

**Measurement of specific number of
muon-induced neutron using
Large Volume Detector**

Measurement of the cosmogenic neutron seasonal variations with LVD

LVD collaboration

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Winter

Summer

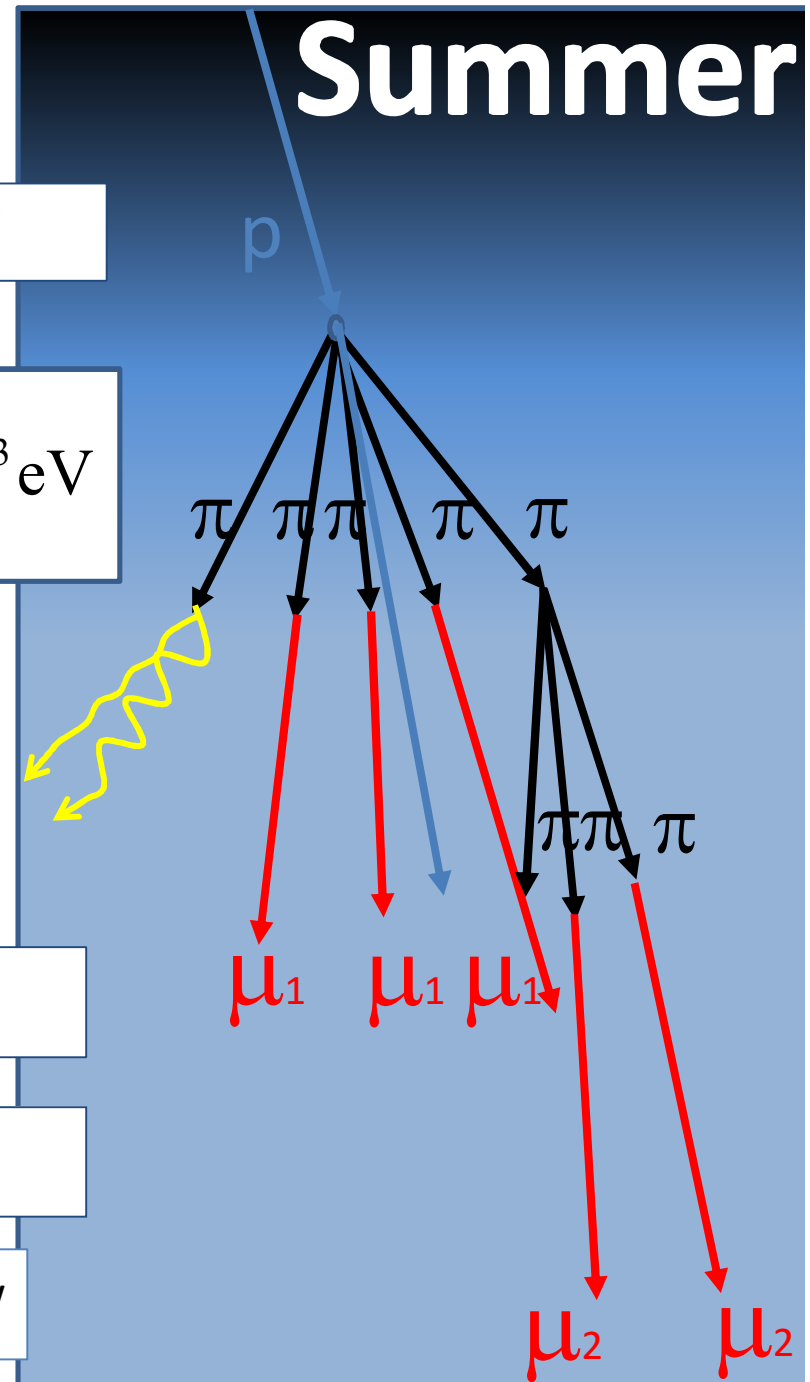
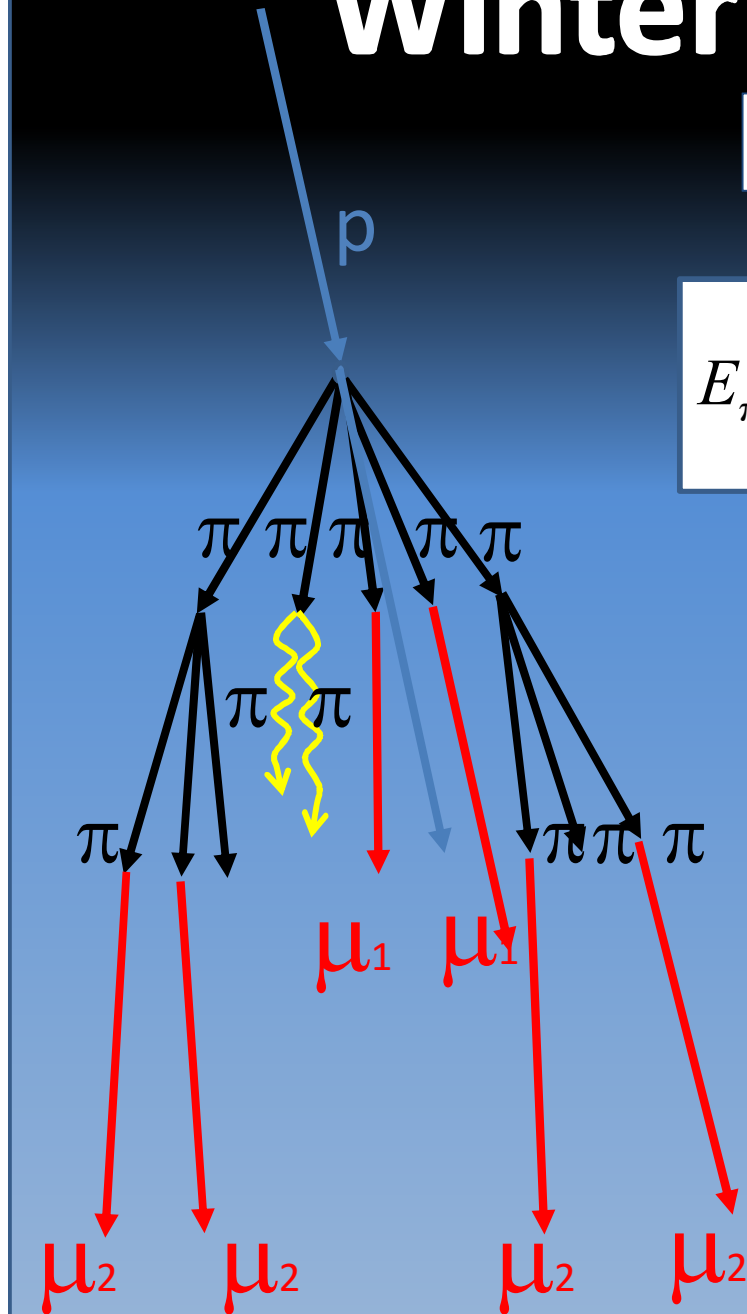
$$E_p \sim 10^{14} \text{ eV}$$

$$E_\pi \approx \frac{1}{10} E_p \approx 10^{13} \text{ eV}$$

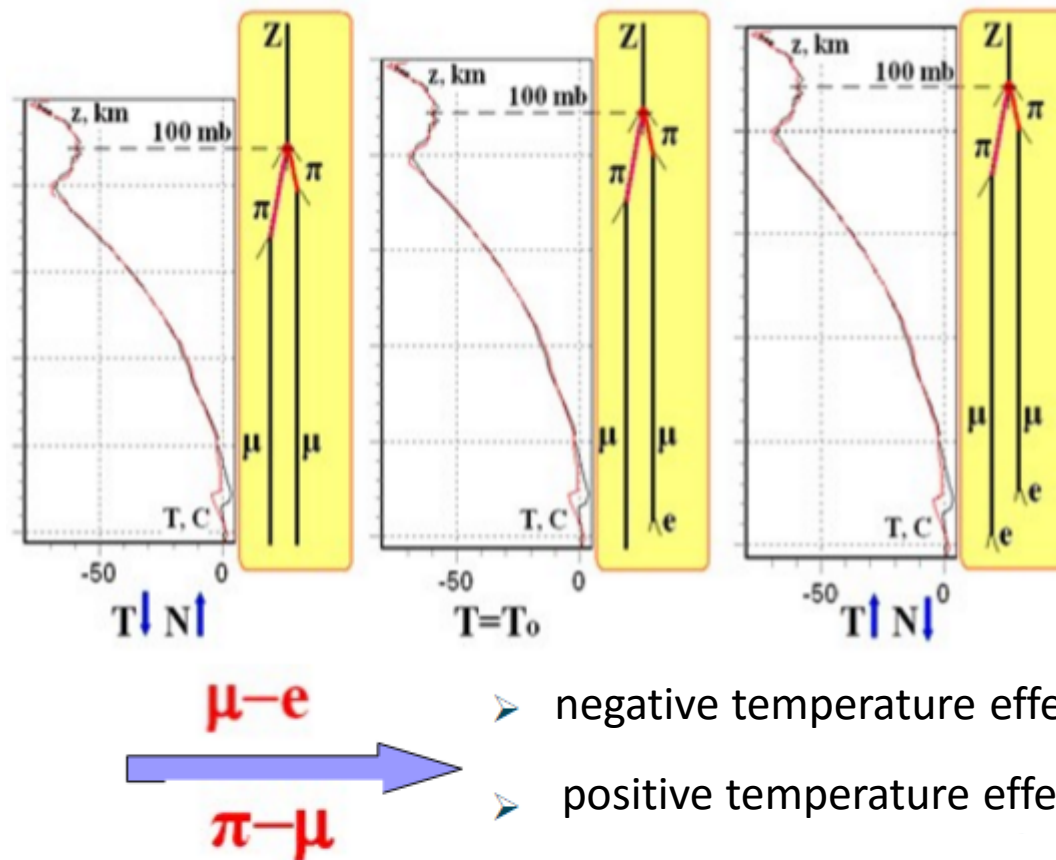
$$I_{\mu_1}^S > I_{\mu_1}^W$$

$$I_{\mu_2}^S < I_{\mu_2}^W$$

$$E_{(\mu)}^S > E_{(\mu)}^W$$



Temperature effect

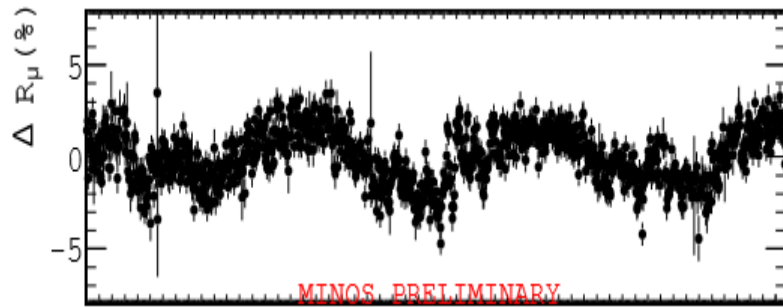


The temperature effect of the muon component is caused by a competition between decay of π/κ and μ and their interaction with the atmospheric nuclei due to the change of geometric atmosphere dimensions.

