

Searching for new physics with rare kaon decays

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- Outline

I- New Physics in flavor transitions

II- Pattern of deviations in rare K decays

Conclusion

New Physics in flavor transitions

A. The New Physics flavor puzzle

- Most New Physics (NP) models have either *new flavored particles*, or *new flavor-breaking interactions* between quarks and leptons.
- At the same time, there is *no signal of NP in flavor experiments*.

↳ Experiments \sim SM predictions

↳ $\left\{ \begin{array}{l} b \rightarrow s: \\ |V_{tb}^* V_{ts}| \sim \lambda^2 \end{array} \right. \quad \left\{ \begin{array}{l} b \rightarrow d: \\ |V_{tb}^* V_{td}| \sim \lambda^3 \end{array} \right.$

$$\left\{ \begin{array}{l} s \rightarrow d: \\ |V_{ts}^* V_{td}| \sim \lambda^5 \end{array} \right.$$

- New Physics cannot be *both light and generic*:

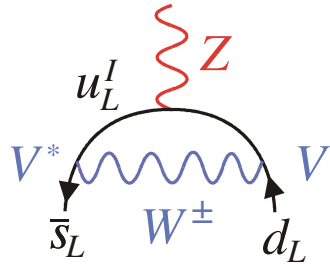
$$\mathcal{L}_{eff} = \frac{c_{bs}}{\Lambda^2} (\bar{b}\Gamma s)(\bar{\nu}\Gamma \nu) + \frac{c_{bd}}{\Lambda^2} (\bar{b}\Gamma d)(\bar{\nu}\Gamma \nu) + \frac{c_{sd}}{\Lambda^2} (\bar{s}\Gamma d)(\bar{\nu}\Gamma \nu) + \dots$$

Most constraining!

- $c_{sd} \approx 1, \Lambda \gtrsim 75 \text{ TeV}$: NP very massive, beyond the reach of LHC,
- $\Lambda \approx 1 \text{ TeV}, c_{sd} \lesssim V_{ts}^* V_{td}$: NP flavor structures highly non-generic.

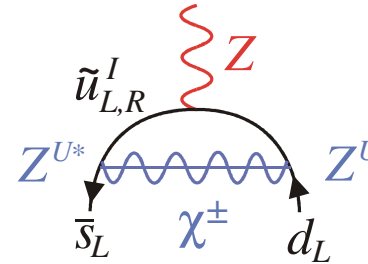
B. Application to the MSSM

Squarks are new flavored particles, not aligned with quarks:



CKM = small mismatch between quark mass and gauge eigenstates.

?



Large mass and gauge eigenstate mismatch for squarks?

Squarks must be quasi parallel to quarks (e.g., $Z^U \approx V_{CKM}$).

Minimal Flavor Violation: $c_{qq'} \sim V_{tq}^* V_{tq'}$

Systematic symmetry principle allowing to parametrize all NP flavor-breaking in terms of the SM Yukawa couplings.

Hall, Randall '90/D'Ambrosio et al. '02

C. SUSY implementations of Minimal Flavor Violation

Hall, Randall '90
 D'Ambrosio et al. '02
 Colangelo, Nikolidakis, CS '08

1- Electroweak-scale MFV

- Squark soft SUSY-breaking terms fixed in terms of the Yukawa couplings.
- Allows for several new CP-violating phases, beside the CKM one.

$$\begin{aligned}
 & \text{Im}(\delta_{LL}^{23,13}) \neq 0 ! \\
 \mathbf{m}_Q^2 &= m_0^2 (a_1 \mathbf{1} + b_1 \mathbf{Y}_u^\dagger \mathbf{Y}_u + b_2 \mathbf{Y}_d^\dagger \mathbf{Y}_d + c_1 \mathbf{Y}_u^\dagger \mathbf{Y}_u \mathbf{Y}_d^\dagger \mathbf{Y}_d + c_1^* \mathbf{Y}_d^\dagger \mathbf{Y}_d \mathbf{Y}_u^\dagger \mathbf{Y}_u) \\
 \mathbf{A}_u &= A_0 \mathbf{Y}_u (a_2 \mathbf{1} + b_3 \mathbf{Y}_u^\dagger \mathbf{Y}_u + b_4 \mathbf{Y}_d^\dagger \mathbf{Y}_d + c_2 \mathbf{Y}_u^\dagger \mathbf{Y}_u \mathbf{Y}_d^\dagger \mathbf{Y}_d + c_3 \mathbf{Y}_d^\dagger \mathbf{Y}_d \mathbf{Y}_u^\dagger \mathbf{Y}_u) \\
 & \text{Im}(\delta_{RL}) \neq 0 !
 \end{aligned}$$

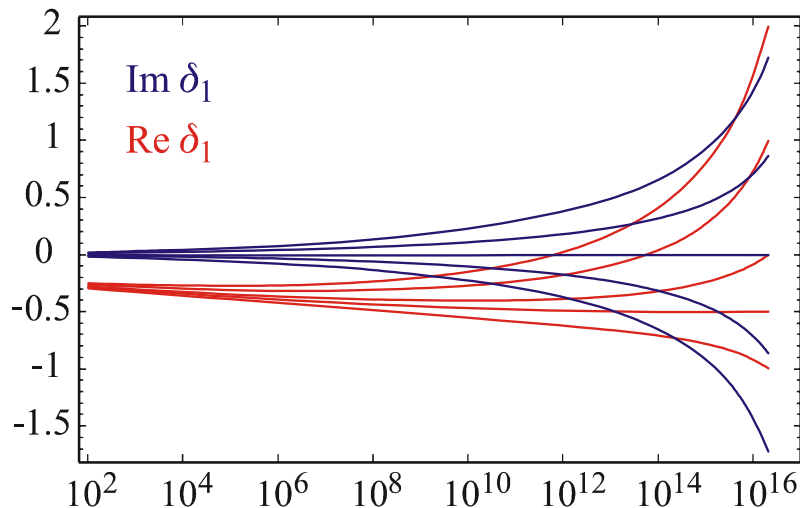
For K physics:

- Small impact on ϵ_K since δ_{LL}^{12} does not feel the new phase (note $\delta_{LL}^{23} \sim \delta_{LL}^{13}$).
- Double LR mass-insertion, relevant for rare K, stays essentially real:

$$(\delta_{RL}^U)_{32}^* (\delta_{RL}^U)_{31} \sim m_t^2 V_{ts}^* V_{td} |A_0 a_2^* - \cot \beta \mu|^2 .$$

2- Running down GUT-scale MFV

- “Running *infrared fixed points*” \leftrightarrow predictions for all *mass-insertions*.
(essentially: the mSUGRA-like a_i , running as the gluino mass, dominates)
- All seven new *CP-violating phases* run towards zero (in the squark sector).

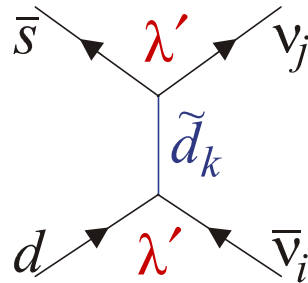


$$\delta_1 \equiv \frac{(\delta_{RL}^U)^{32}}{V_{ts}} = \frac{(\delta_{RL}^U)^{31}}{V_{td}}$$

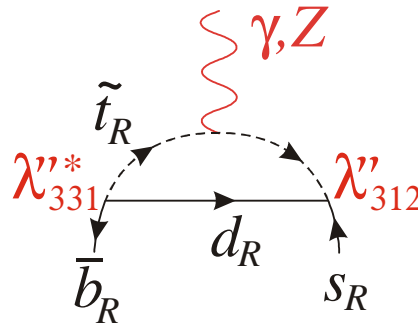
(similar for other mass-insertions)

- *Running up* from MFV at the electroweak scale, starting away from the fixed points does not lead to MFV at the GUT scale.

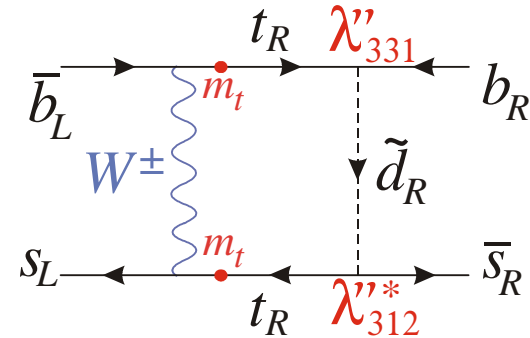
3- Electroweak-scale MFV without R-parity



Grossman, Isidori, Murayama '03,
Deandrea, Welzel, Oertel '04, ...



Chakraverty, Choudhury '01, ...



Barbieri, Masiero '86,
Slavich '00, ...

- Surprisingly, *MFV alone is sufficient to pass all proton decay bounds.*
- All *lepton-violating couplings are tiny*, proportional to neutrino masses.
- Strong *hierarchy of baryon-violating couplings* suppresses their contributions

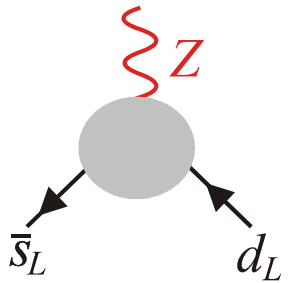
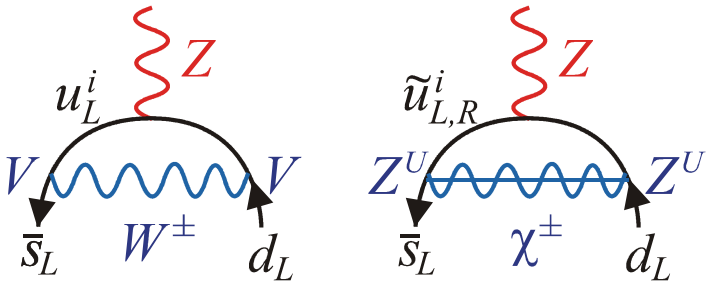
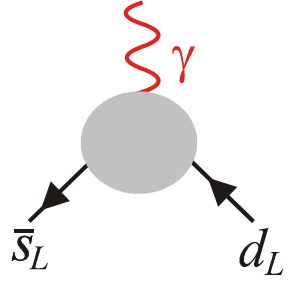
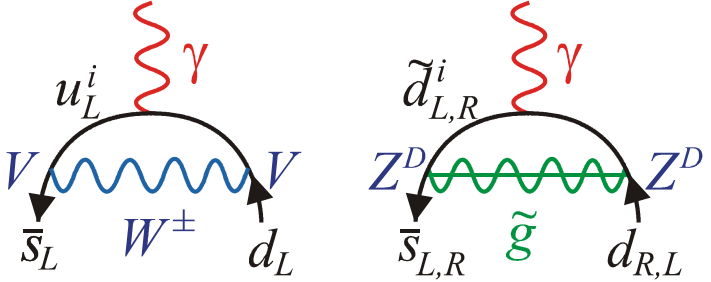
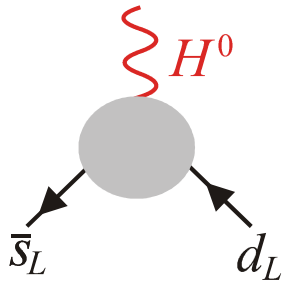
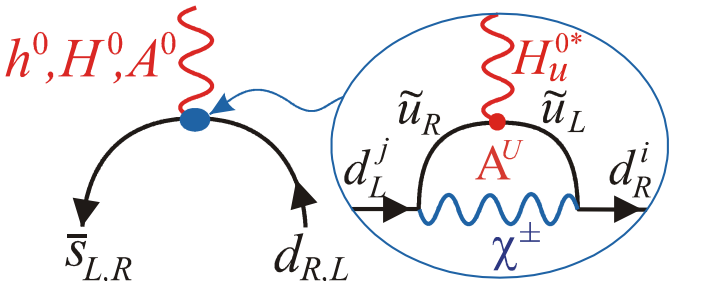
$$b \rightarrow s : |\lambda''_{312} \lambda''^*_{331}| < 10^{-3}, \quad b \rightarrow d : |\lambda''_{312} \lambda''^*_{323}| < 10^{-5}, \quad s \rightarrow d : |\lambda''_{313} \lambda''^*_{323}| < 10^{-8}$$

