

# Ring-Lasers seismic rotational sensing

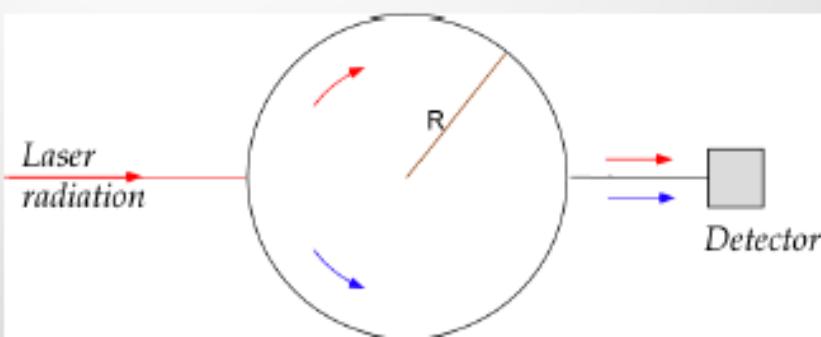
*Angela Di Virgilio-INFN-Pisa*

The Sagnac effect  
G-Pisa sensitivity and some data taken  
at VIRGO in 2010-2011  
GP2    GINGERino    G-Las

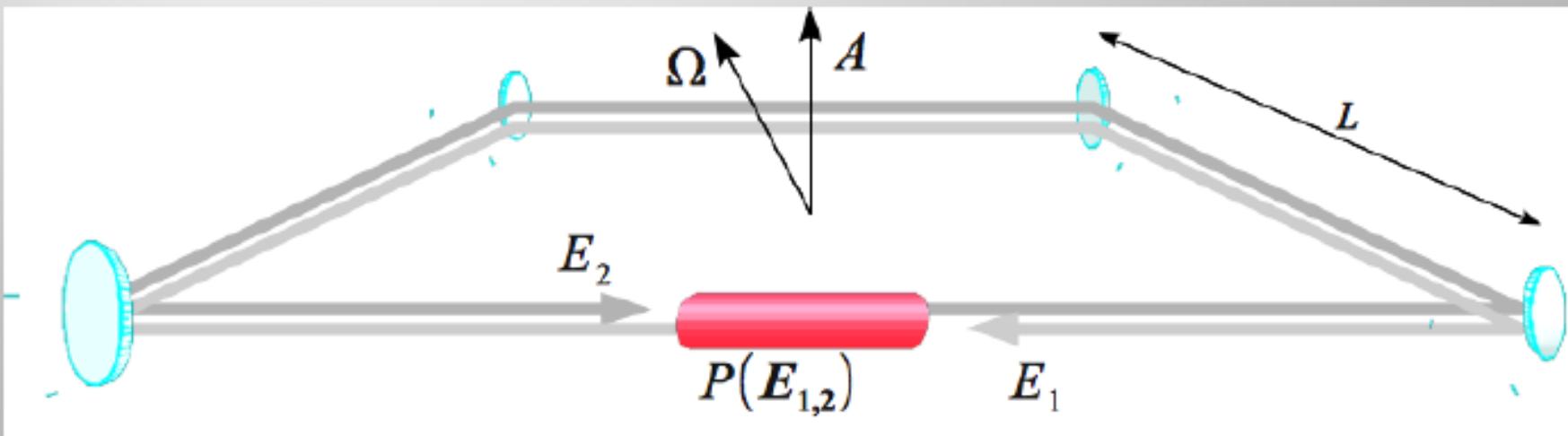
## Sagnac Effect

and basic of ring

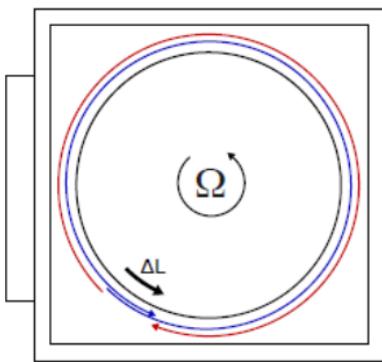
# The Sagnac Effect and the ring-laser



$$f_{\text{Sagnac}} = |f_{\text{CW}} - f_{\text{CCW}}| = \frac{4\vec{A} \cdot \vec{\Omega}}{\lambda p}$$

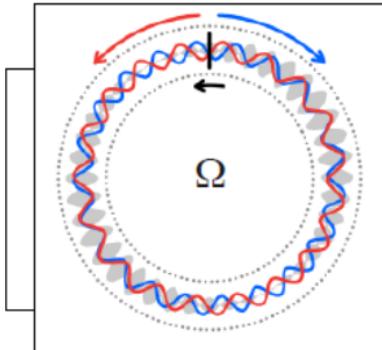


# Angular Rotation Inertial Sensor- No moving parts



Sagnac effect

$$\Delta t_{Sagnac} = \frac{4A}{c^2} \vec{\Omega} \cdot \vec{n}$$



Resonant cavity

$$\Delta f_{Sagnac} = \frac{4A}{P\lambda} \vec{\Omega} \cdot \vec{n}$$

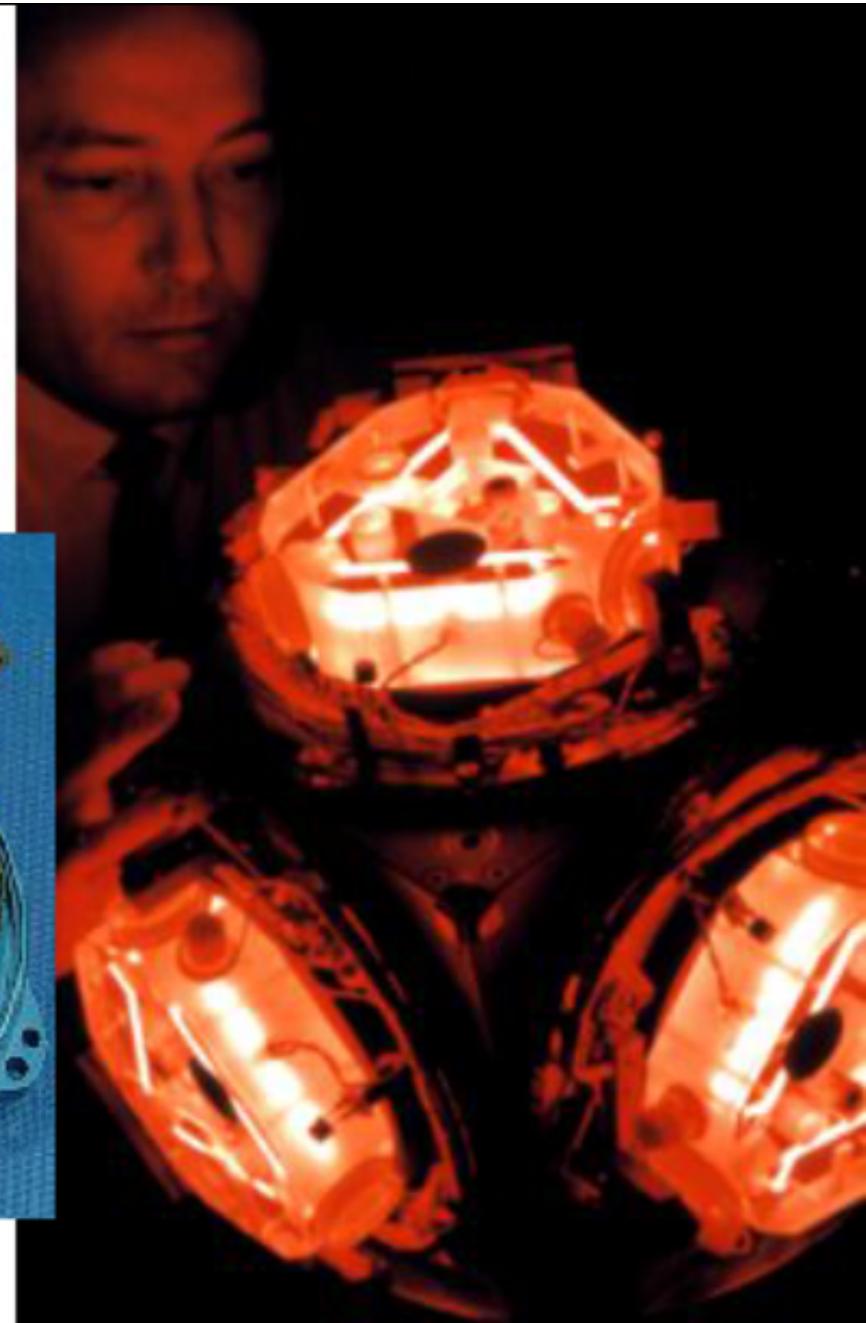
## Advantages

- No moving masses
- No signal for a linearly accelerating reference-frame
- $L > 1 \text{ m} \rightarrow$  Earth rotation is the bias

## Quantum limit

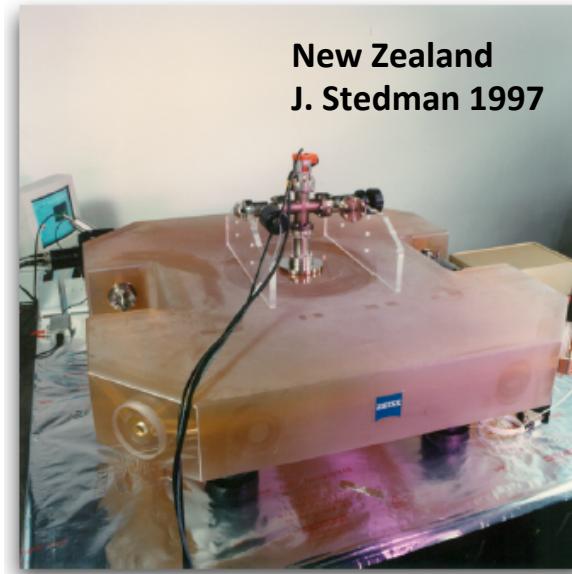
$$\delta \Omega_{shot} = \frac{c P}{4 A Q} \left( \frac{h \nu T}{2 P_{out} t} \right)^{1/2}$$

- Low cavity losses
- High power
- Large size



# Status of the Art of ring-laser

- Ring laser have a large application in navigation
- Few large frame rings have been developed for geodetic and geophysical application



- Prototype: C-II (1997)
- Perimeter 4 m
- He-Ne (632.8 nm)
- Cavity in Neutral Plane
- UHV-Compatibility
- RF-Excitation
- $\Delta\Omega/\Omega < 10^{-6}$  @ 1000 s

Feasibility of Concept shown

# **OUR INFN PROTOTYPES**

- Hetero-lithic mechanical design
- Stable by control

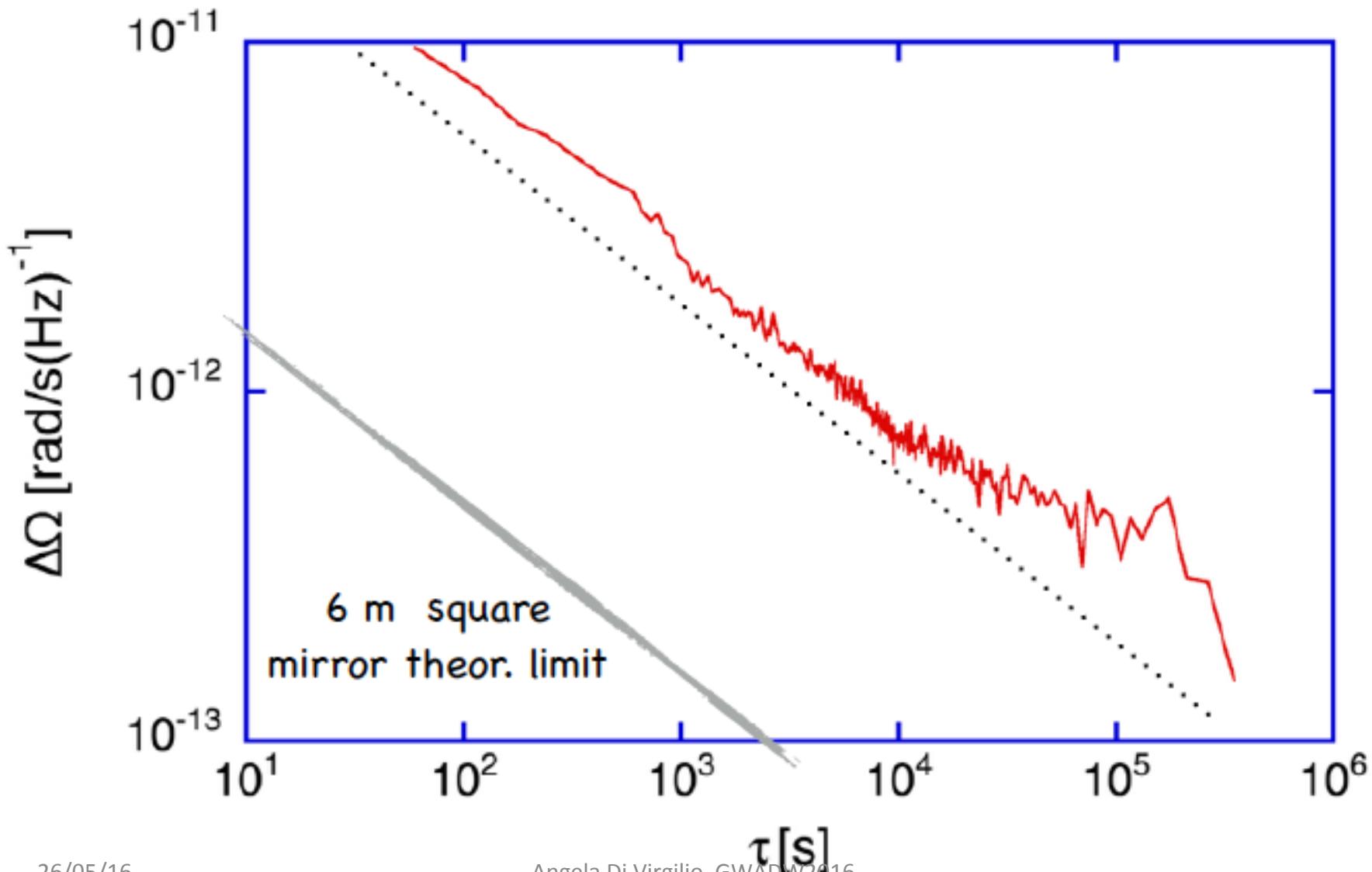
**LONG TERM STABILITY IS OUR MAIN CONCERN**

Since 2008, in collaboration with U. Schreiber of the GrossRing G  
of the Geodetic observatory of Wettzell

# What ‘long term’ stability means for us:

Courtesy U. Schreiber

TDEV G Ring (self-referenced)



# Ringlaser/Seismology

- Colocate one ring-laser+seismometer
- The simultaneous measurement of ground translation and rotation
- dispersion curve of Love waves over a broad frequency range, from which a local shear-wave velocity profile can be inferred with resolutions on the order of 100 m and penetration depths up to several tens of kilometers.

