

---

# WGV summary

*$\varphi_3/\gamma$  from tree decays*

A. Bondar

on behalf of conveners and speakers of WGV

1. Unitarity Angle Gamma T.Gershon
2. Gamma from charged B decays at Babar V.Tisserand
3. Belle results for  $\phi_3$  measurements A.Bondar
4. Gamma from neutral B decays at Babar V.Sordini
5. Time-dependent CP asymmetry in  $B^0 \rightarrow D^{*\mp} \pi^\pm$  M.Iwabuchi
6. CLEO\_c Impact on ADS Determination of gamma J.Libby
7. CLEO\_c Impact on gamma from  $B \rightarrow DK$ ,  $D \rightarrow K_S \pi \pi$  J.Rademacker
8. Measuring weak phases using  $B \rightarrow D^* V$  modes R.Sinha
9. Test of flavor SU(3) symmetry and weak phase gamma from  $B \rightarrow K \rho$  C-W.Chang
10. Gamma from UTFIT V.Sordini
11. Gamma from CKM fitter K.Trabelsi
12. Time dependent measurements of gamma at LHCb A.Carbone
13. Gamma at LHCb with ADS/GLW strategies A.Powell
14. Gamma at LHCb: Dalitz fit and global precision G.Wilkinson
15. Prospects for gamma ( $\phi_3$ ) at the SuperKEKB P.Krokovny
16. Prospects for gamma at Super Flavor Factory F.Martinez-Vidal

---

# Importance of $\gamma$

T.Gershon

- $\gamma$  plays a unique role in flavour physics

the only CP violating parameter that can be measured through tree decays (\*)

(\*) more-or-less

- A benchmark Standard Model reference point
  - doubly important after New Physics is observed
- How precise is precise enough?
  - 10% ⊗ At 3 sigma hardly exclude anything
  - 1% ☆ Seems the right level to test NP
  - 0.1% ⊗ Good luck if you can get the funding ...

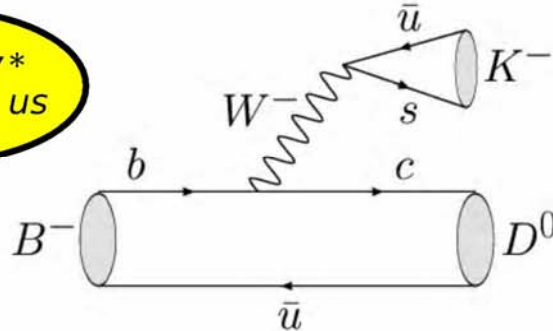
# How To Measure $\gamma$

T.Gershon

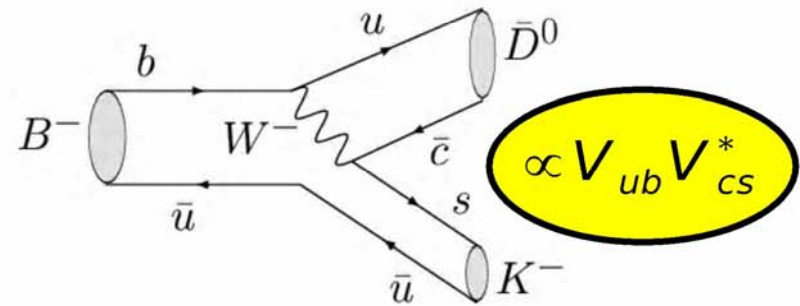
- Focus on theoretically pristine measurement

– Interference between

$\propto V_{cb} V_{us}^*$



- colour allowed
- final state contains  $D^0$



$\propto V_{ub} V_{cs}^*$

- colour suppressed
- final state contains  $\bar{D}^0$

Relative magnitude of suppressed amplitude is  $r_B$

Relative weak phase is  $-\gamma$ , relative strong phase is  $\delta_B$

---

# One Method, Many Modes

T.Gershon

- $B \rightarrow DK$  with any D decay mode that is accessible to both  $D^0$  and  $\bar{D}^0$  is sensitive to  $\gamma$ 
  - M.Gronau & D.Wyler, [PLB 253, 483 \(1991\)](#)
  - M.Gronau & D.London, [PLB 265, 172 \(1991\)](#)
  - D.Atwood, I.Dunietz and A.Soni, [PRL 78, 3257 \(1997\)](#); [PRD 63, 036005 \(2001\)](#)
- Different D decay modes in use
  - CP eigenstates (eg.  $K^+K^-$ ,  $K_S \pi^0$ ) “GLW”
  - Doubly-suppressed decays (eg.  $K\pi$ ) “ADS”
  - Singly-suppressed decays (eg.  $KK^*$ ) “GLS”
  - Three-body decays (eg.  $K_S \pi^+ \pi^-$ ) “GGSZ / Dalitz”
  - Other possibilities exist ...

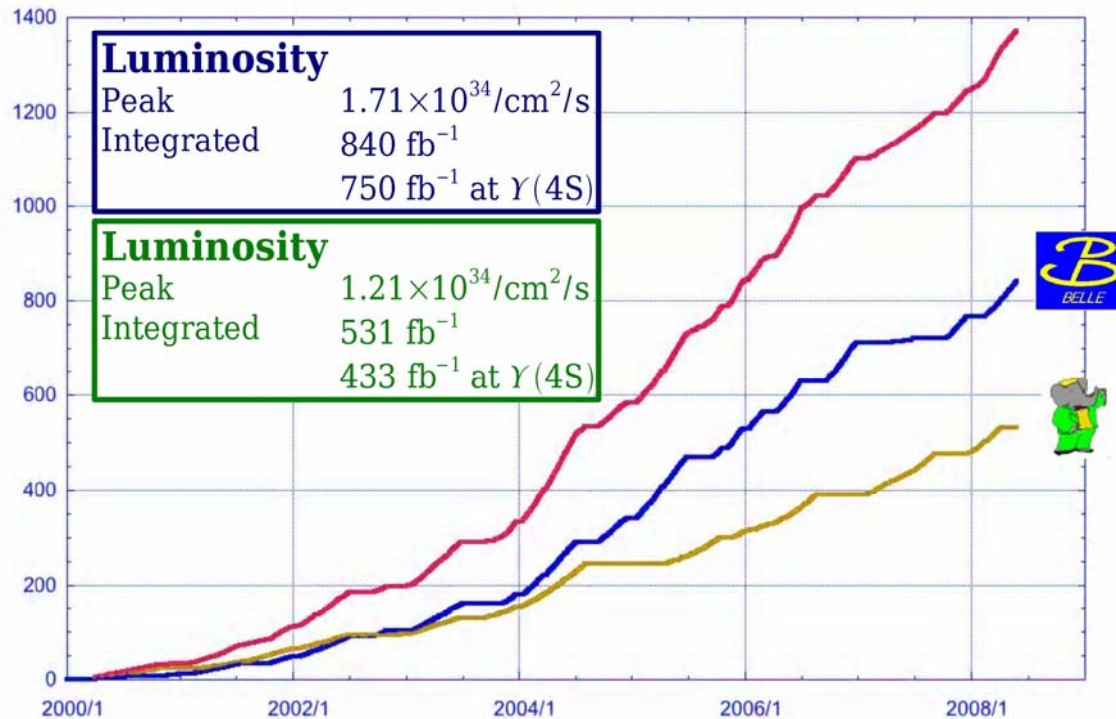
- Why has neither experiment published a combined constraint on  $\gamma$  from its  $B \rightarrow DK$  measurements?
- What auxiliary measurements should be made?
  - eg.  $DK^*$  hadronic parameters in  $DK_S \pi$  DP analysis?
- How can we solve the problem of model dependence in Dalitz plot analyses?
  - Will we reach necessary agreement to enable model independent analysis?
- How much data is needed before statistical issues in  $\gamma$  extraction become irrelevant?

# B factories: BaBar and Belle

K.Trabelsi

Luminosity ( $\text{fb}^{-1}$ )

cumulated stat:  $\sim 1400 \text{fb}^{-1} !!$

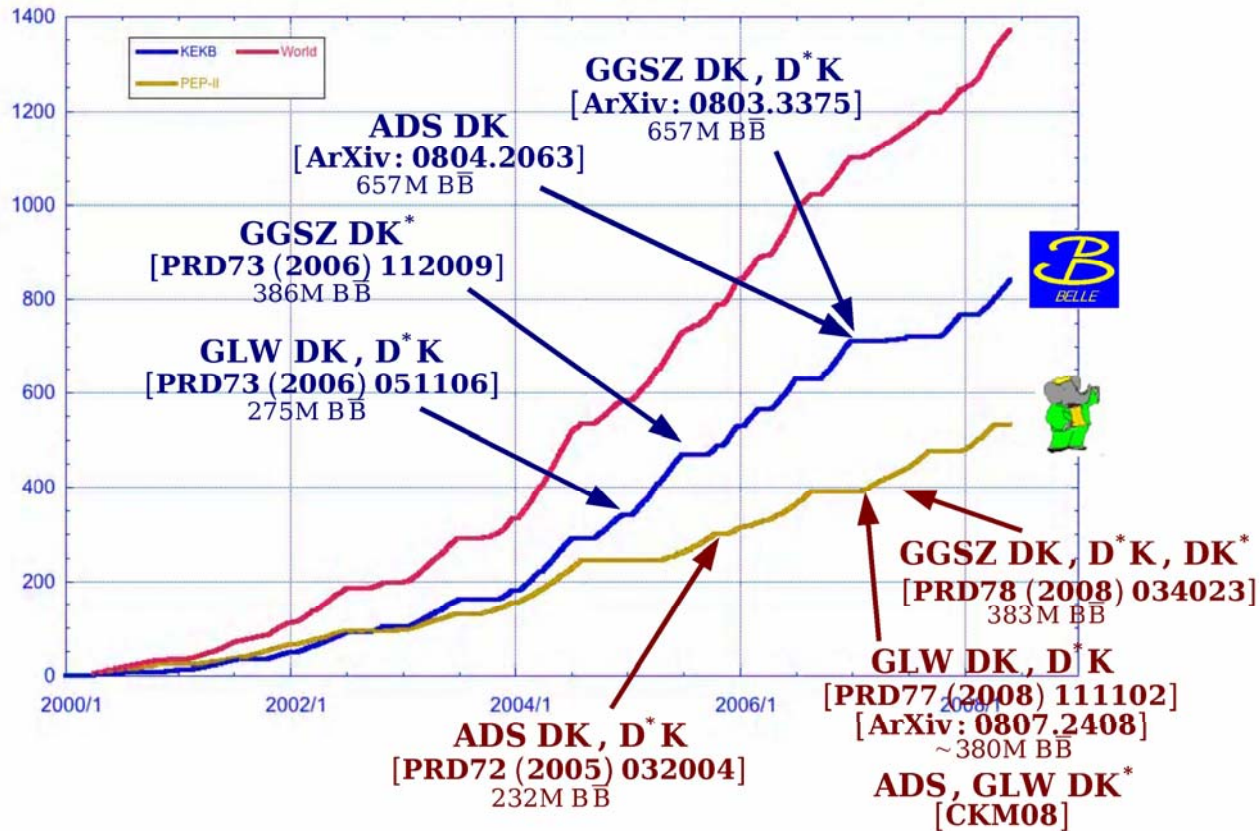


# B factories: BaBar and Belle

K.Trabelsi

and CDF (GLW) !

Luminosity ( $\text{fb}^{-1}$ )





# GLW analysis

M. Gronau, D. London, D. Wyler PLB **253**, 483 (1991); PLB **265**, 172 (1991)

CP eigenstate of  $D$ -meson is used ( $D_{CP}$ ).

