Interplay between collective and single particle excitations around neutron-rich doubly-magic nuclei

NuSpIn

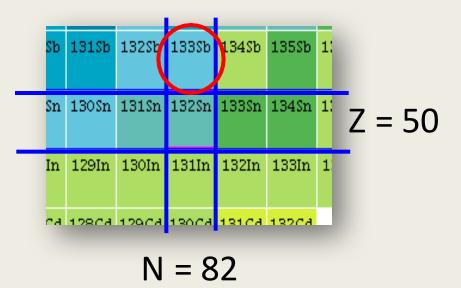
NUSPIN 2016 Workshop on the Nuclear Spectroscopy Instrumentation Network and AGATA Physics Workshop

Giovanni Bocchi Venezia - 2016

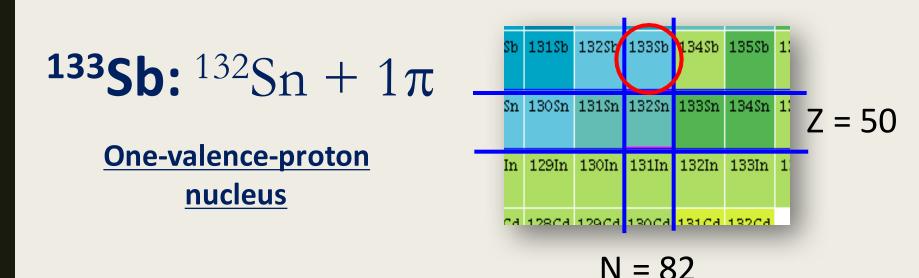
Physics Motivation

133Sb:
$$^{132}Sn + 1\pi$$

One-valence-proton nucleus

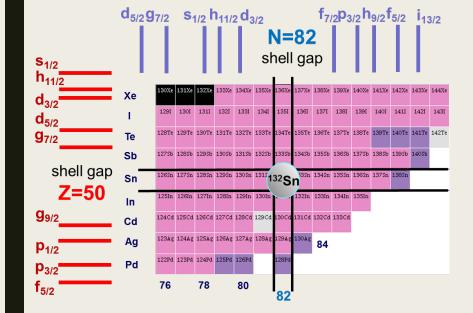


Physics Motivation

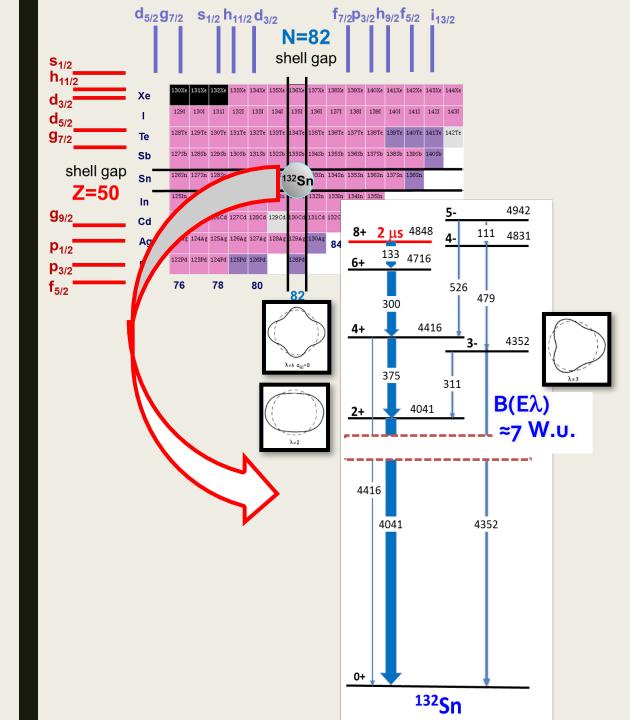


An ideal system to investigate both:

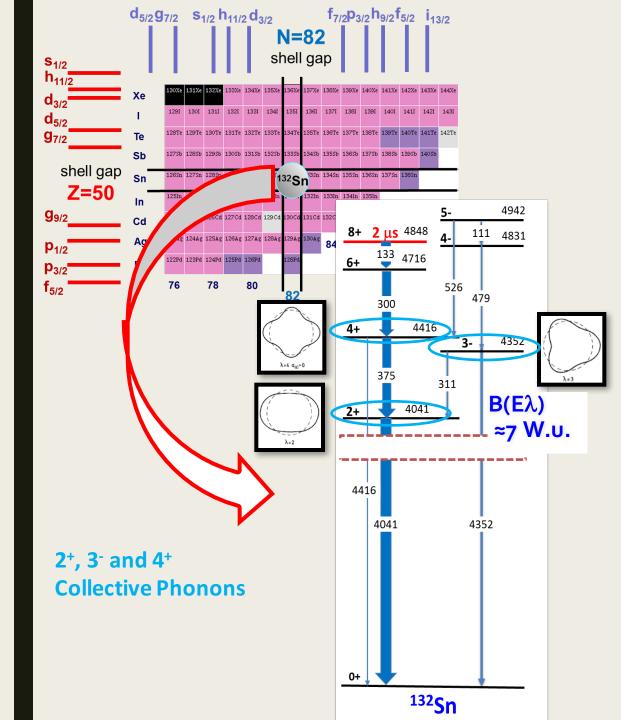
- Single particle excited states
- Coupling between valence particle and core excitations collective (phonons) and non-collective (pure 1p-1h)



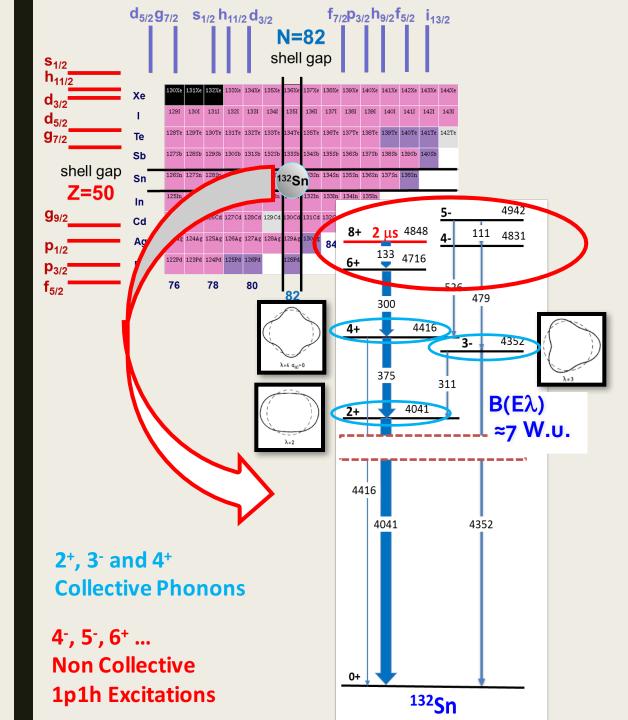
- Single particle levels
- **Couplings** between particle and core excitations



