

# Summary WG 2 - Theory

Matthias Neubert

Johannes Gutenberg University Mainz

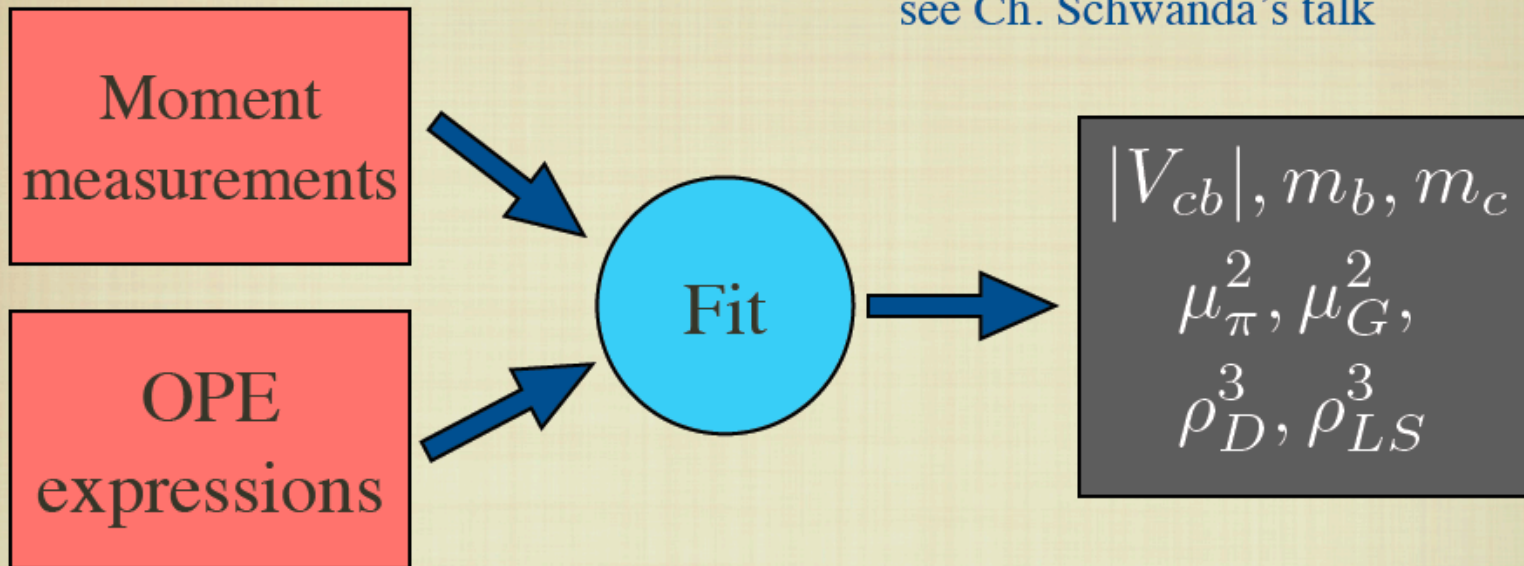
13.9.08

# Presentations

- **Nils Offen:** Form factor determinations from light-cone sum rules
- **Junko Shigemitsu:**  $B \rightarrow \pi$  semileptonic decays - Status report from lattice QCD
- **Thomas Becher:**  $B \rightarrow X_c l \nu$  theory - Status and prospects
- **Jack Laiho:** Determination of  $F(1)$  and  $G(1)$
- **Nazario Tantalo:** Future prospects for LQCD form factor calculations
- **Einan Gardi:** Theoretical review -  $B \rightarrow X_s \gamma$  spectrum and moments
- **Paolo Gambino:** Status and prospects of inclusive  $b \rightarrow u l \nu$  theory
- **Vicent Mateu:** Charm and bottom mass determination from sum rules