$$b \rightarrow s : |V_{tb}^* V_{ts}| \sim 10^{-2}, \quad b \rightarrow d : |V_{tb}^* V_{td}| \sim 10^{-3}, \quad s \rightarrow d : |V_{ts}^* V_{td}| \sim 10^{-4}$$

⇒ at most a few % of the SM contributions.

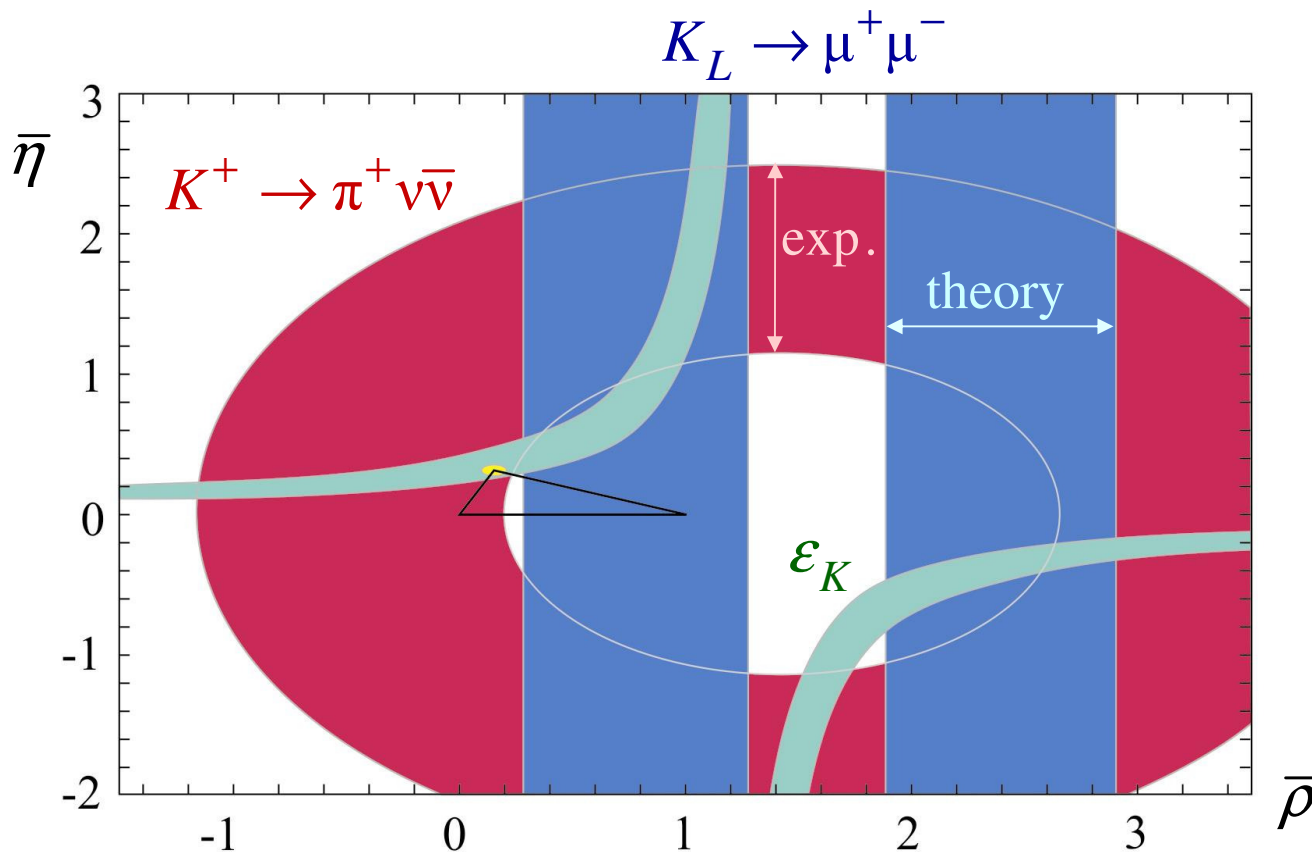
Patterns of deviations

A. Probing EW structures with rare K decays

| EW Penguin | SM and/or example of SUSY diagram | Contributes to |
|--|---|---|
|  |  | $K \rightarrow \pi \nu \bar{\nu}$ $K_L \rightarrow \pi^0 \ell^+ \ell^-$ $K_L \rightarrow \ell^+ \ell^-$ |
|  |  | $K_L \rightarrow \pi^0 \ell^+ \ell^-$ |
|  |  | $K_L \rightarrow \pi^0 \mu^+ \mu^-$ $K_L \rightarrow \mu^+ \mu^-$ (helicity-suppressed) |

New Physics to be identified by looking at patterns of deviations!

