

Hints on the effective interaction from low energy reaction dynamics (EOS studies with SPES)

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Dissipative reaction mechanisms, involving heavy ions, can probe several aspects of the nuclear effective interaction and nuclear EOS

Outline

- The tool: **mean-field models** (TDHF, Vlasov, SMF) and **effective interactions**
- Some examples of suitable low-energy ($E/A \sim 5-10 \text{ MeV}/A$) **reaction mechanisms**
- Covariance analysis:
Sensitivity of selected **observables** to specific ingredients of the **effective interaction**

Mean-field models and effective interactions

One-body description

ρ_1 : one-body density

$$i\hbar \frac{\partial}{\partial t} \rho_1(t) = [H_{\text{eff}}, \rho_1(t)] + K(\rho_1) + \delta K(\rho_1, \delta\sigma)$$

TDHF
ETDHF

semi-classical approximation

$$\frac{\partial f(r, p, t)}{\partial t} + \{f, H_{\text{eff}}\} = k_l[f] + \delta k$$

Vlasov
BUU, SMF

Residual interaction:
in-medium NN cross section σ_{NN}
2-body correlations, Fluctuations

H_{eff} : effective Hamiltonian

- Expectation value of physical quantities :

$$E = \langle \Psi | \hat{H} | \Psi \rangle$$

$$\approx \langle \Phi | \hat{H}_{\text{eff}} | \Phi \rangle = E[\hat{\rho}]$$

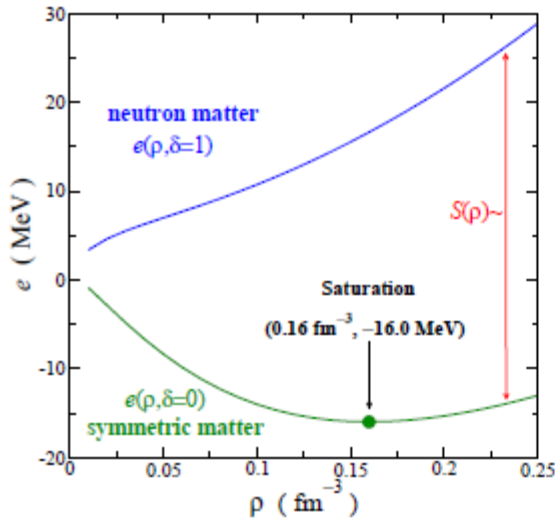
- Effective interactions are phenomenological (ex: **Skyrme** interactions, ...)

- Fitted parameters incorporate the effects of correlations beyond mean-field

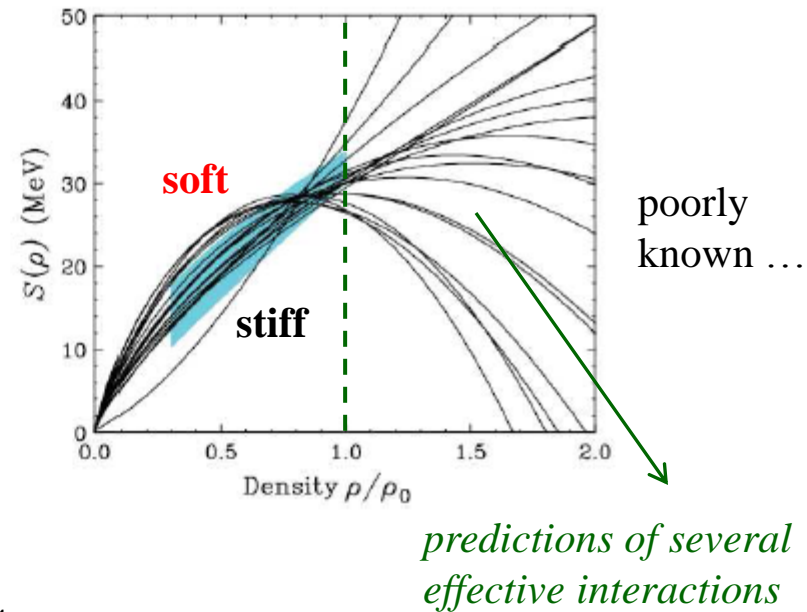
functions of isoscalar, spin, isospin densities, currents ... ➡ DTF, Nuclear matter EOS

The nuclear Equation of State (T = 0)

Energy per nucleon E/A (MeV)



