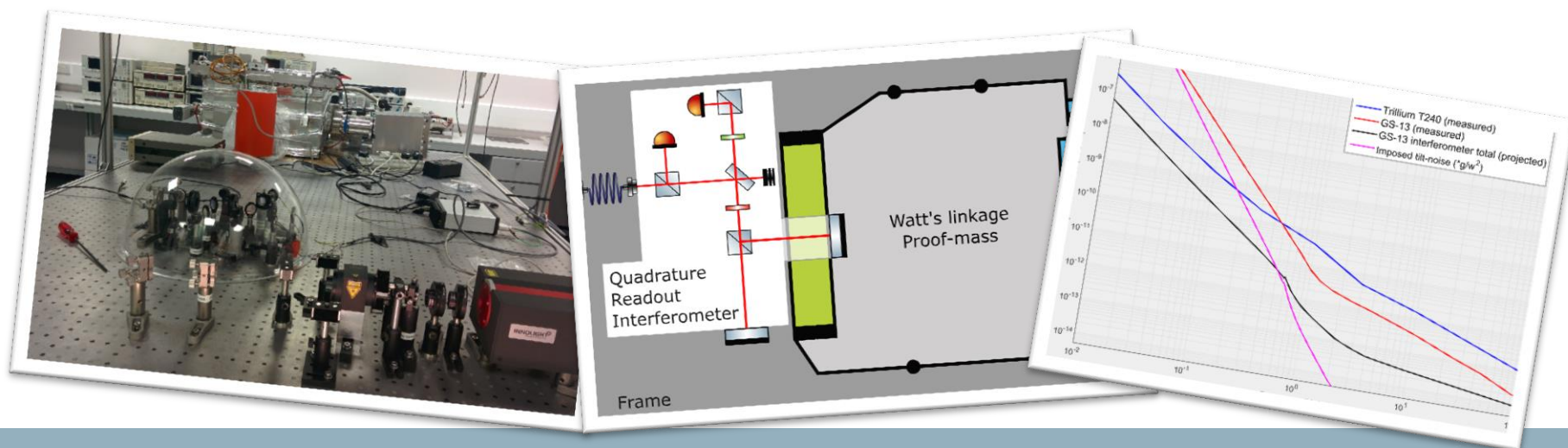


# Low-frequency Sensors, 10mHz to 10Hz

A quick summary of some current projects and design considerations

**Conor Mow-Lowry**

Including substantial work by **Sam Cooper**



# Motivation

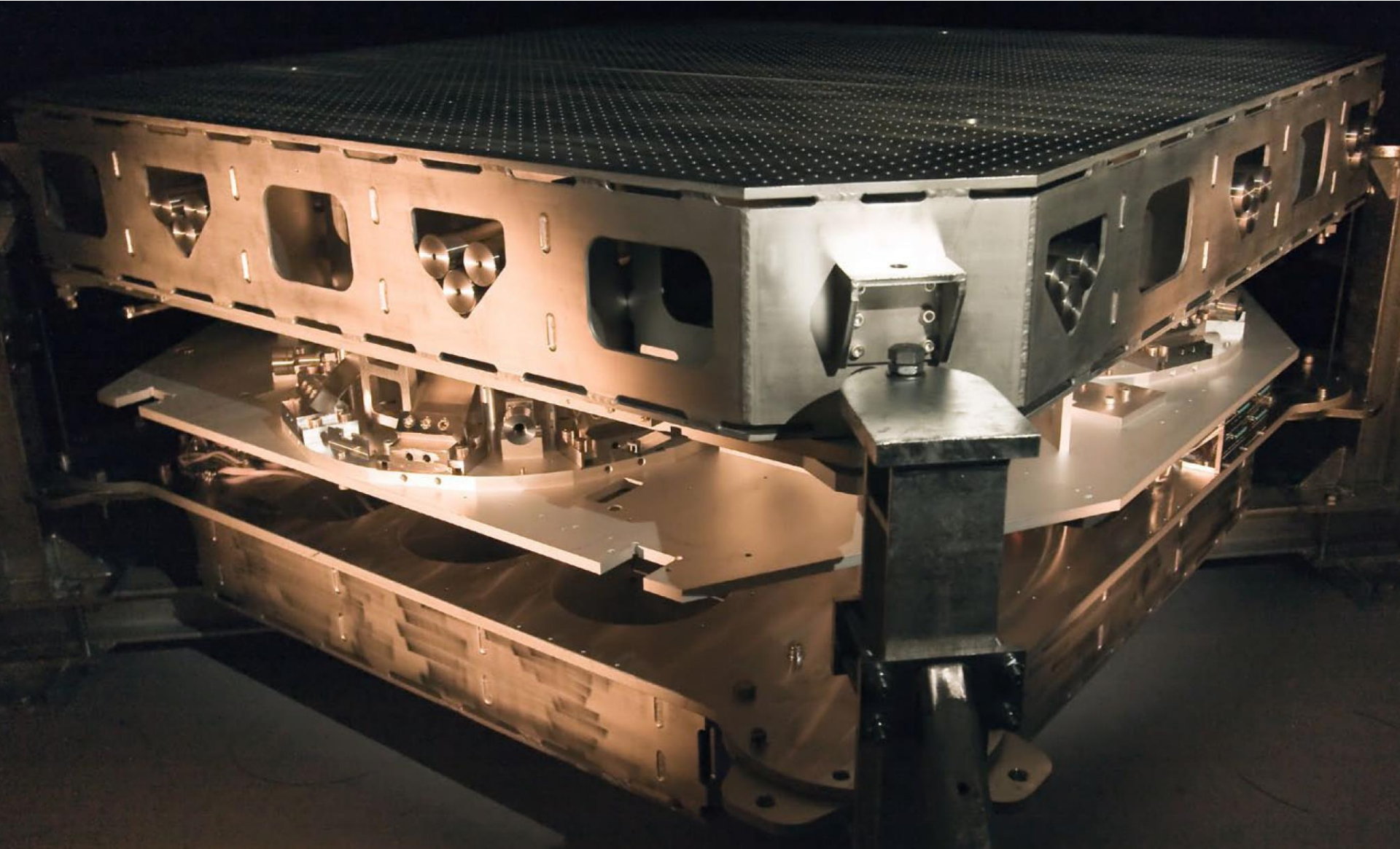
Inertial sensors: Lock acquisition and duty cycle.

Position sensors: Improved suspension damping, reduced 10Hz+ noise injection, simpler global controls.

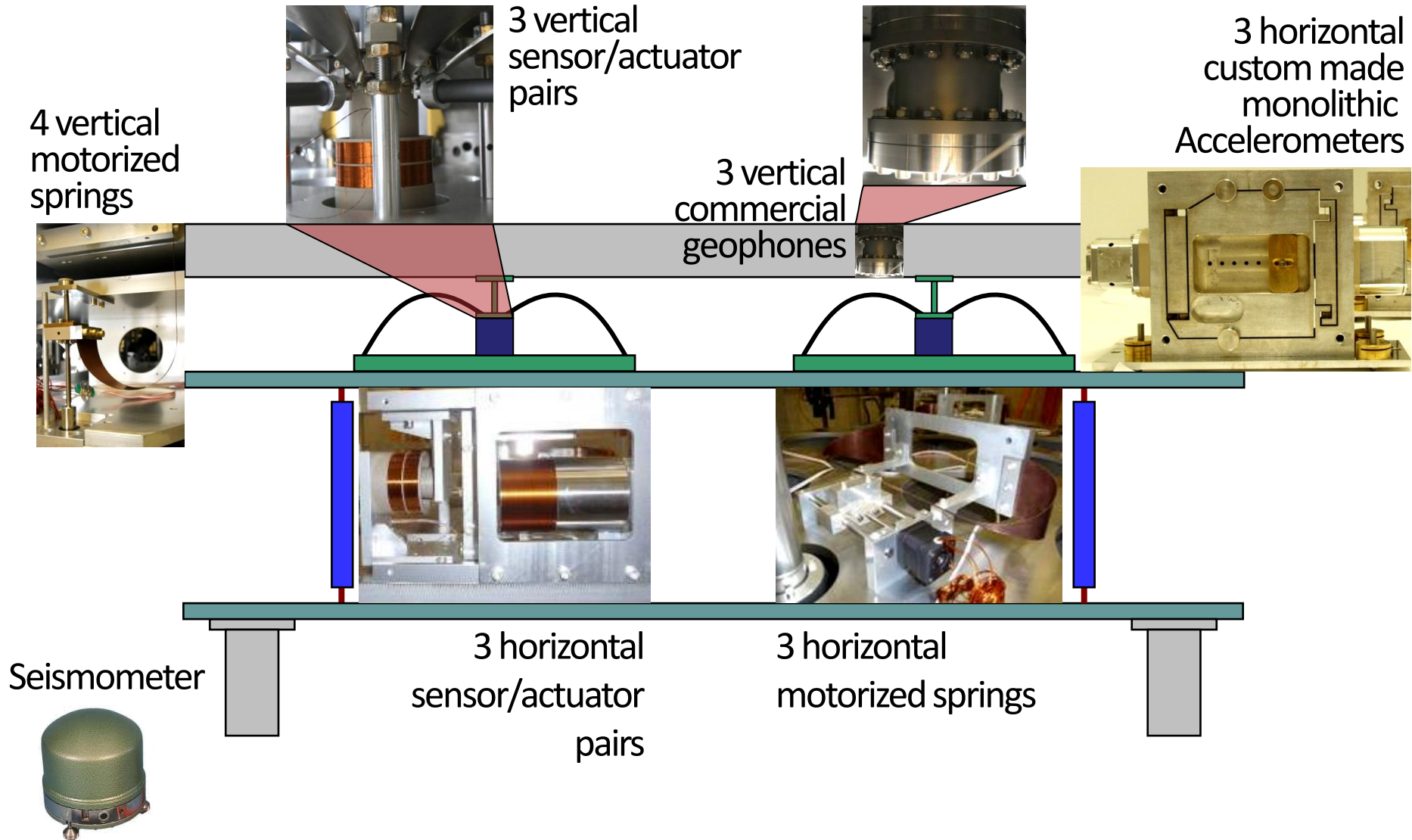
Low-frequency GW experiments such as TOBAs or Atom interferometers need (way) more low-f isolation.

Geophysics? Space-based accelerometers?

# My personal inspiration



# Sensor blending with noisy sensors



A. Wanner *et al.*, Class. Quantum Grav. **29**, 245007 (2012)



# Design considerations with inertial sensors

- ‘Ideal’ sensors are limited by suspension thermal noise: roughly white in force noise ( $1/f^{2\text{-ish}}$  in inertial-equivalent displacement). More bending material = more noise.
- $g$  is large. Vertical sensors need to be strong, which needs lots of material. Hard to get low resonant frequencies.
- White readout noise becomes  $1/f^2$  below resonance.
- Horizontal sensors couple tilt like  $g/w^2$ , but low-loss anti-springs make good low- $f$  sensors.