B. Where do we stand?



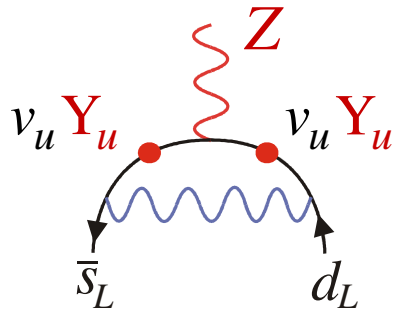
$$K_L \rightarrow \pi^0 \nu \bar{\nu} : \bar{\eta} < 17$$

$$K_L \rightarrow \pi^0 e^+ e^- : \bar{\eta} < 3.3$$

$$K_L \rightarrow \pi^0 \mu^+ \mu^- : \bar{\eta} < 5.4$$

- For $K_L \rightarrow \mu^+ \mu^-$: large error due to $K_L \rightarrow \gamma\gamma \rightarrow \mu^+ \mu^-$, only upper bound for the contribution corresponding to the range 1 - 3 GeV. *Isidori, Unterdorfer '04*
- Interference SD-LD fixed from the Q_1 operator evolution, to be confirmed experimentally with $K^+ \rightarrow \pi^+ \gamma\gamma$ and/or $K_S \rightarrow \pi^0 \gamma\gamma$. *Gerard, Trine, C.S '05*

C. The Z penguin (and its associated W box)

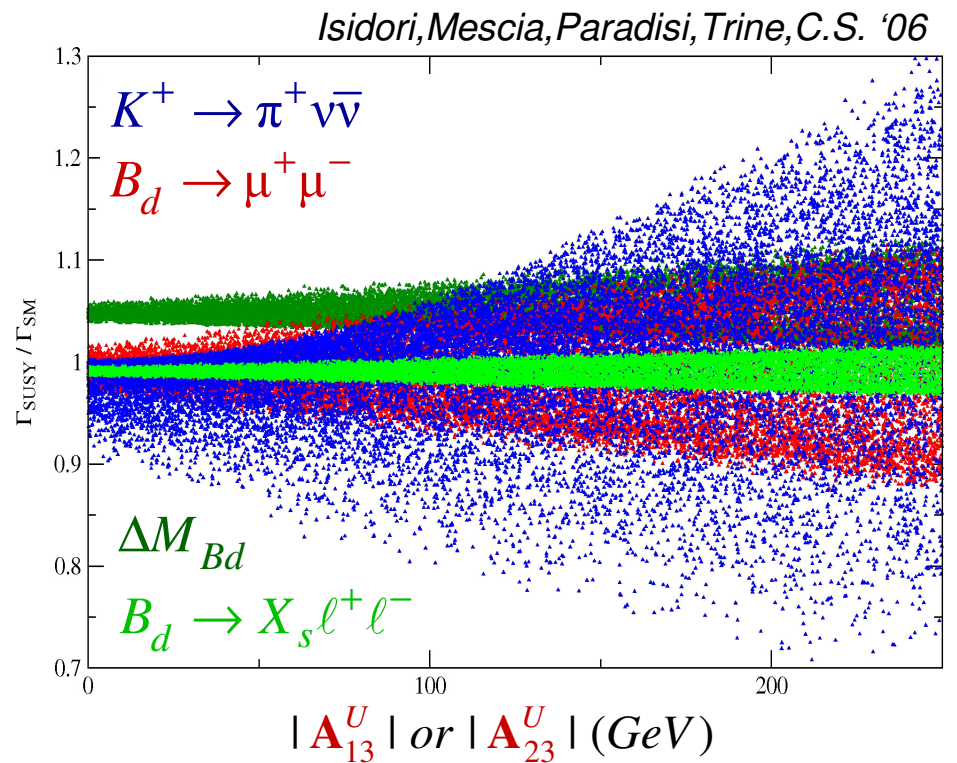
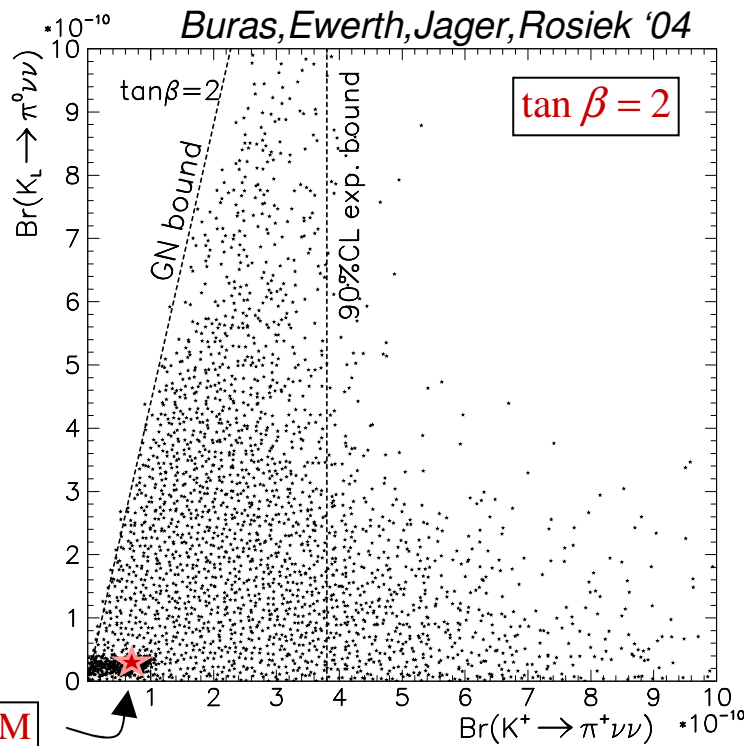


