

A NEW APPROACH TO THE THERMAL EVOLUTION OF NEUTRON STARS

Rodrigo Negreiros – IF/UFF

Stefan Schramm - FIAS

Fridolin Weber – SDSU

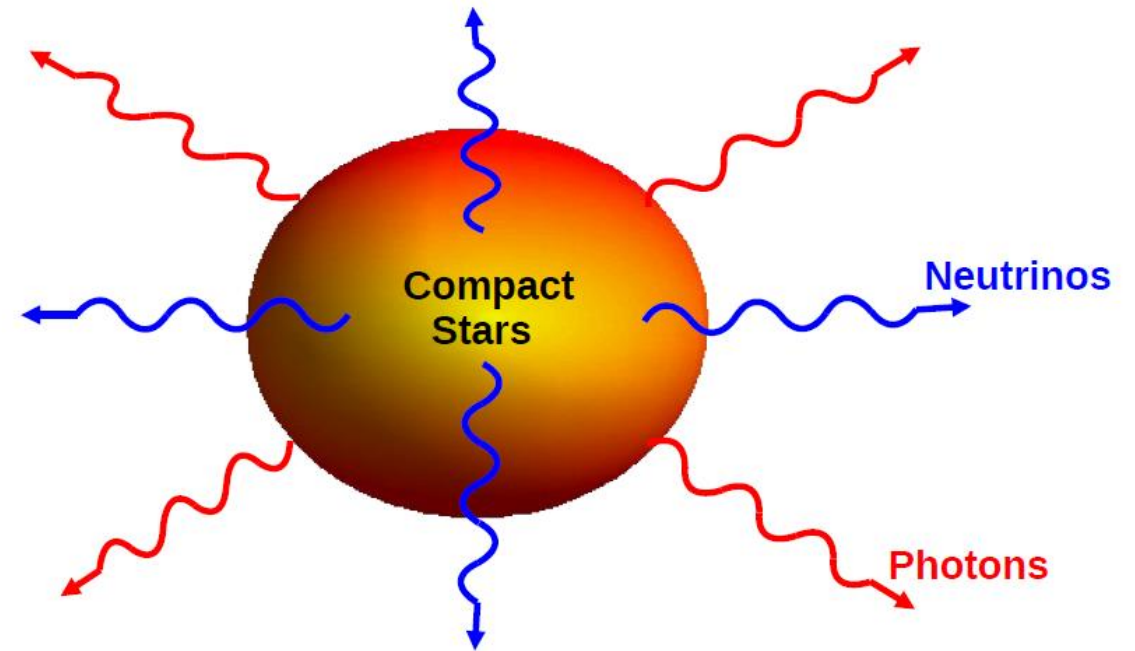


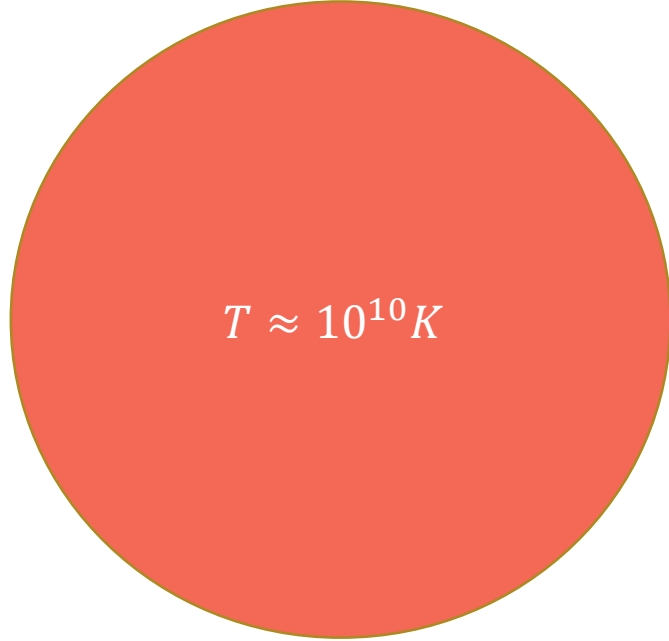
ACKNOWLEDGMENTS

- CAPES
- CNPq
- Manuel Malheiro (!!)
- Organizes

INTRODUCTION

- Thermal evolution is driven by neutrino emissions from the core, and photon emission from the surface.
- Neutrino emissions strongly depend on the core composition.
- Depending on its mass, a neutron star may exhibit fast or slow cooling.

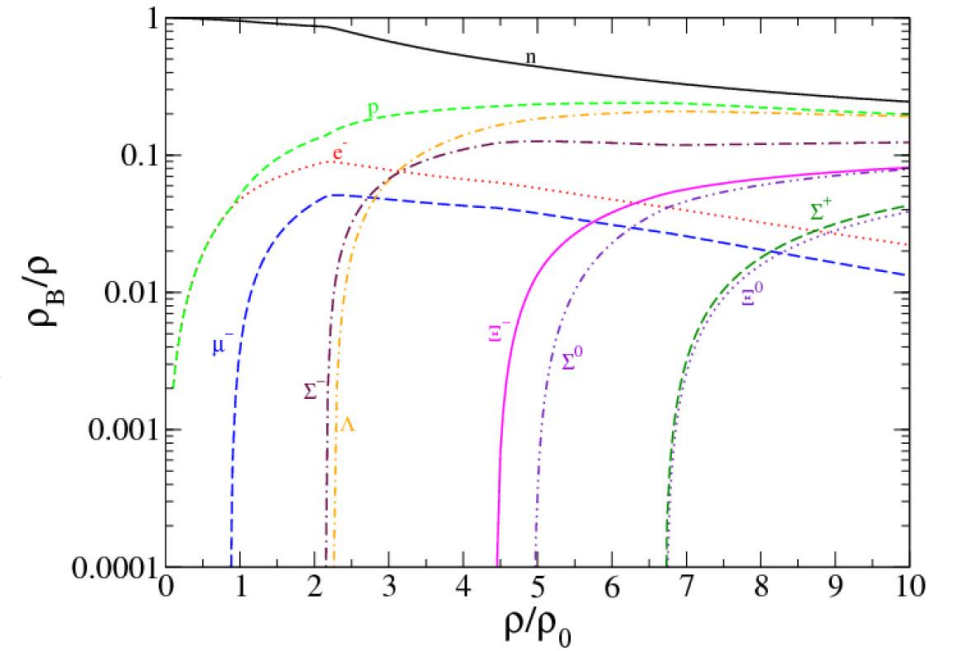
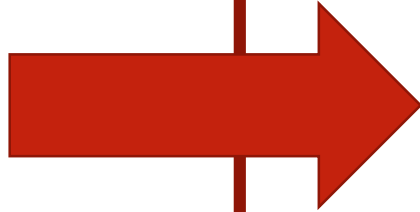




