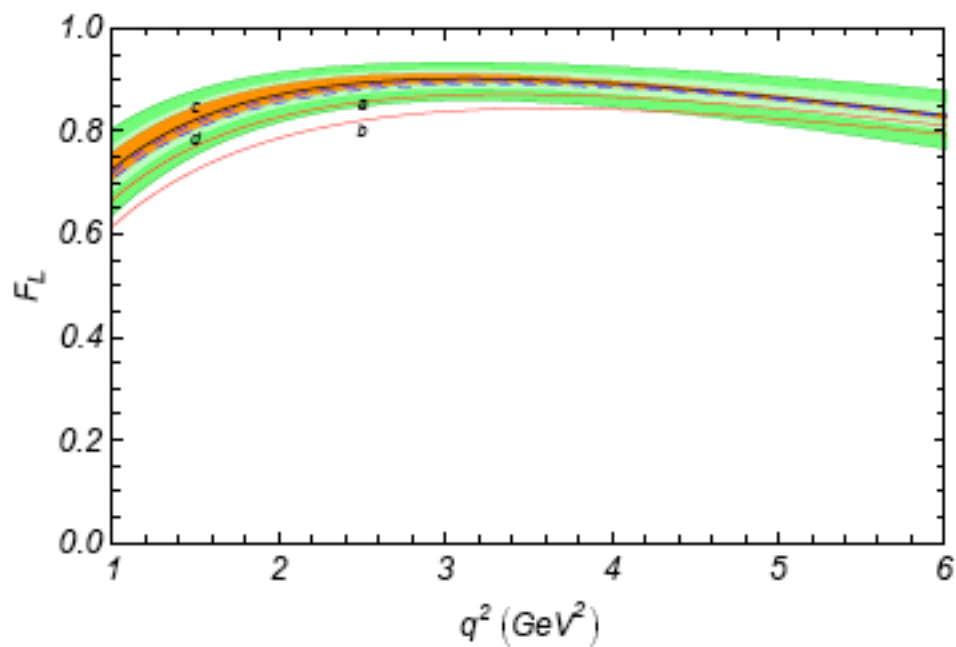
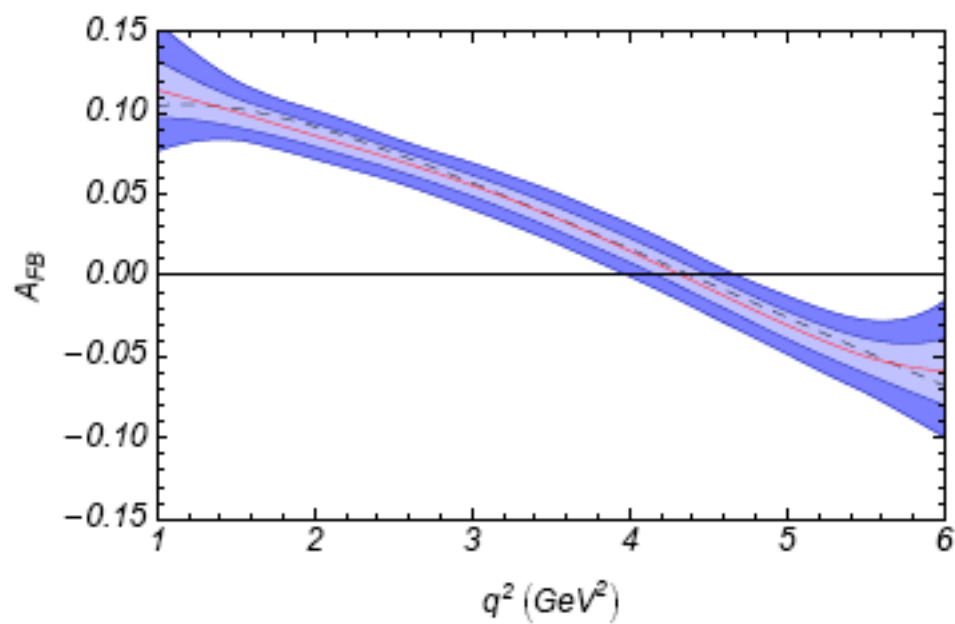
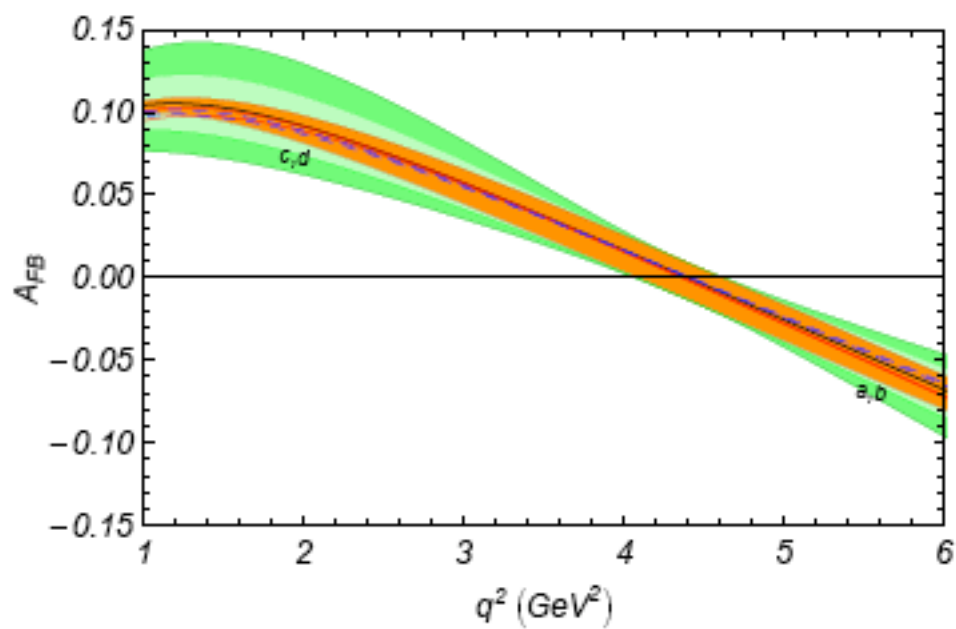
Babar FPCP 2008

