



Forbush decreases caused by expanding ICMs: analytical model and observation

Mateja Dumbović¹, Vršnak, B.¹, Čalogović J.¹, Heber, B.², Herbst, K.², Kuhl, P.², Galsdorf, D.², Veronig, A.³, Temmer, M.³, Mostl, C.³

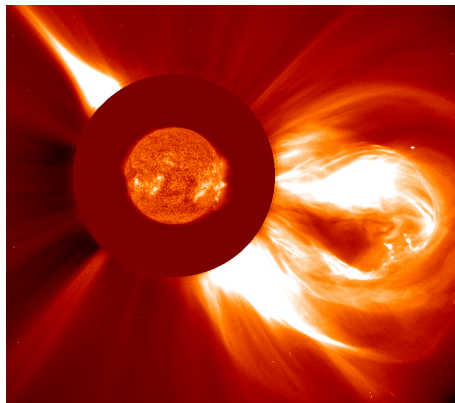
1 - Hvar Observatory, Uni. Zagreb, Croatia

2 - Institute for Extraterrestrial Physics, Uni. Kiel, Germany

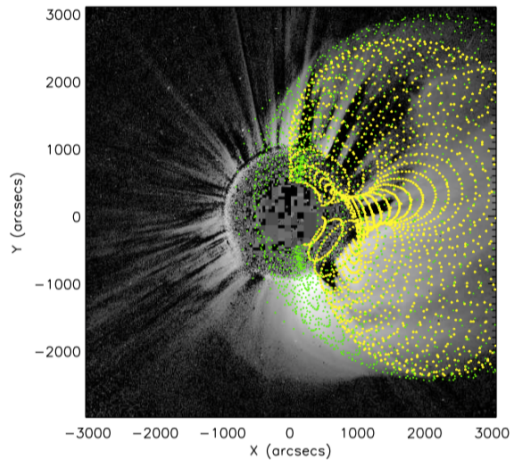
3 - IGAM, Uni. Graz, Austria

Forbush decreases caused by Interplanetary Coronal Mass Ejections (ICMEs)

REMOTE OBSERVATION

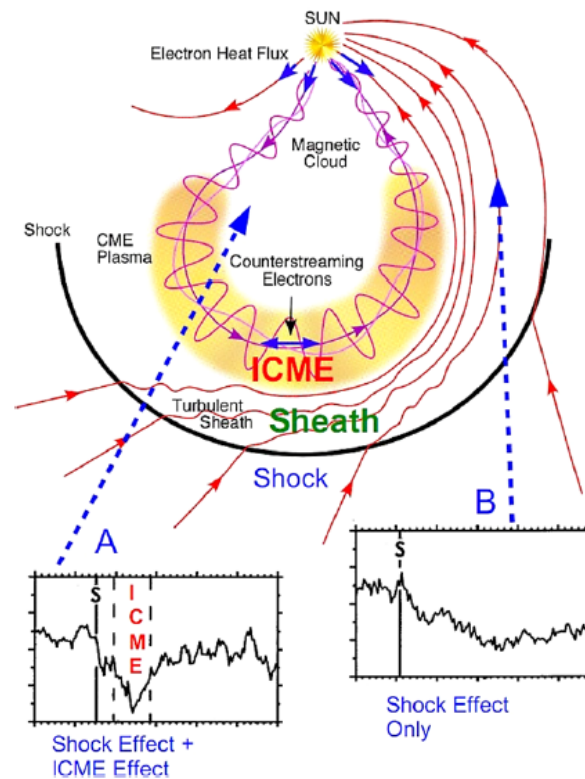


SOHO/LASCO C2 image



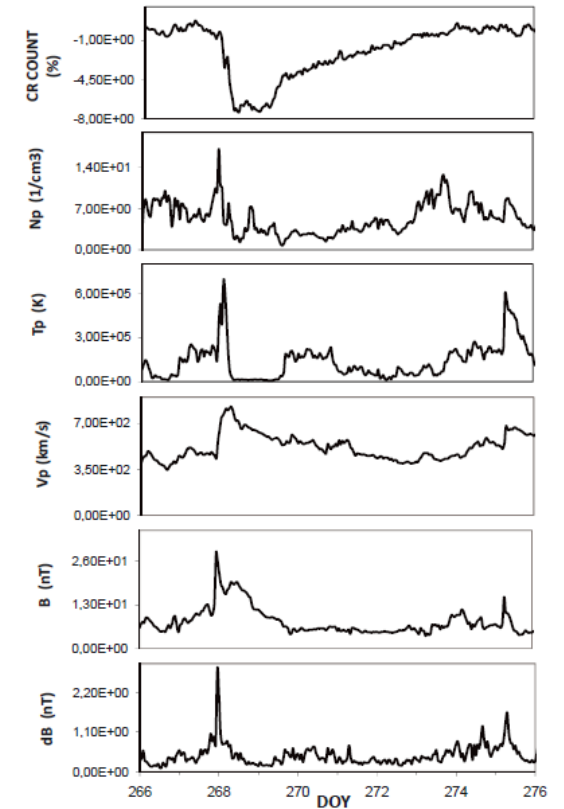
Temmer & Nitta (2015)