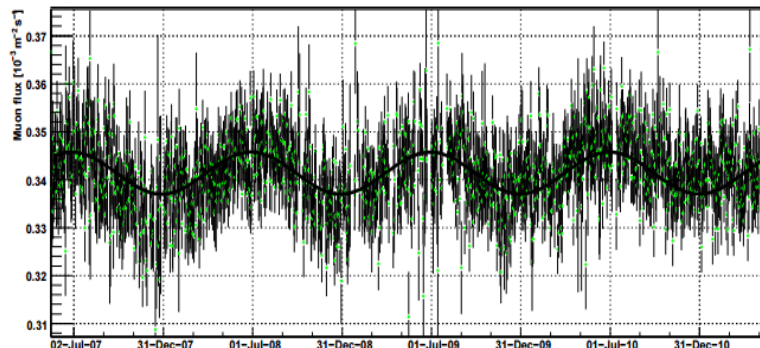
With atmosphere heating and its consequent expansion the number of π/κ decays is increasing and this results in positive temperature effect. Simultaneously with the atmosphere expansion the μ path to the detector is increasing what results in the negative temperature effect as μ decay becomes more possible.

The set of the available muon intensity variation measurements:

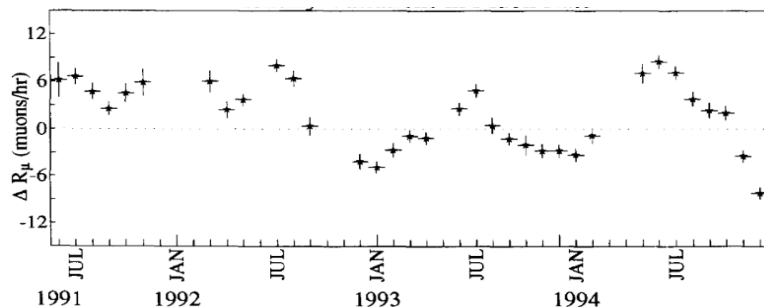
1. MACRO (1991 - 1994)
2. AMANDA (225 days 1997)
3. MINOS (1096 days)
4. LVD (2001 - 2008)
5. BOREXINO (2007 - 2011)
6. IceCube (18 month 2007-2008)



MINOS (E.W. GRASHORN for Minos coll., Observation of Seasonal Variations with the MINOS Far Detector, 30ICRC, arXiv:0710.1616)

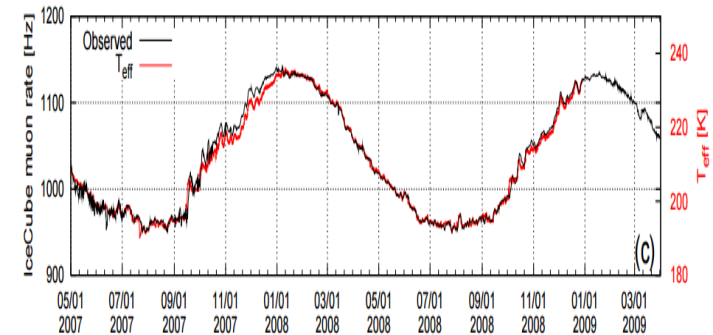


Borexino (Davide D'Angelo for Borexino coll. Seasonal modulation in the Borexino cosmic muon signal, arXiv:1109.3901)

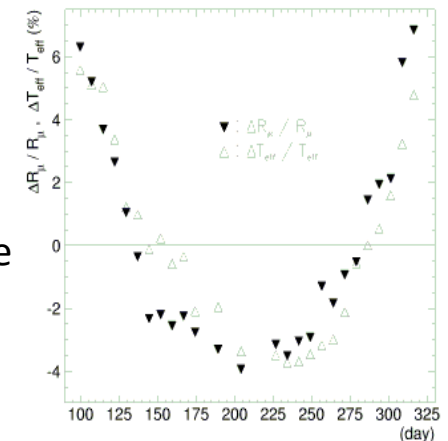


MACRO Coll (M. Ambrosio, Seasonal variations in the underground muon intensity as seen by MACRO, Astroparticle Physics, 7 (1997) 109-124)

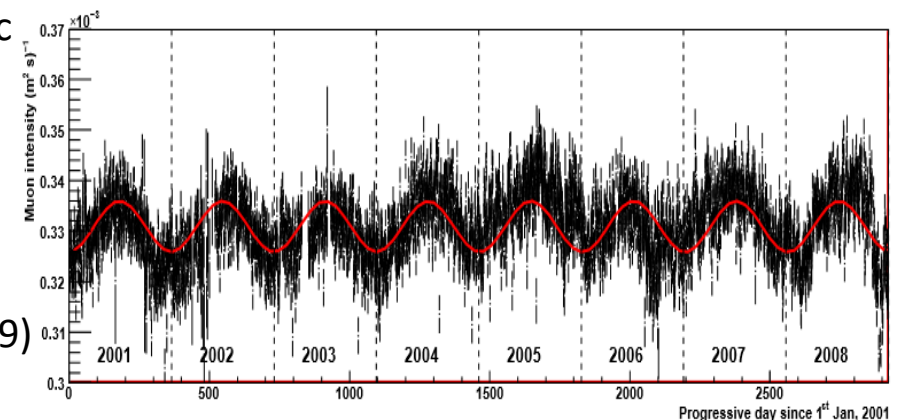
IceCube (Serap Tilav for IceCube coll., Atmospheric Variations as observed by IceCube, arXiv:1001.0776)



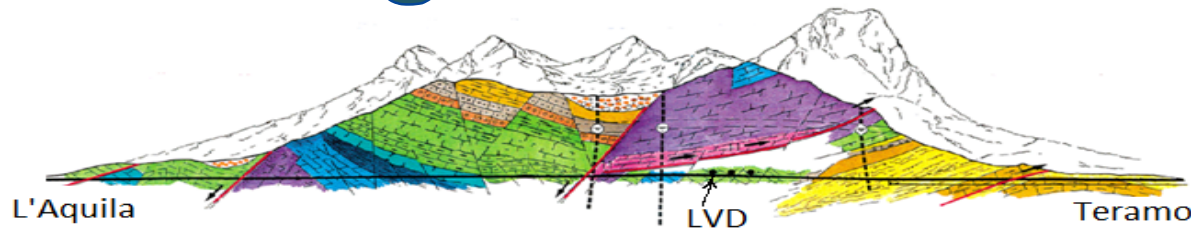
AMANDA Coll. (A. Bouchta for Amanda coll., Seasonal variation of the muon flux seen by Amanda, 26 ICRC, 1999)



LVD (M. Selvi for LVD Coll., Analysis of the seasonal modulation of the cosmic muon flux in the LVD detector during 2001-2008, 31 ICRC, 2009)



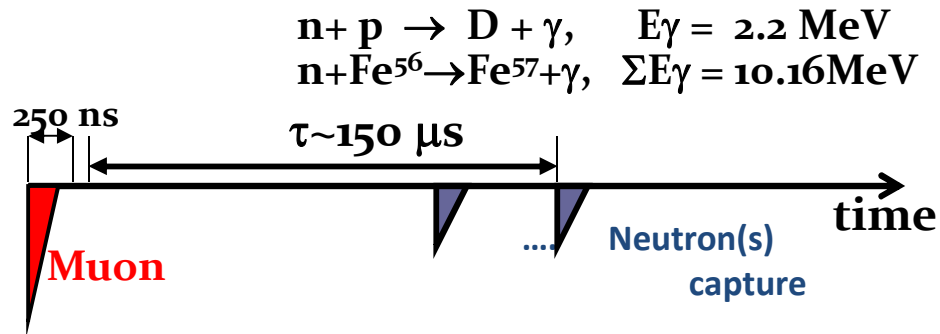
Large Volume detector LVD



Length × Width × Height	22.7 × 13.2 × 10 m
Iron mass	1020 τ
Scintillator mass	1008 τ
Amount of scintillation counters	840
Number of PMTs	2520
Average depth minimal	3620 m w.e. 3000 m w.e.
Mean muon energy	280 GeV
E_{μ} on see level (min.)	1.3 TeV
Muon rate (on 1 tower)	~ 120 h ⁻¹
Threshold ε_{th}	5MeV

The main goal: **detection of neutrinos from the collapse of stellar cores**

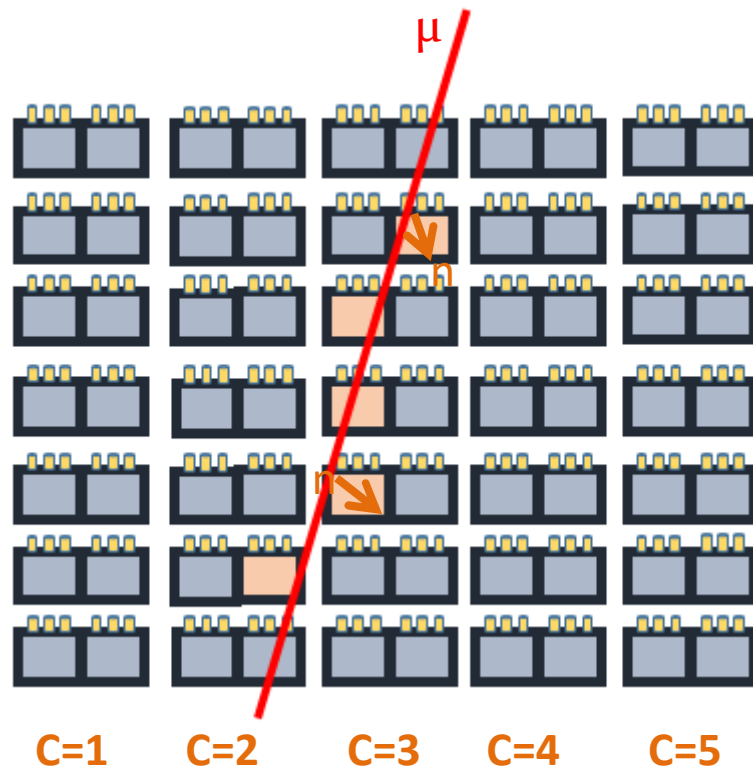
Muon selection and neutron detection:



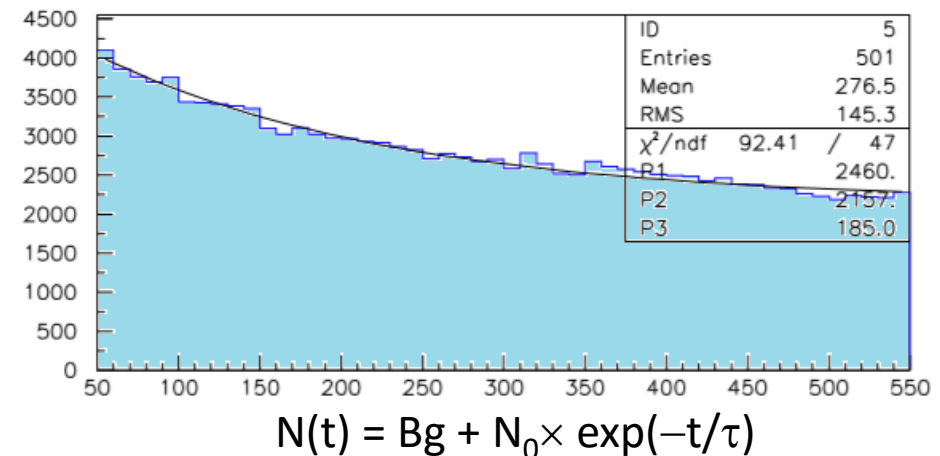
An event is selected as

'muon event' if there are at least 2 distinct counters with $E_{\text{tr}} > 10 \text{ MeV}$ and time difference $\Delta t < 250 \text{ ns}$.

