

Belle Results on Time-dependent CP Asymmetry for
 $B \rightarrow D^{*-} \pi^+$
and Search for $B \rightarrow D^{*+} \pi^0$ Decay

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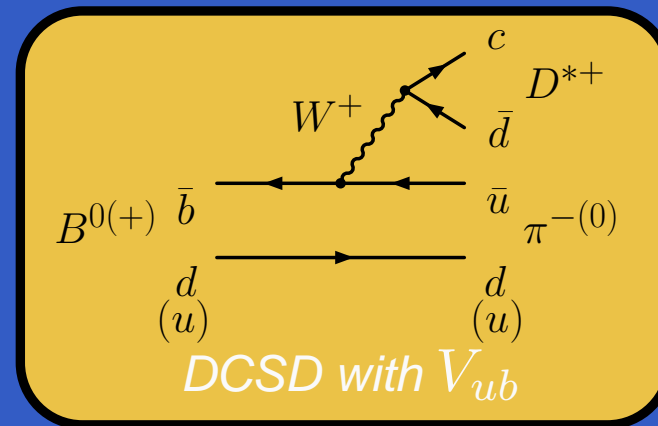
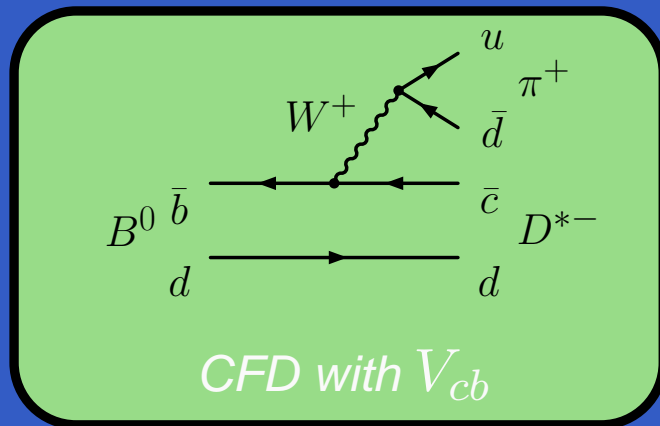
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Tsukuba, Japan



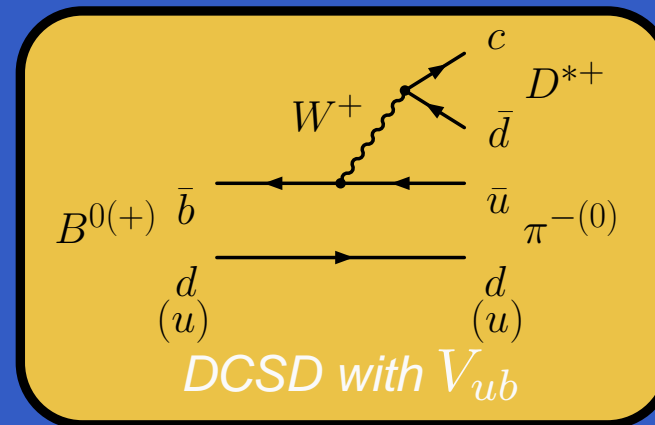
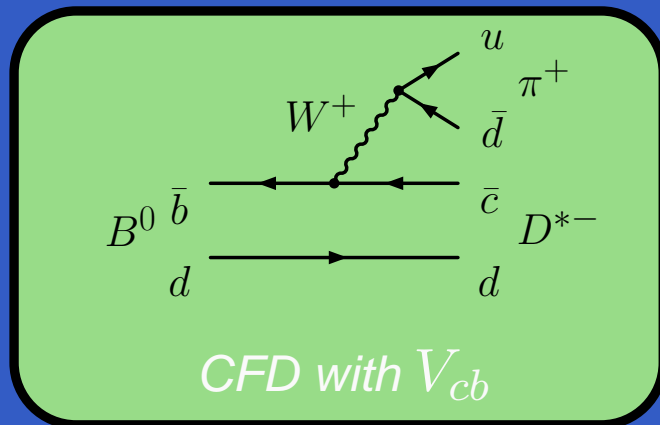
Introduction

- Interference of different tree diagrams with V_{ub} ($\rightarrow \phi_3$) through $B\bar{B}$ mixing ($\rightarrow 2\phi_1$)



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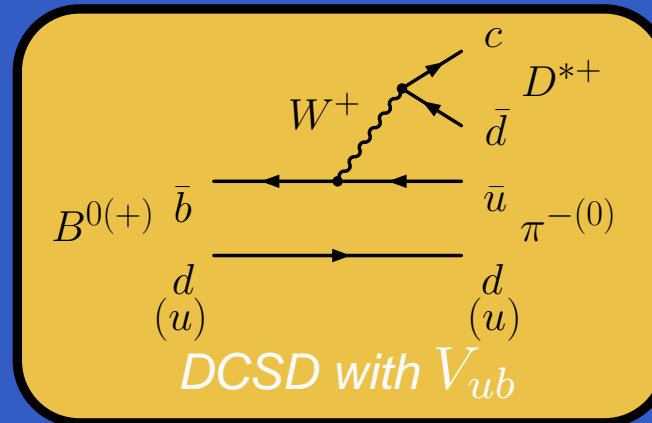
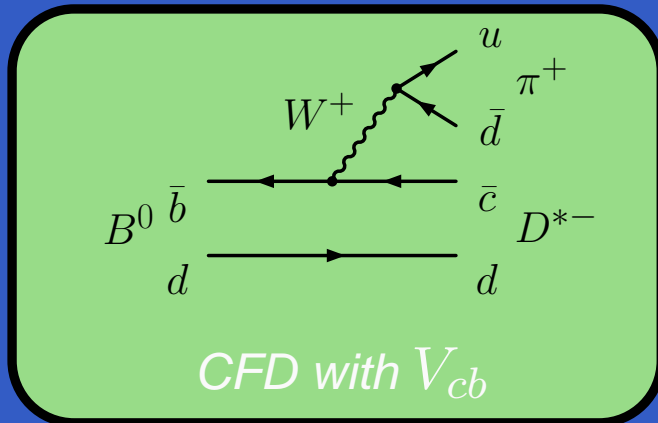


- Time-dependent asymmetry can be derived using the relation,

$$\frac{\Gamma(\bar{B}^0(\Delta t \rightarrow f)) - \Gamma(B^0(\Delta t \rightarrow f))}{\Gamma(\bar{B}^0(\Delta t \rightarrow f)) + \Gamma(B^0(\Delta t \rightarrow f))} = S \sin(\Delta m_d) - C \cos(\Delta m_d)$$

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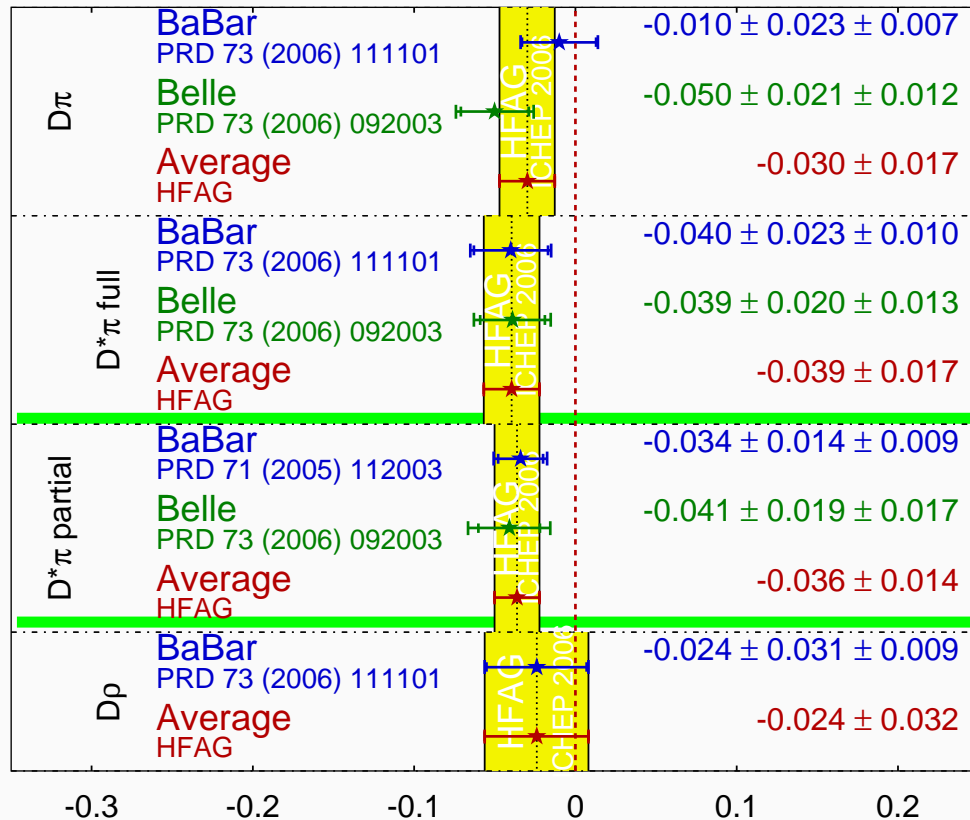
$$S^\pm = -2R \sin(2\phi_1 + \phi_3 \pm \delta) \quad C = \pm 1$$

$$\text{for } B \rightarrow D^{*\pm} \pi^\mp \text{ final states} \quad (|C| = (1 - R^2)/(1 + R^2) \simeq 1)$$