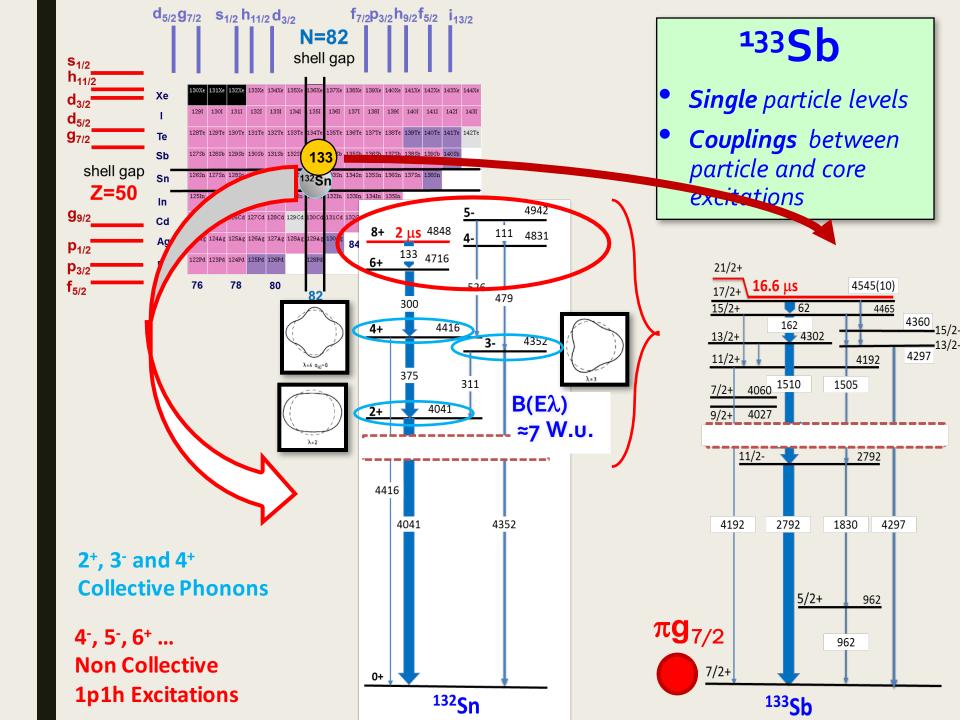
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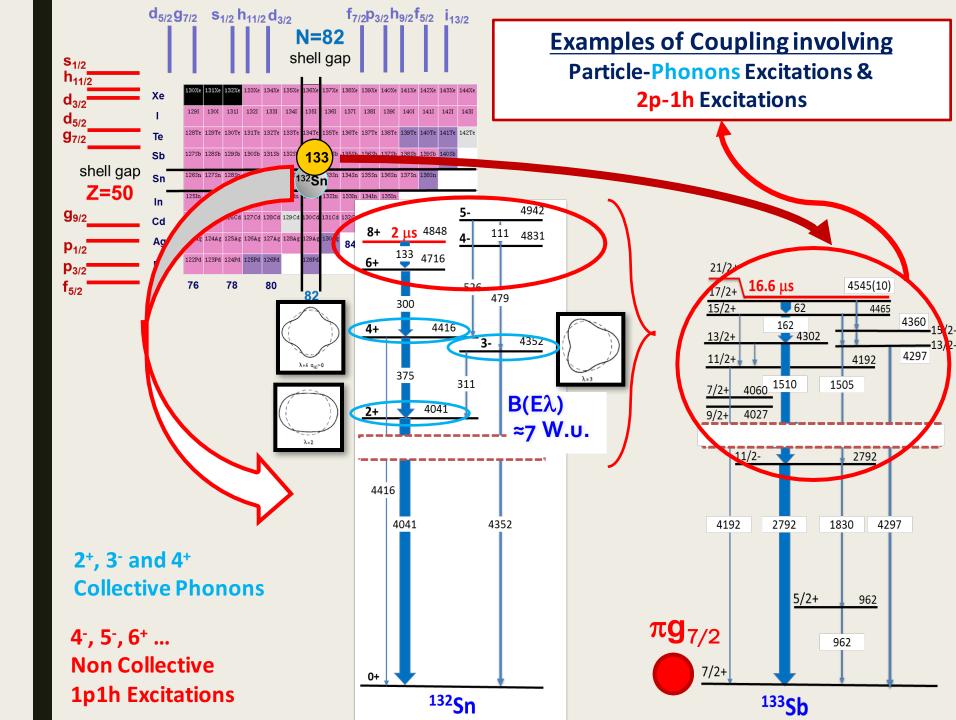


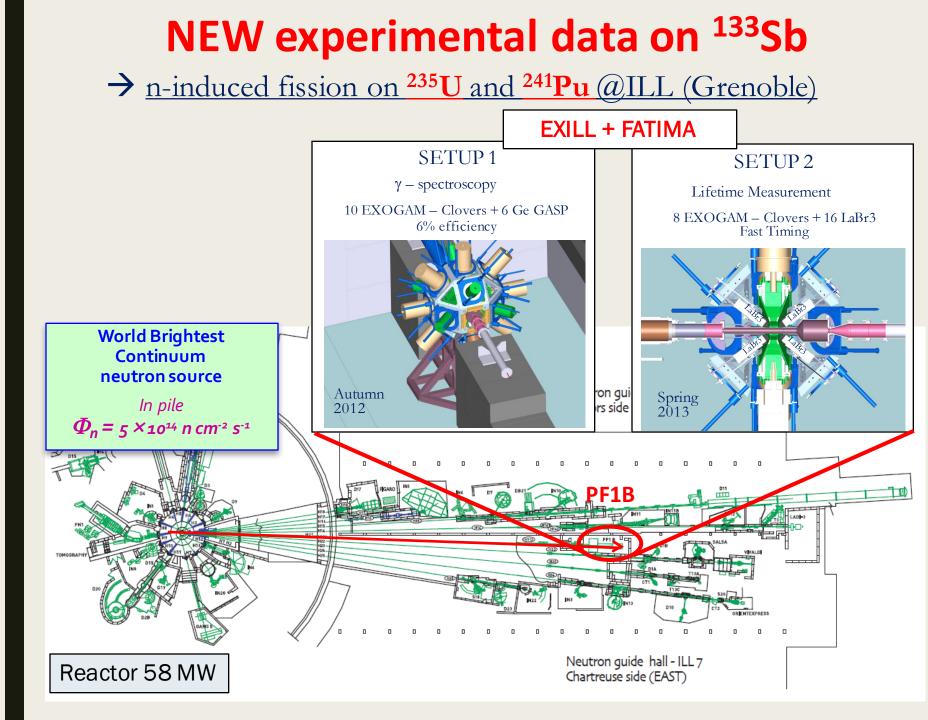
- Single particle levels
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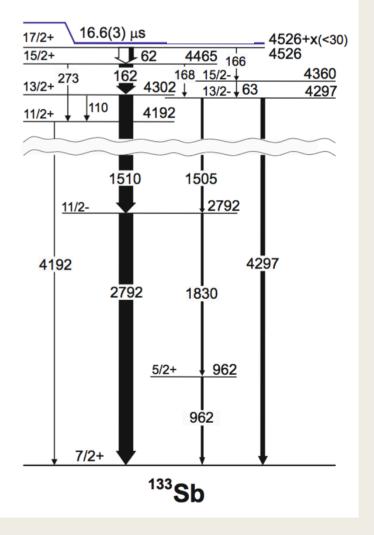
- Single particle levels
- **Couplings** between particle and core excitations





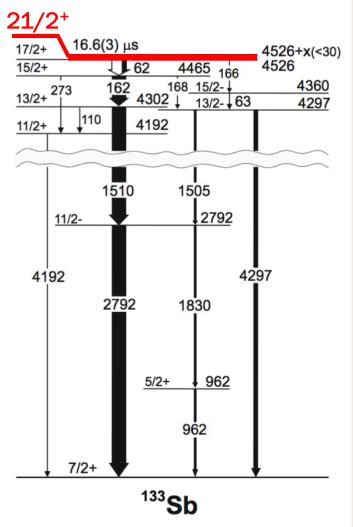


W. Urban et al., PRC79(2009)037304



Isomer Decay Measured at the focal plane of LOHENGRIN separator (ILL)

W. Urban et al., PRC79(2009)037304

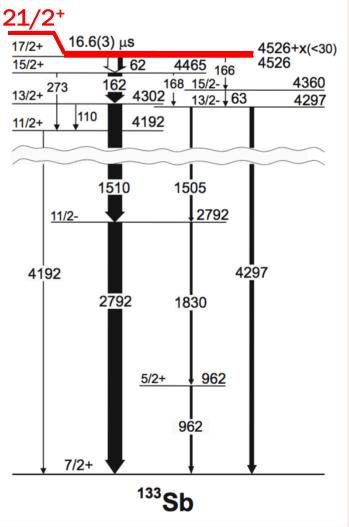


Isomer Decay Measured at the focal plane of LOHENGRIN separator (ILL)

Starting Point

- Isomeric state @ 4.5 MeV with a lifetime of 16.6 μs
- No information above 21/2⁺

W. Urban et al., PRC79(2009)037304



Isomer Decay Measured at the focal plane of LOHENGRIN separator (ILL)

