

Test I

• Test 2

Test III

Two OLD methods to
measure
the electron-neutrino
MASS

$$Z[i] \rightarrow (Z+1)[f] + e^- + \bar{\nu}_e$$

$$\frac{d\Gamma}{dE_e} = \frac{1}{2}\,|\mathcal{M}|^2\,F(E_e)\,\Phi, \quad Q \equiv M_i - M_f$$

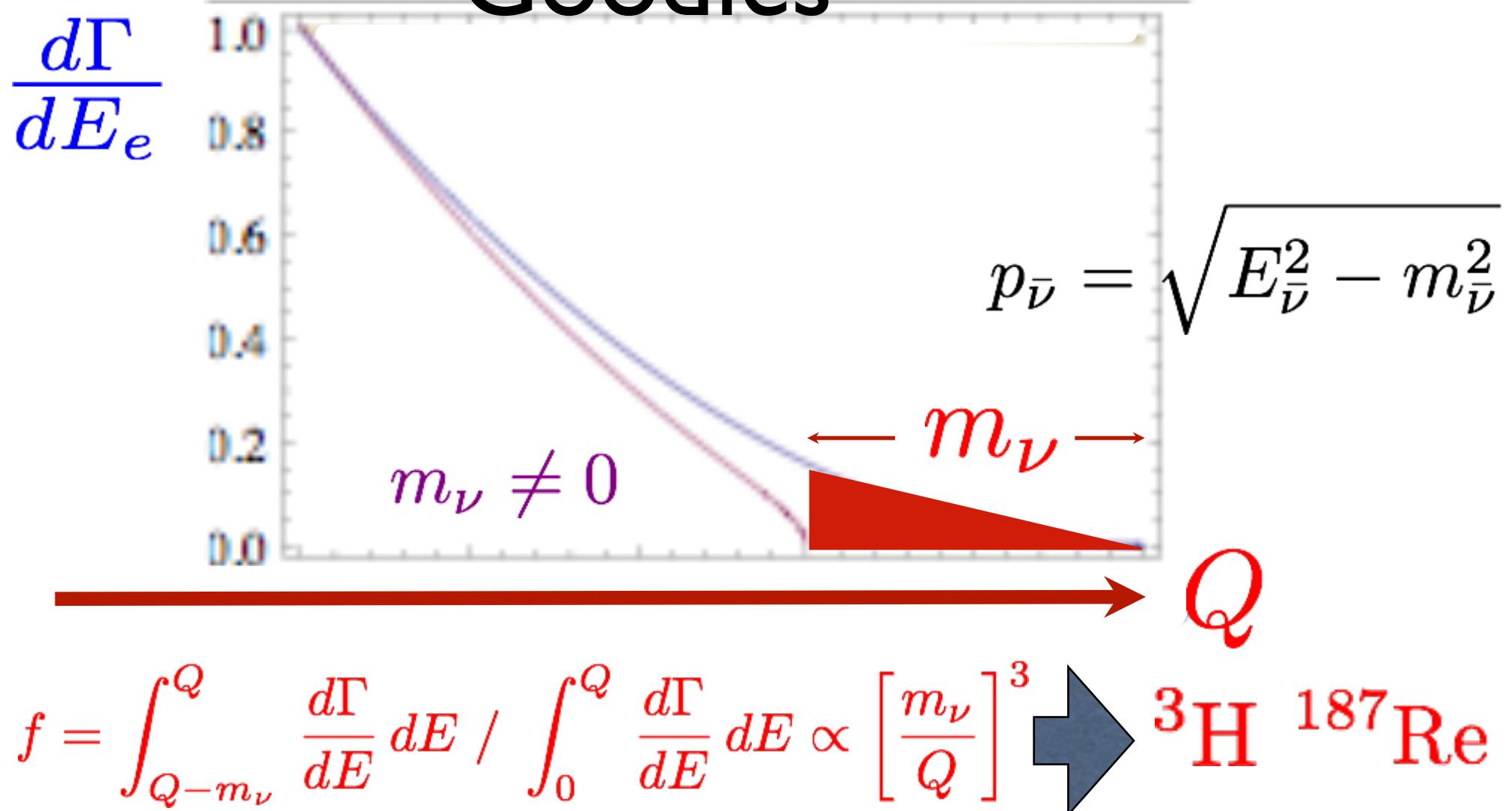
$$|\mathcal{M}|^2 \approx 32\,G_F^2\,\cos^2\theta_C\,M_i\,M_f |\mathcal{M}_N|^2 E_e\,E_{\bar{\nu}}$$

$$F(E_e) : \text{ Fermi function } \qquad n : \uparrow 1 + 3\,g_A^2$$

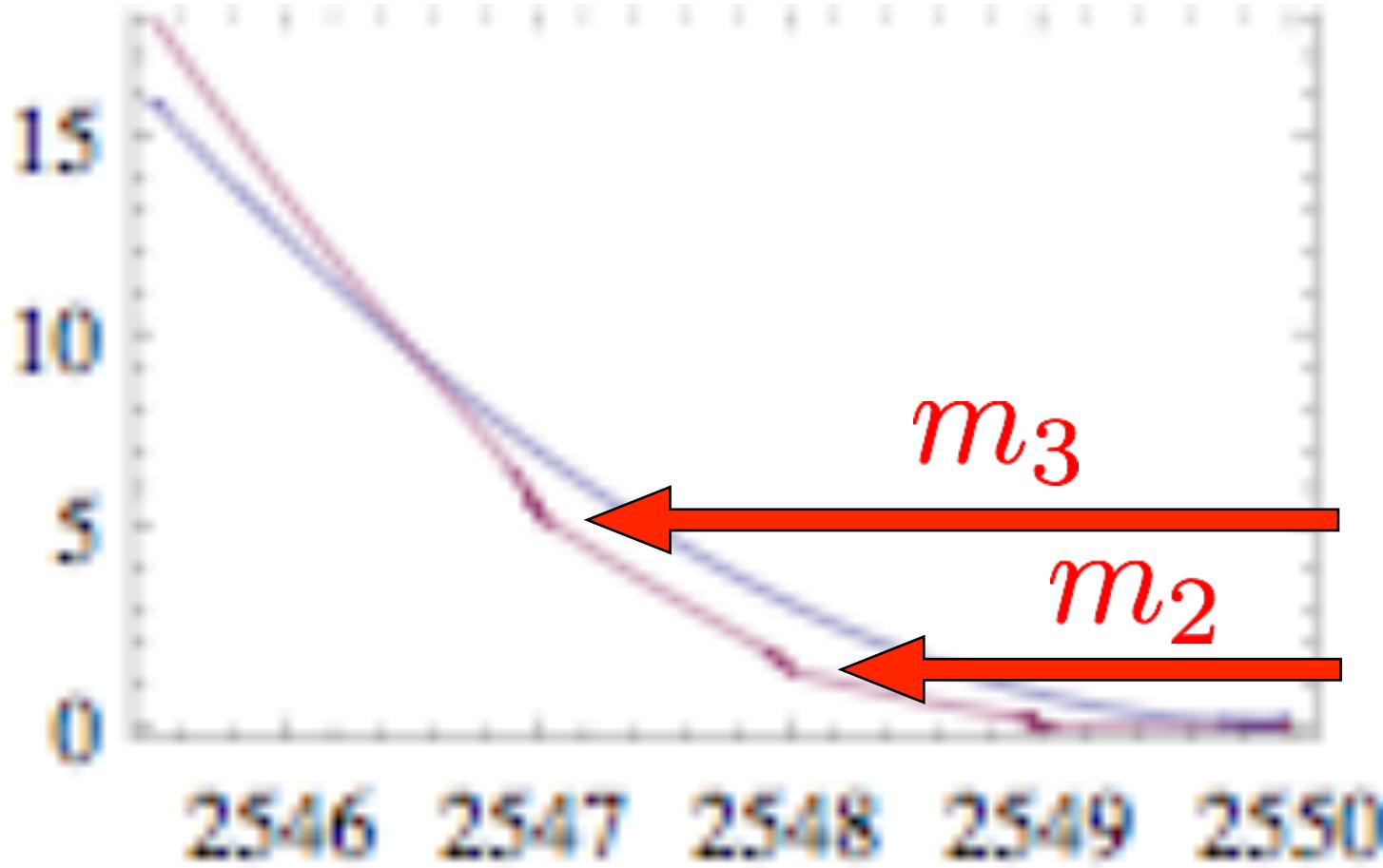
$$\Phi_3 = \frac{1}{8\,\pi^3}\,\frac{p_e\,p_{\bar{\nu}}}{M_i\,M_f},$$

$$p_{\bar{\nu}} = \sqrt{E_{\bar{\nu}}^2 - m_{\bar{\nu}}^2}\,, \quad E_{\bar{\nu}} = Q - E_e$$

Fraction f of “Goodies”



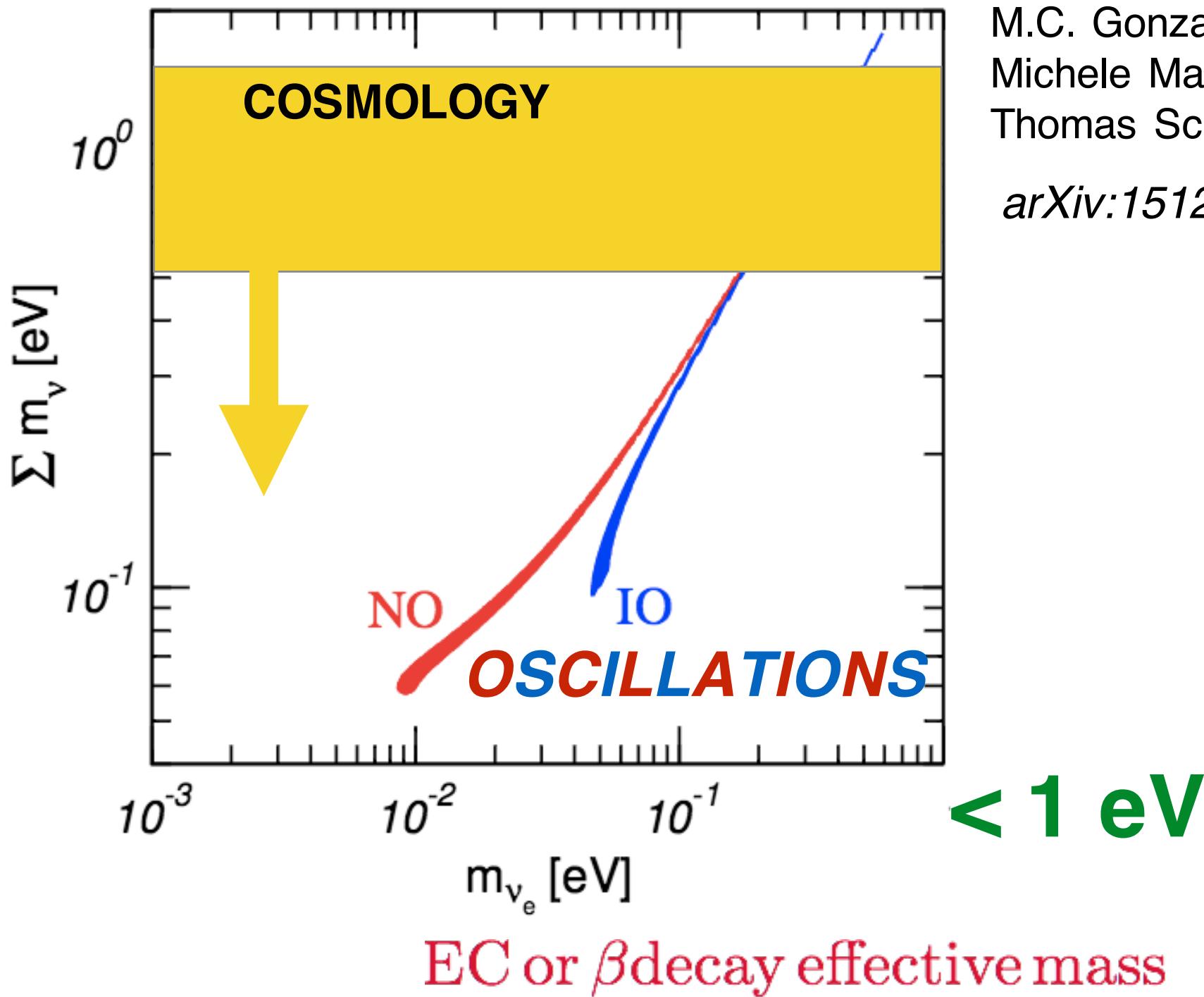
“Difficulty” $\propto 1/m_{\bar{\nu}}^3$ Q in keV 18.6 2.47

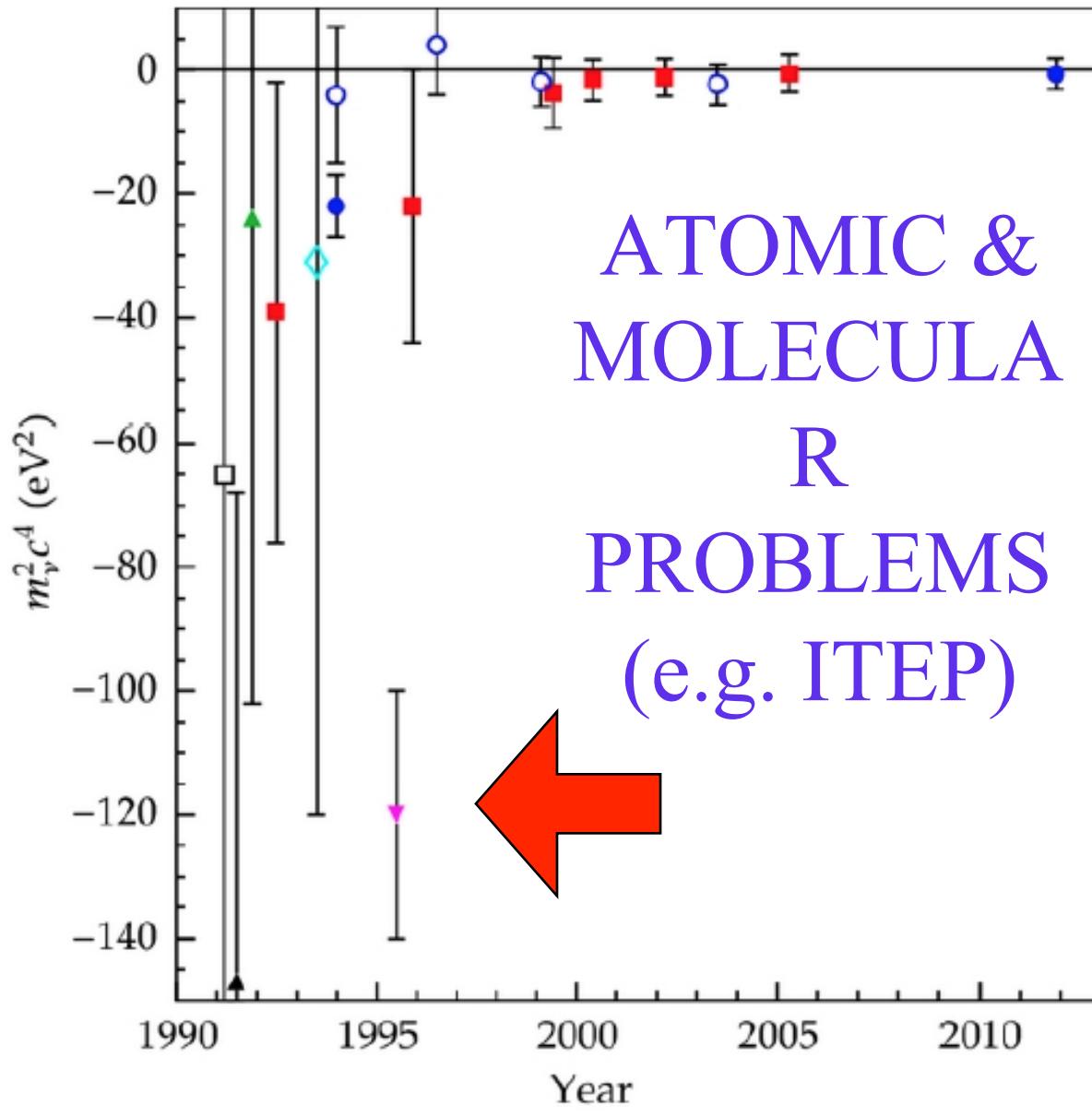


$$m_\beta = \sqrt{\sum_i |U_{ei}|^2 m_i} \quad \text{if unresolved}$$

M.C. Gonzalez-Garcia,
Michele Maltoni,
Thomas Schwetz

arXiv:1512.06856





- ◊ Beijing
- ▼ Livermore
- ▲ Los Alamos
- Mainz

- Tokyo
- Troitsk
- Troitsk step fcn
- ▲ Zuerich

$m_{\bar{\nu}} < 2.3 \text{ eV}$
(95% C.L.)

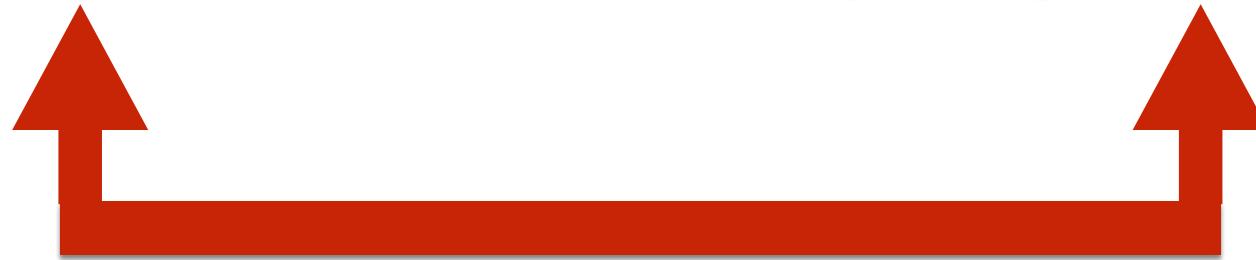
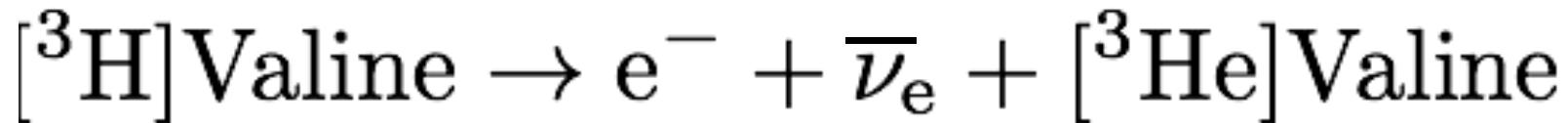
(Mainz)

$m_{\bar{\nu}} < 2.05 \text{ eV}$
(95% C.L.)

(Troitsk)

