

A. Boso^{1,2*}, S. M. Lenzi^{1,2}, F. Recchia^{1,2}, S. Aydin³, M. A. Bentley⁴, B. Cederwall⁵, E. Clement⁶, G. de France⁶, A. Di Nitto⁷, A. Dijon⁶, M. Doncel⁵, F. Ghazi-Moradi⁵, A. Gottardo⁸, T. Henry⁴, T. Hüyük⁹, G. Jaworski¹⁰, P.R. John^{1,2}, K. Juhsz¹¹, I. Kuti¹², B. Melon¹³, D. Mengoni^{1,2}, C. Michelagnoli^{1,2}, V. Modamio⁸, D.R. Napoli⁸, B.M. Nyakó¹², J. Nyberg¹⁴, M. Palacz¹⁰, J.J. Valiente-Dobón⁸

¹ Dipartimento di Fisica e Astronomia Università di Padova, Padova, Italy. ² INFN, Sezione di Padova, Padova, Italy. ³ Aksaray Universitesi, Department of Physics, Aksaray, Turkey ⁴ University of York, York, United Kingdom. ⁵ Royal Institute of Technology, Stockholm, Sweden ⁶ GANIL, Caen, France. ⁷ Dipartimento di Scienze Fisiche and INFN, Sezione di Napoli, Napoli, Italy ⁸ INFN, Laboratori Nazionali di Legnaro, Legnaro (Padova) Italy. ⁹ IFIC-CSIC, Valencia, Spain. ¹⁰ Heavy Ion Laboratory, Warsaw University, Warszawa, Poland ¹¹ University of Debrecen, H-4032 Debrecen, Hungary ¹² MTA Atomki, H-4001 Debrecen, Hungary ¹³ Dipartimento di Fisica e INFN, Sezione di Firenze, Firenze, Italy ¹⁴ Department of Physics and Astronomy, Uppsala University, Uppsala, Sweden

Physics Case

Isospin Symmetry implies identical level schemes for mirror nuclei. Differences in excitation energies in mirror nuclei are therefore an evidence of **Isospin Symmetry Breaking (ISB)**

The **Mirror Energy Differences (MED)** are defined as:

$$\text{MED}_{J,T} = E_{J,T,T_z=-T}^* - E_{J,T,T_z=T}^*$$

and give information on nuclear structure.