Introduction (Cont'd)

a parameters

HFAG
ICHEP 2006
PRELIMINARY



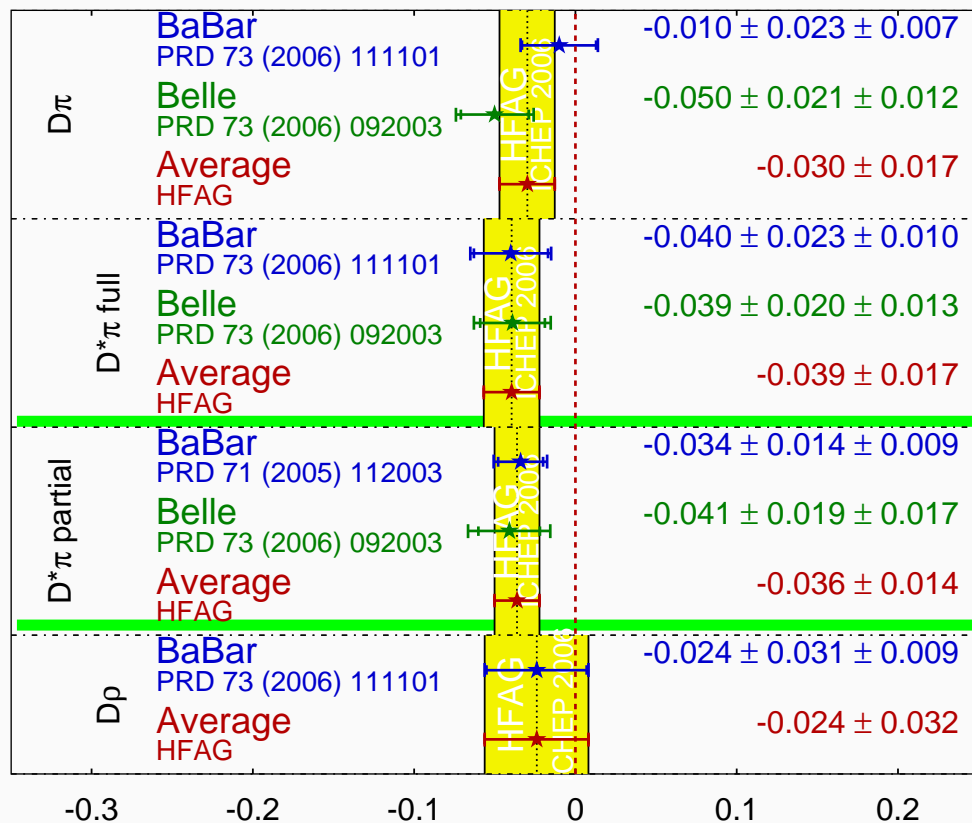
HFAG notation:

$$a = -\frac{S^+ + S^-}{2}, \quad c = -\frac{S^+ - S^-}{2}$$

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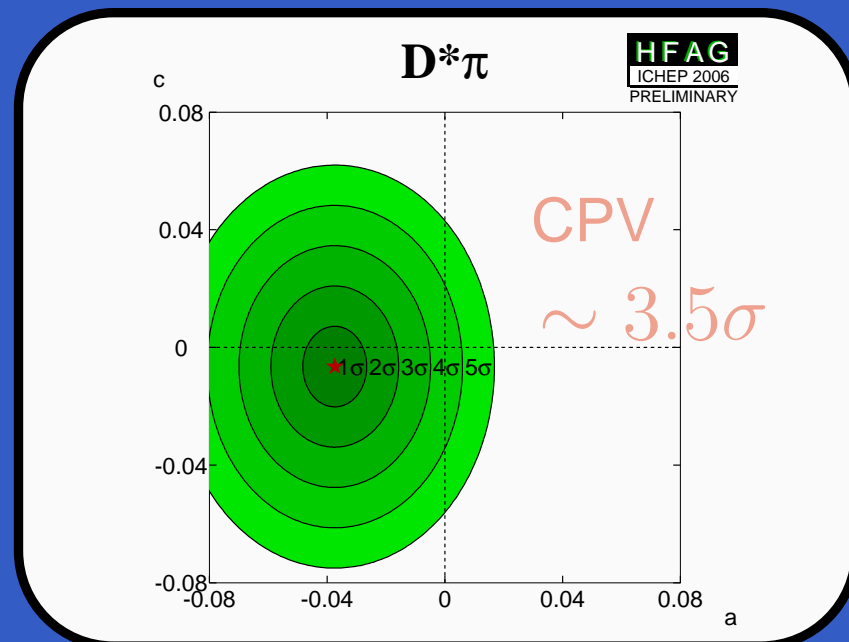
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HFAG average for $D^*\pi$ [2006]:
(full and partial, Babar and Belle)

$$a = -0.037 \pm 0.011$$

$$c = -0.006 \pm 0.014$$



Introduction (Cont'd)

- **AD**: CFD fraction $\mathcal{B}(B^0 \rightarrow D^{*-} \pi^+)$ is large (2.76×10^{-3}).

DA: the amplitude ratio is not sizable,

$$R \equiv \mathcal{A}(B^0 \rightarrow D^{*+} \pi^-) / \mathcal{A}(B^0 \rightarrow D^{*-} \pi^+) \simeq 0.02.$$

: $B^0 \rightarrow \bar{B}^0 \rightarrow D^{*+} \pi^-$ (CFD) is large compared to the DCSD amplitude.

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- Two possible ways for reaching R :

- ◆ $R = \tan \theta_c \frac{f_{D^*}}{f_{D_s^*}} \sqrt{\frac{\mathcal{B}(B^0 \rightarrow D_s^{*+}\pi^-)}{\mathcal{B}(B^0 \rightarrow D^{*-}\pi^+)}}$

allowing the error from the assumption of SU(3) symmetry.

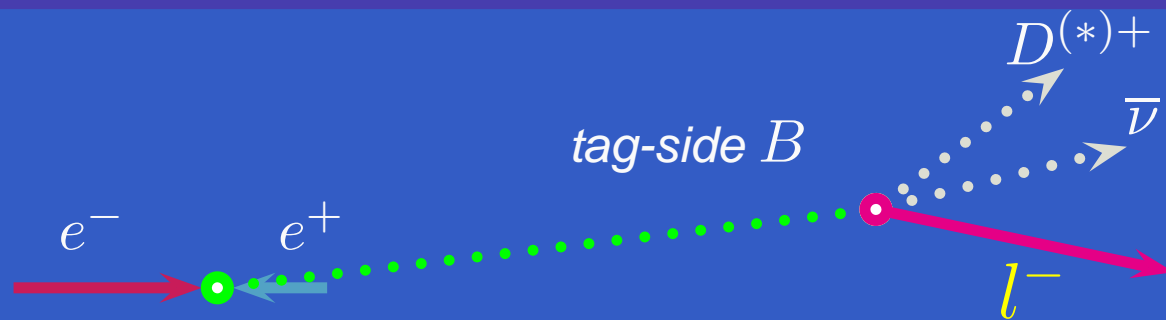
- ◆ $R = \sqrt{\frac{\tau_{B^0}}{\tau_{B^+}} \frac{2\mathcal{B}(B^+ \rightarrow D^{*+}\pi^0)}{\mathcal{B}(B^0 \rightarrow D^{*-}\pi^+)}}$

as suggested by Duniez, PLB 427 (1998), using the isospin relation.

$B^0 \rightarrow D^* \pi$ partial reconstruction

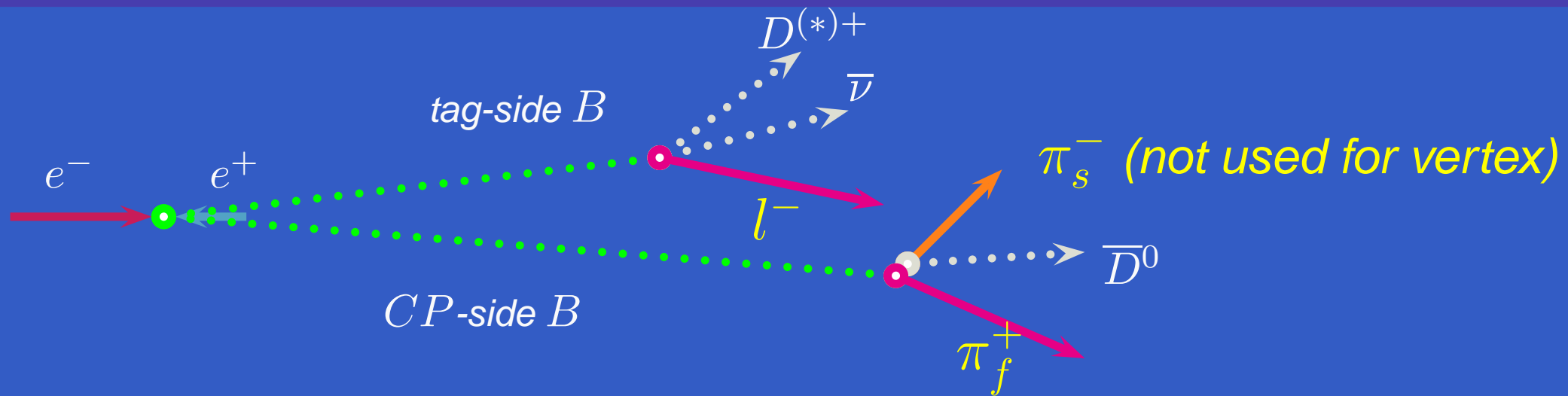


$B^0 \rightarrow D^* \pi$ partial reconstruction



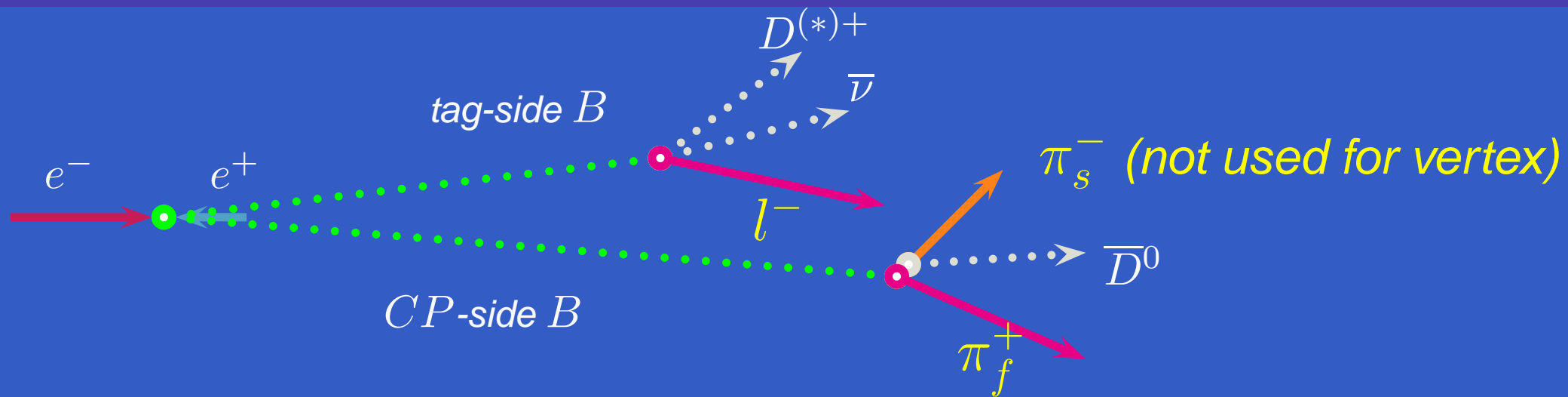
- High-momentum lepton is required in tag-side.