# Moment fit & HQ parameters

see Ch. Schwanda's talk



## Fit Results in the Kinetic Scheme

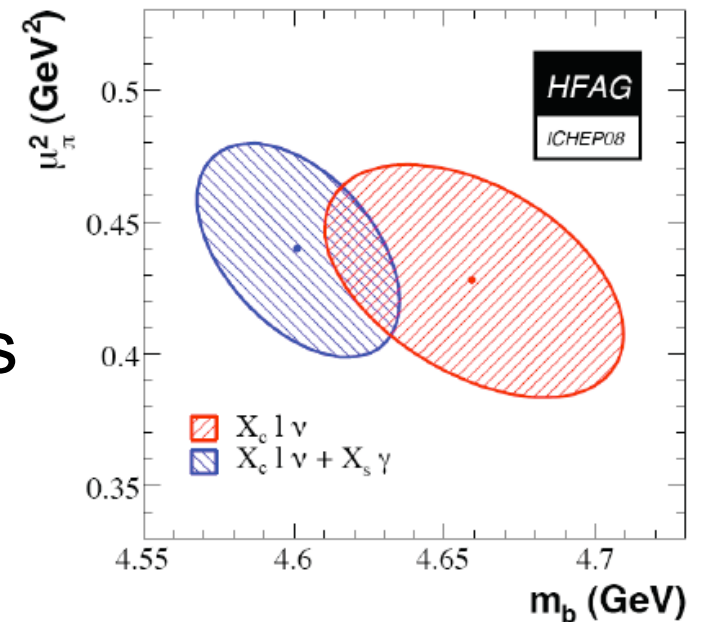
Input	$ V_{cb}  (10^{-3})$	$m_b^{\text{kin}}$ (GeV)	$\mu_\pi^2$ (GeV <sup>2</sup> )		$\chi^2/\text{ndf.}$
all moments ( $X_{c\text{lnu}}$ and $X_{s\text{gamma}}$ )	41.67 +/- 0.43(fit) +/- 0.08( $\tau_B$ ) +/- 0.58(th)	4.601 +/- 0.034	0.440 +/- 0.040	<a href="#">details</a>	29.7 / (64-7)
$X_{c\text{lnu}}$ only	41.48 +/- 0.47(fit) +/- 0.08( $\tau_B$ ) +/- 0.58(th)	4.659 +/- 0.049	0.428 +/- 0.044	<a href="#">details</a>	24.1 / (53-7)

# Moment fit & HQ parameters

- OPE predictions for  $B \rightarrow X_c l \nu$  moments now available (soon ...) including  $O(\alpha_s^2)$  and  $O(\alpha_s/m_b^2)$  corrections, and parametrization of  $O(1/m_b^4)$  effects [Becher]
- Expected to remove important theoretical limitations, could potentially shift  $|V_{cb}|$  and  $m_{b,c}$  values [Schwanda]