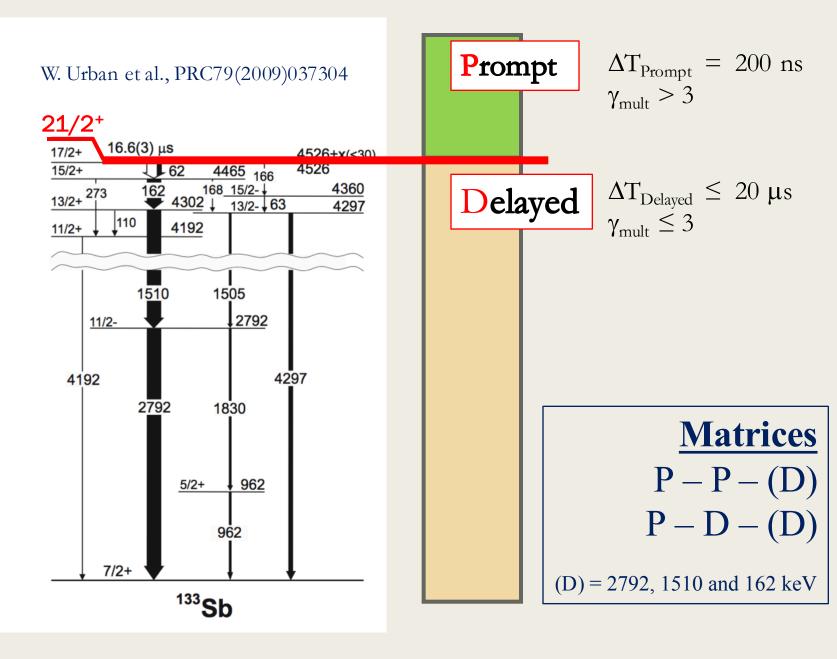
Starting Point

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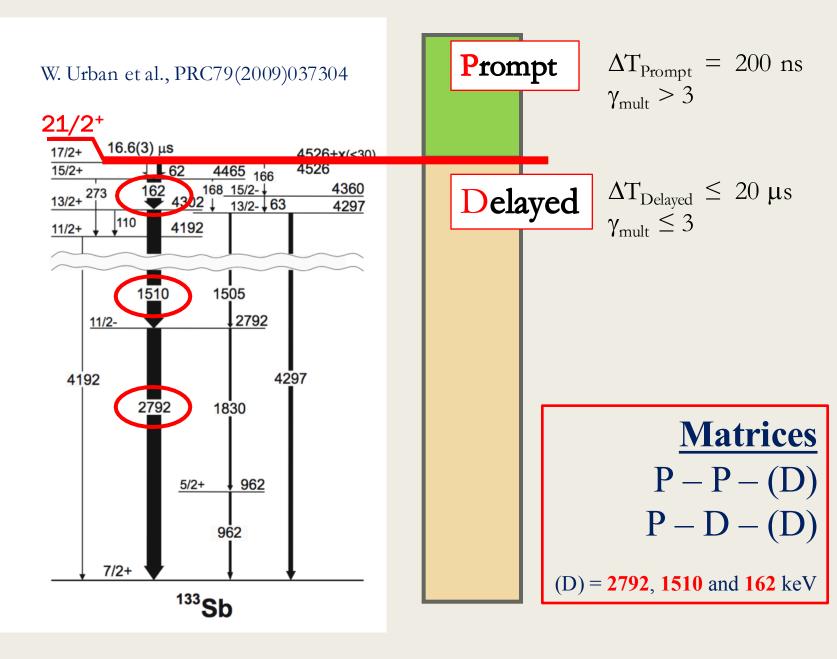
<u>Goal</u>

New high spin yrast states above the long-lived 16.6 μs isomer

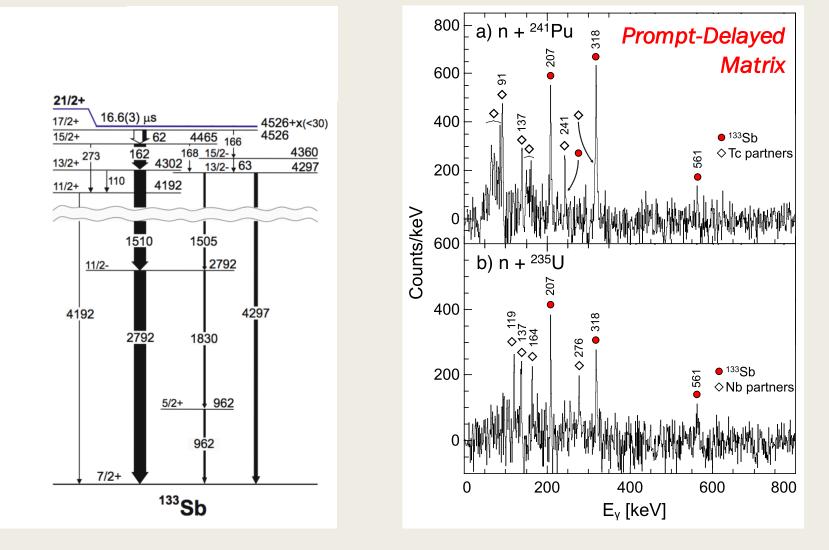
A Fully Digital Approach, TRIGGERLESS acq.



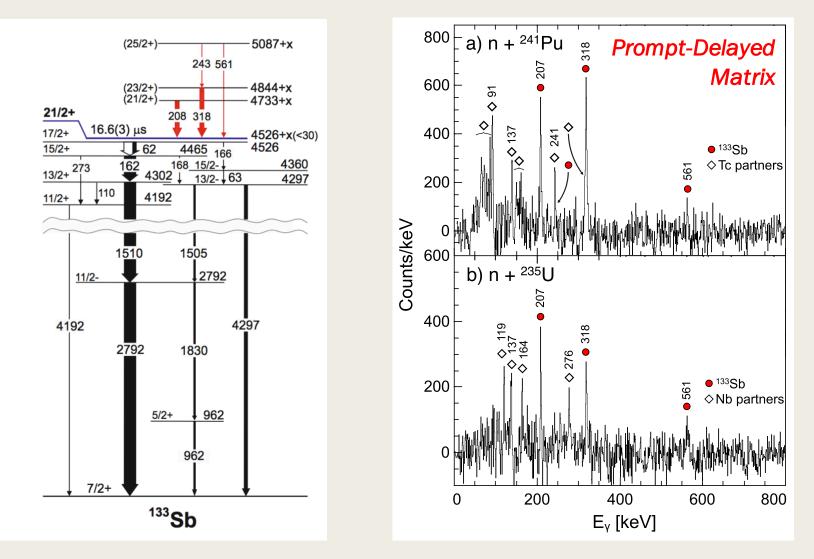
A Fully Digital Approach, TRIGGERLESS acq.



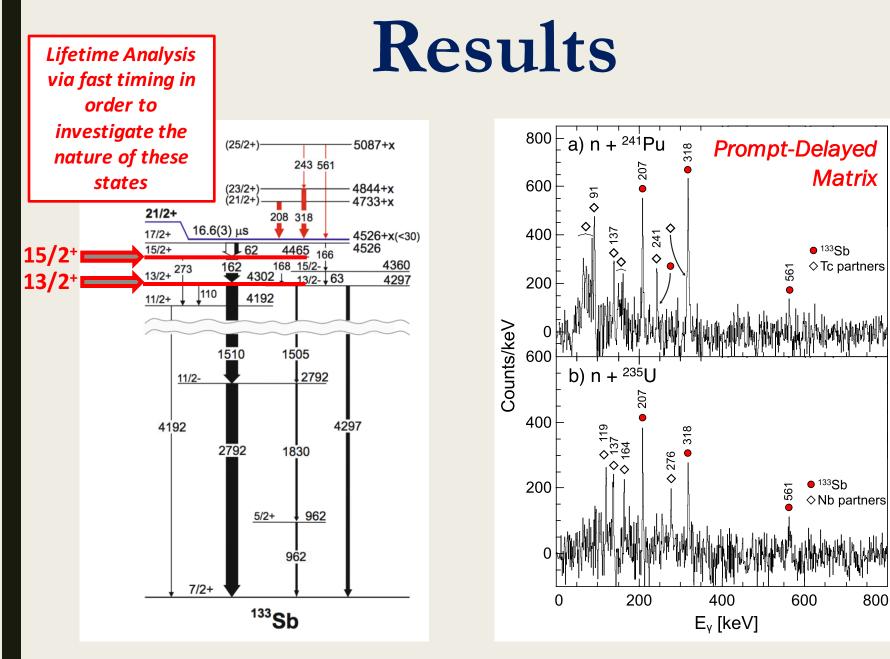
Results



Results

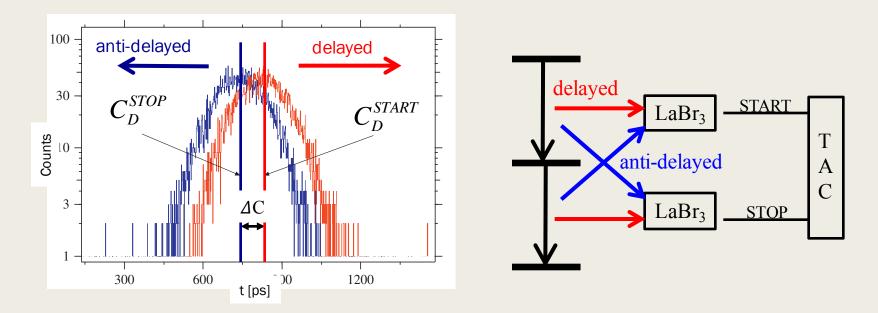


2 targets play a crucial rule in order to confirm new y-transitions



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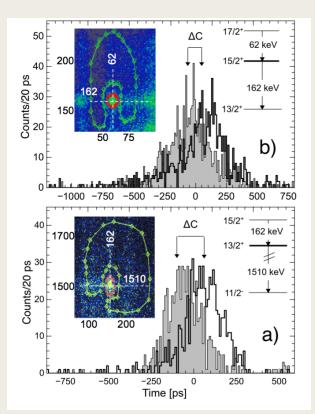
Lifetime Analysis: Generalized Centroid Difference Method (GCD) with LaBr₃(Ce)

