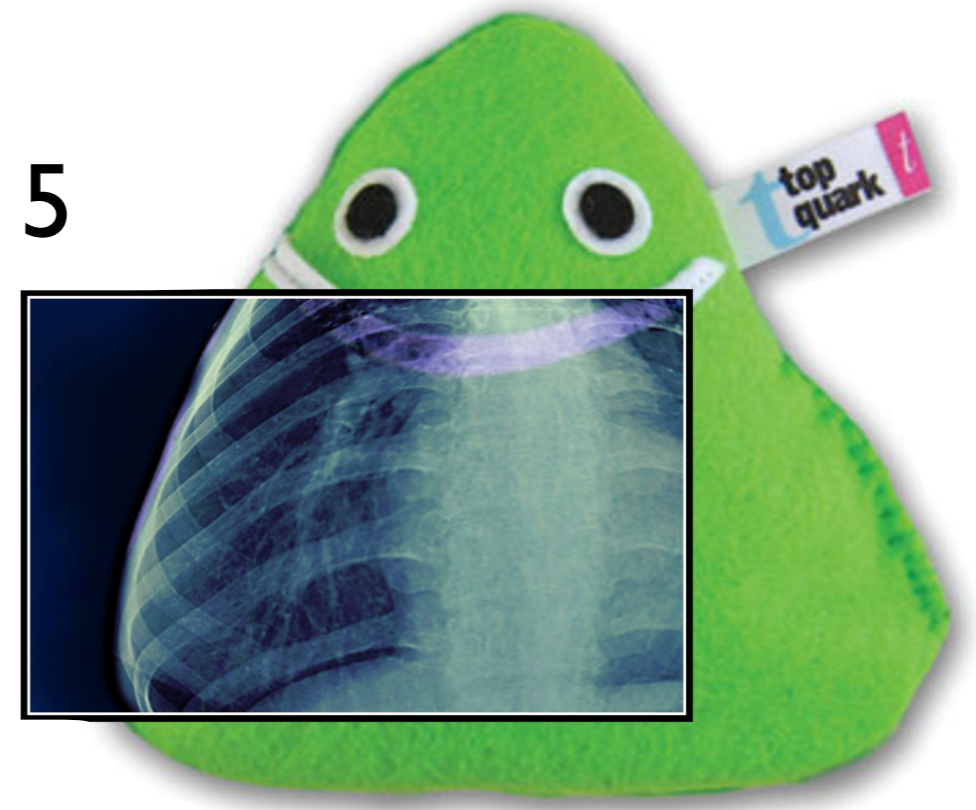


# Top physics at future hadron colliders

Lepton and Future Colliders 2015  
Trento

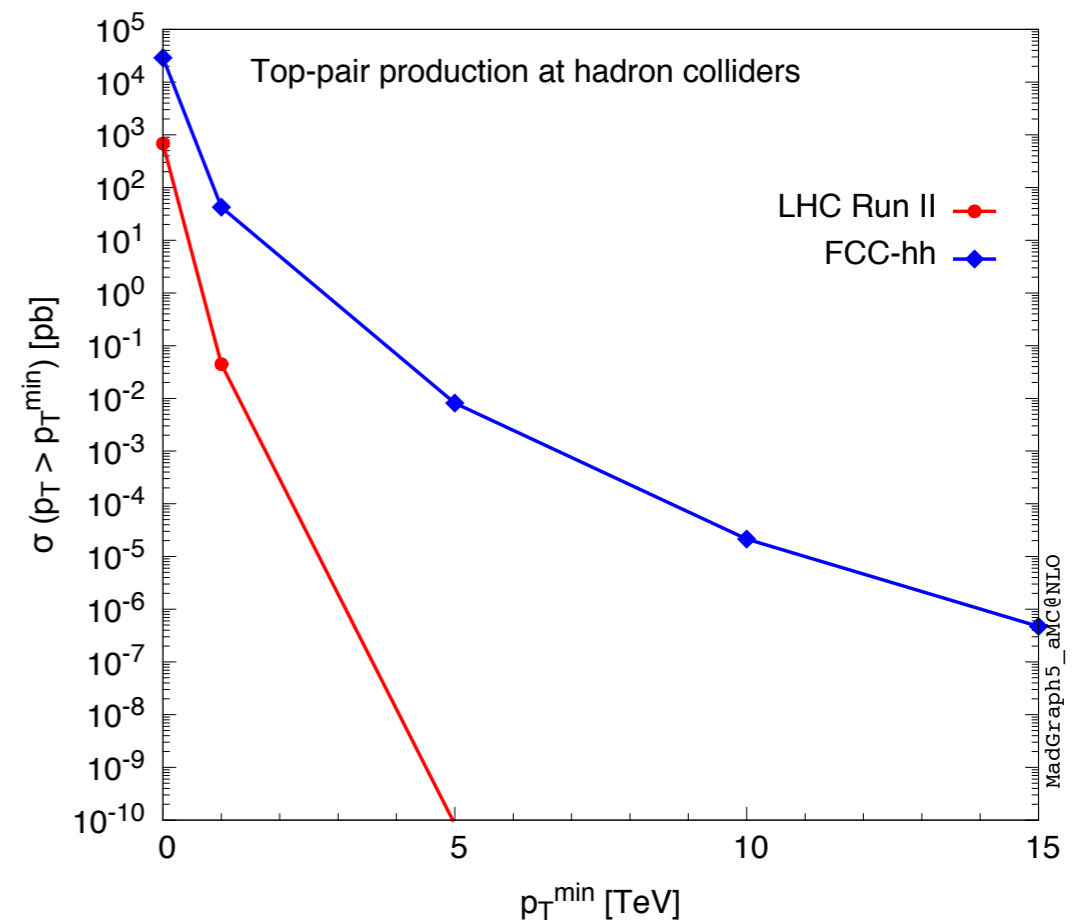
Marco Zaro  
*LPTHE - Université Pierre et Marie Curie  
Paris - France*



# Top & FCC-hh facts

- A huge amount of top-quark pairs will be produced at a 100 TeV hadron collider:  $\sigma_{\text{NLO}} \sim 30 \text{ nb}$  ( $\sim 40 \times$  LHC run II)
- $3 \cdot 10^{10}$  top pair produced with  $10 \text{ ab}^{-1}$
- Many tops will be boosted
- Can we detect all them?
- What can we do with them?
- Is it just  $t\bar{t}$ ?

$c\bar{s}$	electron+jets	muon+jets	tau+jets	all-hadronic	
$u\bar{d}$					
$\tau^+\tau^-$	$e\tau$	$\mu\tau$	$\tau\tau$	tau+jets	
$\mu^+\mu^-$	$e\mu$	$\mu\mu$	$\tau\mu$	muon+jets	
$e^+e^-$	$e\tau$	$e\mu$	$e\tau$	electron+jets	
$W$ decay	$e^+$	$\mu^+$	$\tau^+$	$u\bar{d}$	$c\bar{s}$



# Tagging top quarks at a FCC-hh

Larkoski, Maltoni, Selvaggi, arXiv:1503.03347

- **Challenges:**

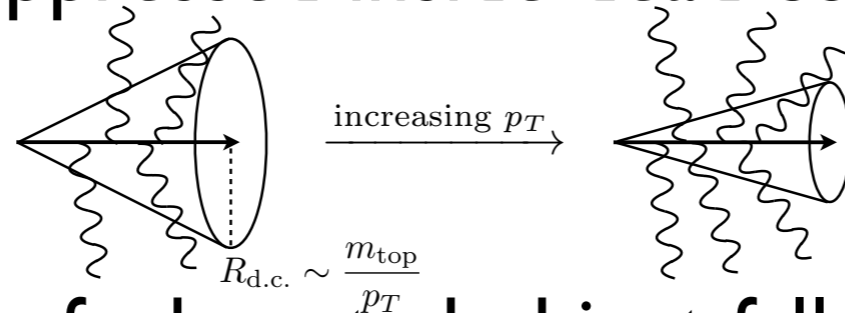
- Boosted objects radiate a lot, both ISR and FSR (before the decay). Jet-mass measurement affected:

$$m^2 \sim m_t^2 + p_T p_T^{\text{ISR}} R^2$$

In the very boosted regime ( $p_T \sim 10 \text{ TeV}$ ),  $p_T^{\text{ISR}} \sim 5 \text{ GeV}$  can give large distortions for  $R \sim 1$

Grooming methods never studied in such an extreme regime

FSR radiation suppressed inside dead cone:  $R_{\text{d.c.}} \sim m_t/p_T$



- Decay products of a boosted object fall inside a very narrow cone:  $R \sim 2m_t/p_T$ .

$R \sim 0.05$  for  $p_T = 7.5 \text{ TeV}$ , comparable with the resolution of ATLAS/CMS E-M calorimeters.