# Several INFN experiments, from 2008 G-Pisa/ G-GranSasso-DS/ G-GranSasso-RD

At present G-GranSasso-RD (CommII):

Pisa: J. Belfi, N. Beverini, G. Carelli, A. Di Virgilio, U. Giacomelli, E. Maccioni, A. Simonelli

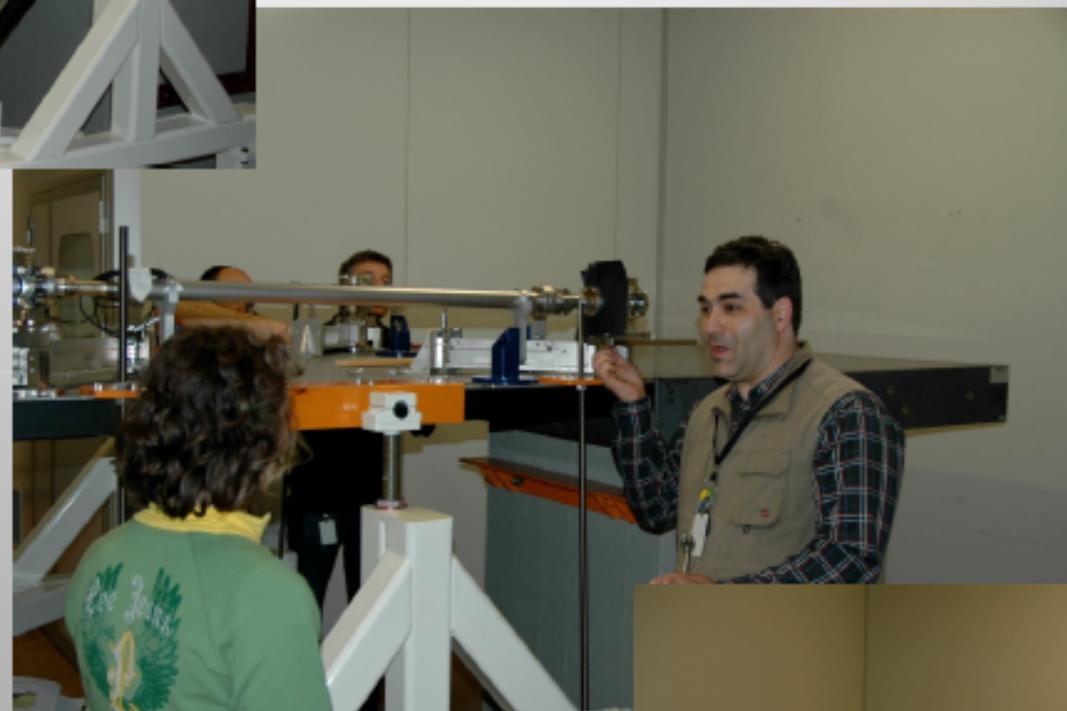
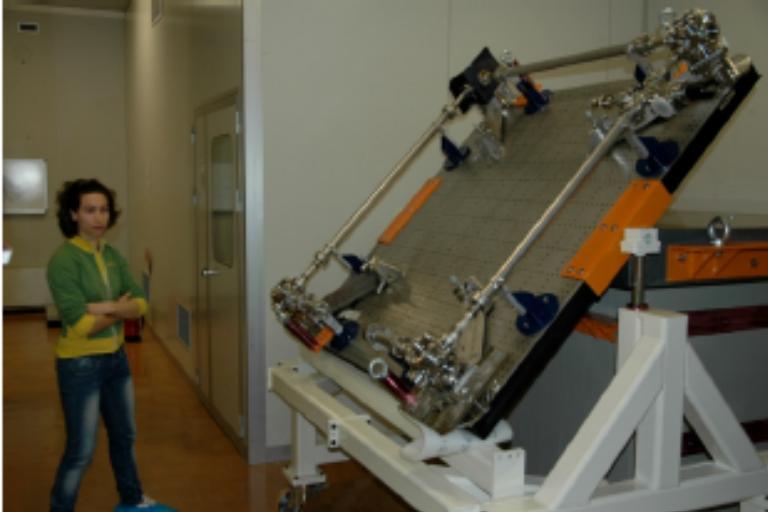
LNL: A. Ortolan

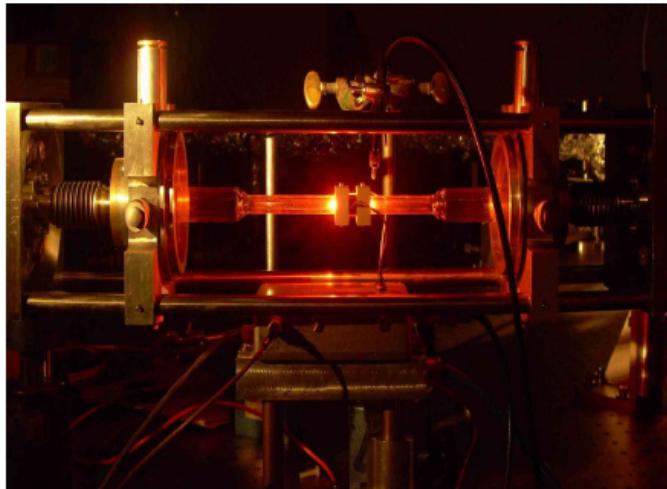
Padova-DEI: A. Beghi, D. Cuccato, A. Donazzan, G. Naletto, M. Pelizzo

Napoli: C. Altucci, A. Porzio, R. Velotta

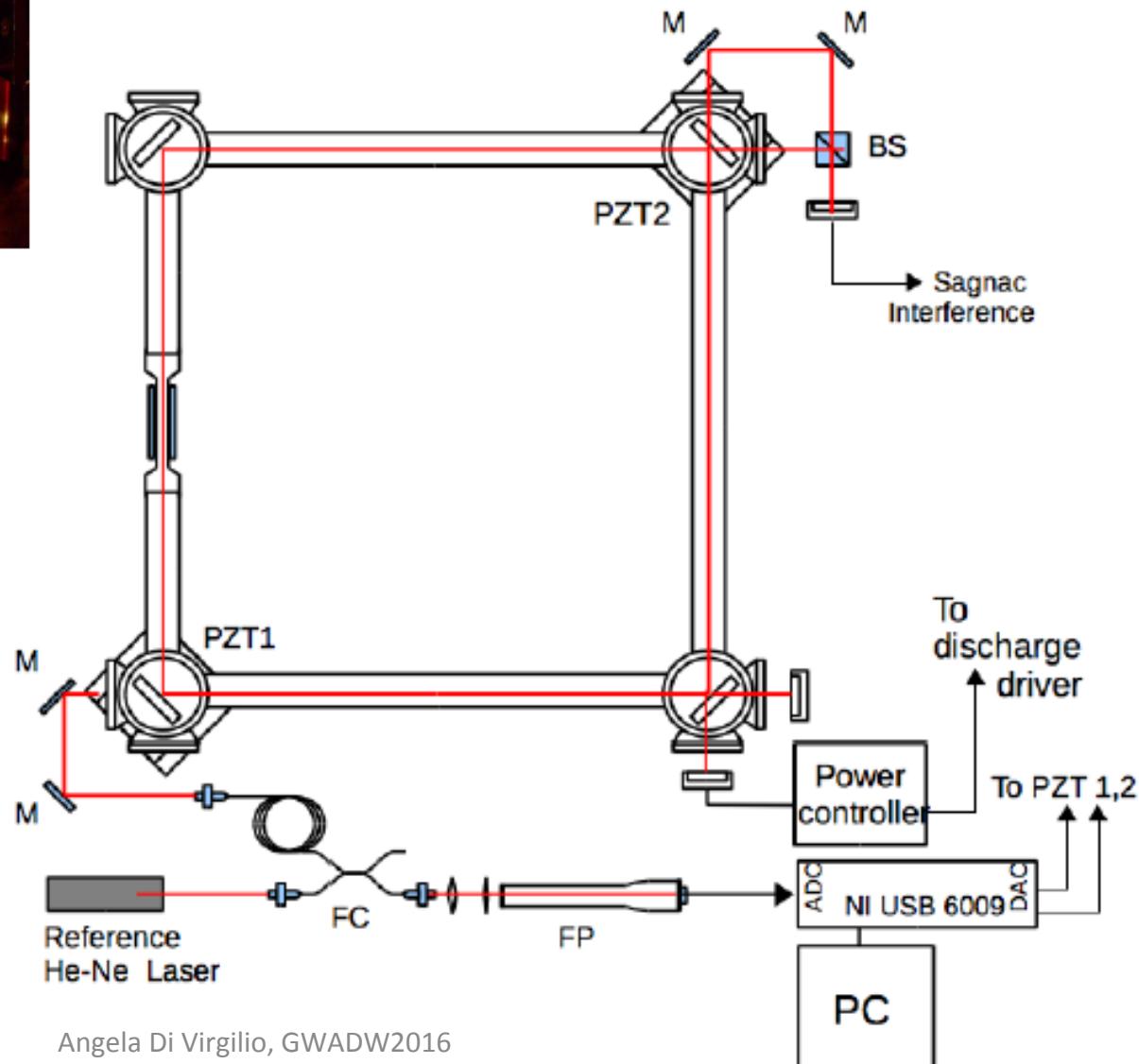
Torino: ML Ruggiero, A. Tartaglia *General Relativity theory*

G-Pisa during the installation in Virgo





**Getters pumps avoid  
the aging of the gas**



# Ring Lasers are Shot-Noise Limited

- sensitivity improves quadratically with L (Q & p/A)
- $P_{out}$ , typically 10-20 nW, but should be possible go up to 500mW-1mW
- Typical wavelength 633nm, but infrared and green are feasible
- Squeezing in principle feasible, but no experience so far

Quantum limit     $\Omega_{SN} = \frac{c p}{2 Q A} \sqrt{h \frac{v_L}{P_{out} t}}$

# Sensitivity depends on several parameters

- Wavelength, losses and transmission of the mirrors, side length, output power

# Example: 4.5 total losses, 633nm (other wavelength feasible-infrared and green)

Side/power	1. m, PSD rad/s 1 s	2m
10 nW	<b><math>3.8 \cdot 10^{-10}</math></b>	<b><math>1.9 \cdot 10^{-10}</math></b>
50 nW	<b><math>1.7 \cdot 10^{-10}</math></b>	<b><math>8.5 \cdot 10^{-10}</math></b>
500 nW	<b><math>5 \cdot 10^{-11}</math></b>	<b><math>2.7 \cdot 10^{-11}</math></b>

# Bandwidth depends on the ringdown time of the cavity

- Size of the ring and quality of the mirrors
- Typical value in our prototypes (meter size): from 80 $\mu$ s up to 660 $\mu$ s

