

The search for the Higgs boson at the Tevatron and the LHC

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QCD@Work, Martina Franca, june 20 2010

Outline

- Introduction
- Higgs production through gluon-gluon fusion
 - Theoretical predictions
 - Tevatron results: the importance of radiative corrections
 - Fully exclusive computations
- Summary

The heritage

Standard Electroweak theory based on $SU(2)_L \otimes U(1)_Y$ gauge theory



A. Salam



S. Weinberg



S. Glashow

Quantum Chromo Dynamics (QCD): $SU(3)_c$ gauge theory



D. Gross



F. Wilczek



D. Politzer




Altogether a beautiful theory describing high-energy phenomena at a surprising level of accuracy

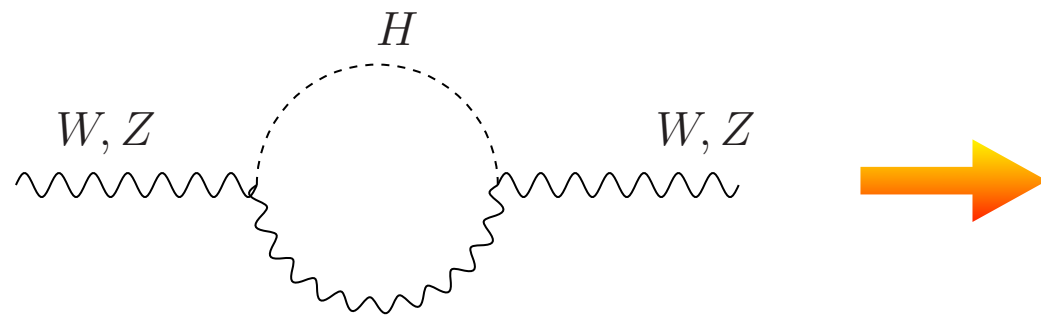
But how do elementary particles acquire their mass ?

The “last” mystery

- The standard solution: masses are generated by the Higgs boson (scalar particle) through Spontaneous Symmetry Breaking
- The mass of the Higgs boson is not predicted by the theory
- Theoretical arguments (or prejudices) suggest
 $50 \text{ GeV} \lesssim m_H \lesssim 800 \text{ GeV}$ (with new physics at the TeV scale)
- LEP has put a lower limit on the mass of the SM Higgs boson at $m_H \geq 114.4 \text{ GeV}$ at 95% CL
- The most sought particle in history (LEP, Tevatron, LHC) !

Other constraints come from:

 **Precision electroweak data:
radiative corrections are
sensitive to the mass of
virtual particles**



$$m_H = 87_{-26}^{+35} \text{ GeV}$$

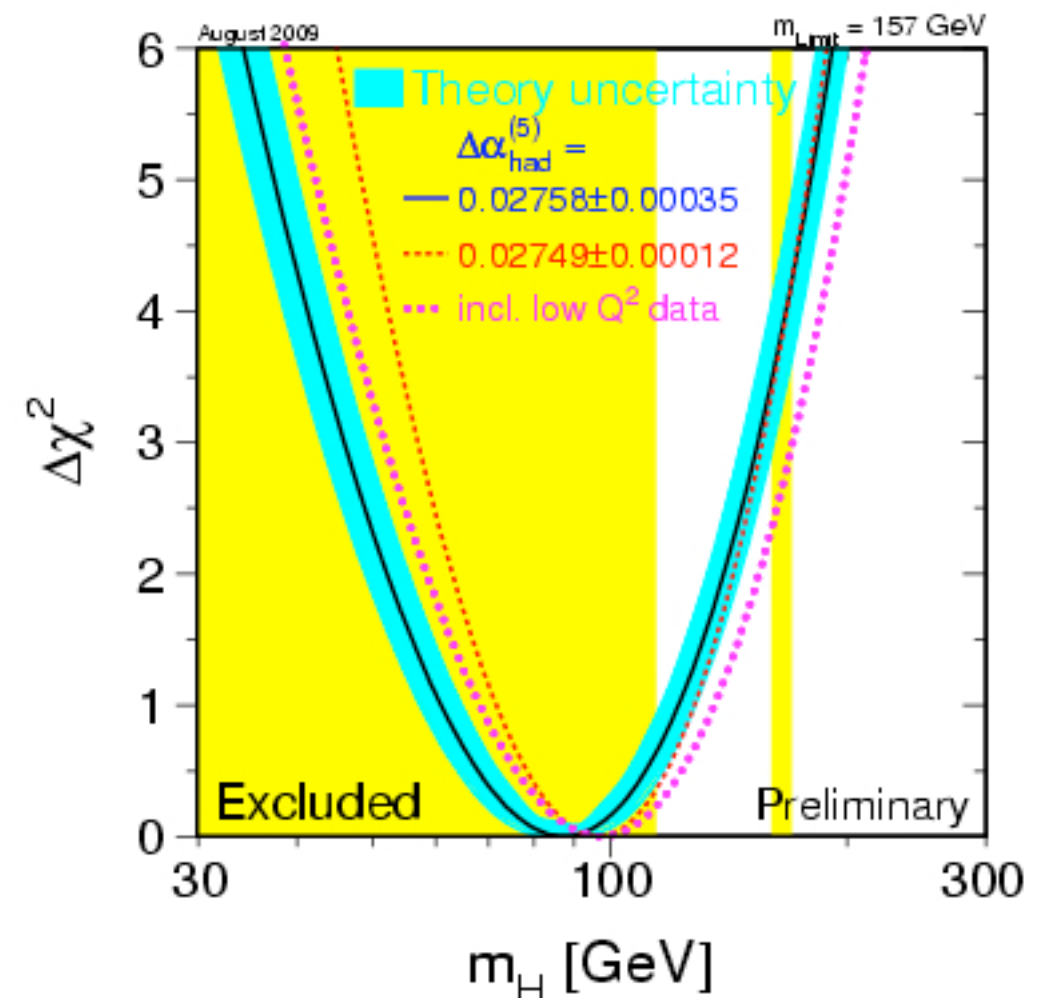
$$m_H < 157 \text{ GeV at 95 \% CL}$$

LEP EWWG, summer 2009

Taking into account LEP limit:

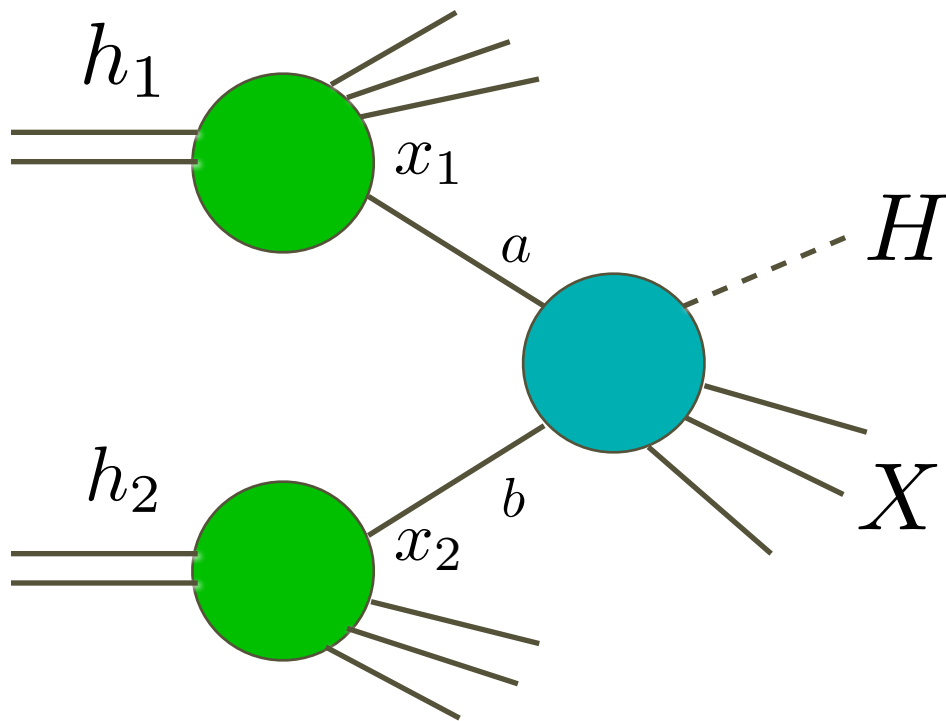
$$m_H < 186 \text{ GeV at 95 \% CL}$$

.... but screening effect: the
dependence is only logarithmic at
one loop (for top quark the
dependence is quadratic →
 m_{top} predicted before discovery !)



Theoretical predictions at hadron colliders

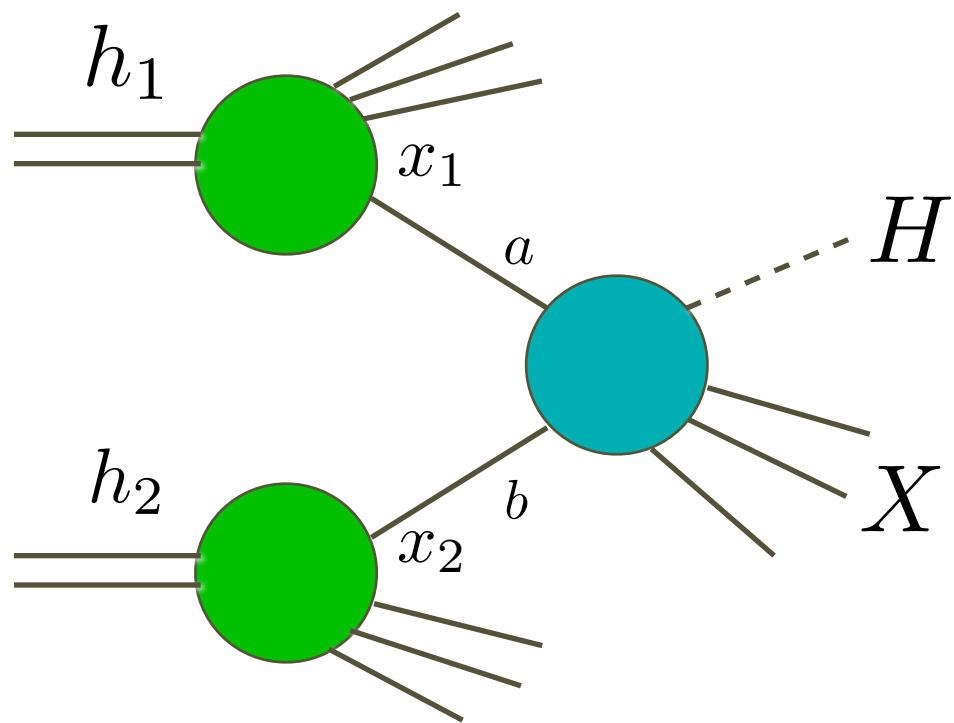
The framework: QCD factorization theorem



$$\sigma(p_1, p_2; M_H) = \sum_{a,b} \int_0^1 dx_1 dx_2 f_{h_1,a}(x_1, \mu_F^2) f_{h_2,b}(x_2, \mu_F^2) \times \hat{\sigma}_{ab}(x_1 p_1, x_2 p_2, \alpha_S(\mu_R^2); \mu_F^2)$$

Theoretical predictions at hadron colliders

The framework: QCD factorization theorem

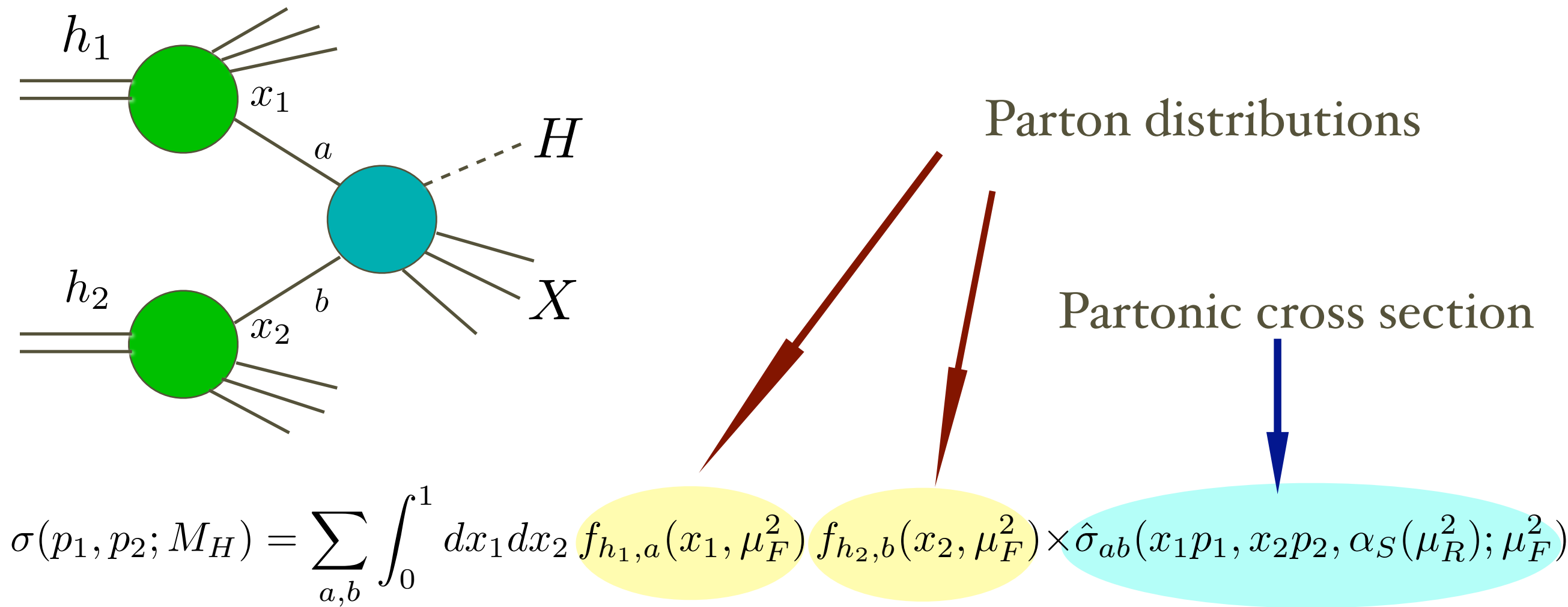


Parton distributions

$$\sigma(p_1, p_2; M_H) = \sum_{a,b} \int_0^1 dx_1 dx_2 f_{h_1,a}(x_1, \mu_F^2) f_{h_2,b}(x_2, \mu_F^2) \times \hat{\sigma}_{ab}(x_1 p_1, x_2 p_2, \alpha_S(\mu_R^2); \mu_F^2)$$