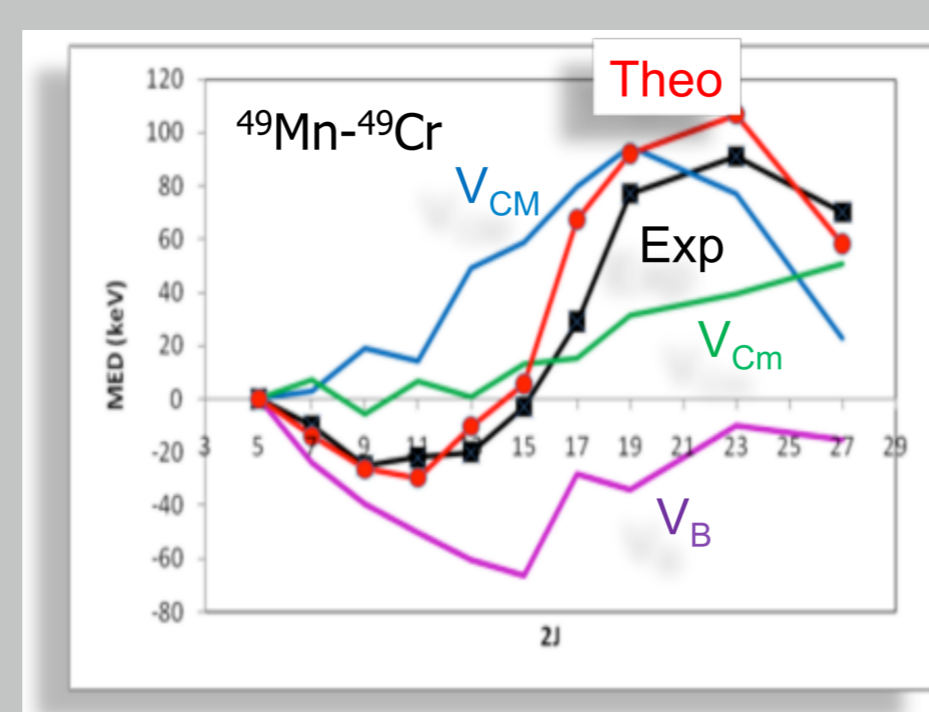
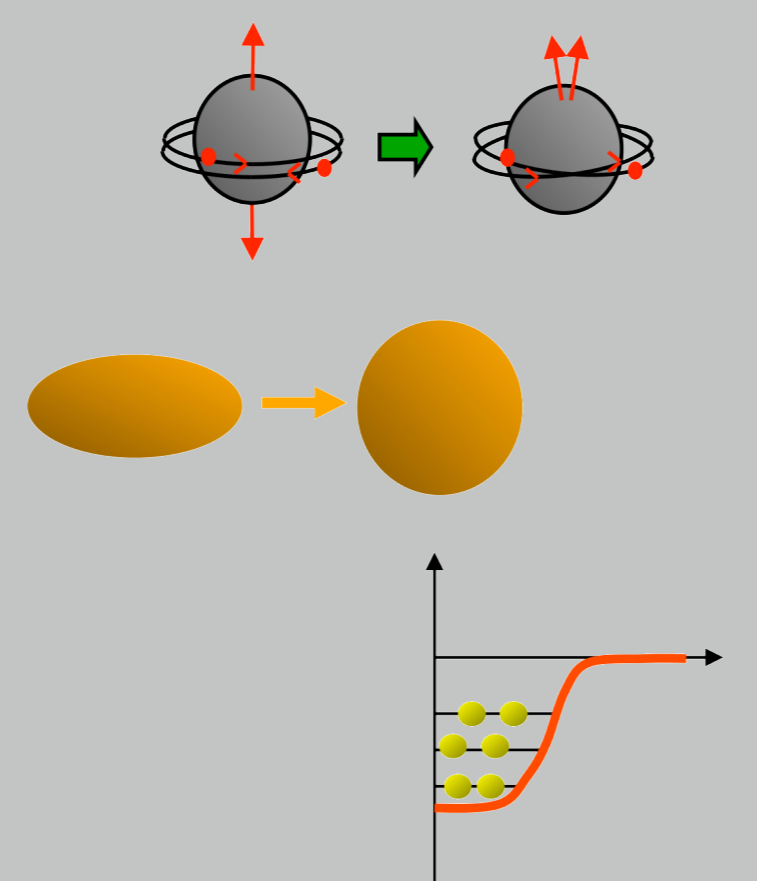
- ▶ The main contribution to MED comes from the **Coulomb interaction** This gives information on:

- ▶ The way the nucleus **aligns** its protons

- ▶ The nuclear **radius variation** with **J**

- ▶ **Single particle energies** of different orbitals

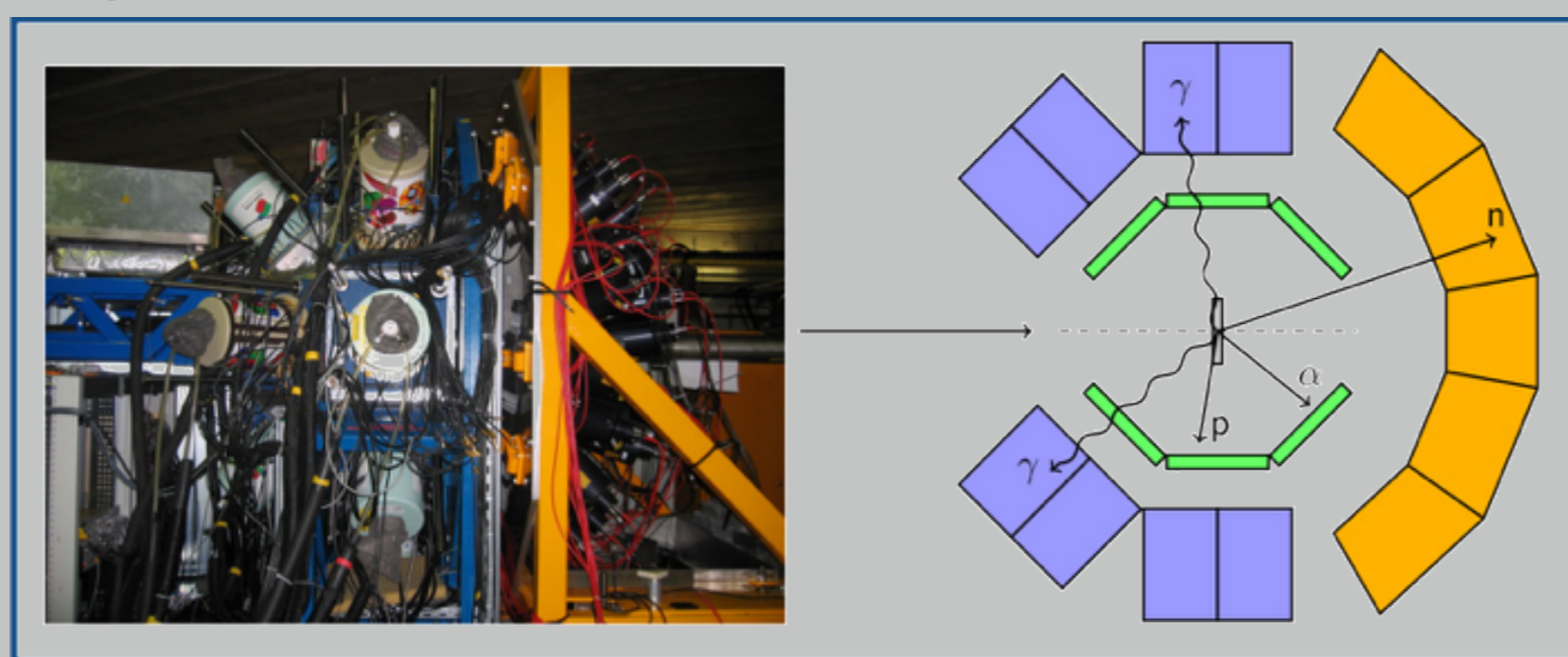
- ▶ In the $f_{7/2}$ shell an additional ISB term of **nuclear** origin must be added to reproduce the experimental MEDs **J=2 Anomaly**



Is it needed also in other mass regions?

The experiment

- ▶ Aim: Study mirror nuclei $^{23}\text{Mg} - ^{23}\text{Na}$ up to **high spin**
- ▶ Reaction: $^{16}\text{O} + ^{12}\text{C}$ at 60-70 MeV. $^{23}\text{Mg} - ^{23}\text{Na}$ populated in $\alpha n - \alpha p$ channels respectively
- ▶ Experimental setup



- ▶ **EXO GAM**: 11 HPGe Clover for γ -ray detection
- ▶ **DIAMANT**: 80 CsI scintillators for charged particles detection
- ▶ **NEUTRON WALL**: 50 liquid scintillators for neutron detection