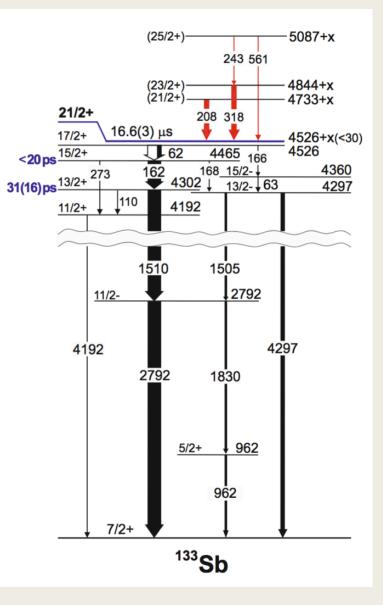


$$C^{D}_{start} = C^{P}_{start} - \tau \qquad \Delta C = C^{D}_{stop} - C^{D}_{start} = C^{P}_{stop} - C^{P}_{start} + 2\tau \qquad 2\tau = \Delta C - PRD$$
$$C^{D}_{stop} = C^{P}_{stop} + \tau \qquad C^{P}_{stop} - C^{P}_{start} + 2\tau$$

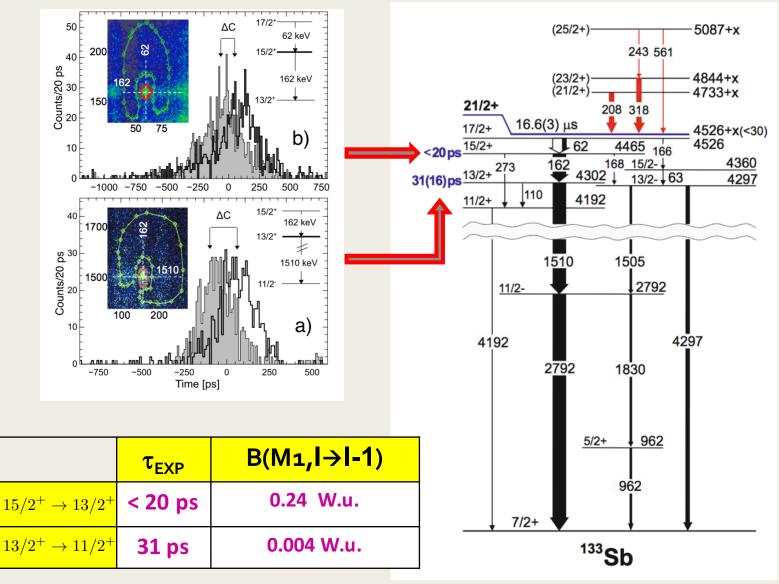
Régis, J. M. et al. Nucl. Instr. and Meth. in Phys. Rev. A 763, 210–220 (2014)

Lifetimes Analysis by FAST-TIMING: Nature of particle-CORE coupled states



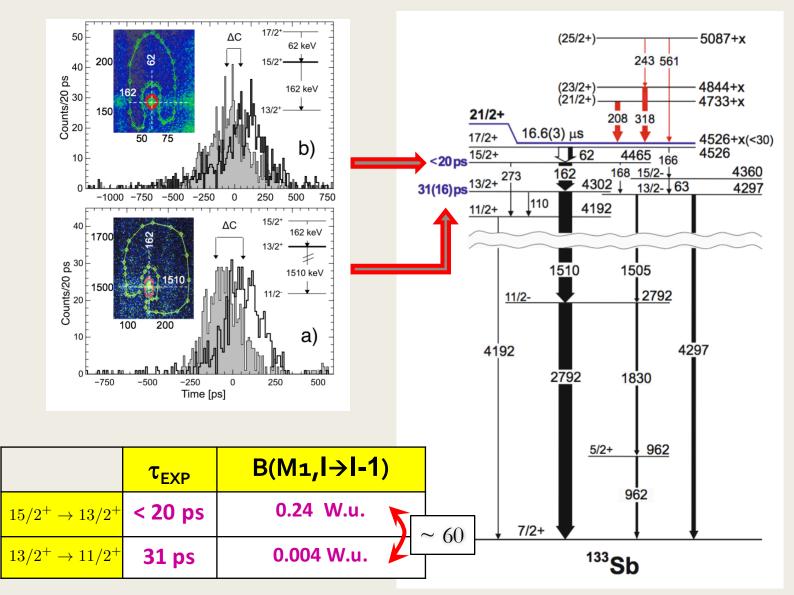


Lifetimes Analysis by FAST-TIMING: Nature of particle-CORE coupled states

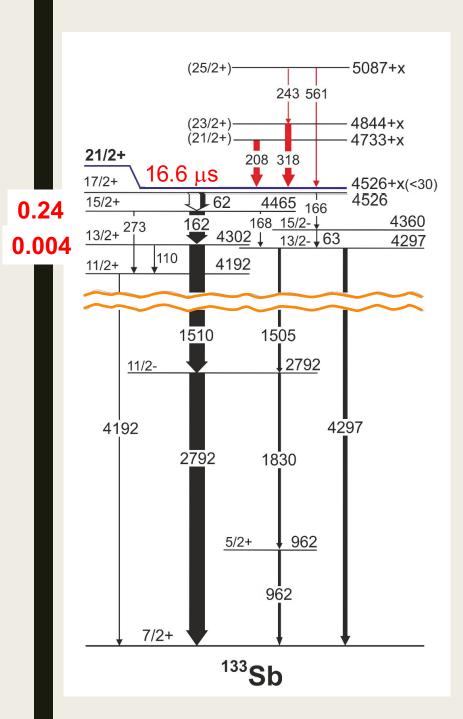


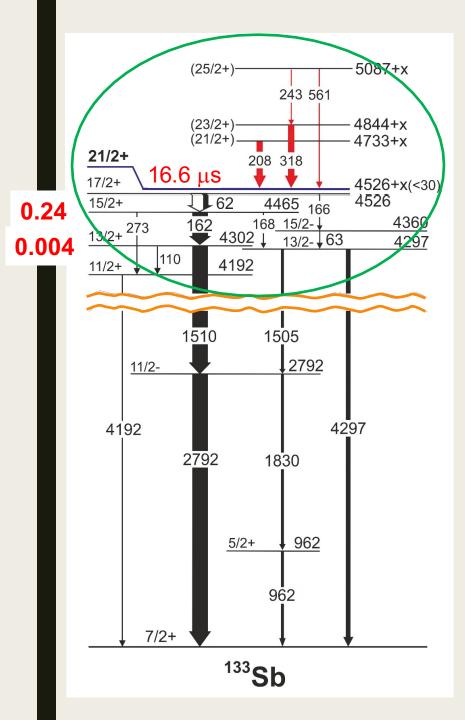
Accepted: Physics Letters B.

Lifetimes Analysis by FAST-TIMING: Nature of particle-CORE coupled states



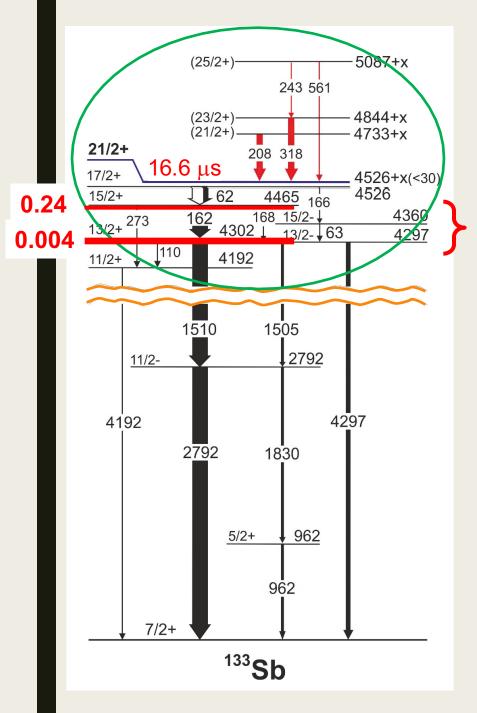
Indication of Different Nature of Excitations!





