

# Top quark physics at Linear Colliders



Roman Pöschl



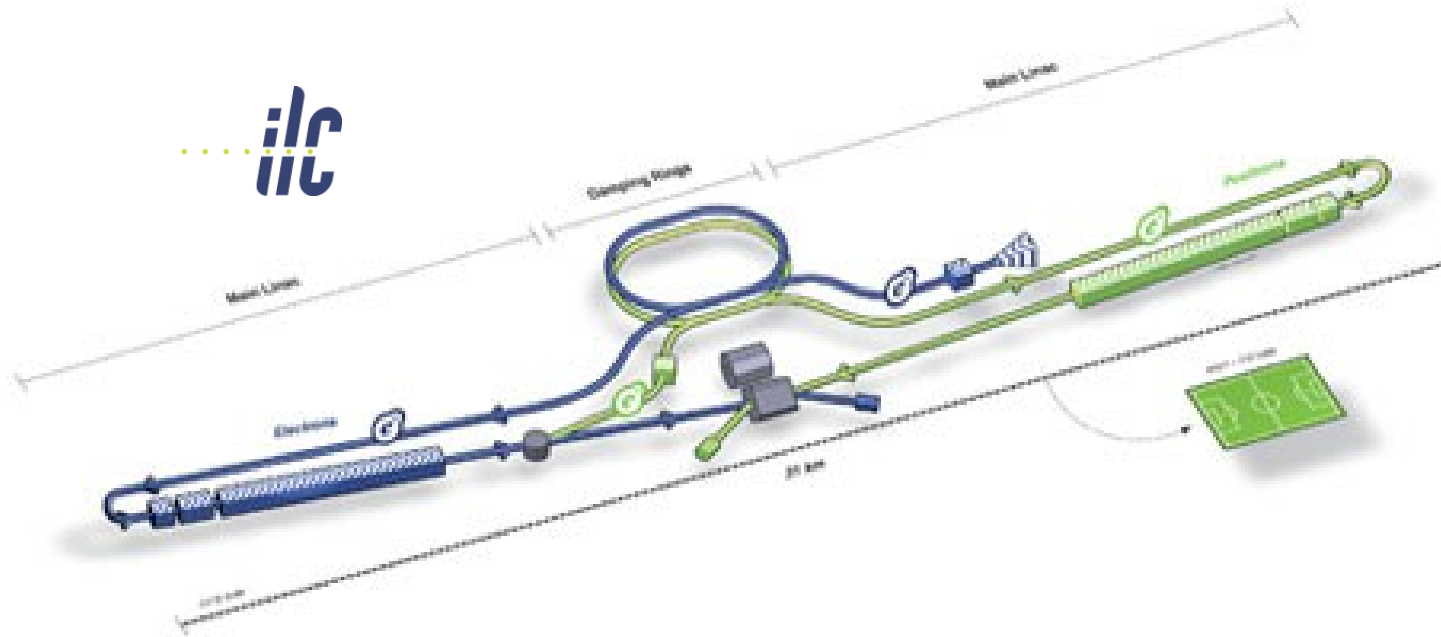
On behalf of ...

... many people contributing to  
top physics at the LC  
... the LC Collaboration

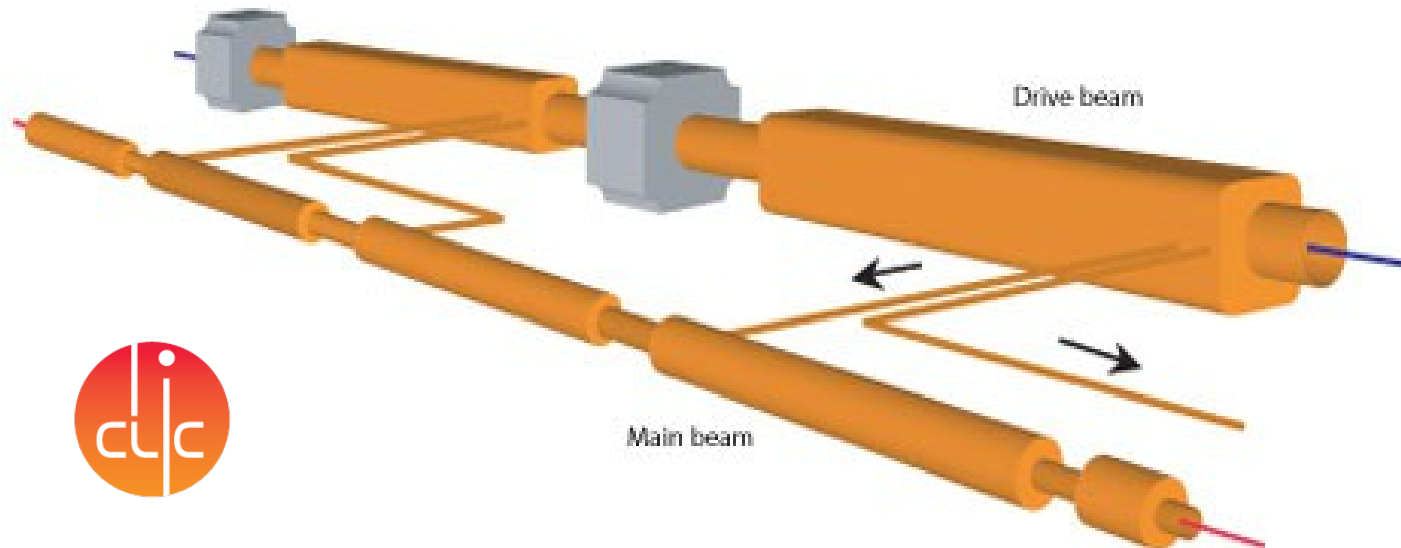
Latest reference document:

[arxiv:1506.05992](https://arxiv.org/abs/1506.05992) – ILC Physics case

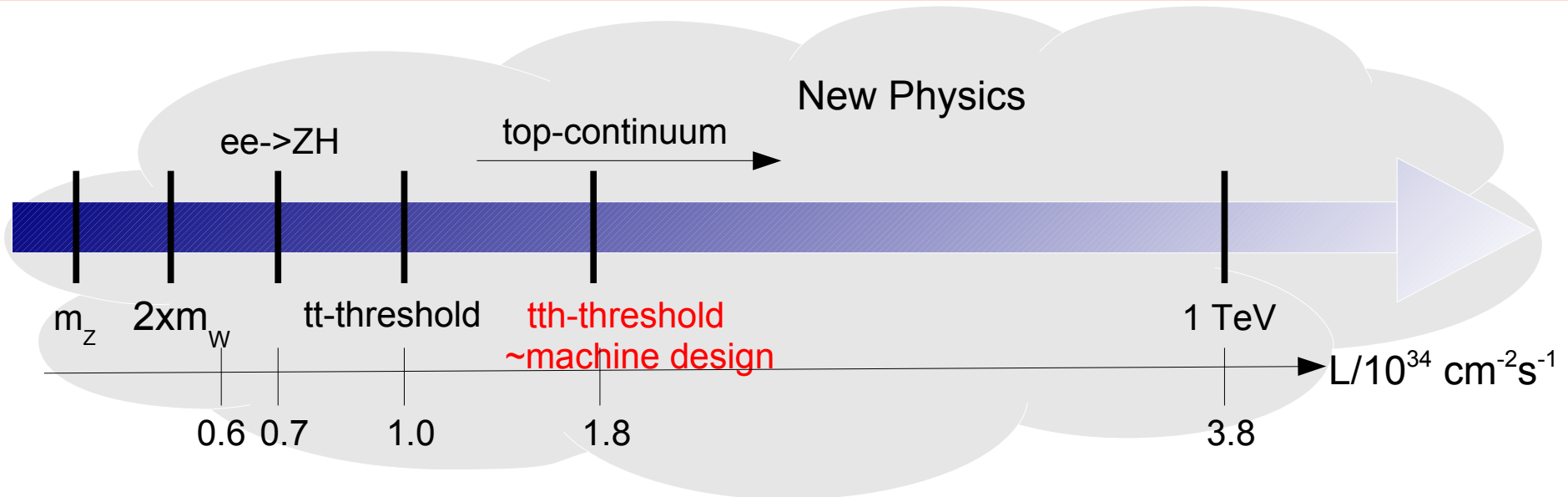
LFC 2015 – Trento/Italy September 2015



**Energy: 0.1 - 1 TeV**  
**Electron (and positron)**  
**polarisation**  
**TDR in 2013**  
**+ DBD for detectors**  
 Footprint 31 km



**Energy: 0.5 - 3 TeV**  
**CDR in 2012**  
 Footprint 48km



- All Standard Model particles within reach of ILC
  - High precision tests of Standard Model over wide range to detect onset of New Physics
- Machine settings can be “tailored” for specific processes
  - Centre-of-Mass energy
  - Beam polarisation

$$\sigma_{P,P'} = \frac{1}{4} [(1 - PP')(\sigma_{LR} + \sigma_{RL}) + (P - P')(\sigma_{RL} - \sigma_{LR})]$$

- “Background free” searches for BSM through beam polarisation

Track momentum:  $\sigma_{1/p} < 5 \times 10^{-5}/\text{GeV}$  (1/10 x LEP)

( e.g. Measurement of Z boson mass in Higgs Recoil)

Impact parameter:  $\sigma_{d_0} < [5 \oplus 10/(p[\text{GeV}]\sin^{3/2}\theta)] \mu\text{m}$  (1/3 x SLD)

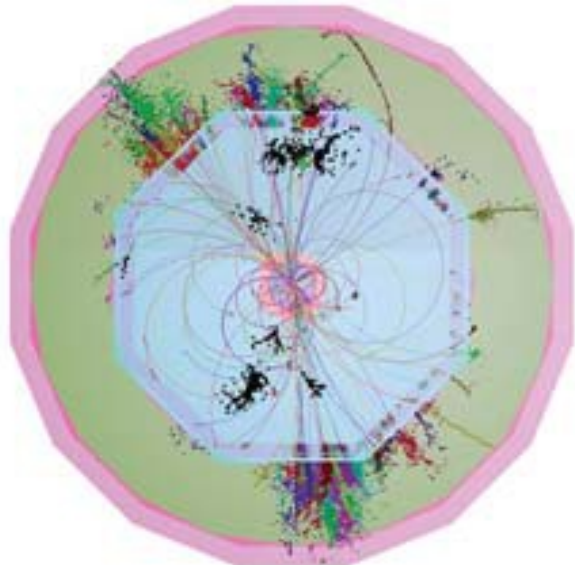
(Quark tagging c/b)

Jet energy resolution :  $dE/E = 0.3/(E(\text{GeV}))^{1/2}$  (1/2 x LEP)

(W/Z masses with jets)

Hermeticity :  $\theta_{\min} = 5 \text{ mrad}$

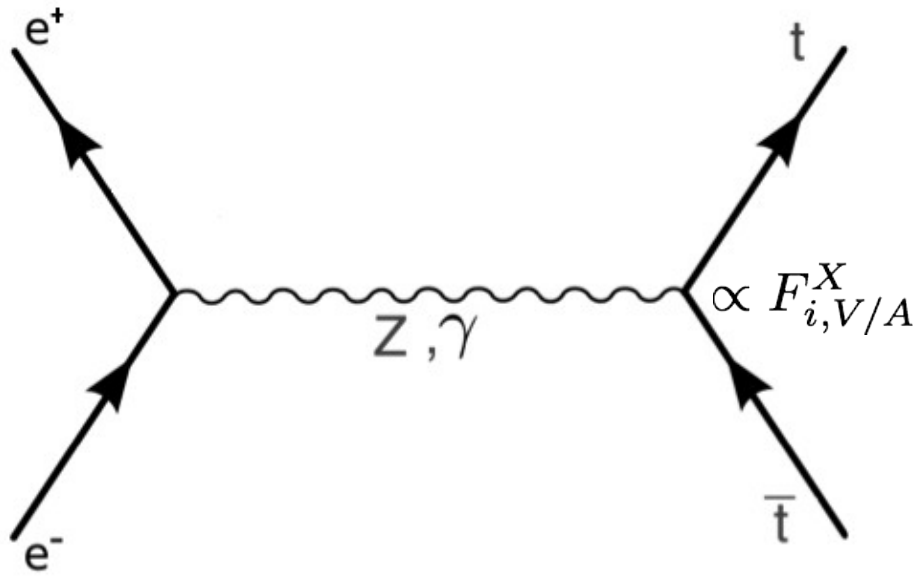
(for events with missing energy e.g. SUSY)



Final state will comprise events with a large number of charged tracks and jets(6+)

- High granularity
- Excellent momentum measurement
- High separation power for particles
- **Particle Flow Detectors**

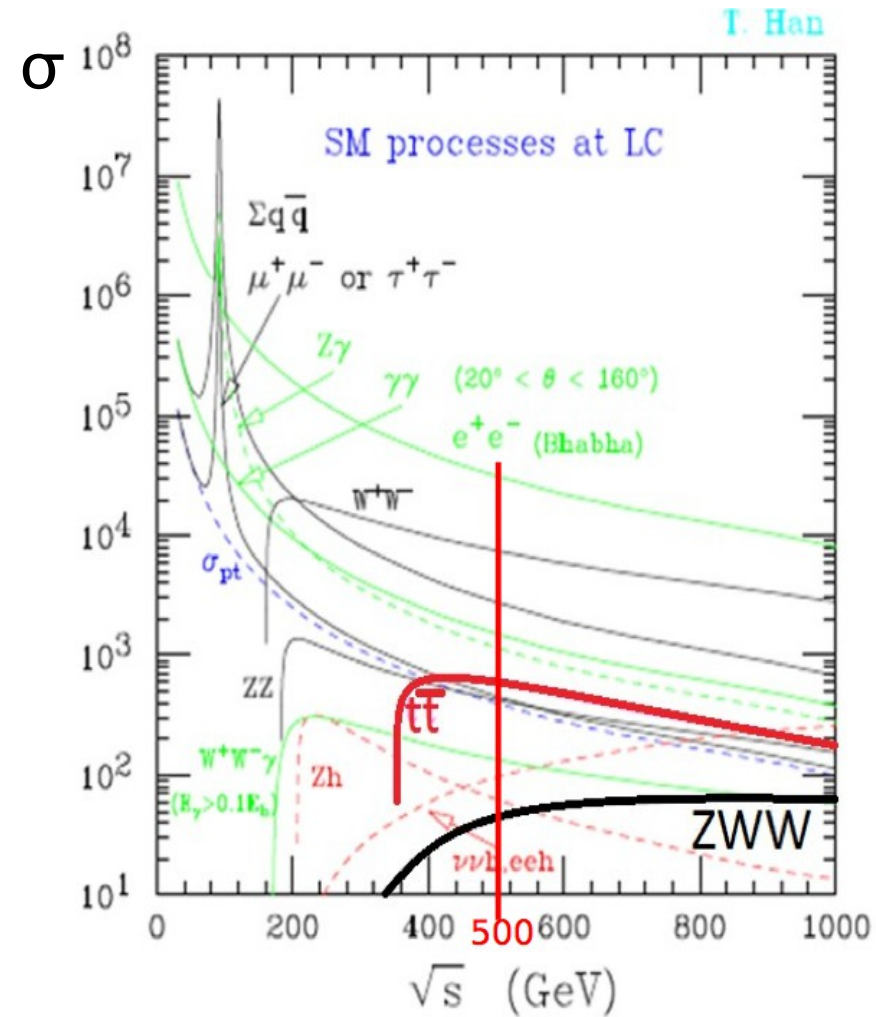
Advanced concepts: ILD, SiD and CLIC Detector



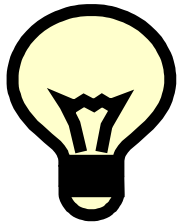
- Top quark production through electroweak processes  
no competing QCD production => Small theoretical errors!

## - High precision measurements

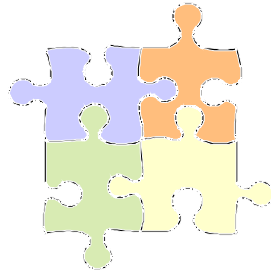
- Top quark mass at  $\sim 350$  GeV through threshold scan
- Polarised beams allow testing chiral structure at  $t\bar{t}X$  vertex  
=> Precision on form factors  $F$  and couplings  $g$



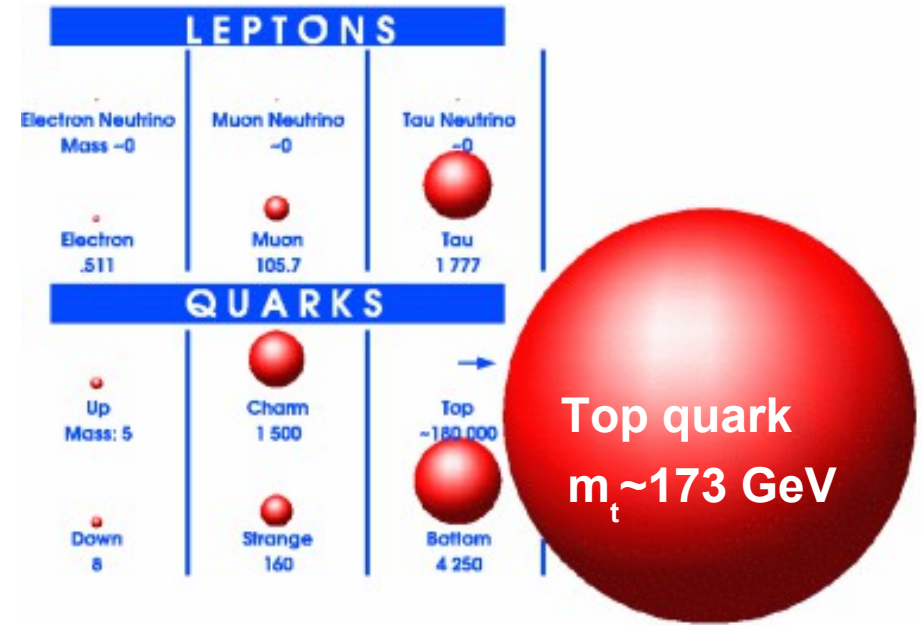




Elementary Scalar?



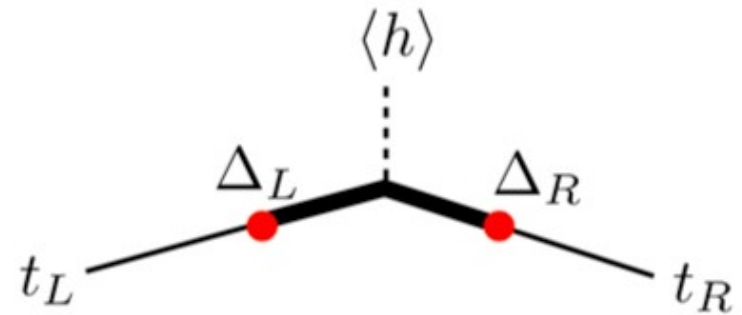
Composite object?



- Higgs and top quark are intimately coupled!  
Top Yukawa coupling  $O(1)$  !  
=> Top mass important SM Parameter

- New physics by compositeness?  
Higgs and top composite objects?