Results: γ -ray spectra and level schemes

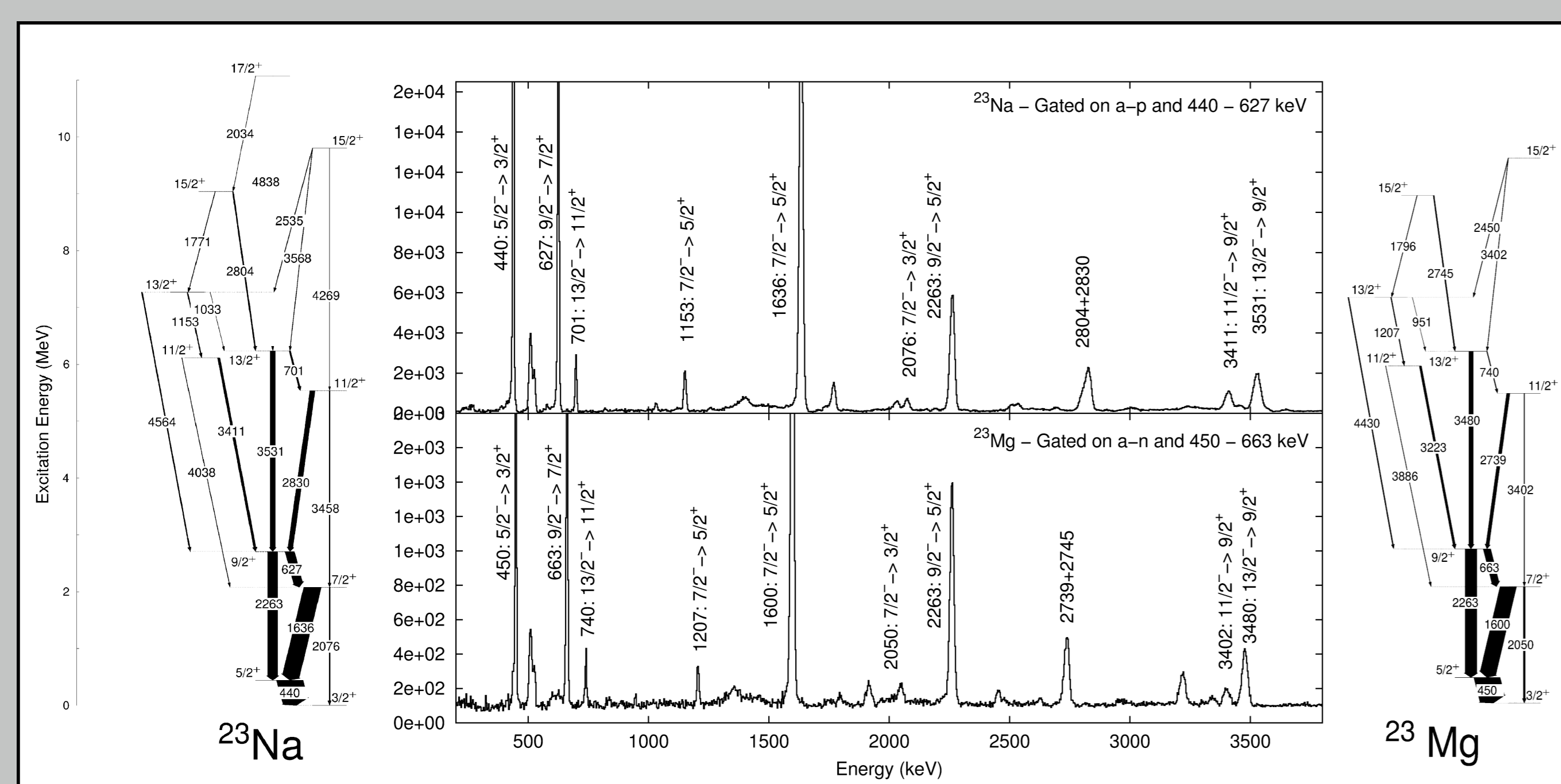
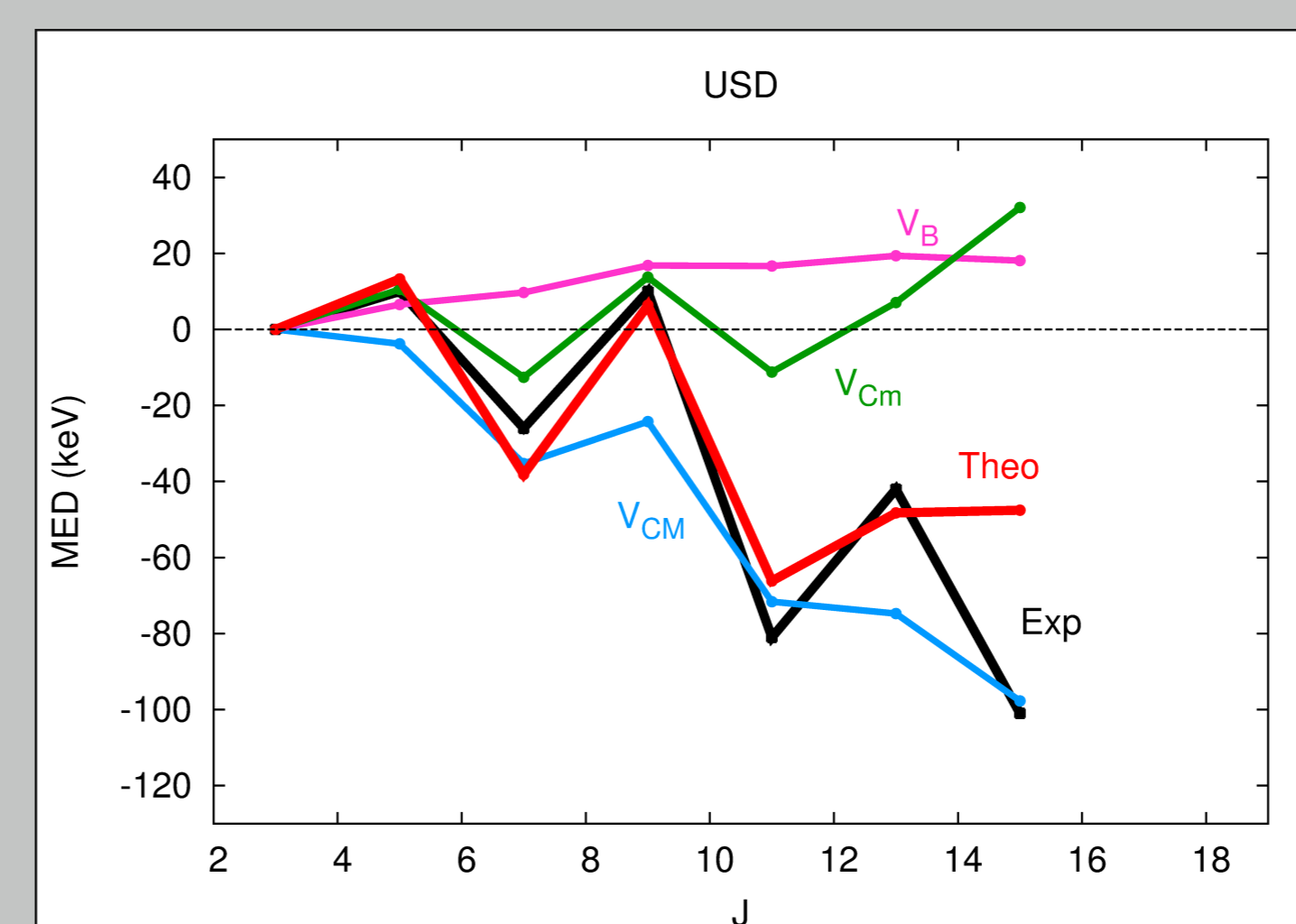