Restricted SHELL Model Calculations

considering only $\pi g_{7/2} \otimes f_{7/2} h^{-1}_{11/2}$ reproduce the energy sequence of states



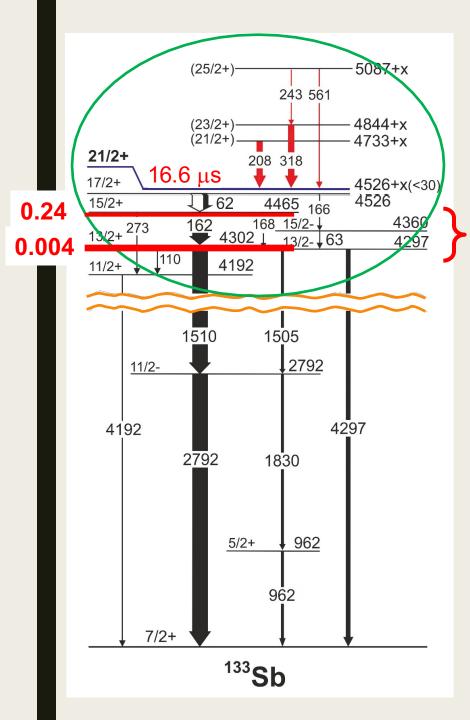
Restricted SHELL Model Calculations

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Experiment: Breaking of the core

LARGE SHELL Model Calculations Involving complex CORE-excitations are NOT possible !

→ 3p – 3h excitations take weeks with 10⁶ processors



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A new approach: HYBRID Model G. Colò, P.F. Bortignon (Milano)

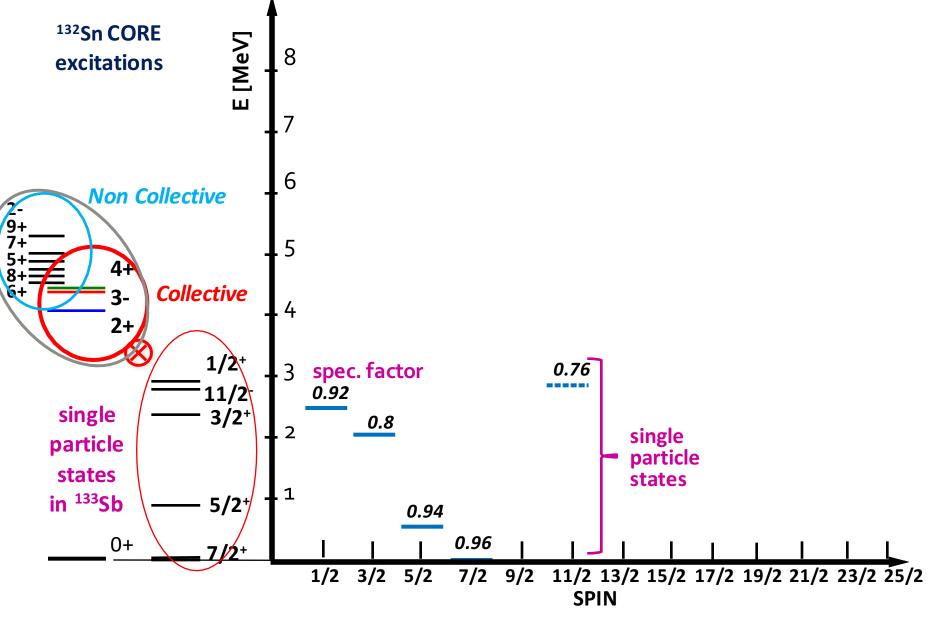
Core excitations of ¹³²Sn (RPA) <u>&</u> Proton States (HF)

HYBRID Model – Main ingredients

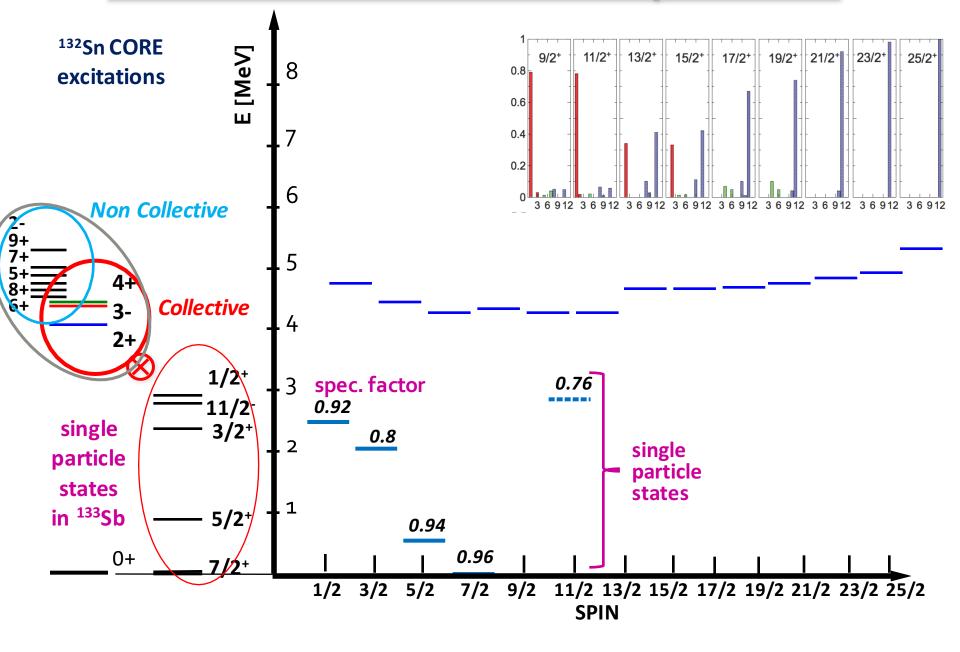
		E		There	tion strength	Main componente		
120 0			Energy		tion strength	-		
¹³² Sn		Exp.	Theory	Exp.	Theory	Theory		
U II			(RPA)		(RPA)	(RPA)		
CORE Excitations	Phonons							
	2+	4.041	3.87	7	4.75	$\nu h_{11/2}^{-1} f_{7/2}$ (0.56), $\pi g_{9/2}^{-1} d_{5/2}$ (0.19), $\pi g_{9/2}^{-1} g_{7/2}$ (0.14)		
E* < 5.5 MeV	3-	4.352	5.02	> 7.1	9.91	$\nu s_{1/2}^{-1'} f_{7/2}$ (0.40), $\nu d_{3/2}^{-1'} f_{7/2}$ (0.12), $\pi p_{1/2}^{-1'} g_{7/2}$ (0.12)		
	× 4 ⁺	4.416	4.46	7	5.10	$\nu h_{11/2}^{-1} f_{7/2} (0.63), \pi g_{0/2}^{-1} g_{7/2} (0.21)$		
$J^{\pi} < 11^{(+,-)}$	Other Excitations Phonons							
	6^{+}	4.716	4.73		1.65	$\nu h_{11/2}^{-1} f_{7/2}$ (0.86), $\pi g_{9/2}^{-1} g_{7/2}$ (0.11)		
	4^{-}	4.831	5.68		0.16	$\nu s_{1/2}^{-1} f_{7/2} (0.91)$		
	8+	4.848	4.80		0.28	$\nu h_{11/2}^{1/2} f_{7/2} (0.98)$		
	5^{+}	4.885	4.77		0.61	$\nu h_{11/2}^{11} f_{7/2} (0.99)$		
	7^{+}	4.942	4.80		0.81	$\nu h_{11/2}^{-1} f_{7/2} (0.98)$		
	5^{-}	4.919	5.98		0.96	$\nu d_{3/2}^{-1/2} f_{7/2}(0.96)$		
	(9+) 5.280	4.99		0.16	$\nu h_{11/2}^{-1} f_{7/2} (0.99)$		
	2^{-}	/	5.44		1.77	$ \nu d_{3/2}^{11/2} f_{7/2}(0.79) $		
¹³³ Sb	<u> </u>					3/21/2 ()		
Single Particle states					1			
ongle i ai tiele states	g 7/2		$d_{5/2}$	C	$l_{3/2}$	h _{11/2} s _{1/2}		
	0		0.587		.439	2.831 2.97 [MeV]		

→ Coupling matrix elements between single particle and RPA states are consistently calculated with the same SkX interaction [B. A. Brown, Phys. Rev. C 58, 220 (1998)]