- High energy lepton colliders perfectly suited to decipher both particles

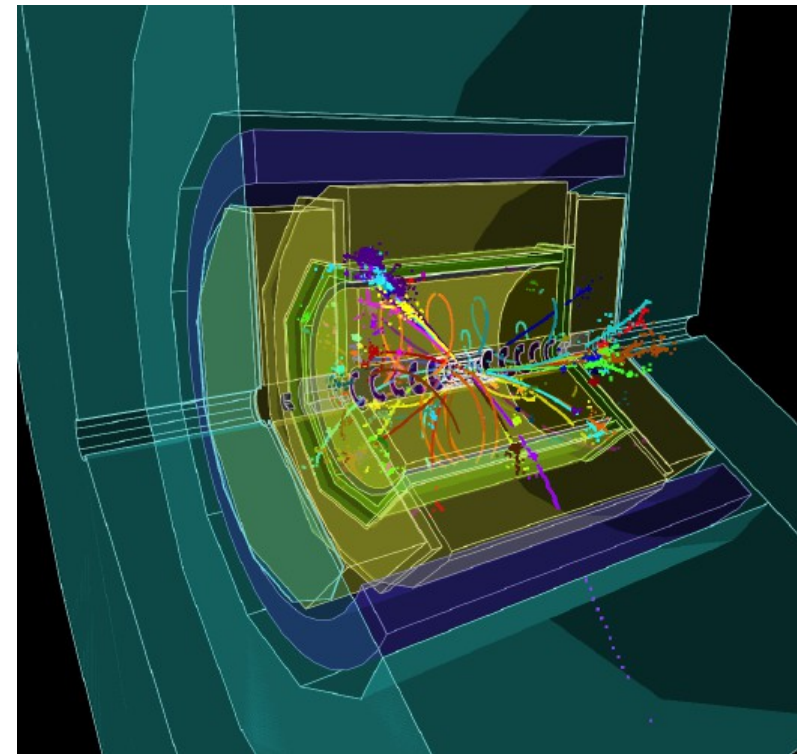
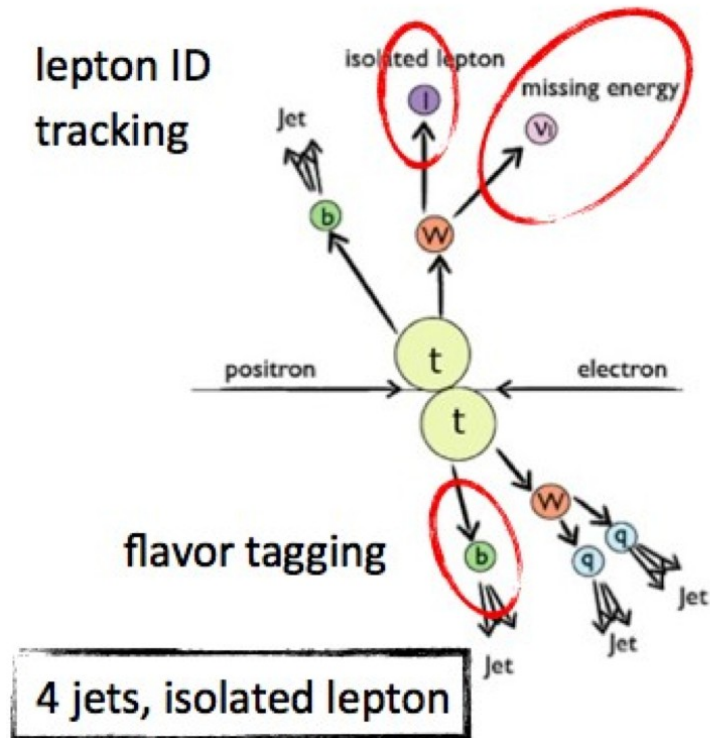


Courtesy of S. Rychkov

Three different final states:

- 1) Fully hadronic (46.2%) → 6 jets
- 2) Semi leptonic (43.5%) → 4 jets + 1 charged lepton and a neutrino
- 3) Fully leptonic (10.3%) → 2 jets + 4 leptons

$$t\bar{t} \rightarrow (bW)(bW) \rightarrow (bqq')(bl\nu)$$



**Final state reconstruction uses all detector aspects**

Results shown in the following are based on full simulation of LC Detectors

- Event generator **WHIZARD** interfaced to **PYTHIA**  
Alternative generators **PYTHIA** or **PHYSIM**
- **LC Detectors** benefit from a complete software suite
  - **GEANT4** for event simulation
  - e.g. **Mokka/DD4HEP** as geometry interface to **GEANT4**
  - **MARLIN** for event reconstruction and analysis framework
  - Interface to toolkits such as **PandoraPFA** or **LCFIVertex**
  - Extensive use of grid resources
- Detector simulation is based on input from worldwide detector R&D



## ILC:

	Stage	500			500 LumiUP		
Scenario	$\sqrt{s}$ [GeV]	500	350	250	500	350	250
G-20	$\int \mathcal{L} dt$ [fb <sup>-1</sup> ]	1000	200	500	4000	-	-
	time [years]	5.5	1.3	3.1	8.3	-	-
H-20	$\int \mathcal{L} dt$ [fb <sup>-1</sup> ]	500	200	500	3500	-	1500
	time [years]	3.7	1.3	3.1	7.5	-	3.1
I-20	$\int \mathcal{L} dt$ [fb <sup>-1</sup> ]	500	200	500	3500	1500	-
	time [years]	3.7	1.3	3.1	7.5	3.4	-

	Stage	500			500 LumiUP		
Scenario	$\sqrt{s}$ [GeV]	250	500	350	250	350	500
Snow	$\int \mathcal{L} dt$ [fb <sup>-1</sup> ]	250	500	200	900	-	1100
	time [years]	4.1	1.8	1.3	3.3	-	1.9

For details see: [arxiv: 1506.07830](https://arxiv.org/abs/1506.07830)

## CLIC:

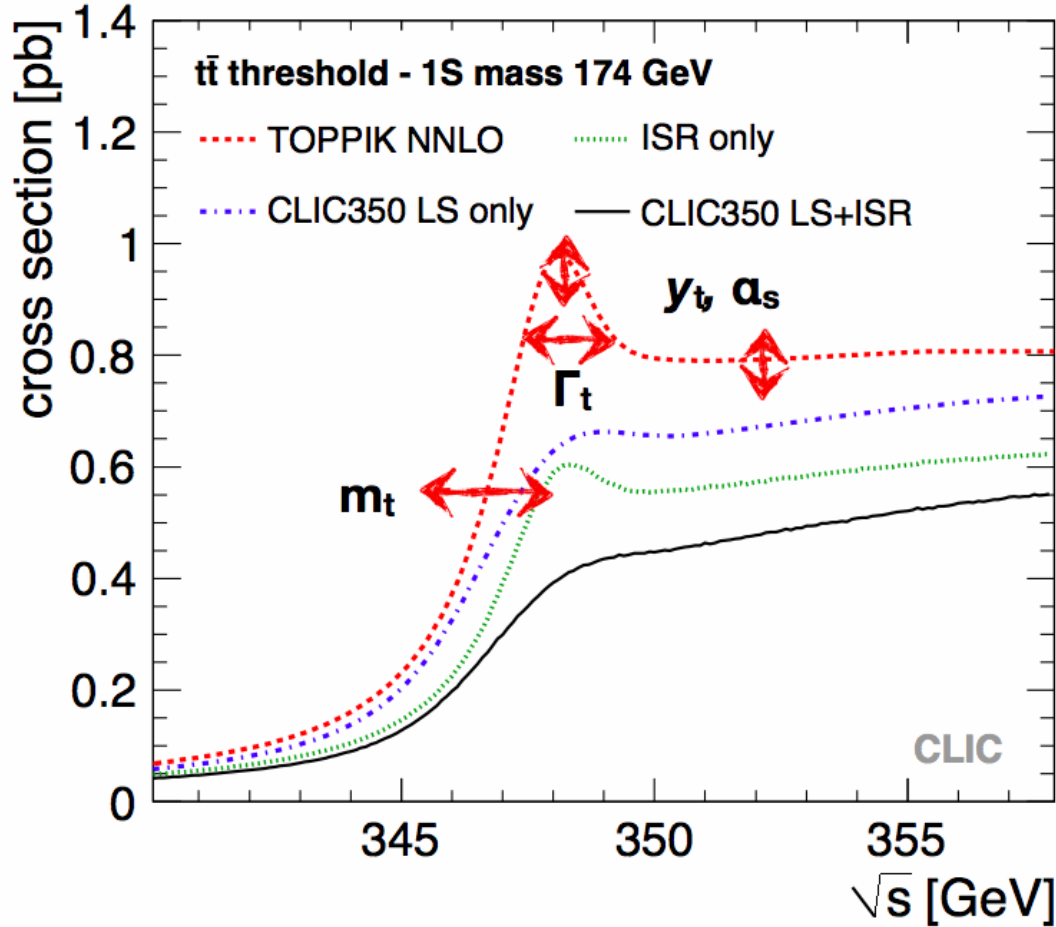
~380 GeV 500 fb<sup>-1</sup>: precision Higgs and **top physics**

~1.4 TeV 1.5ab<sup>-1</sup>: BSM physics, precision Higgs physics and **top physics**

~ 3 TeV, 2ab<sup>-1</sup>: BSM physics, precision Higgs

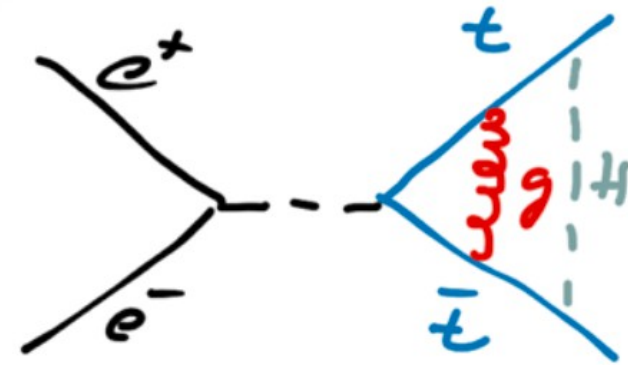
**Running scenarios favour early start of top physics programme**

Small size of  $t\bar{t}$  “bound state” at threshold ideal remise for precision physics

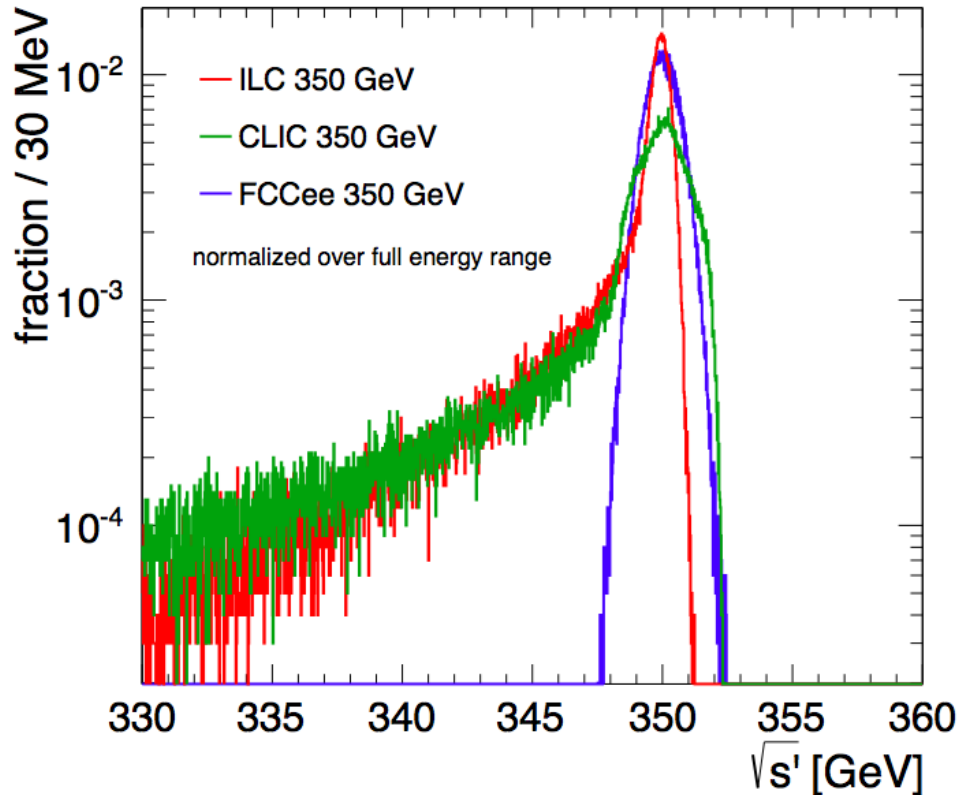


Cross section around threshold is  
Affected by several properties  
Of the top quark and by QCD

- Top mass, width Yukawa coupling
- Strong coupling constant

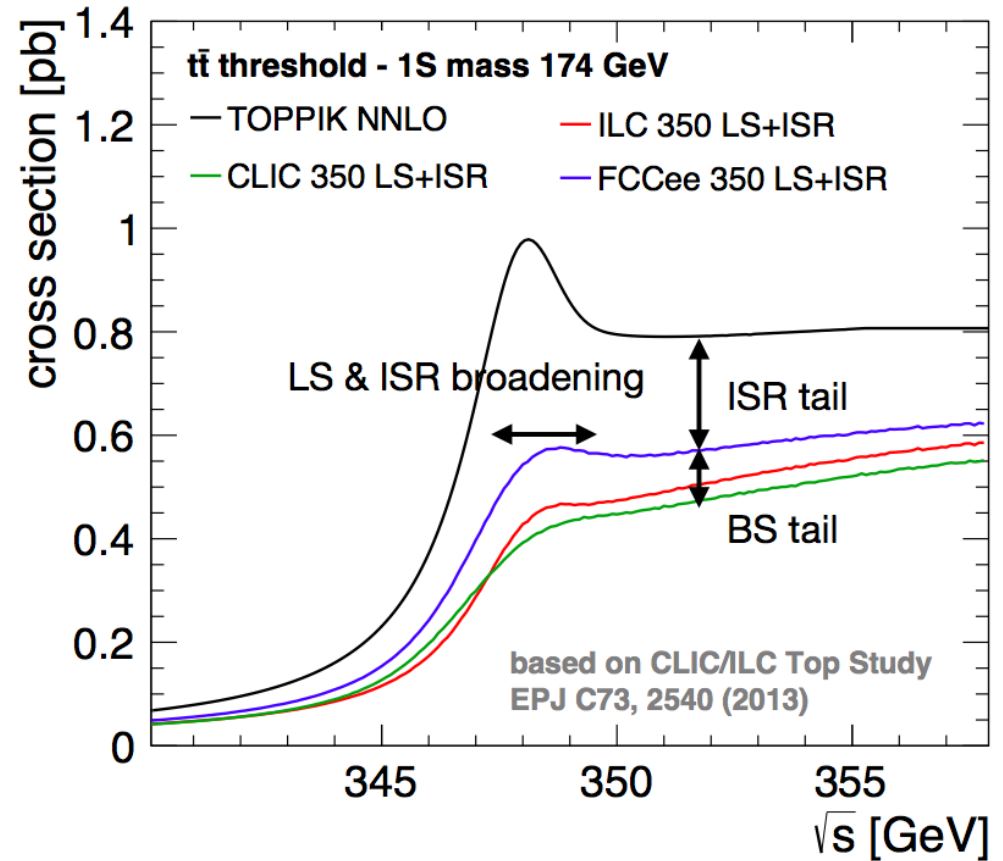


Effects of some parameters are correlated:  
Dependence on Yukawa coupling rather weak,  
Precise external  $\alpha_s$  helps



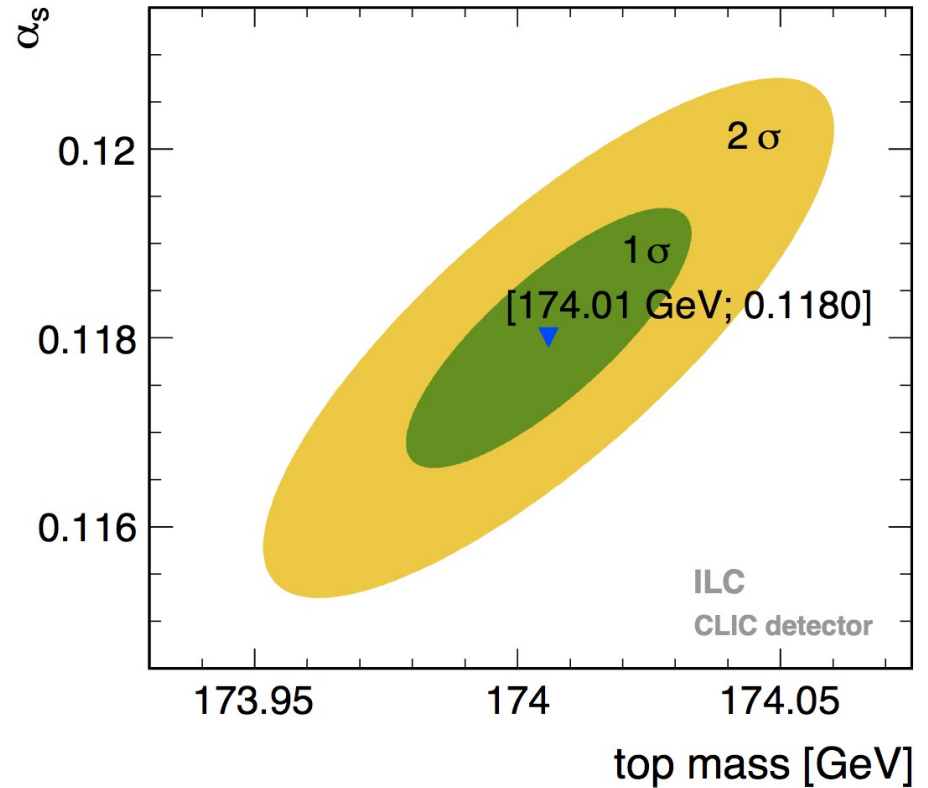
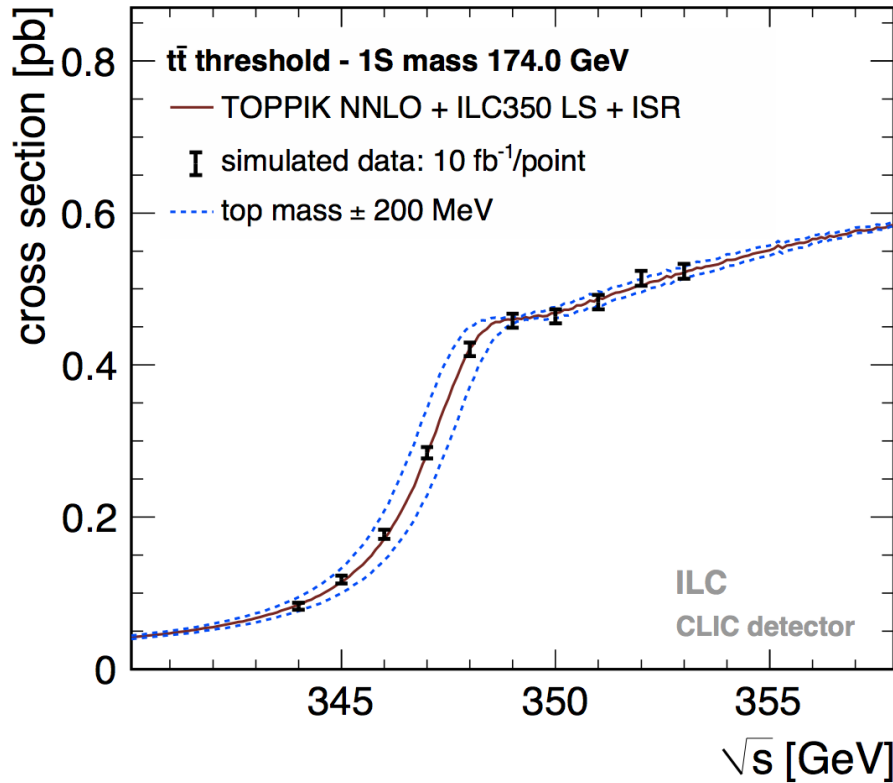
- Slight changes in statistics due to cross section, changes in sensitivity due to steepness of threshold turn on
- For 100 fb<sup>-1</sup>, no polarisation, 1D mass fit  
16 MeV → 18 MeV → 21 MeV (stat.)  
FCCee      ILC      CLIC

