The background of the slide is a detailed image of the Crab Nebula, a supernova remnant. It features a complex, multi-colored structure with a bright blue and cyan core, surrounded by intricate filaments of green, yellow, and orange. The overall appearance is that of a turbulent, expanding cloud of gas and dust in space.

# Very-High Energy Steady Spectrum of Crab Nebula and Particle Acceleration

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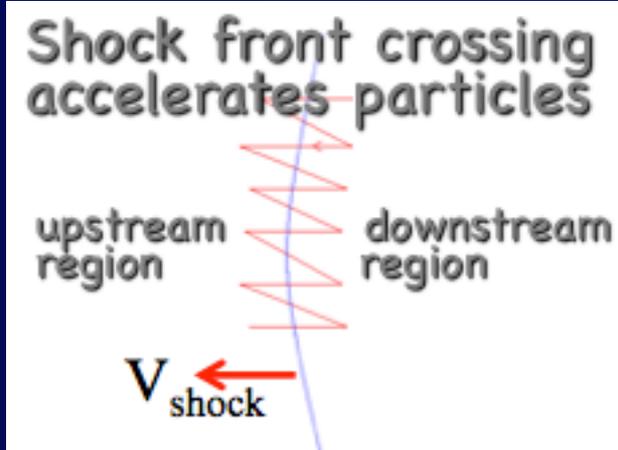
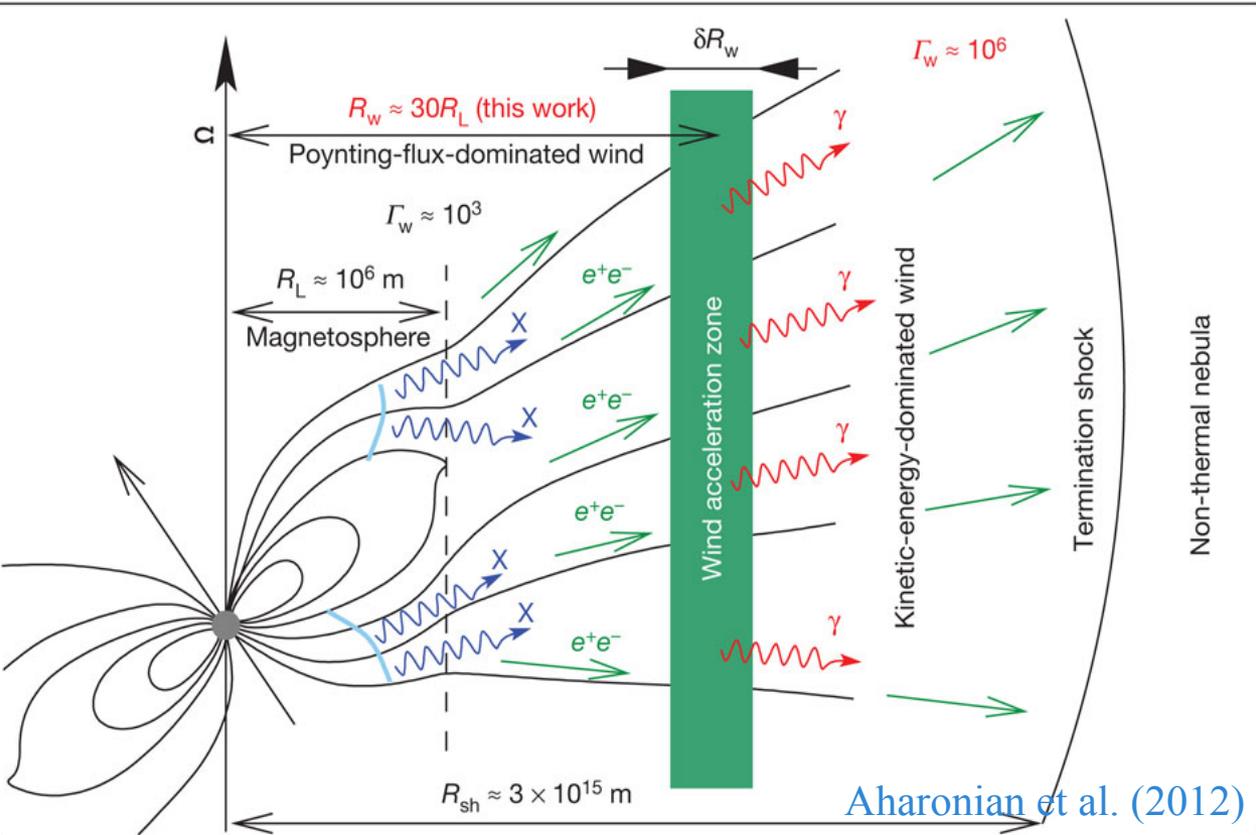
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# Outline