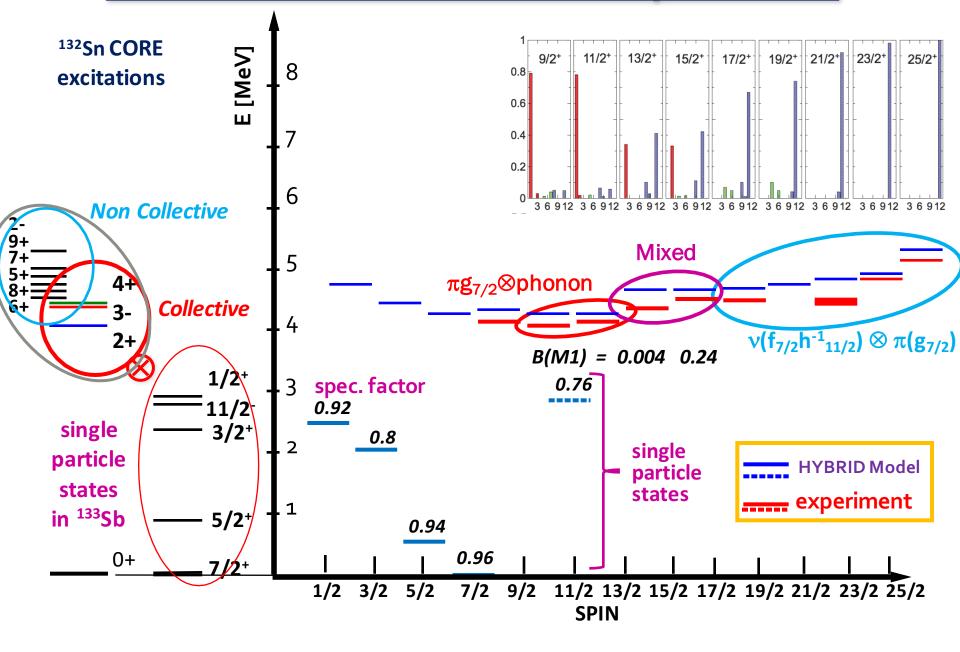
<u>HYBRID Model – ¹³³Sb spectrum</u>



HYBRID Model – ¹³³Sb spectrum



HYBRID Model – ¹³³Sb spectrum



Conclusion

1. EXPERIMENT provides evidence for MIXED configurations of YRAST STATES

Conclusion

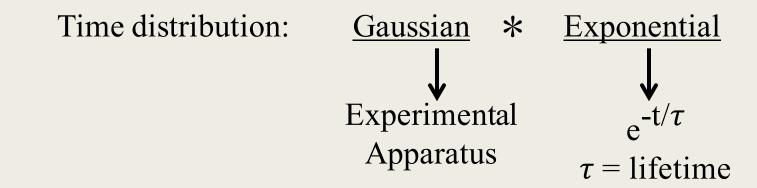
- 1. EXPERIMENT provides evidence for MIXED configurations of YRAST STATES
- 2. The HYBRID Model (just developed) describes this observation (for the YRAST STATES) very satisfactorily (in terms of the coupling of different types of CORE excitations (phonons or particle hole excitations) to the valence particle.

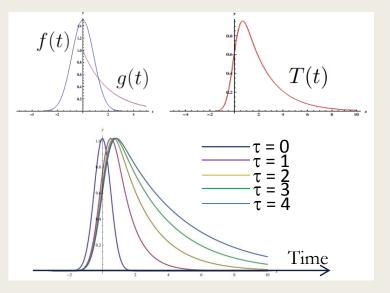
Conclusion

- 1. EXPERIMENT provides evidence for MIXED configurations of YRAST STATES
- 2. The HYBRID Model (just developed) describes this observation (for the YRAST STATES) very satisfactorily (in terms of the coupling of different types of CORE excitations (phonons or particle hole excitations) to the valence particle.
- 3. This might be the way to describe sistematically structures involving core excitations in nuclei around doubly magic cores.

... Thanks

Il Generalized Centroid Difference method (GCD)





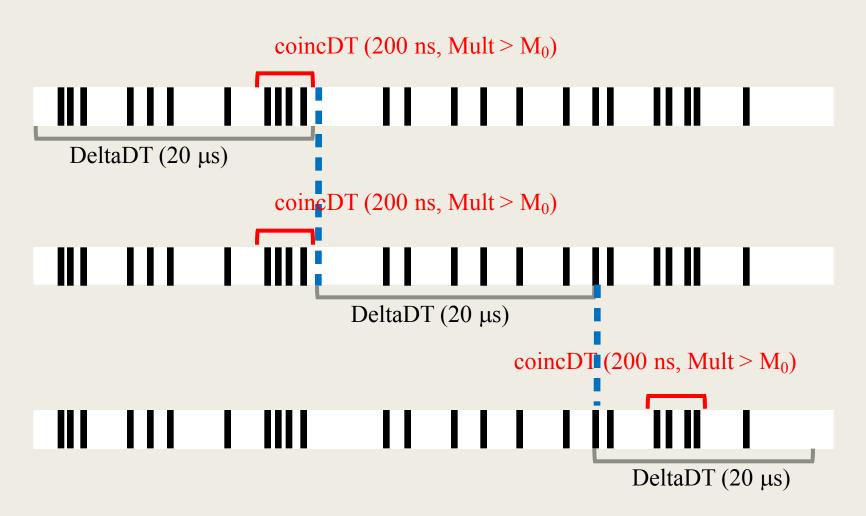
aupprox 0	Prompt	C_{P}
$\tau > 0$	Delayed	C _D

 $C_{\rm D} = C_{\rm P} + \tau \quad \longrightarrow \quad \tau = C_{\rm D} - C_{\rm P}$

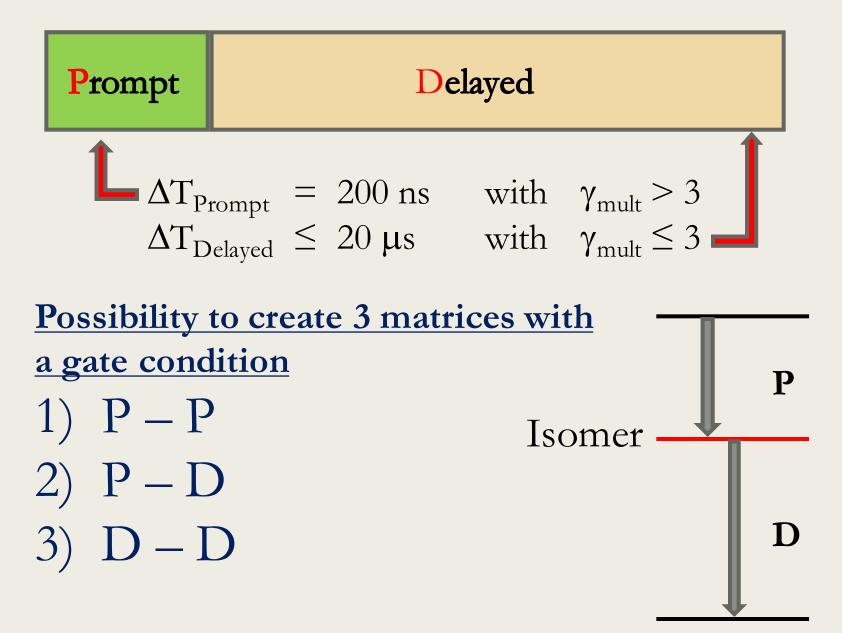
Event Building for µs ISOMER studies Need to define a "Fission" Trigger

Critical Parameter to identify FISSION: $M_0 = 3$

Determination of **Prompt** & **Delayed** events



Event Building for µs ISOMER studies



Base

 $|jm\rangle = a_{jm}^{\dagger}|0\rangle, \qquad |[j' \otimes NJ]_{jm}\rangle$ S.P. S.P x PHONON

