Self-interacting dark matter

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Cold collisionless dark matter paradigm

Dark matter (DM) is about 25% of the Universe









To date, evidence for DM from gravity only



Non-gravitational dark matter interactions







WIMP paradigm: expect dark matter in one or more of these channels

Can we learn about the dark sector if DM has highly suppressed couplings to SM?

Non-gravitational dark matter interactions









Outline

• Issues with CDM (cold collisionless DM)

 Discrepancies between N-body simulations and astrophysical observations

- Self-interacting dark matter
 - Probe dark sector independent of couplings to SM
 - Particle physics implications
 - Complementarity with WIMP searches

CDM in trouble

- 1. Core-vs-cusp problem Moore (1994), Flores & Primack (1994)
 - $\quad \mbox{Central densities of halos are cored} \\ \mbox{DM density: } \rho \sim r^{\alpha} \qquad \alpha \sim -1 \mbox{ (cusp/NFW)} \quad \mbox{or} \quad \alpha \sim 0 \mbox{ (core)} \\ \end{array}$
- 2. Too-big-to-fail problem Boylan-Kolchin, Bullock, Kaplinghat (2011 + 2012)
 - Simulations predict O(10) massive MW satellites more massive than observed MW dSphs
- 3. Missing satellite problem Klypin et al (1999), Moore et al (1999)
 - Fewer small MW dSphs than predicted by simulation
 - Small enough to fail

1. Core-vs-cusp problem

Cores seem fairly ubiquitous:

- 1. Field dwarfs
- 2. Satellite dwarf galaxies
- 3. Low surface brightness galaxies (LSBs)
- 4. Clusters

Cores in field dwarfs

Moore (1994), Flores & Primack (1994), ...

THINGS (dwarf galaxy survey) - Oh et al. (2011)



Cores in MW dwarf spheroidals



Stellar subpopulations (metal-rich & metal-poor) as "test masses" in gravitational potential

Walker & Penarrubia (2011)



See also: Kuzio de Naray et al (2007); Kuzio de Naray & Spekkens (2011)

log(*p*/[M_© pc⁻³]





Use multiple measurements to study dark matter halo

Newman et al (2012)

Weak gravitational lensing at large distance

Gravitational lensing arcs (strong lensing) at medium distance

Stellar kinematics for the cluster center



Newman et al (2012)

Radius [kpc]

2. Too-big-to-fail problem

Boylan-Kolchin, Bullock, Kaplinghat (2011 + 2012)

MW galaxy should have O(10) satellite galaxies which are more massive than the most massive (classical) dwarf spheroidals



From Weinberg, Bullock, Governato, Kuzio de Naray, Peter (2013)

2. Too-big-to-fail problem

Is there a problem beyond the Milky Way? ^{Tollerud et al. (2014)} Garrison-Kimmel et al. (2014)



CDM Problems

- Problem with our interpretation of observations
 - Can't use DM-only simulations to model real DM+baryons Universe
 - Supernova feedback (THINGS dwarfs) Governato et al. (2012); Onorbe et al (2015)

Martizzi et al (2012)

- Environmental interaction (MW satellites) Zolotov, et al (2012)
- AGN feedback (clusters)
- Astrophysical observations not being modeled correctly
 - Intrinsic scatter in number of MW satellites (Too big to fail) Purcell & Zentner (2012)
 - MW halo mass unknown within factor of two (Too big to fail)
 - Anisotropy in stellar motions (MW satellites and clusters) Strigari et al (2014); Schaller et al (2014)
- Dark matter may not be CDM

Self-interacting dark matter

CDM structure problems are solved if dark matter is **self-interacting**

Dark matter particles in halos elastically scatter with other dark matter particles. *Spergel & Steinhardt (2000)*





No scattering Self-scattering $V^2(R) = \frac{GM_{\text{encl}}(R)}{R}$ Radius

Self-interactions solve core-vs-cusp

Particles get scattered out of dense halo centers

Self-interactions solve too-big-to-fail

Rotation curves reduced (less enclosed mass) Simulated satellites matched to observations

N-body simulations for SIDM

Vogelsberger, Zavala, Loeb (2012); see also Rocha et al, Peter et al (2012)



Self-interacting dark matter

• What is the self-scattering cross section?