- $SU(2)_L$ breaking: $SM : v_u^2 Y_u^{*32} Y_u^{31} \sim m_t^2 V_{ts}^* V_{td}$

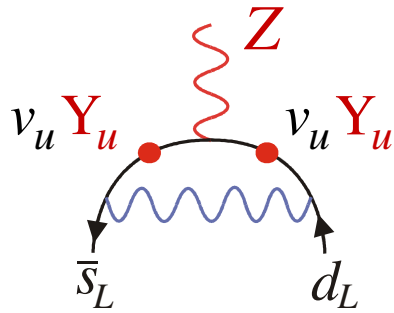
$MSSM : v_u^2 A_{\tilde{u}}^{*32} A_{\tilde{u}}^{31} \sim m_t^2 \times O(1) ?$

$MFV : v_u^2 A_{\tilde{u}}^{*32} A_{\tilde{u}}^{31} \sim m_t^2 V_{ts}^* V_{td} |A_0 a_2^* - \cot \beta \mu|^2.$

- Relatively slow decoupling (w.r.t. boxes or tree).



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- $SU(2)_L$ breaking: $SM : v_u^2 Y_u^{*32} Y_u^{31} \sim m_t^2 V_{ts}^* V_{td}$

$MSSM : v_u^2 A_{\tilde{u}}^{*32} A_{\tilde{u}}^{31} \sim m_t^2 \times O(1) ?$

$MFV : v_u^2 A_{\tilde{u}}^{*32} A_{\tilde{u}}^{31} \sim m_t^2 V_{ts}^* V_{td} |A_0 a_2^* - \cot \beta \mu|^2 .$

- Relatively slow decoupling (w.r.t. boxes or tree).

Most *NP models effects of this type*, or give essentially the same eff. operator:

MSSM moderate $\tan\beta$ (chargino),

Nir, Worah '98, Buras, Romanino, Silvestrini '98

Colangelo, Isidori '98

MSSM large $\tan\beta$ (charged Higgs),

Isidori, Paradisi '06

R-parity violation (non MFV),

Grossman, Isidori, Murayama '03

Deshpande, Ghosh, He '04, Deandrea, Welzel, Oertel '04

EEWP,

Buras, Fleischer, Recksiegel, Schwab '04

Little Higgs,

Rai Choudhury, Gaur, Joshi, McKellar '04

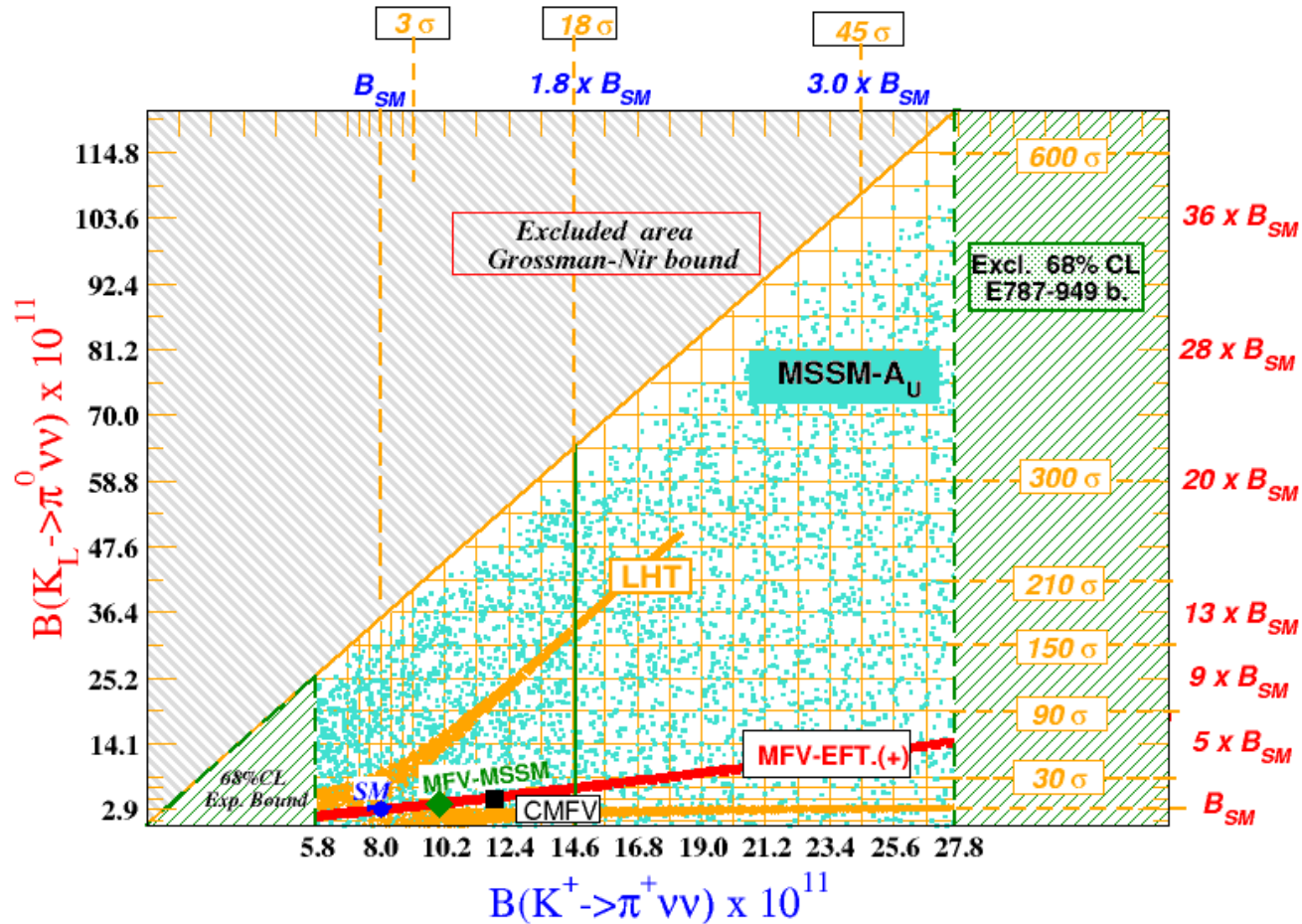
Blanke et al '06, '07

Extra Dimensions,

Buras, Spranger, Weiler '02

...

- $K \rightarrow \pi \nu \bar{\nu}$: best probe, and their correlation tests various possible models



Mescia '06

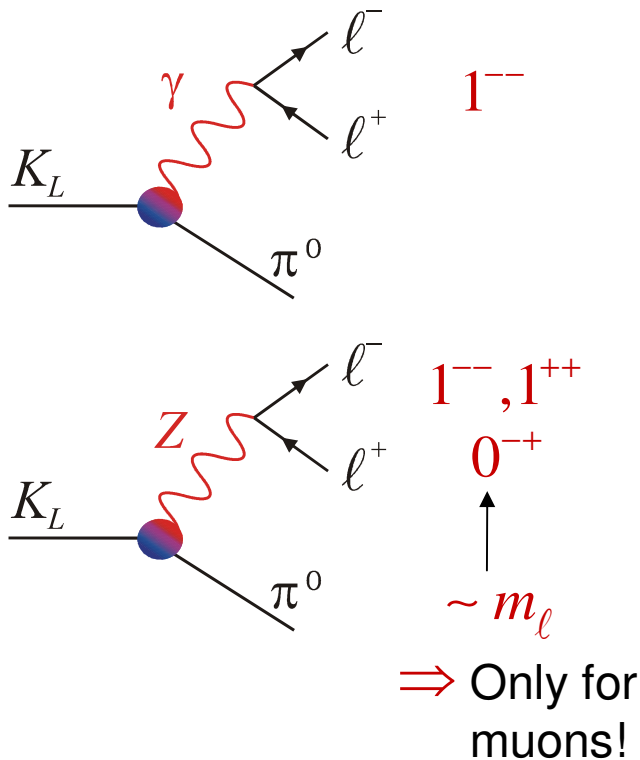
- $K_L \rightarrow \pi^0 \ell^+ \ell^-$: does not bring in any new information here

- $K_L \rightarrow \mu^+ \mu^-$: effect directly correlated to that in $K \rightarrow \pi \nu \bar{\nu}$, but CP-conserving.

With MFV: in general both are simultaneously larger or smaller!

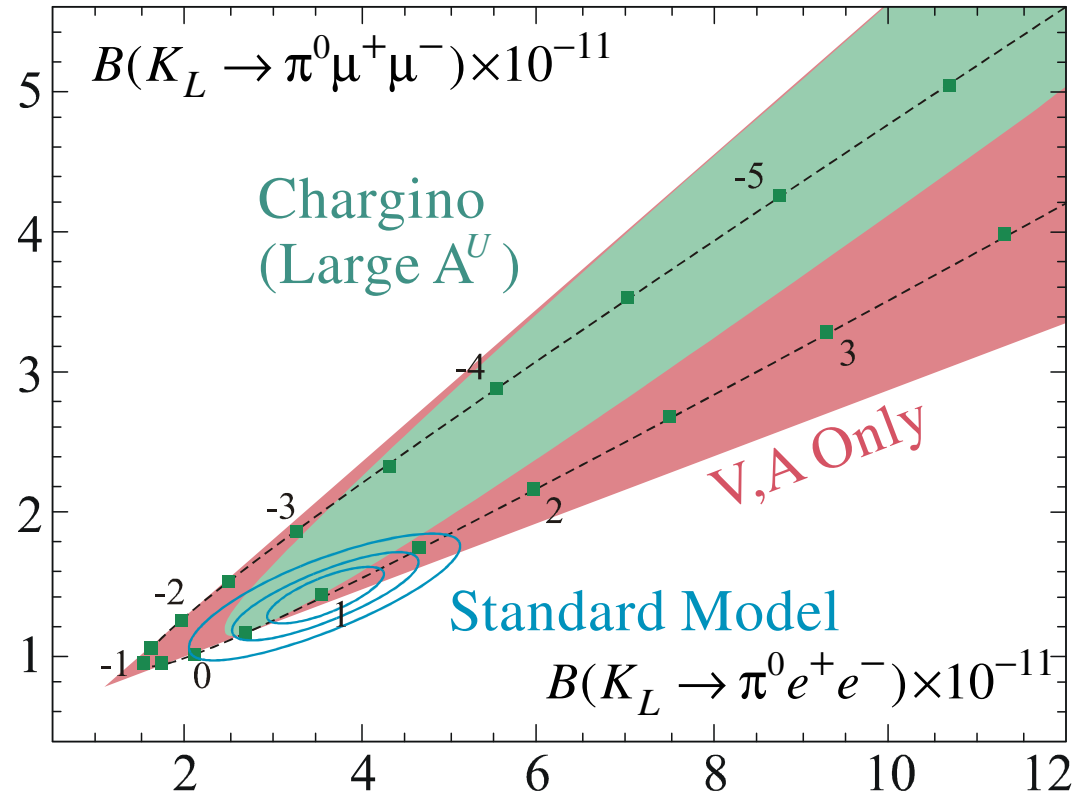
D. Helicity-suppressed New Physics effects