ATOMIC & MOLECULAR PROBLEMS

??
ITEP experiment

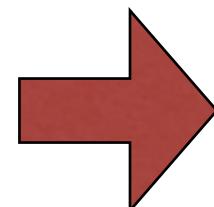


$$E_\nu + E_e = Q = \Delta M$$



**Spectrum = Sum of spectra
with different endpoints**

KATRIN,
Project 8

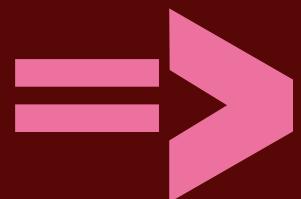


Gaseous ${}^3\text{H}_2$

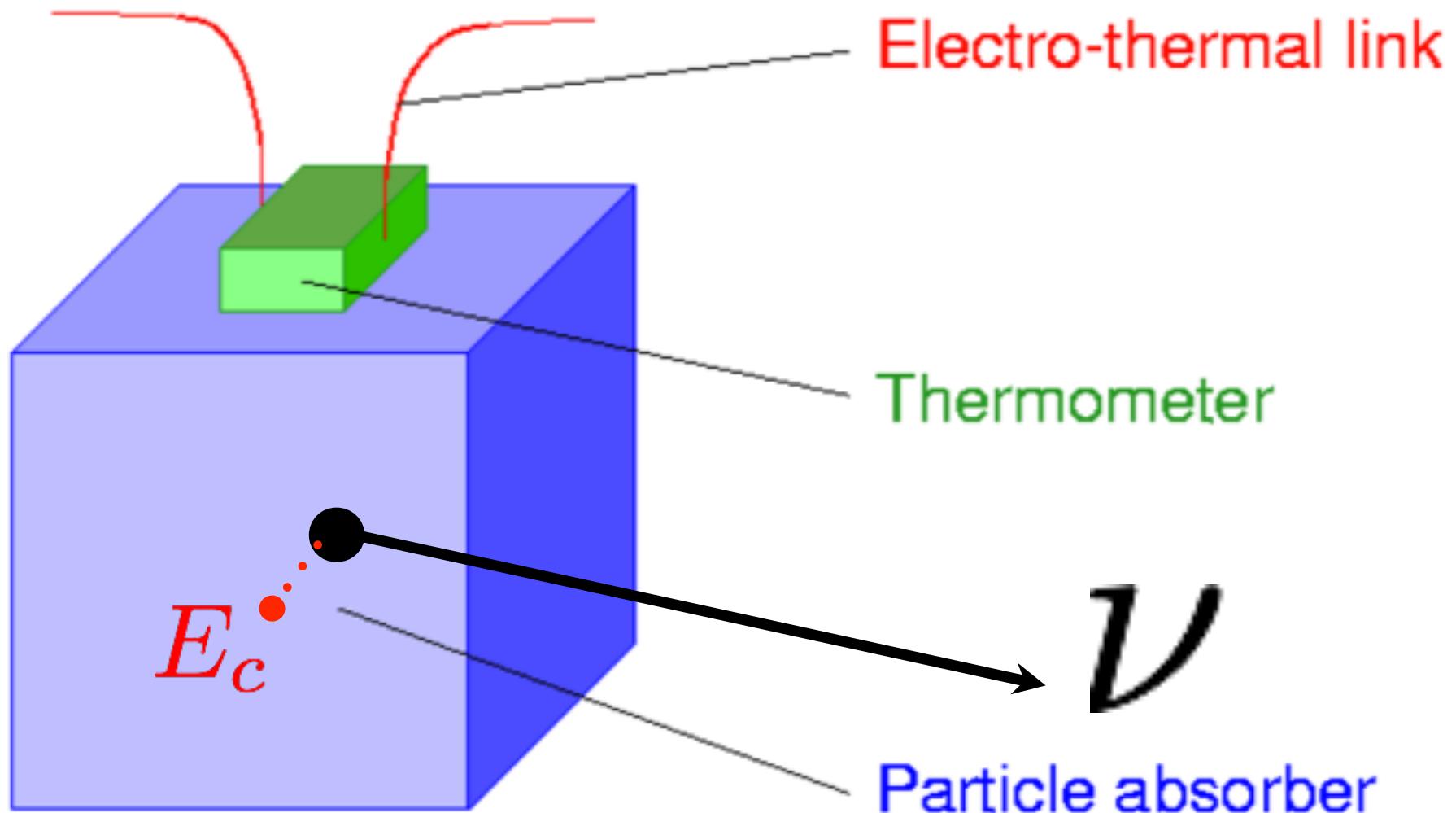


KATRIN on her way

**A UNIQUE Q
for ALL
DECAYS ?**



CALORIMETRY



$$D[\text{before}] \rightarrow D[\text{after}] + E_c + \nu$$

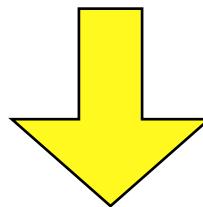
3-body phase space, as in beta decay

$Q = \text{MD}[\text{before}] - \text{MD}[\text{after}]$ *Indep. of decay chain*

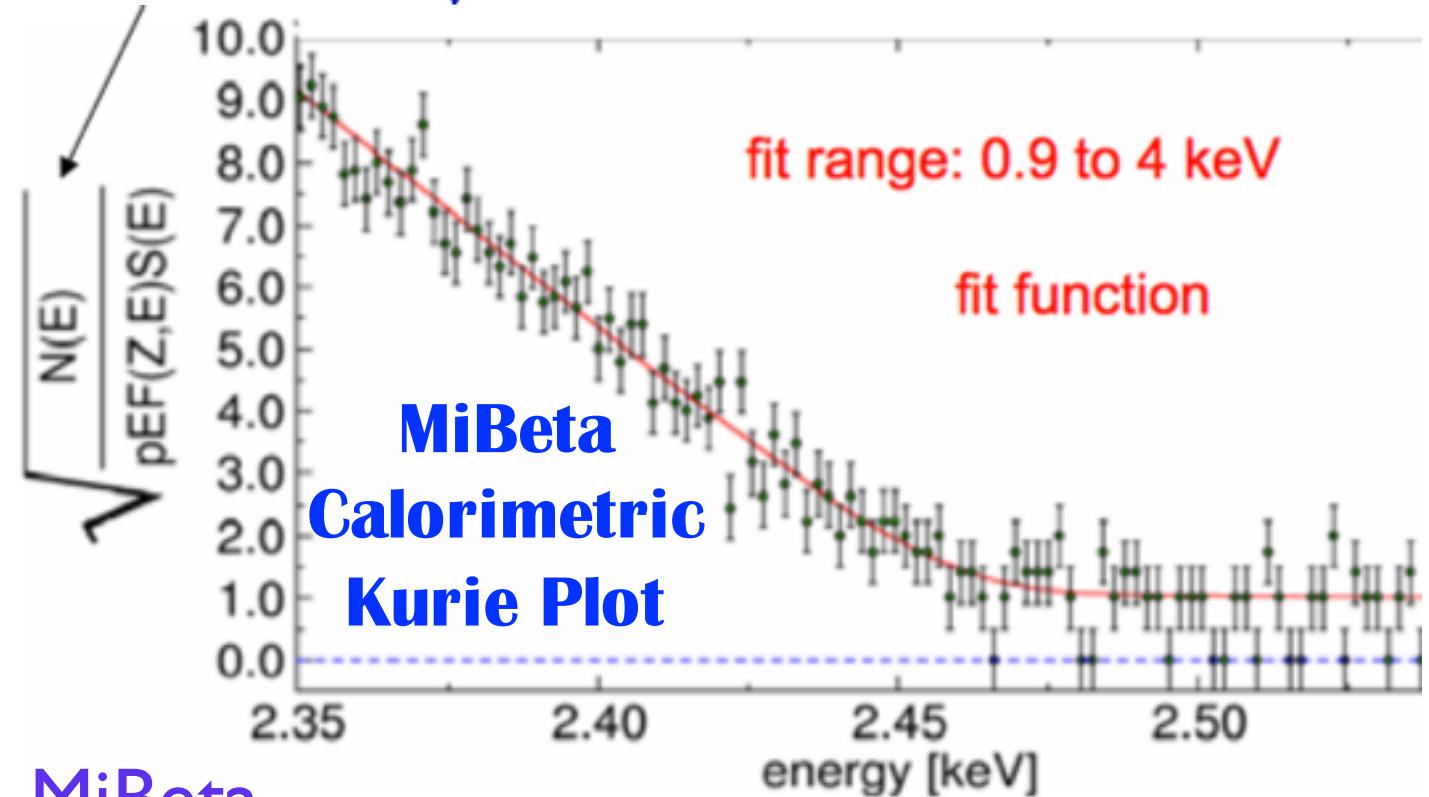
$$K(E_e) \equiv \sqrt{\frac{d\Gamma}{F(E_e) p_e E_e dE_e}} \propto \sqrt{E_{\bar{\nu}} p_{\bar{\nu}}}$$

$$= \sqrt{(Q - E_e) \sqrt{(Q - E_e)^2 - m_{\bar{\nu}}^2}}$$

$^{187}\text{Re}(5/2)^+$



$^{187}\text{Os}(1/2)^-$



MaNu
(Genova)

MiBeta

(Milano/Como) $m_{\bar{\nu}} < 15.6 \text{ eV} \text{ (90\% C.L.)}$

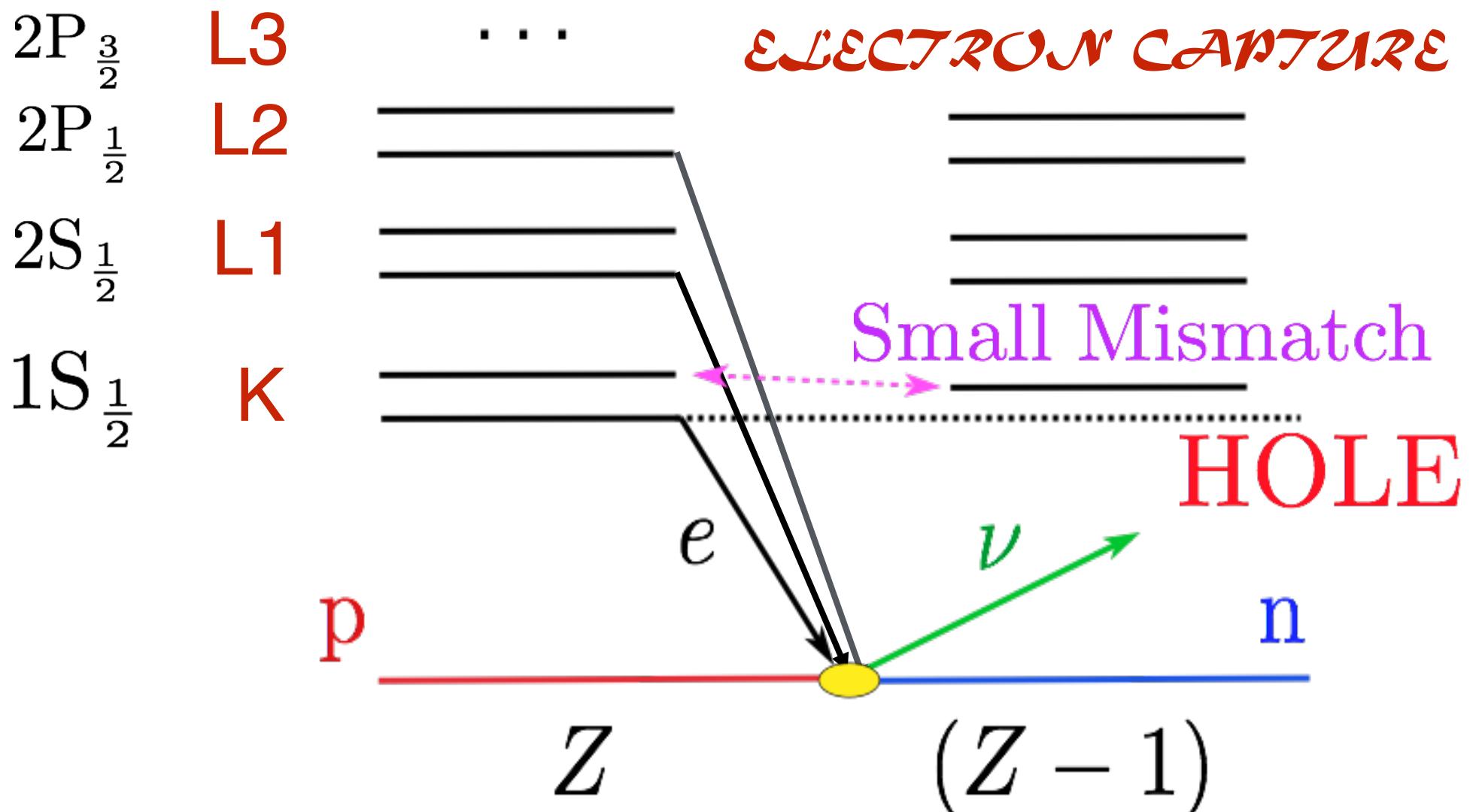
Atomic beta decay by electron capture

The e-neutrino mass(es)
Calorimetric measurements

Maurizio Lusignoli

ADR, Maurizio Lusignoli 1982

Experimental Progress, e.g.: Galeazzi et al.,
Ranitsch et al., Gastaldi et al.,
Sisti et al., Nuccioti et al., Eliseev et al...



Requires $\varphi_{\text{H}}(0) \neq 0$

Small-component
 $\mathcal{O}(\alpha Z)$ mixing

$$n l_j = n S_{1/2}$$

$$n l_j = n P_{1/2} \leftrightarrow n S_{1/2}$$

$$Z \rightarrow (Z - 1)^H + \nu$$

$$\begin{aligned} M_Z &= M_{Z-1} + E_H + E_\nu \\ &> 0 \end{aligned}$$

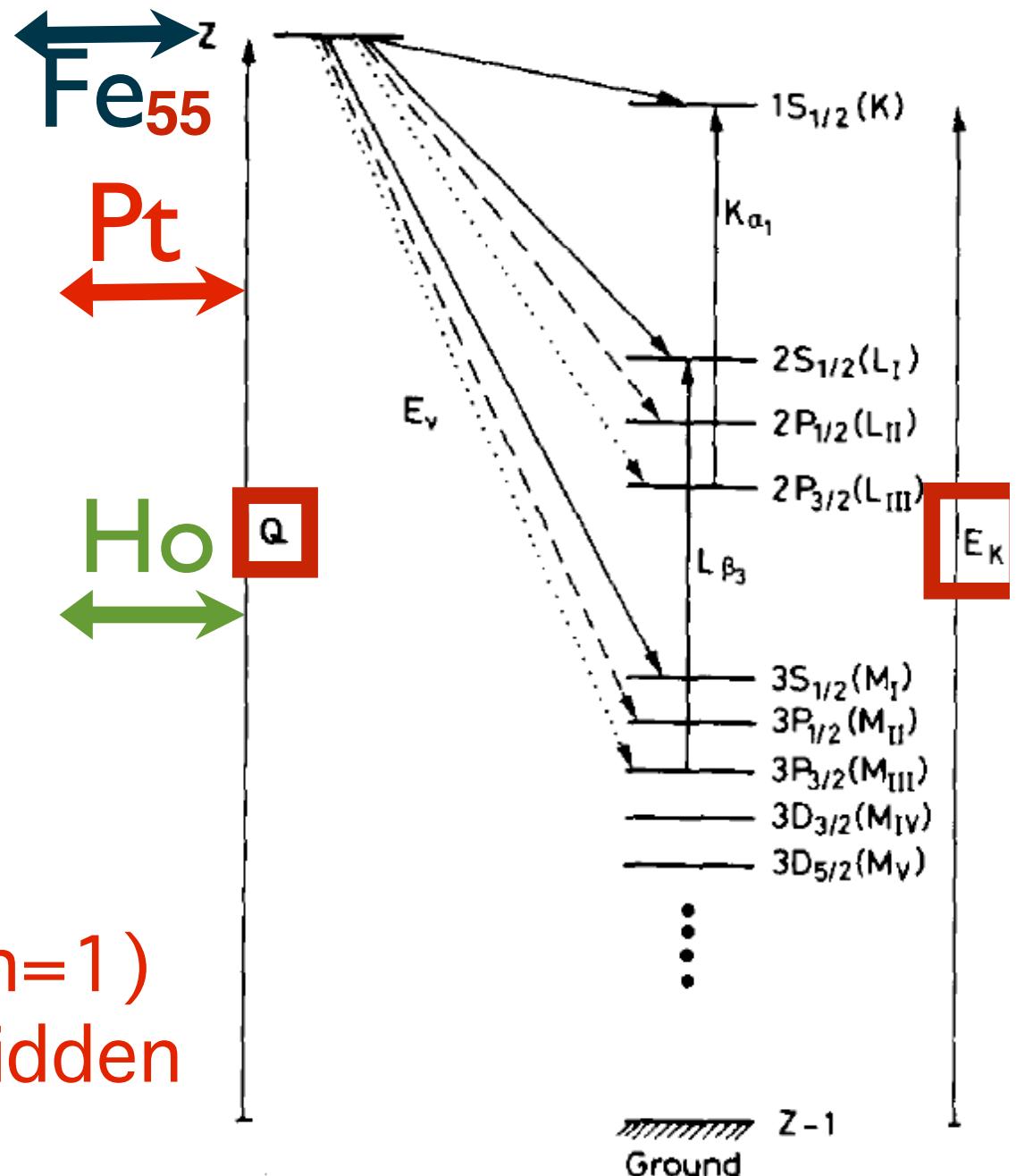
$$\begin{aligned} Q &\equiv M_Z - M_{Z-1} \\ &= E_H + E_\nu \end{aligned}$$

$$E_H \pm i\Gamma_H \rightarrow E_c$$

\sum Holes

$^{193}_{78}\text{Pt}$ K ($n=1$)
 forbidden

$^{163}_{67}\text{Ho}$ K, L ($n=1,2$) forbidden

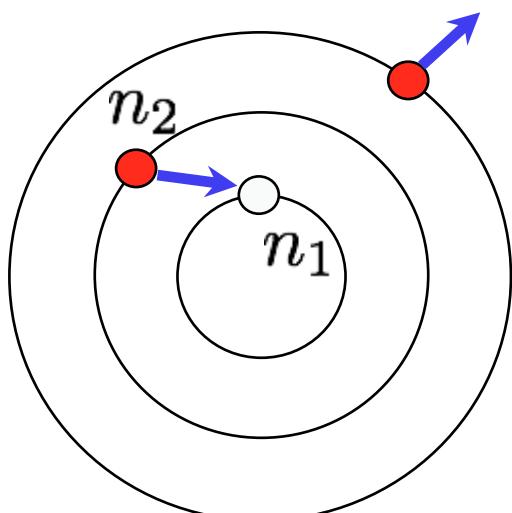


$$Z \rightarrow (Z - 1)^H + \nu$$

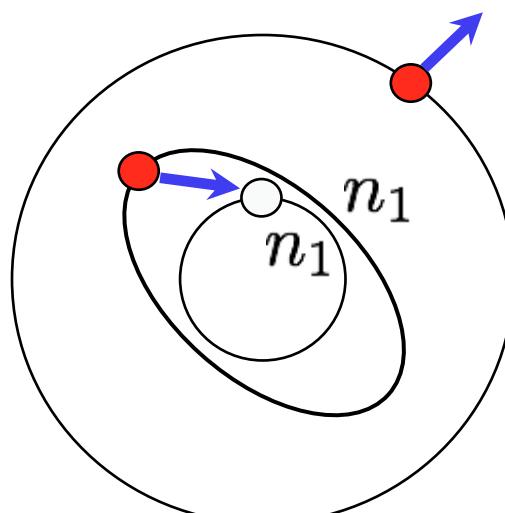
H decay ?

In a [clean] calorimetric measurement all endpoints of all decay channels coincide at $E_c = Q = MD[\text{before}] - MD[\text{after}] - m_\nu$

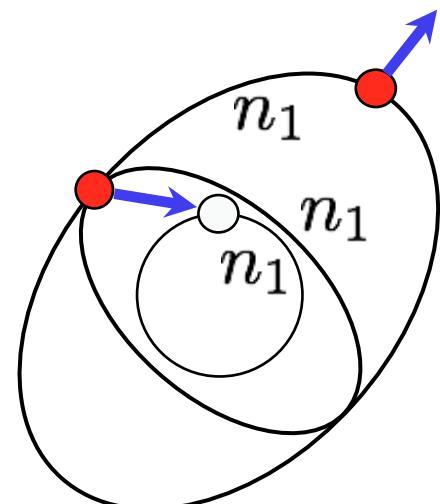
This includes all photon- or electron-emission atomic de-excitations



Auger

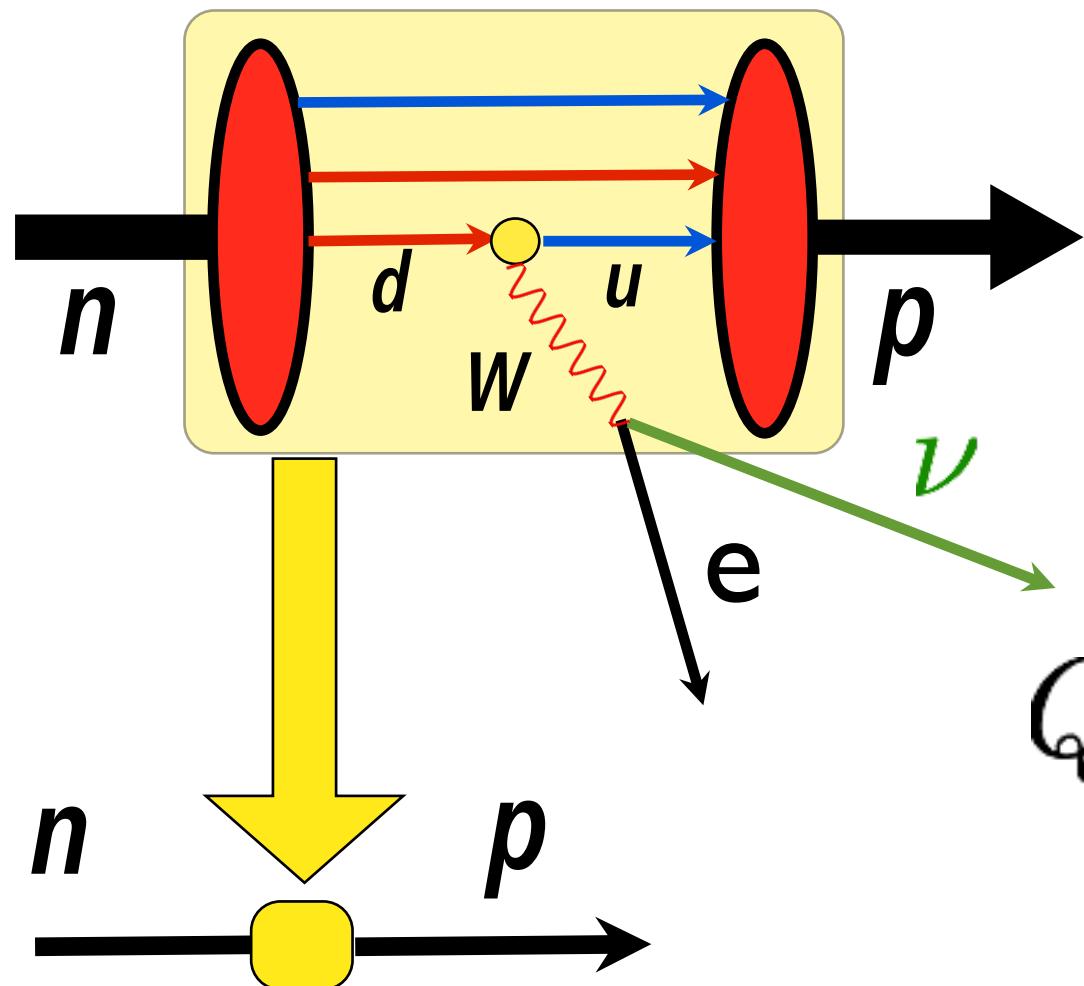


Coster-Kronig



Super-Coster-Kronig

“Effective” neutron-decay theory



*High spacial
resolution totally
UNNECESSARY*

$$Q = m_n - m_p$$

PROCEED

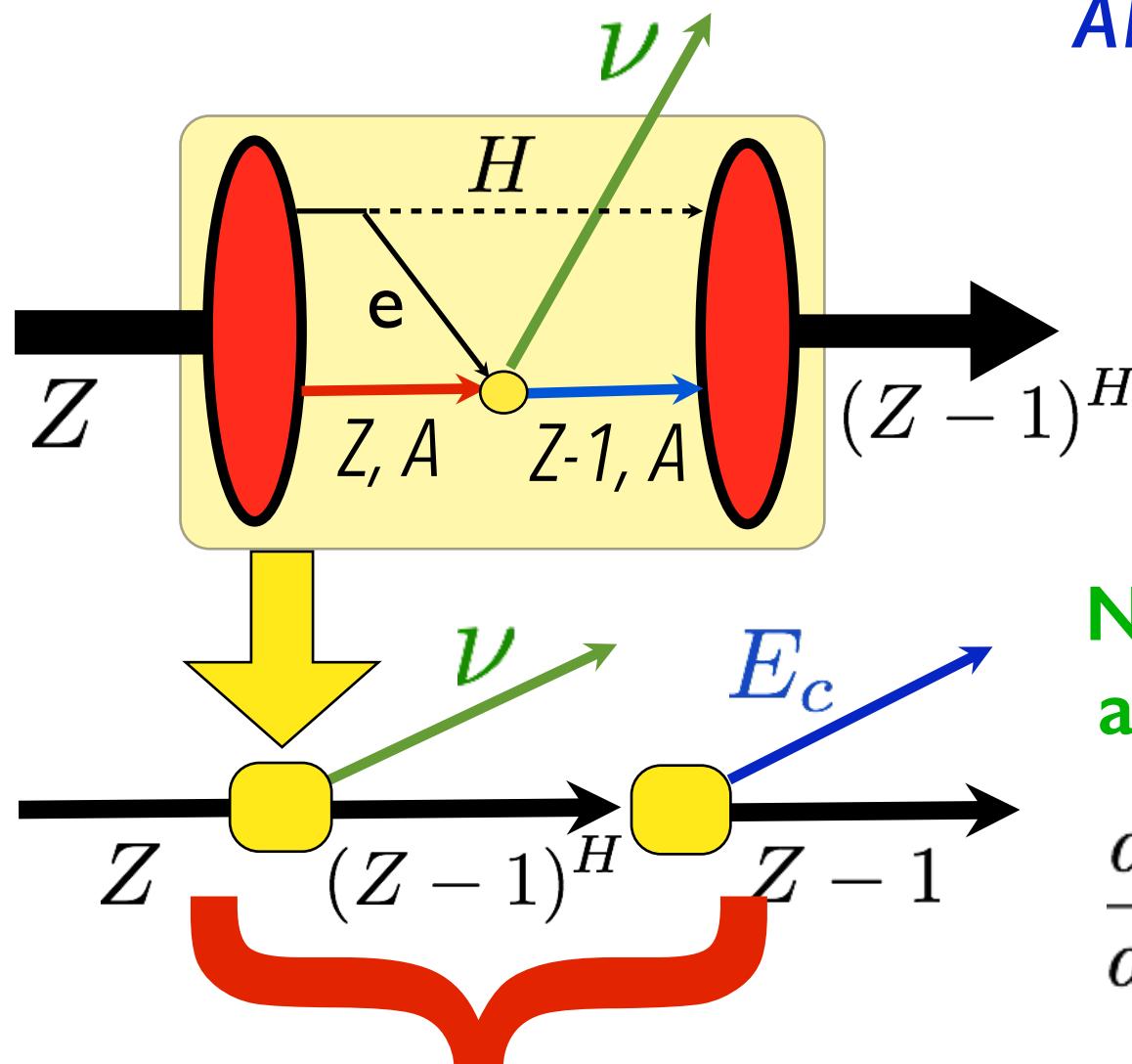
$$\gamma_\mu (1 + g_A \gamma_5)$$

$$E_e \sim Q$$

$$\frac{d\Gamma}{dE_e} \propto E_\nu p_\nu$$

“Effective” calorimetric theory,

ADR & Lusignoli (1982)



$$Q = M[\text{det., before}] - M[\text{det., after}]$$

$$(Chem. \rho \text{ure detector})$$

$$Q = E_\nu + E_c$$

No matter what H was
and how it deexcited !

$$\frac{dW}{dE_c} = -\frac{dW}{dE_\nu} \Big|_{E_\nu = Q - E_c}$$

$$\frac{dW}{dE_c} \propto \frac{(Q - E_c)}{E_\nu} \sqrt{\frac{(Q - E_c)^2 - m_\nu^2}{p_\nu}} \sum_H \frac{\varphi_H^2(0) \Gamma_H}{(E_c - E_H)^2 + \Gamma_H^2/4}$$

In EC, the Holes are
RESONANCES

that, if close to the
endpoint,
enormously enhance
the matrix element

^{163}Ho Q-value ?