$$P = P(\rho, T = 0, \Omega = 0)$$

$$M = M(\rho, T = 0, \Omega = 0)$$

$$R = R(\rho, T = 0, \Omega = 0)$$



$$\varepsilon = \varepsilon(\rho, T)$$

$$K = K(\rho, T)$$

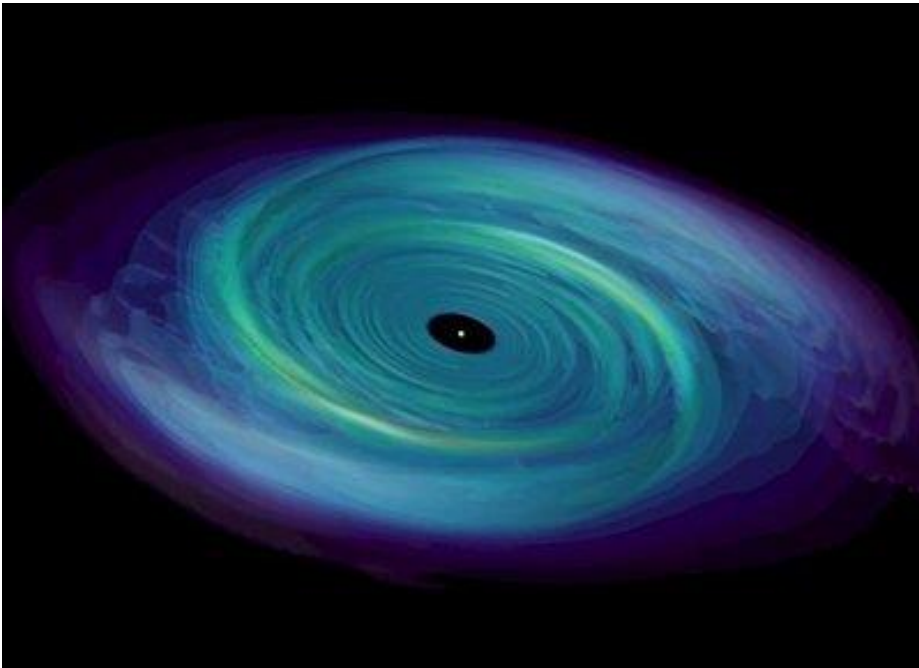
$$c_v = c_v(\rho, T)$$



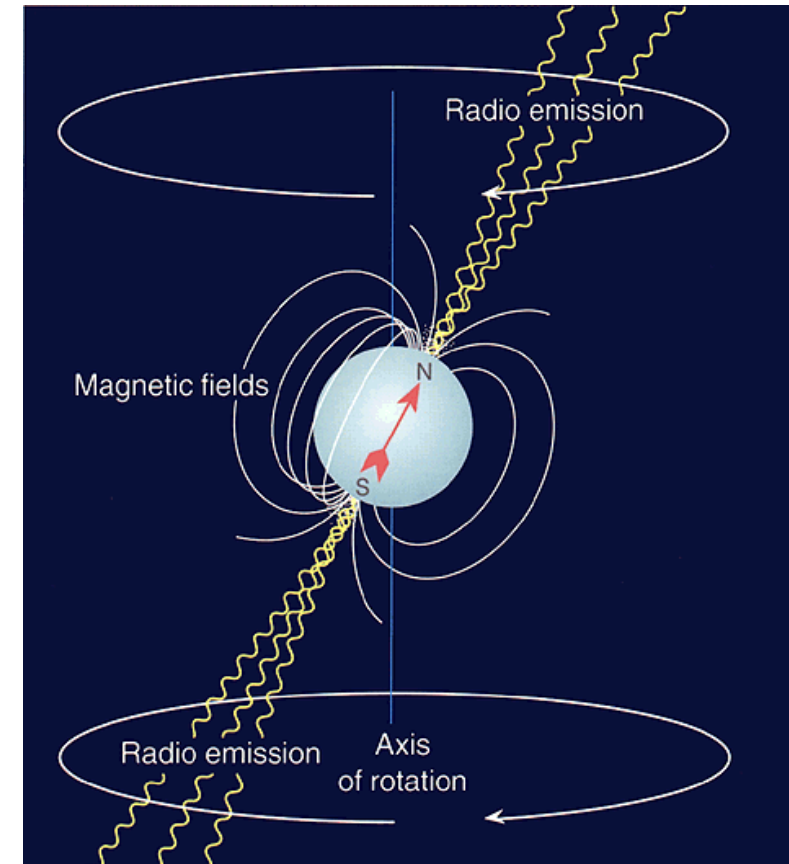
TRADITIONAL PICTURE

- Structure and composition frozen in time - “Frozen In”
- Thermal properties only change due to temperature evolution
- Dynamic => TEMPERATURE (ONLY !!)

STRUCTURE/COMPOSITION MAY NOT BE STATIC

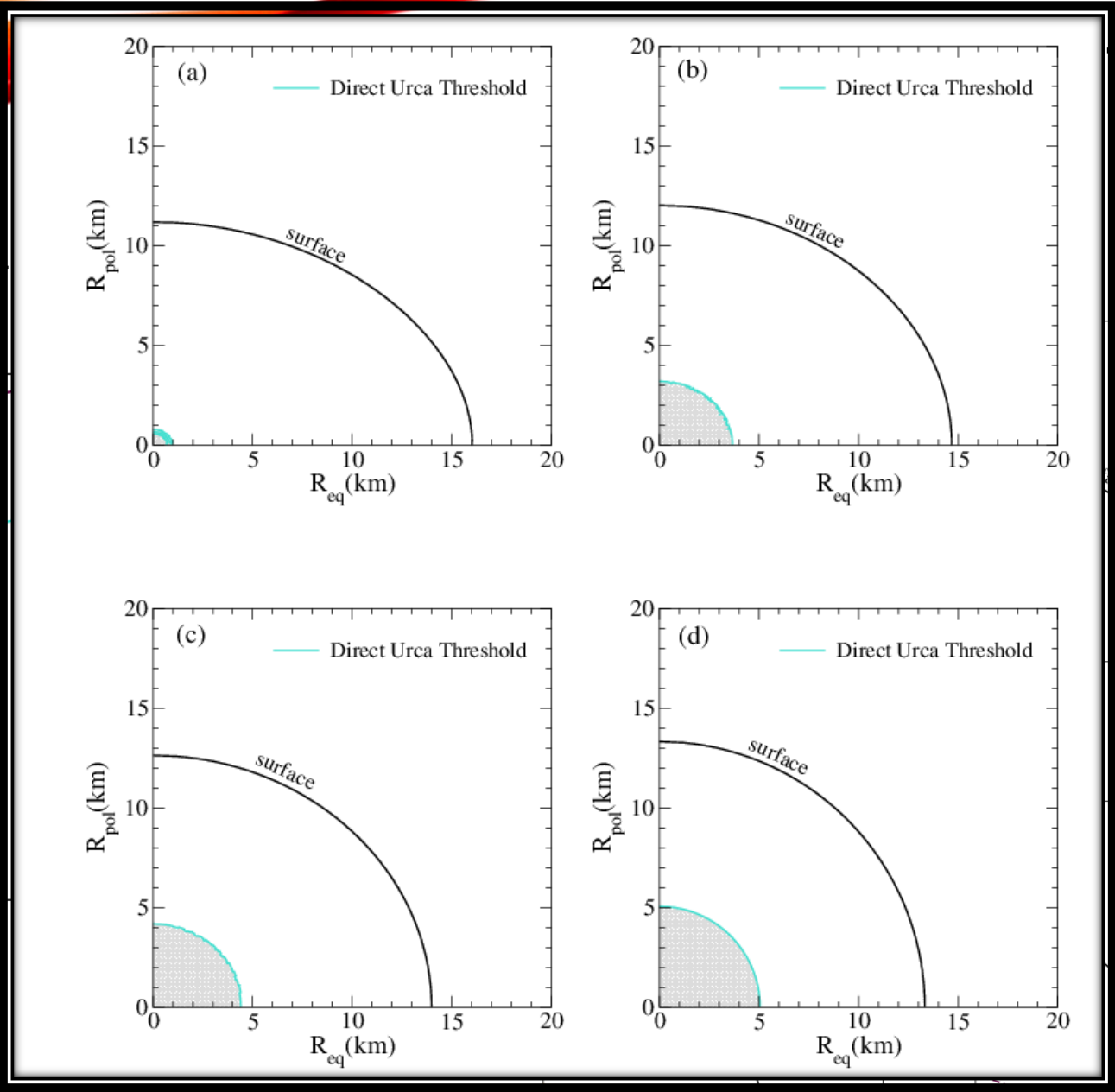
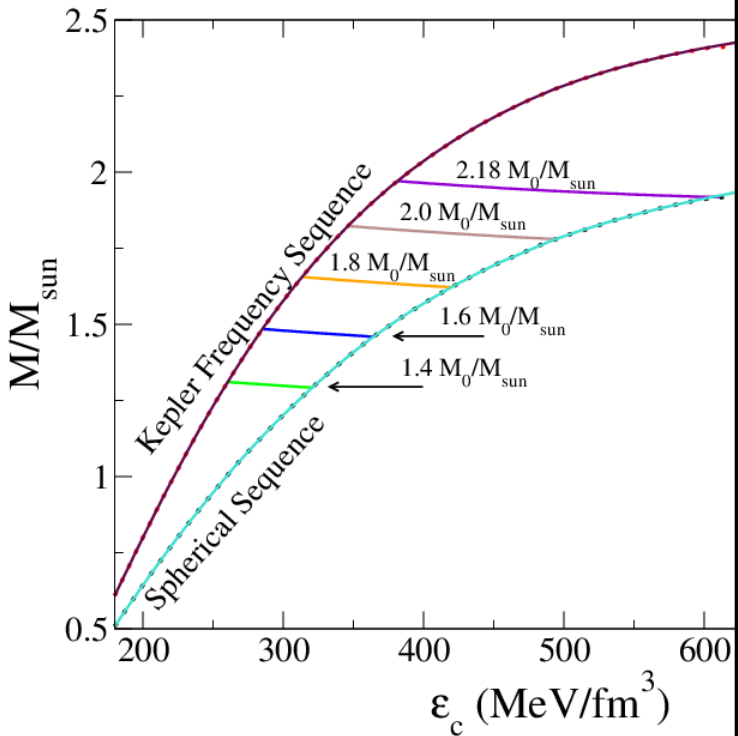


Accretion

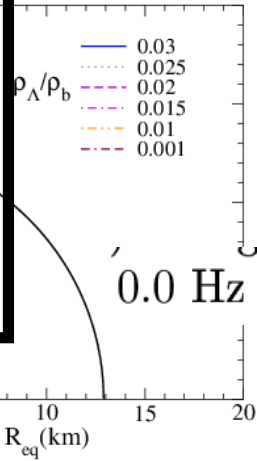
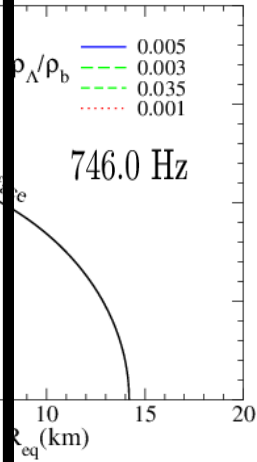