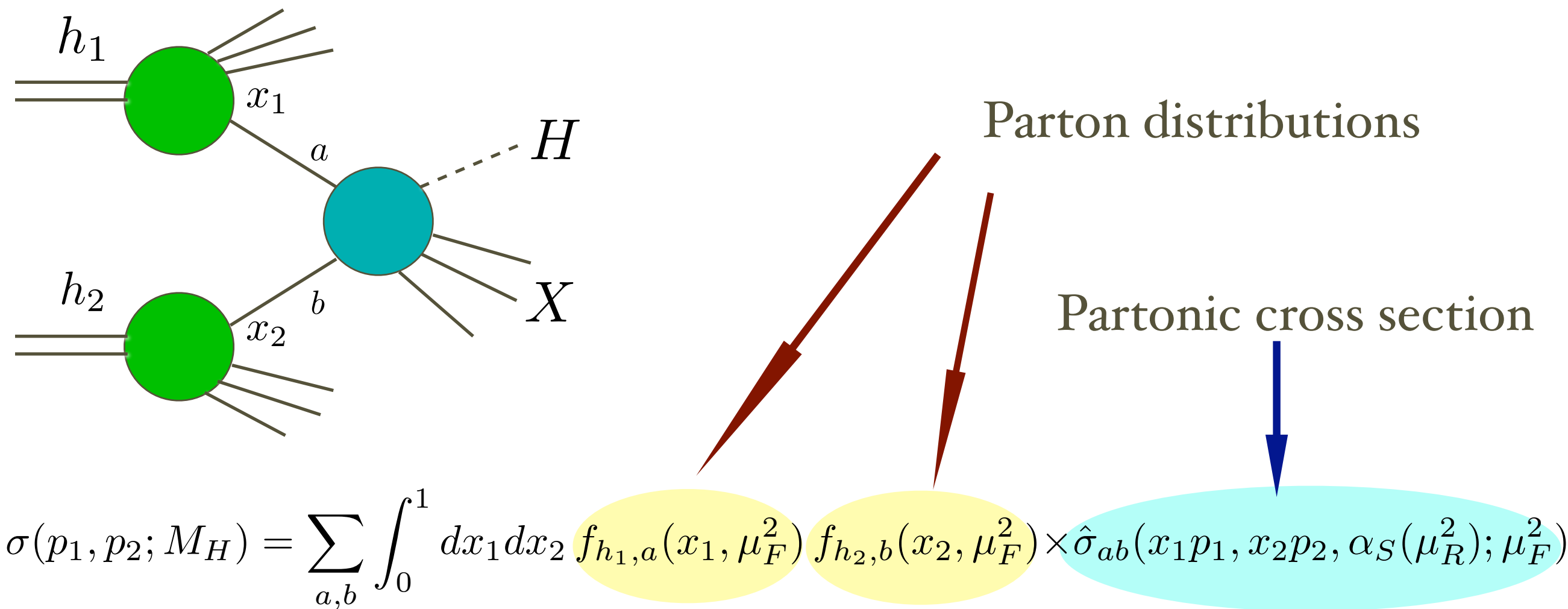
Theoretical predictions at hadron colliders

The framework: QCD factorization theorem



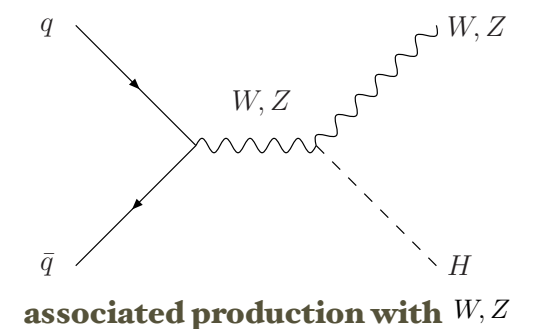
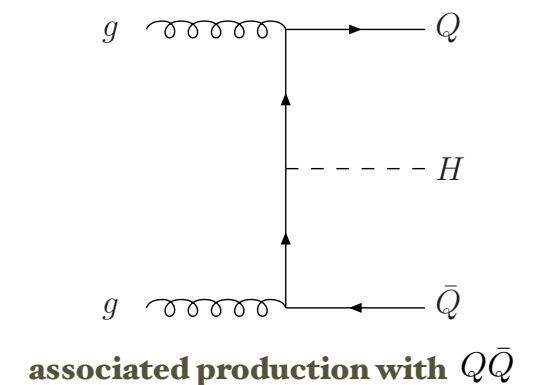
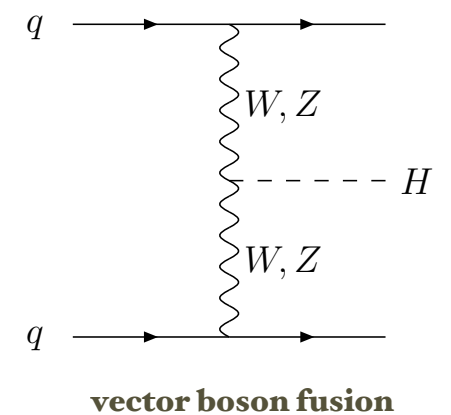
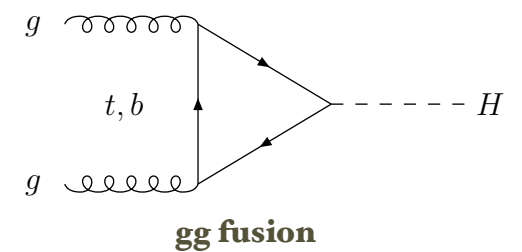
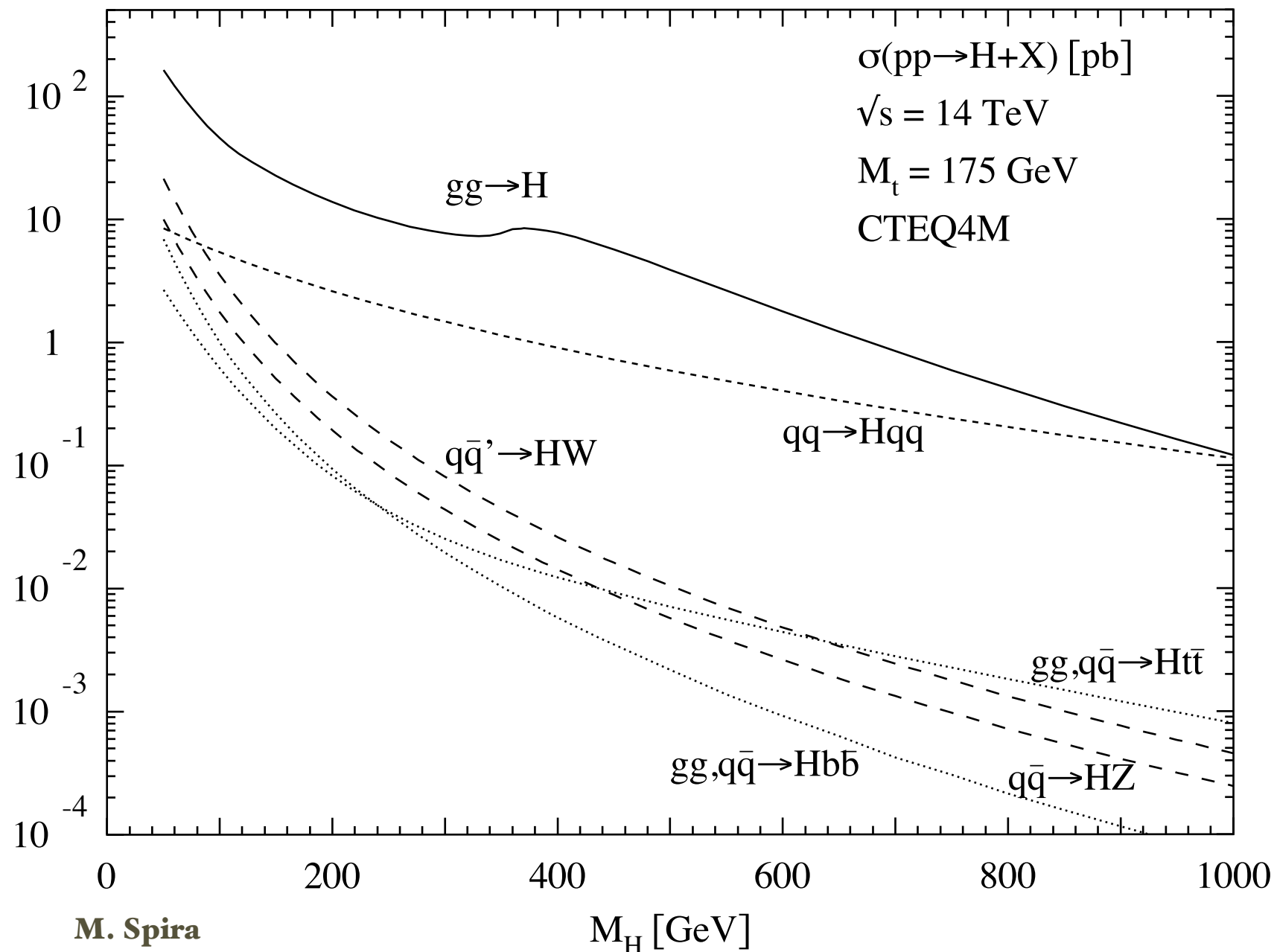
Theoretical predictions at hadron colliders

The framework: QCD factorization theorem



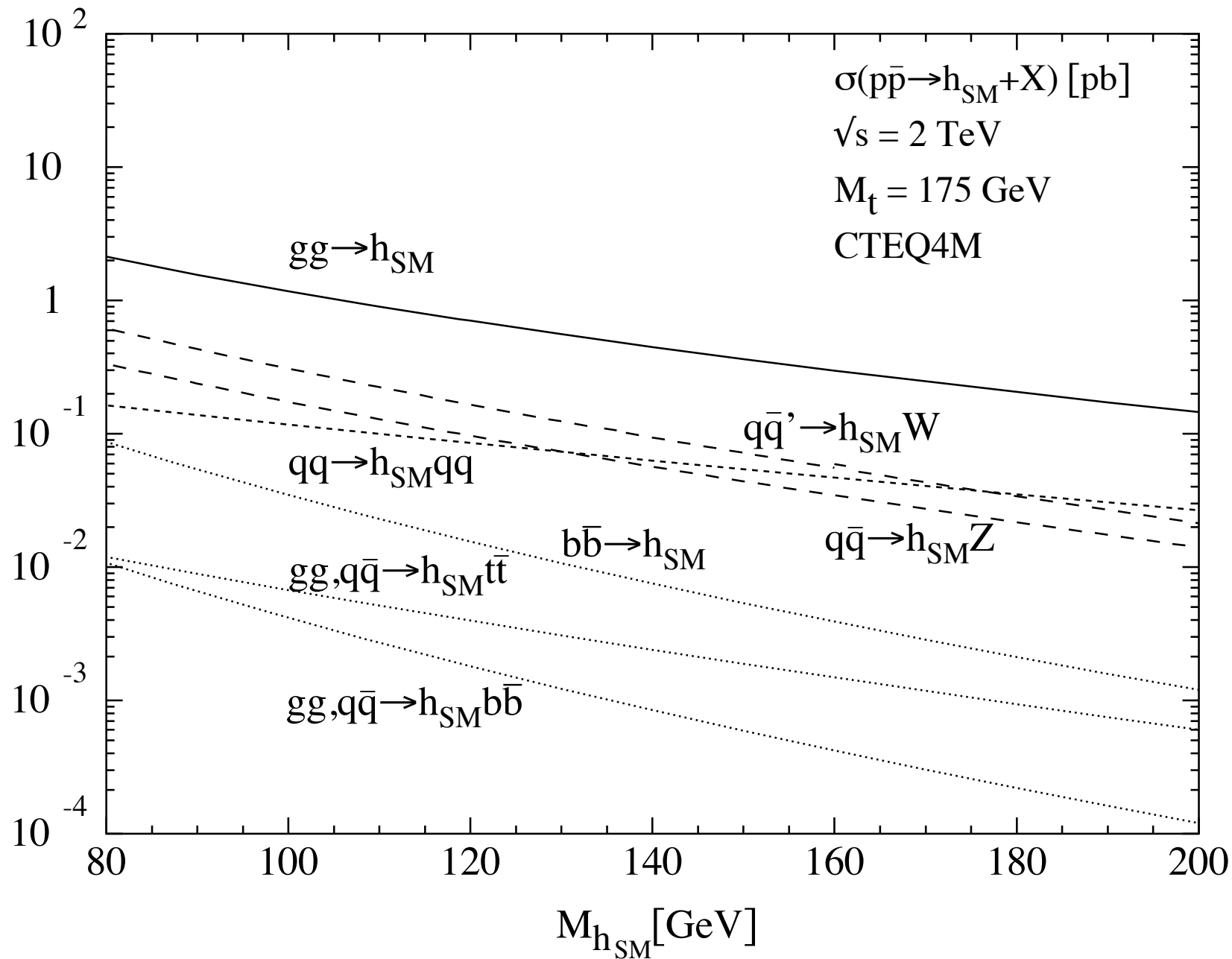
Precise predictions for σ depend on good knowledge of
BOTH $\hat{\sigma}_{ab}$ and $f_{h,a}(x, \mu_F^2)$