- To be consistently measured in each e-capture experiment itself, but ...

$$Q[\text{recommended}] = 2555 \pm 16 \text{ eV}$$

$$Q[\text{Penning trap}] = 2833(30)_{\text{stat}}(15)_{\text{sys}} \text{ eV}$$

Eliseev et al. PRL 115 (2015) 062501

“Wrong Direction”

3 current $^{163}Ho \rightarrow ^{163}Dy + \nu_e$ e-capture EXPERIMENTS

ECHo

<https://www.kip.uni-heidelberg.de/echo/>

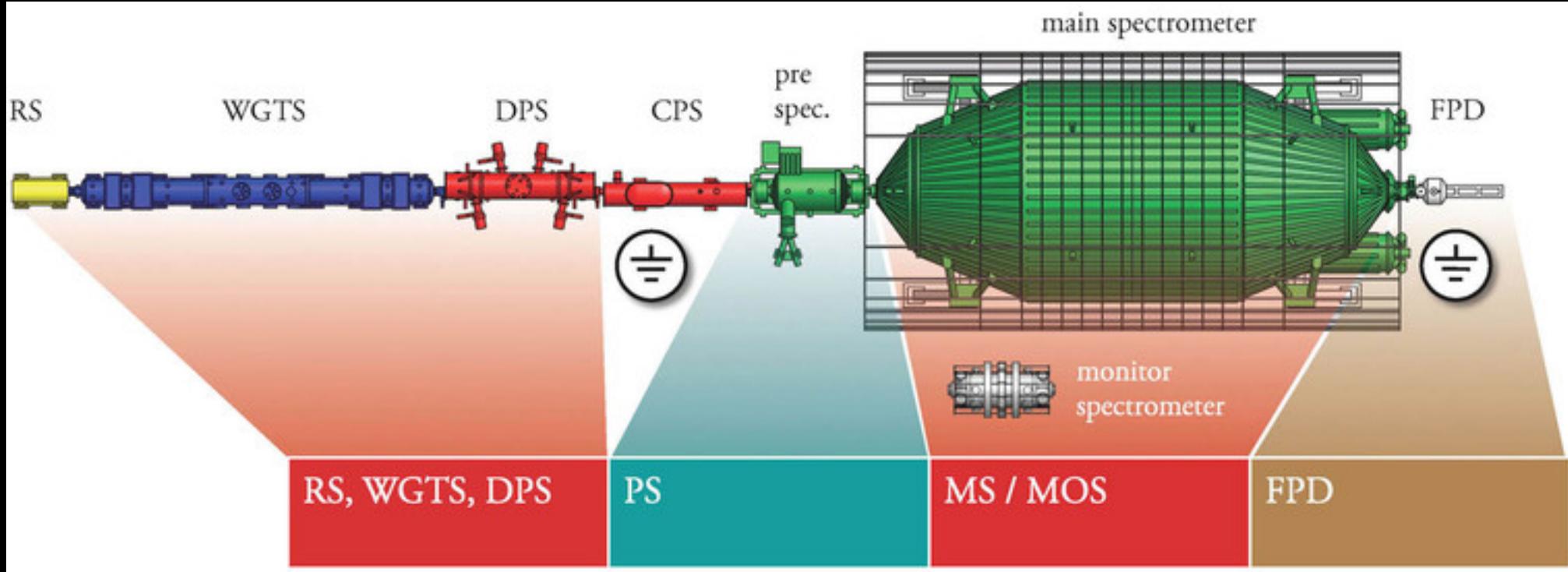
HOLMES

<http://artico.mib.infn.it/nucriomib/>

NuMECS

<http://p25ext.lanl.gov/~kunde/NuMECS/>

β decay KATRIN



70 m

SHOW AND TELL

c)

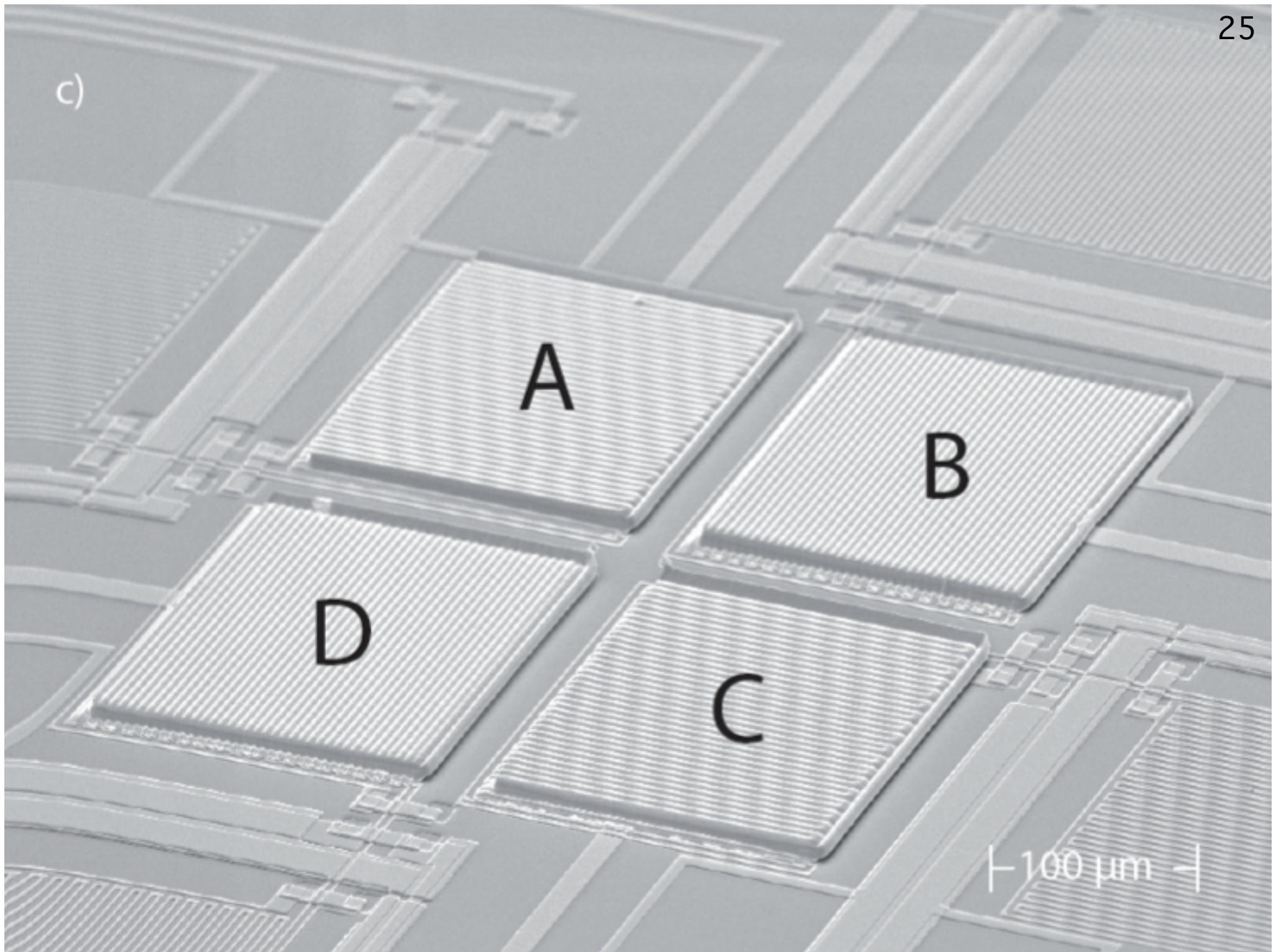
A

B

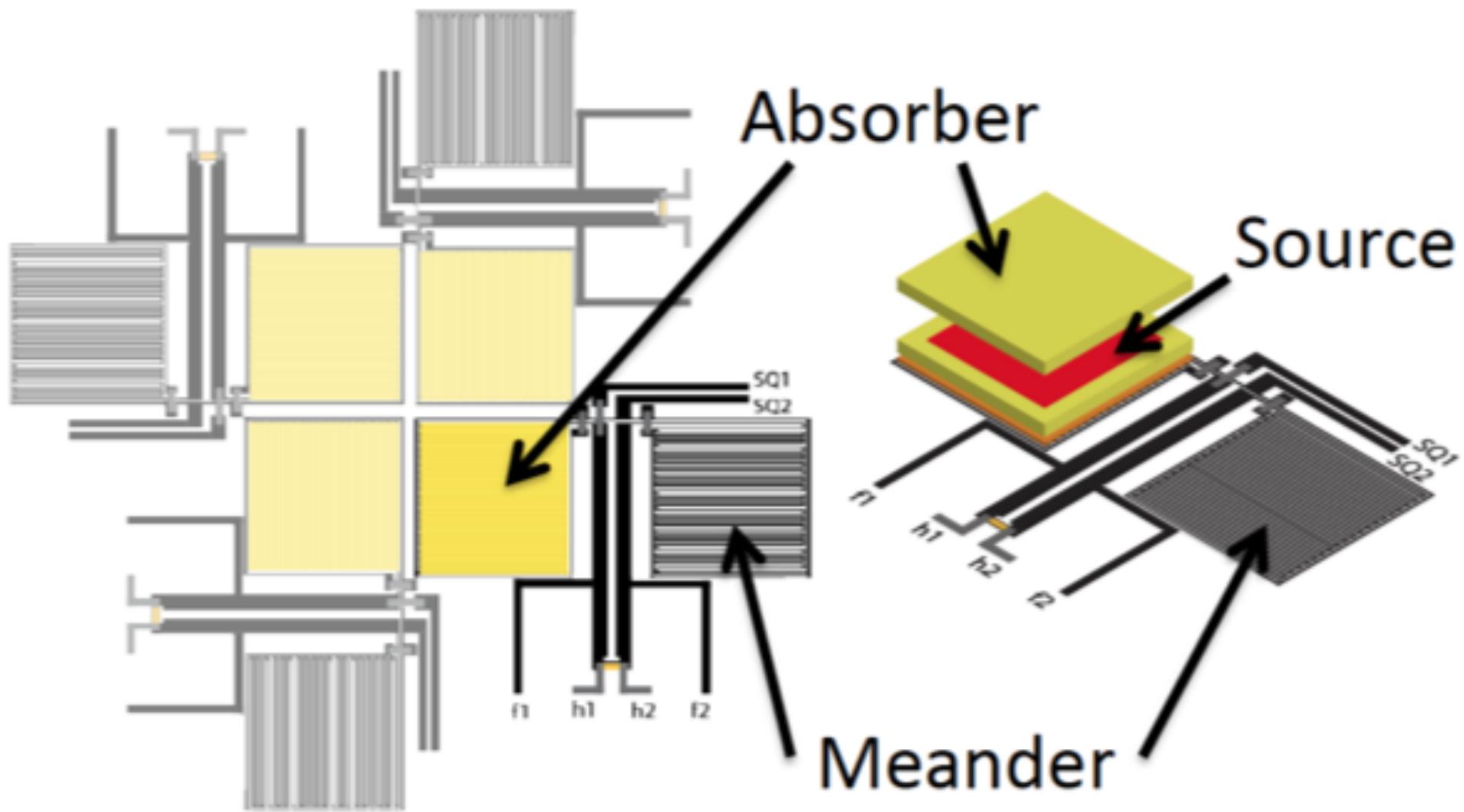
D

C

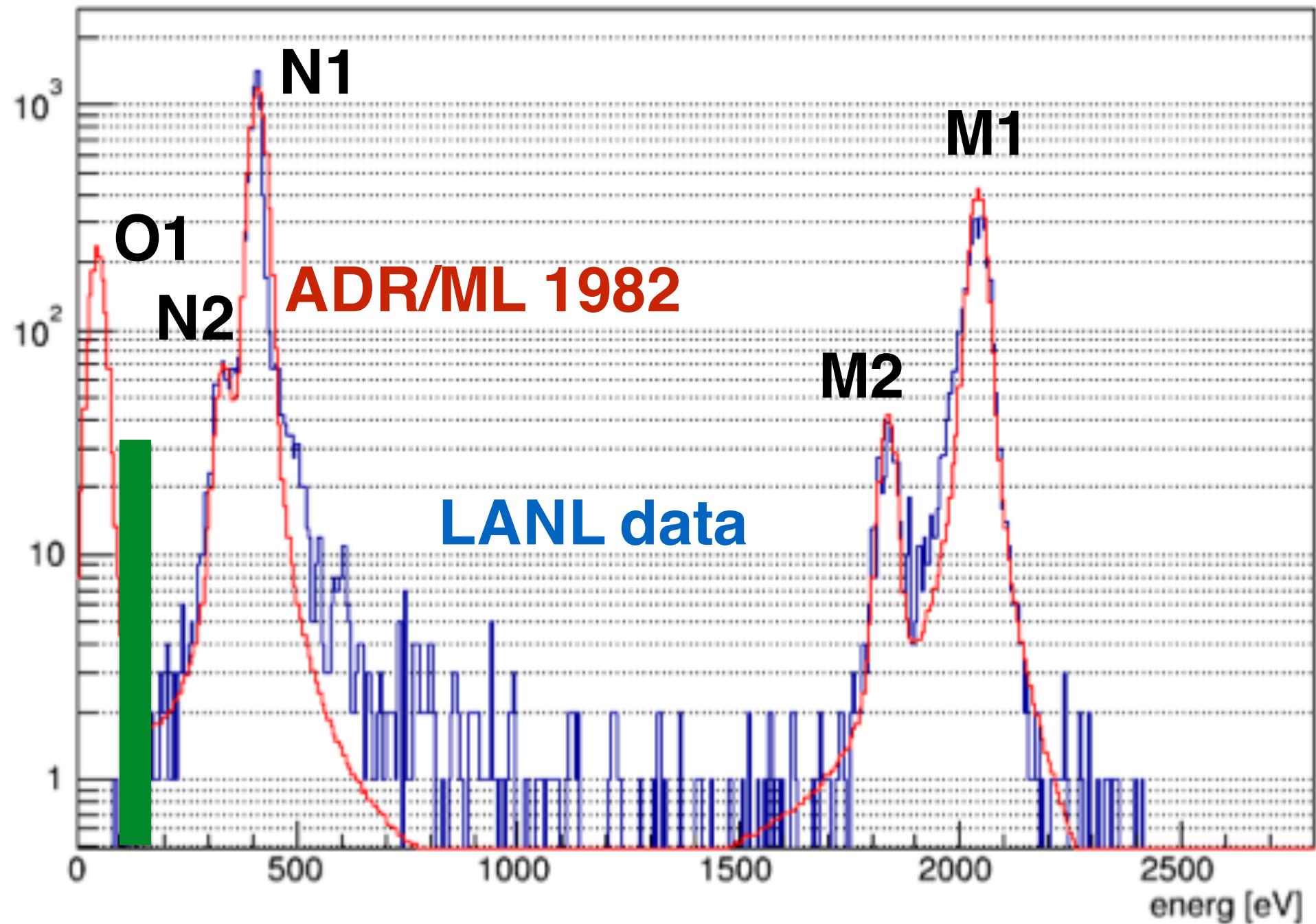
+100 µm -|

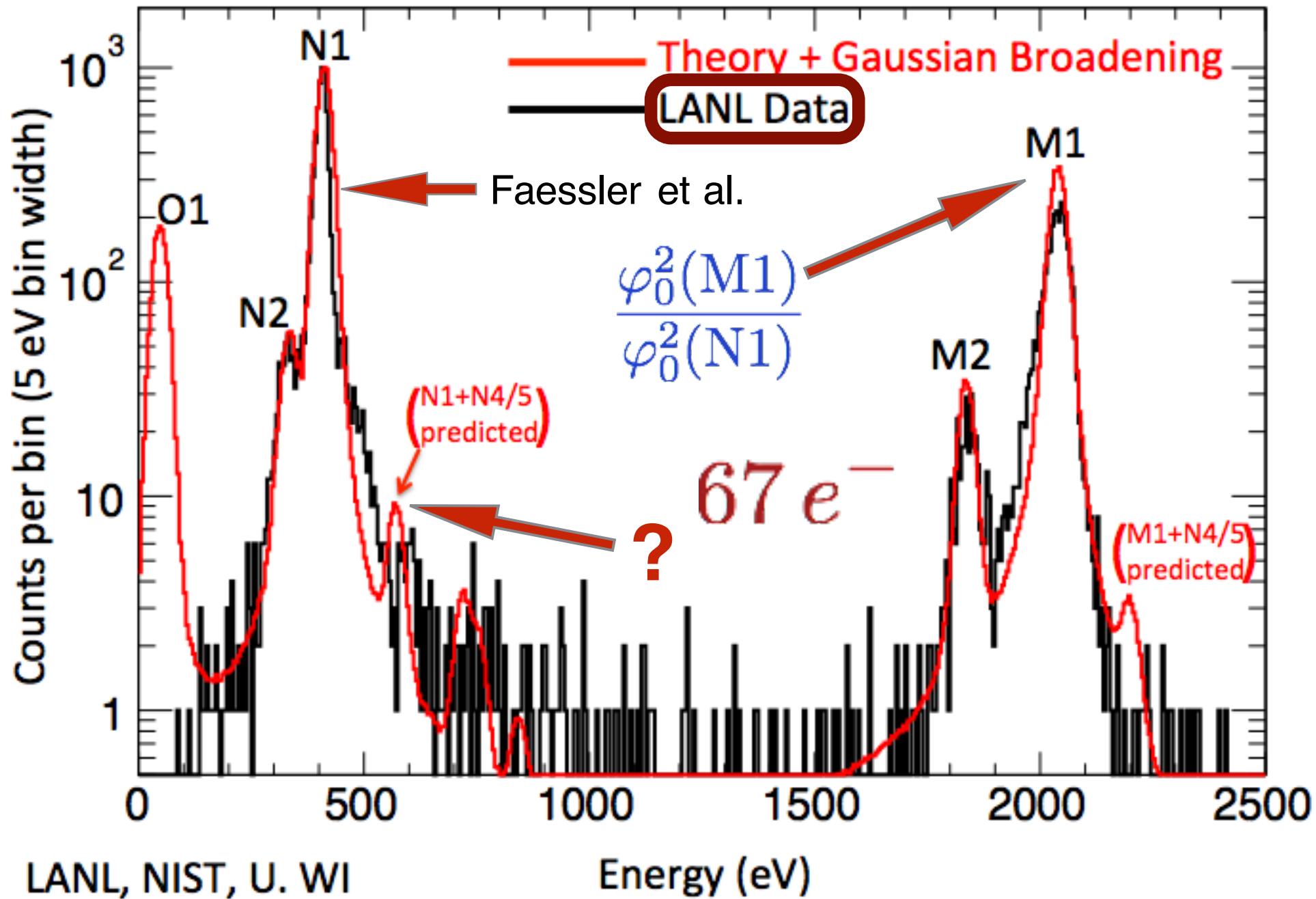


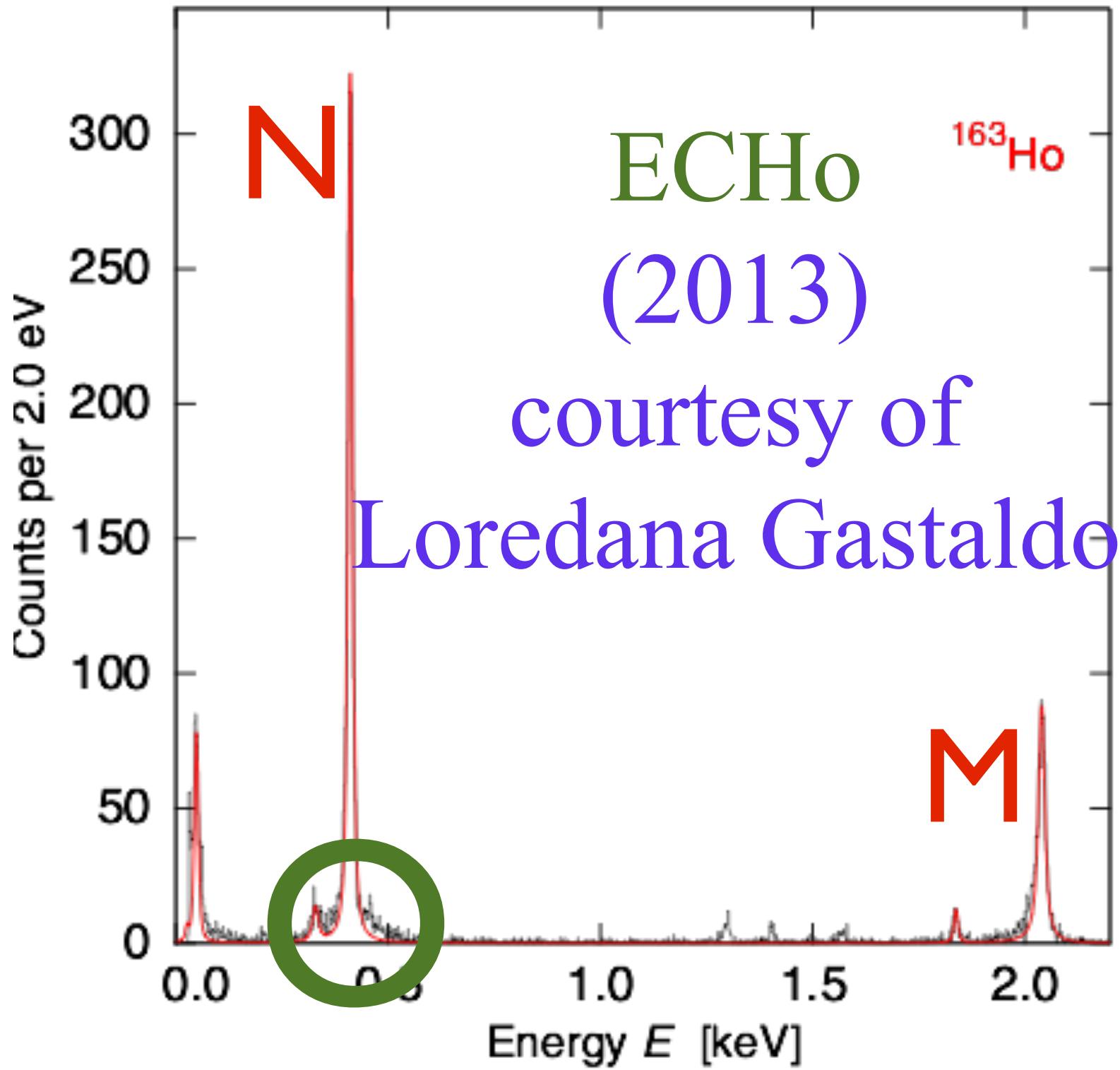
ECHO

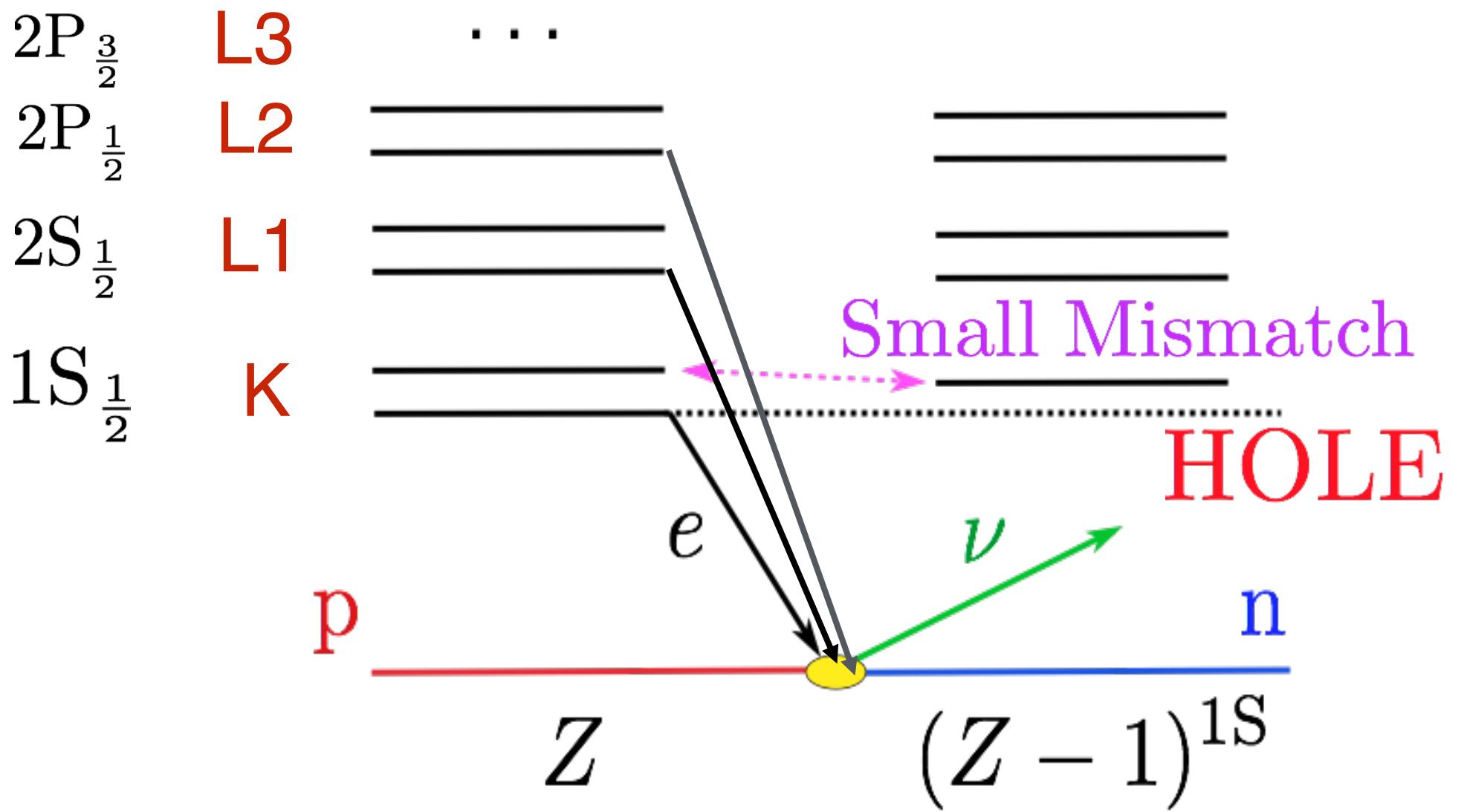


Is the God
good
enough?







