

# Measurements of four-jet differential cross sections in $\sqrt{s} = 8$ TeV proton-proton collisions using the ATLAS detector

Sabrina Sacerdoti  
on behalf of the Atlas Collaboration

Universidad de Buenos Aires

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# Outline

1. Introduction
2. Event Reconstruction and Selection
3. Cross-section definition
4. Predictions
5. Results
6. Conclusion

# Introduction and Motivation

**Test of predictions** at LO and NLO: the predictions are expected to display various levels of agreement with data in different kinematic regimes.

Data-MC comparisons were made in order to study how theoretical predictions describe:

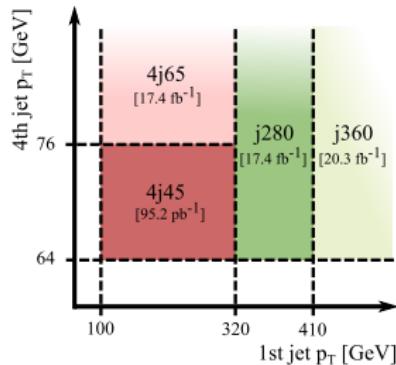
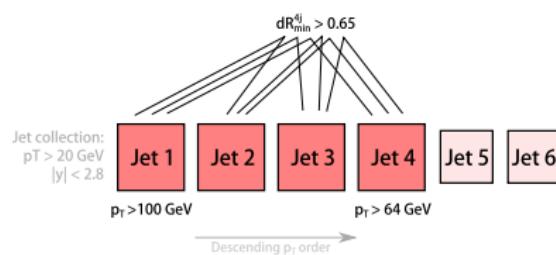
- ▶ **inclusive variables**,
- ▶ **angular variables**,
- ▶ the range of **energy scales** within an event,
- ▶ regimes sensitive to **NLO effects**,
- ▶ **low- $x$**  (large  $\Delta y$ ) distributions.

**Study of QCD background**: several new physics searches have many jets in the final state;  
it is thus crucial to understand the QCD contribution to this kind of events.

# Event Reconstruction and Selection

Jets:

- reconstructed using the anti- $k_t$  algorithm, with radius parameter  $R=0.4$
- calibrated using data-driven methods



**Phase-space** At least 4 jets within the rapidity region  $|y| < 2.8$ , with  $p_T^{(1)} > 100 \text{ GeV}$  &  $p_T^{(4)} > 64 \text{ GeV}$ , separated by  $\Delta R_{ij} > 0.65$ .

**Trigger** Exclusive combination of two single-jet and two 4-jet triggers. The  $p_T$  and  $\Delta R_{ij}$  cuts are implemented to have  $> 99\%$  trigger efficiency.

# Cross-section definitions

Probed multijet topologies by measuring the distributions of **event variables**:

- |                 |   |
|-----------------|---|
| <b>Momentum</b> | ► $p_T^{(i)}$ : $p_T$ of the $i$ -th jet, $i = 1, 2, 3, 4$<br>► $H_T$ : scalar sum of the $p_T$ of the 4 jets<br>► $\Sigma p_T^{\text{central}}$ : scalar sum of the $p_T$ of the 2 central jets  |
| <b>Mass</b>     | ► $m_{4j}$ : invariant mass of the 4 jets<br>► $m_{2j}^{\min} / m_{4j}$ : ratio of the minimum invariant mass of 2 jets and $m_{4j}$  |
| <b>Angular</b>  | ► $\Delta y_{2j}^{\min}, \Delta\phi_{2j}^{\min}$ : minimum angular separation between 2 jets<br>► $\Delta y_{3j}^{\min}, \Delta\phi_{3j}^{\min}$ : minimum angular separation between 3 jets<br>► $\Delta y_{2j}^{\max}$ : maximum rapidity separation between 2 jets |
- 
- Only the 4 leading jets in  $p_T$  are used.
  - **Inclusive cuts** were applied to the transverse momentum, rapidity and mass in order to probe different kinematic regimes.
  - Distributions were unfolded using the **Bayesian Iterative** method.
  - 4 examples shown today; all results can be found in JHEP 12(2015)105.

# Theoretical Predictions

Monte Carlo simulations are used to:

- ▶ estimate experimental systematic uncertainties,
- ▶ deconvolute detector effects,
- ▶ compare with data.

Name	Hard scattering + PS/UE	LO/NLO	PDF
Pythia 8	Pythia 8 + Pythia 8	LO ( $2 \rightarrow 2$ )	CT10
Herwig++	Herwig++ + Herwig++	LO ( $2 \rightarrow 2$ )	CTEQ6L1
MadGraph	Madgraph + Pythia 6	LO ( $2 \rightarrow 4$ )	CTEQ6L1
HEJ	HEJ <sup>†</sup>		CT10
BlackHat	BlackHat / Sherpa	NLO ( $2 \rightarrow 4$ )	CT10
NJet	NJet / Sherpa	NLO ( $2 \rightarrow 4$ )	CT10

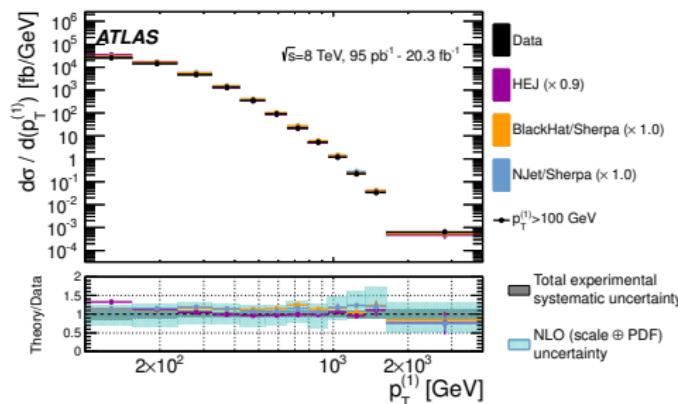
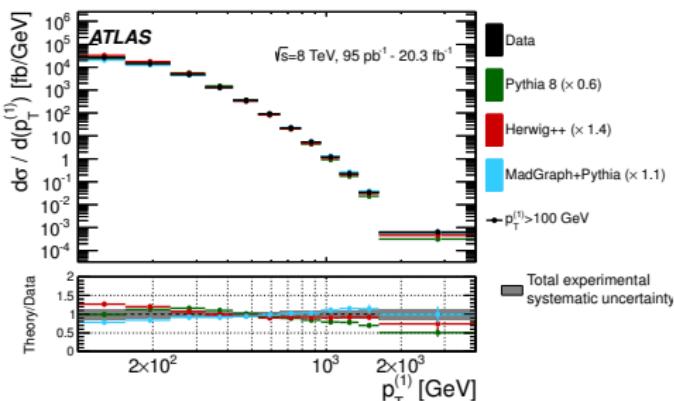
(†) The HEJ sample is based on an approximation to all orders in  $\alpha_s$ .

- ▶ Pythia 8 is used for unfolding and to estimate systematic uncertainties.
- ▶ Herwig++ and Madgraph were used for cross checks and uncertainties.
- ▶ All predictions were compared to data.
- ▶ The LO and HEJ simulations were rescaled to facilitate comparison with the data.

# Results: Momentum Variables

First leading jet  $p_T$  ( $p_T^{(1)}$ ).

Data compared to LO (left) and NLO and HEJ (right) predictions.

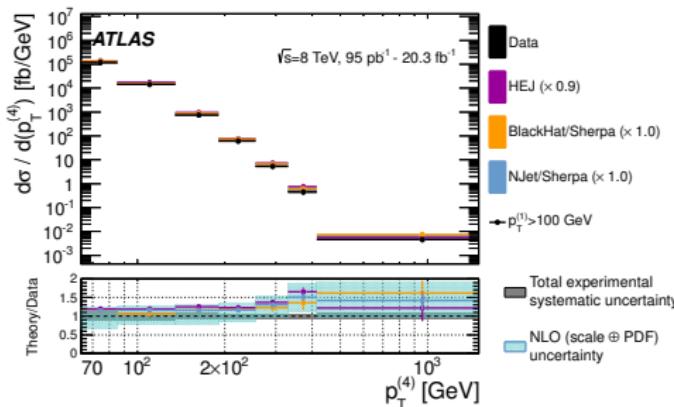
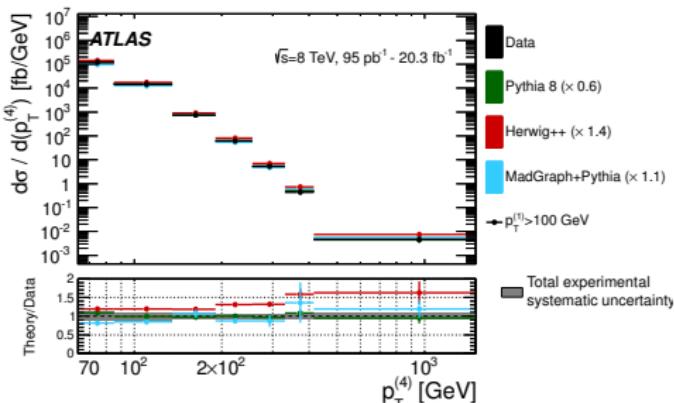


- ▶ All LO generators show a slope with respect to data, Madgraph being the only one with a positive slope in  $p_T^{(1)}$ .
- ▶ NJet and HEJ do well in the leading jet spectrum, but might benefit from matching to PS in the  $p_T^{(4)}$  case.
- ▶ Pythia is better in  $p_T^{(4)}$ . Madgraph does reasonably well in all.

# Results: Momentum Variables

## Fourth leading jet $p_T$ ( $p_T^{(4)}$ ).

Data compared to LO (left) and NLO and HEJ (right) predictions.