# A variable-R jet algorithm

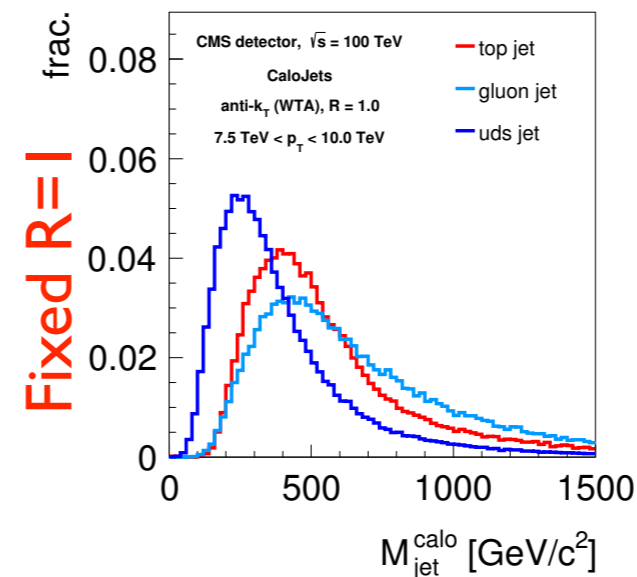
- Jet-mass degradation due to ISR can be reduced using a jet radius  $R(p_T) = C m_t / p_T$ 
  - First cluster jets using anti- $k_T$  with fixed R
  - Recluster the constituents of each jet with  $R(p_T)$
  - Keep the hardest subjet as the top jet
  - Mass jet contamination now reduced to  $m^2 = m_t^2 (1 + C^2 p_T^{\text{ISR}}/p_T)$
  - Dead-cone effect also reduces contamination from FSR



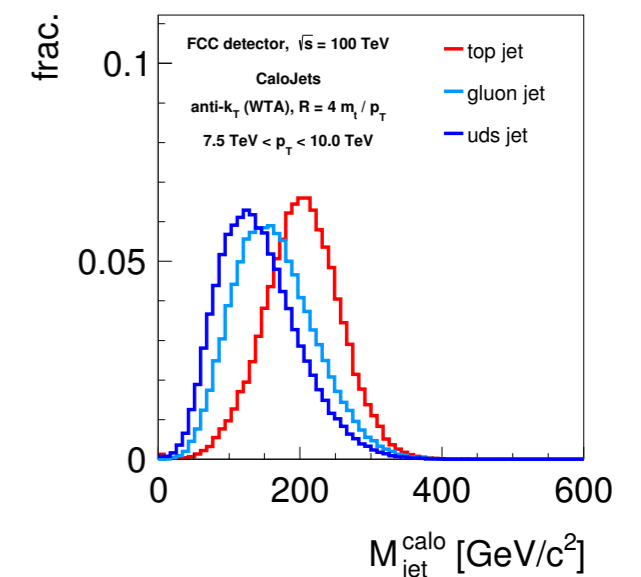
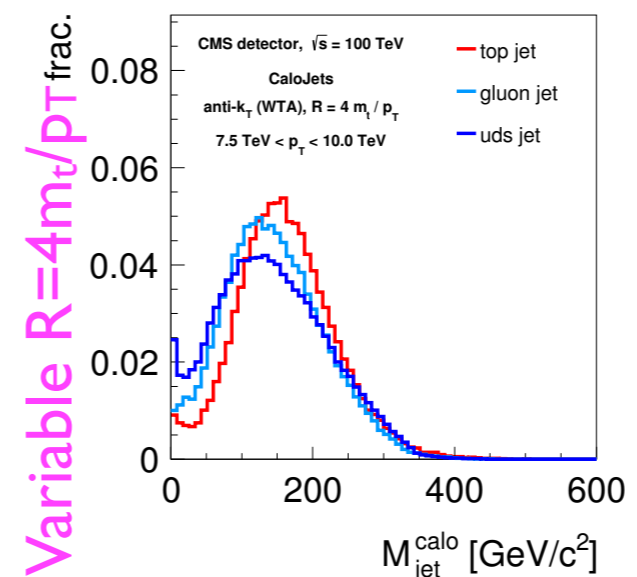
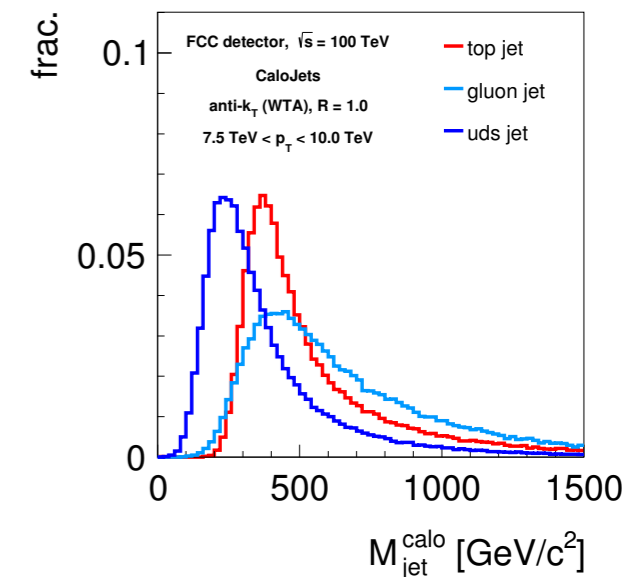
# A variable-R jet algorithm: effects on jet-mass distribution

- Fixed-radius jets show poor mass discrimination between **signal** and **background**
- Using a  $p_T$ -dependent radius improves the picture, but effects due to calorimeter granularity appear
- Calo-only based analysis insufficient  
Cutting on the mass will degrade tagging efficiency

CMS-like detector

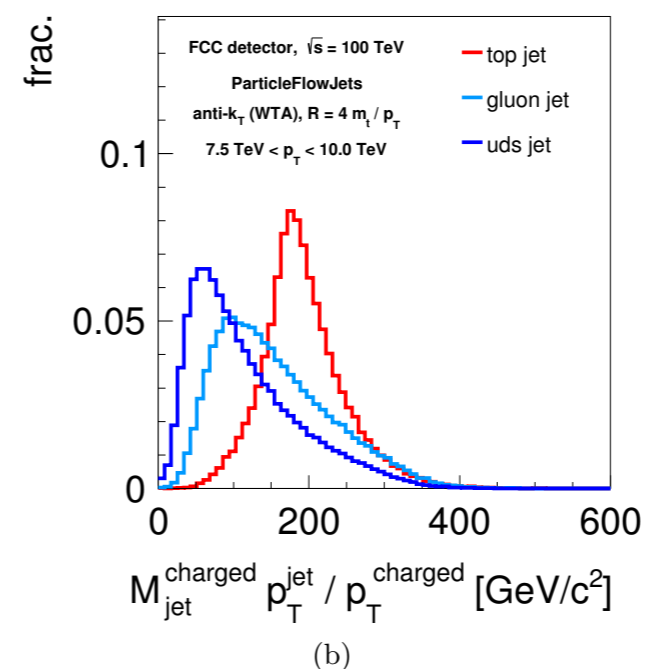
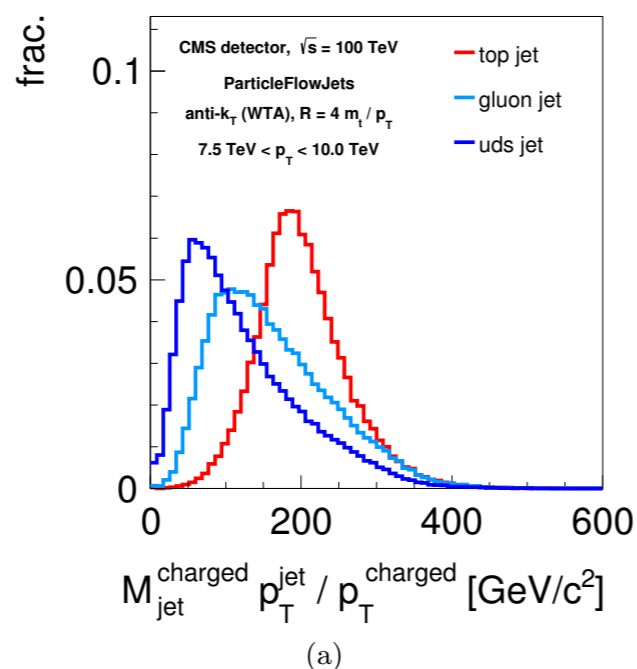


FCC detector



# Improving the mass resolution with tracks

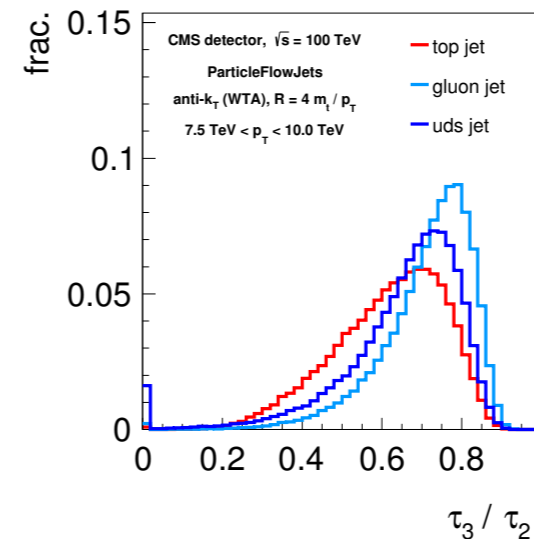
- Track-based information can help to achieve a better mass resolution
- Use charged tracks and reconstruct full jet mass as  $m = m^{\text{ch}} p_T / p_T^{\text{ch}}$
- Mass discrimination much improved, even for detectors with poor calo granularity
- Further improvements based on jet substructure