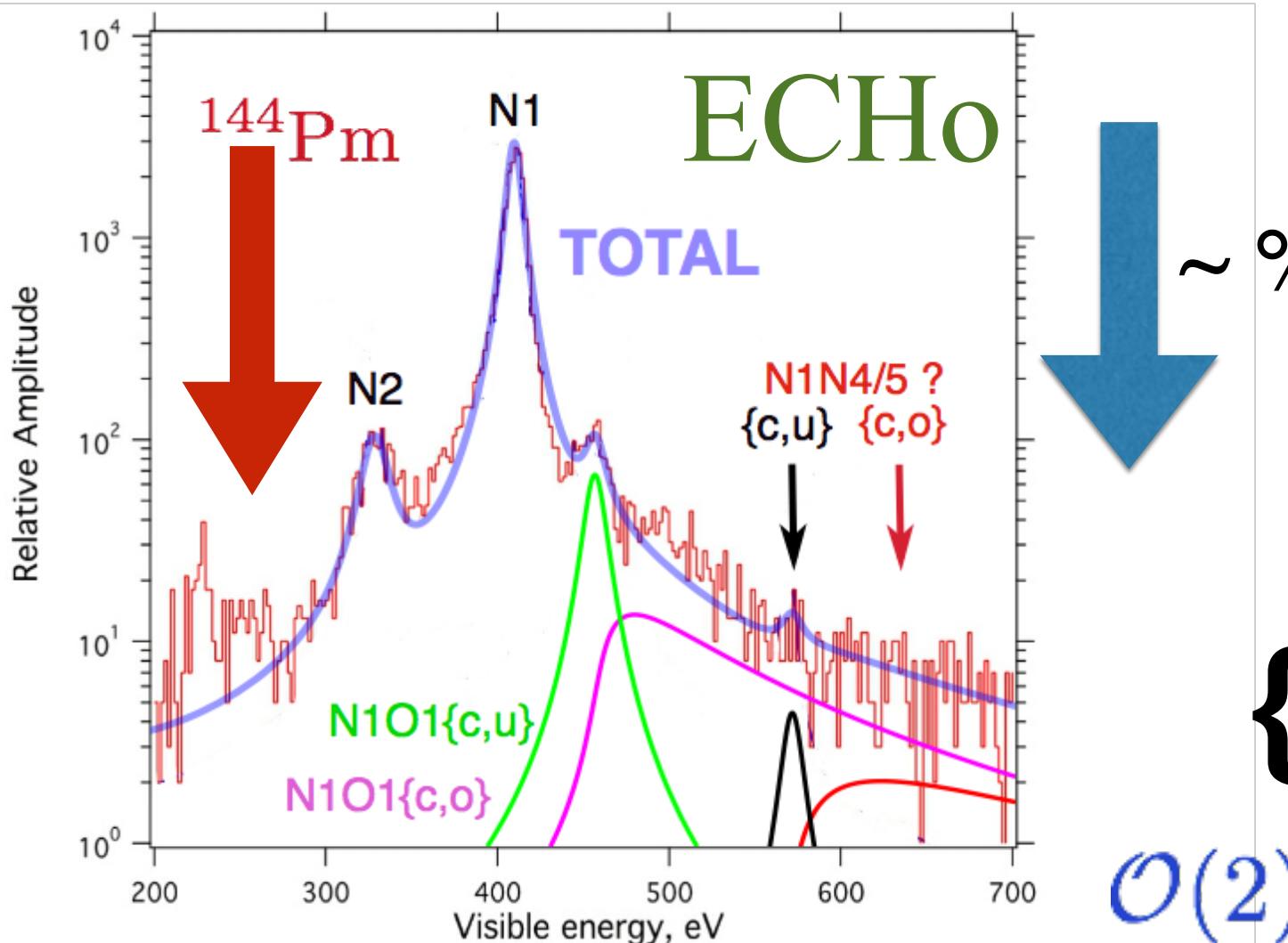


Requires $\varphi_H(0) \neq 0$

Small-component
 $\mathcal{O}(\alpha Z)$ mixing

$$n l_j = n S_{1/2}$$

$$n l_j = n P_{1/2} \leftrightarrow n S_{1/2}$$



Maurizio
Lusignoli
+ ADR
(à la 1967
Intemann
& Pollock)

{ , }

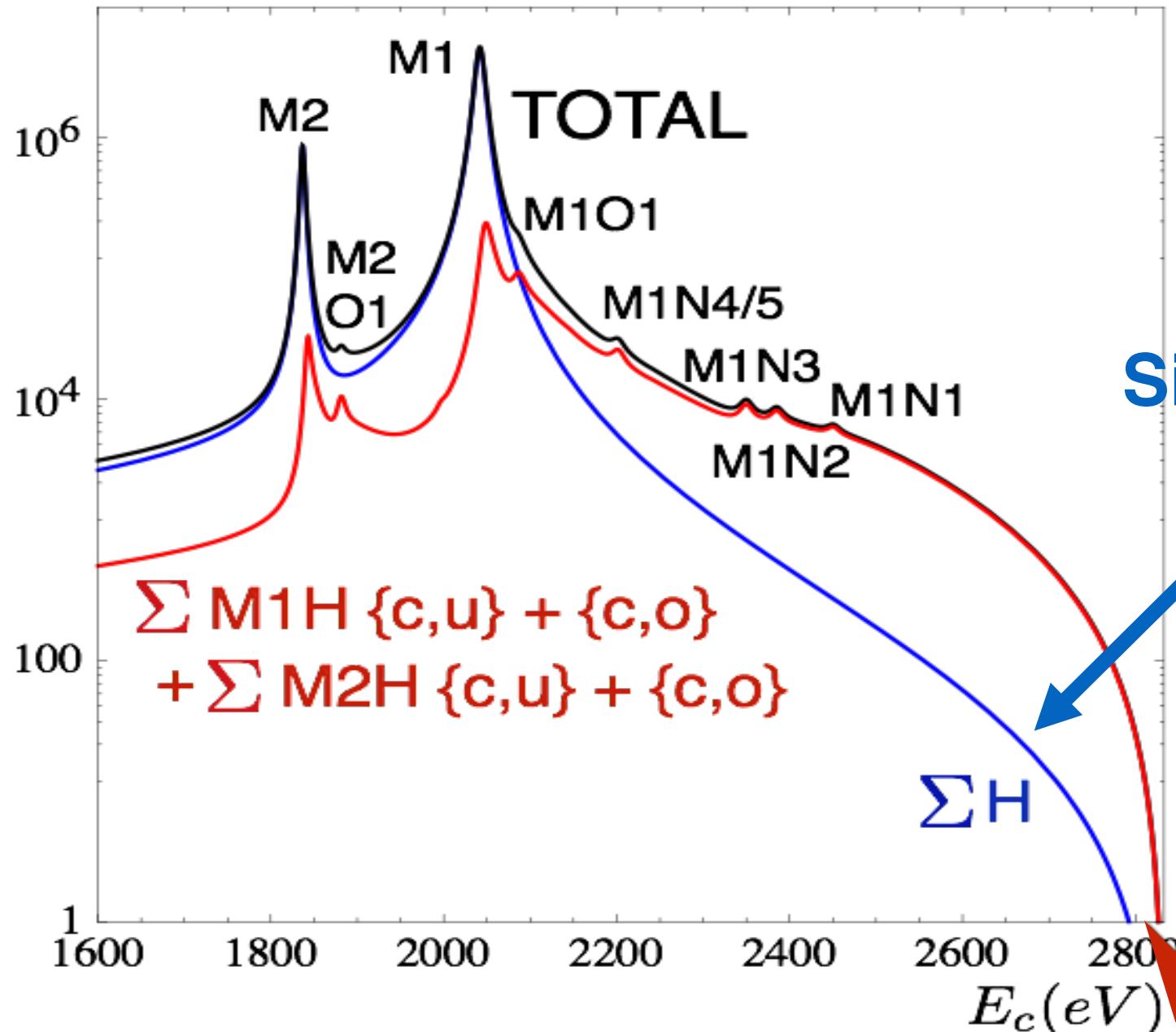
$\mathcal{O}(2)$ Massage

$\{c,u\}$ 1 e captured; 1 e up to unoccupied level

$\{c,o\}$ 1 e captured; 1 e off to the continuum

Electron ShakeOff previously FORGOTTEN!!

Are Souhle
holes an
endpoint's
nightmare ?



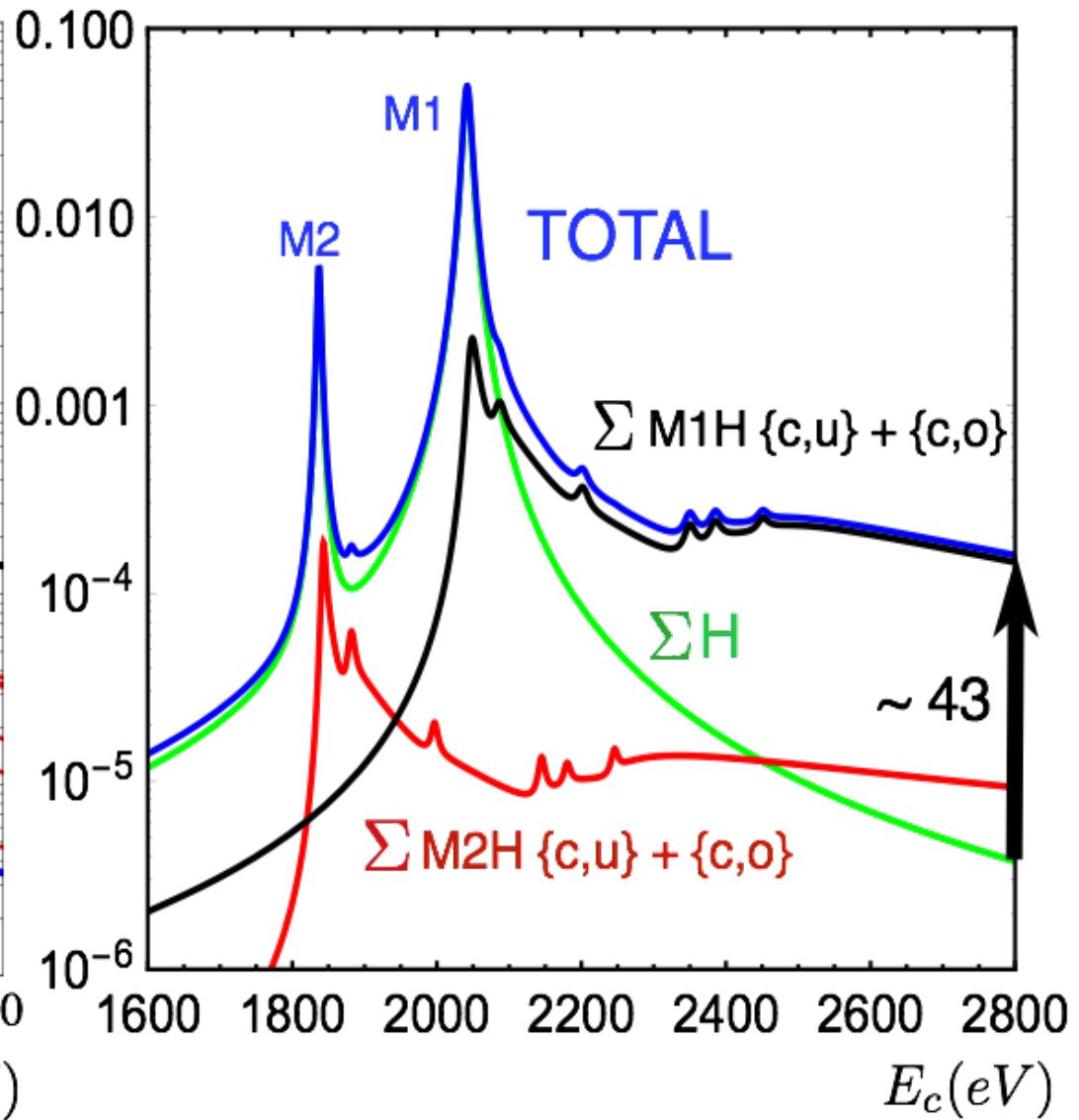
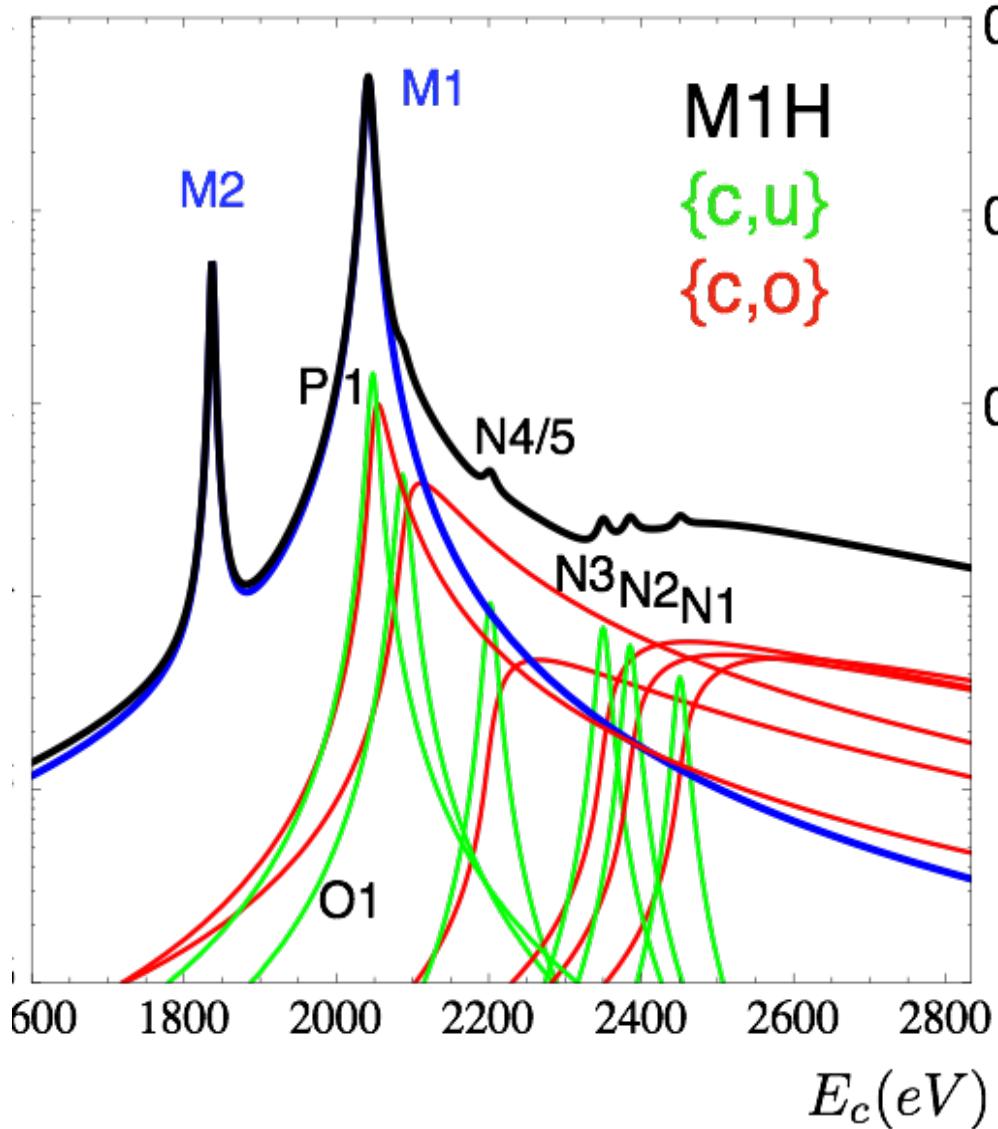
Single hole
~ M1

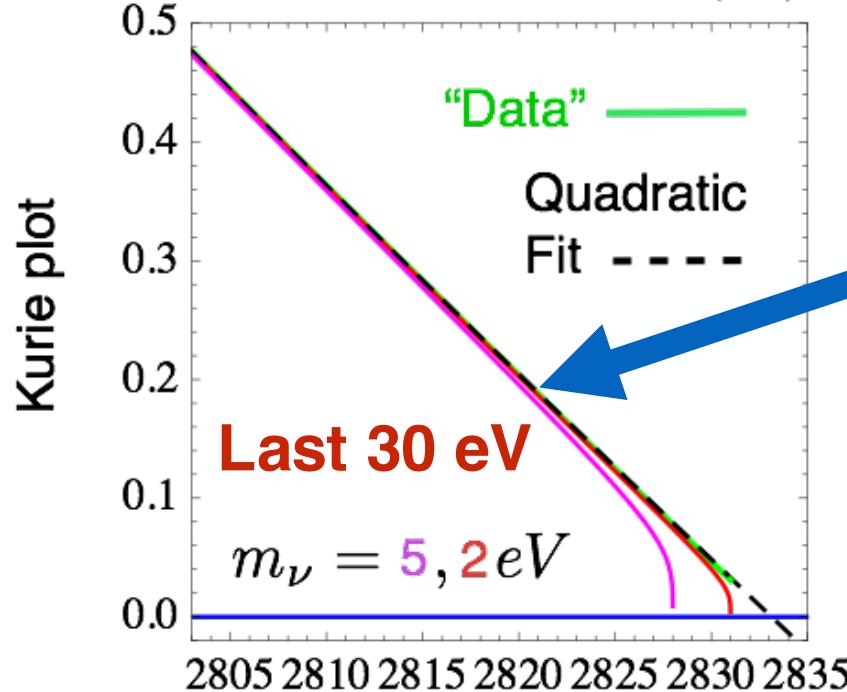
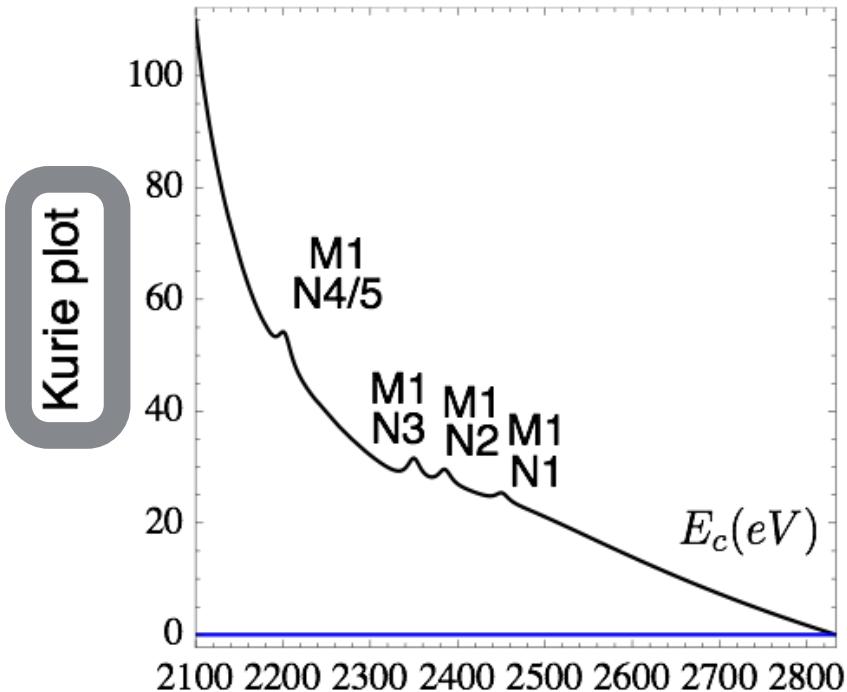
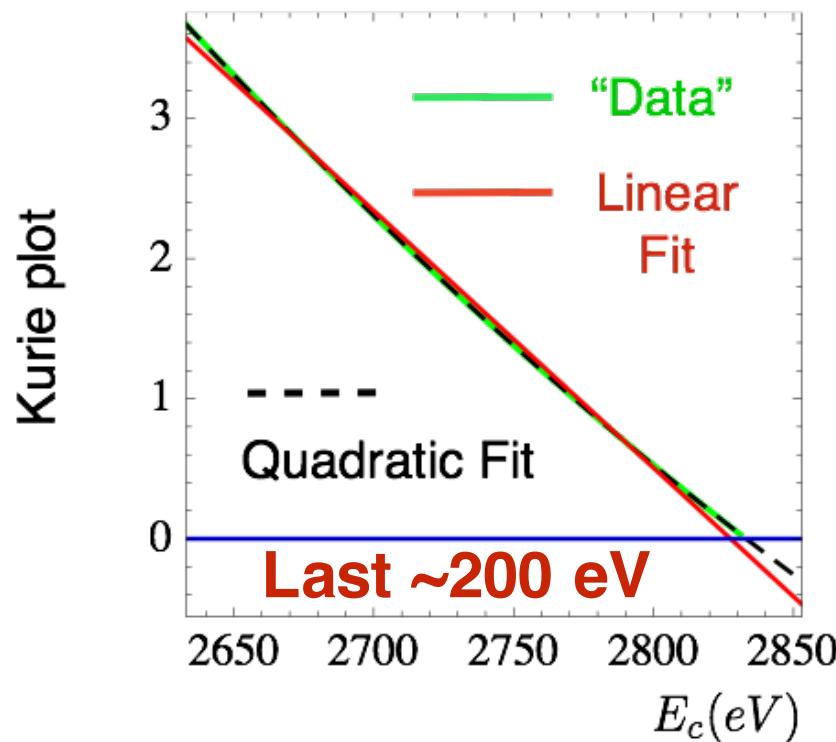
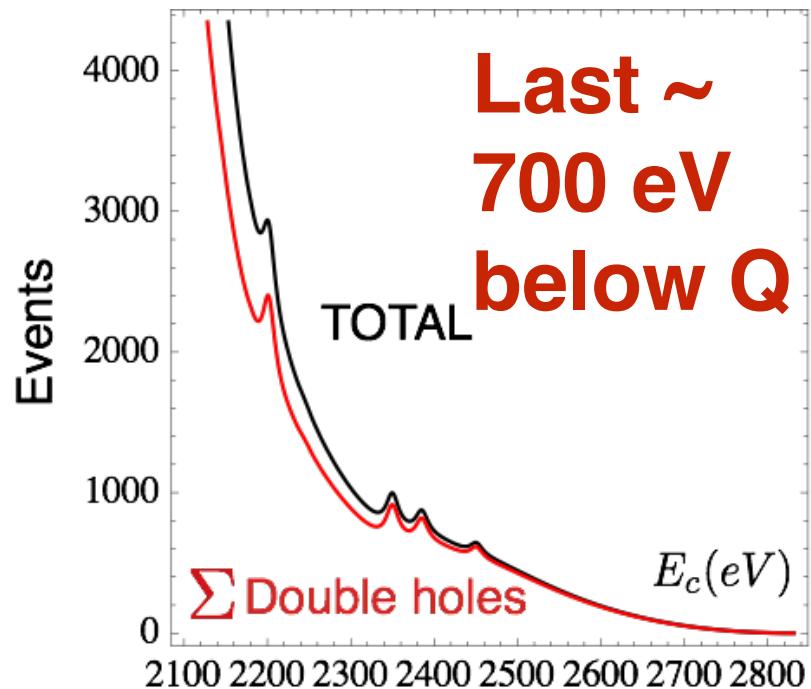
ΣH