$B^0 \rightarrow D^* \pi$ partial reconstruction



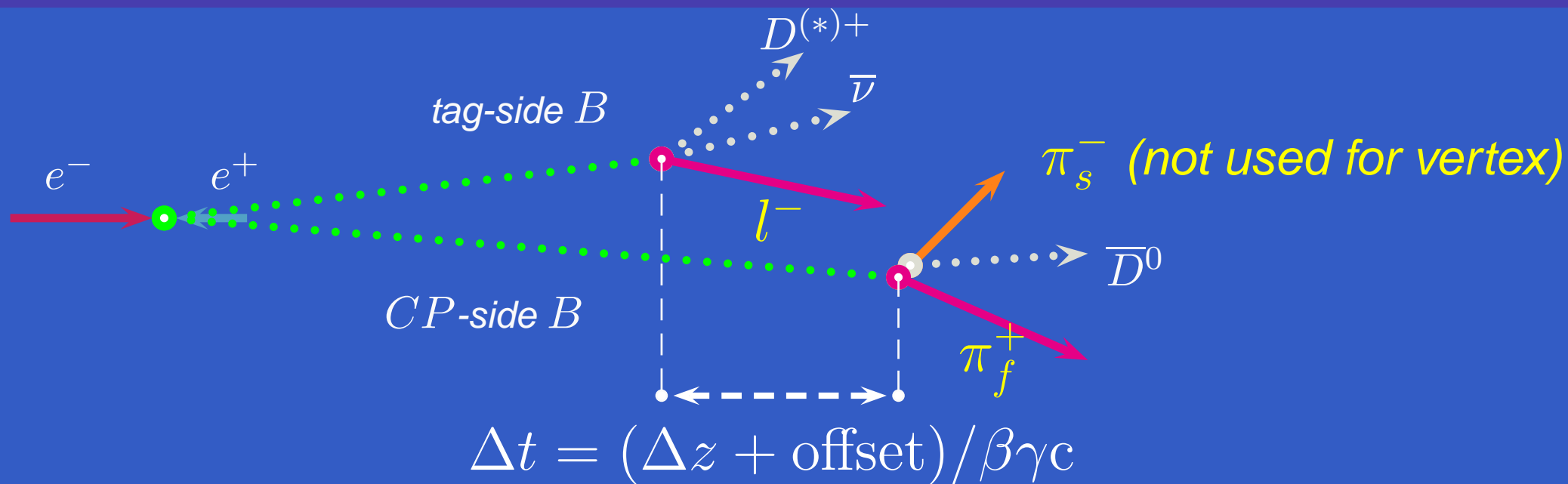
- High-momentum lepton is required in tag-side.
- Two charged pions must have high and low momentum.

$B^0 \rightarrow D^* \pi$ partial reconstruction



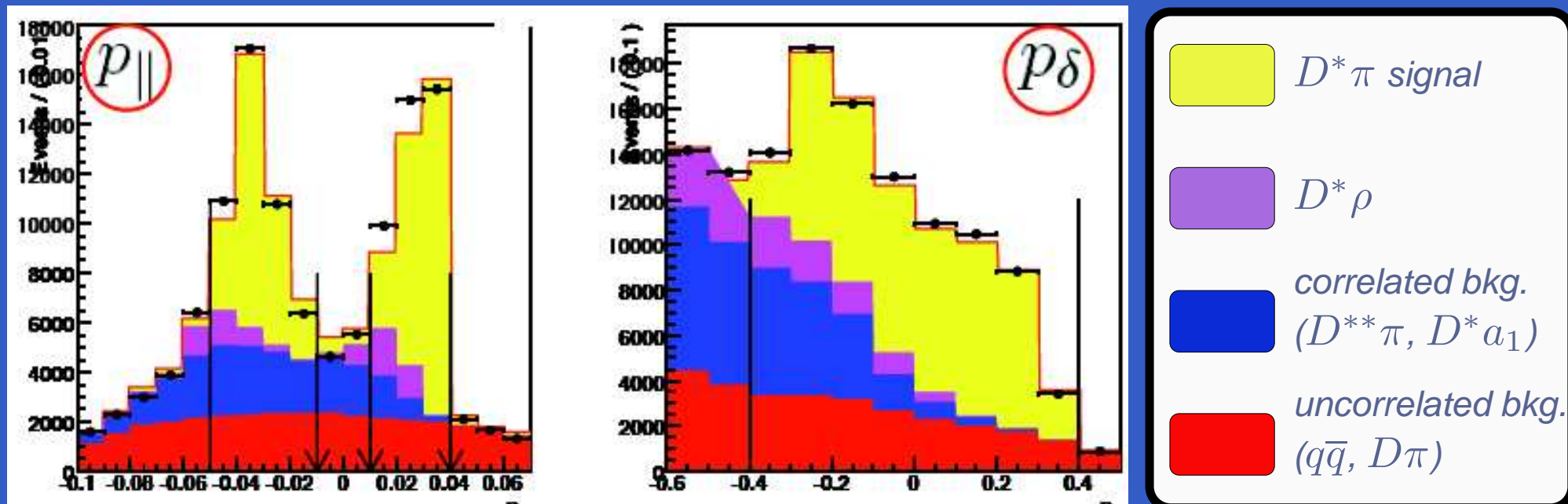
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$B^0 \rightarrow D^* \pi$ partial reconstruction



- High-momentum lepton is required in tag-side.
- Two charged pions must have high and low momentum.
- Vertex positions are obtained from single tracks.
- Proper-time difference can be derived from Δz .

Yield extraction for $B^0 \rightarrow D^* \pi$



- Fit in two kinematical dimensions: π_s momentum along the opposite direction of π_f (p_{\parallel}) and momentum difference between π_f and D^* (p_{δ}).

Experiment	$N_{B\bar{B}}$	N_{sig} in signal region	$S/(S+B)$	cut for lepton
Belle (PRD 73, 092003 (2006))	386 M	$21,773 \pm 214$	66%	$> 1.2 \text{ GeV}/c$
Belle 2008 Summer	657 M	$50,196 \pm 286$	59%	$> 1.1 \text{ GeV}/c$

■ Unbinned ML fit :

to minimize the quantity $-2 \sum_i \ln \mathcal{L}_i$,

$$\mathcal{L}_i = f_{D^*\pi} P_{D^*\pi} + f_{D^*\rho} P_{D^*\rho} + f_{\text{unco}} P_{\text{unco}} + f_{\text{corr}} P_{\text{corr}}$$

■ Time-dependent decay rates :

$$P(B^0 \rightarrow D^{*\pm} \pi^\mp) = (1/8\tau_{B^0}) e^{-|\Delta t|/\tau_{B^0}} [1 \mp C \cos(\Delta m \Delta t) - S^\pm \sin(\Delta m \Delta t)]$$

$$P(\bar{B}^0 \rightarrow D^{*\pm} \pi^\mp) = (1/8\tau_{B^0}) e^{-|\Delta t|/\tau_{B^0}} [1 - C \cos(\Delta m \Delta t) \mp S^\pm \sin(\Delta m \Delta t)]$$

■ Mistagging :

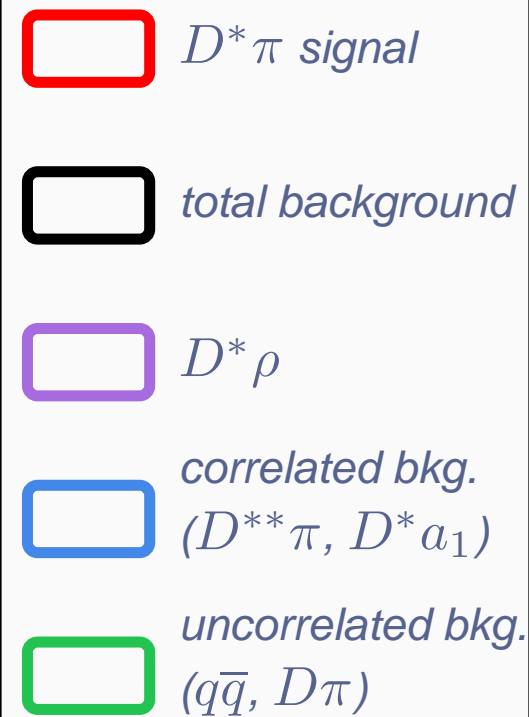
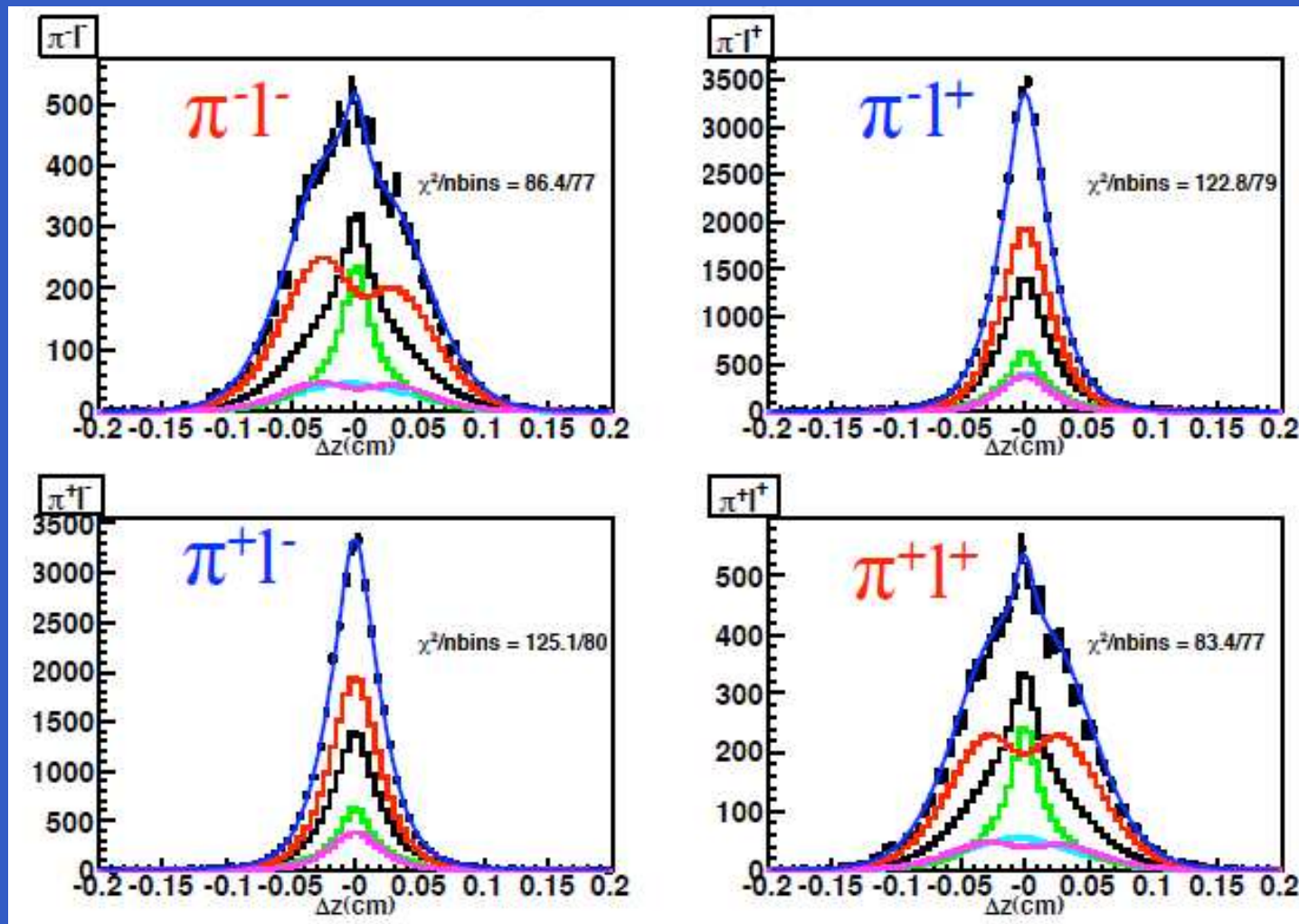
taken into account in the fit,