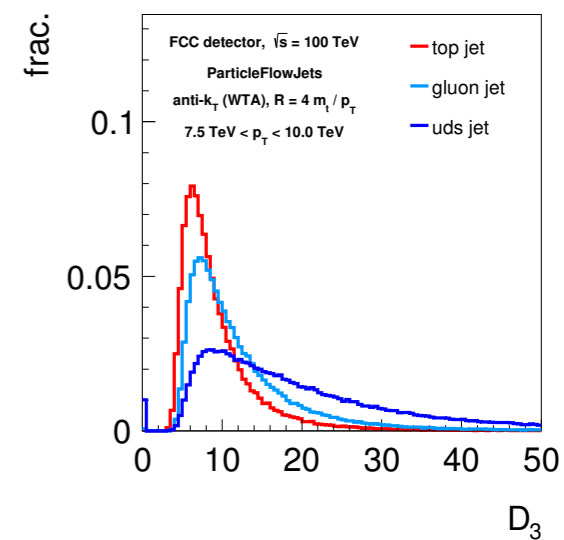
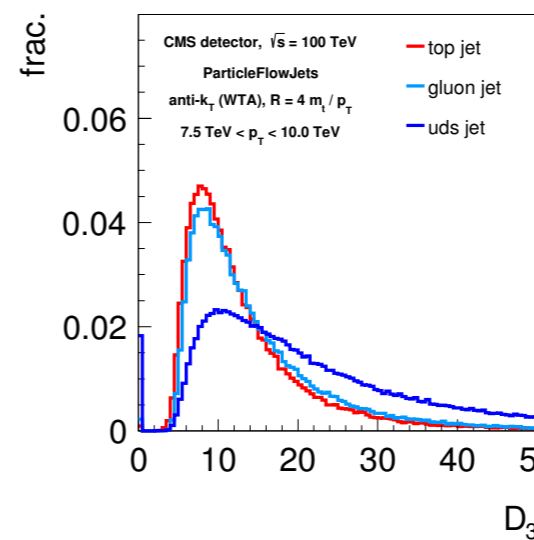
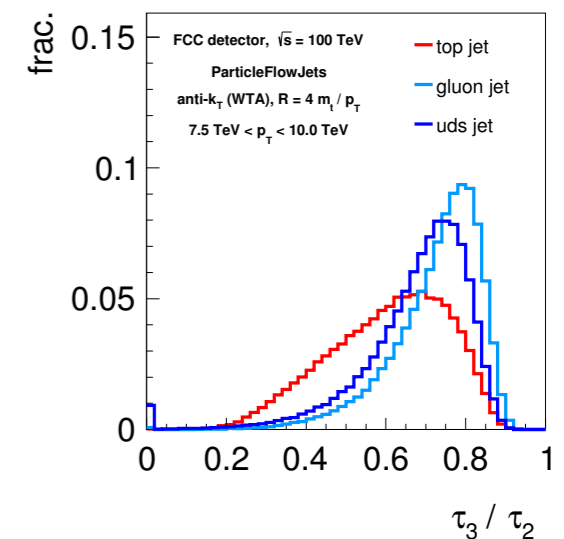
# Exploiting substructure information

- Select 3-prongs-like jets using N-subjettiness ratio  $\tau_{3,2}$  and ECF  $D_3$
- N-subjettiness sensitive to top/gluon discrimination, ECF to top/uds
- @50% top efficiency:
  - mass cut +  $\tau_{3,2} \rightarrow 83\%$  gluon rejection
  - mass cut +  $D_3 \rightarrow 94\%$  uds rejection

CMS-like detector



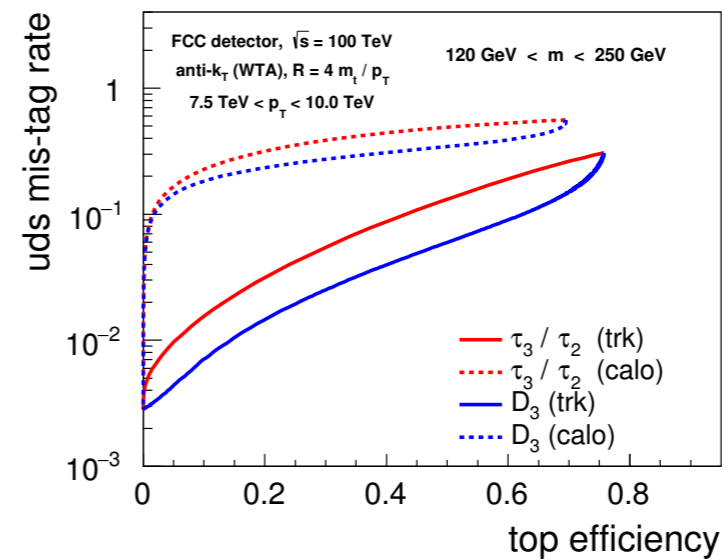
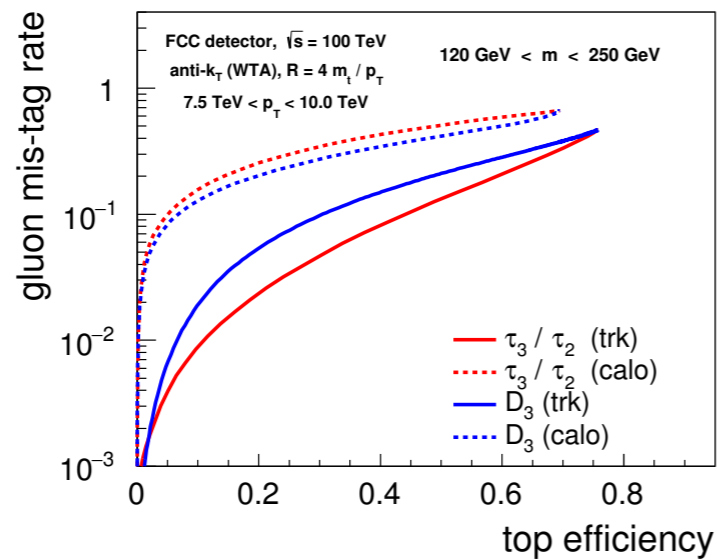
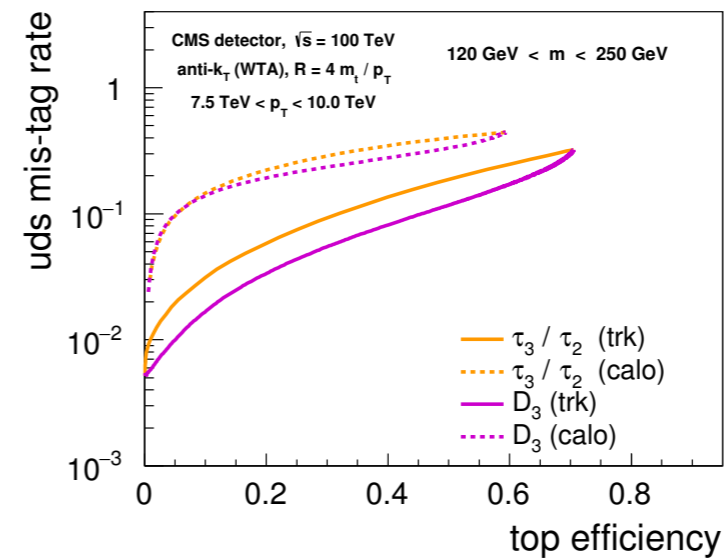
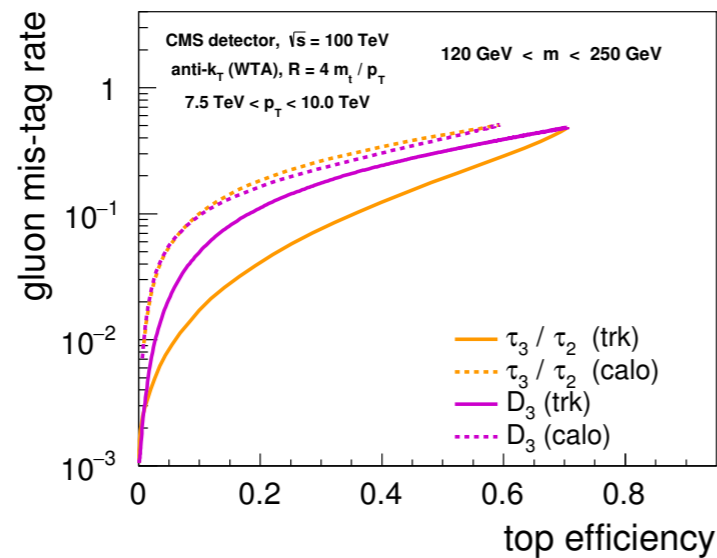
FCC detector