Belle ICHEP 2008

$$F_L(s) = \frac{|A_0|^2}{|A_0|^2 + |A_{\parallel}|^2 + |A_{\perp}|^2}$$



LHCb ($10fb^{-1}$) will clarify the situation



Side remark: Minimal Flavour Violation hypothesis

- MFV implies **model-independent** relations between FCNC processes

$$\Delta F = 2 \quad \text{UTfit, arXiv:0707.0636} \quad \Delta F = 1 \quad \text{H., Isidori, Kamenik, Mescia, arXiv:0807.5039}$$

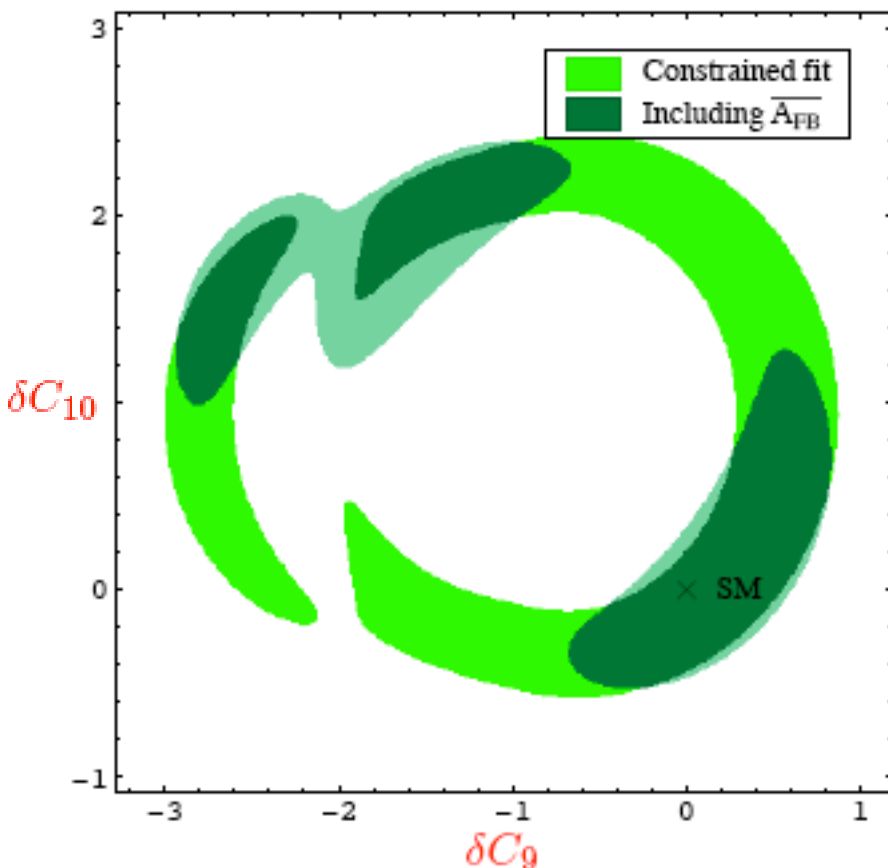
- The usefulness of MFV-bounds/relations is obvious; **any measurement beyond those bounds indicate the existence of new flavour structures**