Symmetry energy E_{sym} (MeV)



$$\frac{E}{A}(\rho, \beta) = \frac{E}{A}(\rho, \beta = 0) + E_{\text{sym}}(\rho)\beta^2 + O(\beta^4)$$

symm. matter

symm. energy

expansion around normal density

$$\beta = \text{asymmetry parameter} = (\rho_n - \rho_p)/\rho$$

➤ analogy with **Weizsacker mass formula** for nuclei (symmetry term) !

$$E_{\text{sym}}(\rho) = S_0 + L \frac{\rho - \rho_0}{3\rho_0} + \dots$$

$$25 \leq J \leq 35 \text{ MeV} \quad 20 \leq L \leq 120 \text{ MeV}$$

Low-energy reaction mechanisms: a study within mean-field models

- **Fusion vs Quasi fission or
Deep Inelastic**

- **Ternary breaking**

- **Charge equilibration**



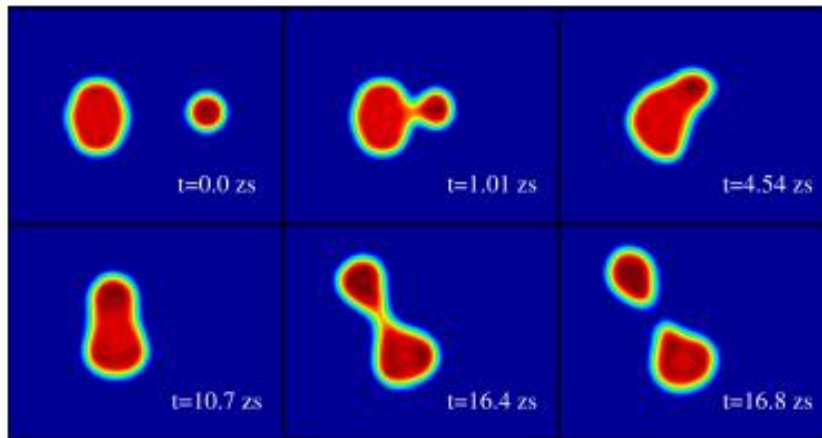
- **Fragmentation**

- **Isospin diffusion**

(Fermi energies)

Fusion vs. Quasi Fission: towards the synthesis of SHE

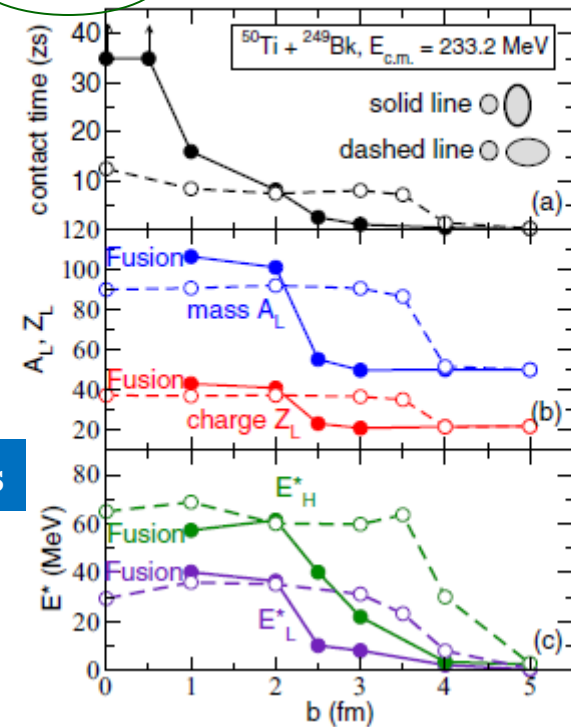
$^{50}\text{Ti} + ^{249}\text{Bk}$ 233 MeV



FUSION

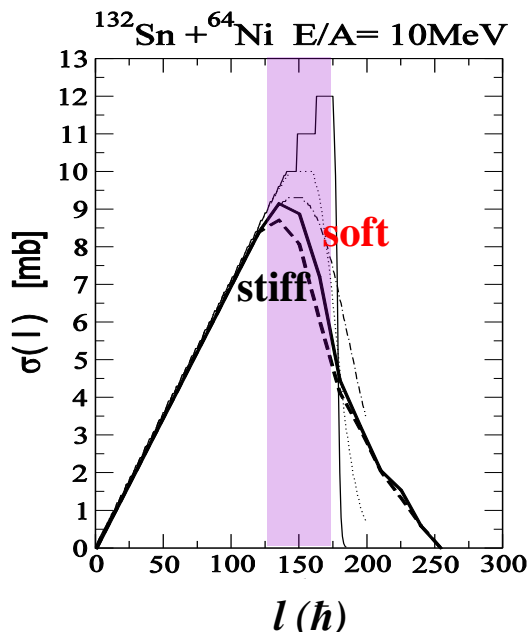
PHYSICAL REVIEW C 94, 024605 (2016)

Umar, Oberacker, Simenel



tip
side

TDHF calculations



• Fusion probability depends on the deformation/orientation of colliding nuclei

➤ Possible summetry energy effects ??