# DoF design considerations

DoF	Type	$f_0$ (Hz)	Design considerations
Z	Mass-spring	$\sim 1$	Thermal noise, low-f readout noise ( $1/f^2$ ), very low cross-coupling
Z	Anti-Spring	$\sim 0.2$	Huge thermal noise
X,Y	Pendulum	1	Readout noise ( $1/f^2$ ), tilt-coupling ( $1/f^2$ )
X,Y	Watt's linkage	$\sim 0.1$	Tilt-coupling ( $1/f^2$ ), low thermal noise
RX,RY	Differential-Z	$\sim 1$	Small signal, large common mode, huge low-f readout noise (effectively $1/f^4$ )
RX,RY	BRS	$\sim 0.01$	Small signal, Mechanical tuning and drift/control, low-f readout (effectively $1/f^2$ )
RZ	Torsion balance	$\sim 0.001$	Tiny signal, large RMS rotation
RZ	Differential-X,Y	$\sim 0.1$	Tiny signal, tilt-rejection

# Some randomly sampled work in the LSC

Tilt-coupling is seeing quite some attention,

Tilt-free seismometry (Dooley)

BRS for tilt-correction (Venkateswara)

Differential-Z for closed-loop (Mow-Lowry)

Interferometric readout

Watt's linkage with Michelson (van Heijningen)

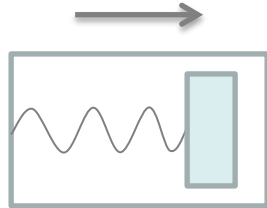
EUCLID-type readout (Mow-Lowry)

Thermal noise via exotic springs (not discussed here)

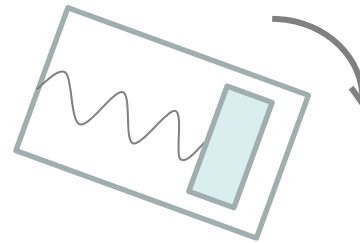
Most remaining slides are courtesy of Kate, Krishna, and Joris.

# Tilt versus Horizontal displacement

- Conventional seismometers and tiltmeters cannot differentiate between horizontal displacement and ground tilt.



$$\delta x \propto a_x$$



$$\delta x \propto g\theta$$

Tilt response to horizontal displacement response for all seismometers =  $-g/\omega^2$

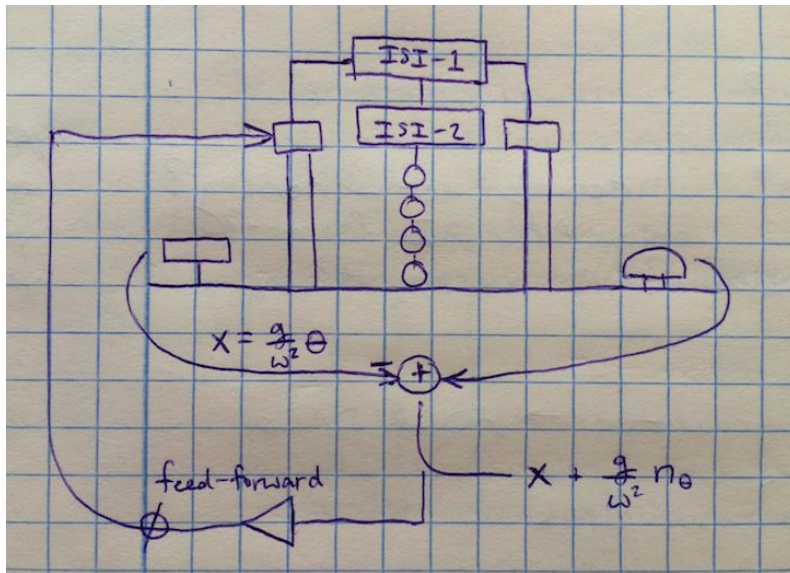
$\Rightarrow$  Tilt is confused with horizontal motion at low frequencies (below  $\sim 0.1$  Hz).

Solution: Inertial rotation sensors, Tilt-free seismometers or ring-laser gyroscopes...



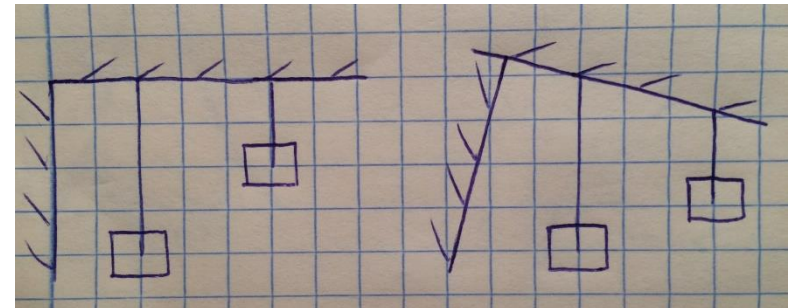
# Two different approaches

## Measuring tilt



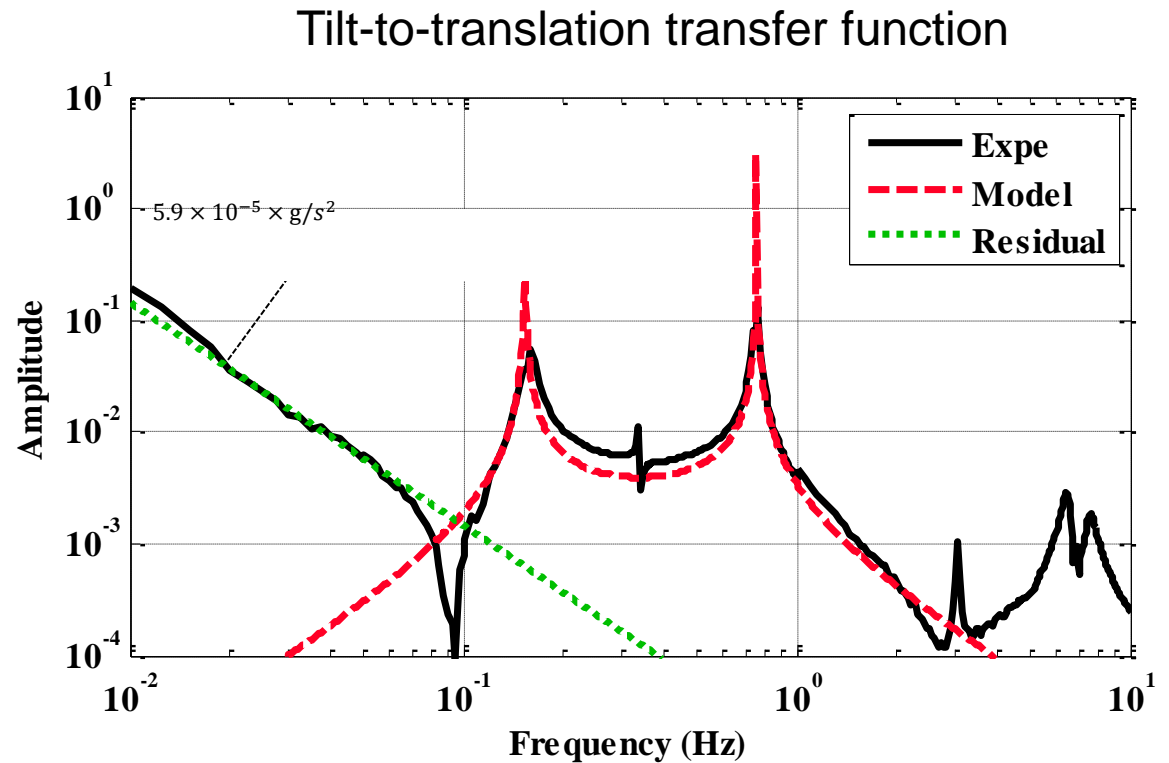
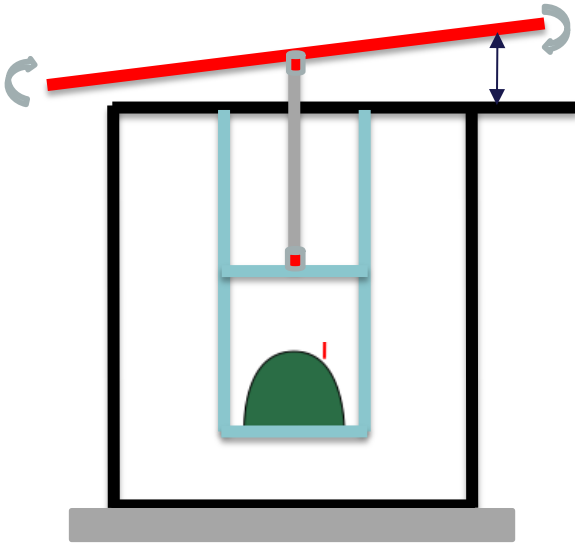
Independently measure ground tilt  
and subtract it.

## Filtering tilt



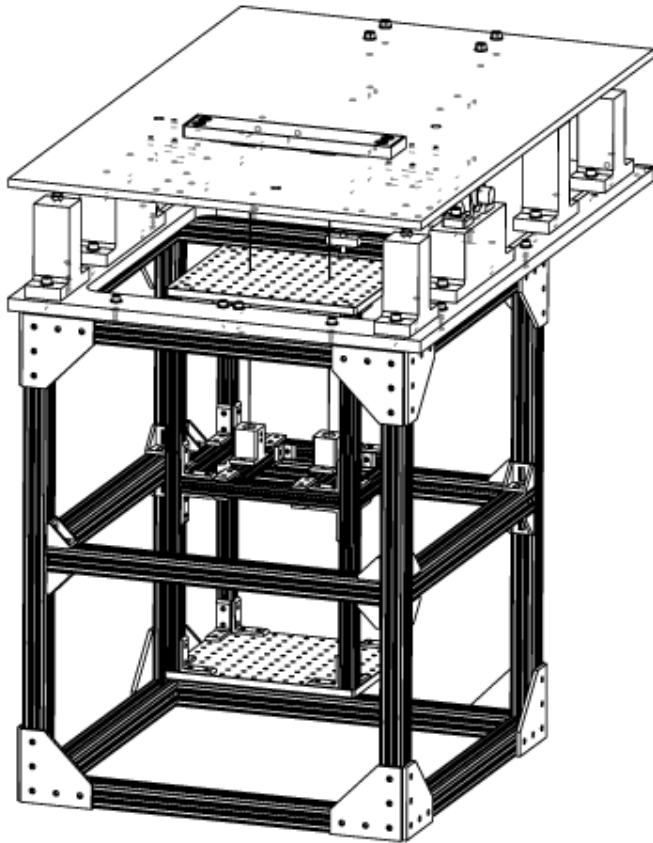
Mechanically filter tilt from reaching the seismometer in the first place