$$\bar{B}_d \rightarrow \bar{K}^{*0} \mu^+ \mu^-$$

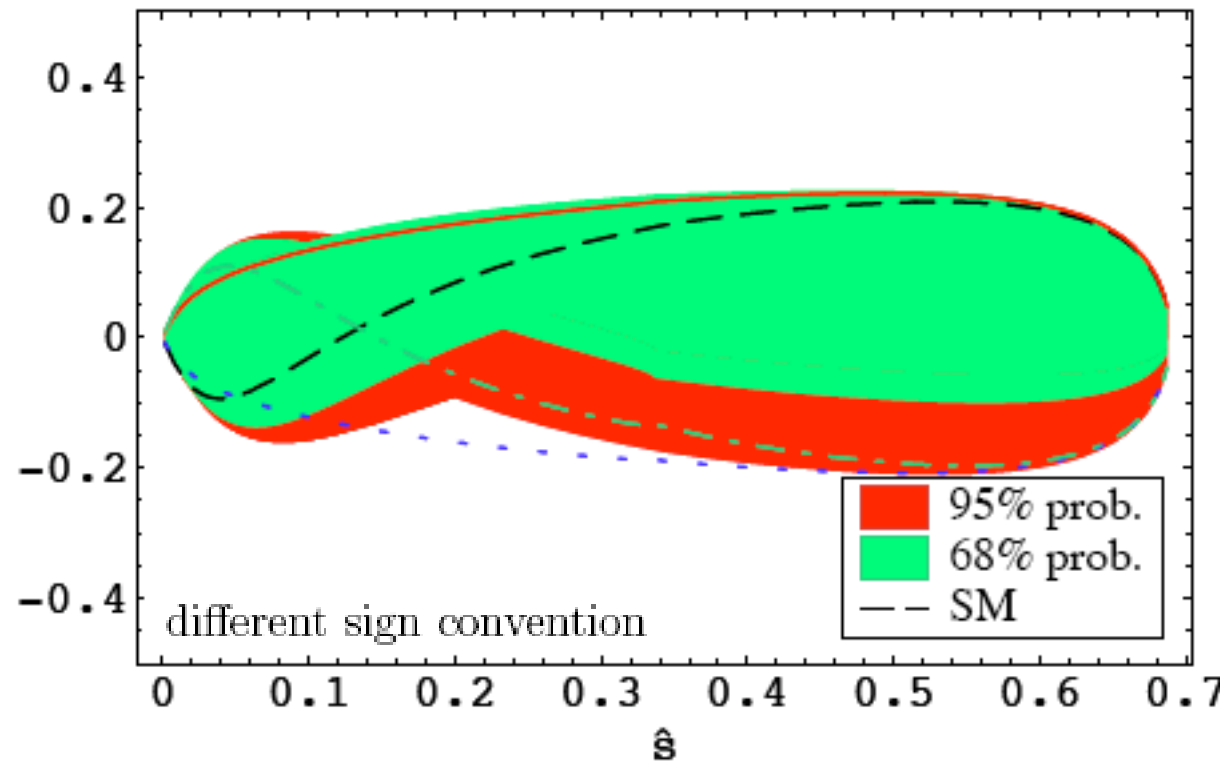
Impact on MFV constraints

(only Babar data included yet)

H., Isidori, Kamenik, Mescia, arXiv:0807.5039



A_{FB}



Remark:

- * SuperLHCB/SuperB can offer more precision

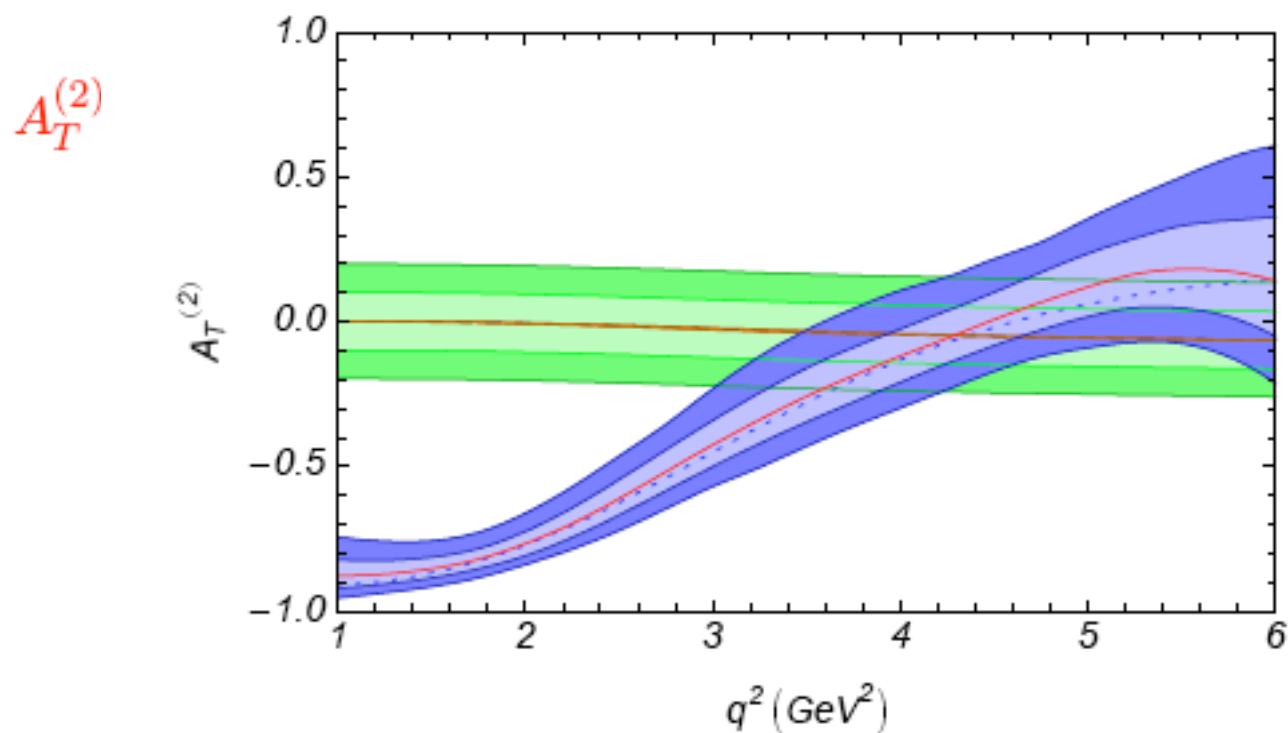
Crucial: theoretical status of Λ/m_b corrections has to be improved

Outlook:

- * Angular distributions offer great opportunities in new physics search
- * Sensitivity to other new physics operators, work in progress
- * Angular distributions allow for the measurement of 7 CP asymmetries
(Krüger,Seghal,Sinha² 2000,2005; Bobeth,Hiller,Piranishvili 2008)