CP-even:  $D_1 \rightarrow K^+ K^-, \pi^+ \pi^-$ , CP-odd:  $D_2 \rightarrow K_S \pi^0, K_S \omega, K_S \phi, K_S \eta \dots$

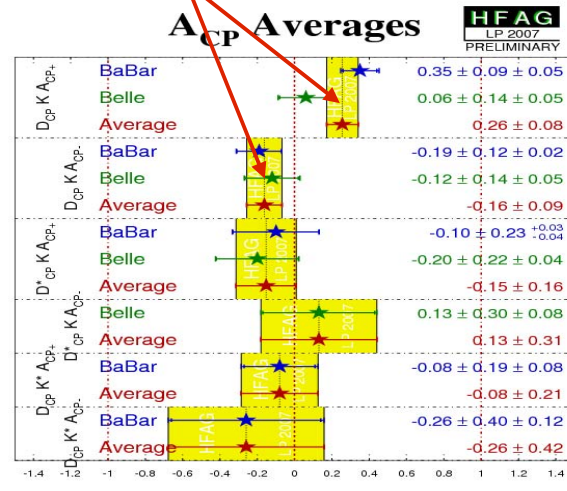
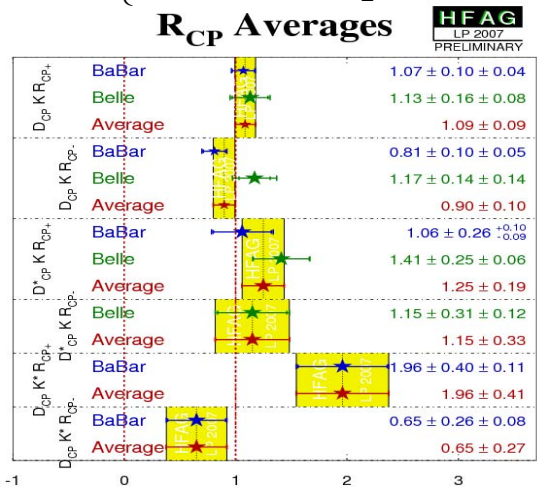
Double ratio:

$$R_{CP\pm} = \frac{Br(B \rightarrow D_{CP\pm} K) / Br(B \rightarrow D_{CP\pm} \pi)}{Br(B \rightarrow D^0 K) / Br(B \rightarrow D^0 \pi)} = 1 + r_B^2 + 2r_B \cos \delta' \cos \varphi_3$$

CP-asymmetry:

$$A_{CP\pm} = \frac{Br(B^+ \rightarrow D_{CP\pm} K^+) - Br(B^- \rightarrow D_{CP\pm} K^-)}{Br(B^+ \rightarrow D_{CP\pm} K^+) + Br(B^- \rightarrow D_{CP\pm} K^-)} = \frac{2r_B \sin \delta' \sin \varphi_3}{R_{CP\pm}}$$

$$\delta' = \begin{cases} \delta & \text{for } D_1 \\ \delta + \pi & \text{for } D_2 \end{cases} \Rightarrow A_{1,2} \text{ have opposite signs}$$



Alternative variables:

$$x_{\pm} = r_B \cos(\delta \pm \varphi_3)$$

$$= \frac{R_{CP+}(1 \mp A_{CP+}) - R_{CP-}(1 \mp A_{CP-})}{4}$$

$$r_B^2 = \frac{R_{CP+} + R_{CP-} - 2}{2}$$

# GLW : $B^- \rightarrow D^0_{CP} K^-$

PRD 77, 111102(R) (June 2008)

$382 \times 10^6 B\bar{B}$



V. Tisserand

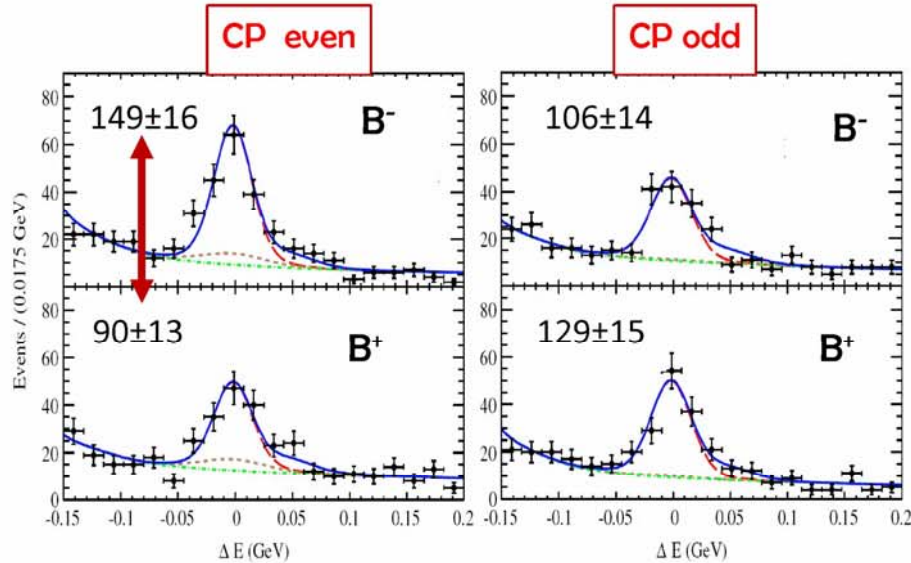
- Selection based on  $m_{ES}$  and event shape variables.
- Extended max. likelihood fit to  $\Delta E$  and Cherenkov angle  $\theta_C$  of the prompt track.
- Use of  $B^- \rightarrow D^0 \pi^-$  as normalization channel and control sample, and  $D^0$  mass side-bands..
- No  $D^0 \rightarrow K^0_s \phi$  mode (GGSZ  $D^0 \rightarrow K^0_s K^+ K^-$ )

$N_{CP+} = 239 \pm 21$   
 $N_{CP-} = 235 \pm 21$   
 $N_{K\pi} = 1872 \pm 51$

$\pm \text{stat.} \pm \text{syst.}$

$A_{CP+} = 0.27 \pm 0.09 \pm 0.04$   
 $A_{CP-} = -0.09 \pm 0.09 \pm 0.02$   
 $R_{CP+} = 1.06 \pm 0.10 \pm 0.05$   
 $R_{CP-} = 1.03 \pm 0.10 \pm 0.05$

$x_+ = -0.09 \pm 0.05 \pm 0.02$   
 $x_- = +0.10 \pm 0.05 \pm 0.03$   
 $r_B^2 = +0.05 \pm 0.07 \pm 0.03$



1. Direct CPV at  $2.8 \sigma$  for CP+ decays
2. Not enough sensitivity to  $\gamma$ , but :
  - most precise GLW measurement.
  - $x_{\pm}$  compatible with GGSZ and as precise.

$$x_{\pm} = r_B \cos(\delta_B \pm \gamma) = \frac{R_{CP+}(1 \mp A_{CP+}) - R_{CP-}(1 \mp A_{CP-})}{4}$$

$$r_B^2 = \frac{R_{CP+} + R_{CP-} - 2}{2}$$

**GLW :  $B^- \rightarrow D^{*\circ} \text{CP} [\rightarrow D^0 \pi^0 / \gamma] K^-$**

arXiv:0807.2408 hep/ex  
(July 2008), submitted to PRD

$383 \times 10^6 B\bar{B}$



V. Tisserand

- Selection based on  $m_{ES}$  and event shape variables.
- Extended max. likelihood fit to  $\Delta E$  and  $dE/dx$  + Cherenkov PID of fast track.
- Use of  $B^- \rightarrow D^{*\circ} \pi^-$  as normalization channel and control sample and  $D^0$  mass side-bands.
- $D^{*\circ}$  CP flips for  $D^0 \pi^0$  and  $D^0 \gamma$  same  $D^0$  final states (PRD 70, 091503 (2004))

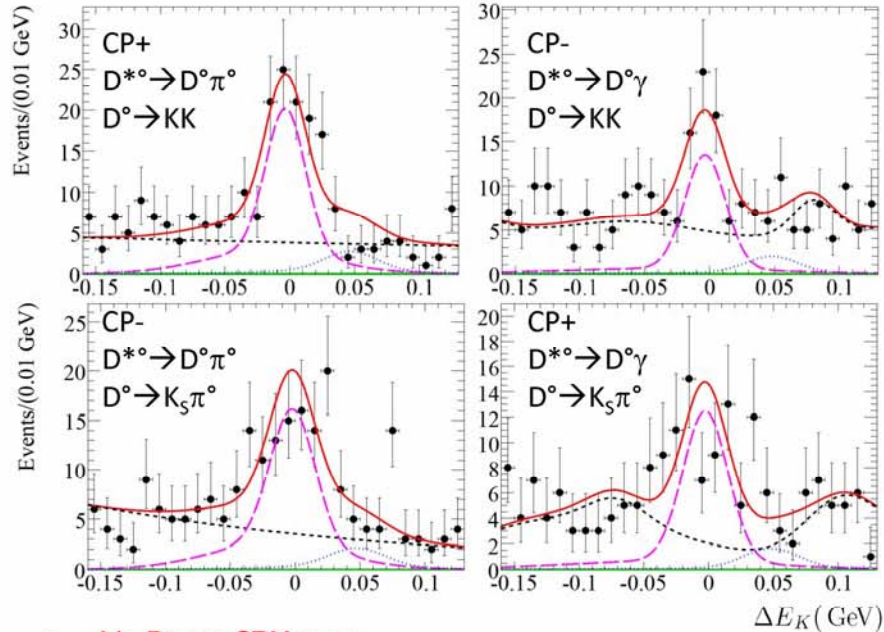
$$\begin{aligned} N_{CP+} &= 244 \pm 22 \\ N_{CP-} &= 225 \pm 23 \\ N_{K\pi} &= 1410 \pm 57 \end{aligned}$$

$\pm \text{stat.} \pm \text{syst.}$

$$\begin{aligned} A_{CP+}^* &= -0.11 \pm 0.09 \pm 0.01 \\ A_{CP-}^* &= 0.06 \pm 0.10 \pm 0.02 \\ R_{CP+}^* &= 1.31 \pm 0.13 \pm 0.04 \\ R_{CP-}^* &= 1.10 \pm 0.12 \pm 0.04 \end{aligned}$$

$$\begin{aligned} x_+^* &= +0.09 \pm 0.07 \pm 0.02 \\ x_-^* &= -0.02 \pm 0.06 \pm 0.02 \\ r_B^{*2} &= +0.22 \pm 0.09 \pm 0.03 \end{aligned}$$

( $K^0_s \phi$  removed for Cartesian coords.)



1. **No Direct CPV seen.**

2. **Not enough sensitivity to  $\gamma$ , but :**

- most precise  $D^*K$  GLW measurement.
- $x_{\pm}^*$  compatible with GGSZ and as precise,  $r_B^*$  expected large.

379x10<sup>6</sup> B $\bar{B}$

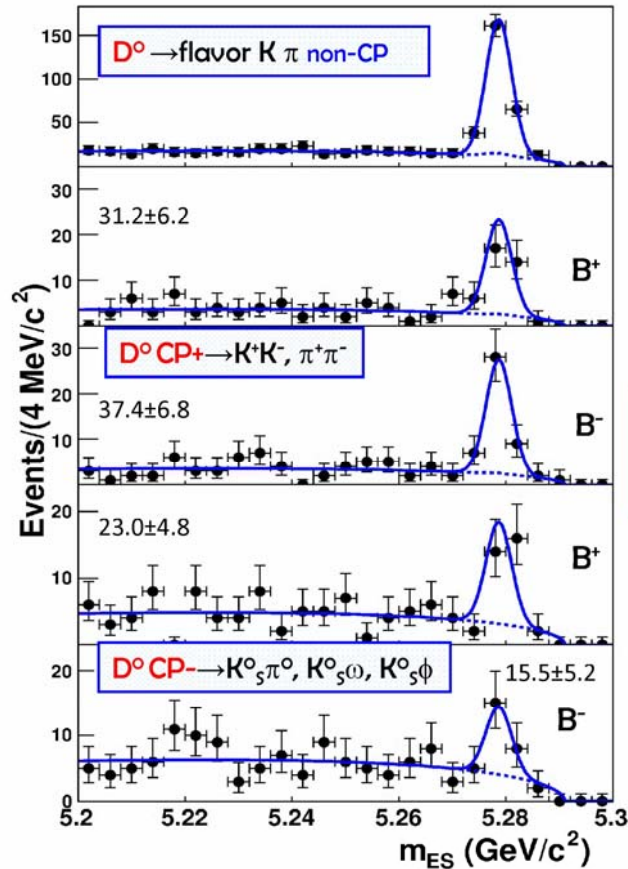
GLW : B<sup>-</sup> → D<sup>0</sup><sub>CP</sub> K<sup>\*-</sup> [→ K<sup>0</sup><sub>S</sub> π<sup>-</sup>]



NEW

PRELIMINARY

V. Tisserand



- Selection re-optimized and event shape in Neural Net wrt 2005 (higher eff'cy, bkg. rejection, and stat.)
- (peaking)-bkg. from ΔE and mD<sup>0</sup> sidebands.
- CP+ pollution for K<sup>0</sup><sub>S</sub>(K<sup>+</sup>K<sup>-</sup>)non-φ & K<sup>0</sup><sub>S</sub>(π<sup>+</sup>π<sup>-</sup>π<sup>0</sup>)non-ω measured in the data.
- Vary by 2π the δ strong phases from S-wave Kπ pairs in K<sup>\*-</sup>[K<sup>0</sup><sub>S</sub>π<sup>-</sup>] decays.