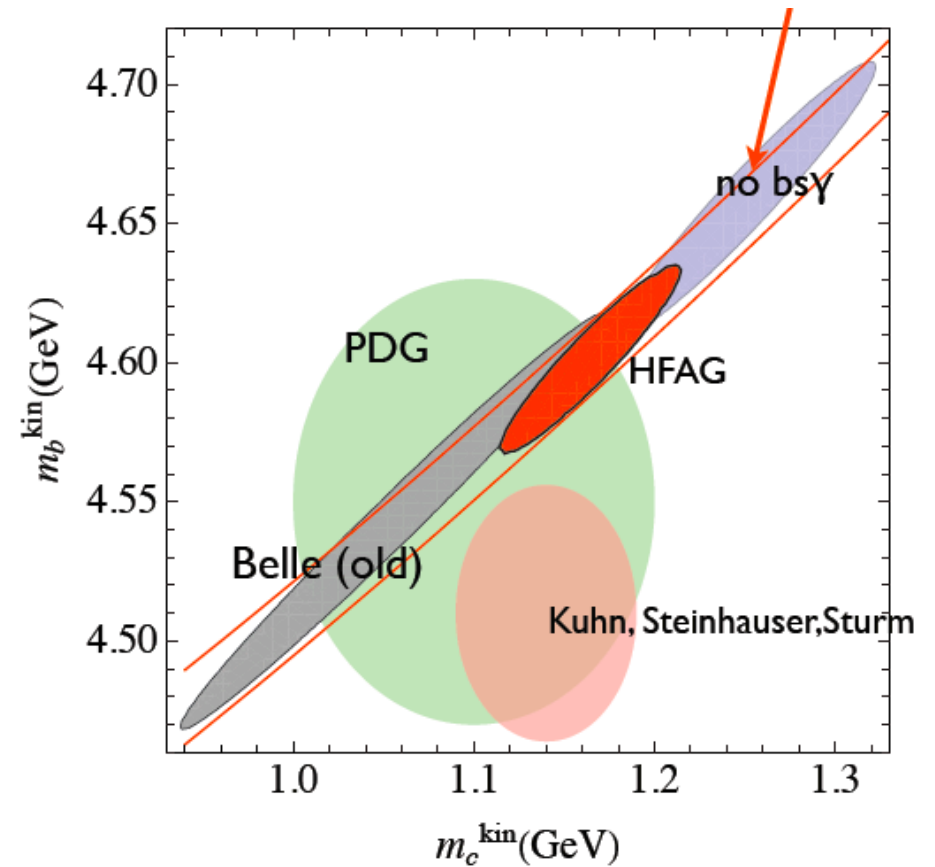
# Moment fit & HQ parameters

- Issues: [Becher, Gardi]
  - quark-hadron duality ( $X_c = D, D^*$  for  $\sim 80\%$  of events  $\rightarrow$  hadronic mass moments?)
  - use of  $B \rightarrow X_s \gamma$  moments introduces uncontrolled systematics due to shape function ( $E_0 = 1.8 - 2.0$  GeV) and non-OPE contributions [Lee, MN, Paz (in prep.)]



# Moment fit & HQ parameters

- Use of  $B \rightarrow X_s \gamma$  moments driven by desire to break  $m_{b,c}$  degeneracy and lower  $m_b$  to “reasonable” values
- Perhaps better to use independent determinations of  $m_{b,c}$  instead



[Gambino]

# Moment fit & HQ parameters

- Heavy-quark masses extracted from  $e^+e^-$  sum rules promising (many-loop results exist)
- Preliminary results (using contour-improved perturbation theory):

$$m_c = 1.283 \pm 0.040_{\text{exp}} \pm 0.016_{\mu} \pm 0.014_{\text{method}} \pm 0.001_n$$

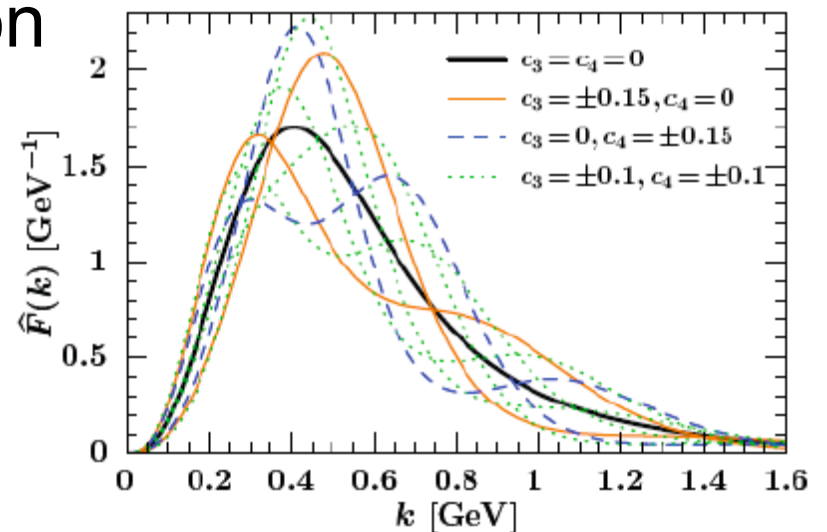
$$m_b = 4.153 \pm 0.003_{\mu} \pm 0.009_{\text{method}} \pm 0.016_n \quad [\text{Matteu}]$$

- very competitive errors
- more conservative than previous analysis by Kühn et al. (?)

# Inclusive $|V_{ub}|$

- Much recent progress in theory: [\[Gambino\]](#)
  - $O(\beta_0\alpha_s^2)$  corrections to spectra calculated
  - $O(\alpha_s^2)$  corrections in shape-function region calculated [\[Asatryan, Greub, MN, Pecjak \(in prep.\)\]](#)
  - Flexible parametrization of shape functions investigated

