

The CKM angle γ from neutral B decays in BaBar



Outline

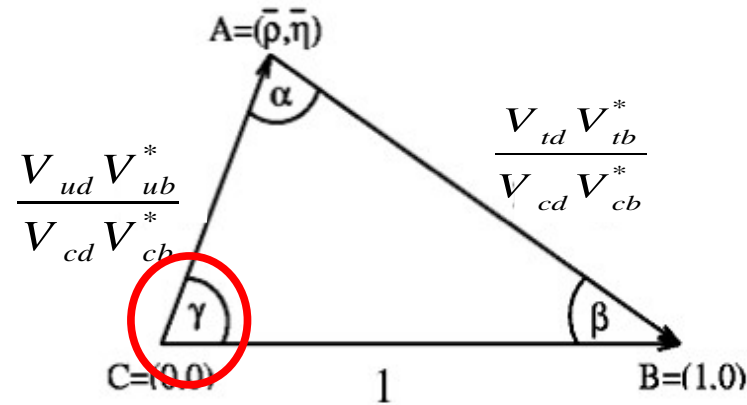
- The CKM angle γ and the r_B ratios
- Some news on $\sin(2\beta+\gamma)$ from $B \rightarrow D^{(*)\mp} \pi^\pm(\rho^\pm)$
- Time dependent Dalitz analysis of $B \rightarrow D^{\mp} K^0 \pi^\pm$ decays for the determination of $2\beta+\gamma$
- The $B^0 \rightarrow D^0 K^{*0}$ system
 - ADS analysis of $B^0 \rightarrow D^0 K^{*0}$ decays for the determination of the ratio $r_s = |A(b \rightarrow u)| / |A(b \rightarrow c)|$
 - Dalitz analysis of $B^0 \rightarrow D^0 K^{*0}$ decays for the determination of γ
- Conclusions

The CKM angle γ

Wolfenstein parametrization:

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(\bar{\rho} - i\bar{\eta}) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A\lambda^3(1 - \bar{\rho} - i\bar{\eta}) & -A\lambda^2 & 1 \end{pmatrix}$$

$\lambda \sim 0.22, A \sim 0.8$



$$\gamma = \arg \left\{ -\frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*} \right\}$$

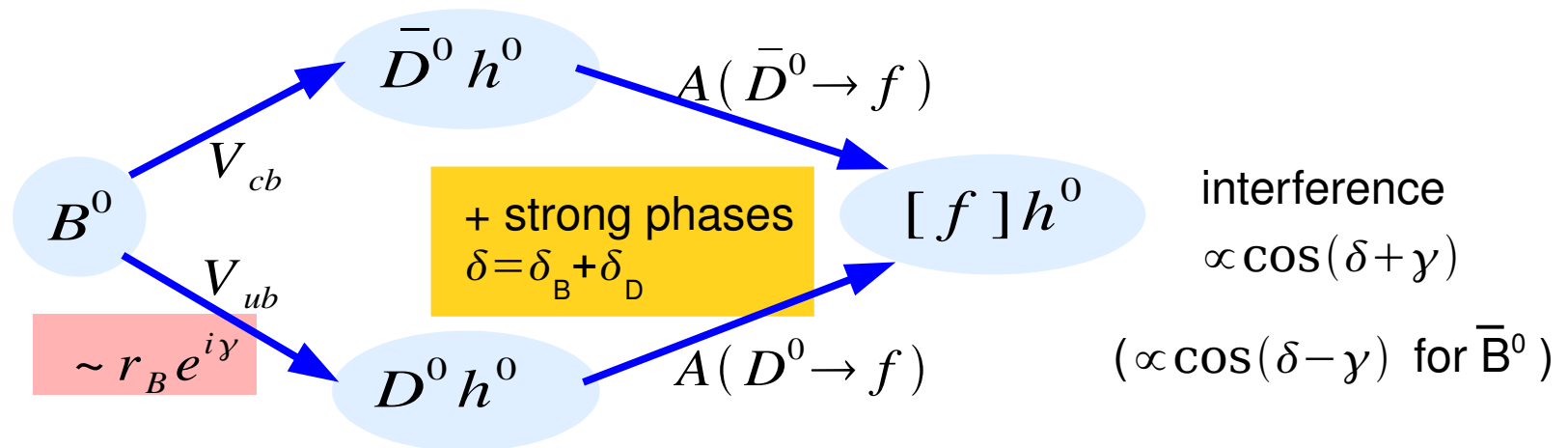
In Wolfenstein parametrization, $V_{ub} = \sqrt{\bar{\rho}^2 + \bar{\eta}^2} e^{-i\gamma} \rightarrow \gamma$ is the phase of V_{ub}^*

The angle determined exploiting the interference between $b \rightarrow u$ and $b \rightarrow c$ transitions in $B \rightarrow D\pi$ and $B \rightarrow DK$ decays

Interference scheme

Interference in the $B \rightarrow D\pi$ and $B \rightarrow DK$ system allows the determination of γ

$$|A_1 + A_2 e^{i\phi}|^2 = A_1^2 + A_2^2 + 2A_1 A_2 \cos(\phi)$$



Main characters: γ , r_B , δ

Sensitivity to γ is driven by the ratio $r_B = |A(\mathbf{b} \rightarrow \mathbf{u})|/|A(\mathbf{b} \rightarrow \mathbf{c})|$ (channel-dependent).

$\sin(2\beta+\gamma)$ from $B \rightarrow D^{(*)\mp} \pi^\pm(\rho^\pm)$: some news...

Relative weak phase within Cabibbo-favoured amplitude ($B^0 \rightarrow D^- \pi^+$) and Cabibbo-suppressed ($B^0 \rightarrow D^+ \pi^-$) one gives sensitivity to γ .

When combined with the B_d mixing phase $\rightarrow 2\beta+\gamma$.

Size of CP violating effect proportional to $r_{D\pi} = |A(B^0 \rightarrow D^+ \pi^-)| / |A(B^0 \rightarrow D^- \pi^+)| \sim 0.02$.

Assuming SU(3) and neglecting annihilation contributions, one can estimate $BR(B^0 \rightarrow D^{(*)+} \pi^-(\rho^-))$ and r_D ratios from **$BR(B^0 \rightarrow D_s^{(*)+} \pi^-(\rho^-))$**

New Babar measurement (Phys.Rev.D78:032005, 2008):

- tests the hypothesis of negligible annihilation (from $B^0 \rightarrow D_s^- K^+$ BR) contribution
- measures:

$$BR(B^0 \rightarrow D_s^+ \pi^-) = (2.5 \pm 0.4 \pm 0.2) 10^{-5}$$

$$BR(B^0 \rightarrow D_s^{*+} \pi^-) = (2.6_{-0.4}^{+0.5} \pm 0.2) 10^{-5}$$

$$BR(B^0 \rightarrow D_s^+ \rho^-) = (1.1_{-0.8}^{+0.9} \pm 0.3) 10^{-5}$$



$$r_{D\pi} = (1.78_{-0.13}^{+0.14} \pm 0.08 \pm 0.10) \%$$

$$r_{D^*\pi} = (1.81_{-0.15}^{+0.16} \pm 0.09 \pm 0.10) \%$$

$$r_{D\rho} = (0.71_{-0.27}^{+0.29} \pm 0.10 \pm 0.04) \%$$

all **amplitude ratios** below 2%:
very low sensitivity to $\sin(2\beta+\gamma)$ in
 $B \rightarrow D^\mp \pi^\pm(\rho^\pm)$ channels!

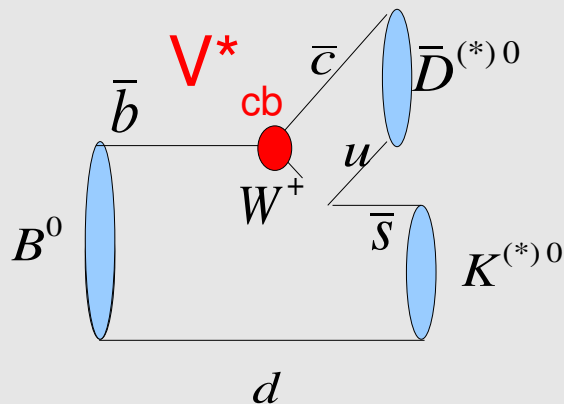
SU(3)
no annihilation
 $f_{D^{(*)}_s} / f_{D^{(*)}} = 1.24 \pm 0.07$

γ in neutral $B \rightarrow DK$ decays

Relative weak phase between V_{ub} and V_{cb} CKM elements, studied in the $B \rightarrow DK$ system, in the interference between $b \rightarrow c$ and $b \rightarrow u$ transitions when both the B^0 and B^0 bar decay to the same final state.