N<sub>CP+</sub> = 68.6 ± 9.2  
 N<sub>CP-</sub> = 38.5 ± 7.0  
 N<sub>Kπ</sub> = 231 ± 17

±stat. ±syst.  
 A<sup>S</sup><sub>CP+</sub> = 0.09 ± 0.13 ± 0.05  
 A<sup>S</sup><sub>CP-</sub> = -0.23 ± 0.21 ± 0.07  
 R<sup>S</sup><sub>CP+</sub> = 2.17 ± 0.35 ± 0.09  
 R<sup>S</sup><sub>CP-</sub> = 1.03 ± 0.27 ± 0.13

x<sub>S+</sub> = 0.18 ± 0.14 ± 0.05  
 x<sub>S-</sub> = 0.38 ± 0.14 ± 0.05

1. No Direct CPV seen.
2. Precision improved wrt 2005, results confirmed, world's only measurement.

V. Tisserand, LAPP, CKM08

CKM-angle γ from charged B decays at BABAR

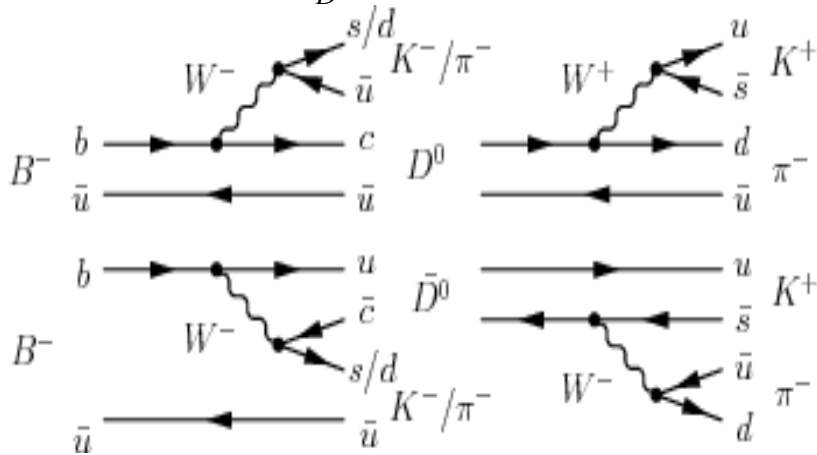
6

# ADS analysis

D. Atwood, I. Dunietz and A. Soni, PRL **78**, 3357 (1997)

Enhance magnitude of CP violation by using Doubly Cabibbo-suppressed  $D$  decays

e.g.  $B^- \rightarrow [K^+\pi^-]_D K^-$ :

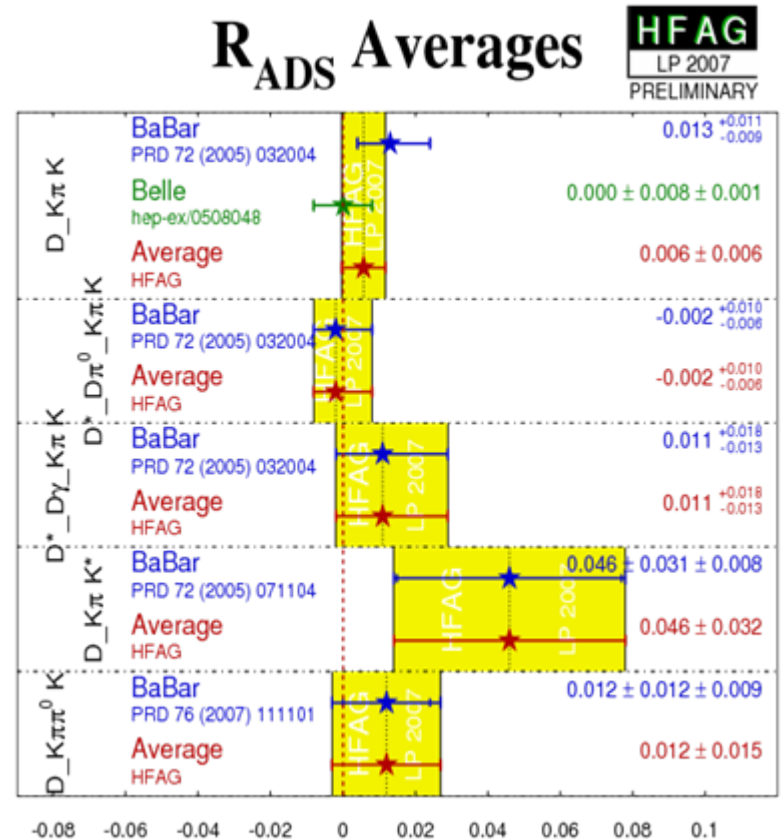


Observable:

$$R_{ADS} = \frac{Br(B \rightarrow D_{\text{supp}} K)}{Br(B \rightarrow D_{\text{fav}} K)} = r_B^2 + r_D^2 + 2r_B r_D \cos \varphi_3 \cos \delta$$

where

$$\delta = \delta_B + \delta_D, \quad r_D = \left| \frac{\Lambda(D^0 \rightarrow K^- \pi^+)}{\Lambda(D^0 \rightarrow K^+ \pi^-)} \right| = 0.0578 \pm 0.0008$$



# ADS analysis (Belle)

Belle collaboration, 657M BB pairs [[arXiv: 0804:2063, submitted to PRD\(RC\)](#)]  
 $B^- \rightarrow [K^- \pi^+]_D K^-$  (suppressed) and  $B^- \rightarrow [K^+ \pi^-]_D K^-$  (favored) modes are selected.

- Cut on  $M_{bc}$ ,  $M_D$ , PID likelihood, event shape
- Fit  $\Delta E$  to extract signal yield

$$R_{ADS} = (8.0^{+6.3}_{-5.7} \quad +2.0_{-2.8}) \times 10^{-3}$$

CP asymmetry:

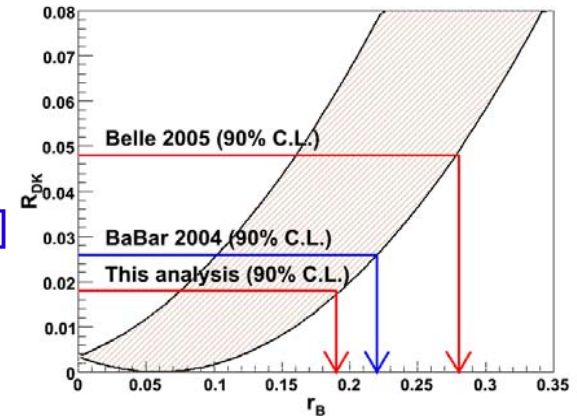
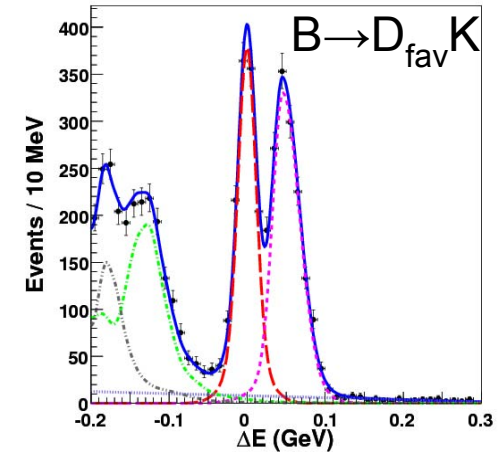
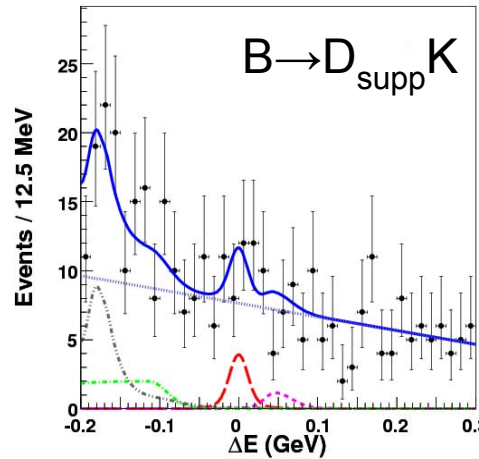
$$A_{ADS} = -0.13^{+0.98}_{-0.88} \pm 0.26$$

$$r_B < 0.19 \text{ at } 90\% \text{ CL}$$

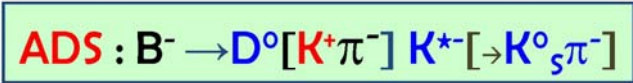
(with the conservative assumption  $\cos \varphi_3 \cos \delta = -1$ )

Using CLEO measurement  $\delta_D = (22^{+11}_{-12} \quad +9_{-11})^\circ$  [[arXiv: 0802:2268](#)]

and  $\varphi_3, \delta_B$  measurements from Dalitz analysis, tighter  $r_B$  constraint can be obtained.

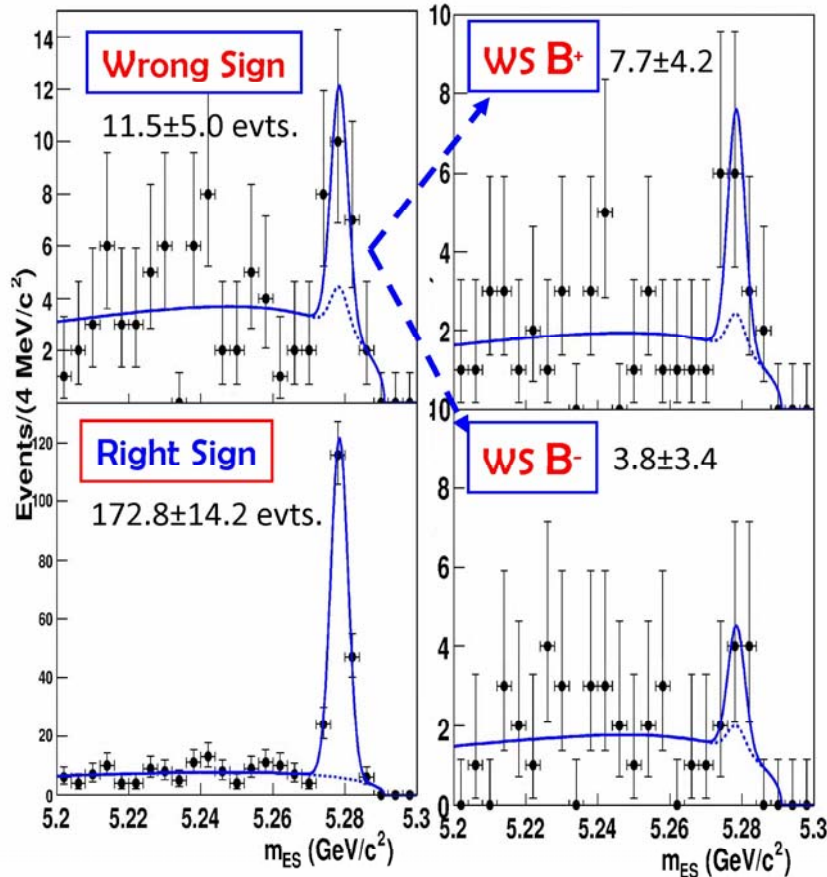


379x10<sup>6</sup> B $\bar{B}$



**NEW**  
PRELIMINARY

V. Tisserand



- 11.5±5.0 WS ADS signal events.
- Accounts for (K<sup>0</sup><sub>s</sub>π<sup>-</sup>)non-K<sup>\*</sup> with S-waves pairs, directly determined from the data.
- Syst.: detector asymmetry, peaking bkg., and same final state bkgd. (K<sup>+</sup>π<sup>-</sup>K<sup>\*-</sup> charmless bkg. ...).

±stat.±syst.

$$A_{ADS}^S = -0.34 \pm 0.45 \pm 0.16$$

$$R_{ADS}^S = 0.066 \pm 0.029 \pm 0.010$$

1. No Direct CPV seen.
2. Better precision wrt 2005 result, again unique in the world.

V. Tisserand, LAPP, CKM08

CKM-angle  $\gamma$  from charged B decays at BABAR

8

# Dalitz analysis method

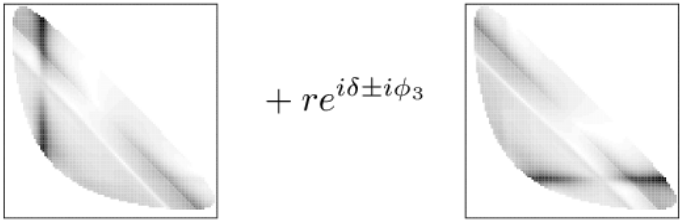
A. Giri, Yu. Grossman, A. Soffer, J. Zupan, PRD **68**, 054018 (2003)

A. Bondar, Proc. of Belle Dalitz analysis meeting, 24-26 Sep 2002.

$$|D^0\rangle + re^{i\theta} |\bar{D}^0\rangle$$

Using 3-body final state, identical for  $D^0$  and  $\bar{D}^0$ :  $K_S\pi^+\pi^-$ .