Hamiltonian

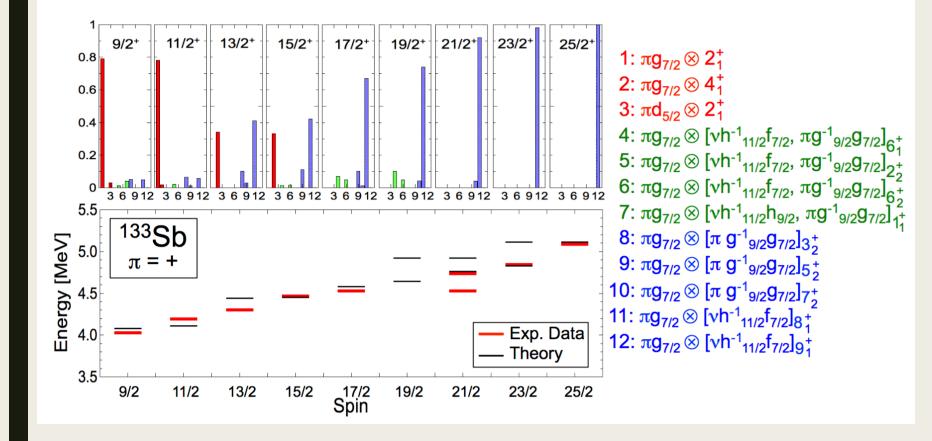
$$\begin{split} H &= H_0 + V, \\ H_0 &= \sum_{jm} \epsilon_j a_{jm}^{\dagger} a_{jm} + \sum_{NJM} \hbar \omega_{NJ} \Gamma_{NJM}^{\dagger} \Gamma_{NJM}, \\ V &= \sum_{jmj'm'} \sum_{NJM} h(jm;j'm',NJM) a_{jm} \left[a_{j'}^{\dagger} \otimes \Gamma_{NJ}^{\dagger} \right]_{jm}, \end{split}$$

$$\mathsf{H} = \begin{pmatrix} \varepsilon_{n_{1}lj} & 0 & \frac{\langle n_{1}lj||V||n_{1}'l_{1}'j_{1}'N_{1}J_{1}\rangle}{\hat{j}} & \frac{\langle n_{1}lj||V||n_{1}'l_{2}'j_{2}'N_{2}J_{2}\rangle}{\hat{j}} \\ 0 & \varepsilon_{n_{2}lj} & \frac{\langle n_{2}lj||V||n_{1}'l_{1}'j_{1}'N_{1}J_{1}\rangle}{\hat{j}} & \frac{\langle n_{2}lj||V||n_{1}'l_{2}'j_{1}'N_{1}J_{1}\rangle}{\hat{j}} & \frac{\langle n_{2}lj||V||n_{1}'l_{2}'j_{2}'N_{2}J_{2}\rangle}{\hat{j}} \\ \frac{\langle n_{1}lj||V||n_{2}'l_{2}'j_{2}'N_{2}J_{2}\rangle}{\hat{j}} & \frac{\langle n_{2}lj||V||n_{1}'l_{2}'l_{2}'N_{2}J_{2}\rangle}{\hat{j}} & 0 & \varepsilon_{n_{2}'l_{2}'j_{2}'} + \hbar\omega_{N_{2}J_{2}} \end{pmatrix}$$

HYBRID Model – Main ingredients

			E,	orgu	Trana	ition strongth	Main components			
1220				nergy Theory	1	ition strength Theory	Main components Theory			
¹³² Sn			Exp.		Exp.					
				(RPA)		(RPA)	(RPA)			
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E* < 5.5 MeV	$\left(\right)$	3^{-}	4.352	5.02	> 7.1	9.91	$\nu s_{1/2}^{-1'} f_{7/2}$ (0.40), $\nu d_{3/2}^{-1'} f_{7/2}$ (0.12), $\pi p_{1/2}^{-1'} g_{7/2}$ (0.12)			
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		(9^+)	5.280	4.99		0.16	$\nu h_{11/2}^{-1} f_{7/2} (0.99)$			
		(3)	0.200	5.44		1.77	$\nu d_{11/2}^{-1/7/2} (0.55)$ $\nu d_{3/2}^{-1} f_{7/2} (0.79)$			
122.01		2		0.44		1.11	$\nu d_{3/2} r_{7/2} (0.13)$			
¹³³ Sb										
Single Particle states						_				
ongle i ai tiele states		g 7/2		$d_{5/2}$		$d_{3/2}$	h _{11/2} s _{1/2}			
Hartree-Fock (Skyrme X)		0		0.587		2.439	2.831 2.97 [MeV]			

→ Coupling matrix elements between single particle and RPA states are consistently calculated with the same SkX interaction



Reduced Transition Probabilities

$$B(X\lambda) \equiv \frac{1}{2j_f + 1} |\langle \alpha_f j_f || \hat{O}(X\lambda) || \alpha_i j_i \rangle|^2,$$

$$\begin{split} \langle \alpha_{f} j_{f} \| \hat{O}(X\lambda) \| \alpha_{i} j_{i} \rangle &= \sum_{if} X_{i}^{\alpha_{i}} X_{f}^{\alpha_{f}} \langle f j_{f} \| \hat{O}(X\lambda) \| i j_{i} \rangle \\ &= \sum_{if} X_{i}^{\alpha_{i}} X_{f}^{\alpha_{f}} \langle j_{f} \| \hat{O}(X\lambda) \| j_{i} \rangle + \\ &+ \sum_{if} X_{i}^{\alpha_{i}} X_{f}^{\alpha_{f}} \langle [j_{f}' \otimes J_{f}']_{j_{f}} \| \hat{O}(X\lambda) \| j_{i} \rangle + \\ &+ \sum_{if} X_{i}^{\alpha_{i}} X_{f}^{\alpha_{f}} \langle j_{f} \| \hat{O}(X\lambda) \| [j_{i}' \otimes J_{i}]_{j_{i}} \rangle + \\ &+ \sum_{if} X_{i}^{\alpha_{i}} X_{f}^{\alpha_{f}} \langle [j_{f}' \otimes J_{f}']_{j_{f}} \| \hat{O}(X\lambda) \| [j_{i}' \otimes J_{i}]_{j_{i}} \rangle, \end{split}$$

$$\begin{split} \langle \alpha_{f} j_{f} \| \hat{O}(X\lambda) \| \alpha_{i} j_{i} \rangle &= \sum_{if} \xi_{i}^{\alpha_{i}} \xi_{f}^{\alpha_{f}} \langle j_{f} \| \hat{O}(X\lambda) \| j_{i} \rangle + \\ &+ \sum_{if} \xi_{i}^{\alpha_{i}} \xi_{f}^{\alpha_{f}} \delta(J_{f}', \lambda) \delta(j_{f}', j_{i}) \frac{\hat{j}_{f}}{\hat{\lambda}} \langle J_{f}' \| \hat{O}_{ph} \| 0 \rangle + \\ &+ \sum_{if} \xi_{i}^{\alpha_{i}} \xi_{f}^{\alpha_{f}} \delta(J_{i}', \lambda) \delta(j_{i}', j_{f}) \frac{\hat{j}_{i}}{\hat{\lambda}} \langle J_{i}' \| \hat{O}_{ph} \| 0 \rangle (-)^{j_{i}-j_{f}+\lambda+\binom{+1}{+0}} + \\ &+ \sum_{if} \xi_{i}^{\alpha_{i}} \xi_{f}^{\alpha_{f}} \hat{j}_{f} \hat{j}_{i} \left\{ (-)^{j_{f}+J_{i}'+\lambda+j_{i}'}_{i} \left\{ \frac{j_{i}}{J_{f}'} \frac{j_{f}}{J_{i}'} \right\} \delta(j_{f}', j_{i}') \times \\ &\times \sum_{ph,p'h'} \left[X_{ph}^{f} X_{p'h'}^{i} + (-)^{J_{f}'-J_{i}'+\lambda} Y_{ph}^{f} Y_{p'h'}^{i} \right] \times \\ &\times \left(\delta(h,h') \hat{J}_{f}' \hat{J}_{i}' (-)^{j_{h}+j_{p}+J_{i}'+\lambda} \left\{ \frac{j_{h}}{J_{j}} \frac{J_{i}'}{J_{j}'} \right\} \langle j_{p} \| \hat{O}_{sp} \| j_{p'} \rangle + \\ &- \delta(p,p') \hat{J}_{f}' \hat{J}_{i}' (-)^{j_{h}+j_{p}+J_{i}'}_{i} \left\{ \frac{j_{p}}{J_{h}'} \frac{J_{i}'}{J_{j}'} \right\} \langle j_{n'} \| \hat{O}_{sp} \| j_{h} \rangle \right) + \\ &+ (-)^{j_{i}+j_{f}'+\lambda+J_{f}'} \left\{ \frac{j_{f}}{J_{i}'} \frac{j_{i}}{J_{f}'} \right\} \delta(J_{f}', J_{i}') \langle j_{f}' \| \hat{O}_{sp} \| j_{i}' \rangle \right\}. \end{split}$$

Reduced Transition Probabilities

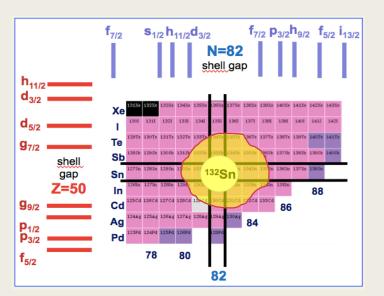
D.A. Varshalovich, World Scientific Publishing Company, Incorporated, 1988 A. Bohr, B.R. Mottelson, Nuclear Structure, I and II, W.A. Benjamin, 1975

Physics Motivation

Low lying excited states in **DOUBLY MAGIC** Nuclei are dominated by complex, collective excitations

2⁺, 3⁻, 4⁺, ... **PHONONS**

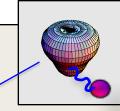




The Structure of Nuclei with **one** or **two valence particles** is influenced by

Particle-Phonon couplings

excited core (phonon)



Key Ingredient for:

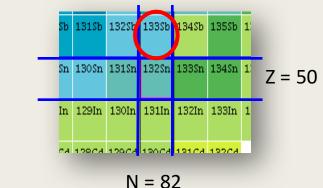
- Quenching of Spectroscopic Factors,
- Anharmonicity of vibrational spectra
- Damping of Giant Resonances, ...