Some slides for discussion session

More on right-handed currents



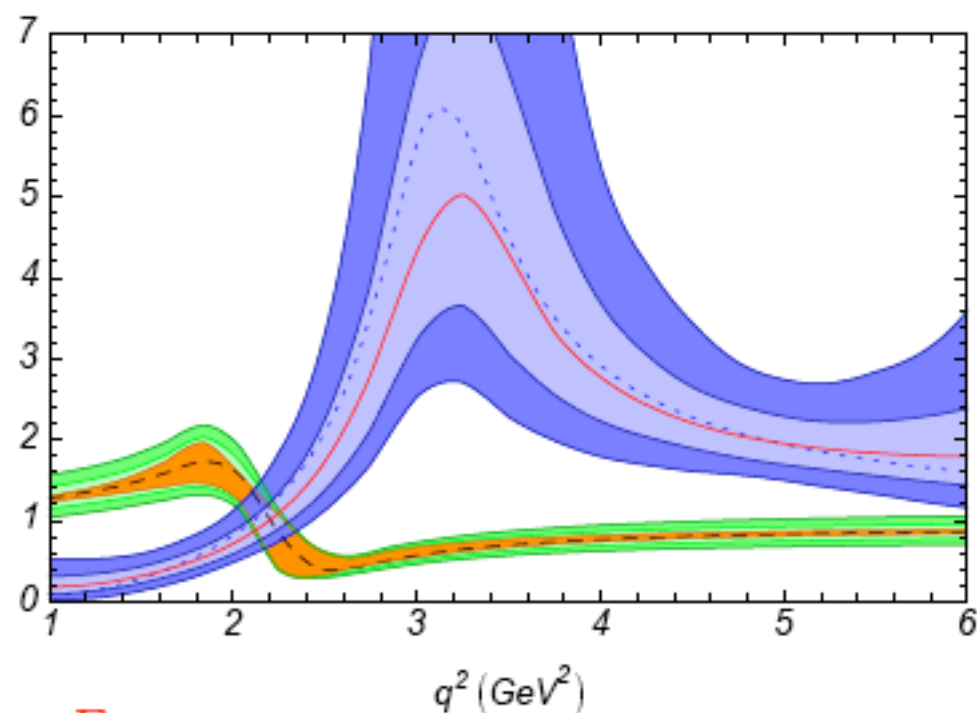
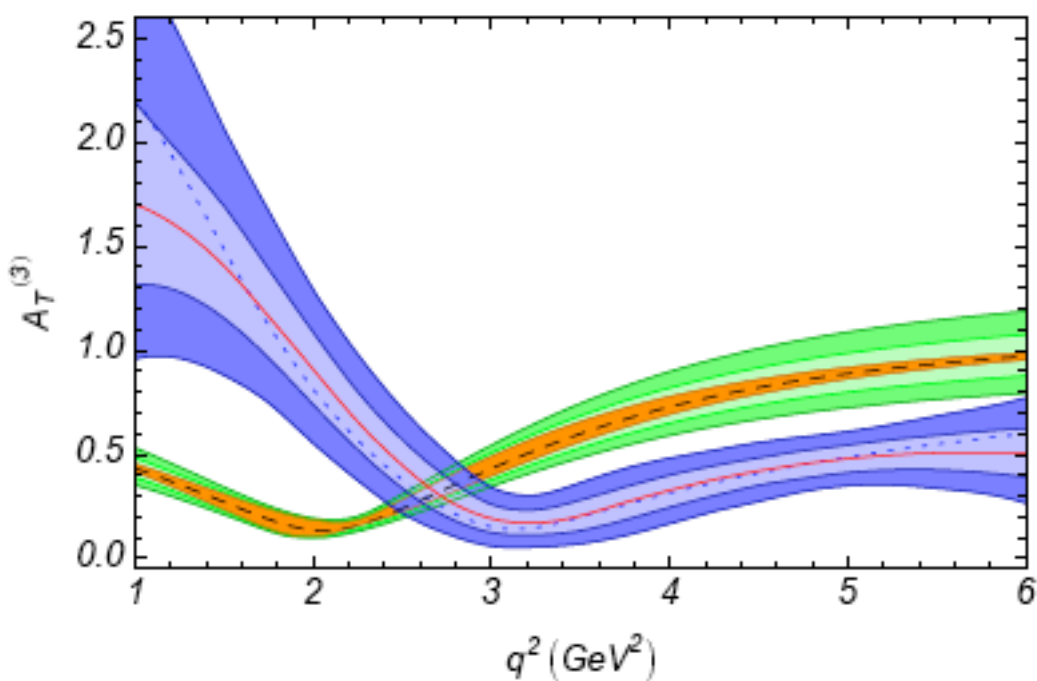
The experimental errors assuming SUSY scenario (b) with large-gluino mass and positive mass insertion, is compared to the theoretical errors assuming the SM.