Multi-detector steady-state VHE (GeV and multi-TeV) spectrum of Crab nebula

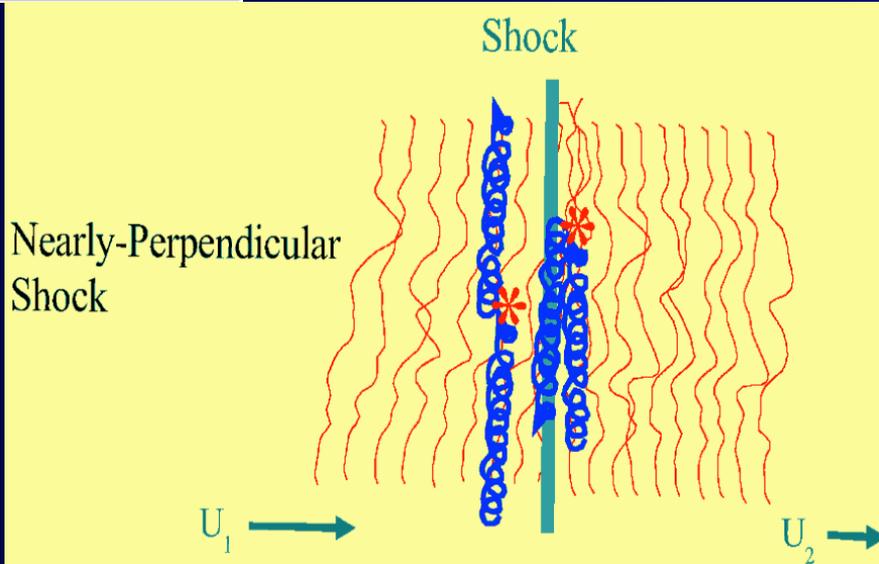
New accurate theoretical determination of the Inverse-Compton spectrum for the joint Fermi/LAT –VHE data up to 100 TeV

Microscopic parameters of the population of energetic electrons directly connected to observations