Number of scatterings = $\sigma x (\rho/m) x$ velocity x t_{age}

Figure-of-merit:
$$\sigma/m_{\chi} \sim 1 \ {\rm cm}^2/{\rm g} ~\approx~ 2 \ {\rm barns/GeV}$$

Typical cross section required to solve small scale anomalies

Constraints on self-interactions

Ellipticity of galaxy cluster MS2137 (gravitational lensing)

Miralda-Escude bound (2003): $\sigma/m < 0.02 \text{ cm}^2/\text{g}$ Peter et al. (2012): bound overestimated by 10^2 (!)

Ellipticity of massive elliptical galaxy (x-rays) Buote et al. (2002); Feng et al. (2010) Weaker than previously thought due to baryonic contribution to the potential Kaplinghat et al (2014)



Bullet cluster constraint: $\sigma/m < 1 \text{ cm}^2/g$ Randall et al. (2007)

Constant cross section σ/m ~ 0.5 – 1 cm²/g may be OK with all constraints *Vogelsberger, Zavala, Loeb (2012); Rocha et al, Peter et al (2012)*



What is the cross section for dwarfs?

Elbert et al (2015)

Core size



Cluster Abell 3827

Elliptical galaxy N1 appears separated from its DM halo by $1.62^{+0.47}_{-0.49} \, \mathrm{kpc}$

Massey et al (2015)

~ 3σ outlier from expected off-set from N-body sim.

Schaller et al (2015)

Required SIDM cross section:

$$\sigma/m \sim (1.7 \pm 0.7) \times 10^{-4} \left(rac{t_{
m infall}}{10^9 \, {
m yrs}}
ight)^{-2} {
m cm}^2 / {
m g}.$$

Massey et al (2015)



Limit assumed off-set = $\Delta x \sim \Delta f_{drag} t^2$ but neglected restoring force attracting DM and baryons $\sigma/m \sim 1.5 - 3 \text{ cm}^2/g$ (depending on angular dependence of scattering)

Kahlhoefer et al (2015)

Dark matter self-interactions





 χ = dark matter particle

φ = mediator particle(dark photon, dark Higgs,dark pion, ...)

Lots of model building possibilities

WIMPs have self-interactions (weak interaction)



Cross section:

$$\sigma \sim \frac{g^4 m_{\chi}^2}{m_Z^4} \sim 10^{-36} \, {\rm cm}^2$$

Mass:

$$\chi$$
 = dark matter (e.g. SUSY particle)

Z boson = mediator particle

 $m_{\chi} \sim m_Z \sim 100 \text{ GeV}$

WIMP self-interaction cross section is way too small

$$\sigma/m_{\chi} \sim 10^{-14} \text{ cm}^2/\text{g}$$

Large cross section required $\sigma/m_{\chi} \sim 1 \text{ cm}^2/\text{g}$



Cross section:
$$\sigma ~\sim ~ {g^4 m_\chi^2 \over m_\phi^4}$$

Mediator mass below than weak scale $m_\phi \sim 1-100~{
m MeV}$

Lesson #1: self-interactions require new dark sector states (mediator) below 1 GeV.

Lesson #2: Light mediator implies velocitydependent scattering cross section



DM self-interaction cross section



Easy to compute

Compute nonrelativistic potential V(r) Solve Schrodinger equation for phase shifts Cross section obtained from partial waves

$$\chi \underbrace{-\frac{1}{4}}_{\chi} \chi + \chi \underbrace{-\frac{1}{4}}_{\chi} \chi + \chi \underbrace{-\frac{1}{4}}_{\chi} \chi + \chi \underbrace{-\frac{1}{4}}_{\chi} \chi + \dots$$

Like Sommerfeld enhancement for scattering

DM self-interaction cross section

Example: Dark matter + dark photon model $\mathscr{L}_{\mathrm{int}} = g_X X \gamma^\mu X \phi_\mu$

Potential: $V(r) = \pm \frac{\alpha_X}{r} e^{-m_{\phi}r}$

Parameters: m_{χ} , m_{ϕ} , α_{χ}

Complicated velocity dependent cross section

Want to consider $\sigma(v)$, rather than σ as a fixed number



Even simple DM + dark photon model has a complicated behavior

Different halos have different velocities

Cores in different systems are probing self-interactions at different energies



Low energies (v/c ~ 10^{-4})