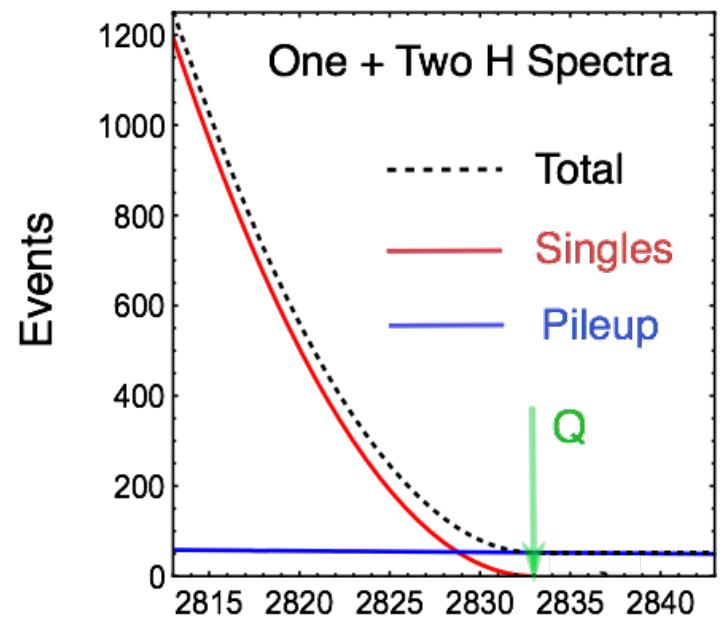
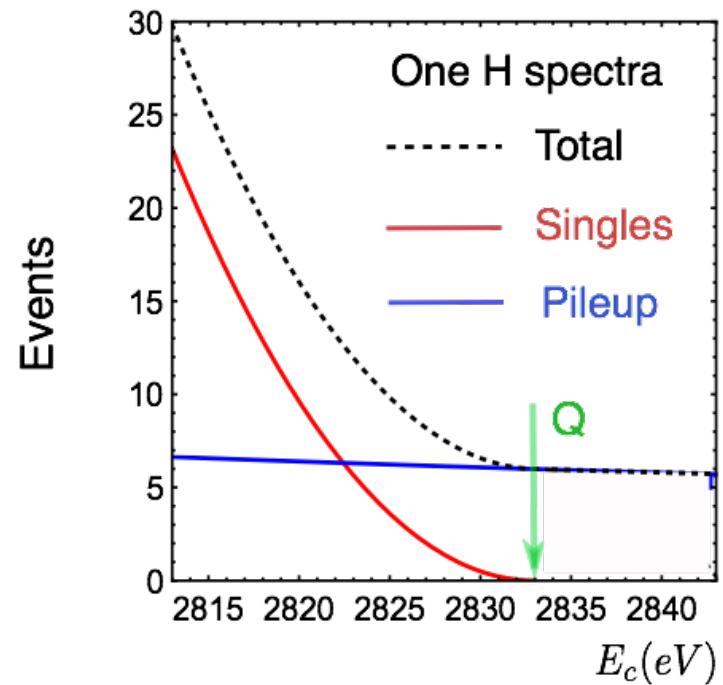
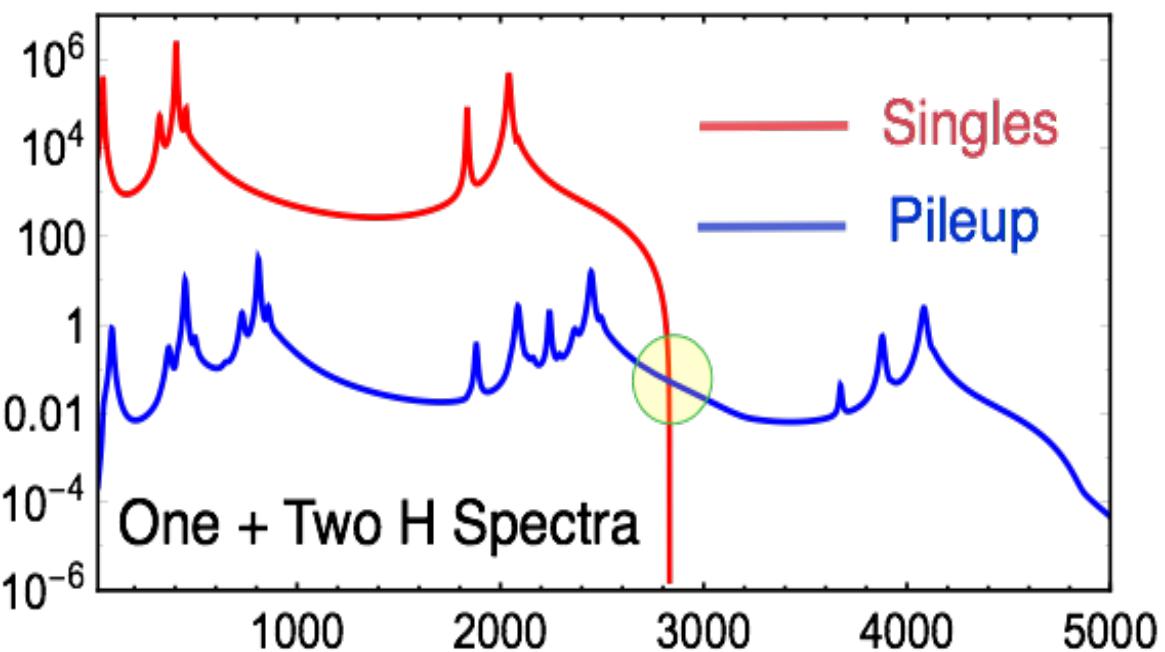
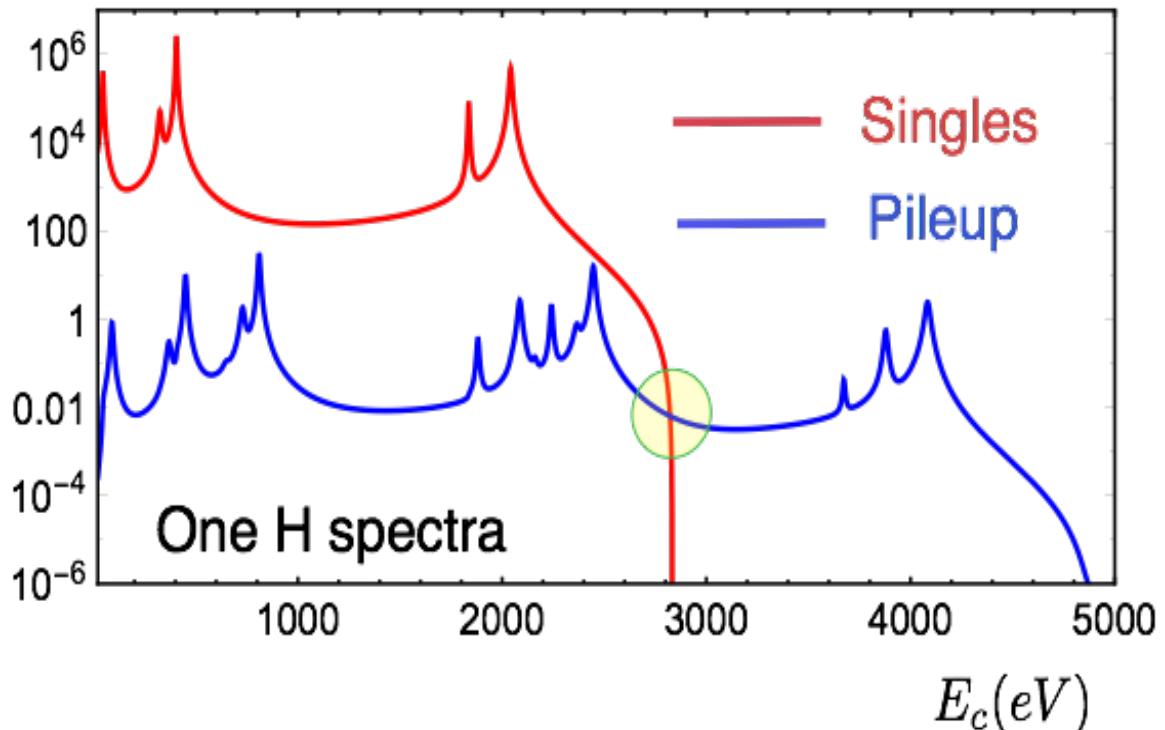
$E_c(eV)$

$$E_\nu p_\nu = (Q - E_c) \sqrt{(Q - E_c)^2 - m_\nu^2}$$

Take out E_ν p $_\nu$ factor







$x \sim 6$ IMPROVEMENT

CONCLUSIONS

Double Holes **not** a problem
but possibly... a **BLESSING**:
~ 40 statistics, ~ 1/6 pileup

Theory **PRELIMINARY!**

Experiments will improve.
With their help, so should TH

Parameters of our universe chosen

$\exists \nu$ Physics ♣♣♣

$\Delta m_{ij}^2, \theta_{ij}, \delta?$

$E(CRs), h(atms); \rho(atms), \tau(\mu), \tau(\pi^\pm)$

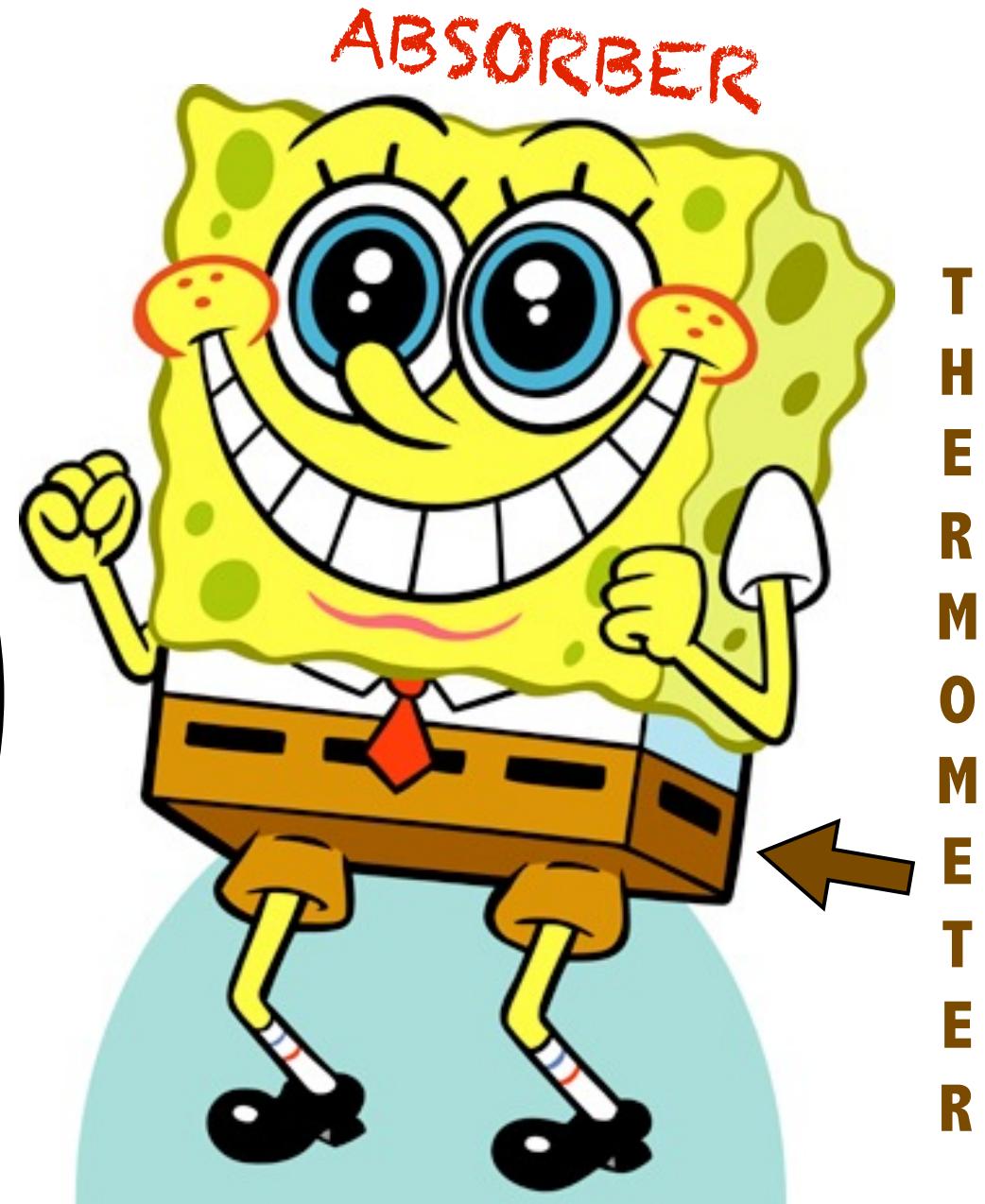
$R_\odot, \rho_\odot, R_\odot, \rho_\odot \quad \exists$ Reactors ♣♣♣

\mathcal{EC} measurements of e-neutrino "mass" ??

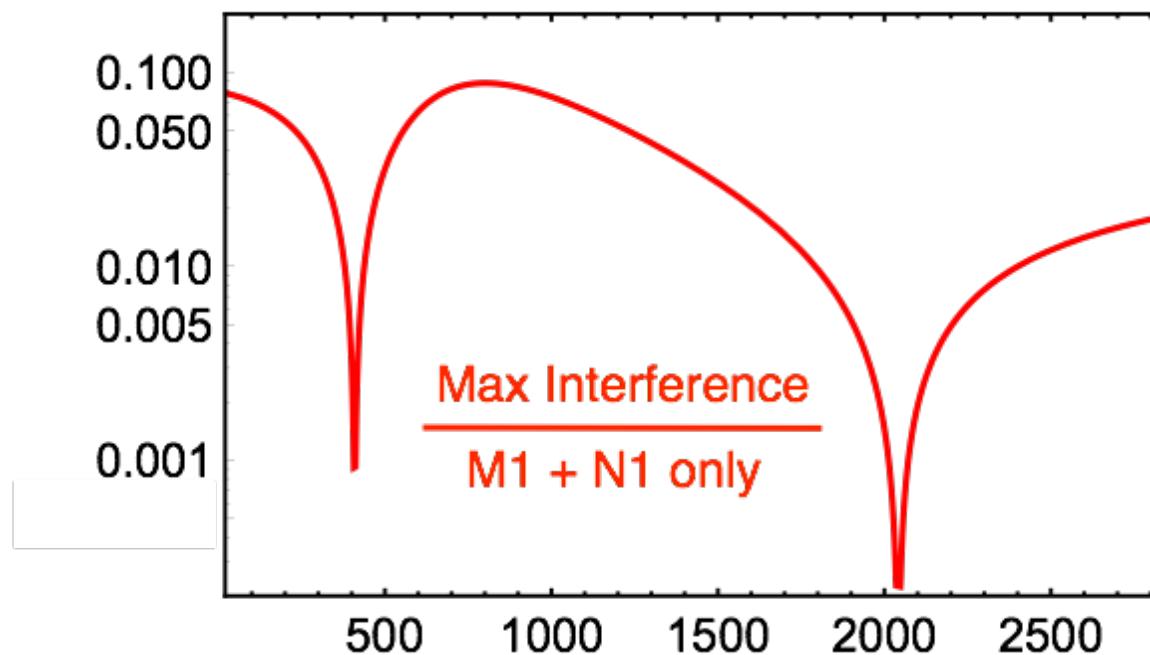
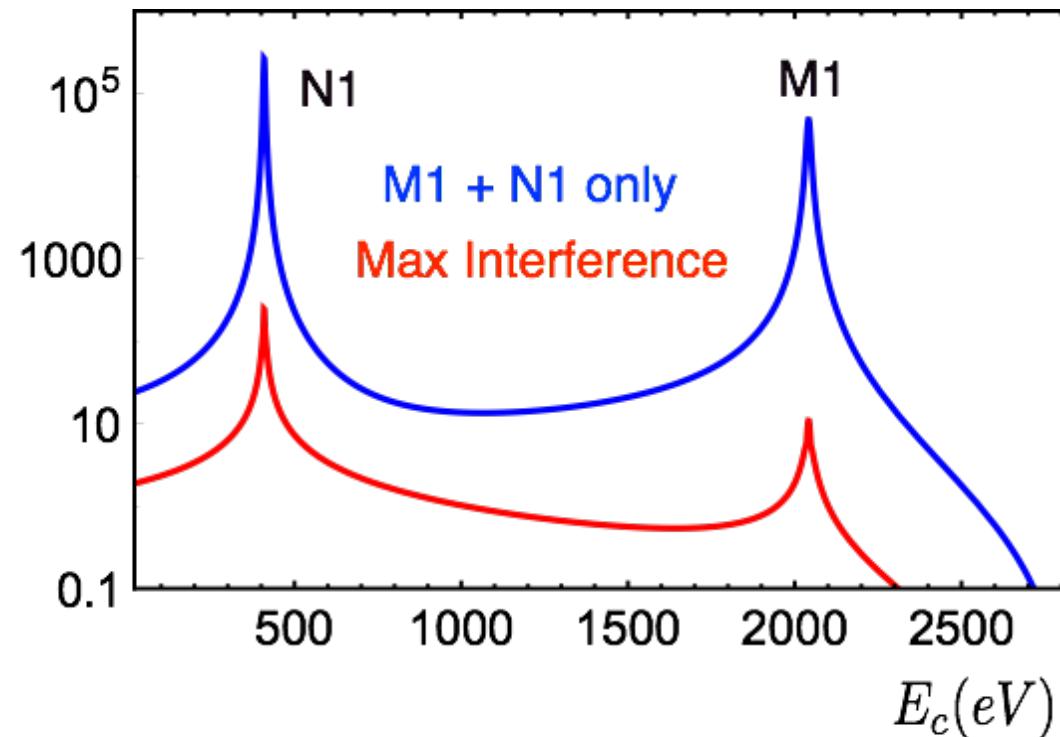
Microcalorimeters, etc !!

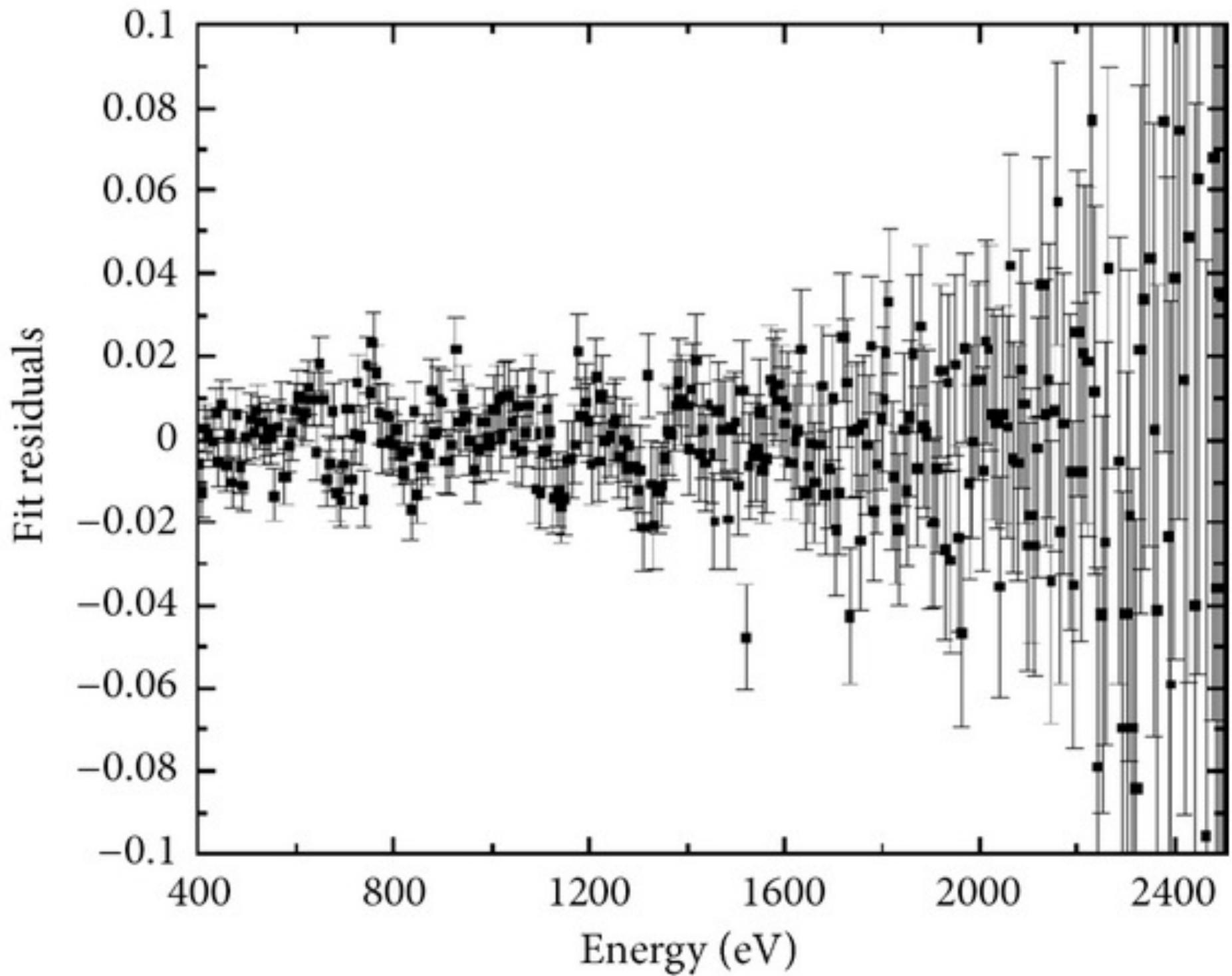
\exists Hope for $m(\nu_e)$ experiments

Holmium From Latin "Holmia": Stockholm.