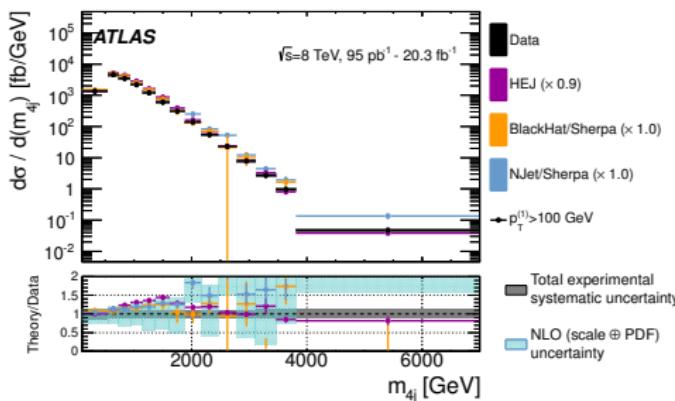
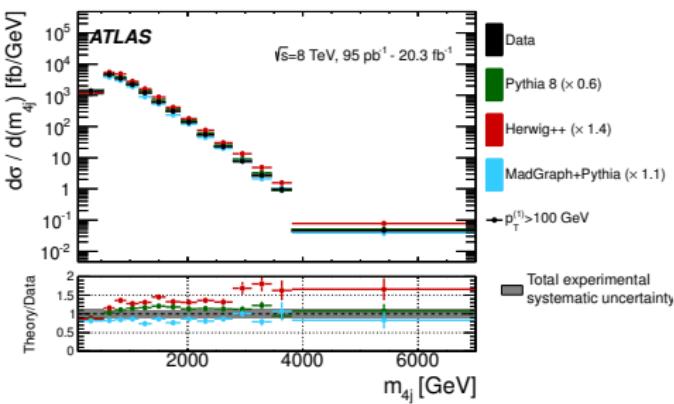


- ▶ All LO generators show a slope with respect to data, Madgraph being the only one with a positive slope in  $p_T^{(1)}$ .
- ▶ NJet and HEJ do well in the leading jet spectrum, but might benefit from matching to PS in the  $p_T^{(4)}$  case.
- ▶ Pythia is better in  $p_T^{(4)}$ . Madgraph does reasonably well in all.

# Results: Mass Variables

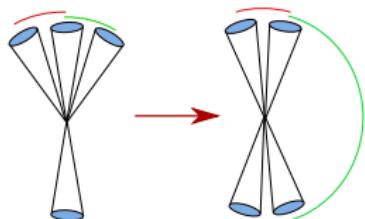
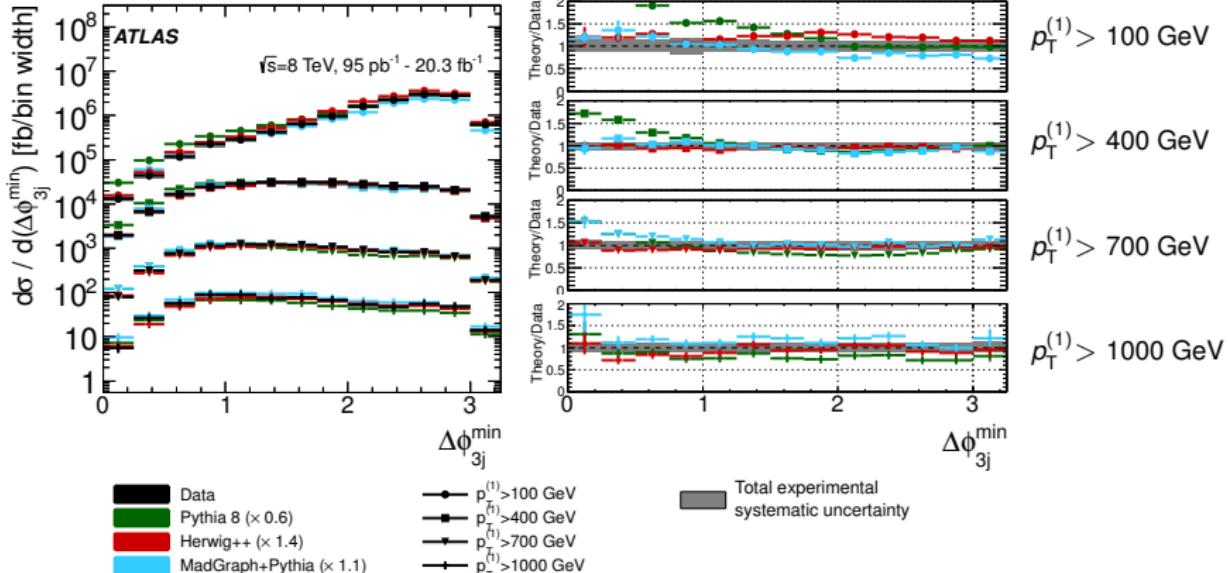
Invariant Mass of the 4 leading jets ( $m_{4j}$ ).

Data compared to LO (left) and NLO and HEJ (right) predictions.



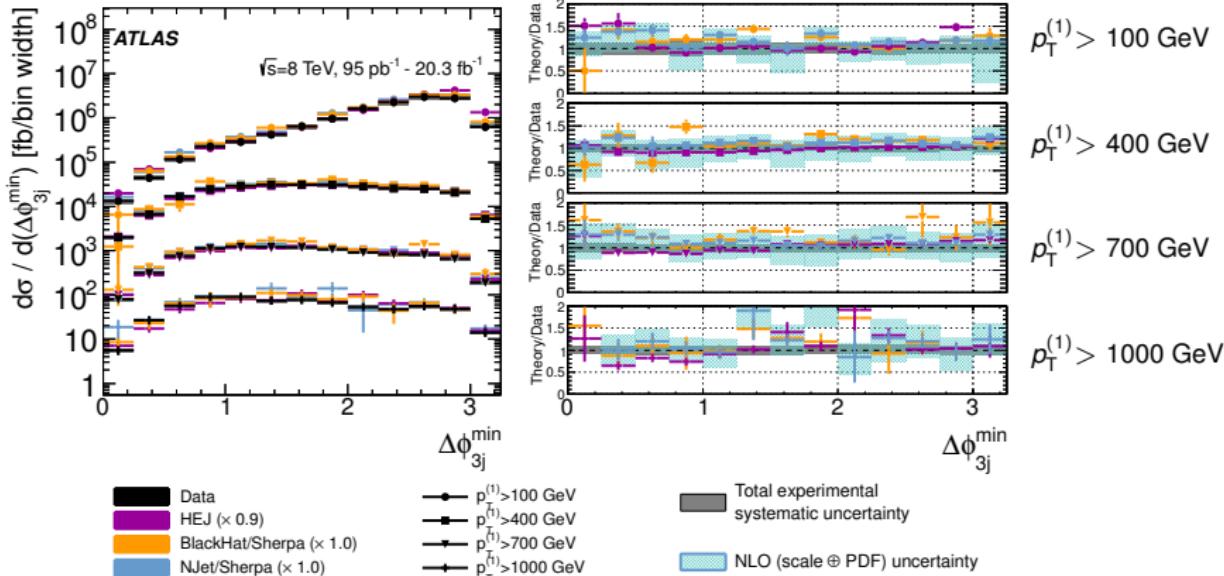
- ▶ Variable sensitive to the separation between jets.
- ▶ Pythia and Madgraph describe the data well, as does Herwig above 1 TeV.
- ▶ HEJ and NJet present a bump structure in the 1-2 TeV region; the difference is covered by the NLO uncertainties.

# Results: Angular Variables - LO



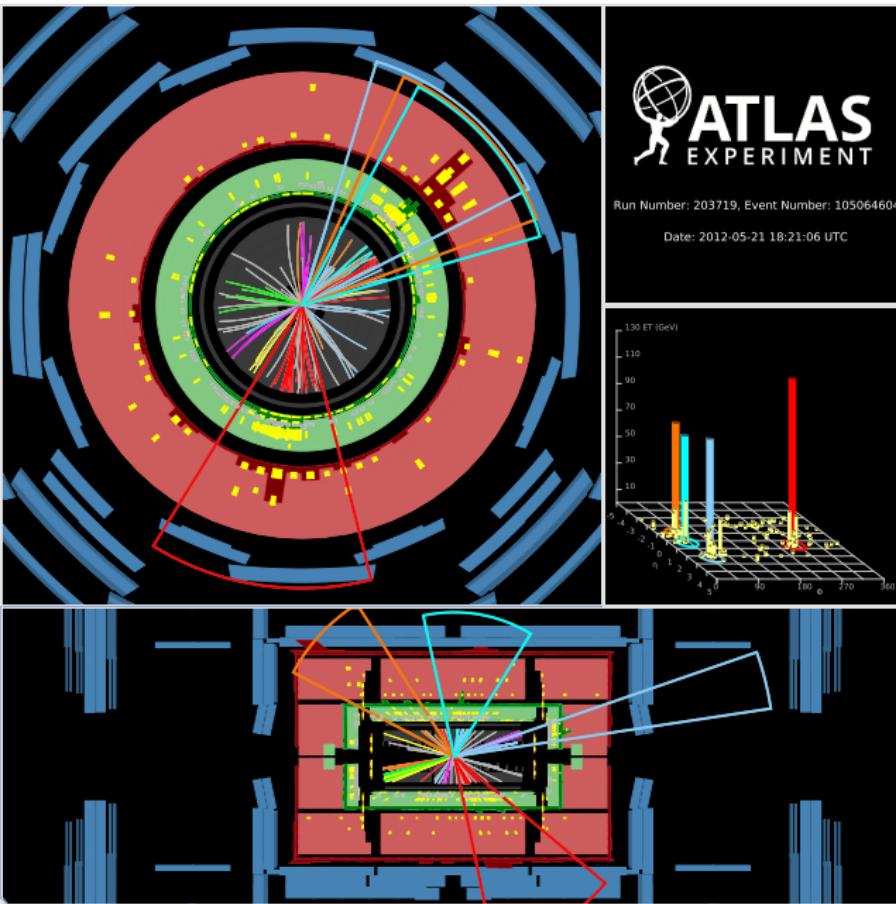
$$\Delta\phi_{ijk}^{\min} = \min_{i,j,k \in [1,4]} (|\Delta\phi_{ij}| + |\Delta\phi_{jk}|) \quad i \neq j \neq k$$

