

Charm Activities

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outline:

- charm golden channels
- status of the ongoing work
- new ideas & projects

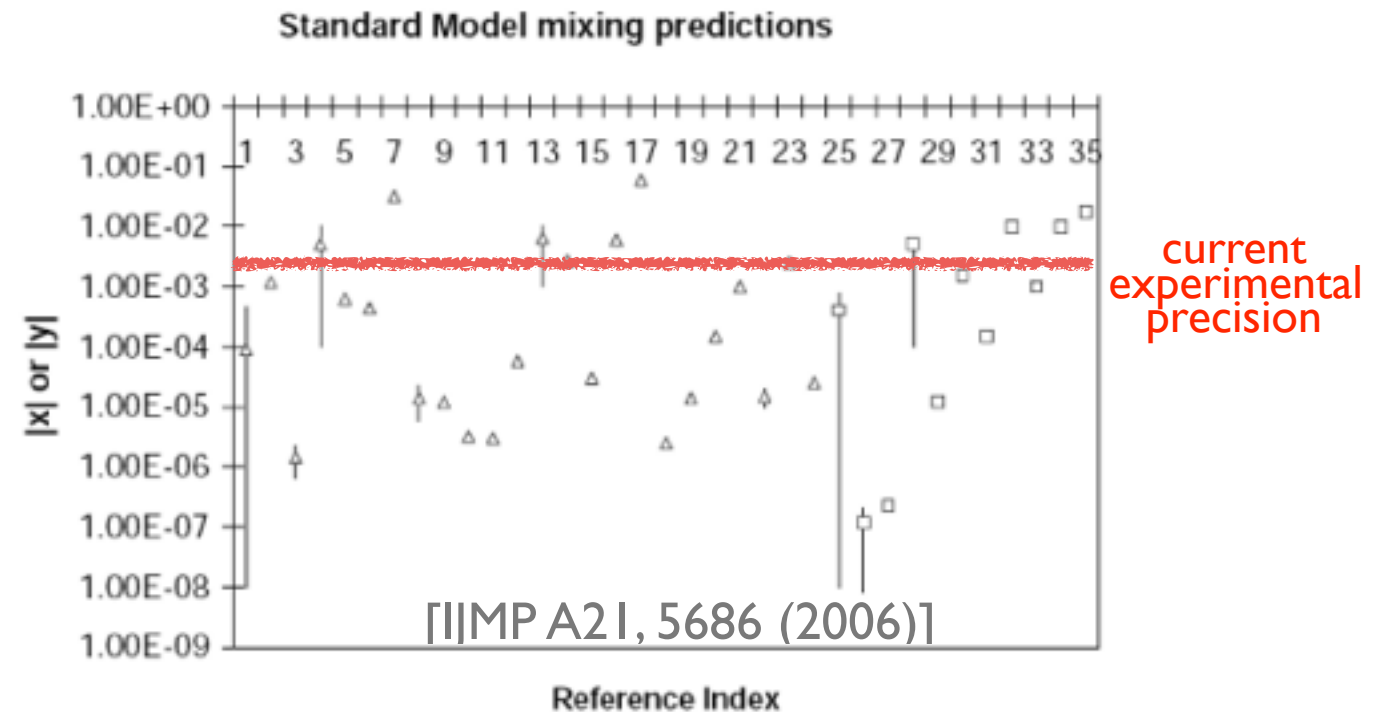
B2TiP charm brainstorm session attendance
(+ few more people connected remotely)



Are there Golden Channels in Charm?

➔ The Standard Model *predictions* on mixing and CP Violation parameters are affected by large uncertainties due to the difficulties in the computation of the dominant long-distance contributions:

- computation of D-mixing diagrams is non perturbative
- the available computational power is not enough for lattice QCD



➔ Theory needs experimental inputs not only to check the final predictions but also to test the model hypotheses

- employ a parameterisation that is appropriate for the level of precision expected in the BelleII/LHCb-upgrade era
- infer the presence of NP in direct CPV measurements using SM SU(3) relations (+ evaluate SU(3) breaking)

➔ Golden Channel does not only mean “sensitive to NP” charm.

- e.g. $D^+ \rightarrow \pi^+ \pi^0$ is golden since SM contribution to A_{CP} is small and there are no QCD penguins to estimate

The (many) Charm Golden Channels

2. Hadronic Modes

time-dependent CPV & mixing,
time-integrated analyses, A_{CP}

← (a) $D^0 \rightarrow K^+ \pi^-, K^+ K^-, \pi^+ \pi^-$

time-integrated analyses, A_{CP}

← (b) $D^0 \rightarrow K_S^0 K_S^0, \pi^0 \pi^0, D^+ \rightarrow \pi^+ \pi^0, D^0 \rightarrow K_S \pi^0, \text{ more FCNC}$

Dalitz Plot Analyses

time-dependent CPV & mixing

← (c) $D^0 \rightarrow K_S^0 K^+ K^-, K_S^0 K^+ \pi^-, K^+ \pi^- \pi^0, K_S^0 \pi^+ \pi^-, \pi^+ \pi^- \pi^0$

3. Semileptonic Modes

+ T violation with $D^0 \rightarrow K_S \pi^0 \pi^+ \pi^-$

4. Leptonic and Radiative Decays

important for lattice QCD

← (a) $D_{(s)}^+ \rightarrow e^+ \nu, \mu^+ \nu, \tau^+ \nu$

NP searches

← (b) $D^0 \rightarrow \rho^0 \gamma, D^0 \rightarrow w \gamma, D^0 \rightarrow \gamma \gamma$

5. Other (more exotic stuff)

e.g. light dark matter searches

← (a) missing energy modes

(b) glueballs

(c) $D_s^+ \rightarrow p \bar{n}$

basf2 Simulation Studies

Alan is studying BelleII sensitivity to CPV, given the improvement in t resolution

Giulia (+...any volunteer?) will start looking at the A_{CP} analysis in basf2

time-dependent CPV & mixing, time-integrated analyses, A_{CP} , time-dependent CPV & mixing, Dalitz Plot Analyses

what's the ultimate prediction on x ?

(a) $D^0 \rightarrow K^+ \pi^-$, $K^+ K^-$, $\pi^+ \pi^-$

(b) $D^0 \rightarrow K_S^0 K_S^0$, $\pi^0 \pi^0$, $D^+ \rightarrow \pi^+ \pi^0$, $D^0 \rightarrow K_S \pi^0$, more FCNC

(c) $D^0 \rightarrow K_S^0 K^+ K^-$, $K_S^0 K^+ \pi^-$, $K^+ \pi^- \pi^0$, $K_S^0 \pi^+ \pi^-$, $\pi^+ \pi^- \pi^0$

The $D^0 \rightarrow K_S \pi^0 \pi^+ \pi^-$ analysis is ongoing in Belle, $\Rightarrow$ estimate sensitivity at BelleII (Chennai)

T violation with $D^0 \rightarrow K_S \pi^0 \pi^+ \pi^-$

4. Leptonic and Radiative Decays

important for lattice QCD

(a) $D_{(s)}^+ \rightarrow e^+ \nu$, $\mu^+ \nu$, $\tau^+ \nu$

Jake (CMU) will start looking at leptonic reconstruction in basf2

NP searches

(b) $D^0 \rightarrow \rho^0 \gamma$, $D^0 \rightarrow w \gamma$, $D^0 \rightarrow \gamma \gamma$

The $D^0 \rightarrow V \gamma$ analysis is near completion in Belle, (FC stuff)
 $\Rightarrow$ estimate sensitivity at BelleII (Ljubljana)

The $D^0 \rightarrow \gamma \gamma$ analysis is near completion in Belle,
 $\Rightarrow$ estimate sensitivity at BelleII (TATA)

e.g. light dark matter searches $\leftarrow$ (a) missing energy modes

(b) glueballs

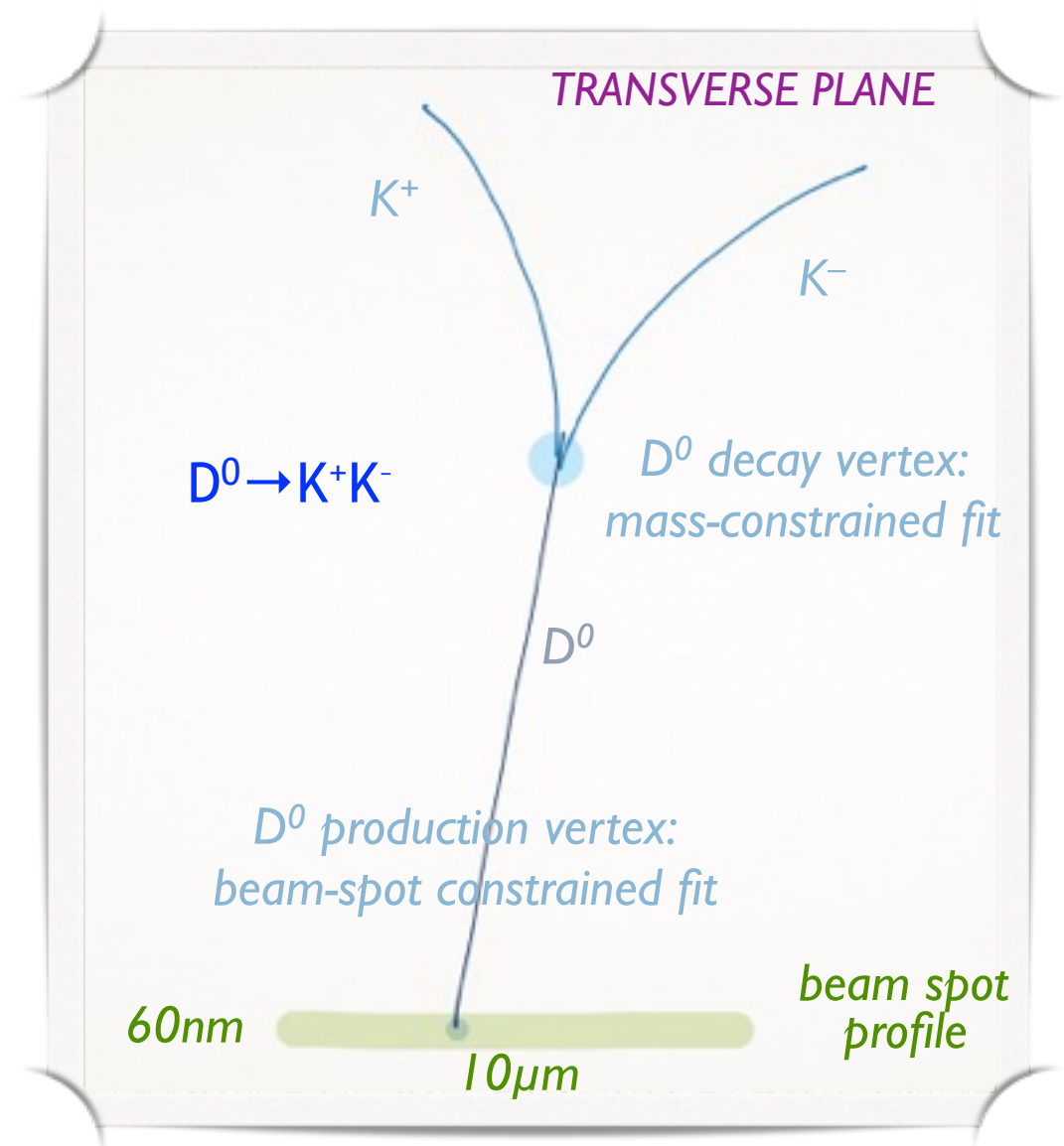
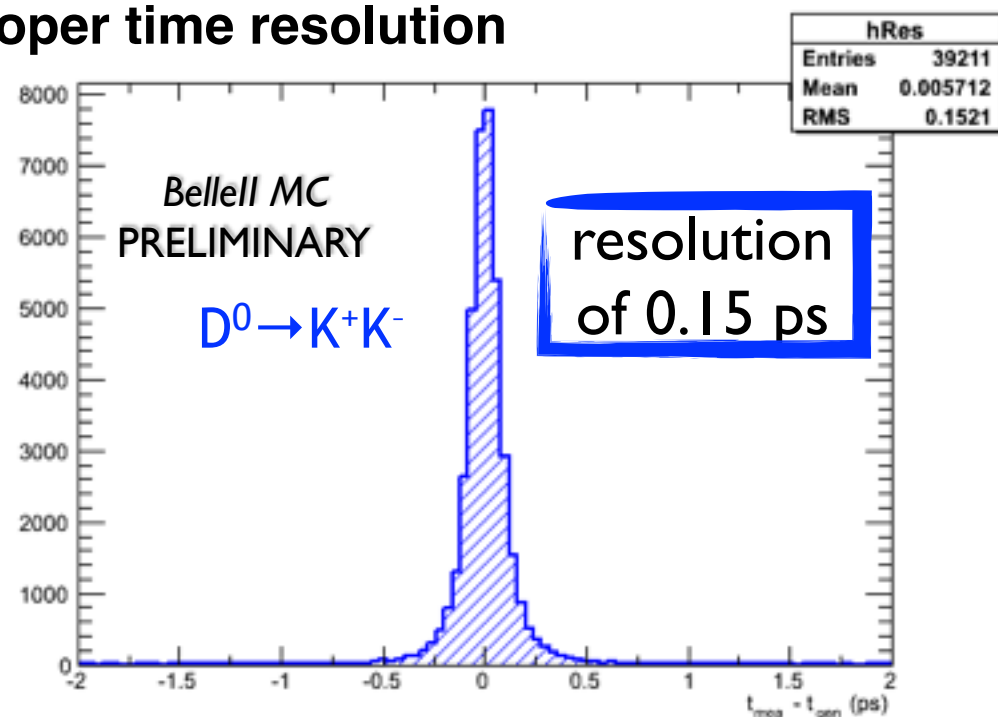
(c) $D_s^+ \rightarrow p \bar{n}$

Giacomo (Pisa) is studying the feasibility of prompt D^0 flavour tagging: increase the statistics + provide control samples for many analysis

Proper Time Resolution for $e^+e^- \rightarrow D X$

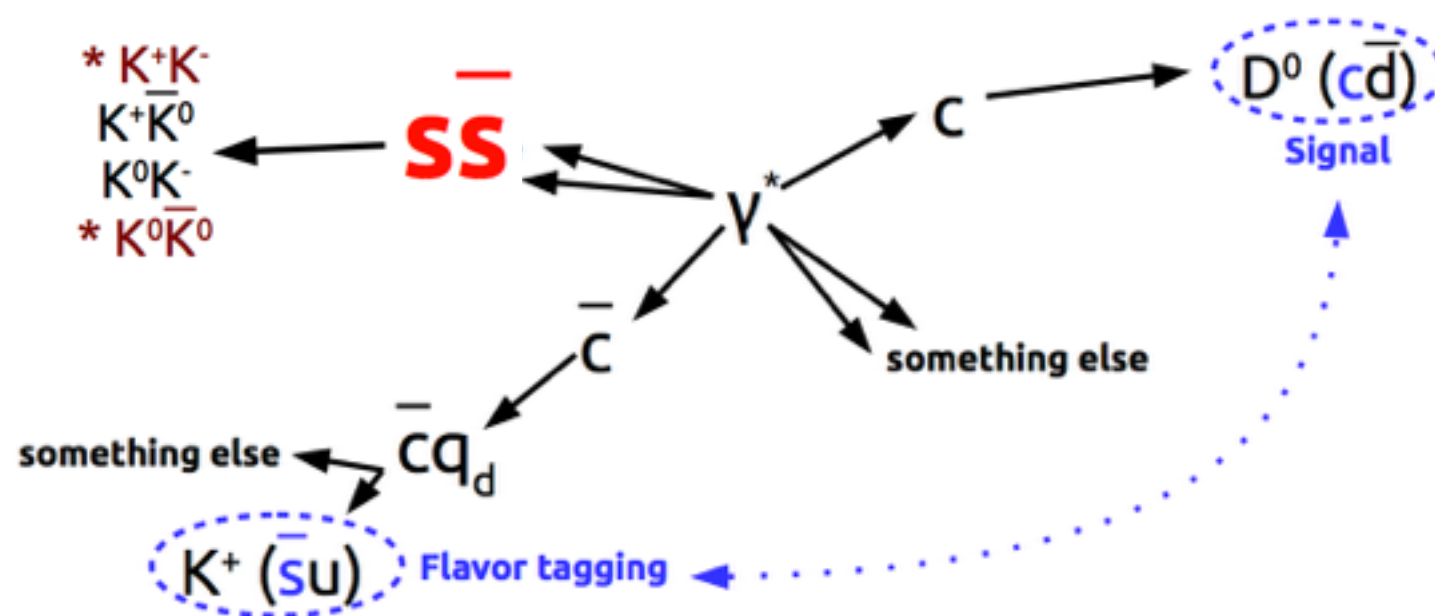
- ➔ We can measure the proper time of D^0 coming directly from the hadronization of the charm quark with comparable precision.
- ➔ This measurement was not possible at B-Factories
- ➔ The flavour of the D^0 at production cannot be tagged in the standard way ($D^* \rightarrow D^0 \pi$)

proper time resolution

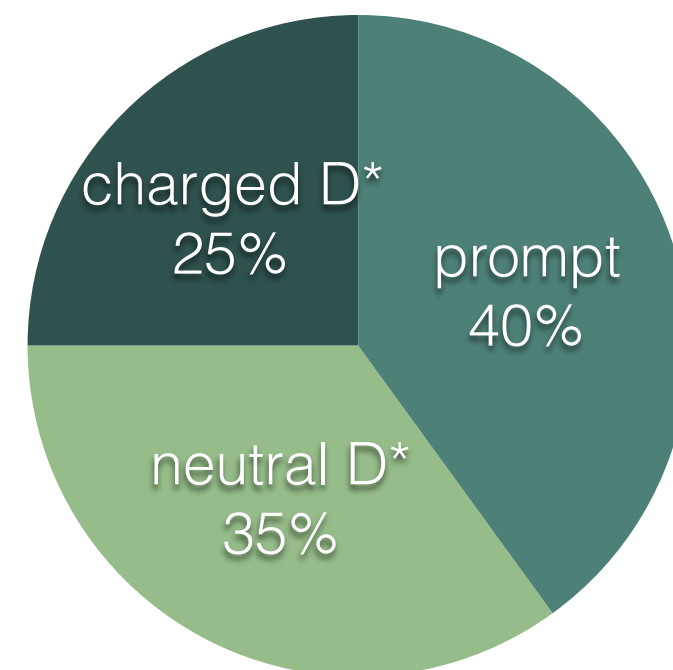


NOTE: the cartoon is not to scale

- ➔ Only 1/4 of the D^0 produced in the $e^+e^- \rightarrow c\bar{c}$ events are flavour tagged with $D^{*+} \rightarrow D^0\pi^+$ and used for CP violation measurements
- ➔ Implement a reconstruction technique that allows to tag the flavour the rest 75% of produced D^0 looking at the rest of the event
 - select events with one single charged K in the rest of the event



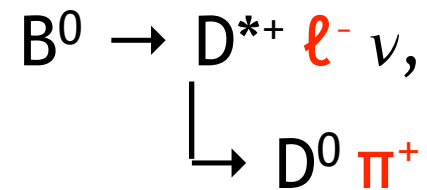
D^0 mothers in $c\bar{c}$ events



see Giacomo's slides

- ➔ First Results are encouraging 20% reconstruction efficiency

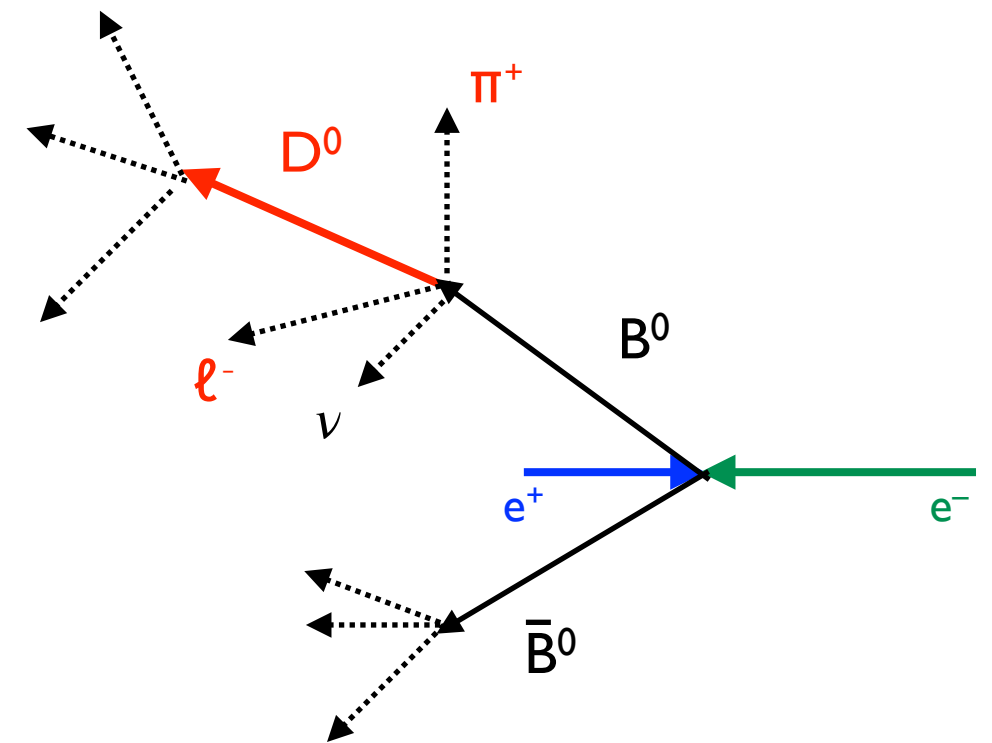
Charm from B Decays



Partial Reconstruction of the B assuming...

- ➔ B^0 is at rest in the center-of-mass of the $Y(4S)$ ($p=380\text{MeV}/c$)
- ➔ D^0 produced at rest in the center-of-mass of the D^{*+} , therefore:
 - $p(D^{*+}) = \alpha + \beta p(\pi_s)$
 - D^{*+} and π_s have the same direction

...allows to compute the M_v^2 peaking at 0 for signal.



Estimate from BABAR (200fb^{-1} onPeak + 22fb^{-1} offPeak):
[M.Rotondo, F.Simonetto]

tag	# signal	purity
e	2150	52%
μ	1740	55%

1 ab^{-1}
6M
4.8M

= 10M/ab tagged D^0



Dark Matter Searches in Charm?



- ➡ $D \rightarrow \nu\nu$ decay is helicity suppressed in the SM resulting in a tiny branching ratio:
 - $\text{BR}(D \rightarrow \nu\nu) \approx 1.1 \cdot 10^{-30}$, adding a photon in the final state $\text{BR}(D \rightarrow \nu\nu\gamma) \approx 4 \cdot 10^{-14}$
- ➡ **New Physics** may enhance the branching ratio:
 - add a particle in the final state
 - introduce other ways of flipping helicity
- ➡ Missing Energy does not always mean neutrinos!
 - can be **light dark matter** candidates: $D \rightarrow \text{invisible}$ puts nice constraints on light dark matter properties!
- ➡ *Extremely* challenging from the experimental side
 - can use D from B decays and fully reconstruct the other B...
 - expected dominant background from K_L



Conclusions

- ➡ *BelleII* can do better in charm w.r.t. B-Factories than just luminosity scaling!
- ➡ basf2 simulations are needed in order to better estimate the improvements of channels already done at B-Factories and to have the first estimations on new channels/analyses
- ➡ The simulation activity has started!
 - mostly Belle students extrapolating to *BelleII*
 - Giacomo De Pietro on prompt D^0 tagging
 - Jake Bennet (on leptonic/semileptonic reconstruction)
 - more people needed...
- ➡ There are interesting things to do: new/better detector = new things we can do
- ➡ Let's grow the Italian contribution to charm...







General Comments from the Experimental Side

“Golden mode” definition:

a mode in which Belle II will be competitive (with LHCb) and, if NP is present at a sufficiently large level, its signature will be measured/identified

- ★ good criteria to select among the many channels and observables

Future work to complete our report:

A. Schwartz

- Belle II decay time resolution: *improvement over Belle due to pixel layers*
 - Systematic error budget: *which errors are scalable with luminosity, which are not (and how to treat them)*
 - BASFII simulation: *more realistic MC study with proper Belle II detector acceptance/response (esp: pixels, SVD, CDC tracking, iTOP)*
- ★ Need basf2 simulation studies in order to have a better estimate of the expected precision that takes into account improvements in the detector & reconstruction techniques for the other channels
 - the impact of the better time resolution on the mixing parameters has been evaluated with basf2 simulation + ToyMC

CP Asymmetries

2. Hadronic Modes

time-dependent CPV & mixing,
time-integrated analyses, A_{CP}

time-integrated analyses, A_{CP}

Delitz Plot Analyses

time-depe

impor

e.g. light c

$$(a) \quad D^0 \rightarrow K^+ \pi^-, K^+ K^-, \pi^+ \pi^-$$

$$(b) \quad D^0 \rightarrow K_S^0 K_S^0, \pi^0 \pi^0, D^+ \rightarrow \pi^+ \pi^0, D^0 \rightarrow K_S \pi^0, \text{ more FCNC}$$

$$D^0 \rightarrow K^+ K^-, D \rightarrow \pi^+ \pi^-$$

[t] remember the ΔA_{CP} saga: is it NP or SM? Need to estimate the size of penguin/penguin contractions VS tree: hard to do

[t] measuring BR and A_{CP} one can combine modes using sum rules and getting rid of the direct estimation of the SM contribution

[e] it's worth doing these evergreen modes, the extrapolated final precision is comparable with LHCb

$$D^+ \rightarrow \pi^+ \pi^0$$

[t] golden since SM contribution to A_{CP} is small

[t] no QCD penguin contribution (hard to estimate)

[e] can do modes with neutrals in the final state that LHCb can't do

[e] improved K_S reconstruction efficiency

$$\pi^0 \pi^+ \pi^-$$

Time-Dependence on A_{CP}

2. Hadronic Modes

time-dependent CPV & mixing,
time-integrated analyses, A_{CP}

time-integrated analyses, A_{CP}

Dalitz Plot Analyses

time-dependent CPV & mixing

(a) $D^0 \rightarrow K^+ \pi^-, K^+ K^-, \pi^+ \pi^-$

(b) $D^0 \rightarrow K_S^0 K_S^0, \pi^0 \pi^0, D^+ \rightarrow \pi^+ \pi^0, D^0 \rightarrow K_S \pi^0, \text{ more FCNC}$

(c) $D^0 \rightarrow K_S^0 K^+ K^-, K_S^0 K^+ \pi^-, K^+ \pi^- \pi^0, K_S^0 \pi^+ \pi^-, \pi^+ \pi^- \pi^0$

3. Semileptonic Modes

+ T violation, with $D^0 \rightarrow K e \pi^0 \pi^+ \pi^-$

$$A_{CP}(t)$$

import

[t] study the time-dependence of A_{CP} to increase sensitivity to CPV in the interference between decays with and without mixing

[e] We can do it. Time resolution may not be sufficient to give precision measurement of the *difference* in oscillation period between D^0 and $\bar{D}^0$, need to be studied.

[e] D^0 from D^* and prompt D^0 have compatible time resolutions, and a factor 2 better than Belle

e.g. light da

(b) glueballs

(c) $D_s^+ \rightarrow p \bar{n}$

NP Searches in Radiative Decays

2. Hadronic Modes

$$D^0 \rightarrow \rho^0 \gamma, D^0 \rightarrow \omega \gamma \text{ (i.e.: } D^0 \rightarrow V \gamma \text{)}$$

[e] BelleII can do modes with photons in the final state that LHCb can not do

[t] long distance (LD) contributions are dominant

[t] LD contributions complicate the interpretations of the measurements

[t] find combinations of channels in which the LD contributions cancel:

$$R_{\omega\gamma} = (\Gamma(D^0 \rightarrow \omega \gamma) - \Gamma(D^0 \rightarrow \rho \gamma)) / \Gamma(D^0 \rightarrow \omega \gamma)$$

$$\rho^0 = (\underline{u}u - \underline{d}d)/\sqrt{2} \quad \text{vs} \quad \omega = (\underline{u}u + \underline{d}d)/\sqrt{2}$$

NP searches ← (b) $D^0 \rightarrow \rho^0 \gamma, D^0 \rightarrow \omega \gamma, D^0 \rightarrow \gamma \gamma$

5. Other (more exotic stuff)

[t] also consider isospin asymmetries:

$$R_I = (2\Gamma(D^0 \rightarrow \rho^0 \gamma) - \Gamma(D^+ \rightarrow \rho^+ \gamma)) / (\text{the sum})$$

[same for ω]

$\pi^+ \pi^-$

$\pi^+ \pi^-$

$\pi^+ \pi^-$

Modes with K_S in the Final State

2. Hadronic Modes

time-dependent CPV & mixing,
time-integrated analyses, A_{CP}

time-integrated analyses, A_{CP}

Dalitz Plot Analyses

time-dependent CPV & mixing

(a) $D^0 \rightarrow K^+ \pi^-, K^+ K^-, \pi^+ \pi^-$

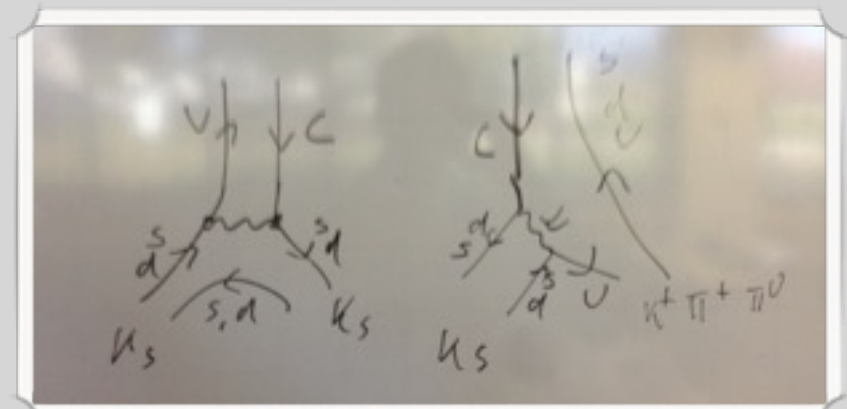
(b) $D^0 \rightarrow K_S^0 K_S^0, \pi^0 \pi^0, D^+ \rightarrow \pi^+ \pi^0, D^0 \rightarrow K_S \pi^0$, more FCNC

(c) $D^0 \rightarrow K_S^0 K^+ K^-, K_S^0 K^+ \pi^-, K^+ \pi^- \pi^0, K_S^0 \pi^+ \pi^-, \pi^+ \pi^- \pi^0$

$D^0 \rightarrow K_S K_S$ & K_S in the final states

import

[t] Uli Nierste: SM direct CPV contribution smaller than 1.1% ($D^0 \rightarrow K_S K_S$)
(Phys. Rev. D 92, 054036)



e.g. light da

[e] K^0 regeneration in the material may be one of the limiting systematics at 50 ab^{-1} for A_{CP} measurements and it should be carefully evaluated
[e] CPV in K^0 should also be treated correctly

Other Scattered Comments on Hadronic Modes

2. Hadronic Modes

- time-dependent CPV & mixing, time-integrated analyses, A_{CP} ← (a) $D^0 \rightarrow K^+ \pi^-, K^+ K^-, \pi^+ \pi^-$
- time-integrated analyses, A_{CP} ← (b) $D^0 \rightarrow K_S^0 K_S^0, \pi^0 \pi^0, D^+ \rightarrow \pi^+ \pi^0, D^0 \rightarrow K_S \pi^0, \text{ more FCNC}$
- Dalitz Plot Analyses time-dependent CPV & mixing ← (c) $D^0 \rightarrow K_S^0 K^+ K^-, K_S^0 K^+ \pi^-, K^+ \pi^- \pi^0, K_S^0 \pi^+ \pi^-, \pi^+ \pi^- \pi^0$
3. Semileptonic Modes + T violation with $D^0 \rightarrow K_S \pi^0 \pi^+ \pi^-$

important

- [t] look for CP asymmetries in localised regions of the Dalitz Plots
- [e] Yes we can do it, done already with $D^0 \rightarrow K^+ \pi^- \pi^0$ at $BABAR$
- [t] $D \rightarrow VV$ modes can help constrain LD contributions to the mixing parameters

4. Other (more exotic stuff)

- e.g. light dark matter searches ← (a) missing energy modes
- (b) glueballs
- (c) $D_s^+ \rightarrow p \bar{n}$

Leptonic Decays

2. Hadronic Modes

- [e] D^+ decays not measured at Belle: no estimation on BR
- [e] Anze has provided some results with Belle MC
- [e] K_L will be the limitation of this measurement, a veto must be studied
- [e] can try new reconstruction techniques given the better performances of tracking and vertexing

FCNC

$\pi^+\pi^-\pi^0$

$\pi^0\pi^+\pi^-$

4. Leptonic and Radiative Decays

important for lattice QCD $\leftarrow$ (a) $D_{(s)}^+ \rightarrow e^+\nu, \mu^+\nu, \tau^+\nu$

NP searches $\leftarrow$ (b) $D^0 \rightarrow \rho^0\gamma, D^0 \rightarrow w\gamma, D^0 \rightarrow \gamma\gamma$

5. Other (more exotic stuff)

- e.g. light dark matter searches $\leftarrow$
- (a) missing energy modes
 - (b) glueballs
 - (c) $D_s^+ \rightarrow p\bar{n}$

Dark Matter Searches

2. Hadronic Modes

time-dependent CPV & mixing,
time-integrated analyses, A_{CP}

time-integrated analyses, A_{CP}

time-depen

import

← (a) $D^0 \rightarrow K^+ \pi^-, K^+ K^-, \pi^+ \pi^-$

← (b) $D^0 \rightarrow K_S^0 K_S^0, \pi^0 \pi^0, D^+ \rightarrow \pi^+ \pi^0, D^0 \rightarrow K_S^0 \pi^0$ more FCNC

$D \rightarrow \text{invisible}, D \rightarrow \text{invisible } \gamma$

$\pi^- \pi^0$

$D^0 \pi^+ \pi^-$

- [t] branching ratio of $D \rightarrow \nu \bar{\nu}$ is tiny in SM (helicity suppression)
- [t] branching ratio of $D \rightarrow \nu \bar{\nu}(\gamma)$ is still tiny in SM
- [t] missing energy can be something different from neutrinos!
- [t] nice constraints on light dark matter (and light higgs) properties
- [e] experimentally very challenging. Can think of using D from fully reconstructed B events to reduce the background, but pay in terms of reconstruction efficiency

e.g. light dark matter searches ← (a) missing energy modes

(b) glueballs

(c) $D_s^+ \rightarrow p \bar{n}$

Theory Motivational Speech

What did we learn from Δa_{CP} saga?

★ Is it Standard Model or New Physics? Theorists used to say...

Naively, any CP-violating signal in the SM will be small, at most $O(V_{ub}V_{cb}^*/V_{us}V_{cs}^*) \sim 10^{-3}$
 Thus, $O(1\%)$ CP-violating signal can provide a "smoking gun" signature of New Physics

...what do you say now?

★ assuming SU(3) symmetry, $a_{CP}(\pi\pi) \sim a_{CP}(KK) \sim 0.15\%$. Looks more or less 0.1%...

★ let us try Standard Model

- need to estimate size of penguin/penguin contractions vs. tree

Find new observables!

★ Find processes where the Standard Model contribution to A_{CP} is small

★ Look at non-leptonic decays $D \rightarrow \pi\pi$

★ Look at non-leptonic decays $D \rightarrow KsKs$

no contributions from QCD penguins

Rare and radiative decays

★ Can New Physics be "hiding" in the up-type quark transitions

- explicit models can be constructed where it can be done
- long-distance effects complicate interpretation
- must use exp and theo tricks to sort out

Maybe correlations between different measurements can help sorting out NP in charm?

★ Standard Model contribution to $D \rightarrow \gamma\gamma$ - SM contribution is dominated by LD effects

★ Try to find combinations of decays where LD contributions cancel

★ Radiative decays $D \rightarrow \gamma X$, $\gamma\gamma$: FCNC transition $c \rightarrow u \gamma$

- SM contribution is dominated by LD effects
- dominated by SM anyway: useless for NP studies?

★ Consider exclusive decays $D \rightarrow \gamma \rho$, $\gamma \omega$: $\omega^{(I=0)} = \frac{1}{\sqrt{2}}(\bar{u}u + \bar{d}d)$, $\rho^{(I=1)} = \frac{1}{\sqrt{2}}(\bar{u}u - \bar{d}d)$

- Extract $c \rightarrow uu \gamma$: LD contribution cancels $R_{uu\gamma} = \frac{\Gamma(D^0 \rightarrow \omega\gamma) - \Gamma(D^0 \rightarrow \rho^0\gamma)}{\Gamma(D^0 \rightarrow \omega\gamma)}$

- Consider **isospin** asymmetries $R_I = \frac{2\Gamma(D^0 \rightarrow \rho^0\gamma) - \Gamma(D^+ \rightarrow \rho^+\gamma)}{2\Gamma(D^0 \rightarrow \rho^0\gamma) + \Gamma(D^+ \rightarrow \rho^+\gamma)}$

- isospin asymmetries are sensitive to 4-fermion operators with photon emissions from "spectators"

★ Standard Model contribution to $D \rightarrow \mu\mu$

- could be used to study **NP effects in correlation with D-mixing**

Rare D(B)-decays with missing energy

➤ D-decays with missing energy can probe both heavy and light (DM) NP

★ SM process: $D \rightarrow \nu\nu$ and $D \rightarrow \nu\nu\gamma$:

- for B-decays $J_{Oa}^\mu = \bar{q}_L \gamma^\mu b_L$
- for D-decays $J_{Qq}^\mu = \bar{u}_L \gamma^\mu c_L$

★ For B(D) $\rightarrow \nu\nu$ decays SM branching ratios are tiny

- SM decay is helicity suppressed, e.g.

$$\mathcal{B}(B_s \rightarrow \nu\bar{\nu}) = \frac{G_F^2 \alpha^2 f_B^2 M_B^3}{16\pi^3 \sin^4 \theta_W \Gamma_{B_s}} |V_{tb} V_{ts}^*|^2 X(x_t)^2 x_\nu^2$$

- NP: other ways of flipping helicity?
- add a third particle to the final state?

What would happen if a photon is added to the final state?

★ For B(D) $\rightarrow \nu\nu\gamma$ decays SM branching ratios are still tiny

- need form-factors to describe the transition
- helicity suppression is lifted

★ BUT: missing energy does not always mean neutrinos

- nice constraints on light Dark Matter properties!!!

Decay	Branching ratio
$B_s \rightarrow \nu\bar{\nu}$	3.07×10^{-24}
$B_d \rightarrow \nu\bar{\nu}$	1.24×10^{-25}
$D^0 \rightarrow \nu\bar{\nu}$	1.1×10^{-30}

Decay	Branching ratio
$B_s \rightarrow \nu\bar{\nu}\gamma$	3.68×10^{-8}
$B_d \rightarrow \nu\bar{\nu}\gamma$	1.96×10^{-9}
$D^0 \rightarrow \nu\bar{\nu}\gamma$	3.96×10^{-14}

Badin, AAP (2010)

Extrapolations on Time-Integrated Measurements

mode	$\mathcal{L}$ (fb $^{-1}$)	A_{CP} (%)	Belle II at 50 ab $^{-1}$
$D^0 \rightarrow K^+ K^-$	976	$-0.32 \pm 0.21 \pm 0.09$	± 0.03
$D^0 \rightarrow \pi^+ \pi^-$	976	$+0.55 \pm 0.36 \pm 0.09$	± 0.05
$D^0 \rightarrow \pi^0 \pi^0$	976	$\sim \pm 0.60$	± 0.08
$D^0 \rightarrow K_s^0 \pi^0$	791	$-0.28 \pm 0.19 \pm 0.10$	± 0.03
$D^0 \rightarrow K_s^0 \eta$	791	$+0.54 \pm 0.51 \pm 0.16$	± 0.07
$D^0 \rightarrow K_s^0 \eta'$	791	$+0.98 \pm 0.67 \pm 0.14$	± 0.09
$D^0 \rightarrow \pi^+ \pi^- \pi^0$	532	$+0.43 \pm 1.30$	± 0.13
$D^0 \rightarrow K^+ \pi^- \pi^0$	281	-0.60 ± 5.30	± 0.40
$D^0 \rightarrow K^+ \pi^- \pi^+ \pi^-$	281	-1.80 ± 4.40	± 0.33
$D^+ \rightarrow \phi \pi^+$	955	$+0.51 \pm 0.28 \pm 0.05$	± 0.04
$D^+ \rightarrow \eta \pi^+$	791	$+1.74 \pm 1.13 \pm 0.19$	± 0.14
$D^+ \rightarrow \eta' \pi^+$	791	$-0.12 \pm 1.12 \pm 0.17$	± 0.14
$D^+ \rightarrow K_s^0 \pi^+$	977	$-0.36 \pm 0.09 \pm 0.07$	± 0.03
$D^+ \rightarrow K_s^0 K^+$	977	$-0.25 \pm 0.28 \pm 0.14$	± 0.05
$D_s^+ \rightarrow K_s^0 \pi^+$	673	$+5.45 \pm 2.50 \pm 0.33$	± 0.29
$D_s^+ \rightarrow K_s^0 K^+$	673	$+0.12 \pm 0.36 \pm 0.22$	± 0.05

$$\sigma_{BelleII} = \sqrt{(\sigma_{stat}^2 + \sigma_{sys}^2) \frac{\mathcal{L}_{Belle}}{50 \text{ ab}^{-1}} + \sigma_{ired}^2}$$

Extrapolations on Time-Dependent Measurements

$D^0 \rightarrow K^{(*)-} \ell^+ \nu$	492 fb ⁻¹	50 ab ⁻¹
R_M	$(1.3 \pm 2.2 \pm 2.0) \times 10^{-4}$	$\pm 0.3 \times 10^{-4}$
$D^0 \rightarrow K^+ K^-, \pi^+ \pi^-$	976 fb ⁻¹	50 ab ⁻¹
y_{CP}	$(1.11 \pm 0.22 \pm 0.11)\%$	$\pm 0.04\%$
A_Γ	$(-0.03 \pm 0.20 \pm 0.08)\%$	$\pm 0.03\%$
$D^0 \rightarrow K^+ \pi^-$	400 fb ⁻¹	50 ab ⁻¹
x'^2	$(1.8 \pm 2.2 \pm 1.1) \times 10^{-4}$	$\pm 0.22 \times 10^{-4}$
y'	$(0.06 \pm 0.40 \pm 0.20)\%$	$\pm 0.04\%$
A_M	0.67 ± 1.20	± 0.11
$ \phi $	0.16 ± 0.44	± 0.04
$D^0 \rightarrow K_s^0 \pi^+ \pi^-$	921 fb ⁻¹	50 ab ⁻¹
x	$(0.56 \pm 0.19 \pm 0.06 \pm 0.08)\%$	$\pm 0.08\%$
y	$(0.30 \pm 0.15 \pm 0.06 \pm 0.04)\%$	$\pm 0.05\%$
$ q/p $	$0.90 \pm 0.16 \pm 0.04 \pm 0.06$	± 0.06
ϕ	$-0.10 \pm 0.19 \pm 0.04 \pm 0.07$	± 0.07

$$\sigma_{BelleII} = \sqrt{(\sigma_{stat}^2 + \sigma_{sys}^2) \frac{\mathcal{L}_{Belle}}{50 \text{ ab}^{-1}} + \sigma_{ired}^2}$$