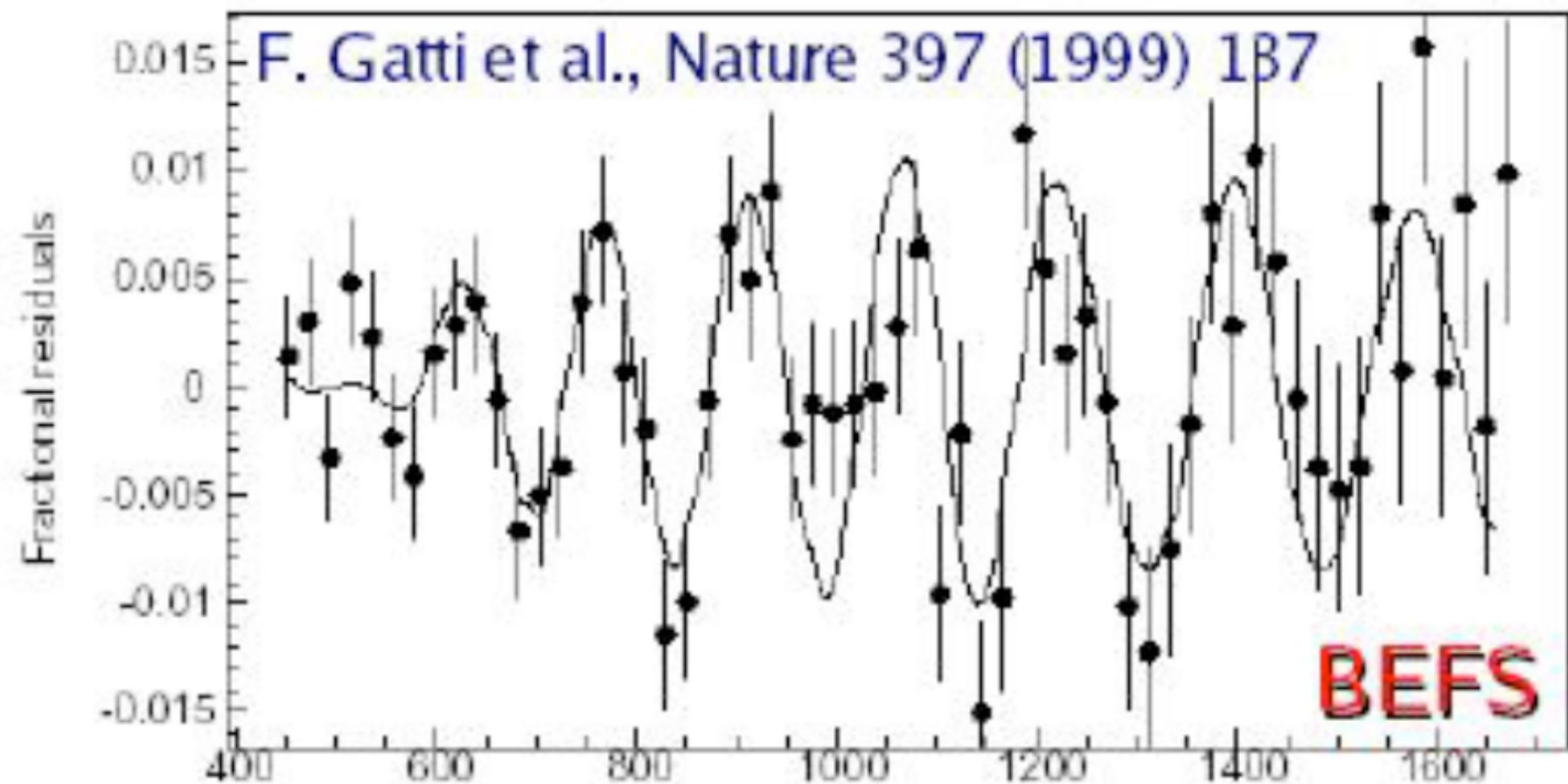


ELECTRO-
THERMAL LINK

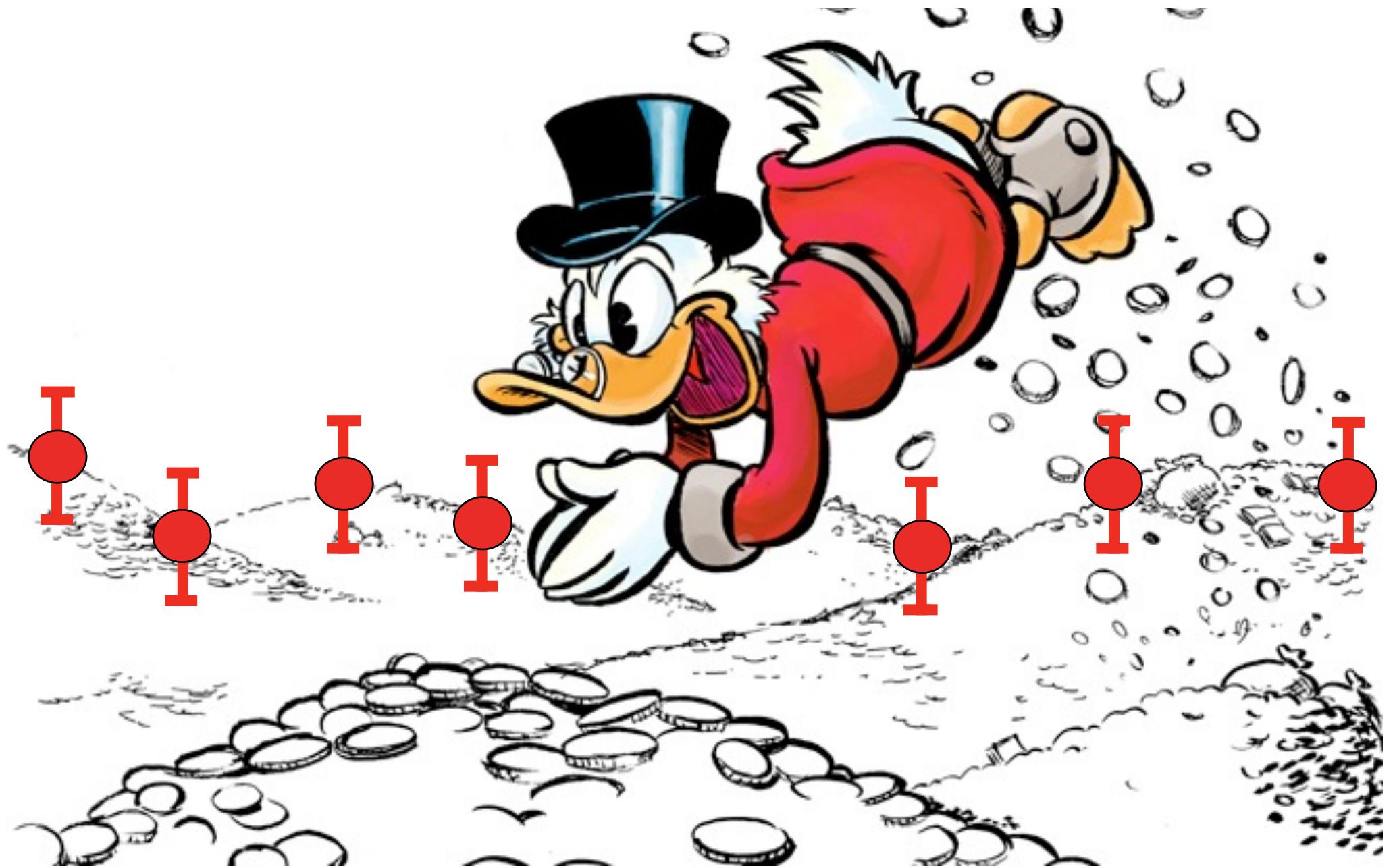




Enlarged bins



?????????????????????



Beta-Environmental Fine Structure (BEFS)

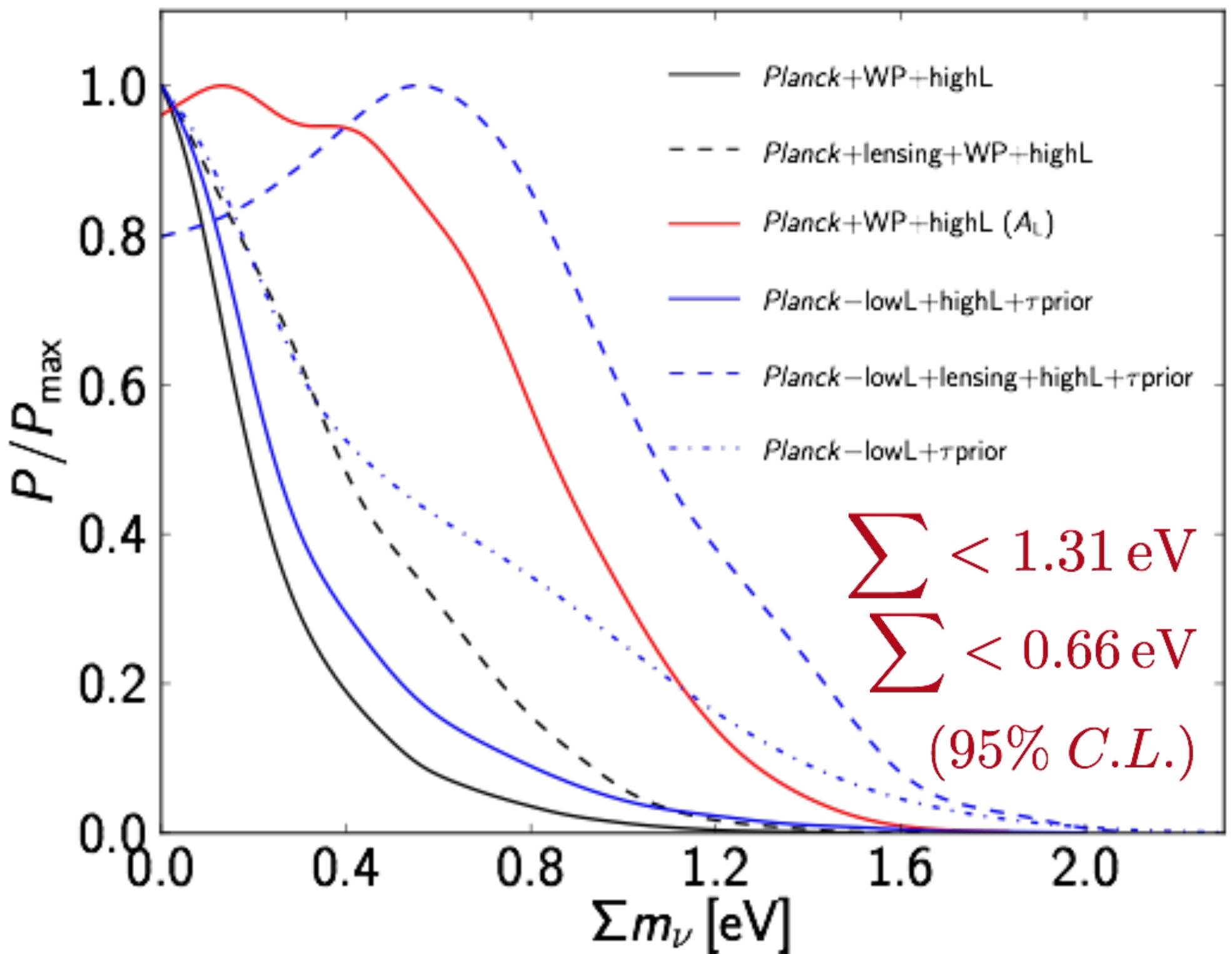
OSCILLATIONS

$\sum m$ limits depend on M-Hierarchy

$\sum_i m_{\nu_i} > 0.06 \text{ eV}$, “NORMAL”

$\sum_i m_{\nu_i} > 0.1 \text{ eV}$, “INVERTED”

e.g. Gonzalez-García et al.

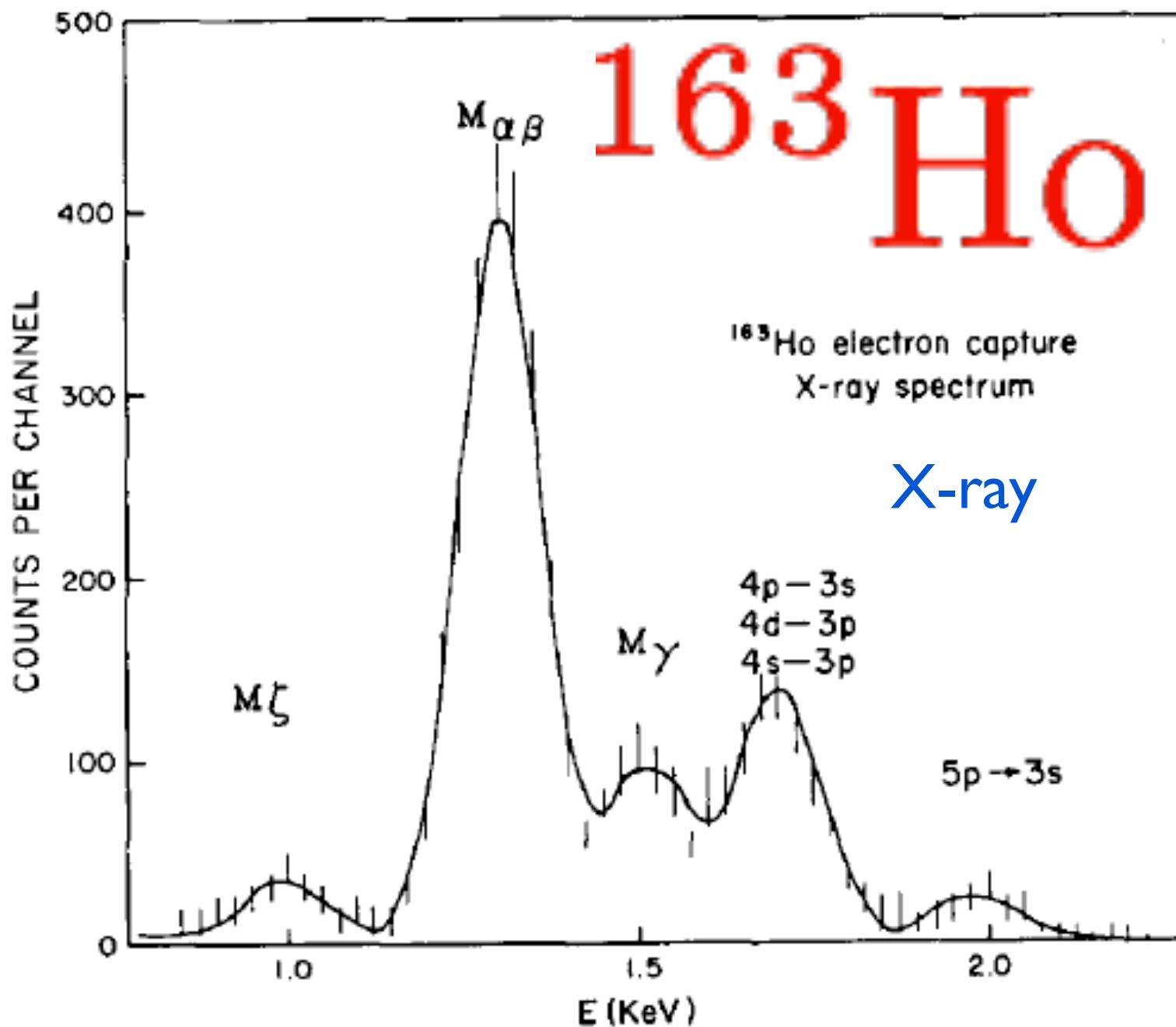


In EC, the X-rays are
RESONANCES

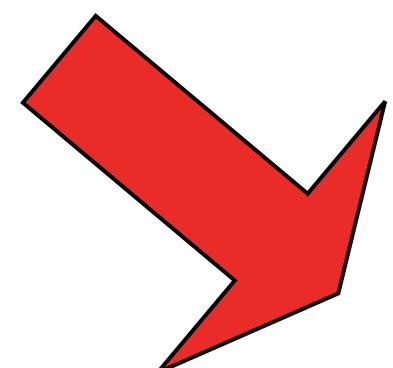
that enormously
enhance the
matrix element

Φ is 3 body as in β decay
in all useful cases

Bennett et al. 1981



...
NOT
ATO
MIC
PHY
CISI
STS





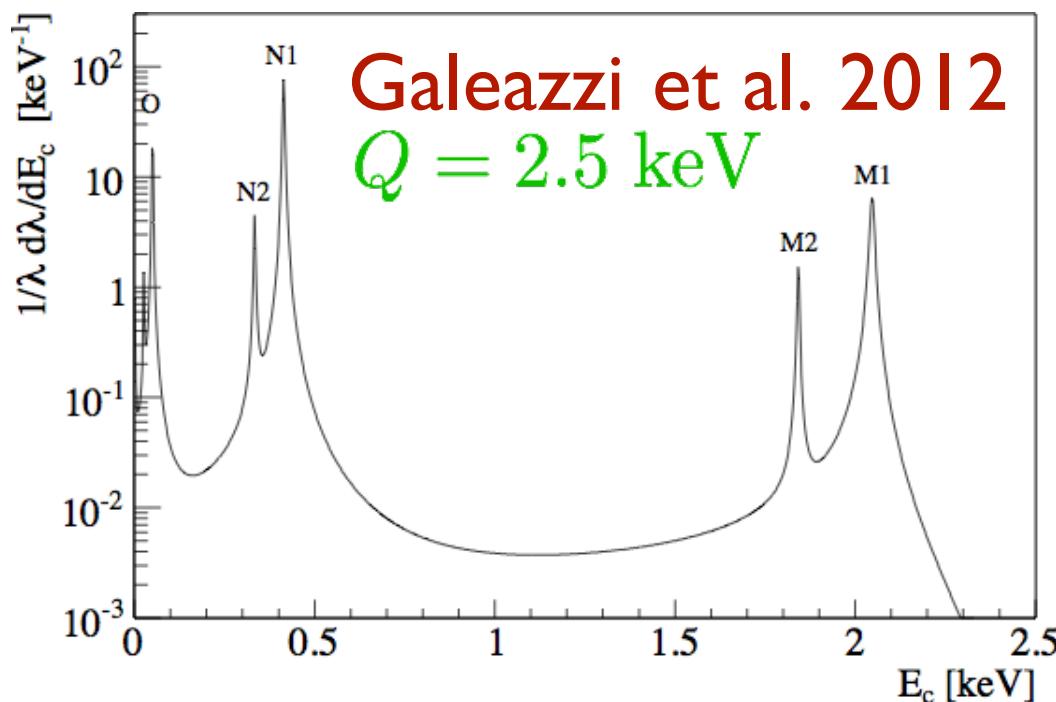
$$Q = 2.3 \text{ to } 2.8 \text{ keV}$$

$$Q = 2.58 \pm 0.10 \text{ keV}; T_{1/2} = (7 \pm 2) 10^3 \text{ y}$$

Anderson et al. 1982

$$Q = 2.30 \pm 0.15 \text{ keV}; T_{1/2} = 900 \begin{array}{l} +500 \\ -200 \end{array} \text{ y}$$