Magnetic/Spin evolution

- Structure and Composition

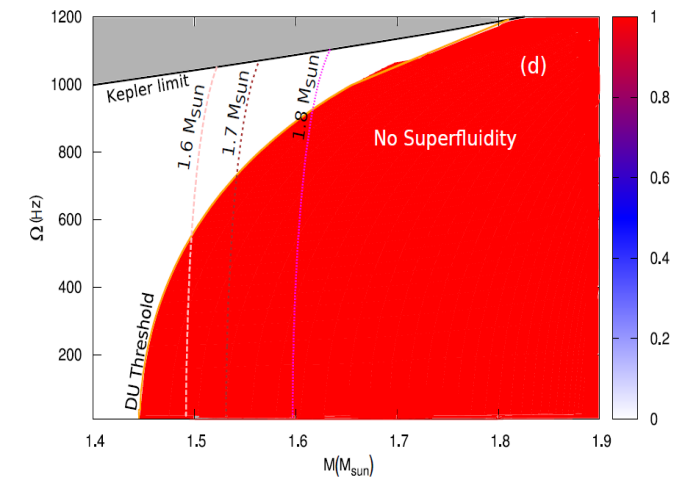
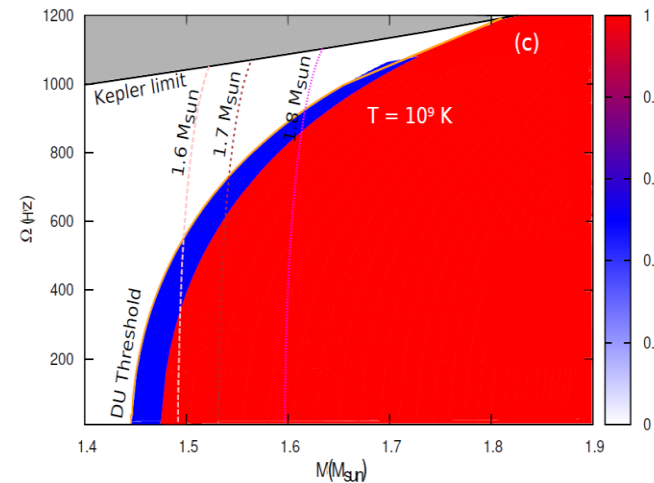
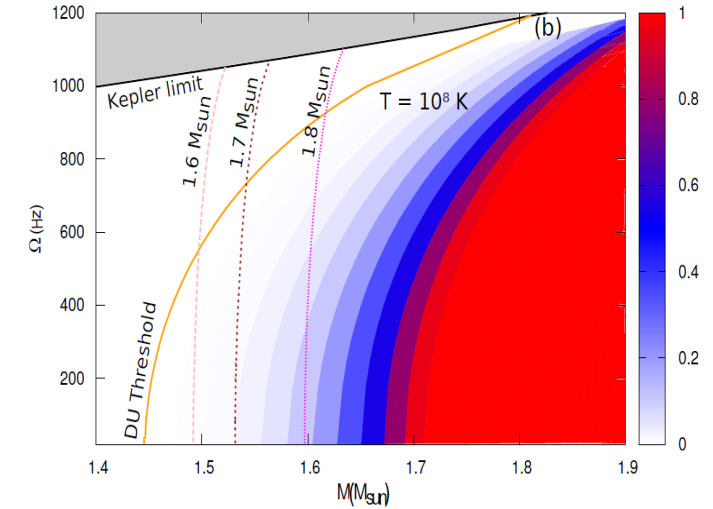
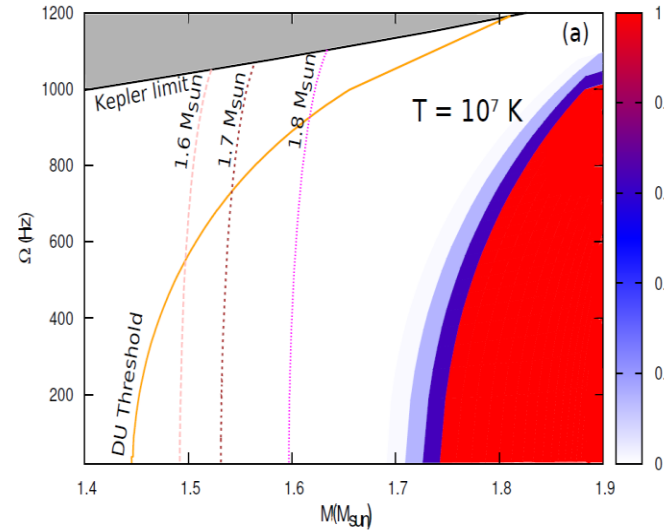


STUDIES



PREVIOUS STUDIES

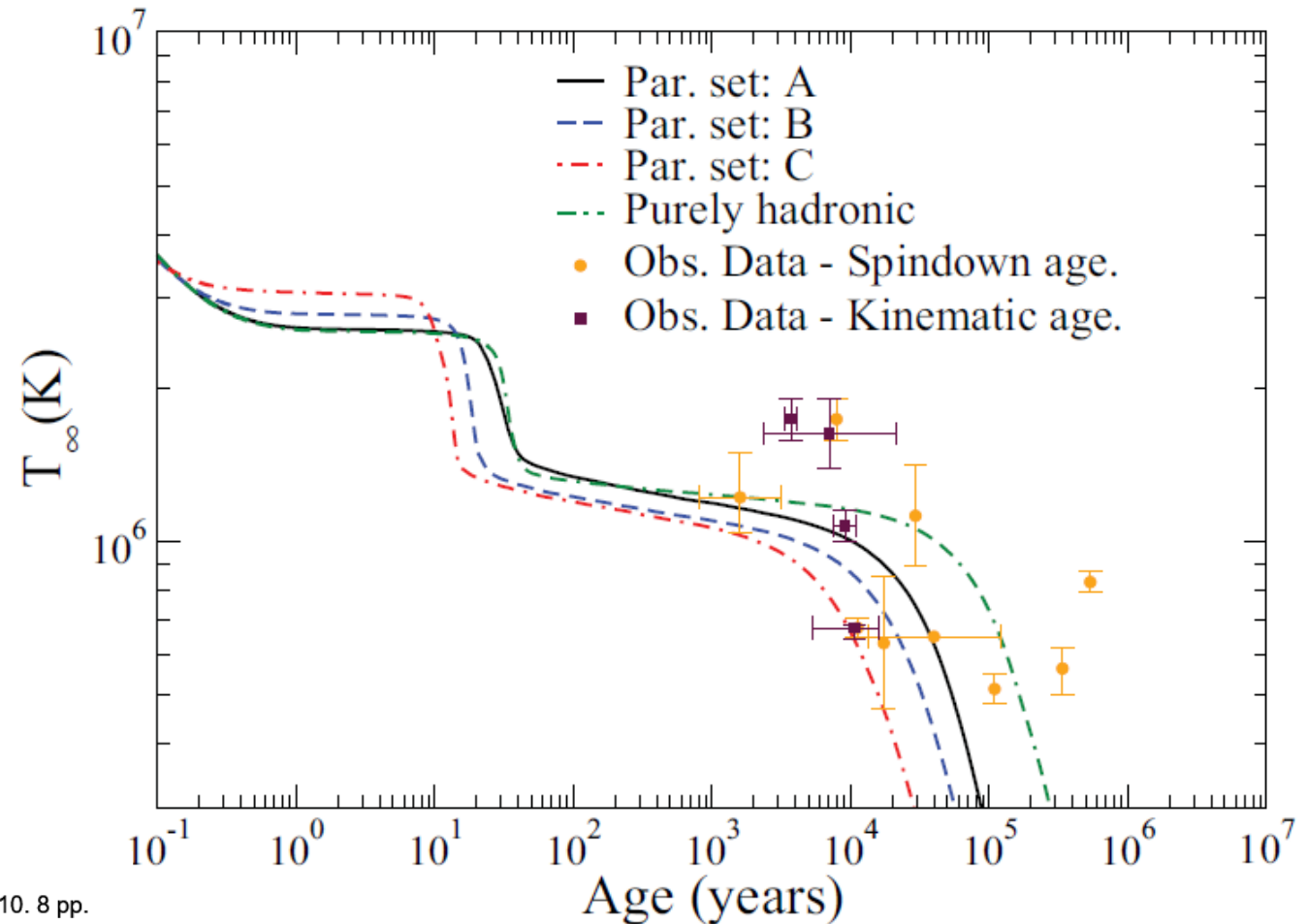
- Direct Urca and superfluidity



PREVIOUS STUDIES

- Quark core impact

Parameter set	M_q/M	R_q (km)	R (km)	M (M_\odot)
A	0.48	8.28	13.26	1.33
	0.60	9.14	13.15	1.55
B	0.62	8.21	12.20	1.33
	0.74	8.86	11.82	1.55
C	0.82	8.21	10.89	1.33
	0.89	8.29	10.03	1.55



A NEW APPROACH

- Consider a dynamic structure and composition.
- Go beyond spherically symmetric stars.