$120 < m < 250$



# Performance: top efficiency vs mistag rate



# Exploring top properties #1:

## The chromo-electric/magnetic moment

Aguilar-Saavedra, Fuks, Mangano, arXiv:1412.6654

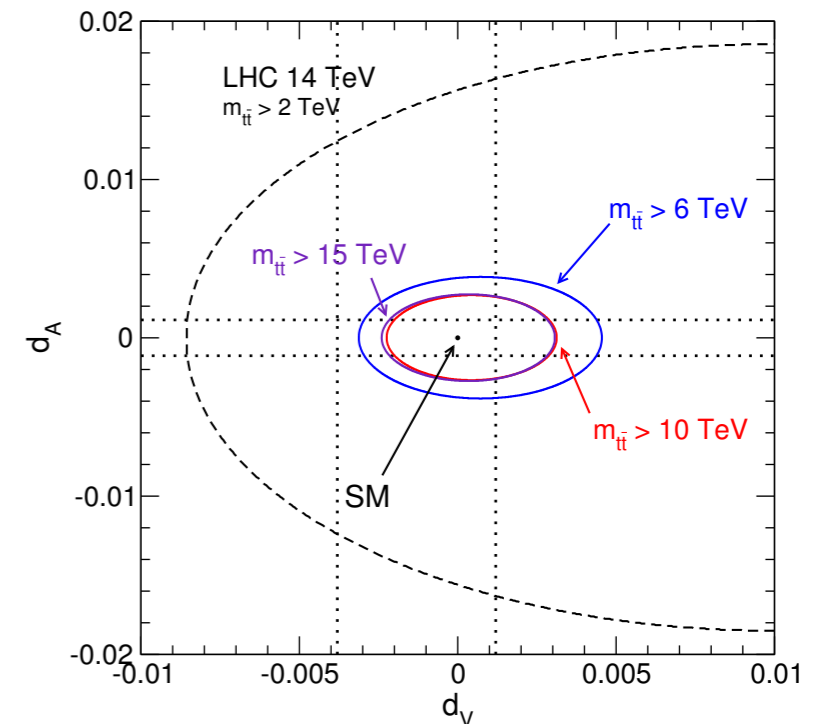
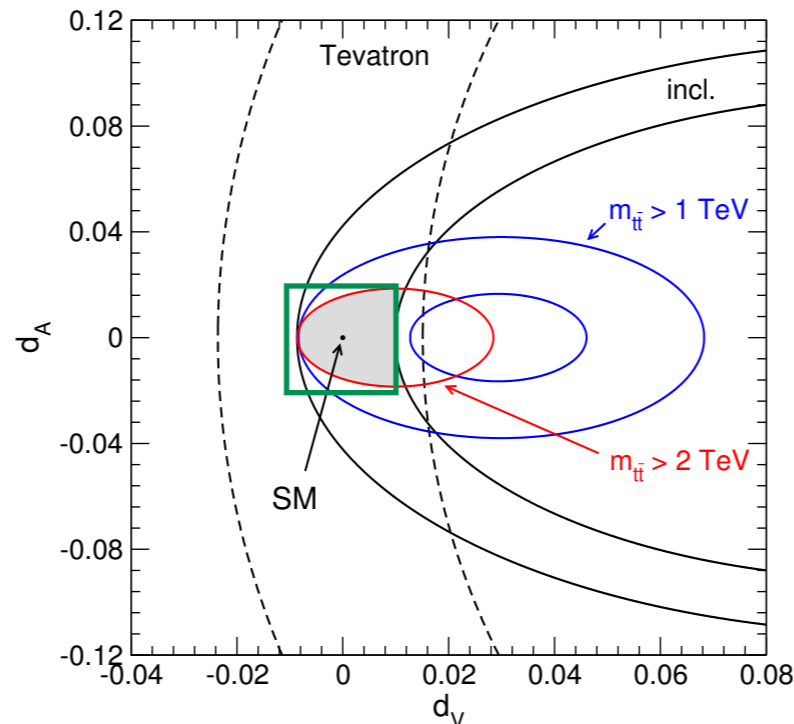
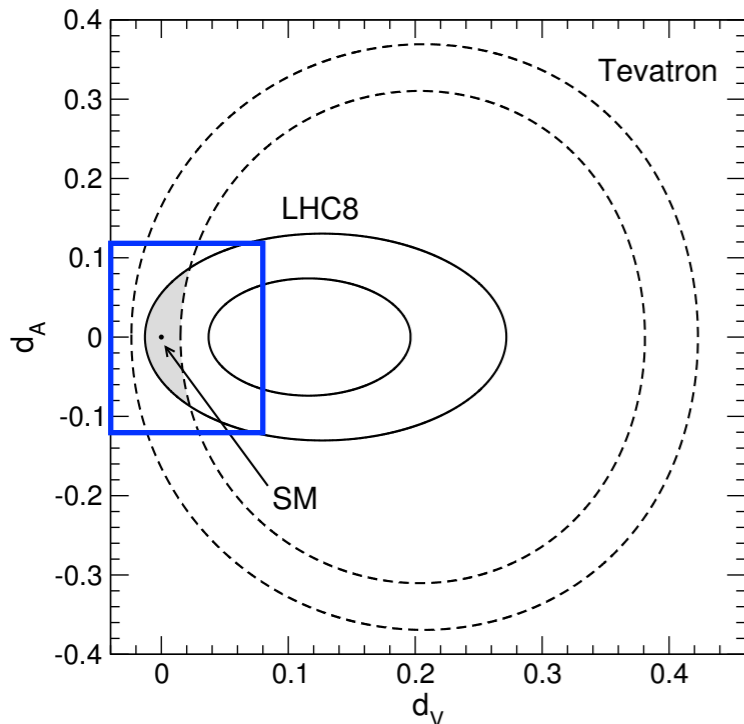
- Top dipole moments are generated via loops in the SM, and are very small

$$\mathcal{L}_{tg} = -g_s \bar{t} \gamma^\mu \frac{\lambda_a}{2} t G_\mu^a + \frac{g_s}{m_t} \bar{t} \sigma^{\mu\nu} \left( \overset{\text{chromo-magnetic}}{d_V} + \overset{\text{chromo-electric}}{i d_A \gamma_5} \right) \frac{\lambda_a}{2} t G_{\mu\nu}^a$$

- Most stringent bounds from low- $Q^2$  ( $|d_{V,A}| \lesssim 10^{-3}$ )
- In the SM  $d_V^{\text{loop}} = 0.007$ ,  $d_A$  negligible
- Weakly interacting NP at the TeV scale  $\rightarrow d_{V,A} \sim 0.05$
- The cross-section depends on  $d_{V,A}$  as a polynomial  $\rightarrow$  cross-section measurements can be used to constrain the moments

$$\begin{aligned} \sigma_{t\bar{t}}^{(8)}(\text{nb}) &= \sigma_{\text{SM}}^{(8)}(\text{nb}) - 1.53 d_V + 10.1 d_V^2 - 23.0 d_V^3 \\ &\quad + 28.6 d_V^4 + 7.0 d_A^2 + 28.6 d_A^4 - 23.1 d_V d_A^2 + 57.3 d_V^2 d_A^2 \end{aligned}$$

# Present and future constraints on dipole moments



## Tevatron and LHC Run I

- Use most recent experimental measurements +  $\sigma_{SM}$  @NNLO
- Stronger bounds than those from spin-correlations

Bernreuther, Si, arXiv:1305.2066  
CMS-PAS-TOP-14-005

## LHC Run II (100fb<sup>-1</sup>)

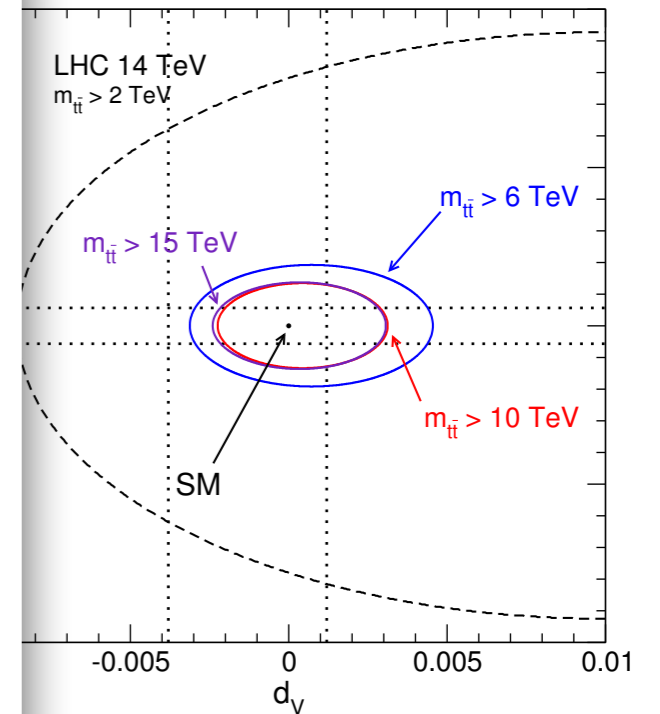
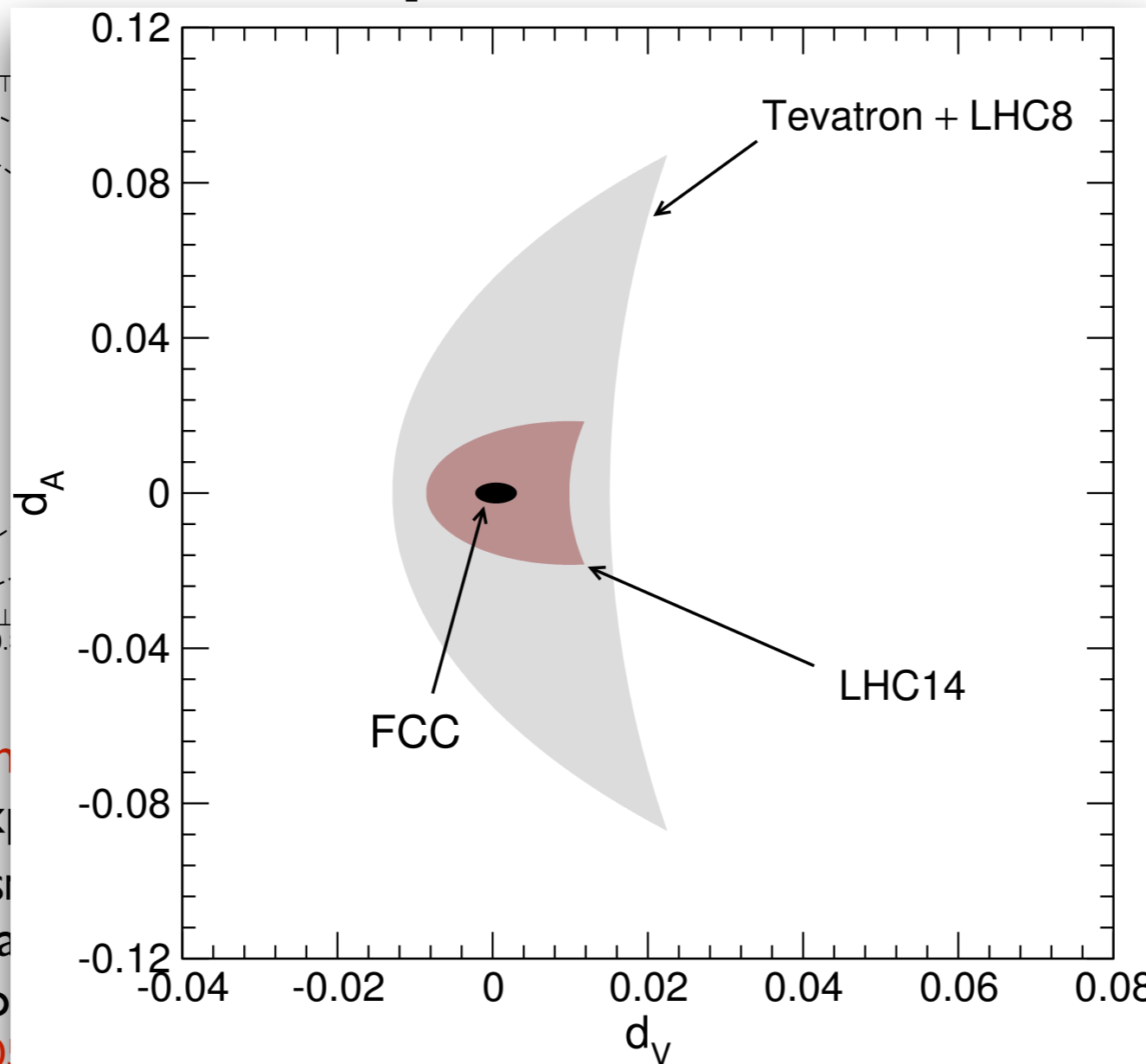
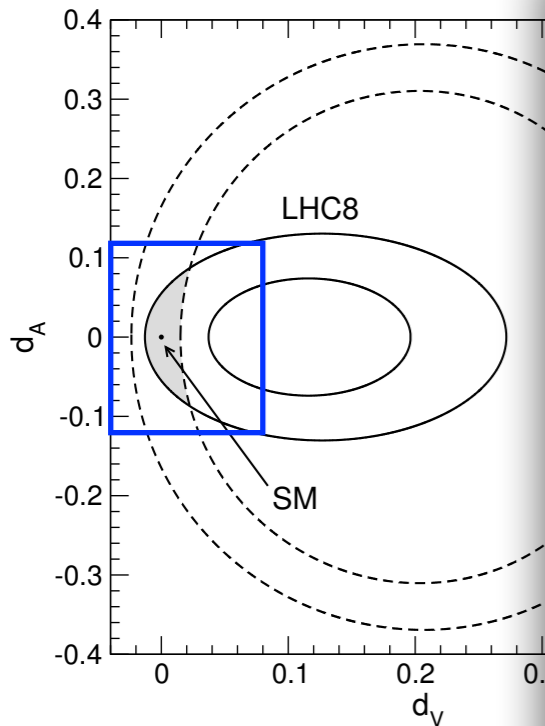
- Use information both on total xsect and on xsect at large invariant mass
- Use CMSTopTagger (WVP3) for boosted tops