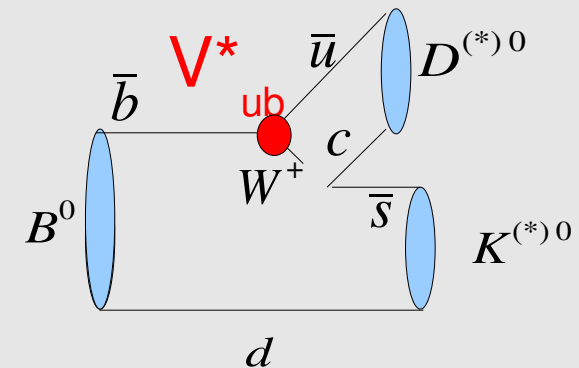
$b \rightarrow c$ transition

$$B^0 \rightarrow D^{(*)0} K^{*0}$$



$b \rightarrow u$ transition

$$B^0 \rightarrow D^{(*)0} K^{*0}$$



The B^0 and B^0 bar mix, time dependent analyses, sensitivity to $(2\beta + \gamma)$

If the flavour of the neutral B can be determined, sensitivity to γ

the r_B ratios

Sensitivity to γ in each channel driven by the ratio $r_B = |A(b \rightarrow u)| / |A(b \rightarrow c)|$

$$r_B(D^0 K^+) = \frac{|A(B^+ \rightarrow D^0 K^+)|}{|A(B^+ \rightarrow \bar{D}^0 K^+)|} = \frac{|V_{cs} V_{ub}^*|}{|V_{us} V_{cb}^*|} \frac{|\bar{C} + A|}{|T + C|}$$

T tree
C, \bar{C} colour-suppressed
A annihilation

Hadronic elements,
complex quantities.

$|C|/|T| \sim 0.3$
 $|A|/|C| \sim 0.2$

$$r_B(D^0 K^0) = \frac{|A(B^0 \rightarrow D^0 K^0)|}{|A(B^0 \rightarrow \bar{D}^0 K^0)|} = \frac{|V_{cs} V_{ub}^*|}{|V_{us} V_{cb}^*|} \frac{|\bar{C}|}{|C|}$$

$$R_b \sim 0.35$$

$$R_b = \frac{|V_{ud} V_{ub}^*|}{|V_{cd} V_{cb}^*|} = \sqrt{\rho^2 + \eta^2} = \left(1 - \frac{\lambda^2}{2}\right) \frac{1}{\lambda} \left| \frac{V_{ub}}{V_{cb}} \right|$$

For the $B^+ \rightarrow D^{(*)0} K^+$, the r_B ratio is of the order ~ 0.1 (in amplitude!)

For the $B^0 \rightarrow D^{(*)0} K^{(*)0}$, the r_B ratio is expected to be of the order ~ 0.4

Need to be measured!

Time dependent Dalitz plot analysis of



Phys. Rev. D 77: 071102, 2008

- $D^{*0}[D\pi]K^0$ states, interference between $b \rightarrow u$ and $b \rightarrow c$ transitions through the mixing
- one B fully reconstructed in $D^{\mp} K^0 \pi^{\pm}$, the flavour of the other one identified at decay
- three-body B decay: $2\beta + \gamma$ (2-fold ambiguity) from analysis of Dalitz distribution (\vec{x}) as a function of proper time difference Δt .

Likelihood:

$$P(\vec{x}, \Delta t, \xi, \eta) = \frac{A_c^2(\vec{x}) + A_u^2(\vec{x})}{2} \frac{e^{-|\Delta t|/\tau_b}}{4\tau_B} \{ 1 - \eta \xi C(\vec{x}) \cos(\Delta m_d \Delta t) + \xi S_{\eta}(\vec{x}) \sin(\Delta m_d \Delta t) \}$$

$$S_{\eta}(\vec{x}) = \frac{2 \operatorname{Im}(A_c(\vec{x}) A_u(\vec{x}) e^{i(2\beta + \gamma) + \eta i(\Phi_c(\vec{x}) - \Phi_u(\vec{x}))})}{A_c^2(\vec{x}) + A_u^2(\vec{x})} \quad C(\vec{x}) = \frac{A_c^2(\vec{x}) - A_u^2(\vec{x})}{A_c^2(\vec{x}) + A_u^2(\vec{x})}$$

$$\xi = 1 (-1) \text{ for } B^0 (\bar{B}^0) \quad \eta = 1 (-1) \text{ for } D^+ (D^-)$$

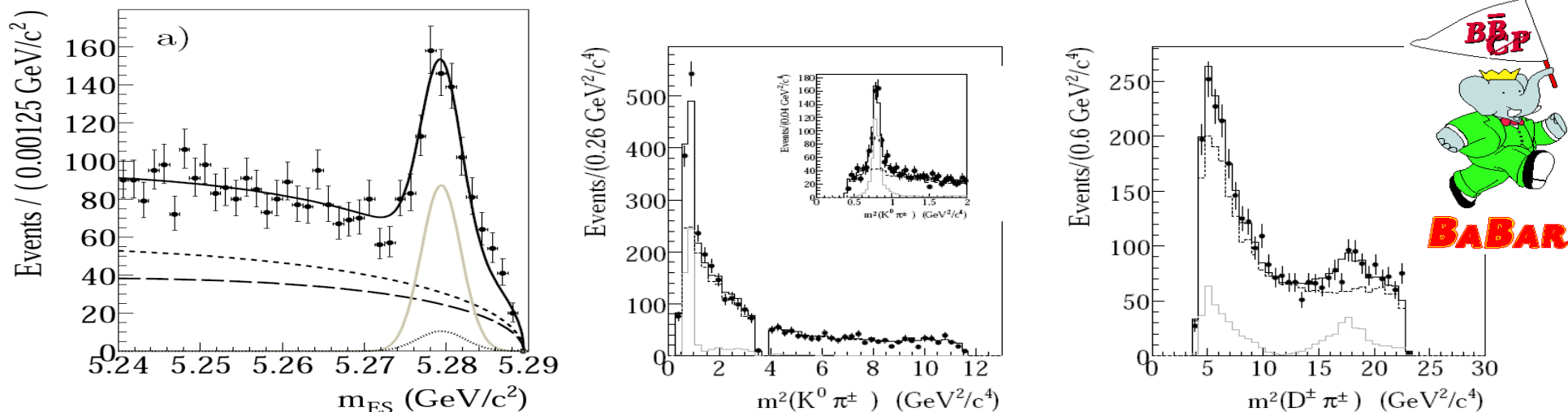
- B Dalitz distribution written as a sum of intermediate 2-body states with resonances
- amplitudes A_c and phases Φ_c, Φ_u floated in the fit. Ratio $r = |A_u/A_c|$ fixed to 0.3 (± 0.1 variation included in systematics)

Time dependent Dalitz plot analysis of $B \rightarrow D^{\mp} K^0 \pi^{\pm}$, results on $2\beta + \gamma$

Phys. Rev. D 77: 071102, 2008

Analysis performed on 347 millions of BB pairs.

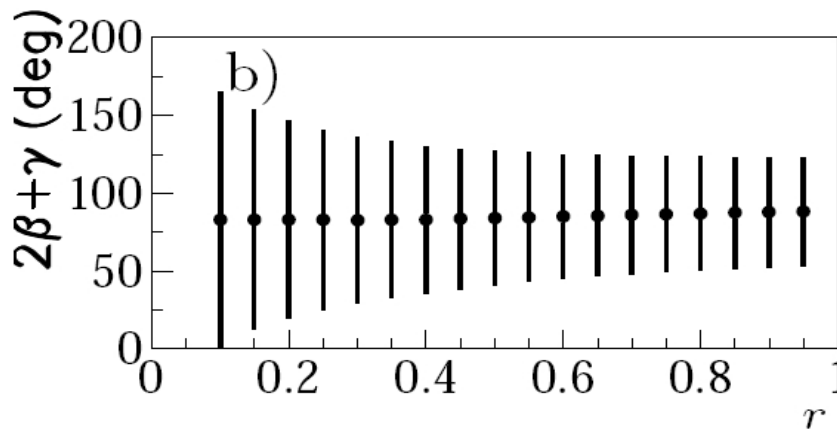
Number of signal events $N = 558 \pm 34$ (likelihood fit on m_{ES} , ΔE and event shape variables)



$$2\beta + \gamma = (83 \pm 53 \pm 20)^{\circ} (\text{mod. } 180^{\circ})$$

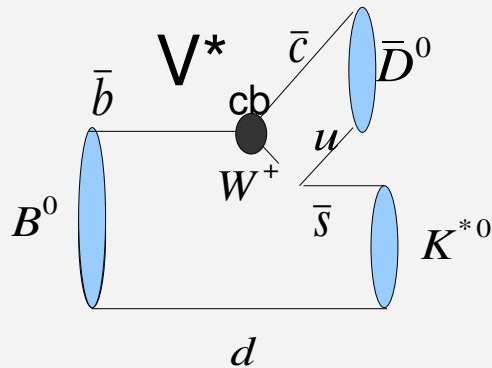
error statistically dominated, main systematics from the background Dalitz plot parametrization

Behaviour of the error for different fixed r values: scan of $2\beta + \gamma$ as a function of $r = |A_c/A_u|$



$B^0 \rightarrow D^0 K(892)^{*0} [K^+ \pi^-]$: a self tagging system

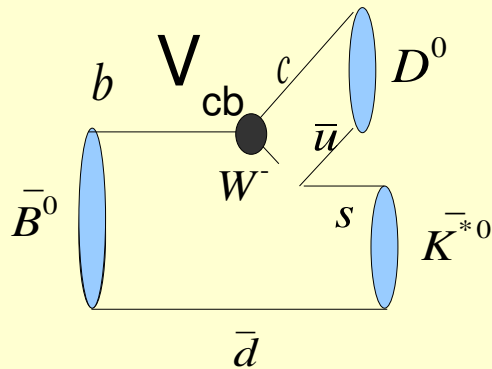
Other Babar analyses exploit the $B^0 \rightarrow D^0 K^{*0} [K^+ \pi^-]$ system



$$B^0 \rightarrow D^{(*)0} K^{*0}$$

A B^0 always decays into a K^{*0} in the final state, which decays into $K^+ \pi^-$

$$K^{*0} \rightarrow K^+ \pi^-$$



$$\bar{B}^0 \rightarrow D^{(*)0} \bar{K}^{*0}$$

A \bar{B}^0 always decays into a \bar{K}^{*0} in the final state, which decays into $K^- \pi^+$