VISUALISATION



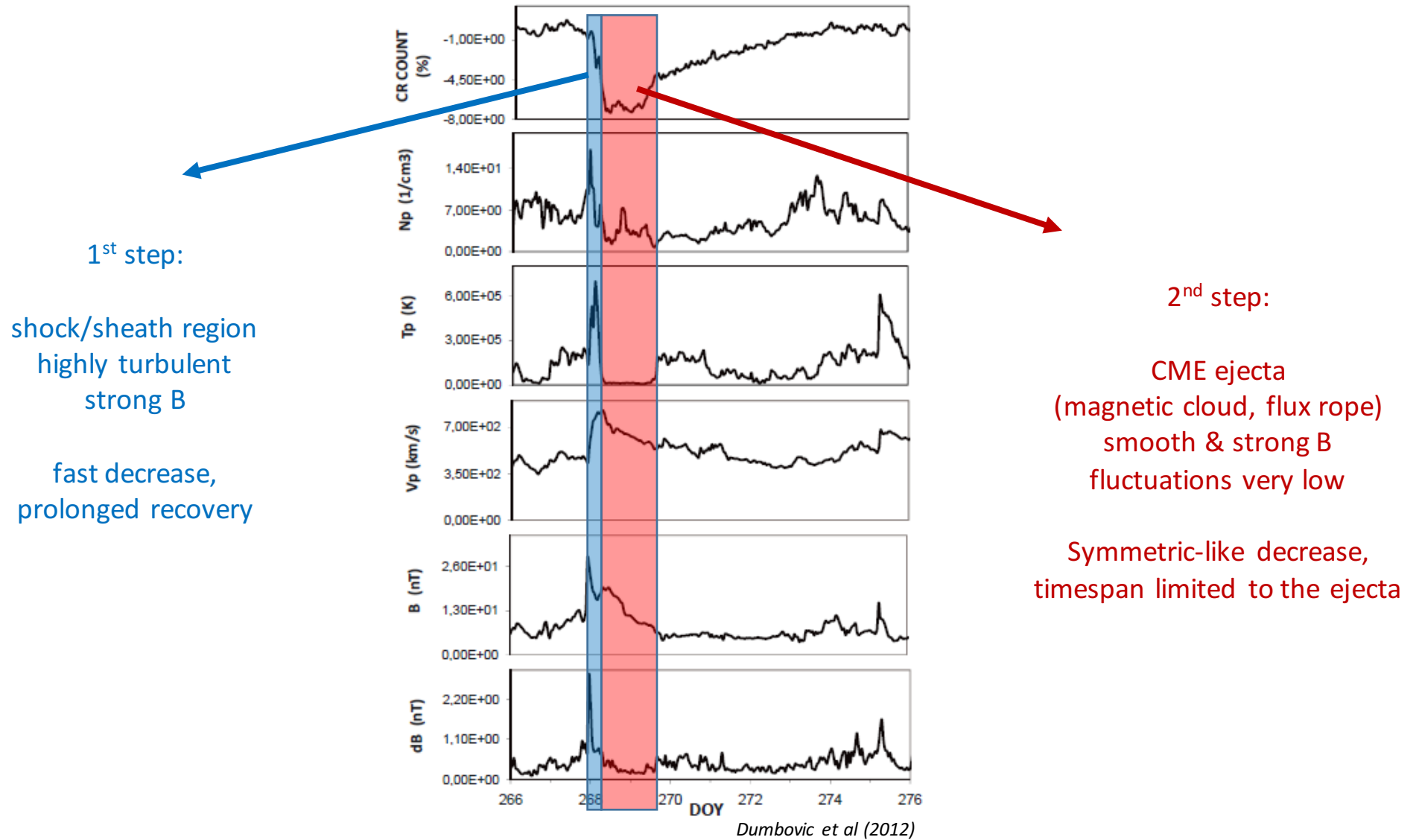
Richardson & Cane (2011)

IN SITU MEASUREMENTS

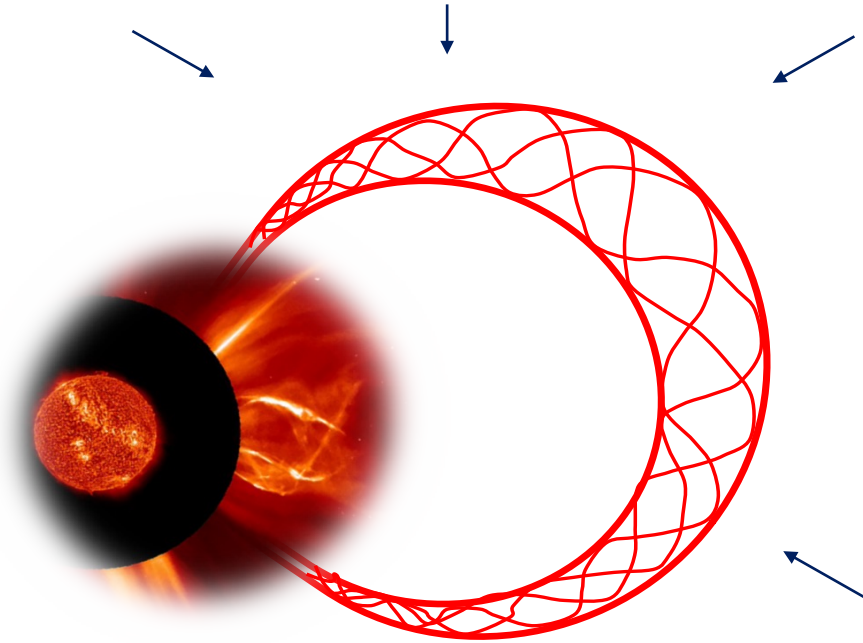


Dumbovic et al (2012)

Two-step Forbush decreases caused by ICMEs

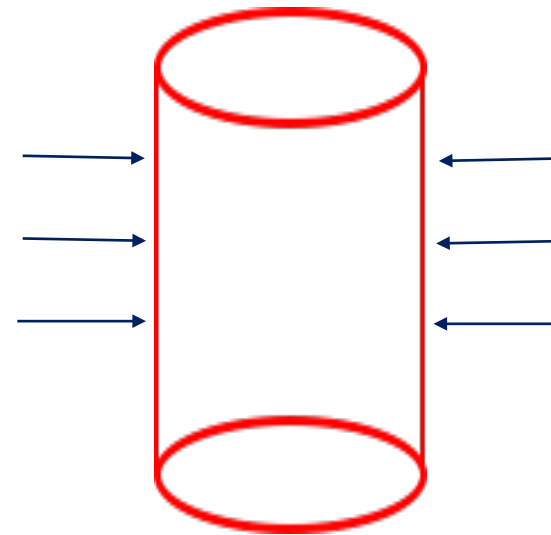


The analytical model - assumptions



magnetic ejecta (ICME, magnetic cloud, flux rope)