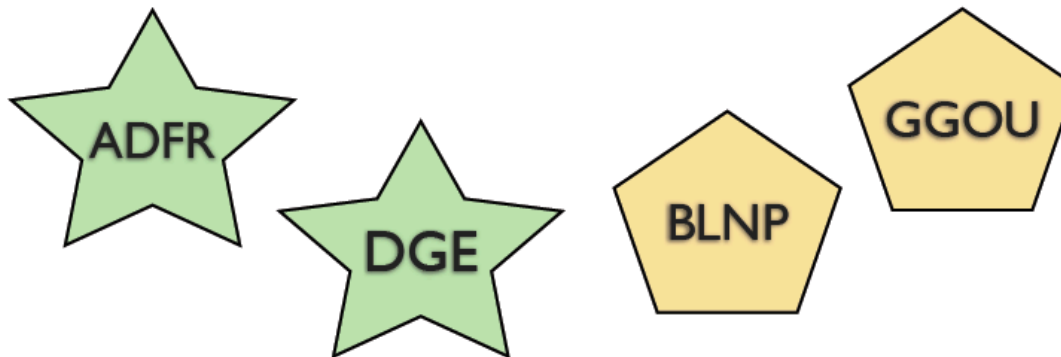
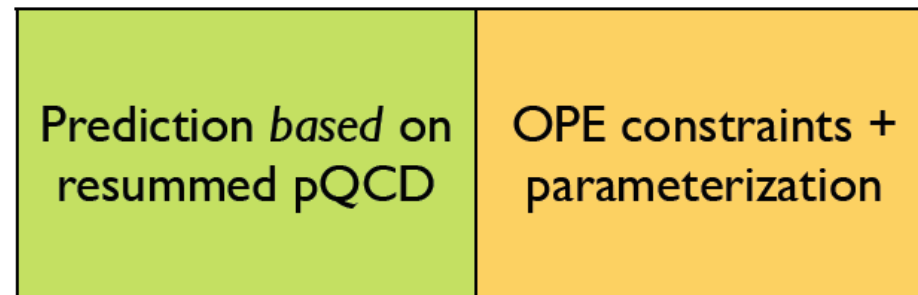
[\[Ligeti et al.\]](#)





# Inclusive $|V_{ub}|$

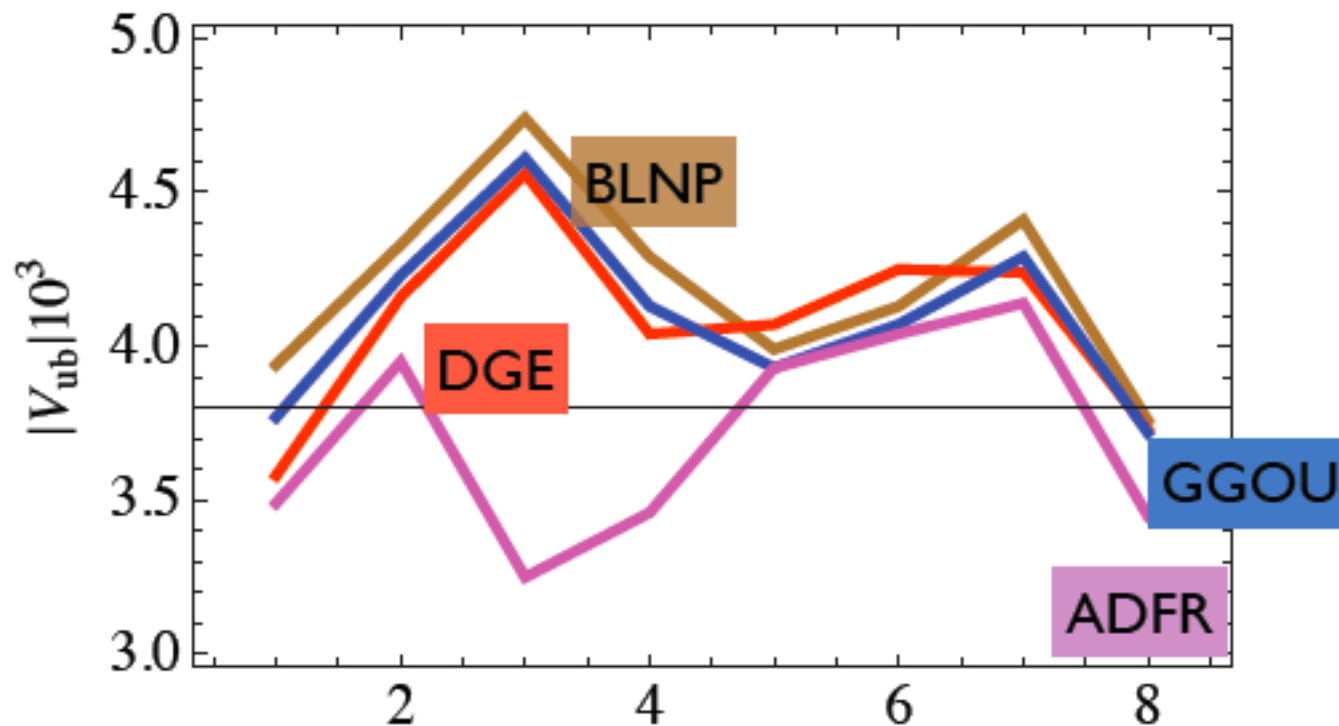
- Detailed comparisons of different methods being performed