We have selected from muon events the inner counter triggers having energy $E_{\text{tr}} > 50 \text{ MeV}$.



- Neutron searching for in the same counter where muon trigger is produced ($E_{\text{tr}} > 50 \text{ MeV}$);
- Energy of gamma pulses: 1 – 12 MeV;
- Time window: 50 – 550 microseconds

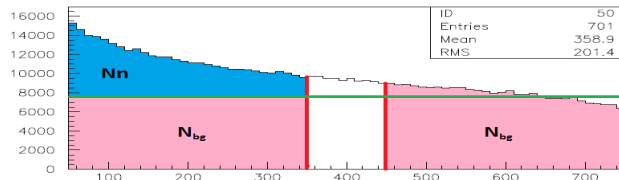


Methods of the N_n/N_{tr} determination :

Specific number of muon-induced neutron is the determined number of neutrons divided by number of triggers in the same counter.

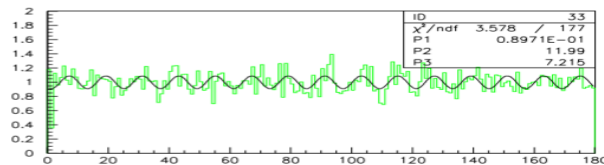
Epoch folding method

Background determination



$$N_n = N_{tot} - N_{bg}$$

N_n/N_{tr} (during 180 months)

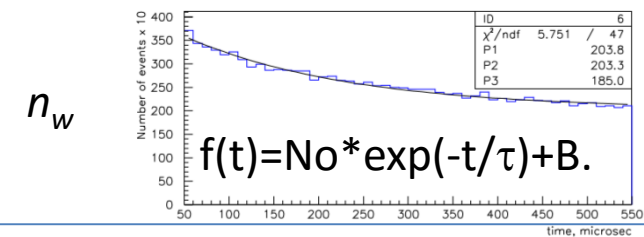


$$F(t) = 1 + \delta \cdot \cos(2\pi(t - \varphi)/T)$$

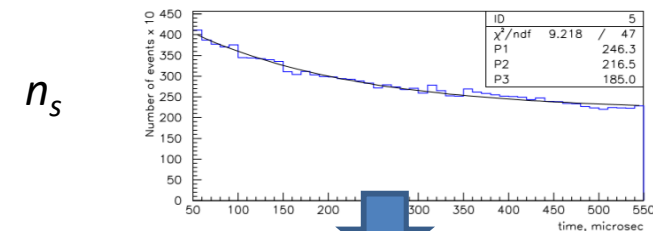
Residual method

«summer» - «winter»

Winter: 3 mon. x 15 year = 45 months

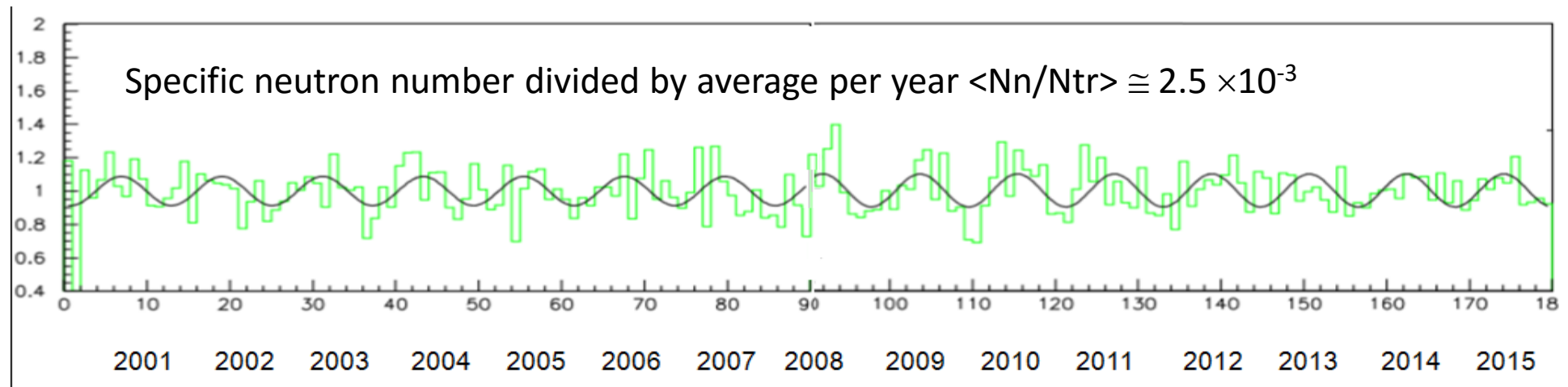
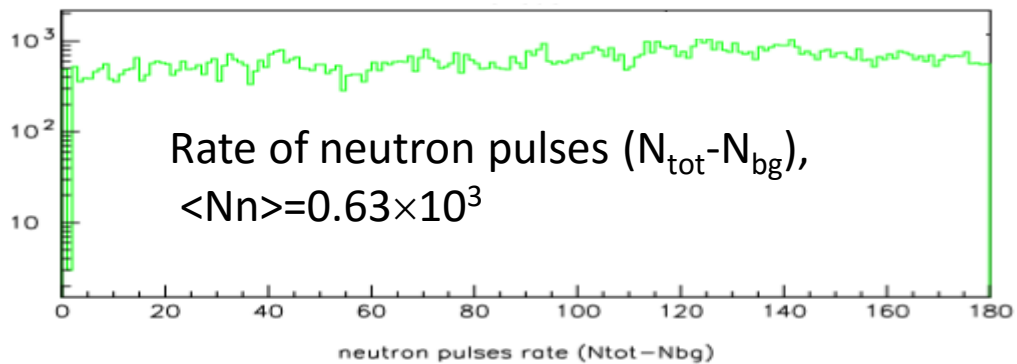
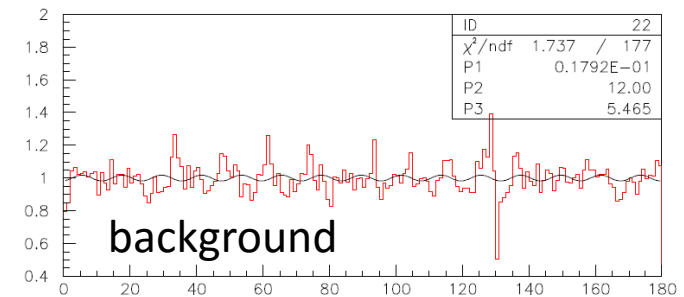
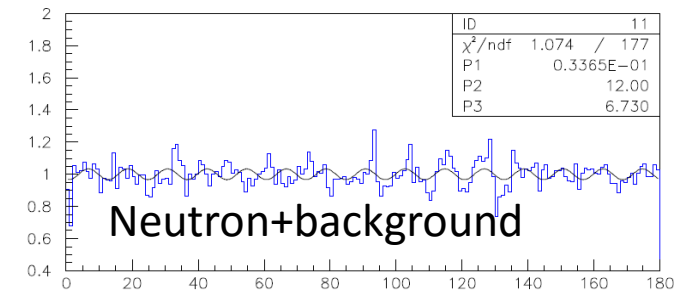
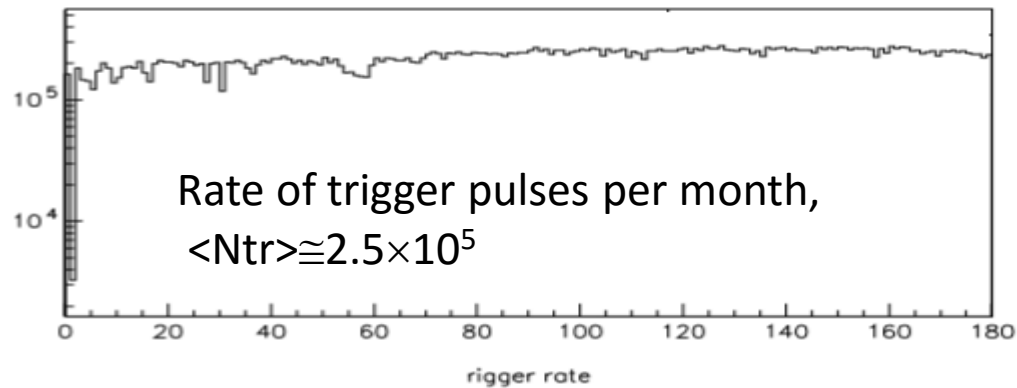