- a closed magnetic structure: no direct magnetic connection between the inside and the outside
=> particles can enter into the ejecta via perpendicular diffusion and/or drift (simplicity reasons -> only diffusion)
- **initially empty**



magnetic ejecta (ICME, magnetic cloud, flux rope)

- cylindrical form
- **moves with constant velocity**
- **does not vary in shape or size**

Building the analytical model

equation for the particle density:

$$\frac{\partial U}{\partial t} = \frac{1}{r} \left(\frac{\partial}{\partial r} \left(r D_{\perp} \frac{\partial}{\partial r} \right) \right),$$

- radial diffusion
- D does not change throughout ejecta

initial & boundary conditions:

$$U(r, t) = \begin{cases} 0, & 0 < r < a, t = 0 \\ U_0, & r = a, t \geq 0 \end{cases}$$

- initially empty
- Density outside constant

Exact analytical solution:

$$U(r, t) = U_0 \left(1 - \frac{2}{a} \sum_{n=1}^{\infty} \frac{J_0(\lambda_n r)}{\lambda_n J_1(\lambda_n a)} e^{-D \lambda_n^2 t} \right),$$

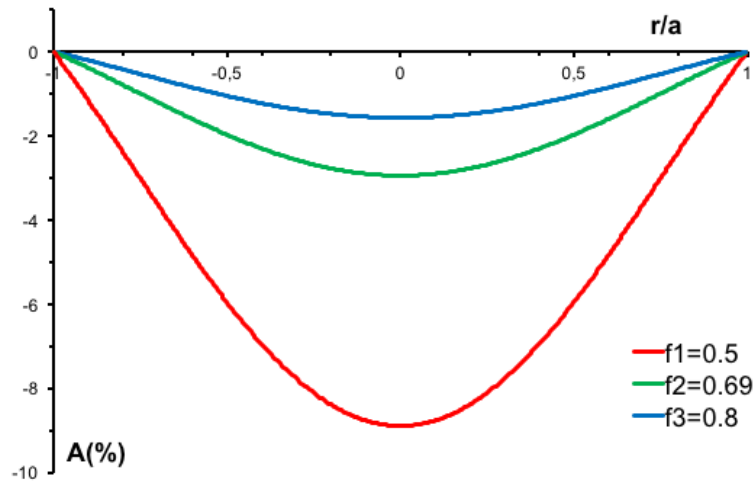
oscillatory

rapidly decreasing

We neglect terms with $n > 1$ and renormalize according to initial & boundary conditions to get the solution:

$$U(r, t) = U_0 \left(1 - J_0\left(\alpha_1 \frac{r}{a}\right) e^{-D \left(\frac{\alpha_1}{a}\right)^2 t} \right).$$

The analytical model - results



$$U(r, t) = U_0 \left(1 - J_0 \left(\alpha_1 \frac{r}{a} \right) e^{-D \left(\frac{\alpha_1}{a} \right)^2 t} \right).$$

$$f = f(a, t, D)$$

a = radius of ICME

t = diffusion (transit) time

D = diffusion coefficient

Forbush decrease depends on:

- ✓ - Radius of ICME *Blanco et al (2013)*
- ✓ - Diffusion (transit) time *Blanco et al (2013)*

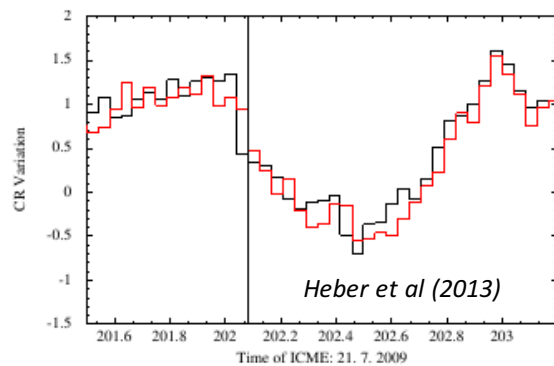
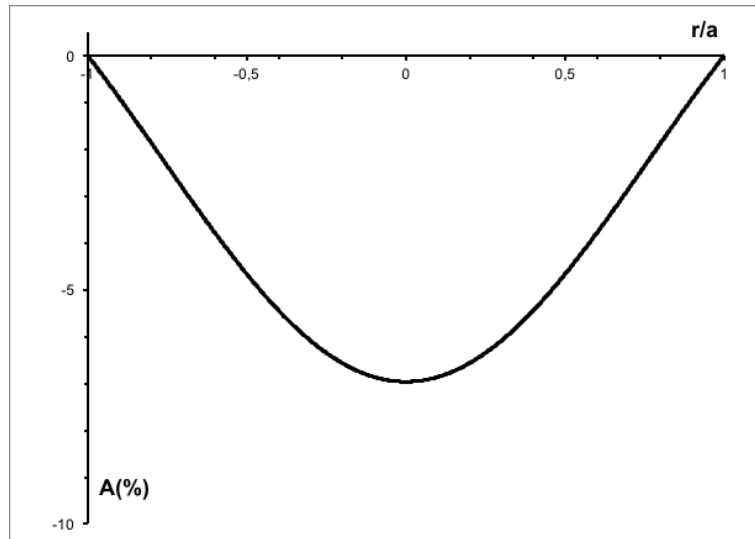
❓ Diffusion coefficient:

e.g. Dumbovic et al (2012)

✓ depends on the strength of B
- but how?

What is a typical diffusion coefficient in magnetic cloud and compared to normal solar wind??