# Example results: tilt-filtering demonstration



Matichard et al. P1400061

# Outlook and message

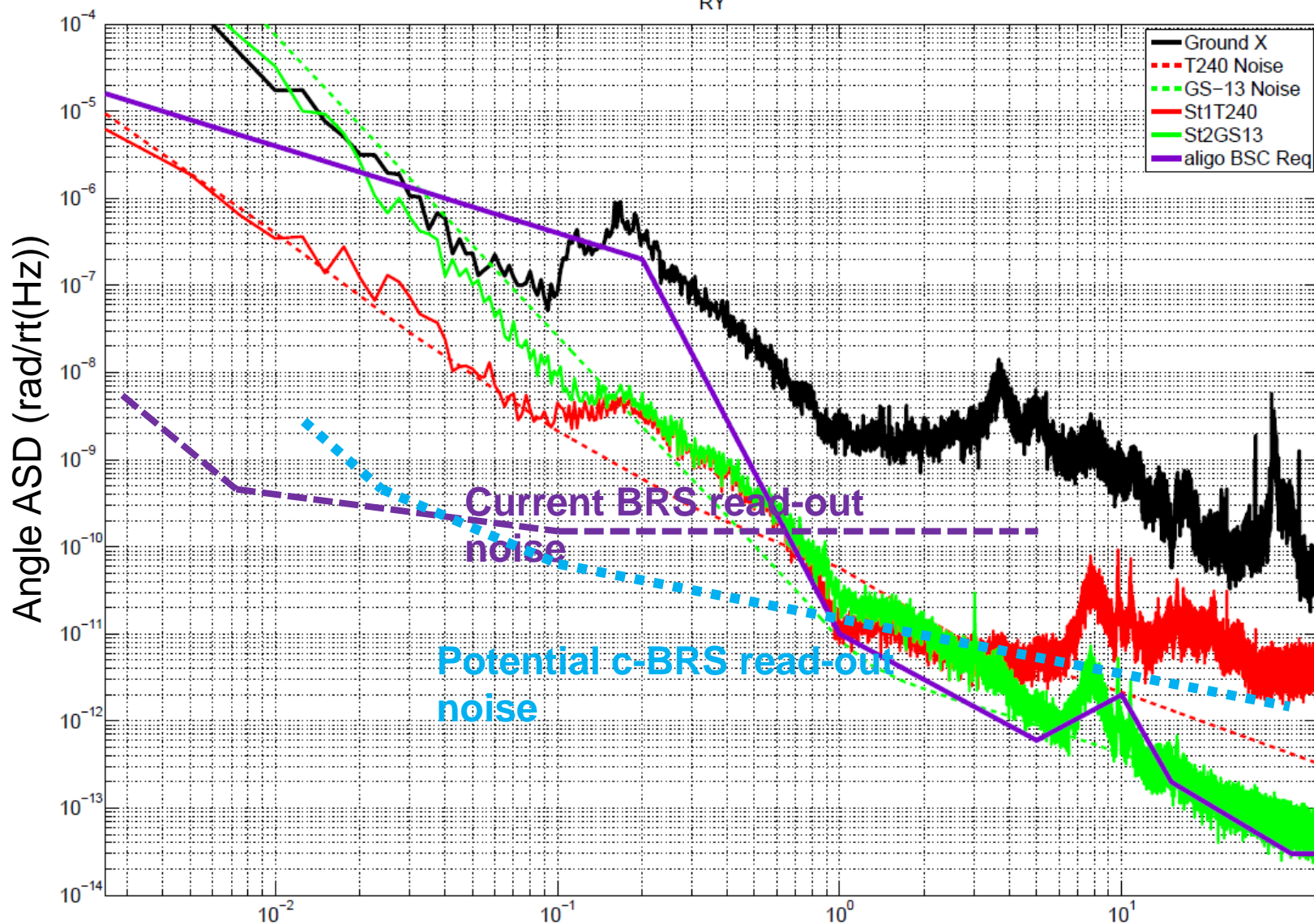


- Build prototype suspension and measure transfer functions using commercial seismometer
- Conduct huddle test
- Build and test custom seismometer (inverted pendulum with Michelson readout)

# Sensitivity comparison

Source: Krishna Venkateswara

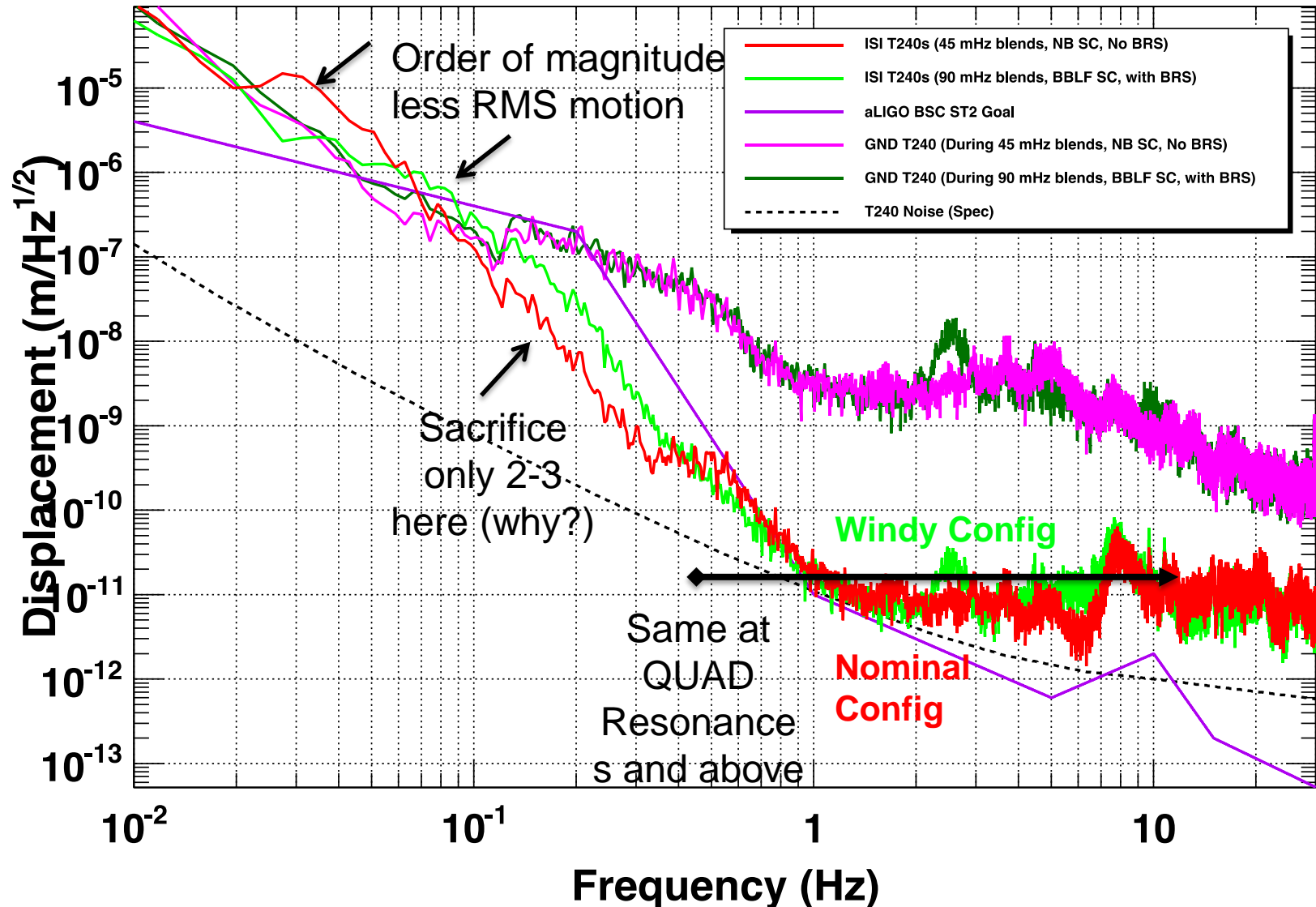
Final Performance, ETMX  
RY



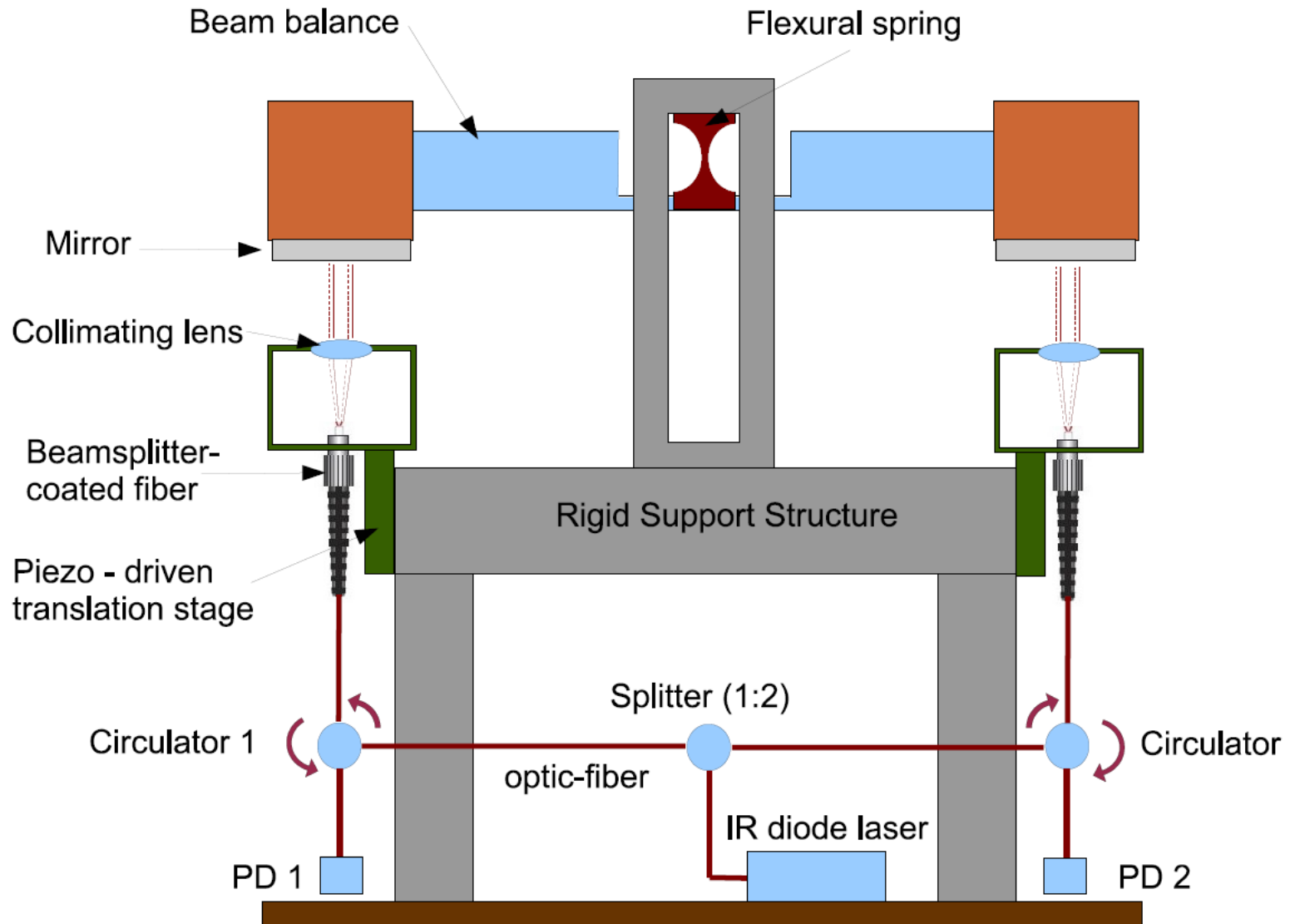
Extra Source: J. Warner, LHO 17197

# Improving ISI performance with BRS

([LHO aLOG 17729](#))

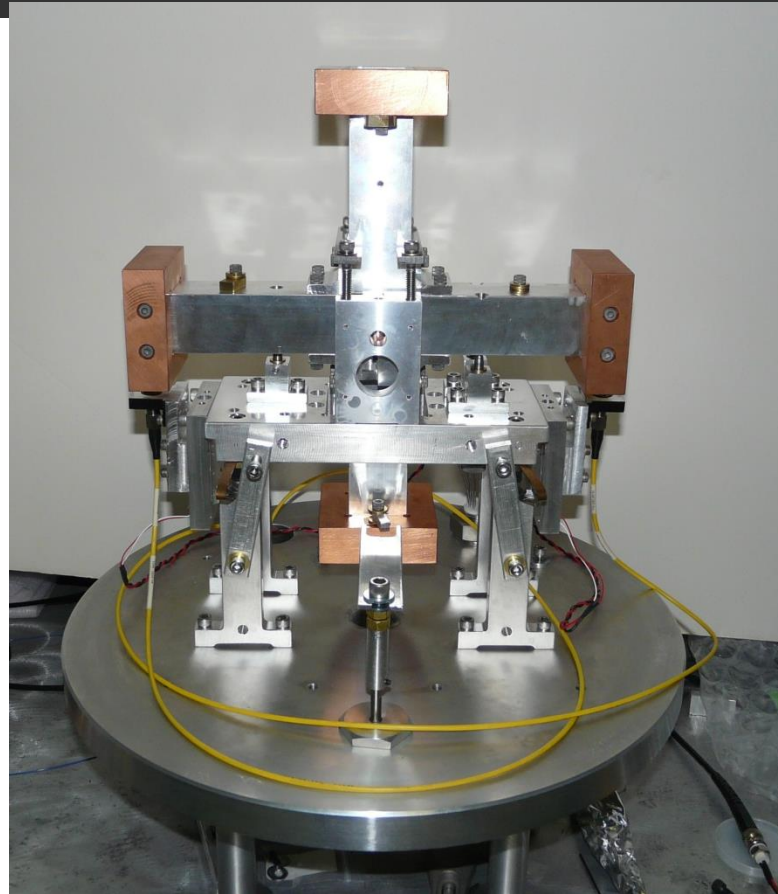
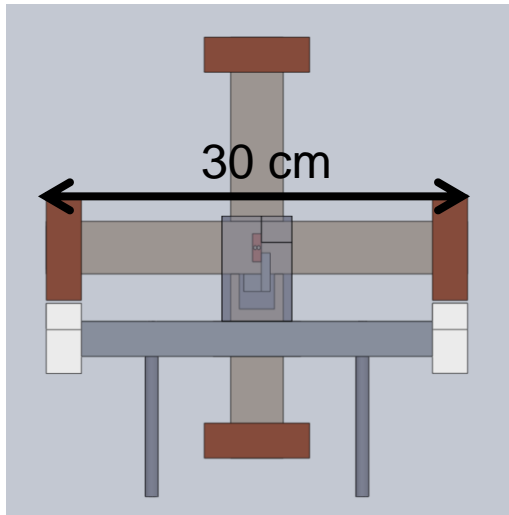


# Schematic





# Compact-BRS



## New features

1. Cross Shape ( $\sim 0$  quadrupole moment) ensures first order insensitivity to gravity gradient noise.
2. New compact interferometric readout with  $\sim 10X$  better sensitivity.
3. Kinematic seat for transportation/repositioning (?)

# Inertial Sensors with Interferometers

Non-contact, low-noise readout

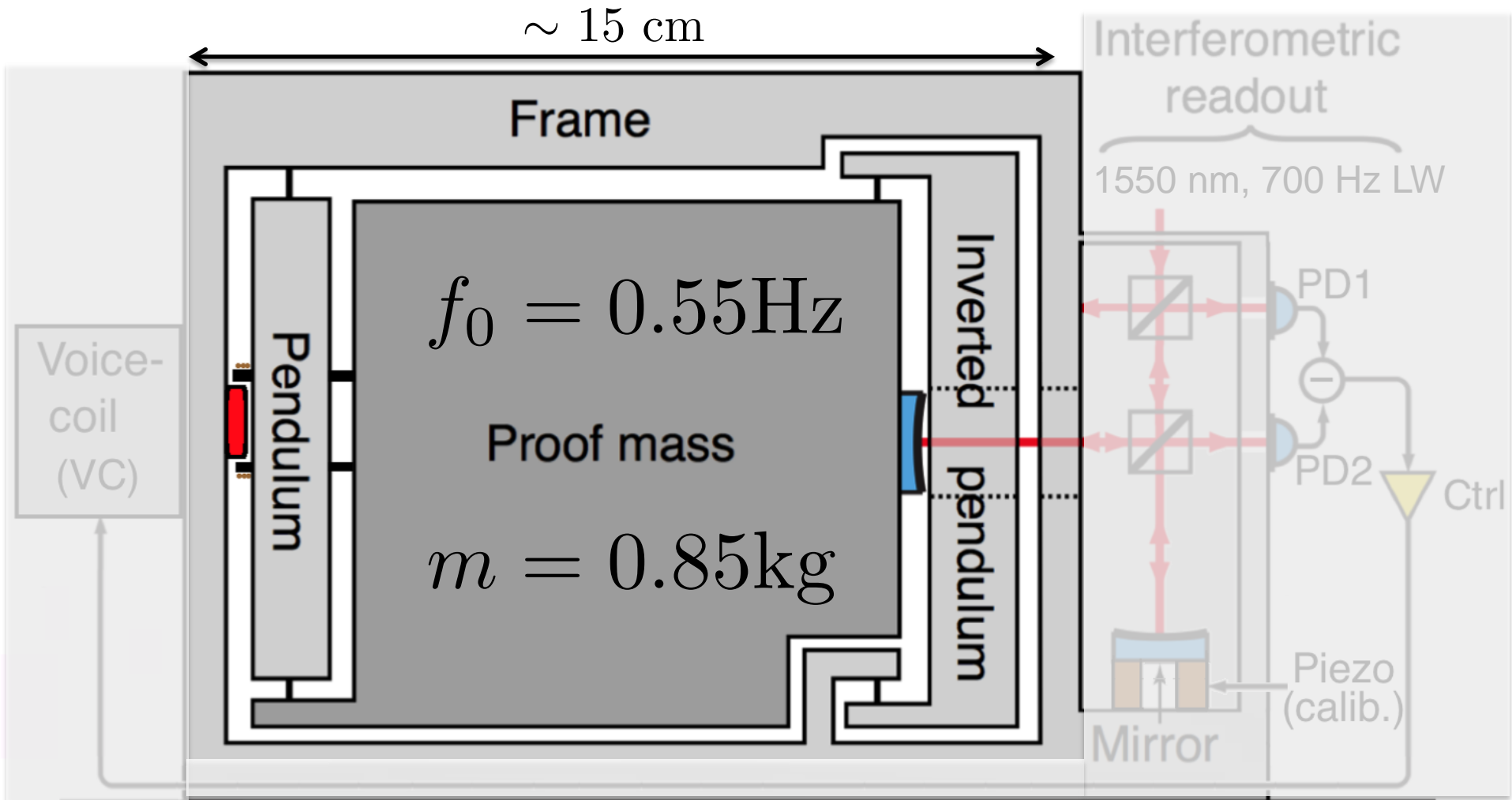
Michelson or Fabry-Perot

- Extreme sensitivity
- Small dynamic range (closed loop required)
- Lots of experience in the field

Homodyne phasemeters (e.g. EUCLID)

- Huge dynamic range (~cm range, ~cm/second speed)
- (Potentially) High sensitivity ( $10^{-14}\text{m}/\sqrt{\text{Hz}}$ )
- No actuators required (magnets, wires, cables)
- Excellent calibration (fixed to the optical wavelength)

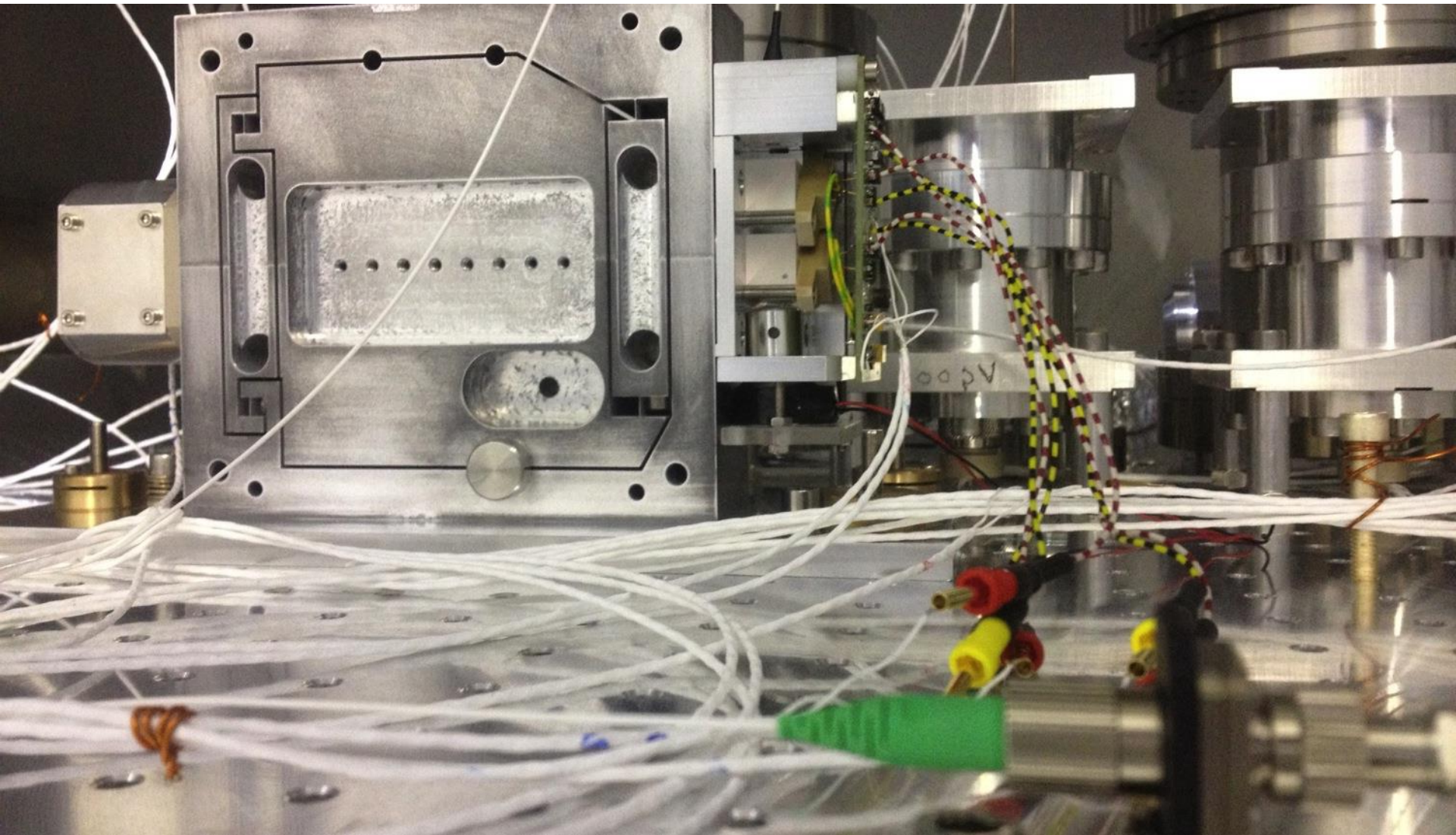
# Nikhef interferometric Watt's linkage



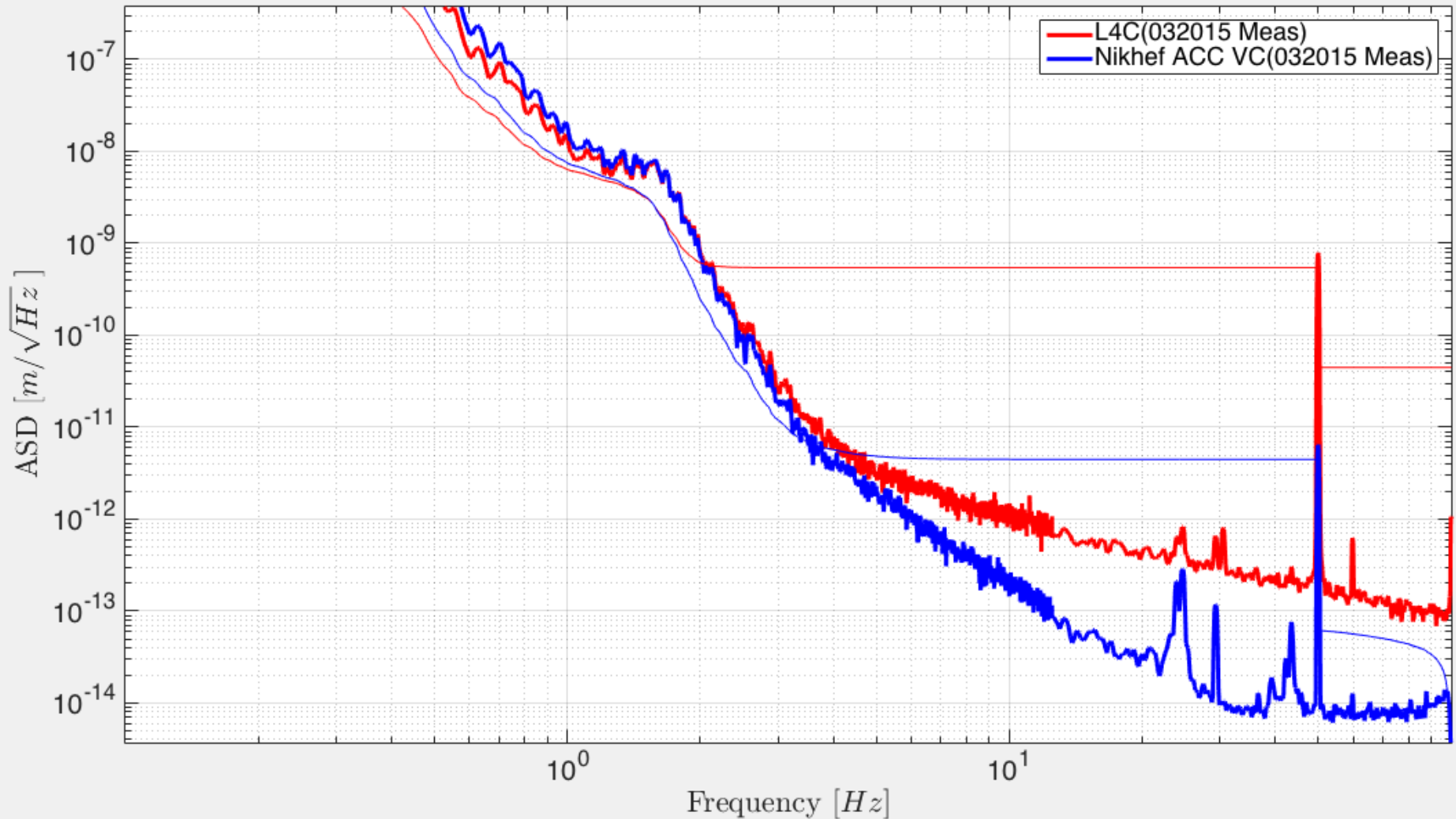
A. Bertolini et al., NIM A, 556, pp 616-623 (2006)

M.B. Gray et al., Opt.Quant.Electron., 31, pp 571-582 (1999)