Higgs production at hadron colliders



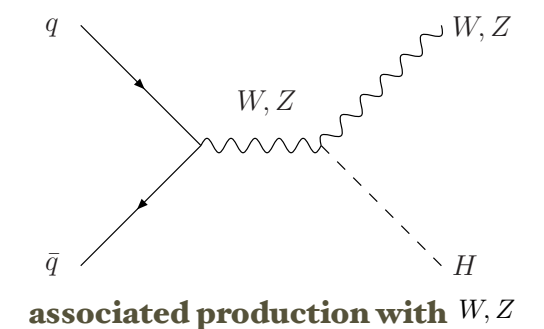
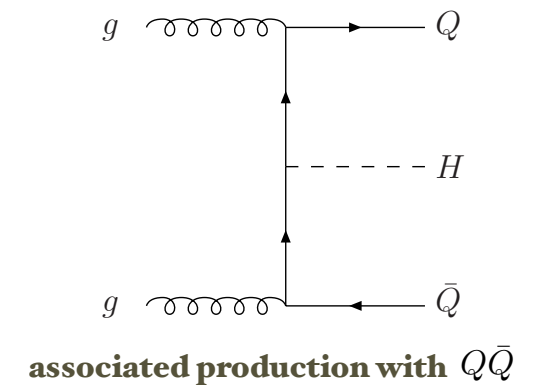
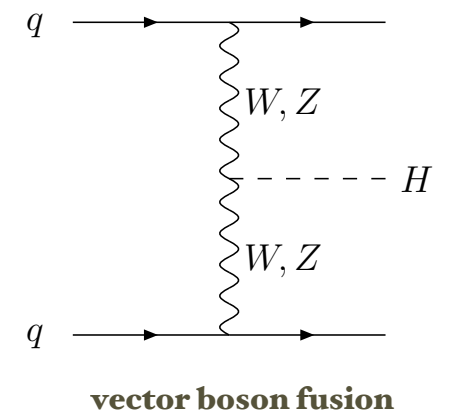
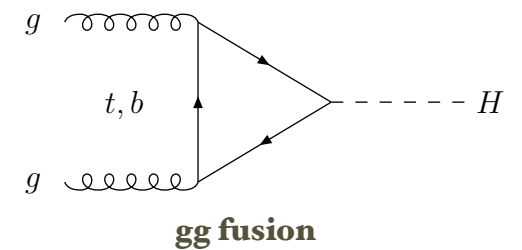
Large gluon luminosity  gg fusion is the dominant production channel over the whole range of m_H

Higgs production at hadron colliders

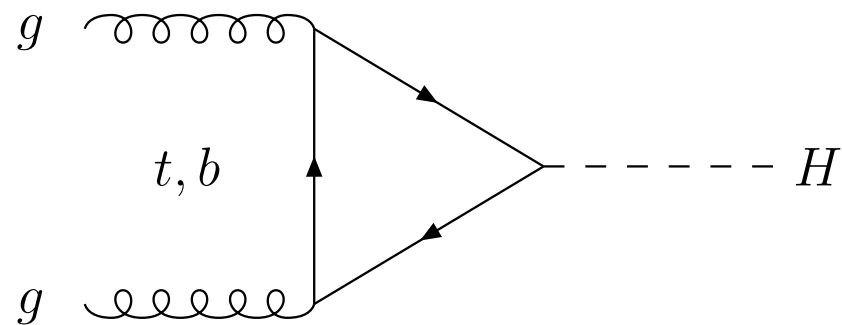


M. Spira

Similar situation at the Tevatron
(although gg dominance less pronounced)



gg fusion



The Higgs coupling is proportional to the quark mass

→ top-loop dominates

It is a one-loop process already at Born level

→ calculation of higher order corrections is very difficult

NLO QCD corrections to the total rate computed already 20 years ago and found to be large

They increase the LO result by about **80-100 %** !


A. Djouadi, D. Graudenz,
M. Spira, P. Zerwas (1991)

They are well approximated by the large- m_{top} limit

S.Dawson (1991)
M.Kramer, E. Laenen, M.Spira(1998)

$gg \rightarrow H$ at NNLO

NLO corrections are well approximated by the large- m_{top} limit

This is not accidental: the bulk of the effect comes from virtual and real radiation at relatively low transverse momenta: weakly sensitive to the top loop  **reason: steepness of the gluon density at small x**

NNLO corrections computed in the large- m_{top} limit

Dominance of soft-virtual effects persists at NNLO


R. Harlander (2000)

S. Catani, D. De Florian, MG (2001)

R. Harlander, W.B. Kilgore (2001, 2002)

C. Anastasiou, K. Melnikov (2002)

V. Ravindran, J. Smith, W.L. Van Neerven (2003)

 This is good because the effects of very hard radiation are precisely those that are not accounted properly by the large- m_{top} approximation

The large- m_{top} approximation

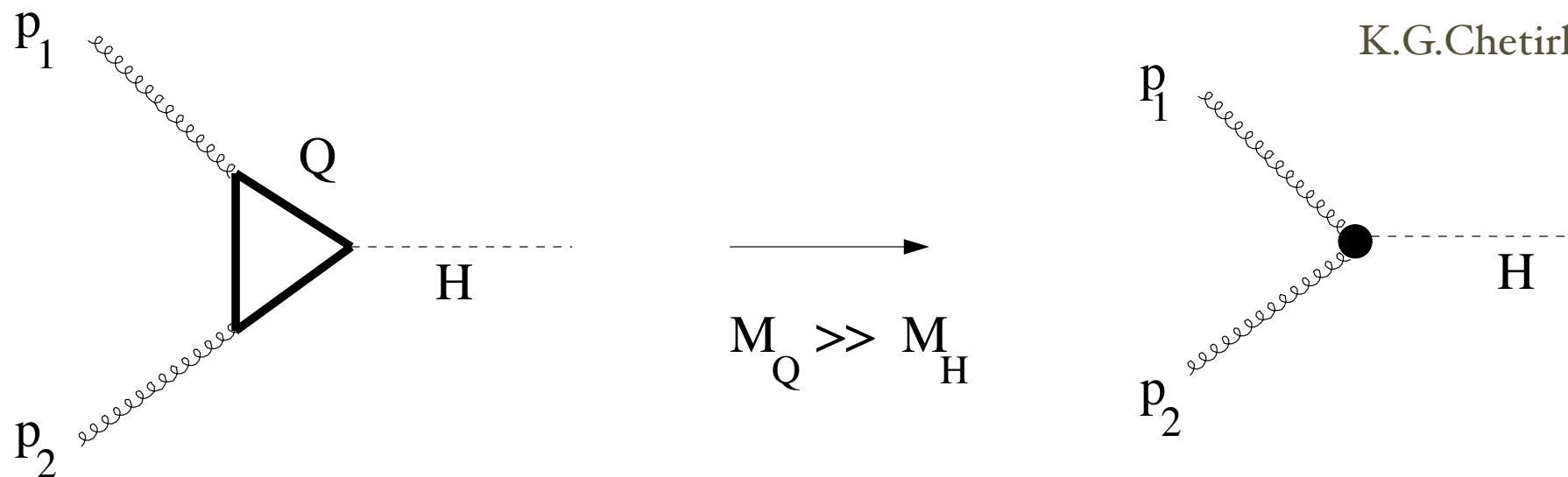
For a light Higgs it is possible to use an effective lagrangian approach obtained when $m_{\text{top}} \rightarrow \infty$

J.Ellis, M.K.Gaillard, D.V.Nanopoulos (1976)
M.Voloshin, V.Zakharov, M.Shifman (1979)

$$\mathcal{L}_{eff} = -\frac{1}{4} \left[1 - \frac{\alpha_S}{3\pi} \frac{H}{v} (1 + \Delta) \right] \text{Tr } G_{\mu\nu} G^{\mu\nu}$$

Known to $\mathcal{O}(\alpha_S^3)$

K.G.Chetirkin, M.Steinhauser, B.A.Kniehl (1997)



**Effective vertex:
one loop less !**

Recently the subleading terms in large- m_{top} limit at NNLO have been evaluated

R.Harlander, K.Ozeren (2009),
M.Steinhauser et al. (2009)

➡ **The approximation works to better than 0.5 % for $m_H < 300 \text{ GeV}$**

Soft-gluon resummation

S.Catani, D. de Florian, P.Nason, MG (2003)

Soft-virtual effects are important

 **All-order resummation of soft-gluon effects provides a way to improve our perturbative predictions**

Soft-virtual effects are logarithmically enhanced at $z = m_H^2 / \hat{s} \rightarrow 1$

 Partonic CM energy

The dominant behaviour can be organized in an all order resummed formula

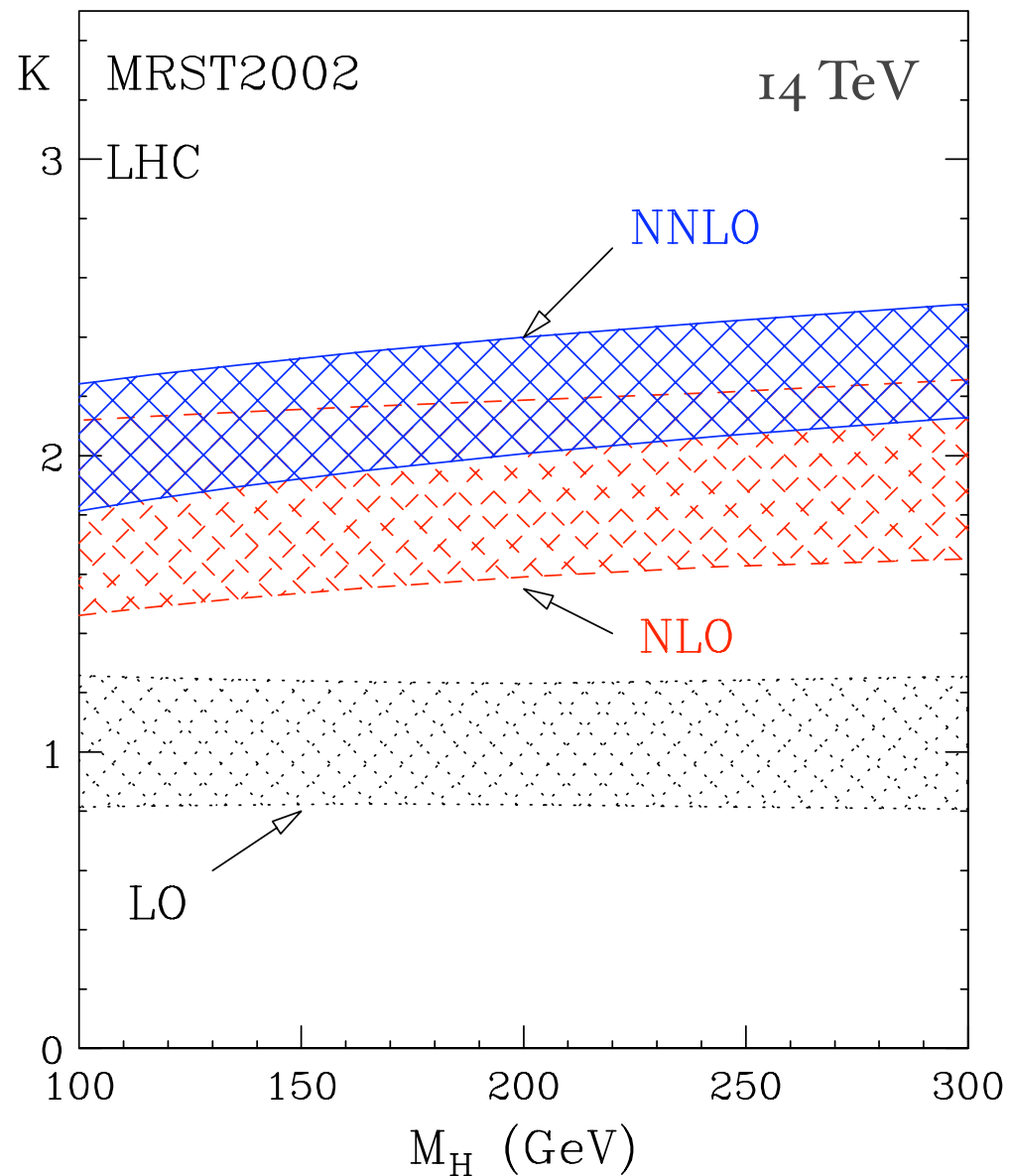
Resummation works in Mellin space $L = \ln N$

$$\sigma^{\text{res}} \sim C(\alpha_S) \exp\{Lg_1(\alpha_S L) + g_2(\alpha_S L) + \alpha_S g_3(\alpha_S L) + \dots\}$$