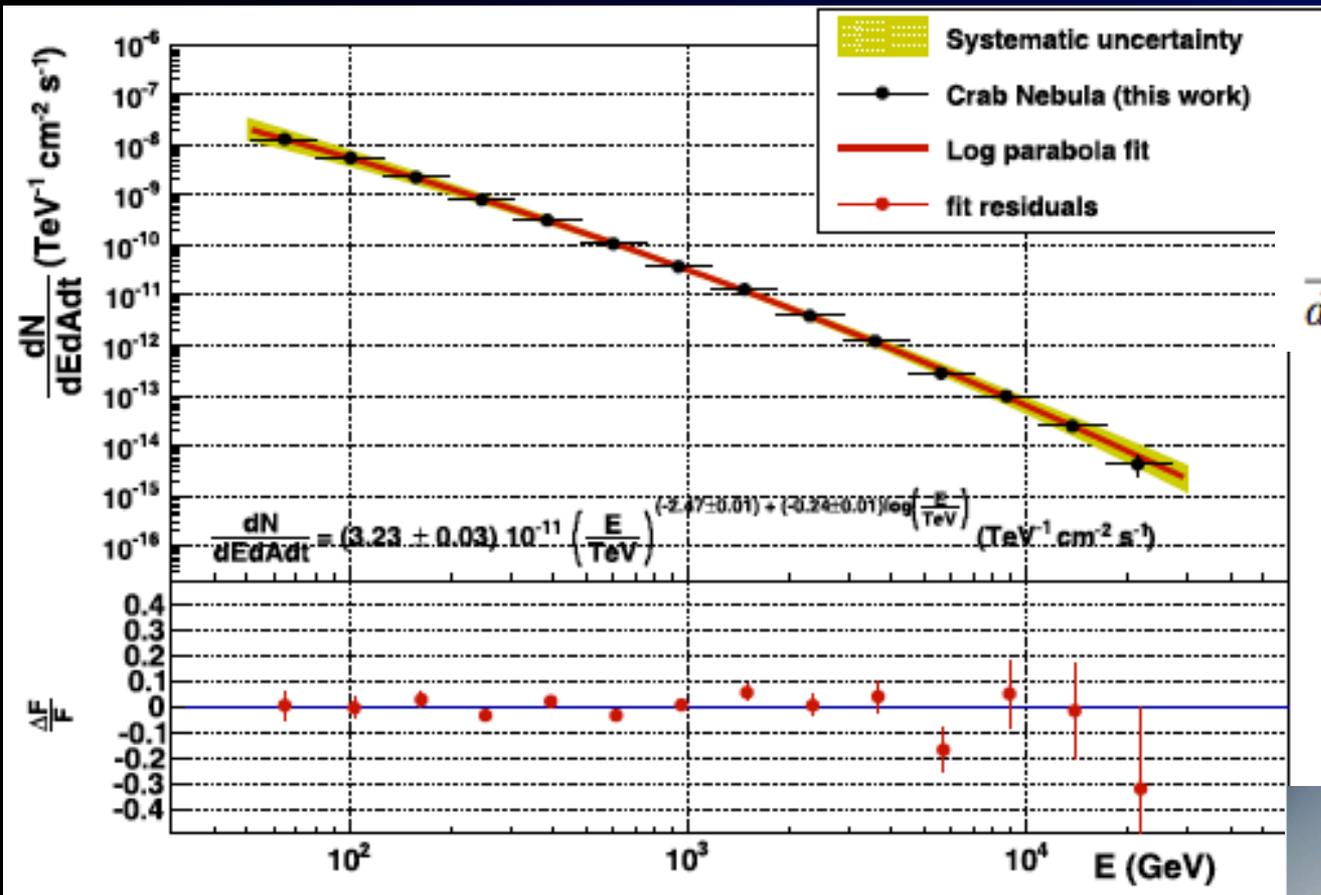


TS is a large-scale quasi-perpendicular shock

Relativistic  $e^+e^-$  advected in the magnetized wind are accelerated at termination shock (Aarons & Tavani 1994) or through shock-driven reconnection in the stripe wind (Petri & Lyubarsky 2007)



# MAGIC differential flux



Photon VHE spectrum:

$$\frac{dN}{dEdAdt} \propto \left( \frac{E}{E_0} \right)^{[\alpha + \beta \cdot \log(E/E_0)]}$$