The analytical model - results

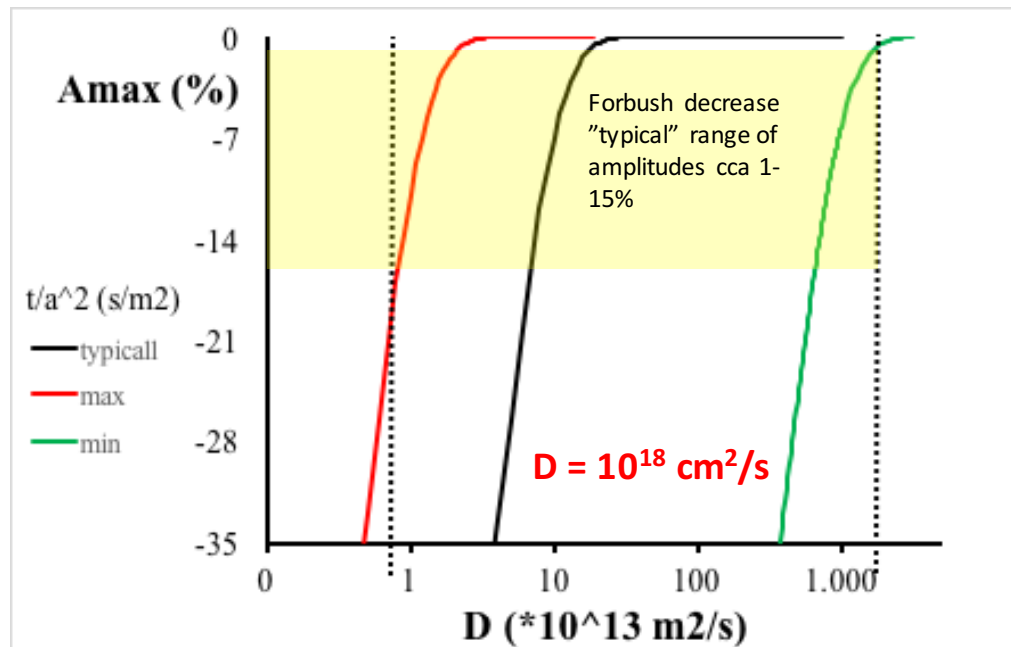


Typical values:
Transit time 72 hours
MC radius 0.05 AU
Forbush decrease 6-7%



Diffusion coefficient $10^{18} \text{ cm}^2/\text{s}$
($10^{14} \text{ m}^2/\text{s}$)

Estimation based on theoretical consideration



max:
a=0.02 AU
TT=96h

Typical:
a=0.05 AU
TT=72h

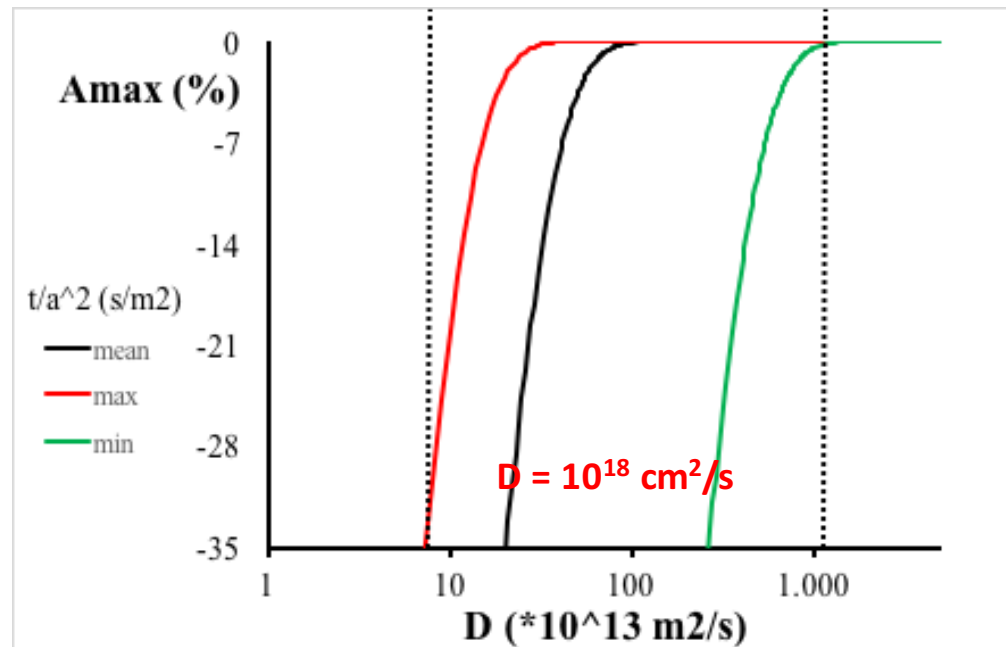
min:
a=0.2 AU
TT=12h

estimated range for the diffusion coefficient:

$D_{\min} = 7 \cdot 10^{16} \text{ cm}^2/\text{s}$
 $D_{\max} = 2,4 \cdot 10^{20} \text{ cm}^2/\text{s}$