Comparison between old and new observables

new observables

$A_T^{(3)}$

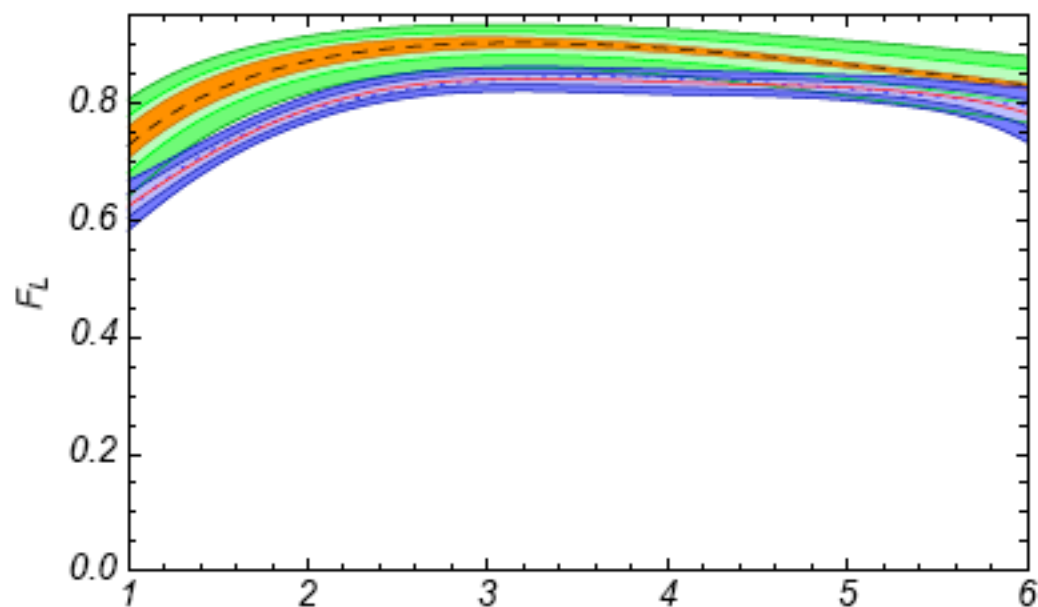
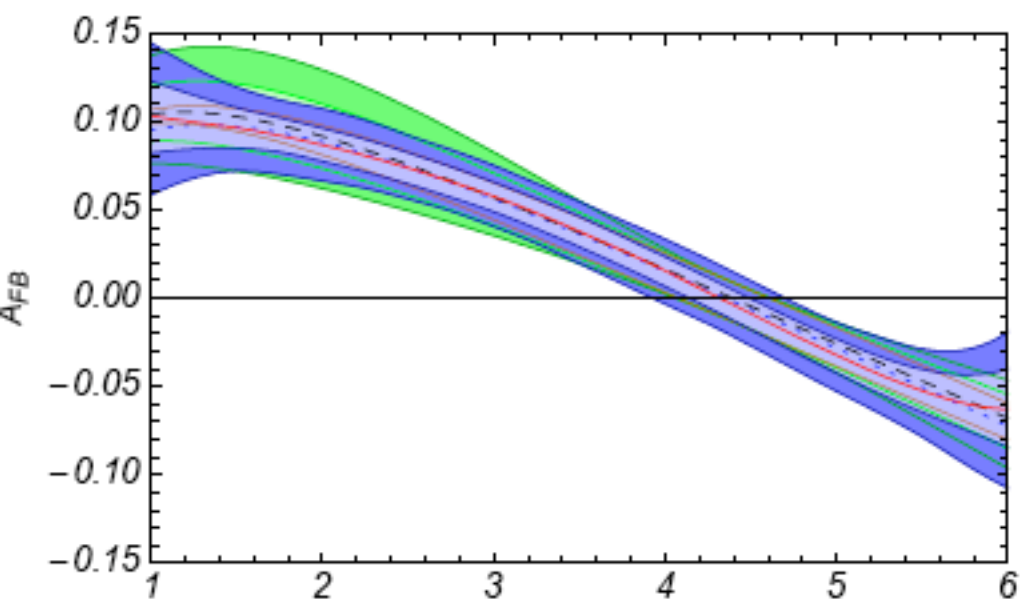
$A_T^{(4)}$