# Results: Angular Variables - NLO and HEJ

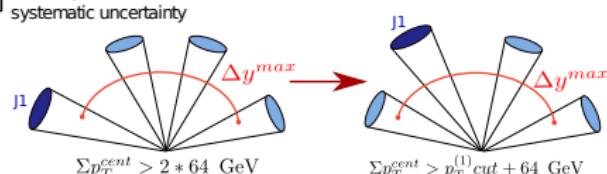
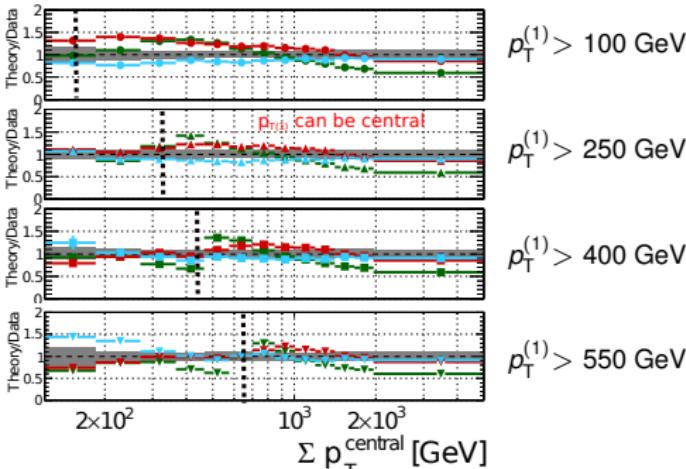
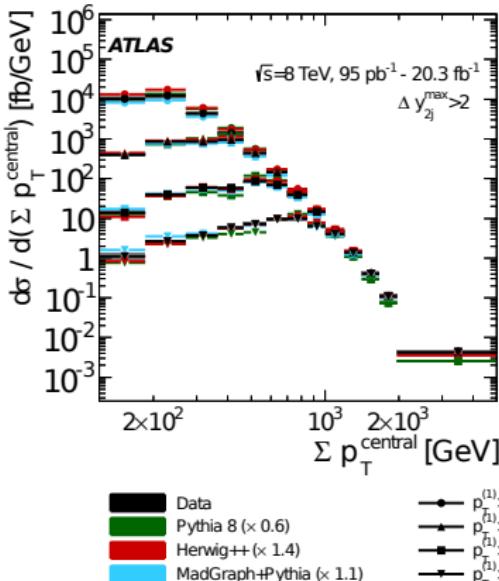


- ▶ HEJ provides a good description of all angular variables for  $p_T^{(1)} > 400 \text{ GeV}$ , but shows significant discrepancies in all variables for lower  $p_T^{(1)}$  values.
- ▶ NJet describes the data well within uncertainties.

# Event with small value of $\Delta\phi_{ijk}^{min}$

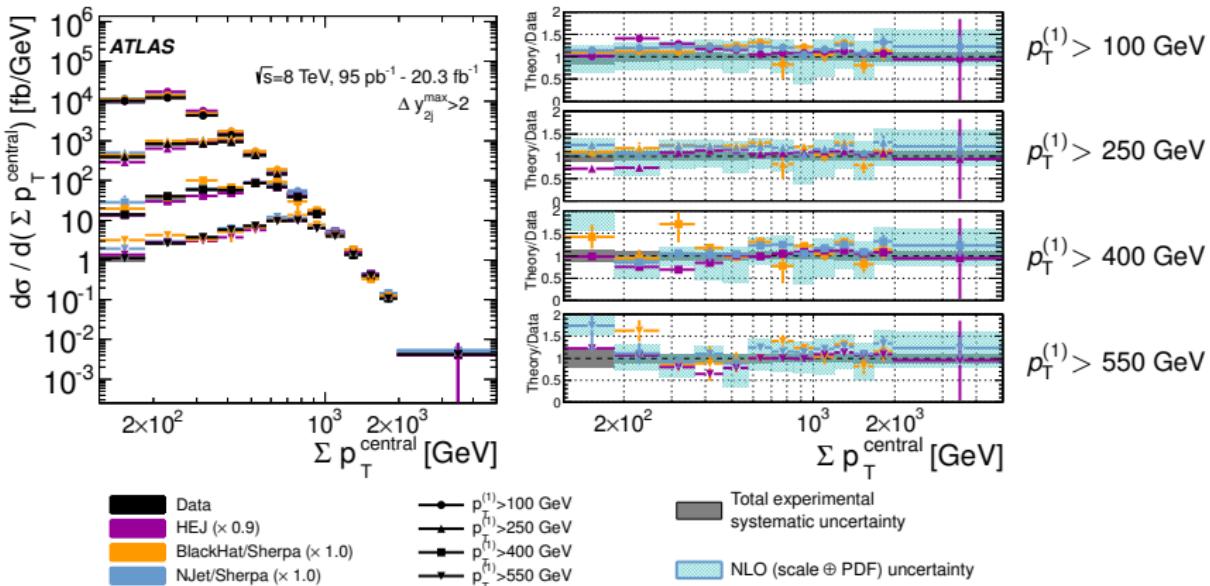


# Results: $\sum p_T^{\text{central}}$ for $\Delta y_{2j}^{\max} > 2$ - LO



- All  $2 \rightarrow 2$  predictions have issues describing this transition.
- The discrepancies worsen for larger  $\Delta y_{2j}^{\max}$  and  $p_T^{(1)}$  cuts.
- Madgraph provides the best description, especially at low  $p_T^{(1)}$ .

# Results: $\Sigma p_T^{\text{central}}$ for $\Delta y_{2j}^{\max} > 2$ - NLO and HEJ



- ▶ Testing the HEJ framework, which is set to describe topologies with 2 jets significantly separated, and 2 additional high- $p_T$  jets.
- ▶ HEJ describes better the high  $\Sigma p_T^{\text{central}}$  region, the lower part shows more shape differences.
- ▶ NJet overestimates the values for low  $\Sigma p_T^{\text{central}}$  but otherwise describes the data well.

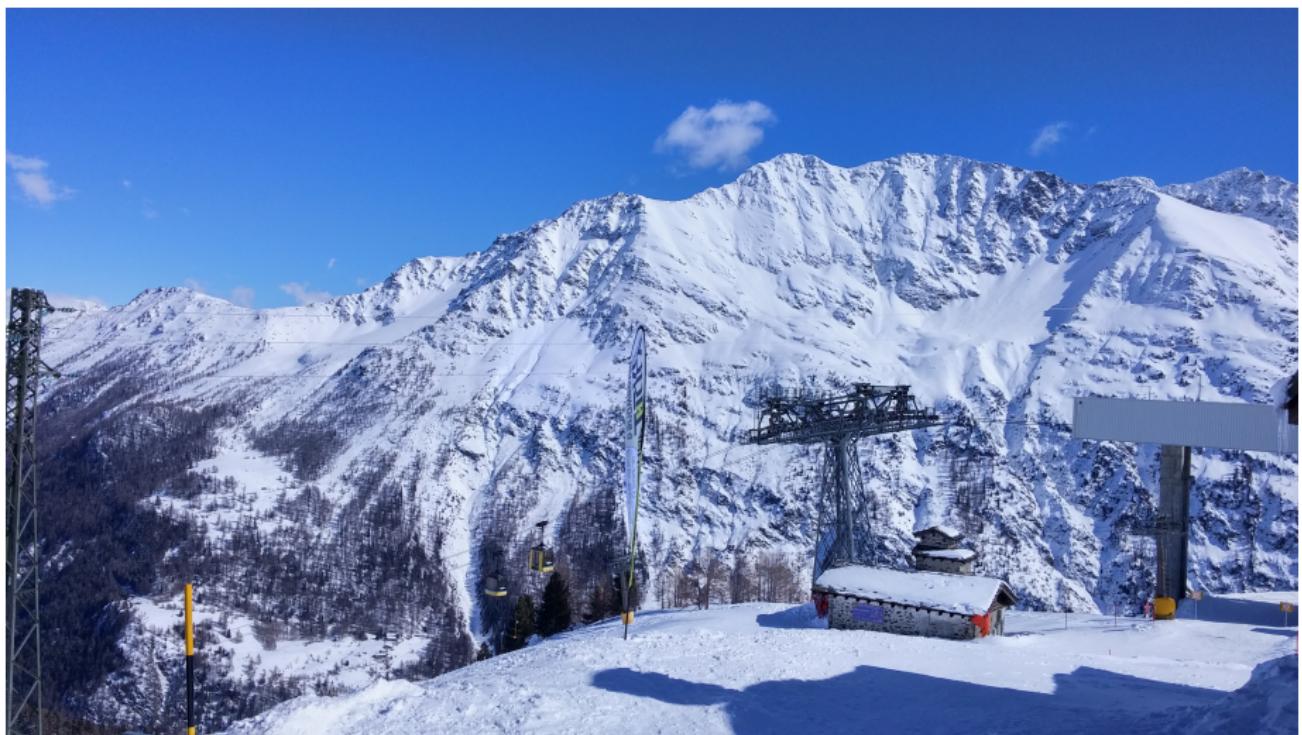
# Conclusions

- ▶ Four-jet differential cross sections were studied for various kinematic and topological variables

## Performance of the predictions:

- ▶ The NLO predictions BlackHat/Sherpa and NJet/Sherpa are mostly compatible with data within theoretical uncertainties, which are found to be large ( $\mathcal{O}(30\%)$  at low momenta) and asymmetric.
- ▶ HEJ, BlackHat/Sherpa and NJet/Sherpa provide good descriptions of the leading jets but disagree with data for  $p_T^{(4)}$
- ▶ Madgraph provides a good description of all variables, although it shows a slope in the jet  $p_T$ 's.
- ▶ Mass & angular variables: BlackHat/Sherpa, NJet/Sherpa, HEJ and Madgraph+Pythia do a remarkable job overall

These measurements expose the shortcomings of  $2 \rightarrow 2$  plus parton shower predictions in a variety of scenarios and highlight the importance of the more sophisticated calculations.