**$\sim$ 1kHz bandwidth**

**They can run continuously unattended**

# Transportable

## **Our first prototype G-Pisa:**

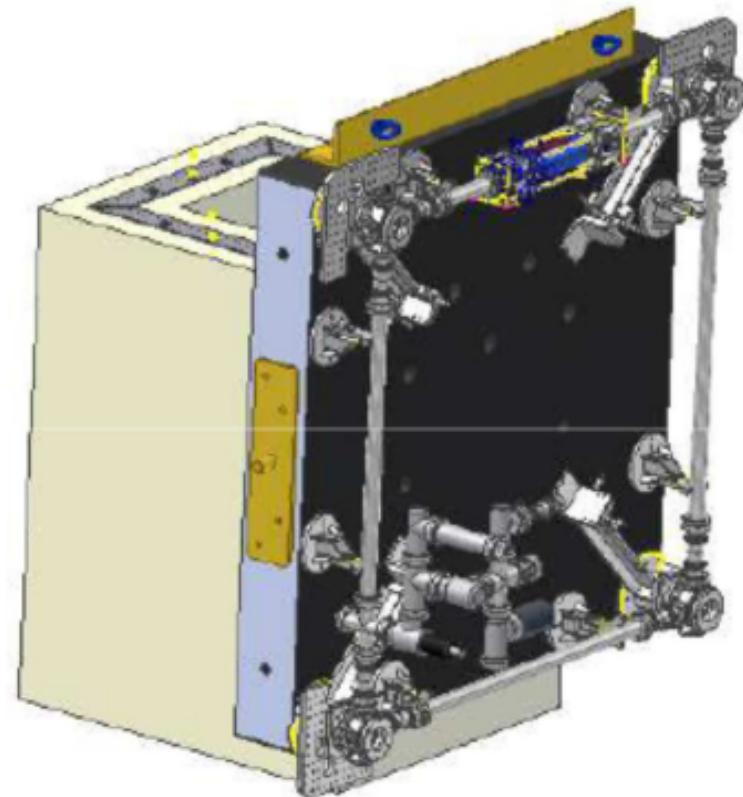
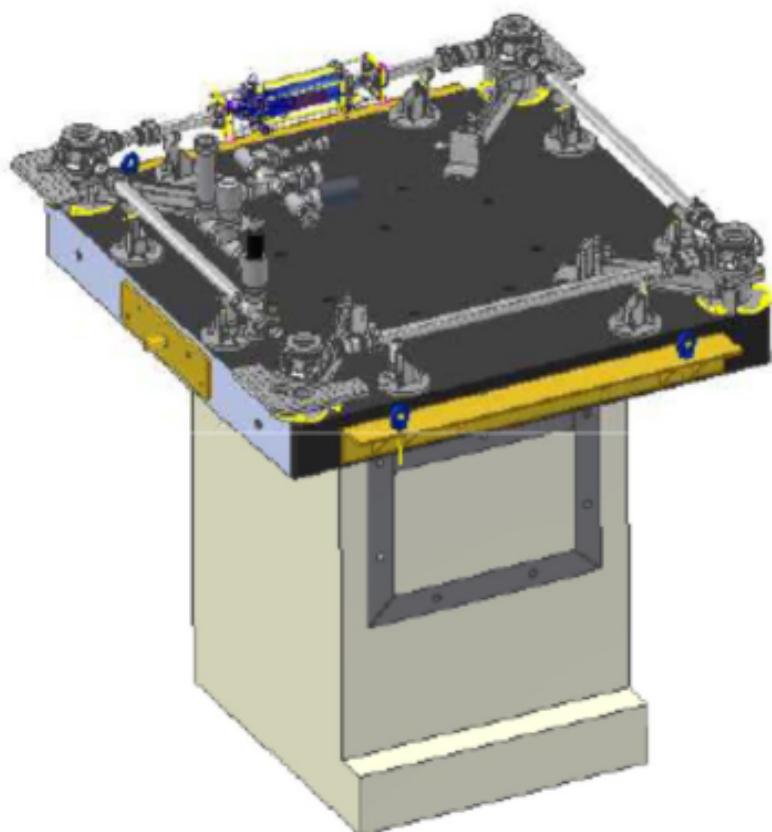
- assembled in Pisa, and has taken data in Pisa
- moved to the VIRGO central area
- has taken data for several months during last Virgo run  
(data stored in the raw data)
- Has been moved to S.Piero, and has taken data there
- Has been moved to the GranSasso national lab. And  
has taken data there
- In 2015 it has been disassembled and the mechanical  
parts are now user for the new prototype GINGERino