SMF calculations with neutron rich systems

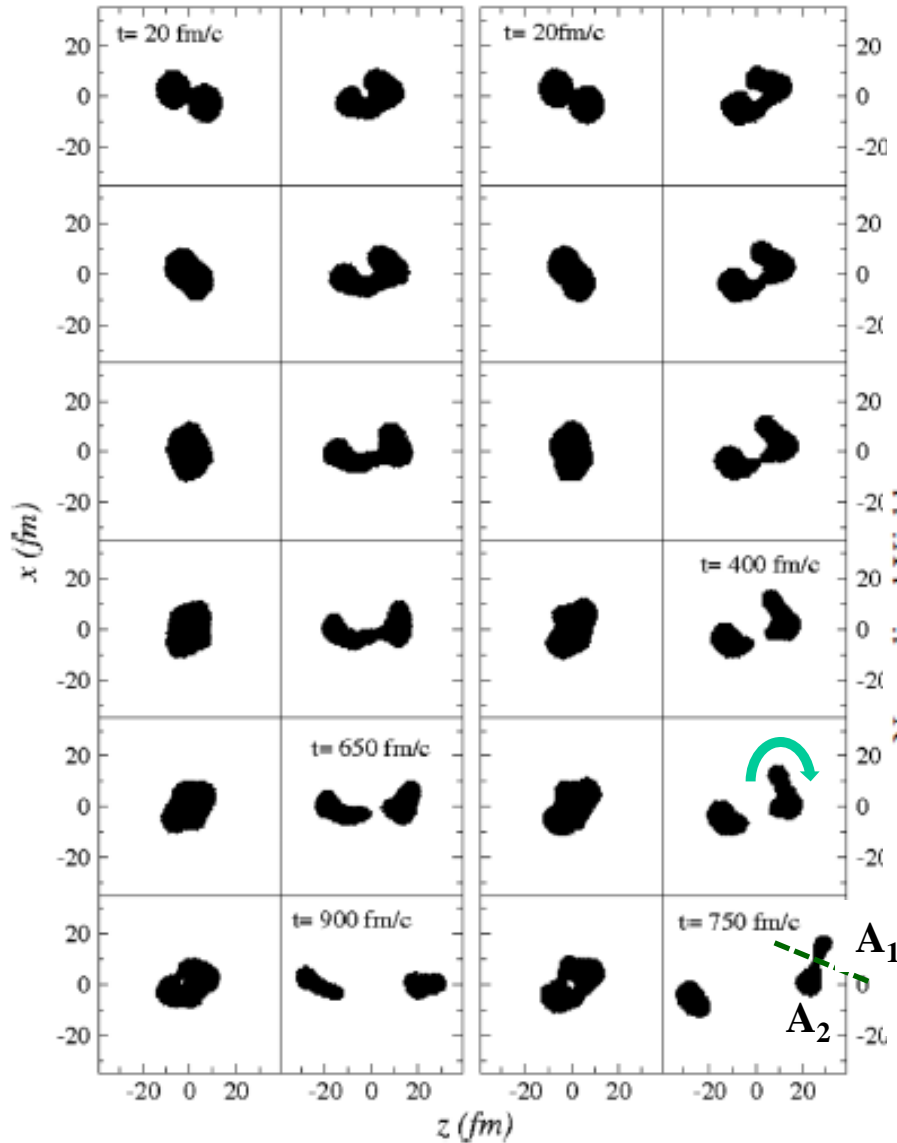


➤ A recent investigation: Ternary Quasi Fission

SMF

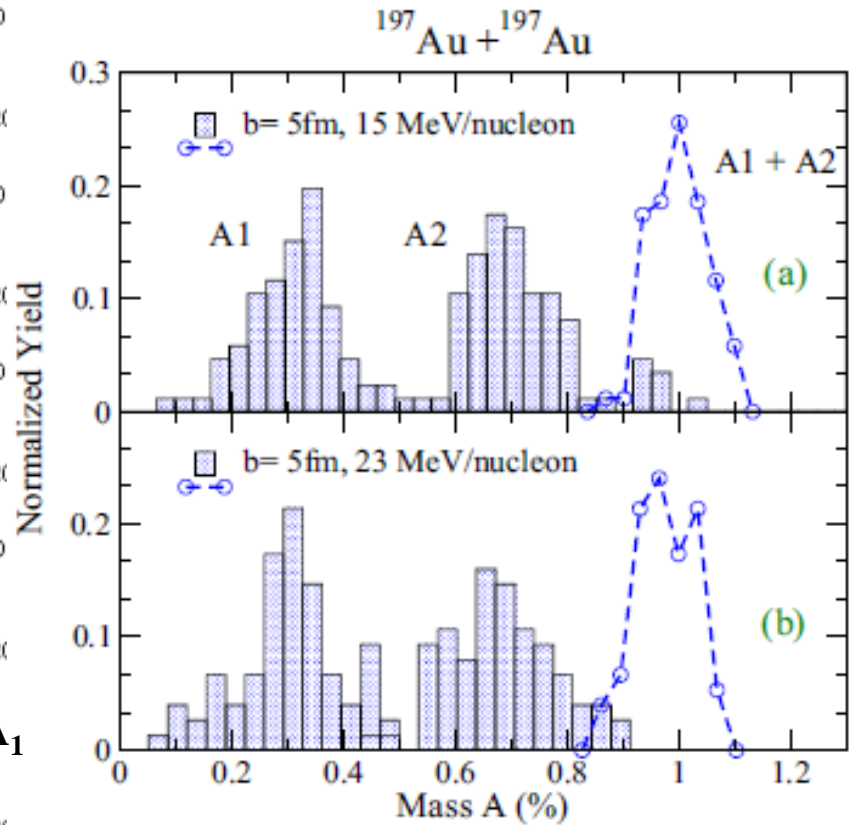
Skyrme forces

$^{197}\text{Au} + ^{197}\text{Au}$ 23 MeV/nucleon
 $b = 5 \text{ fm}$ $b = 6 \text{ fm}$