Summer: 3 mon. x 15 year = 45 months

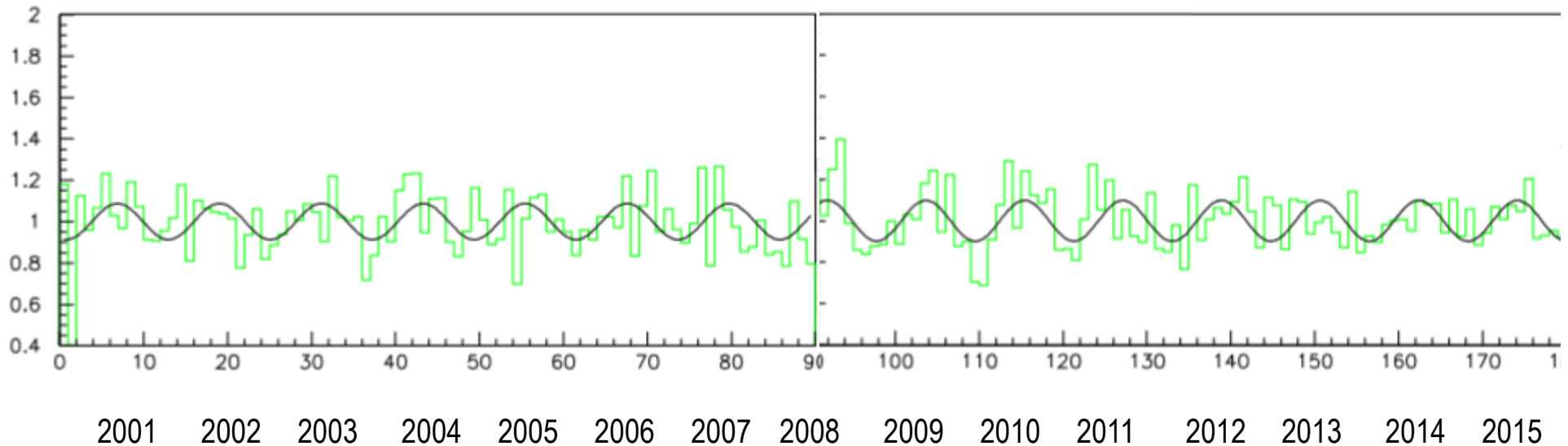


$$\delta = (n_w - n_s) / (n_w + n_s)$$

Specific neutron number N_n/N_{tr}



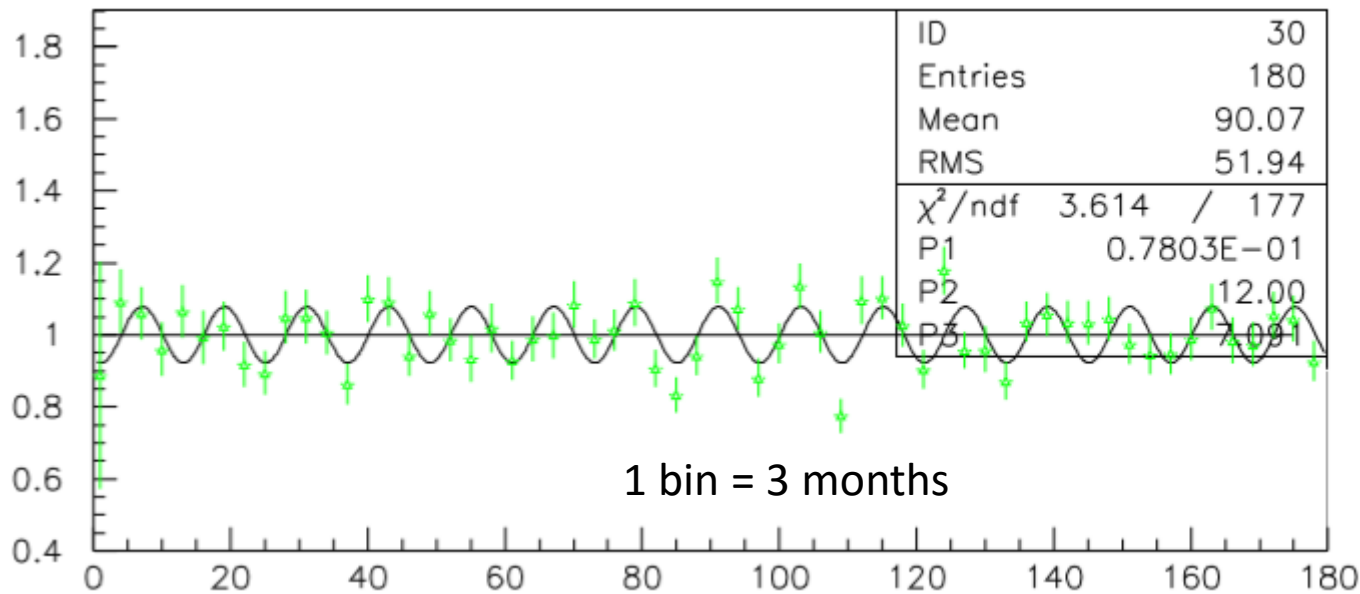
Epoch folding method



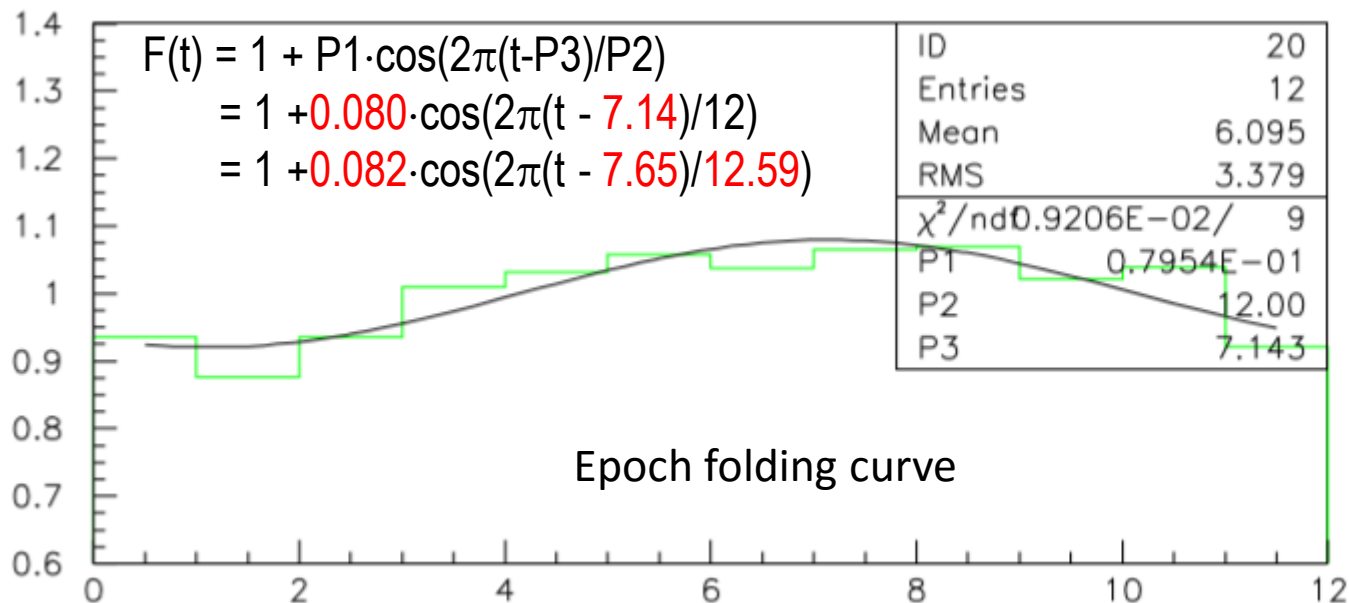
We analyzed the whole available data set with the detector in its final configuration (T1+T2+T3), starting in 1 January 2001 and ending in 31 December 2015.

$$\delta \equiv \delta \left(\frac{N_n}{N_{tr}} \right) \propto \delta N_n \left(\overline{E}_\mu \right)$$

Epoch folding method



Here the T value is fixed: T=12 month.
If all three parameters are fitted:
T=11.99,
f=7.153,
 $\delta=0.078$



Here the T value is fixed: T=12 month.
If all three parameters are fitted:
T=12.59,
f=7.165,
 $\delta=0.082$

$$\delta N_n = 0.08 \pm 0.02$$

Residual method

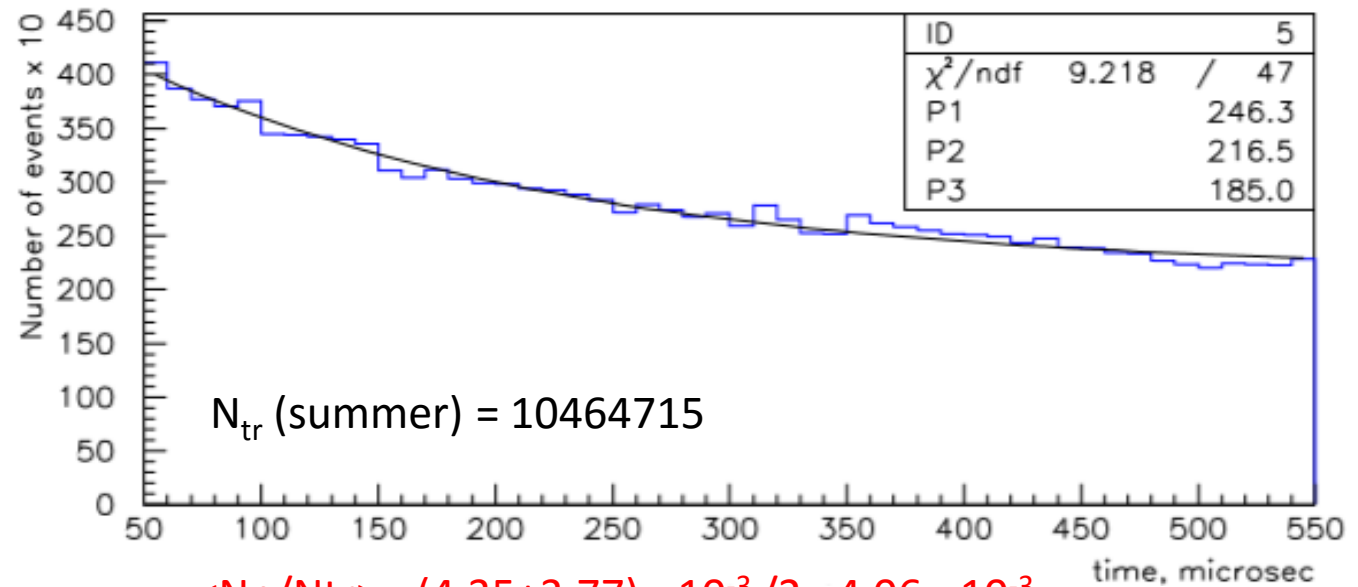
$$N_n/N_{tr}(s) = 246.3 \times 185 / 10464715 = 4.35 \times 10^{-3};$$