$$P(l, \pi_f) = (1 - w_-) P(B^0 \rightarrow D^* \pi) + (1 - w_+) P(\bar{B}^0 \rightarrow D^* \pi) \quad (w_{+/-} \sim 5\%)$$

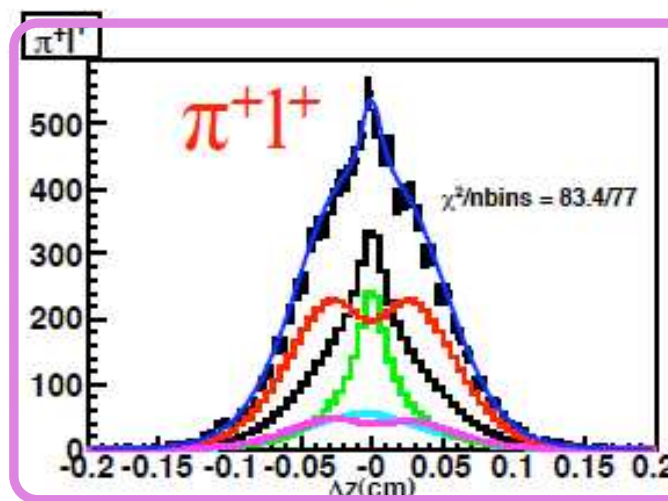
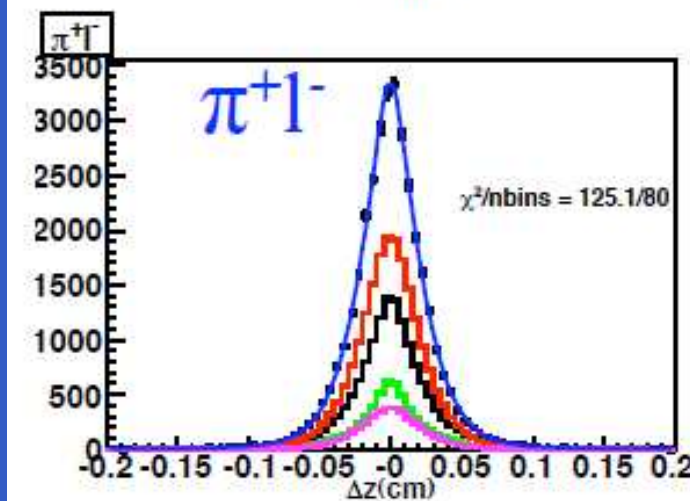
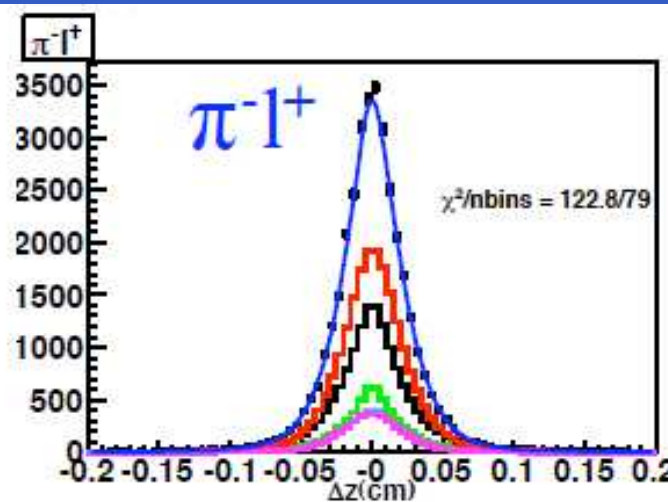
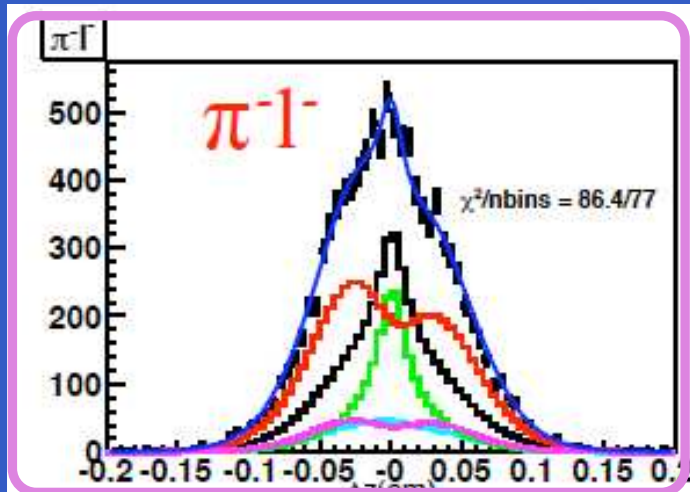
■ Detector resolution function :

J/ψ events are analysed and $\Delta z = z_{\mu^+} - z_{\mu^-}$ is used.

Δz fit results



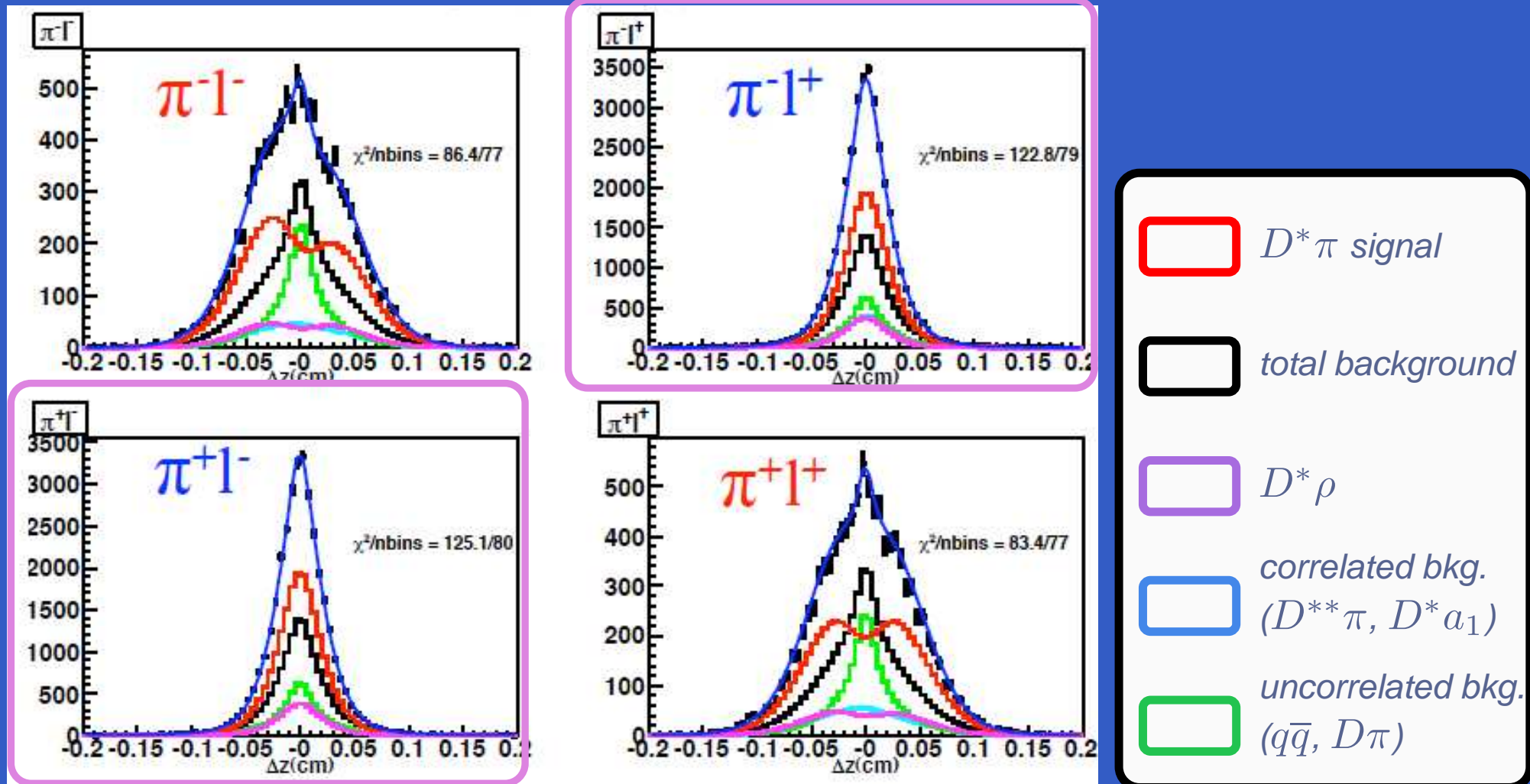
Δz fit results



SF (same flavor)