Thank you!

**BACK UP SLIDES**

# Cross-section definitions

## Momentum

variable	definition	cuts
$p_T^{(i)}$	transverse momentum	64/100 GeV - 2 TeV
$H_T$	$\sum_{i=1}^4 p_T^{(i)}$	290 GeV - 7 TeV
$\Sigma p_T^{\text{central}}$	$ p_T^c  +  p_T^d $	$\Delta y_{2j}^{\max} > 1, 2, 3, 4, p_T^{(1)} > 100, 250, 400, 550$

## Mass

$m_{4j}$	$\left( \left( \sum_{i=1}^4 E_i \right)^2 - \left( \sum_{i=1}^4 \mathbf{p}_i \right)^2 \right)^{1/2}$	100 GeV - 7 TeV
$m_{2j}^{\min} / m_{4j}$	$\min_{\substack{i,j \in [1,4] \\ i \neq j}} \left( (E_i + E_j)^2 - (\mathbf{p}_i + \mathbf{p}_j)^2 \right)^{1/2} / m_{4j}$	$m_{4j} > 0.5, 1, 1.5, 2 \text{ TeV}$

## Angular

$\Delta\phi_{2j}^{\min}$	$\min_{\substack{i,j \in [1,4] \\ i \neq j}} ( \phi_i - \phi_j )$	$p_T^{(1)} > 100, 400, 700, 1000 \text{ GeV}$
$\Delta y_{2j}^{\min}$	$\min_{\substack{i,j \in [1,4] \\ i \neq j}} ( y_i - y_j )$	$p_T^{(1)} > 100, 400, 700, 1000 \text{ GeV}$
$\Delta\phi_{3j}^{\min}$	$\min_{\substack{i,j,k \in [1,4] \\ i \neq j \neq k}} ( \phi_i - \phi_j  +  \phi_j - \phi_k )$	$p_T^{(1)} > 100, 400, 700, 1000 \text{ GeV}$
$\Delta y_{3j}^{\min}$	$\min_{\substack{i,j,k \in [1,4] \\ i \neq j \neq k}} ( y_i - y_j  +  y_j - y_k )$	$p_T^{(1)} > 100, 400, 700, 1000 \text{ GeV}$
$\Delta y_{2j}^{\max}$	$\Delta y_{jj}^{\max} = \max_{i,j \in [1,4]} ( y_i - y_j )$	$p_T^{(1)} > 100, 250, 400, 550$

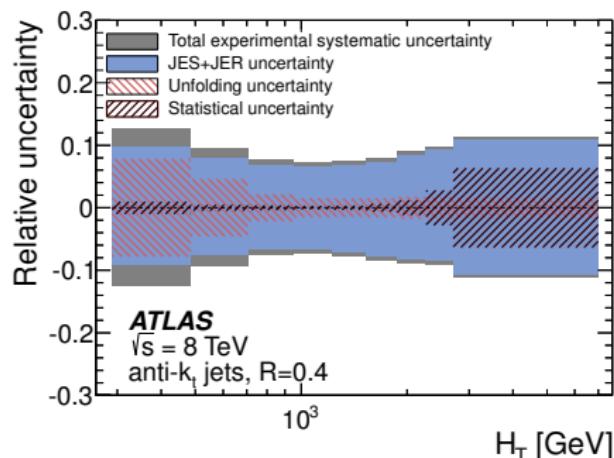
# Uncertainties

## Experimental Uncertainties

- ▶ The Jet Energy Scale, Jet Energy Resolution, Jet Angular Resolution and Luminosity uncertainties were estimated and taken into account.
- ▶ The **JES** is the dominating uncertainty. **Typical size is 4-15%..**

**Unfolding uncertainties** Main component comes from the different MC descriptions of the particle- and reco-level association efficiency. **Typical size is 2-10%**

**Theoretical uncertainties** The scale and PDF uncertainties are obtained for **NJet** and **HEJ**. (Only **NJet**'s are shown.)



# Unfolding Method

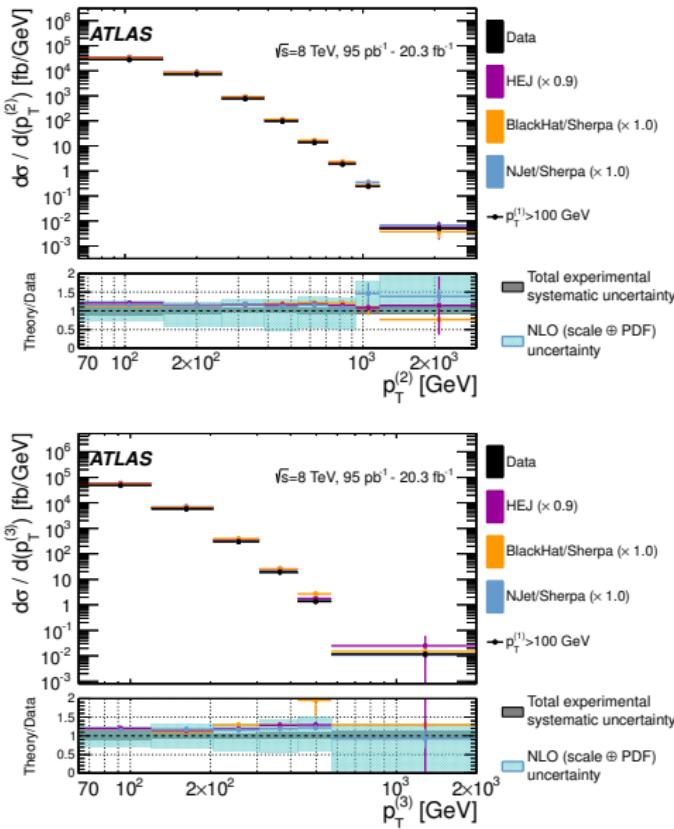
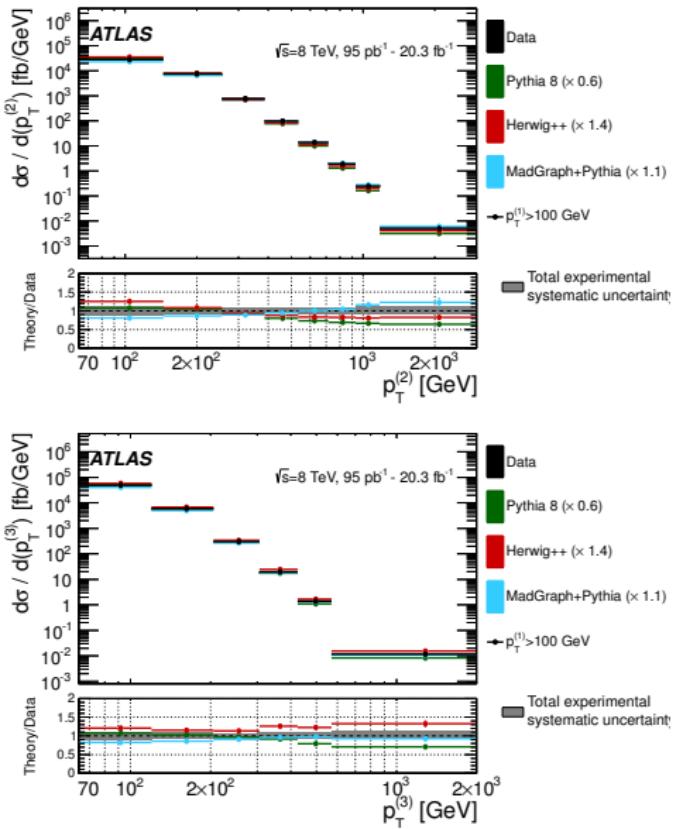
Bayesian Iterative method is used, using 2 iterations. This method corrects for:

- ▶ migrations between bins
- ▶ background events
- ▶ detector inefficiencies

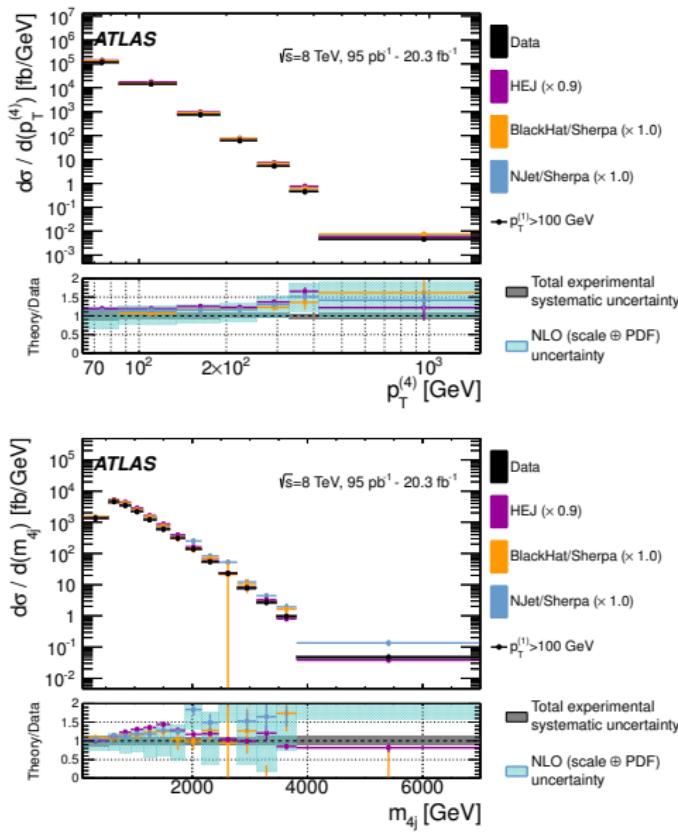
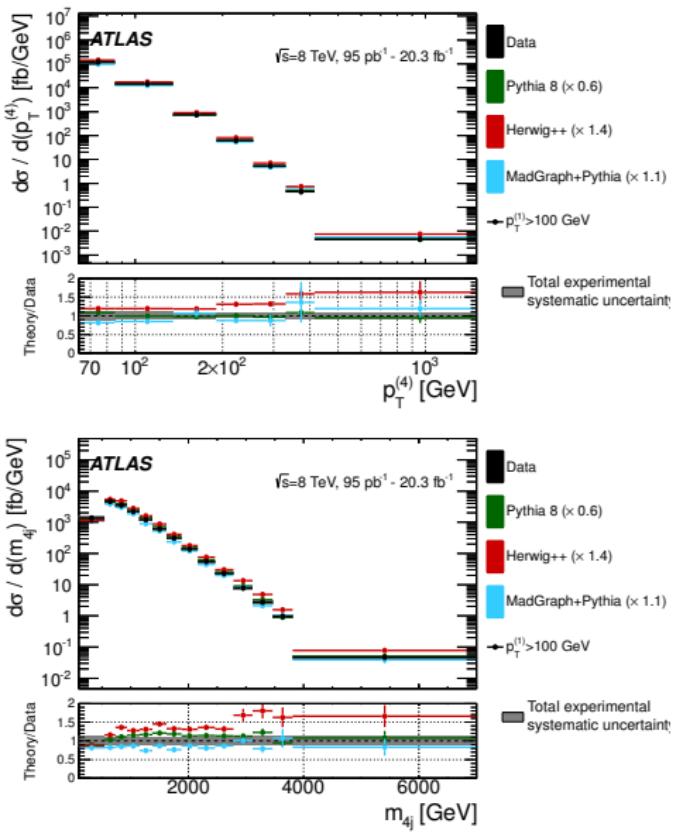
Unfolding matrix built with Pythia, with event by event reco-level and particle-level matching. No jet-by-jet spatial matching is applied.

Binning was determined to get a bin by bin purity between 70 and 90%, and a statistical uncertainty in data below 10%

# Results: $p_T^{(2)}$ and $p_T^{(3)}$

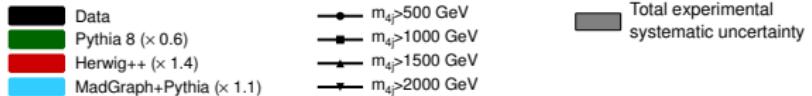
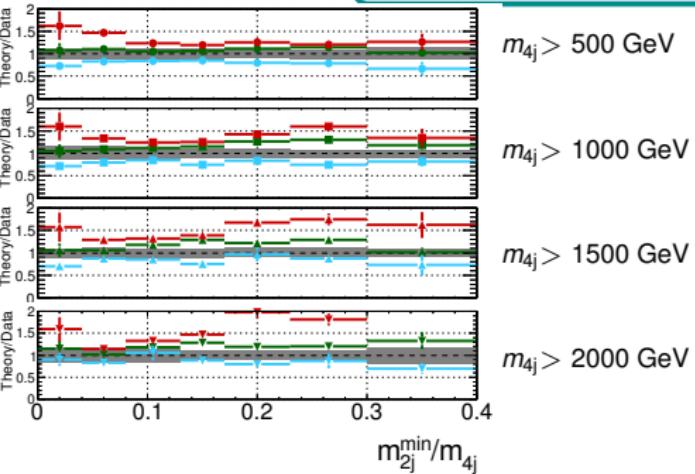
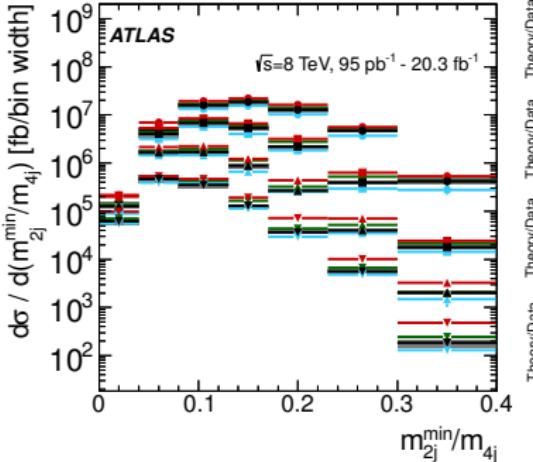


# Results: $p_T^{(4)}$ and $m_{4j}$



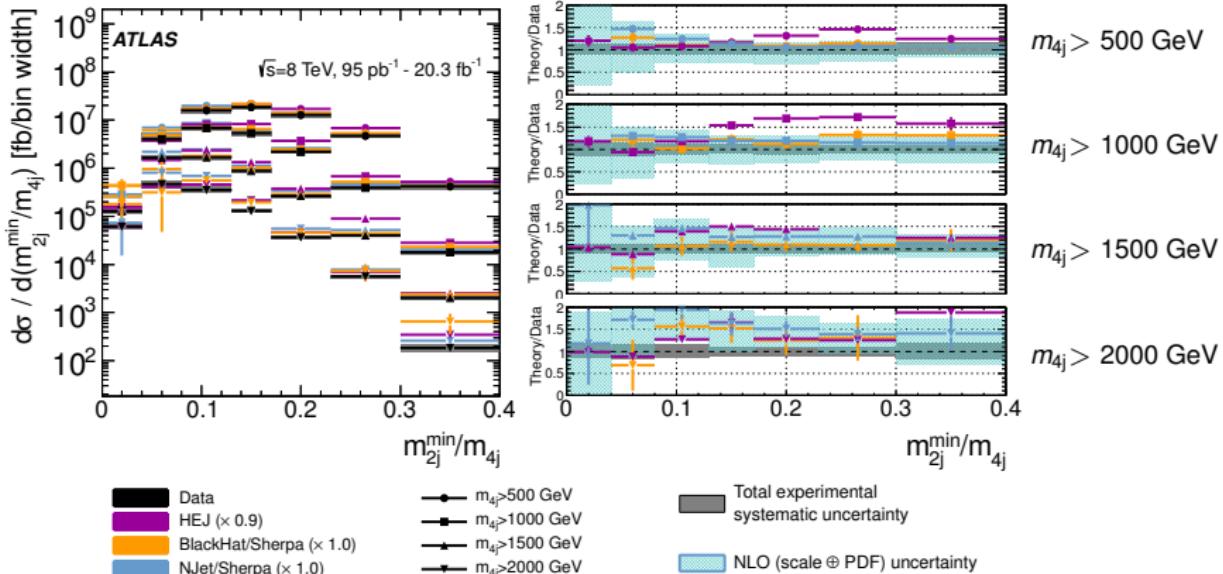
# Results: Mass Variables - LO

$$\frac{m_{2j}^{\min}}{m_{4j}} = \frac{\text{minimum 2 jet mass}}{m_{4j}}$$



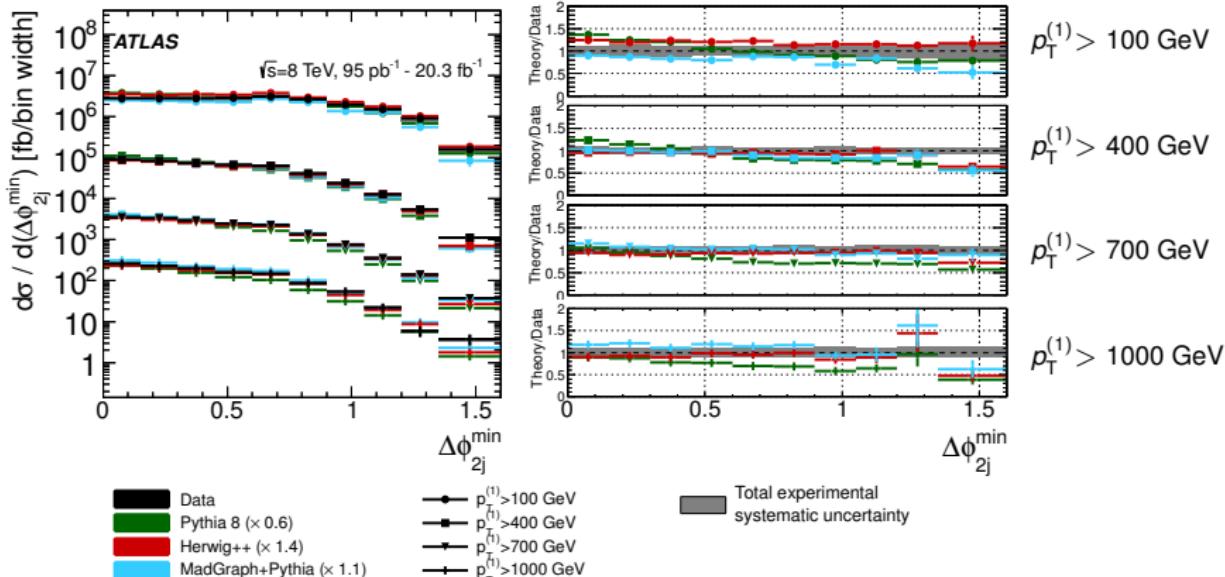
- Mass variables are sensitive to the separation between the jets
- $m_{4j} > 1 \text{ TeV}$  is well described by the LO predictions, particularly Madgraph, but normalisation is off by 20-40%.
- Pythia and Herwig overestimate the events for low  $m_{2j}^{\min}/m_{4j}$ , worse for higher  $m_{4j}$ .
- $m_{2j}^{\min}/m_{4j}$  is well described by Madgraph for all  $m_{4j}$  cuts, providing the best description for mass variables.