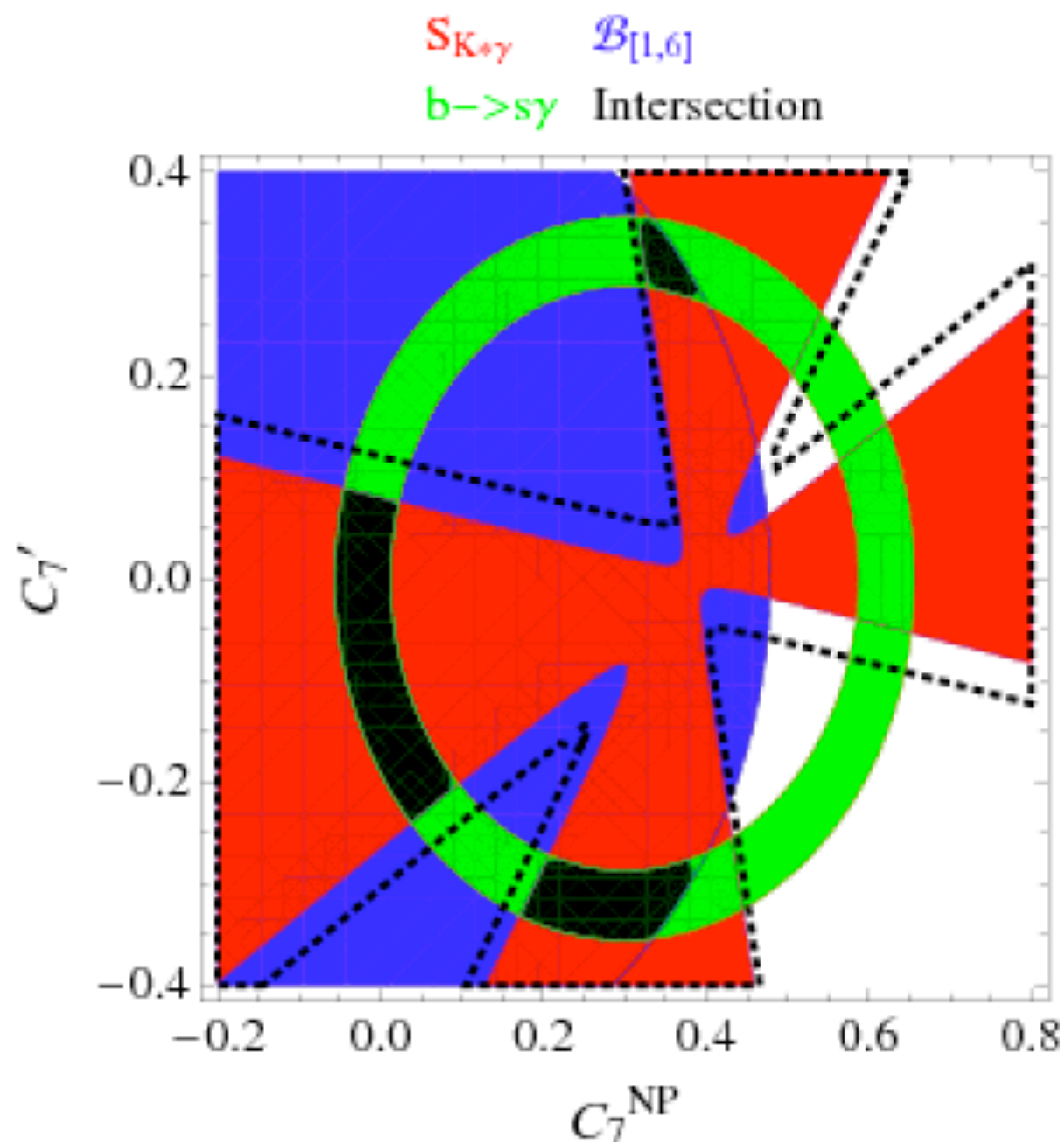


old observables

A_{FB}

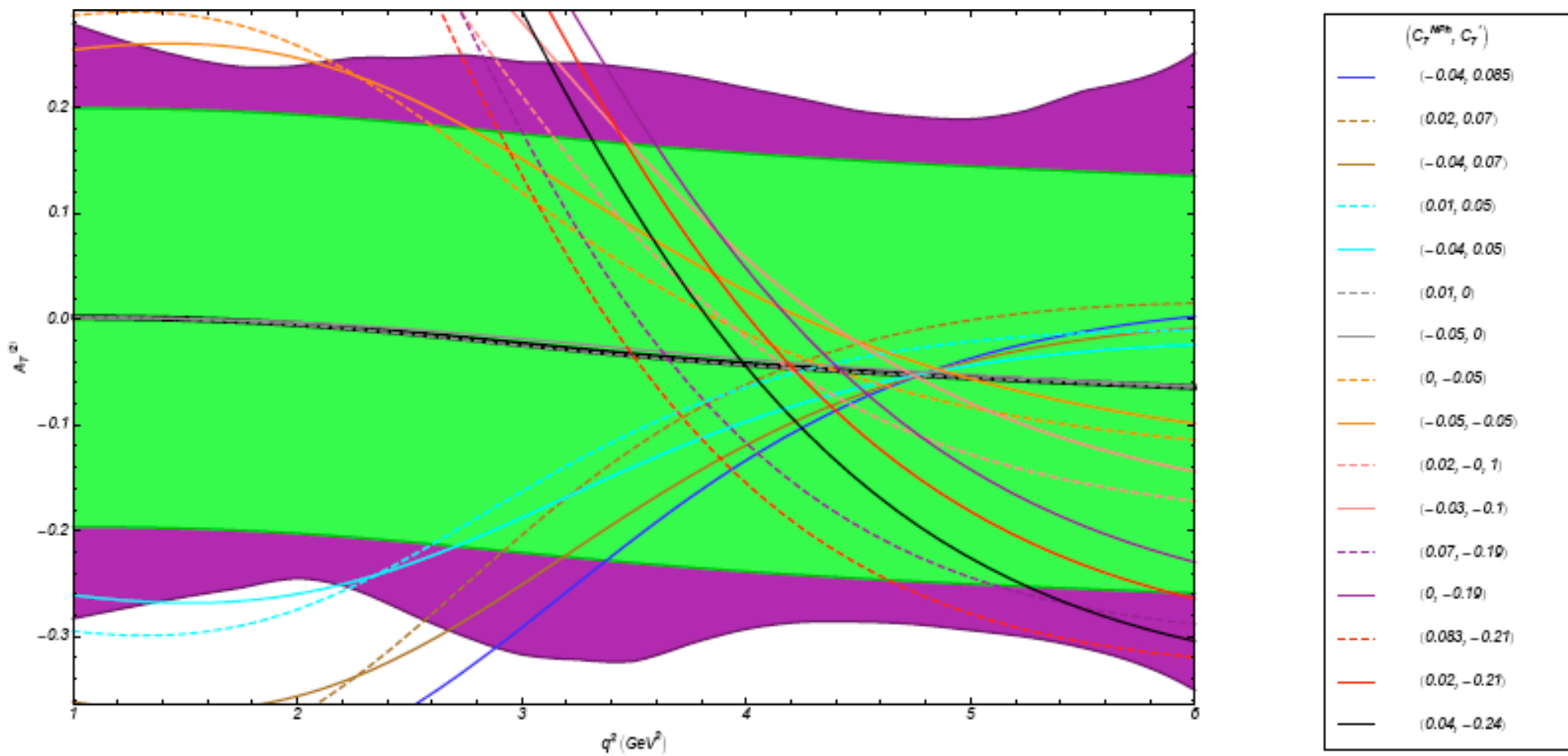