: π_f and tagging lepton have same charge

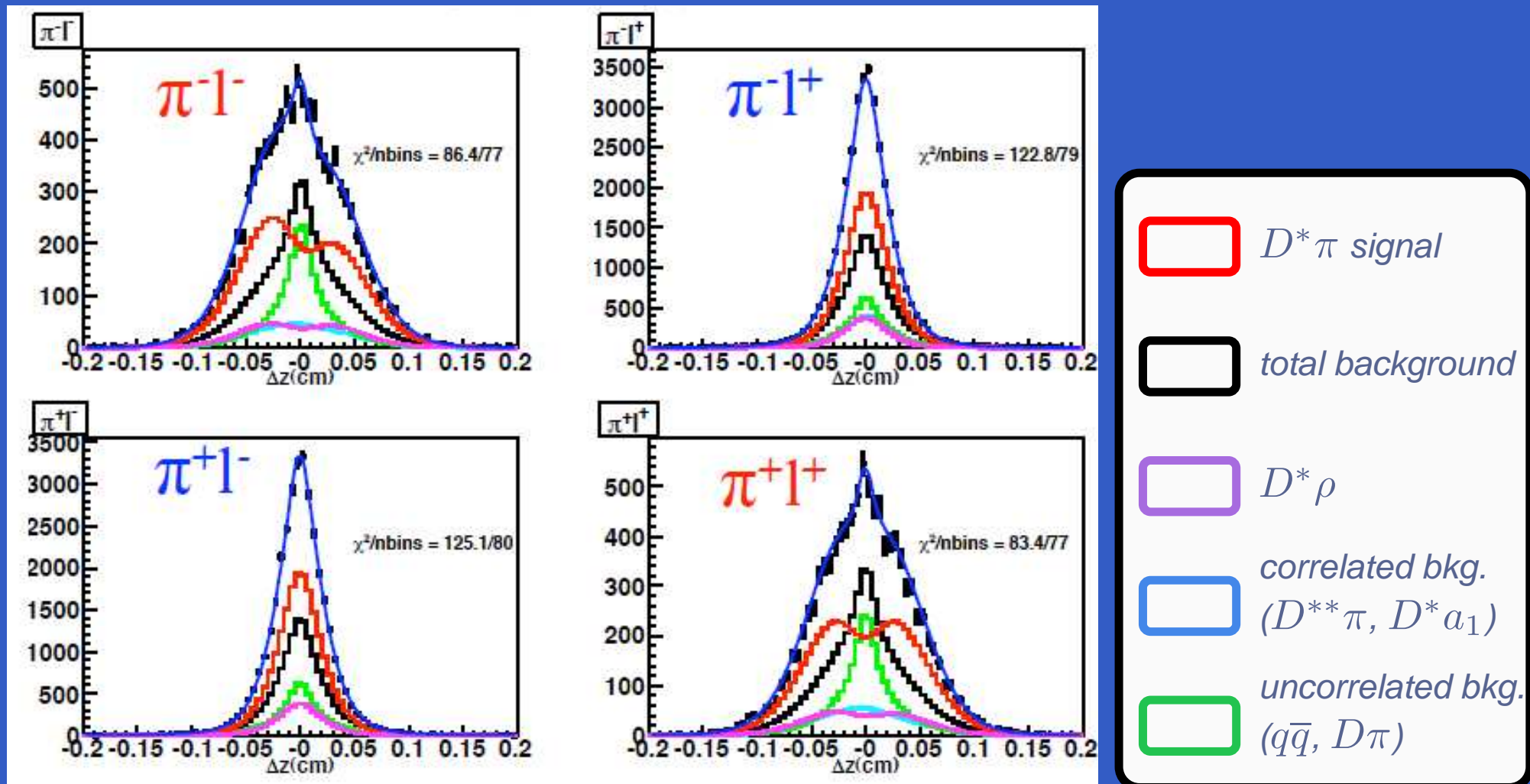
Δz fit results



OF (opposite flavor)

: π_f and tagging lepton have opposite charge

Δz fit results

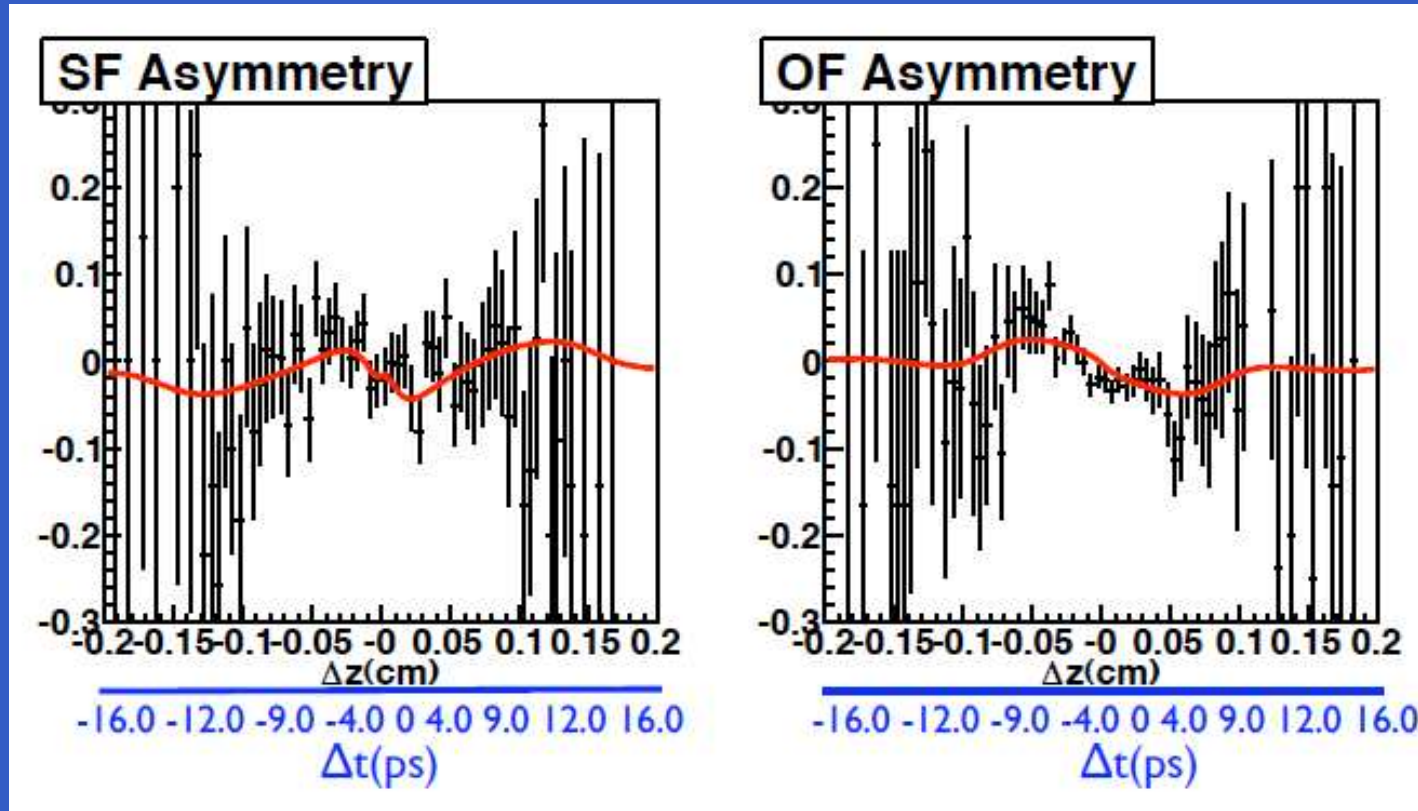


■ $S^+ = 0.057 \pm 0.019$ (stat.), $S^- = 0.038 \pm 0.020$ (stat.)