Typical D for unperturbed solar wind:
 $D \sim 10^{21} \text{ cm}^2/\text{s}$

Estimation based on observational consideration



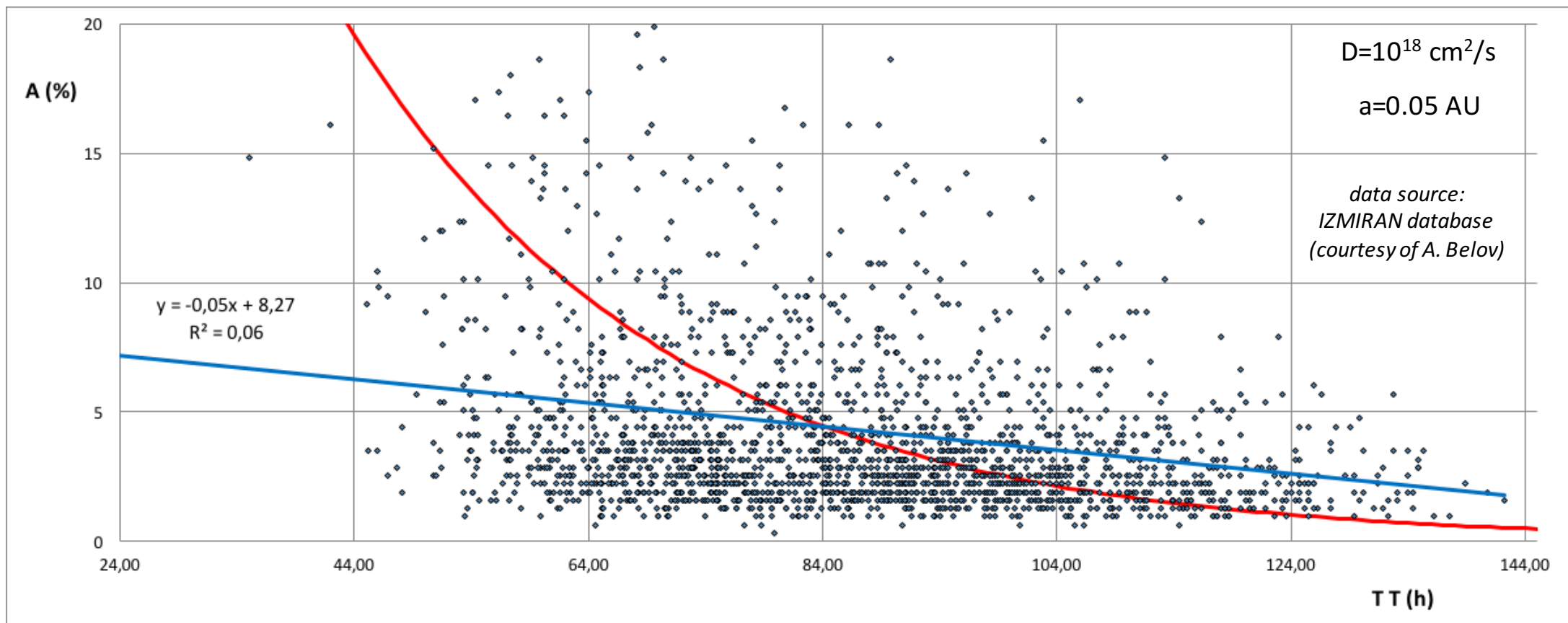
estimation of the diffusion coefficient range based on the empirical distribution of t/a^2 for MCs derived from Richardson & Cane (2010) list

estimated range for the diffusion coefficient:

$D_{\min} = 7 \cdot 10^{17} \text{ cm}^2/\text{s}$
 $D_{\max} = 1,2 \cdot 10^{20} \text{ cm}^2/\text{s}$

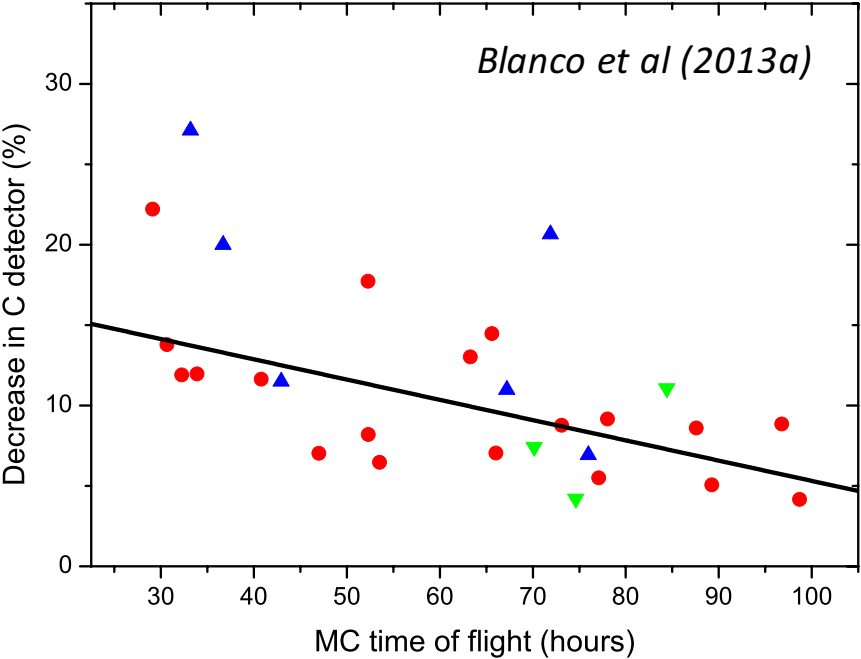
The model vs observation: ground based measurements at Earth