Medium energies (v/c $\sim 10^{-3}$)



High energies (v/c ~ 10^{-2})

Lesson #3: Different size dark matter halos have different characteristic velocities

Different halos have different velocities

Cores in different systems are probing self-interactions at different energies



Low energies (v/c $\sim 10^{-4}$)



Medium energies (v/c ~ 10^{-3})



High energies (v/c $\sim 10^{-2}$)

Each galaxy and cluster is like a different particle physics collider with a different beam energy



Dark matter halos as colliders

Kaplinghat, ST, Yu (2015)

- Cores in dwarfs, LSBs, and clusters probing $\sigma(v)$ at different velocity
- Can observations of cores in all systems be explained in a consistent particle physics picture?
- Caveat: assuming no baryonic feedback to generate cores

Modeling SIDM without N-body simulations

Expect there is a transition radius r₁ between SIDM profile and NFW profile



Density at r₁ defines cross section where 1 scattering has occurred

Modeling SIDM without N-body simulations



Inner region: isothermal halo Hydrostatic equilibrium + ideal gas law $\nabla p = -\rho \nabla \Phi$ $p = k_B T \rho/m$ Outer region: NFW halo (CDM) Require $\rho(r)$ and $M_{encl}(r)$ are continuous at $r = r_1$.

Strategy: Scan over halo parameters and fit to astrophysical data. Only consider core-growing solution (smaller cross section)

Relaxing this assumption: work in progress: Sophia Nasr, ST

SIDM fits to dwarfs, LSBs, and clusters

Kaplinghat, Tulin, Yu (2015)

Astrophysical dataset:

6 Clusters (MS2137, A963, A611, A2537, A2667, A2390) Newman et al (2012)

8 LSB galaxies (UGC4325, F563-V2, F563-1, DDO64, F568-3, UGC5750, F583-4, F583-1) *Kuzio de Naray et al (2007)*

6 THINGS dwarf galaxies (IC2574, NGC2366, HO II, DDO53, M81dwB, DDO154) Oh et al 2011

Work in progress: expanding data set with ~100 galaxies *Pace, Kaplinghat, Tulin, Yu, Andrade*

Galactic rotation curves

(Even better fit than MOND)



Clusters

Scan over SIDM halo parameters and fit to stellar kinematics data



SIDM fits to dwarfs, LSBs, and clusters



N-body sim data for SIDM 1cm²/g (calibration)

Note: error bars don't include **systematic** errors (factor of 2)

SIDM fits to dwarfs, LSBs, and clusters



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Note: error bars don't include **systematic** errors (factor of 2)

Self-interacting DM model



DM particle X + mediator particle $\boldsymbol{\varphi}$

Example case: Asymmetric dark matter with dark photon

Nonrelativistic scattering described by repulsive Yukawa potential

$$V(r) = \frac{\alpha'}{r} e^{-\mu r}$$

Only three parameters: DM mass, ϕ mass, coupling α'

Self-interacting DM model

Dark coupling constant $\alpha' = \alpha_{em} = 1/137$



Self-interacting DM model

Dark coupling constant $\alpha' = \alpha_{em} = 1/137$



SIDM paradigm



DM particle X + mediator particle $\boldsymbol{\varphi}$

Self-interactions can provide a consistent explanation of the shapes of dark matter halos from dwarf galaxies to clusters

Are there any other implications?

SIDM and the visible sector (SM)

SIDM story is independent of how mediator couples to SM.

MeV-GeV scale mediator ϕ must decay, otherwise dominates DM density. Minimal possibility: $\phi \rightarrow$ SM particles.

Dark photon model: mediator ϕ couples via kinetic mixing with photon

$$\mathscr{L}_{\rm mix} = -\frac{\varepsilon_{\gamma}}{2} \, \phi_{\mu\nu} F^{\mu\nu}$$

Holdom (1984), Pospelov et al (2007), Arkani-Hamed et al (2009), + many others

Decay lifetime: $\tau_{\phi} \approx 3 \text{ seconds} \times \left(\frac{\varepsilon_{\gamma}}{10^{-10}}\right)^{-2} \left(\frac{m_{\phi}}{10 \text{ MeV}}\right)^{-1}$

Lifetime $\tau < 1$ sec OK. Longer lifetimes may have tension with BBN (entropy dilution, energetic decay products)

BBN sets minimal coupling between DM and SM.