Dalitz distribution density:  $dp(m_{K_S\pi^+}^2, m_{K_S\pi^-}^2) \sim |f_D|^2 dm_{K_S\pi^+}^2 dm_{K_S\pi^-}^2$

$$f_D(m_{K_S\pi^+}^2, m_{K_S\pi^-}^2) = \left[ \text{Plot 1} + re^{i\delta \pm i\phi_3} \text{Plot 2} \right]^2$$


(assuming CP-conservation in  $D^0$  decays)

If  $f_D(m_{K_S\pi^+}^2, m_{K_S\pi^-}^2)$  is known, parameters  $(\varphi_3/\gamma, r_B, \delta)$  are obtained from the fit to Dalitz distributions of  $D \rightarrow K_S\pi^+\pi^-$  from  $B^\pm \rightarrow DK^\pm$  decays

Need to know a complex form of the  $D^0$  decay amplitude, but only  $|f_D|^2$  is obtained from  $D^* \rightarrow D\pi$

$\Rightarrow$  Need to use model description, model uncertainty as a result



**Fit results: 12 (3x4) Cartesian coordinates**

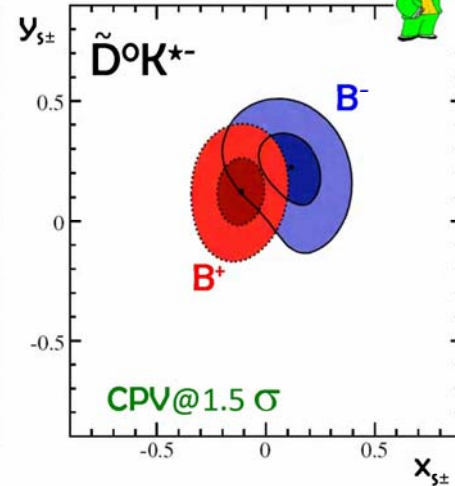
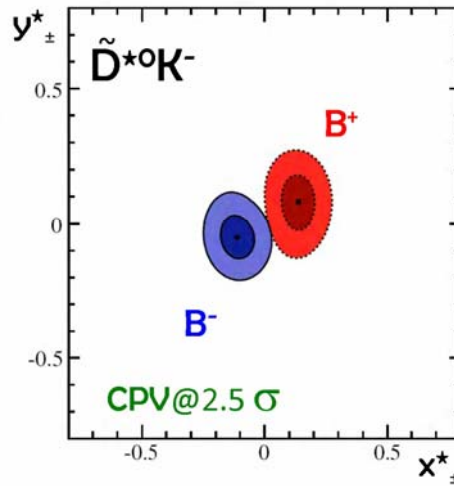
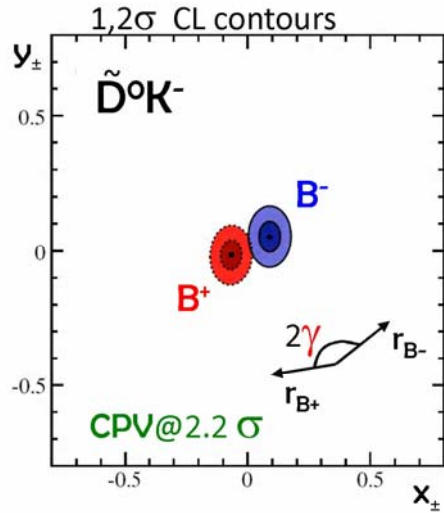
PRD78, 034023 (2008)

383x10<sup>6</sup> BB

V. Tisserand

$$\mathbf{z}^{(*)}_{(s)\pm} \equiv (\mathbf{x}^{(*)}_{(s)\pm}, \mathbf{y}^{(*)}_{(s)\pm}) = (\mathbf{Re}, \mathbf{Im}) \{ r^{(*)}_{sB} e^{i(\delta^{(*)}_{(s)B} \pm \gamma)} \}$$

→ Almost Gaussian behavior near physical bounds ( $r_B \approx 0$ ), better than the 7 physics params.



$x^- = 0.090 \pm 0.043 \pm 0.015 \pm 0.011$   
 $y^- = 0.053 \pm 0.056 \pm 0.007 \pm 0.015$   
 $x^+ = -0.067 \pm 0.043 \pm 0.014 \pm 0.011$   
 $y^+ = -0.015 \pm 0.055 \pm 0.006 \pm 0.008$

$x^{*-} = -0.111 \pm 0.069 \pm 0.014 \pm 0.004$   
 $y^{*-} = -0.051 \pm 0.080 \pm 0.009 \pm 0.010$   
 $x^{*+} = 0.137 \pm 0.068 \pm 0.014 \pm 0.005$   
 $y^{*+} = 0.080 \pm 0.102 \pm 0.010 \pm 0.012$

$x_{s^-} = 0.115 \pm 0.138 \pm 0.039 \pm 0.014$   
 $y_{s^-} = 0.226 \pm 0.142 \pm 0.058 \pm 0.011$   
 $x_{s^+} = -0.113 \pm 0.107 \pm 0.028 \pm 0.018$   
 $y_{s^+} = 0.125 \pm 0.139 \pm 0.051 \pm 0.010$

±stat. ±syst.(exp.) ±syst.(Dalitz model)

$|z_{B^+} - z_{B^-}| \neq 0 \rightarrow$  direct CPV@ 3.0σ combined

**Dalitz :  $\gamma$  results for  $B^- \rightarrow \tilde{D}^{(*)0} K^{*-}$**

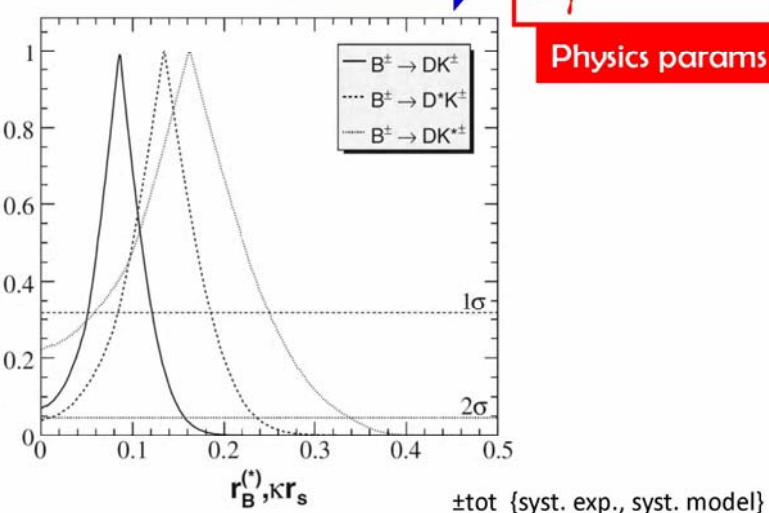
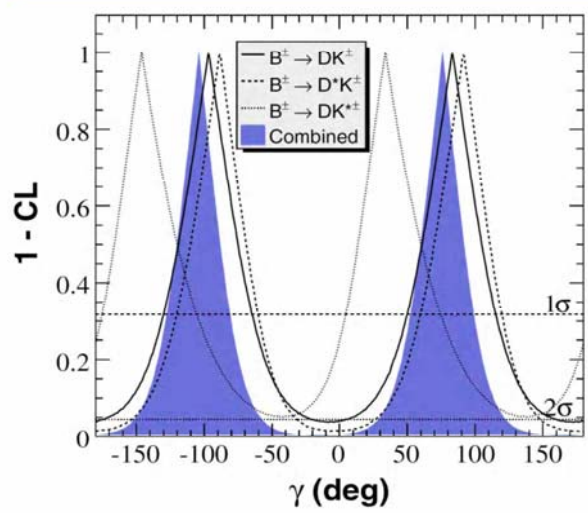


PRD78, 034023 (2008)  
383x10<sup>6</sup> BB

From measured CP parameters:  $(x^\pm, y^\pm), (x^{*\pm}, y^{*\pm}), (x_s^\pm, y_s^\pm)$   
perform **combined fit** to pseudo experiments : **frequentist approach** removing unphysical regions ( $r_{B^+} \neq r_{B^-} \dots$ )

extract 1D CL intervals

- V Tisserand
- $r_B, r_B^*, r_{sB}$
  - $\delta_B, \delta_B^*, \delta_{sB}$
  - $\gamma$
- Physics params



$$\gamma[\text{mod } \pi] = (76^{+23}_{-24})^\circ \{5, 5\}^\circ$$

$$r_B(\text{DK}) = (8.6 \pm 3.5)\% \{1.0, 1.1\}\%$$

$$r_B(\text{D}^*K) = (13.5 \pm 5.1)\% \{1.1, 0.5\}\%$$

$$r_B(\text{DK}^*) = (16.3^{+8.8}_{-10.5})\% \{3.7, 2.1\}\%$$

→ Statistics limited, small  $r_B \sim 10\%$  favored (limits sensitivity to  $\gamma$ ).

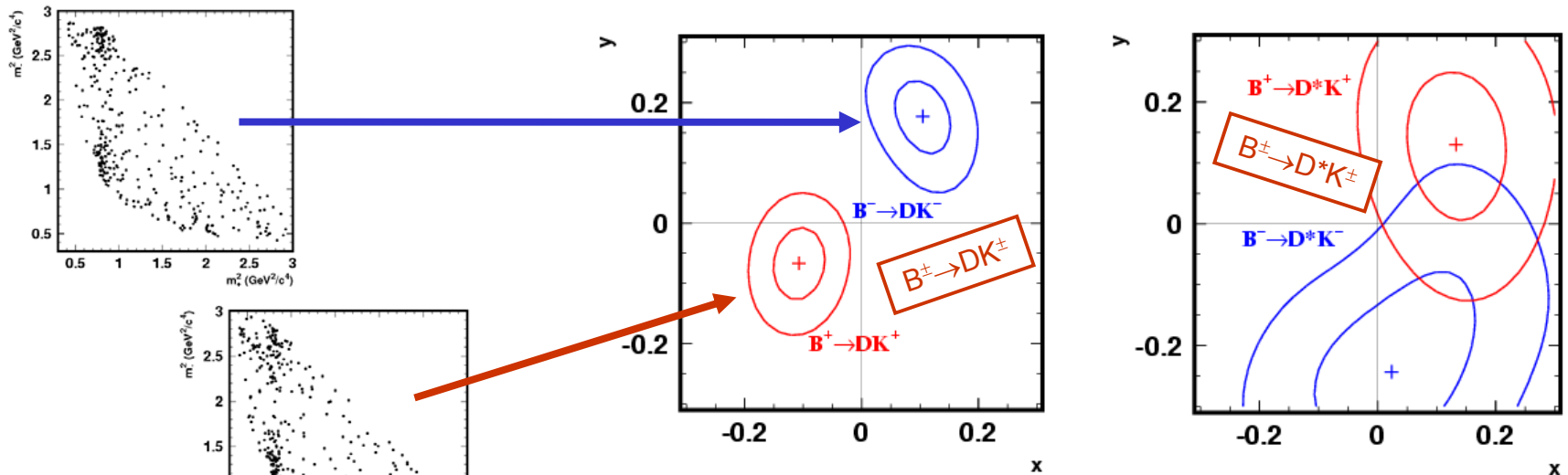
# Belle Dalitz: fit results

[preliminary]

Fit parameters are  $x_{\pm} = r_B \cos(\pm\varphi_3 + \delta)$  and  $y_{\pm} = r_B \sin(\pm\varphi_3 + \delta)$

Unbinned maximum likelihood fit with event-by-event background treatment

( $\Delta E$ ,  $M_{bc}$ ,  $|\cos\theta_{thr}|$ ,  $F$  included into likelihood)