The $K_L \rightarrow \pi^0 \ell^+ \ell^-$ modes permit to isolate the γ penguin:



Specific regions in the plane for specific correlations between γ and Z penguins.

Isidori, Unterdorfer, C.S. '04

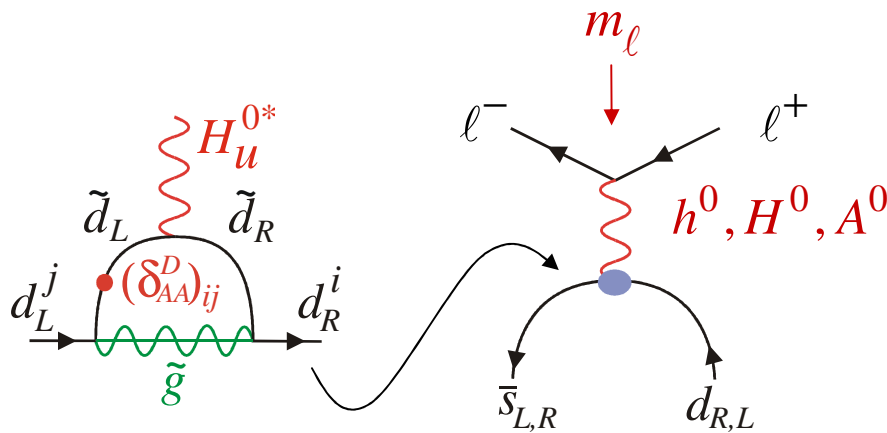


$$\Leftrightarrow 0.1 + 0.24 B_e \leq B_\mu \leq 0.6 + 0.58 B_e$$

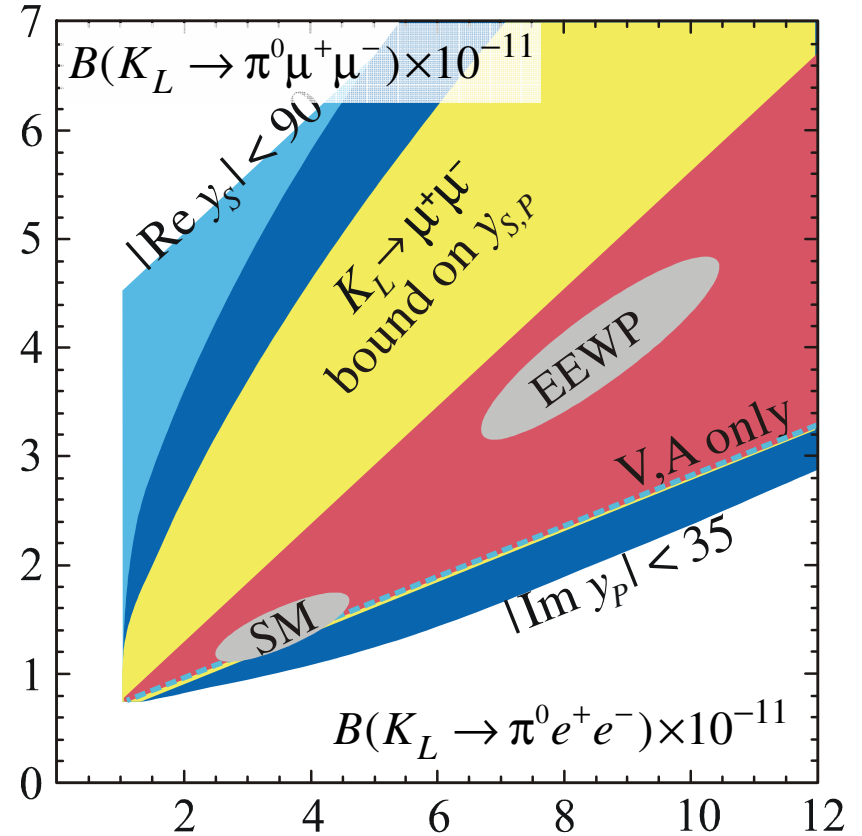
$$\text{with } B_\ell \equiv B(K_L \rightarrow \pi^0 \ell^+ \ell^-) \cdot 10^{11}$$

They also probe a broad class of helicity-suppressed NP effects, as those generated by *neutral Higgs penguins*.

Isidori, Retico '01, '02
Mescia, Trine, CS '06



$$H_{eff} \sim y_S (\bar{s}d)(\bar{l}l) + y_P (\bar{s}d)(\bar{l}\gamma_5 l)$$



Even if directly correlated with $K_L \rightarrow \mu^+ \mu^-$, *large effects still possible*.