# Inclusive $|V_{ub}|$

- Detailed comparisons of different methods being performed

[Gambino]



# Inclusive $|V_{ub}|$

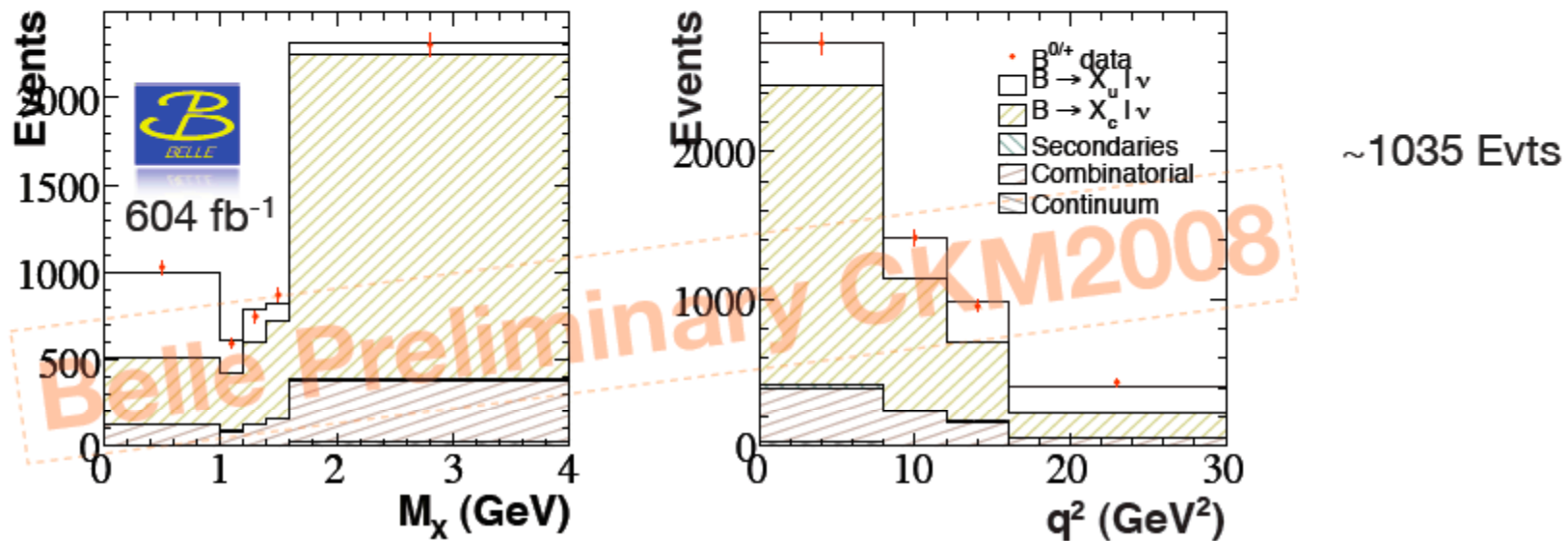
- Overall quite good consistency
- Some issues remain (*weak annihilation!*)
- Not all approaches of equal rigor (inclusion of subleading shape functions, consistency with OPE, systematic error estimates, ...)
- When stakes are high ( $|V_{ub}|$ ), only systematic approaches (BLNP, GGOU, DGE) should be used

# Inclusive $|V_{ub}|$

- More inclusive measurements (less restrictive cuts) reduce theory uncertainties and  $m_b$  dependence

Recent Belle measurement of uncut  $B \rightarrow X_u l \nu$  rate (only requires  $E_l > 1$  GeV) goes a long way and validates large  $|V_{ub}|$  values!