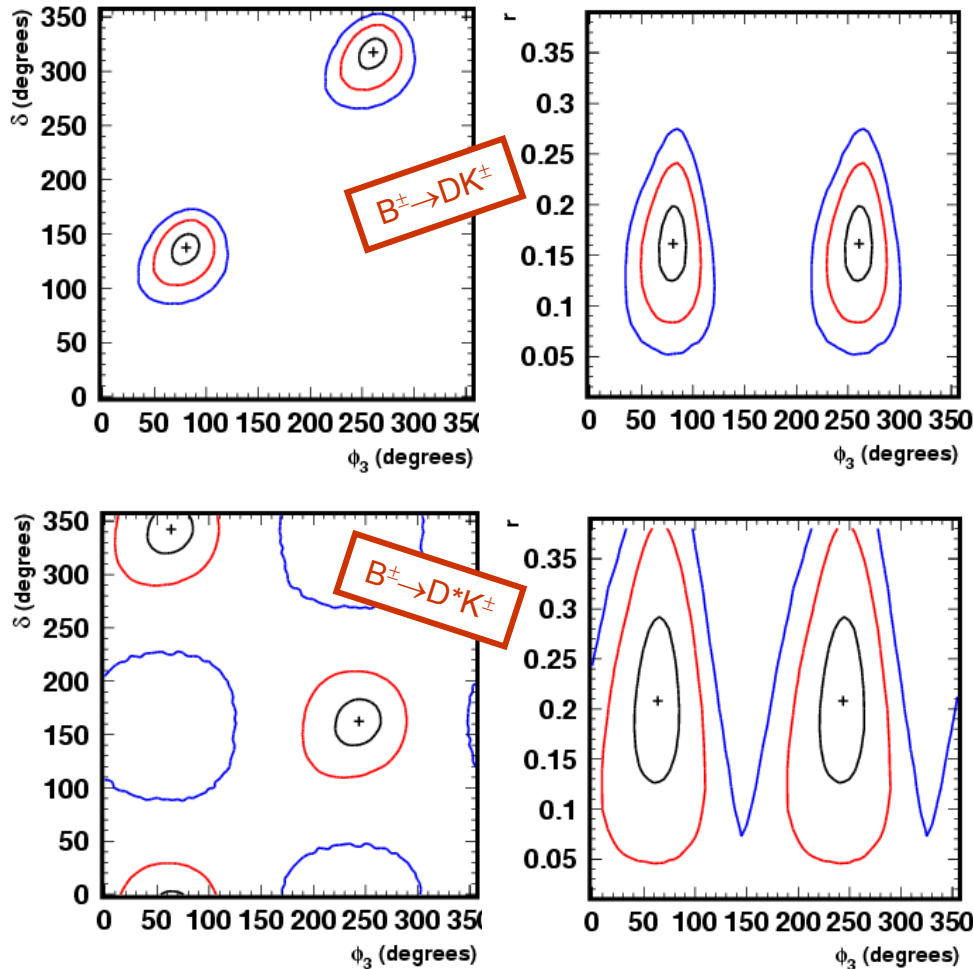
$x_- = +0.105 \pm 0.047 \pm 0.011$   
 $y_- = +0.177 \pm 0.060 \pm 0.018$   
 $x_+ = -0.107 \pm 0.043 \pm 0.011$   
 $y_+ = -0.067 \pm 0.059 \pm 0.018$

$x_- = +0.024 \pm 0.140 \pm 0.018$   
 $y_- = -0.243 \pm 0.137 \pm 0.022$   
 $x_+ = +0.133 \pm 0.083 \pm 0.018$   
 $y_+ = +0.130 \pm 0.120 \pm 0.022$

Errors are statistical and experimental systematic. Model error not included.

# Belle Dalitz: fit results

[preliminary]



$B^\pm \rightarrow DK^\pm$  only:

$$\varphi_3 = 81_{-15}^{+13} \pm 5^\circ (\text{syst}) \pm 9^\circ (\text{model})$$

$B^\pm \rightarrow D^*K^\pm$  only:

$$\varphi_3 = 64_{-23}^{+21} \pm 4^\circ (\text{syst}) \pm 9^\circ (\text{model})$$

$B^\pm \rightarrow DK^\pm, B^\pm \rightarrow D^*K^\pm$  combined:

$$\varphi_3 = 76_{-13}^{+12} \pm 4^\circ (\text{syst}) \pm 9^\circ (\text{model})$$

$$r_{DK} = 0.16 \pm 0.04 \pm 0.01 (\text{syst}) \pm 0.05 (\text{model})$$

$$r_{D^*K} = 0.21 \pm 0.08 \pm 0.01 (\text{syst}) \pm 0.05 (\text{model})$$

$$\delta_{DK} = 136_{-16}^{+14} \pm 4^\circ (\text{syst}) \pm 23^\circ (\text{model})$$

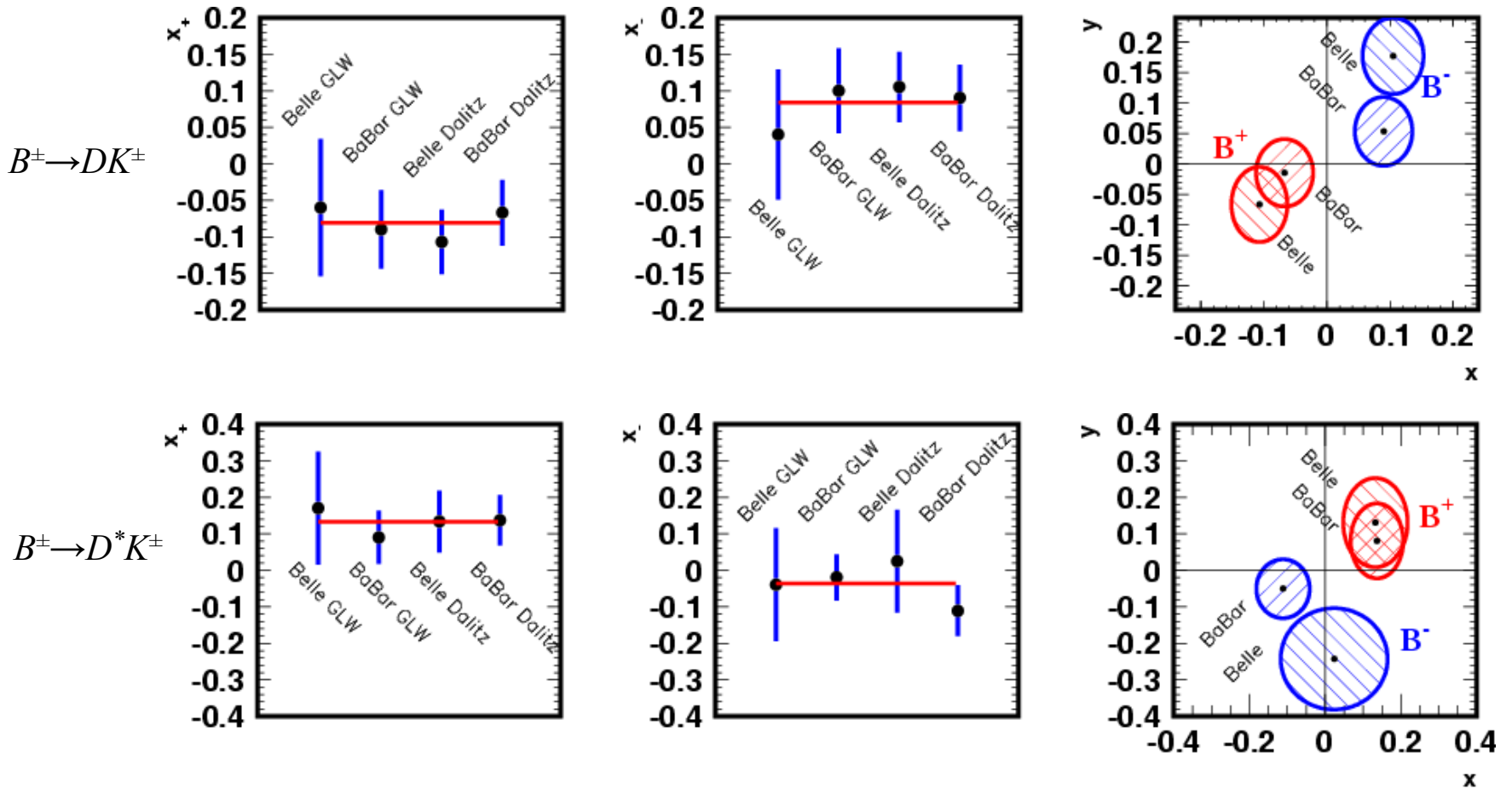
$$\delta_{D^*K} = 343_{-22}^{+20} \pm 4^\circ (\text{syst}) \pm 23^\circ (\text{model})$$

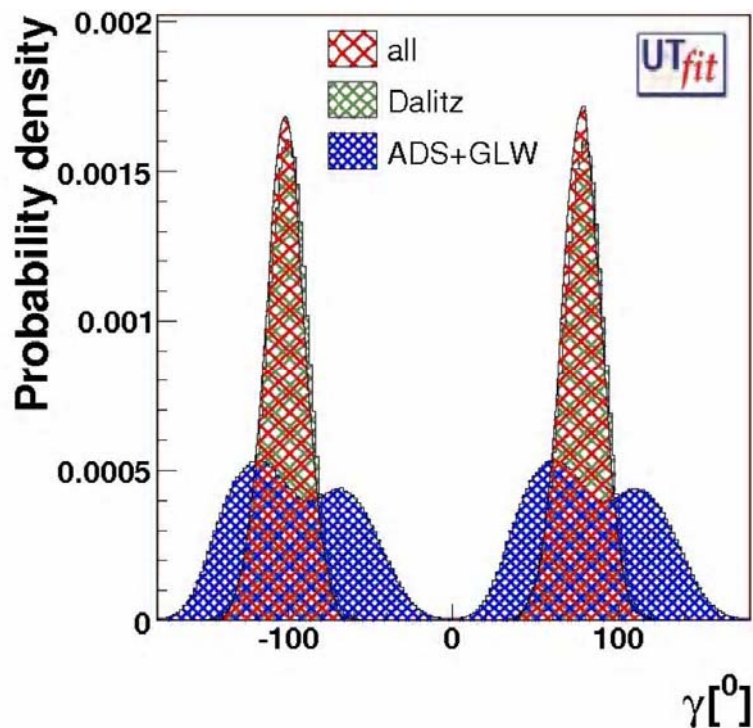
Model error estimate is the same as in previous analysis.

Stat. CL of CPV:  $(1-5.5 \cdot 10^{-4})$  or  $3.5\sigma!$

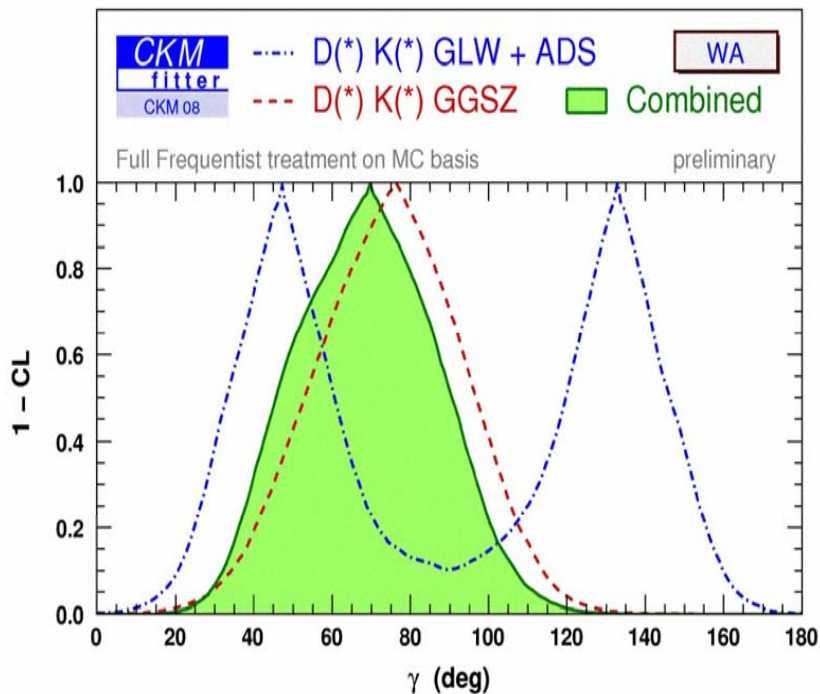
# Comparison of measurements

GLW and Dalitz methods in Cartesian variables (x,y):





$$\gamma = (78 \pm 12)^\circ, [2\sigma] = (54^\circ, 100^\circ)$$



$$\gamma = (70_{-29}^{+27})^\circ, [2\sigma] = (29^\circ, 113^\circ)$$

# Model-independent analysis

Model-independent way: obtain  $D^0$  decay strong phase from  $\psi(3770) \rightarrow D\bar{D}$  data

$$P_D(m_+^2, m_-^2) = |f_D(m_+^2, m_-^2)|^2 \quad \bar{P}_D(m_+^2, m_-^2) = |f_{\bar{D}}(m_+^2, m_-^2)|^2$$

$$P_{B^\pm}(m_+^2, m_-^2) = |f_D + (x+iy)\bar{f}_D|^2 = P_D + r_B^2 \bar{P}_D + 2\sqrt{P_D \bar{P}_D} [x_\pm C + y_\pm S] \quad (1)$$

where  $\left. \begin{array}{l} x_\pm = r_B \cos(\delta \pm \varphi_3) \\ y_\pm = r_B \sin(\delta \pm \varphi_3) \end{array} \right\}$  Free parameters