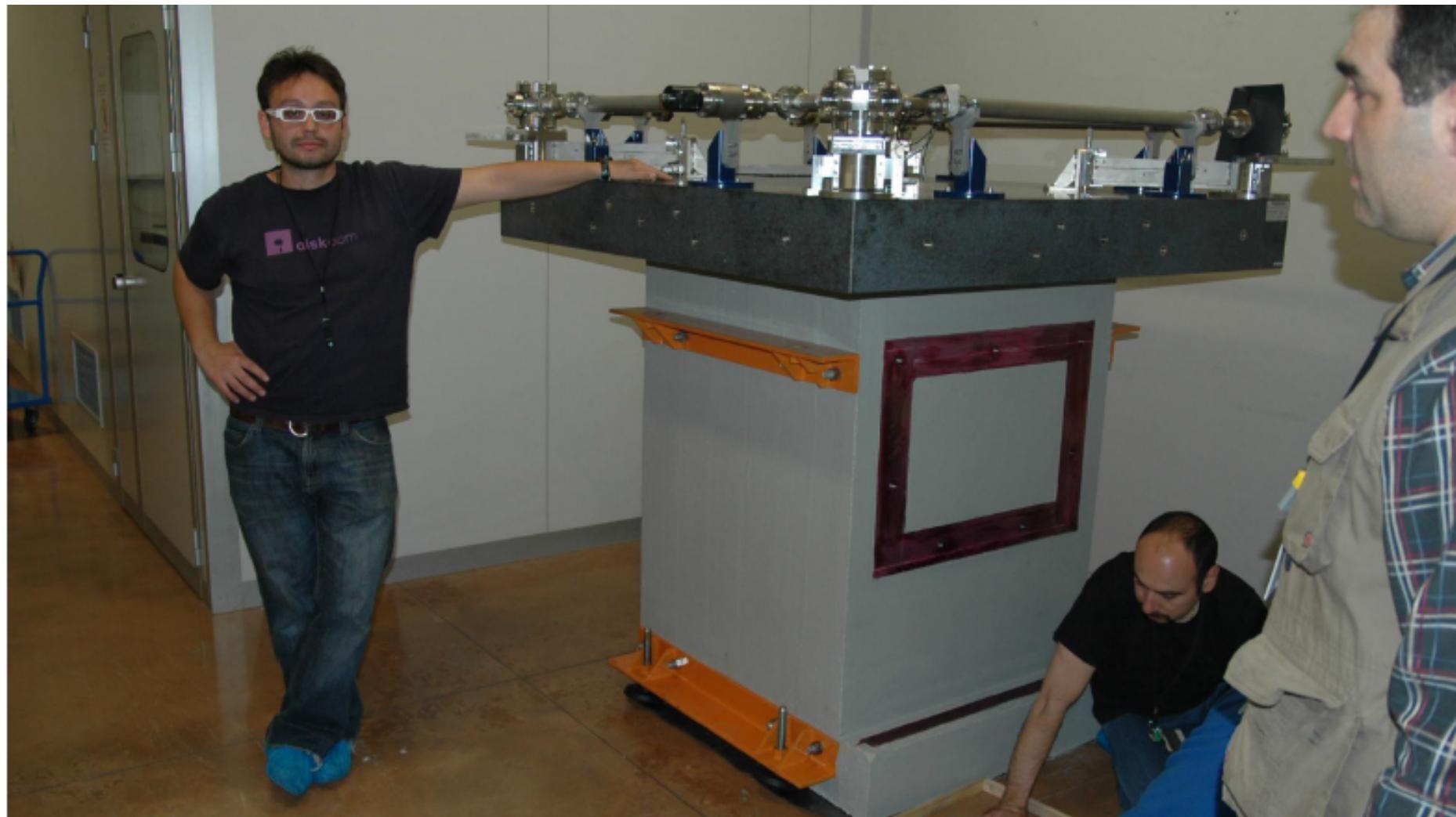


26/05/16

Angel Angela Divisione WADW 2011

# Horizontal and vertical gyrolaser operation

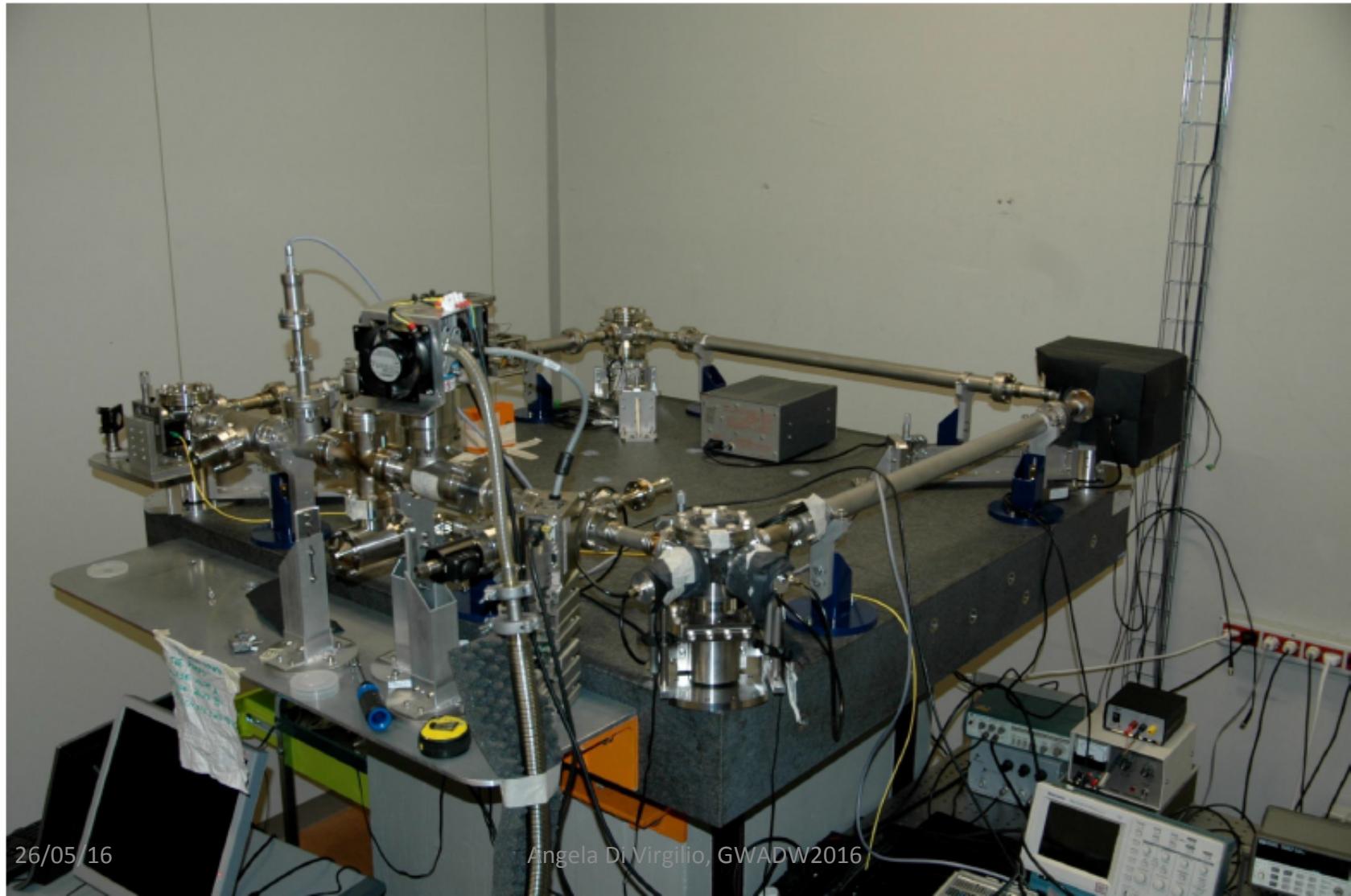




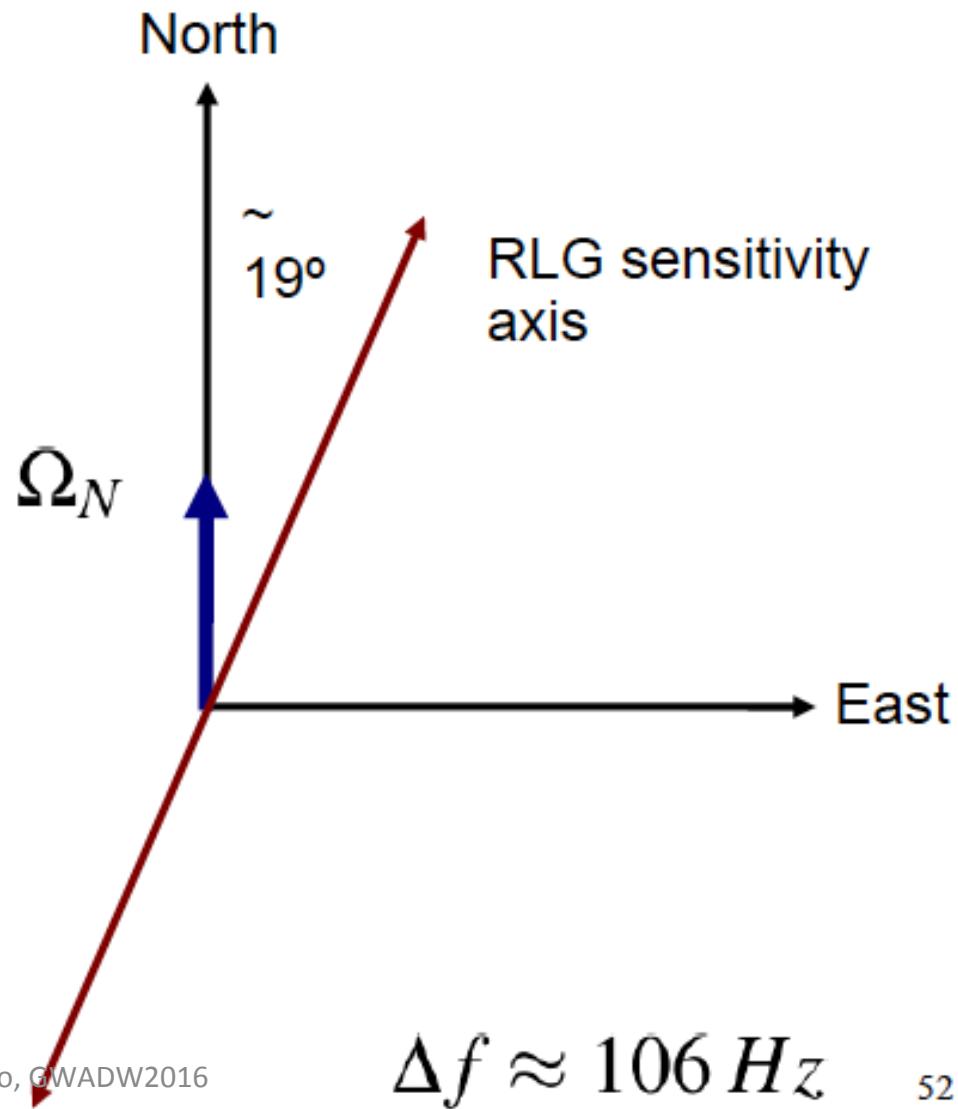
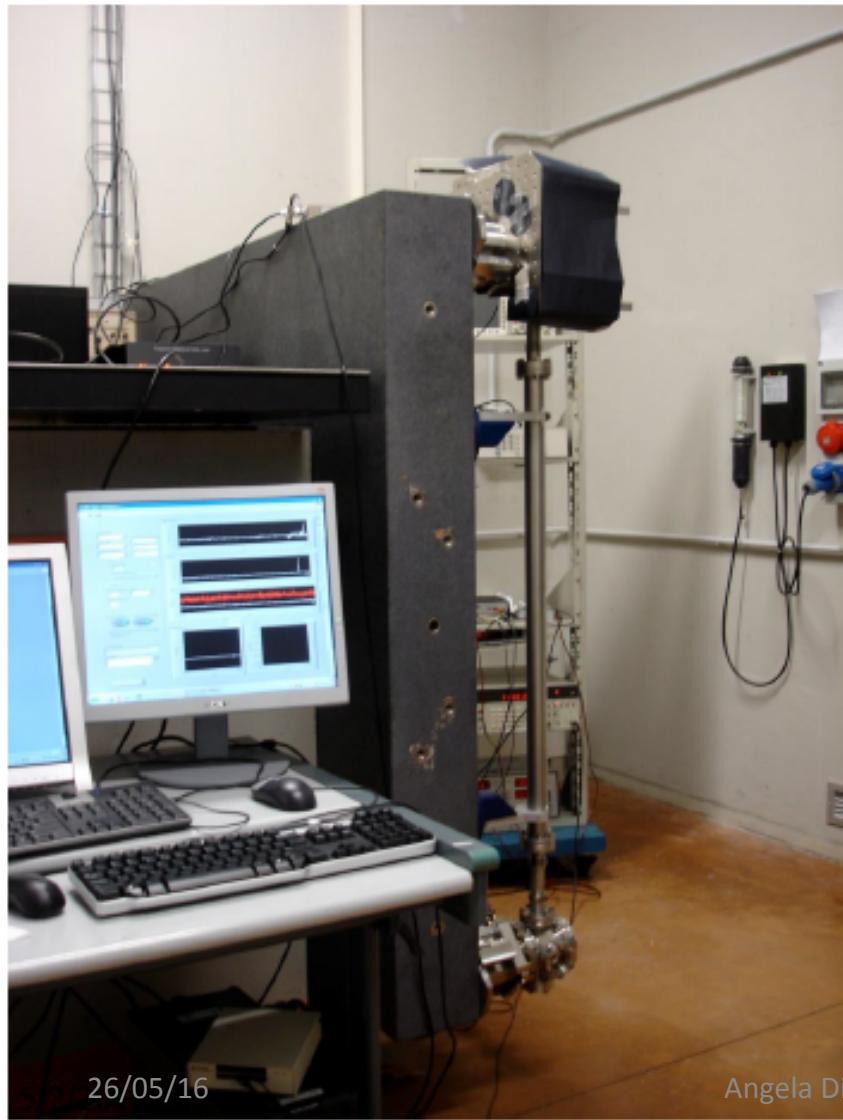
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# G-Pisa in the Virgo Central Area



# G-Pisa RLG



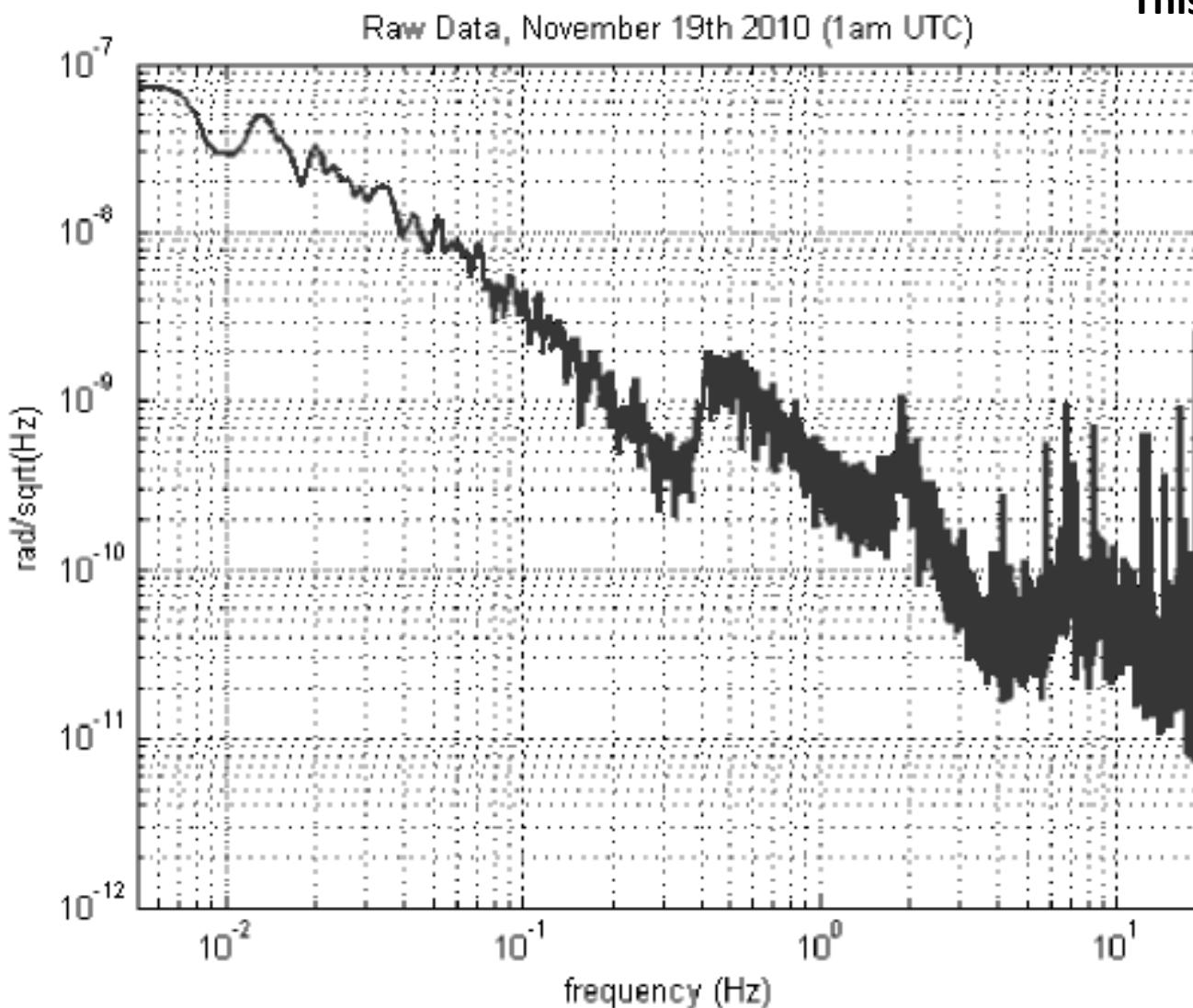
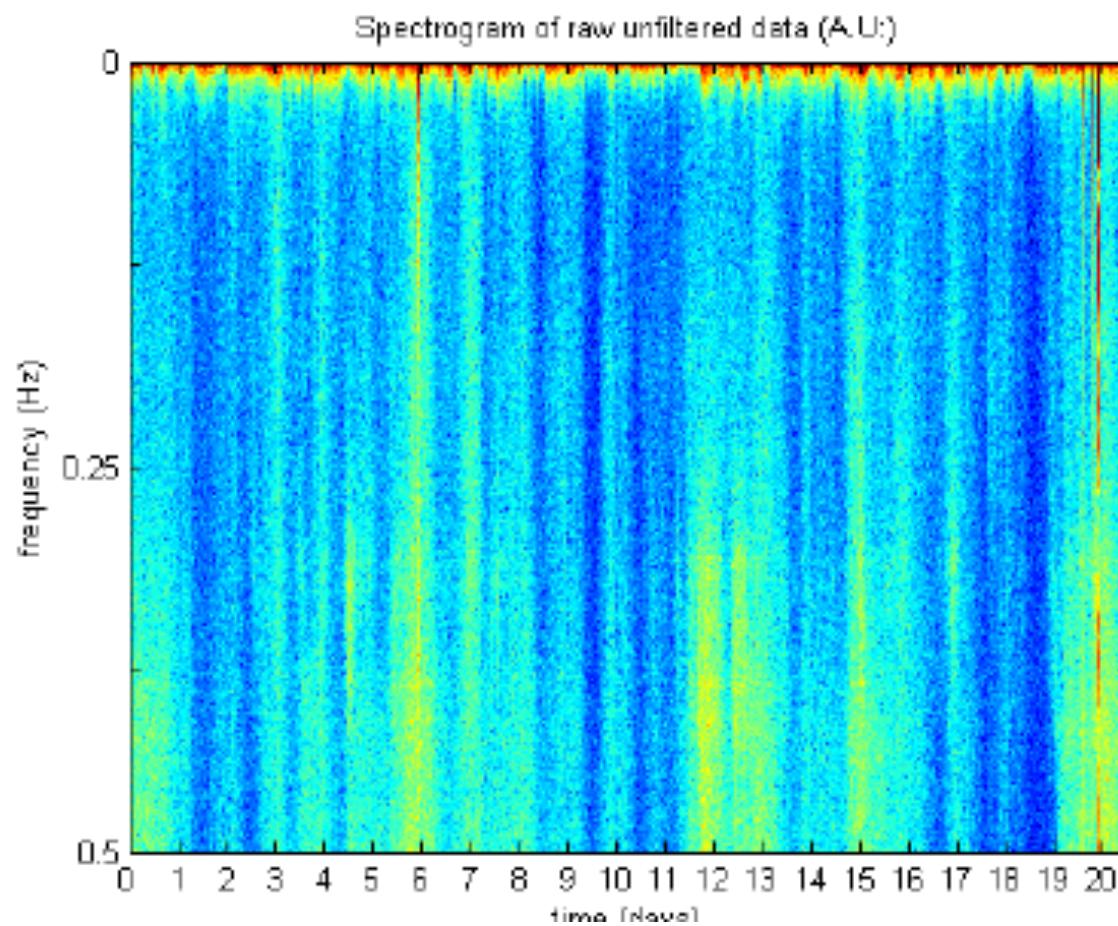
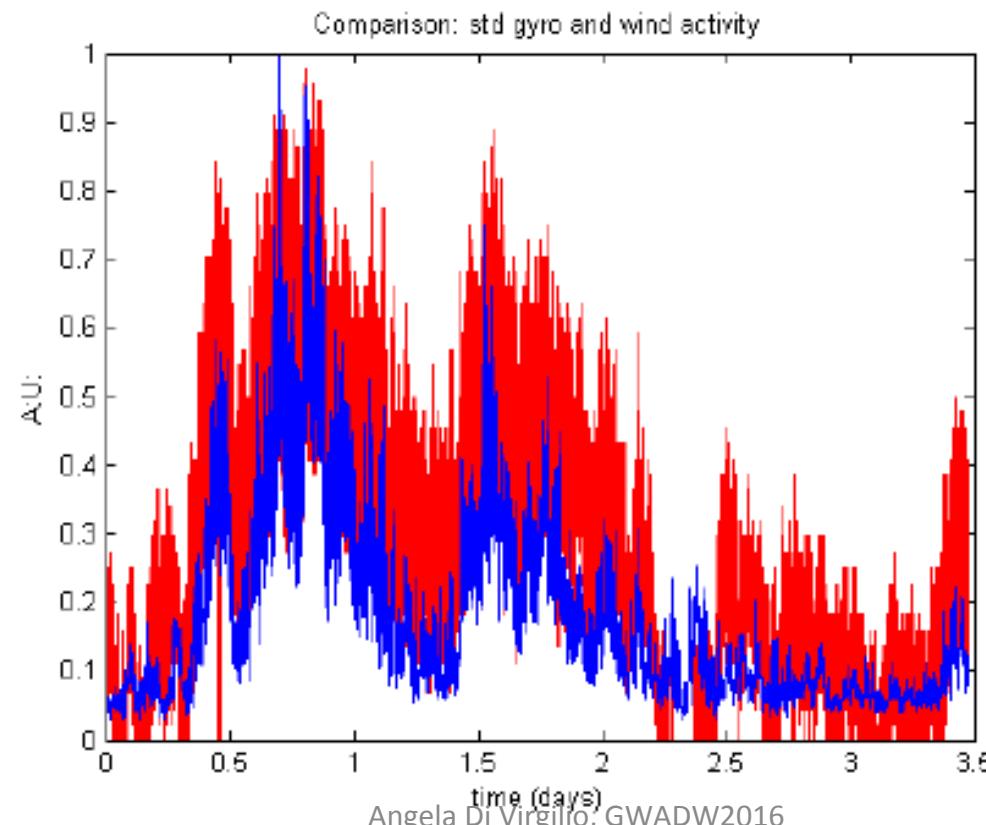


Fig. 10 Tilt sensitivity in a very quiet period, the requirements of AdVirgo are  $10^{-8} \text{ rad}/\sqrt{\text{Hz}}$  in the range 5 – 500 mHz.