Yasumi et al. 1982



$K(n=1)$, $L(n=2)$
Capture forbidden

$M_1(3S_{1/2})$, $M_2(3P_{1/2})$
 $N_1(4S_{1/2})$, $N_2(4P_{1/2})$
etc allowed

Bennett et al. 1981

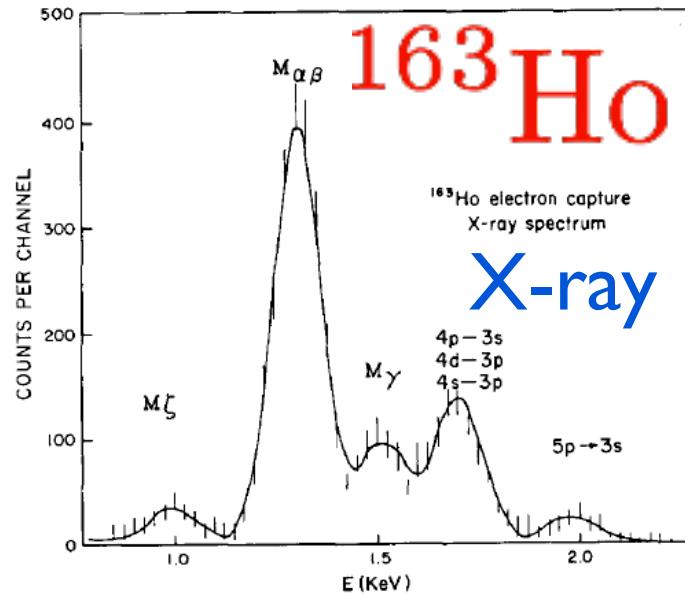
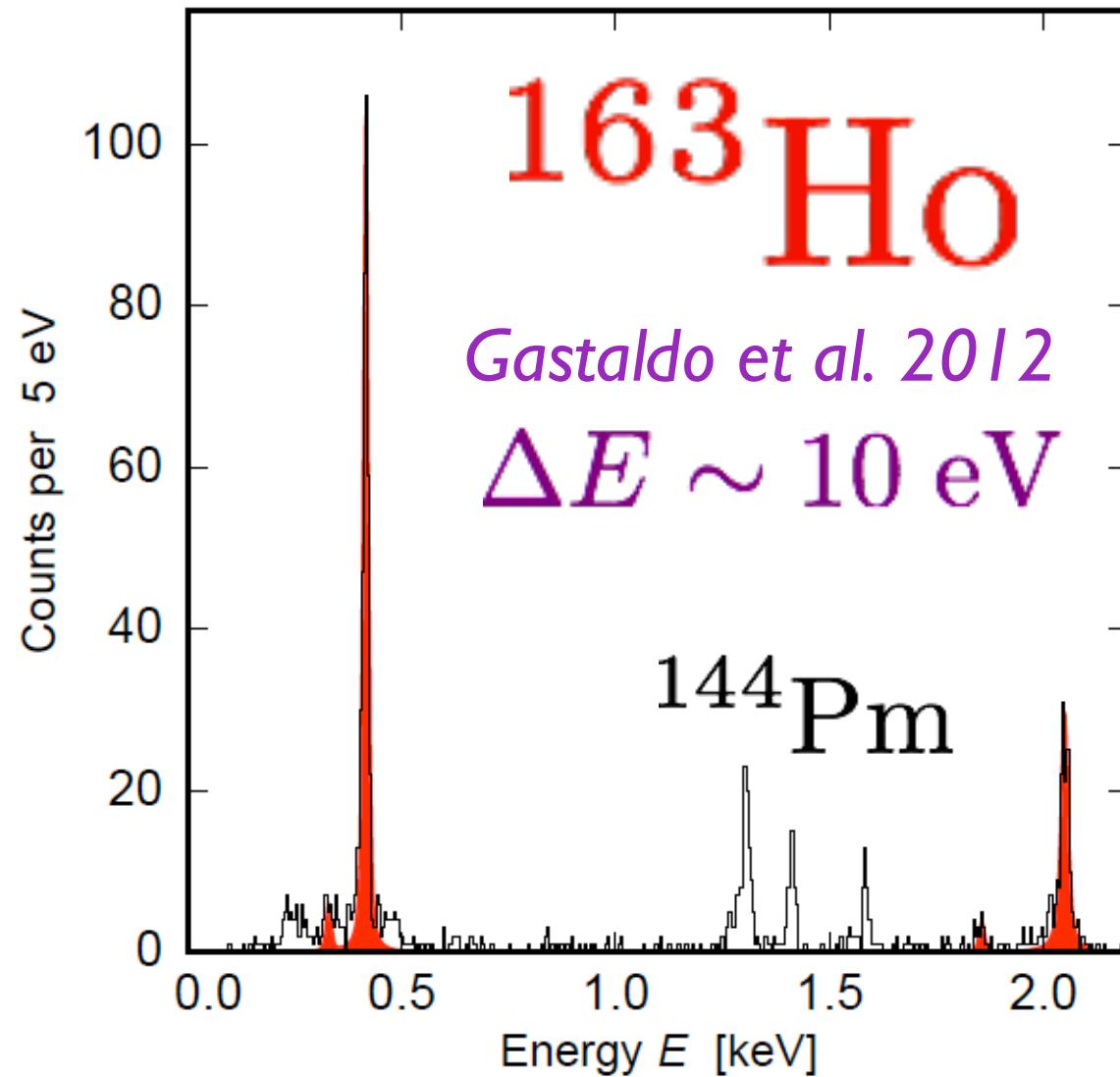
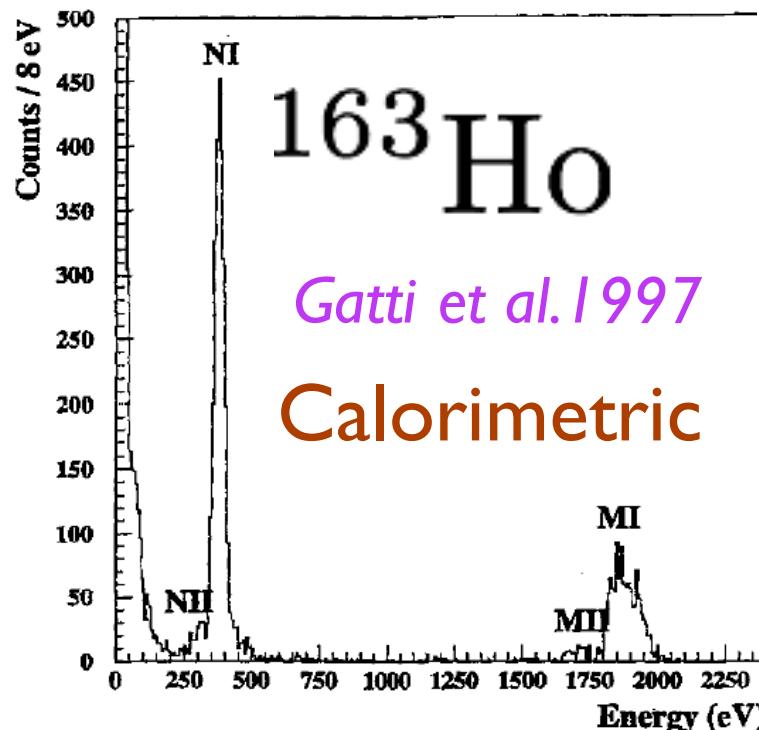
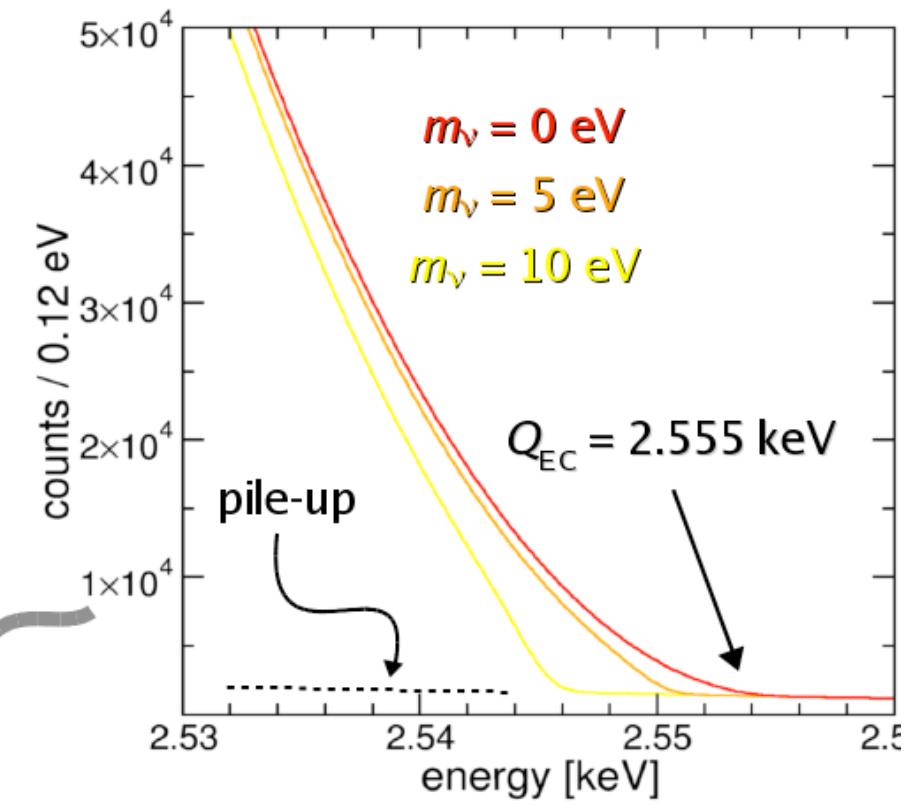
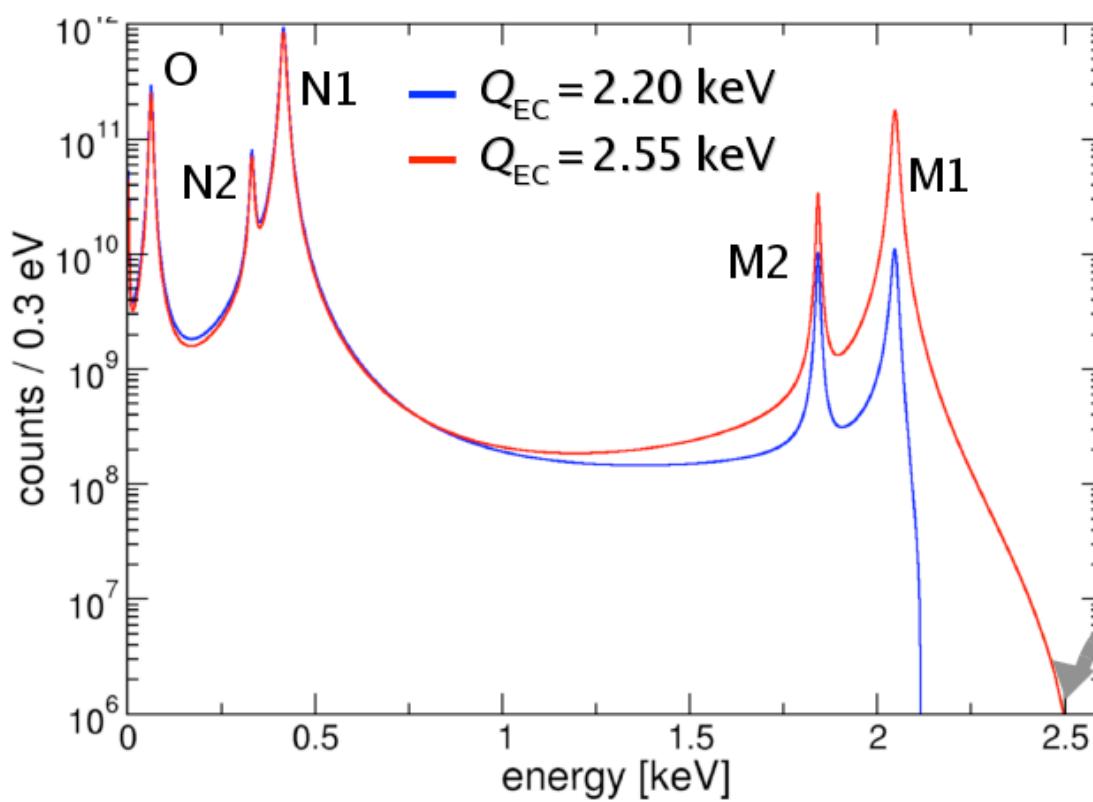


Fig. 1. The X-ray spectrum observed following decay of ¹⁶³Ho. Lines are labeled by either Siegbahn notation or the transition involved.