We can perform the resummation up to NNLL+NNLO accuracy

This means that we include the full NNLO result plus all-order resummation of the logarithmically enhanced terms  No information is lost

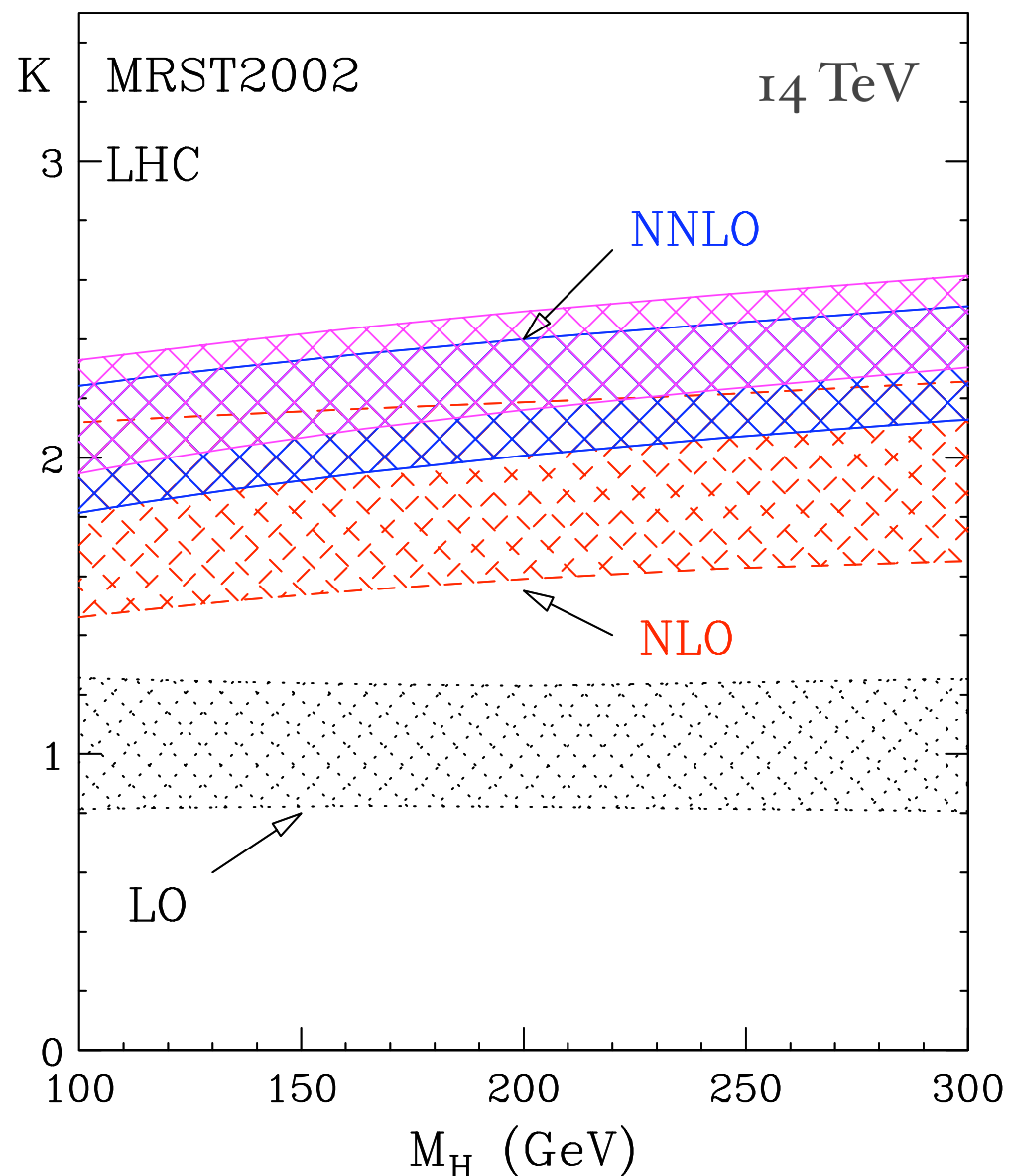
Inclusive results at the LHC



For a light Higgs:
NNLO effect +15 – 20 %

- K-factors defined with respect $\sigma_{LO}(\mu_F = \mu_R = M_H)$
- With $\mu_{F(R)} = \chi_{L(R)} M_H$ and $0.5 \leq \chi_{L(R)} \leq 2$ but $0.5 \leq \chi_F / \chi_R \leq 2$

Inclusive results at the LHC



Inclusion of soft-gluon effects at all orders

S. Catani, D. De Florian,
P. Nason, MG (2003)

For a light Higgs:
NNLO effect +15 – 20 %

NNLL effect + 6%

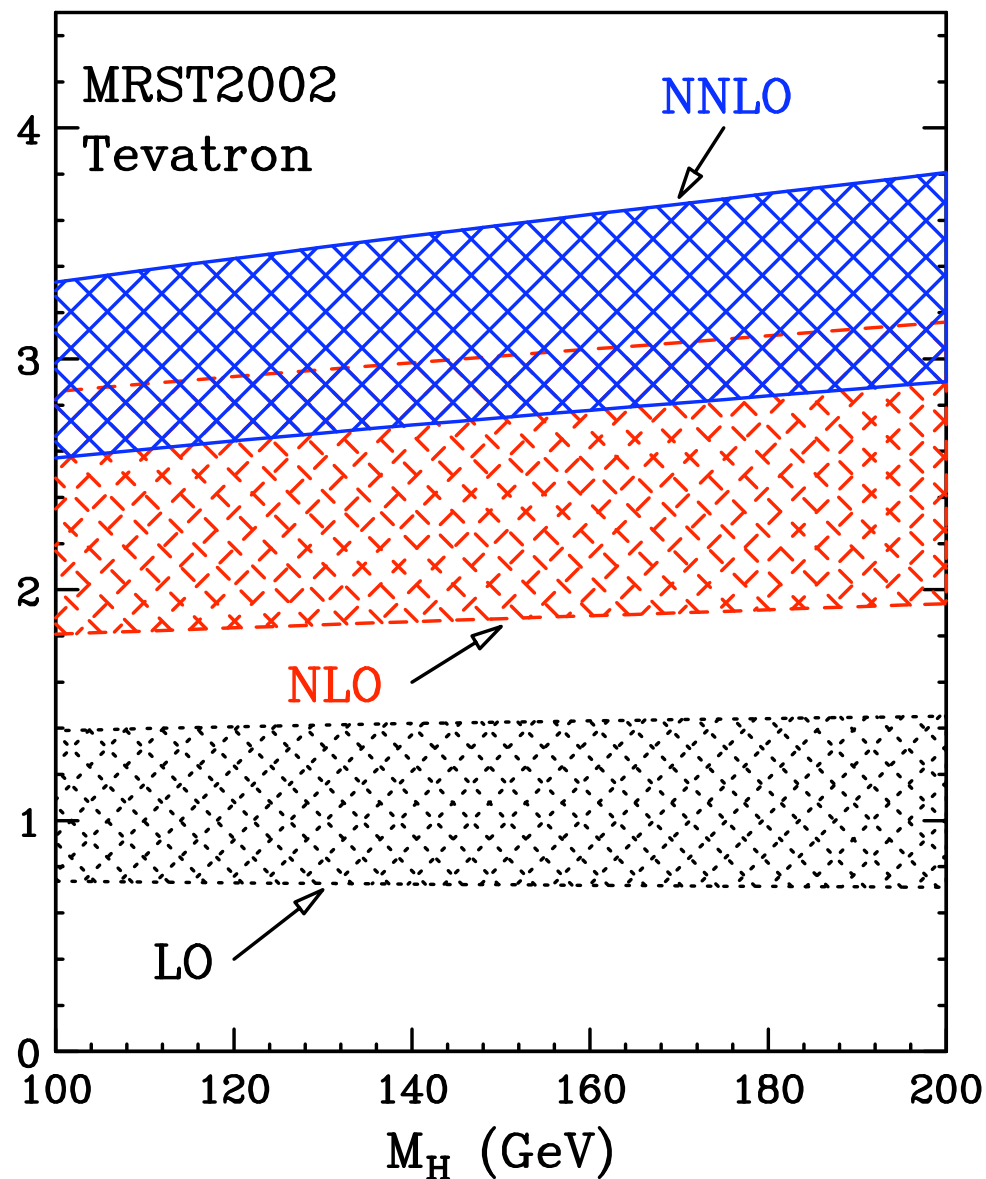
Good stability of
perturbative result

Nicely confirmed by computation of soft
terms at $N^3\text{LO}$

S. Moch, A. Vogt (2005),
E. Laenen, L. Magnea (2005)

- K-factors defined with respect $\sigma_{LO}(\mu_F = \mu_R = M_H)$
- With $\mu_{F(R)} = \chi_{L(R)} M_H$ and $0.5 \leq \chi_{L(R)} \leq 2$ but $0.5 \leq \chi_F / \chi_R \leq 2$

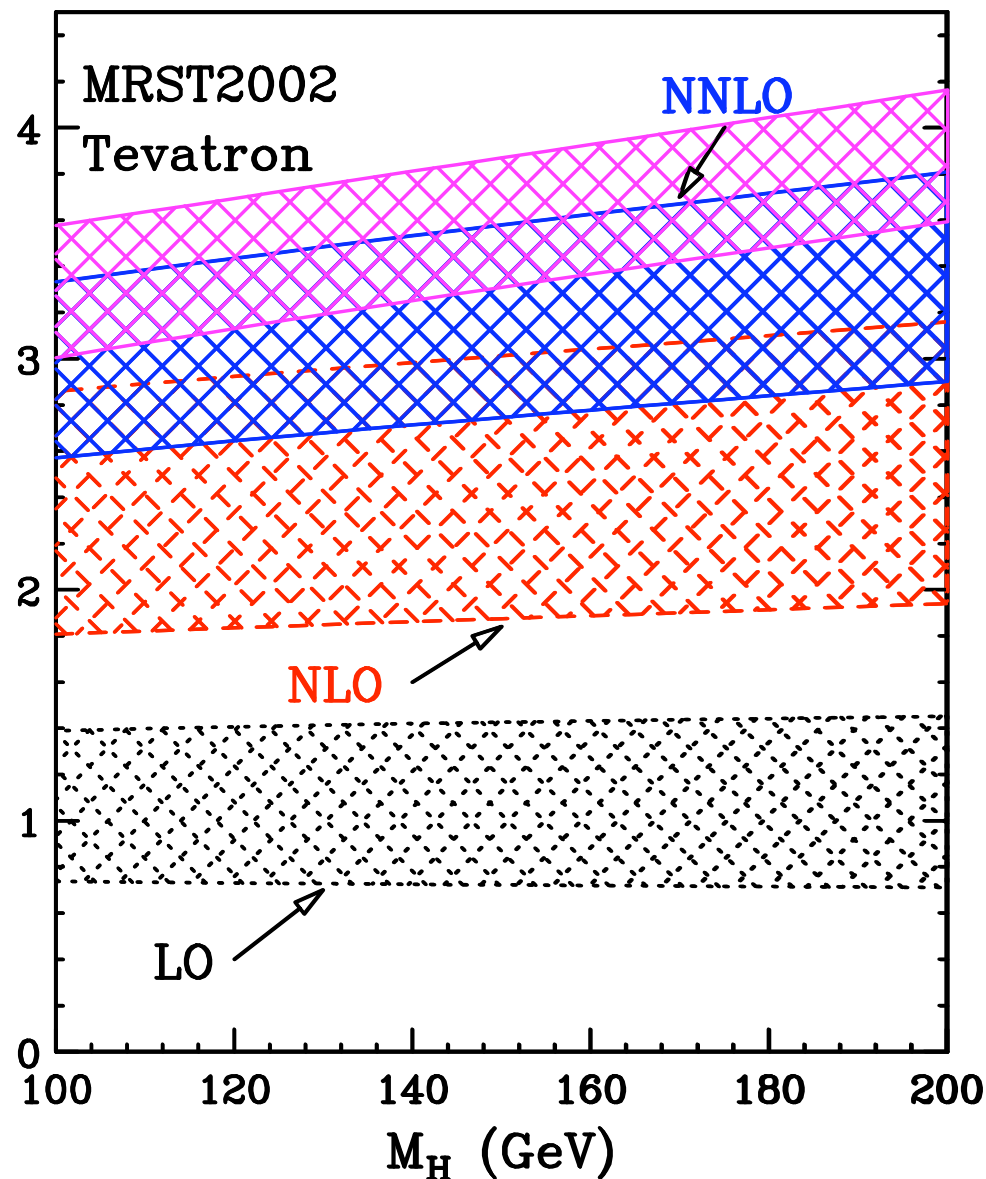
Inclusive results at the Tevatron



For a light Higgs:
NNLO effect +40%

- K-factors defined with respect $\sigma_{LO}(\mu_F = \mu_R = M_H)$
- With $\mu_{F(R)} = \chi_{L(R)} M_H$ and $0.5 \leq \chi_{L(R)} \leq 2$ but $0.5 \leq \chi_F / \chi_R \leq 2$

Inclusive results at the Tevatron



Inclusion of soft-gluon effects at all orders

S. Catani, D. De Florian,
P. Nason, MG (2003)

For a light Higgs:
NNLO effect +40%

NNLL effect +12 – 15%

Impact of higher order
effects larger than at LHC

- K-factors defined with respect $\sigma_{LO}(\mu_F = \mu_R = M_H)$
- With $\mu_{F(R)} = \chi_{L(R)} M_H$ and $0.5 \leq \chi_{L(R)} \leq 2$ but $0.5 \leq \chi_F / \chi_R \leq 2$

Tevatron Higgs search

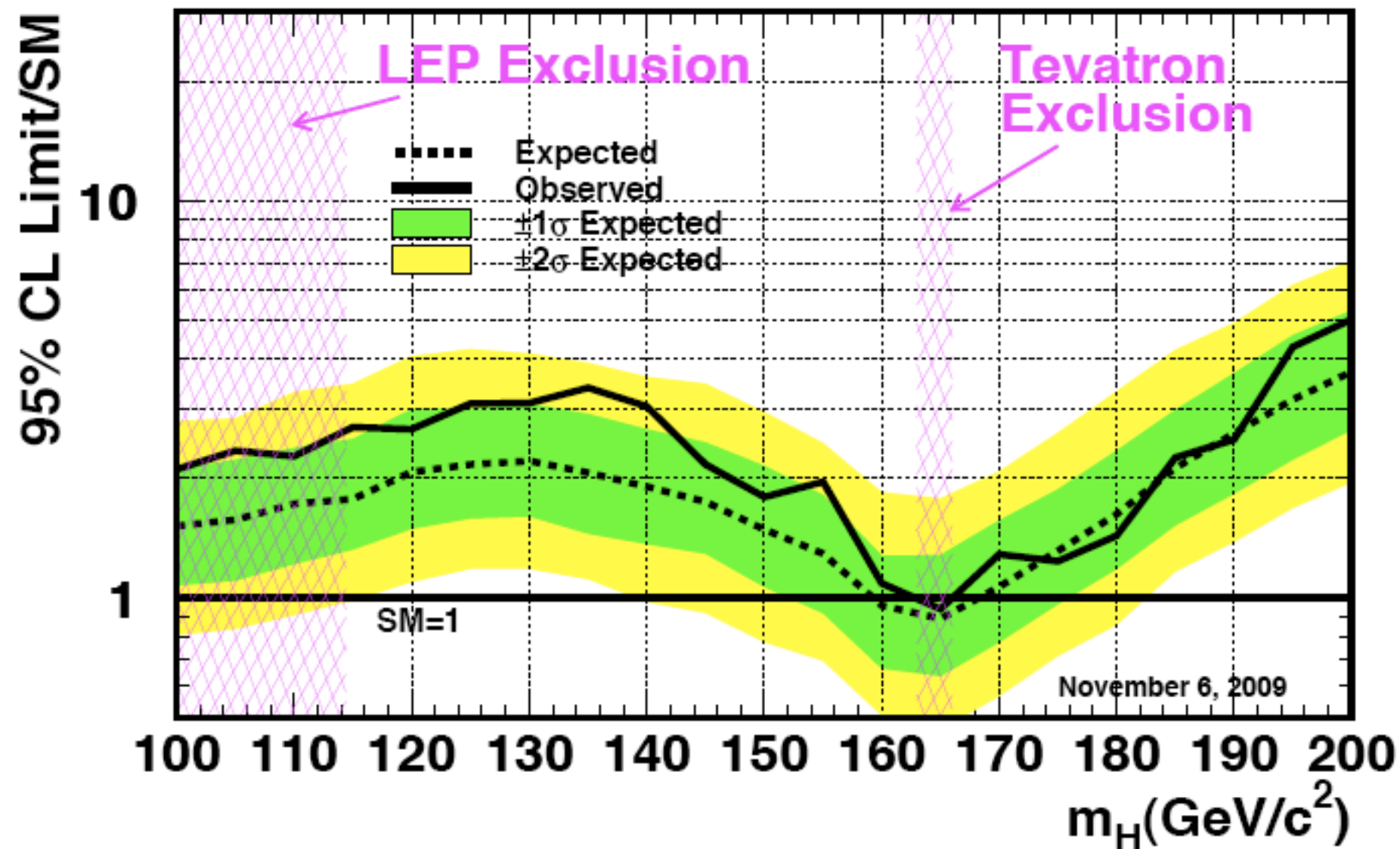
Latest results presented up to $L=5.4 \text{ fb}^{-1}$

Expressed in terms of $R=95\%$ CL limits/SM



Now sensitive to the region $m_H \approx 160-170 \text{ GeV}$

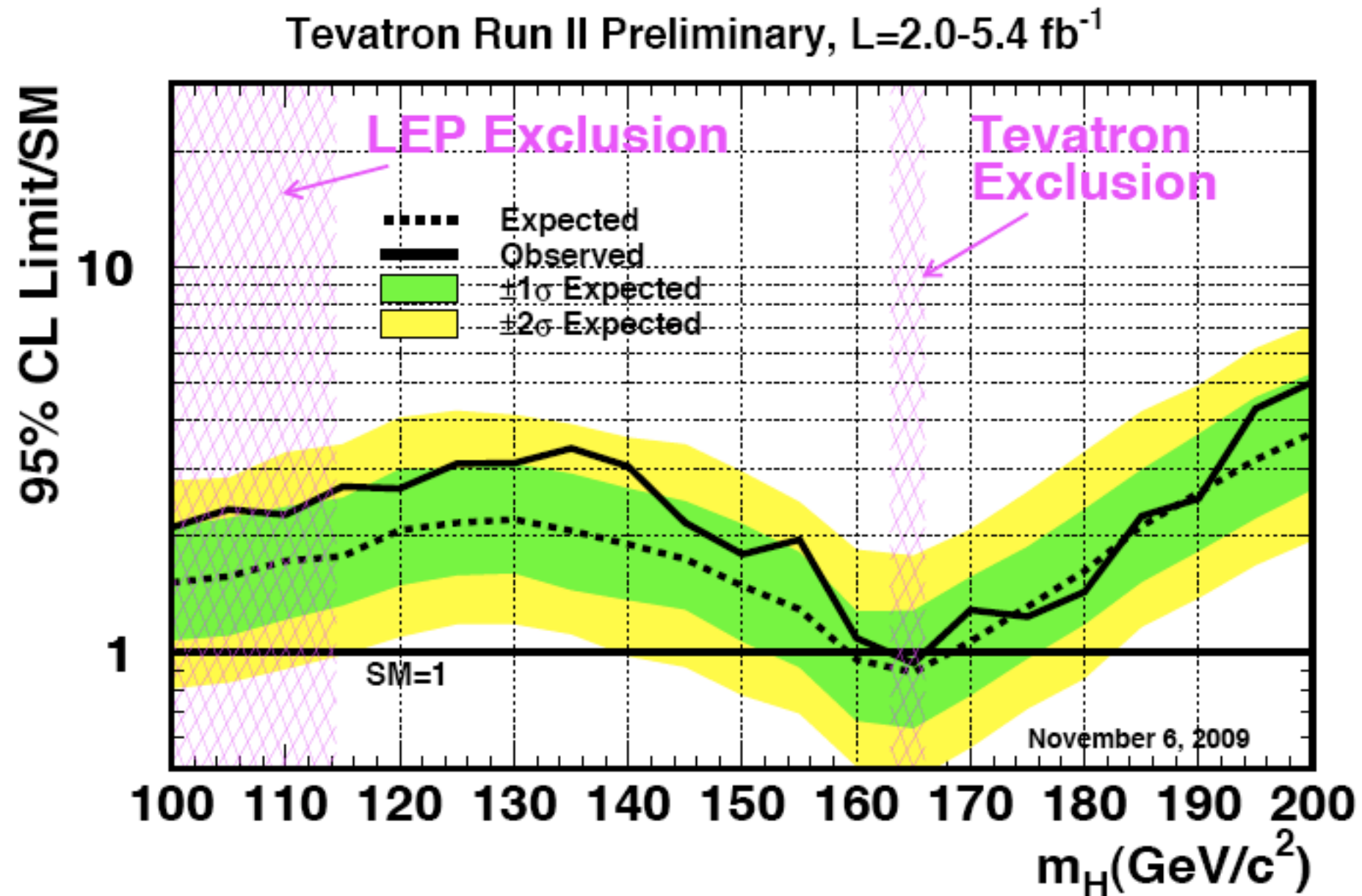
Tevatron Run II Preliminary, $L=2.0-5.4 \text{ fb}^{-1}$



The relevance of higher orders

The recent Tevatron exclusion is based on our recent (updated) result

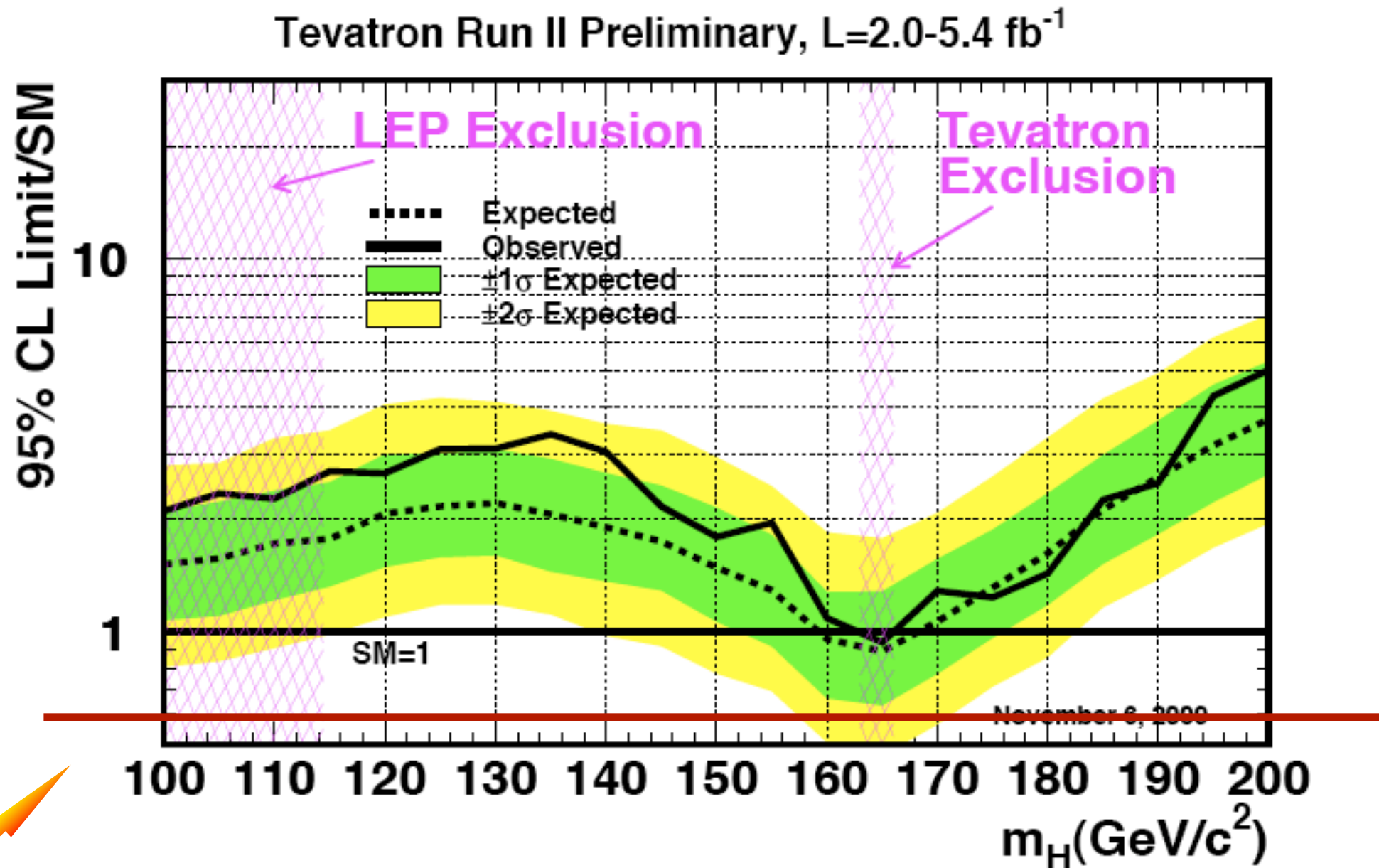
D. De Florian, MG (2009)



The relevance of higher orders

The recent Tevatron exclusion is based on our recent (updated) result

D. De Florian, MG (2009)

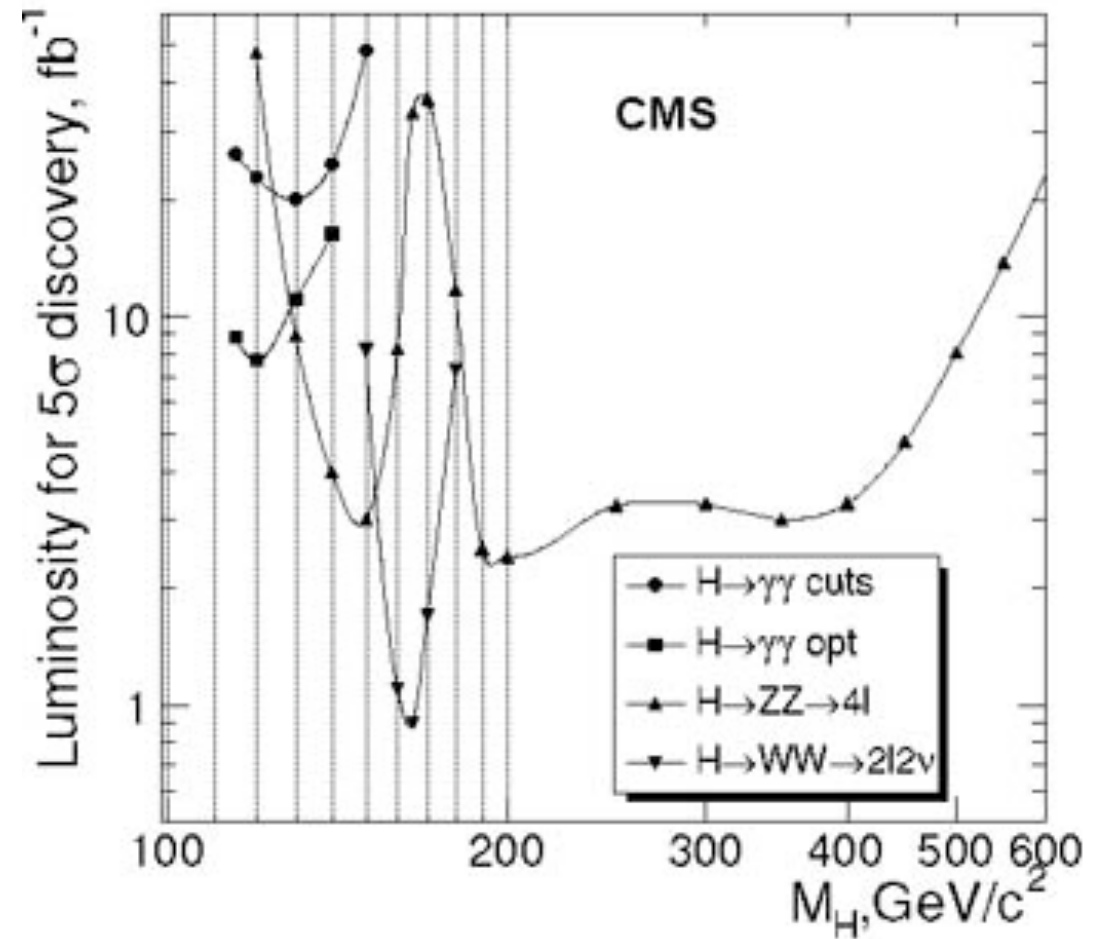
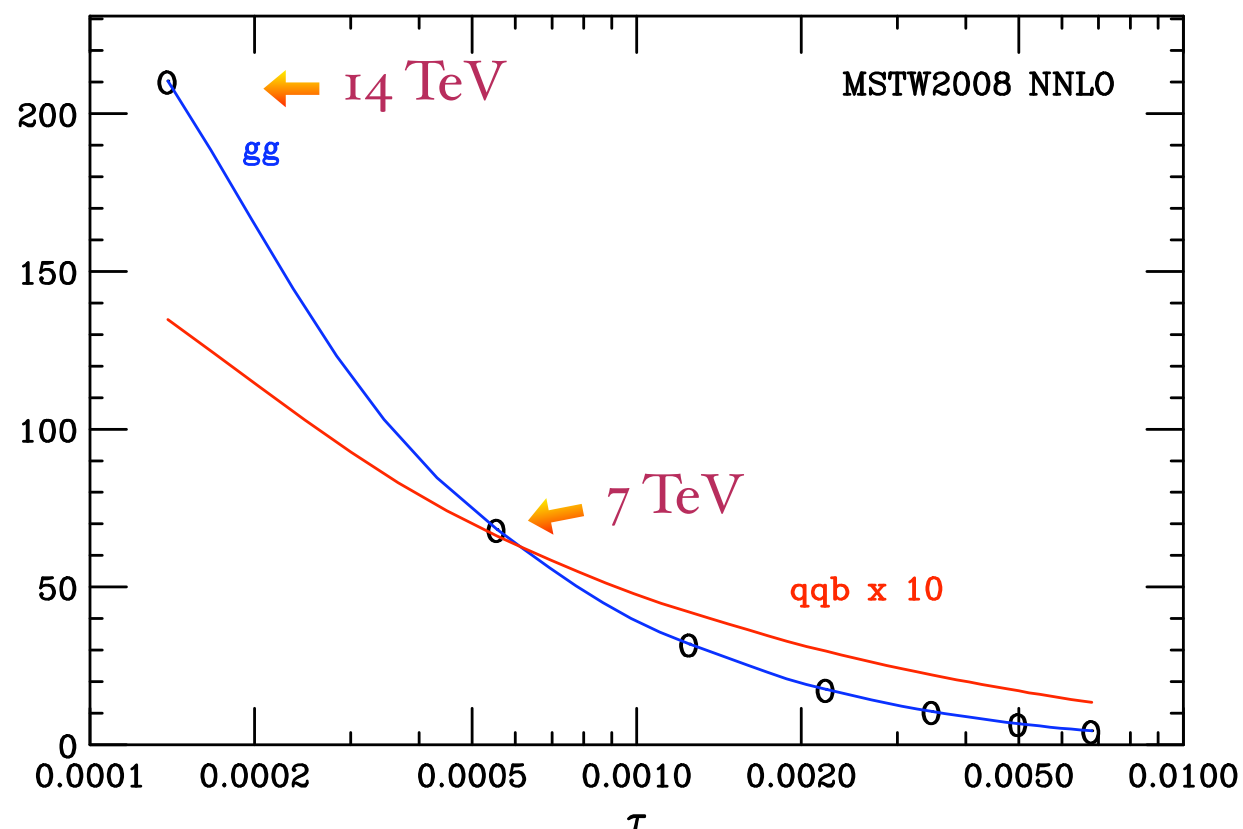


This would be the situation if the NLO result had been used !

LHC @ 7 TeV

At 14 TeV a SM Higgs boson with $m_H \sim 160$ GeV can be discovered with about 1 fb^{-1}

From 14 to 7 TeV both signal and background cross sections decrease



But gg parton luminosity drops faster

$$\mathcal{L}_{c\bar{c}}(\tau, \mu_F^2) = \int_{\tau}^1 \frac{dx}{x} f_c(x, \mu_F^2) f_{\bar{c}}(\tau/x, \mu_F^2)$$

Recent NLO study shows that luminosity needed for discovery may be a factor 6-7 larger

E.Berger et al. (2010)

Total cross section is thus OK but....more exclusive observables are needed !

At LO we don't find problems: compute the corresponding matrix element and integrate it numerically over the multiparton phase-space

Beyond LO the computation is affected by **infrared singularities**

Although these singularities cancel between real and virtual contributions, they prevent a straightforward implementation of numerical techniques

At NLO the problem is solved: general methods exist that allow to handle and cancel infrared singularities

W.Giele, N.Glover (1992)

W.Giele, N.Glover, D.Kosower (1993)

S. Frixione, Z.Kunszt, A.Signer (1996)

S.Catani, M.Seymour (1997)

At NNLO, only few fully exclusive computations exist, due to their substantial technical complications

C.Anastasiou et al. (2004,2005)

K.Melnikov, F.Petriello (2006)

S.Catani, MG (2007)

L.Cieri et al . (2009)

Fortunately the NNLO computation is now implemented at fully exclusive level

FEHIP: Based on sector decomposition: computes NNLO corrections for $H \rightarrow \gamma\gamma$ and $H \rightarrow WW \rightarrow l\nu l\nu$

C. Anastasiou,
K. Melnikov, F. Petrello (2005)

HNNLO: Parton level Monte Carlo program that computes NNLO corrections for $H \rightarrow \gamma\gamma$
 $H \rightarrow WW \rightarrow l\nu l\nu$ and $H \rightarrow ZZ \rightarrow 4l$

S. Catani, MG (2007)
MG (2008)

With these programs it is possible to study the impact of higher order corrections with the cuts used in the experimental analysis

Important to assess theoretical uncertainties in the experimental search

The program: HNNLO implements three decay channels

- $H \rightarrow \gamma\gamma$ (higgsdec = 1)
 - $H \rightarrow WW \rightarrow l\nu l\nu$ (higgsdec = 2)
 - $H \rightarrow ZZ \rightarrow 4l$
 - $H \rightarrow e^+e^-\mu^+\mu^-$ (higgsdec = 31)
 - $H \rightarrow e^+e^-e^+e^-$ (higgsdec = 32)
- ➡ includes appropriate interference contribution

The user can choose the cuts and plot the required distributions by modifying the appropriate user subroutines

Now being used by Tevatron and LHC collaborations

Results: $gg \rightarrow H \rightarrow WW \rightarrow l\nu l\nu$

MG (2007)

see also C. Anastasiou, G. Dissertori, F. Stockli (2007)

$$p_T^{\min} > 25 \text{ GeV} \quad m_{ll} < 35 \text{ GeV} \quad \Delta\phi < 45^\circ$$

$$35 \text{ GeV} < p_T^{\max} < 50 \text{ GeV} \quad |y_l| < 2 \quad p_T^{\text{miss}} > 20 \text{ GeV} \quad \text{cuts as in Davatz et al. (2003)}$$

Results for

$$p_T^{\text{veto}} = 30 \text{ GeV}$$

σ (fb)	LO	NLO	NNLO
$\mu_F = \mu_R = M_H/2$	17.36 ± 0.02	18.11 ± 0.08	15.70 ± 0.32
$\mu_F = \mu_R = M_H$	14.39 ± 0.02	17.07 ± 0.06	15.99 ± 0.23
$\mu_F = \mu_R = 2M_H$	12.00 ± 0.02	15.94 ± 0.05	15.68 ± 0.20

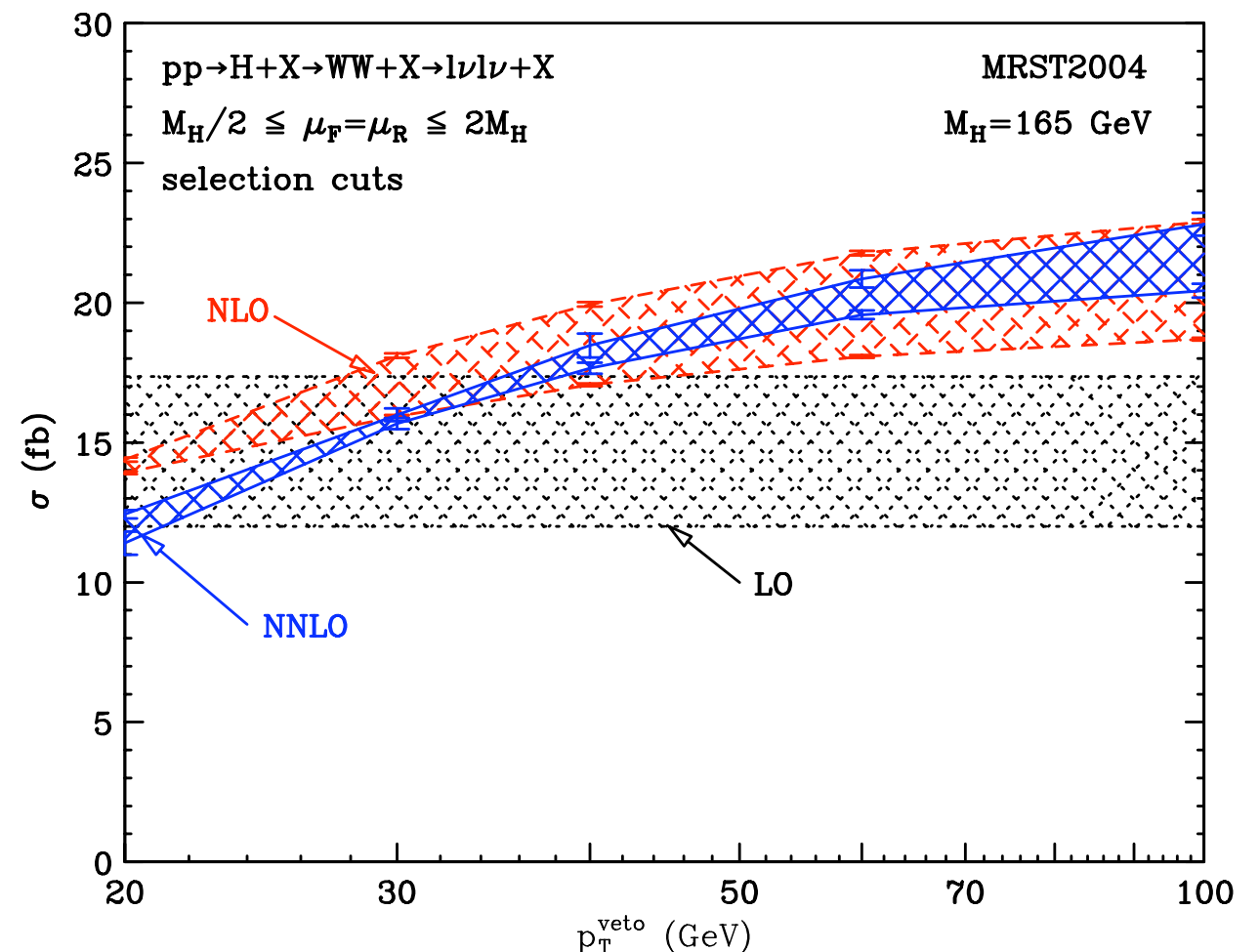
➔ **Impact of higher order corrections strongly reduced by selection cuts**