$$N_n/N_{tr}(w) = 203.8 \times 185 / 10006669 = 3.77 \times 10^{-3};$$

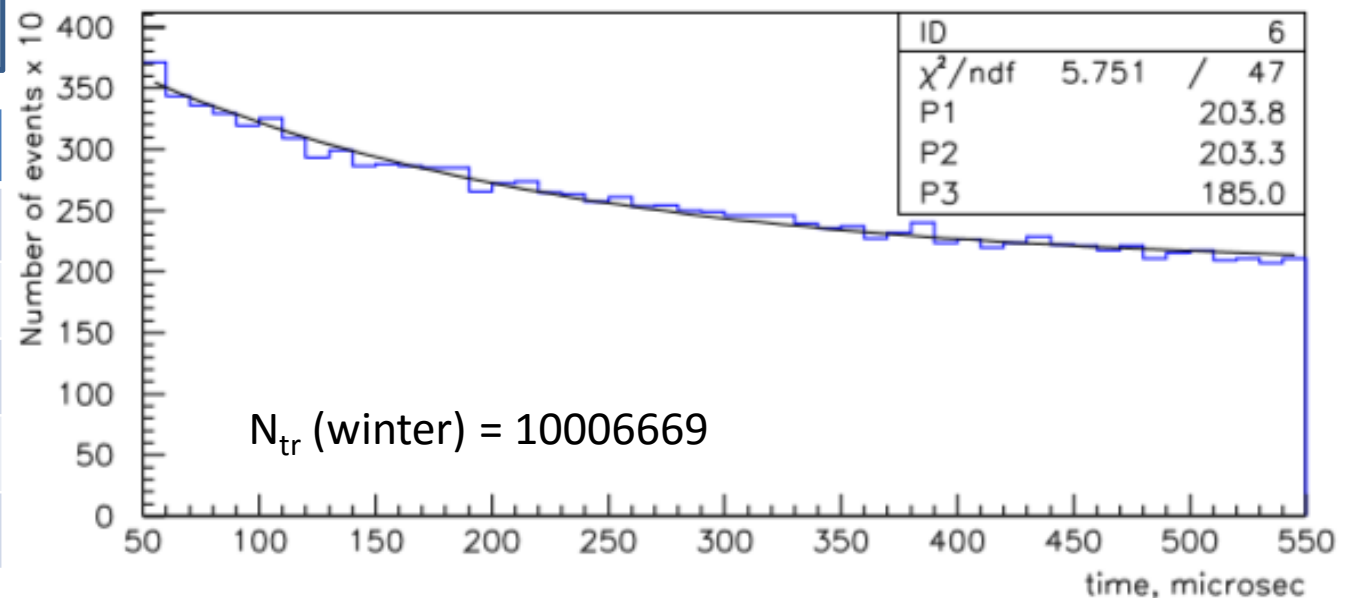
$$\delta N_n = (s-w)/(s+w) = (N_n/N_{tr}(s) - N_n/N_{tr}(w)) / (N_n/N_{tr}(s) + N_n/N_{tr}(w))$$

$$\delta N_n = 0.072 \pm 0.002 \pm 0.008$$

E_{th} , MeV	δ
0.7	0.073
1.0	0.072
1.5	0.072
2.0	0.083
3.0	0.068



$$\langle N_n/N_{tr} \rangle = (4.35 + 3.77) \times 10^{-3} / 2 = 4.06 \times 10^{-3}$$



Determination of modulation amplitude δ of the average muon energy underground:

$$\frac{N_n + \delta N}{N_n} = \left(\frac{E_\mu + \delta E}{E_\mu} \right)^{0.78}$$



$$\begin{aligned} N_n &\sim E_\mu^{0.75} && \text{for hadronic} \\ &&& \text{showers;} \\ N_n &\sim E_\mu^{0.78} && \text{for hadronic and} \\ &&& \text{electromagnetic} \\ &&& \text{showers} \end{aligned}$$

$$\frac{\delta E}{E_\mu} = \left(1 + \frac{\delta N}{N_n} \right)^{1/0.78} - 1$$

$$\frac{\delta E}{E_\mu} = (1 + 0.076)^{1/0.78} - 1 \approx 0.10$$

Changing energy muons 10% leads to a change 8% in the specific number of neutrons.

Conclusions:

- ❑ The seasonal variations of the average energy of muon flux underground has been found using number of muon induced neutrons:
- ❑ The characteristics of the muon induced neutron variations are defined using different methods
 - residual method (summer - winter): variation magnitude is $\delta N_n = 0.072 \pm 0.002 \text{ (stat)} \pm 0.016 \text{ (sys)}$;
 - epoch folding method: $f(t) = 1 + \delta \cdot \cos(2\pi(t - \varphi)/T)$,
 $\delta N_n = 0.08 \pm 0.02$, $\varphi = 7.15 \pm 0.5$
- ❑ The measured characteristics of the neutron variations indicate seasonal variations in the average energy of muons at the LVD depth of 280 GeV with an amplitude of 10%: $\bar{E}_\mu = 280 \pm 28 \text{ GeV}$.
- ❑ The neutron flux produced by muons underground undergoes seasonal variations with the amplitude $1 + \delta\Phi_n = (1 + \delta I_\mu)(1 + \delta N_n) = 1.076 \times 1.015$
 $\delta\Phi_n(I_\mu, N_n) = 9.2\%$
- ❑ It was assumed that the neutron flux is proportional to the intensity of muons with an amplitude variation of 1.5%. We have shown that the neutron flux has an amplitude of seasonal variations 6 times more, because the energy muons also varies with the amplitude of $\sim 10\%$.

Thank you!

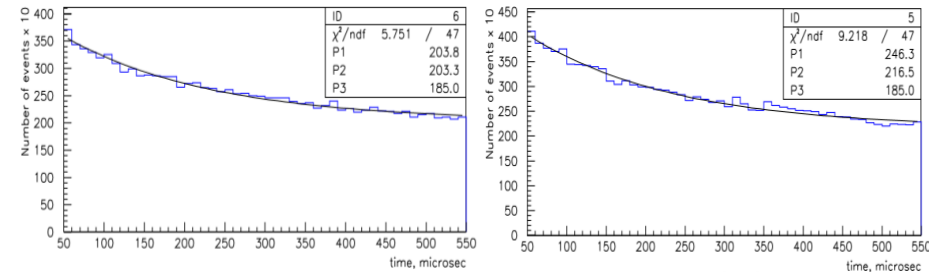
The definition uncertainties of the modulation amplitude value

□ For residual method:

Statistic uncertainty – 2.6 %

number of triggers: $N_{tr} = 1.0 \times 10^7$,

number of neutrons: $N_\gamma = 1.5 \times 10^3$,



Systematic uncertainty – 22 %

$$\delta \delta = \delta \left(\frac{n_s - n_w}{n_s + n_w} \right) \quad \delta \delta = \sqrt{\delta^2 (n_s - n_w) + \delta^2 (n_s + n_w)}$$

$$\delta^2 (n_s + n_w) = \delta^2 (n_s - n_w) = \sqrt{\delta^2 n_s + \delta^2 n_w}$$

$$n_s \approx n_w \Rightarrow \delta \delta = \sqrt{4\delta^2 n_s} \quad \delta n_s = \delta (N_0 \times \tau / N_{tr})$$

$$\delta = 0.072 \pm 0.002 \text{ (stat)} \pm 0.016 \text{ (sys)}$$



$$\delta \delta = 0.22$$

$$\sqrt{\left(\frac{35}{1263} \right)^2 + \left(\frac{20}{185} \right)^2} = 0.11$$

□ For epoch folding method:

From fitting procedure – 20.0 %

$$\delta = 0.08 \pm 0.02 \text{ (sys)}$$

Muon-induced neutron yield Y_{sc} and Y_{Fe} using value of the specific neutron number:

$$Y_n \sim \frac{N_n}{N_\mu} \frac{1}{\rho l_i} \frac{q_i(\eta_{sc}, \eta_{Fe})}{\epsilon_1 \epsilon_2}$$