# Belle Multivariate analysis (NEW @ CKM2008) 2/2



2D fit in  $q^2$   $m_x$ . (projections shown)

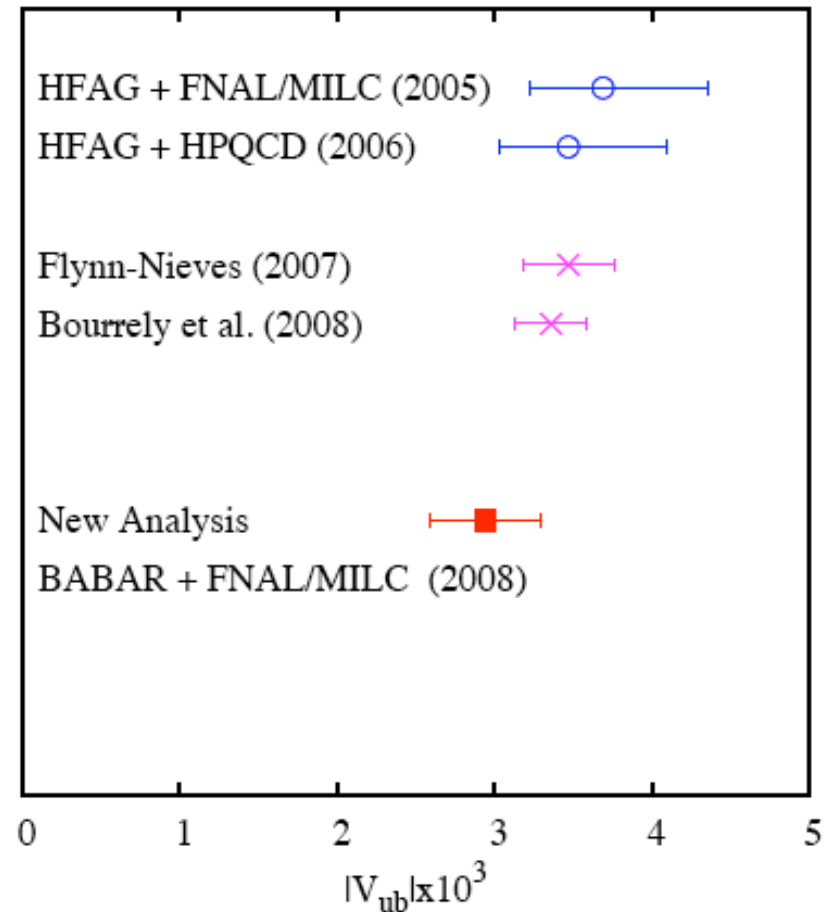
Kinematic Region	$B(B \rightarrow X_{u/l} \nu) \times 10^{-3}$	$m_b$	$ V_{ub}  (10^{-3})$ % error	Theory
	$\Delta$ (stat. sys.)			
$P_{lepton} > 1.0$ GeV	$1.96 \times (1 \pm 0.088 \pm 0.076)$	(kinetic) 4.613 GeV, $m_{\pi l} = 0.440 \text{ GeV}^2$	4.42 ( $\pm 3.1 \pm 5.1$ )	GGOU (thanks P. Giordano)
		(MSbar) 4.243 GeV	4.47 ( $\pm 6.7$ )	DGE (thanks E. Gardi)

$\sim 90^+$  % total phase space, thus theory error less correlated to other  $V_{ub}$  determinations

$\sim$  same for BLNP [Urquijo]

# Exclusive $|V_{ub}|$

- Lattice QCD predicts  $B \rightarrow \pi$  form factor
- Recent improvements in analysis method (chiral and continuum extrapolations, simultaneous fits to lattice and experiment (+LCSR))
- Significant statistical and fitting errors remain
- Unquenched results based on staggered fermions, results using other actions needed for validation



[Shigemitsu]

# Exclusive $|V_{ub}|$

- Light-cone sum rules provide alternative to lattice QCD, but method is “inherently approximate”
- No systematic error analysis (10% ?)