Figure 1: γ -ray spectra and level schemes of mirror nuclei $^{23}\text{Mg} - ^{23}\text{Na}$

Discussion: "Standard" shell model approach

- ▶ **USD** interaction
- ▶ Coulomb term V_{CM} calculated in harmonic oscillator basis
- ▶ Radial term V_{CM} obtained from the **occupation numbers** of the $s_{1/2}$ shell
- ▶ Correction applied to single particle energies
- ▶ "Nuclear" ISB term V_{B} parameterized from A=42 mirror nuclei

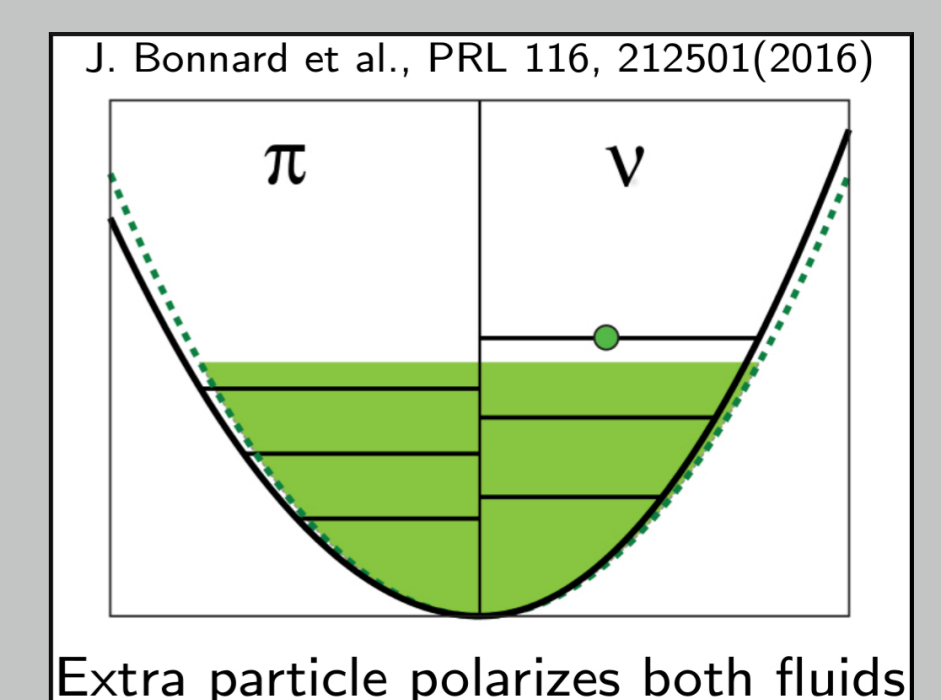


- ▶ The **Coulomb** term reproduces the trend of the MED
- ▶ The V_{CM} term is needed: this confirms the **importance** of the $s_{1/2}$ shell
- ▶ "Nuclear" ISB term V_{B} makes the things worse: **J=2 Anomaly??**