preliminary

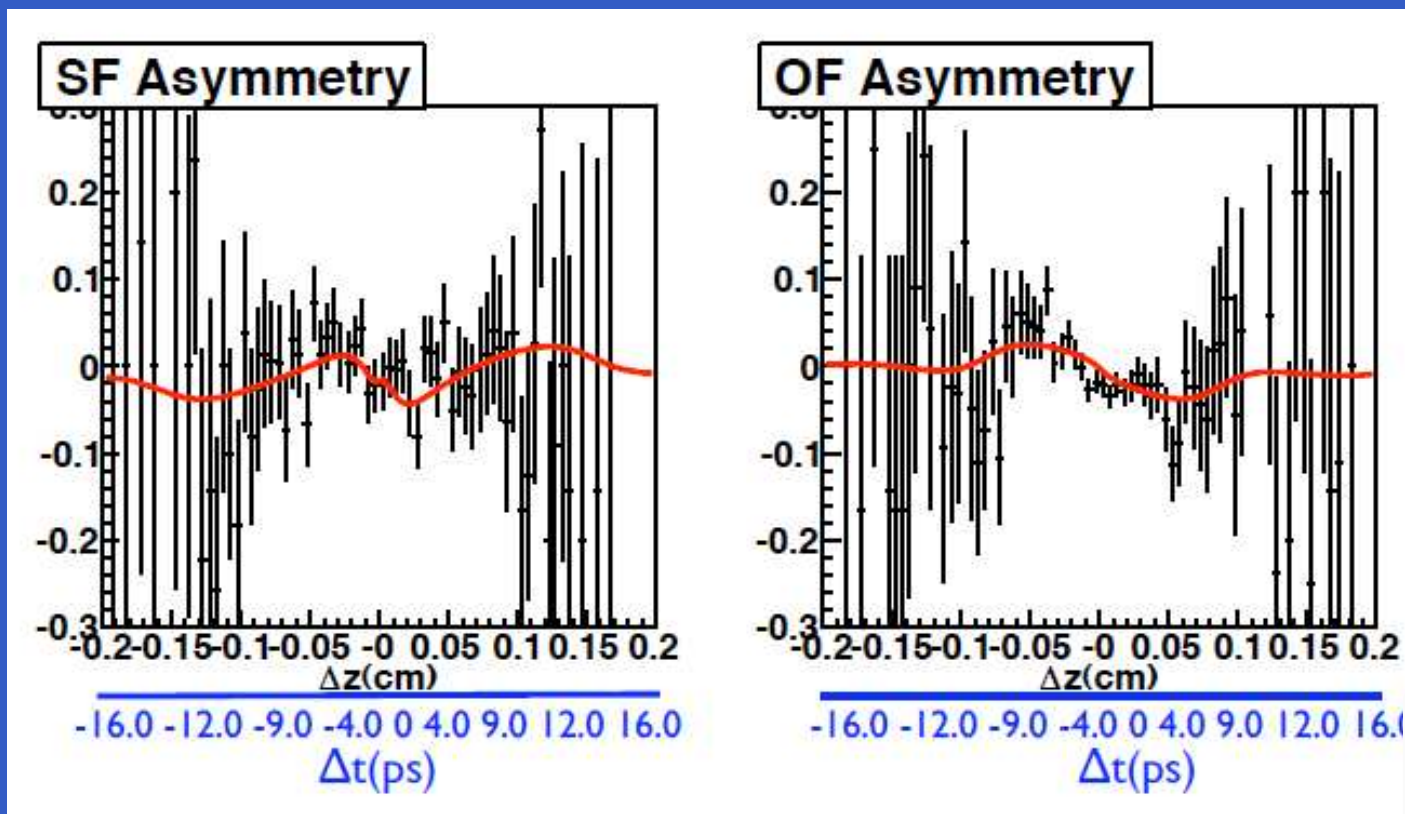
CP asymmetry

■ $\mathcal{A} = \frac{N_{\pi^- l^-}(\Delta z) - N_{\pi^+ l^+}(\Delta z)}{N_{\pi^- l^-}(\Delta z) + N_{\pi^+ l^+}(\Delta z)}$ (SF) $\mathcal{A} = \frac{N_{\pi^+ l^-}(\Delta z) - N_{\pi^- l^+}(\Delta z)}{N_{\pi^+ l^-}(\Delta z) + N_{\pi^- l^+}(\Delta z)}$ (OF)



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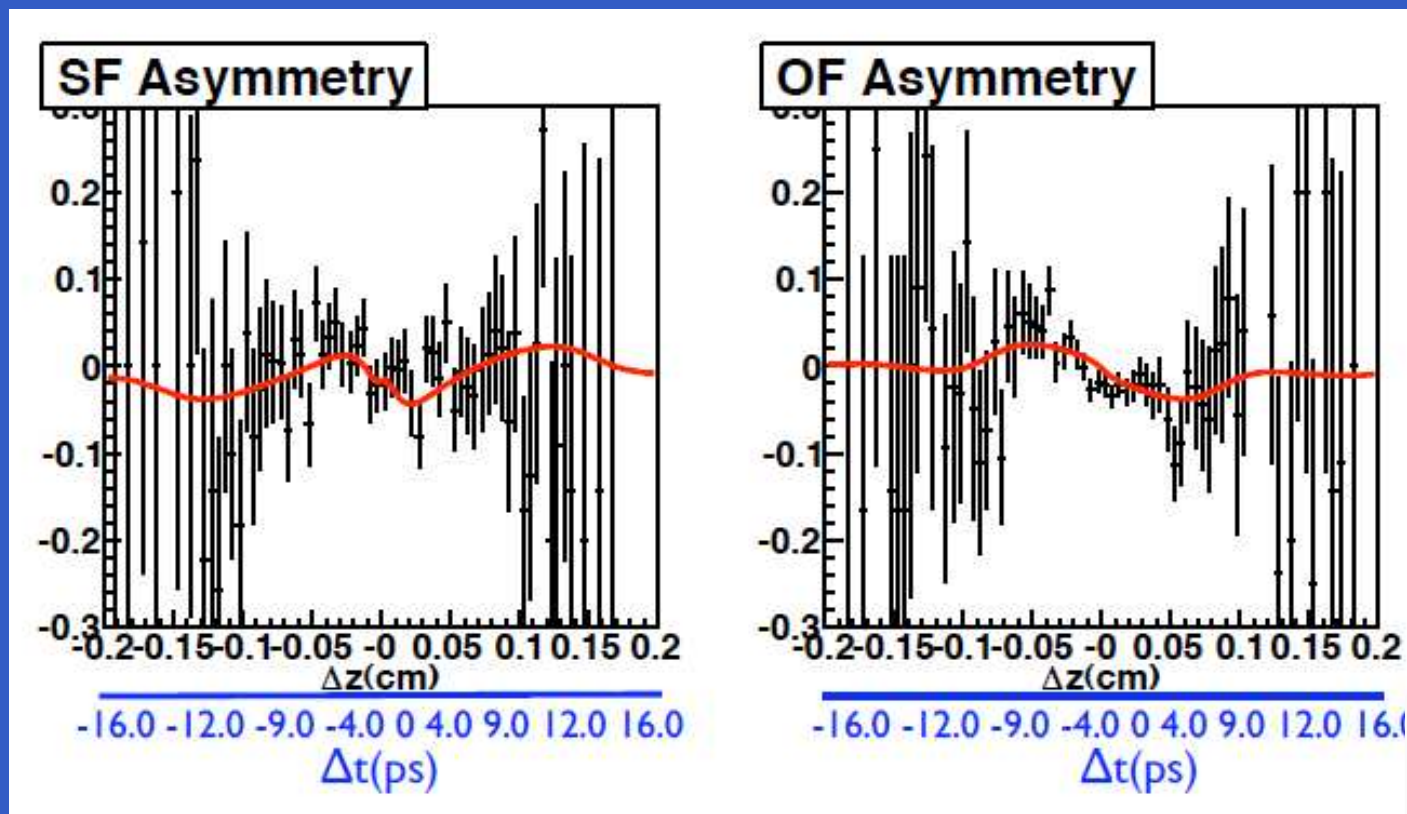


$a = 0.047 \pm 0.014 \pm 0.012$

$c = 0.009 \pm 0.014 \pm 0.012$

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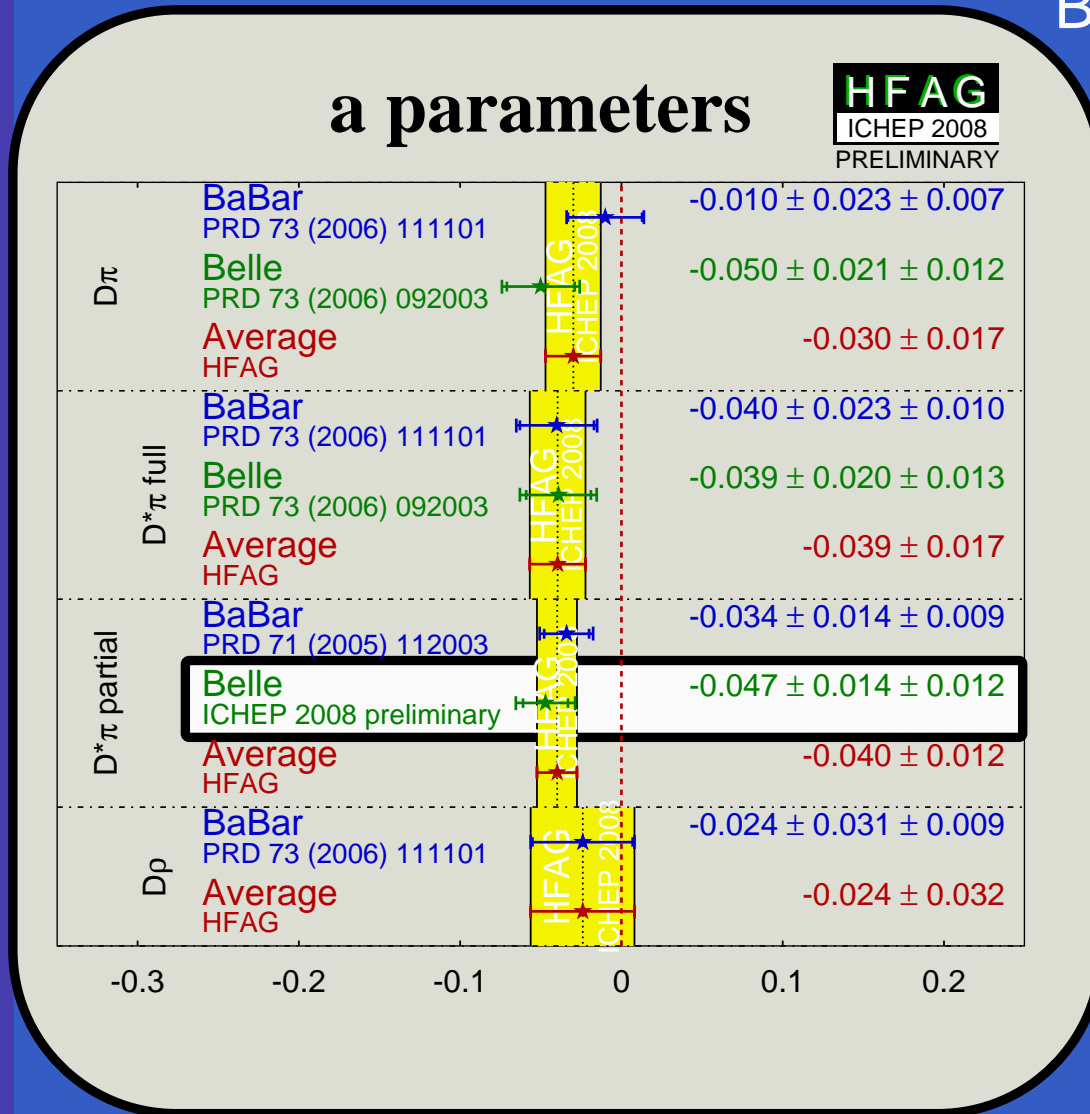
significance of CPV is 2.6σ

Systematic uncertainties for S^\pm

Source	S_+	S_-
Δz offsets	0.002	0.003
R_k	0.002	0.003
R_{det}	0.002	0.002
R_{np}	0.008	0.007
Background param.	0.004	0.004
Phys. param.	0.004	0.004
Yield fit	0.003	0.003
Resol. model	0.006	0.002
Δz offsets floated in bkg.	0.002	0.003
Total	0.012	0.010