$$P = P(\rho, T = 0, \Omega = 0)$$

$$M = M(\rho, T = 0, \Omega = 0)$$

$$R = R(\rho, T = 0, \Omega = 0)$$

$$\varepsilon = \varepsilon(\rho, T)$$

$$K = K(\rho, T)$$

$$c_v = c_v(\rho, T)$$



$$P = P(\rho, T = 0, \Omega(t), B(t))$$

$$M = M(\rho, T = 0, \Omega(t), B(t))$$

$$R = R(\rho, T = 0, \Omega(t), B(t))$$

$$\varepsilon = \varepsilon(\rho, T, \Omega(t), B(t))$$

$$K = K(\rho, T, \Omega(t), B(t))$$

$$c_v = c_v(\rho, T, \Omega(t), B(t))$$

PROOF OF CONCEPT: - STRUCTURE OF ROTATING NEUTRON STARS

- Metric $ds^2 = -e^{\gamma+\rho} dt^2 + e^{2\alpha}(dr^2 + r^2 d\theta^2) + e^{\gamma-\rho} r^2 \sin^2 \theta (d\phi - \omega dt)^2$
- Sources $T^{\mu\nu} = (\epsilon + p)u^\mu u^\nu + pg^{\mu\nu} + \text{magnetic terms}$
- Einstein's Equation $G^{\mu\nu} = R^{\mu\nu} - \frac{1}{2}g^{\mu\nu}R = 8\pi T^{\mu\nu}$
- Hydrostatic Equilibrium $dp - (\epsilon + p)[d \ln u^t + u^t u_\phi d\Omega] = 0 + \text{magnetic terms}$

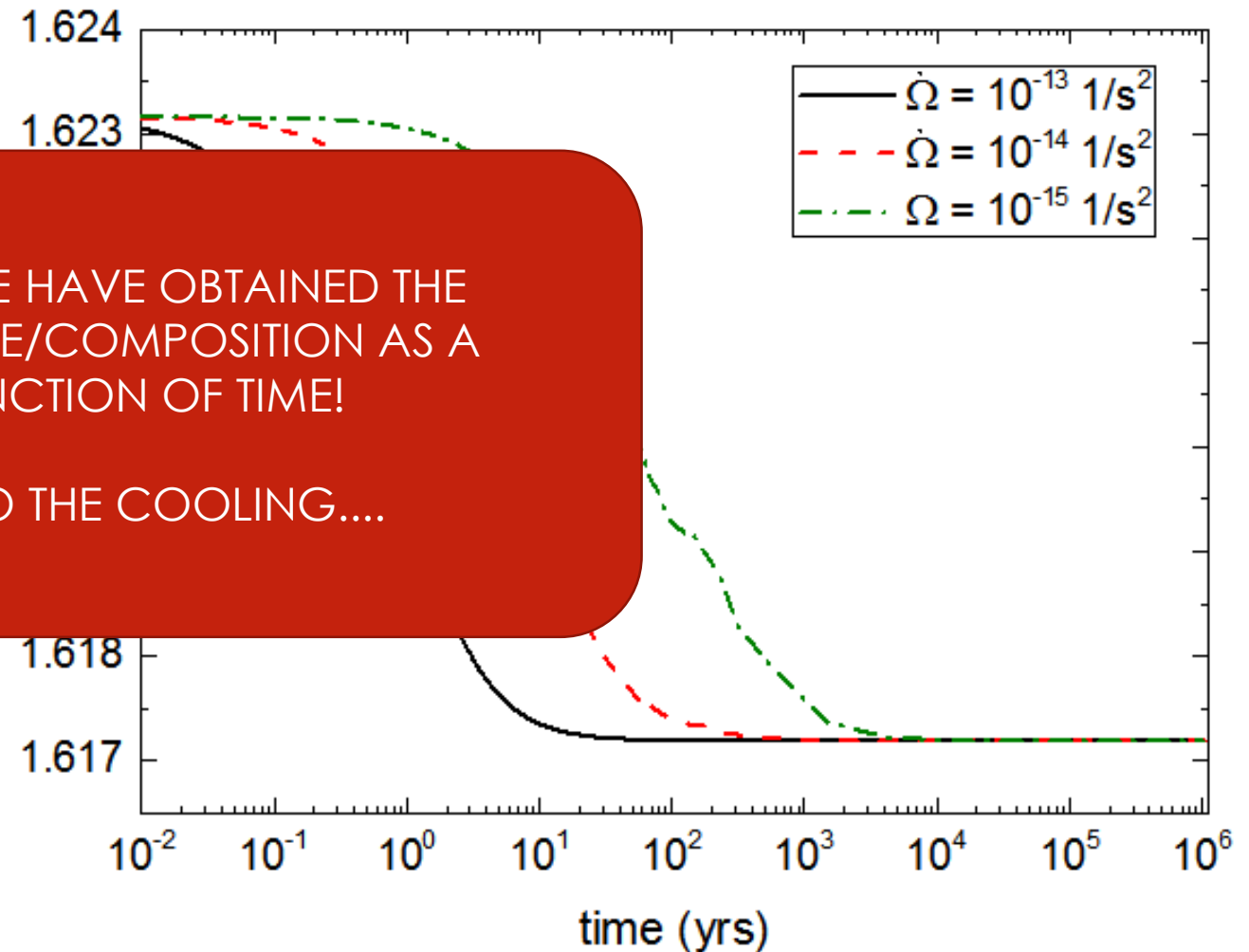
PROOF OF CONCEPT: - STRUCTURE OF ROTATING NEUTRON

- Magnetic Braking model

$$\dot{\Omega} = -K \Omega^n$$

NOW, WE HAVE OBTAINED THE
STRUCTURE/COMPOSITION AS A
FUNCTION OF TIME!

ONTO THE COOLING....



THERMAL EVOLUTION OF AXIS-SYMMETRIC NEUTRON STARS

$$P = P(\rho, T = 0, \Omega(t), B(t))$$

$$M = M(\rho, T = 0, \Omega(t), B(t))$$

$$R = R(\rho, T = 0, \Omega(t), B(t))$$

$$\varepsilon = \varepsilon(\rho, T, \Omega(t), B(t))$$

$$K = K(\rho, T, \Omega(t), B(t))$$

$$c_v = c_v(\rho, T, \Omega(t), B(t))$$



$$\begin{aligned} \partial_r \tilde{H}_{\bar{r}} + \frac{1}{r} \partial_{\theta} \tilde{H}_{\bar{\theta}} &= -r e^{\phi+2\omega} \left(\frac{1}{\Gamma} e^{2\nu} \epsilon + \Gamma C_V \partial_t \tilde{T} \right) \\ &\quad - r \Gamma U e^{\nu+2\phi+\omega} \left(\partial_r \Omega + \frac{1}{r} \partial_{\theta} \Omega \right), \end{aligned}$$

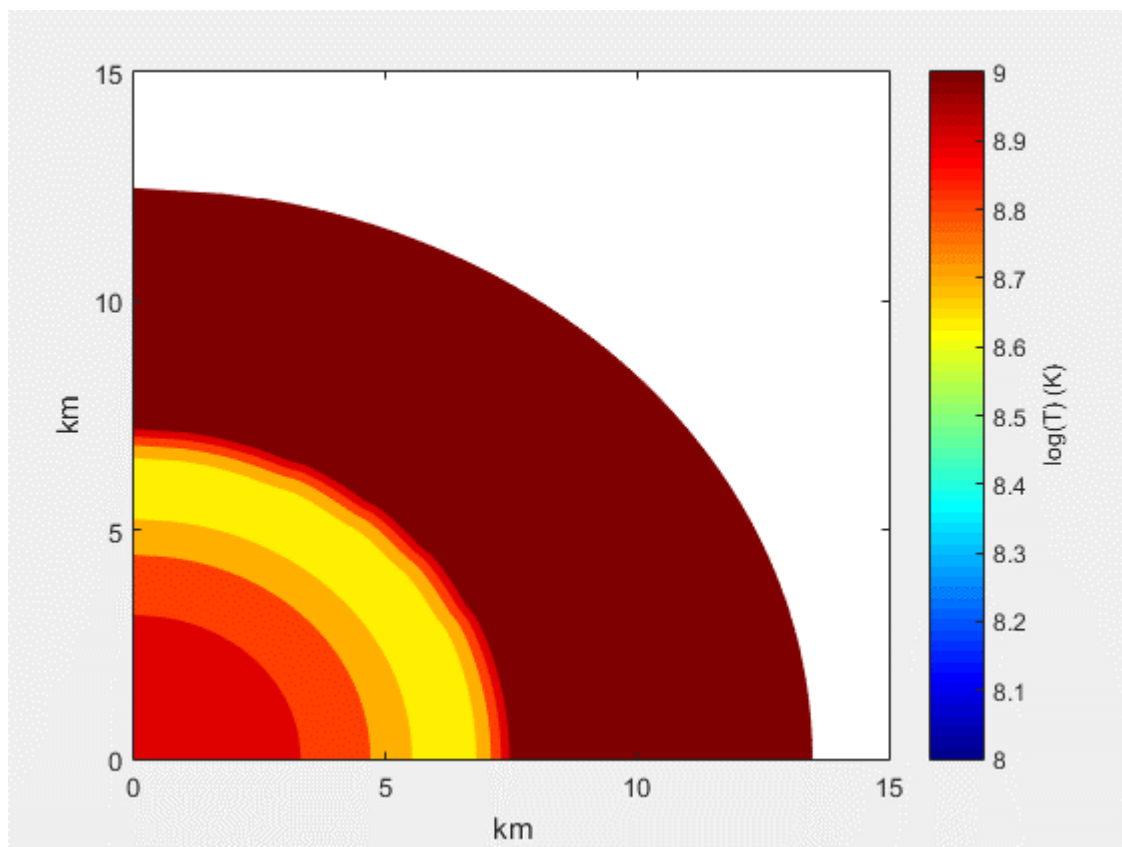
$$\partial_r \tilde{T} = -\frac{1}{r\kappa} e^{\nu-\phi} \tilde{H}_{\bar{r}} - \Gamma^2 U e^{-\nu+\phi} \tilde{T} \partial_r \Omega,$$

$$\frac{1}{r} \partial_{\theta} \tilde{T} = -\frac{1}{r\kappa} e^{-\nu-\phi} \tilde{H}_{\bar{\theta}} - \Gamma^2 U e^{-\nu+\phi} \tilde{T} \frac{1}{r} \partial_{\theta} \Omega$$

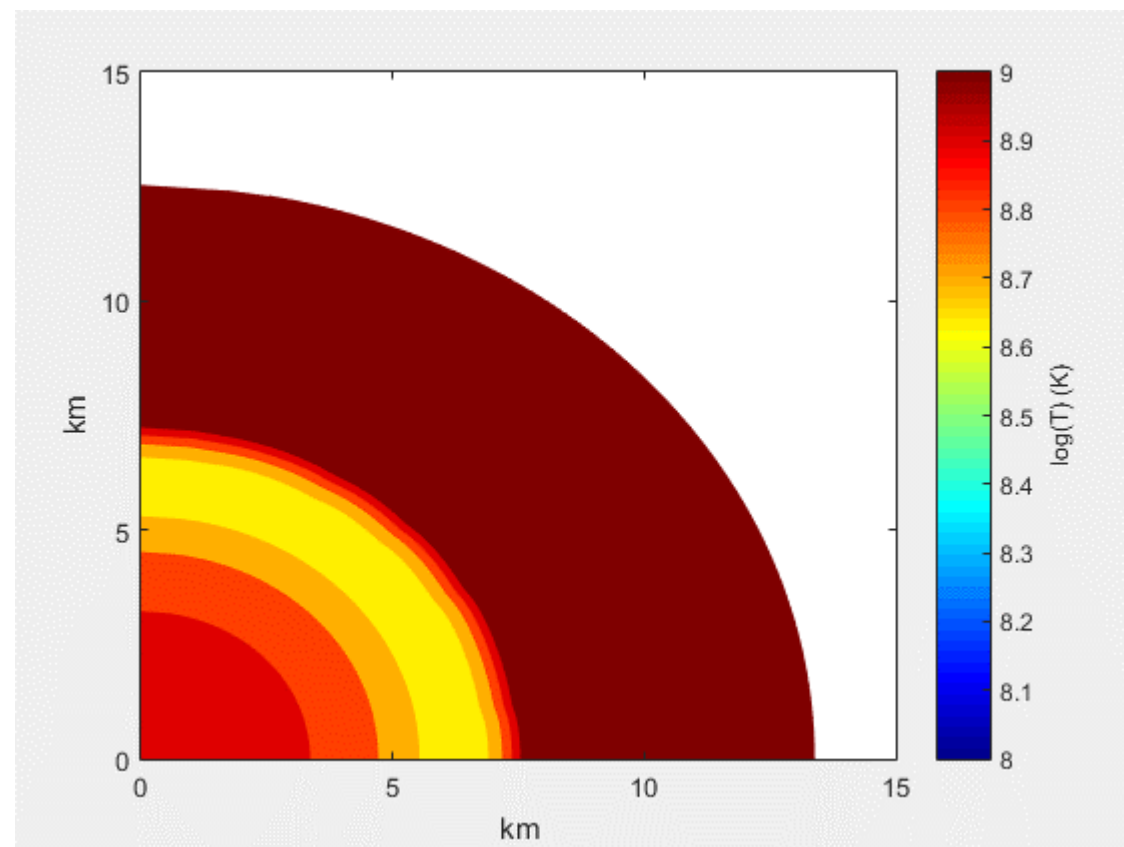
$$\Gamma U \partial_t \tilde{T} = -\frac{1}{r\kappa} e^{-\omega-\phi} \tilde{H}_{\bar{\varphi}},$$

THERMAL EVOLUTION OF AXIS-SYMMETRIC NEUTRON STARS

- $M_0 = 1.8 M_{\text{sun}}$, $\Omega_0 = 500$ Hz



$$\dot{\Omega} = 10^{-15} \text{ s}^{-2}$$

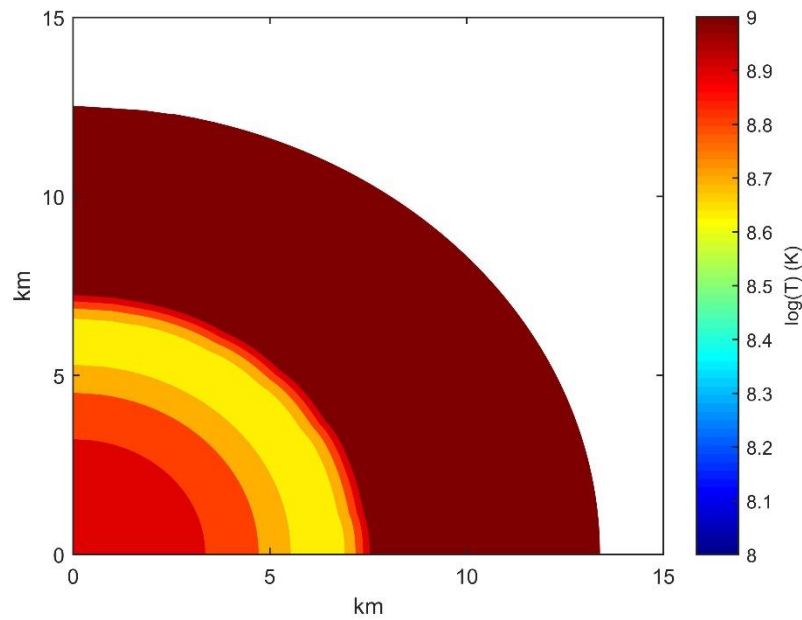


$$\dot{\Omega} = 10^{-13} \text{ s}^{-2}$$

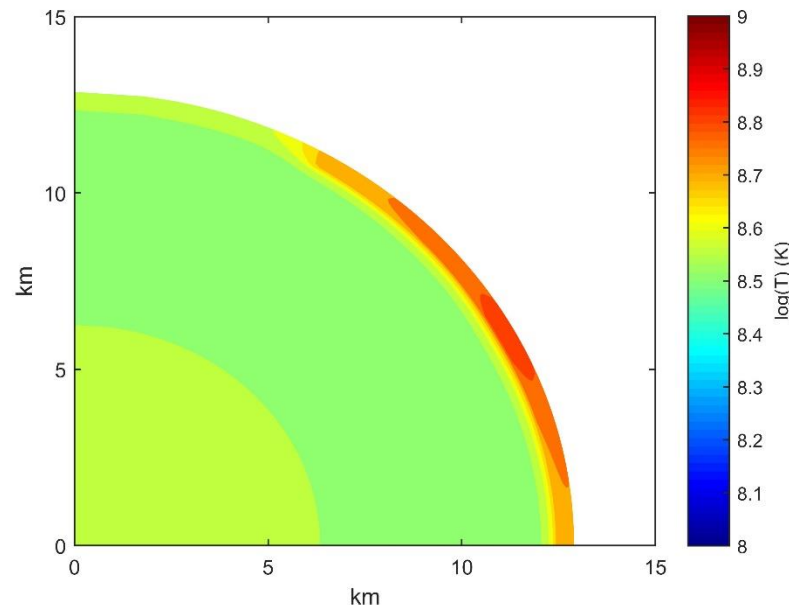
THERMAL EVOLUTION OF AXIS-SYMMETRIC NEUTRON STARS

- $M_0 = 1.8 M_{\text{sun}}, \Omega_0 = 500 \text{ Hz}$

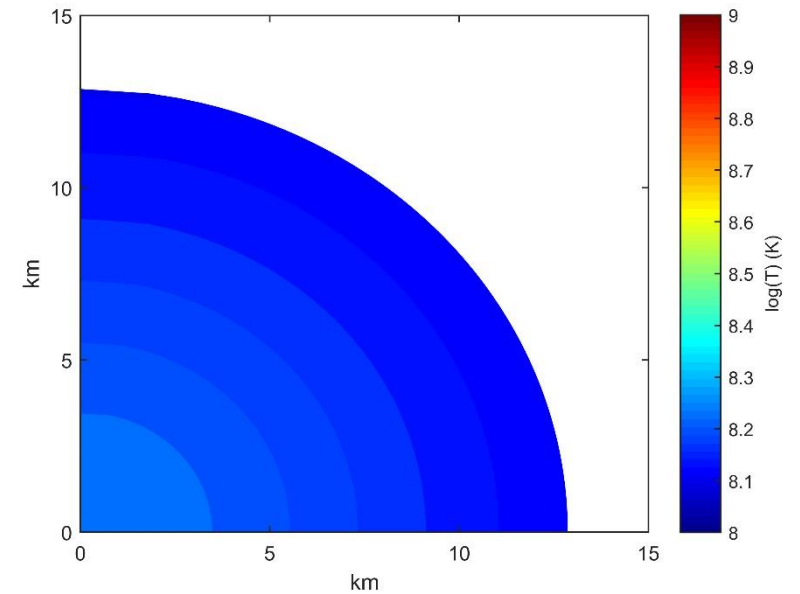
$$\dot{\Omega} = 10^{-13} \text{ s}^{-2}$$