## FCC (10ab<sup>-1</sup>)

- Ask one muonic top + cut on muon energy to reject QCD background
- Very high invariant mass region (>15TeV) limited by statistics
- Compatible with current indirect limits



# Present and future constraints on dipole moments



## Tevatron and LHC Run 1

- Use most recent experimental measurements +  $\sigma_{SI}$
  - Stronger bounds than from spin-correlation
- Bernreuther, Si, arXiv:1301.0001  
CMS-PAS-TOP-14-005

## 10ab<sup>-1</sup>)

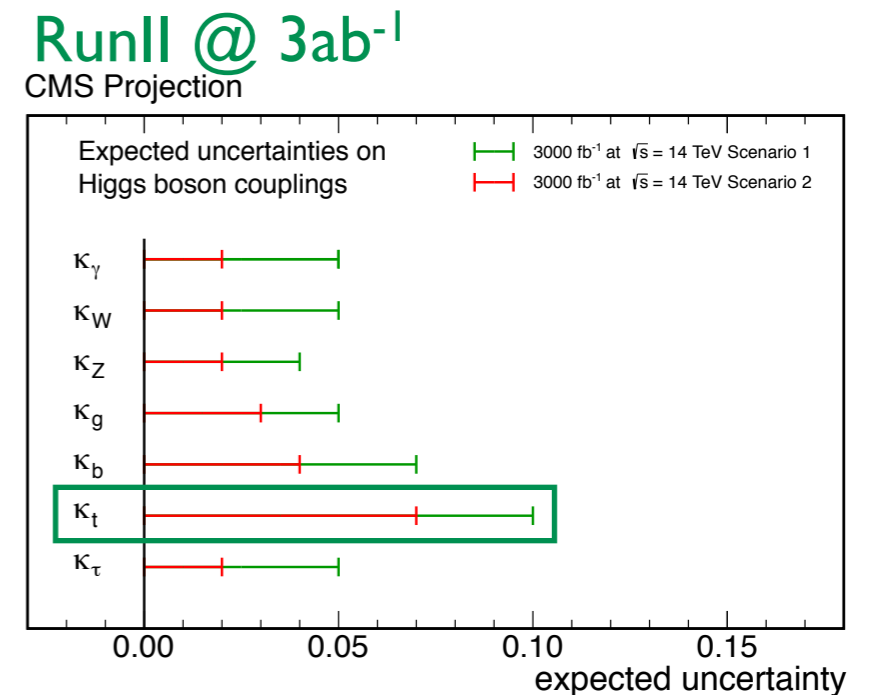
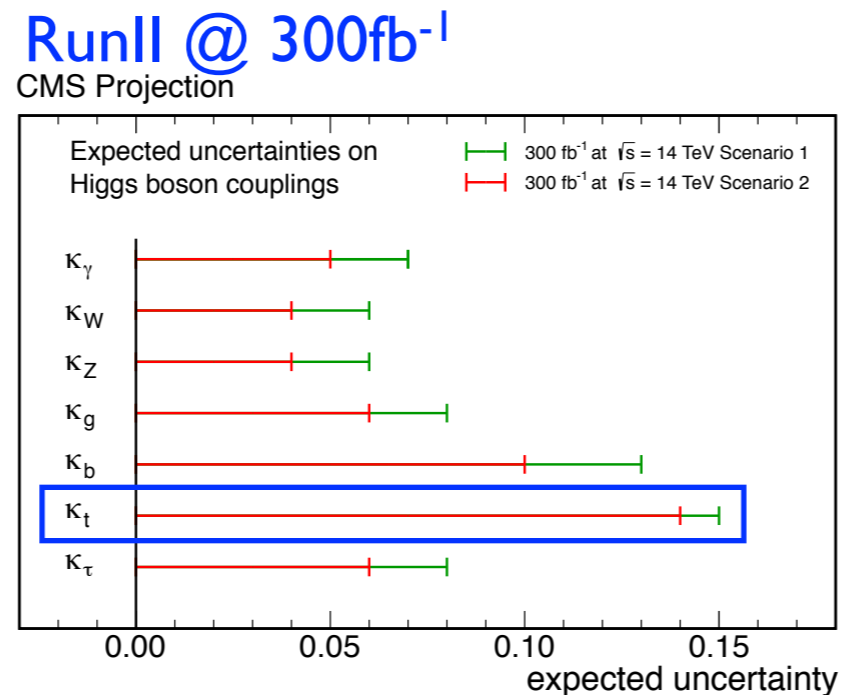
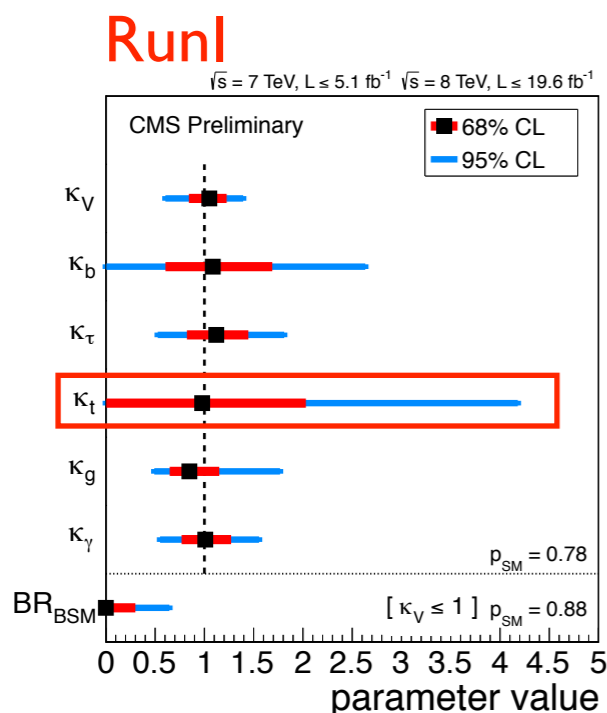
one muonic top + cut on invariant mass  
on energy to reject QCD background

high invariant mass region  
(5TeV) limited by statistics

- Compatible with current indirect limits

# Exploring top properties #2: The top Yukawa coupling

- The determination of the top Yukawa is of utmost importance for present and future colliders
- $t\bar{t}H$  is the only channel where  $y_t$  can be **directly** measured
  - Not discovered at the RunI, looking forward for RunII
- Prospects from RunII:  $y_t$  known at 7-10% level, with  $3ab^{-1}$
- Can we go down to 1% with the FCC?



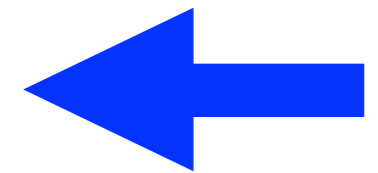
# Ratios can help...