$^{197}\text{Au} + ^{197}\text{Au}$ collisions - 15 and 23 MeV/A

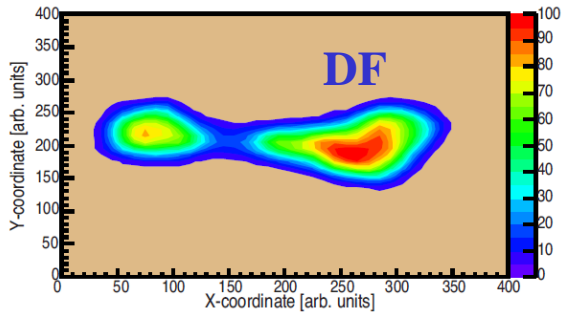
● Mass distribution of fragments emitted by DF fragment



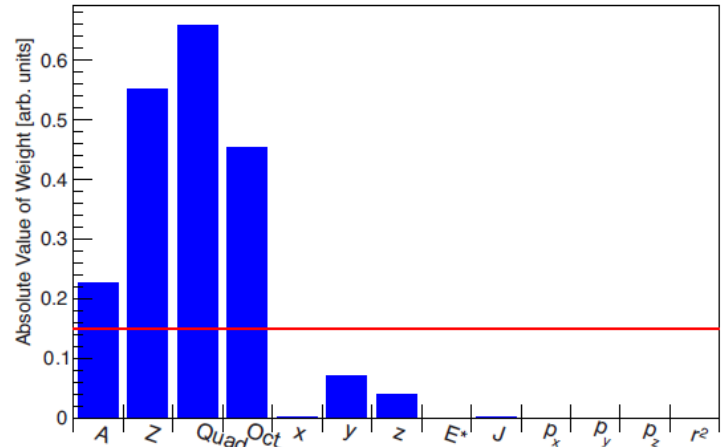
A1: lightest fragment
 A2: heaviest fragment

Ternary breakup in n-rich systems: Sensitivity to E_{sym} & Multidimensional Analysis