F_L





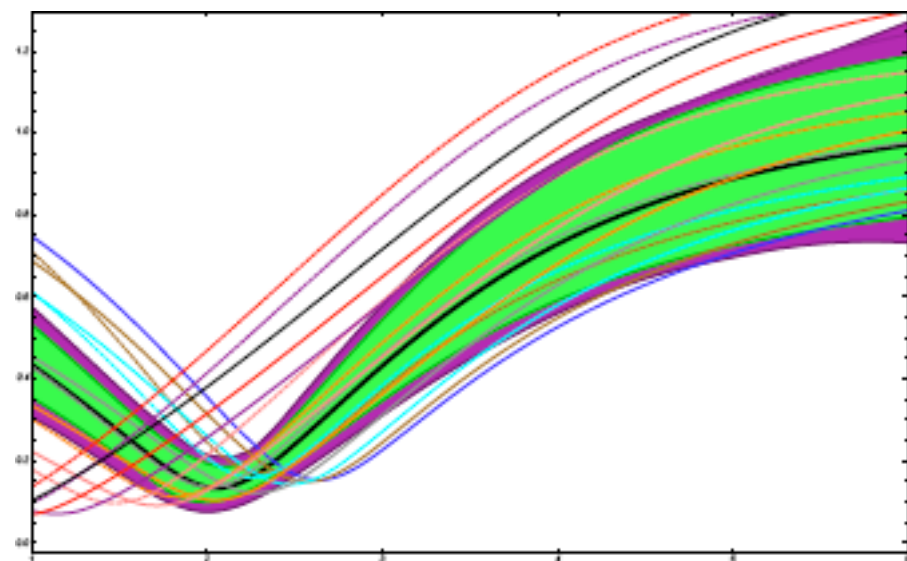
Test of allowed region around $C_7' = 0$ in the C_7 and C_7' plane