SIDM paradigm



Direct detection

Minimal coupling from BBN constraint ($\epsilon_{\gamma} \sim 10^{-10}$) puts SIDM just within reach for direct detection

Kaplinghat, Tulin, Yu (2013); Del Nobile et al (2015)



Spin-independent proton-DM cross section (momentum transfer $q^2 = 0$)

$$\sigma_{Xp}^{\mathrm{SI}} \approx 1.5 \times 10^{-24} \mathrm{~cm}^2 \times \varepsilon_{\gamma}^2 \times \left(\frac{\alpha_X}{10^{-2}}\right) \left(\frac{m_{\phi}}{30 \mathrm{~MeV}}\right)^{-4}$$

Nontrivial feature of SIDM: mediator mass m_{ϕ}^2 can be comparable to q^2

m_X (GeV)	m_{ϕ} (MeV)	$q_{\rm Xe}~({\rm MeV})$	$q_{\rm Ge}~({\rm MeV})$
1000	3	127	74
100	15	62	46
10	20	10	10
5	20	5	5

Typical momentum transfer for Xenon/Germanium

Del Nobile et al (2015)

Direct detection limits on SIDM

Del Nobile et al (2015)



Nuclear recoil rate suppressed by form factor. Sensitivity plateaus for $m_{\phi} < q$.

 $\frac{m_\phi^4}{(m_\phi^2+q^2)^2}$

Distinguishing SIDM from WIMPs



Other SIDM models

• ϕ^4 -theory (contact interaction), $m_{\phi} \sim 10$ MeV e.g. dark glueballs, dark pions, SIMPs

Hochberg et al, Boddy et al

Scalar/vector mediators (Yukawa potential)
 e.g. Dark photon, dark Higgs, composite sectors

Loeb & Weiner; Buckley & Fox; Ackerman et al (+many others)

- Pseudoscalar interactions (one pion-exchange potential)
 Bellazzini et al
 e.g. dark nuclear physics, pseudo-Nambu-Goldstone bosons
- Axial vector/dipole moment interactions (more complicated potentials)
- Dark atoms (Van der Waals potential)

Cline et al, Cyr-Racine & Sigurdson

Self-interactions described by nonrelativistic potential V(r) in Schrodinger equation

Some thoughts on pseudoscalar mediators for SIDM (motivated by Felix's talk)

Work in progress



Schrodinger equation analysis is rather complicated

$$V(\mathbf{r}) = \frac{\alpha_X}{m_X^2} e^{-m_{\phi}r} \left[(\mathbf{S}_1 \cdot \hat{\mathbf{r}}) (\mathbf{S}_2 \cdot \hat{\mathbf{r}}) \left(\frac{3}{r^3} + \frac{3m_{\phi}}{r^2} + \frac{m_{\phi}^2}{r} \right) - (\mathbf{S}_1 \cdot \mathbf{S}_2) \left(\frac{1}{r^3} + \frac{m_{\phi}}{r^2} + \frac{4\pi}{3} \delta^3(\mathbf{r}) \right) \right]$$

Tensor operator couples orbital angular momenta ℓ, ℓ±2

$$S_{12}(\mathbf{r}) \equiv 3(\boldsymbol{\sigma}_1 \cdot \hat{\mathbf{r}})(\boldsymbol{\sigma}_2 \cdot \hat{\mathbf{r}}) - (\boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2)$$

Singular potential ~ 1/r³ must be regulated and renormalized (Cross section depends on input for counter terms, predictability?)