# Interferometer testing

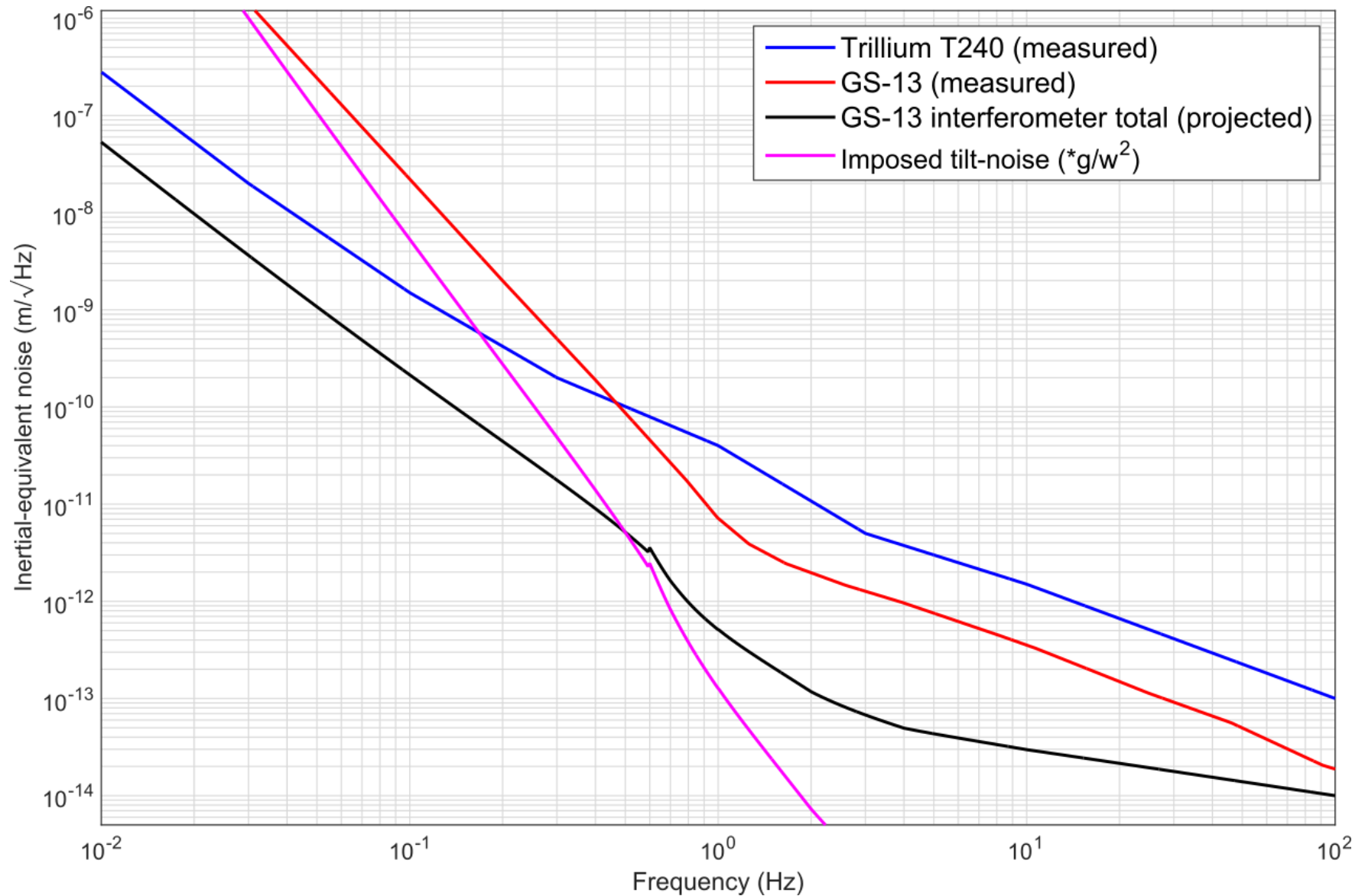


# Spectra on undamped Multi-SAS bench



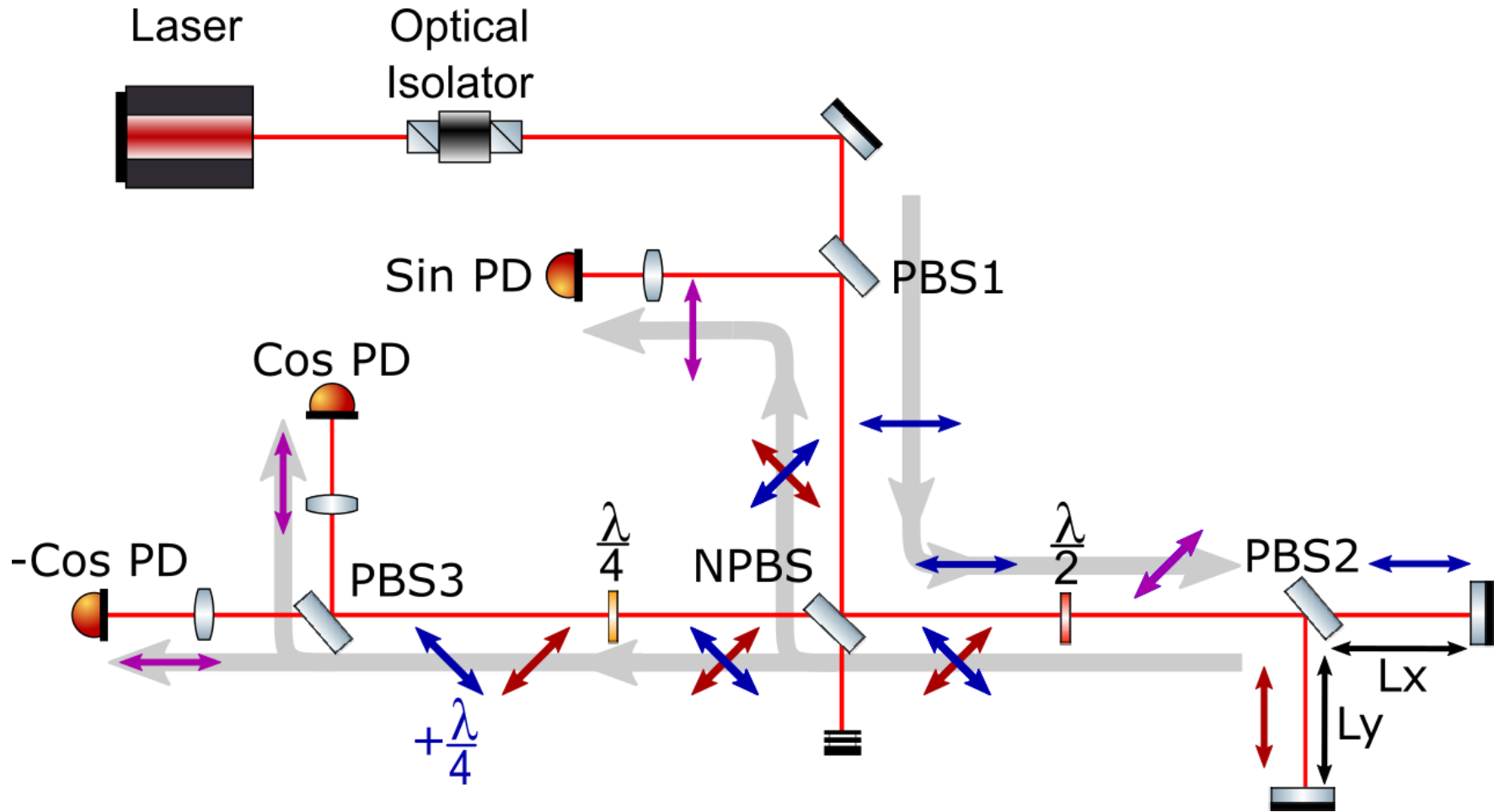


# Design aim for GS-13 readout

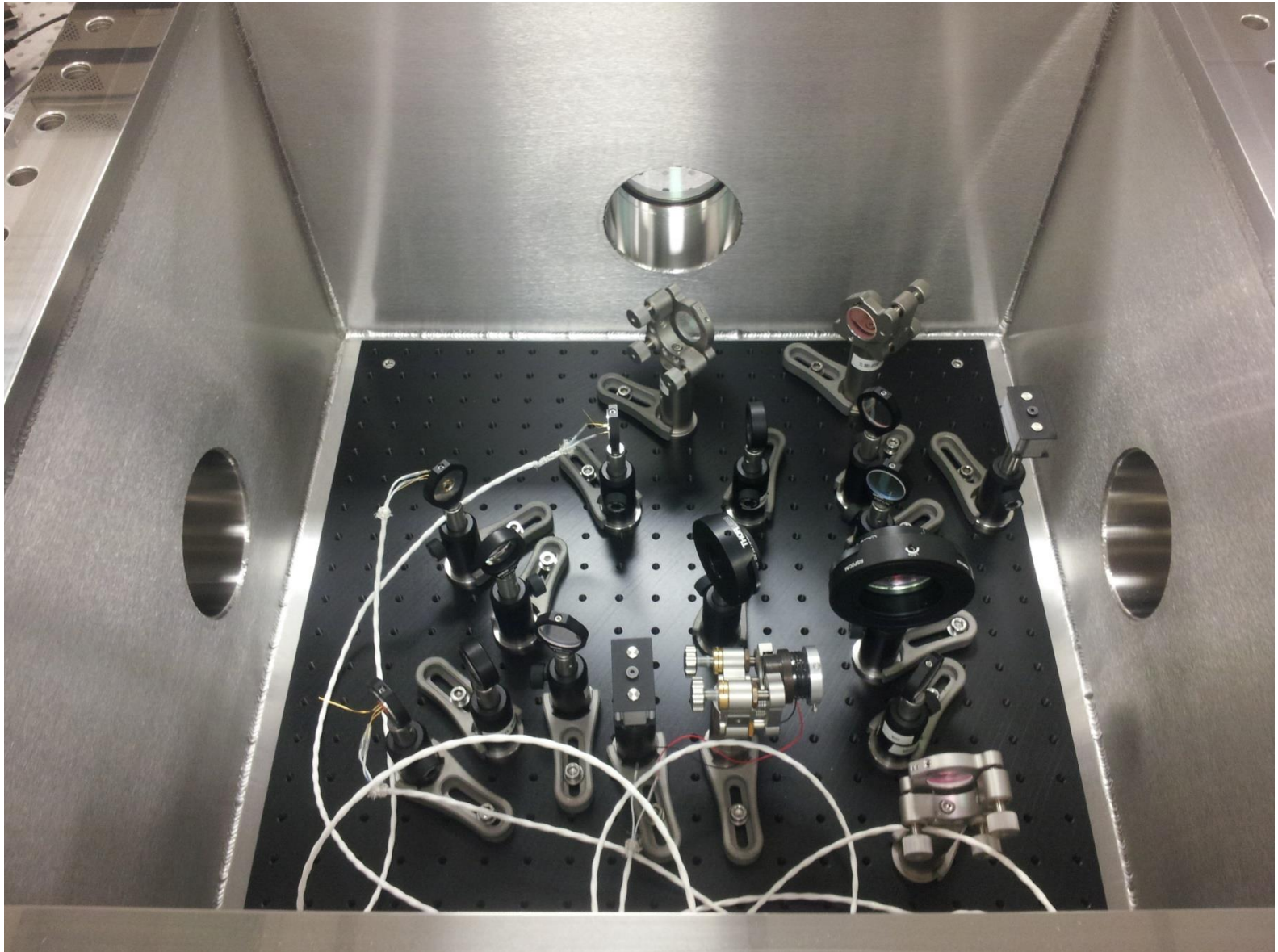




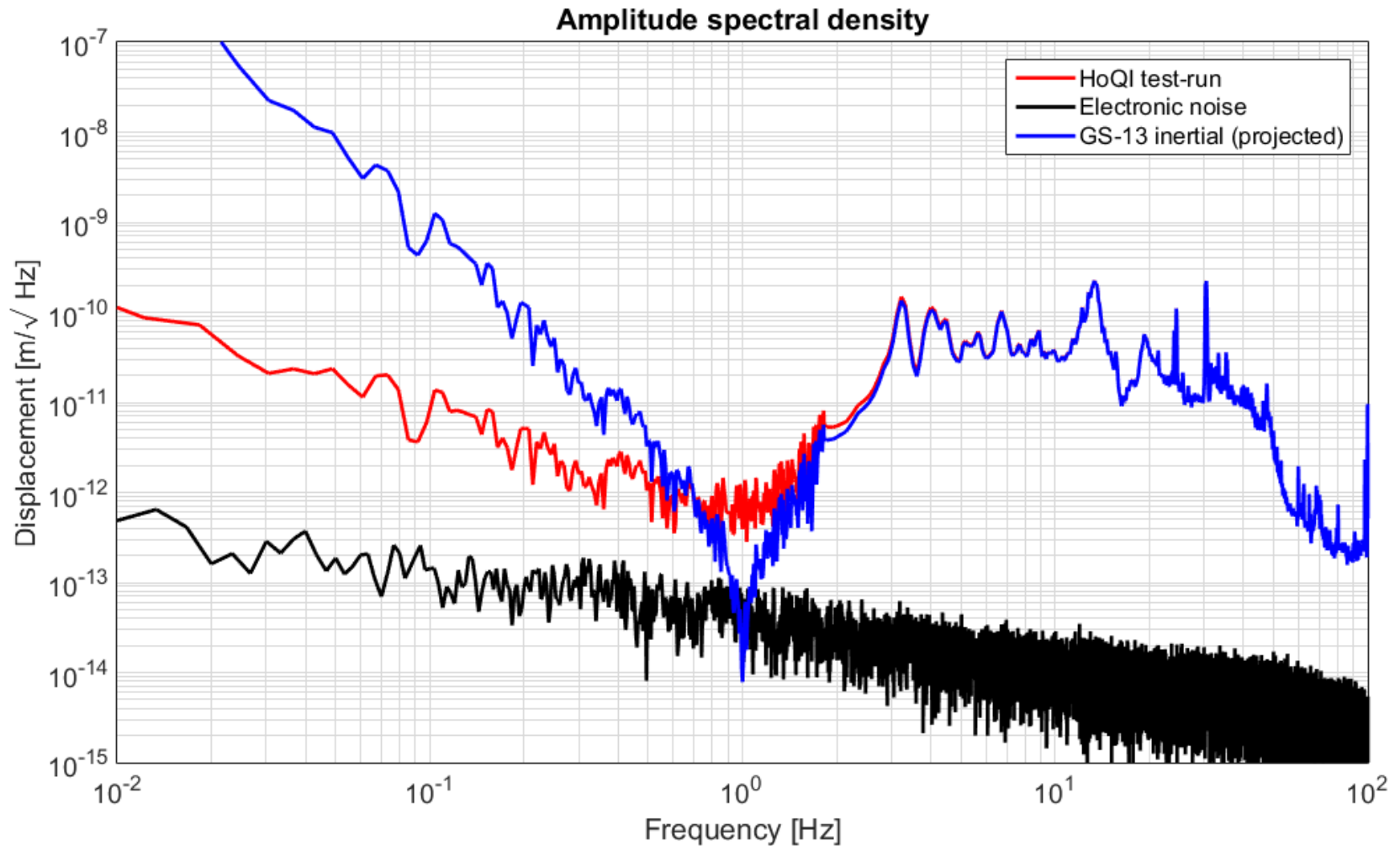
# Homodyne Quadrature Interferometer



# Homodyne Quadrature Interferometer



# HoQI trial measurement (in vacuum)

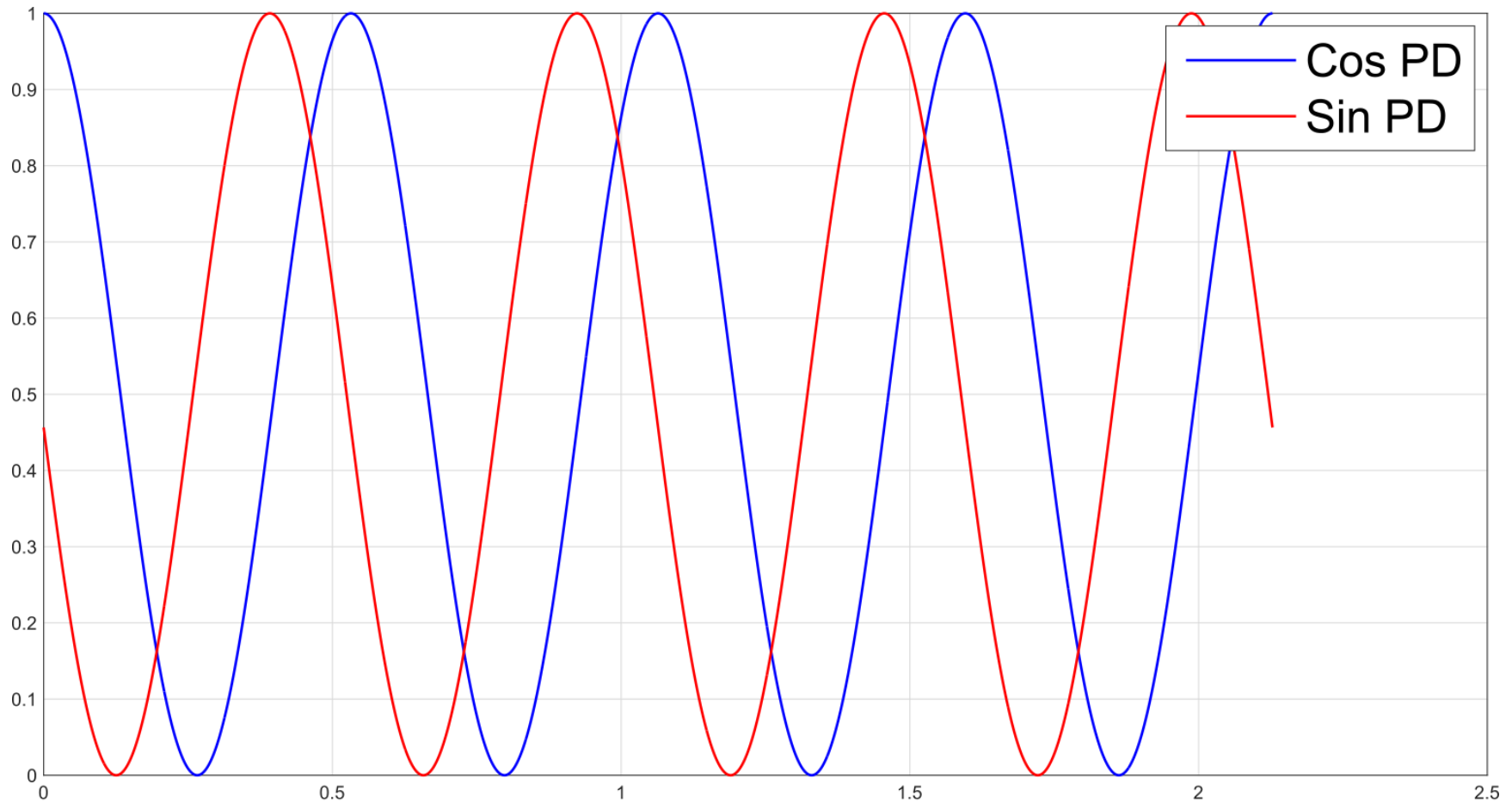


# Future inertial sensor work

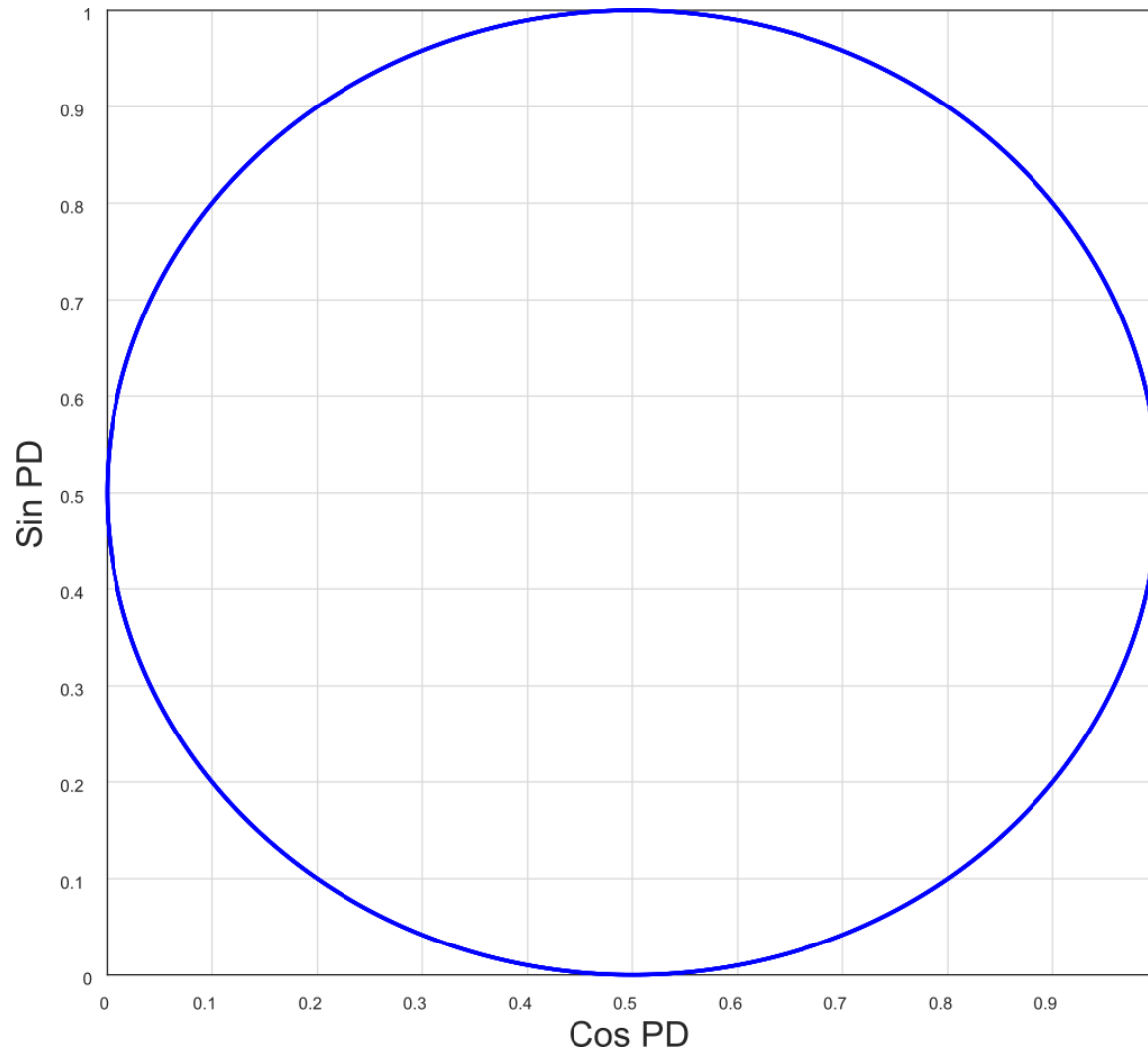
There are many topics that still need much more work here, just a few include:

- New materials,
- Spurious forces on home-made sensors,
- UHV compatibility,
- Non-mechanical devices (eg SCGs)

# Homodyne Quadrature Interferometer



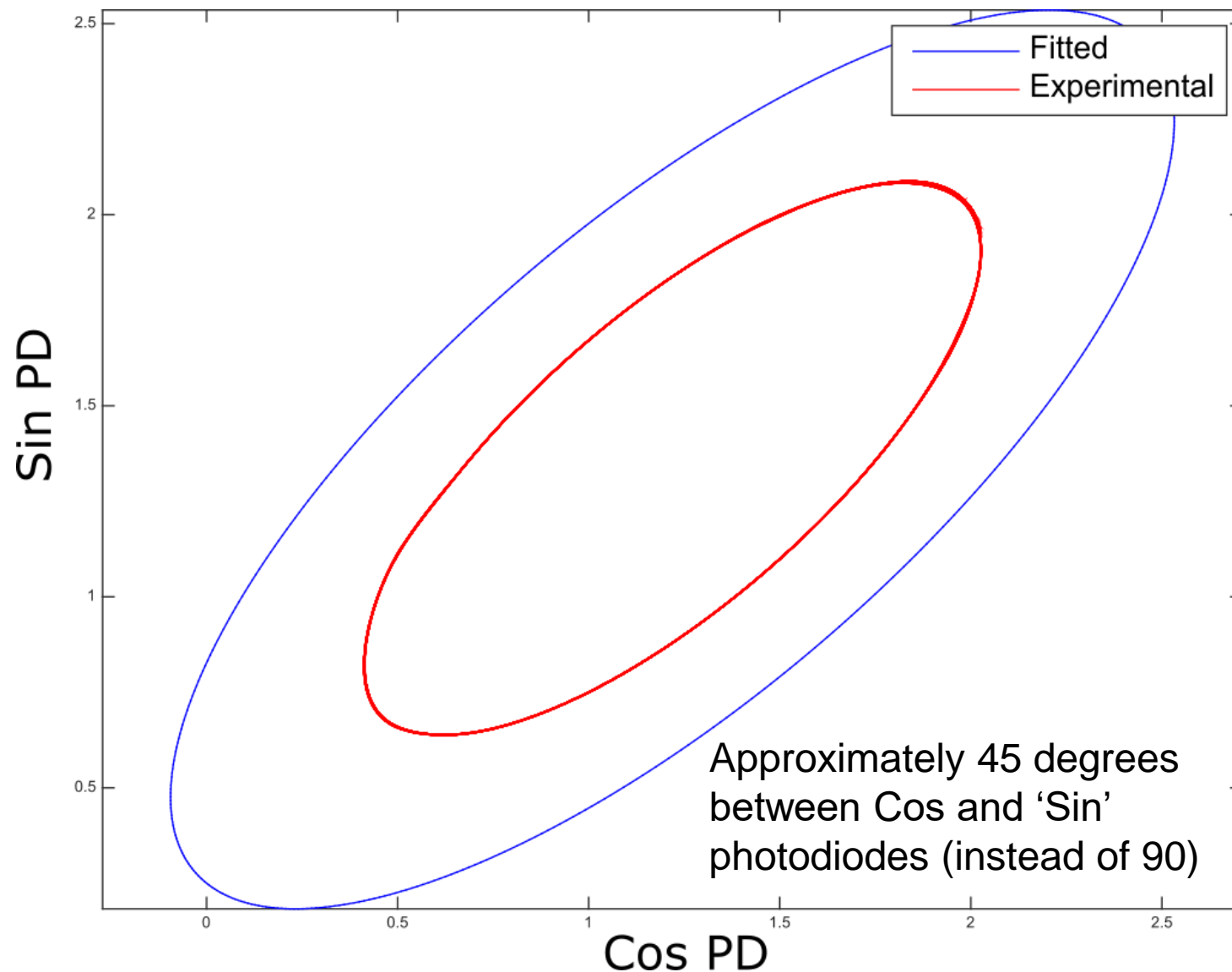
# Homodyne Quadrature Interferometer



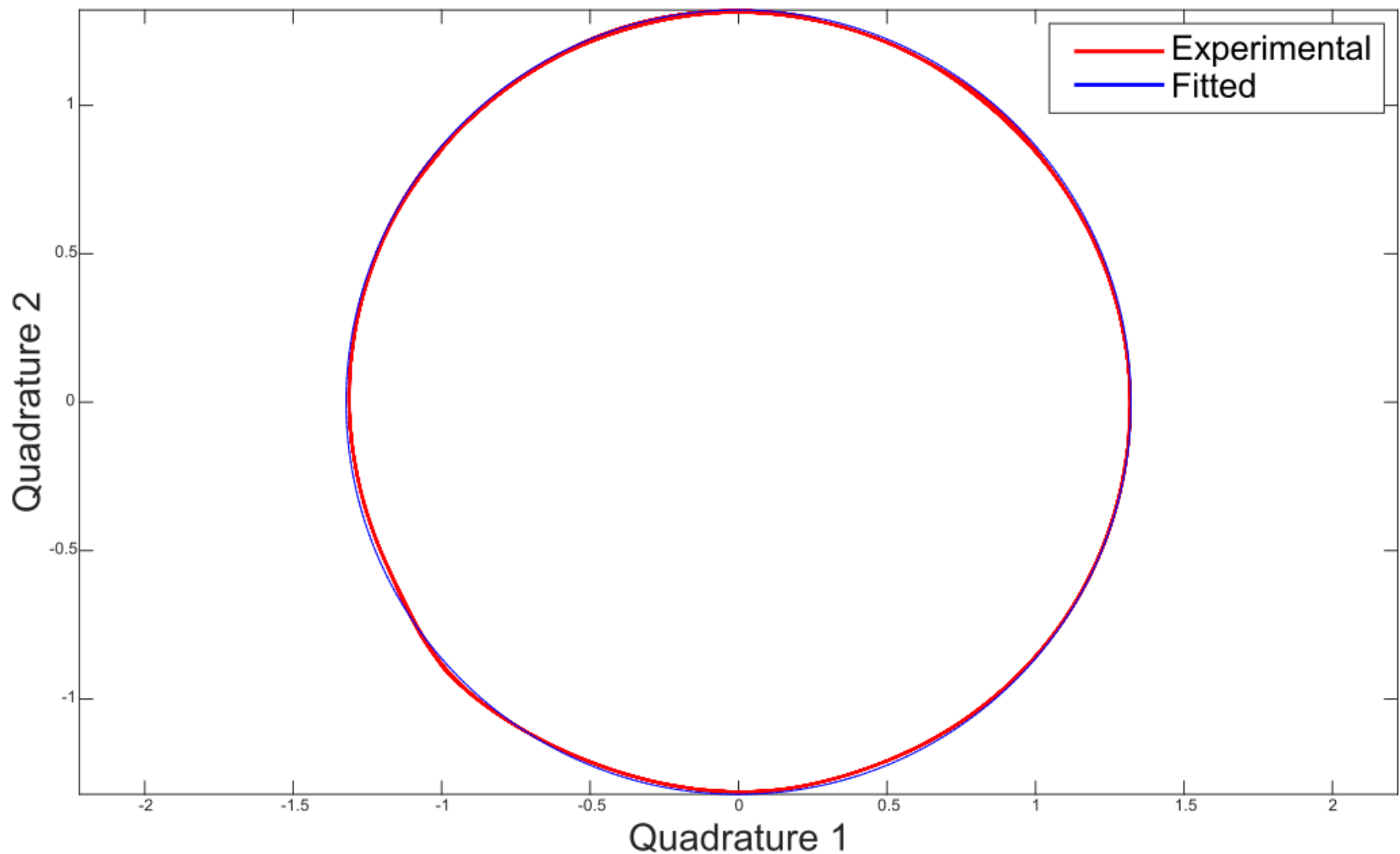
- Sin vs Cos plot creates a circle
- The centre is shifted to 0,0
- Simple arctangent (or a cordic engine) reads out the optical phase, over multiple fringes
- This repeating pattern is our Lissajous figure.
- Roughly speaking, deviations from a circle will create non-linearities in the readout.