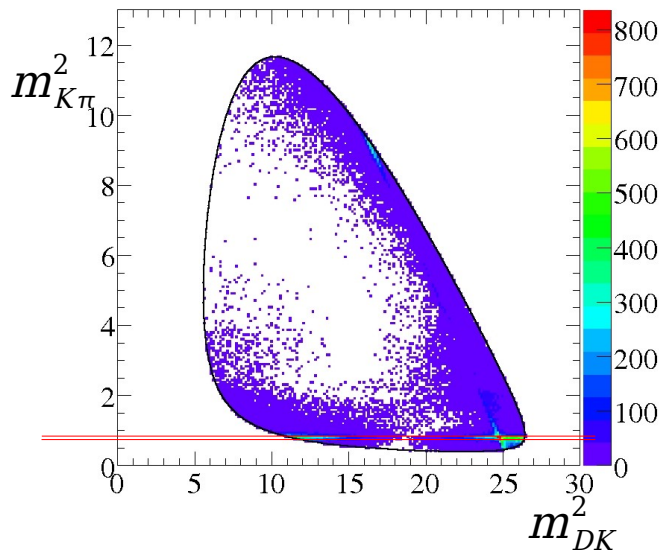
$$\bar{K}^{*0} \rightarrow K^- \pi^+$$

The charge of the kaon in the final state identifies the flavour of the neutral B, sensitivity to γ

$B^0 \rightarrow D^0 K^{*0} [K^+ \pi^-]$: the ratio r_S

Natural width of the K^* has to be considered, effective parameters are introduced:

M.Gronau, Phys.Lett. B557 (2003) 198-206



$$r_S^2 \equiv \frac{\Gamma(B^0 \rightarrow D^0 K^+ \pi^-)}{\Gamma(B^0 \rightarrow \bar{D}^0 K^+ \pi^-)} = \frac{\int dp A_u^2(p)}{\int dp A_c^2(p)},$$

$$k e^{i\delta_S} \equiv \frac{\int dp A_c(p) A_u(p) e^{i\delta(p)}}{\sqrt{\int dp A_c^2(p) \int dp A_u^2(p)}},$$

$B \rightarrow DK^*(K\pi)$

p indicates the point on the $B \rightarrow DK\pi$ Dalitz plot

where k accounts for contributions of non- $K^{*0}(892)$ resonances and in principle is an additional unknown (in case of two-body B decay, $k \rightarrow 1$, $r_S \rightarrow r_B$, $\delta_S \rightarrow \delta_B$).

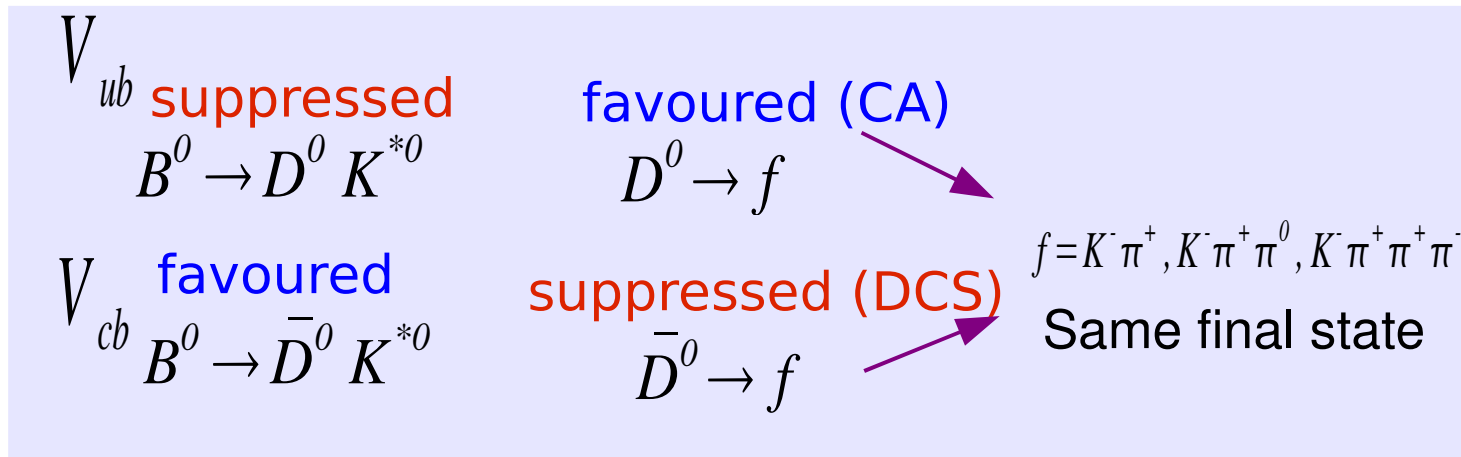
It is evaluated to be 0.95 ± 0.03 with a simulation study.

S.Pruvot, M.-H.Schune, V.Sordini, A.Stocchi in hep-ph/0703292
(to appear in Nagoya CKM workshop proceedings)

Integrals over the $B \rightarrow DK\pi$ Dalitz plot in a region corresponding to the K^* .
Quantities dependent on the cuts applied on the Dalitz plot plane (cuts on K^* mass and helicity) !

The ADS method

D.Atwood, I.Dunietz and A.Soni, Phys.Rev.Lett. 78, 3257 (1997)



"opposite sign" events (the kaon from the K^* and the one from the D have **OPPOSITE** charge)

$$R_{ADS} \equiv \frac{\Gamma(B^0 \rightarrow f K^{*0}) + \Gamma(\bar{B}^0 \rightarrow \bar{f} \bar{K}^{*0})}{\Gamma(B^0 \rightarrow \bar{f} K^{*0}) + \Gamma(B^0 \rightarrow f K^{*0})} \begin{matrix} \longrightarrow V_{cb} DCS + V_{ub} CA \\ \longrightarrow V_{cb} CA + V_{ub} DCS \end{matrix}$$

"same sign" events (the kaon from the K^* and the one from the D have the **SAME** charge)

$$R_{ADS}(K\pi) \equiv \frac{\Gamma(B^0 \rightarrow K^- \pi^+ [K^+ \pi^-]_{K^{*0}}) + \Gamma(\bar{B}^0 \rightarrow K^+ \pi^- [K^- \pi^+]_{K^{*0}})}{\Gamma(B^0 \rightarrow K^+ \pi^- [K^+ \pi^-]_{K^{*0}}) + \Gamma(B^0 \rightarrow K^- \pi^+ [K^- \pi^+]_{K^{*0}})}$$

The ADS method multi-body D decay

The three R_{ADS} ratios can be written as:

$$R_{ADS}(K\pi) = r_S^2 + r_D^2(K\pi) + 2k r_S r_D(K\pi) \cos(\delta_D(K\pi) + \delta_S) \cos\gamma$$

$$R_{ADS}(K\pi\pi^0) = r_S^2 + r_D^2(K\pi\pi^0) + 2k k_D(K\pi\pi^0) r_S r_D(K\pi\pi^0) \cos(\delta_D(K\pi\pi^0) + \delta_S) \cos\gamma$$

$$R_{ADS}(K3\pi) = r_S^2 + r_D^2(K3\pi) + 2k k_D(K3\pi) r_S r_D(K3\pi) \cos(\delta_D(K3\pi) + \delta_S) \cos\gamma$$

$$r_D = \sqrt{\frac{BR(D^0 \rightarrow \bar{f})}{BR(D^0 \rightarrow f)}} \quad \delta_D \text{ relative strong phase between } D^0 \rightarrow f \text{ and } D^0 \rightarrow \bar{f}$$

multi-body D final state

$$k_D e^{i\delta_D} = \frac{\int A_D \bar{A}_D e^{i(\bar{\delta}(m) - \delta(m))} dm}{\sqrt{\int |\bar{A}_D|^2 dm \int |A_D|^2 dm}}$$

$r_D \ll r_S$ ($r_D \sim 0.05$):