0.10 years



36 years

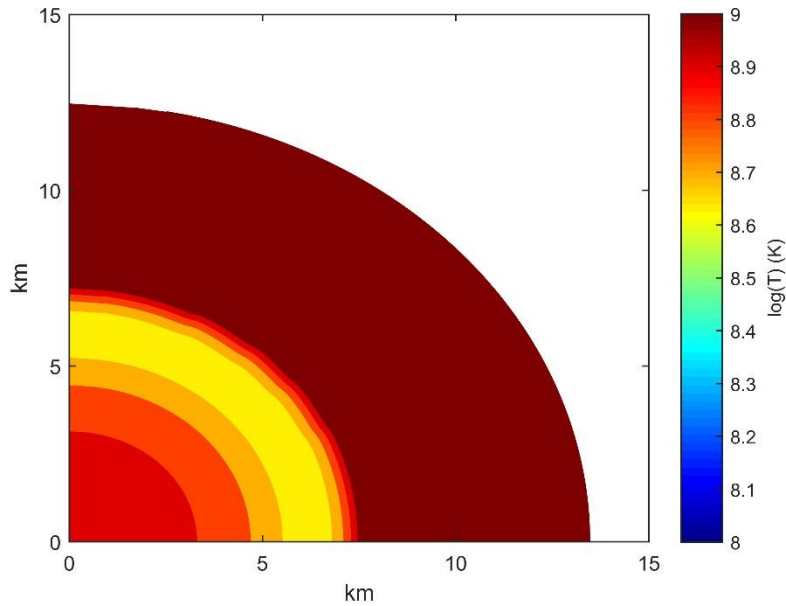


8.0E5 years

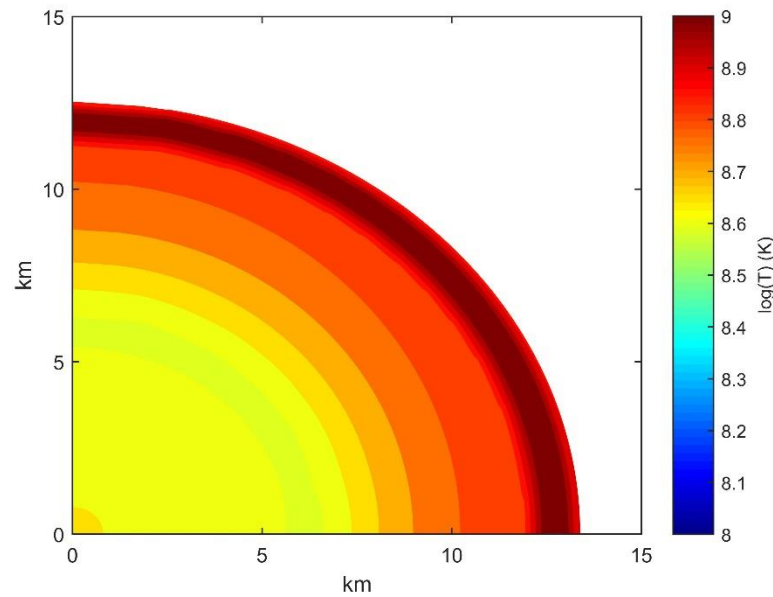
THERMAL EVOLUTION OF AXIS-SYMMETRIC NEUTRON STARS

- $M_0 = 1.8 M_{\text{sun}}, \Omega_0 = 500 \text{ Hz}$

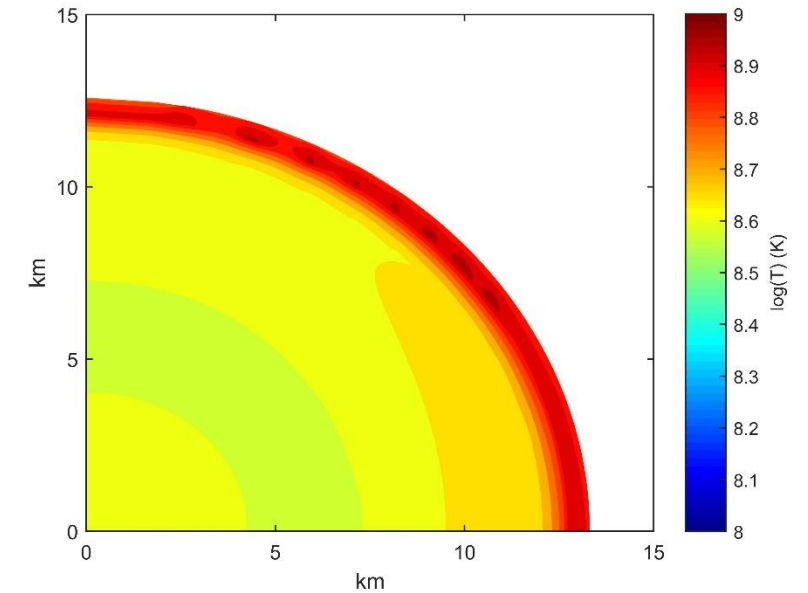
$$\dot{\Omega} = 10^{-15} \text{ s}^{-2}$$