- Somewhat different luminosity spectra for different machines
- No beamstrahlung in storage ring
- Sharper main peak at ILC broader for CLIC





## Mass and $\alpha_s$



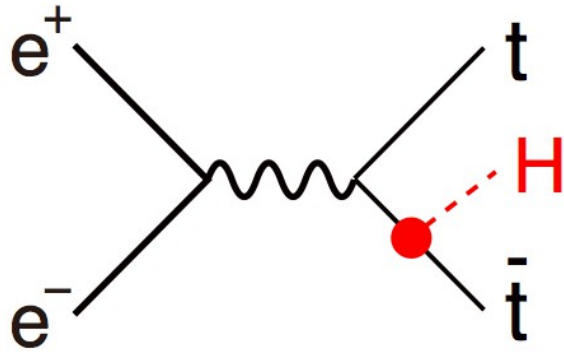
~100 MeV

### 1S top mass and $\alpha_s$ combined 2D fit

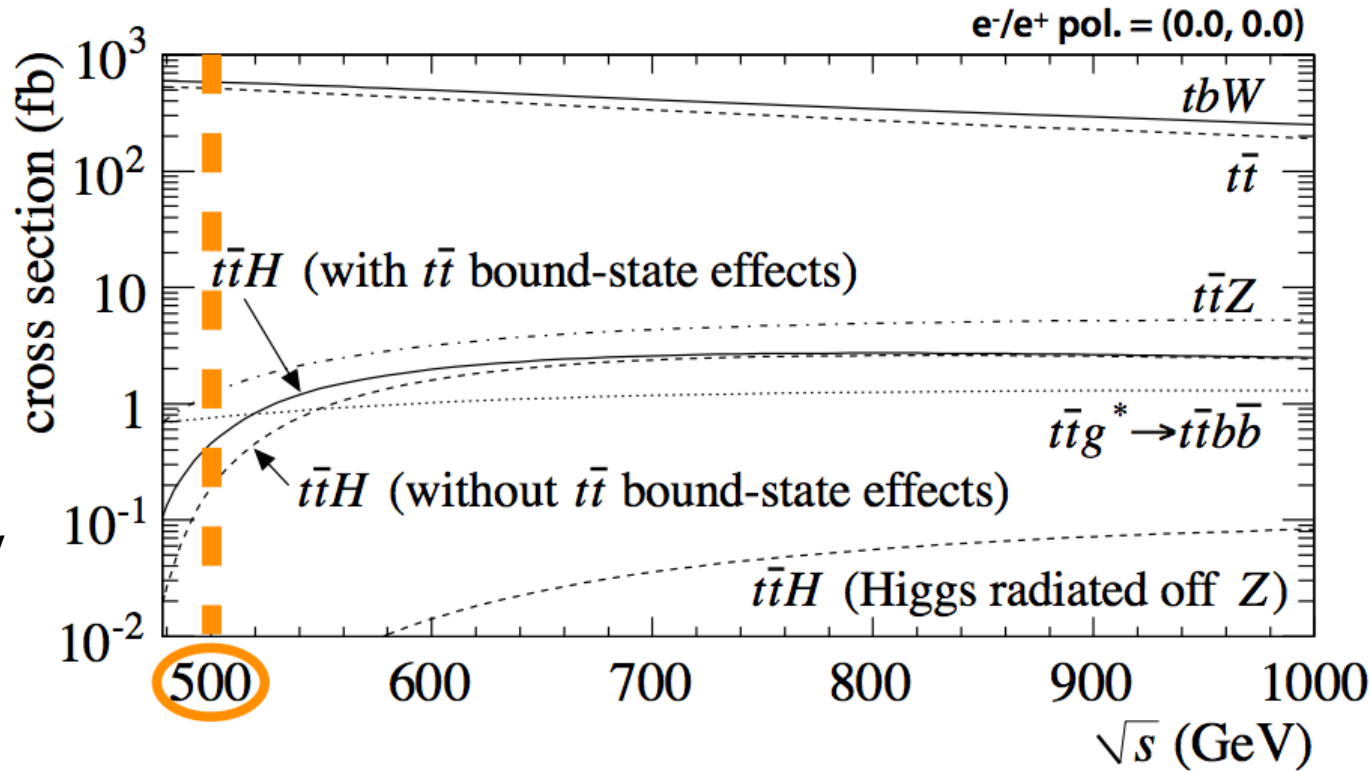
$m_t$ stat. error	27 MeV
$m_t$ theory syst. (1%/3%)	5 MeV / 9 MeV
$\alpha_s$ stat. error	0.0008
$\alpha_s$ theory syst. (1%/3%)	0.0007 / 0.0022

- Expected statistical uncertainty **10 – 30 MeV**
- Experimental systematics
  - Beam energy: **~30 MeV** or lower
  - Non-ttbar background, selection efficiencies: **~ 15 MeV**
  - Luminosity spectrum: **10 MeV**
  - Single top contamination: **< 30 MeV**
- Theory uncertainties
  - Normalisation: **~55 MeV (naive estimate)** much smaller due to recent NNNLO calculations arxiv: 1506.06864, arxiv:1506.06542
  - When not included in the fit:  $\sim 3 \text{ MeV per } 10^{-4}$  uncertainty on  $\alpha_s$  today  $\rightarrow$  **~18 MeV**
  - Conversion from 1S/PS masses to MSbar mass Currently: **~50 MeV**  
However conversion now known to N<sup>4</sup>LO (arxiv:1502.01030)
  - Now at point where results become sensitive to effects other than QCD





- Coupling of Higgs to heaviest particle known today
- Up to eight final state jets



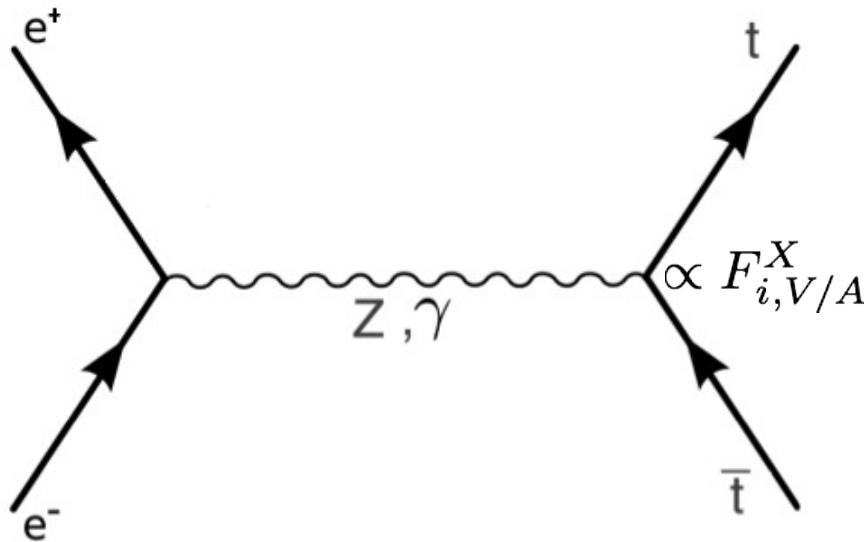
$\Delta g_{ttH}/g_{ttH}$	H20 - 500	H20 - 500 Lumi Up
Standard ILC	18%	6.3%
ILC @ $\sqrt{s} = 550$ GeV	~9%	~3%

← ILC 2015  
← Technically possible

Running at 1 TeV would allow precision at the 1 – 2% level



- Fermion mass generation closely related to the origin electroweak symmetry breaking
- Expect residual effects for particles with masses closest to symmetry breaking scale



## Manifestation of New Physics:

- Modification of Ztt coupling  
Mixing between top and partners  
Mixing Z/Z'
- s-channel exchange of New Z'  
Including interference effects

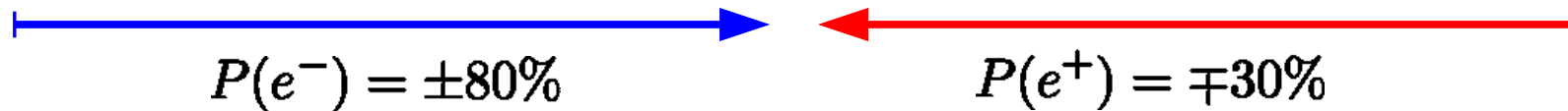
$$\Gamma_{\mu}^{ttX}(k^2, q, \bar{q}) = -ie \left\{ \gamma_{\mu} (F_{1V}^X(k^2) + \gamma_5 F_{1A}^X(k^2)) + \frac{\sigma_{\mu\nu}}{2m_t} (q + \bar{q})^{\nu} (iF_{2V}^X(k^2) + \gamma_5 F_{2A}^X(k^2)) \right\}, \quad (2)$$

Pure  $\gamma$  or pure  $Z^0$  :  $\sigma \sim (F_i)^2 \Rightarrow$  No sensitivity to sign of Form Factors

$Z^0/\gamma$  interference :  $\sigma \sim (F_i) \Rightarrow$  Sensitivity to sign of Form Factors

At ILC **no** separate access to  $ttZ$  or  $tty$  vertex, but ...

**ILC 'provides' two beam polarisations**



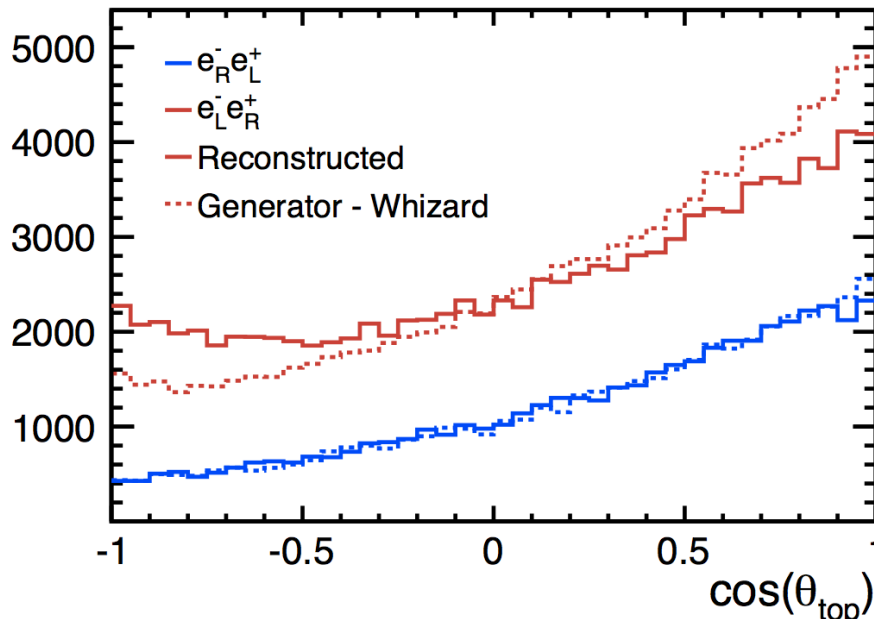
There exists a number of observables sensitive to chiral structure, e.g.

$\sigma_I$	$A_{FB,I}^t = \frac{N(\cos\theta > 0) - N(\cos\theta < 0)}{N(\cos\theta > 0) + N(\cos\theta < 0)}$	$(F_R)_I = \frac{(\sigma_R)_I}{\sigma_I}$
x-section	Forward backward asymmetry	Fraction of right handed top quarks



Extraction of relevant unknowns

$$\begin{array}{c}
 F_{1V}^\gamma, F_{1V}^Z, F_{1A}^\gamma = 0, F_{1A}^Z \\
 F_{2V}^\gamma, F_{2V}^Z
 \end{array}
 \quad \text{or equivalently} \quad
 g_L^\gamma, g_R^\gamma, g_L^Z, g_R^Z$$

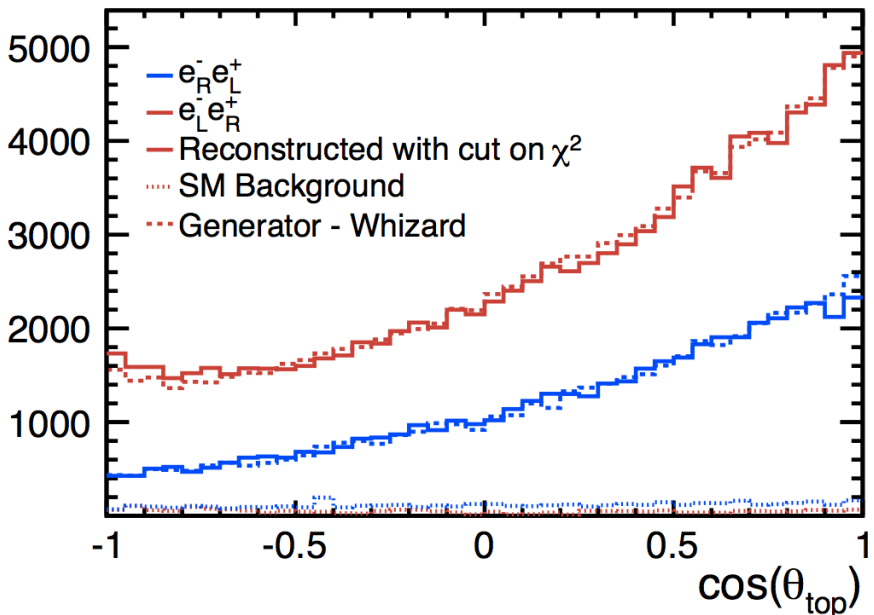


Ambiguities in case of  
**left** handed electron beams  
Due to V-A structure at ttX vertex

Precise reconstruction of  $\theta_{top}$   
in case of **right** handed electron beams

Remedy to address ambiguities:  
Select cleanly reconstructed  
events by  $\chi^2$  analysis

or  
Reconstruction of b quark charge



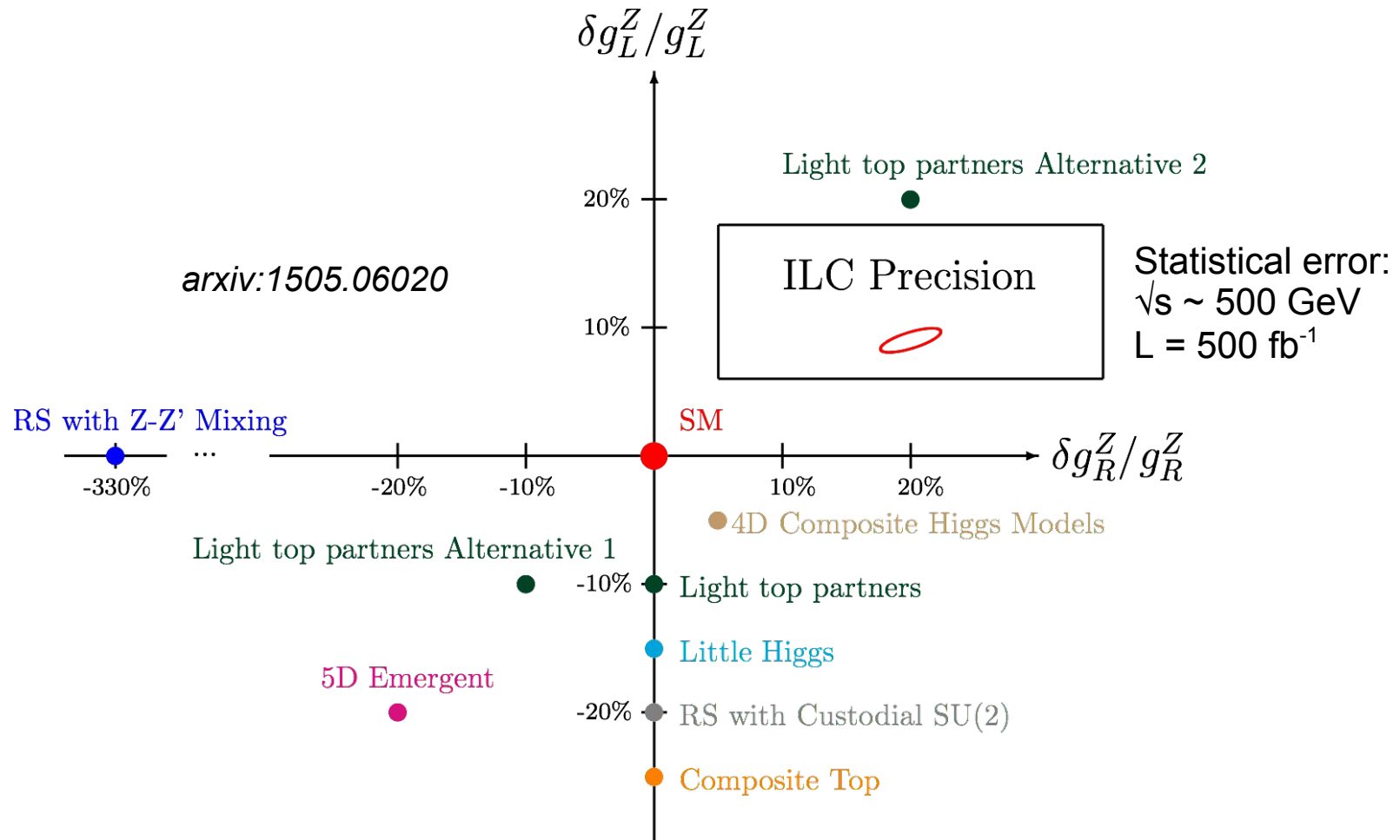
Precise reconstruction for both  
beam polarisations

- Efficiency Penalty for  $e_L$
- $\epsilon_{tot}$ :  $e_R \sim 50\%$ ,  $e_L \sim 30\%$

Results:

$\mathcal{P}_{e-}, \mathcal{P}_{e+}$	$(\delta\sigma/\sigma)_{stat.} [\%]$	$(\delta A_{FB}^t/A_{FB}^t)_{stat.} [\%]$
-0.8, +0.3	0.47	1.8
+0.8, -0.3	0.63	1.3

Top is primary candidate to be a messenger new physics in many BSM models  
Incorporating compositeness and/or extra dimensions



