



Paths towards instability in financial networks

Marco Bardoscia

London Institute for Mathematical Sciences

in collaboration with:

Stefano Battiston, Fabio Caccioli, and Guido Caldarelli

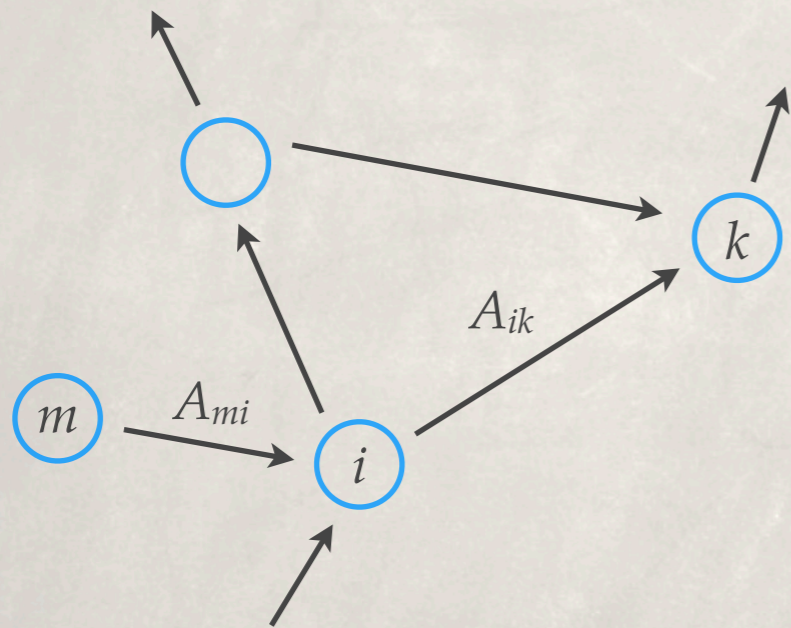
Bari Theory Xmas Workshop - 22nd December 2015

Motivations

- ▶ **Larger markets** can better absorb shocks, and therefore are **more stable**: market integration.
- ▶ From an individual perspective **diversification** lowers risk: **more contract** between banks
- ▶ But... What happens if we take **interactions** into account?
- ▶ Which are the implications for **systemic risk** and **policy making**?