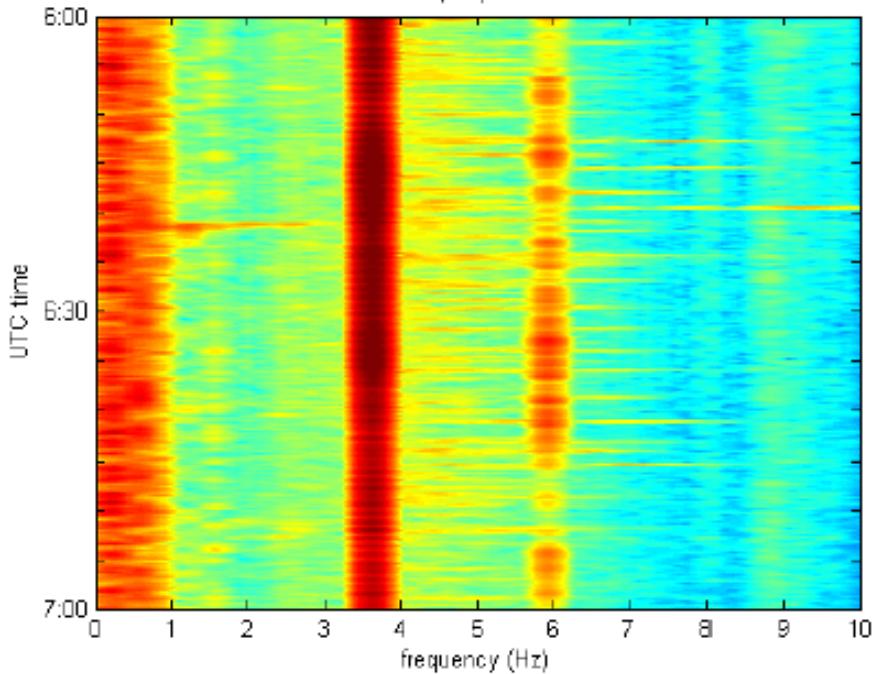
# On month of continuous Data Taking with perimeter locked



# Comparison with the Wind Monitor

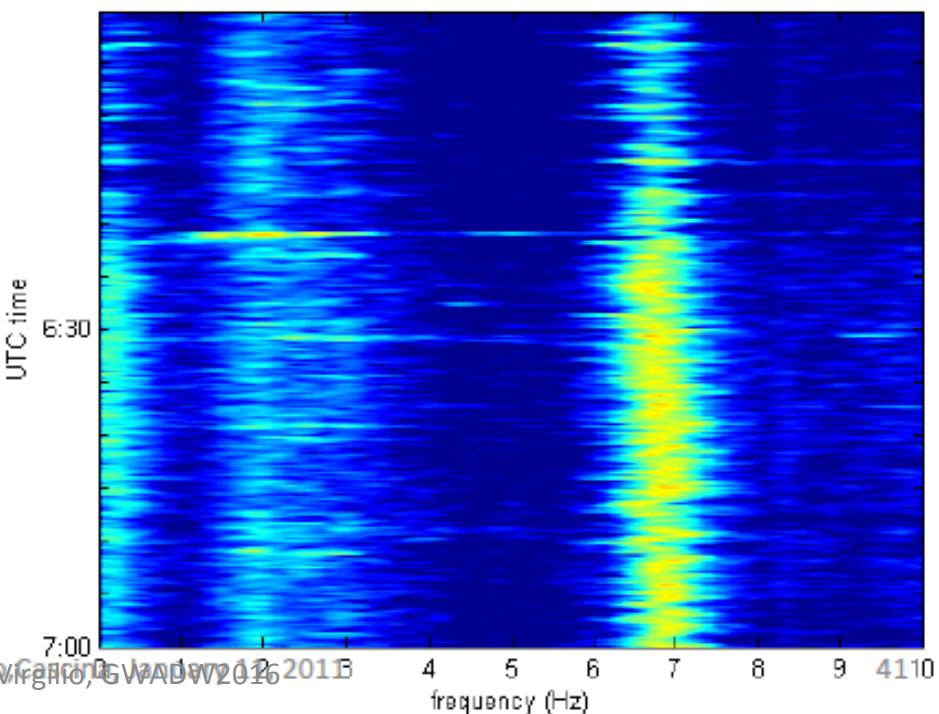


Earthquake Appennini near Modena, DarkFringe  
06:20:32 UTC, September 16 2010



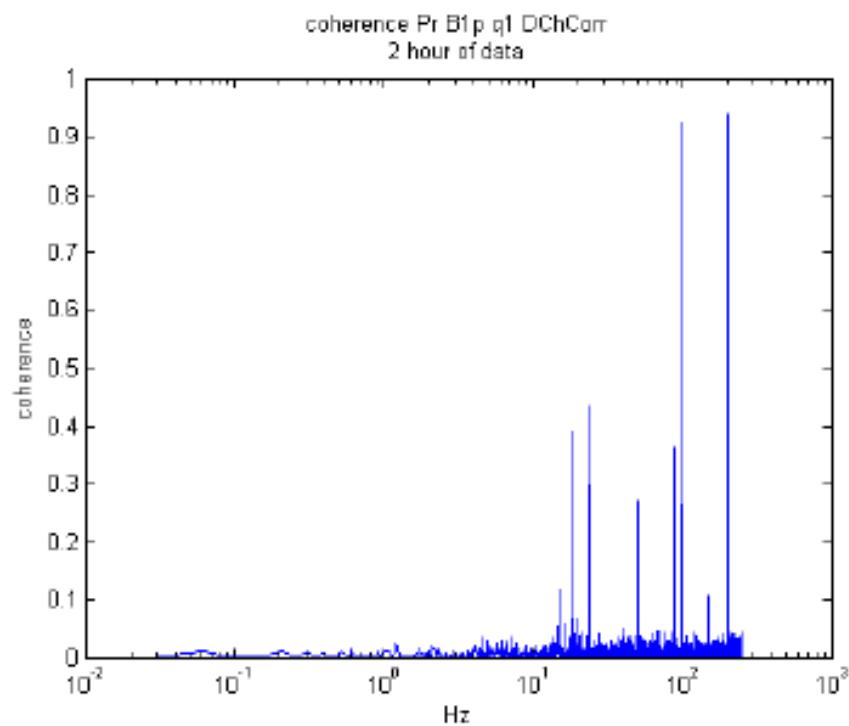
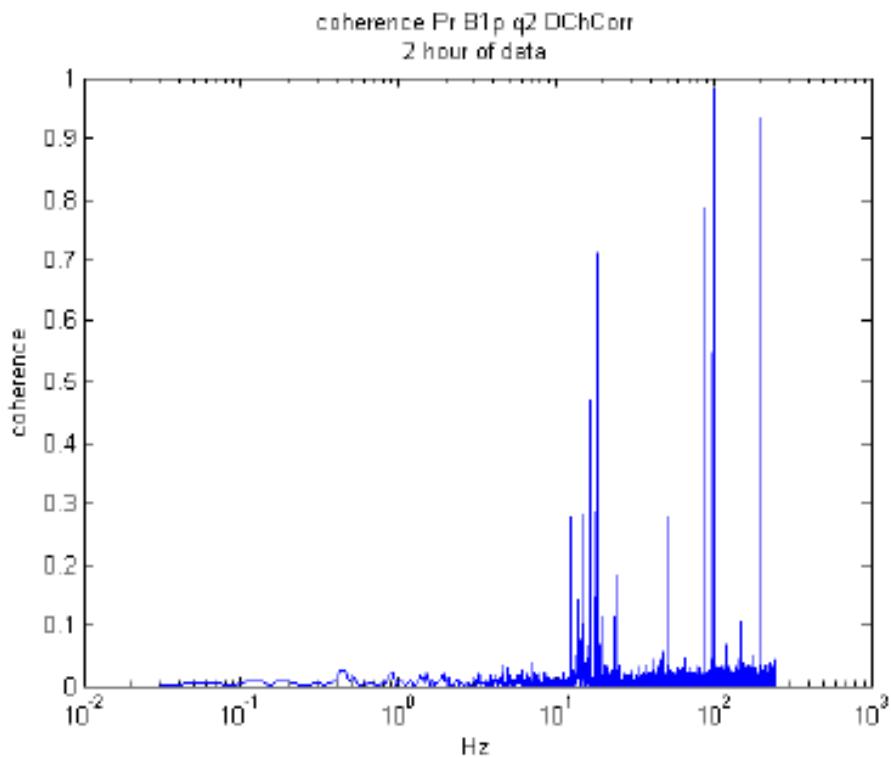
- Virgo was not affected by this
- Shock, no evidence of jitter of the output beam or in the accelerometers
- But the DarkFring has seen it