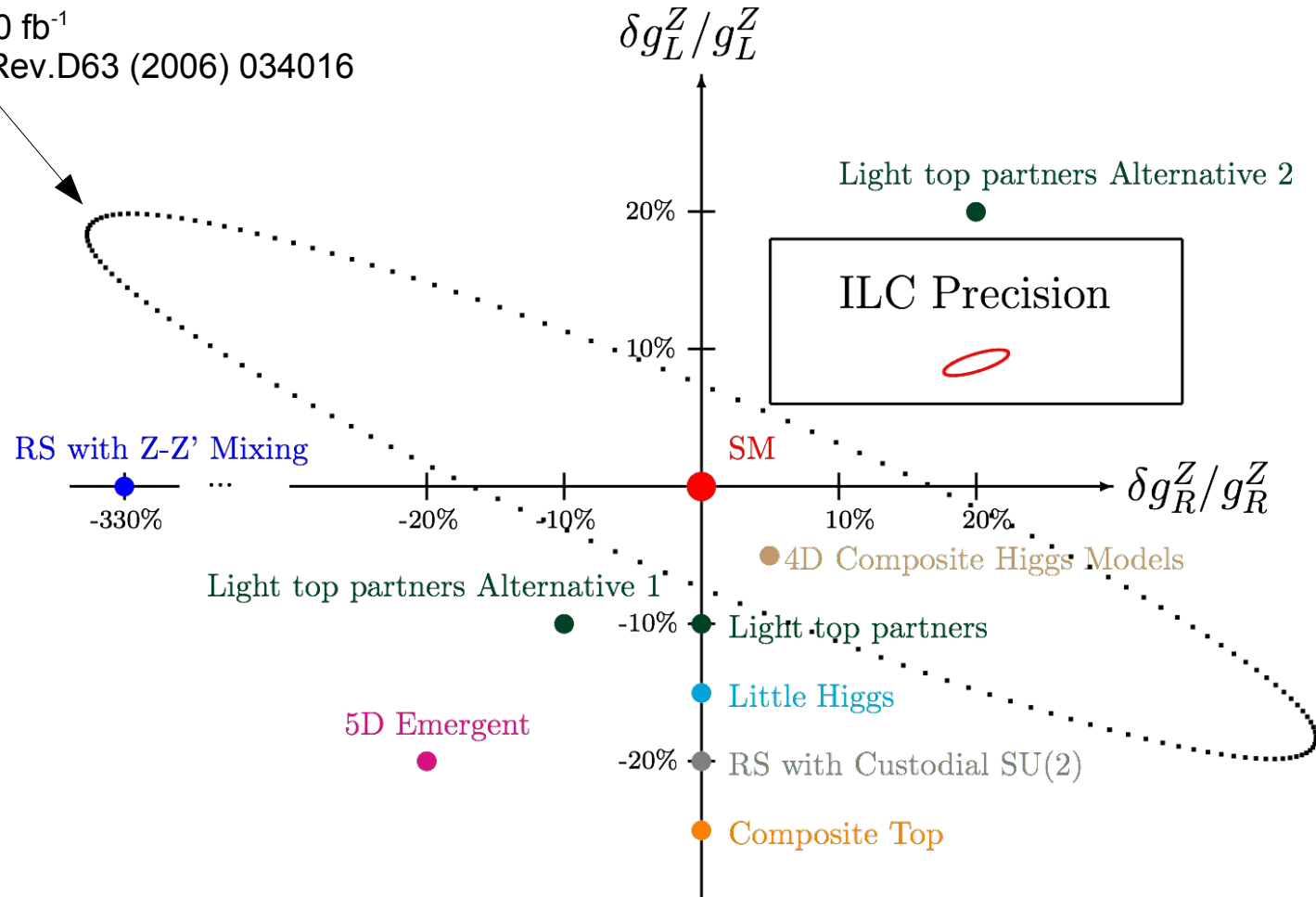
Precision expected for top quark couplings will allow to distinguish between models

Remark: All presented models are compatible with LEP elw. precision data



LHC14, 3000 fb<sup>-1</sup>

From Phys.Rev.D63 (2006) 034016

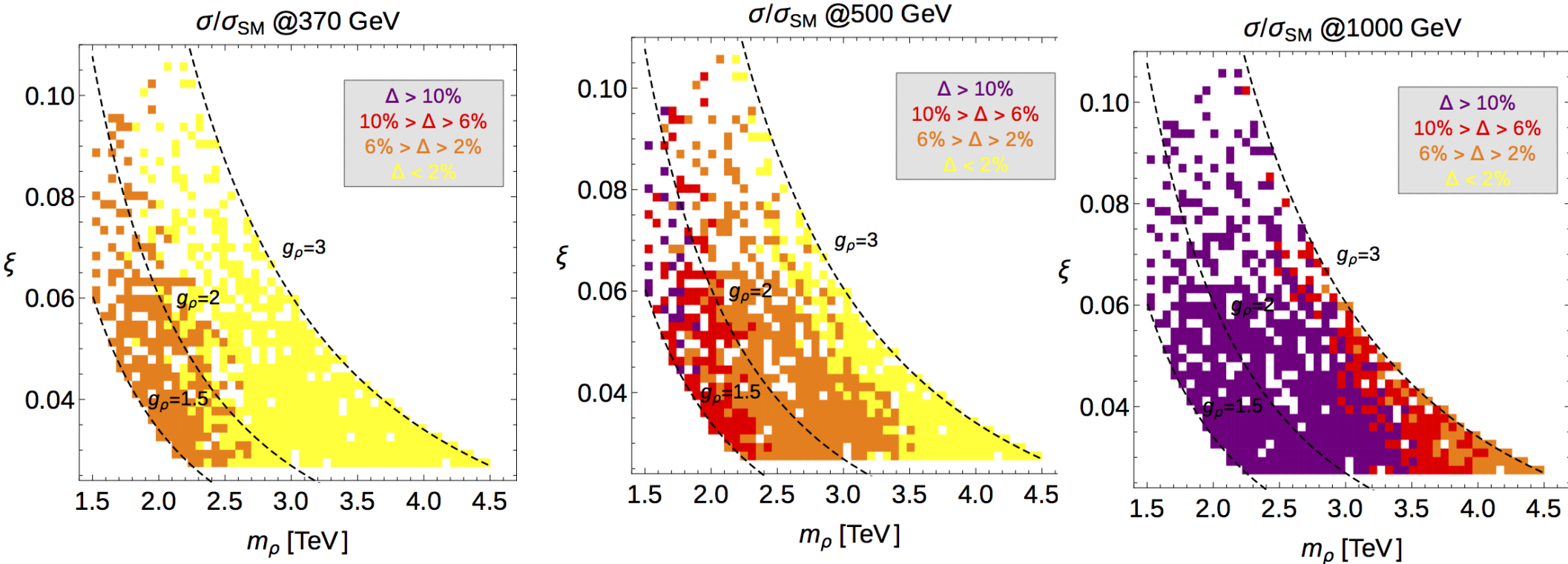


## Linear Collider will outperform LHC results

- Particular poor constraint on  $g_R$  (this holds also for flavor physics results)
- LHC LO QCD analysis, ~30% improvement through NLO QCD
- LHC may still be capable to exclude models

Example: Sensitivity to  $M_{Z'} = M_\rho$  in 4D Higgs Composite Model, arxiv: 1504.05407

$$\frac{\delta g_I}{g_I} \sim \xi \sim \left( \frac{v g_\rho}{M_\rho} \right)^2$$

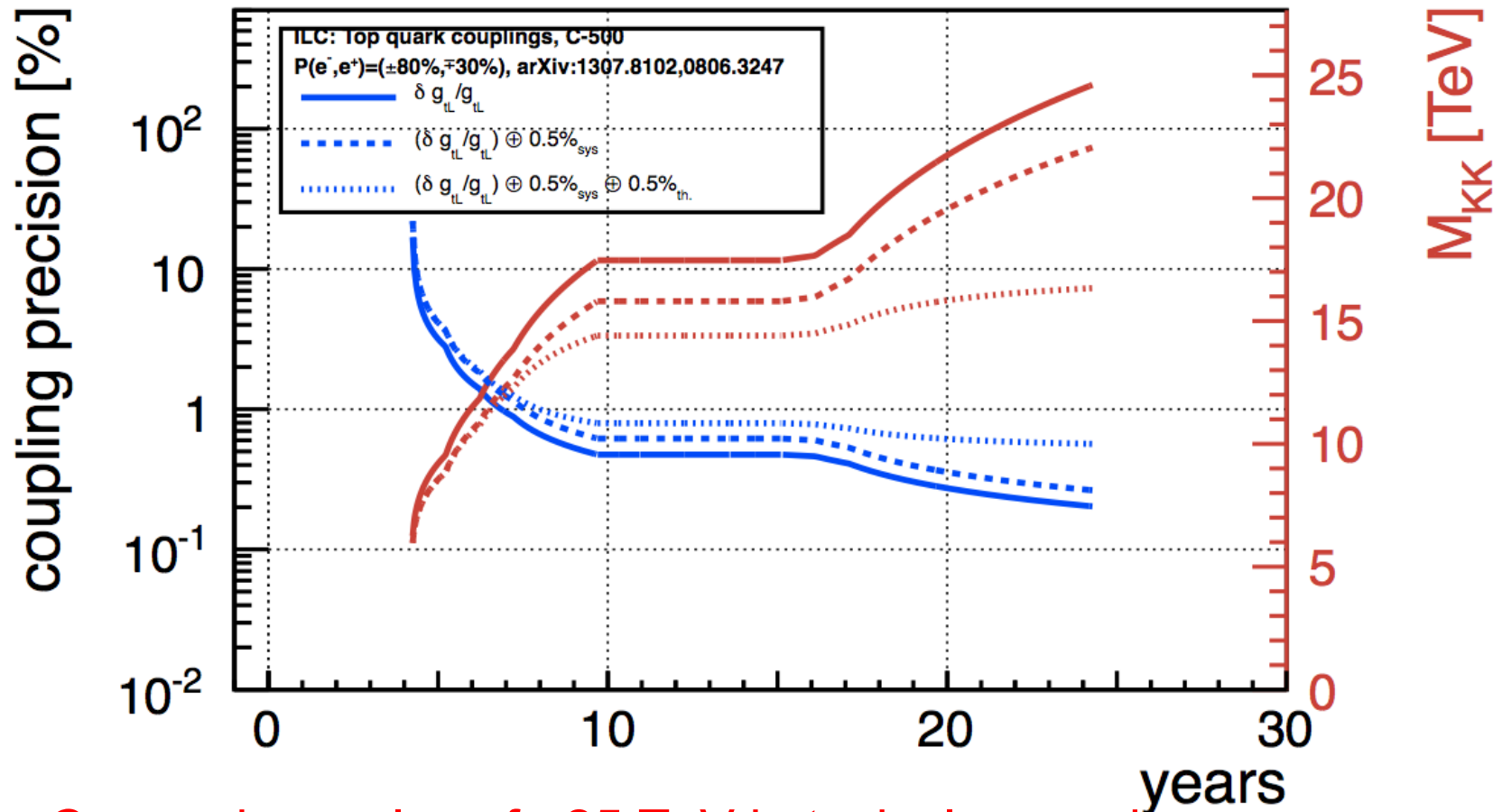


$\sqrt{s}$

Effects observed at smaller energies may be amplified at higher energies

New physics reach for typical BSM scenarios with composite Higgs/Top and or extra dimensions

Based on phenomenology described in Pomerol et al. arXiv:0806.3247



Can probe scales of ~25 TeV in typical scenarios

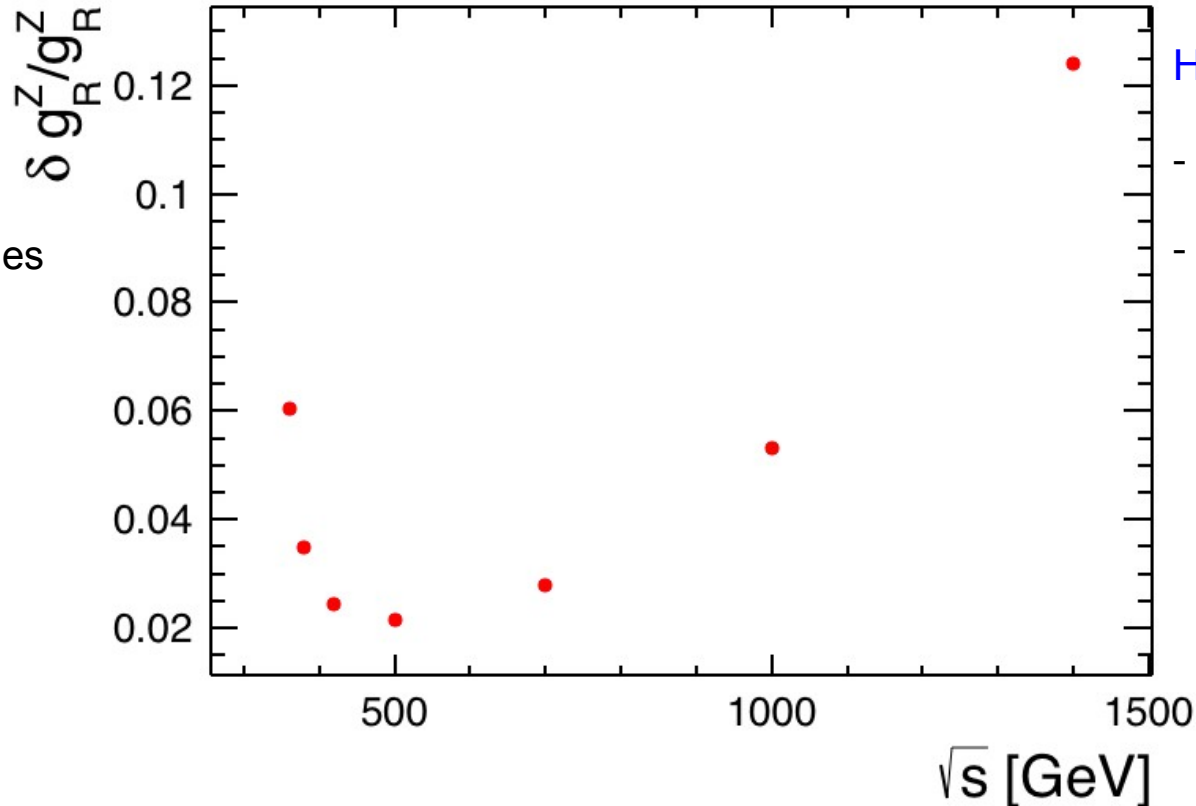
(... and up to 80 TeV for extreme scenarios)

=> Important guidance for e.g. 100 TeV pp-collider

... simplified discussion

Small cms energies:

- Vanishing axial vector coupling
- large QCD uncertainties ... and
- Lumi decreases at linear colliders



High cms energies:

- Quickly decreasing cross section
- ... partially compensated by increasing luminosity

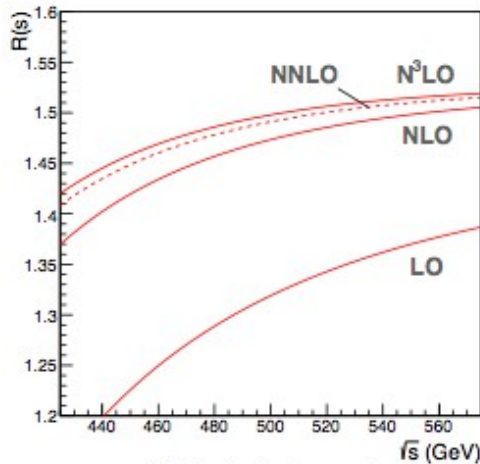
Broad minimum between 400 and 700 GeV

$\sqrt{s} \sim 500$  GeV is “sweet spot” for coupling measurements

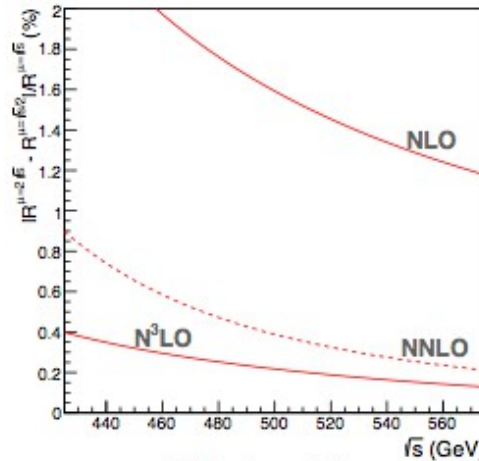
However:

- Sensitivity to CP violating Higgs at smaller cms energies
- New physics at higher energies may increase cross section (see above)

## \*QCD corrections are known up to N<sup>3</sup>LO



(a) Perturbation series

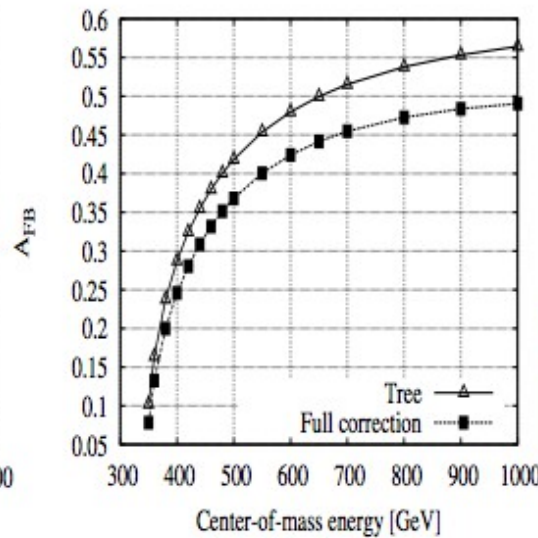
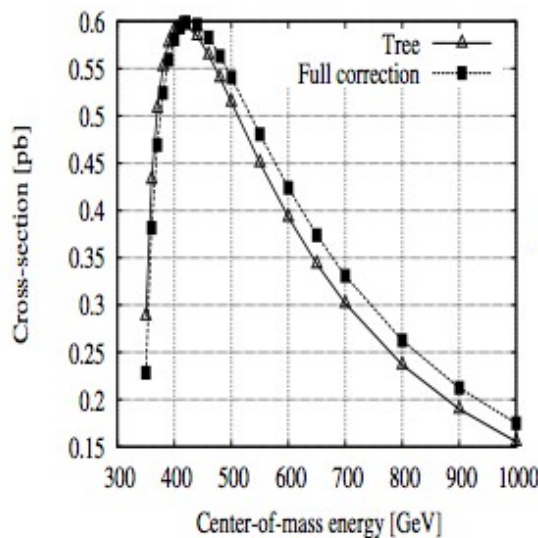


(b) Scale variations

QCD correction (N<sup>3</sup>LO) is at the per mil level

*Kiyo, Maier, Maierhofer, Marquard, NCP B823 ('09)*  
*Bernreuther, Bonciani, Gehrmann, Heinesch, Leineweber, NPB750 ('06)*  
*Hoang, Mateu, Zebarjad, NPB813 ('09)*

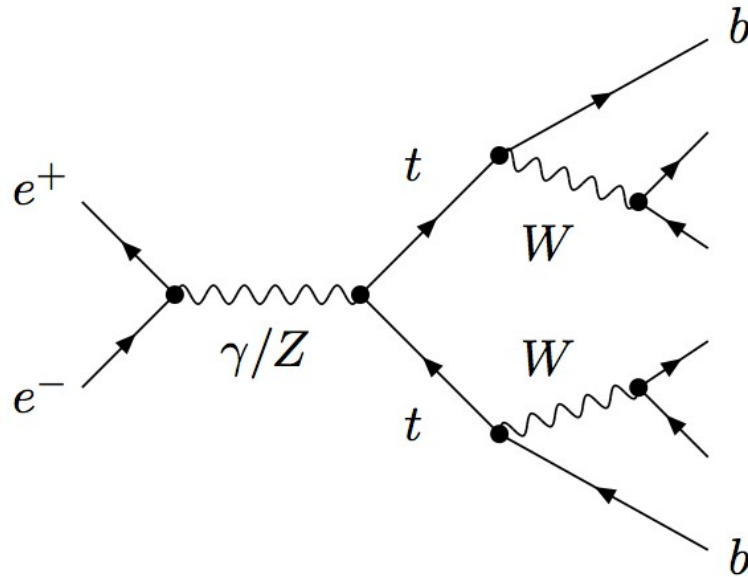
## \*Electroweak corrections are known at one-loop level



EW correction at one-loop is  
 ~5% for cross section  
 ~10% for A<sub>FB</sub>

*Fleischer, Leike, Riemann, Werthenbach, EJPC31 ('03)*  
*Kheim, Fujimoto, Ishikawa, Kaneko, Kato, arXiv:1211.1112*





Top pair production is effectively  $ee \rightarrow 6f$  process

- Role of (indistinguishable) single top production (Eur. Phys. J. C (2015) **75**: 223)  
Only relevant for  $e_L$
- QCD and electroweak corrections for top decay chain
- Effects of finite top width and  $V_{tb}$  instead of  $\Gamma_t$
- Exploitation of information of final state by matrix element method (arxiv: 1503.04247)  
-> Talk by Emi Kou  
Unbiased access to tensorial CP violating form factors !?