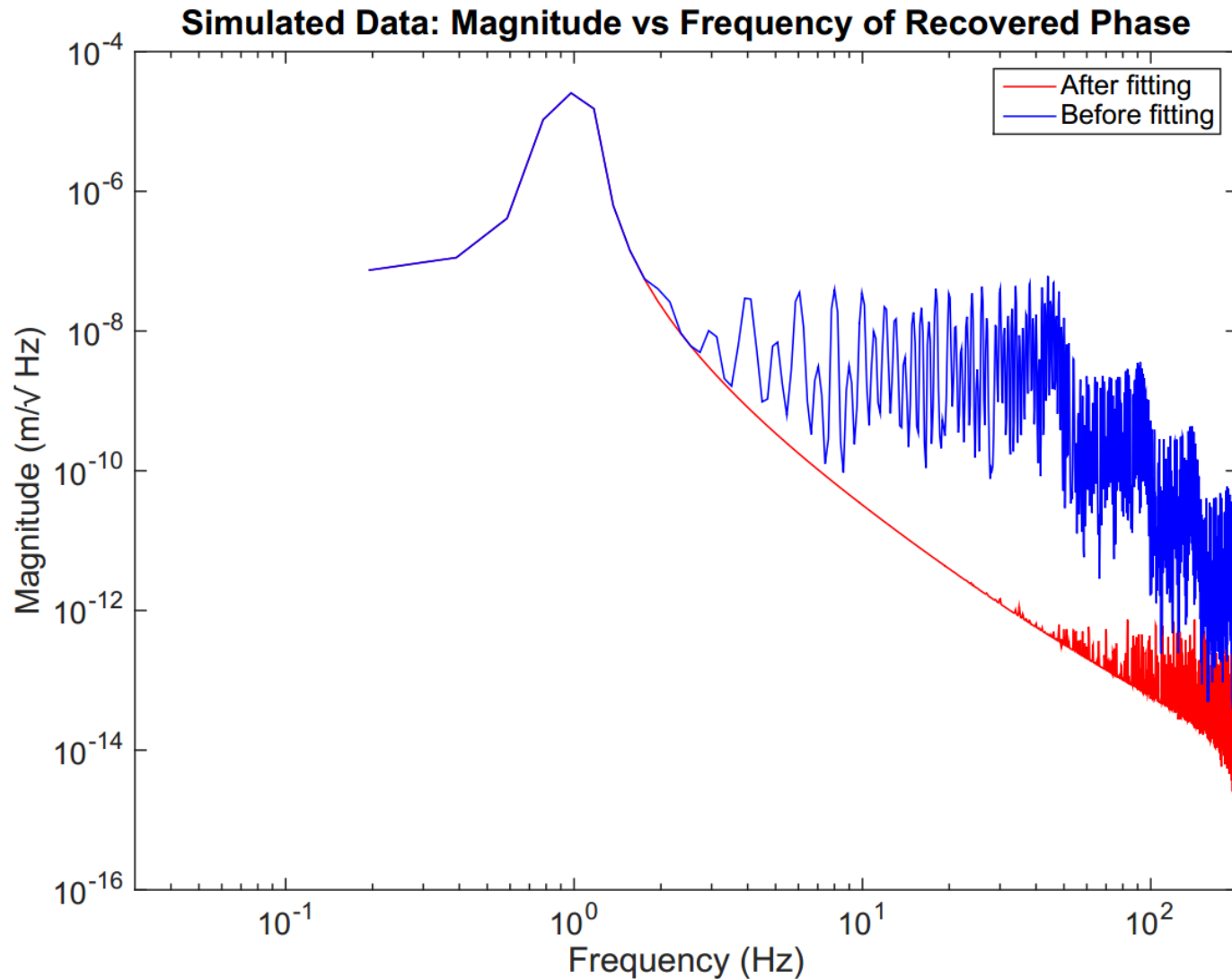
# HoQI Experimental Data



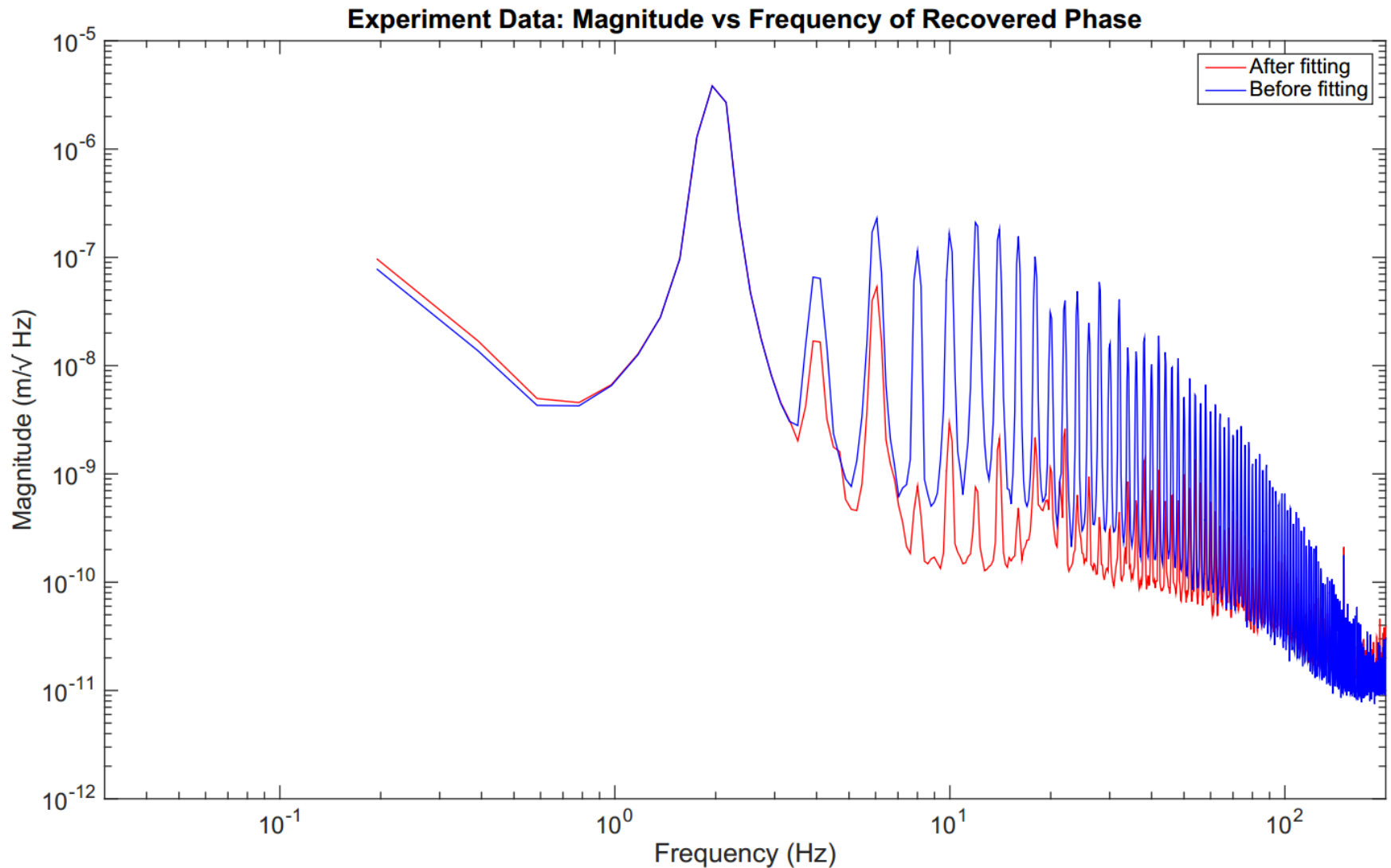
# HoQI Experimental Data



# Homodyne Quadrature Interferometer

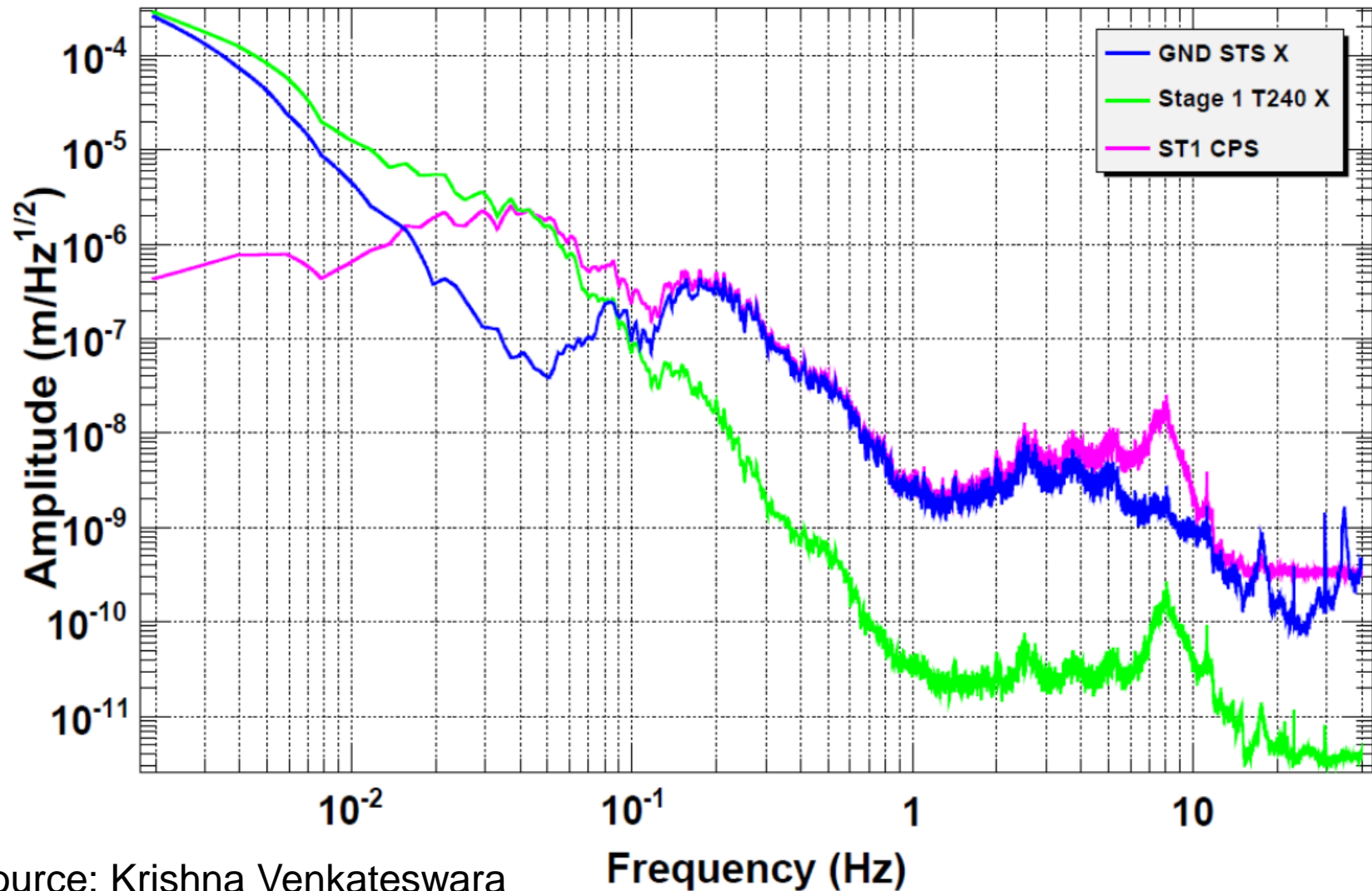


# Homodyne Quadrature Interferometer



# Stage 1 Motion

## Amplitude Spectral Density



Source: Krishna Venkateswara

T0=18/11/2014 22:00:00

Avg=10/Bin=2L

BW=0.00292964