The NNLO band overlaps with the NLO one for $p_T^{\text{veto}} \gtrsim 30 \text{ GeV}$

The bands do not overlap for $p_T^{\text{veto}} \lesssim 30 \text{ GeV}$

NNLO efficiencies found in good agreement with MC@NLO

Anastasiou et al. (2008)



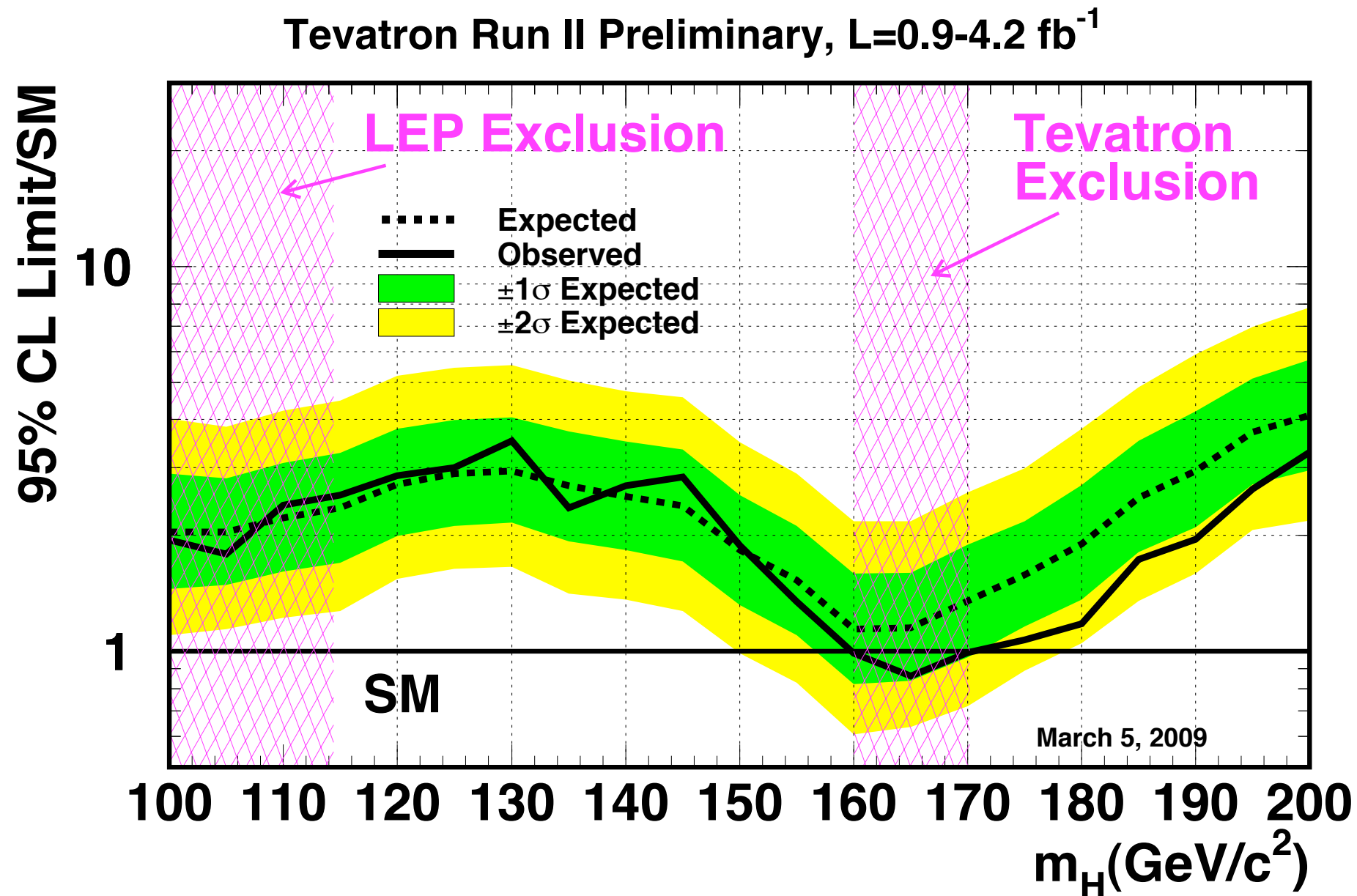
Summary

- Gluon-gluon fusion is the dominant production channel for the SM Higgs boson at hadron colliders for a wide range of m_H
- It is probably also the channel that provides the only possibility to observe or exclude the Higgs in the near future
- A great work has been done to improve the accuracy of the theoretical prediction that is now known at NNLO with all-order resummation of soft-gluon contributions (plus EW corrections)
 - ➔ crucial effect on overall normalization
- NNLO computation now implemented at fully exclusive level
 - ➔ important to assess theoretical uncertainties in the experimental search

BACKUP SLIDES

Tevatron results

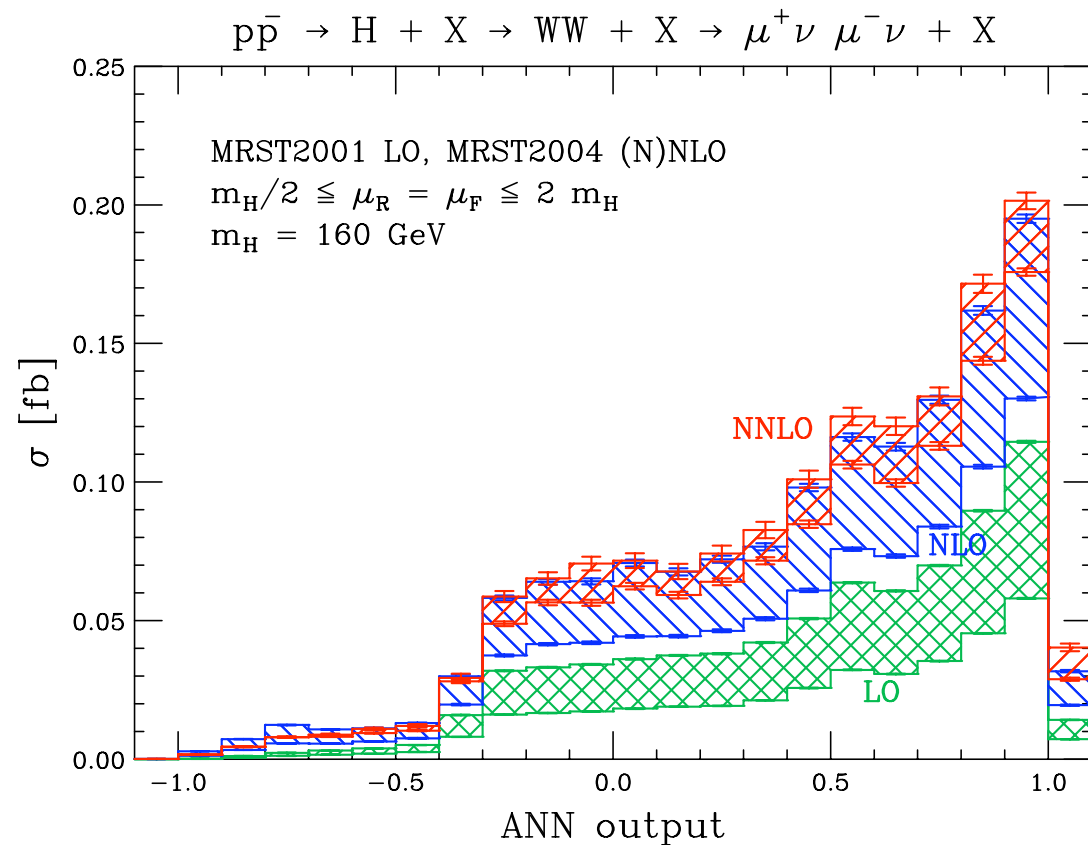
Results with up to $L=4.2 \text{ fb}^{-1}$



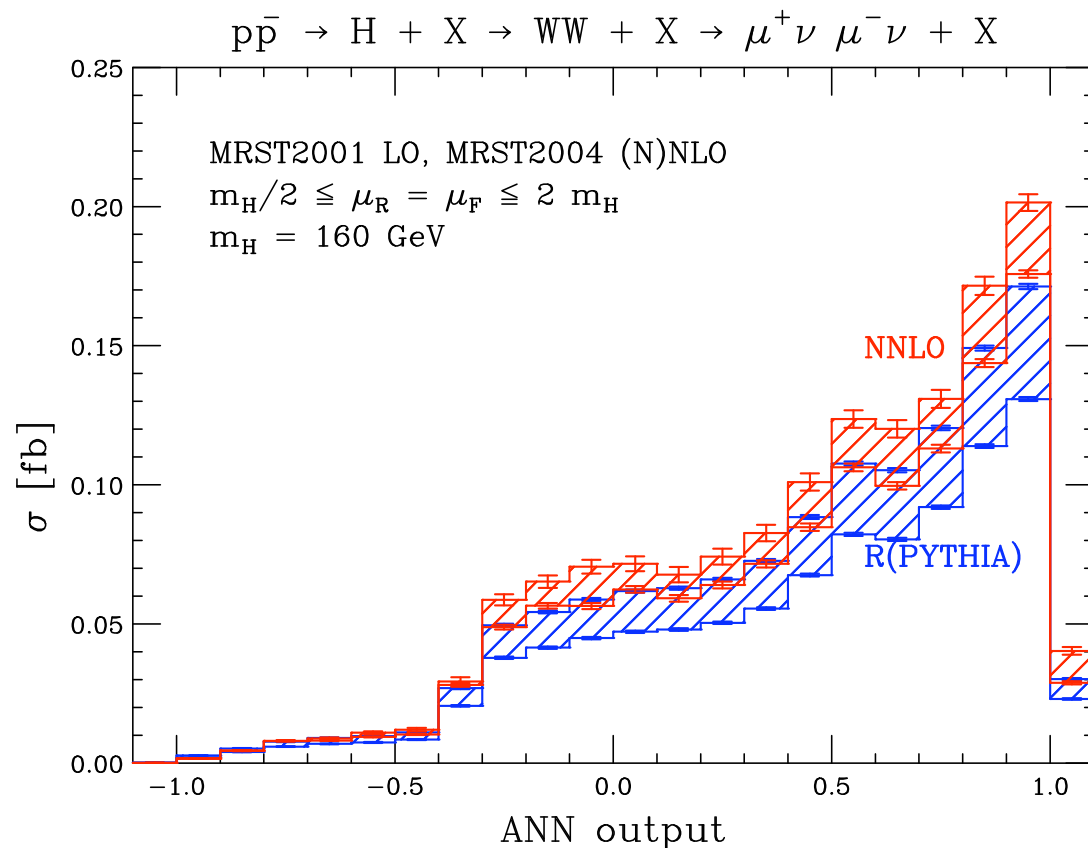
Deficit of events at $m_H \sim 160-170 \text{ GeV}$ gave wider excluded region

When theorists play....

C.Anastasiou,
G.Dissertori,F.Stoeckli,B.Webber, MG



Train a Neural Network with samples
for Higgs, WW and ttbar processes
generated with PYTHIA 8



Study the NN output up to NNLO is as
simple as any other kinematical
distribution !

All the predictions are peaked at ANN~1

A way out: HNNLO

S. Catani, MG (2007)

We propose a new version of the subtraction method to compute higher order QCD corrections to a specific class of processes in hadron collisions (vector boson, Higgs boson production, vector boson pairs.....)