- A LC is the right machine for **rediscovery of the top quark** by precision physics
  - Production top pairs in electroweak production!!!
  - Essential pillar of LC physics program
  - Experimental programme can take full advantage of flexible running (cms energy)
- Full simulation available for LC detectors
  - => Great deal of realism and confidence in perspectives
- Precision on top mass reach 50 MeV regime (200 fb<sup>-1</sup> or less needed)
  - Effort was driven by experimental study, now need to feedback newest theory insights
- Precision on form factors and couplings of the order of 1% with minimal ILC running scenario
  - Sensitivity to new physics up to several 10 TeV
  - Main experimental challenge is control of migrations in  $A_{FB}$
  - Beam polarisation is major asset for control of theoretical and experimental ambiguities
- Start to address full 6 fermion final state instead of tt only
- Keeping all the promises is hardest task in coming years
  - Need full understanding of systematics for optimal detector and machine design

- Get a good guess on systematic errors
- Feed conclusions into machine and detector design  
(Remember total uncertainty needs to remain e.g.  $\sim 0.1\%$  for coupling studies)
- Understanding aspects of 6 fermion final state (experimentally and theoretically)
- Explore full potential of measurement of CP violation
- Impact of higher order electroweak corrections
- Experimental study of matrix element method
- Pros and cons of effective field theory and full /new physics models
- Monitoring and reacting to latest LHC results

**Backup ....**

- Regular workshops, so far three
- May 2012 in Paris (ENS Chimie)  
<http://events.lal.in2p3.fr/conferences/Top-Quark-Physics/Contacts.html>
- March 2014 in Paris (LPNHE)  
<https://agenda.linearcollider.org/event/6296/program>
- June 2015 at IFIC Valencia  
<http://ific.uv.es/~toplc15/index.html>
- 2016 ??? maybe Japan
- Mailing list: [topatlc-l@listserv.in2p3.fr](mailto:topatlc-l@listserv.in2p3.fr) (40 persons registered)
- (Small) funding by LIA TYL/FJPPL => Structuring of French-Japanese Collaboration
- Sessions at Linear Collider Meetings
- Presence at international conferences



ILC design parameters	
$\sqrt{s}$	91-500 GeV
$\mathcal{L}$	$2 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$
$P_{e^-}$	>80%
$P_{e^+}$	upto 30%
Length	~31 km

## Comment

500 GeV is baseline  
Option to upgrade to 1 TeV

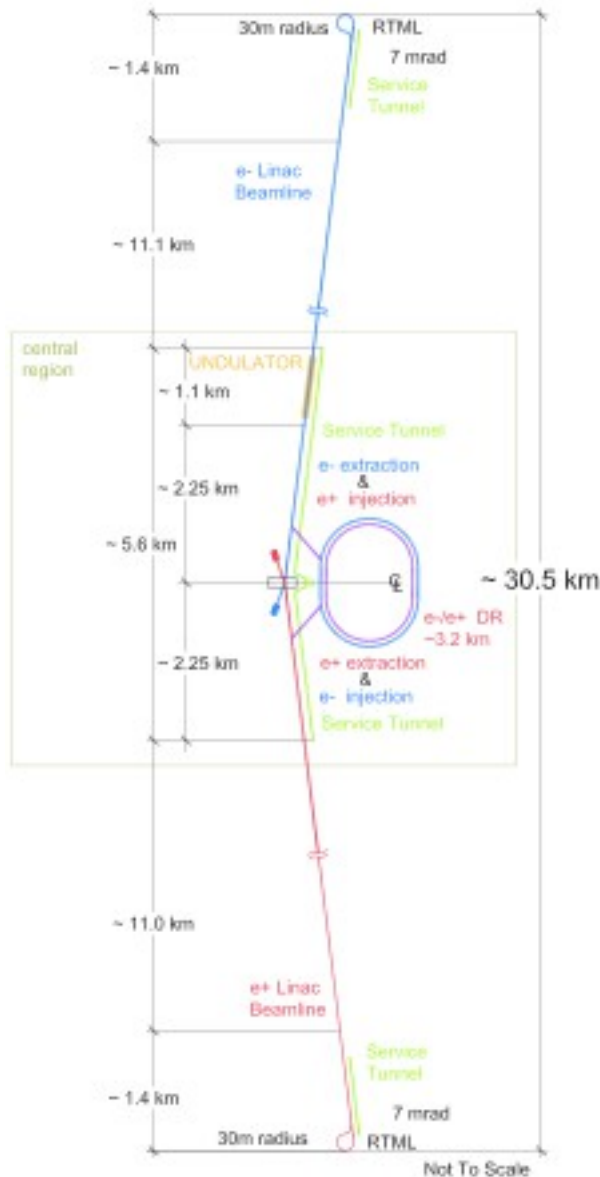
~Factor 4 technically possible

Proven by SLC

~Conservative estimate

Current site allows for 50km

- Discussion on possible running scenarios has started
- Luminosity and running time to achieve at a ~25 years research programme  
That includes running at 250 GeV, 350 GeV, 500 GeV and 1 TeV
- No official statement yet but integrated luminosities indicated in following transparencies are realistic



## • SCRF Technology

- 1.3GHz SCRF with 31.5 MV/m
- 17,000 cavities
- 1,700 cryomodules
- 2×11 km linacs

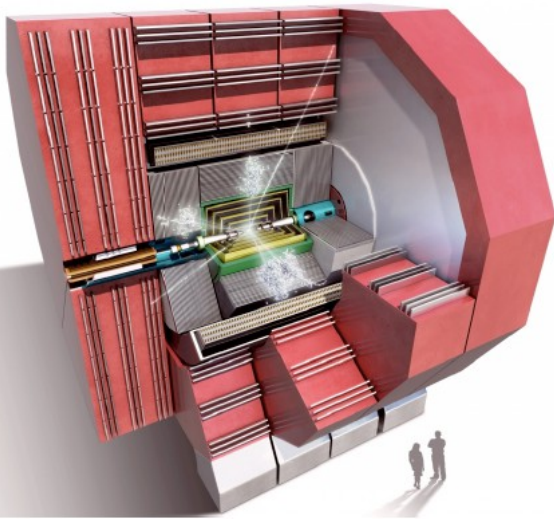
## Luminosity

$$L \propto \frac{\eta_{RF} P_{RF}}{E_{cm}} \sqrt{\frac{\delta_{BS}}{\epsilon_{n,y}}} H_D$$

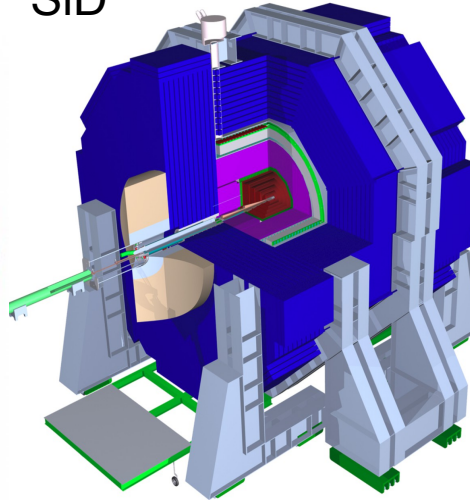
$\eta_{RF} \sim 40\%$  for SCRF technology

**-> efficient technology**

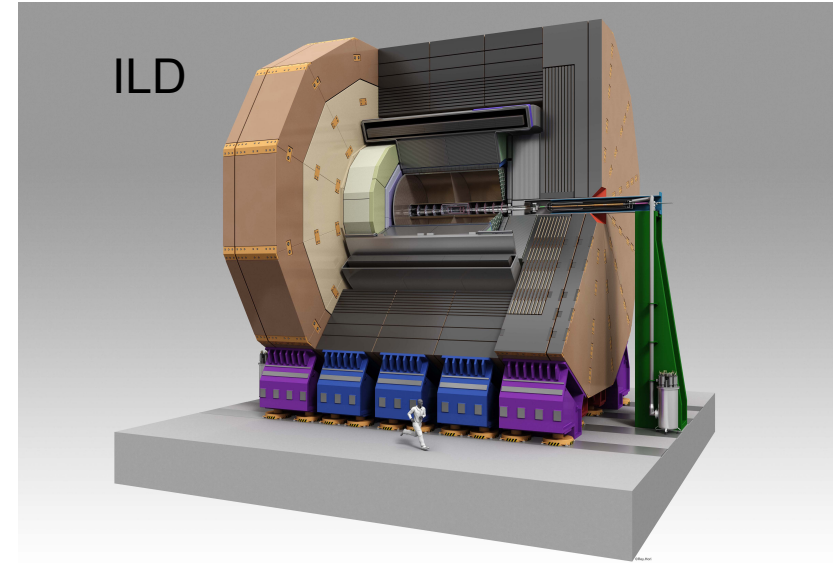
CLIC Detector



SiD



ILD



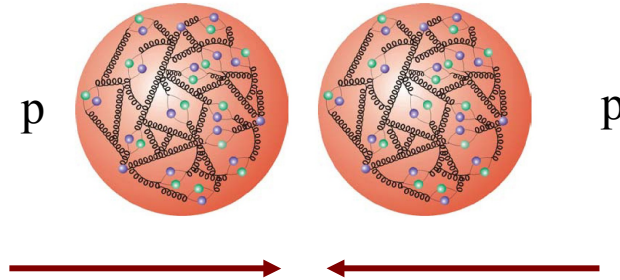
Highly granular calorimeters  
 Central tracking  
 with silicon  
 Inner tracking with silicon

Central tracking  
 with TPC

- CDR 2012  
 Revised since

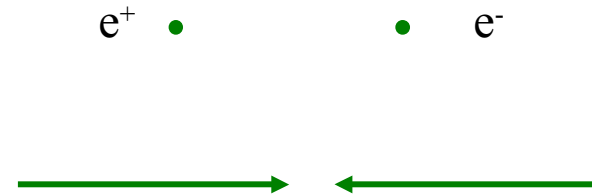
- LOI's Validated by IDAG in 2009  
 - Publication of **D**etector **B**aseline **D**esign in 2013, together with TDR

Concepts based on input from physics studies and detector R&D organised in R&D collaborations



## Proton:

Composed particle (hadron)  
 Unknown energy of collision partners  
 Parasitic reactions  
 Strong interaction  
 => Considerable physics background  
 Advantage: Scan of energy  
 Range within one experiment



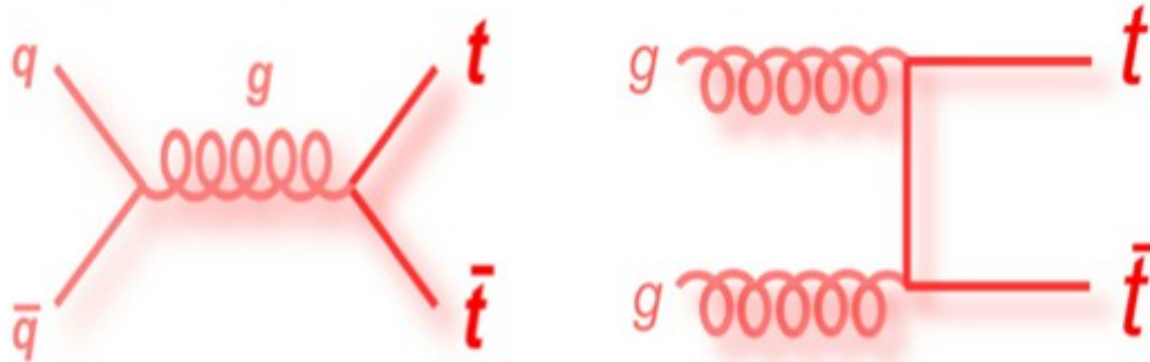
## Electron:

Elementary particle  
 Well known and adjustable energy of collision partners  
  
 Each energy point needs a New set of machine parameters  
  
**High precision measurements**

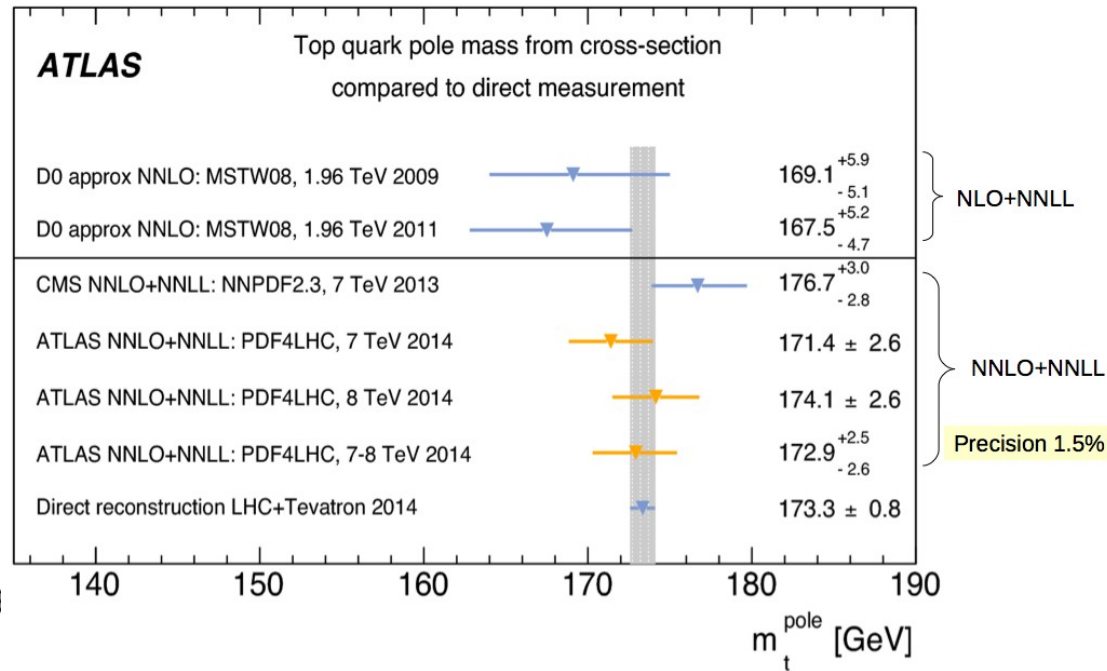
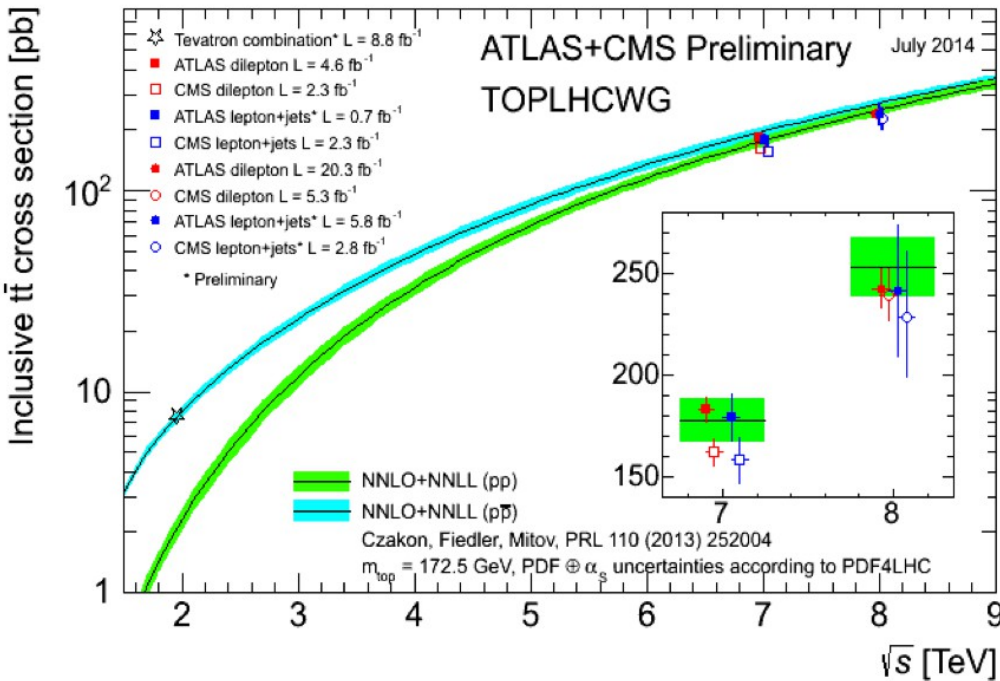




Example diagrams:



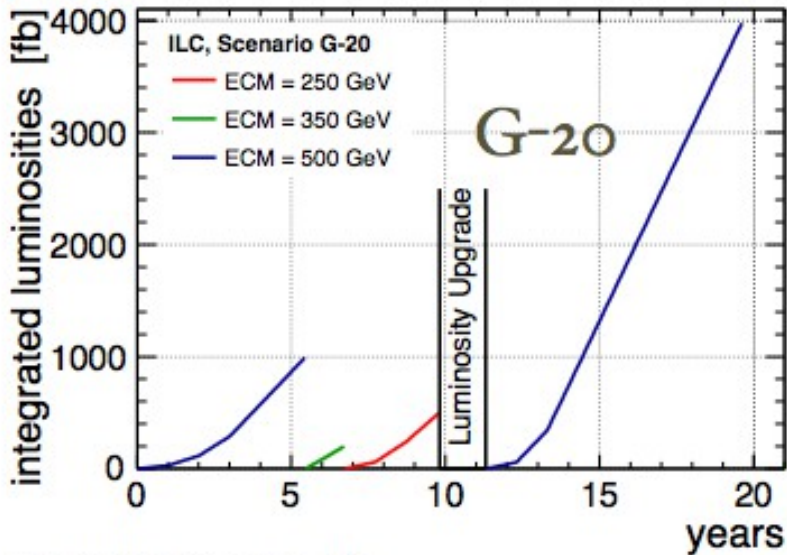
	$\sigma_{gg}/\sigma_{tot}$
Tevatron	$\approx 15\%$
LHC 7 TeV	$\approx 85\%$
LHC 14 TeV	$\approx 90\%$



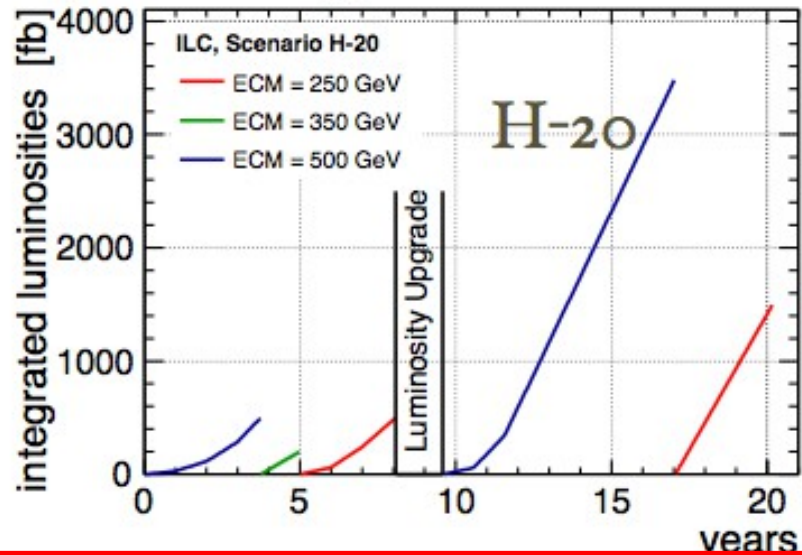
=> High time to see them at lepton colliders!



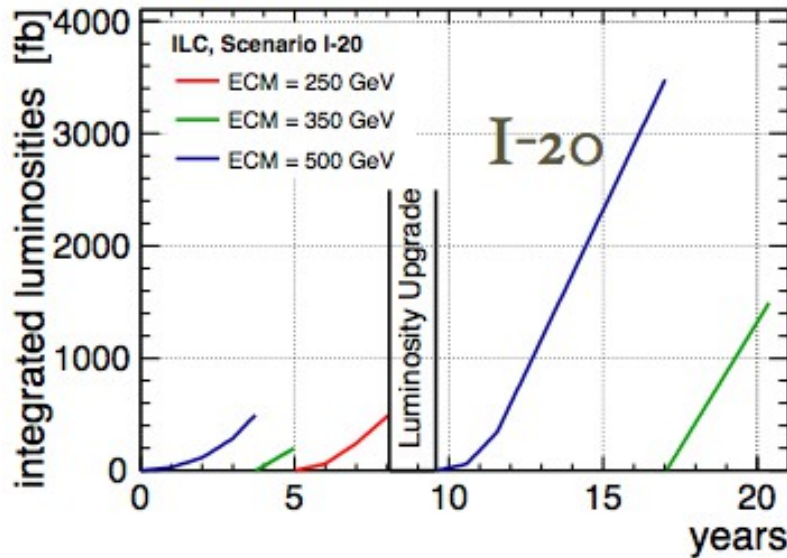
Integrated Luminosities [fb]



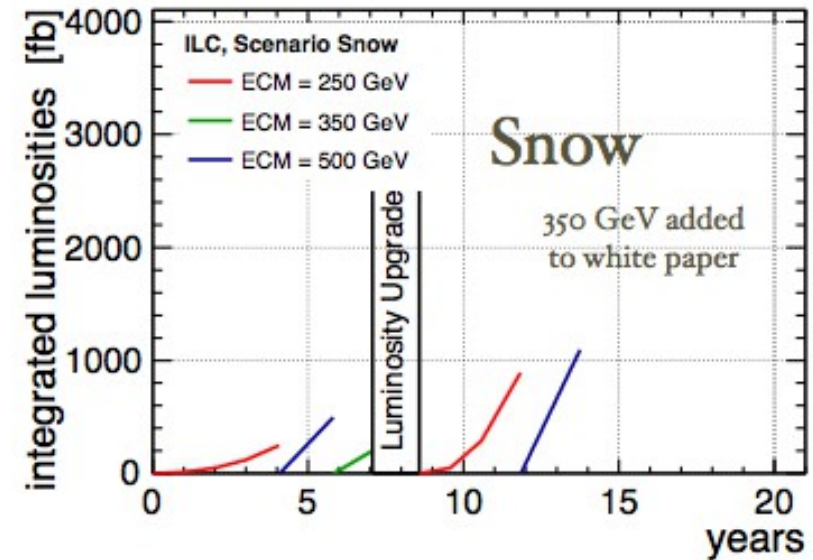
Integrated Luminosities [fb]



Integrated Luminosities [fb]



Integrated Luminosities [fb]



type	final state	$\sigma$ 500 GeV	$\sigma$ 352 GeV
Signal ( $m_{\text{top}} = 174$ GeV)	$t\bar{t}$	530 fb	450 fb
Background	$WW$	7.1 pb	11.5 pb
Background	$ZZ$	410 fb	865 fb
Background	$q\bar{q}$	2.6 pb	25.2 pb
Background	$WWZ$	40 fb	10 fb

## Remarks:

- LC will have polarised beams

=>  $(\sigma_{t\bar{t}})_L \sim 1565\text{fb}^{-1}$ ,  $(\sigma_{t\bar{t}})_R \sim 724\text{fb}^{-1}$  at 500 GeV

- Background varies differently with polarisations

e.g.  $WW$ -Background  $\rightarrow 26000\text{fb}^{-1}$  for  $e_L$  and  $150\text{fb}^{-1}$  for  $e_R$



- The top quark is the heaviest known elementary particle  
Discovery in 1995 at Tevatron
- $m_t \sim 173 \text{ GeV}$  ( $\sim m$  of Gold atom)
- Electrical charge  $Q_t = 2/3$
- Spin  $1/2 \Rightarrow$  fermion
- Lifetime  $\tau \sim 5 \times 10^{-25} \text{ s}$   
(SM decays)
- Total width  $\Gamma_t \sim 1.5 \text{ GeV}$
- No hadronisation, behaves like a free quark
- Predominant decays  
 $t \rightarrow Wb$  (BR $\sim 100\%$ )

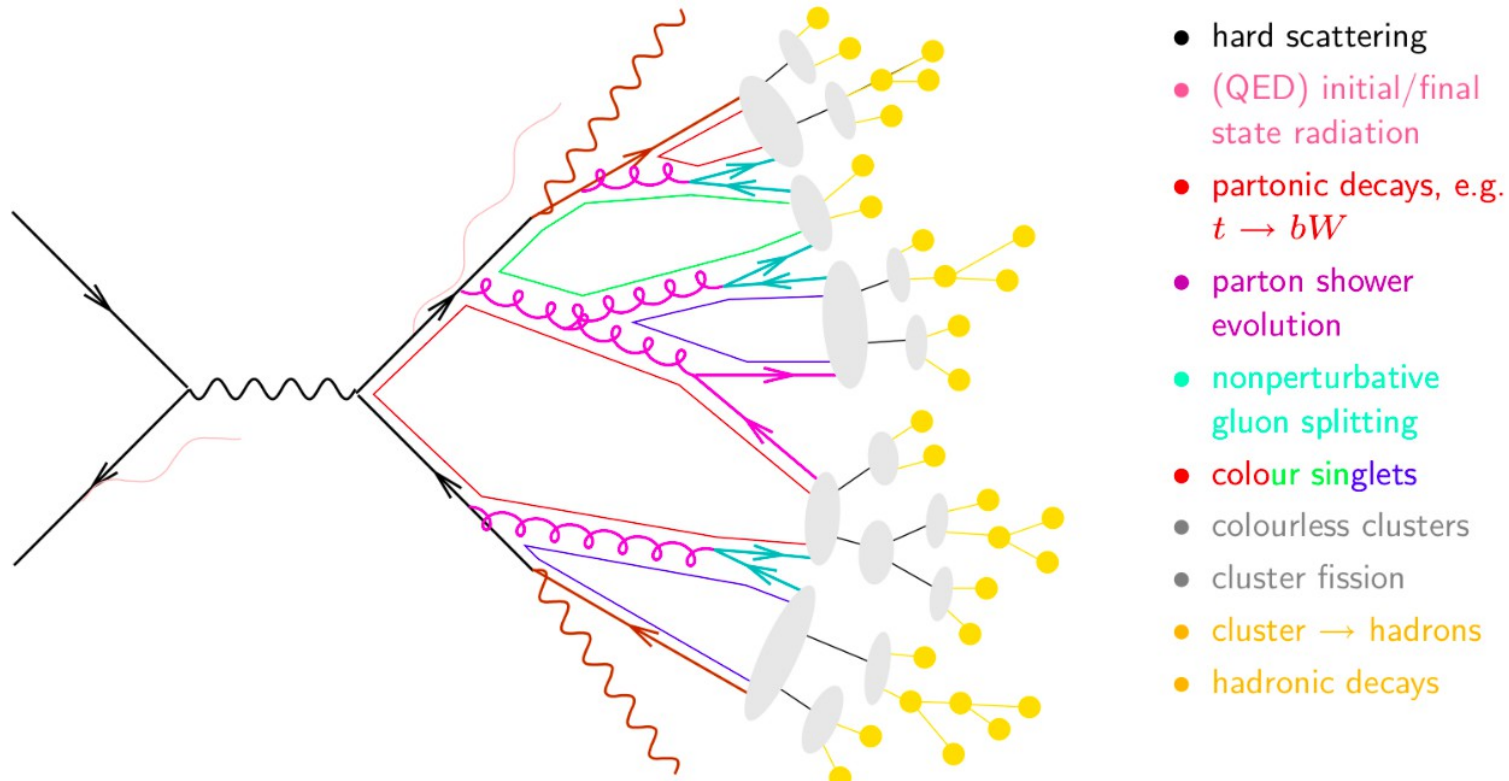
LEPTONS		
Electron Neutrino Mass -0	Muon Neutrino -0	Tau Neutrino -0
Electron .511	Muon 105.7	Tau 1 777
QUARKS		
Up Mass: 5	Charm 1 500	Top ~180 000
Down 8	Strange 160	Bottom 4 250



*Top quark  
Ideal object for  
a machine in Japan ;-)*

*Slide inspired by Lecture of  
Prof. K. Jakobs, Uni Freiburg*

## Extraction of top mass from invariant jet masses (Typical for hadron colliders)



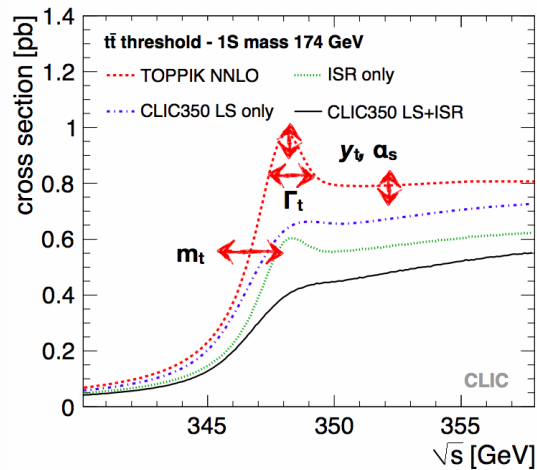
- MC Mass: Mass of (on-shell) top propagator prior to decay  $\Rightarrow$  Pole mass

- Pole mass theoretically unsafe when precision reaches  $O(\Lambda_{\text{QCD}} \sim 1 \text{ GeV})$

(Non absorption of soft virtual corrections)

Stat. Error ( $m_t, \Gamma_t$ :MeV/ $y_t$ :%)	6-Jet			4-Jet		
	$m_t^{PS}$	$\Gamma_t$	$y_t$	$m_t^{PS}$	$\Gamma_t$	$y_t$
Left(50fb <sup>-1</sup> )	47	65	9.6	52	71	11
Right(50fb <sup>-1</sup> )	68	94	14	75	106	16
Left (50fb <sup>-1</sup> ) + Right(50fb <sup>-1</sup> )	<b>39</b>	<b>53</b>	<b>7.9</b>	<b>43</b>	<b>59</b>	<b>9.1</b>

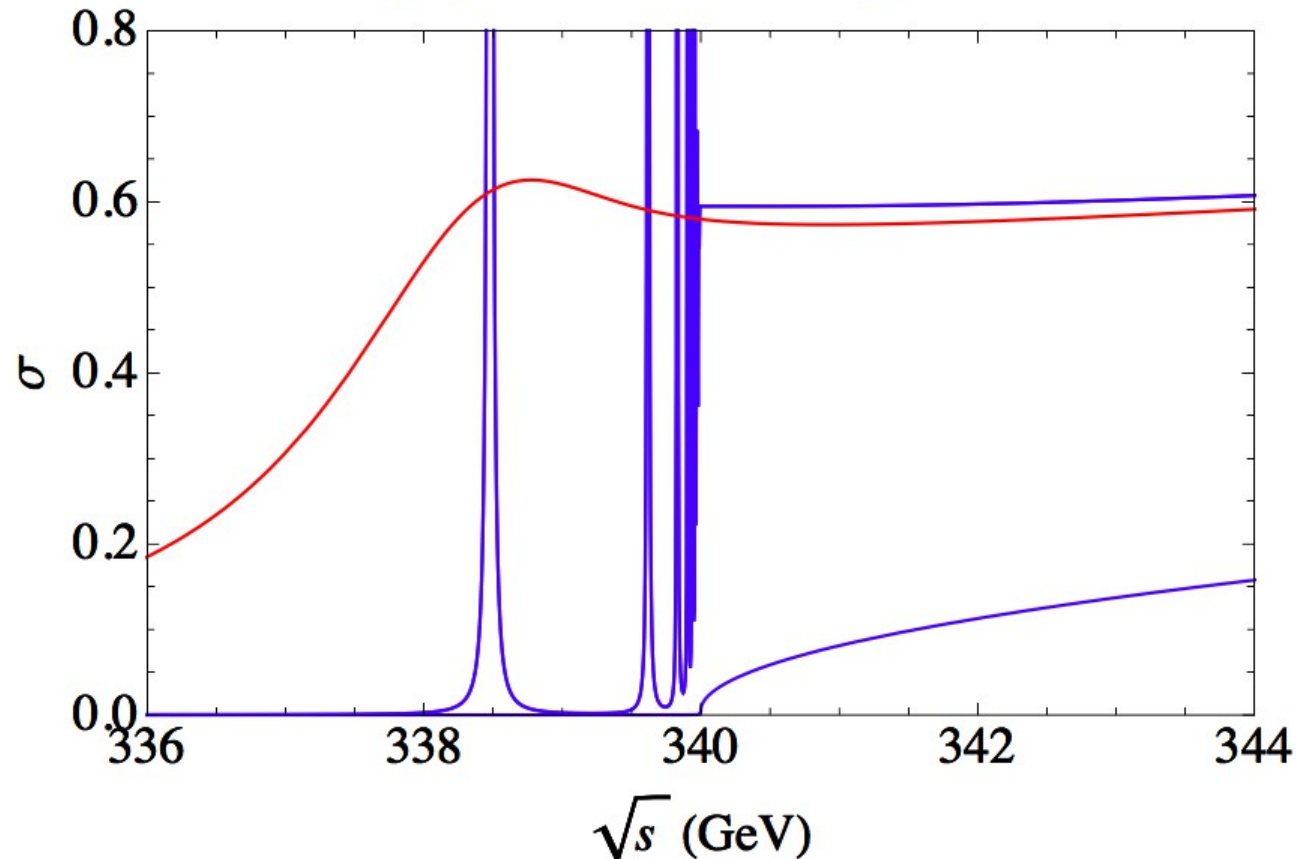
Update of: arxiv 1310.0563



Combined ALL		
$m_t^{PS}$ (GeV)	$\Gamma_t$ (GeV)	$y_t$
$172 \pm 0.029$	$1.4 \pm 0.039$	<b>5.9 %</b>

- Competitive determination of three parameters
- $y_t$  suffers however from large theory uncertainties (~20%)  
=> Indirect determination may not be conclusive
- Systematic studies on e.g. beam spectrum ongoing  
Important for top width

“Bound states” at tt threshold  
**Hydrogen atom of strong interaction**

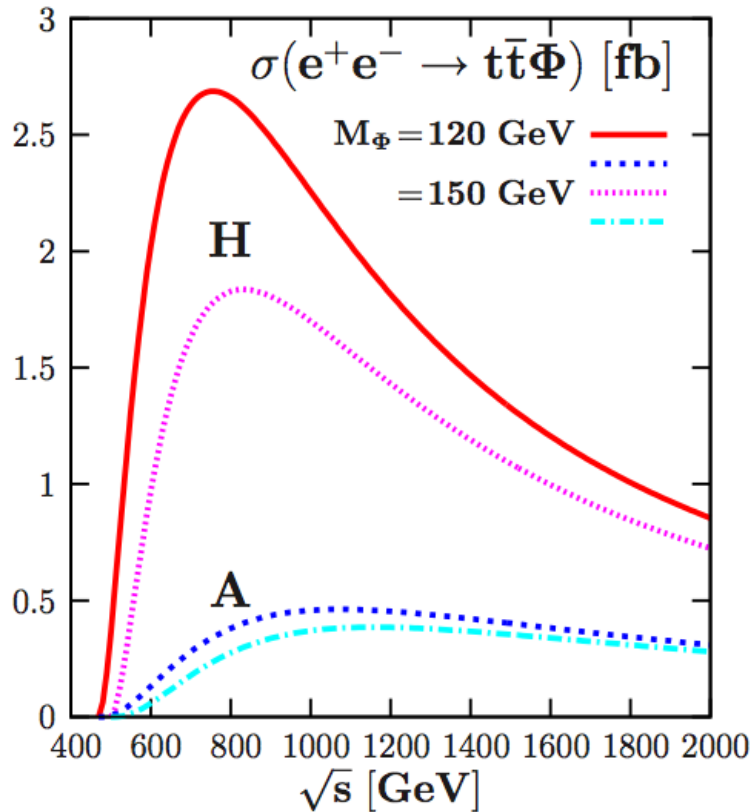


- Size  $O(10^{-17}\text{m})$ , **smallest object known in particle physics**  
 Small scale => Free of confinement effects => Ideal premise for precision calculations  
 Measurement of (a hypothetical)  $1^3S_1$  State
- Decay of top quark smears out resonances in a well defined way