- low sensitivity to γ
- $R_{ADS} \sim r_S^2$

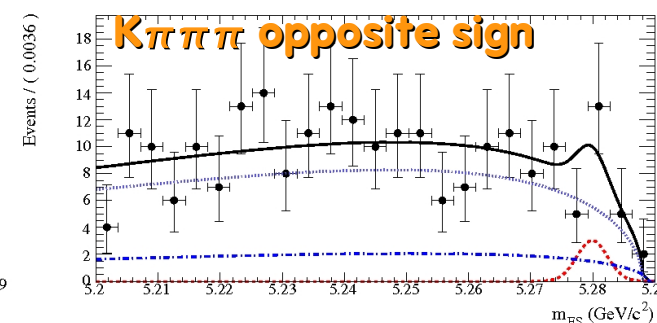
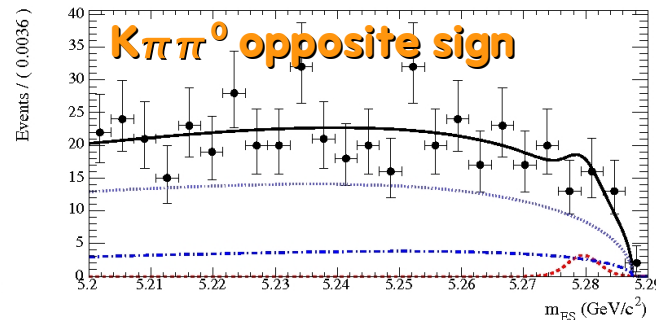
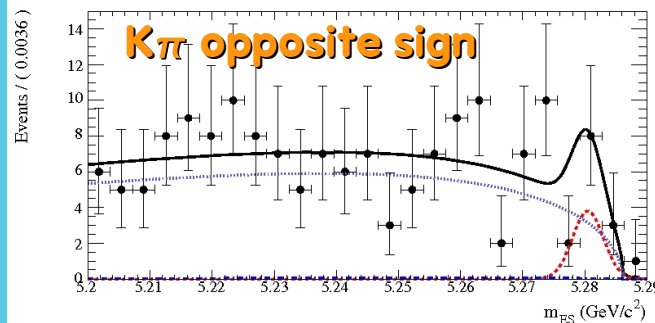
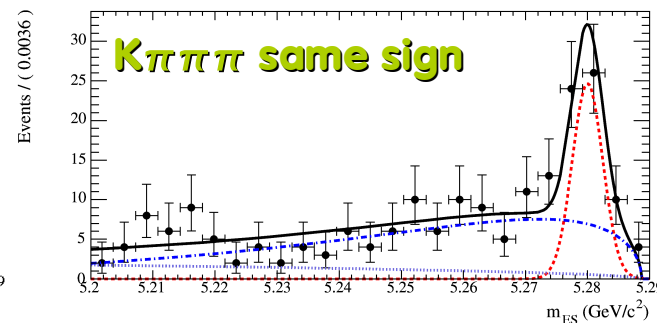
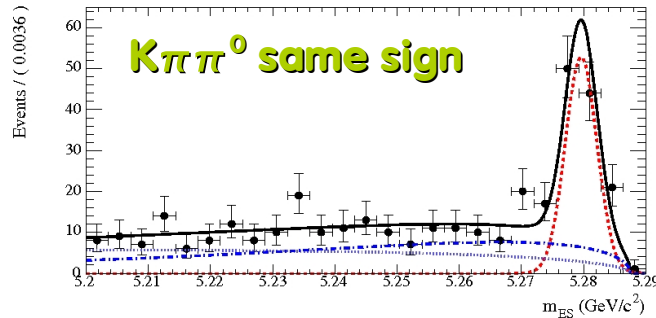
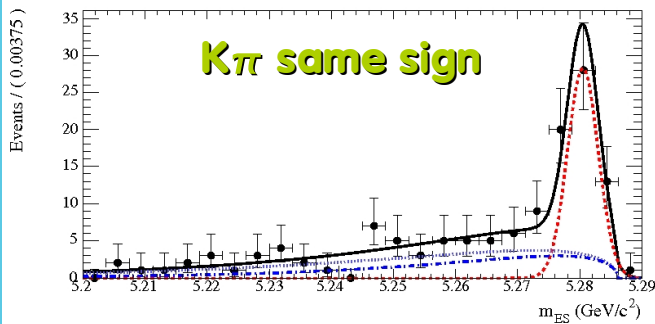
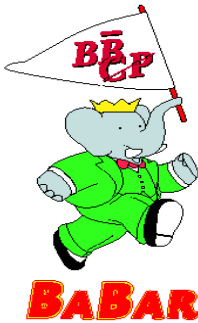
Ratios r_D measured. Input from CLEO-c on k_D and δ_D for $K\pi\pi^0$ and δ_D for $K\pi$

$B^0 \rightarrow D^0 K^{*0} [K^+ \pi^-]$ ADS analysis

$$(D^0 \rightarrow K^{\mp} \pi^{\pm}, K^{\mp} \pi^{\pm} \pi^0, K^{\mp} \pi^{\pm} \pi^{\mp} \pi^{\pm})$$

- analysis performed on 465 millions of BB pairs
- selection optimized on $b \rightarrow u$ events, maximizing $S/\sqrt{(S+B)}$
- likelihood fit to m_{ES} and event shape variables,
total number of **opposite sign** events $N=24^{+14}_{-11}$ (2.2σ significance)
- statistically dominated. Main systematics from peaking background

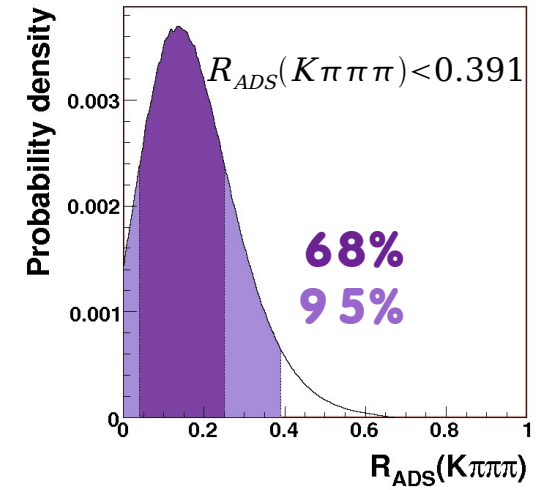
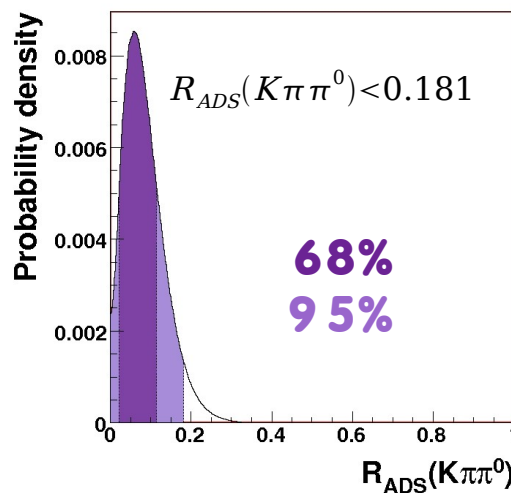
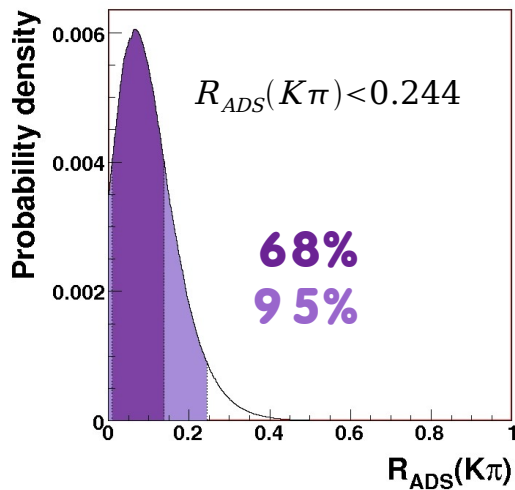
Preliminary, to be submitted to Phys.Rev.D



signal enhanced m_{ES} projections of the likelihood on data

$B^0 \rightarrow D^0 K^{*0} [K^+ \pi^-]$ ADS analysis ($D^0 \rightarrow K^{\mp} \pi^{\pm}, K^{\mp} \pi^{\pm} \pi^0, K^{\mp} \pi^{\pm} \pi^{\mp} \pi^{\pm}$)

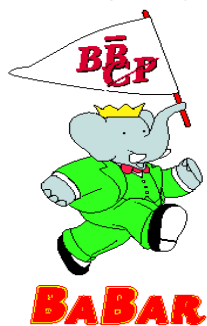
- likelihood scan for the three R_{ADS} ratios and 95% probability bayesian limits



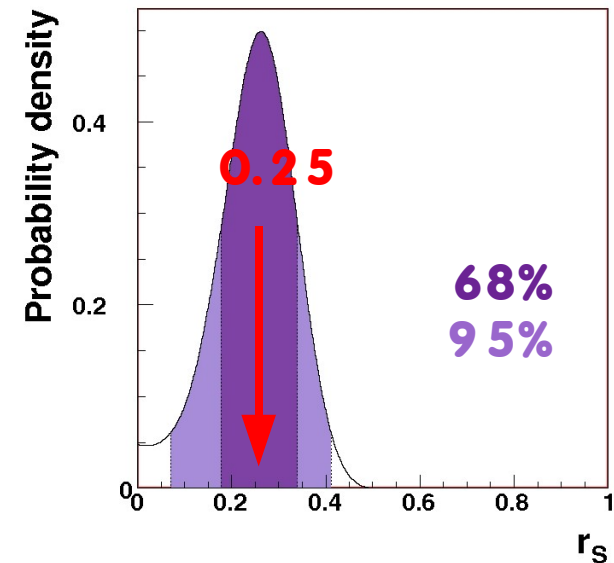
Ignoring differences in r_D and strong phases within the three channels.. $\langle R_{ADS} \rangle = 0.078^{+0.037}_{-0.035}$

Combining the three modes and using external inputs (r_D ratios from the PDG and CLEO-c

likelihood for k_D and δ_D):



$r_S \in [0.18, 0.34]$ at 68% prob.
 $r_S \in [0.07, 0.41]$ at 95% prob.



$B^0 \rightarrow D^0 [K_S \pi^+ \pi^-] K^{*0} [K^+ \pi^-]$ Dalitz analysis

A.Giri, Y.Grossman, A.Soffer and J.Zupan, Phys.Rev.D 68 (2003) 054081

$$A(B^0) \sim f(s_{12}, s_{13}) + r_s e^{i(\delta+\gamma)} f(s_{13}, s_{12})$$

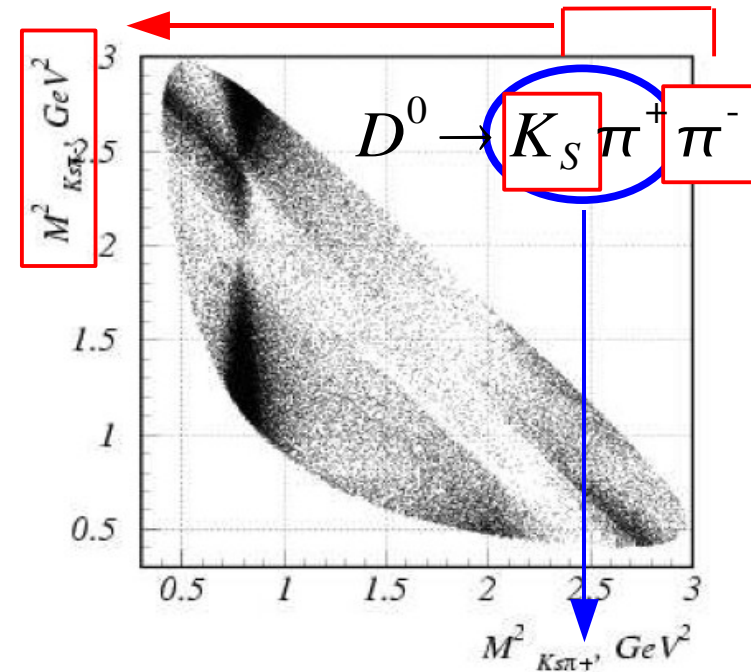
$$A(\bar{B}^0) \sim f(s_{13}, s_{12}) + r_s e^{i(\delta-\gamma)} f(s_{12}, s_{13})$$

V_{cb} amplitude

V_{ub} amplitude
 $(V_{ub} = |V_{ub}| e^{-i\gamma})$

Same final state $B^0 \rightarrow D^0 K^{*0}$:

sensitivity to $\delta-\gamma$ in the interference



D^0 Dalitz plane distribution $f(s_{12}, s_{13})$ parametrized as sum of Breit-Wigner :

same as in charged B Dalitz analysis!

$$f_- = f(s_{13}, s_{12}) \quad f_+ = f(s_{12}, s_{13})$$

$$P_{Sig}(B^0 / \bar{B}^0) = |f_{\mp}|^2 + r_s^2 |f_{\pm}|^2$$

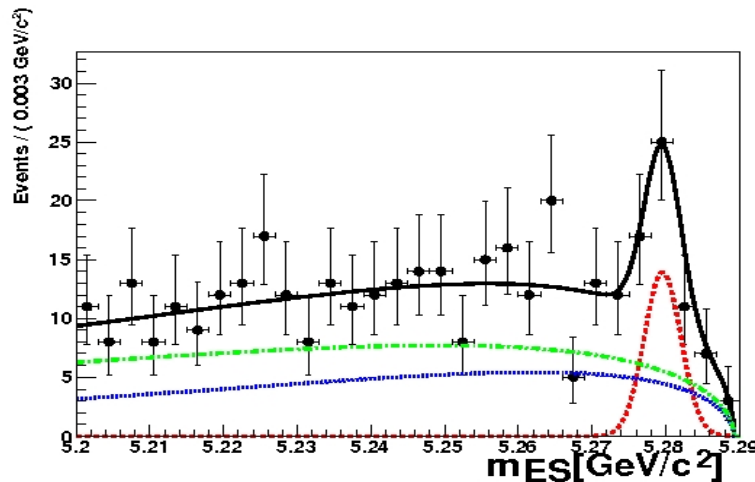
$$+ 2k r_s (\Re \{ f_{\mp} f_{\pm}^* \} \cos(\delta_s \mp \gamma) - \Im \{ f_{\mp} f_{\pm}^* \} \sin(\delta_s \mp \gamma))$$

V_{cb} term is the one from \bar{D}^0 for the B^0 , the one from D^0 for the \bar{B}^0 .

$B^0 \rightarrow D^0 K^{*0} [K^+ \pi^-]$ Dalitz analysis

Preliminary, to be submitted to Phys.Rev.D

- Analysis of $B^0 \rightarrow D^0 K^{*0}$, with $D^0 \rightarrow K_S \pi^+ \pi^-$ and $K^{*0} \rightarrow K^- \pi^+$
- same cuts on $B \rightarrow DK\pi$ Dalitz plot (K^* mass and helicity) as ADS analysis
- first analysis extracting directly γ from neutral $B^0 \rightarrow D^0 K^{*0}$ decays.
- m_{ES} and shape variables used in a maximum likelihood fit to discriminate between signal and background
- all peaking contribution found negligible



Analysis performed on **371M** of BB pairs.
Number of signal events $N=39 \pm 9$

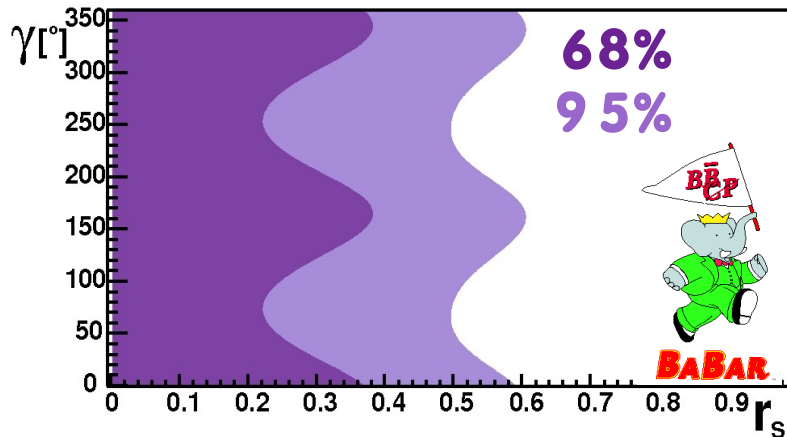


signal enhanced m_{ES} projections of the likelihood on data

$B^0 \rightarrow D^0 K^{*0} [K^+ \pi^-]$ Dalitz analysis

Preliminary, to be submitted to Phys.Rev.D

- D^0 Dalitz distribution used as an input in the fit
- CP fit for extraction of a 3-dimensional likelihood for γ, r_s, δ

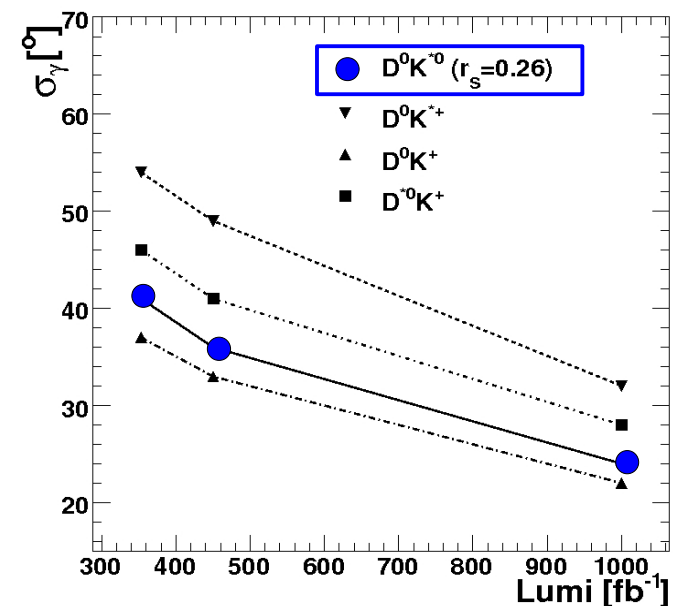


Combined with the likelihood for r_s from B.Aubert et al (Babar coll.) Phys.Rev. D74, 031101 (2006)

$$\gamma = (162 \pm 56)^\circ \pmod{180^\circ}$$

- main error statistical (55°)
- average error on toy-MC, for $r_s=0.3$, is $(45 \pm 14)^\circ$
- main source of systematics from Dalitz model (evaluated on data), assumed Gaussian and convoluted with the 3-dimensional likelihood

From toy-MC studies: this channel sensitivity is comparable with the one of a single channel for the charged B Dalitz analysis



conclusions



- $B \rightarrow D^{(*)\mp} \pi^{\pm} (\rho^{\pm})$ channels confirmed to have low sensitivity to γ ($r_D \sim 2\%$)
- Angle γ known mainly from charged $B \rightarrow DK$, small values of the r_B ratios (~ 0.1)
- Neutral $B \rightarrow DK$ decays can give access to γ as well
- Using a time dependent Dalitz analysis of $B \rightarrow D^{\mp} K^0 \pi^{\pm}$ decays, Babar finds $2\beta + \gamma = (83 \pm 53 \pm 20)^{\circ}$ (with a 180° ambiguity)
- $r_S = |A(b \rightarrow u)| / |A(b \rightarrow c)|$ for $B^0 \rightarrow D^0 K^{*0}$ decays found to be $r_S \sim 0.25$, which makes this channel very promising for γ determinations (preliminary)
- first attempt of exploiting this channel for the extraction of γ using a Dalitz analysis of $B^0 \rightarrow D^0 K^{*0}$ decays gives $\gamma = (162 \pm 56)^{\circ}$ (with a 180° ambiguity) (preliminary)
- With higher statistics, these analyses could give an important contribution to the determination of the angle γ

Backup slides

CPV in the SM

Field theory that describes strong, weak and electromagnetic interactions in terms of gauge group theories, starting from the elementary particles.

strong interactions

gauge group

$$SU(3) \times SU(2) \times U(1)$$

electroweak interactions

color symmetry
(strong interactions)

isospin
symmetry
(weak)

hypercharge
symmetry

6 leptons (antileptons), in three families

$$\begin{pmatrix} \nu_e \\ e \end{pmatrix}, \begin{pmatrix} \nu_\mu \\ \mu \end{pmatrix}, \begin{pmatrix} \nu_\tau \\ \tau \end{pmatrix}$$

6 quarks (antiquarks), in three families

$$\begin{pmatrix} u \\ d \end{pmatrix}, \begin{pmatrix} c \\ s \end{pmatrix}, \begin{pmatrix} t \\ b \end{pmatrix}$$

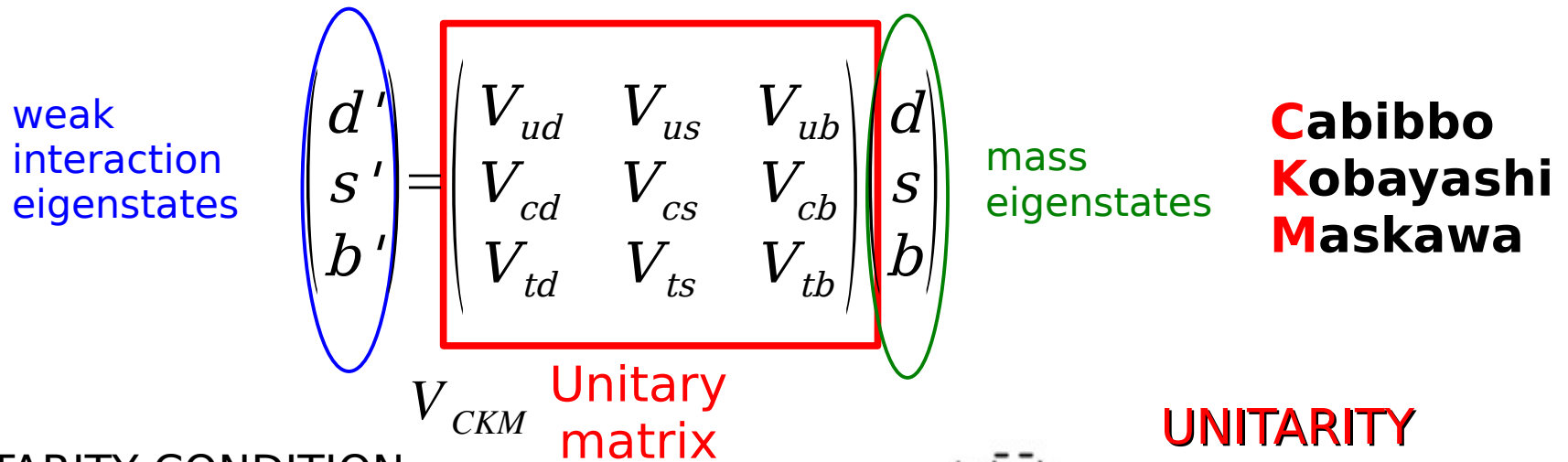
Parity :

$$P(t, \vec{x}) = (t, -\vec{x})$$

Charge conjugation: particle \rightarrow antiparticle

CP violation discovered in 1964 in the K rare decays and then confirmed by the B-factories results

The CKM matrix and the Unitarity Triangle



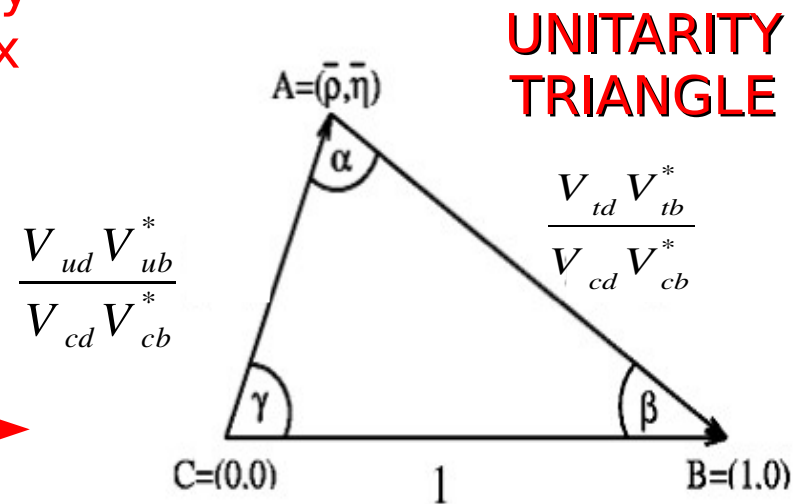
UNITARITY CONDITION:

$$V_{CKM} V_{CKM}^+ = V_{CKM}^+ V_{CKM} = 1$$

six independent relations,
within them we choose:

$$V_{ub}^* V_{ud} + V_{cb}^* V_{cd} + V_{tb}^* V_{td} = 0 \quad \rightarrow$$

B physics



In a complex plane $(\bar{\rho}, \bar{\eta})$

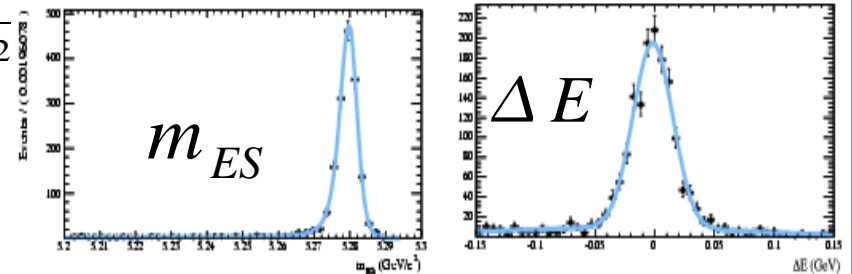
Experimental measurement techniques

Exclusive reconstruction of B decays. Two sources of background: from $B\bar{B}$ events and from **continuum events** ($e^+e^- \rightarrow q\bar{q}$, with $q=u,d,s,c$).

Two almost-independent kinematic variables to characterize the B mesons:

$$m_{ES}(M_{bc}) = \sqrt{(s/2 + \vec{p}_B \vec{p}_{ee})^2 / E_{ee}^2 - \vec{p}_B^2}$$

$$\Delta E = E_B^* - \sqrt{s/2}$$

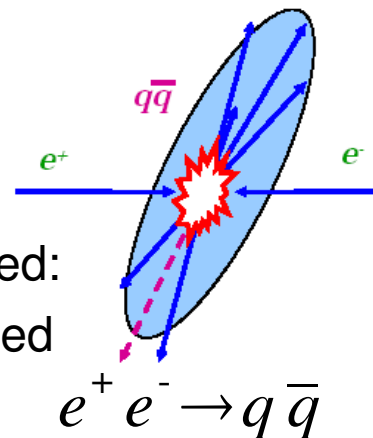


$(E_{B(ee)}, p_{B(ee)})$ = 4-momentum of the reconstructed B or of the e^+e^- initial state in the laboratory frame. The * denotes the e^+e^- center of mass (CM) frame

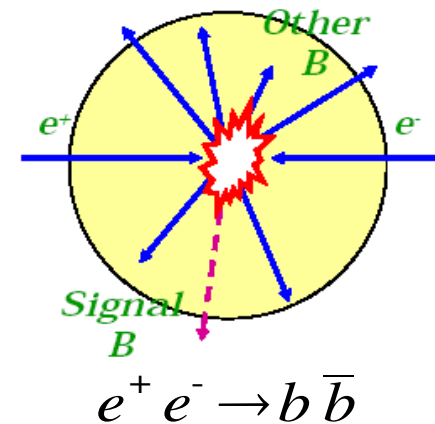
Typically, in all these analyses, dominant source of background: **continuum events** ($e^+e^- \rightarrow q\bar{q}$, with $q=u,d,s,c$).

Different spatial distribution is exploited: several topological variables (combined in a Fisher discriminant)

jet-like shape

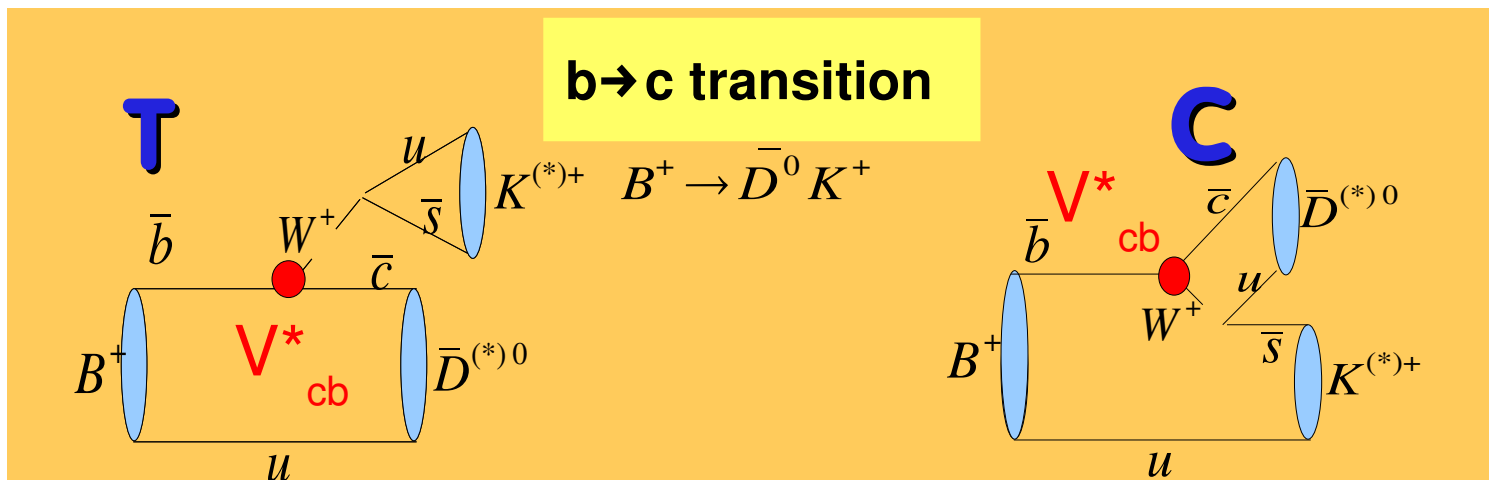


isotropic shape



γ in charged $B \rightarrow DK$ decays

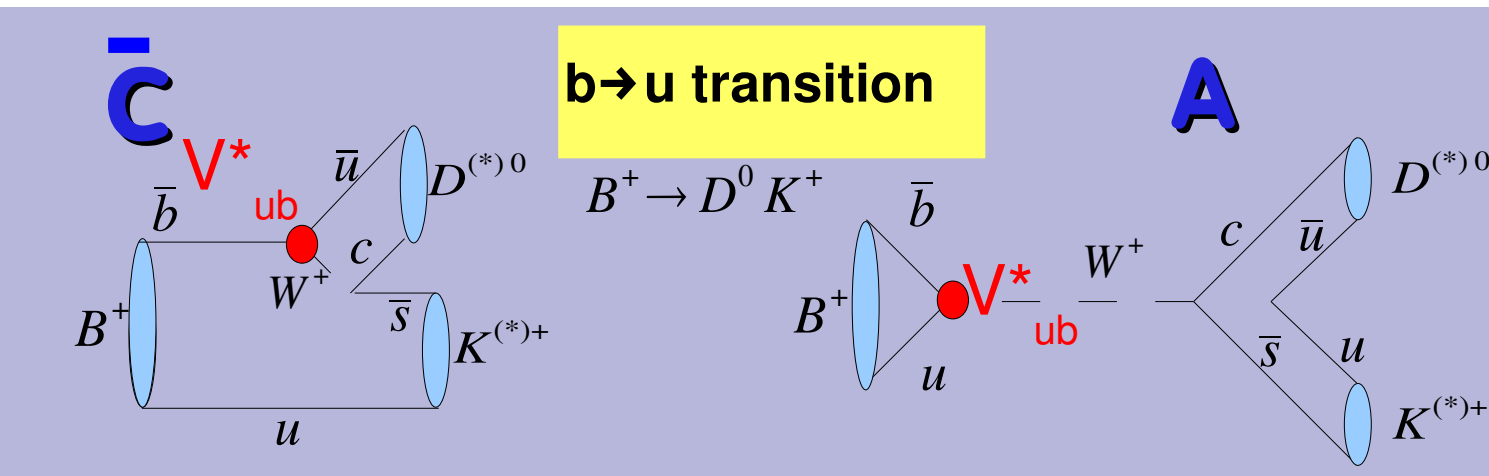
γ weak phase between $b \rightarrow c$ and $b \rightarrow u$ transition



T = tree

C = colour-suppressed

A = annihilation



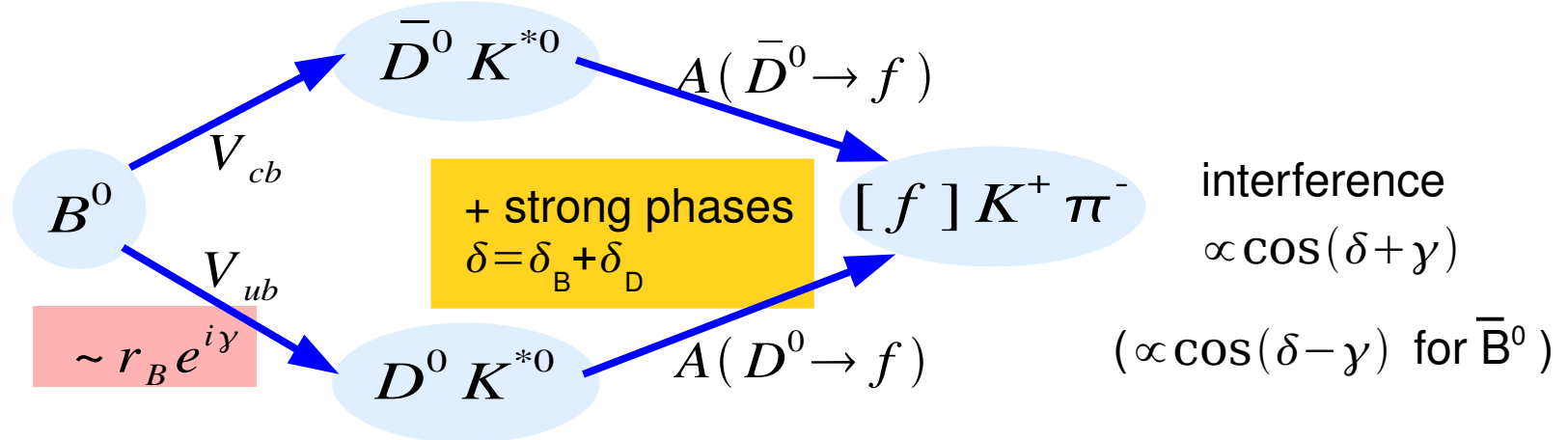
$|C|/|T| \sim 0.3$

$|A|/|C| \sim 0.2$

Interference scheme

CP violation detectable when there are two paths to reach the same final state.
 Interference in the $B \rightarrow DK$ system allows the determination of γ

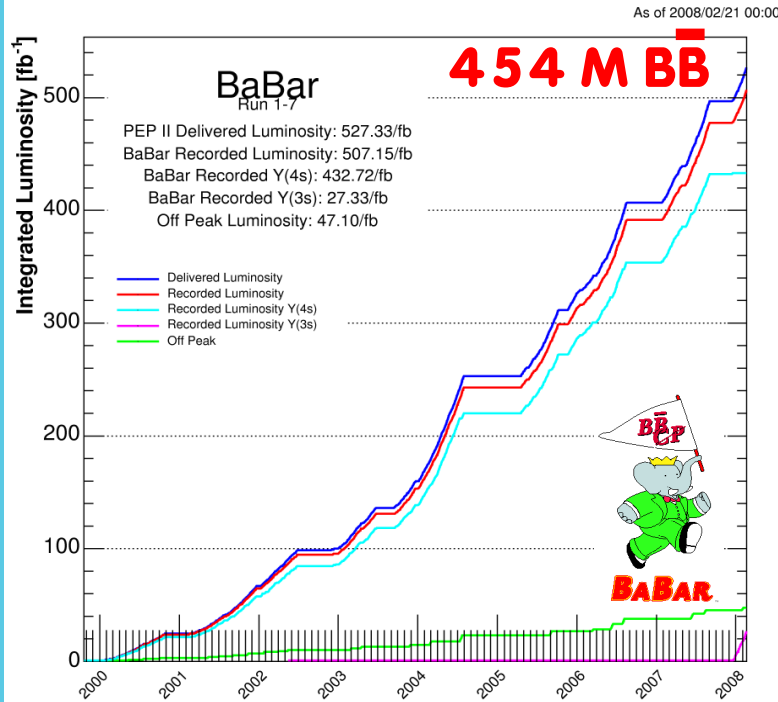
$$|A_1 + A_2 e^{i\phi}|^2 = A_1^2 + A_2^2 + 2A_1 A_2 \cos(\phi)$$



Main characters: γ , r_B , δ

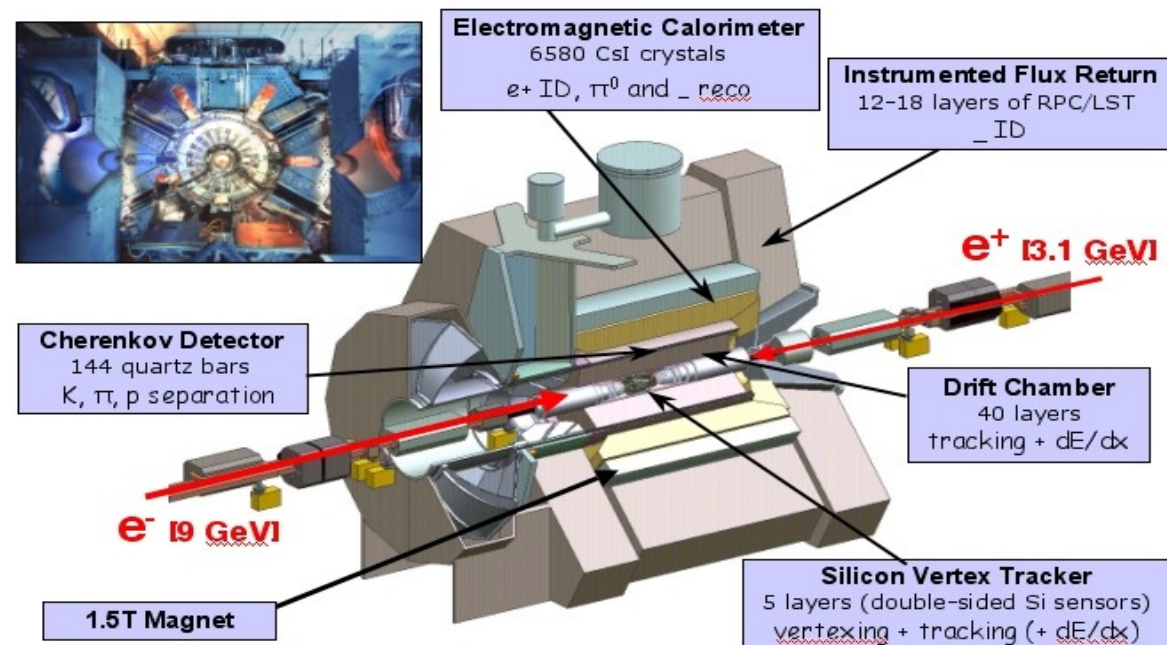
Sensitivity to γ is driven by the ratio $r_B = |A(\mathbf{b} \rightarrow \mathbf{u})|/|A(\mathbf{b} \rightarrow \mathbf{c})|$ (channel-dependent).

PEP II and BABAR



PEP II at SLAC (U.S.A.) e^+e^- collider with asymmetric beam energies @Y(4s) for B meson pairs production.

General purpose detector **Babar**



Different methods

Different methods proposed to study the $B \rightarrow D^0 K$ decays,

- **GLW method:**

D^0 mesons reconstructed in two-body CP-eigenstate final states: K^+K^- , $\pi^+\pi^-$ (CP even) $K_s \pi^0$, $K_s \omega$ (CP odd)

- **ADS method:**

D^0 mesons reconstructed in non CP-eigenstate final states: $K^-\pi^+$, $K^-\pi^+\pi^0$

- **GGSZ (Dalitz) method:**

D^0 mesons reconstructed in three-body CP-eigenstate final states: $K_s \pi^+\pi^-$, $K_s K^+K^-$, $\pi^+\pi^-\pi^0$

more sensitive to r_B

the one that gives the best error on γ

All methods used by Babar and Belle.

Best determination from Dalitz analyses: error on $\gamma \sim 20^\circ$ - 25°

Time dependent Dalitz plot analysis of $B \rightarrow D^{\mp} K^0 \pi^{\pm}$, resonance model

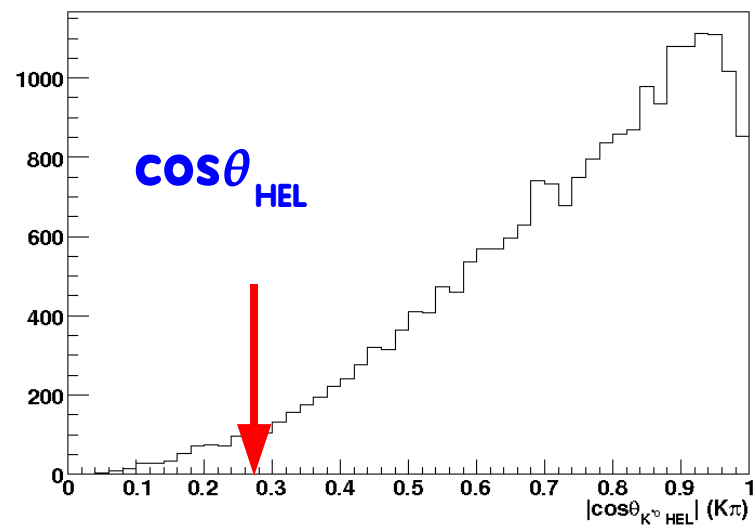
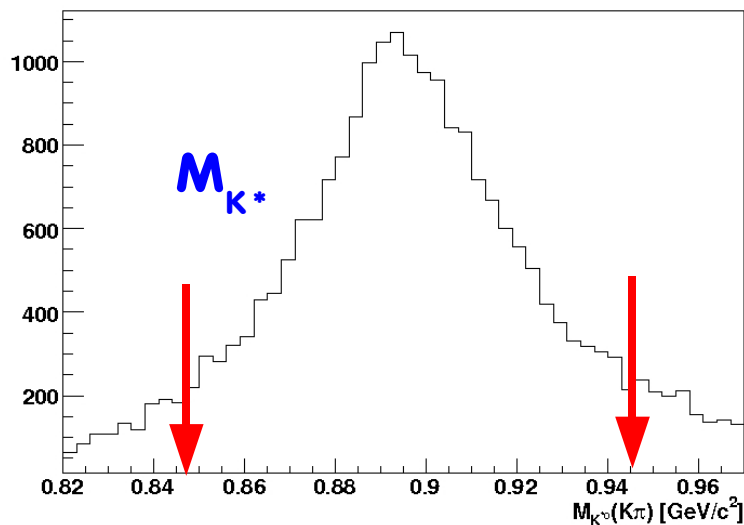
Isobar model

	<i>Mass</i> (GeV/c ²)	<i>Width</i> (GeV/c ²)	<i>J^P</i>	<i>a(V_{cb})</i>	<i>ϕ(V_{cb})^o</i>	<i>a(V_{ub})</i>	<i>ϕ(V_{ub})^o</i>
D_{s2}(2573)[±]	2.572	0.015	2+	-	-	0.02	
D₂[*](2460)⁰	2.461	0.046	2+	0.12	30	0.048	30
D₀(2308)⁰	2.308	0.276	0+	0.12	70	0.048	90
K[*](892)[±]	0.89166	0.0508	1-	1	0	-	-
K₀[*](1430)[±]	1.412	0.294	0+	0.6	80	-	-
K₂[*](1430)[±]	1.4256	0.0985	2+	0.2	0	-	-
K[*](1680)[±]	1.717	0.322	1-	0.3	30	-	-
“Non Resonant”	-	-	-	0.07	0	0.028	30

$B^0 \rightarrow D^0 K^{*0} [K^+ \pi^-]$: cuts on K^{*0}

The selection of the K^* is common to the ADS and Dalitz analyses

Cuts optimized maximizing the statistical significance $S / \sqrt{(S+B)}$



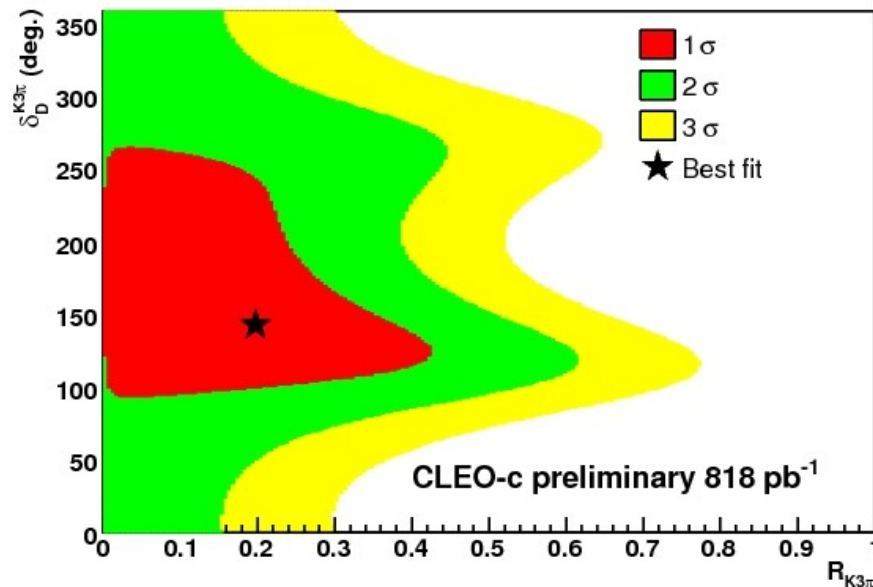
Distributions for signal

Inputs from CLEO-c

As shown in: [arXiv:0805.1722 \[hep-ex\]](https://arxiv.org/abs/0805.1722)

News from CLEO-c:

- strong phase measured for $K^+\pi^-$, $\delta = (22+14-16)^\circ$
- D Dalitz variables measured for $K^+\pi^- \pi^+ \pi^-$
- analysis ongoing for $K^+\pi^- \pi^0$



The factor $R_{K3\pi} = k_D$ is significantly smaller than 1, as it is reasonable since we do not cut on Dalitz plane.