Forbush decrease amplitude vs transit time

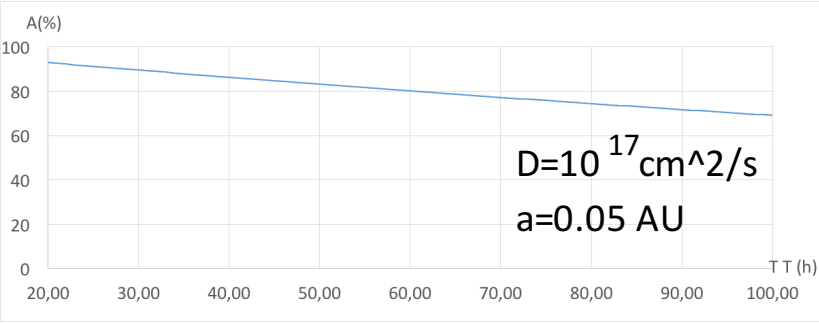
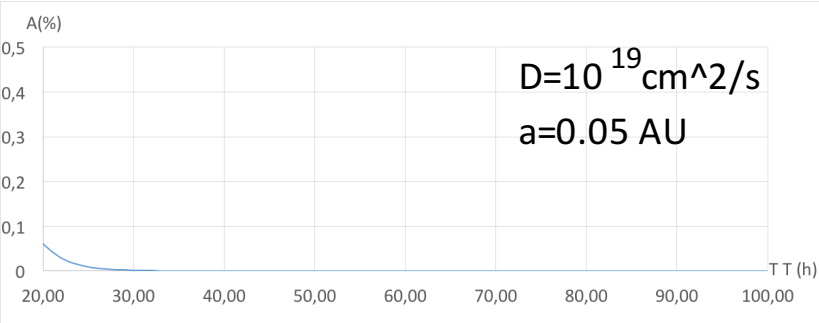
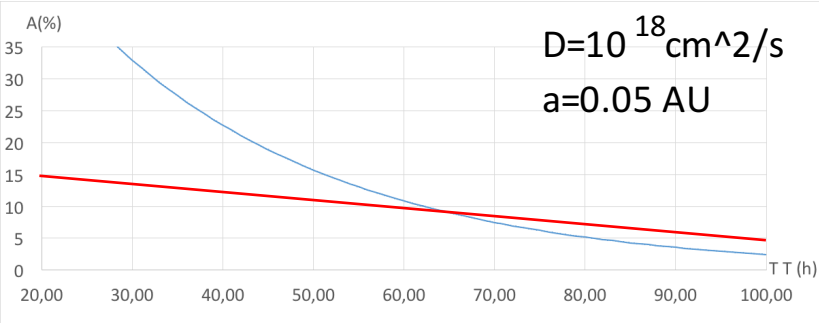


Forbush decrease measurements on Earth ($R \sim 10 \text{ GV}$) shifted to satellite values ($R = 0 \text{ GV}$) using empirical formula from Cane (2000)

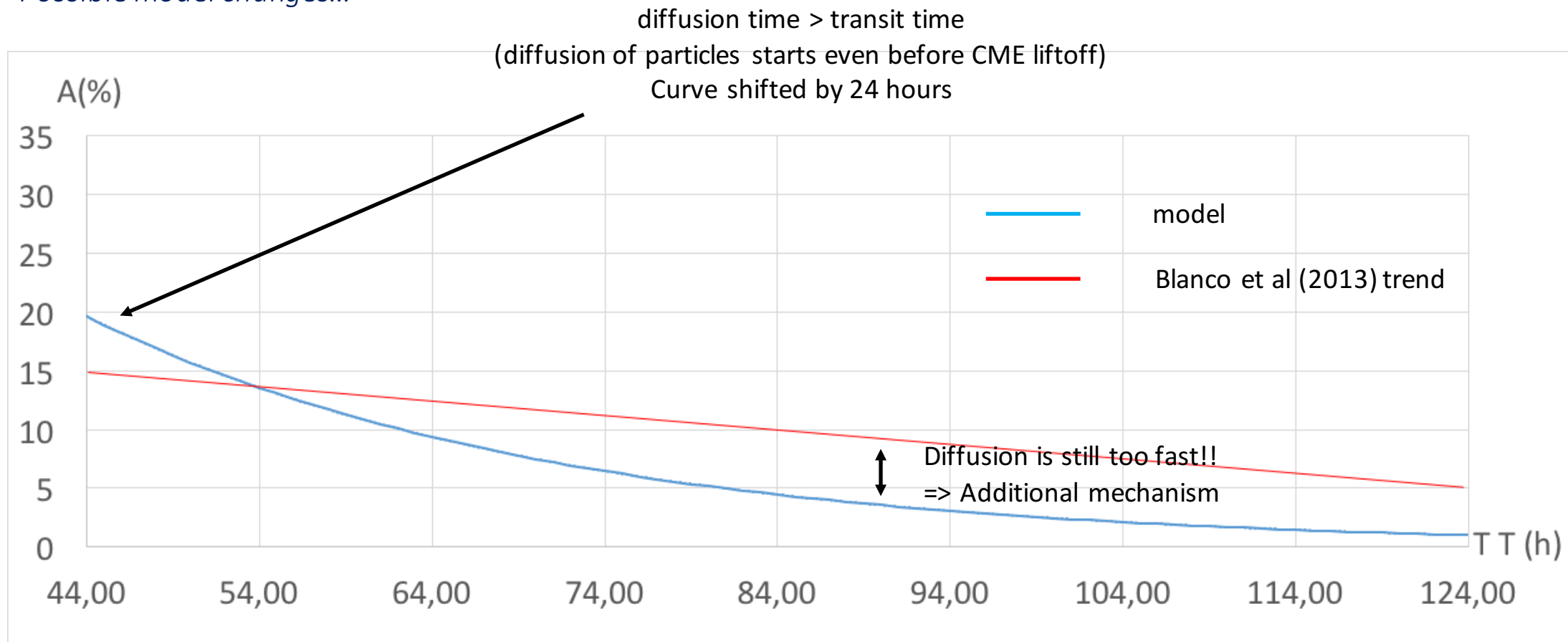
The model vs observation: spacecraft measurements



Measurements from Helios I and II

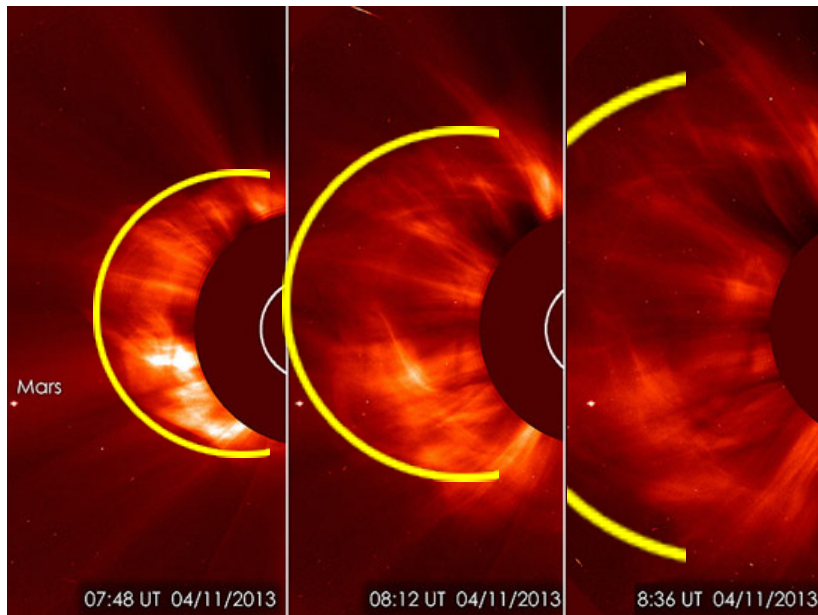


Possible model changes...