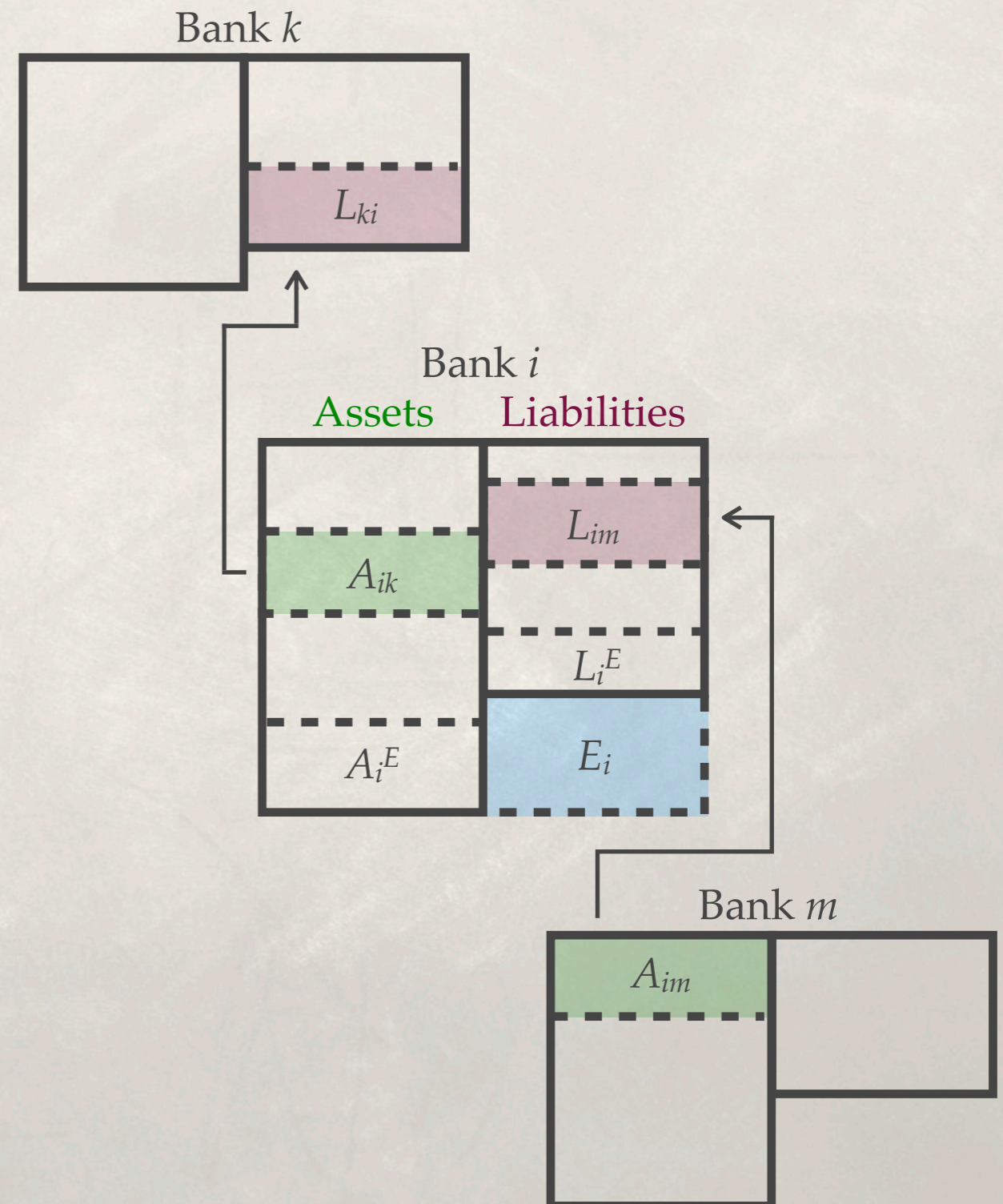
Networks of banks

A_{ik} : money bank k
borrows from bank i



but there is a **balance sheet identity**:

$$E_i = A_i^E - L_i^E + \sum_j A_{ij} - \sum_j L_{ij}$$

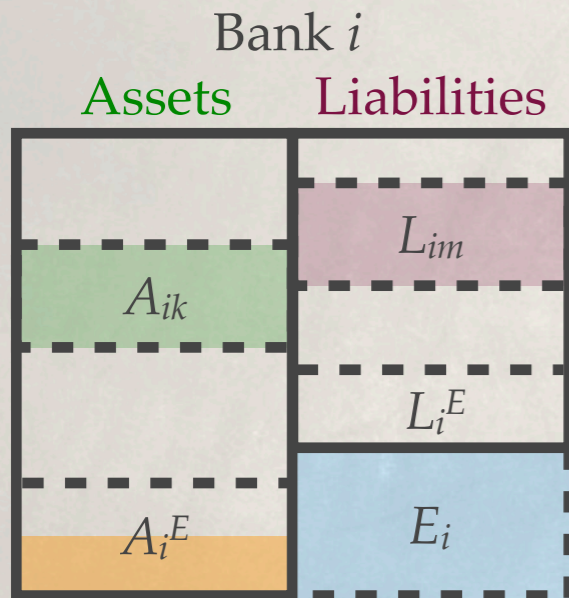


DebtRank

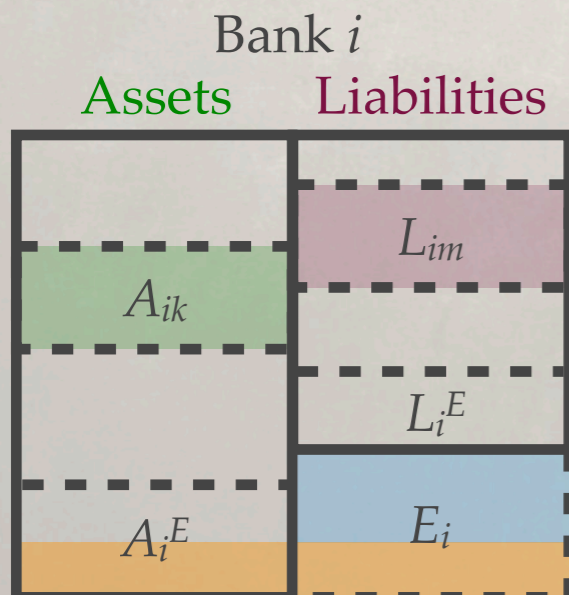
- ▶ DebtRank is an algorithm for **propagating shocks** in the interbank network.
- ▶ Shocks refer to **distress** (opposed to **default**): a bank becomes dangerous before it defaults via devaluation of lender's claims.
- ▶ It can be interpreted as an algorithm **propagating information** so that all banks can agree on a **common evaluation** of assets.
- ▶ DebtRank is applied by the **European Central Bank** for experimental stress tests and we have an ongoing collaboration with the **Bank of England**.

Shock Propagation

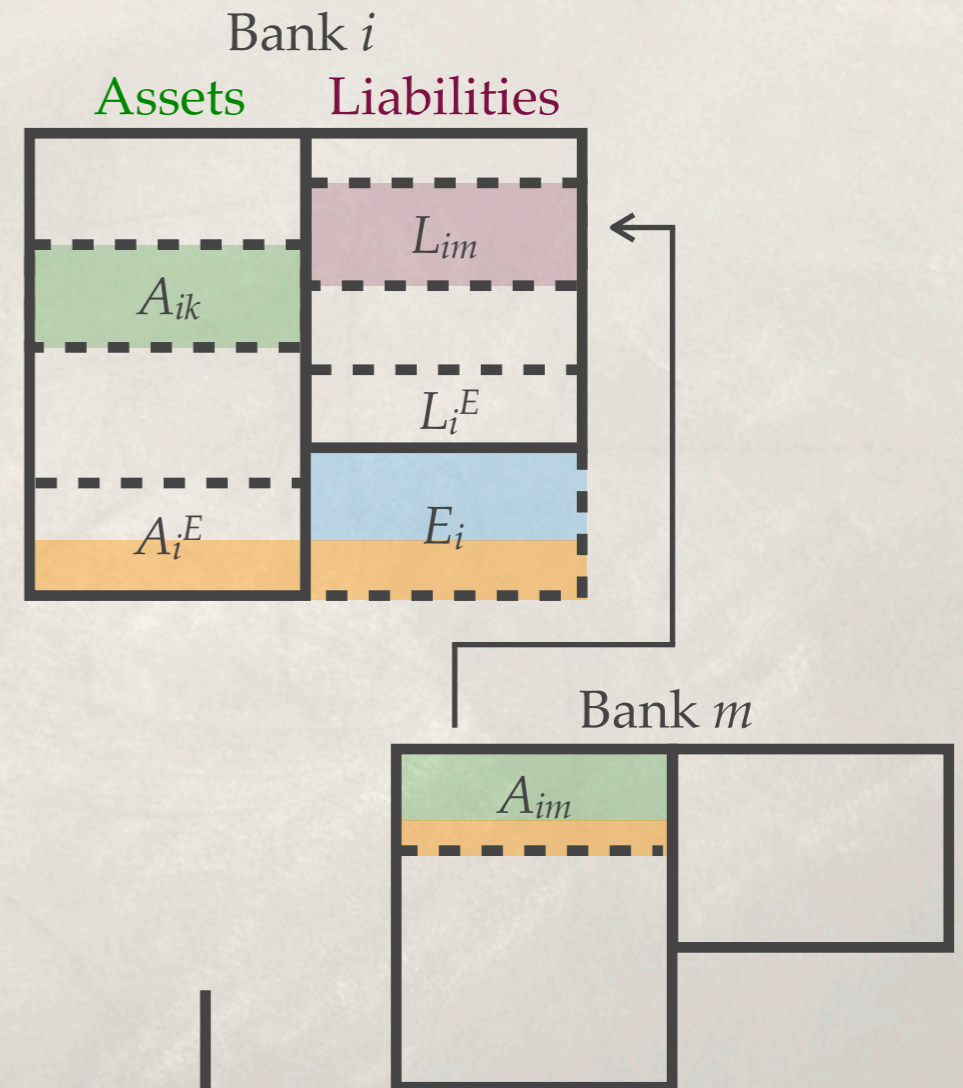
1) Shock in external assets



2) Shock in equity



3) Reassessment of interbank claims



4) Further propagation ...

“Microscopic” approach

- ▶ Equities and interbank assets are consistent with the **balance sheet** identity at any time step:

$$E_i(t) = A_i^E(t) - L_i^E + \sum_j A_{ij}(t) - \sum_j L_{ij}$$

- ▶ Shocks propagate as **lenders** reassess the value of their assets depending on the **probability of default** of **borrowers**:

$$A_{ij}(t + 1) = A_{ij}(0)(1 - p_j(t)) + (1 - \rho)A_{ij}(0)p_j(t)$$

- ▶ The simplest assumption is that the **probability of default** is equal to the relative cumulative loss:

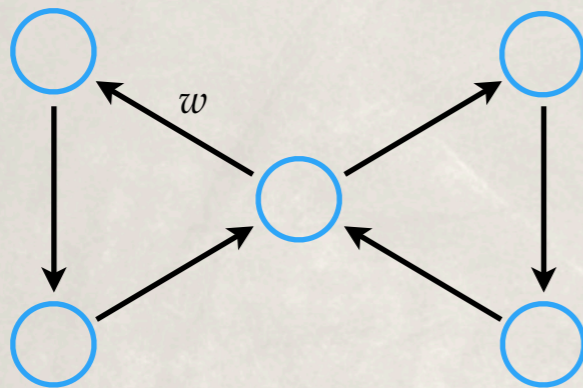
$$p_i(t) = \frac{E_i(0) - E_i(t)}{E_i(0)}$$

Stability

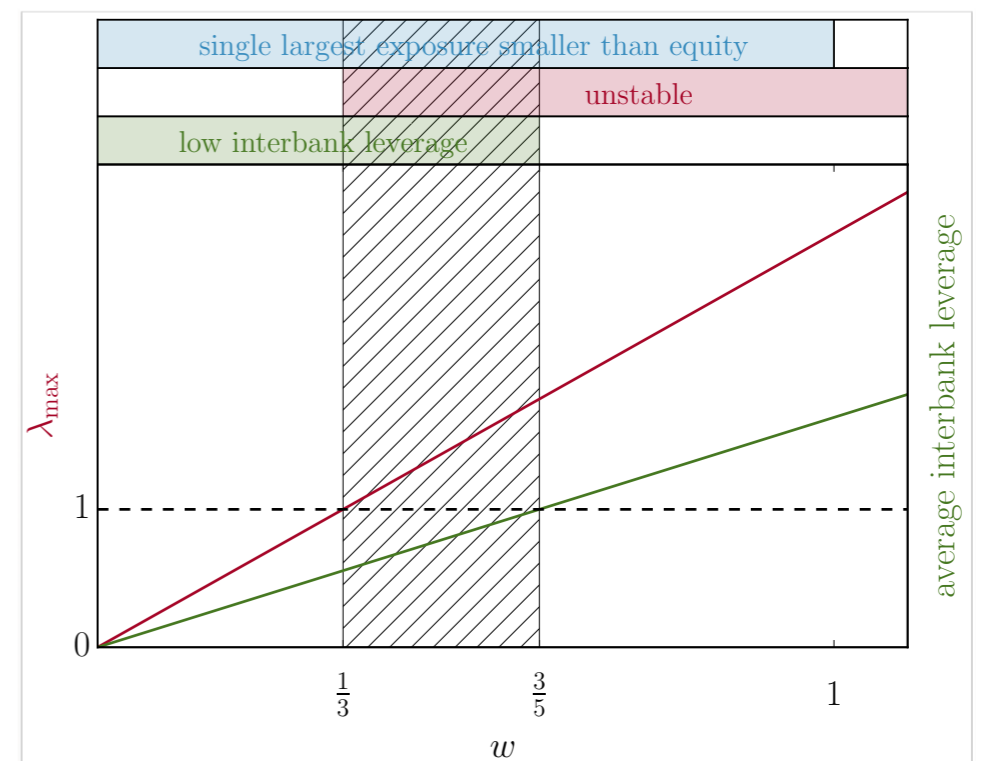
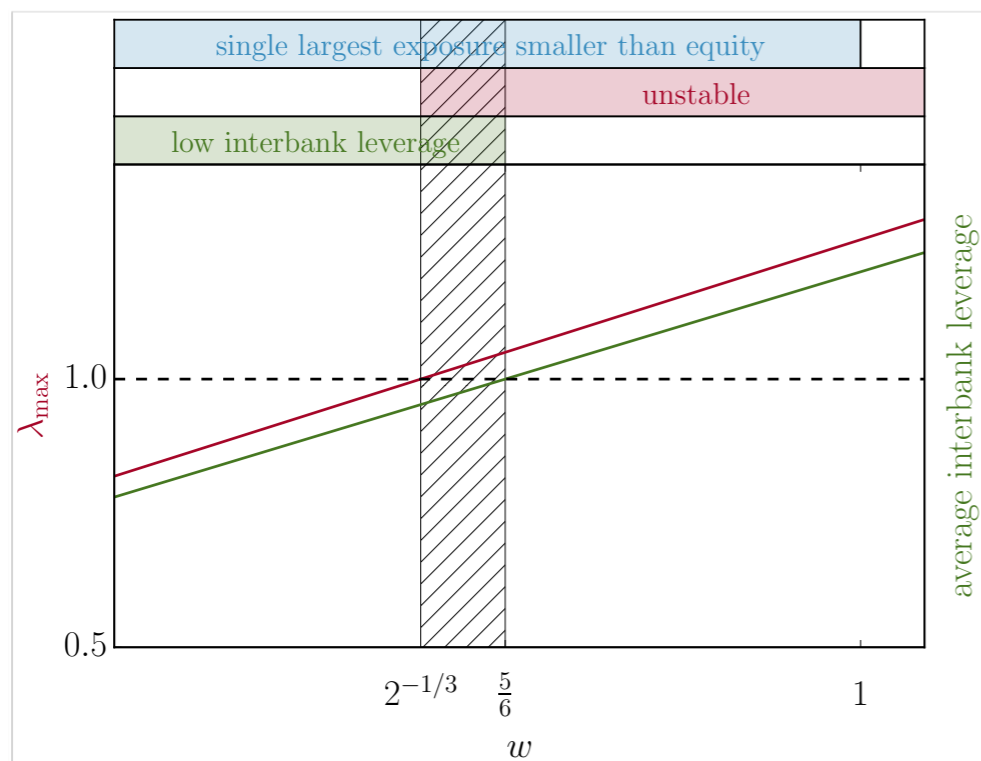
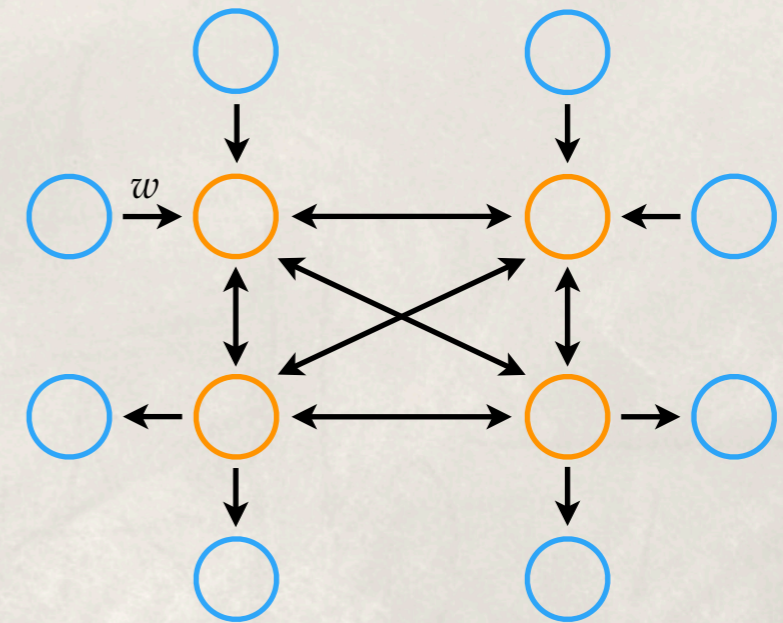
- ▶ The dynamics **in-between defaults** is linear and one can easily study the **stability** of the **banking system**.
- ▶ The crucial quantity is the **interbank leverage matrix**: $\Lambda_{ij}(t) = A_{ij}(t) / E_i(t)$.
- ▶ If $|\lambda_{\max}| < 1$ the system is stable, otherwise is unstable and at least one bank will default. Interbank leverages change after the default and a **previously unstable** system **can become stable**.
- ▶ Any (reasonable) dynamics has DebtRank as its **linear approximation** close to the stable fixed point $\Delta h = 0$.