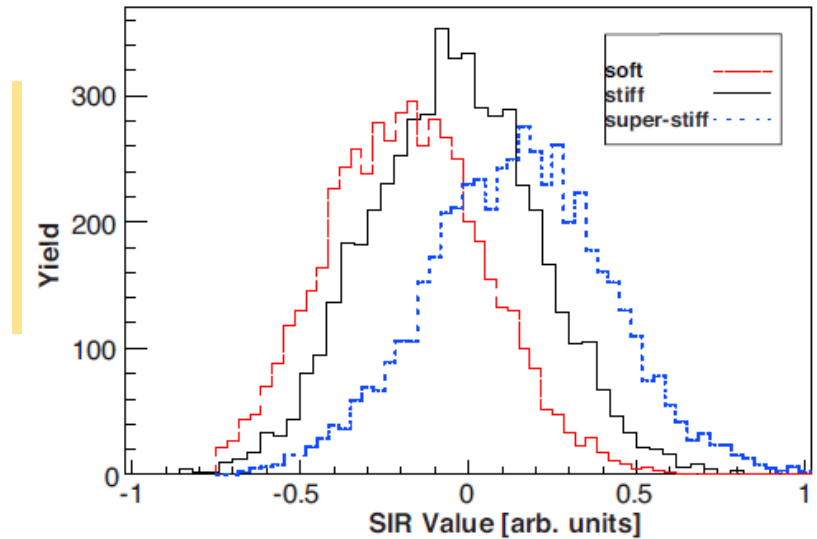
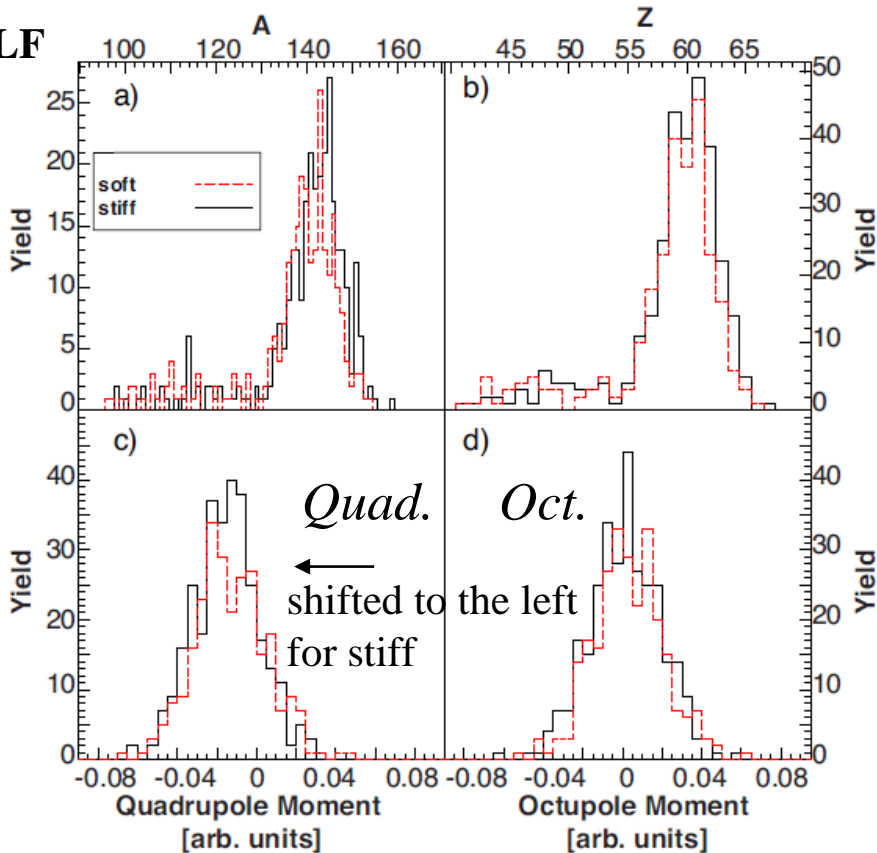
$^{124}\text{Sn} + ^{64}\text{Ni}$, $E/A = 10$ MeV, $b = 6-8$ fm



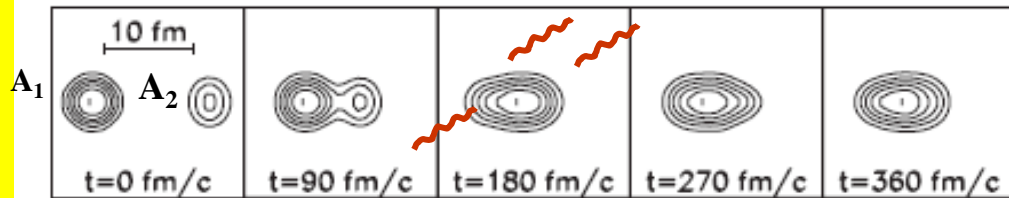
*PLF-TLF
configuration
at separation
time*



PLF



➤ Dipole excitations in heavy ion reactions (Dyn. Dipole)



TDHF
calculations

Simenel et al,
PRC 76, 024609 (2007)