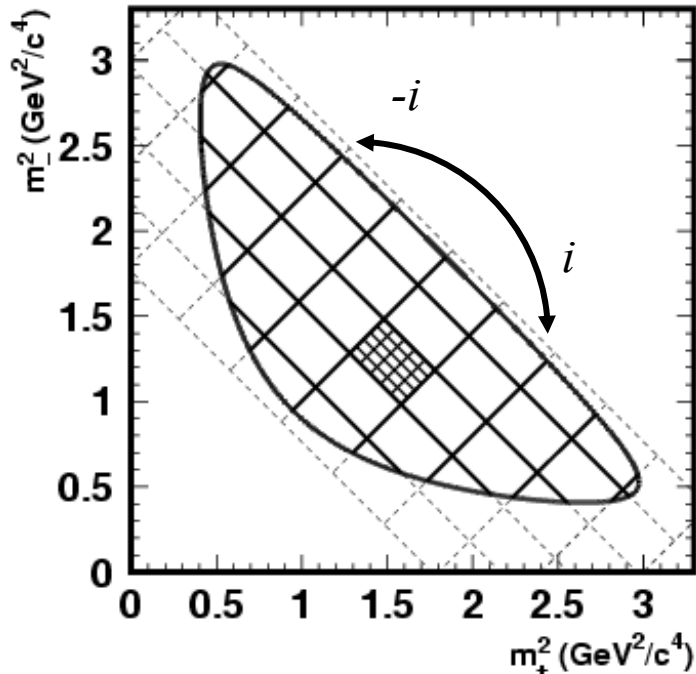
$$\left. \begin{array}{l} C(m_+^2, m_-^2) = \cos(\delta_D(m_+^2, m_-^2) - \delta_D(m_-^2, m_+^2)) \\ S(m_+^2, m_-^2) = \sin(\delta_D(m_+^2, m_-^2) - \delta_D(m_-^2, m_+^2)) \end{array} \right\} \text{Unknown, can be obtained from charm data:}$$

$$D_{CP} \rightarrow K_S \pi^+ \pi^-: \quad P_{CP^\pm}(m_+^2, m_-^2) = |f_D \pm \bar{f}_D|^2 = P_D + \bar{P}_D \pm 2\sqrt{P_D \bar{P}_D} C \quad (2)$$

$$\psi(3770) \rightarrow (K_S \pi^+ \pi^-)_D (K_S \pi^+ \pi^-)_{\bar{D}}: \quad \begin{aligned} P_{Corr}(m_+^2, m_-^2, m_+^{\prime 2}, m_-^{\prime 2}) &= |f_D \bar{f}'_D - \bar{f}_D f'_D|^2 = \\ &= P_D \bar{P}'_D + \bar{P}_D P'_D - 2\sqrt{P_D \bar{P}_D P'_D \bar{P}'_D} (CC' + SS') \end{aligned} \quad (3)$$

# Binned analysis: $D_{CP}$

[A. Giri, Yu. Grossman, A. Soffer, J. Zupan, PRD 68, 054018 (2003)]



Number of events in  $D^0$ -plot:  $K_i$

Number of events in  $B$ -plot

$$\langle N \rangle_i = h_B [K_i + r_B^2 K_{-i} + 2\sqrt{K_i K_{-i}} (x c_i + y s_i)] \quad (4)$$

Number of events in  $D_{CP}$ -plot

$$\langle M \rangle_i = h_{CP} [K_i + K_{-i} \pm 2\sqrt{K_i K_{-i}} c_i] \quad (5)$$

$$c_i = \frac{\int_{\mathcal{D}_i} \sqrt{p\bar{p}} \cos \Delta\delta(\mathcal{D}) d\mathcal{D}}{\sqrt{\int_{\mathcal{D}_i} p d\mathcal{D} \int_{\mathcal{D}_i} \bar{p} d\mathcal{D}}} \equiv \langle \cos \Delta\delta(\mathcal{D}) \rangle_{\mathcal{D}_i}$$

$$s_i = \langle \sin \Delta\delta(\mathcal{D}) \rangle_{\mathcal{D}_i}$$

$$c_i^2 + s_i^2 \leq 1$$

(=1 if bin size is small enough)



# Binned analysis: $D_{CP}$

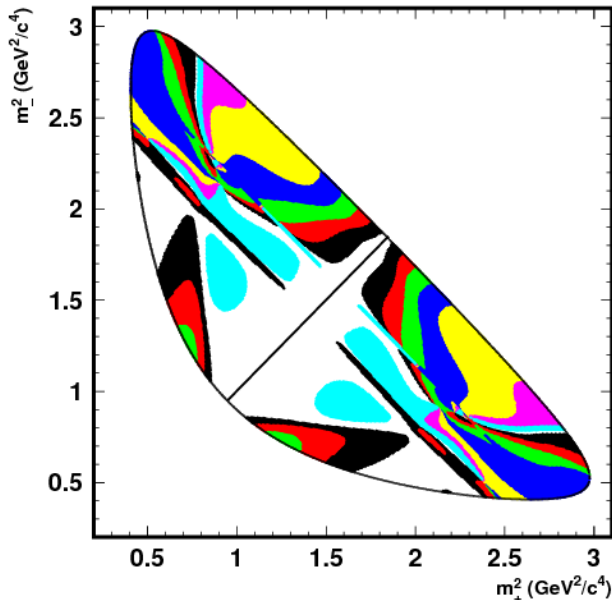
[A. Bondar, A. Poluektov, hep-ph/0703267]

To use the limited CLEO-c data:

- Find binning with optimal sensitivity
  - Get rid of bias due to  $s_i = \pm\sqrt{1-c_i^2}$
- } Satisfy simultaneously for  $c_i^2 + s_i^2 \approx 1$  binning with

Good approximation: uniform binning in  $\Delta\delta_D$ :

$$2\pi(i-1/2)/\mathcal{N} < \Delta\delta_D(m_+^2, m_-^2) < 2\pi(i+1/2)/\mathcal{N}$$



But the optimal binning depends on  $D^0$  model.  $\Rightarrow$  bias if it differs from actual one (same  $\sim 10^\circ$ ).

$s_i = \pm\sqrt{1-c_i^2}$  causes unavoidable model sensitivity. Reduces as data increases (by applying finer binning).

# Binned analysis: $(K_S\pi^+\pi^-)^2$

---

2 correlated Dalitz plots, 4 dimensions:

$$\langle M \rangle_{ij} = h[K_i K_{-j} + K_j K_{-i} - 2\sqrt{K_i K_{-i} K_j K_{-j}} (c_i c_j + s_i s_j)] \quad (6)$$

Can use maximum likelihood technique:

$$-2 \log \mathcal{L} = -2 \sum \log p_{Poisson}(M_{ij}, \langle M \rangle_{ij}) \rightarrow \min \quad (7)$$

with  $c_i$  and  $s_i$  as free parameters.

For the same binning as in  $D_{CP}$ , number of bins is  $\mathcal{N}^2$  (instead of  $\mathcal{N}$ ), but the number of unknowns is the same.

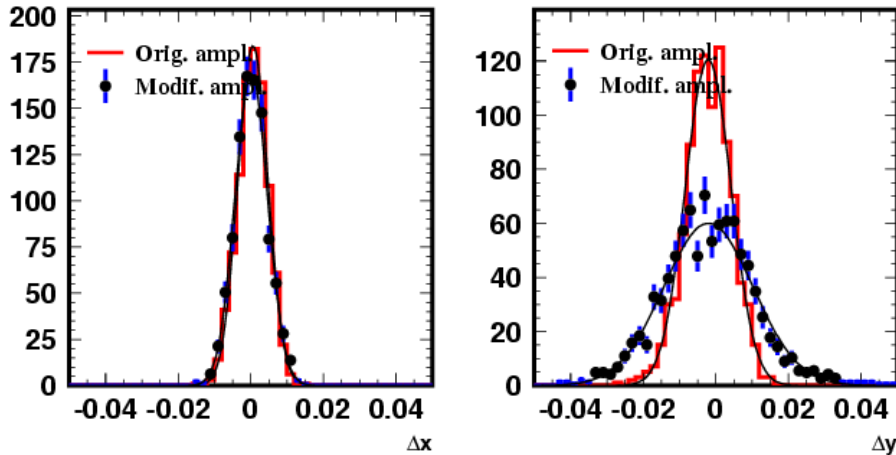
With Poisson PDF, it's OK to have  $N_{ij} < 1$ .

Can obtain both  $c_i$  and  $s_i$ .

It's convenient to use combined likelihood of  $(K_S\pi^+\pi^-)^2$  and B data to account for errors in  $c_i$  and  $s_i$ .

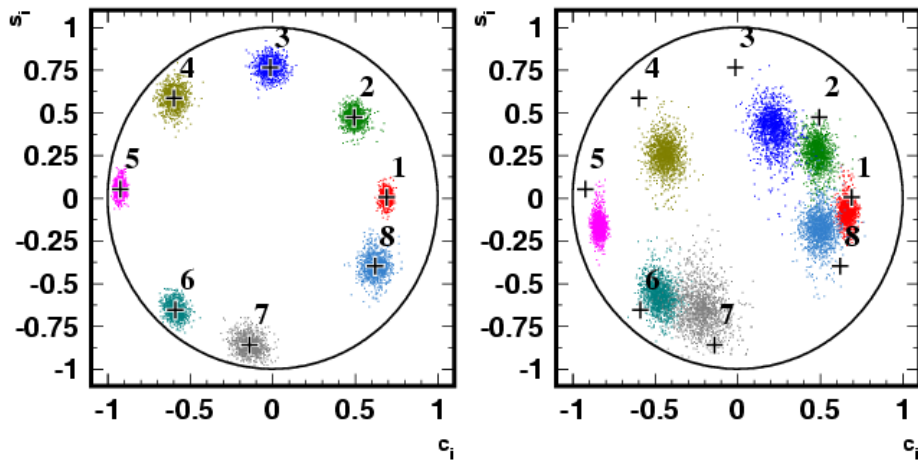
---

# MC simulation of the bias in $\phi_3$ measurement

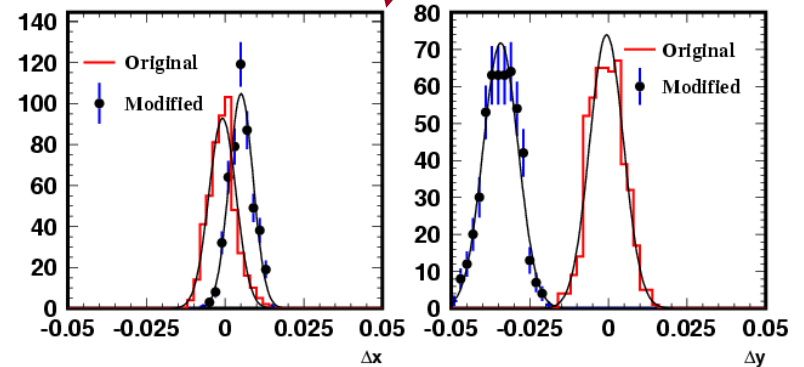


Model dependence for 2x8 bins in  $(K_S\pi^+\pi^-)^2$  case:

No bias when changing the model, but stat. error degrades.