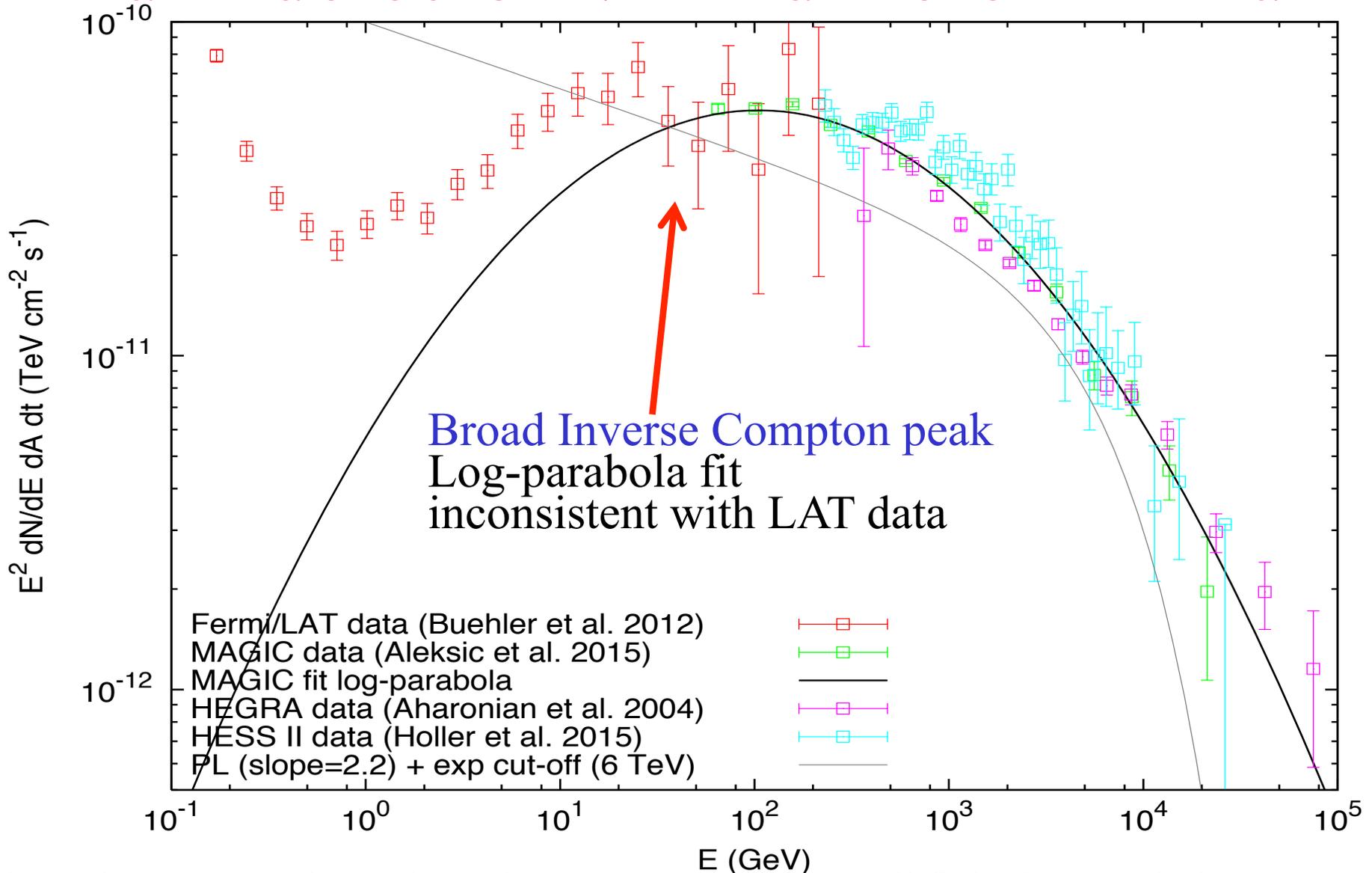
Log-parabola

Aleksic et al. 2015 (2009-11 data)

Most likely explanation:  
 $E > 1$  GeV photons Inverse Compton up-scattering  
 off the relativistic  $e^-$  within the nebula  
 (target photons from dust or CMB or synchrotron  
 self-Compton)



# Multi-detector VHE differential flux

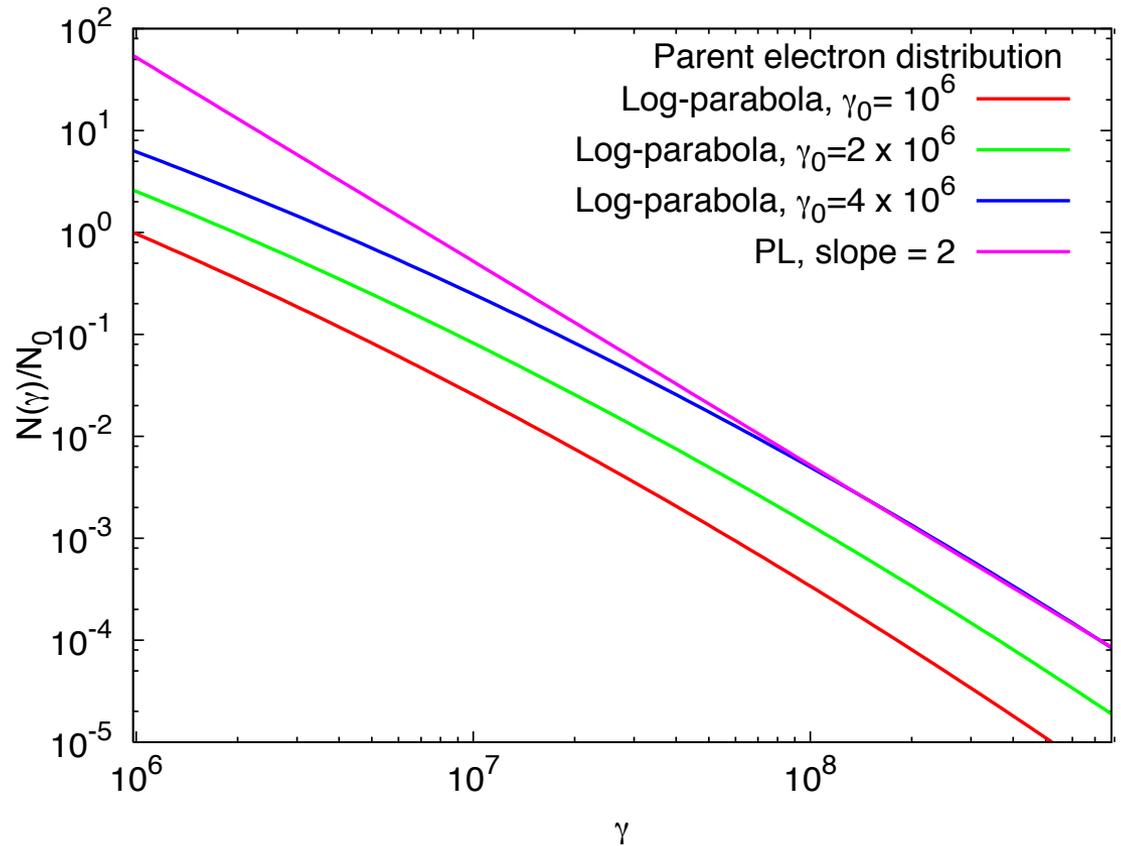


Blazars' **X-ray** non-thermal synchrotron spectrum are well fit by log-parabola. Such spectrum originates from log-parabola energetic electrons spectrum (Massaro et al. 2004). What about **VHE**?

# Microscopic assumptions

VHE-emitting electrons accelerated by the nebula TS have a **log-parabola** distribution, not power-law as expected from standard diffusive acceleration model for shocks

$$N(\gamma) = N_0(\gamma/\gamma_0)^{-[s-1+r\log(\gamma/\gamma_0)]}$$



## Key assumptions on the IC power

Monochromatic target photon field up-scattering off energetic electrons

Extreme Klein-Nishina limit  $\frac{4\varepsilon_0\gamma}{m_e c^2} \gg 1$   $\varepsilon_0$  : energy of photon target

# New VHE steady spectrum I

$$\frac{dN}{d\epsilon dAdt}(\epsilon) = \left[ 1 + (-s + 1 - 2r \log(\epsilon/\bar{\epsilon}_0)) \cdot \left( \ln \frac{4\epsilon_0\epsilon}{(m_e c^2)^2} - \frac{11}{6} \right) \right] \text{Peak width}$$

$$\times \mathcal{A}(\epsilon_0, \bar{\epsilon}_0) \left( \frac{\epsilon}{\bar{\epsilon}_0} \right)^{-[s+r \cdot \log(\epsilon/\bar{\epsilon}_0)]}$$

log-parabola

$\bar{\epsilon}_0 = m_e c^2 \gamma_0$

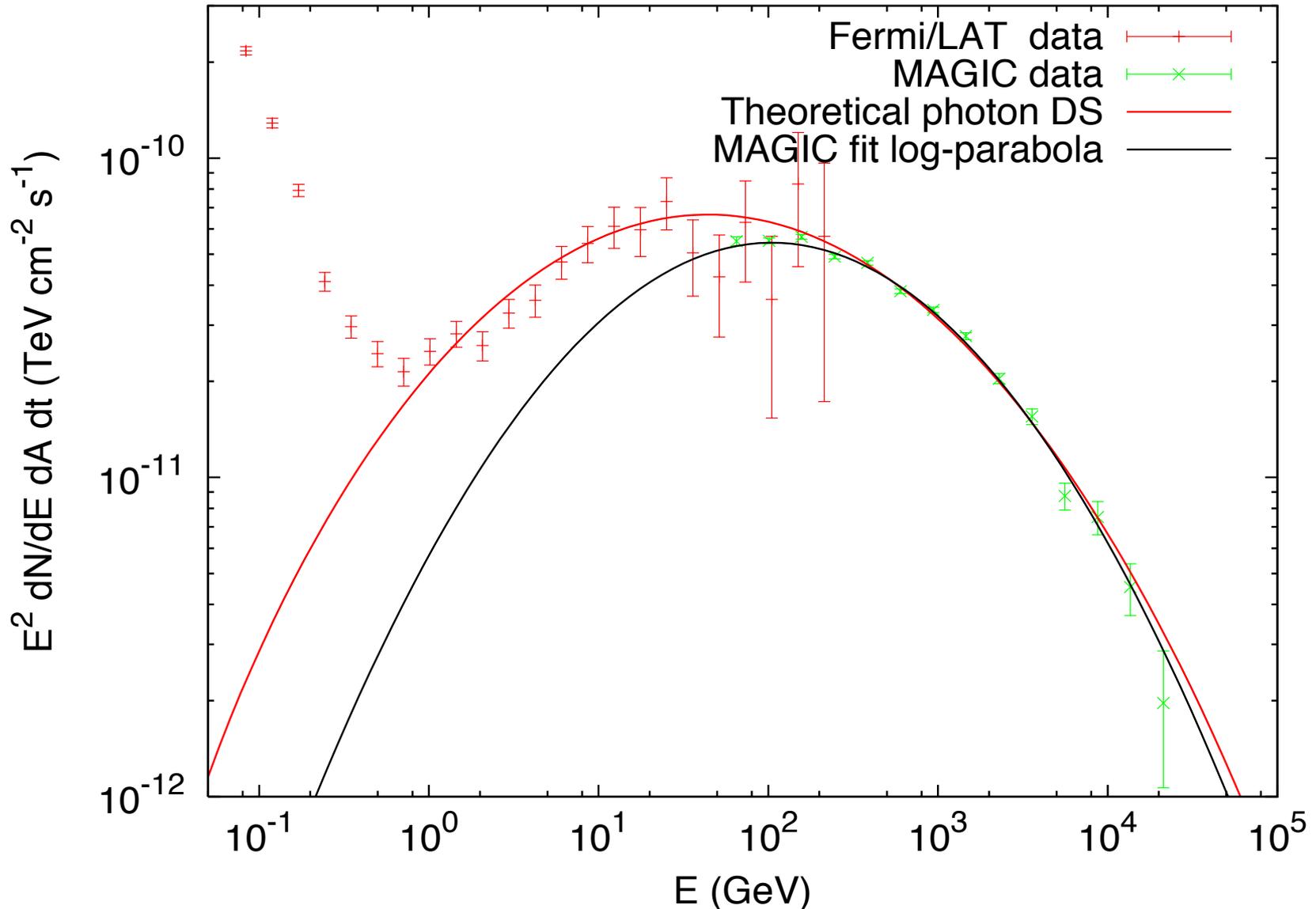
The new VHE steady-state spectrum is a standard **log-parabola** with a pre-factor governing the **width** of the IC peak

$$s=2.42 \text{ (} 2.47 \pm 0.01 \text{)}, r = 0.15 \text{ (} 0.24 \pm 0.01 \text{)}, \bar{\epsilon}_0 = 982 \text{ GeV}$$

Folded with mono-chromatic assumption for the IC characteristic photon energy:  $h\nu_{\text{IC}} = m_e c^2 \gamma$

In extreme Klein-Nishima limit, the photon acquires a sizeable fraction of the electron energy. CMB ruled out (Synchrotron self-Compton  $\rightarrow$  ).