comparison of exclusive determinations		
Method	$ V_{ub}  \times 10^{-3}$	Ref.
Lattice-QCD	$3.78 \pm 0.25 \pm 0.52$	Fermilab/MILC '05
Lattice-QCD	$3.55 \pm 0.25 \pm 0.50$	HPQCD '07
Omnes-FF	$3.47 \pm 0.29 \pm 0.03$	Flynn, Nieves '07
BCL-FF	$3.36 \pm 0.23 \pm 0.01$	Bourenly et al. 08
LCSR	$3.5 \pm 0.4 \pm 0.1$	Ball '06
<b>LCSR</b>	<b><math>3.5 \pm 0.4 \pm 0.2 \pm 0.1</math></b>	Duplančić et al. 08

[Offen]

# The $|V_{ub}|$ Crisis

$$|V_{ub}|_{\text{incl}} \sim (4.0 - 4.5) \cdot 10^{-3}$$

$$|V_{ub}|_{\text{excl}} \sim (3.0 - 3.5) \cdot 10^{-3}$$

may stay with us for a long time ...



# Inclusive $|V_{cb}|$

- $|V_{cb}|$  is output of global moment fit
- Present value might be reduced when theoretical improvements (higher-order corrections) will have been included

	$ V_{cb}  (10^{-3})$	$m_b$ (GeV)	$\mu_{\pi}^2$ (GeV <sup>2</sup> )	$\chi^2/\text{ndf}$
default	41.67 $\pm$ 0.43(fit) $\pm$ 0.08( $\tau_B$ ) $\pm$ 0.58(th)	4.601 $\pm$ 0.034	0.440 $\pm$ 0.040	29.7/57
new	40.85 $\pm$ 0.68(fit) $\pm$ 0.08( $\tau_B$ ) $\pm$ 0.57(th)	4.605 $\pm$ 0.031	0.312 $\pm$ 0.060	54.2/57

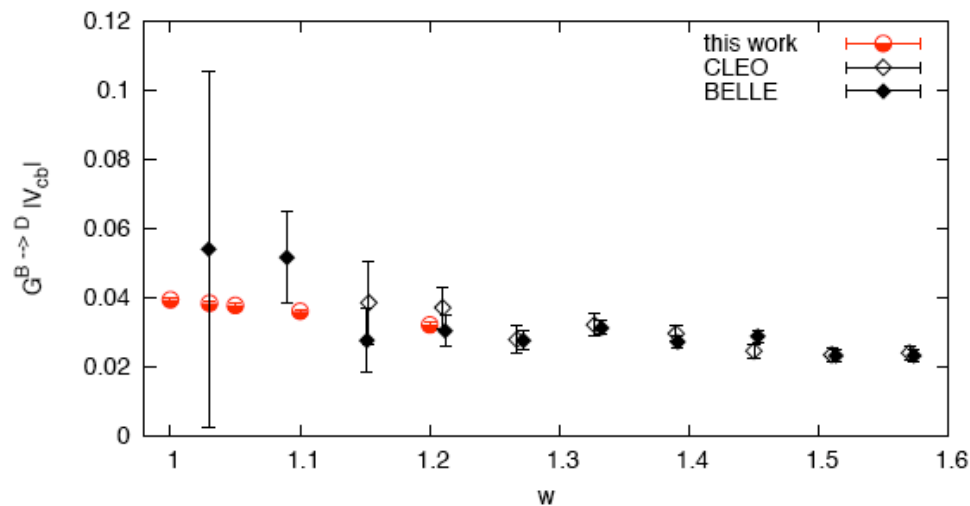
(rough estimate of “theory correlations”)

[Schwanda]

# Exclusive $|V_{cb}|$

- Lattice QCD results in good shape [Laiho]
- New results based on  $B \rightarrow D \ell \nu$  BaBar analysis encouraging

de Divitiis, et al, arXiv:0707.0582



[Tantalo]

New result using a step-scaling method. ← a big advance (?)

# Exclusive $|V_{cb}|$

- New unquenched result for  $B \rightarrow D^* l \nu$ :

$$h_{A_1}(1) = 0.921(13)(20) \quad \text{Fermilab/MILC}$$

$$|V_{cb}| = (38.7 \pm 0.9_{exp} \pm 1.0_{theo}) \times 10^{-3} \quad \text{[Laiho]}$$

- Somewhat larger value obtained from  $B \rightarrow D l \nu$

# The $|V_{cb}|$ Situation

Prospects for a consistent value of  $|V_{cb}|$  from both inclusive and exclusive methods

(if we're lucky ...)