E. Looking for the unexpected?

1- $K_L \rightarrow \pi^0 \ell^+ \ell^-$ probe the (pseudo-)scalar and (pseudo-)tensor operators:

$$H_{eff} \sim y_S^{IJ} (\bar{s}d)(\bar{\ell}^I \ell^J) + y_P^{IJ} (\bar{s}d)(\bar{\ell}^I \gamma_5 \ell^J) + y_T (\bar{s} \sigma_{\mu\nu} d)(\bar{\ell} \sigma^{\mu\nu} \ell) + \dots$$

Presumably killed by $K_L \rightarrow ee, e\mu$...but tensors still free.

2- Similar operators for $K \rightarrow \pi \nu \bar{\nu}$ require *active right-handed neutrinos*.

3- Decays into *other invisible state(s)*?

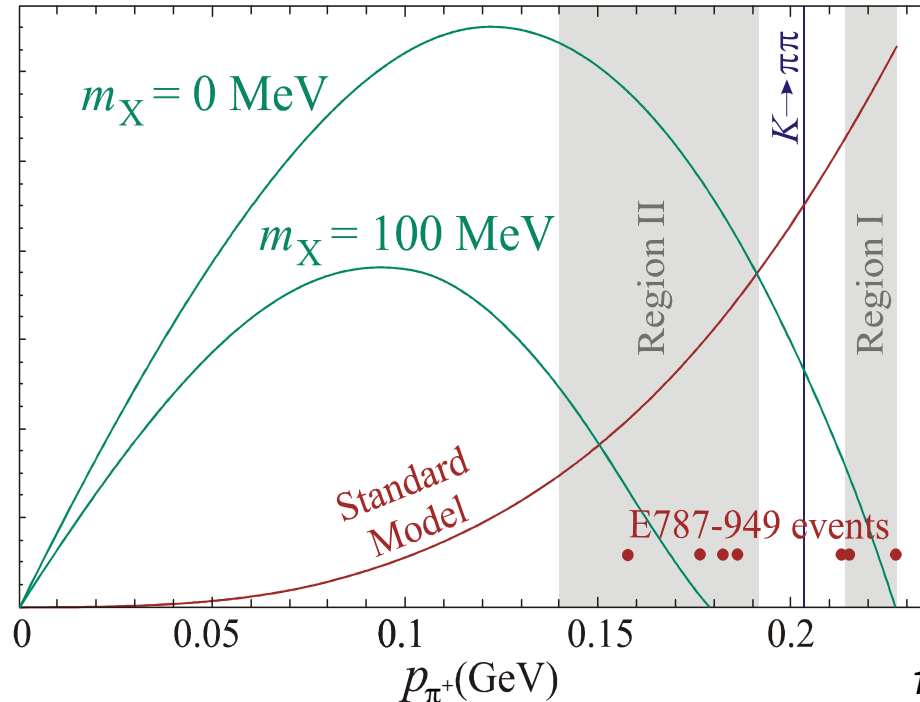
Beware of the kinematics!

- Two-body peak for $K \rightarrow \pi + X$

- Spectrum for $K \rightarrow \pi + X + X$

Depicted for scalar coupling,

$$H_{eff} \sim y_S (\bar{s}d)(\bar{X}X).$$



Conclusion

1- $K \rightarrow \pi\nu\bar{\nu}$ and $K_L \rightarrow \pi^0\ell^+\ell^-$ decays are unique windows into the $s \rightarrow d$ sector.

Essential to constrain (and discriminate among) New Physics models.

2- Still, *do not forget* $K_L \rightarrow \mu^+\mu^-$, the only mode measured with precision.

Further theoretical work would be much welcome on the two-photon contribution.

(or, alternatively, wait for $K_L \rightarrow \pi^0\mu^+\mu^-$, much cleaner and more sensitive)

3- *Message to experimentalists*: Go for the $K \rightarrow \pi\nu\bar{\nu}$ modes, they are the cleanest,

But do not disregard other modes:

$K_L \rightarrow \pi^0\ell^+\ell^-$: Sensitive to a larger class of NP effects

$K_S \rightarrow \pi^0\ell^+\ell^-$, $K_L \rightarrow \pi^0\gamma\gamma$, $K_{\ell 3}$: Theoretical control for rare K decays

$K_S \rightarrow \pi^0\gamma\gamma$, $K^+ \rightarrow \pi^+\gamma\gamma$: Theoretical control over $K_L \rightarrow \mu^+\mu^-$

$K \rightarrow (\pi)e\mu$: Probably too small, but one never knows...

...

Backup

Interference sign fixed from that of $A(K_L \rightarrow \gamma\gamma)$

Gerard, Trine, C.S ('05)

Driven by $Q_1 \rightarrow$ vanishes at LO in SU(3) ChPT.

$$A_{\gamma\gamma} \approx \overbrace{\left(G_8^S + \frac{2}{3}G_{27}^S\right)}^{\sim C_1(\mu_{\text{hadr.}})} (0.46_\pi - 1.83_\eta - 0.12_{\eta'}) \Leftrightarrow B(K_L \rightarrow \gamma\gamma)^{\text{exp}} \Rightarrow G_8^S / G_8 \approx \pm \frac{1}{3}$$

Theoretically, G_8^S estimated from the smooth Q_1, Q_2 non-perturbative evolution

$$(C_1 + C_2)^2 (C_2 - C_1) = 1.0 \pm 0.3 \Rightarrow G_8^S / G_8 = -0.38 \pm 0.12$$

Experimentally, G_8^S could be fixed from either:

