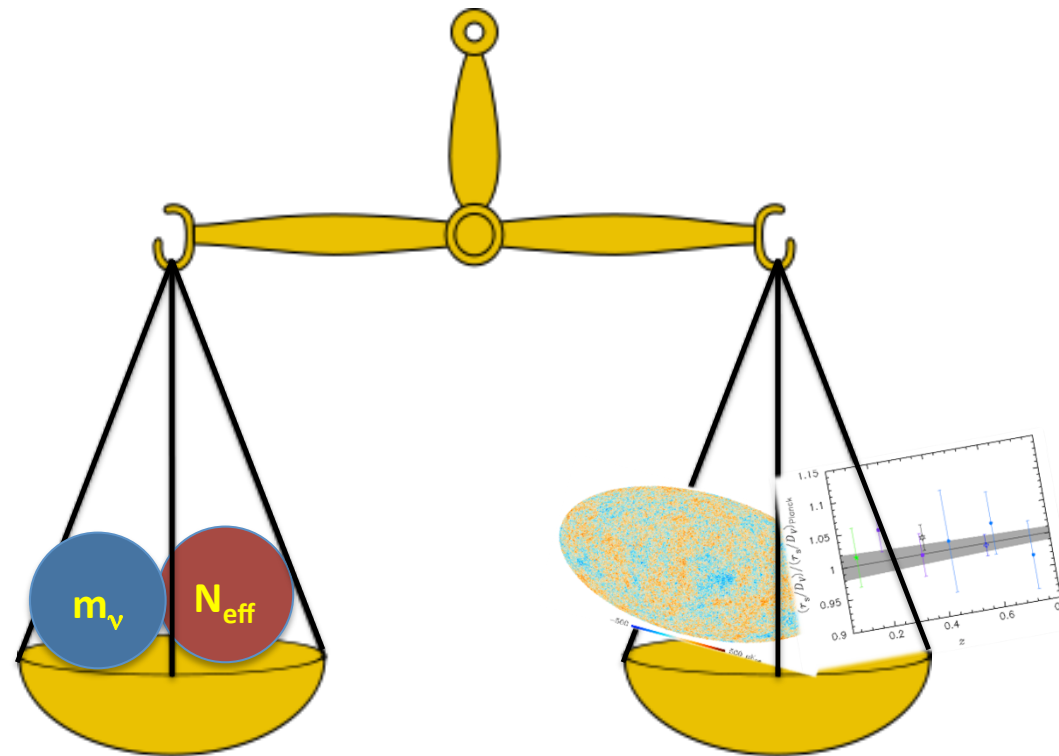


Neutrino properties from cosmological observables after Planck



ASTROPARTICLES
Astroparticles and High Energy Physics Group

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(IFIC Valencia)

Genova
22 October 2015



VNIVERSITAT
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Outline



Introduction: the Cosmic Neutrino Background

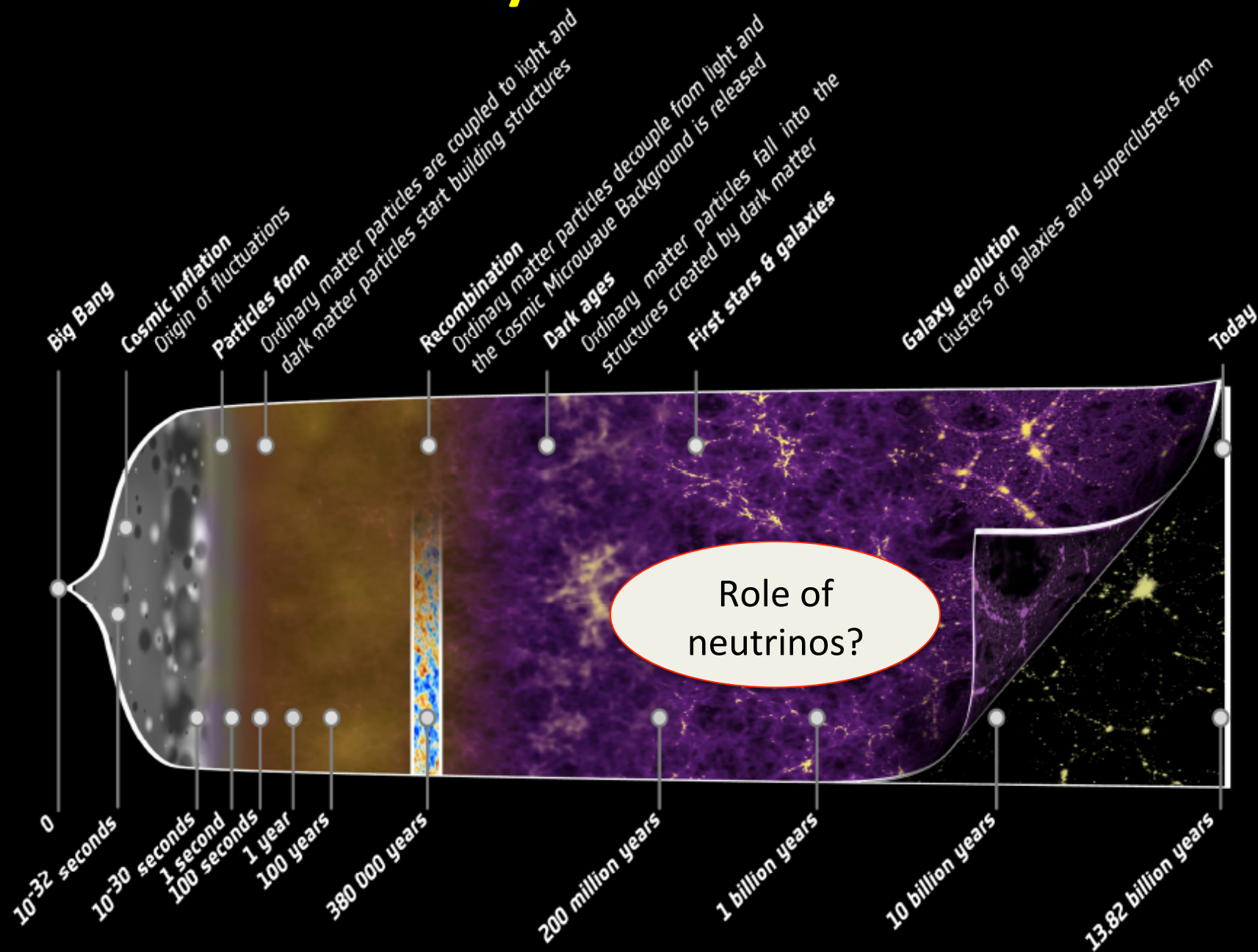
Neutrinos as Dark Matter

The radiation content of the Universe (N_{eff})

Bounds on neutrino properties from Planck (& other cosmo data)

Introduction: the Cosmic Neutrino Background

History of the Universe



History of the Universe

Neutrinos coupled
by weak interactions

BIG BANG

Inflation

t 10^{-44} 10^{-37} s
 T 10^{32} 10^{28}
 E 10^{19} 10^{15}

high-energy cosmic rays
Tevatron
RHIC

possible dark matter relics

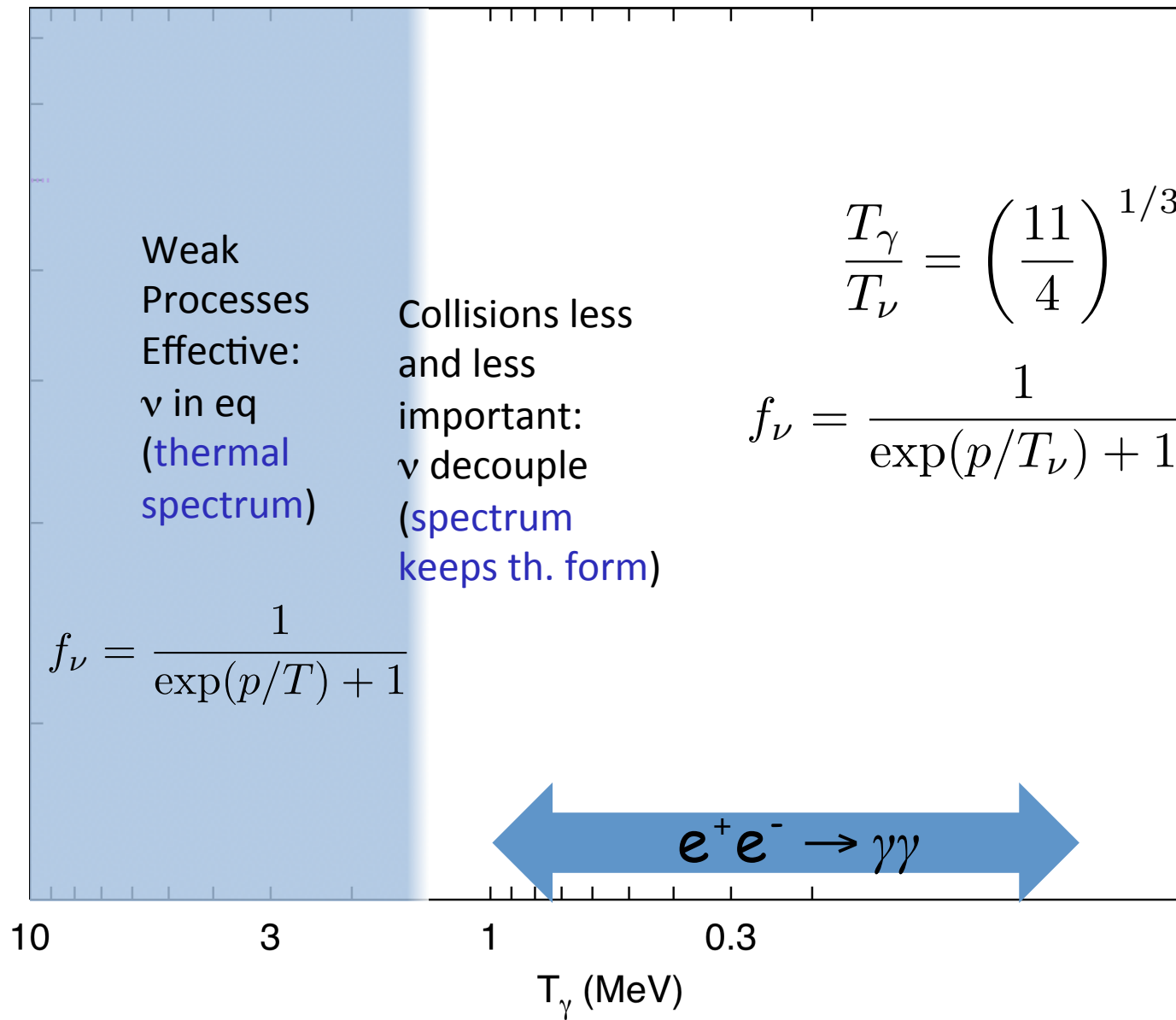
$T \sim \text{MeV}$
 $t \sim \text{sec}$

Primordial
Nucleosynthesis

Key: W, Z bosons photon
q quark meson galaxy
g gluon baryon star
e electron ion atom black hole
 μ muon τ tau
 ν neutrino

Particle Data Group, LBNL, © 2008. Supported by DOE and

ν Decoupling and $e^\pm$ annihilations

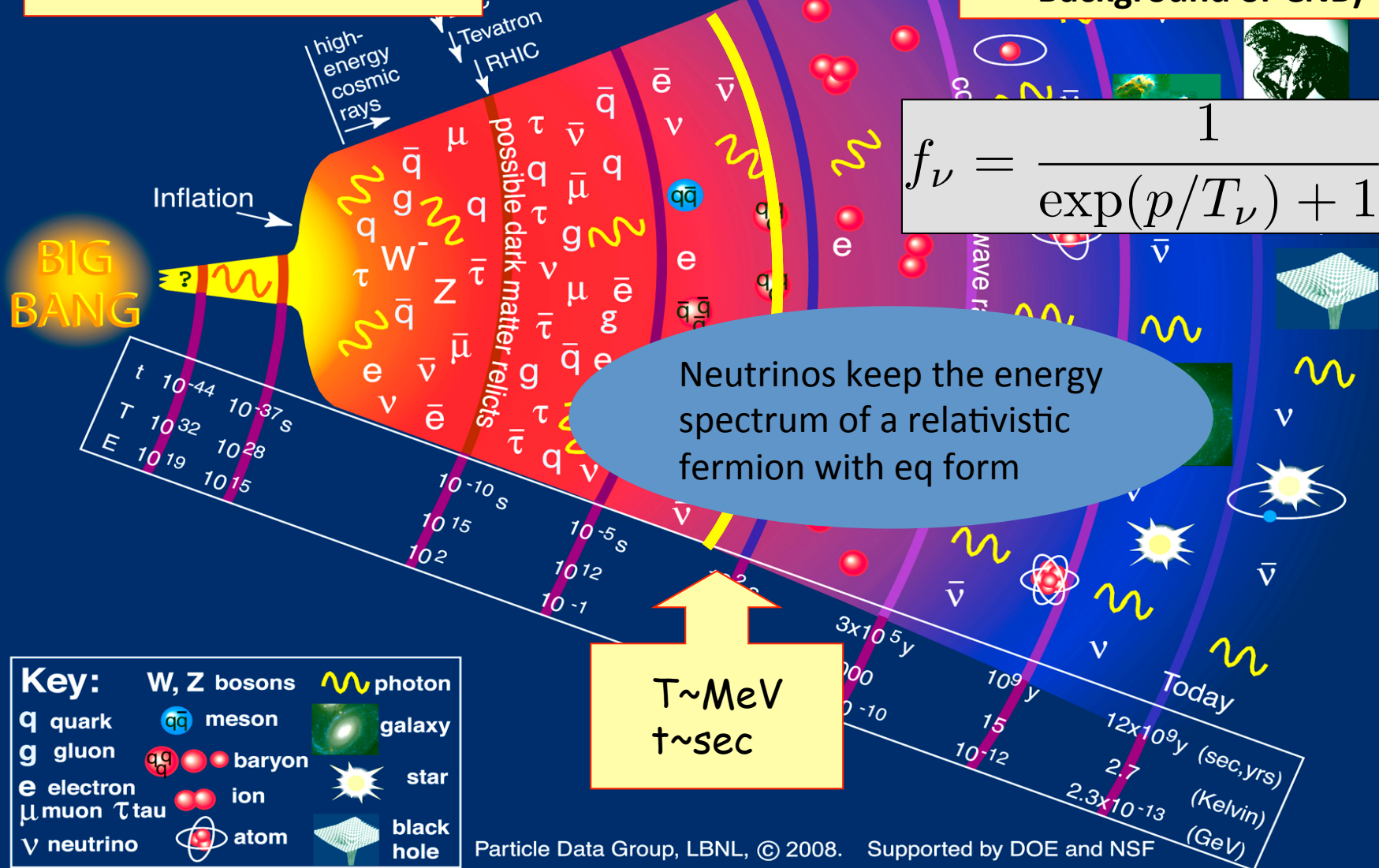


Expansion of the universe

History of the Universe

Neutrinos coupled
by weak interactions

Decoupled neutrinos
(Cosmic Neutrino
Background or CNB)



History of the Universe

BIG BANG

Inflation →

Accelerators
↓ LHC
↓ Tevatron
↓ RHIC

high-energy cosmic rays →

possible

Relativistic neutrinos

$T \sim m\nu$

cosmic microwave radiation visible

At least 2 species are NR today

quarks ($q, \bar{q}$), leptons ($e, \mu, \tau, \bar{\nu}, \nu$), gluons (g), photons (γ)

- The CNB contributes to **radiation at early times** and to **matter at late times** (info on the number of neutrinos and their masses)
- Cosmological observables can be used to **test standard or non-standard neutrino properties**

The Cosmic Neutrino Background

Neutrinos decoupled at $T \sim \text{MeV}$, keeping a spectrum as that of a relativistic species

$$f_\nu(p, T) = \frac{1}{e^{p/T_\nu} + 1}$$

- Number density

$$n_\nu = \int \frac{d^3 p}{(2\pi)^3} f_\nu(p, T_\nu) = \frac{3}{11} n_\gamma = \frac{6\zeta(3)}{11\pi^2} T_{CMB}^3$$

- Energy density

$$\rho_{\nu_i} = \int \sqrt{p^2 + m_{\nu_i}^2} \frac{d^3 p}{(2\pi)^3} f_\nu(p, T_\nu) \rightarrow \frac{7\pi^2}{120} \left(\frac{4}{11}\right)^{4/3} T_{CMB}^4 \quad \text{Massless}$$

The Cosmic Neutrino Background

Neutrinos decoupled at $T \sim \text{MeV}$, keeping a spectrum as that of a relativistic species

$$f_\nu(p, T) = \frac{1}{e^{p/T_\nu} + 1}$$

- Number density

At present $112 (\nu + \bar{\nu}) \text{ cm}^{-3}$ per flavour

- Energy density

Contribution to the energy density of the Universe

$$\Omega_\nu h^2 \simeq 1.7 \times 10^{-5} \quad \text{Massless} \quad \Omega_i = \rho_i / \rho_{\text{crit}}$$

The Cosmic Neutrino Background

Neutrinos decoupled at $T \sim \text{MeV}$, keeping a spectrum as that of a relativistic species

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- Number density

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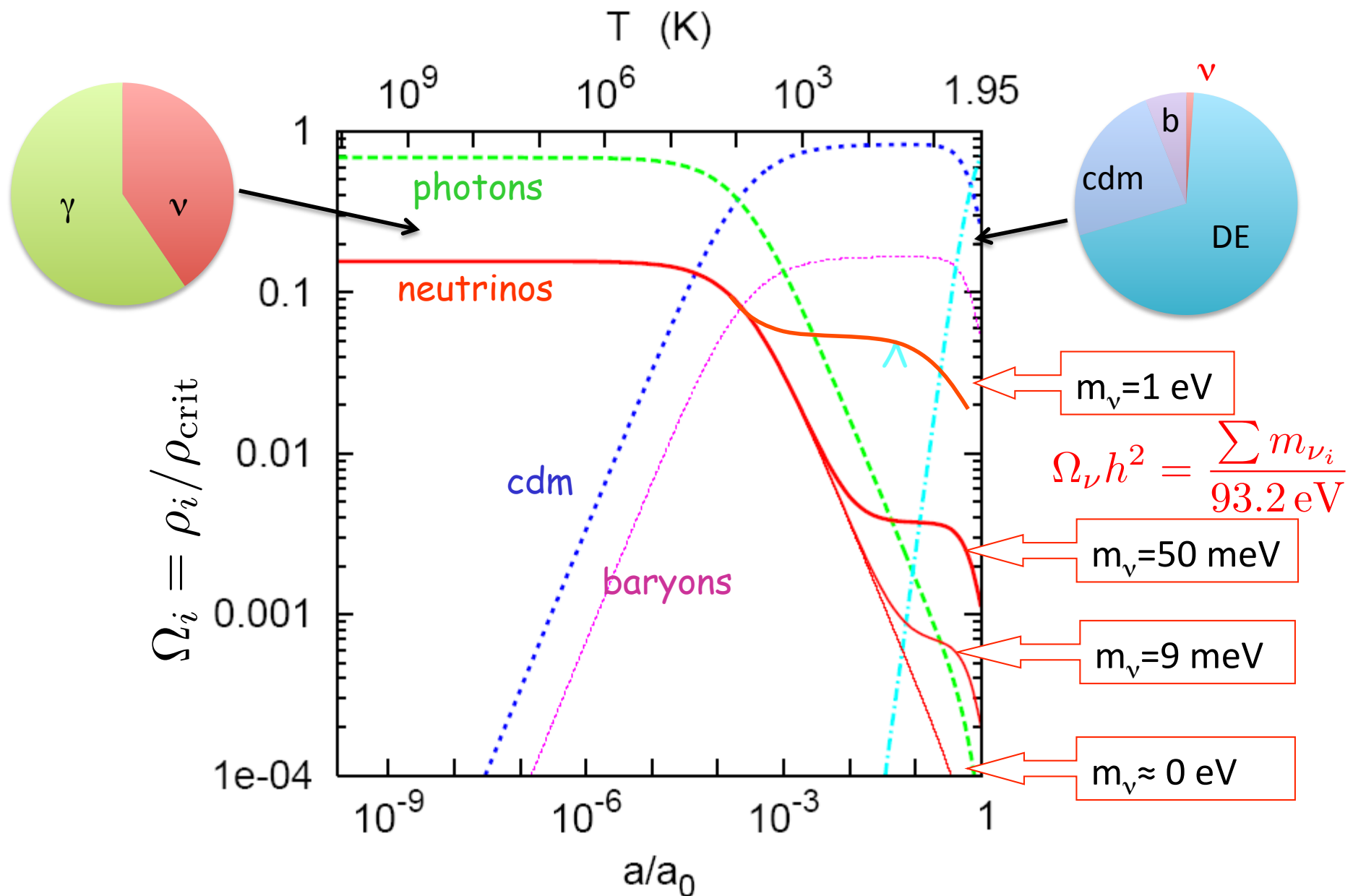
- Energy density

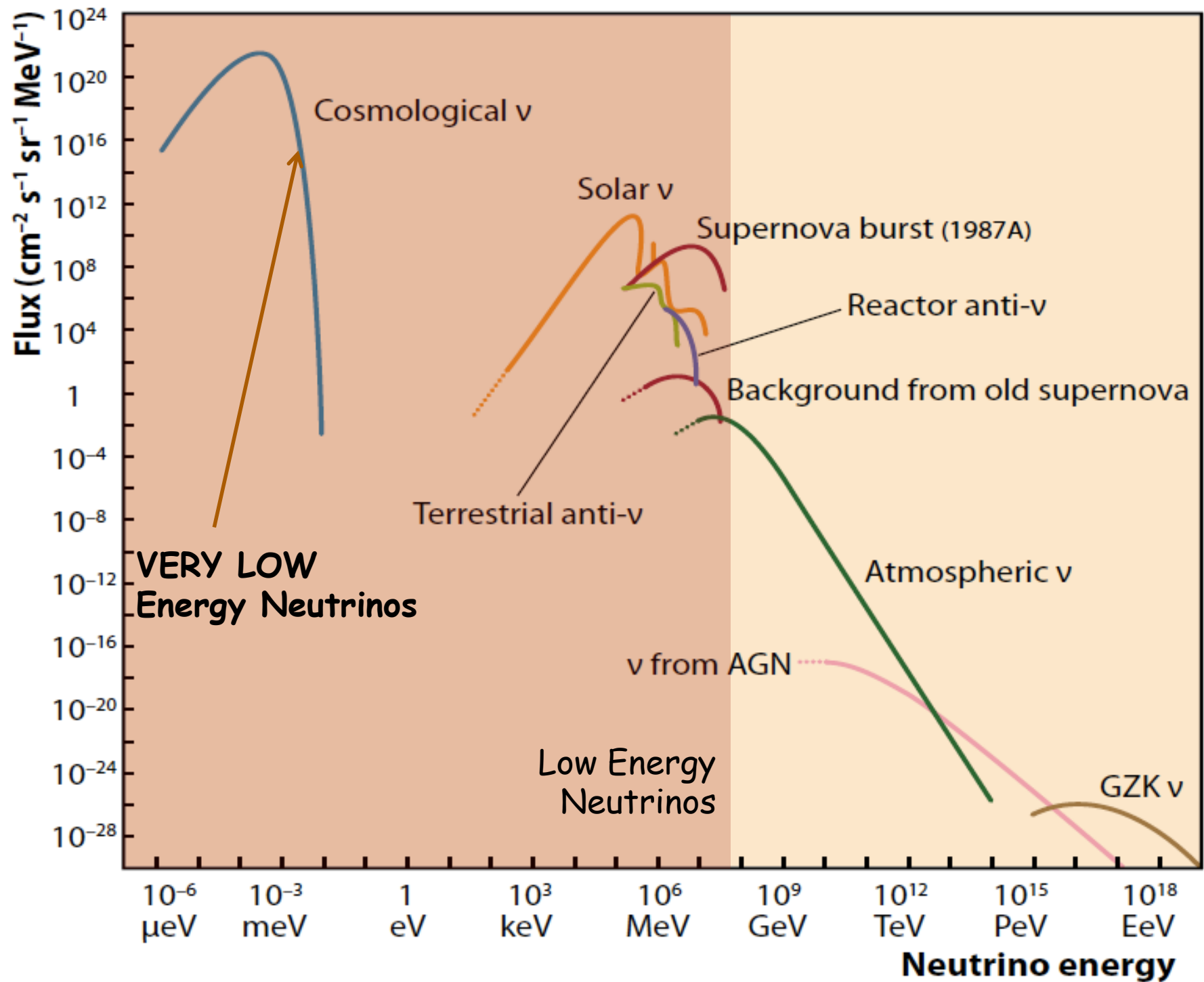
Contribution to the energy density of the Universe

$$\Omega_\nu h^2 \simeq 1.7 \times 10^{-5} \quad \text{Massless}$$

$$\Omega_\nu h^2 = \frac{\sum m_{\nu_i}}{93.2 \text{ eV}} \quad \begin{array}{l} \text{Massive} \\ m_\nu \gg T \end{array}$$

Background densities: 1 MeV $\rightarrow$ now

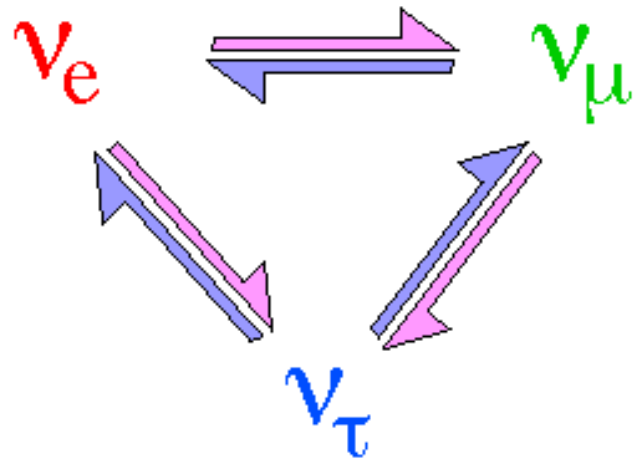




Neutrinos as Dark Matter

We know that flavour neutrino oscillations exist

From present evidences of oscillations from experiments measuring atmospheric, solar, reactor and accelerator neutrinos

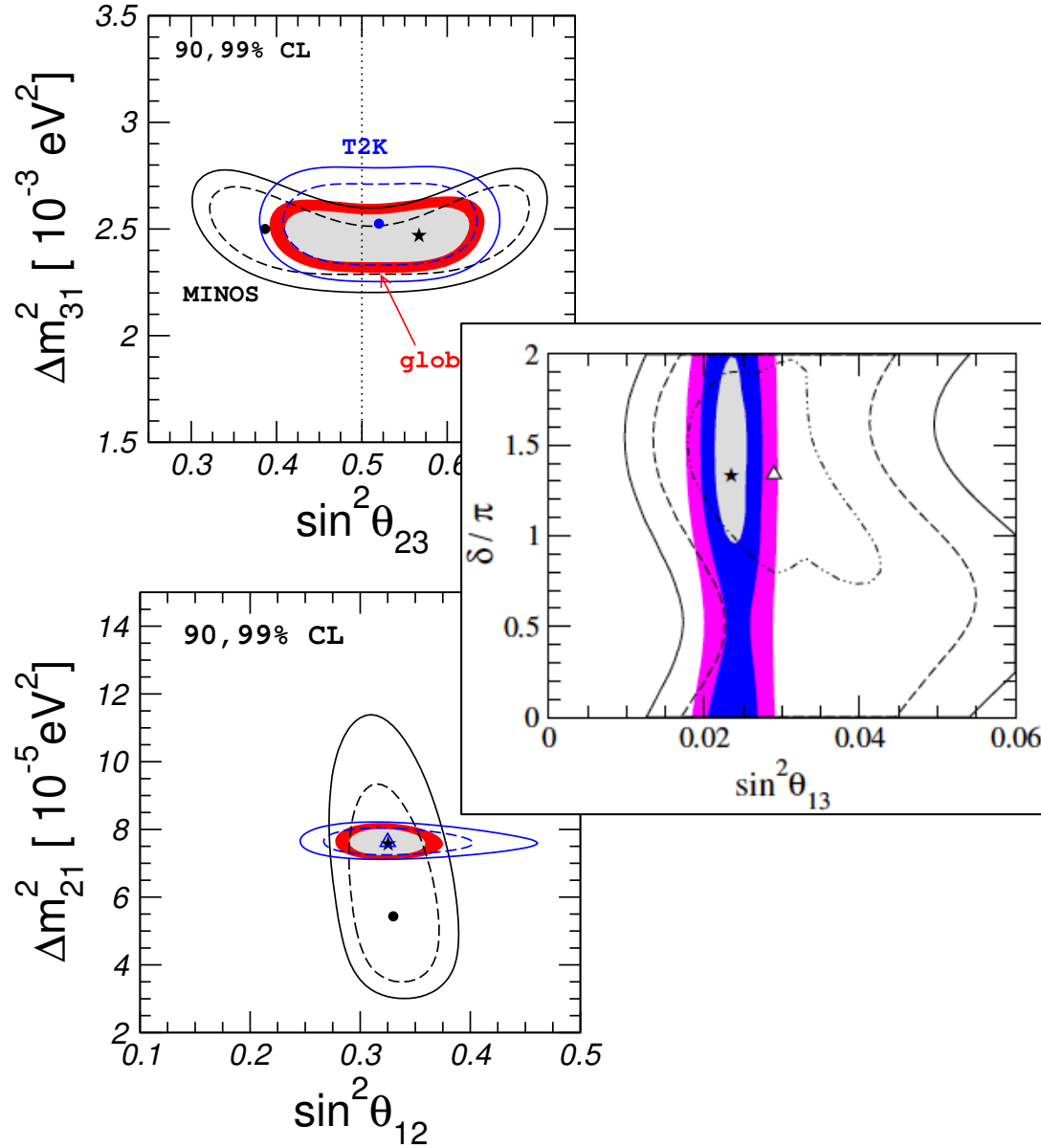


$$(e, \mu, \tau) \leftrightarrow (\nu_1, \nu_2, \nu_3)$$

$$\nu_{\alpha L} = \sum_{i=1}^3 U_{\alpha i} \nu_{iL}, \quad (\alpha = e, \mu, \tau)$$

$$\begin{array}{c} \nu_e \\ \nu_\mu \\ \nu_\tau \end{array} \begin{bmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{bmatrix} \times \text{diag}(e^{i\alpha_1/2}, e^{i\alpha_2/2}, 1) .$$

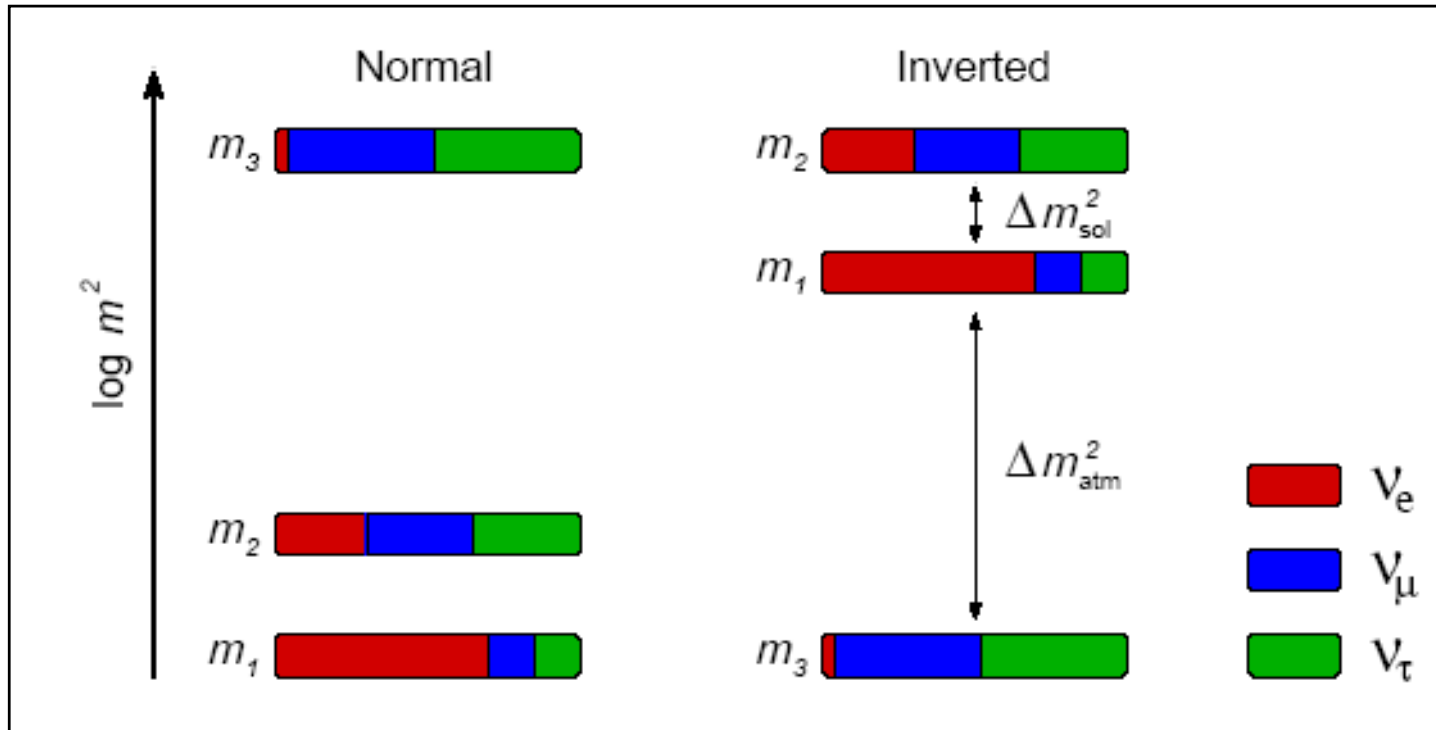
Forero, Tórtola & Valle,
PRD 90 (2014) 093006



parameter	best fit $\pm 1\sigma$	2σ range	3σ range
Δm_{21}^2 [10 ⁻⁵ eV ²]	$7.60^{+0.19}_{-0.18}$	7.26–7.99	7.11–8.18
$ \Delta m_{31}^2 $ [10 ⁻³ eV ²] (NH)	$2.48^{+0.05}_{-0.07}$	2.35–2.59	2.30–2.65
$ \Delta m_{31}^2 $ [10 ⁻³ eV ²] (IH)	$2.38^{+0.05}_{-0.06}$	2.26–2.48	2.20–2.54
$\sin^2 \theta_{12}/10^{-1}$	3.23 ± 0.16	2.92–3.57	2.78–3.75
$\theta_{12}/^\circ$	34.6 ± 1.0	32.7–36.7	31.8–37.8
$\sin^2 \theta_{23}/10^{-1}$ (NH)	$5.67^{+0.32}_{-1.24}^a$	4.14–6.23	3.93–6.43
$\theta_{23}/^\circ$	$48.9^{+1.8}_{-7.2}$	40.0–52.1	38.8–53.3
$\sin^2 \theta_{23}/10^{-1}$ (IH)	$5.73^{+0.25}_{-0.39}$	4.35–6.21	4.03–6.40
$\theta_{23}/^\circ$	$49.2^{+1.5}_{-2.3}$	41.3–52.0	39.4–53.1
$\sin^2 \theta_{13}/10^{-2}$ (NH)	2.26 ± 0.12	2.02–2.50	1.90–2.62
$\theta_{13}/^\circ$	$8.6^{+0.3}_{-0.2}$	8.2–9.1	7.9–9.3
$\sin^2 \theta_{13}/10^{-2}$ (IH)	2.29 ± 0.12	2.05–2.52	1.93–2.65
$\theta_{13}/^\circ$	8.7 ± 0.2	8.2–9.1	8.0–9.4
δ/π (NH)	$1.41^{+0.55}_{-0.40}$	0.00–2.0	0.0–2.0
$\delta/^\circ$	254^{+99}_{-72}	0–360	0–360
δ/π (IH)	1.48 ± 0.31	0.00–0.09 & 0.86–2.0	0.0–2.0
$\delta/^\circ$	266 ± 56	0–16 & 155–360	0–360

see also Fogli et al, PRD 89 (2014) 093018; González-García et al, JHEP 1411 (2014) 052

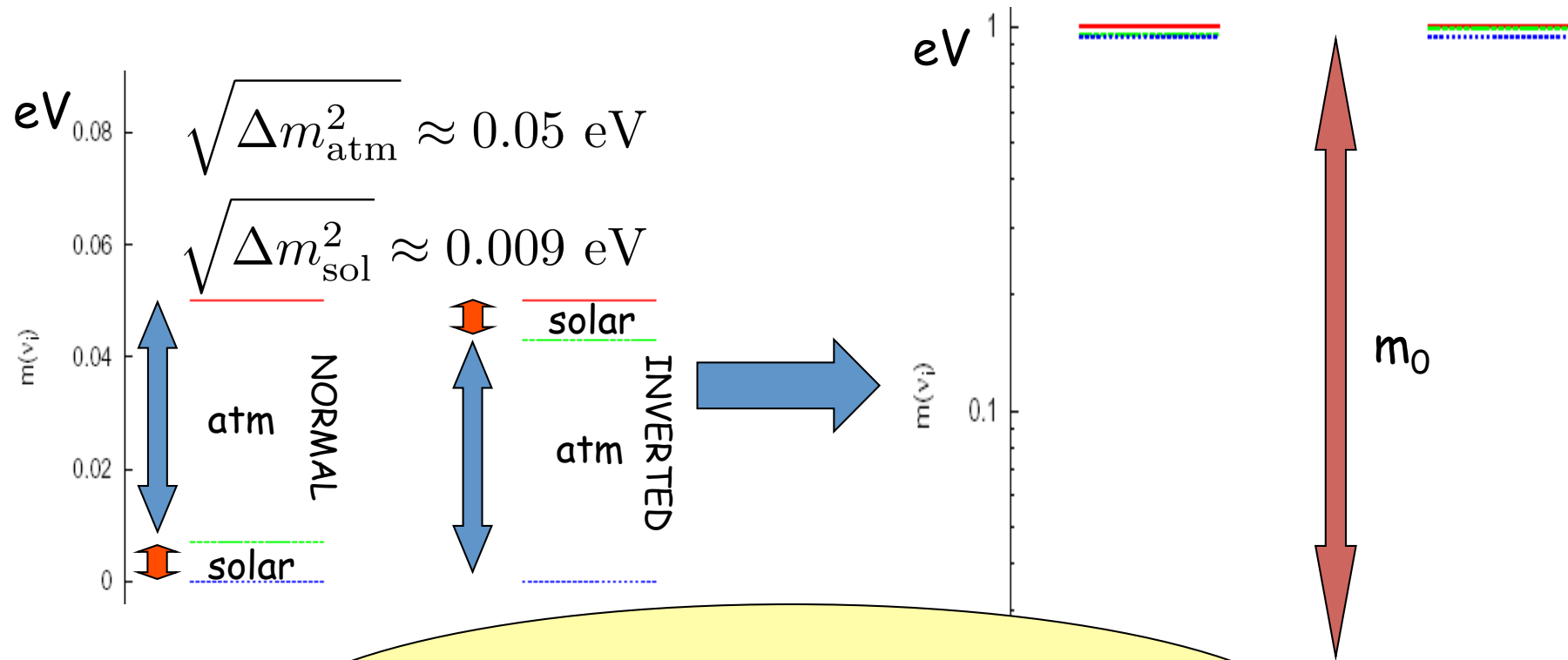
Neutrino masses



$$\nu_{\alpha L} = \sum_{i=1}^3 U_{\alpha i} \nu_{iL}, \quad (\alpha = e, \mu, \tau)$$

Neutrino masses

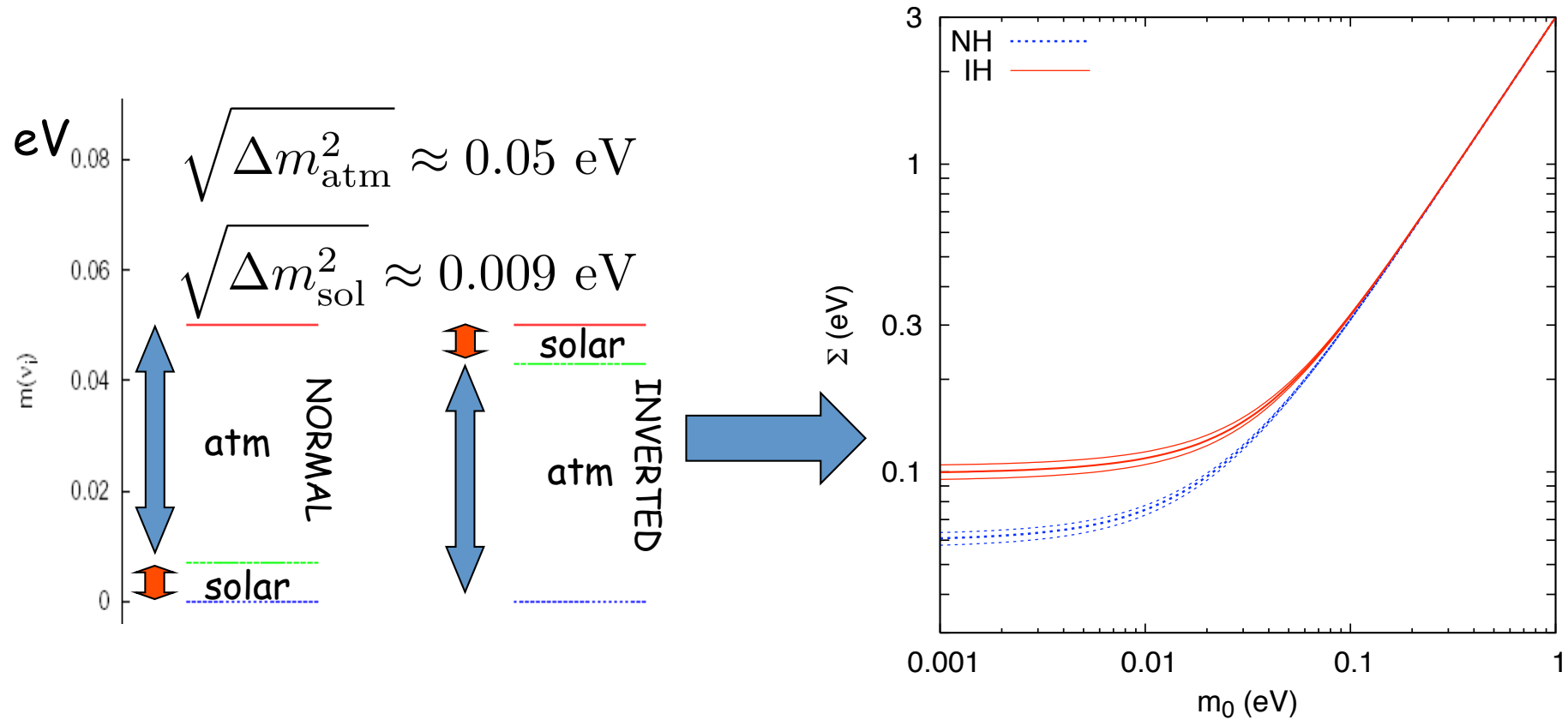
Data on flavour oscillations do not fix the absolute scale of neutrino masses



What is the value of m_0 ?

Neutrino masses

Data on flavour oscillations do not fix the absolute scale of neutrino masses



$$0.06(0.1) \text{ eV} \lesssim \sum_i m_i \lesssim 6 \text{ eV}$$

The Cosmic Neutrino Background

Neutrinos decoupled at $T \sim \text{MeV}$, keeping a spectrum as that of a relativistic species

$$f_\nu(p, T) = \frac{1}{e^{p/T_\nu} + 1}$$

- Number density

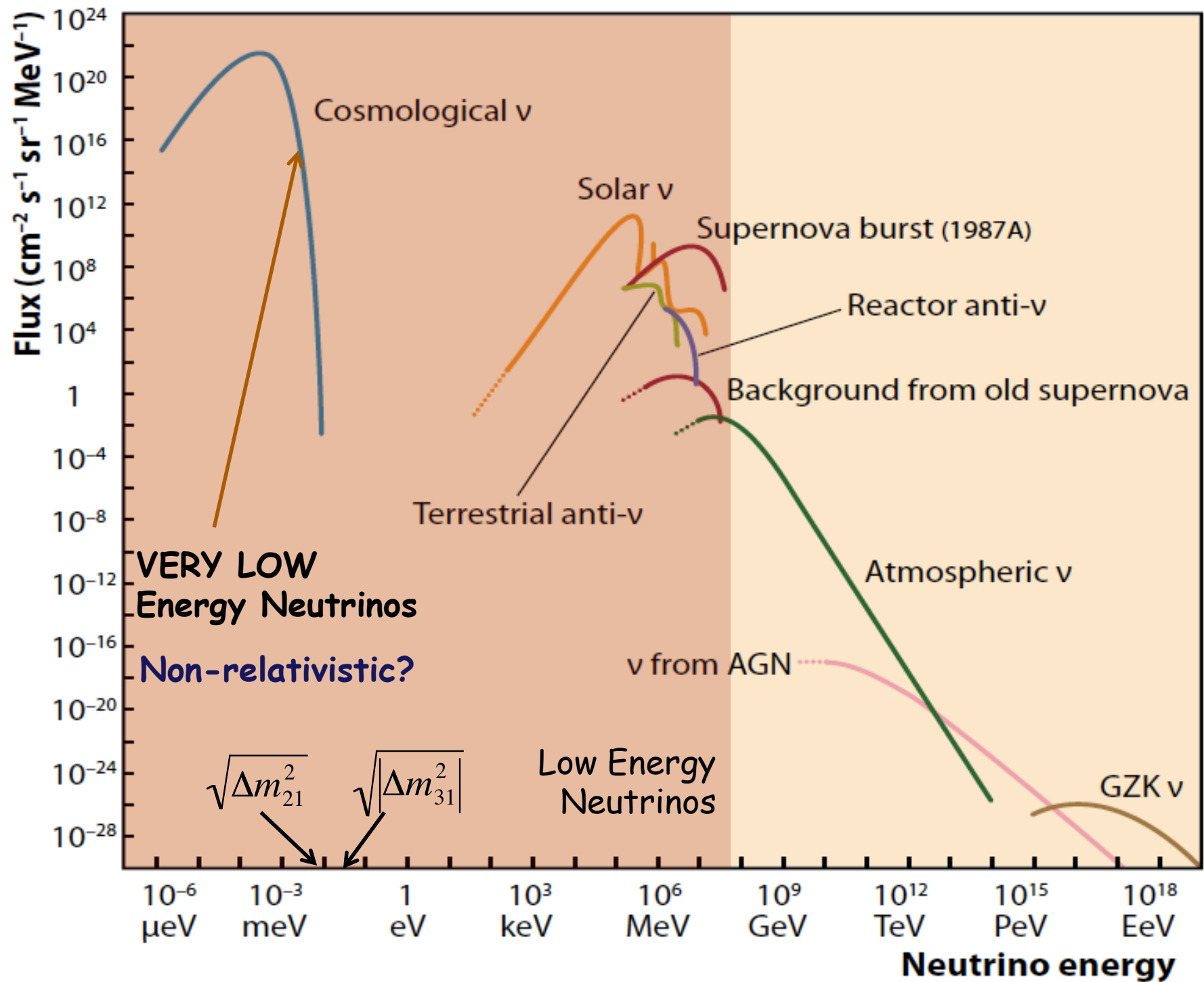
At present $112 (\nu + \bar{\nu}) \text{ cm}^{-3}$ per flavour

- Energy density

Contribution to the energy density of the Universe

$$\Omega_\nu h^2 \simeq 1.7 \times 10^{-5} \quad \text{Massless}$$

$$\Omega_\nu h^2 = \frac{\sum m_{\nu_i}}{93.2 \text{ eV}} \quad \begin{array}{l} \text{Massive} \\ m_\nu \gg T \end{array}$$



Neutrinos as Dark Matter

- Neutrinos are natural DM candidates

$$\Omega_\nu h^2 = \frac{\sum_i m_i}{93.2 \text{ eV}} \quad \Omega_\nu < 1 \rightarrow \sum_i m_i \lesssim 46 \text{ eV}$$

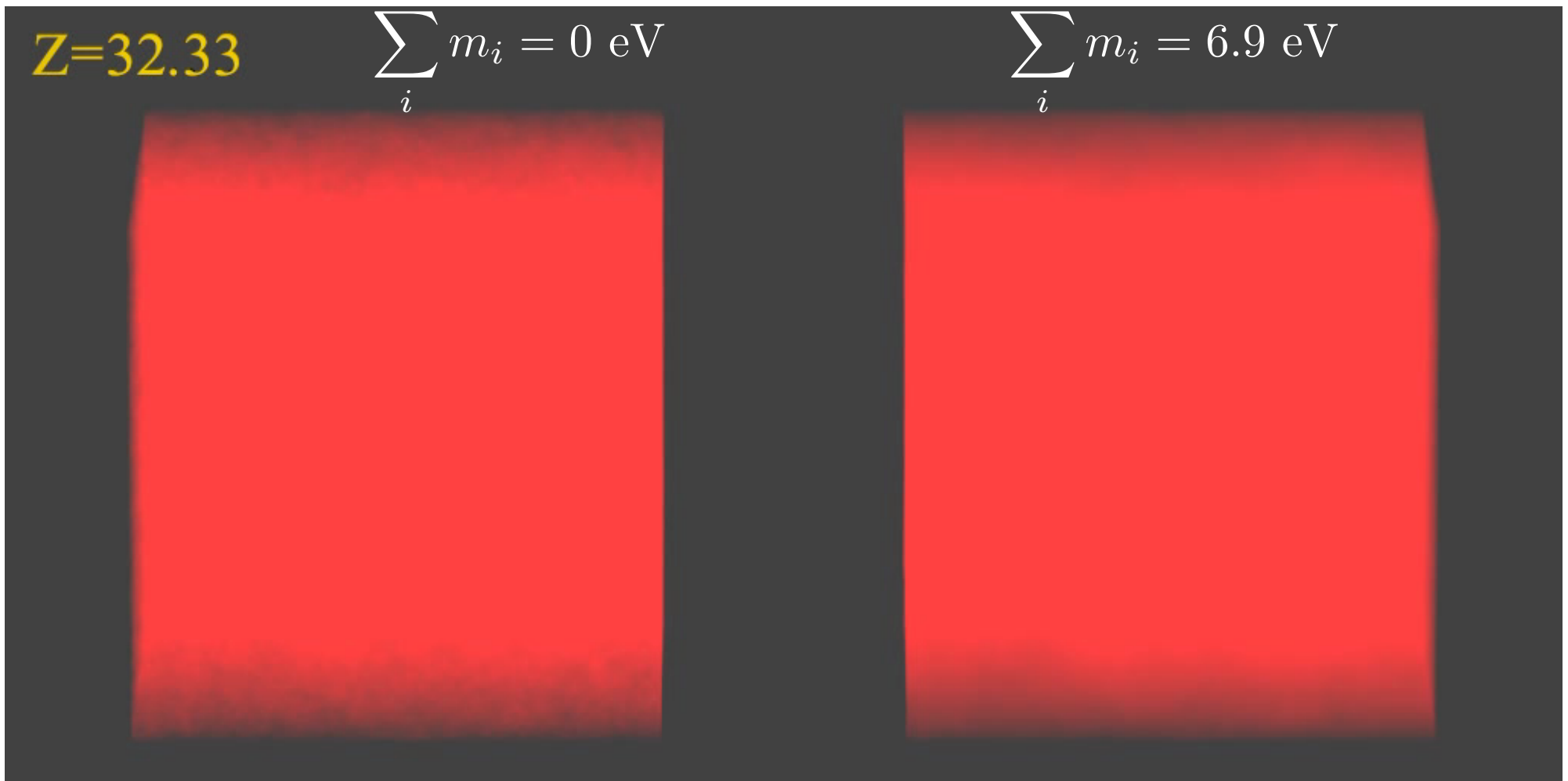
$$\Omega_\nu < \Omega_m \simeq 0.3 \rightarrow \sum_i m_i \lesssim 15 \text{ eV}$$

- They stream freely until non-relativistic (collisionless phase mixing) 
Neutrinos are HOT Dark Matter (large thermal motion)
- First structures to be formed when Universe became matter –dominated are very large
- Ruled out by structure formation  CDM

Massive Neutrinos can still be subdominant DM: **limits on m_ν from Structure Formation (combined with other cosmological data)**

Neutrinos as Hot Dark Matter

Massive Neutrinos can still be subdominant DM: limits on m_ν from Structure Formation (combined with other cosmological data)



The radiation content of the Universe (N_{eff})

Relativistic particles in the Universe

At $T < m_e$, the radiation content of the Universe is

$$\rho_r = \rho_\gamma + \rho_\nu + \rho_x = \left[1 + \frac{7}{8} \left(\frac{4}{11} \right)^{4/3} N_{\text{eff}} \right] \rho_\gamma$$

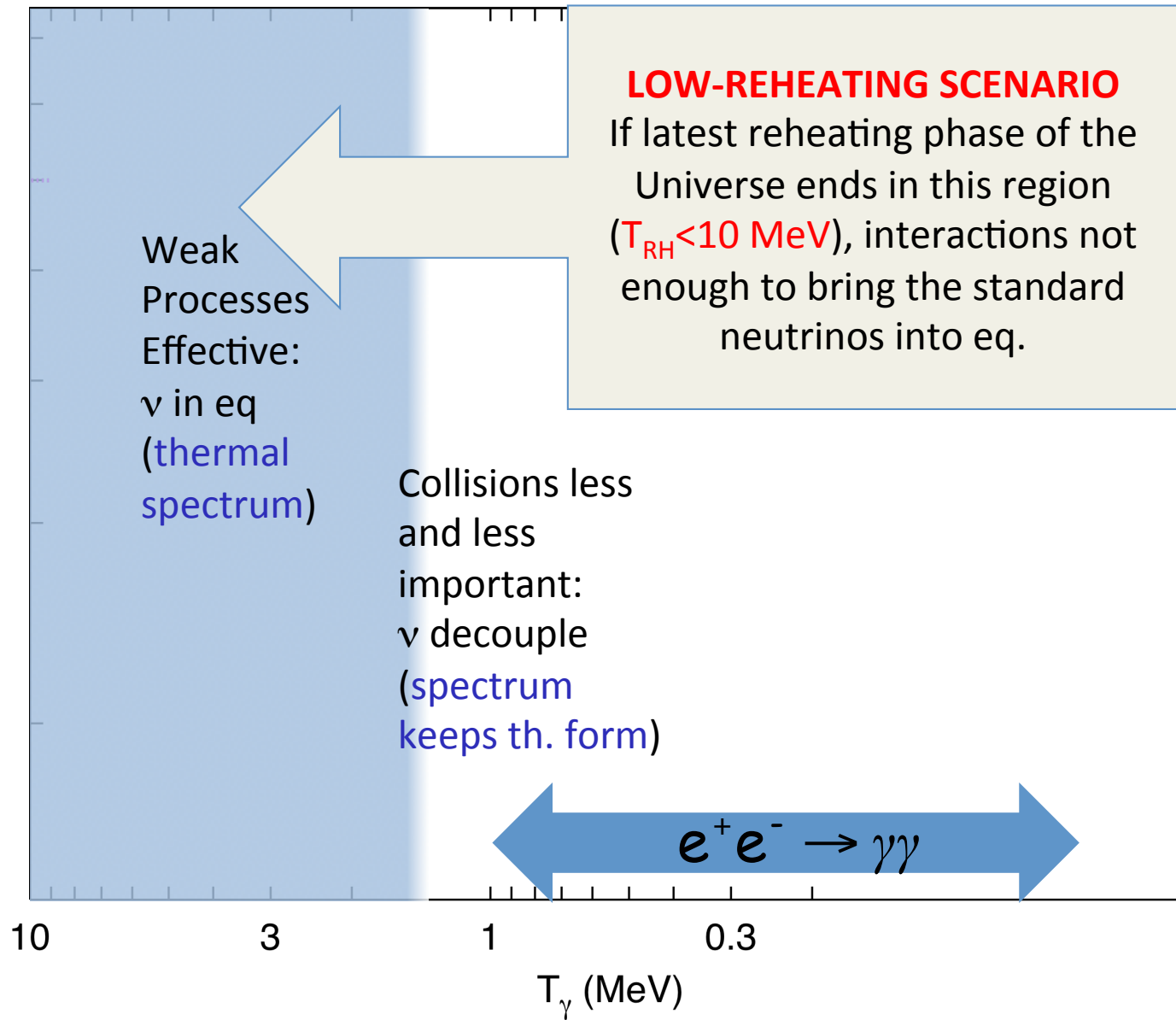
Effective number of relativistic neutrino species

Traditional parametrization of ρ stored in relativistic particles

N_{eff} is a way to measure the ratio $\frac{\rho_\nu + \rho_x}{\rho_\gamma}$

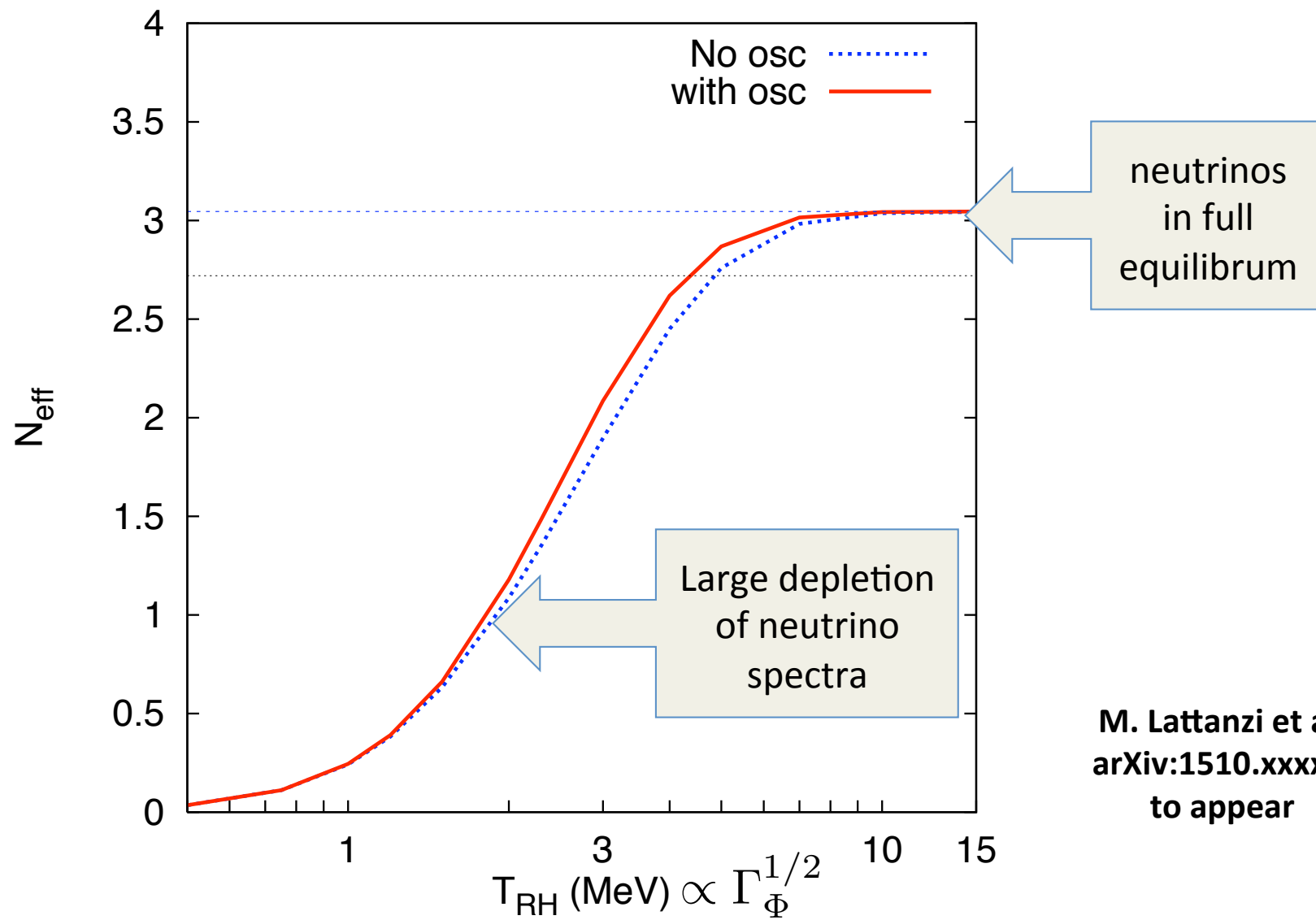
➤ standard neutrinos only: $N_{\text{eff}} \simeq 3$ (3.046)

$$N_{\text{eff}} < 3 ?$$



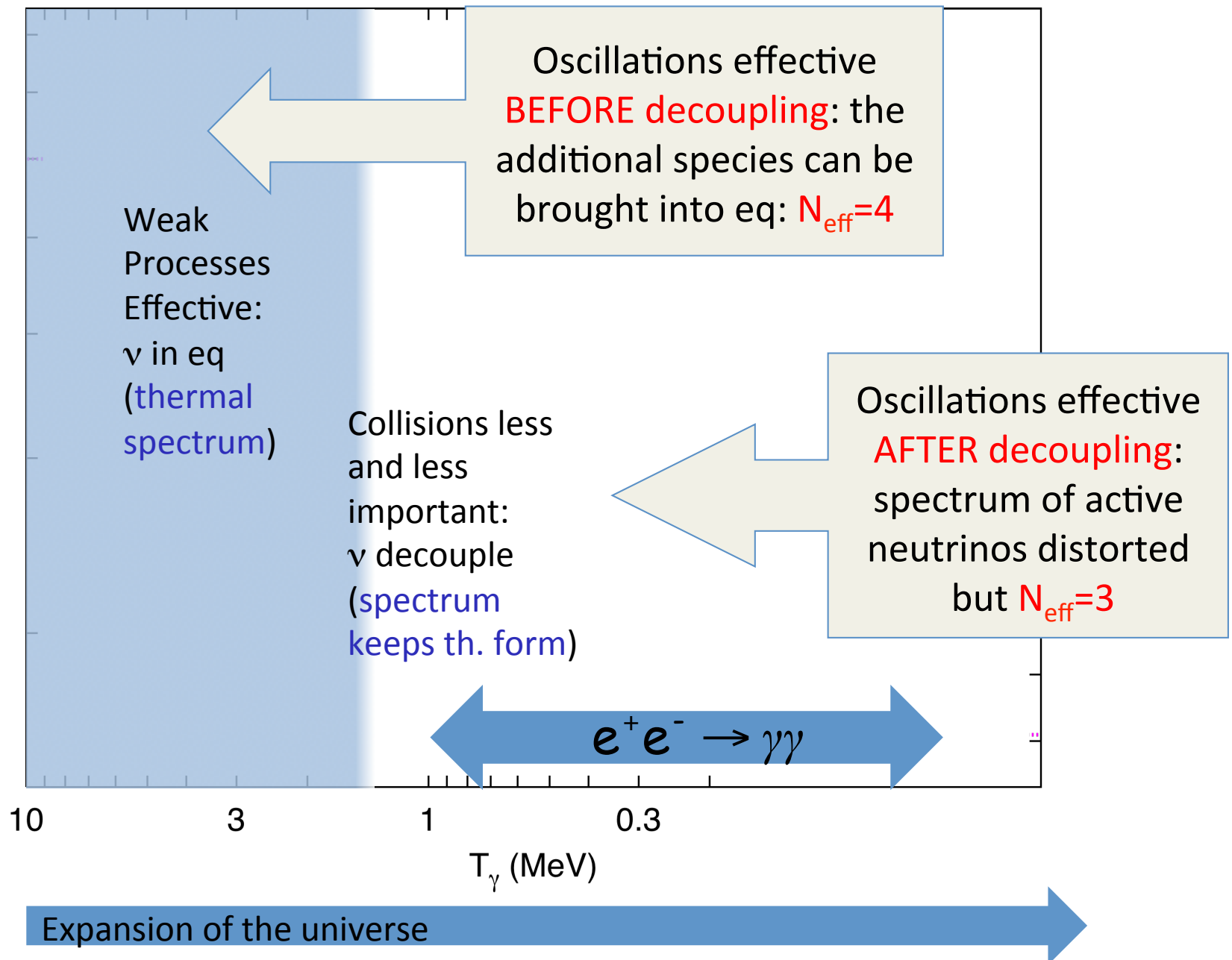
Expansion of the universe

$$N_{\text{eff}} < 3 ?$$

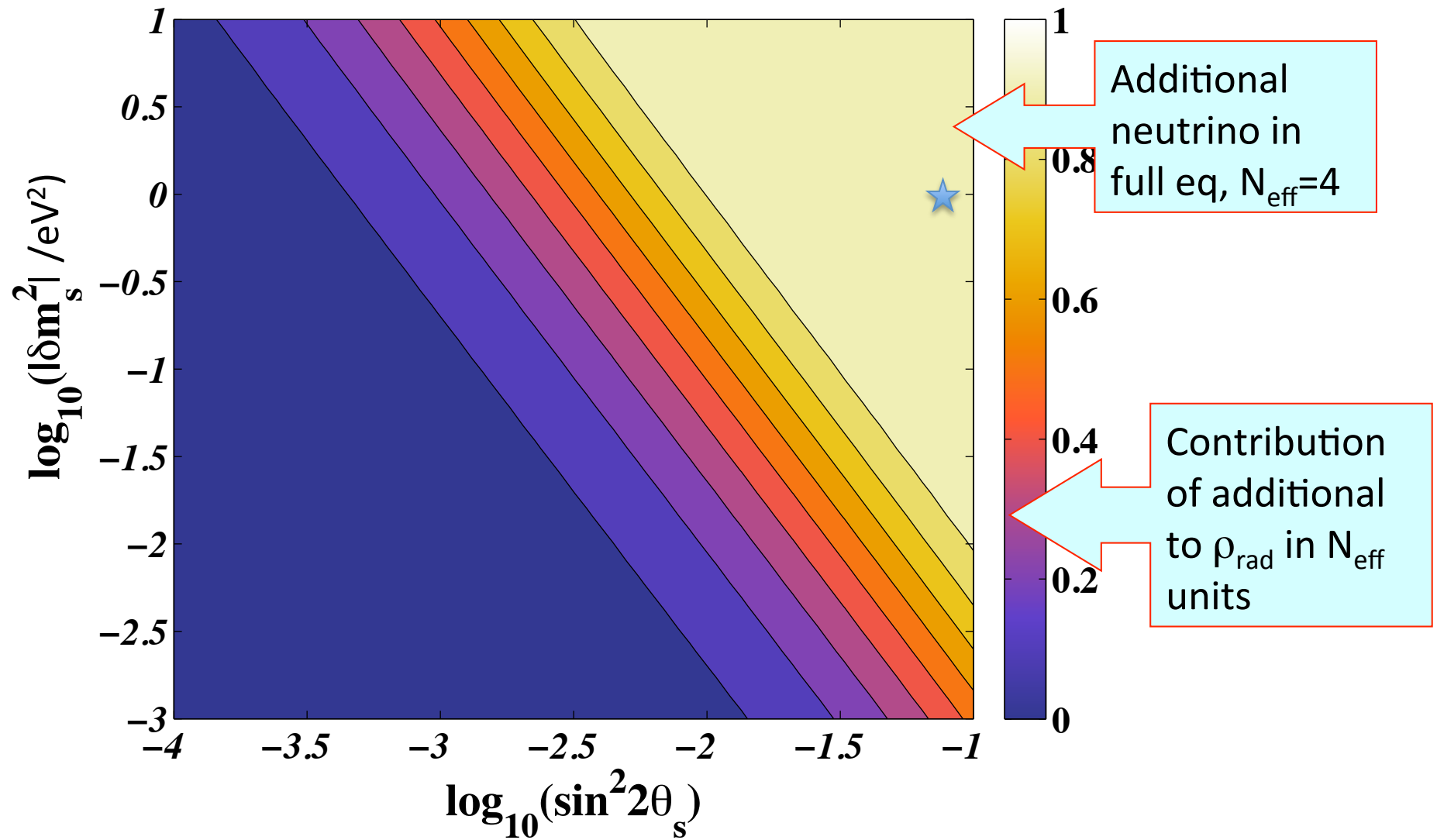


M. Lattanzi et al,
 arXiv:1510.xxxxx,
 to appear

N_{eff} & Active-sterile neutrino oscillations

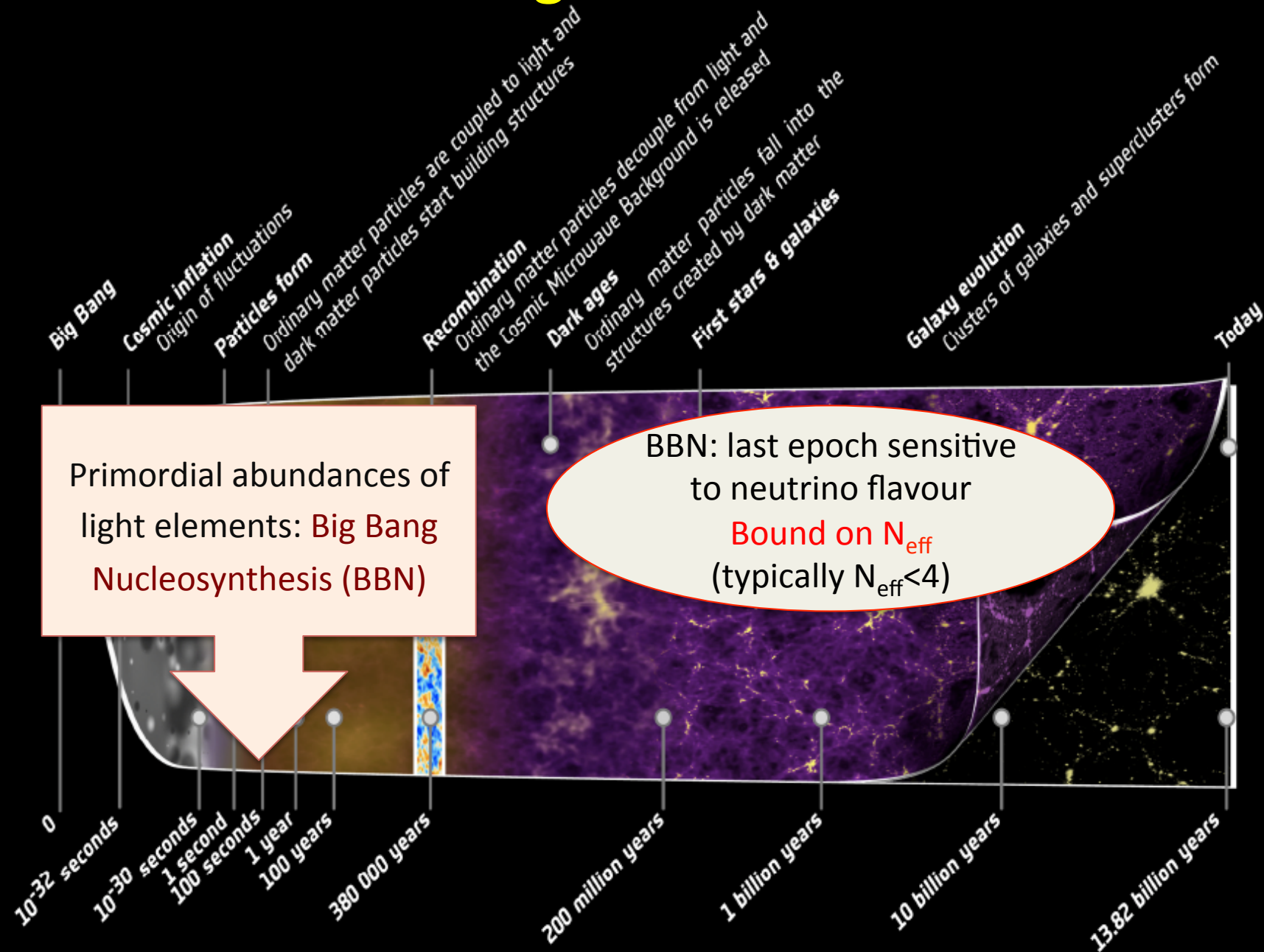


N_{eff} & Active-sterile neutrino oscillations

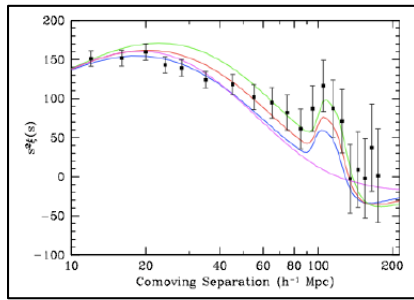


Cosmological Observables

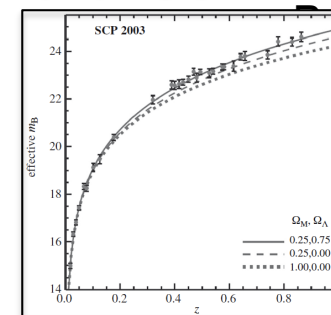
Cosmological Observables



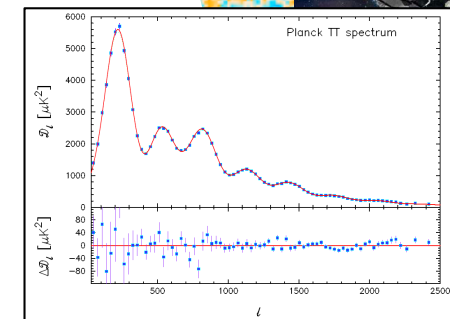
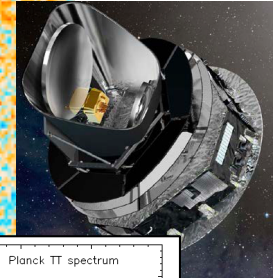
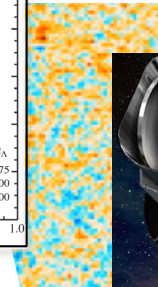
Cosmological Observables



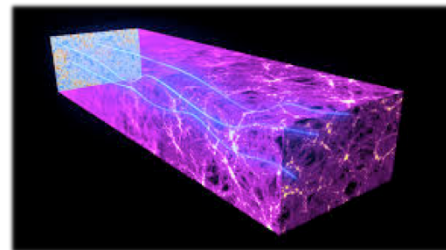
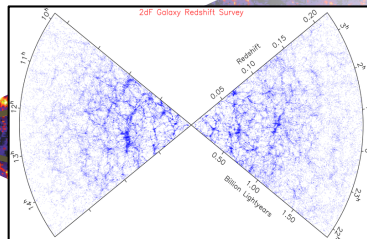
Hubble constant H_0 & cosmic distances
measurements: SN Ia and Baryon
Acoustic Oscillations (BAO)



combination



Today



matter density fluctuations

LSS [galaxy / cosmic shear /
 $\text{Ly}\alpha$] spectrum

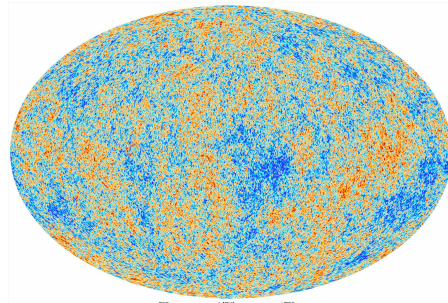
Photon momentum
after decoupling

CMB secondary anisotropy
spectrum

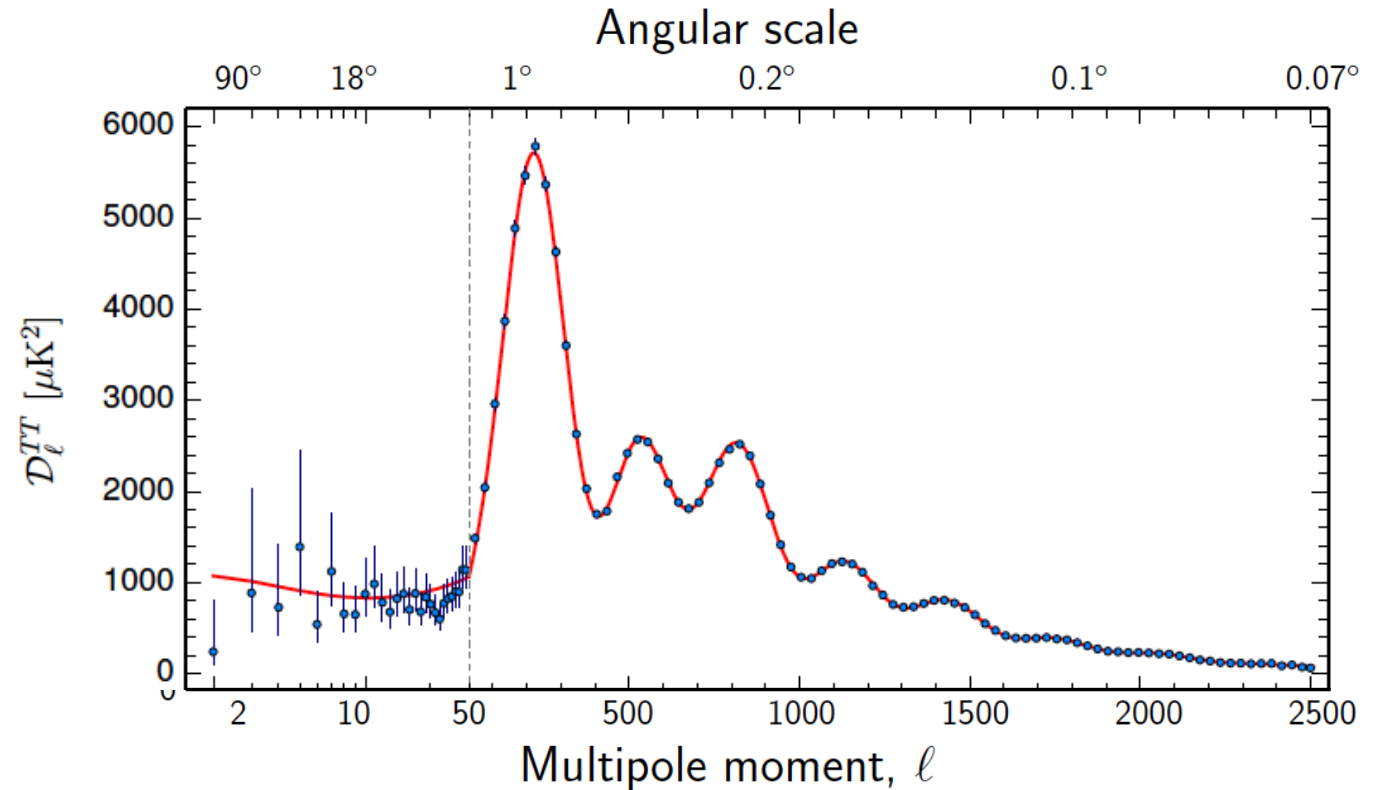
Photon density fluctuations
before decoupling

CMB primary anisotropy
spectrum (temp+pol)

CMB data from Planck



Map of CMBR temperature Fluctuations $\Delta(\theta, \varphi) = \frac{T(\theta, \varphi) - \langle T \rangle}{\langle T \rangle}$
Multipole Expansion $\Delta(\theta, \varphi) = \sum_{\lambda=0}^{\infty} \sum_{m=-\lambda}^{\lambda} a_{\lambda m} Y_{\lambda m}(\theta, \varphi)$
Angular Power Spectrum $C_l = \langle a_{lm}^* a_{lm} \rangle = \frac{1}{2l+1} \sum_{m=-l}^l a_{lm}^* a_{lm}$

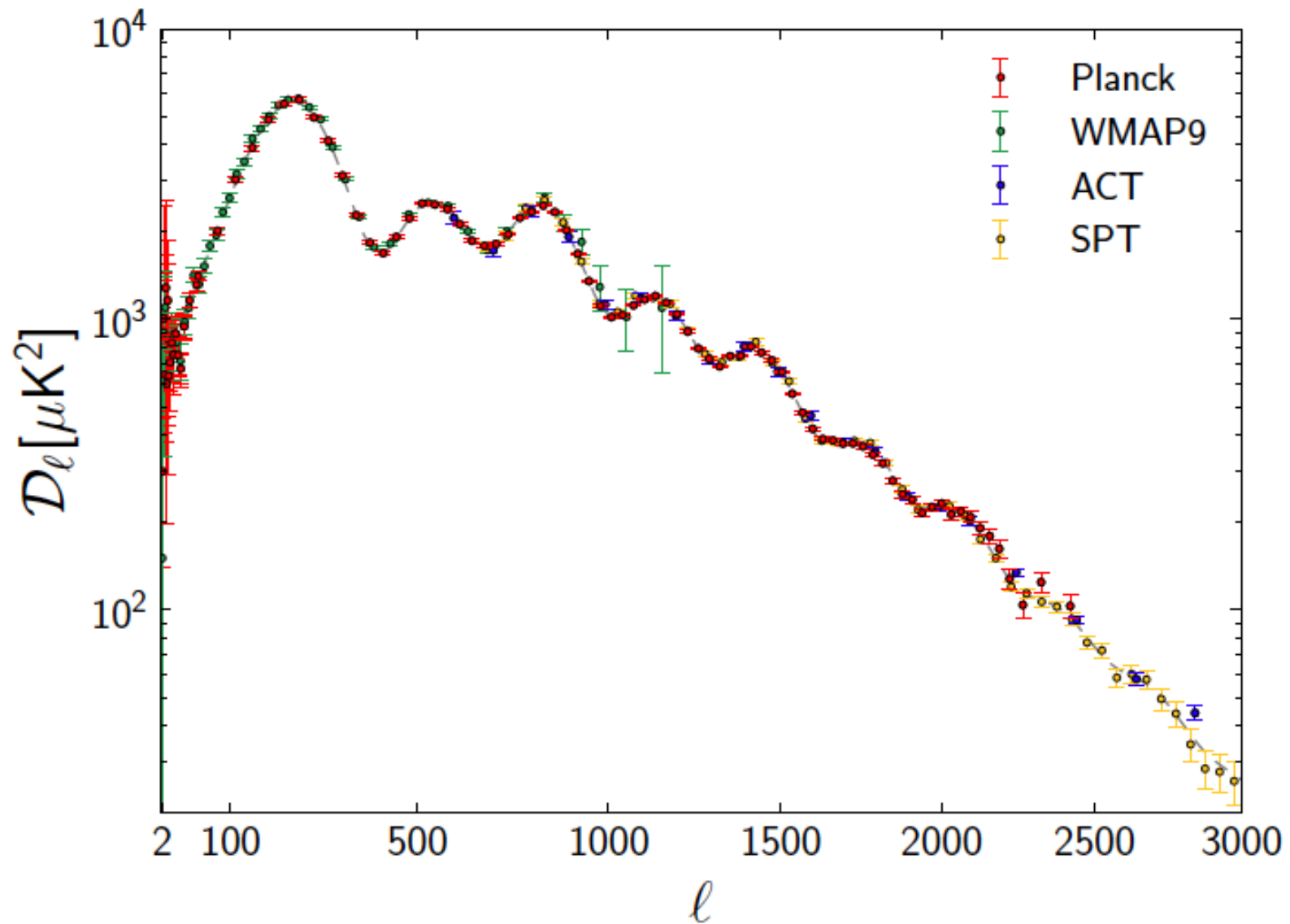


PLANCK 2015: full-mission Planck observations of temperature and polarization anisotropies

P.A.R. Ade et al, arXiv:1502.01589

Present CMB data

Planck vs other experiments



Bounds on neutrino properties from Planck (& other cosmo data)

The minimal Λ CDM model fits very well Planck data

Parameter	TT+lowP 68 % limits	TT+lowP+lensing 68 % limits	TT+lowP+lensing+ext 68 % limits
$\Omega_b h^2$	0.02222 ± 0.00023	0.02226 ± 0.00023	0.02227 ± 0.00020
$\Omega_c h^2$	0.1197 ± 0.0022	0.1186 ± 0.0020	0.1184 ± 0.0012
$100\theta_{MC}$	1.04085 ± 0.00047	1.04103 ± 0.00046	1.04106 ± 0.00041
τ	0.078 ± 0.019	0.066 ± 0.016	0.067 ± 0.013
$\ln(10^{10} A_s)$	3.089 ± 0.036	3.062 ± 0.029	3.064 ± 0.024
n_s	0.9655 ± 0.0062	0.9677 ± 0.0060	0.9681 ± 0.0044
H_0	67.31 ± 0.96	67.81 ± 0.92	67.90 ± 0.55
Ω_Λ	0.685 ± 0.013	0.692 ± 0.012	0.6935 ± 0.0072
Ω_m	0.315 ± 0.013	0.308 ± 0.012	0.3065 ± 0.0072
Parameter	TT,TE,EE+lowP 68 % limits	TT,TE,EE+lowP+lensing 68 % limits	TT,TE,EE+lowP+lensing+ext 68 % limits
$\Omega_b h^2$	0.02225 ± 0.00016	0.02226 ± 0.00016	0.02230 ± 0.00014
$\Omega_c h^2$	0.1198 ± 0.0015	0.1193 ± 0.0014	0.1188 ± 0.0010
$100\theta_{MC}$	1.04077 ± 0.00032	1.04087 ± 0.00032	1.04093 ± 0.00030
τ	0.079 ± 0.017	0.063 ± 0.014	0.066 ± 0.012
$\ln(10^{10} A_s)$	3.094 ± 0.034	3.059 ± 0.025	3.064 ± 0.023
n_s	0.9645 ± 0.0049	0.9653 ± 0.0048	0.9667 ± 0.0040
H_0	67.27 ± 0.66	67.51 ± 0.64	67.74 ± 0.46
Ω_Λ	0.6844 ± 0.0091	0.6879 ± 0.0087	0.6911 ± 0.0062
Ω_m	0.3156 ± 0.0091	0.3121 ± 0.0087	0.3089 ± 0.0062

1-parameter extensions of the Λ CDM model

Parameter	TT	TT+lensing	TT+lensing+ext
Ω_K	$-0.052^{+0.049}_{-0.055}$	$-0.005^{+0.016}_{-0.017}$	$-0.0001^{+0.0054}_{-0.0052}$
Σm_ν [eV]	< 0.715	< 0.675	< 0.234
N_{eff}	$3.13^{+0.64}_{-0.63}$	$3.13^{+0.62}_{-0.61}$	$3.15^{+0.41}_{-0.40}$
Y_p	$0.252^{+0.041}_{-0.042}$	$0.251^{+0.040}_{-0.039}$	$0.251^{+0.035}_{-0.036}$
$dn_s/d \ln k$	$-0.008^{+0.016}_{-0.016}$	$-0.003^{+0.015}_{-0.015}$	$-0.003^{+0.015}_{-0.014}$
$r_{0.002}$	< 0.103	< 0.114	< 0.114
w	$-1.54^{+0.62}_{-0.50}$	$-1.41^{+0.64}_{-0.56}$	$-1.006^{+0.085}_{-0.091}$

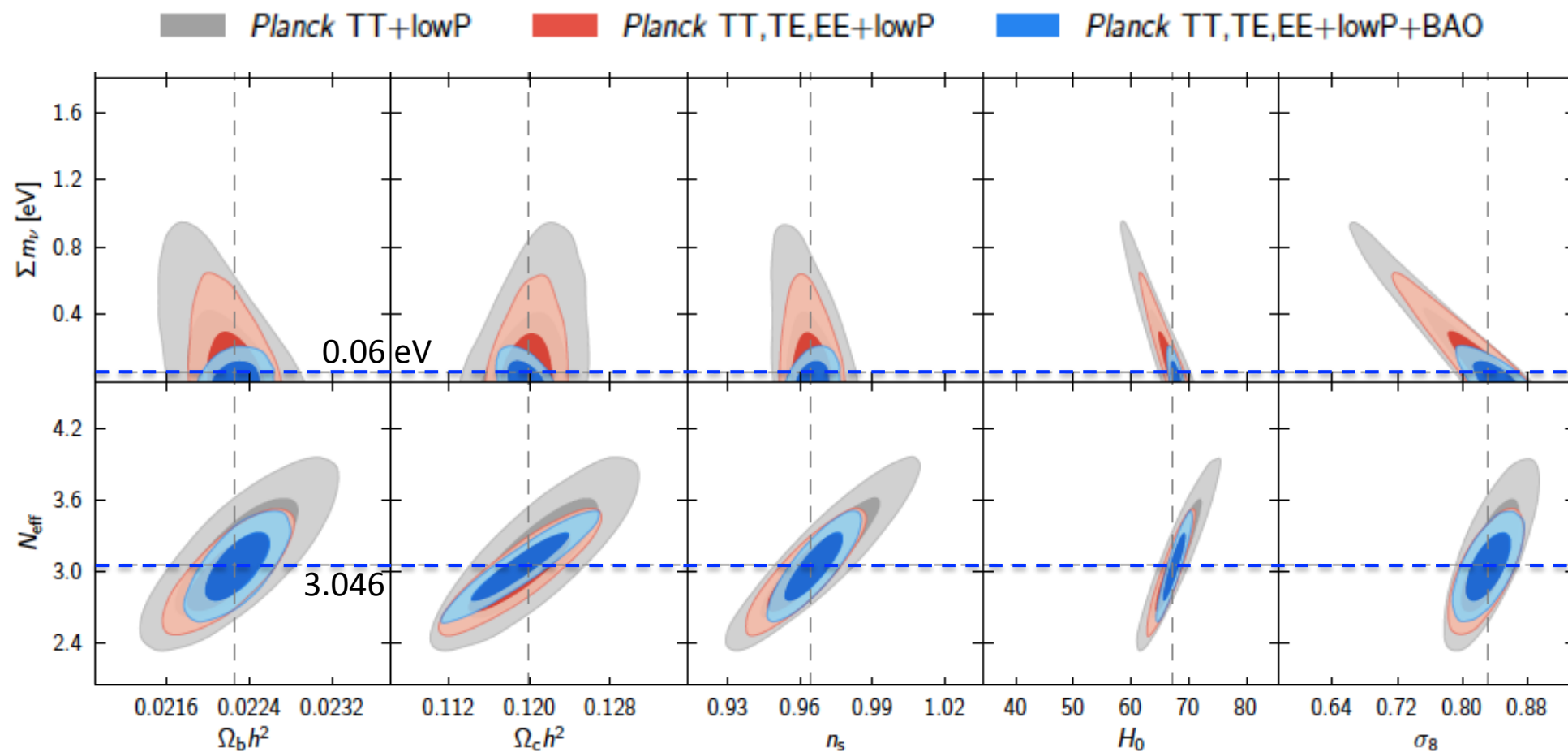
95% CL
limits

Parameter	TT, TE, EE	TT, TE, EE+lensing	TT, TE, EE+lensing+ext
Ω_K	$-0.040^{+0.038}_{-0.041}$	$-0.004^{+0.015}_{-0.015}$	$0.0008^{+0.0040}_{-0.0039}$
Σm_ν [eV]	< 0.492	< 0.589	< 0.194
N_{eff}	$2.99^{+0.41}_{-0.39}$	$2.94^{+0.38}_{-0.38}$	$3.04^{+0.33}_{-0.33}$
Y_p	$0.250^{+0.026}_{-0.027}$	$0.247^{+0.026}_{-0.027}$	$0.249^{+0.025}_{-0.026}$
$dn_s/d \ln k$	$-0.006^{+0.014}_{-0.014}$	$-0.002^{+0.013}_{-0.013}$	$-0.002^{+0.013}_{-0.013}$
$r_{0.002}$	< 0.0987	< 0.112	< 0.113
w	$-1.55^{+0.58}_{-0.48}$	$-1.42^{+0.62}_{-0.56}$	$-1.019^{+0.075}_{-0.080}$

Ext =BAO + JLA + H_0

Planck collaboration, arXiv:1502.01589

1-parameter extensions of the Λ CDM model

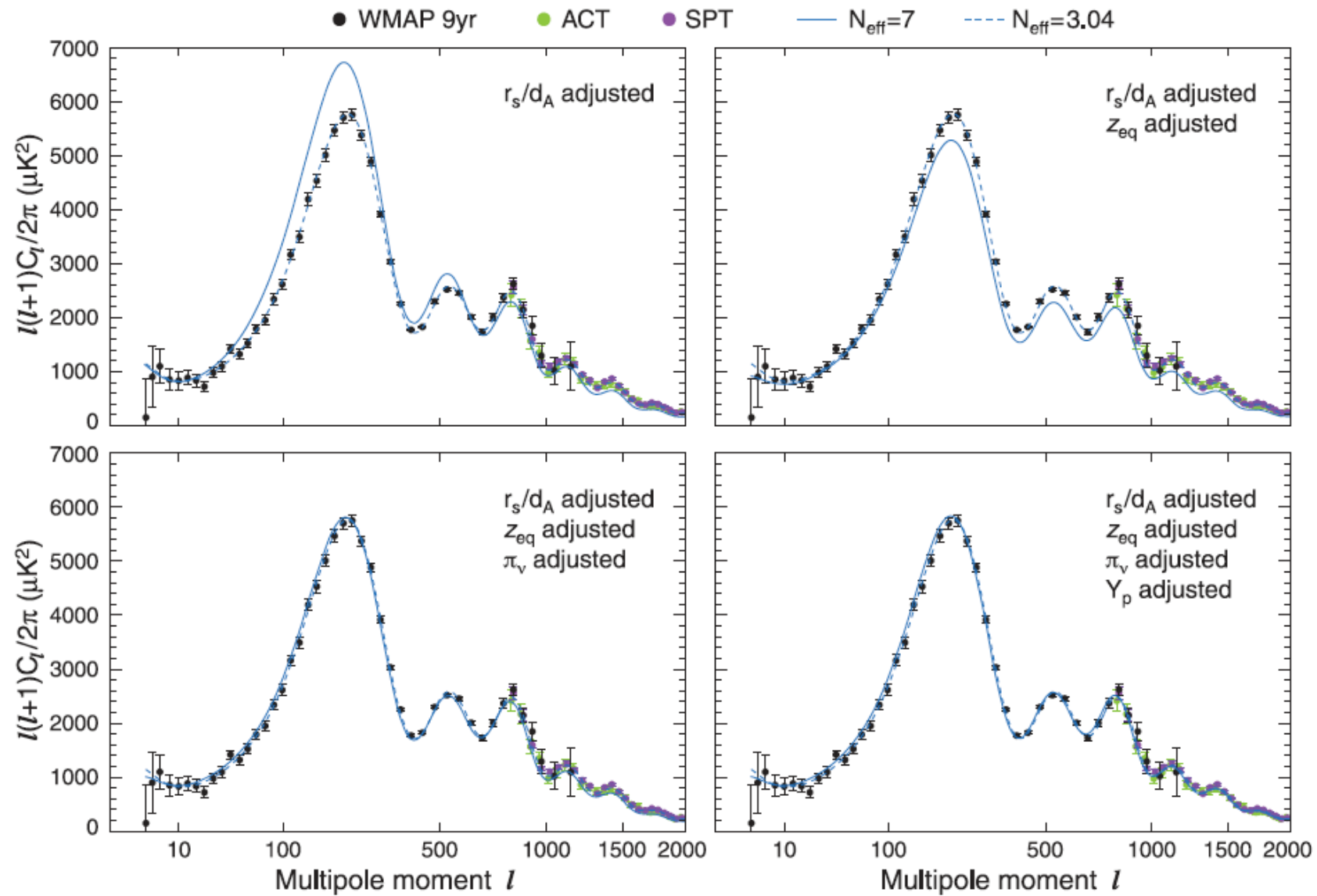


68+95%
Conf regions

Measuring N_{eff}

- N_{eff} is a parameter for the relativistic density in general
- “background effects” (change in expansion history) versus “perturbation effects” (gravitational interactions between photons and relativistic species)
- “effect of N_{eff} ” depends on what is kept fixed.
- Fixing quantities best probed by CMB (angular peak scale, redshift of equality, ...):
 - possible with simultaneous enhancement of radiation, matter, Λ densities, with fixed photon and baryon densities
 - then increase in N_{eff} goes with increase in H_0 : positive correlation between the two

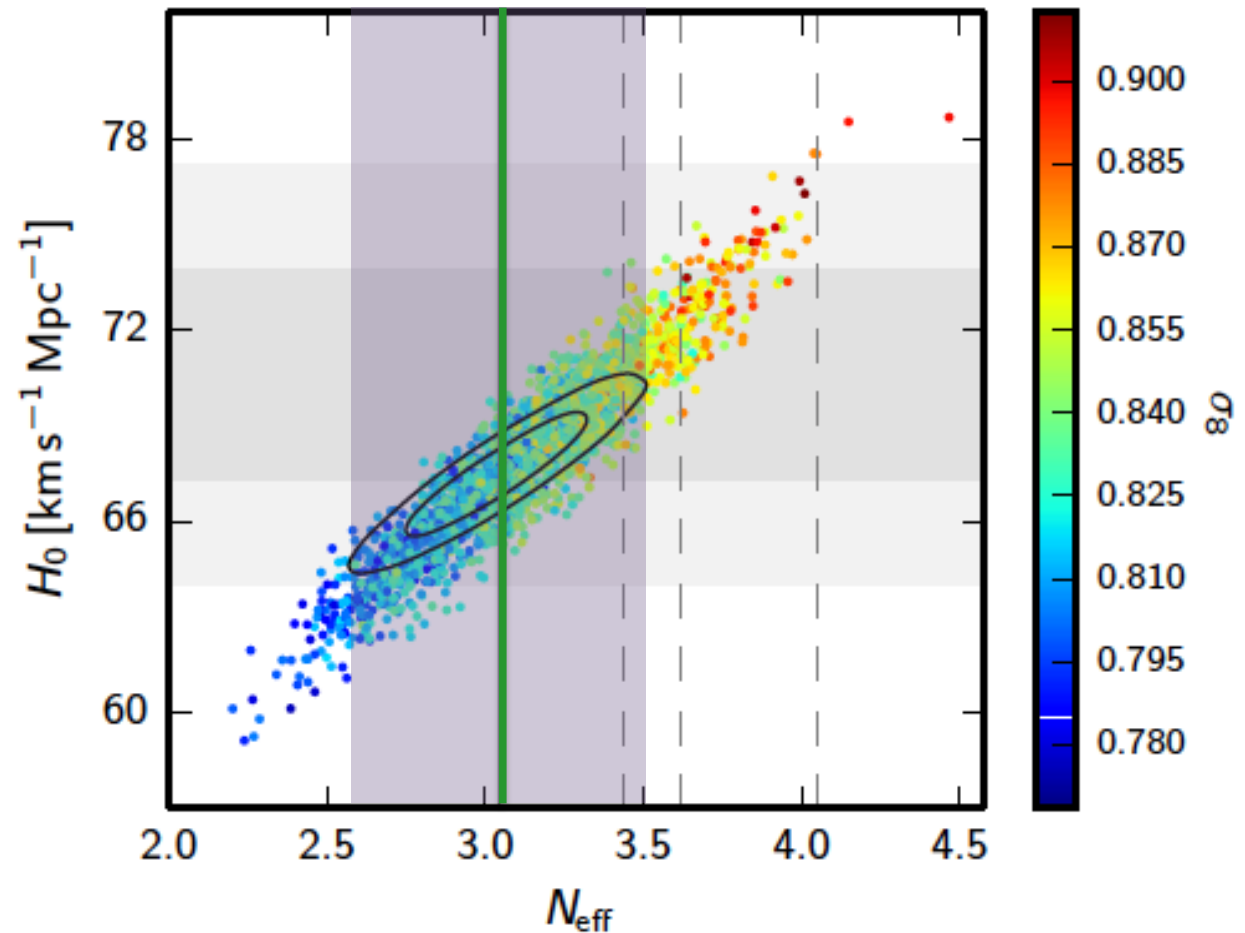
Measuring N_{eff}



Hinshaw et al, arXiv:1212.5226

Measuring N_{eff}

Indirect detection of
CNB at $10\text{-}17\sigma$



$$N_{\text{eff}} = 3.13 \pm 0.32 \quad \text{Planck TT+lowP};$$

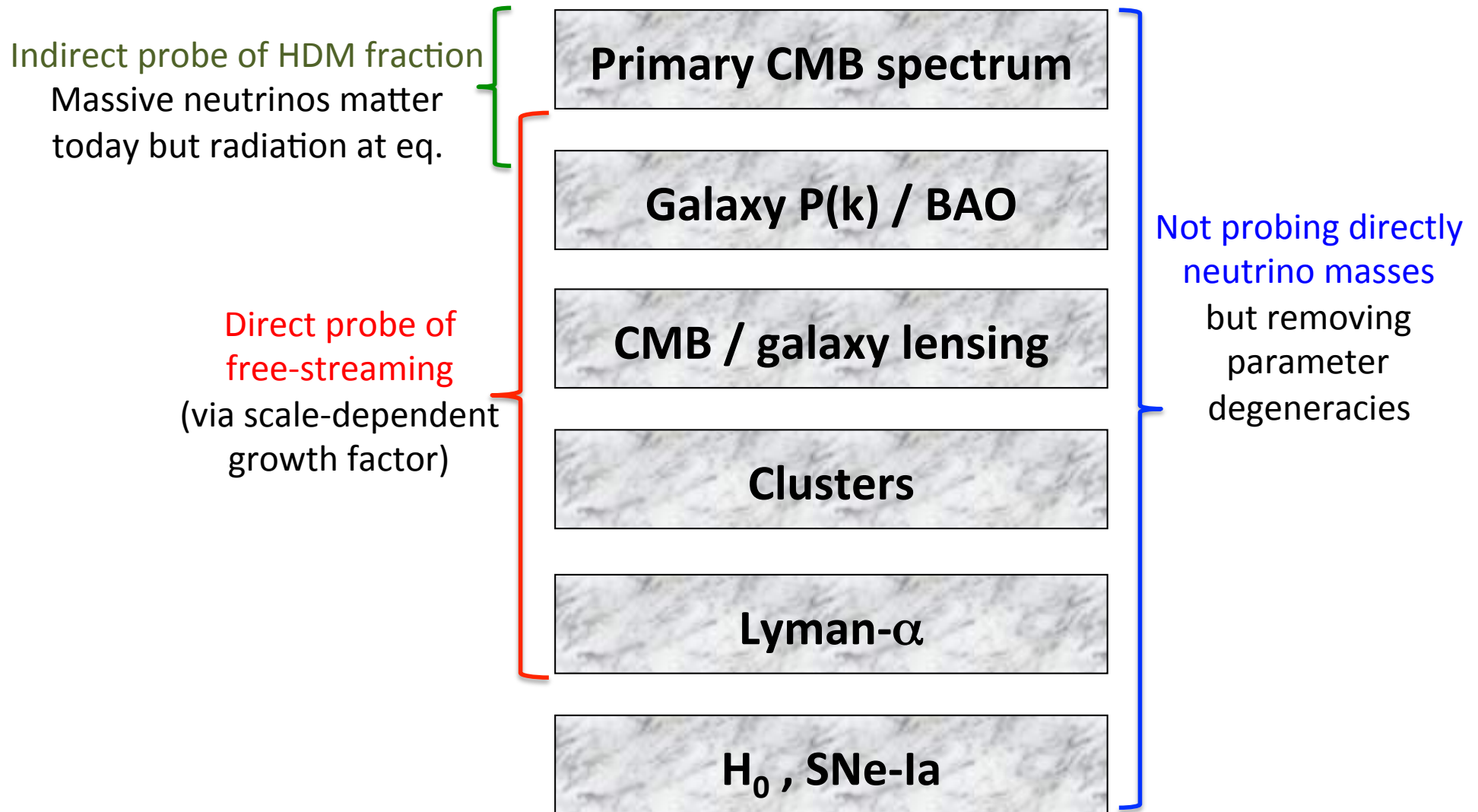
$$N_{\text{eff}} = 3.15 \pm 0.23 \quad \text{Planck TT+lowP+BAO};$$

$$N_{\text{eff}} = 2.99 \pm 0.20 \quad \text{Planck TT, TE, EE+lowP};$$

$$N_{\text{eff}} = 3.04 \pm 0.18 \quad \text{Planck TT, TE, EE+lowP+BAO}.$$

All 68%CL

Probing neutrino masses with cosmo data



Measuring m_ν with the CMB

- Neutrinos contribute to **radiation** at early times and **non-relativistic matter** at late times
- If $m_\nu < 0.6$ eV, neutrinos are relativistic at photon decoupling. In principle the primary CMB TT spectrum sensitive to $\Sigma m_\nu > 1.5$ eV
- “effect of m_ν ” depends on what is kept fixed
- Leave both “early cosmology” and angular diameter dist. to decoupling invariant:
 - Possible by fixing photon, cdm and baryon densities, while tuning H_0 , Ω_Λ
 - then increase in m_ν goes with decrease in H_0 : **negative correlation** between the two
 - “base model” in Planck has (0.06, 0, 0) eV masses: shifts best-fitting H_0 by -0.6 h/km/Mpc with respect to massless case

Measuring m_ν with Planck

CMB alone (Planck TT+lowP):

$$\Sigma m_\nu < 0.72 \text{ eV}$$

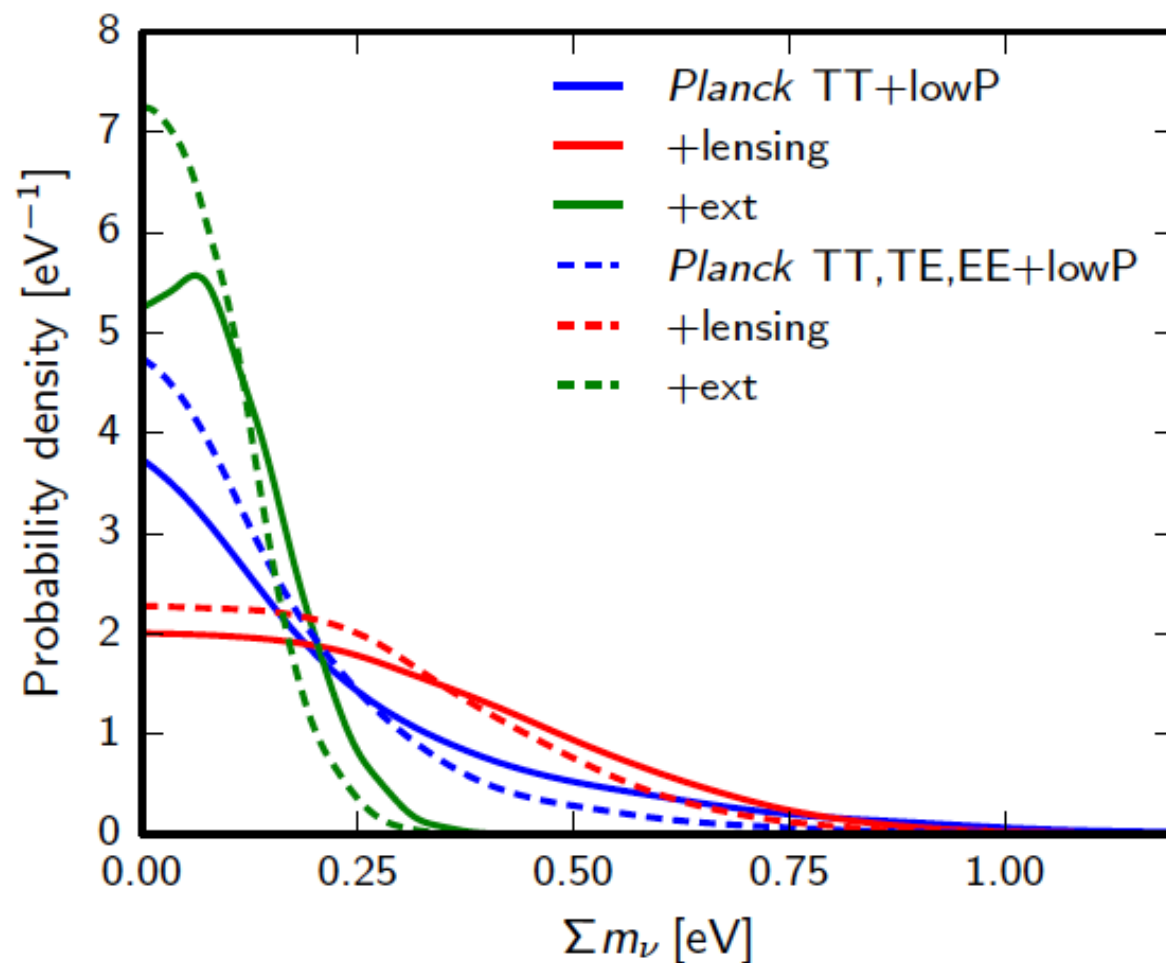
+ TE,EE+ lensing:

$$\Sigma m_\nu < 0.59 \text{ eV}$$

Planck TT+lowP+lensing+ext:

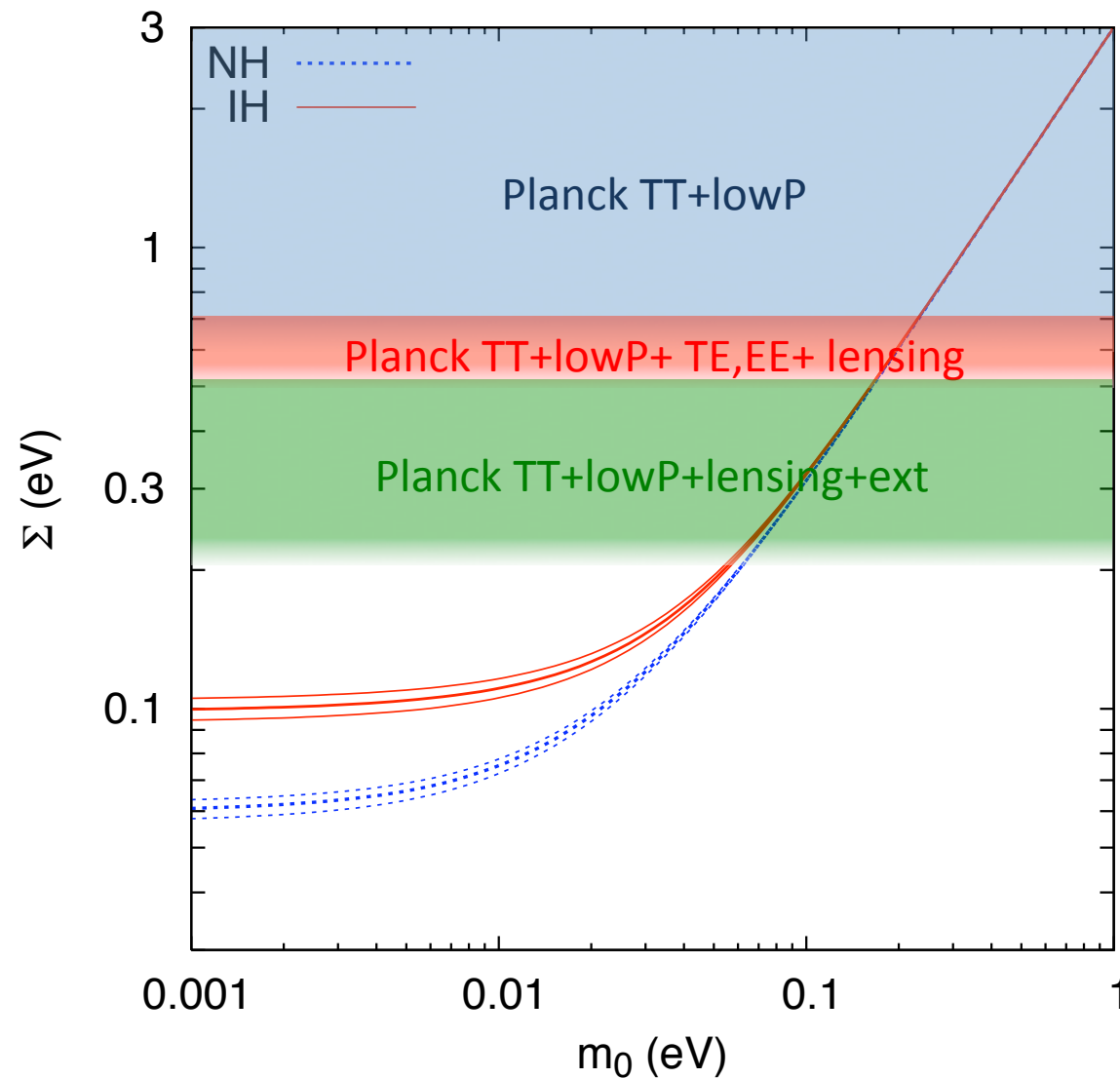
$$\Sigma m_\nu < 0.23 \text{ eV}$$

All 95% CL.



Measuring m_ν with Planck

Cosmological upper limits on the sum of neutrino masses



Some combination of data leads to $m_\nu > 0$

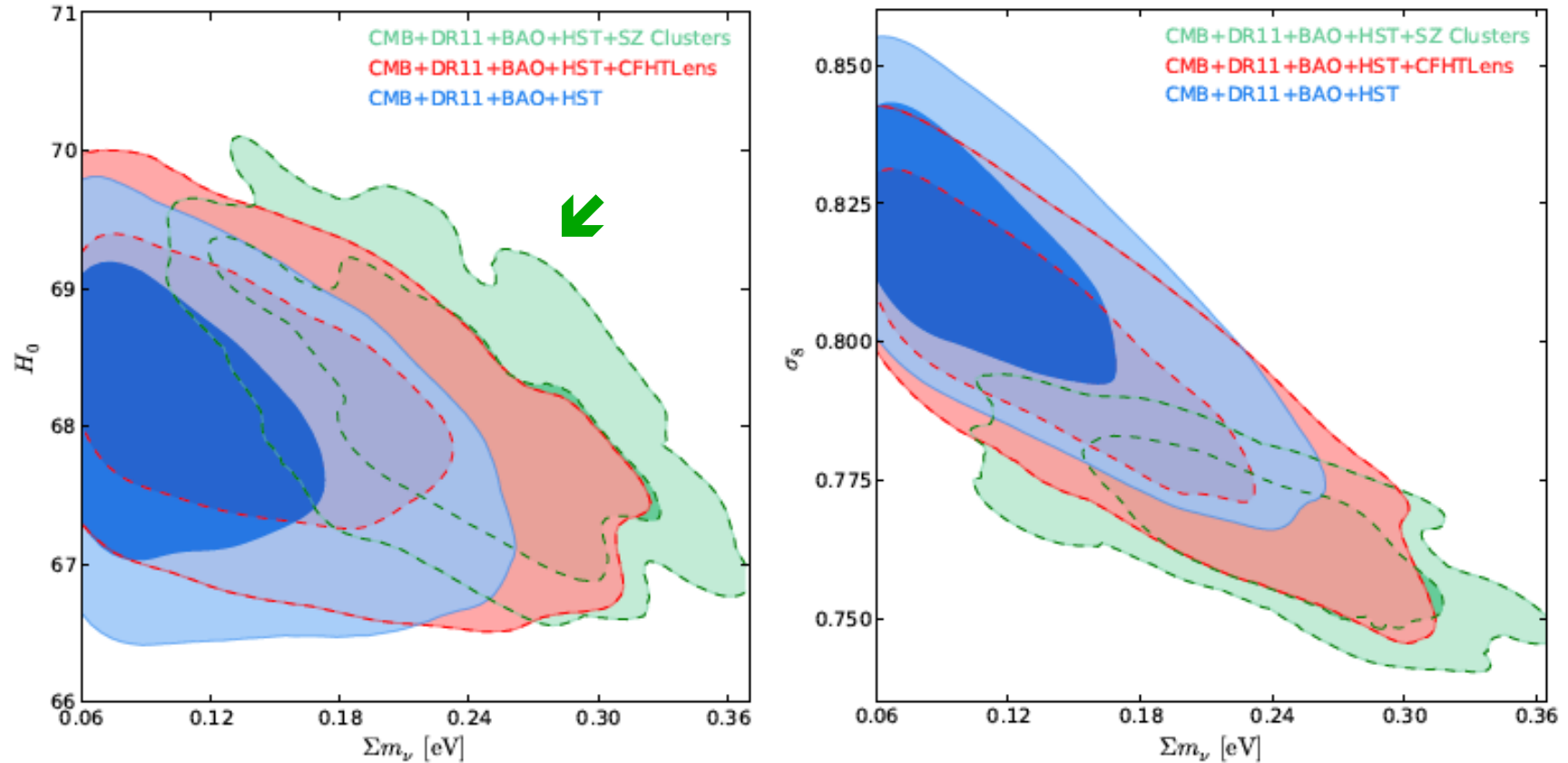
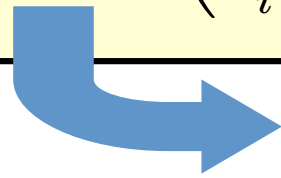


FIG. 1: Left panel: the blue contours show the 68% and 95% CL allowed regions from the combination of CMB data, BOSS DR11 BAO measurements, additional BAO measurements and a prior on the Hubble constant from HST in the $(\Sigma m_\nu$ (eV), H_0) plane. The red (green) contours depict the results when the $\sigma_8 - \Omega_m$ weak lensing (galaxy number counts) constraint is added in the analysis. Right panel: as in the left panel but in the $(\Sigma m_\nu$ (eV), σ_8) plane.

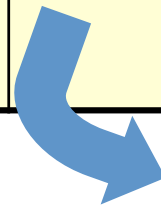
Probing the absolute neutrino mass scale

Tritium β decay	$m_\beta = \left(\sum_i U_{ei} ^2 m_i^2 \right)^{1/2}$	2.2 eV
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$$[c_{13}^2 c_{12}^2 m_1^2 + c_{13}^2 s_{12}^2 m_2^2 + s_{13}^2 m_3^2]^{1/2}$$

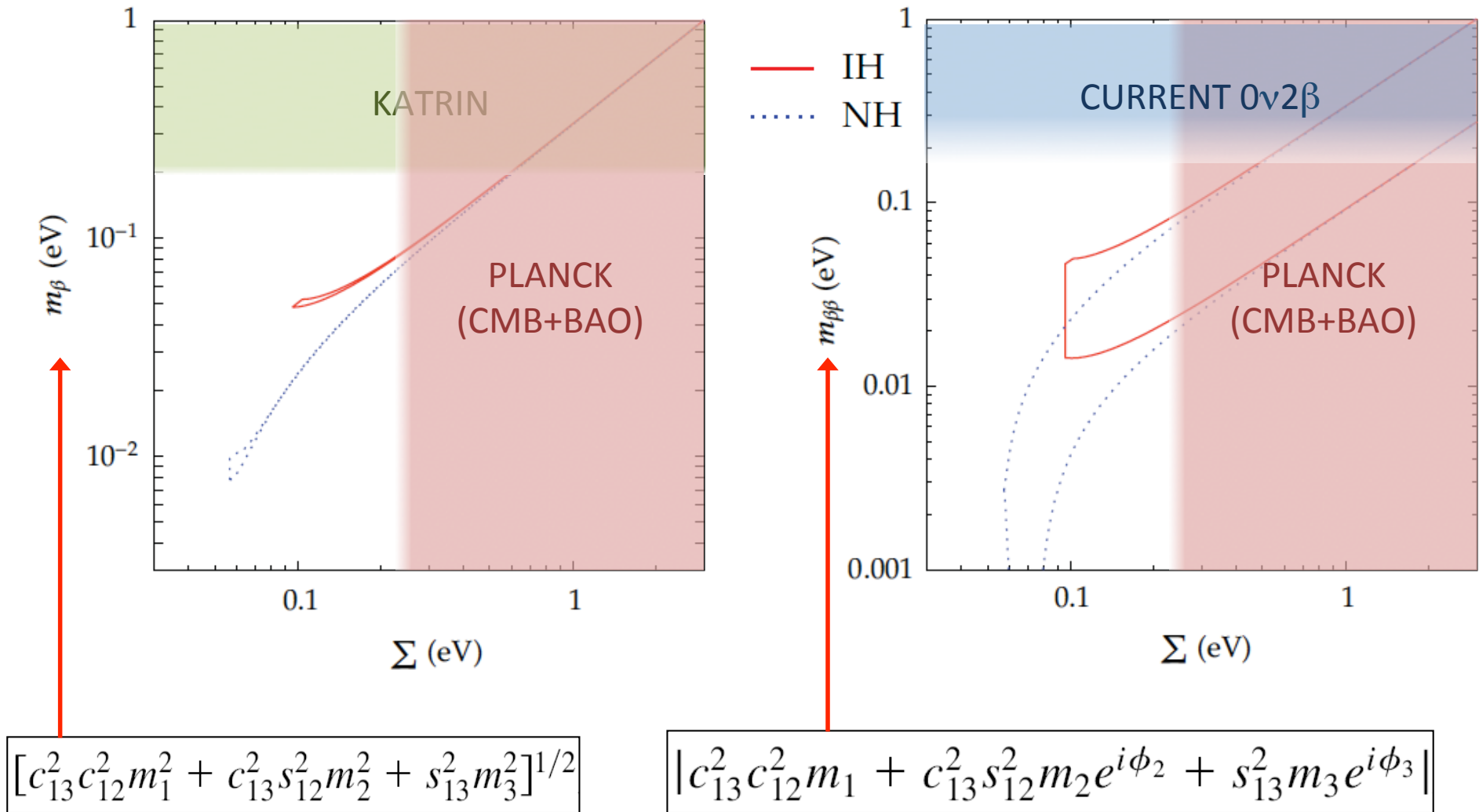
Neutrinoless double beta decay	$m_{\beta\beta} = \left \sum_i U_{ei}^2 m_i \right $	$< 0.2-0.8$ eV
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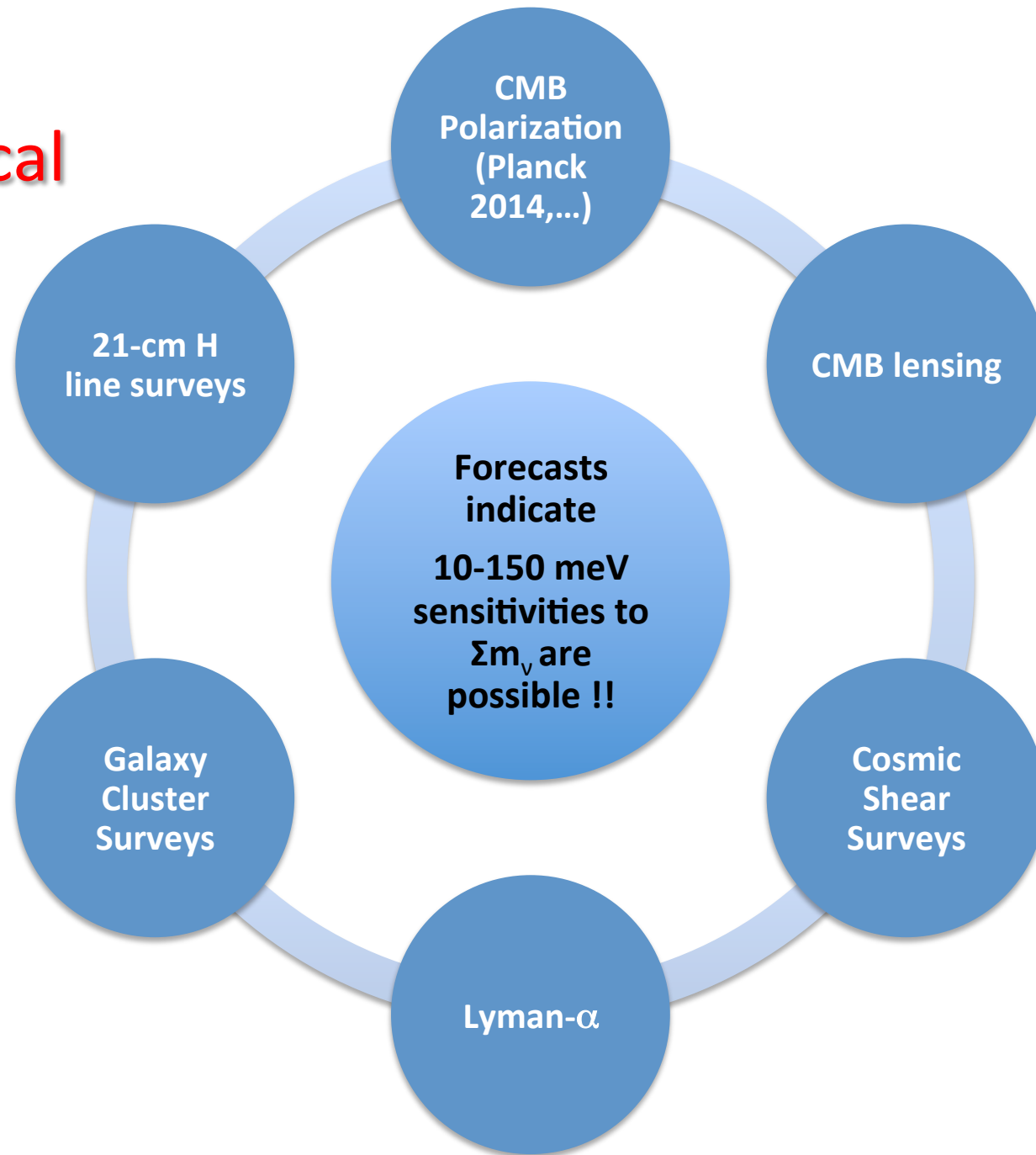
$$|c_{13}^2 c_{12}^2 m_1 + c_{13}^2 s_{12}^2 m_2 e^{i\phi_2} + s_{13}^2 m_3 e^{i\phi_3}|$$

Cosmology	$\sim \sum_i m_i$	$< 0.23-0.7$ eV
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Tritium β decay, $0\nu 2\beta$ and Cosmology

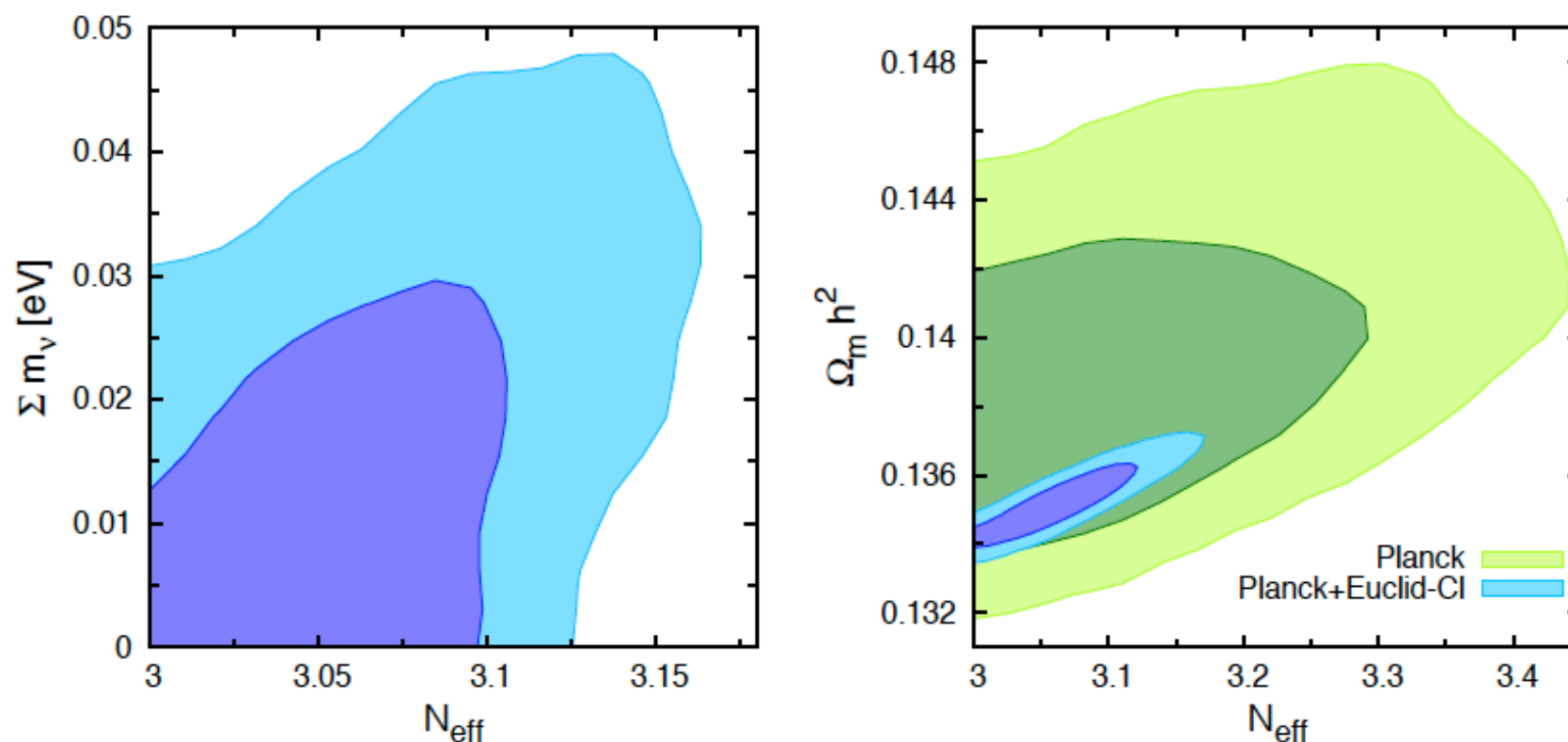


Future cosmological data



Future sensitivities to N_{eff} and Σm_ν

Example of forecast: PLANCK + Euclid-like photometric galaxy cluster survey



Data		Planck+Euclid-Cl	
Model		$w\text{CDM}+m_\nu+N_{\text{eff}}$	$\Lambda\text{CDM}+m_\nu+N_{\text{eff}}+\Omega_k$
Σm_ν [eV]	68% CL	< 0.024	< 0.024
	95% CL	< 0.046	< 0.046
N_{eff}	95% CL	< 3.16	< 3.17

M.C.A. Cerbolini et al,
JCAP 06 (2013) 020
[arXiv:1303.4550]

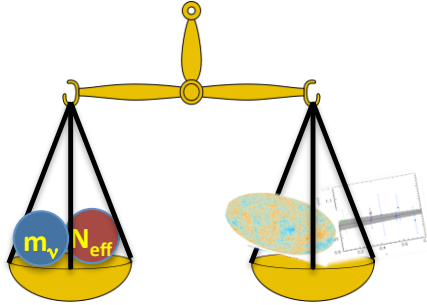
Future sensitivities on neutrino masses

5-7 years

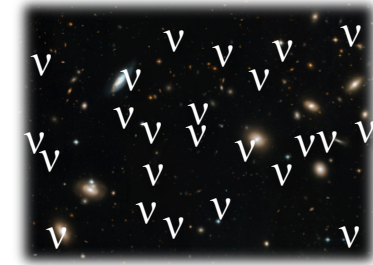
7-15 years

Probe	Potential sensitivity (short term)	Potential sensitivity (long term)
CMB	0.4-0.6	0.4
CMB with lensing	0.1-0.15	0.04
CMB + Galaxy Distribution	0.2	0.05-0.1
CMB + Lensing of Galaxies	0.1	0.03-0.04
CMB + Lyman- α	0.1-0.2	Unknown
CMB + Galaxy Clusters	-	0.05
CMB + 21 cm	-	0.0003-0.1

Table 1. Future probes of neutrino mass, as well as their projected sensitivity to neutrino mass. Sensitivity in the short term means achievable in approximately 5-7 years, while long term means 7-15 years.



Conclusions



- ✓ With Planck data, including CMB lensing, we can measure combinations of cosmological parameters with high precision. Still Λ CDM fits very well the data
- ✓ No evidence yet for nonzero neutrino masses or an enhanced radiation density (N_{eff}). Bounds $\Sigma m_\nu < 0.2-0.7$ eV (95% CL) and $N_{eff} = 3.15 \pm 0.23$ (68% CL), depending on data
- ✓ Improved sensitivities from a variety of future cosmological data to reach $\Sigma m_\nu < 0.1$ eV

For more details...