0.10 years



10.05 years

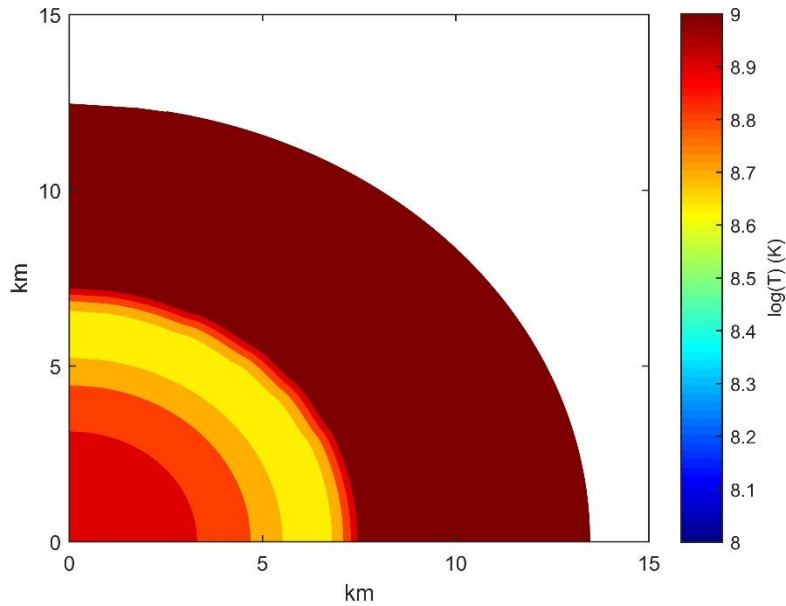


22.45 years

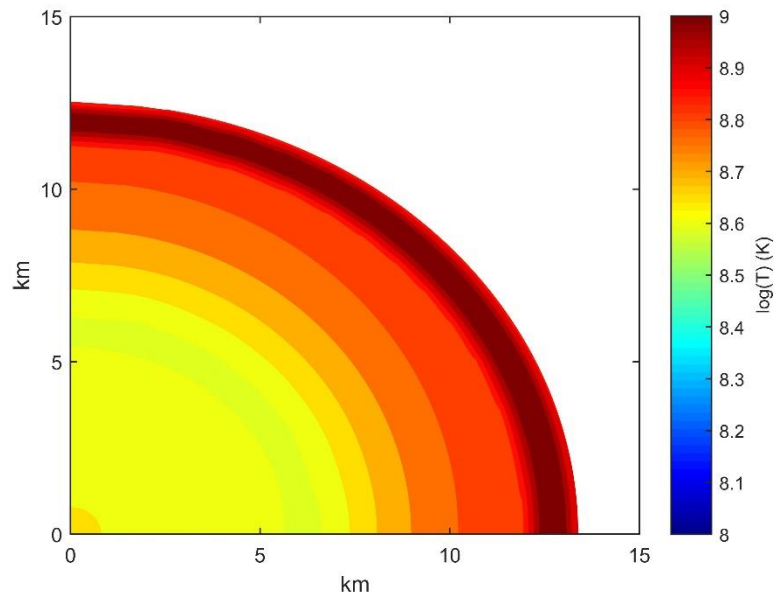
THERMAL EVOLUTION OF AXIS-SYMMETRIC NEUTRON STARS

- $M_0 = 1.8 M_{\text{sun}}$, $\Omega_0 = 500 \text{ Hz}$

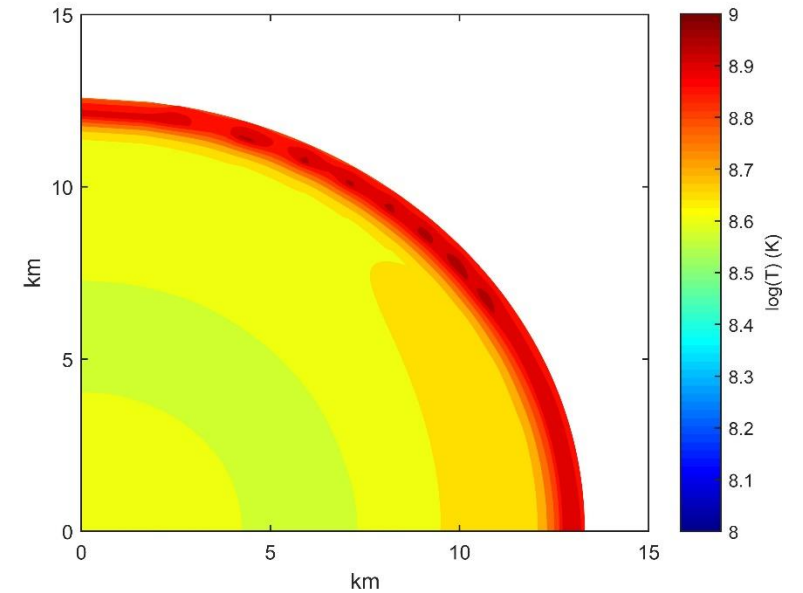
$$\dot{\Omega} = 10^{-13} \text{ s}^{-2}$$



0.10 years



10.05 years

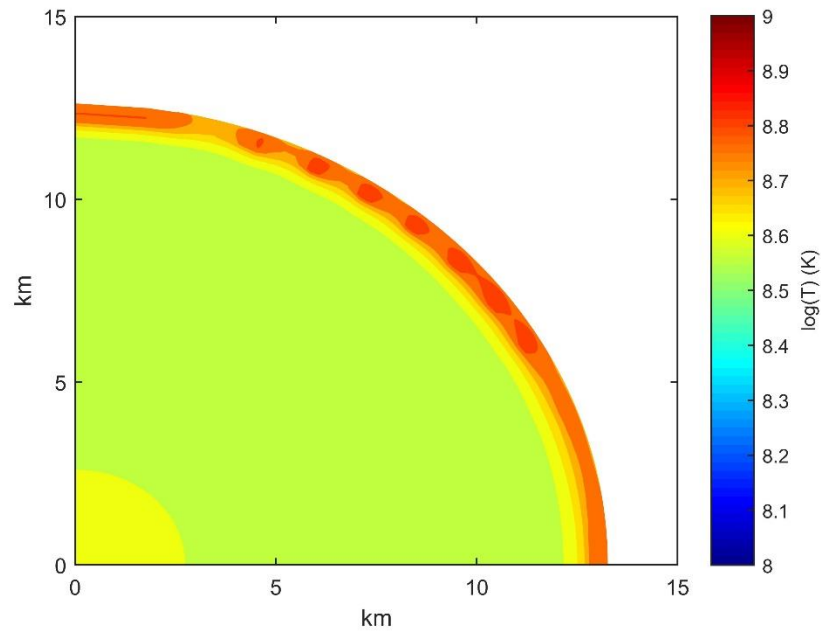


22.45 years

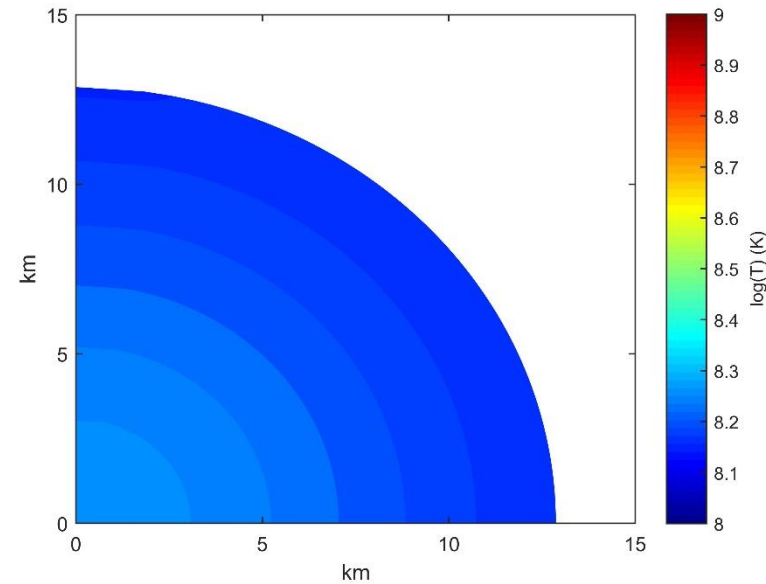
THERMAL EVOLUTION OF AXIS-SYMMETRIC NEUTRON STARS

- $M_0 = 1.8 M_{\text{sun}}, \Omega_0 = 500 \text{ Hz}$

$$\dot{\Omega} = 10^{-15} s^{-2}$$



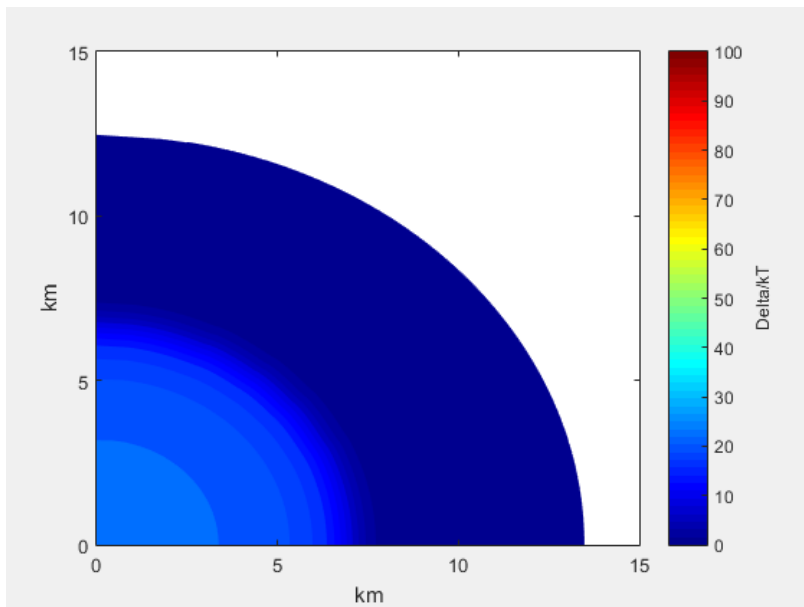
31.67 years



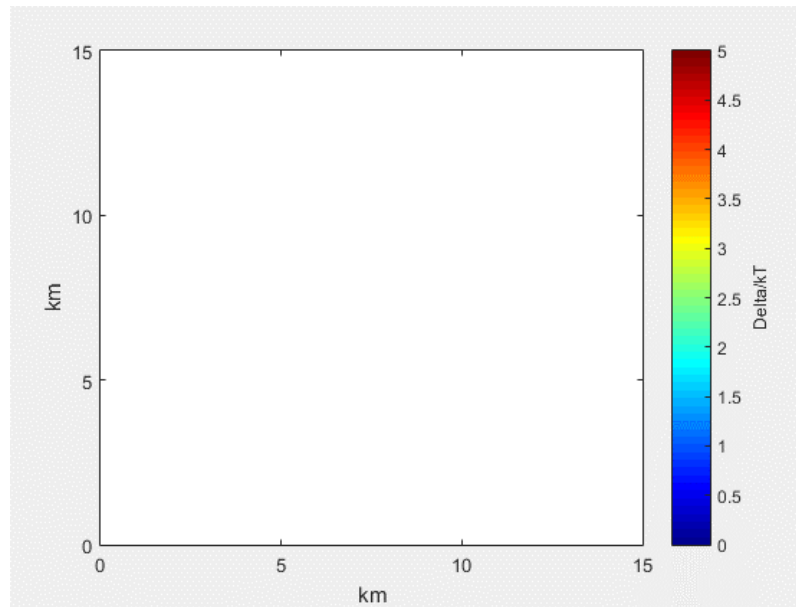
5.0E5 years

THERMAL EVOLUTION OF AXIS-SYMMETRIC NEUTRON STARS

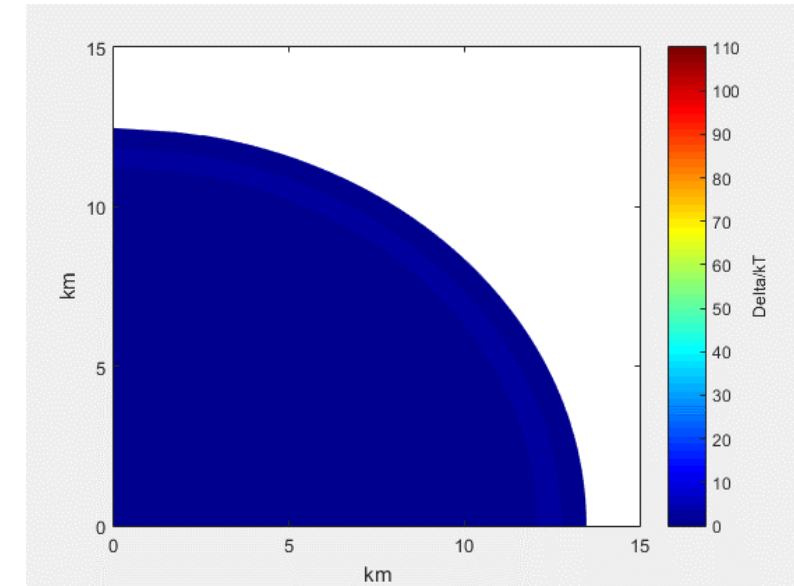
- $M_0 = 1.8 M_{\text{sun}}$, $\Omega_0 = 500 \text{ Hz}$ -> MICROSCOPIC PROPERTIES