4.06×10^{-3}

$Y_{sc},$ $n/\mu/(g/cm^2)$	$Y_{Fe},$ $n/\mu/(g/cm^2)$
3.24×10^{-4}	16.3×10^{-4}

$$\rho l_{sc} = 65 \text{ g/cm}^2,$$

$$\rho l_{Fe} = 59 \text{ g/cm}^2,$$

$$q_{sc}(E_{th} > 1.5 \text{ MeV}) = 1.084$$

$$q_{Fe}(E_{th} > 1.5 \text{ MeV}) = 4.940$$

$$\epsilon_1 = 0.24 \text{ (geom.factor),}$$

$$\epsilon_2 = 0.87 \text{ (tay-Bruno effect)}$$

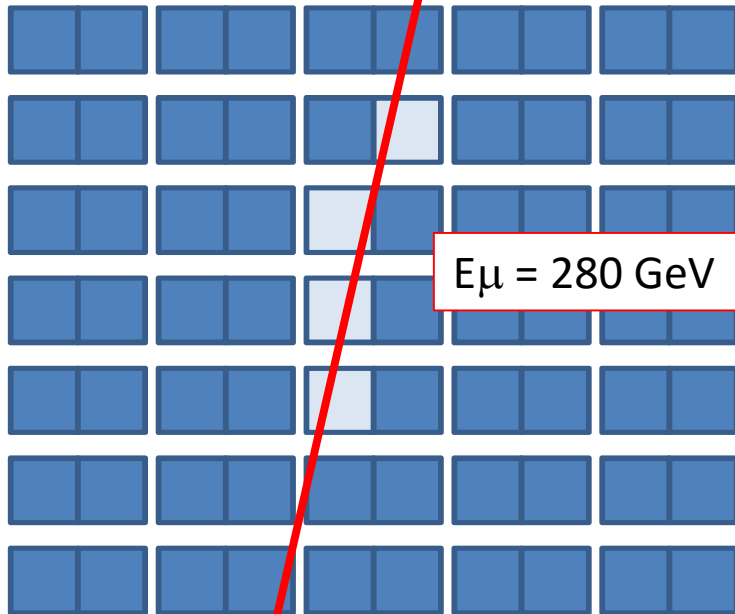
$$\eta_{sc} = 0.33$$

$$\eta_{Fe} = 0.13$$

$$q_{sc} = \frac{Q}{Q\eta_{sc} + (1-Q)\eta_{Fe}},$$

$$q_{Fe} = \frac{(1-Q)}{Q\eta_{sc} + (1-Q)\eta_{Fe}} \quad Q = 0.18$$

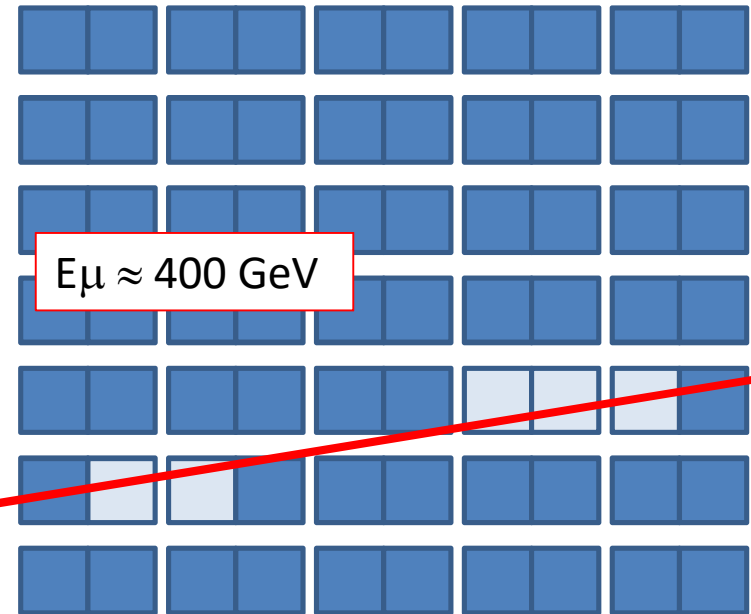
Quasi-Vertical Muons
E_{tr}>100 MeV



E_μ = 280 GeV

muons	2428151
neutrons	9858
length	65 g/sm ²
Y _{sc, n/μ/(g/sm²)}	3,2×10 ⁻⁴

Quasi-horizontal muons
E_{tr}>100 MeV, level L=±1



E_μ ≈ 400 GeV

muons	11510
neutrons	71
length	75,6 g/sm ²
Y _{sc, n/μ/(s/sm²)}	4,3×10 ⁻⁴

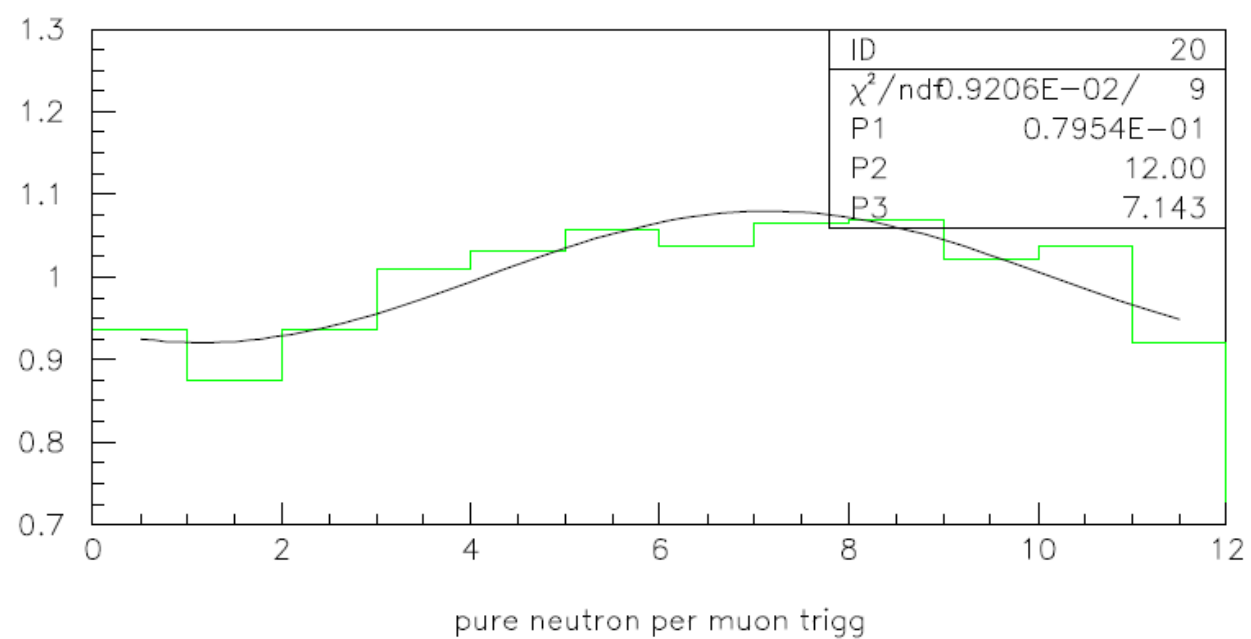
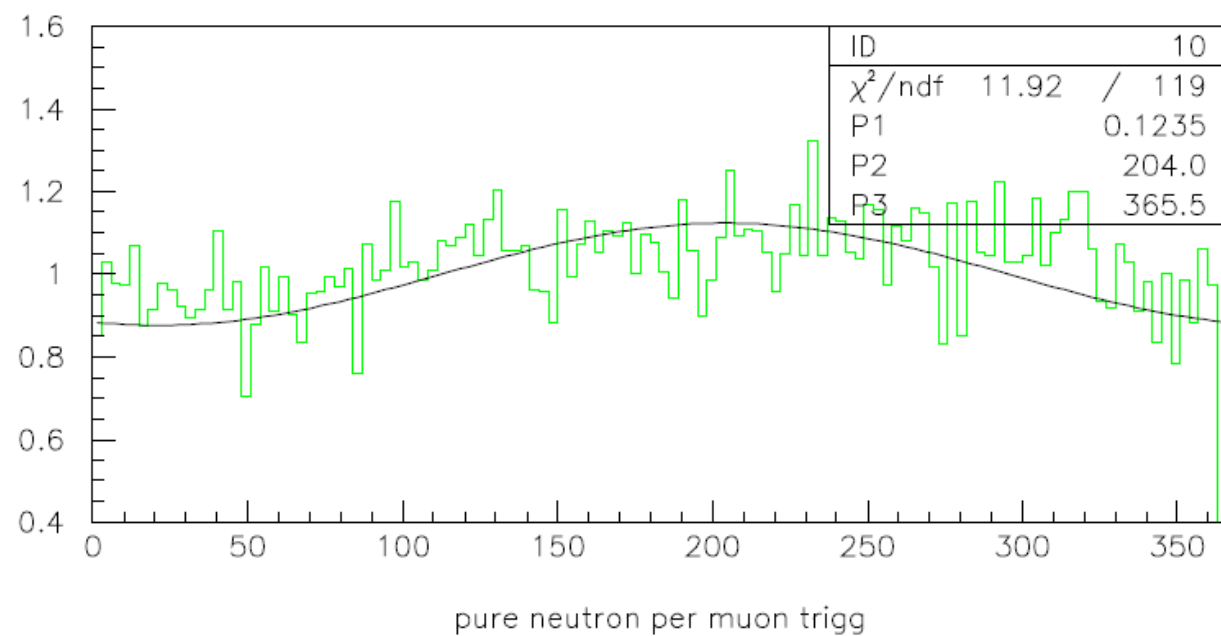
$$\frac{N_n + \delta N}{N_n} = \frac{4.3 \cdot 10^{-3} - 3.24 \cdot 10^{-3}}{3.24 \cdot 10^{-3}} = 0.33$$

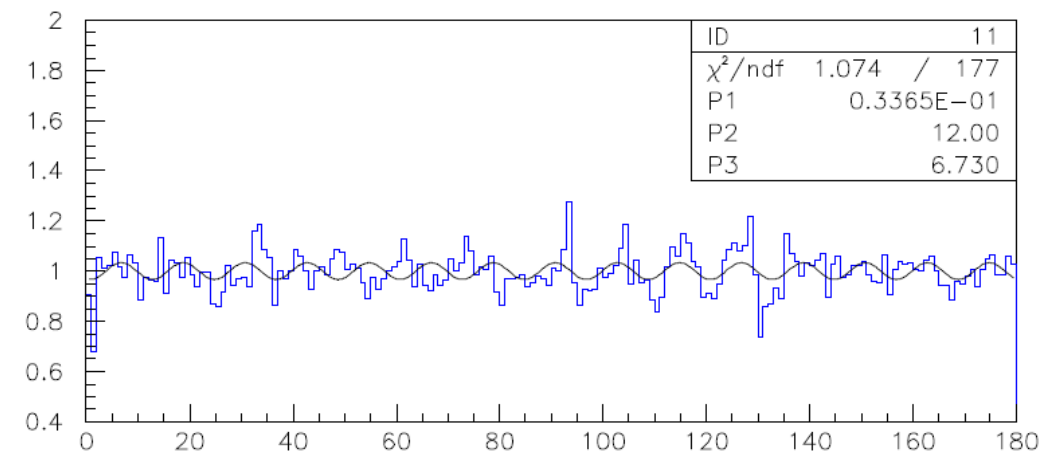
$$\frac{N_n + \delta N}{N_n} \sim \left(\frac{E_\mu + \delta E}{E_\mu} \right)^{0.78} \Rightarrow \frac{\delta E}{E} = (1 + 0.33)^{1/0.78} - 1 = 0.44$$



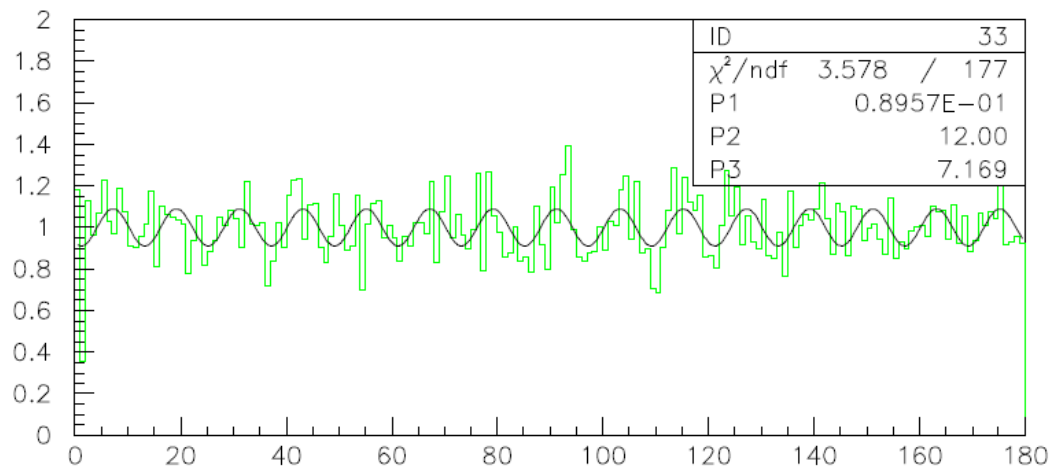
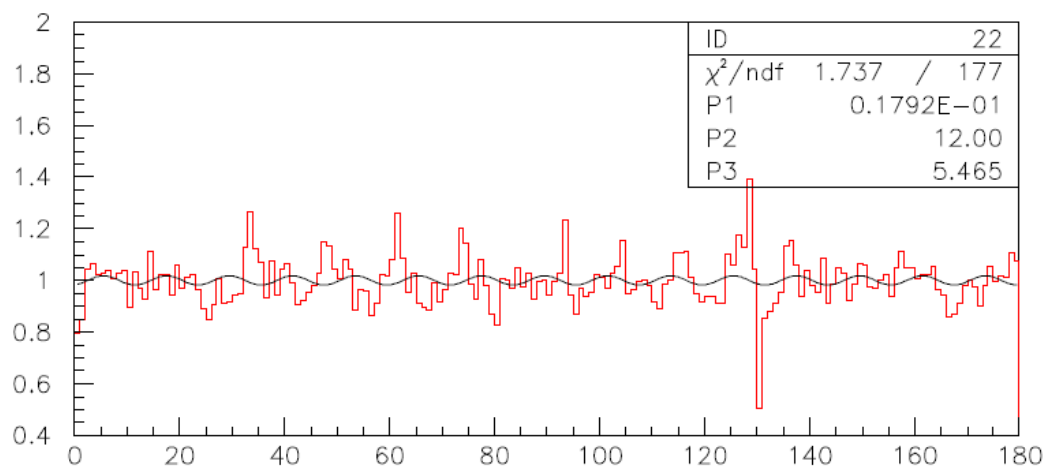
$$280 \text{ GeV} + 280 \times 0.44 \approx 400 \text{ GeV}$$