Mangano, Plehn, Reimitz, Schell, Shao, arXiv:1507.08169

- $t\bar{t}H$  and  $t\bar{t}Z$  are quite similar processes, with rather large theoretical uncertainties ( $\sim 10\%$ ).
- Dominant production mode (gg) has identical diagrams

## Correlated QCD corrections, scale and $\alpha_s$ systematics

NLO QCD	$\sigma(t\bar{t}H)$ [pb]	$\sigma(t\bar{t}Z)$ [pb]	$\sigma(t\bar{t}H)/\sigma(t\bar{t}Z)$
13 TeV	0.475 <span style="border: 1px solid red; padding: 2px;">+5.79%+3.33% -9.04%-3.08%</span>	0.785 <span style="border: 1px solid red; padding: 2px;">+9.81%+3.27% -11.2%-3.12%</span>	0.606 <span style="border: 1px solid blue; padding: 2px;">+2.45%+0.525% -3.66%-0.319%</span>
100 TeV	33.9 <span style="border: 1px solid red; padding: 2px;">+7.06%+2.17% -8.29%-2.18%</span>	57.9 <span style="border: 1px solid red; padding: 2px;">+8.93%+2.24% -9.46%-2.43%</span>	0.585 <span style="border: 1px solid blue; padding: 2px;">+1.29%+0.314% -2.02%-0.147%</span>



- Almost identical kinematics boundaries ( $m_Z \sim m_H$ )

## Correlated PDF and $m_t$ systematics

100TeV	$\frac{\sigma(t\bar{t}H)}{\sigma(t\bar{t}Z)}$		$\frac{\sigma(t\bar{t}H)}{\sigma(t\bar{t}Z)}$
MSTW2008	0.585 <span style="border: 1px solid red; padding: 2px;">+1.29%+0.0526% -2.02%-0.0758%</span>	default	0.585 <span style="border: 1px solid blue; padding: 2px;">+1.29% -2.02%</span>
CT10	0.584 <span style="border: 1px solid red; padding: 2px;">+1.27%+0.189% -1.99%-0.260%</span>	$\mu_0 = m_t + m_{H,Z}/2$	0.580 <span style="border: 1px solid blue; padding: 2px;">+1.16% -1.80%</span>
NNPDF2.3	0.584 <span style="border: 1px solid red; padding: 2px;">+1.29%+0.0493% -2.01%-0.0493%</span>	$m_t = y_t v = 174.1$ GeV	0.592 <span style="border: 1px solid blue; padding: 2px;">+1.27% -2.00%</span>
		$m_t = y_t v = 172.5$ GeV	0.576 <span style="border: 1px solid blue; padding: 2px;">+1.27% -1.99%</span>
		$m_H = 126.0$ GeV	0.575 <span style="border: 1px solid blue; padding: 2px;">+1.25% -1.95%</span>

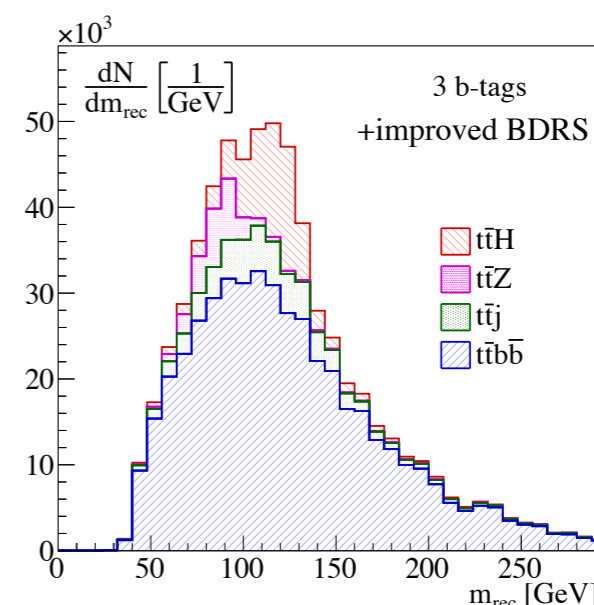
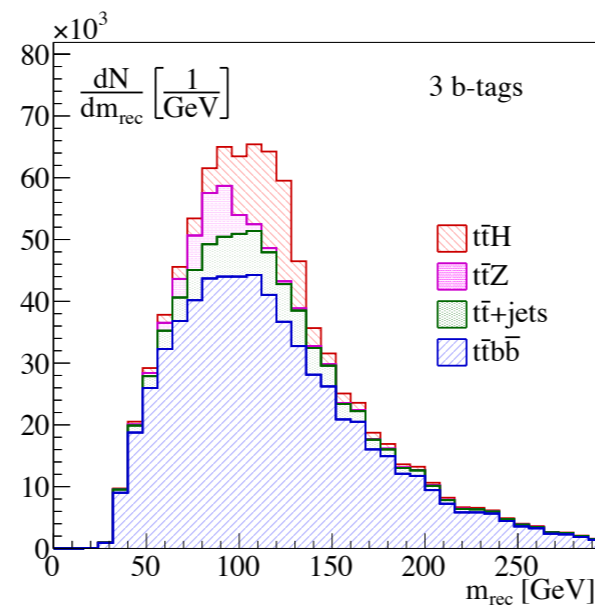
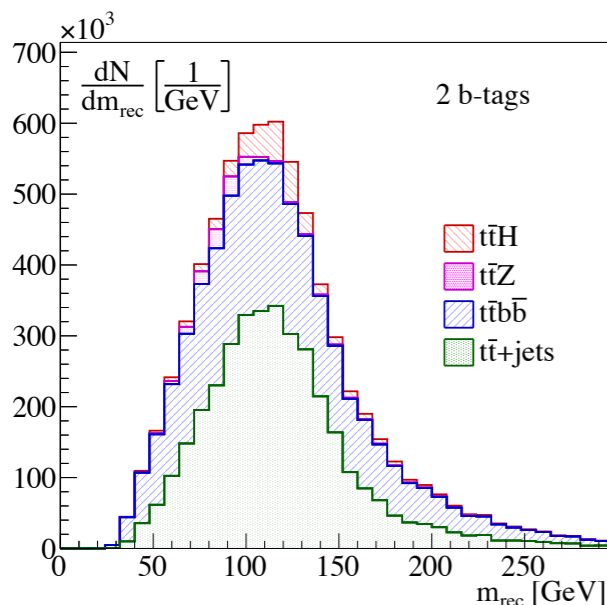


# Is a 1% measurement of $y_t$ possible at the FCC?

- Exploit  $t\bar{t}Z$  measurements and uncertainties correlation in the ratio  $t\bar{t}H/t\bar{t}Z$
- Exploit harder spectra at 100TeV than at 13TeV (boosted regime) to enhance S/B
- Use improved HepTopTagger2/BDRS Higgs tagger
  - Add information from N-subjettiness
  - Use OptimalR mode, to reduce the jet size until some decay subjects are dropped

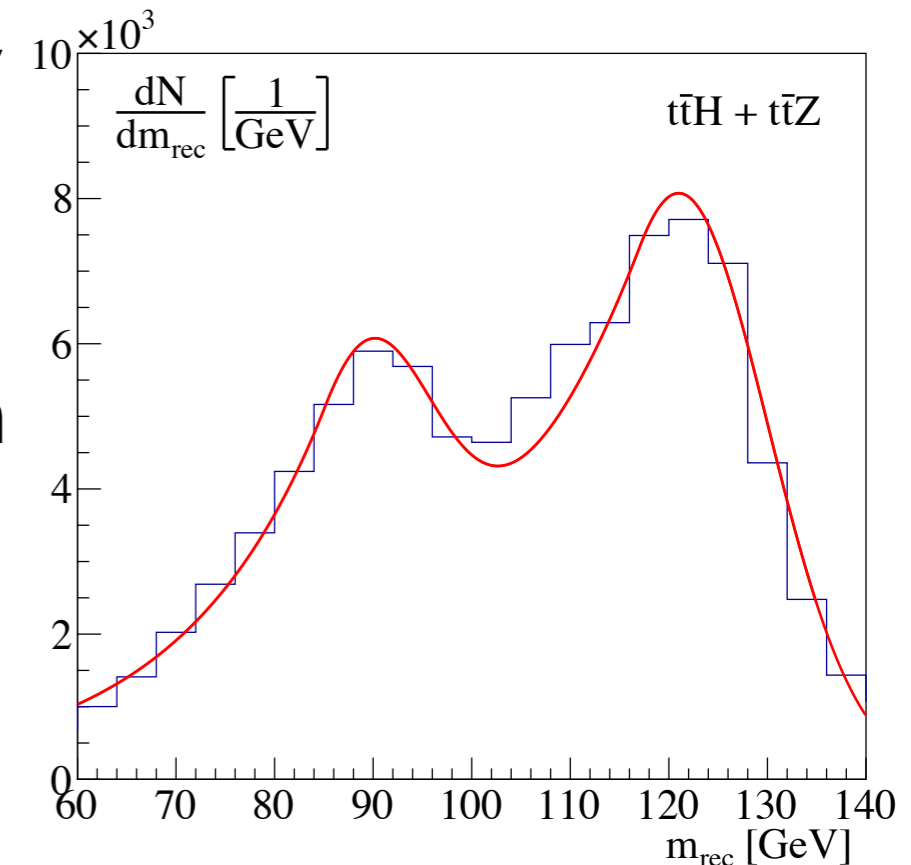
# Signal and background processes and selection

- Leading backgrounds to be simulated are  $t\bar{t}b\bar{b}$ ,  $t\bar{t}Z$ ,  $t\bar{t}+\text{jets}$
- Simulated semileptonic top decay, Higgs and Z decay to  $b\bar{b}$
- Require:
  - One isolated lepton,  $|y_l| < 2.5$ ,  $p_T(l) > 15 \text{ GeV}$
  - Two fat jets (C/A,  $R=1.8$ ,  $p_T > 200 \text{ GeV}$ )
    - One HepTopTagged jet
    - One BDRS Higgs Tagged jet, with 2 b-tags inside
    - An extra b-tag in the “rest” of the event (to suppress  $t\bar{t}+\text{jets}$ )



# Signal extraction

- Subtract the background by interpolating the two sidebands regions  $m_{bb} \in [0, 60]$  GeV U  $[160, 300]$  GeV
- In the signal region ( $m_{bb} \in [104, 136]$  GeV) one expects 44700 signal events, with S/B  $\sim 0.33$  (at  $20\text{ab}^{-1}$ )
- Assuming perfect background subtraction the stat. error on signal is  $N_s = 0.013N_s$
- $N_H/N_Z = 2.80 \pm 0.03$ , with systematic and theoretical uncertainties cancelling in the ratio





# Exploring top properties #3:

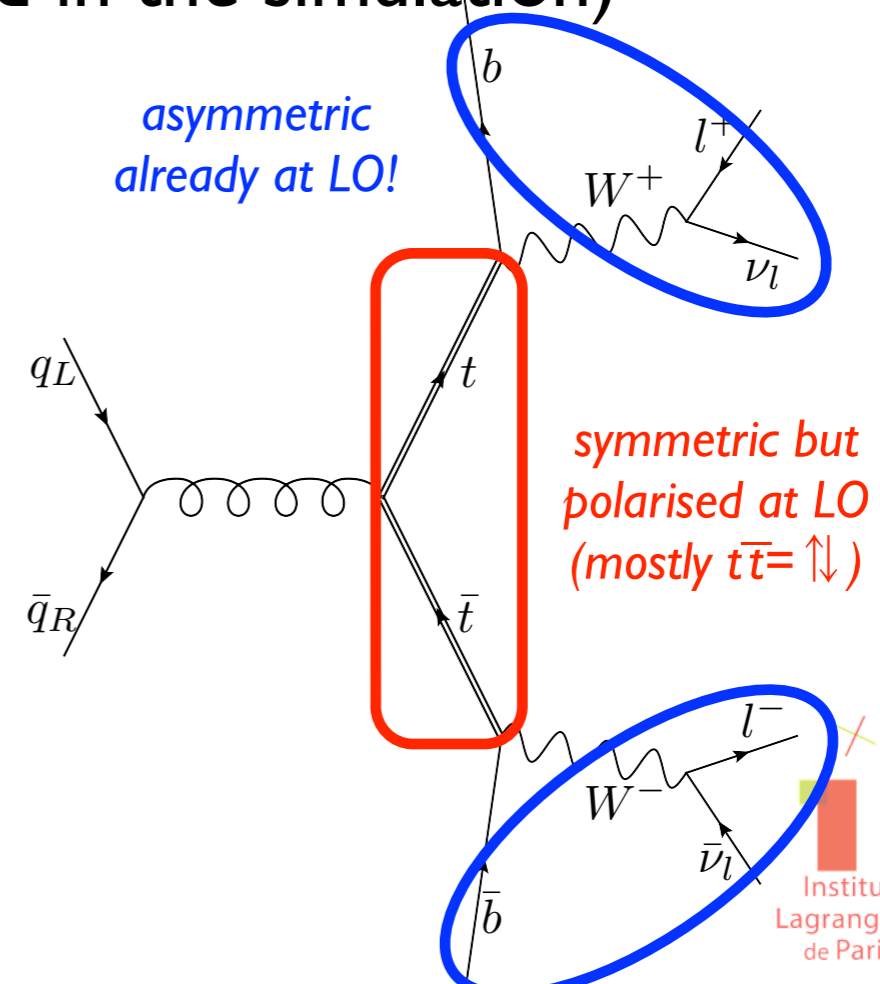
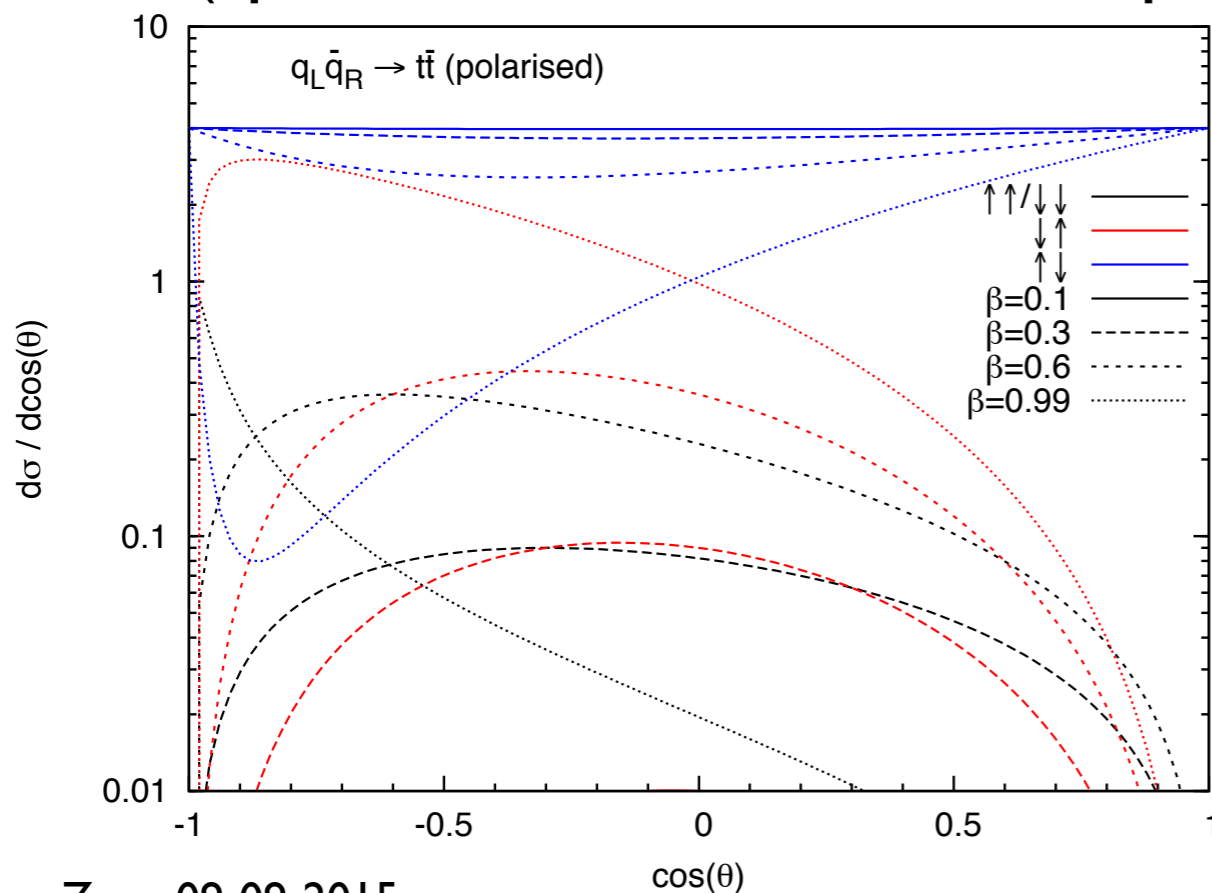
## Top asymmetry and polarisation in $t\bar{t}W$

Maltoni, Mangano, Tsirikos, MZ, arXiv:1406.3262

- Top asymmetry and polarisation can provide useful (indirect) informations on the nature of new physics
- A measurement of the top asymmetry does not seem feasible at the FCC, because  $t\bar{t}$  is essentially produced via  $gg$  only
- $t\bar{t}W$  production can be an alternative
  - $q\bar{q}$  induced at LO, has a rather large asymmetry at NLO
    - $A_t^{t\bar{t}}=0.45$ ,  $A_t^{t\bar{t}W}=2.24$  @LHC RunII
    - $A_t^{t\bar{t}}=0.12$ ,  $A_t^{t\bar{t}W}=1.85$  @FCC
  - Top quarks are highly polarised

# Polarised top production

- The radiation of a  $W$  boson from the initial line has the effect of polarising the light quarks *for details see Parke, Shadmi, hep-ph:9606419*
  - $t\bar{t}W$  is totally analogous to polarised  $q\bar{q} \rightarrow t\bar{t}$  scattering
  - $t\bar{t}$  pair is highly polarised ( $\uparrow\downarrow$  dominates at threshold)
  - The top decay products are asymmetric already at LO (spin-correlations have to be preserved in the simulation)