# Results: Mass Variables - NLO and HEJ

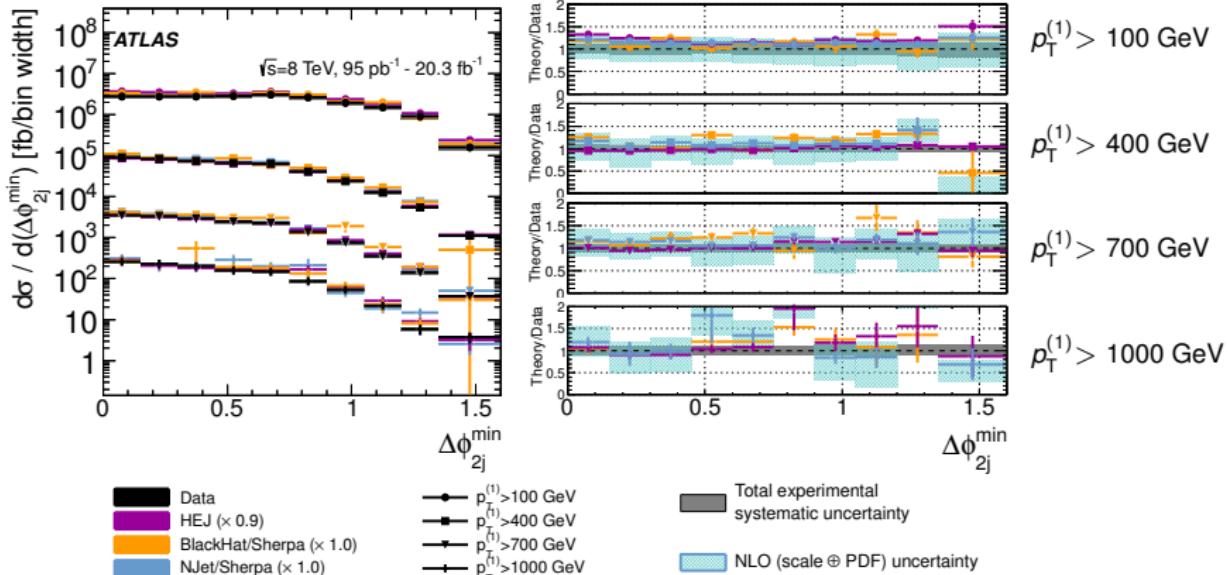


- ▶  $m_{4j}$  is well described by HEJ and NJet, though presenting a bump structure.
- ▶  $m_{2j}^{\min}/m_{4j}$  is well described by HEJ at low  $m_{4j}$ , differences are covered by the large theoretical uncertainties.
- ▶ NJet overestimates the first bin values, but otherwise agrees with data within uncertainties

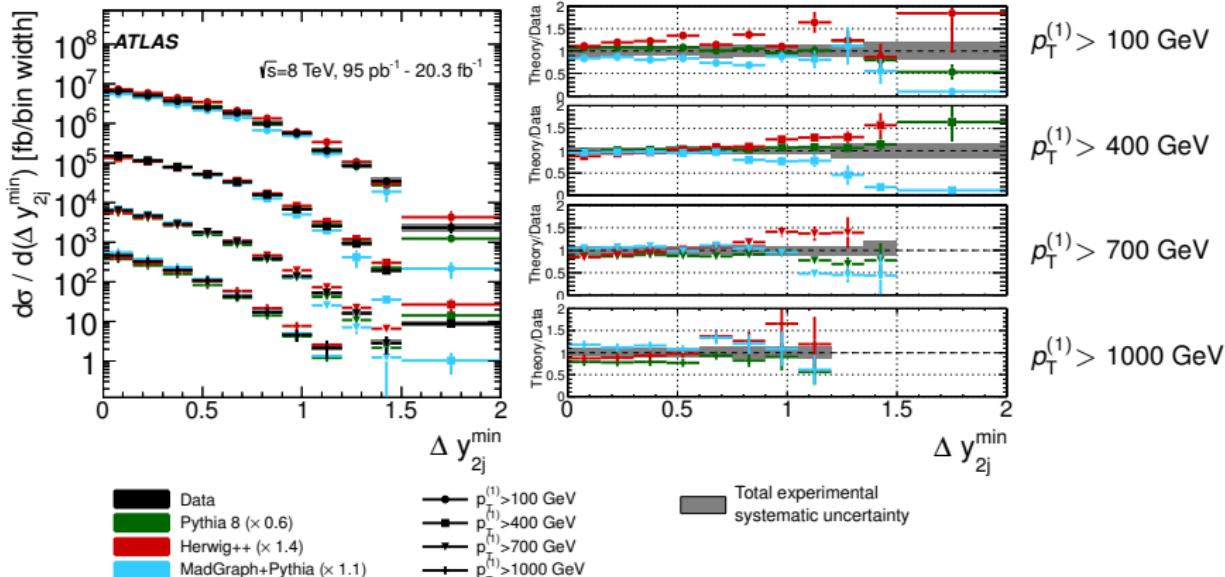
# Results: $\Delta\phi_{2j}^{\min}$ - LO predictions



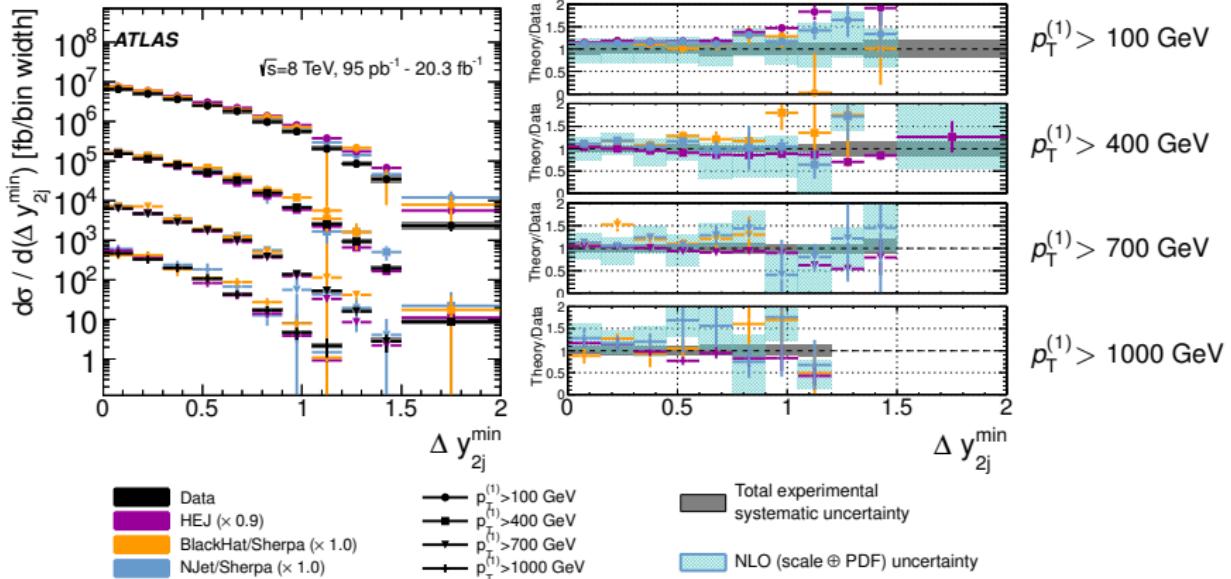
# Results: $\Delta\phi_{2j}^{\min}$ - NLO and HEJ



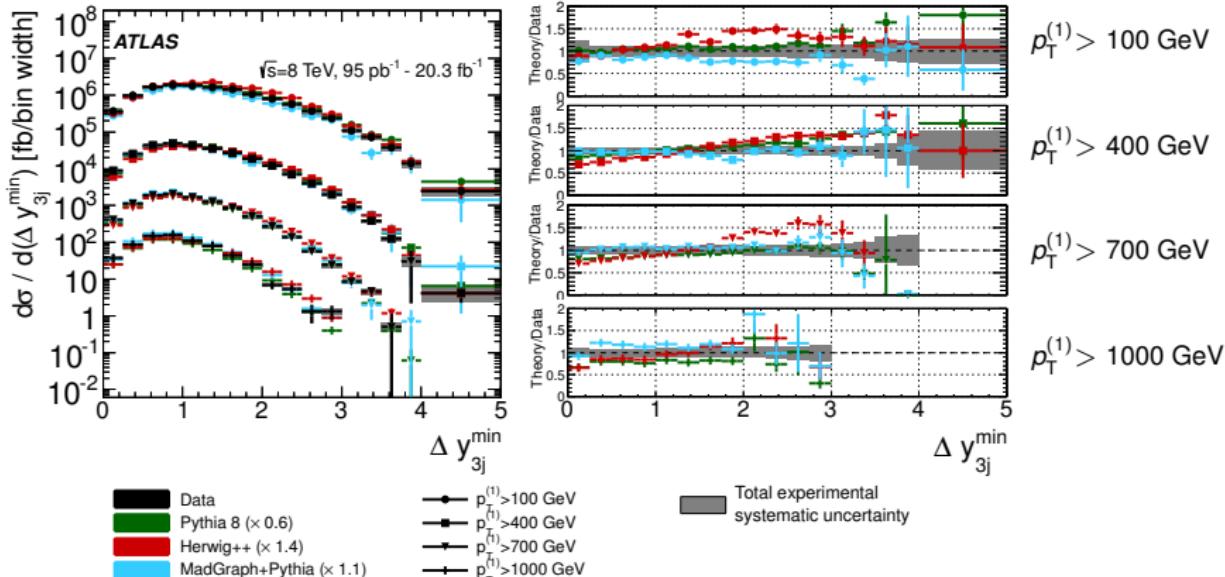
# Results: $\Delta y_{2j}^{\min}$ - LO predictions