Backup slides

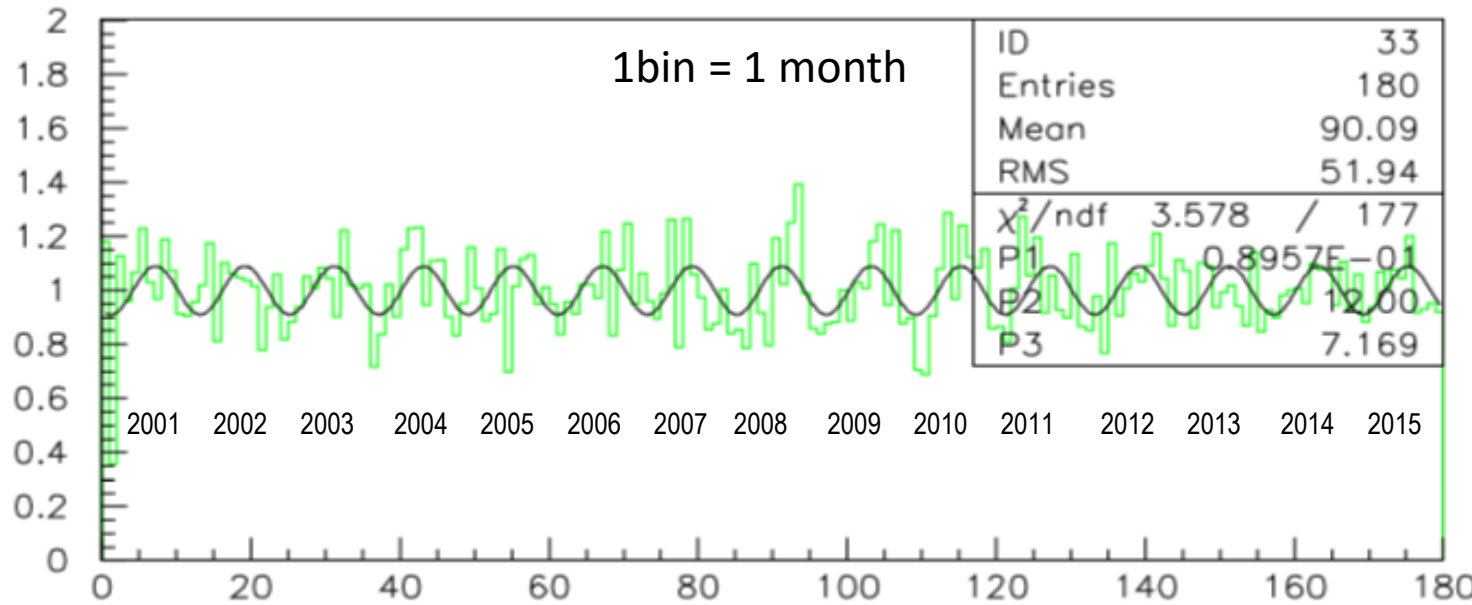




$$F(t)=1+\textcolor{red}{P1}\cdot\cos(2\pi(t-\textcolor{red}{P3})/12.0)$$

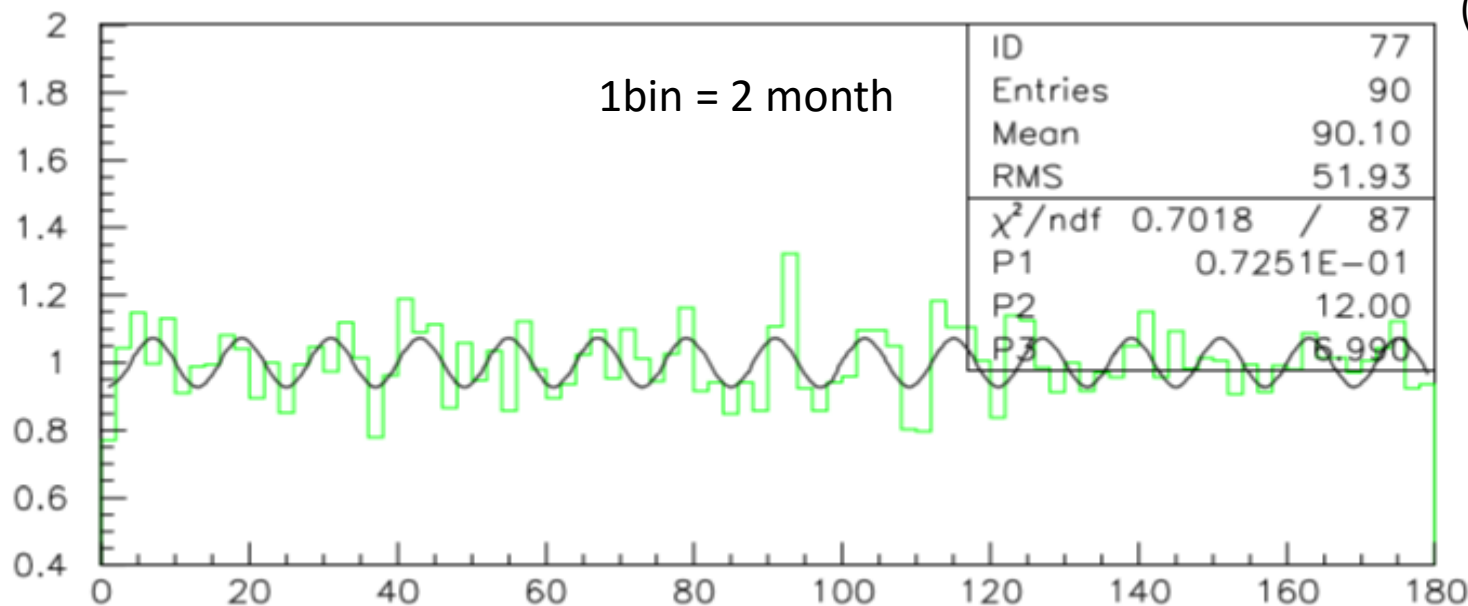


Epoch folding method



To determine the variation phase we use the fitt:

$F(t) = 1 + P1 \cdot \cos(2\pi(t - P3)/P2)$
 $P1 = 0.09 \pm 0.02$ – modulation value,
 $P2 = 12.0 \pm 0.5$ – period,
 $P3 = 7.2 \pm 0.5$ – phase (month),

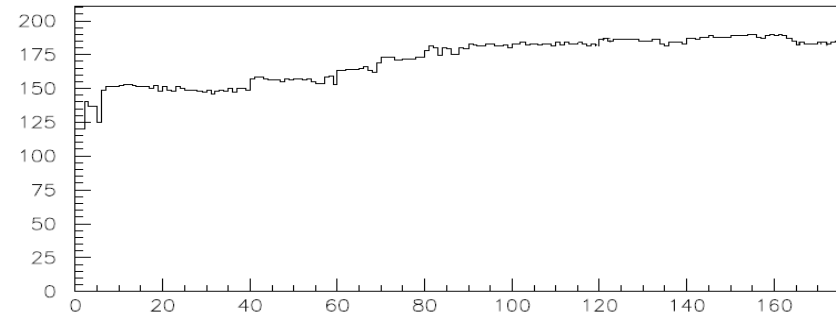


Muon events selection:

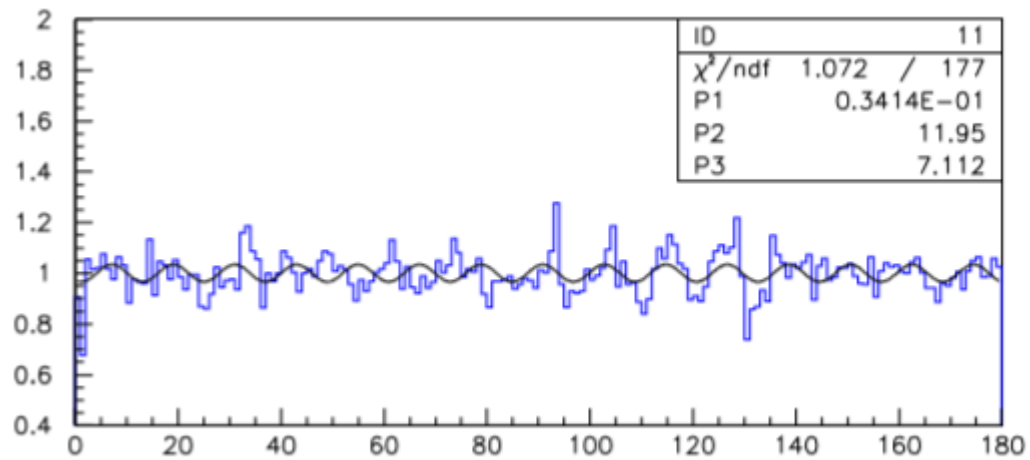
An event is selected as 'muon event' if there are at least 2 distinct counters with $E_{\text{tr}} > 10$ MeV and time difference $\Delta t < 250$ ns.

We have selected from muon events the inner counter triggers having energy $E_{\text{tr}} > 50$ MeV.

We analyzed the whole available data set with the detector in its final configuration (T1+T2+T3), starting in 1 January 2001 and ending in 31 December 2015.