# Decay product asymmetries and prospects for LHC and FCC measurements

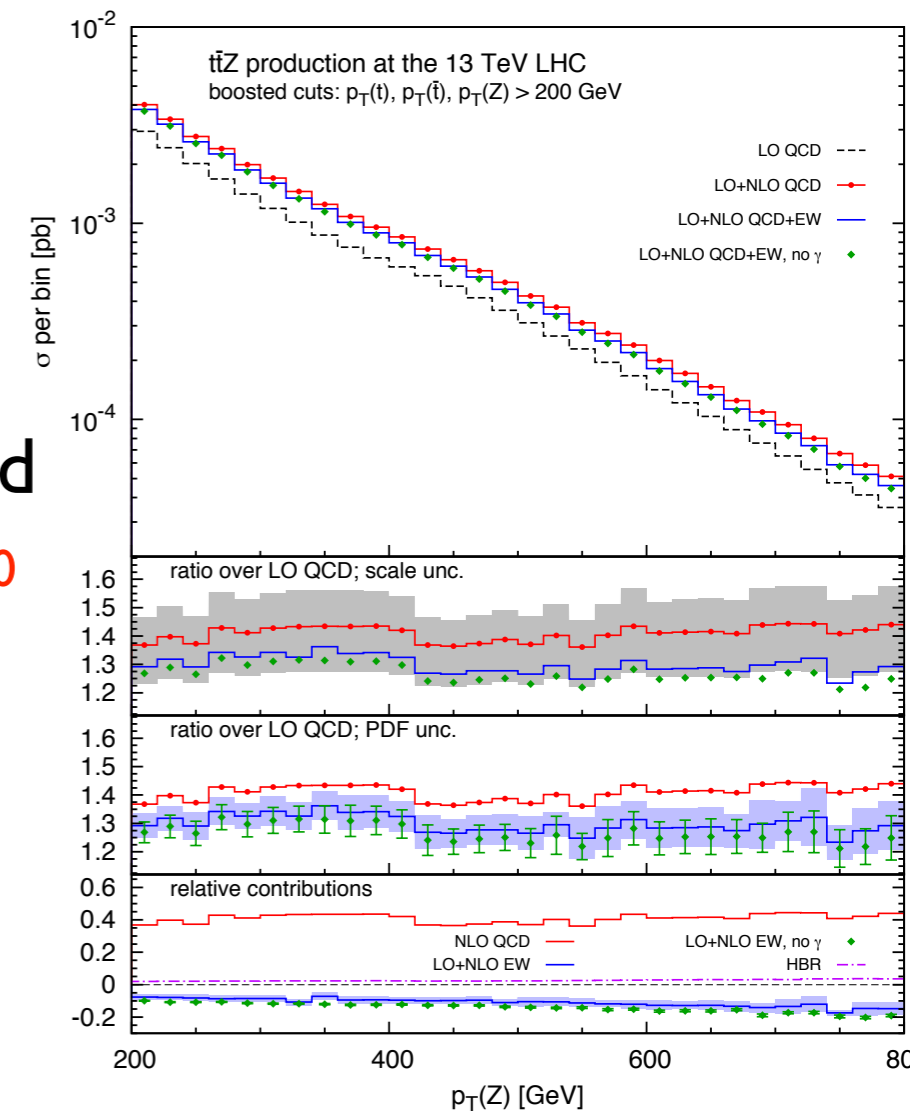
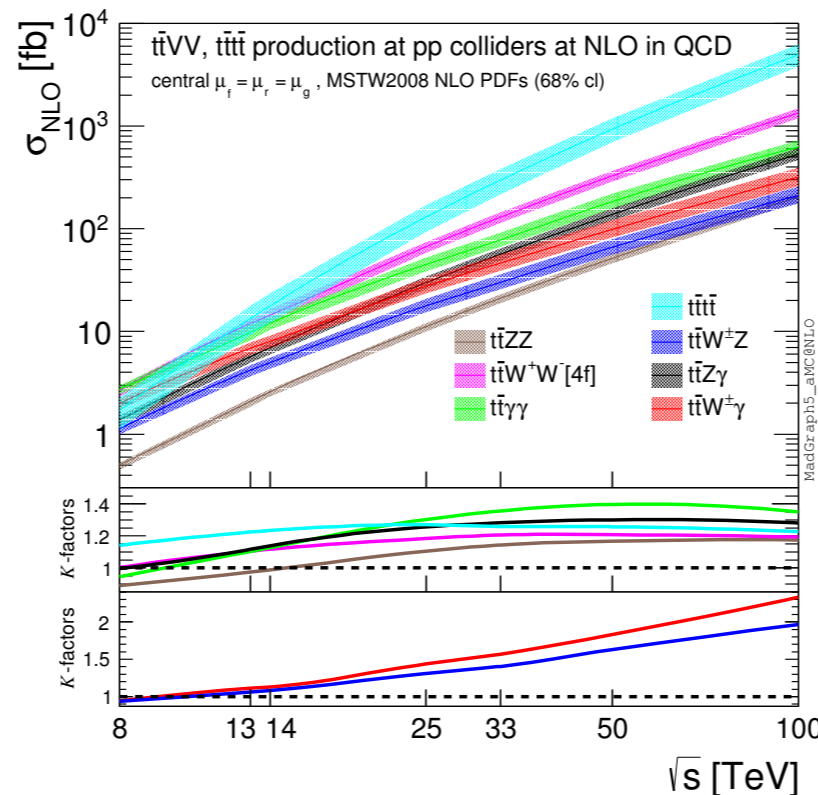
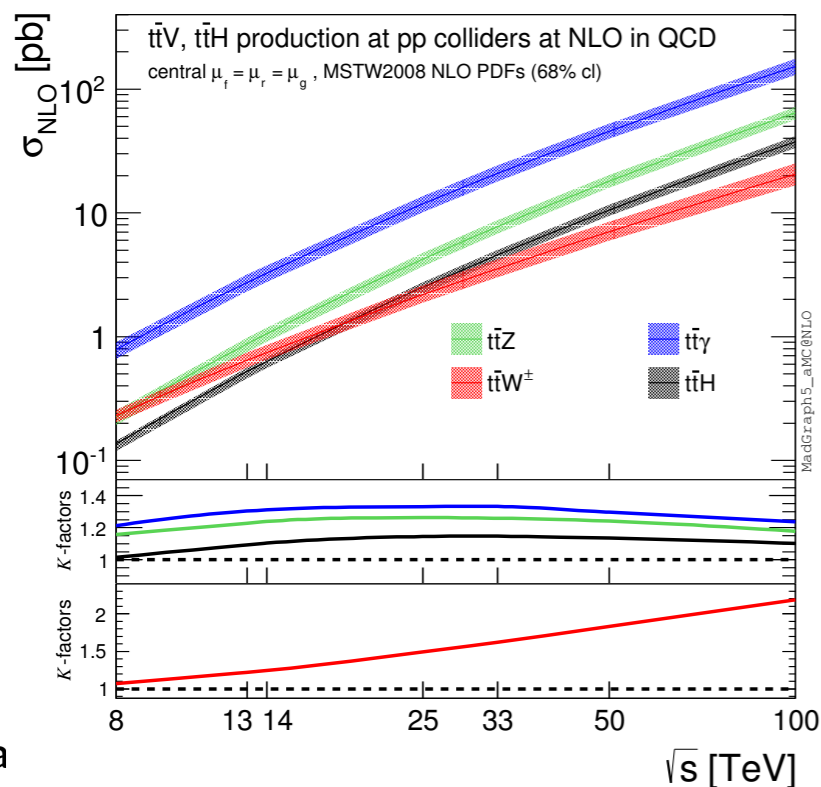
		8 TeV	13 TeV	14 TeV	33 TeV	100 TeV
$t\bar{t}$	$\sigma(\text{pb})$	$198^{+15\%}_{-14\%}$	$661^{+15\%}_{-13\%}$	$786^{+14\%}_{-13\%}$	$4630^{+12\%}_{-11\%}$	$30700^{+13\%}_{-13\%}$
	$A_c^t(\%)$	$0.72^{+0.14}_{-0.09}$	$0.45^{+0.09}_{-0.06}$	$0.43^{+0.08}_{-0.05}$	$0.26^{+0.04}_{-0.03}$	$0.12^{+0.03}_{-0.02}$
$t\bar{t}W^\pm$	$\sigma(\text{fb})$	$210^{+11\%}_{-11\%}$	$587^{+13\%}_{-12\%}$	$678^{+14\%}_{-12\%}$	$3220^{+17\%}_{-13\%}$	$19000^{+20\%}_{-17\%}$
	$A_c^t(\%)$	$2.37^{+0.56}_{-0.38}$	$2.24^{+0.43}_{-0.32}$	$2.23^{+0.43}_{-0.33}$	$1.95^{+0.28}_{-0.23}$	$1.85^{+0.21}_{-0.17}$
	$A_c^b(\%)$	$8.50^{+0.15}_{-0.10}$	$7.54^{+0.19}_{-0.17}$	$7.50^{+0.24}_{-0.22}$	$5.37^{+0.22}_{-0.30}$	$3.36^{+0.15}_{-0.19}$
	$A_c^e(\%)$	$-14.83^{+0.65}_{-0.95}$	$-13.16^{+0.81}_{-1.12}$	$-12.84^{+0.81}_{-1.11}$	$-9.21^{+0.87}_{-1.05}$	$-4.94^{+0.63}_{-0.72}$

- Expected sensitivity on asymmetries (optimistic estimate)

$t\bar{t}W: \delta A/A$	t	b	e/ $\mu$
8TeV 40fb	209%	58%	33%
14TeV 300fb	45%	13%	8%
14TeV 3ab	14%	4%	2%
100TeV 3ab	3%	2%	1%

# $t\bar{t}$ + vector bosons: A quick update

- NLO Electroweak corrections to  $t\bar{t}H/Z/W$  recently computed in [Frixione, Hirschi, Pagani, Shao, MZ, arXiv:1504.03446](#)
- Rather small at 100 TeV
  - 2%  $t\bar{t}H$ , 5%  $t\bar{t}Z$ , 10%  $t\bar{t}W$
- Can be important in boosted or very boosted scenarios, and in tails of distributions
- All  $t\bar{t}+V$ ,  $t\bar{t}+VV$ ,  $t\bar{t}t\bar{t}$  processes studied and simulated at NLO+PS accuracy in [Maltoni, Tsirikos, Pagani, arXiv:1507.05640](#)



# Conclusions

- Top quark physics will be one of the key topics at the FCC
- New techniques are being developed to improve tagging capability at large  $p_T$
- The huge amount of top quarks will allow us to measure top properties with incredible precision
- Much more to come!

# Backup:

## substructure observables

- **N-subjettines:**  $\tau_N^{(\beta)} = \sum_{i \in J} p_{T_i} \min \{ R_{i1}^\beta, \dots, R_{iN}^\beta \}$ 
  - I, N are the candidate subjets
  - It is  $\sim 0$  if there are N jets or less
  - It is  $\gg 0$  if there are at least N+1 subjets
  - Ratio of  $\tau_{N+1}/\tau_N \sim 0$  when there are N+1 subjets

Thaler, Van Tilburg,  
arXiv:1011.2268 & 1108.2701

- **Energy correlation functions (ECFs):**

Larkoski, Salam, Thaler,  
arXiv:1305.0007

$$\text{ECF}(N, \beta) = \sum_{i_1 < i_2 < \dots < i_N \in J} \left( \prod_{a=1}^N p_{T_{i_a}} \right) \left( \prod_{b=1}^{N-1} \prod_{c=b+1}^N R_{i_b i_c} \right)^\beta$$

- N+1 ECF goes to 0 if there are only N subjets
- The dimensionless ratio  $\text{ECF}(N+1)\text{ECF}(N-1) / \text{ECF}(N)^2$  goes to 0 if there are N subjets