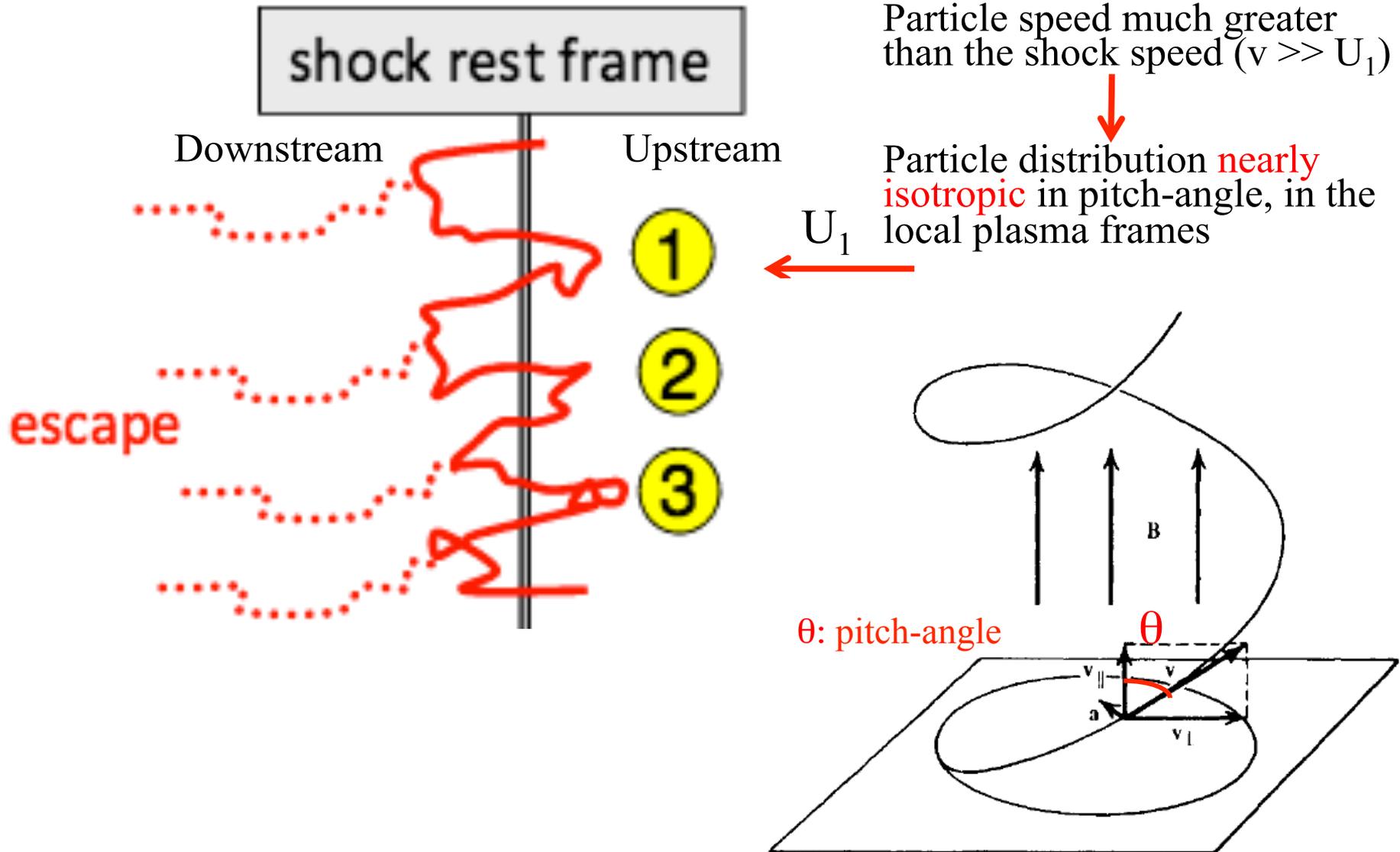
# New VHE steady spectrum II



Natural joint explanation of LAT + VHE data: **IC off far-infrared pool**

# Microscopic interpretation

One back-step to standard model of Diffusive Shock Acceleration



# Standard Model of Diffusive Shock Acceleration

1) Probability of remaining in the acceleration region independent of particle energy  $\gamma$  (only for highest energies)