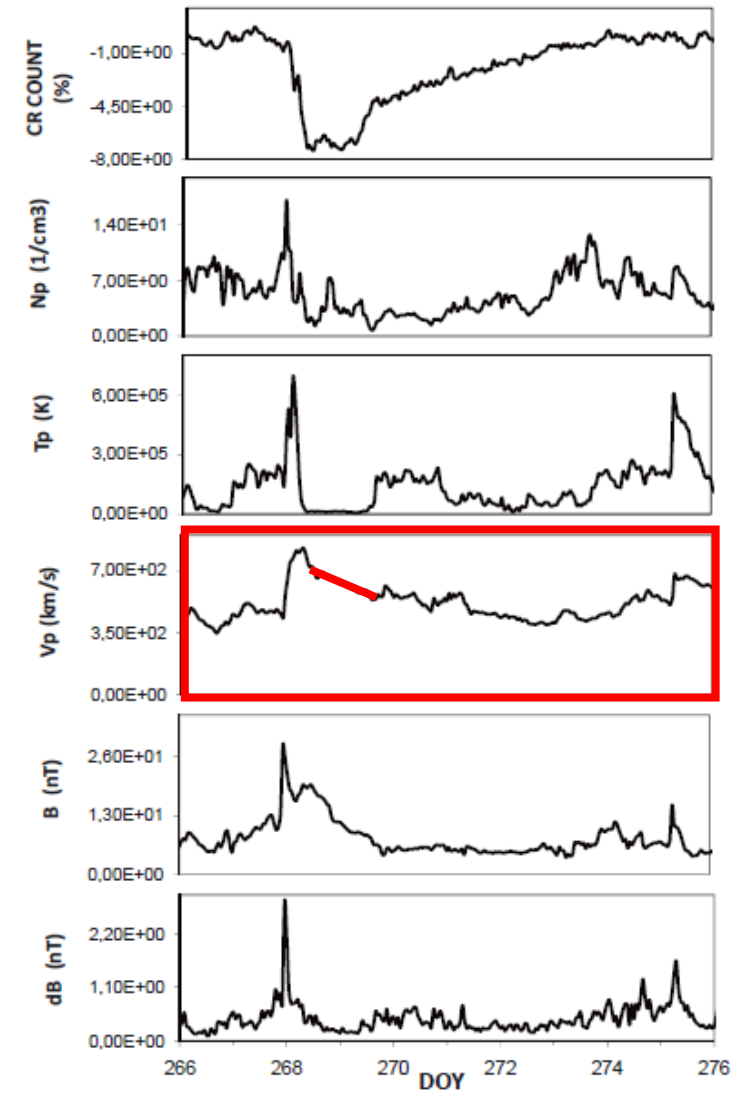
CMEs expand!

SOHO/LASCO C2 image



CME expansion observed remotely near the Sun, in
IP space and in situ measurements!

Dumbovic et al (2012)



Expansion vs diffusion – a very rough estimate

Could expansion be large "enough" factor to counteract diffusion??

$U = 6,5 \cdot R^{-2,4}$ MC density with heliocentric distance, Bothmer & Schwenn, 1998

$U = 7 \cdot R^{-2}$ Solar wind density with heliocentric distance

At 0.3 AU

U (CME) = 117

U (SW) = 78

FD = 10%

At 1 AU

U (CME) = 6,5

U (SW) = 7

FD = 44%

30 % decrease due to expansion

90 % increase due to diffusion

At 0.3 AU

$a = 0.05$ AU

$D = 10^{18} \text{ cm}^2/\text{s}$

FD = 100%

(empty MC)