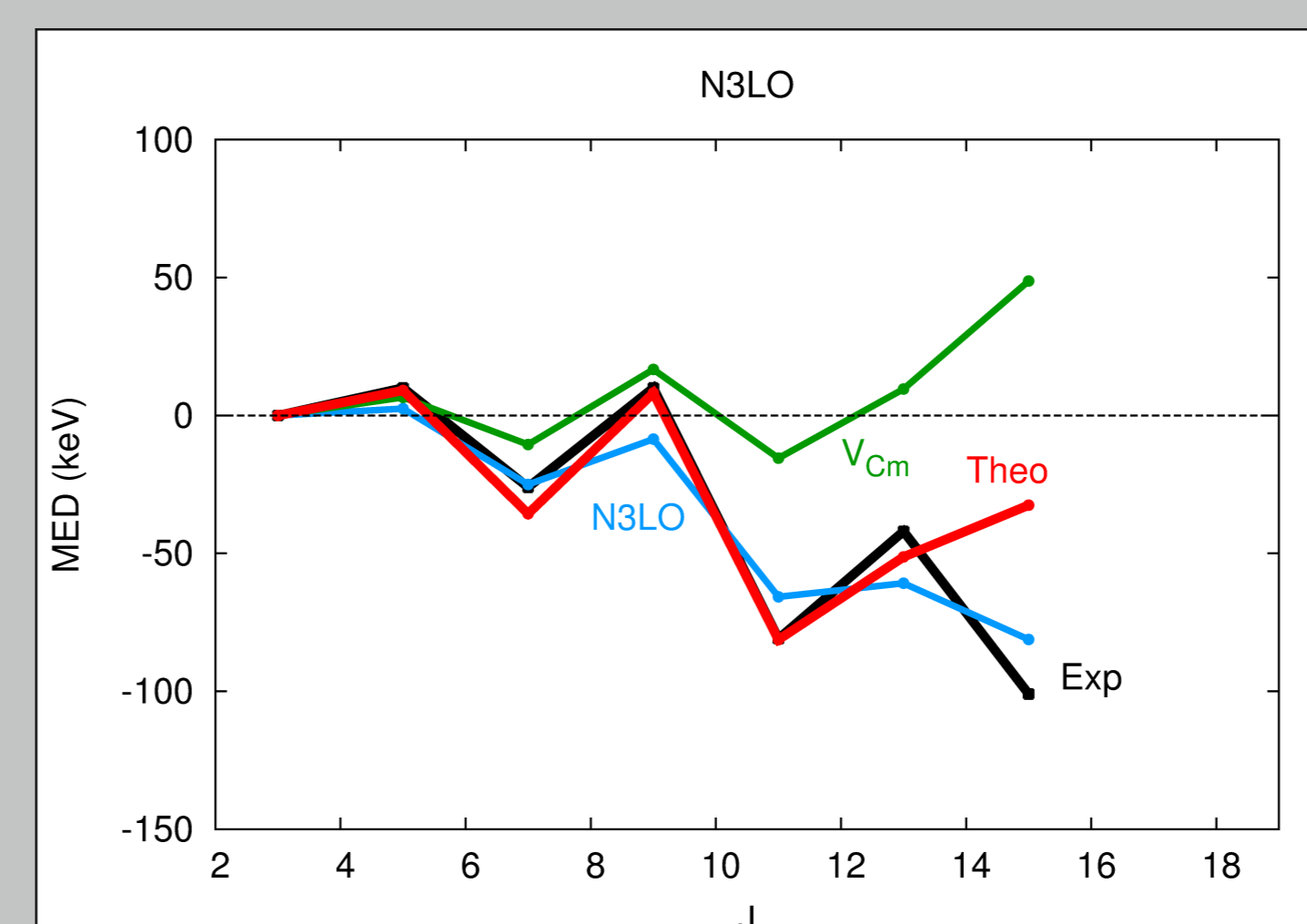
Discussion: Alternative Approach

- ▶ **Realistic NN N3LO** interaction which naturally includes **Coulomb** term, **single particle** energy corrections and **nuclear** ISB term