Earthquake Appennini near Modena, Gyrolaser  
06:20:32 UTC, September 16 2010



More on G-Pisa@VIRGO, 2011

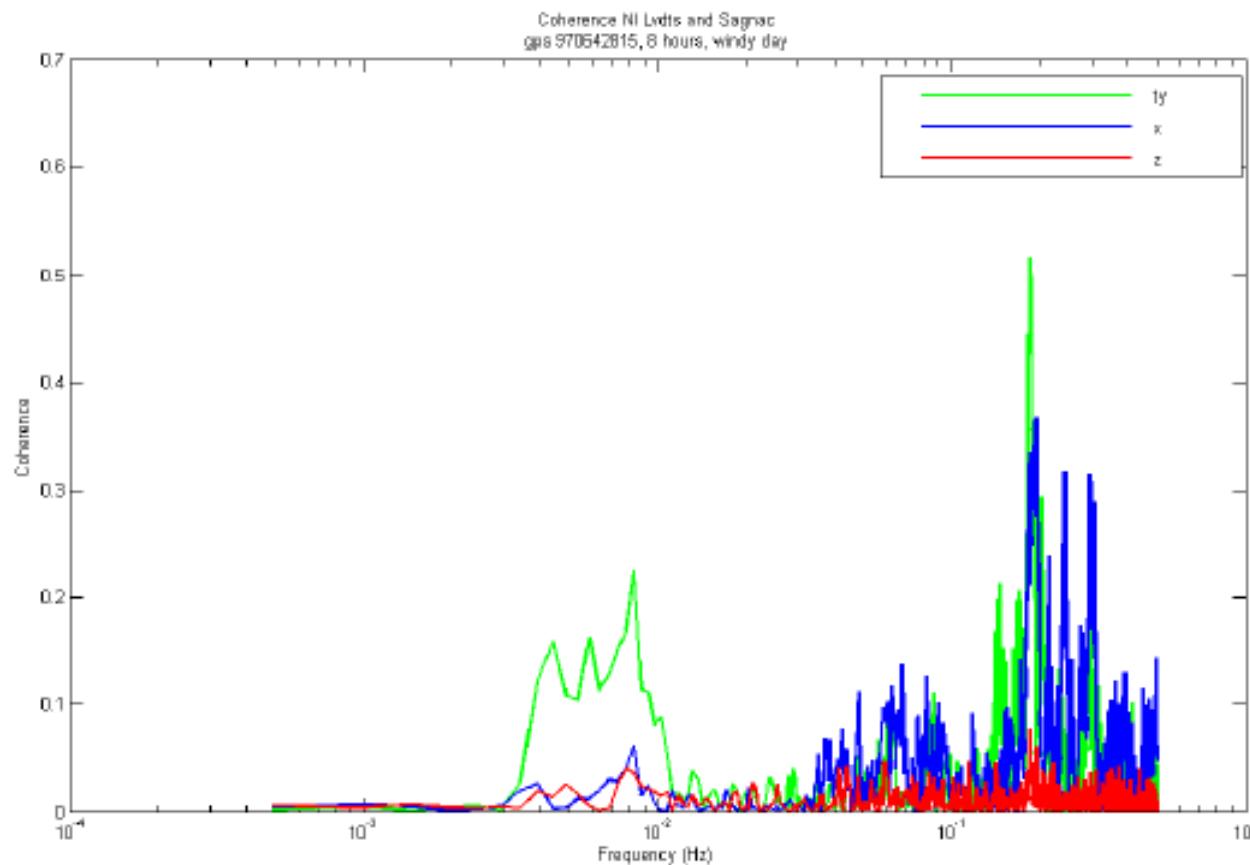
# Coherence with Dark Fringe



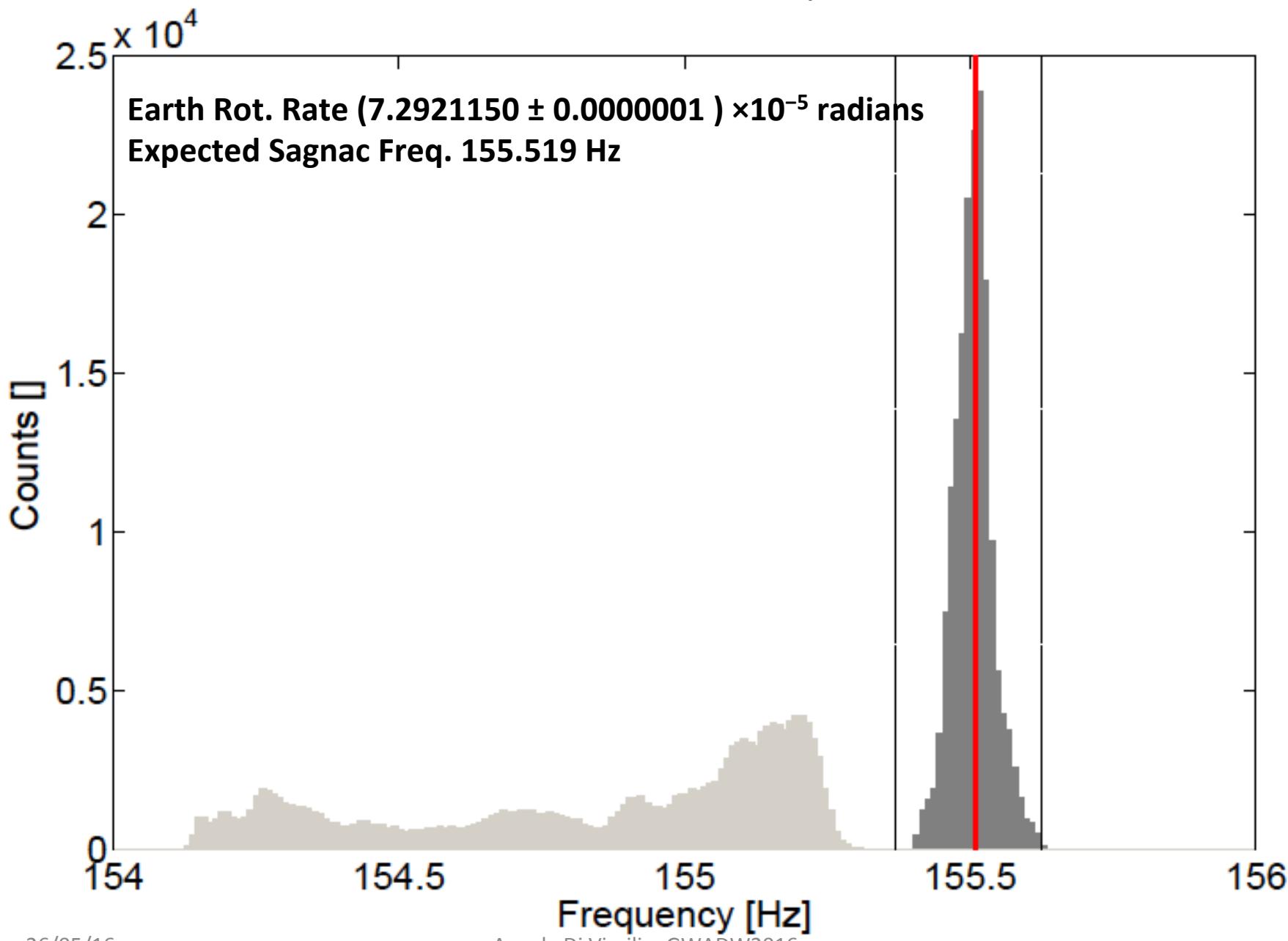
Coherence between our signal and the DarkFringe has not been done extensively, but there is evidence of coherence

G-Pisa bandwidth at the moment is 1kHz

# There is coherence at low frequency between the gyrolaser and LVDT signals



Backscatter noise dominates below 0.1 Hz, it can be subtracted



# Allan Deviation, G-Pisa in a ‘standard laboratory’ 2014 implementable on-line

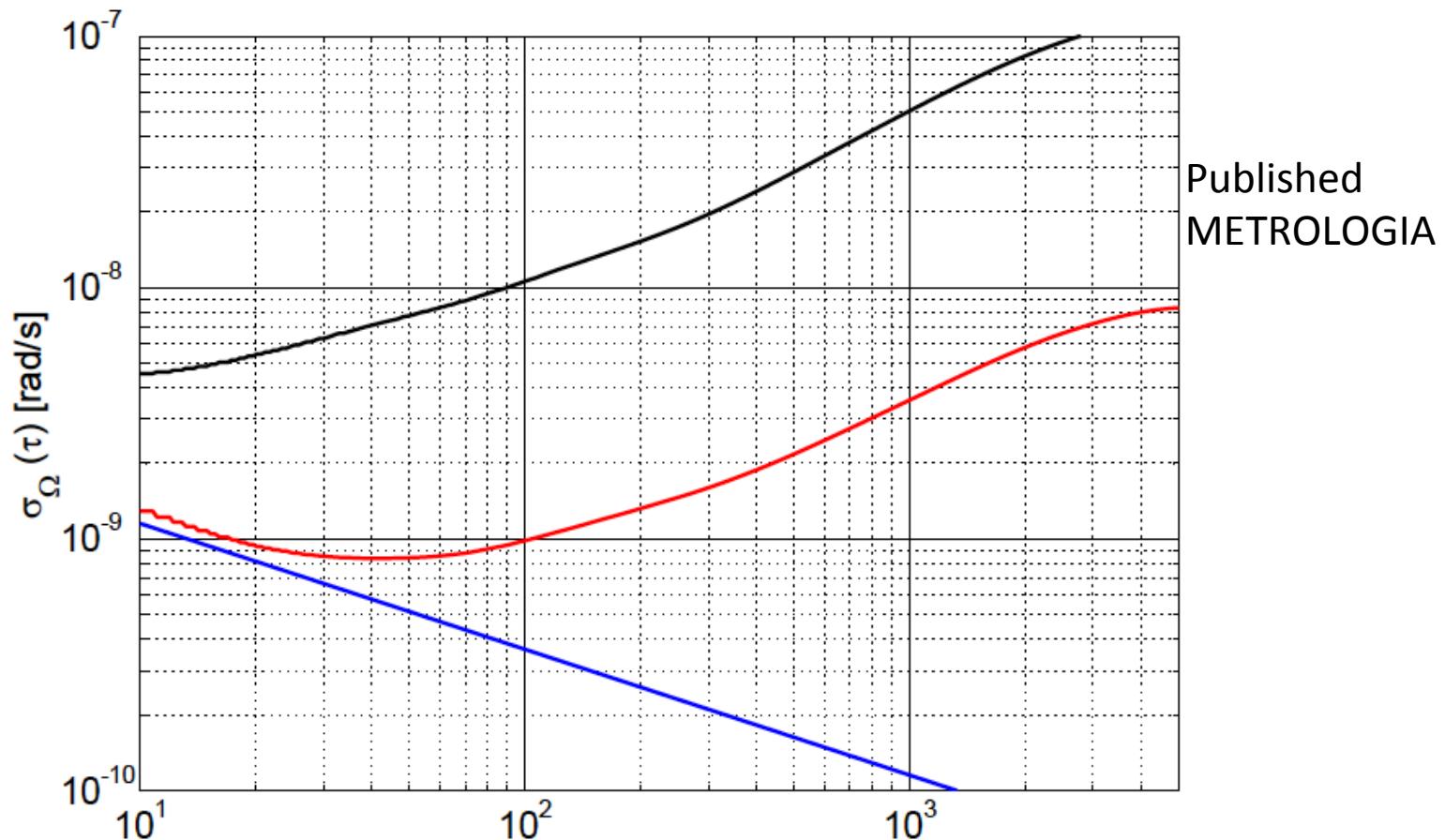
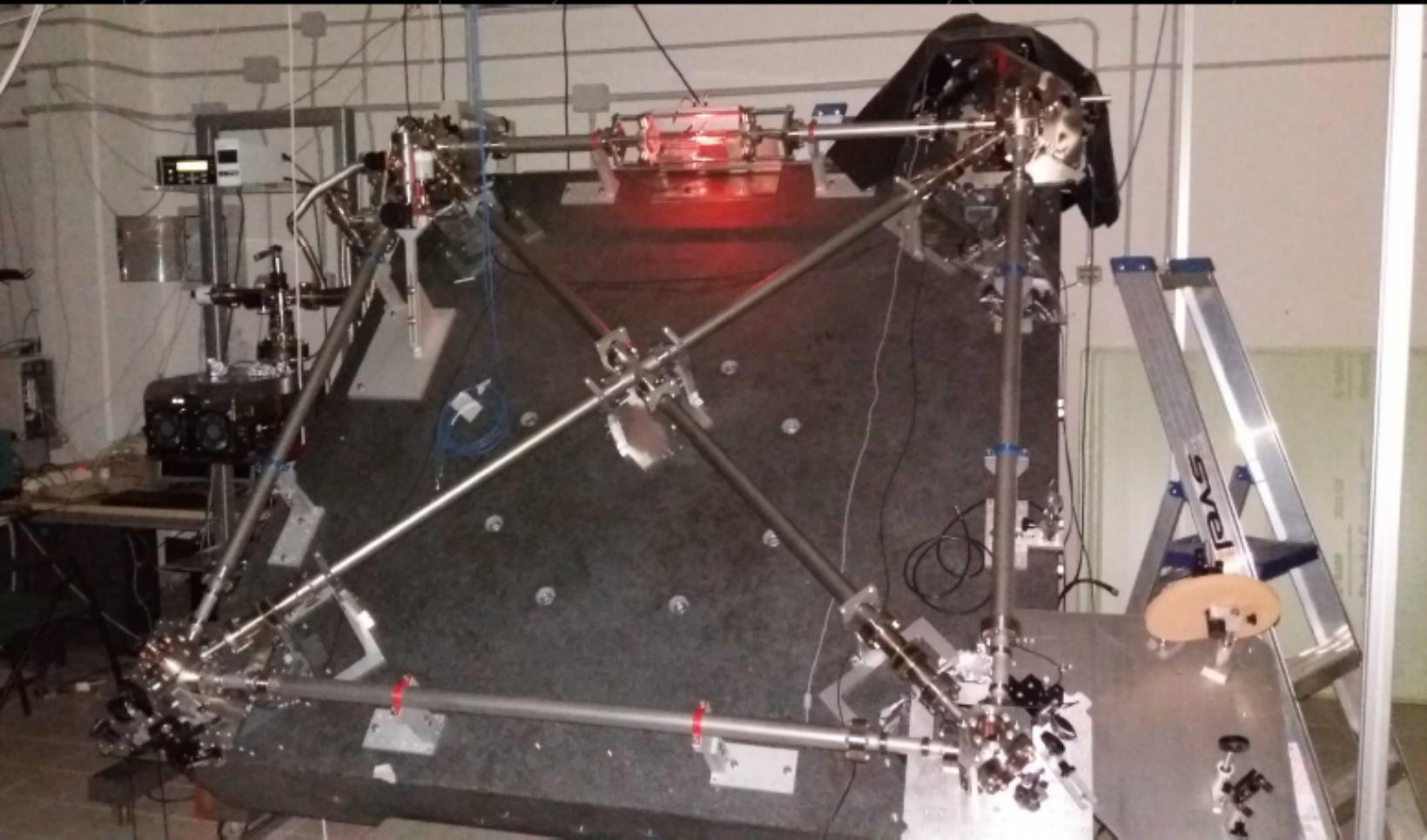


Figure 19: Allan deviations of AR(2) (upper curve) and EKF (lower curve) rotational frequency estimates. The straight line represents the shot noise level of G-PISA for a cavity quality factor of  $5.4 \times 10^{11}$  and an output power of 4 nW.