Unstable Topologies

Butterfly



Core-periphery network



Adding nodes

Wigner-May theorem for an ecosystem with n species, interaction strength α , and connectivity p . A large system is **stable** if:

$$n p \alpha^2 < 1$$

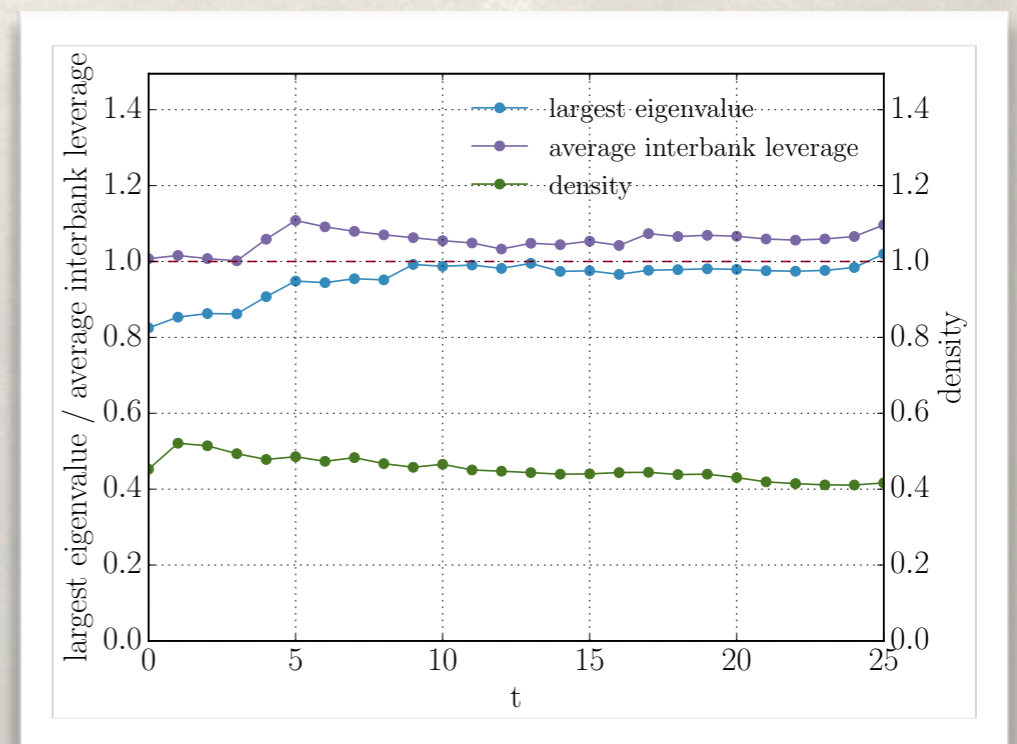
and **unstable otherwise**.

An interbank system with n banks, connectivity p , and mean interbank leverage μ/n is **stable** if:

$$(n - 1) p \mu < 1$$

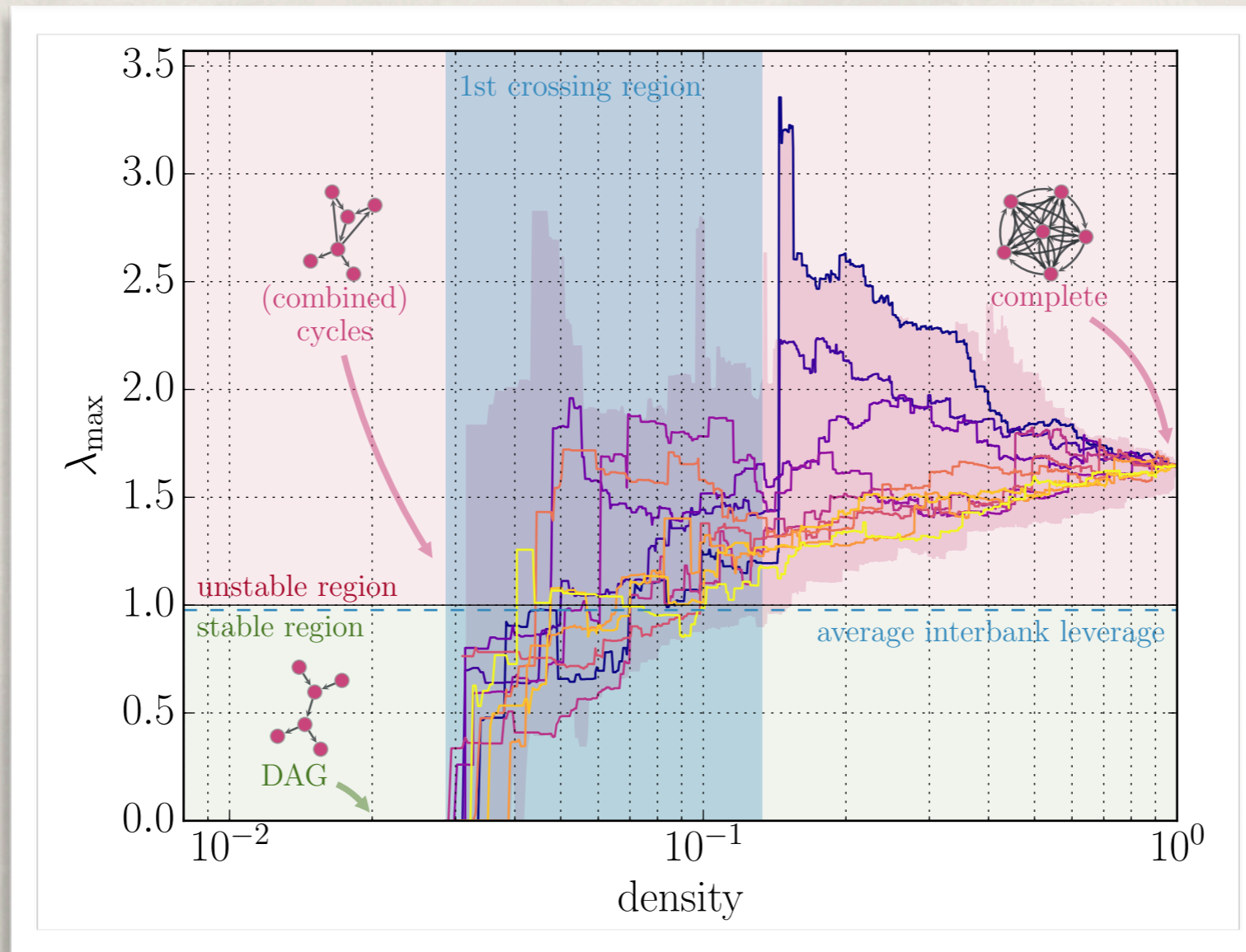
and **unstable otherwise**. (Entries of interbank leverage matrix i.i.d.)

What happens if we simulate a **growth process** starting from a finite network in the “wrong” phase?



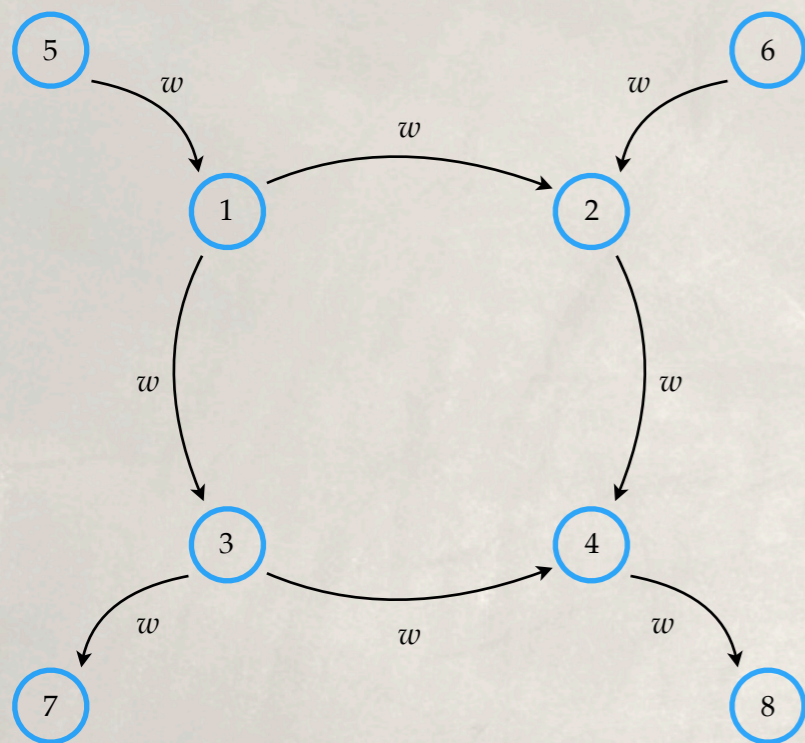
Adding edges

Top 50 EU banks: from a **DAG** to a **complete** graph, keeping consistency with balance sheets: instability arises already at **density** equal to **3%**

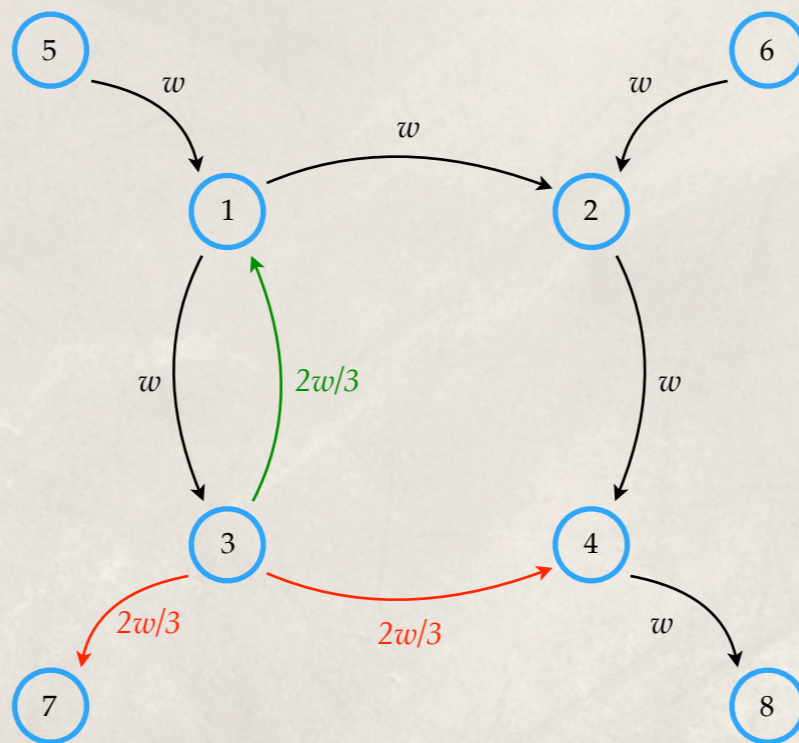


2013 (similar for 2008, ..., 2012)