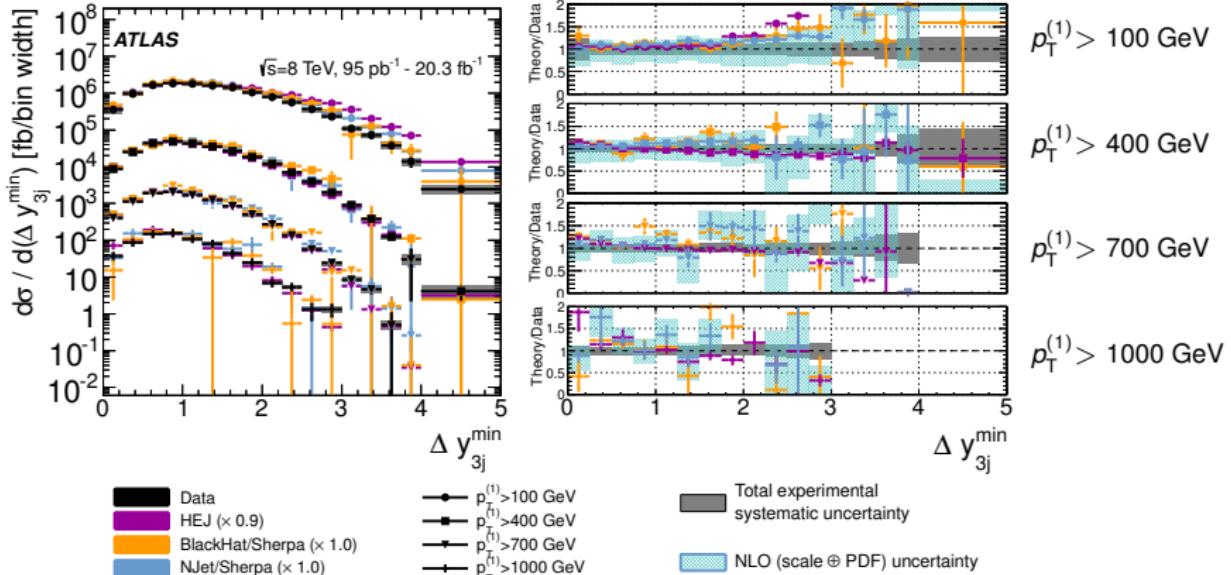
# Results: $\Delta y_{2j}^{\min}$ - NLO and HEJ



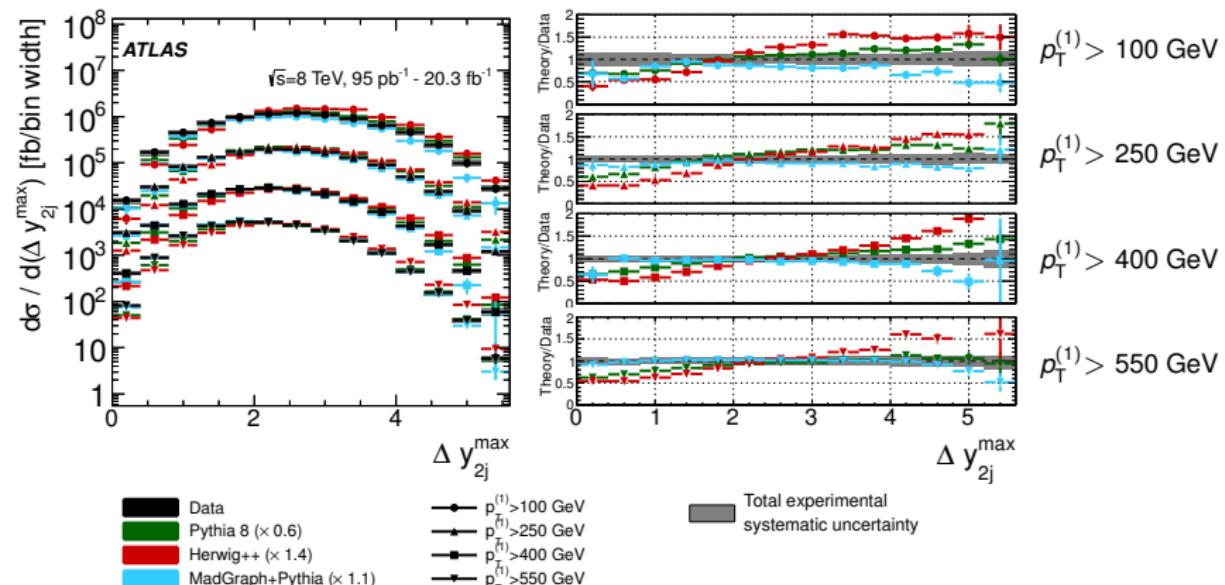
# Results: $\Delta y_{3j}^{\min}$ - LO predictions



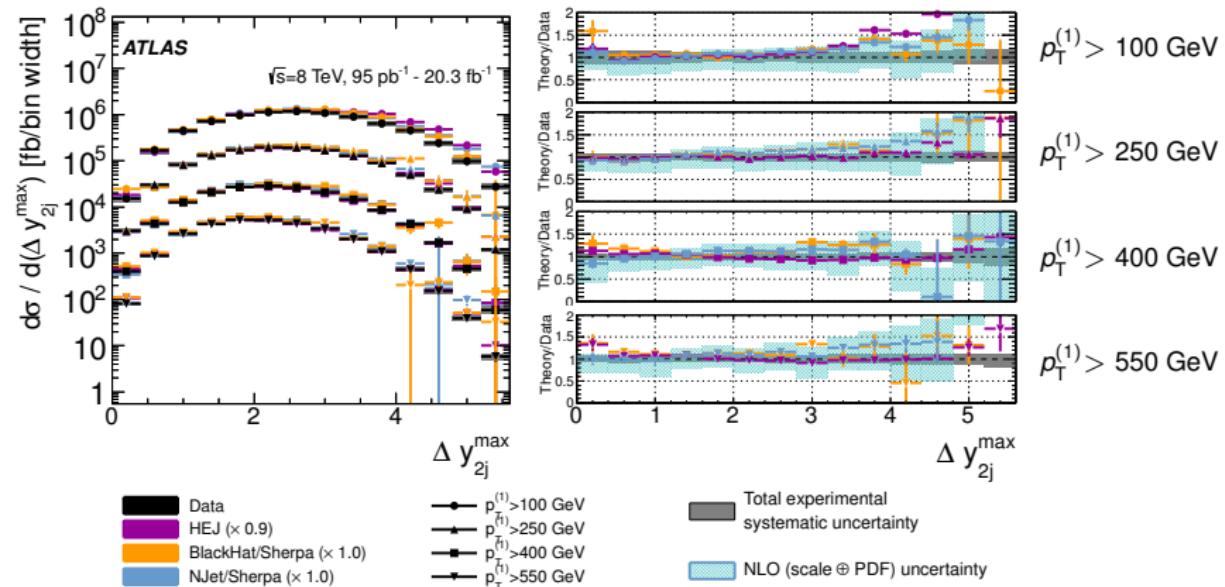
# Results: $\Delta y_{3j}^{\min}$ - NLO and HEJ



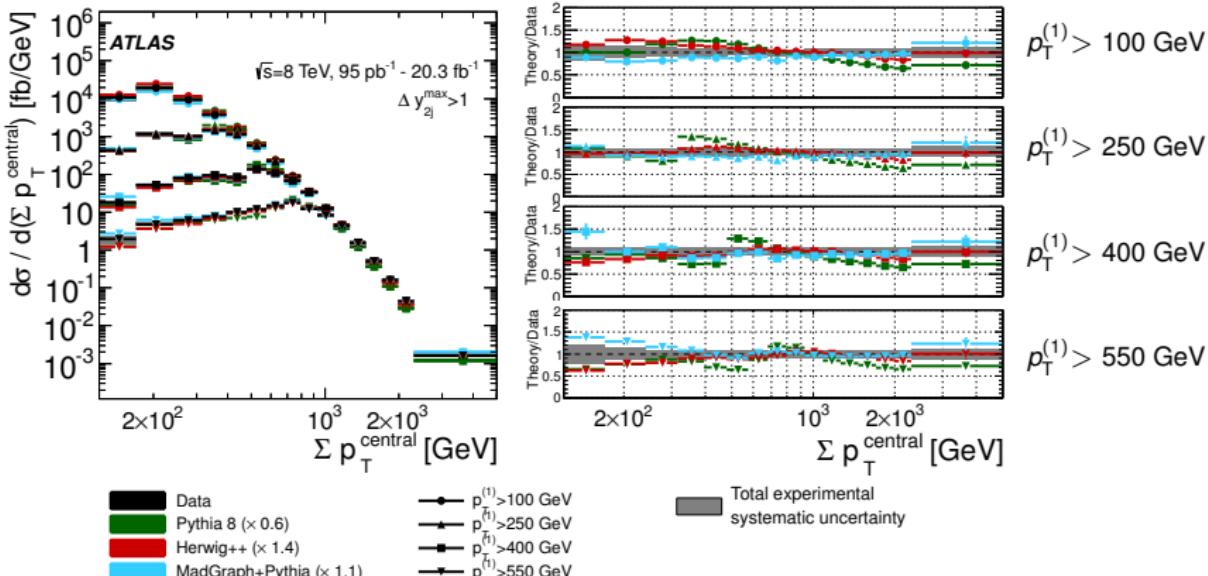
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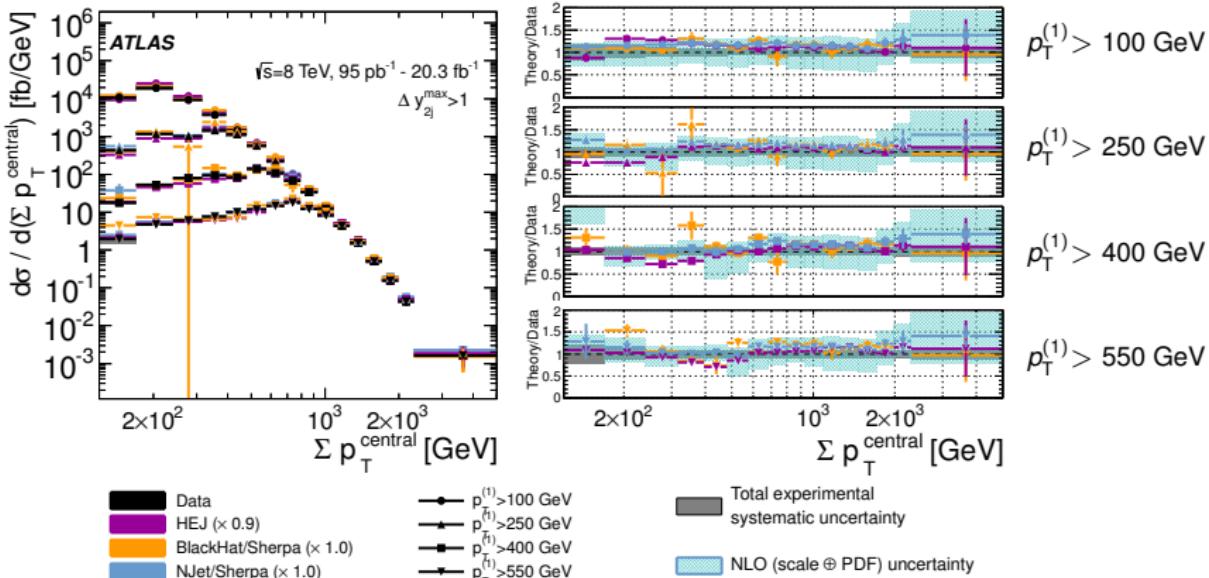
# Results: $\Delta y_{2j}^{\max}$ - NLO and HEJ