- Expected statistical uncertainty **10 – 30 MeV**
- Experimental systematics
  - Beam energy: **~30 MeV** or lower
  - Non-ttbar background, selection efficiencies (Assuming < 5% background uncertainty, 0.5% knowledge on signal selection): **~ 15 MeV**
  - Luminosity spectrum (studied for CLIC LS with reconstruction of spectrum via Bhabha
  - Scattering, scaling from 3 TeV studies, full study on the way): **10 MeV**
  - Single top contamination: **< 30 MeV**
- Theory uncertainties
  - Normalisation: **~55 MeV (naive estimate)** much smaller due to recent NNNLO calculations
  - When not included in the fit:  $\sim 3 \text{ MeV per } 10^{-4} \text{ uncertainty on } \alpha_s \text{ today} \rightarrow \text{~18 MeV}$
  - Conversion from 1S/PS masses to MSbar mass Currently: **~50 MeV**  
However conversion now known to N<sup>4</sup>NLO
  - Now at point where results become sensitive to effects other than QCD

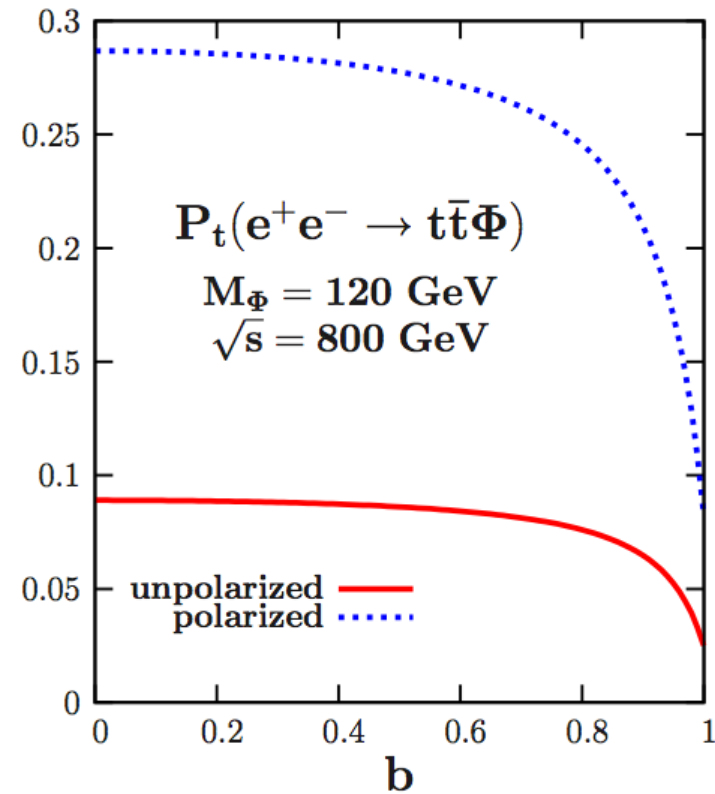
Direct coupling of top quark to CP odd and CP even scalar

Cross section



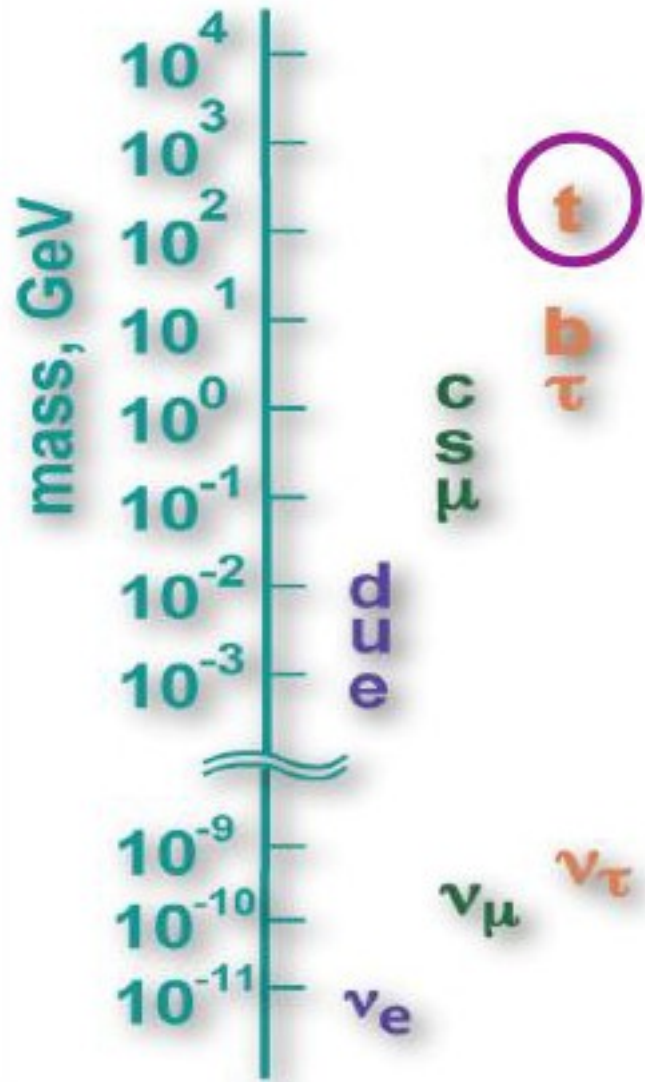
Dramatic differences for  
CP odd and CP even scalar

Top quark polarisation



Sensitivity to CP odd admixture  $b$   
Merit of beam polarisation

Determination of CP nature of scalar boson in an unambiguous way

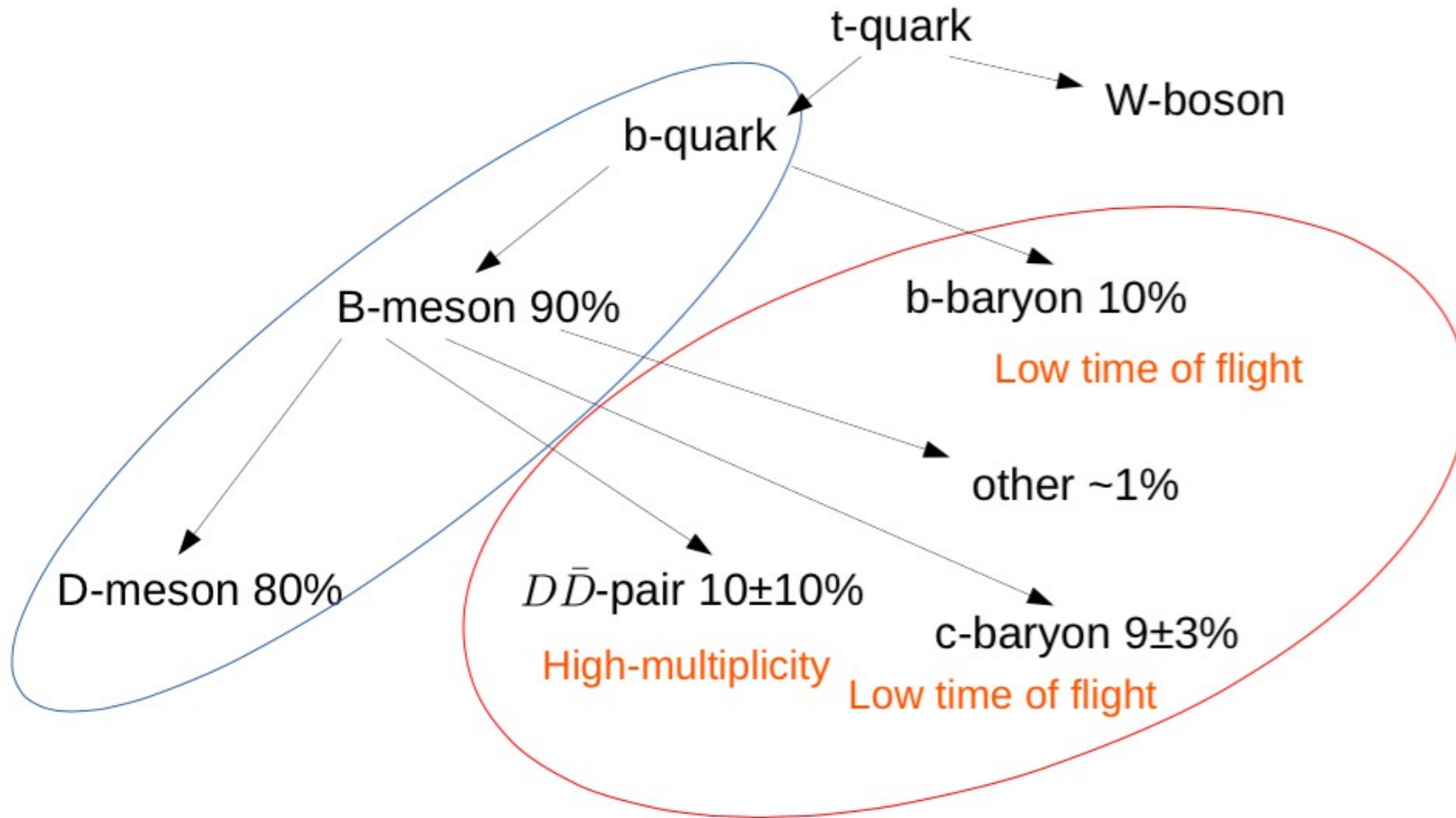


- SM does not provides no explanation for mass spectrum of fermions (and gauge bosons)
- Fermion mass generation closely related to the origin electroweak symmetry breaking
- Expect residual effects for particles with masses closest to symmetry breaking scale
  - $A_{FB}$  anomaly at LEP for b quark

Strong motivation to study chiral structure of top vertex in high energy e+e- collisions



- Hadronization and decay modes of b-quark:

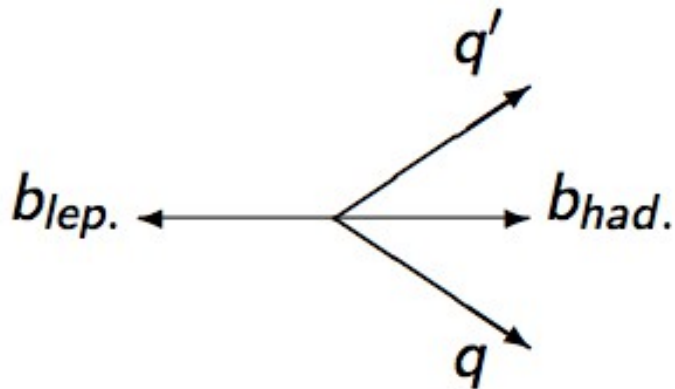


4

> 70% of the tops lead to “straightforward” reconstructable final states  
Exploiting this observation is subject of PhD thesis at LAL

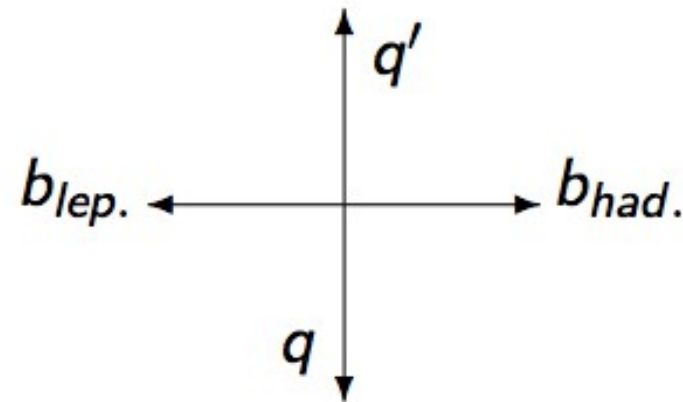
Collaboration within French-Japanese TYL/FJPPL research programme

- To measure  $A_{FB}$  in fully hadronic decays there is no choice
- In semi-leptonic decays there is the charged lepton but ....



Right handed electron beam:

- mainly right handed tops  
In final state (V-A)
- Hard W in flight direction of Top and soft b's
- Flight direction of t from flight direction of W

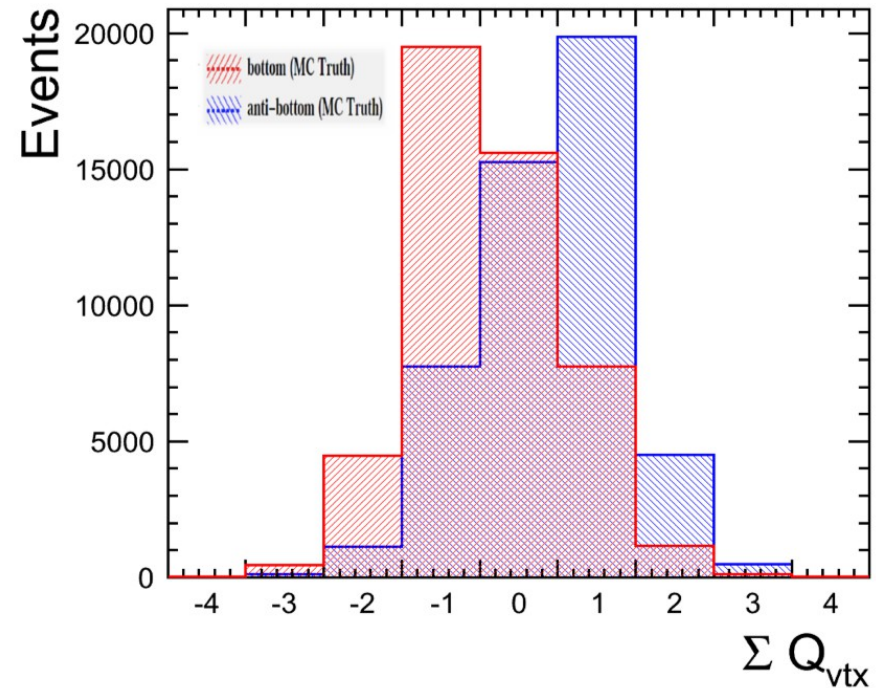
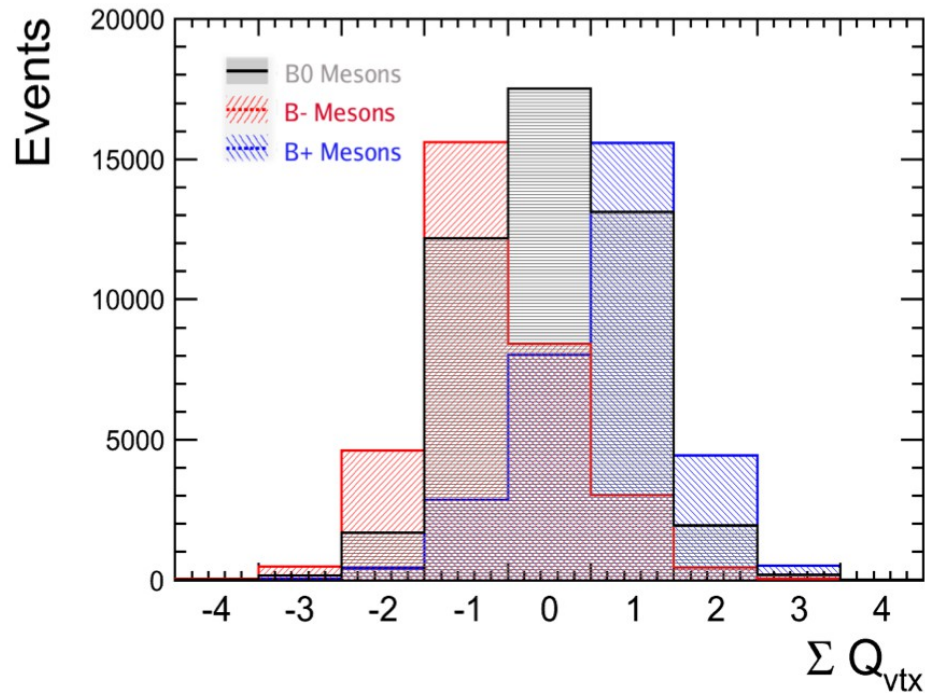


Left handed electron beam:

- mainly left handed tops
- Hard b in flight direction of Top and soft W's
- Flight direction of t from flight direction of b  
=> Wrong association ↔ top flip

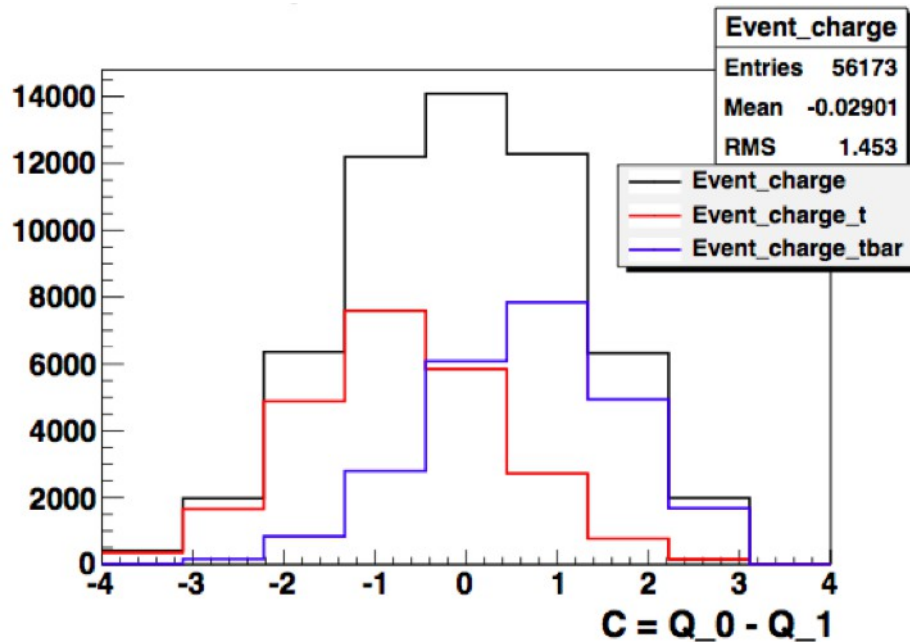
Measurement of b-charge to resolve ambiguities

(N.B. At example of fully hadronic analysis, PhD M.S. Amjad)



- LC vertex and tracking system should allow for determination of b-meson (b-quark) charge
- B-quark charge measured correctly in about 60% of the cases  
Can be increased to 'arbitrary' purity on the expense of smaller statistics
- However ~25% are “accidentally” correct measurements
- LC software (LCFIPlus package) not yet optimised for vertex charge measurement

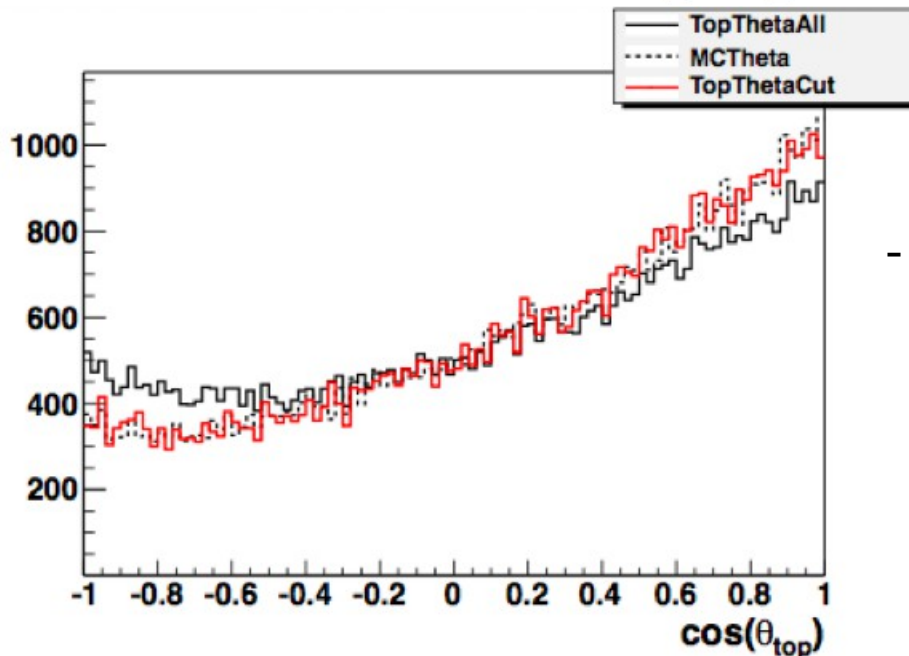
Optimisation of b-quark charge is major topic in ongoing studies and real challenge of LC detectors