$A_T^{(2)}$

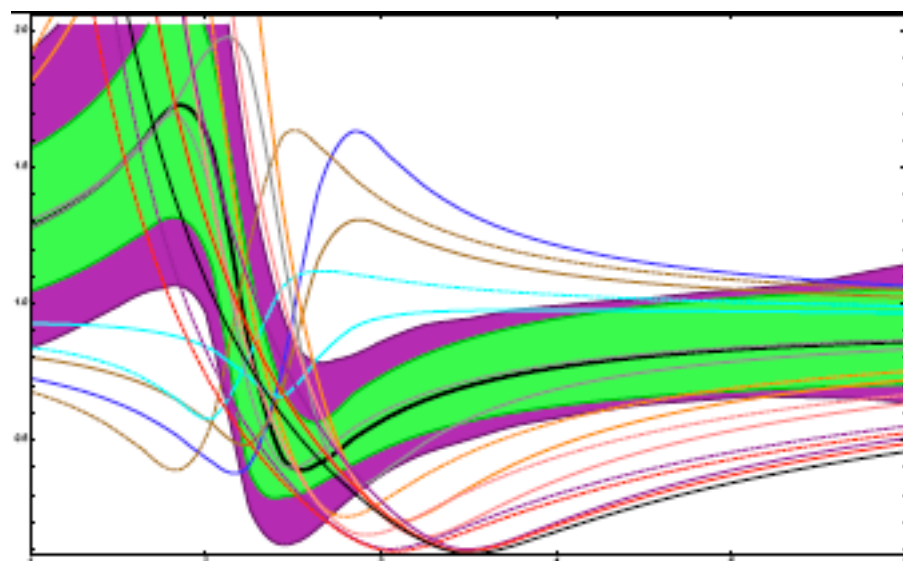


new observables

$$A_T^{(3)}$$

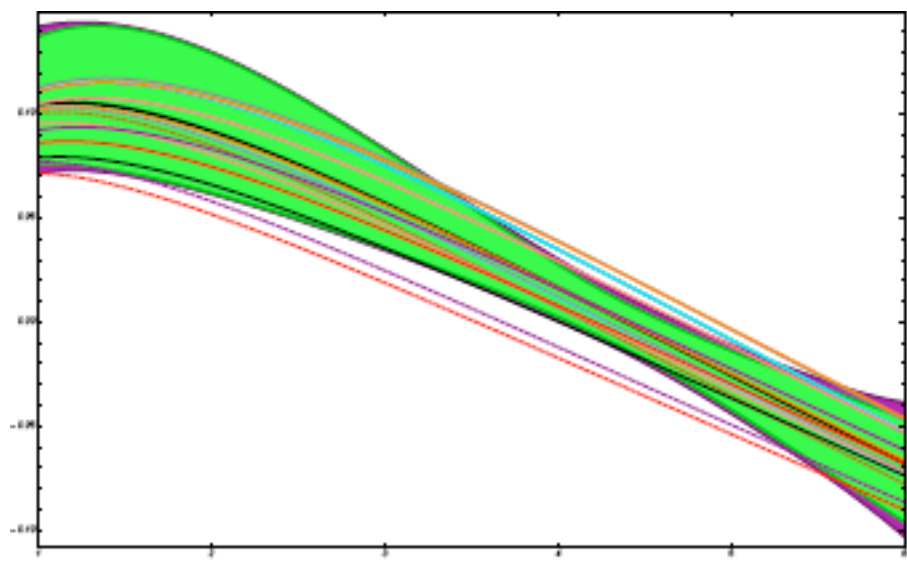


$$A_T^{(4)}$$

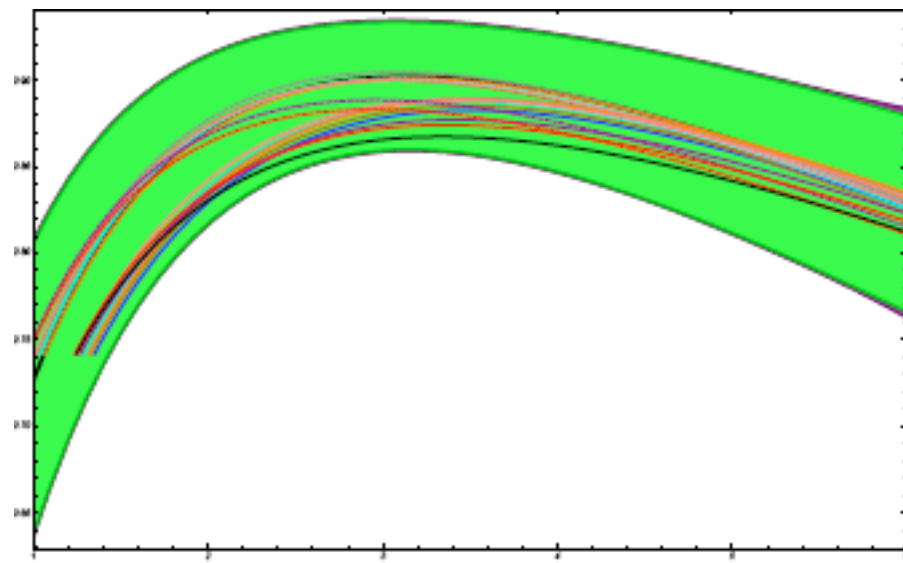


old observables

$$A_{FB}$$



$$F_L$$



Present role of time-dependent CP asymmetry $B \rightarrow K^* \gamma$

Theoretical status of CP asymmetry

- General folklore: within the SM are small, $O(m_s/m_b)$

$$\mathcal{O}_{7L} \equiv \frac{e}{16\pi^2} m_b \bar{s} \sigma_{\mu\nu} P_R b F^{\mu\nu} \quad \mathcal{O}_{7R} \equiv \frac{e}{16\pi^2} m_{s/d} \bar{s} \sigma_{\mu\nu} P_L b F^{\mu\nu} .$$

Mainly: $\bar{B} \rightarrow X_s \gamma_L$ and $B \rightarrow X_s \gamma_R \Rightarrow$ almost no interference in the SM

- But: within the inclusive case the assumption of a two-body decay is made, the argument does not apply to $b \rightarrow s \gamma_{gluon}$

Corrections of order $O(\alpha_s)$, mainly due operator $\mathcal{O}_2 \Rightarrow \Gamma_{22}^{\text{brems}}/\Gamma_0 \sim 0.025$
 \Rightarrow 11% right-handed contamination

Grinstein, Grossman, Ligeti, Pirjol, hep-ph/0412019

- QCD sum rule estimate of the time-dependent CP asymmetry in $B^0 \rightarrow K^{*0} \gamma$ including long-distance contributions due to soft-gluon emission from quark loops versus dimensional estimate of the nonlocal SCET operator series:
Ball, Zwicky, hep-ph/0609037 \leftrightarrow Grinstein, Pirjol, hep-ph/0510104

$$S = -0.022 \pm 0.015_{-0.01}^{+0}, \quad S^{\text{sgluon}} = -0.005 \pm 0.01 \leftrightarrow |S^{\text{sgluon}}| \approx 0.06$$

Note: Expansion parameter is Λ_{QCD}/Q where Q is the kinetic energy of the hadronic part. There is no contribution at leading order. Therefore, the effect is expected to be larger for larger invariant hadronic mass, thus, the K^* mode has to have the smallest effect, below the 'average' 10%

Experiment: $S = 0.19 \pm 0.23$ (HFAG)

Future role of time-dependent CP asymmetry $B \rightarrow K^* \gamma$

$$S_{K^* \gamma} = -\frac{2|r|}{1+|r|^2} \sin\left(2\beta - \arg(C_7^{(0)} C_7')\right), \quad r = C_7'/C_7^{(0)}$$

SuperB: $\Delta S = \pm 0.04$ [arXiv:hep-ex/0406071](#)

LHCb: $B_s \rightarrow \Phi \gamma$

$$S_{\Phi \gamma} = 0 \pm 0.002 \quad \sin(\phi_s)! \quad \text{Muheim, Xie, Zwicky, arXiv:0802.0876}$$

$$A_{\Phi \gamma}^{\Delta\Gamma} = 0.047 \pm 0.025 + 0.015 \quad \cos(\phi_s)!$$

LHCb ($2fb^{-1}$): $\Delta A = 0.22$

[Golutvin et al., LHCb-PHYS-2007-147](#)