Typical
transit
time 60 h

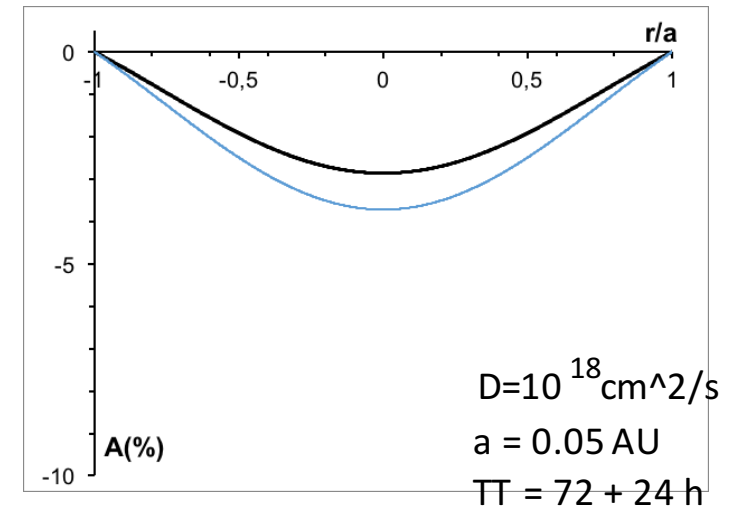
At 1 AU

$a = 0.05$ AU

$D = 10^{18} \text{ cm}^2/\text{s}$

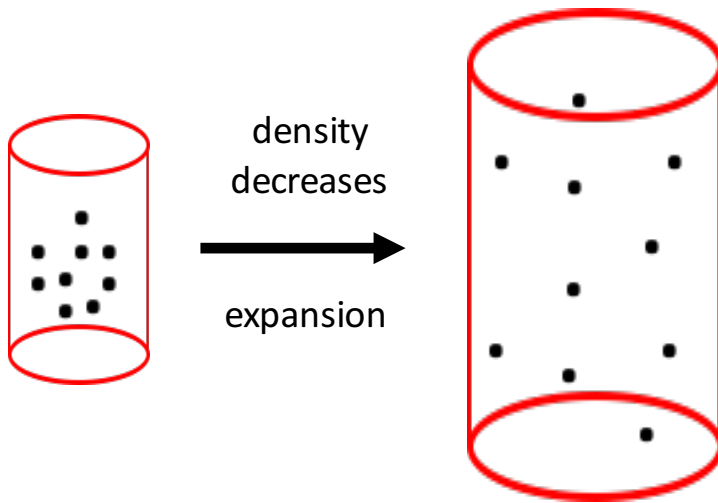
FD = 10%

A very rough
estimation:
Expansion can "slow
down" the diffusion
by roughly 30%



Expansion vs diffusion – a very rough estimate

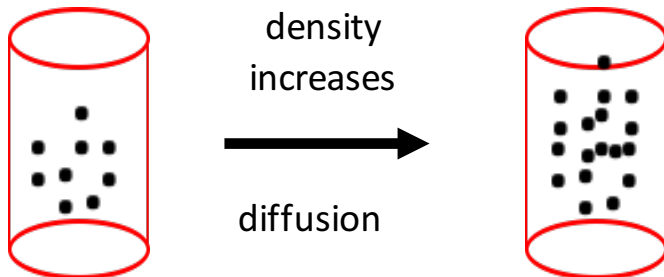
ratio



Calculated based on relative
MC (plasma) density decrease
due to expansion with
respect to solar wind density
decrease due to expansion
(empirical relation from
Bothmer & Schwenn, 1998)

1

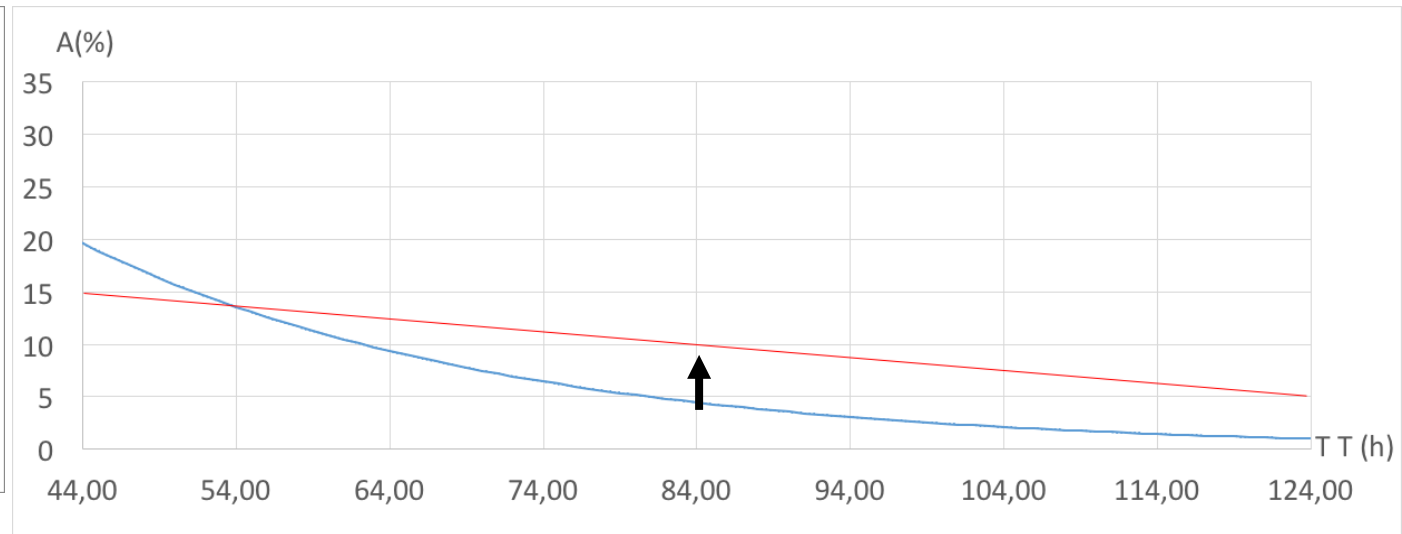
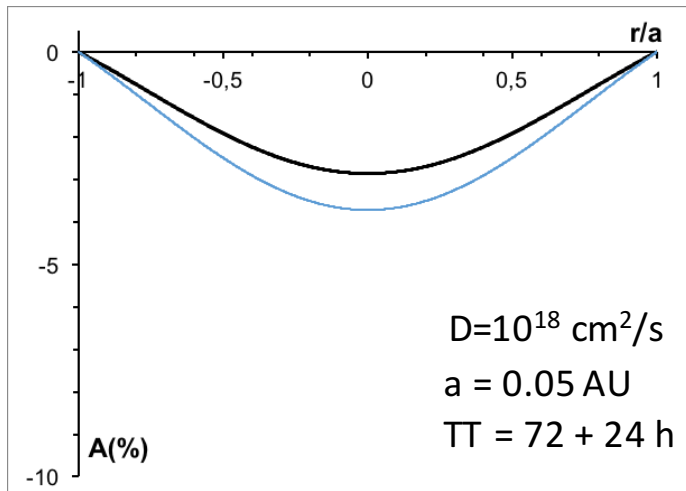
• •



Calculated based on our
model for the same
distance/time as above

3

Expansion vs diffusion – a very rough estimate



A very rough estimation:
Expansion can "slow down" the
diffusion by roughly 30%

CONCLUSIONS:

diffusion-based analytical model in present form qualitatively agrees with observation, but quantitatively suffers from several drawbacks

The qualitative aspect of the model could be improved by including observable facts regarding CMEs (e.g. expansion)

Thank you for your attention!