GP2- 1.6m in side

**GEOMETRY CONTROL STUDY**

necessary for the long term stability



GP2

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INFN-Pisa

# GP2: Geometry control via interferometry



## Problem

The magnitude of the *relativistic frame dragging* term is of 1 part in  $10^9$  of the Earth rotation

- scale factor  $k_s$  stabilization better than  $10^{-10}$ 
  - ▶ accuracy on mirror position better than **1 nm**

## Approach used in the past

Observable: RL optical frequency (cavity perimeter control)

Stabilization methods: comparison with reference laser; by tuning the environmental pressure; by locking to a frequency comb

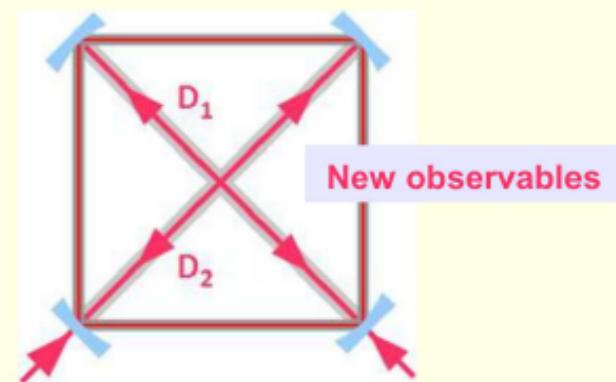
Limitation: variations of mirror inter-distances remain uncontrolled



### Our original approach

Observables: distance between opposite mirrors (& perimeter)

Stabilization methods: lock of diagonal cavities respect to a frequency standard



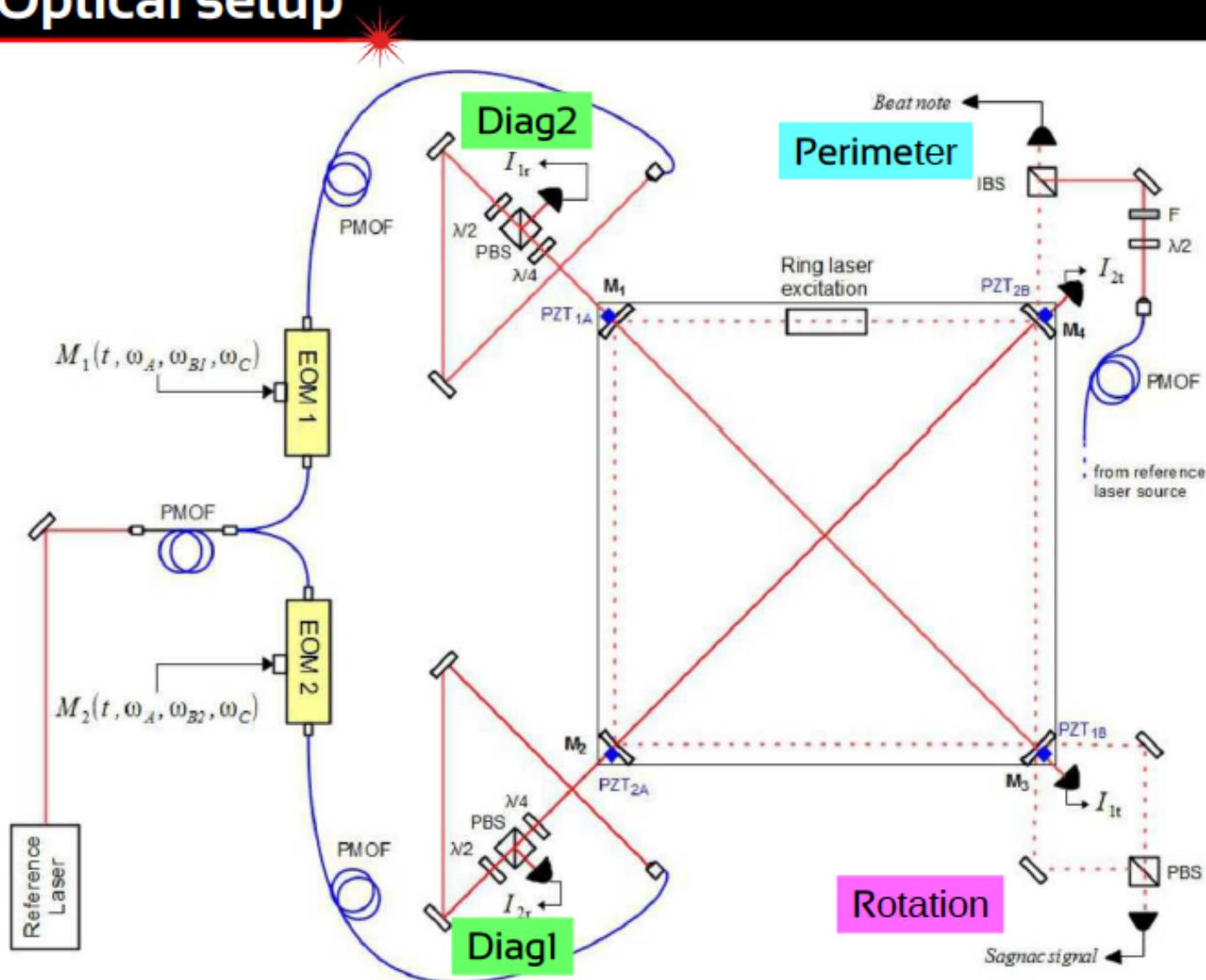
**Interferometric length metrology for the dimensional control of ultra-stable ring laser gyroscopes**, Class. Quantum Grav. 31 (22), 225003, (2014)

26/05/16

Angela Di Virgilio, GWADW2016



# GP2: Optical setup

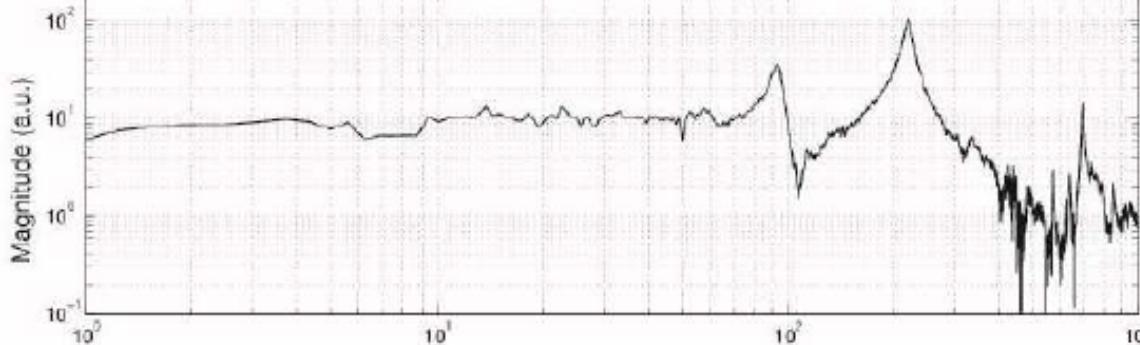
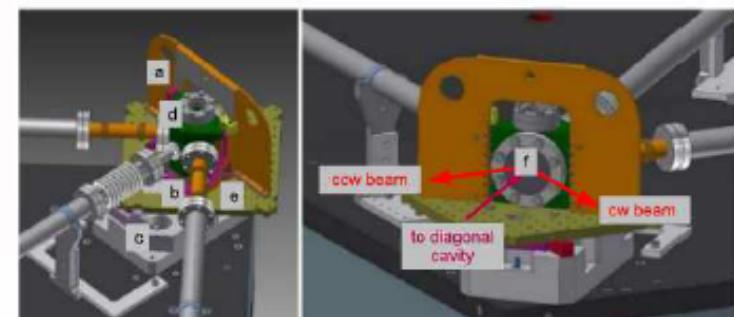
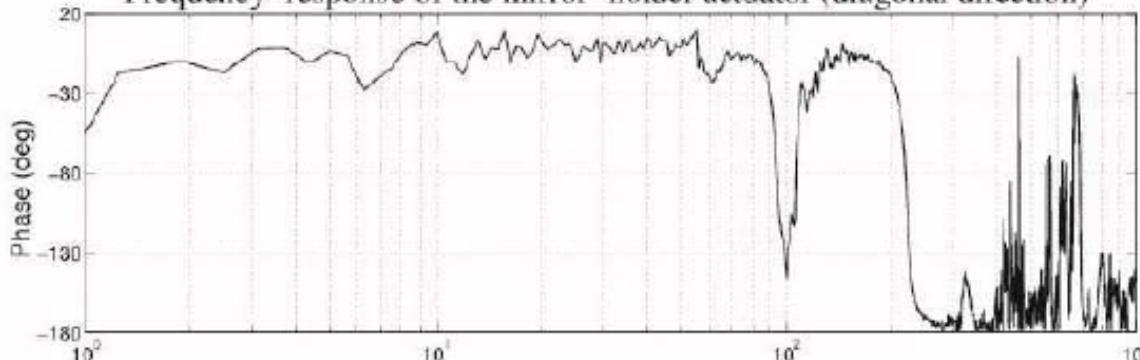


# Mirrors position actuators



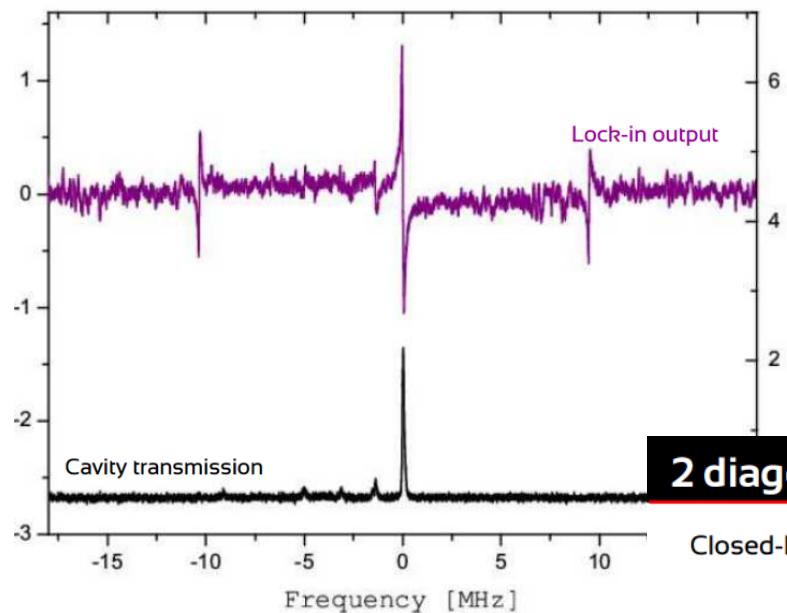
- ▶ #3 1-axial PZT; #1 3-axial PZT
- ▶ dynamic range (measured):  $80 \mu\text{m}$
- ▶ control bandwidth (measured): few tens of Hz

Frequency-response of the mirror-holder actuator (diagonal direction)