We compute the NNLO corrections to $gg \rightarrow H$ implementing them in a fully exclusive parton level generator including all the relevant decay modes

 encompasses previous calculations in a single stand-alone numerical code
it makes possible to apply arbitrary cuts

Strategy: start from NLO calculation of H+jet(s) and observe that as soon as the transverse momentum of the Higgs $q_T \neq 0$ one can write:

$$d\sigma_{(N)NLO}^H|_{q_T \neq 0} = d\sigma_{(N)LO}^{H+jets}$$

Define a counterterm to deal with singular behaviour at $q_T \rightarrow 0$

But.....

the singular behaviour of $d\sigma_{(N)LO}^{H+\text{jet}(s)}$ is well known from the resummation program of large logarithmic contributions at small transverse momenta

G. Parisi, R. Petronzio (1979)

J. Collins, D.E. Soper, G. Sterman (1985)

S. Catani, D. de Florian, MG (2000)

→ choose $d\sigma^{CT} \sim d\sigma^{(LO)} \otimes \Sigma^H(q_T/Q)$

where
$$\Sigma^H(q_T/Q) \sim \sum_{n=1}^{\infty} \left(\frac{\alpha_S}{\pi}\right)^n \sum_{k=1}^{2n} \Sigma^{H(n;k)} \frac{Q^2}{q_T^2} \ln^{k-1} \frac{Q^2}{q_T^2}$$

But.....

the singular behaviour of $d\sigma_{(N)LO}^{H+\text{jet}(s)}$ is well known from the resummation program of large logarithmic contributions at small transverse momenta

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S. Catani, D. de Florian, MG (2000)

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Then the calculation can be extended to include the $q_T = 0$ contribution:

$$d\sigma_{(N)NLO}^H = \mathcal{H}_{(N)NLO}^H \otimes d\sigma_{LO}^H + [d\sigma_{(N)LO}^{H+\text{jets}} - d\sigma_{(N)LO}^{CT}]$$

where I have subtracted the truncation of the counterterm at (N)LO and added a contribution at $q_T = 0$ to restore the correct normalization

Results: $gg \rightarrow H \rightarrow ZZ \rightarrow e^+e^-e^+e^-$

MG (2007)

Inclusive cross sections:

σ (fb)	LO	NLO	NNLO
$\mu_F = \mu_R = M_H/2$	2.457 ± 0.001	4.387 ± 0.006	4.82 ± 0.03
$\mu_F = \mu_R = M_H$	2.000 ± 0.001	3.738 ± 0.004	4.52 ± 0.02
$\mu_F = \mu_R = 2M_H$	1.642 ± 0.001	3.227 ± 0.003	4.17 ± 0.01

$$K_{NLO} = 1.87$$

$$K_{NNLO} = 2.26$$

Consider the *selection cuts* as in the CMS TDR: $|y| < 2.5$

$$p_{T1} > 30 \text{ GeV} \quad p_{T2} > 25 \text{ GeV} \quad p_{T3} > 15 \text{ GeV} \quad p_{T4} > 7 \text{ GeV}$$

Isolation: total transverse energy in a cone of radius $R=0.2$ around each lepton should fulfill $E_T < 0.05 p_T$

For each e^+e^- pair, find the closest (m_1) and next to closest (m_2) to m_Z

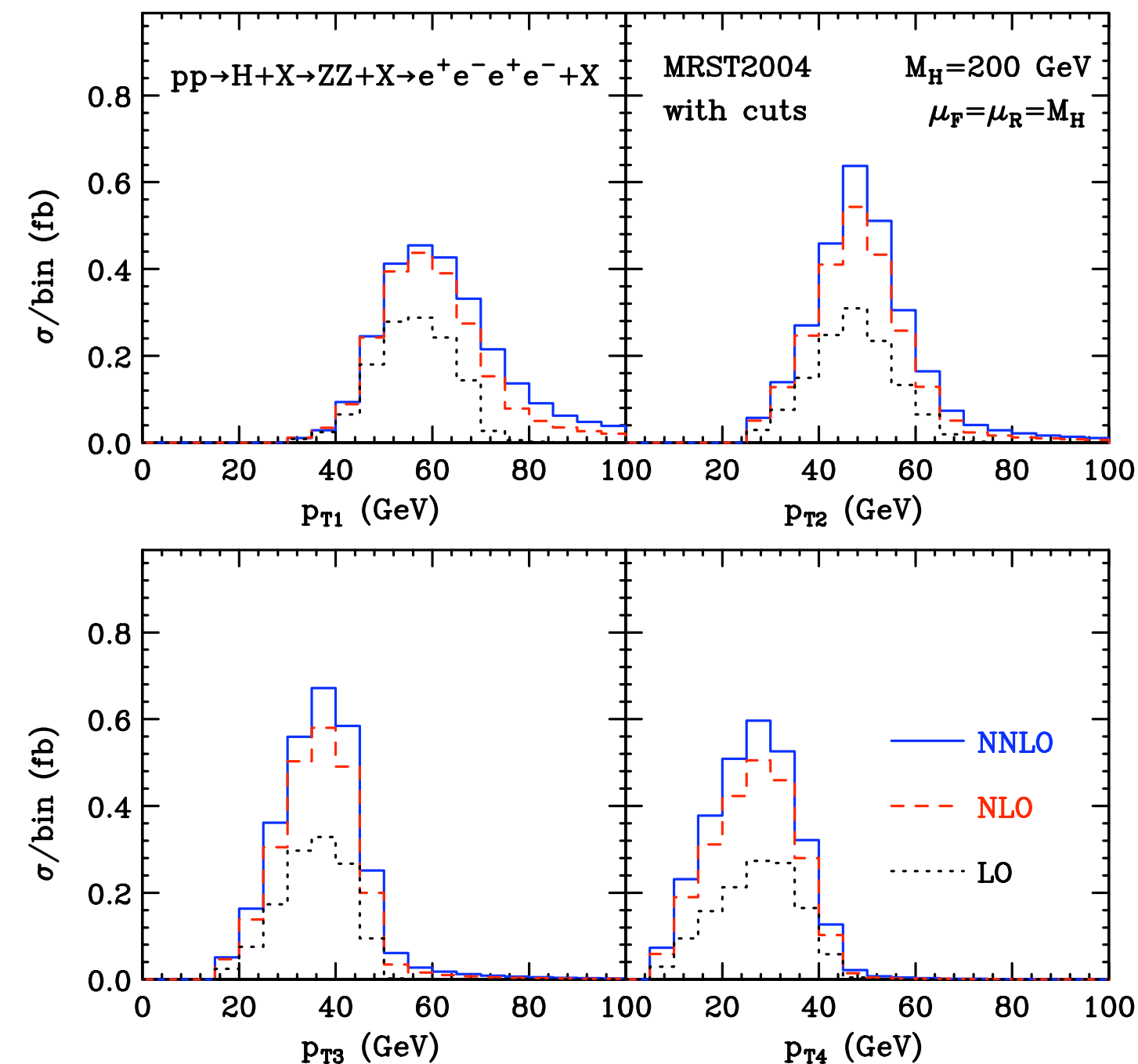
➡ $81 \text{ GeV} < m_1 < 101 \text{ GeV}$ and $40 \text{ GeV} < m_2 < 110 \text{ GeV}$

The corresponding cross sections are:

σ (fb)	LO	NLO	NNLO
$\mu_F = \mu_R = M_H/2$	1.541 ± 0.002	2.764 ± 0.005	2.966 ± 0.023
$\mu_F = \mu_R = M_H$	1.264 ± 0.001	2.360 ± 0.003	2.805 ± 0.015
$\mu_F = \mu_R = 2M_H$	1.047 ± 0.001	2.044 ± 0.003	2.609 ± 0.010

$$K_{NLO} = 1.87$$

$$K_{NNLO} = 2.22$$



in this case the cuts are mild
and do not change significantly
the impact of higher order
corrections

Note that at LO

$$p_{T1}, p_{T2} < M_H/2$$

$$p_{T3} < M_H/3 \quad p_{T4} < M_H/4$$

Behaviour at the kinematical
boundary is smooth

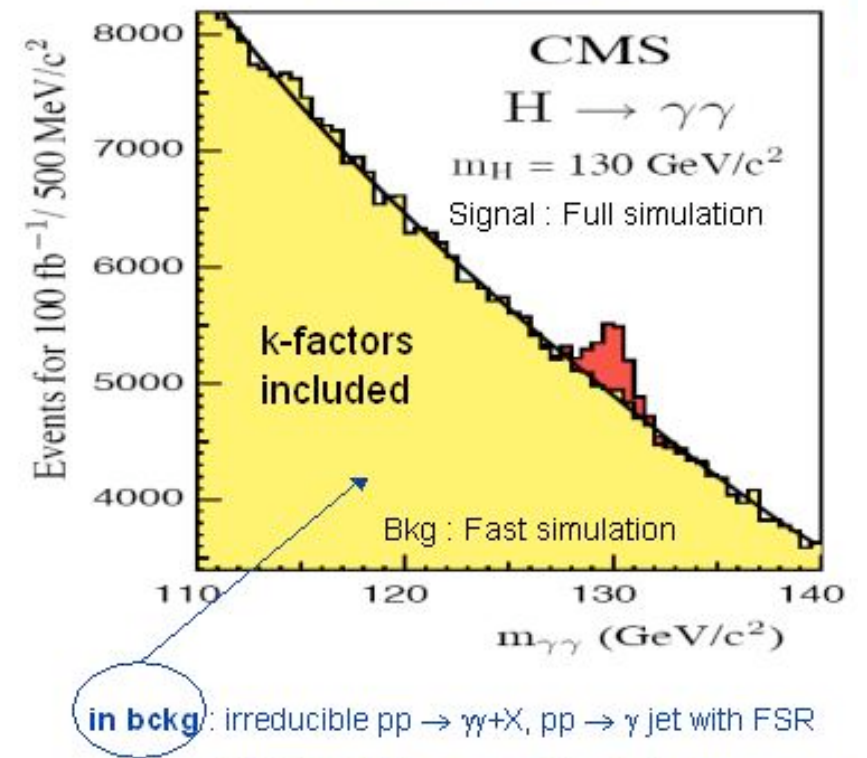


No instabilities
beyond LO

Higgs decays

- $H \rightarrow \gamma\gamma$

Background very large but the narrow width of the Higgs and the excellent mass resolution expected should allow to extract the signal
Background measured from sidebands

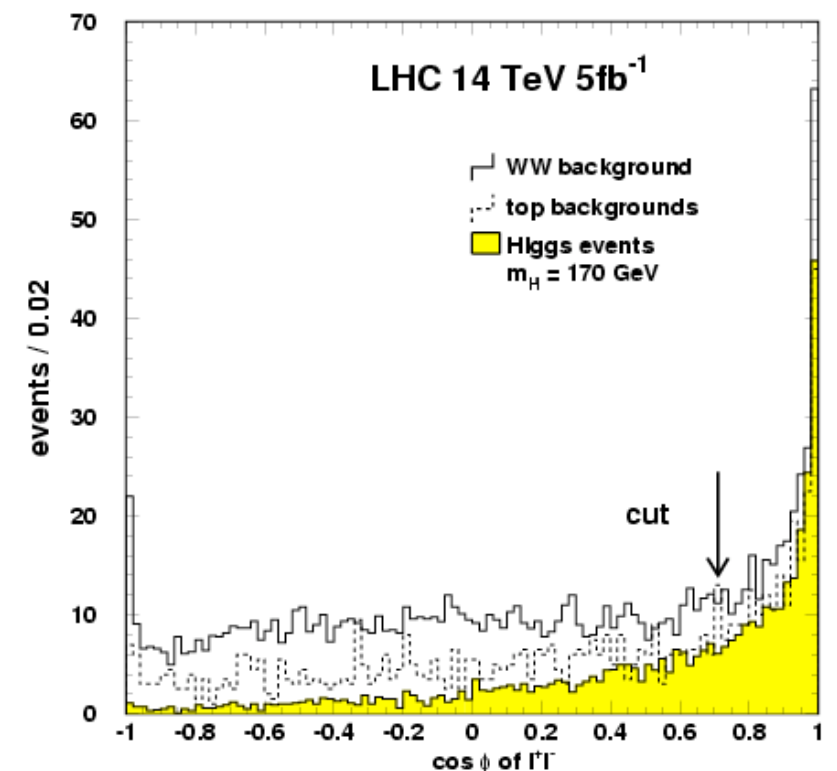
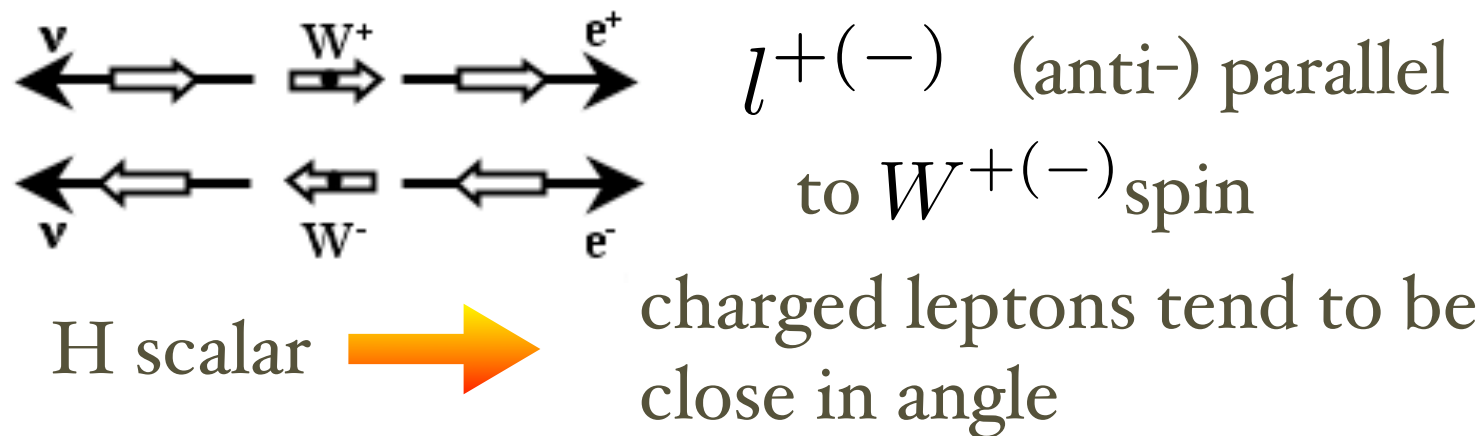


- $H \rightarrow WW^* \rightarrow l\nu l\nu$

No mass peak but strong angular correlations between the leptons

M.Dittmar, H.Dreiner (1996)

V-A interaction:



- $H \rightarrow ZZ \rightarrow 4l$ gold plated → clean four lepton signature