Proton Singlet GAP

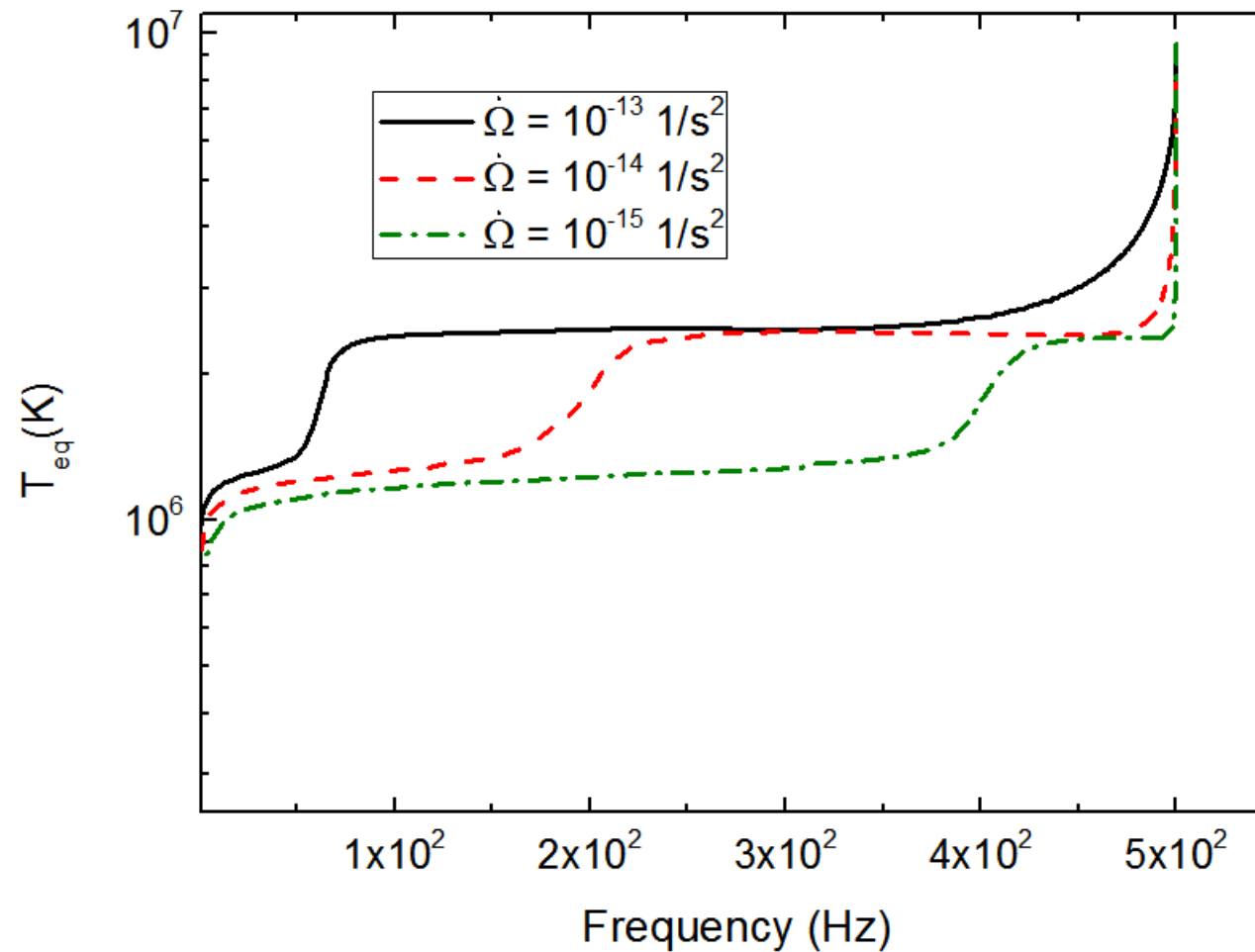


Neutron Triplet GAP



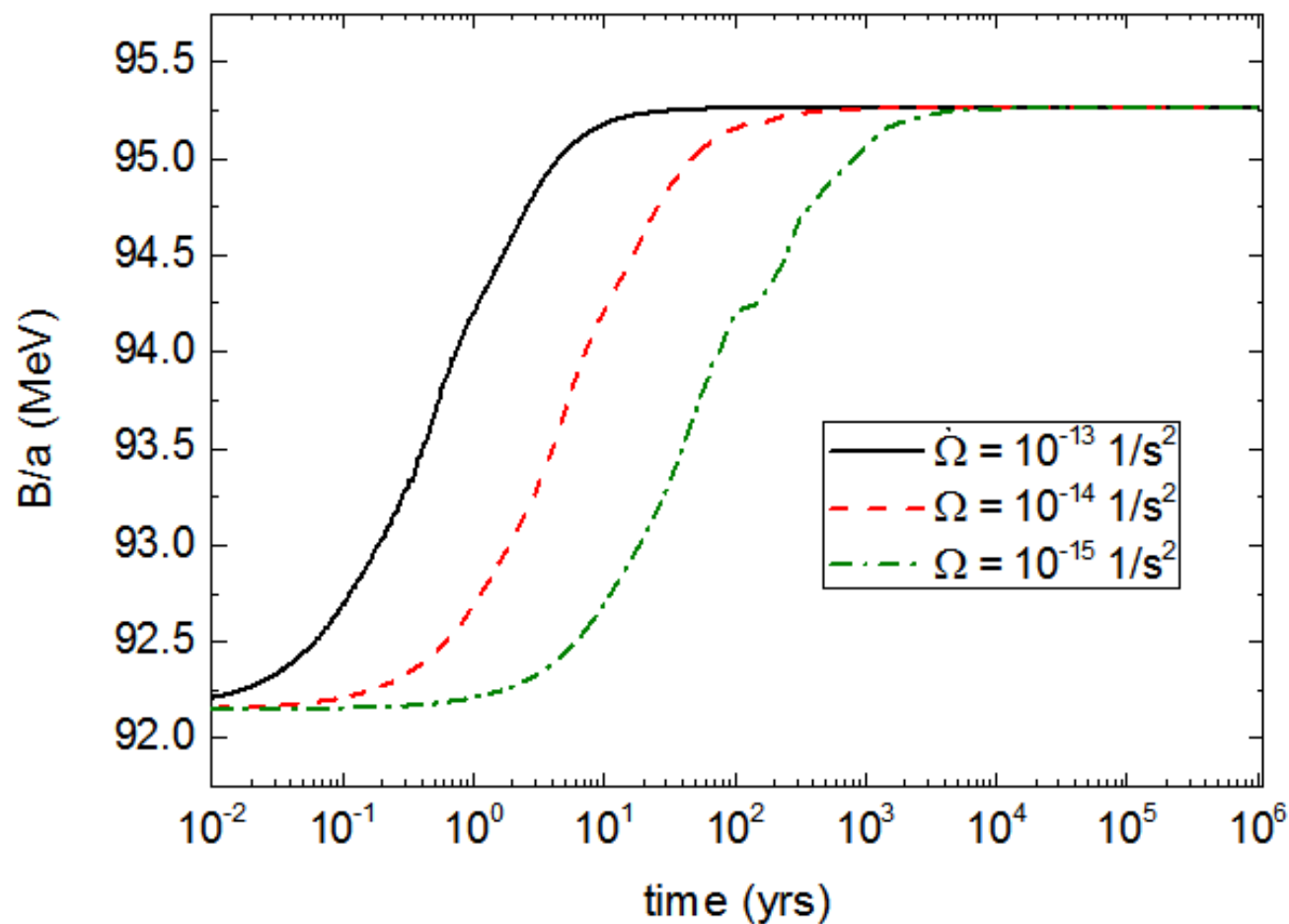
Neutron Singlet GAP

THERMAL-ROTATIONAL EVOLUTION



HEATING(?)

- Possibly
- Not for the magnetic breaking model...





PERSPECTIVES

- We are now in a position to deal fully with axis-symmetric neutron stars thermal evolution.
- We can also consider a dynamic structure/composition.
- Investigate different neutron stars evolution:
 - Magnetic
 - Spin-Up/accreting