Updated HFAG average

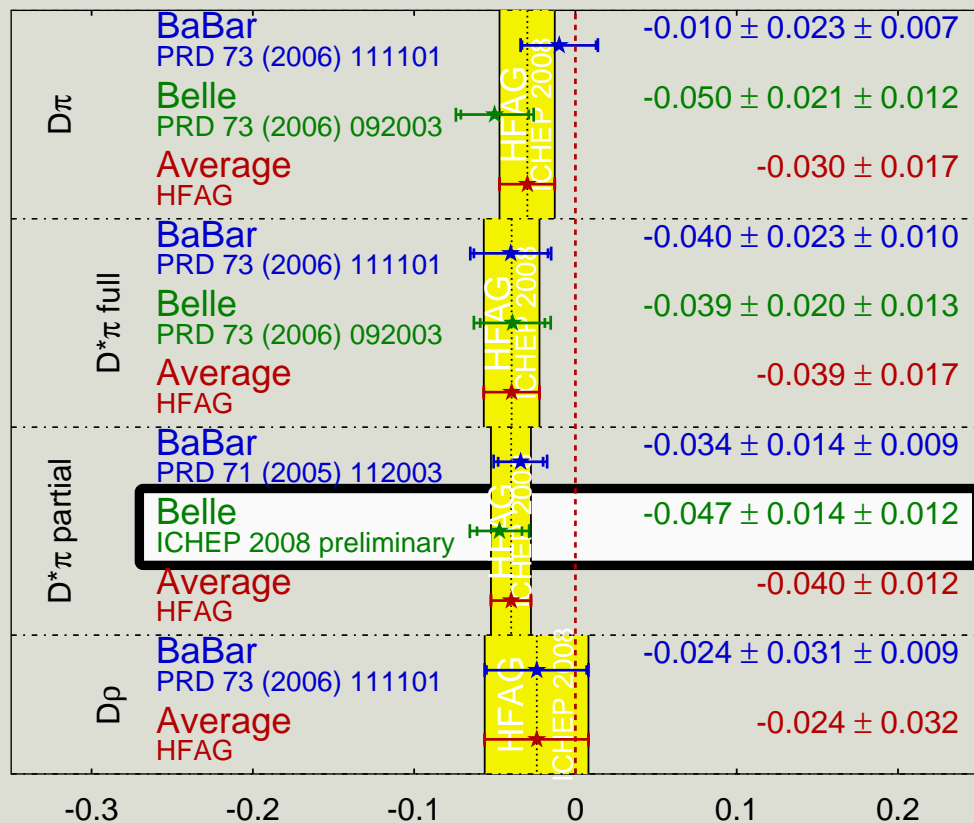
Belle result using partial reconstruction is updated from the previous plot



Updated HFAG average

a parameters

HFAG
ICHEP 2008
PRELIMINARY

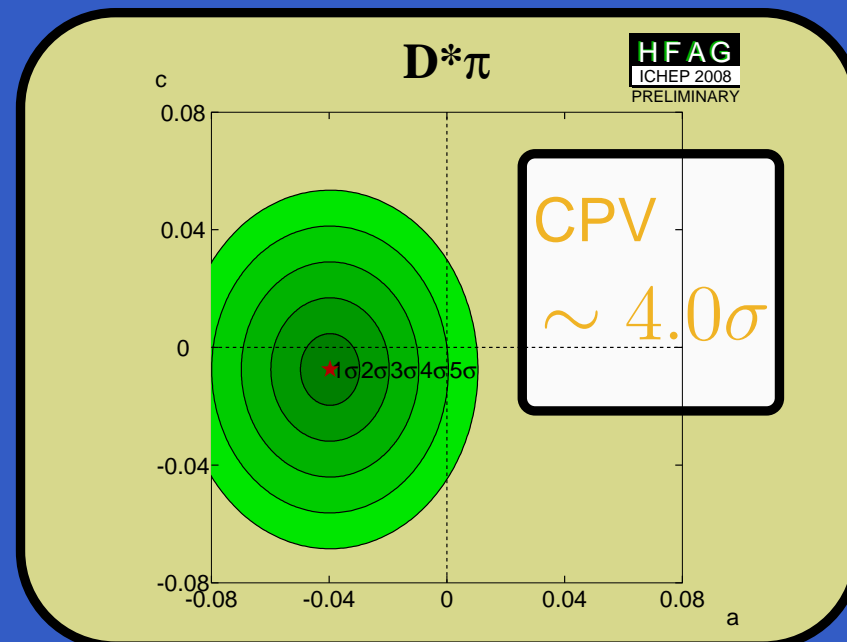


Belle result using partial reconstruction is updated from the previous plot

HFAG average for $D^*\pi$ [2008]:
(full and partial, Babar and Belle)

$$a = -0.040 \pm 0.010$$

$$c = -0.007 \pm 0.012$$



Estimate for R

- $2\phi_1 + \phi_3$ is to be derived from S using the relation,
$$S^\pm = -2 R \sin(2\phi_1 + \phi_3 \pm \delta).$$
- $2\phi_1 + \phi_3$ results in Belle (PRD 73, 092003 (2006)) were assuming SU(3)-breaking effect as 30% on R .
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- Another way using **isospin relation** has not been tested for a decade due to its small amplitude.
 $\mathcal{B}(B^+ \rightarrow D^{*+}\pi^0) < 1.7 \times 10^{-4}$ (90% C.L.) was only available from CLEO's results, PRL 80, 2762 (1998).

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 $\mathcal{B}(B^+ \rightarrow D^{*+}\pi^0) < 1.7 \times 10^{-4}$ (90% C.L.) was only available from CLEO's results, PRL 80, 2762 (1998).
- Assuming $R = 0.02$, and with $\mathcal{B}(B^0 \rightarrow D^{*-}\pi^+) = 2.76 \times 10^{-3}$ from PDG, $\mathcal{B}(B^+ \rightarrow D^{*+}\pi^0) = 5.9 \times 10^{-7}$.

$B^+ \rightarrow D^{*+} \pi^0$ reconstruction

$$B^+ \rightarrow D^{*+} \pi^0$$

$$\hookrightarrow D^0 \pi_s^+$$

$$\hookrightarrow K^- \pi^+$$

$$\hookrightarrow K^- \pi^+ \pi^0$$

$$\hookrightarrow K^- \pi^+ \pi^- \pi^+$$

$$\hookrightarrow K_S \pi^+ \pi^-$$

- 4 sub-decay modes are combined in reconstruction.

$B^+ \rightarrow D^{*+} \pi^0$ reconstruction

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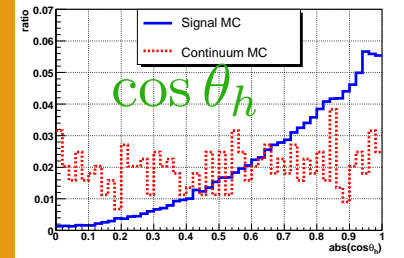
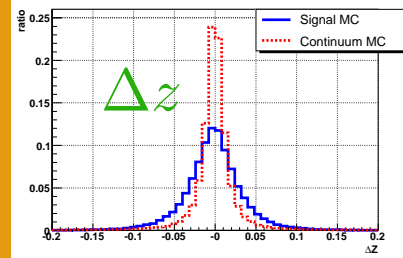
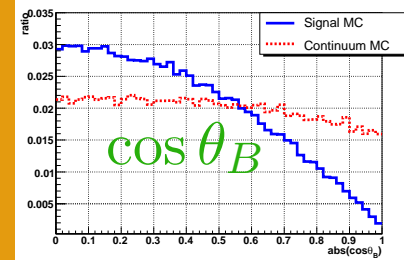
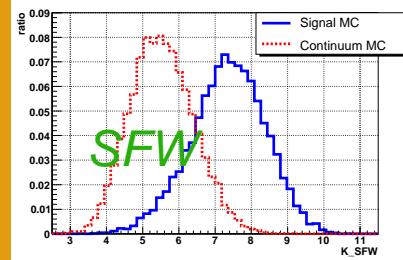
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- 4 sub-decay modes are combined in reconstruction.
- Likelihood is calculated through the combination of SFW, $\cos \theta_B$, Δz and $\cos \theta_h$.

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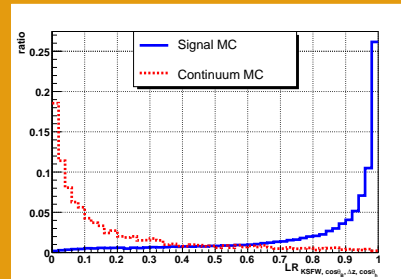
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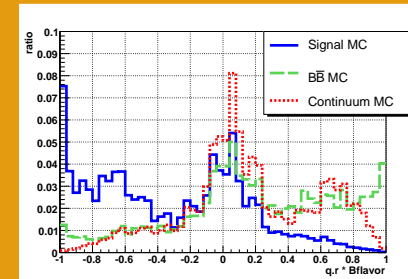
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*combined
likelihood*