Initial Dipole **D(t) : brems. dipole radiation** Compound: stat. GDR

If $N_1/Z_1 \neq N_2/Z_2$

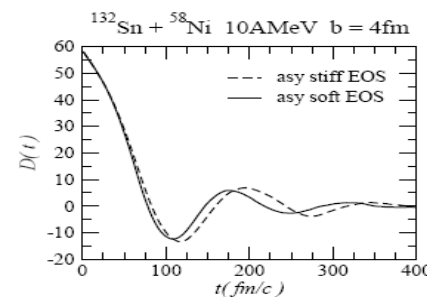
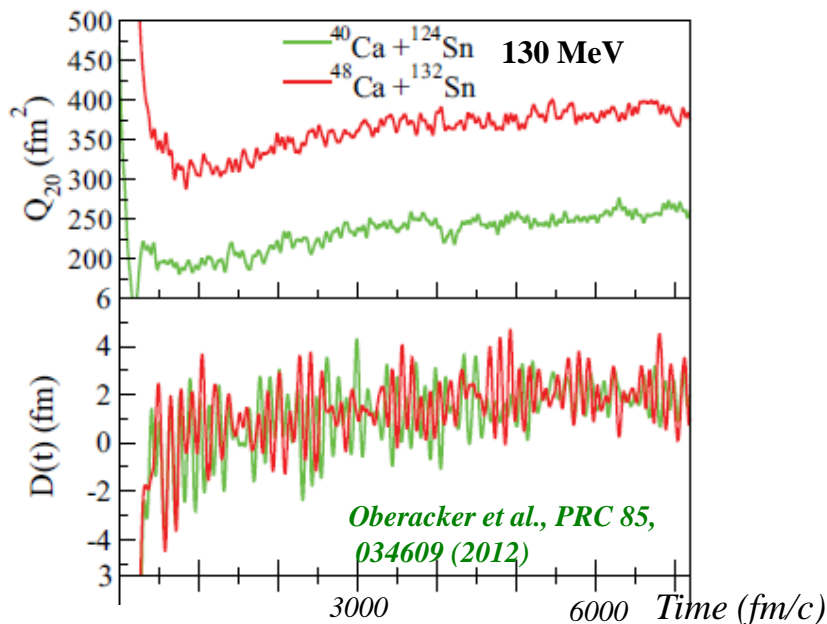
→ **Relative motion of neutron and proton centers of mass**

$$D(t) \equiv \frac{NZ}{A} [X_p(t) - X_n(t)] \rightarrow X_{p,n} \equiv \frac{1}{Z,N} \sum x_i^{p,n}$$

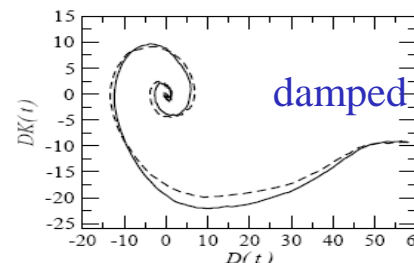
+ 2-body
collisional damping



SMF simulations



$^{132}\text{Sn} + ^{58}\text{Ni}$, $D_0 = 45$ fm
 $E/A = 10$ MeV

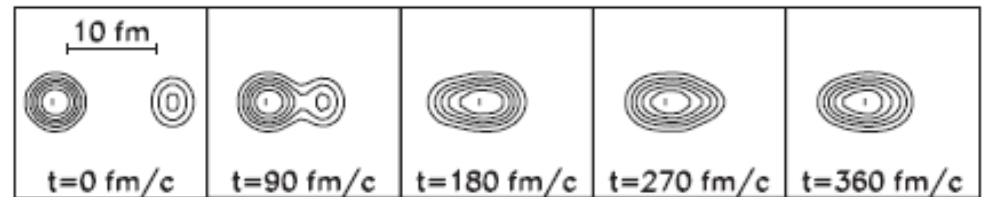


damped oscillations

C.Rizzo et al., PRC 83,
014604 (2011)

Dynamical Dipole in heavy ion reactions (DD)

- The restoring force is provided by the symmetry term (as in the standard GDR) probe the symmetry energy in the density conditions and configurations reached along the reaction path