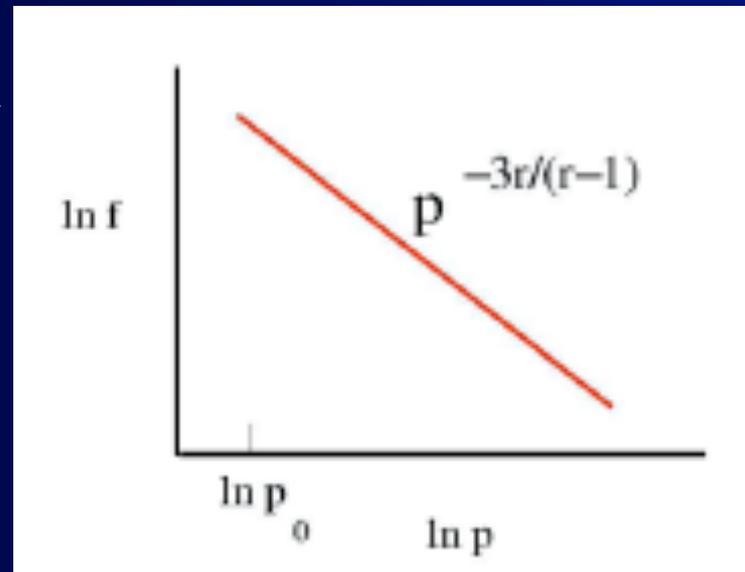


2) Isotropy in the pitch-angle in the local plasma frame



Time-asymptotic (steady-state) solution to transport equation for 1-dimensional shock

The spectrum is a power-law in momentum depending only on the shock compression ratio (if back-reaction of energetic particles is neglected)



# Crab nebula termination shock

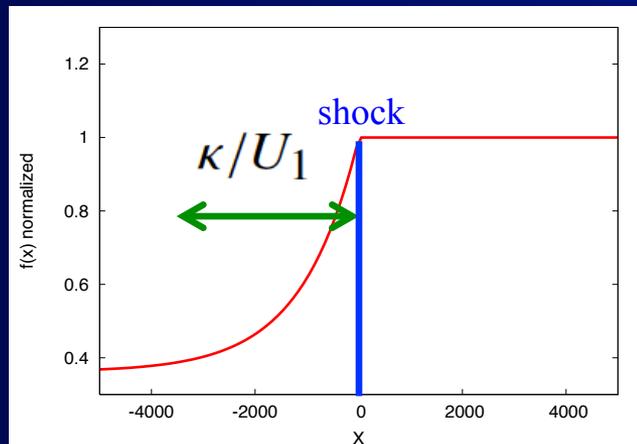
In the mildly relativistic TS ( $U_1 \sim 0.2c$ ) of the Crab nebula, the condition  $v \gg U_1$  still applies

1) Probability of remaining in the acceleration region decreasing with energy:  $P(\gamma) \sim \gamma^{-q}$

30 TeV electrons in  $B_0 = 140 \mu\text{G}$  have Larmor radius  $m_e c^2 \gamma / e B_0 = 0.00034 \text{ pc}$  comparable with diffusion length  $\kappa/U_1$



2) Weakly isotropic in pitch-angle ( $U_1 \sim 0.2c$  and  $\gamma \sim 10^6$ )



$\kappa/U_1 \sim \kappa_{\perp}/U_1$  at TS



$$N(\gamma) = N_0 (\gamma/\gamma_0)^{-[s-1+r \log(\gamma/\gamma_0)]}$$

Connection observations to microscopic parameters:  $\beta \simeq -r = q/2 \log(1 + \Delta p/p)$

$$q = 2rU_1/c$$



$$q = 0.06$$

Small energy dependence  
Qualitative agreement with previous estimates  
(Lemoine & Pelletier 2003)

# Summary & Conclusion

Natural reproduction of the joint Fermi/LAT and VHE spectrum down to  $\sim 1$  GeV, including the broad IC peak at  $\sim 200$  GeV by using a new theoretical derivation of log-parabola spectrum

Microscopic: Probability for TeV electrons of remaining in the acceleration region at mildly relativistic shock weakly decreasing on energy; thus, the distribution in momentum of emitting particles is **not** a power-law

Determination of the synchrotron self-Compton spectra underway ( $e^-$  with  $\gamma < 10^8$  in a  $B = 140 \mu\text{G}$  emit synchrotron up to 25 keV)

Back-up slides

# New VHE steady spectrum I

$$\frac{dN}{d\varepsilon dAdt}(\varepsilon) = \left[ 1 + (-s + 1 - 2r \log(\varepsilon/\bar{\varepsilon}_0)) \cdot \left( \ln \frac{4\varepsilon_0\varepsilon}{(m_e c^2)^2} - \frac{11}{6} \right) \right] \text{Pre-factor: peak width}$$

$$\times \mathcal{A}(\varepsilon_0, \bar{\varepsilon}_0) (\varepsilon/\bar{\varepsilon}_0)^{-[s+r \cdot \log(\varepsilon/\bar{\varepsilon}_0)]}$$