PHENOMENOLOGICAL (Bohr-Mottelson) MICROSCOPIC (Colò, Bortignon, Sagawa, Dabaczewski, Vretenar, ...)

→ VERY limited EXPERIMENTAL Information on Particle-PHONON Couplings around DOUBLY MAGIC NUCLEI

Outline



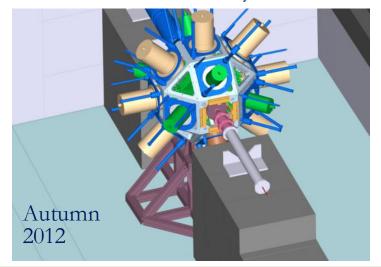


- Physics Motivation:
- EXILL e FATIMA Campaign
- Experimental Setup
- Analysis
- Theory

First time a large HPGe array (52 Ge crystals) installed around a highly collimated cold-neutron beam

SETUP 1

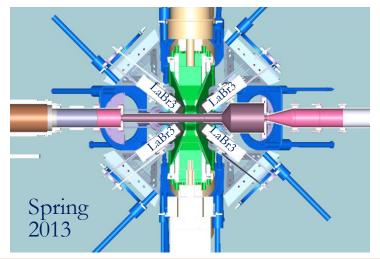
γ – spectroscopy 10 EXOGAM – Clovers + 6 Ge GASP 6% efficiency





Lifetime Measurement

8 EXOGAM – Clovers + 16 LaBr3 Fast Timing



The ACQUISITION SYSTEM

A Fully Digital Approach, TRIGGERLESS

>10 kHz/crystal, >600 kHz total, 10 ns clock Unique opportunity for g-coincidences over several ms time window

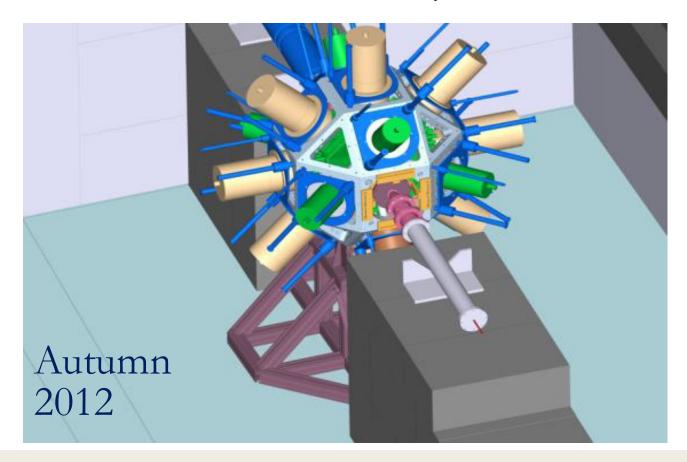
 \rightarrow <u>n-induced fission on ²³⁵U and ²⁴¹Pu and (n, γ) on several targets</u>

2 target play a crucial rule in order to identify partners!!!

EXILL (EXOgam @ ILL)

SETUP 1

γ – spectroscopy 8 EXOGAM – Clovers + 6 Ge GASP + 2 Lohengrin 6% efficiency



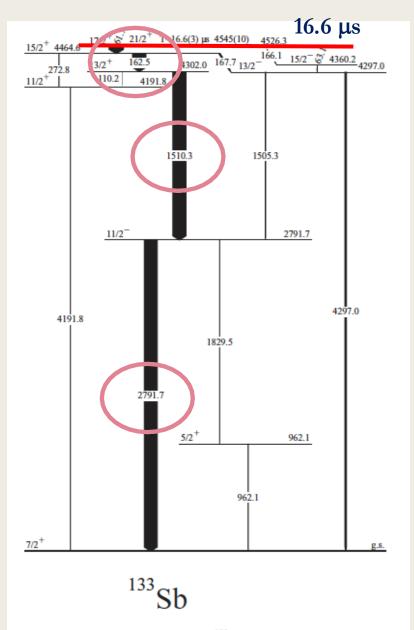


FIG. 5. Partial level scheme of ¹³³Sb as obtained in the present work. Excited levels and γ transitions are labeled with energies given in keV.

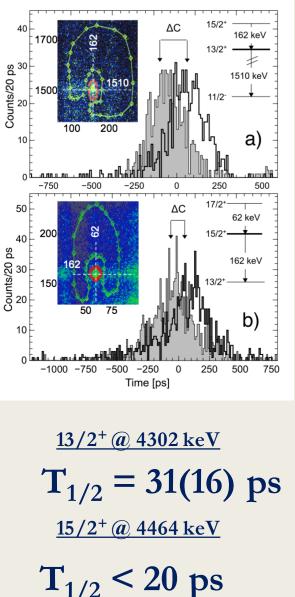
Isomer Decay Measured at the focal plane of LOHENGRIN separator (ILL)

W. Urban et al., PRC79(2009)037304

 $\frac{\text{Matrices}}{P - P - (D)}$ P - D - (D)

(D) = 2792, 1510 and 162 keV

Lifetimes Analysis by FAST-TIMING: Nature of particle-CORE coupled states



INTERPRETATION

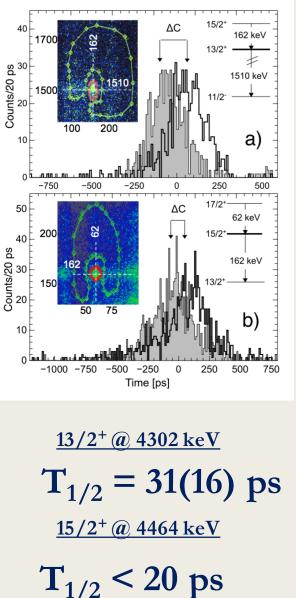
Multiplet of states 11/2⁺, 13/2⁺, ... 25/2⁺

Lifetimes Analysis with Scintillators

	$ au_{EXP}$	B(M1,I→I-1)	
$15/2^+ \to 13/2^+$	≈10 ps	0.7 W.u.	> 100
$13/2^+ \to 11/2^+$	≈40 ps	0.005 W.u.	- 100

Not Simple Configurations !

Lifetimes Analysis by FAST-TIMING: Nature of particle-CORE coupled states



INTERPRETATION

Multiplet of states 11/2⁺, 13/2⁺, ... 25/2⁺

Lifetimes Analysis with Scintillators

	$ au_{EXP}$	B(M1,I→I-1)	
$15/2^+ \to 13/2^+$	≈10 ps	0.7 W.u.	> 100
$13/2^+ \to 11/2^+$	≈40 ps	0.005 W.u. 🟒	- 100



Hybrid Configuration Mixing (G. Colò & P.F. Bortignon)

We start from a **basis** made up with **particles** (or holes) around a core, and with **excitations** of the same core (RPA "phonons").

$$|jm\rangle = a^{\dagger}_{jm}|0\rangle, \qquad |[j' \otimes NJ]_{jm}\rangle$$

Hamiltonian

$$\begin{split} H &= H_0 + V, \\ H_0 &= \sum_{jm} \epsilon_j a_{jm}^{\dagger} a_{jm} + \sum_{NJM} \hbar \omega_{NJ} \Gamma_{NJM}^{\dagger} \Gamma_{NJM}, \\ V &= \sum_{jmj'm'} \sum_{NJM} h(jm;j'm',NJM) a_{jm} \left[a_{j'}^{\dagger} \otimes \Gamma_{NJ}^{\dagger} \right]_{jm}, \end{split}$$