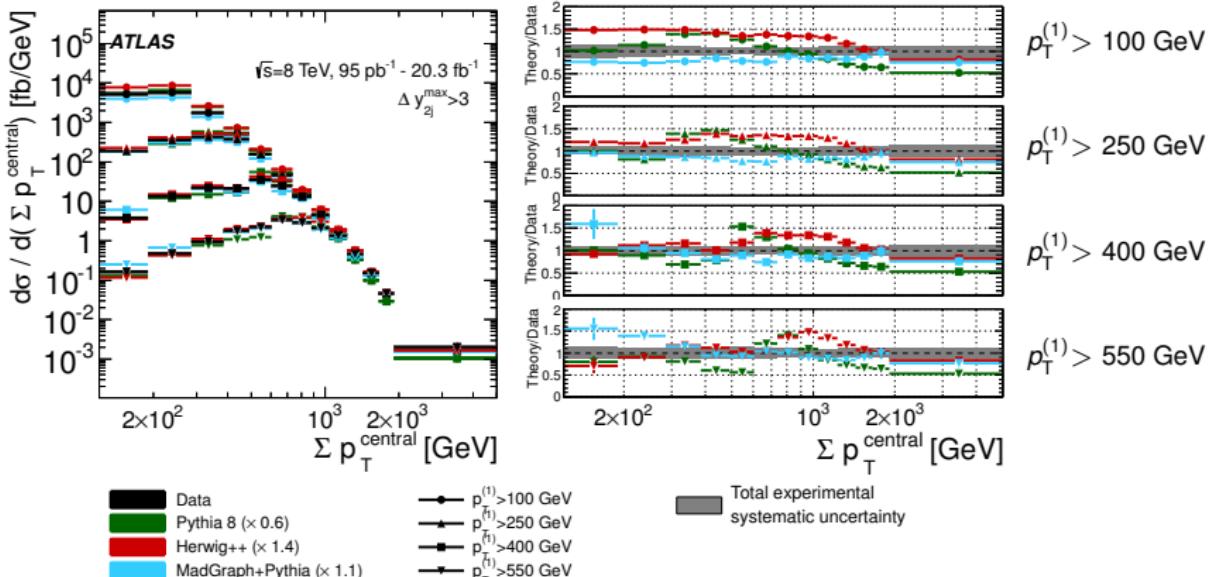
# Results: $\sum p_T^{\text{central}}$ for $\Delta y_{2j}^{\max} > 1$ - LO predictions



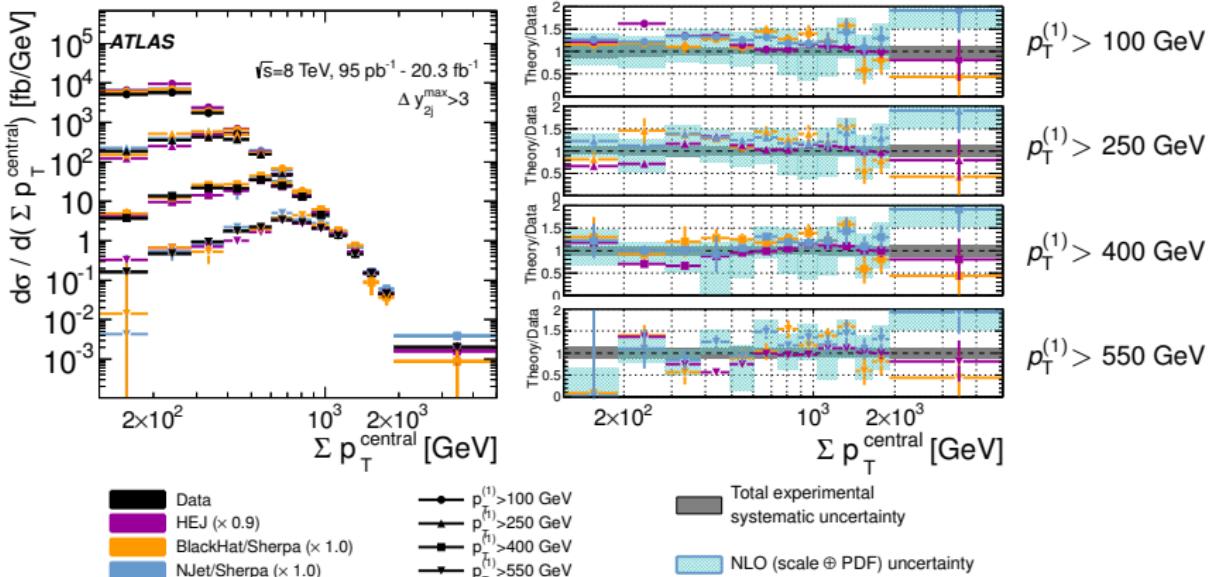
# Results: $\sum p_T^{\text{central}}$ for $\Delta y_{2j}^{\max} > 1$ - NLO and HEJ



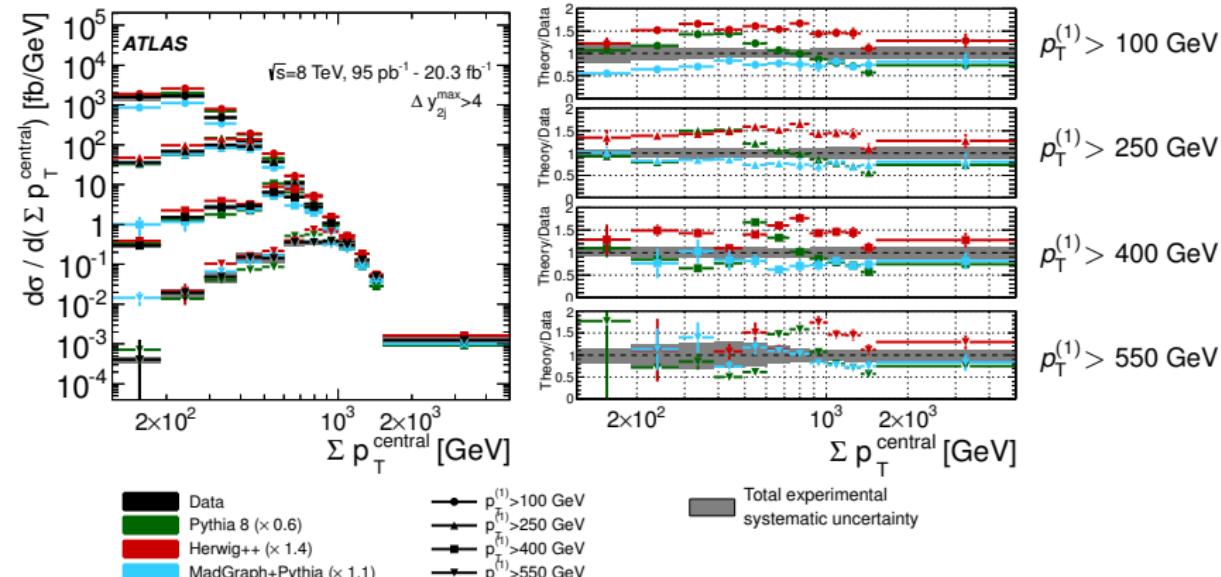
# Results: $\sum p_T^{\text{central}}$ for $\Delta y_{2j}^{\max} > 3$ - LO predictions



# Results: $\sum p_T^{\text{central}}$ for $\Delta y_{2j}^{\max} > 3$ - NLO and HEJ



# Results: $\sum p_T^{\text{central}}$ for $\Delta y_{2j}^{\max} > 4$ - LO predictions



# Results: $\sum p_T^{\text{central}}$ for $\Delta y_{2j}^{\max} > 4$ - NLO and HEJ