- ▶ **Different potential wells** for π and ν : $\hbar\omega_{\pi,\nu}$ is strictly related to the radii $r_{\pi,\nu}$. r_{π} is fitted to the experiment. r_{ν} is obtained from the binding energies. **Different $\hbar\omega_{\pi,\nu}$ for each nucleus**



- ▶ Radial term V_{CM} obtained from the **occupation numbers** of the $s_{1/2}$ shell

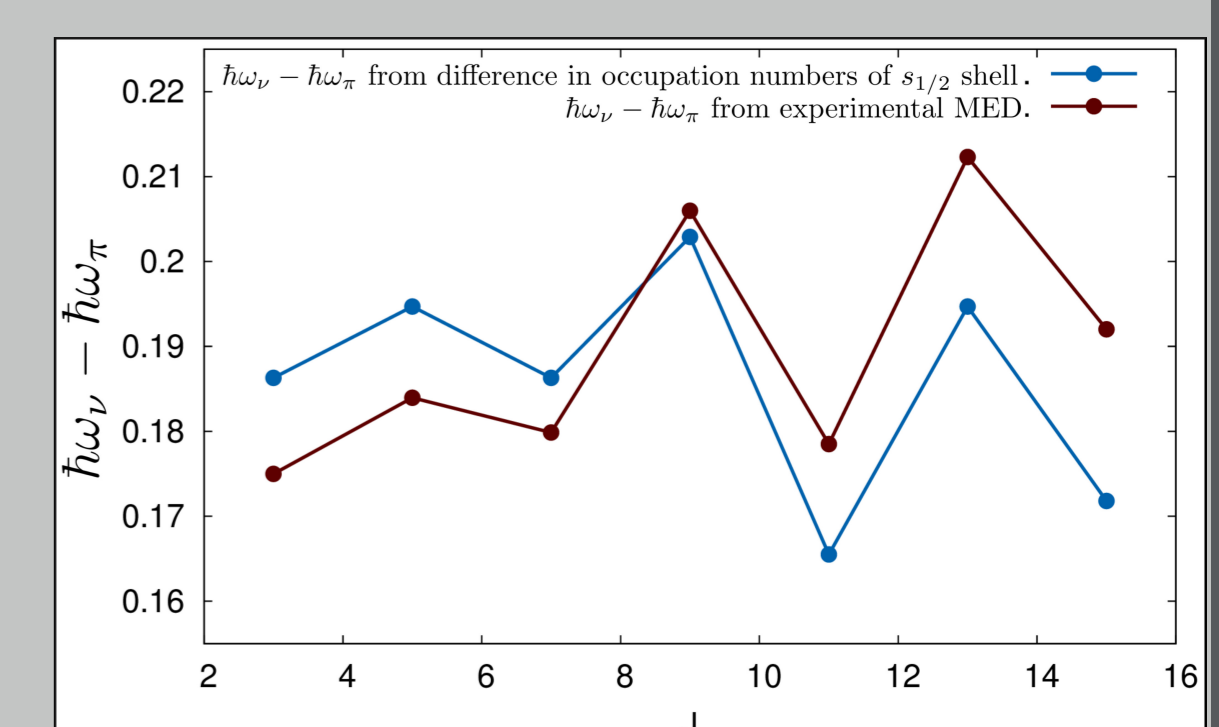


- ▶ **N3LO** interaction reproduces the trend of the MED
- ▶ **Nuclear** ISB term naturally taken into account
- ▶ The V_{CM} term is still needed: **importance** of the $s_{1/2}$ shell confirmed

Perspectives

- ▶ Include the **radial term** V_{CM} in the interaction \rightarrow **Different $\hbar\omega_{\pi,\nu}$ for each J**

- ▶ Idea: exploit the **relation** between $\Delta\hbar\omega = \hbar\omega_{\pi} - \hbar\omega_{\nu}$ and the **difference in occupation numbers** of π and ν in the $s_{1/2}$ shell (related to **neutron skin**)



- ▶ Application of the same approach to the **other nuclei** in the sd shell
- ▶ Application of the same approach to the $f_{7/2}$ shell: **J=2 Anomaly??**

References

- ▶ A. P. Zuker et al., PRL 89, 142502 (2002)
- ▶ M.A. Bentley and S.M. Lenzi, Prog. Part. Nucl. Phys. 59 497 (2007)
- ▶ J. Bonnard et al., PRL 116, 212501 (2016)