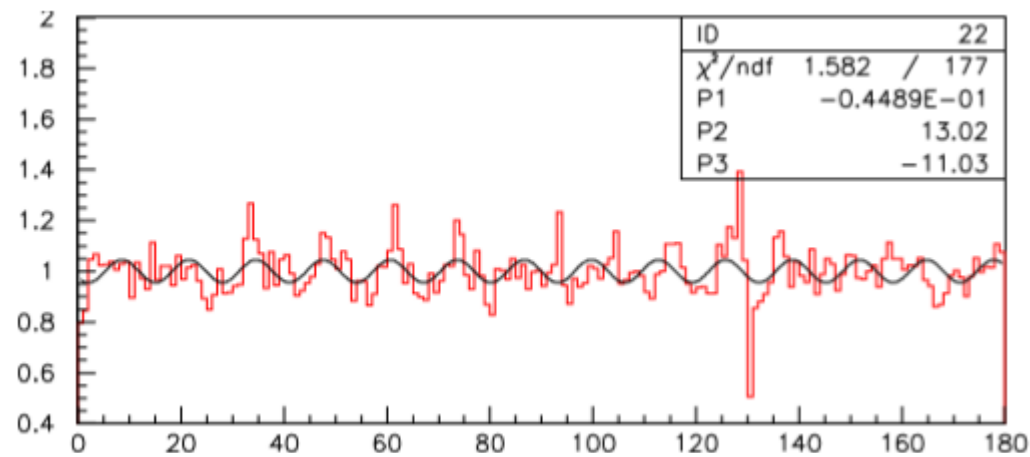


Amount of counters using in analysis (T1+T2+T3)

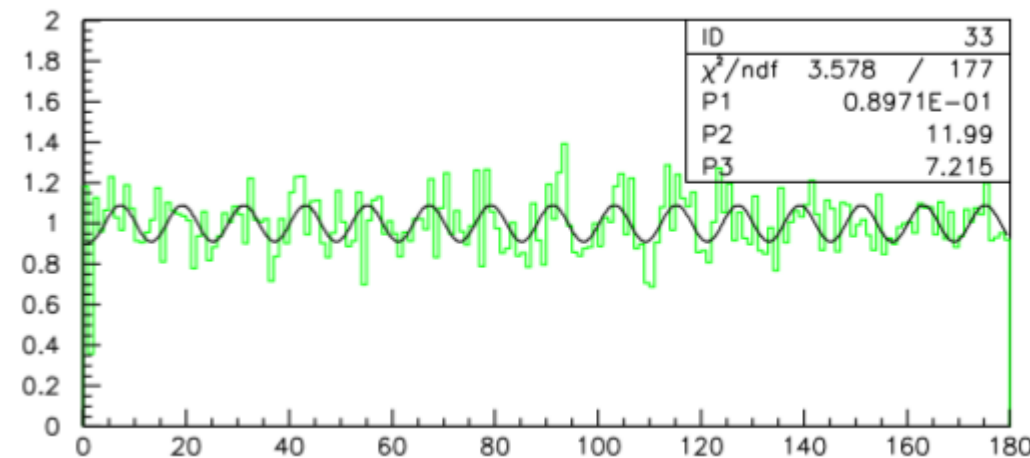


$$F(t) = 1 + P1 \cdot \cos(2\pi(t - P3)/P2)$$

$N_{\text{tot}}/N_{\text{tr}}$ per month
 $\langle N_{\text{tot}}/N_{\text{tr}} \rangle \cong 8.5 \times 10^{-3}$



$N_{\text{bg}}/N_{\text{tr}}$ per month
 $\langle N_{\text{bg}}/N_{\text{tr}} \rangle \cong 6 \times 10^{-3}$



N_n/N_{tr} per month
 $\langle N_n/N_{\text{tr}} \rangle \cong 2.5 \times 10^{-3}$

Specific number of muon-induced neutrons is the determined number of neutrons divided by number of triggers in the same counter.

The specific number is the averaged magnitude over a muon flux. Then the specific number is proportional to a number of neutrons produced by muon at mean E_μ energy of muon flux underground:

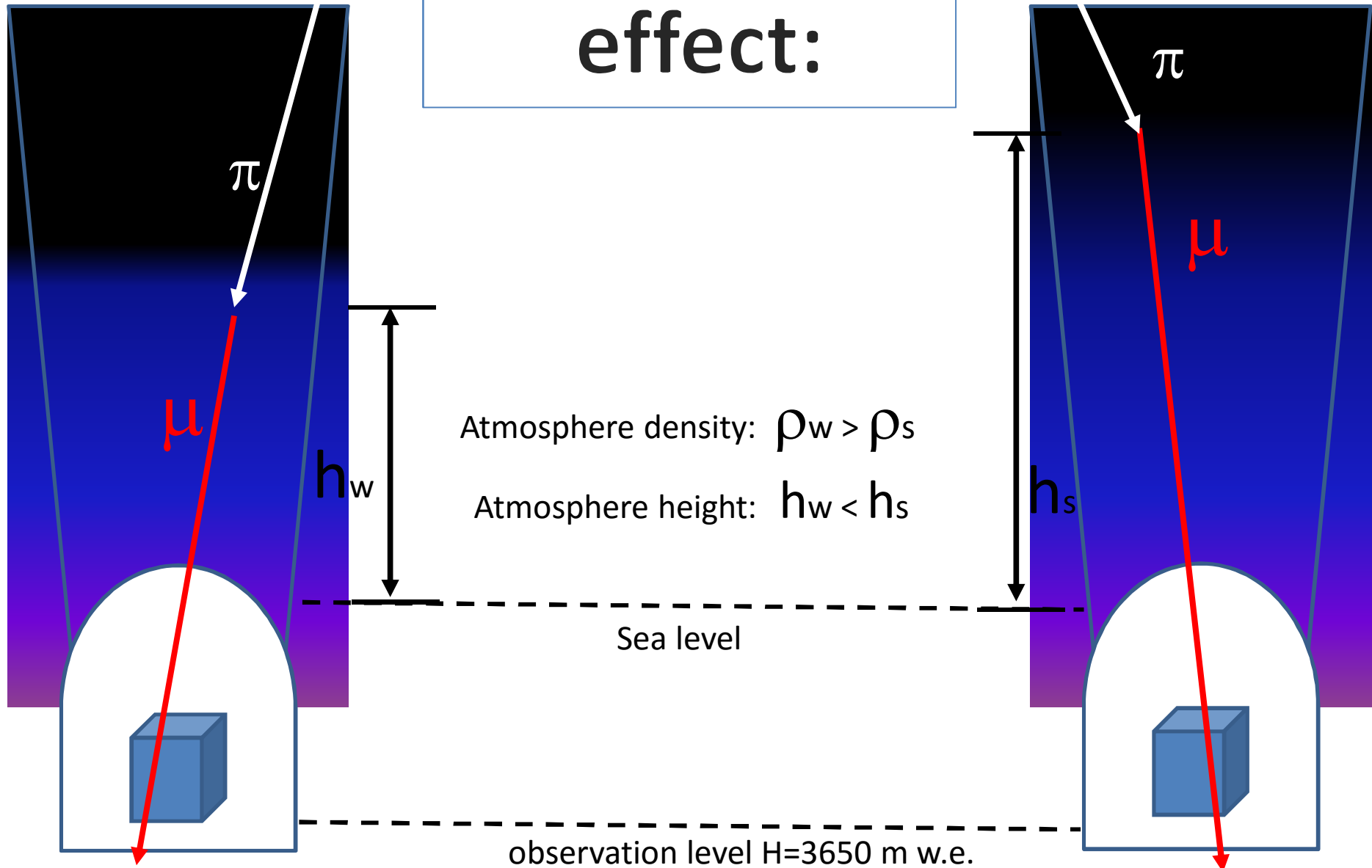
$$\frac{N_n}{N_{tr}} \propto N_n(\overline{E}_\mu)$$

$$\delta \equiv \delta \left(\frac{N_n}{N_{tr}} \right) \propto \delta N_n(\overline{E}_\mu)$$

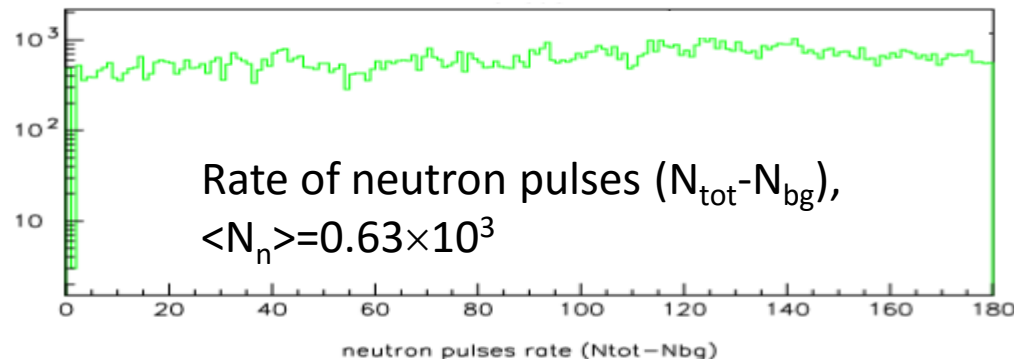
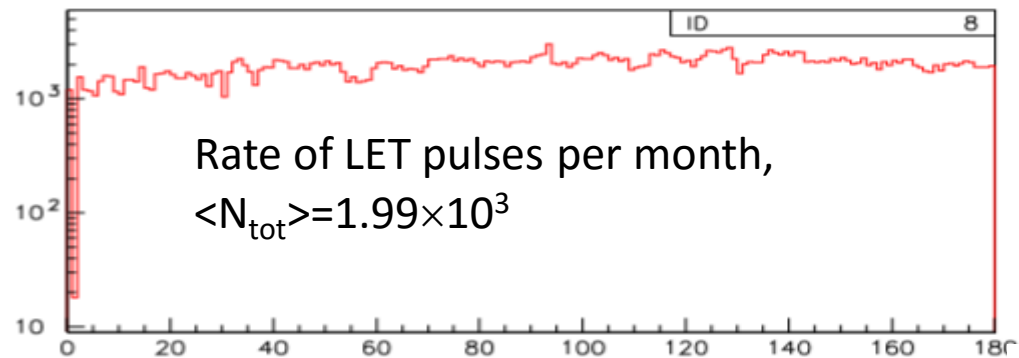
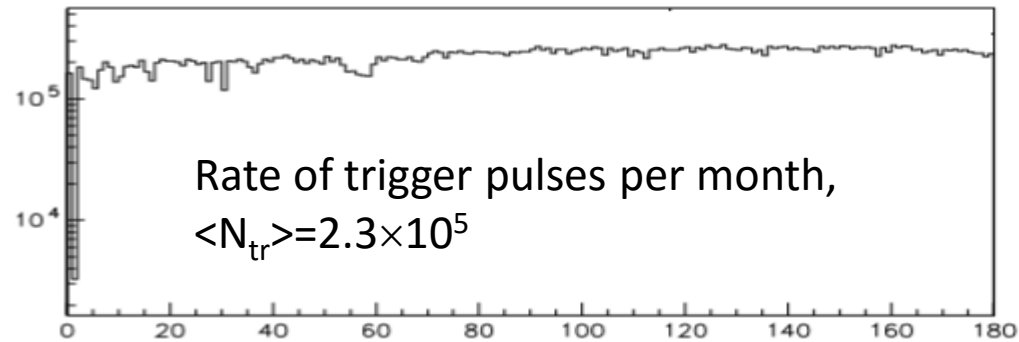
Winter

Temperature
effect:

Summer



Specific neutron number N_n/N_{tr}



$(N_{tot} - N_{bg}) / N_{tr}$ per month