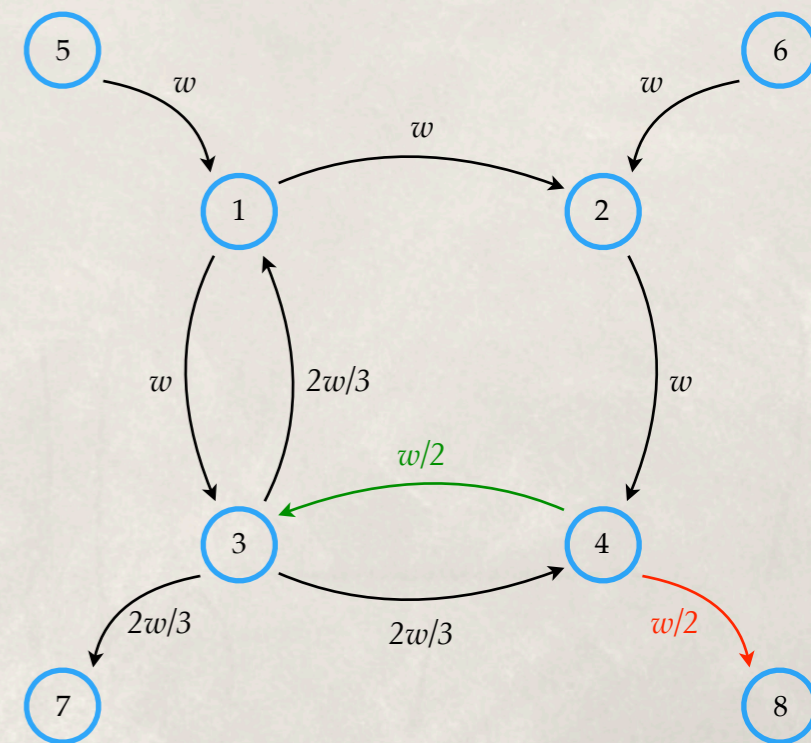
Bumpy paths



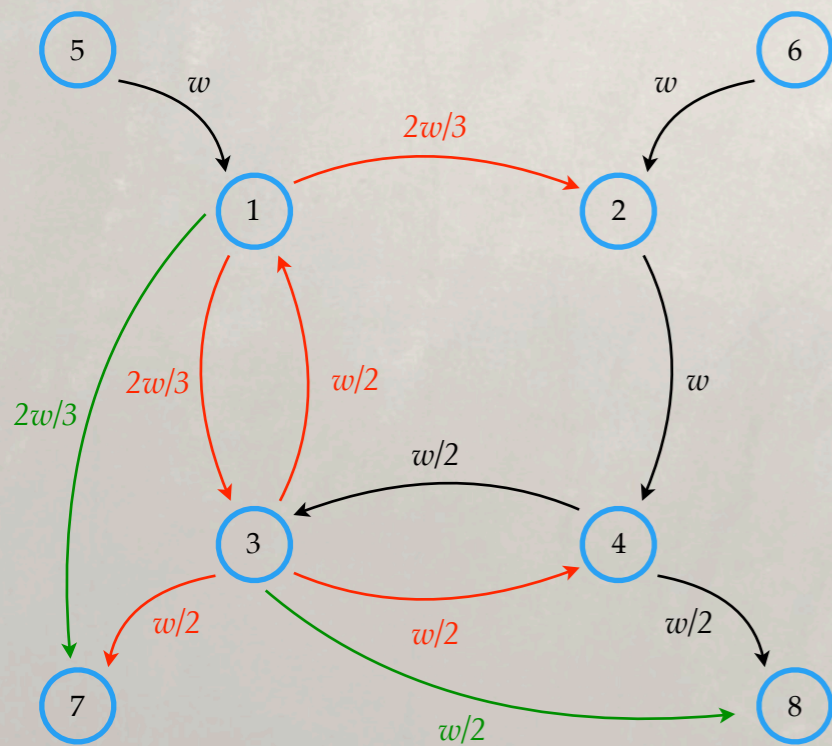
a: $\lambda_{\max} = 0$



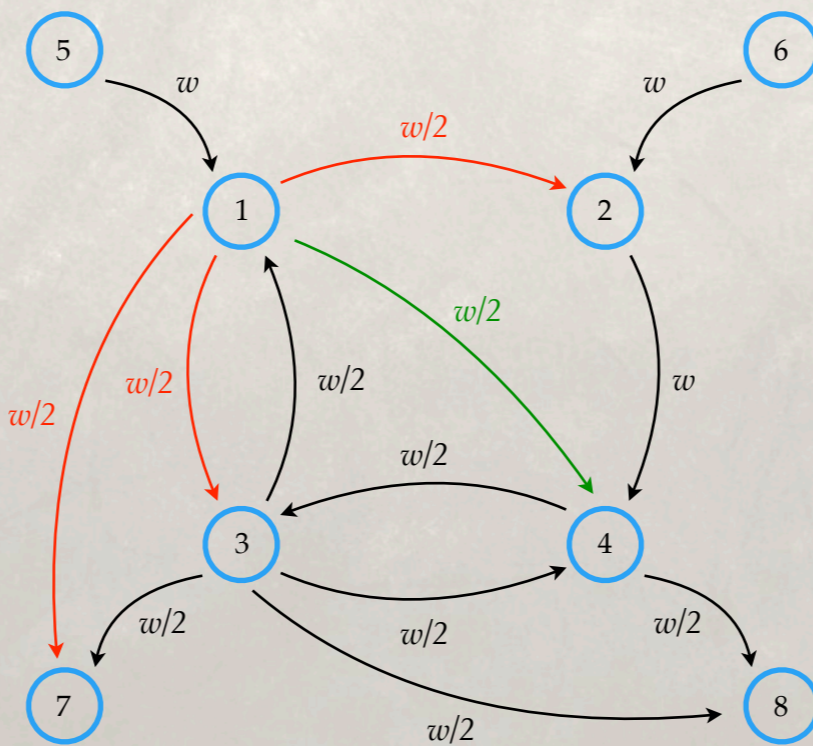
b: $\lambda_{\max} = 0.8165 w$



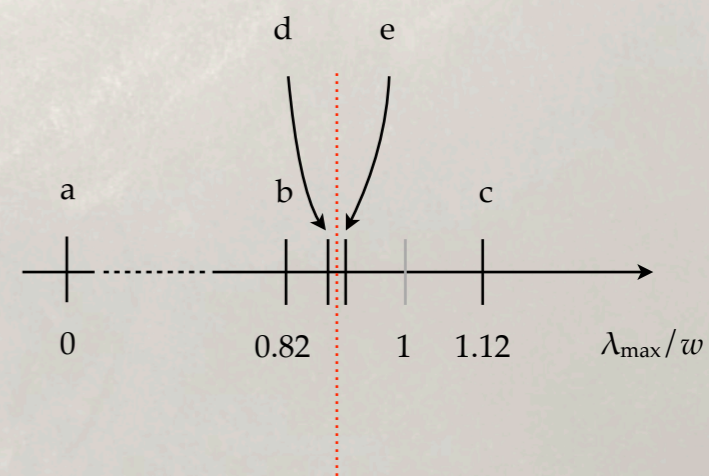
c: $\lambda_{\max} = 1.1242 w$



d: $\lambda_{\max} = 0.8907 w$



e: $\lambda_{\max} = 0.8927 w$




Conclusions

- ▶ We establish a framework to assess the **stability** of the interbank network (we can account for **recovery** too).
- ▶ We show that standard **policy recommendation** might not capture possible sources of instability.
- ▶ We prove the analogous of the **Wigner-May theorem** for the interbank network. **Adding nodes** to an anomalously stable network makes it unstable.
- ▶ Increasing the **interconnectivity** of the network while keeping the interbank leverage constant is a (possibly **bumpy**) path towards **instability**.



marco.bardoscia@gmail.com

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