Model dependence for 2x8 bins in  $D_{cp}$  case:

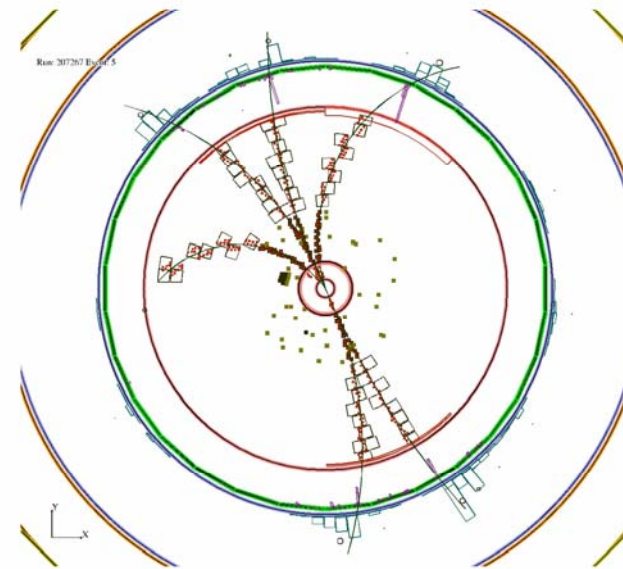


# CLEO-c

$$e^+e^- \rightarrow \psi(3770) \rightarrow D\bar{D}$$

J.Rademacker

- Threshold production of correlated  $D\bar{D}$ .
- Final state must be CP-odd,
- ...and flavour-neutral.
- That gives us access to both amplitude and phase across the Dalitz plot.



$$\psi(3770) \rightarrow D^0(K_S\pi^+\pi^-)\bar{D}^0(K^+\pi^-)$$

# Event Yield Summary

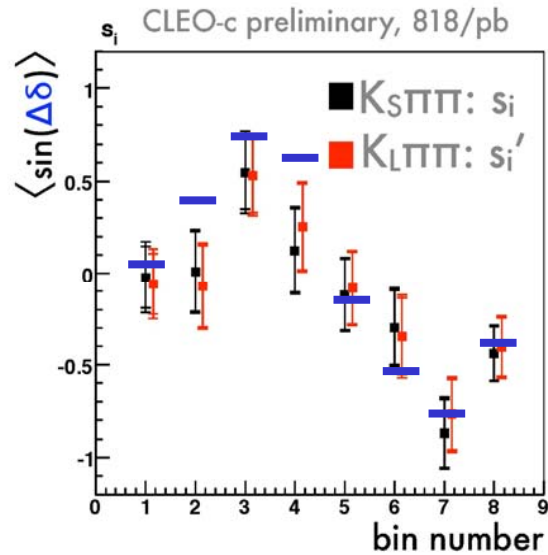
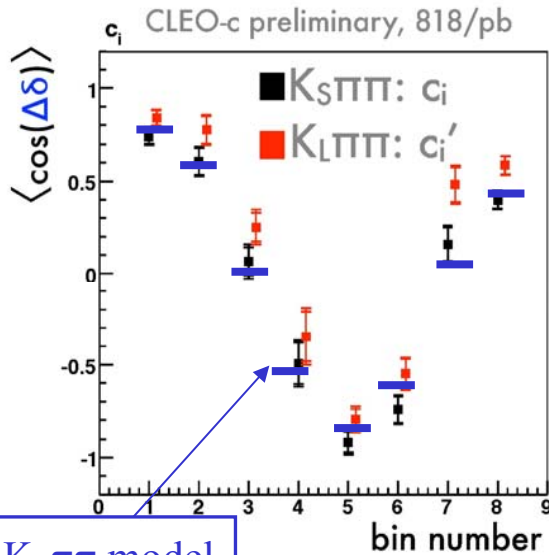
J.Rademacker

- Yields in  $818 \text{ pb}^{-1}$ , all with  $B/S < 0.1$ :
- flavour-tagged: 12k  $K_L\pi^+\pi^-$ , 4k  $K_S\pi^+\pi^-$ .
- 517 CP-odd  $K_L\pi^+\pi^-$       311 CP-even  $K_S\pi^+\pi^-$   
322 CP-even  $K_L\pi^+\pi^-$       471 CP-odd  $K_S\pi^+\pi^-$
- 1.2k  $K_L\pi^+\pi^-$  vs  $K_S\pi^+\pi^-$ ,      475  $K_S\pi^+\pi^-$  vs  $K_S\pi^+\pi^-$
- (Note: larger reconstruction efficiency for  $K_L\pi^+\pi^-$ , but fewer suitable tag modes)
- Nomenclatura trap: Often, esp. within CLEO-c, we refer to “CP-even-tagged”  $K_S\pi^+\pi^-$ . This is  $K_S\pi^+\pi^-$  with CP-even D on the OTHER side. So that’s a CP-odd  $K_S\pi^+\pi^-$ . In this slide CP refers to the CP of the  $K_S\pi^+\pi^-$  (not the tag).

CLEO-c preliminary, 818/pb

# The Result

J. Rademacker



Fit errors (include  $\sigma_{\text{statistical}} \oplus$  errors on  $\Delta c_i, \Delta s_i$  constraints):

- $c_i$ : 0.04-0.11
- $c_i'$ : 0.04-0.14
- $s_i$ : 0.15-0.23
- $s_i'$ : 0.16-0.23

- Results of combined fit in terms of  $c_i, s_i$  in  $K_S\pi\pi$  and  $c_i', s_i'$  in  $K_L\pi\pi$ .
- Each series of results (black/red) contains full information from both  $K_S\pi\pi$  and  $K_L\pi\pi$  data, related by  $\Delta c_i, \Delta s_i$ .
- Systematic errors:
  - $c_i$ : 0.02-0.06
  - $c_i'$ : 0.02-0.07
  - $s_i$ : 0.04-0.10
  - $s_i'$ : 0.06-0.10

Jonas Rademacker (University of Bristol) for CLEO-c;

CKM 2008, Roma 17

# Summary: CLEO-c's impact on $\gamma$

J.Rademacker

- CLEO-c's quantum-correlated D-Dbar pairs give model-independent access to  $C_i, S_i$ .
- Including  $K_L\pi\pi$  in addition to  $K_S\pi\pi$  significantly increases statistics at small systematic cost.
- With CLEO-c 818/pb of data, replace  $4^\circ-9^\circ$  model error on  $\gamma$  from  $B^\pm \rightarrow D(K_S\pi\pi)K^\pm$  with a statistical error:

$$\sigma_{\text{CLEO-input}}(\gamma) \sim 1^\circ-2^\circ \quad \text{CLEO-c preliminary, 818/pb}$$

- Significant reduction in systematics at BaBar/BELLE
- Crucial for LHCb and LHCb-Upgrade, Super-B.

# Results

**First  
determination  
with 281 pb<sup>-1</sup>**

PRL 100, 221801 (2008)  
PRD 78, 012001 (2008)

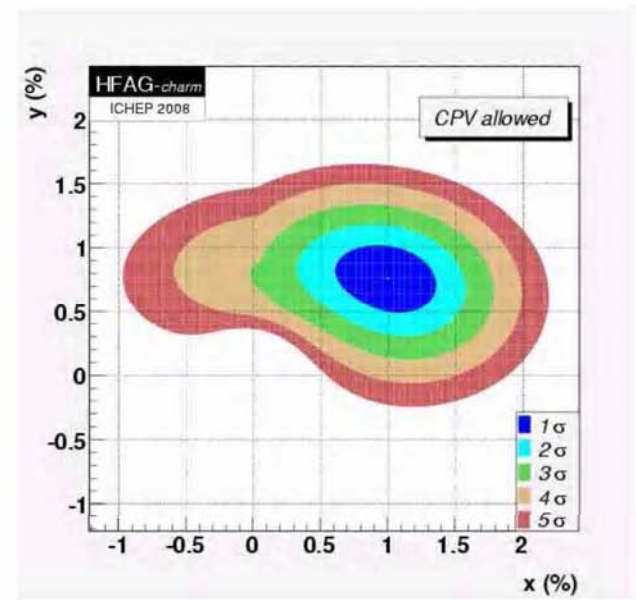
Parameter	Standard Fit	Extended Fit
$y$ ( $10^{-3}$ )	$-45 \pm 59 \pm 15$	$6.5 \pm 0.2 \pm 2.1$
$r^2$ ( $10^{-3}$ )	$8.0 \pm 6.8 \pm 1.9$	$3.44 \pm 0.01 \pm 0.09$
$\cos \delta$	$1.03 \pm 0.19 \pm 0.06$	$1.10 \pm 0.35 \pm 0.07$
$x^2$ ( $10^{-3}$ )	$-1.5 \pm 3.6 \pm 4.2$	$0.06 \pm 0.01 \pm 0.05$
$x \sin \delta$ ( $10^{-3}$ )	0 (fixed)	$4.4 \pm 2.4 \pm 2.9$
$\chi^2_{\text{fit}}/\text{ndof}$	30.1/46	55.3/57

- Standard fit result important component in average of charm mixing
- Extended fit leads to measurement of:

$$\delta = \left( 22^{+11+9}_{-12-11} \right)^\circ$$

From likelihood scan of physically allowed region

- Future improvements:
  - Full  $\psi(3770)$  data set – 818 pb<sup>-1</sup>
  - WS semileptonics vs.  $K\pi$
  - Additional  $K_L^0$  modes
  - C-even information from 4170 MeV data





# Multi-body ADS

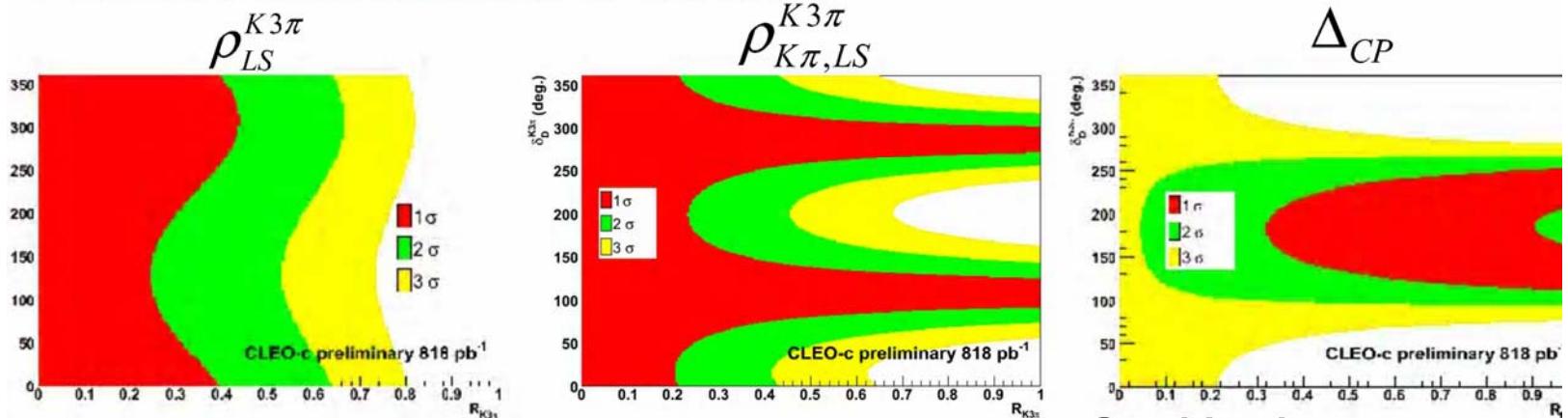
Mode	Branching Ratio
$K\pi$	3.89%
$K\pi\pi^0$	13.9%
$K3\pi$	8.1%

- $B \rightarrow D(K\pi\pi\pi)K$  and  $B \rightarrow D(K\pi\pi^0)K$  can also be used for ADS analyses
  - Significantly larger branching fractions than  $B \rightarrow D(K\pi)K$
- However, need to account for the resonant substructure
  - In principle each point in the phase space has a different strong phase associated with it
- Atwood and Soni [PRD **68** 033003 (2003)] showed how to modify the usual ADS equations for this case
  - Introduce **coherence parameter**  $R_{K3\pi}$  which dilutes interference term sensitive to  $\gamma$

$$\Gamma(B^- \rightarrow (K^+ \pi^- \pi^- \pi^+)_D K^-) \propto r_B^2 + (r_D^{K3\pi})^2 + 2r_B r_D^{K3\pi} R_{K3\pi} \cos(\delta_B + \delta_D^{K3\pi} - \gamma)$$

- $R_{K3\pi}$  ranges from
  - 1=coherent (dominated by a single mode) to
  - 0=incoherent (several significant components)

# $K3\pi$ likelihood scans



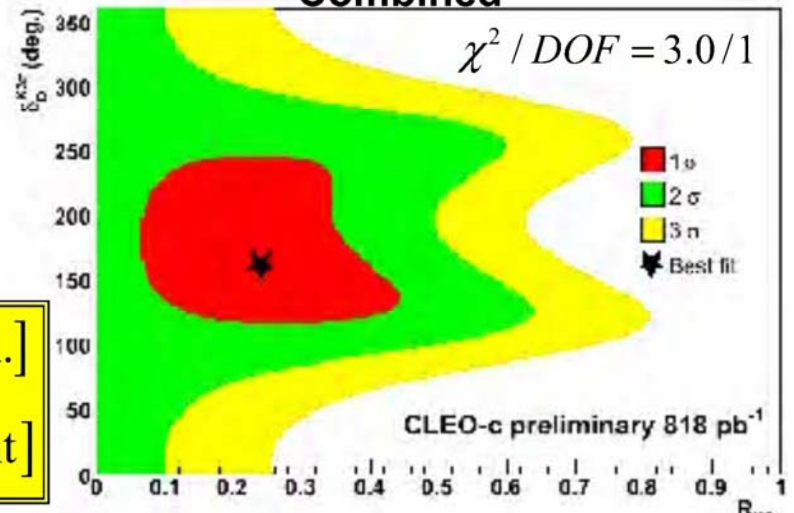
- Fit to observables and external constraints on D mixing parameters and branching fractions
  - Correlations included
- 2D likelihood shows regions R and  $\delta$  space