But the perturbative calculation (Born approx) gives a very simple result:

$$\frac{d\sigma}{d\Omega} = \frac{\alpha_X^2 m_X^2 v^4 \sin^4 \frac{\theta}{2}}{16(m_\phi^2 + m_X^2 v^2 \sin^2 \frac{\theta}{2})^2} = \frac{1}{4} \left(\frac{d\sigma}{d\Omega}\right)_s + \frac{3}{4} \left(\frac{d\sigma}{d\Omega}\right)_t$$

Cross section highly suppressed on dwarf scales $\sigma/m \sim (v/c)^4 \sim 10^{-16}$ for v ~ 30 km/s

When is the Born approximation valid? Consider only spin singlet scattering.

$$\begin{array}{ll} \text{Spin-singlet potential} & V_s(r) = -\frac{\alpha_X m_{\phi}^2}{4m_X^2} \frac{e^{-m_{\phi}r}}{r} + \frac{\pi \alpha_X}{m_X^2} \delta^3(\mathbf{r}) \\ \\ \text{Born approx. valid for} & \frac{\alpha_X m_{\phi}}{m_X} \ll 1 & \text{Generally satisfied for } \mathbf{m}_{\phi} << \mathbf{m}_{\chi} \\ \\ \text{Different than condition for vector/scalar interactions} & \frac{\alpha_X m_X}{m_{\phi}} \ll 1 \end{array}$$

Does the pseudoscalar theory preclude large self-interactions (in dwarfs)?

Claim: No – self-interactions can be sizable, even in the Born limit

Does the pseudoscalar theory preclude large self-interactions (in dwarfs)?

Claim: No – self-interactions can be sizable, even in the Born limit

Pseudoscalar potential

Leading-order q²-suppressed

 $\chi \xrightarrow{\chi} \chi$

Second-order q²-unsuppressed (virtual momentum) Yukawa potential

Two pion exchange looks like scalar exchange (σ meson from QCD) *Oshima et al*

$$V(r) = -\frac{\alpha_{\sigma}}{r}e^{-m_{\sigma}r} \qquad \alpha_{\sigma} \sim 0$$

Low velocity limit: $\sigma/m \sim barn/GeV$ for $m_\sigma \sim$ 10 MeV, $\alpha_x \sim$ 0.1, $m_x \sim$ 10 GeV

 $\frac{\alpha_X^2}{4\pi}$

Conclusions

- We know DM interacts gravitationally and we can test whether gravity is the *only* force influencing DM structure
- Long-standing issues for CDM and structure. Jury still out, but SIDM can provide a consistent solution if there are new light states coupled to DM.
- SIDM paradigm has rich model space and phenomenology

Back up

Cores in field dwarfs

CDM-only simulations poor representation of DM+baryon Universe



Supernova feedback may form cores in THINGS dwarfs (gas-rich dwarfs)

Depends on implementation sub-grid baryonic physics

Requires bursty star formation history

In Governato et al sim, cores formed around $z \sim 2 - 4$.

Cores in field dwarfs

CDM-only simulations poor representation of DM+baryon Universe



Another simulation with supernova feedback

Feedback confirmed, but requires *late-time* star formation epoch (z < 2)

Onorbe et al (2015)

Cores in MW satellites

CDM-only simulations poor representation of DM+baryon Universe

- Supernova feedback mechanism insufficient (not enough baryons) Garrison-Kimmel, et al (2013)
- Supernova feedback may work in biggest satellites with the right star formation history

Onorbe, et al (2015)

• Environmental effect from MW baryonic disk can form DM cores Zolotov, et al (2012)

Cores in MW satellites

Systematic uncertainty in astrophysical interpretation



No cores in MW satellites?

Conclusions depend on assumptions for stellar kinematic distribution

(Only observe line-of-sight velocity and projected position)

Cores in LSBs

- Still an open challenge for baryonic physics
 - Metal-poor (not much star formation)
 - Not recently bursty
 - More massive than THINGS dwarfs (harder to blow out baryons)

CDM-only simulations poor representation of DM+baryon Universe

- AGN feedback may generate cores *Martizzi et al (2012)*
- AGN feedback may be insufficient *Schaller et al (2014)*

Systematic uncertainty in astrophysical interpretation

- Existence of core inferred from stellar kinematics
- Depends on assumptions for the stellar kinematic distribution



Too-big-to-fail problem

Is there a problem beyond the Milky Way?



Too-big-to-fail problem

Caveats:

Variation in number of satellites (~10% "tuning") Purcell & Zentner (2012)

MW mass might be smaller (but combined mass of MW+M31 is relatively well constrained) Tollerud et al. (2014)

Baryons are important

- Environmental effect from parent galaxy generates cores and modifies rotation curves
- Explains TBTF in MW and Andromeda, but not Local Group field dwarfs