- Cooling mechanism in the formation of SHE

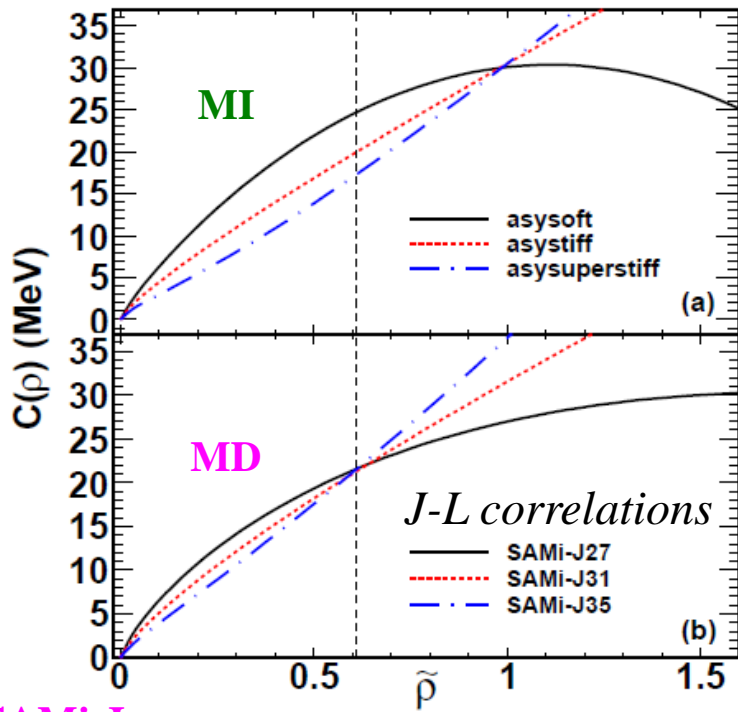
➤ **Few experimental data: more systematic analysis needed**

➤ **Theory:** a more systematic study of the sensitivity of this mechanism to the ingredients of the effective interaction and two-body dissipation needed

Ground state deformation important ???

→ DD in the fusion-evaporation of the $^{40}\text{Ca} + ^{152}\text{Sm}$ heavy system, C.Parascandolo et al., PRC 93, 044619(2016)

DD oscillations: dependence on the effective interaction



SAMi-J:

X. Roca-Maza, G. Colò, H. Sagawa, Phys. Rev. C 86, 031306(R) (2012); X. Roca-Maza *et al.*, Phys. Rev. C 87, 034301 (2013).

Skyrme (MI) : H.Zheng *et al.*,

PHYSICAL REVIEW C 94, 014313 (2016)

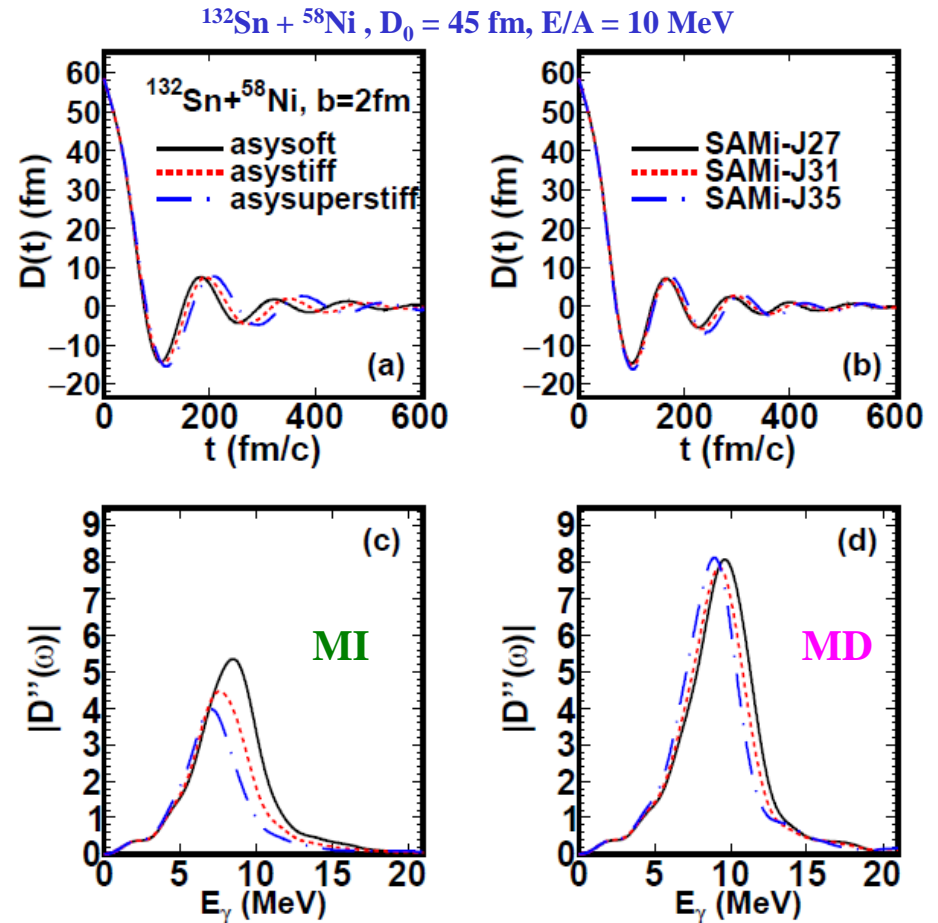
- free n-n cross section

$$\frac{dP}{dE_\gamma} = \frac{2e^2}{3\pi\hbar c^3 E_\gamma} \left| D''(\omega) \right|^2$$



$$P_\gamma \approx D_0^2 E_{centr}^3 \tau_{coll}$$

(damped harmonic oscillator)