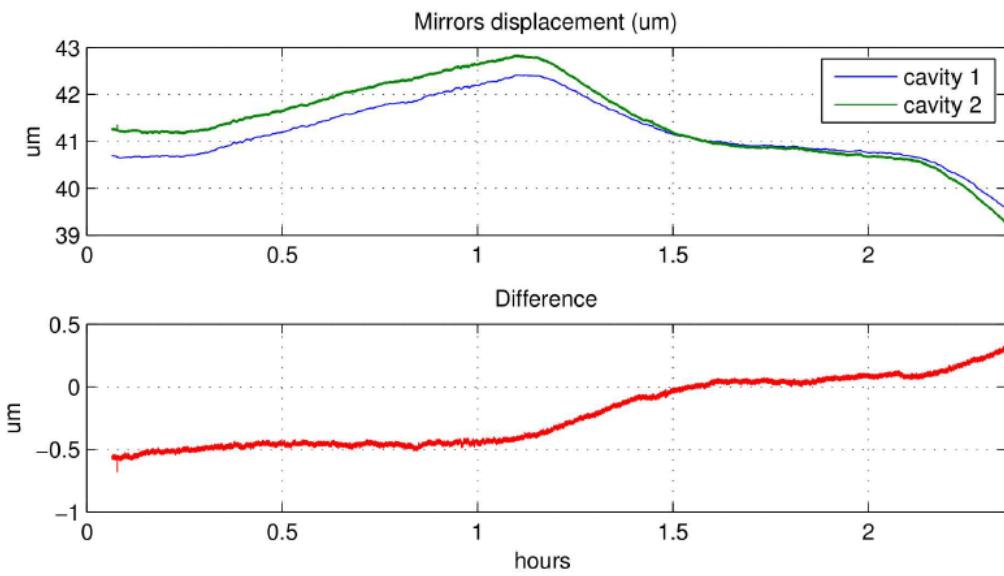
# Carrier error signal on GP2

Digital lock-in amplifier

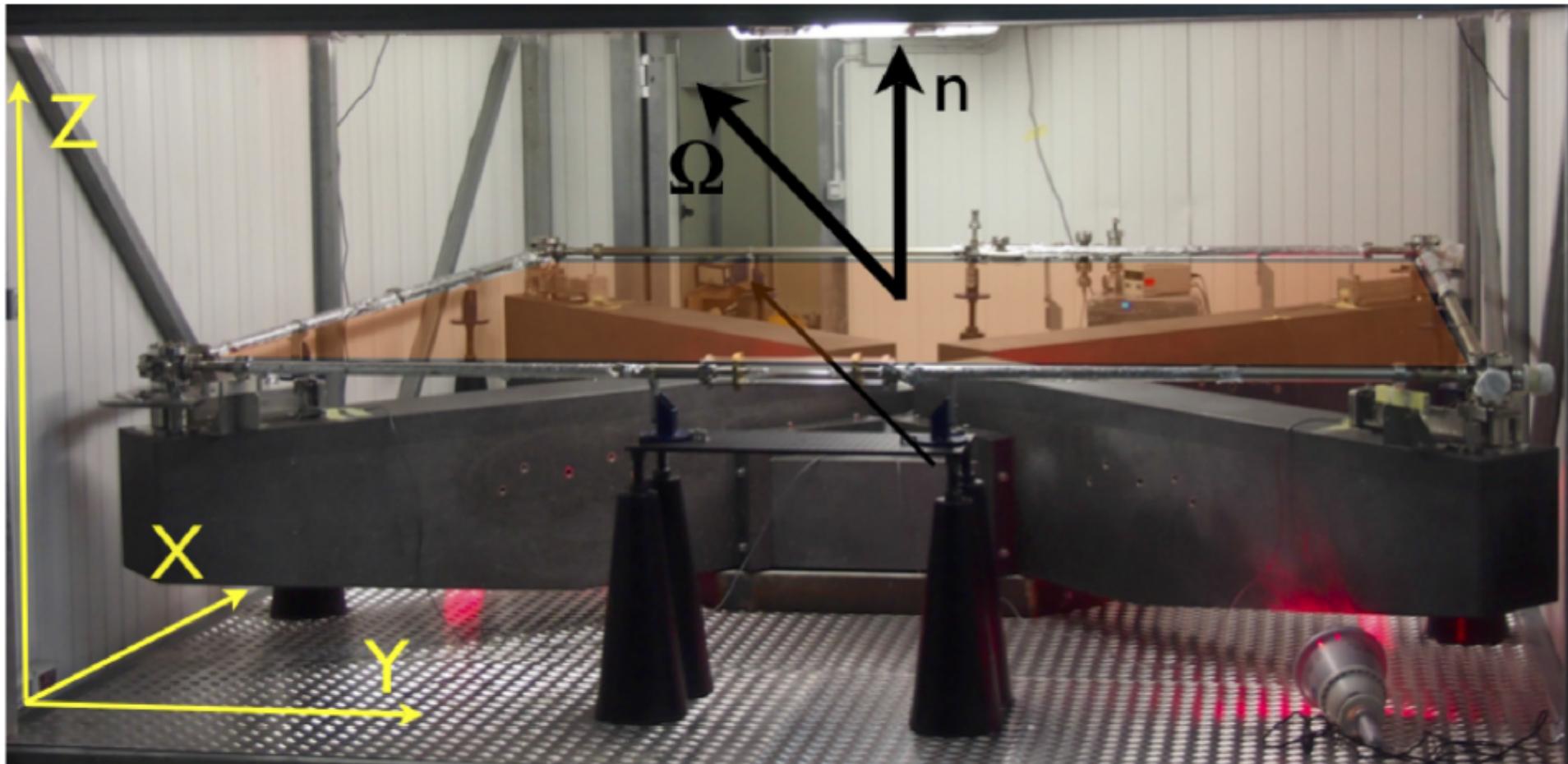


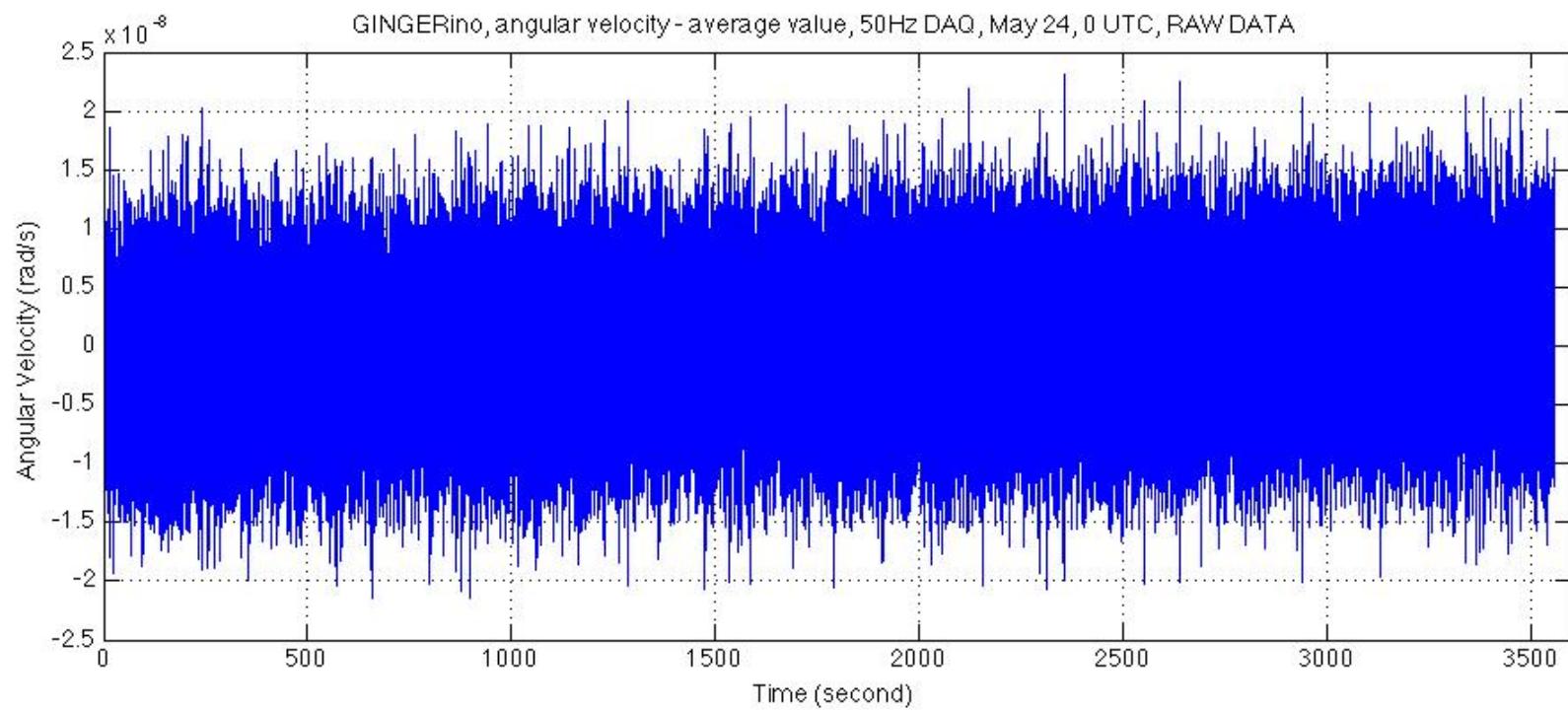
## 2 diagonals stabilization

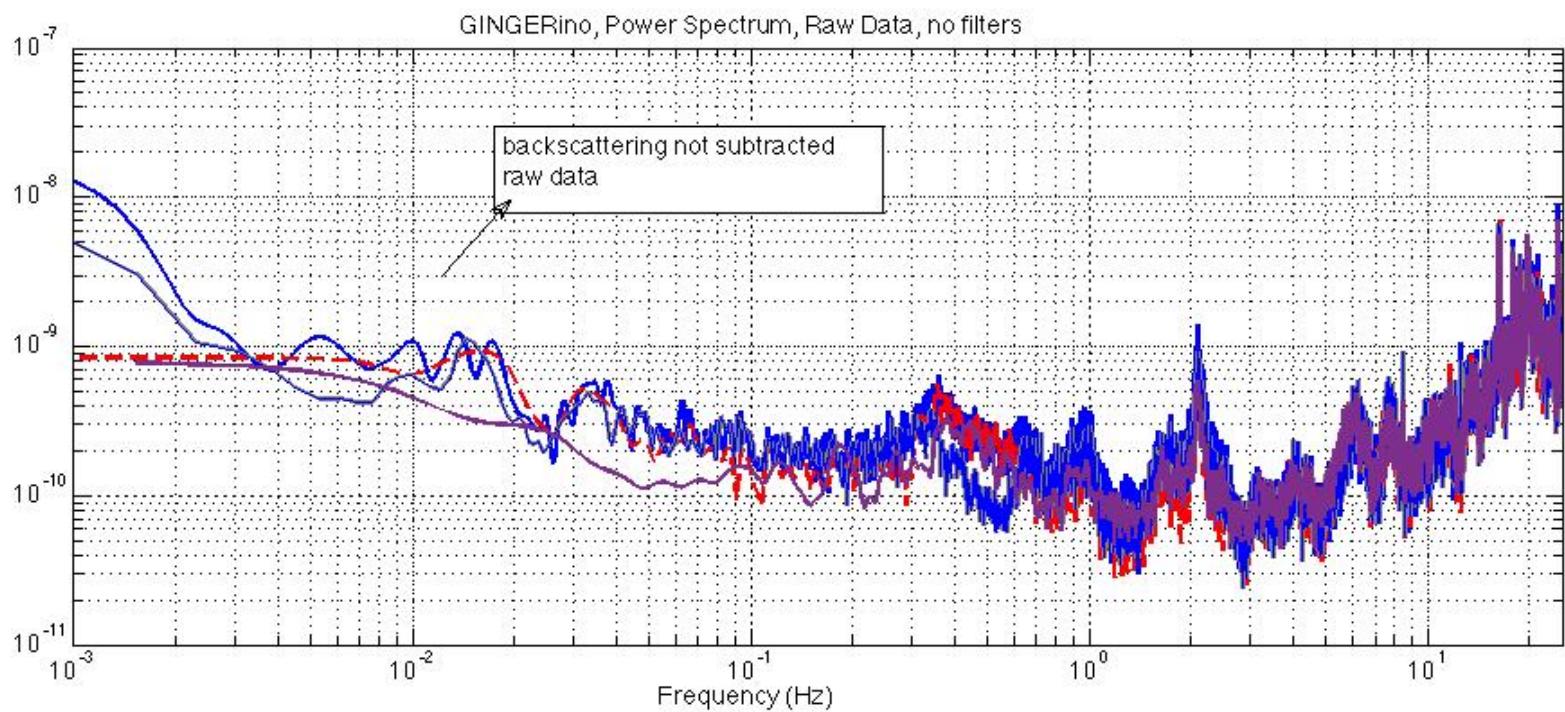
Closed-loop correction to the opposite mirrors (digital PI controller )



# GINGERino, the ring laser inside LNGS, 3.6m in side







# G-LAS, Gyro-Laser Angle Standard under assembling, 0.5 m in side



Fig. 1. Picture of the carbon fibre board mounted on the turntable. Three corner tower and two sides of the ring vacuum chamber has been already fixed on the board .

**Transportable Goniometer for metrology**  
**INRIM/INFN**  
**Accuracy  $5 \cdot 10^{-9}$  rad**

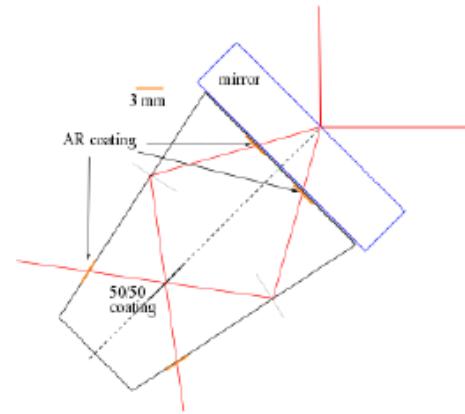
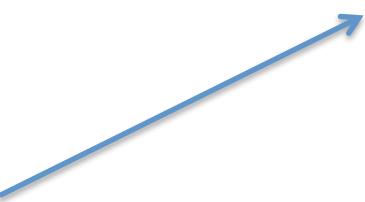


Fig. 3. The combining prism (Koester prism). It consists in two symmetric quartz prism glued together. On the contact region of the two prisms a semitransparent 50/50 coating allows beams combining

# Two papers with the analysis of tele-seismic events: both Love and Rayleigh waves

## References

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- 
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  - [2] A. Simonelli et al. "First deep underground observation of rotational signals from an earthquake at teleseismic distance using a large ring laser gyroscope". In: *Annals of Geophysics* 59 (2016), Fast Track 4. DOI: 10.4401/ag-6970.
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  - [11] F. Bosi et al. "Measuring gravitomagnetic effects by a multi-ring-laser gyroscope". In: *Physical Review D* 84.12 (2011). DOI: 10.1103/PhysRevD.84.122002.
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  - [13] A. Di Virgilio et al. "A LASER GYROSCOPE SYSTEM TO DETECT THE GRAVITO-MAGNETIC EFFECT ON EARTH". In: *International Journal of Modern Physics D* 19.14 (2010), pp. 2331–2343. DOI: 10.1142/s0218271810018360.
  - [14] Angela Di Virgilio et al. "Performances of 'G-Pisa': a middle size gyrolaser". In: *Classical and Quantum Gravity* 27.8 (2010). DOI: 10.1088/0264-9381/27/8/084033.

# Summary

- Ringlaser with ~ 1m in side are robust, bandwidth ~ 1kHz
- Triangular rings feasible
- the independent components of the angular rotation vector can be measured changing the orientation of the ring (ROMY 4 rings array in construction in Baviera, ERC Heiner Igel)
- They are suitable for ‘observatory’, they run unattended
- Sensitivity depends on mirror and size, easily better than  $10^{-9}$  rad/s/sqrt(Hz)