Preliminary

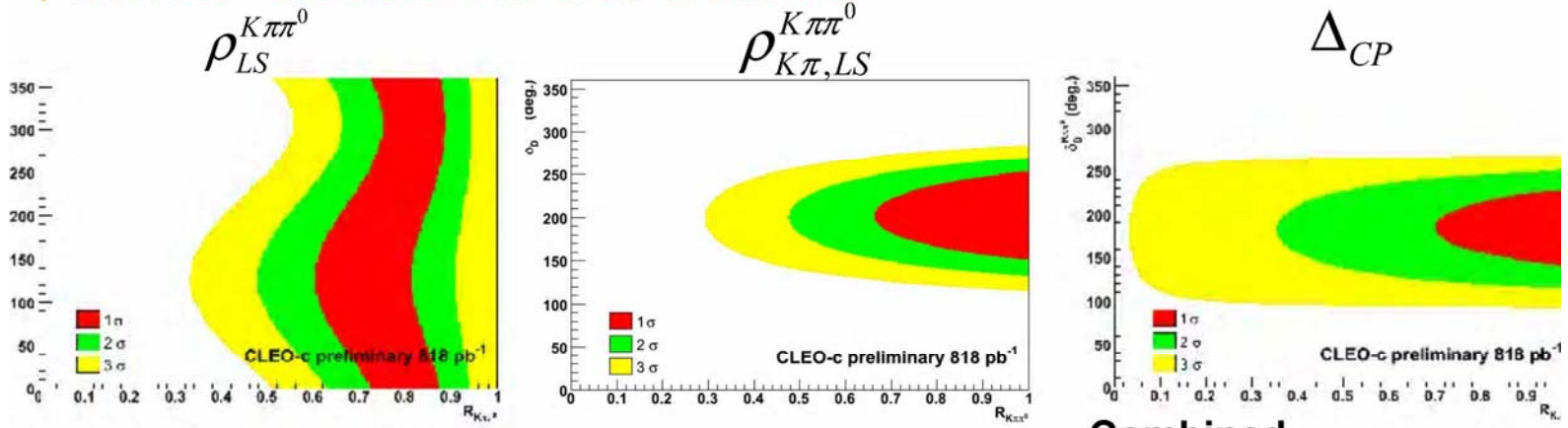
$$R_{K3\pi} = 0.24^{+0.21}_{-0.17} \quad [R_{K3\pi} < 0.57 \text{ at } 95\% \text{ c.l.}]$$

$$\delta_D^{K3\pi} = (161^{+85}_{-48})^\circ \quad [\text{No } 95\% \text{ c.l. constraint}]$$

Combined



# $K\pi\pi^0$ likelihood scans



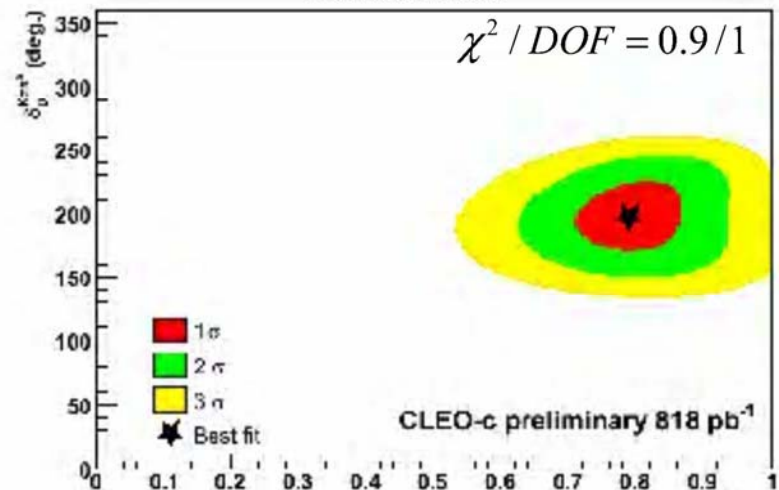
Preliminary

$$R_{K\pi\pi^0} = 0.79 \pm 0.08$$

$$\delta_D^{K\pi\pi^0} = \left(197^{+28}_{-27}\right)^\circ$$

**Coherence observed!**

Combined



# LHCb Global Sensitivity to $\gamma$

With  $B \rightarrow DK$  methods perform global fit of common parameters. In addition consider results from  $B^0$  and  $B_s$  time dependent analyses. (LHCb-2008-031)

Input measurements considered:

$B^- \rightarrow D^0 K^-$ :

- $D^0 \rightarrow K\pi, KK, \pi\pi$  (LHCb-2008-011)
- $D^0 \rightarrow K\pi\pi\pi$  (LHCb-2007-004)
- $D^0 \rightarrow K_S \pi\pi$  (LHCb-2007-048)

$B^0 \rightarrow D^0 K^{*0}$

- $D^0 \rightarrow K\pi, KK, \pi\pi$  (LHCb-2007-050)

Time dependent measurements:

- $B^0 \rightarrow D\pi$  (LHCb-2007-044)
- $B_s \rightarrow D_s K$  (LHCb-2007-041)

Summary of event yields in  $2 \text{ fb}^{-1}$

Channel	Signal	Background
$B^\pm \rightarrow D(K^\pm \pi^\mp) K^\pm$	56k	35k
$B^+ \rightarrow D(K^- \pi^+) K^+$	680	780
$B^- \rightarrow D(K^+ \pi^-) K^-$	400	780
$B^+ \rightarrow D(K^+ K^- + \pi^+ \pi^-) K^+$	3.3k	7.2k
$B^- \rightarrow D(K^+ K^- + \pi^+ \pi^-) K^-$	4.4k	7.2k
$B^\pm \rightarrow D(K^\pm \pi^\mp \pi^\pm \pi^\mp) K^\pm$	61k	40k
$B^+ \rightarrow D(K^- \pi^+ \pi^+ \pi^-) K^+$	470	1.2k
$B^- \rightarrow D(K^+ \pi^- \pi^+ \pi^-) K^-$	350	1.2k
$B^0 \rightarrow D(K^+ \pi^-) K^{*0}, \bar{B}^0 \rightarrow D(K^- \pi^+) \bar{K}^{*0}$	3.4k	1.7k
$B^0 \rightarrow D(K^- \pi^+) K^{*0}$	350	850
$B^0 \rightarrow D(K^+ \pi^-) \bar{K}^{*0}$	230	850
$B^0 \rightarrow D(K^+ K^- + \pi^+ \pi^-) K^{*0}$	150	500
$\bar{B}^0 \rightarrow D(K^+ K^- + \pi^+ \pi^-) \bar{K}^{*0}$	550	500
$B^\pm \rightarrow D(K_S^0 \pi^\pm \pi^\mp) K^\pm$	5k	4.7k
$B_s, \bar{B}_s \rightarrow D_s^\mp K^\pm$	6.2k	4.3k
$B^0, \bar{B}^0 \rightarrow D^\mp \pi^\pm$	1,300k	290k

# Sensitivity to $\gamma$ including all measurement

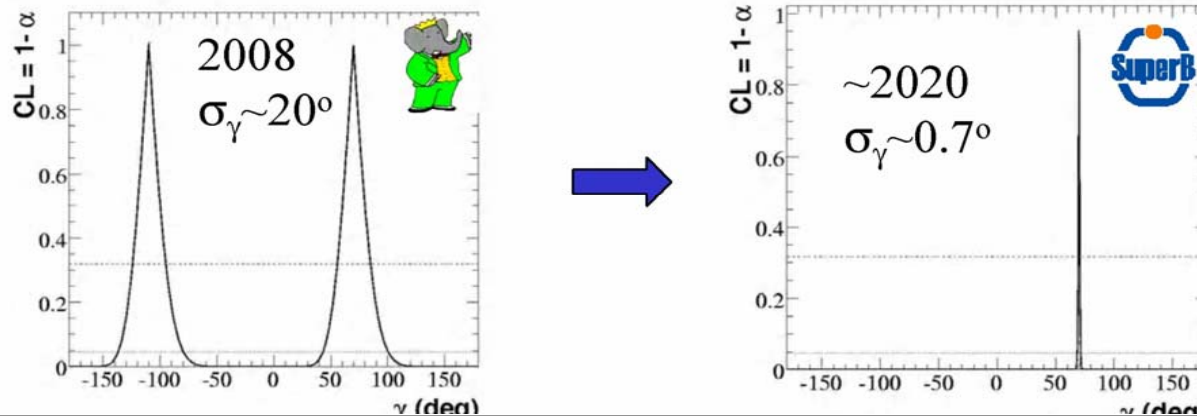
Results shown as function of  $\delta_{B^0}$ , least well known parameter. Sensitivity of  $B^0 \rightarrow D^0 K^{*0}$  improves by factor of two in going from  $\delta_{B^0} = 45 \rightarrow 180^\circ$ . Residual dependence remains in global fit, but diluted due to other measurements.

$\delta_{B^0}$ ( $^\circ$ )	0	45	90	135	180
$\sigma_\gamma$ for $0.5 \text{ fb}^{-1}$ ( $^\circ$ )	8.1	10.1	9.3	9.5	7.8
$\sigma_\gamma$ for $2 \text{ fb}^{-1}$ ( $^\circ$ )	4.1	5.1	4.8	5.1	3.9
$\sigma_\gamma$ for $10 \text{ fb}^{-1}$ ( $^\circ$ )	2.0	2.7	2.4	2.6	1.9

Weight (in %) of each contributing analysis with  $2 \text{ fb}^{-1}$  for two values of  $\delta_{B^0}$ :

Analysis	$\delta_{B^0} = 0^\circ$	$\delta_{B^0} = 45^\circ$
$B^- \rightarrow D^0(hh)K^-, B^- \rightarrow D^0(K^\pm \pi^\mp \pi^+ \pi^-)K^-$	25	38
$B^- \rightarrow D^0(K_S^0 \pi^+ \pi^-)K^-$	12	25
$B^0 \rightarrow D^0(hh)K^{*0}$	44	8
$B_s \rightarrow D_s^\mp K^\pm$	16	24
$B^0 \rightarrow D^\mp \pi^\pm$	3	5

- Measurement of  $\gamma$  at the B Factories was unexpected
  - $r_B$  ratios confirmed to be  $\sim 0.1$  (and  $>0$ )  $\Rightarrow$  reliable predictions
  - $\delta\gamma \sim 20^\circ$  now, largely dominated by  $B^+ \rightarrow D^{(*)}K^{(*)+}$  Dalitz
  - $\delta\gamma \sim 10^\circ$  after final analyses and combinations of current B Factories
- SSF can reach  $\delta\gamma \sim 1^\circ$  and below with:
  - **Combination of charged modes:**  $B^+ \rightarrow D^{(*)}K^{(*)+}$ . Self-tagging neutral modes, e.g.  $B^0 \rightarrow D^{(*)}K^{(*)0}$ , may help
  - **Combination of methods:** Dalitz, GLW, ADS
  - Use of **correlated data** (CP tagged  $K_S\pi\pi, K_S KK$  and doubly tagged  $K_S\pi\pi, K_S KK$ )
    - SSF is a unique facility to provide large samples of correlated charm data
      - Enough with **3 months of data taking at  $\psi'$  (3770)** over a 5 years period
      - Key data also for other analyses (e.g. D-mixing and CPV in charm)
    - **Only way to reach sub degree precision**



# Instead of Conclusion

---

CKM'08 Book

Working Group V       $\Gamma(\phi^3)$  from tree decays      approx 12 pages

Recall      AIM of the book is legacy of the B-factories.

Conveners are requesting very short ( up to 1 page) write-up on the following topics from the persons listed below:

Proposed Table of Contents and contributors

INTRO, motivation etc      (T. Gershon & A. Soni)

Theoretical remarks on  $D^*V$       (R.Sinha)

BELLE recent results      (A. Bondar)

BABAR ..Recent Results      (V. Tisserand)

Gamma from fits      (V. Sordini & K. Trabelsi)

CLEO-c inputs for gamma      (J. Libby and J. Rademacker)

LHCb Outlook for gamma ( $\phi^3$ )      (G. Wilkinson)

Prospects for gamma from SuperKEKB      (P.Krokovny)

Prospects for gamma from SuperFlavorFactory      (F. Martinez-Vidal)

Total ~ 10 pages

Deadline Oct. 15 th PLEASE SEND to us

---