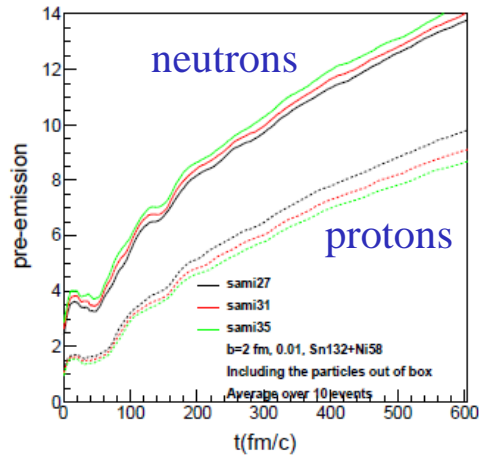
- The DD emission looks sensitive to E_{sym} at $\rho = 0.6 \rho_{sat}$
- Larger strength seen in the MD case:
similar to the enhancement factor in the GDR sum rule

Correlations: observables vs. parameters

A set of 8 parameterizations
in SMF simulations:

Skyrme (MI) and SAMi-J31
+ $\sigma_{NN} = 40 \text{ mb}, *2, /2$

Observables (A):
DD centroid, $D''(\omega)$ **integral**
and **N/Z** of **pre-equilibrium nucleon emission**



Parameters (B):
Symmetry energy slope **L**, effective mass **m***
and NN cross section (**cs**)
 τ_{coll} : collisional damping time

Covariance analysis

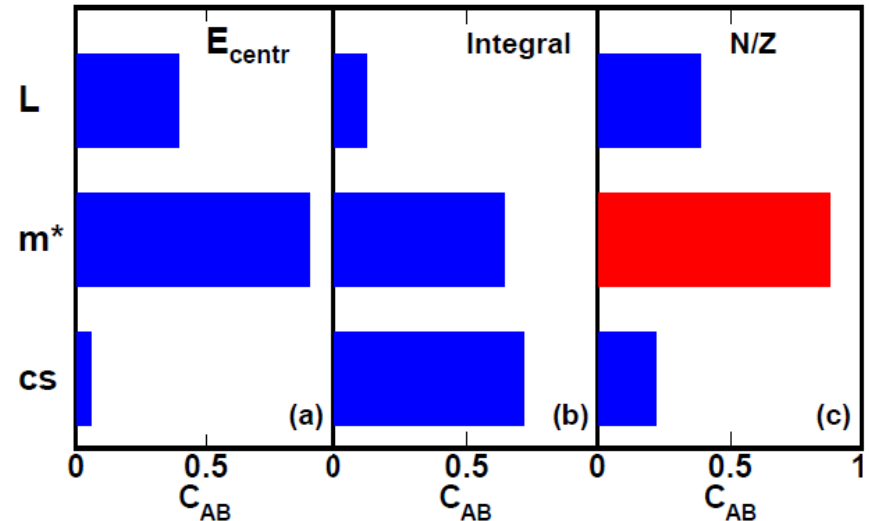
see also Zhang et al, PLB 749, 262 (2015)

$$C_{AB} = \overline{(A_{(n)} - \bar{A})(B_{(n)} - \bar{B})}$$

$$c_{AB} \equiv \frac{C_{AB}}{\sqrt{C_{AA}C_{BB}}}$$

Blue: negative

Red: positive



compare with $P_{\gamma} \approx D_0^2 E_{cent}^3 \tau_{coll}$
(energy-integrated yield)

□ Conclusions

Reactions with RIB's open the opportunity to learn about fundamental properties of the nuclear effective interaction, of interest also in the astrophysical context

➤ Low energy collisions:

Reaction mechanisms at the borderline with nuclear structure:

- role of effective interaction, 2-body dissipation

- n-skin, g.s. deformation

-Competition between reaction mechanisms (n-rich neck dynamics)

-Pre-equilibrium γ and particle emission

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