*tagged B-flavor x
quality parameter*

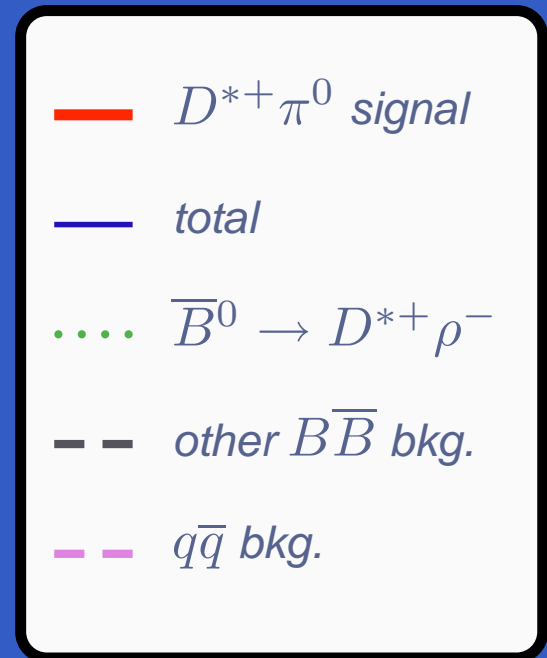
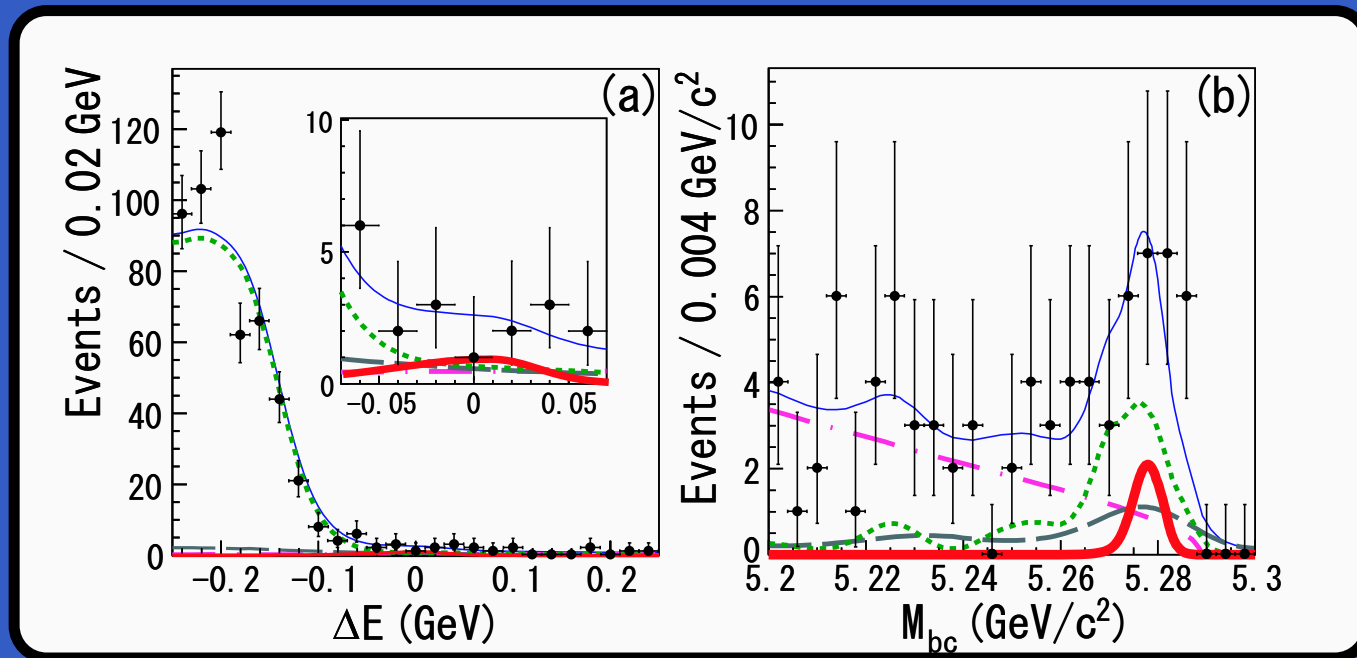
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- Likelihood is calculated through the combination of SFW, $\cos \theta_B$, Δz and $\cos \theta_h$.
- Its requirements are applied with the flavor information, for the maximal point of $S/\sqrt{S+B}$ in the signal region ($|\Delta E| < 0.1 \text{ GeV}$, $5.27 \text{ GeV}/c^2 < M_{bc} < 5.29 \text{ GeV}/c^2$).

Extraction of $B^+ \rightarrow D^{*+} \pi^0$ event and R

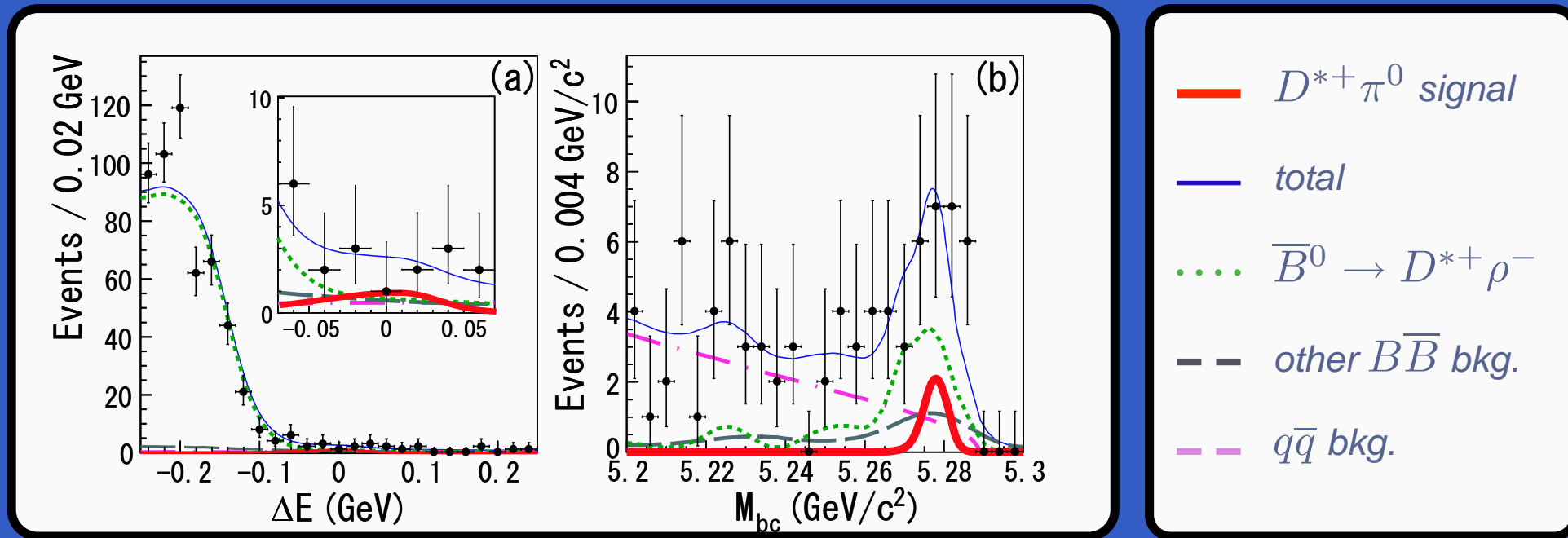
- Two-dimensional unbinned extended-ML fit

Extraction of $B^+ \rightarrow D^{*+} \pi^0$ event and R

- Two-dimensional unbinned extended-ML fit



■ Two-dimensional unbinned extended-ML fit



■ Signal event is extracted as $4.5^{+4.1}_{-3.4}$ in the signal region from 657 $M_{B\bar{B}}$ pairs ($\varepsilon = 0.56\%$ from MC).

$$\mathcal{B}(B^+ \rightarrow D^{*+} \pi^0) = [1.2^{+1.1}_{-0.9}(\text{stat})^{+0.3}_{-0.9}(\text{syst})] \times 10^{-6}$$

($< 3.6 \times 10^{-6}$ at 90% C.L.) $\rightarrow R < 0.051$ (90% C.L.)

Main systematic uncertainties for $\mathcal{B}(B^+ \rightarrow D^{*+}\pi^0)$

Source	Systematic error (number of events)	
	$+\sigma$	$-\sigma$
$ H_0 $ of $\bar{B}^0 \rightarrow D^{*+}\rho^-$	0.7	-1.9
ΔE shift of $\bar{B}^0 \rightarrow D^{*+}\rho^-$	0.0	-0.6
Fraction of backgrounds	0.8	-0.4
Gaussian width of background PDF	0.5	-2.0
2D correlation for $q\bar{q}$ and $B^+ \rightarrow D^{*+}\pi^0$	0.0	-1.3
Fit bias	0.0	-0.5
Quadratic sum	1.2	-3.2

Summary

- $a = 0.047 \pm 0.014 \pm 0.012$ $c = 0.009 \pm 0.014 \pm 0.012$

CPV in $B \rightarrow D^{*-} \pi^+$ is found to be 2.6σ from lepton-tag analysis of 657 M $B\bar{B}$ pairs at Belle.

- $\mathcal{B}(B^+ \rightarrow D^{*+} \pi^0) < 3.6 \times 10^{-6}$ $R < 0.051$ at 90% C.L.

from isospin relation. Estimate of R is still much better in SU(3)-related measurement. (Much data will be needed for using isospin, $\sim \times 10$ or more ..)

- Weak phase $2\phi_1 + \phi_3$ can be extracted using S^\pm . Additional **kaon-tag analysis** will be achieved in near future. SU(3) symmetry will be used to obtain $2\phi_1 + \phi_3$, at that time.

Other systematic uncertainties for $\mathcal{B}(B^+ \rightarrow D^{*+}\pi^0)$

Source	Systematic error (%)
	$\pm\sigma$
\mathcal{L} requirement	3.0
ΔM requirement	3.3
Secondary branching fractions	3.3
Track finding efficiency	5.1
Particle identification	4.4
π^0 reconstruction	4.1
K_S^0 reconstruction	0.3
MC statistics	0.5
Number of $B\bar{B}$ pairs	1.4
Quadratic sum	9.8

Experimental and theoretical estimate for R

$$R = \tan \theta_c \frac{f_{D^*}}{f_{D_s^*}} \sqrt{\frac{\mathcal{B}(B^0 \rightarrow D_s^{*+} \pi^-)}{\mathcal{B}(B^0 \rightarrow D_s^{*-} \pi^+)}}$$

- Belle PRD 73, 092003 (2006)

$$R(\%) = 2.0 \pm 0.7 \text{ (stat and syst)} \pm 0.6 \text{ (SU(3)-breaking)}$$

- Babar PRD 78, 032005 (2008) (for $R_{(D^* \pi)}$)

$$R(\%) = 1.81_{-0.15}^{+0.16} \text{ (stat)} \pm 0.09 \text{ (syst)} \pm 0.10 (f_D) \\ \pm \text{SU(3)-breaking (10 - 15\% on } R)$$

– still 15 – 20% error on R

$$\hookrightarrow \mathcal{B}(B^0 \rightarrow D_s^{*+} \pi^-) = [2.6_{-0.4}^{+0.5} \pm 0.2] \times 10^{-5}$$

$$\mathcal{B}(B^0 \rightarrow D_s^{*-} \pi^+) = [2.76 \pm 0.13] \times 10^{-3}$$

$$f_{D^*} / f_{D_s^*} = 1.24 \pm 0.07 \text{ (lattice QCD)}$$

W -exchange contribution (only seen in $B^0 \rightarrow D^{*\pm} \pi^\mp$) is included ($\sim 5\%$) in SU(3)-breaking.