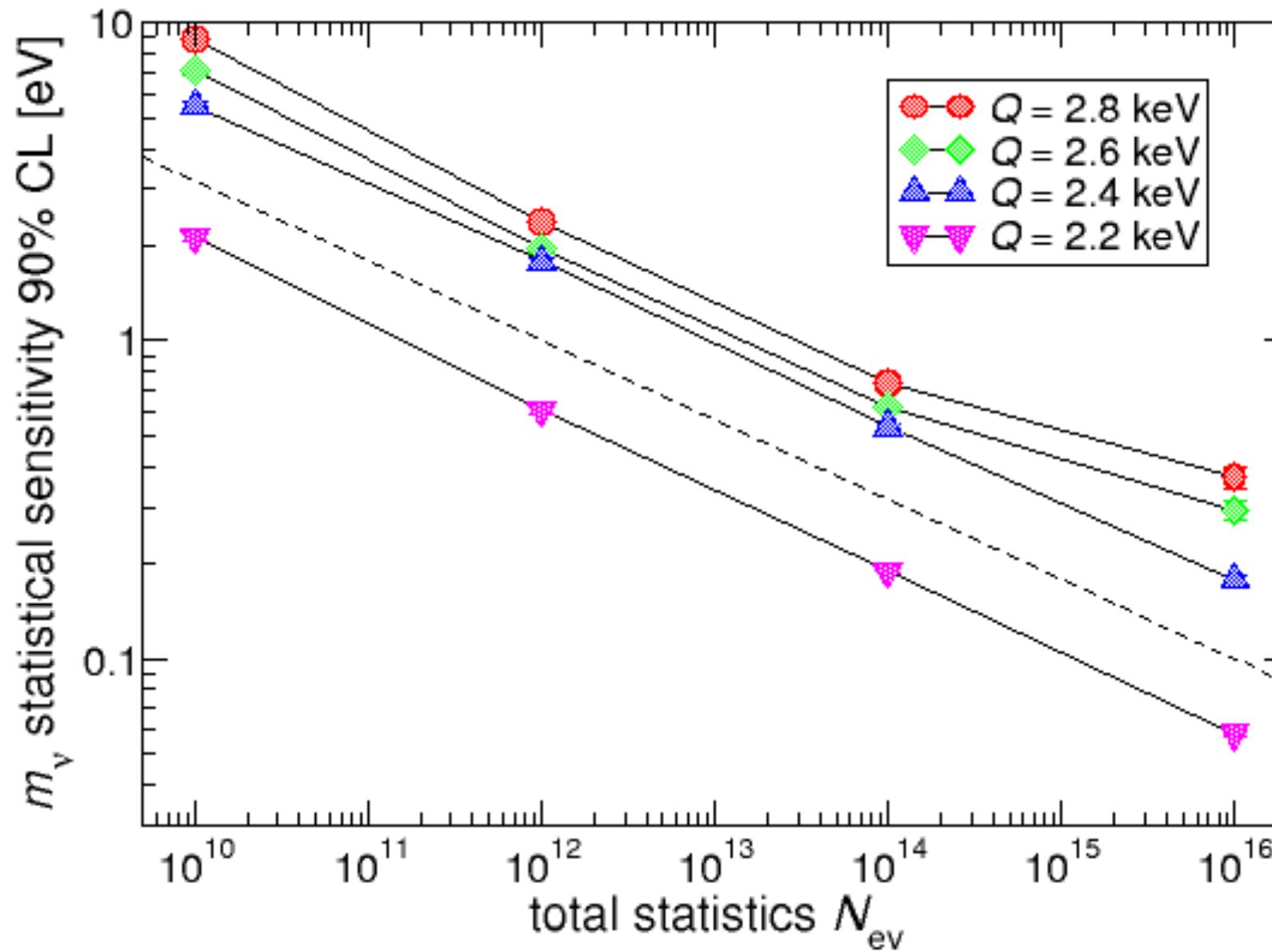


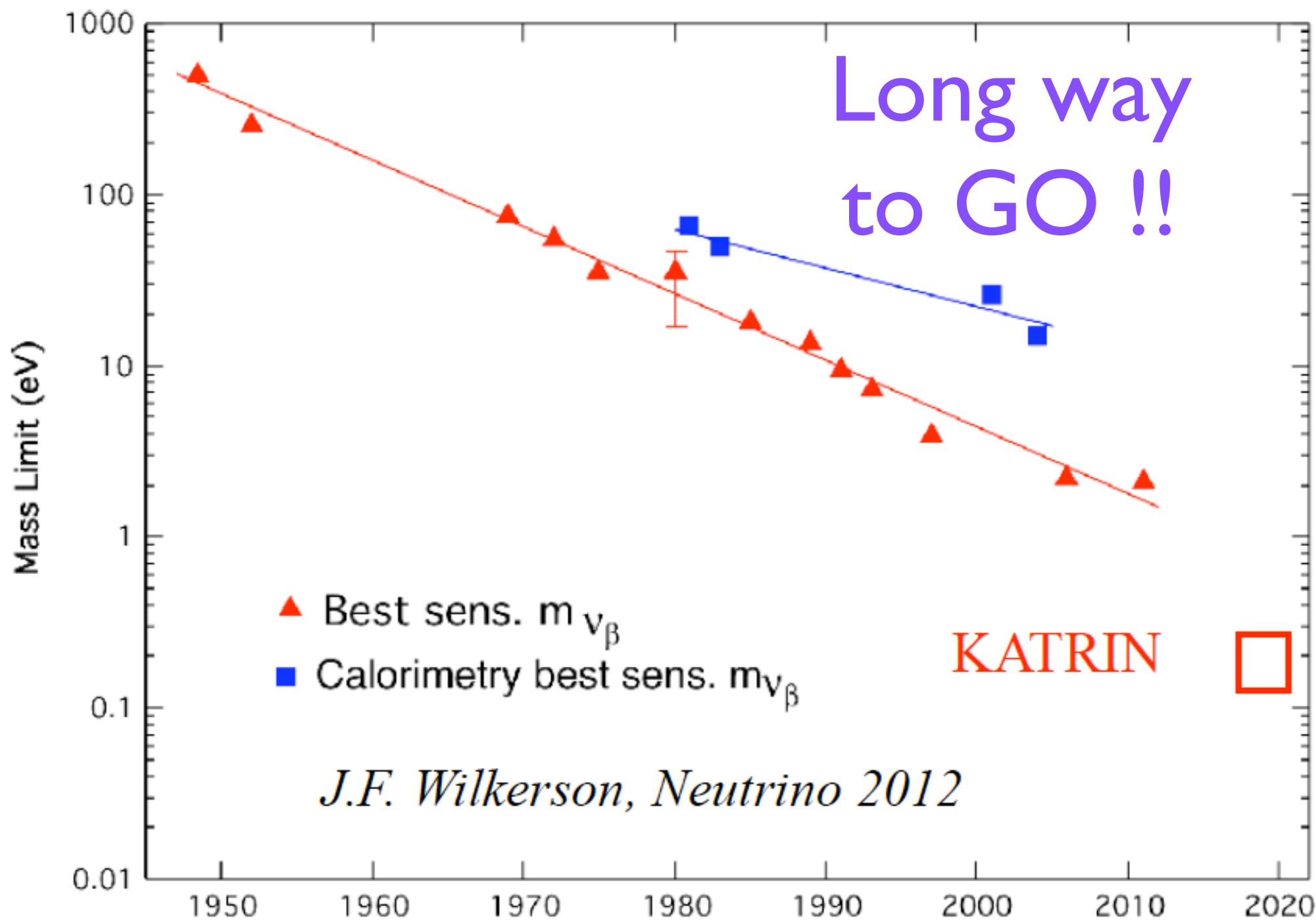
ECHo Calorimetry,
source from ISOLDE

HOLMES

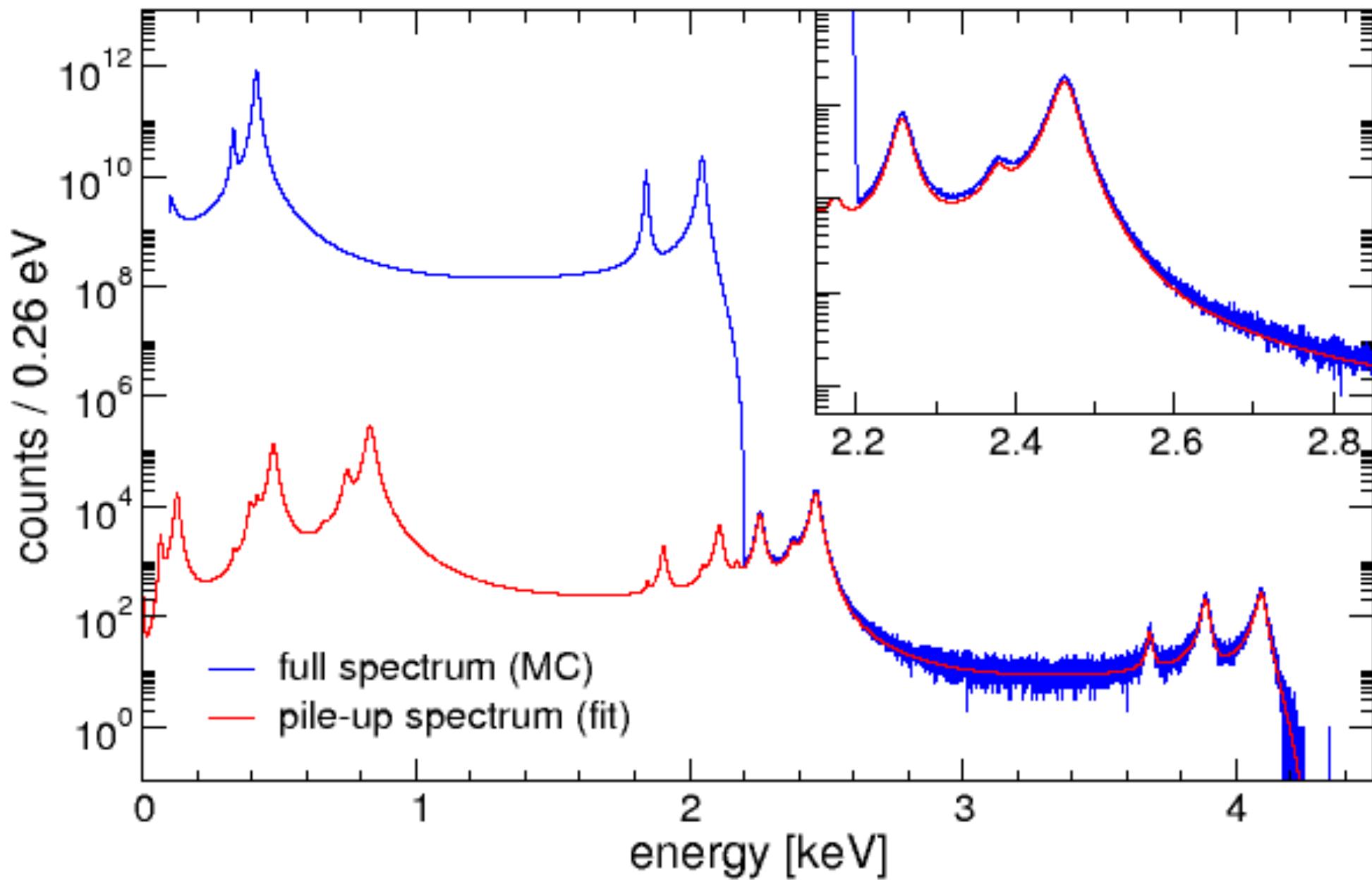


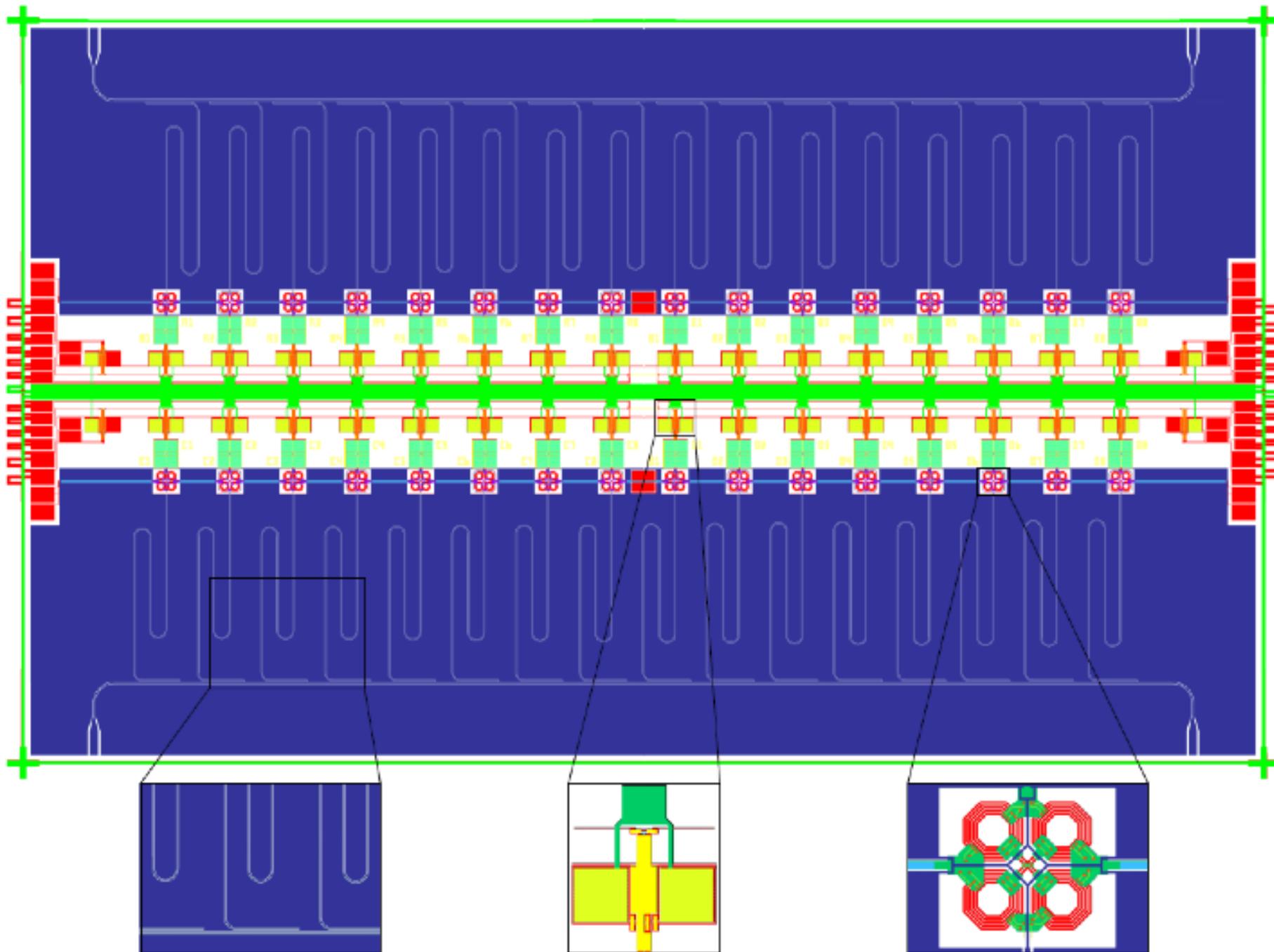
HOLMES



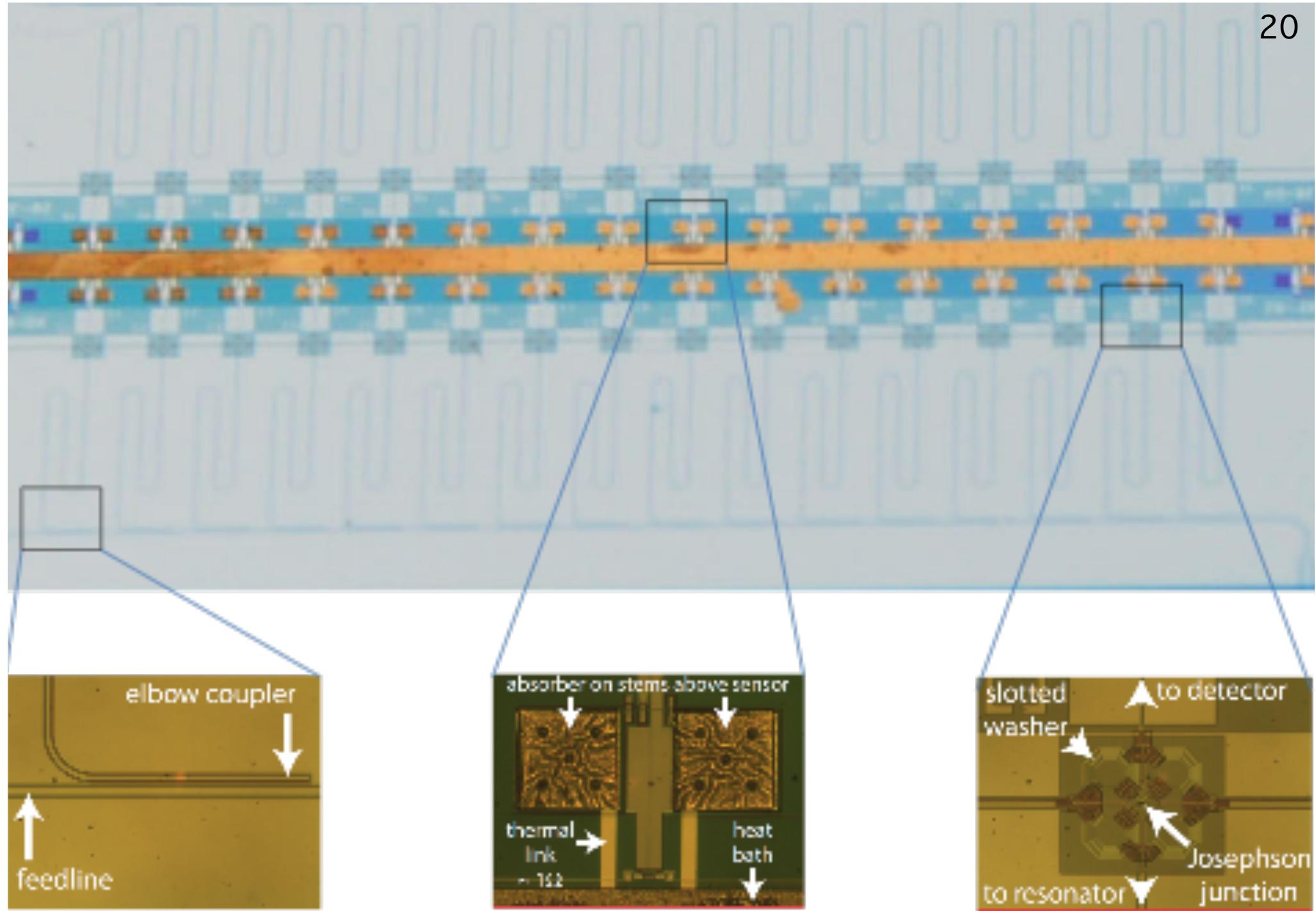


HOLMES

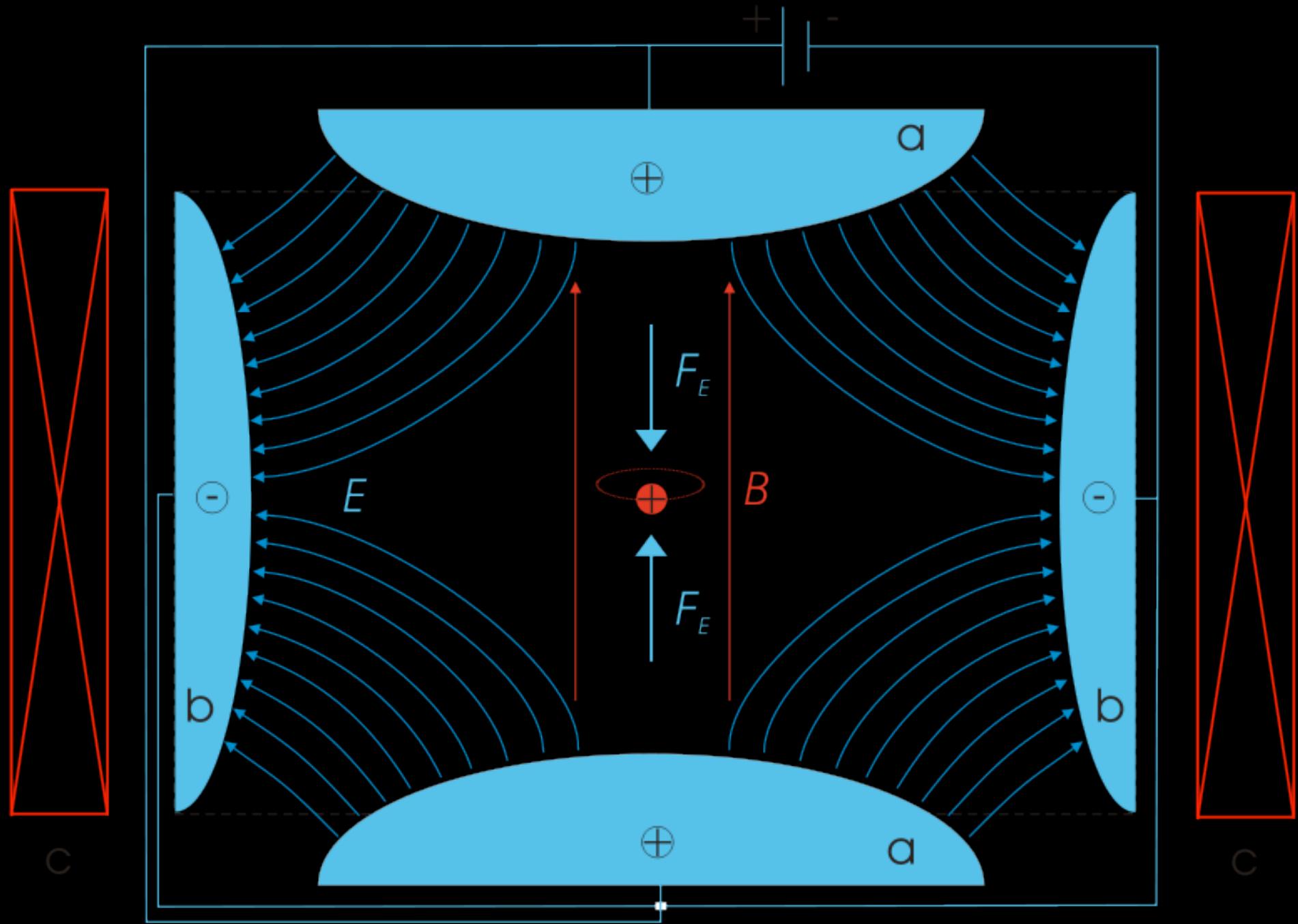




ECHo, courtesy of Loredana Gastaldo

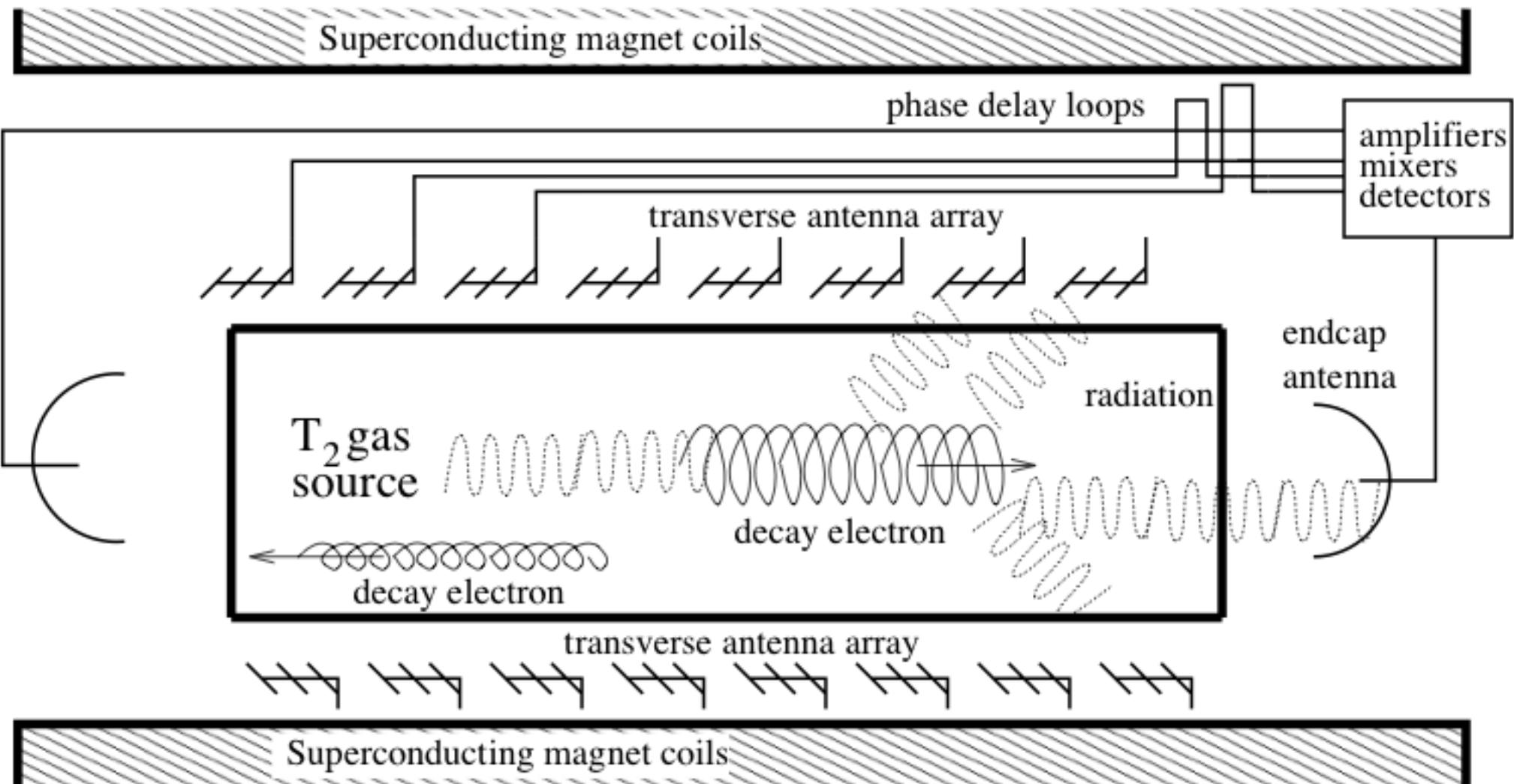


Penning Traps: accurate Q-values



OTHER AMBITIOUS PROJECTS

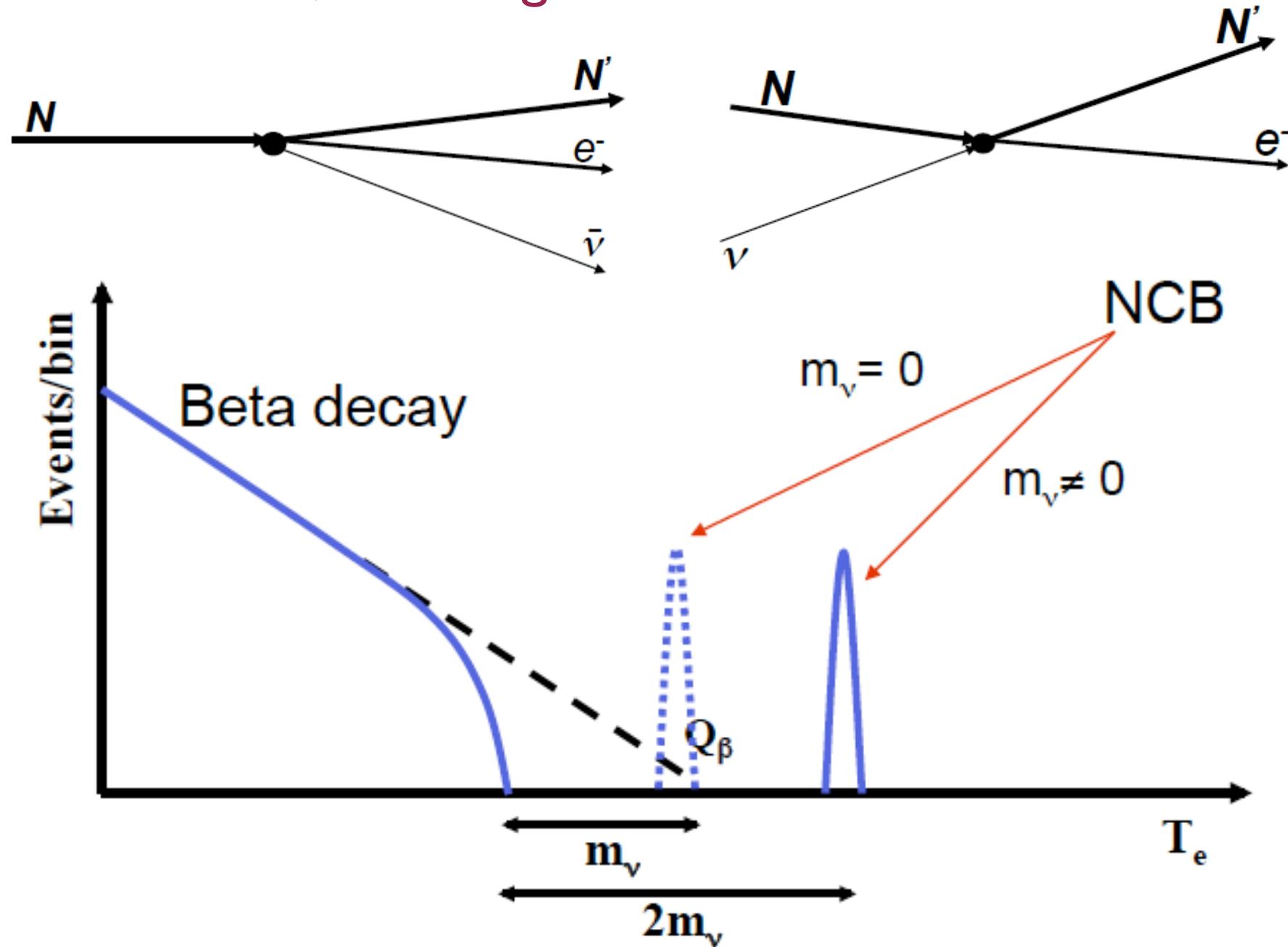
Project 8, B. Montreal & J. Formaggio



Electron E in Tritium decay measured via synchrotron radiation. At B=1T, E=Q: 26 GHz

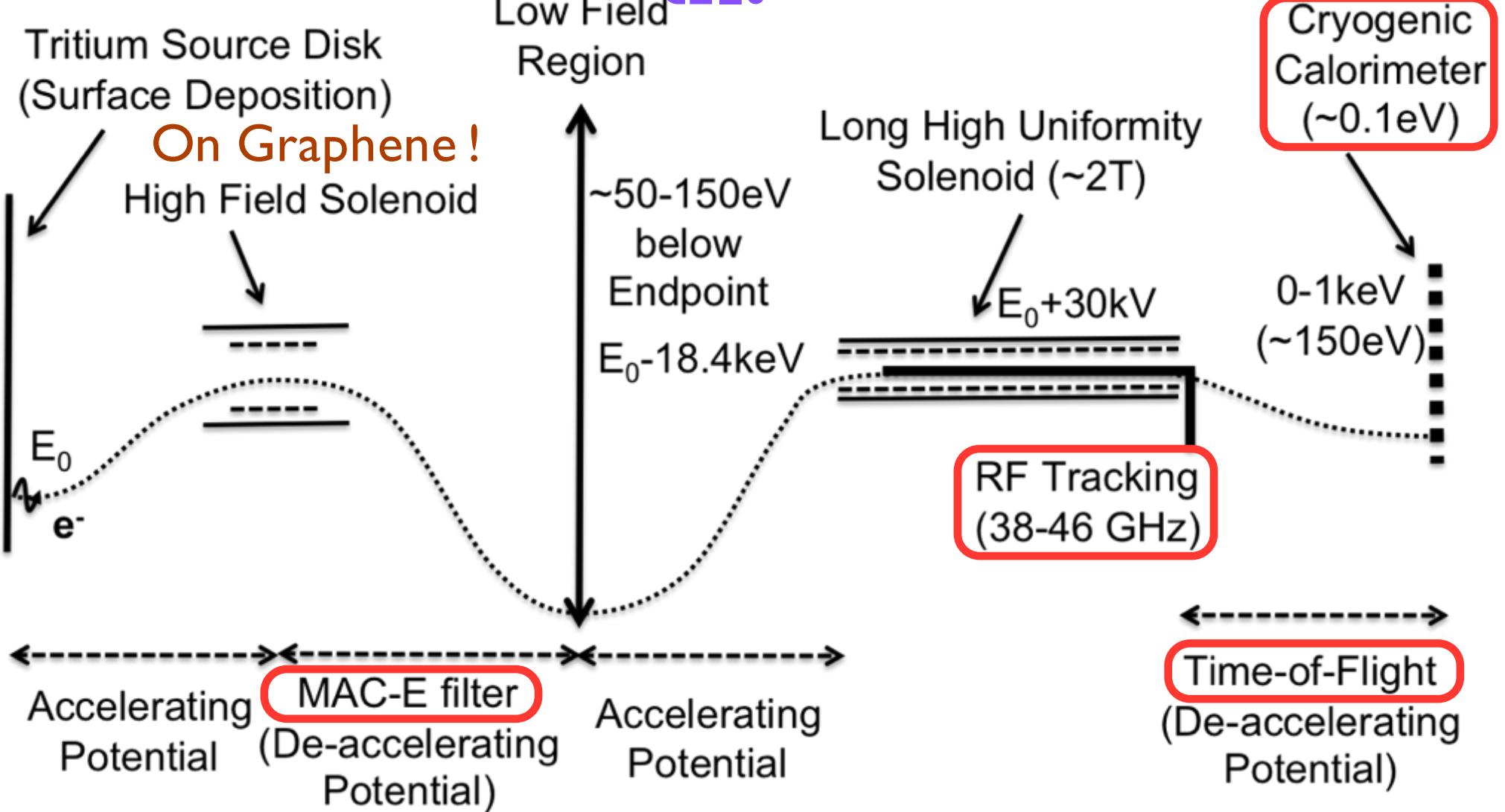
GOAL: 0.05 eV sensitivity in Phase III

Neutrino Cosmic Background (Weinberg 1962 !!! A.G. Cocco, G. Mangano & M. Messina. 2007)



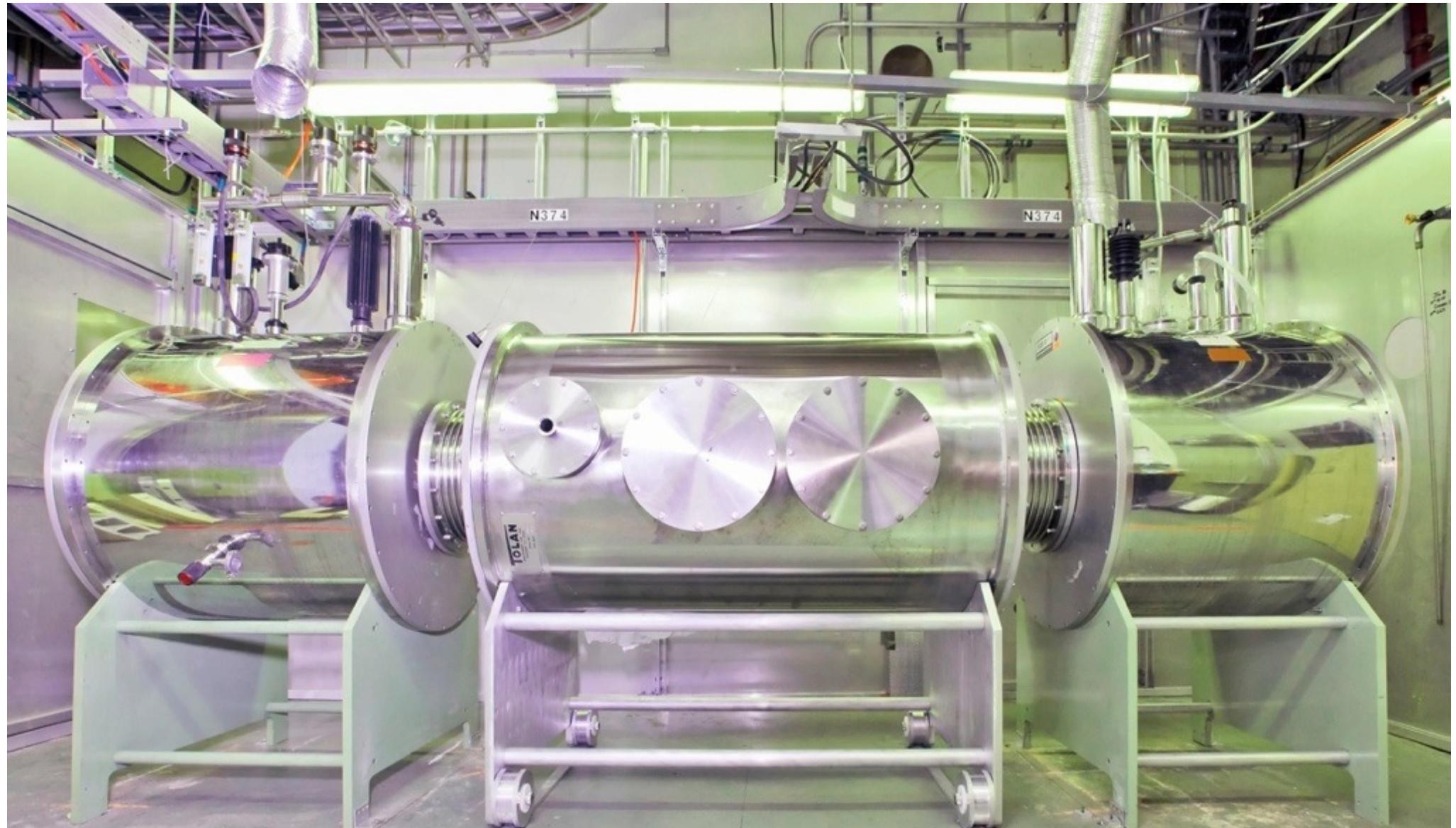
After C/2 no longer considered a joke!!

PTOLEMY; Chris Tully et al.



GOAL: > 9 events/y with 100 gr of T

WORKING PROTOTYPE



Which could improve current limits on $|U_{e4}|^2$

Holmium From Latin "Holmia": Stockholm.

Dysprosium from Greek

"δυσπρόσιτος", "hard to get at".

Rhenium From Latin *Rhenus*, the river Rhine.

Osmium From Greek ὄσμη "a smell".

Gadolinium in honor of Johan Gadolin, one of the founders of Nordic chemistry, discovered Yttrium, and pioneered laboratory exercise teaching.

Samarium after "Samarskite", the mineral

named after "Colonel Vasili Samarsky-

Bulkhovets" a Russian mine official

$$|U| = \begin{pmatrix} 0.795 \rightarrow 0.846 & 0.513 \rightarrow 0.585 & 0.126 \rightarrow 0.178 \\ 0.205 \rightarrow 0.543 & 0.416 \rightarrow 0.730 & 0.579 \rightarrow 0.808 \\ 0.215 \rightarrow 0.548 & 0.409 \rightarrow 0.725 & 0.567 \rightarrow 0.800 \end{pmatrix}$$