Event charge  $C = b_1 - b_2$

In SL can compare charge  $C$  with lepton charge to select clean sample

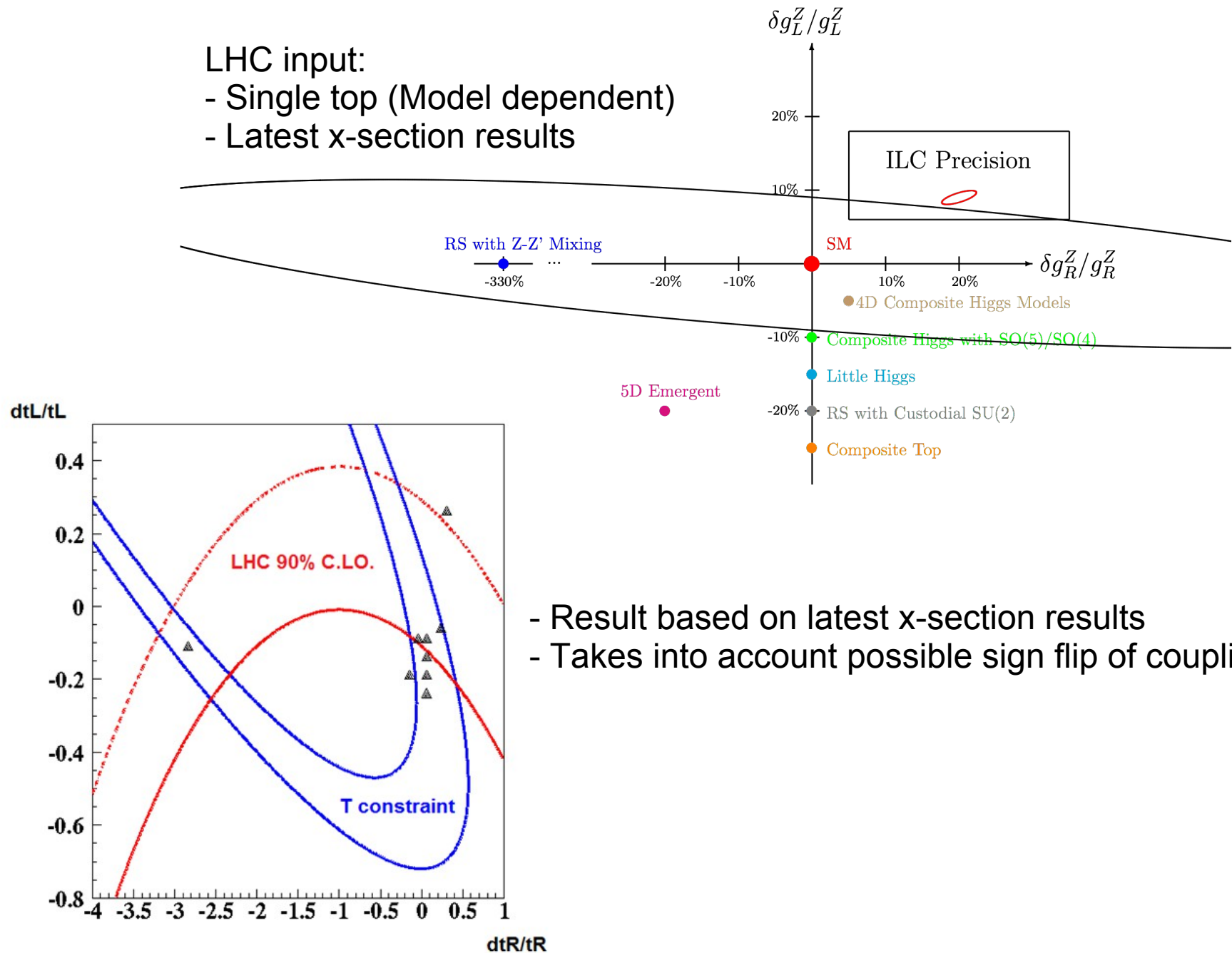
Use only events with correct  $C$  or  $C=0$   
(plus another cut on the Lorentz Factor)



- Clean reconstruction of top quark direction  
 $\epsilon \sim 30\%$   
Will improve with improving charge reconstruction

# Comparison with current LHC results

LHC input:  
 - Single top (Model dependent)  
 - Latest x-section results



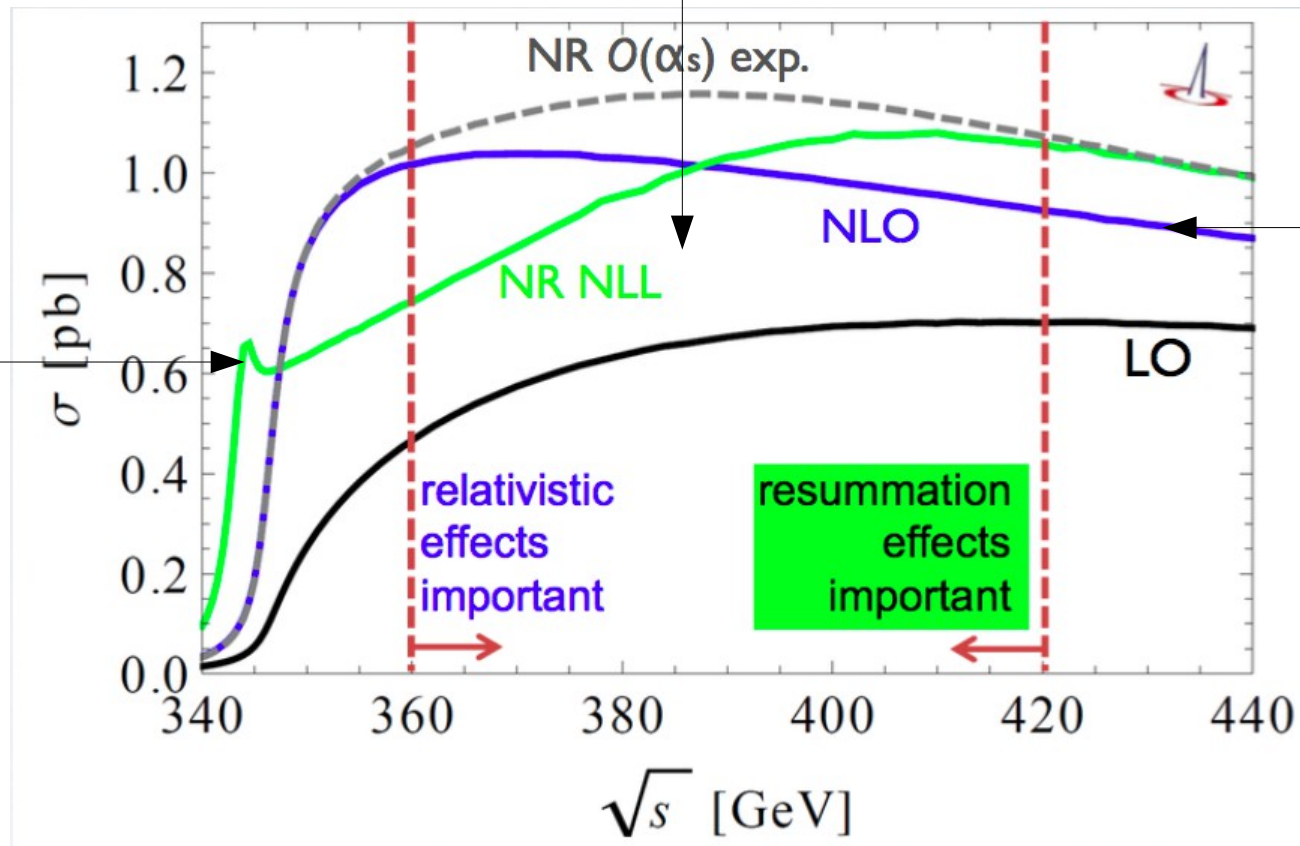
- Result based on latest x-section results  
 - Takes into account possible sign flip of couplings



# Complicated transition region

Transition region  
Difficult to match non-relativistic QCD at threshold  
With relativistic QCD in continuum

Threshold region  
Theoretically  
well under control



Continuum  
Theoretically  
well under control

Considerable theory uncertainties suggest  
to avoid transition region for precision physics

Study by Francois Richard

## Higgs sector

- It should be noted that for what concerns the Higgs sector (non-minimal) contribution there could be a much larger enhancement for the 3d generation  $\mathbf{df} \sim \mathbf{m}^3 \mathbf{f}$  at one-loop
- Higgs exchange is larger near threshold and the sensitivity for  $\text{Re}(F2A)$  drops to 0 at 500 GeV

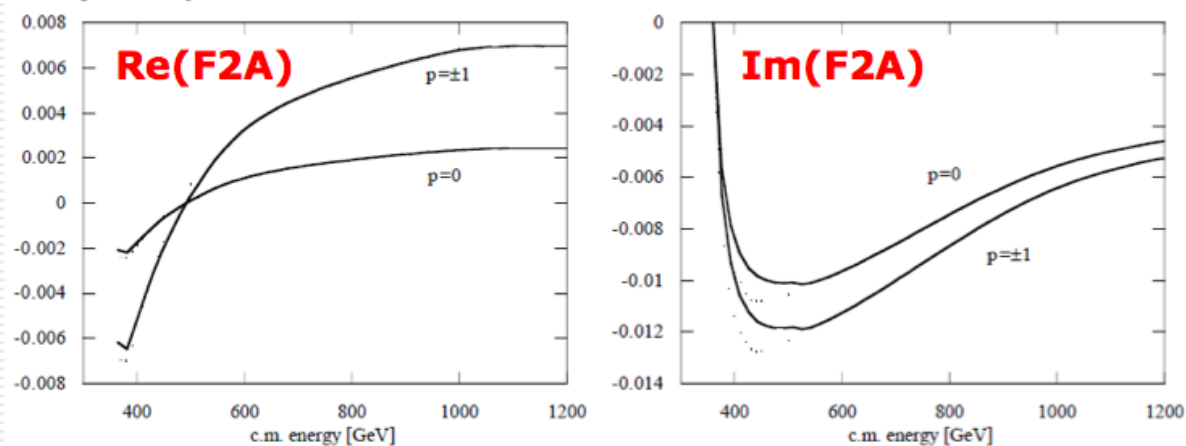
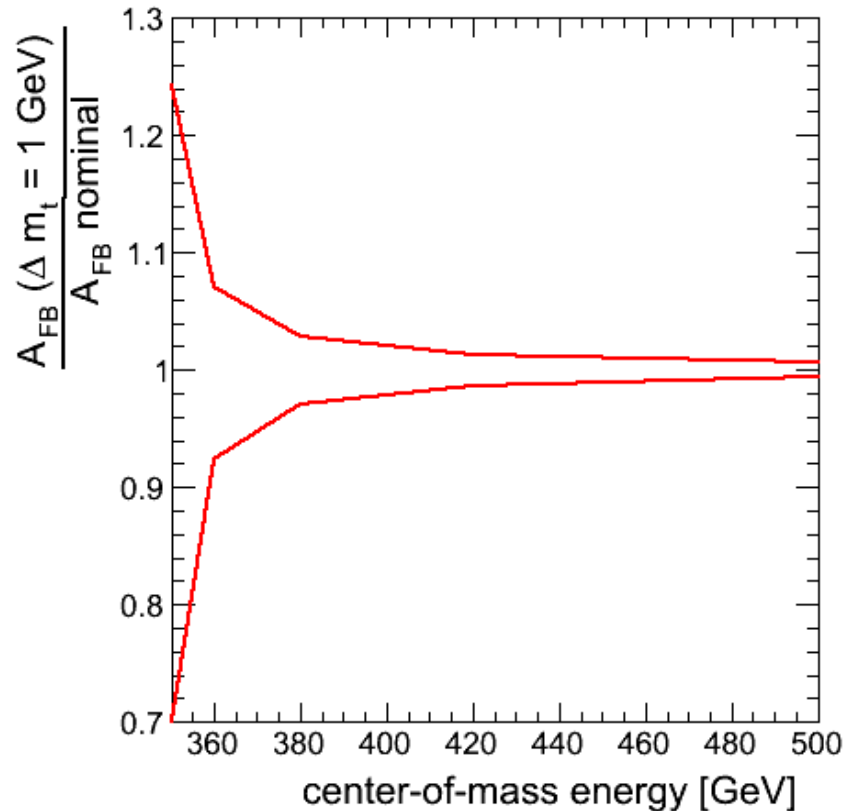


Fig 1: Ratios  $r_1$  (left figure) and  $r_2$  (right figure) for the optimized dispersive and absorptive observables  $\mathcal{O}_{\pm}(i)$ ,  $i = 1, 2$  defined in [6] for  $m_t = 180$  GeV,  $m_{\varphi_1} = 100$  GeV, and  $\gamma_{CP} = 1$ .

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Exchange of CP Violating Higgs is most probable source of CP violation  
In  $t\bar{t}$  production (dixit Werner Bernreuther)





## Influence of the top quark mass on x-sec and $A_{\text{FB}}$

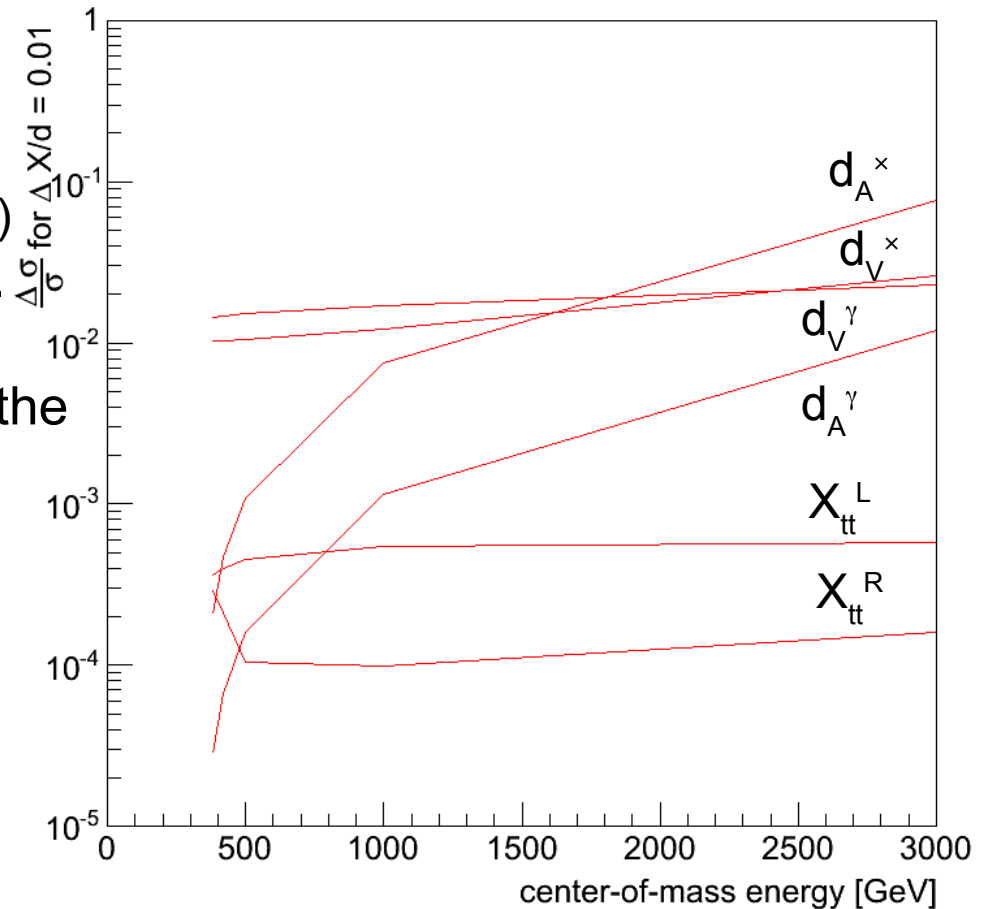
- very pronounced below  $\sqrt{s} = 360$  GeV
- 2.9%/GeV at  $\sqrt{s} = 380$  GeV
- 1.3%/GeV at  $\sqrt{s} = 420$  GeV
- 0.6%/GeV at  $\sqrt{s} = 500$  GeV

With the assumption of a 100 MeV pole mass measurement at threshold, the remaining uncertainty is one per mil or less above 420 GeV

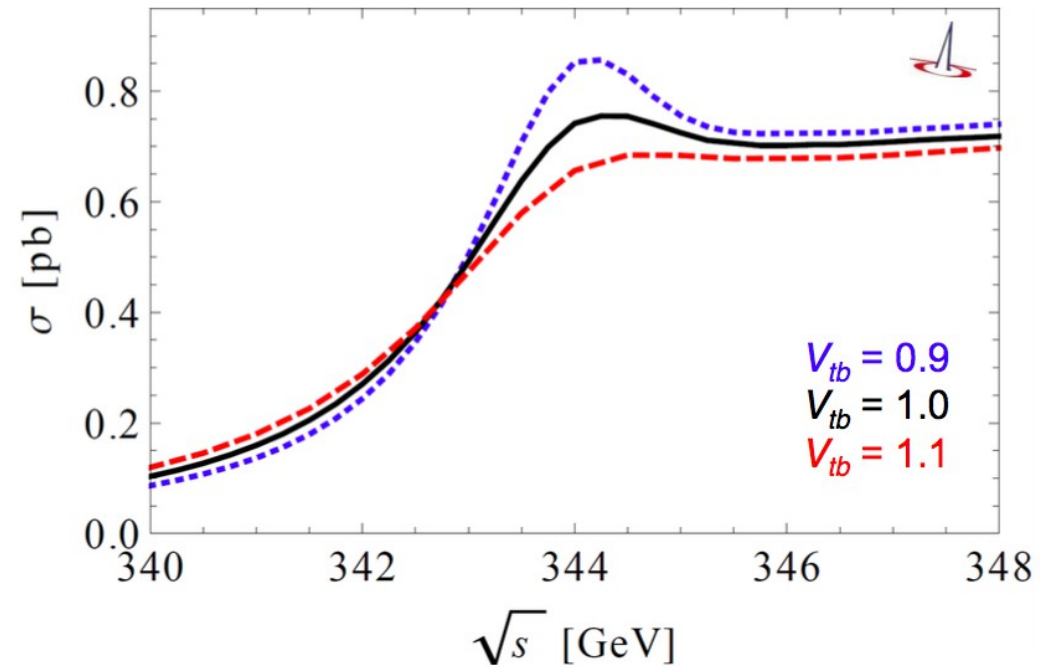
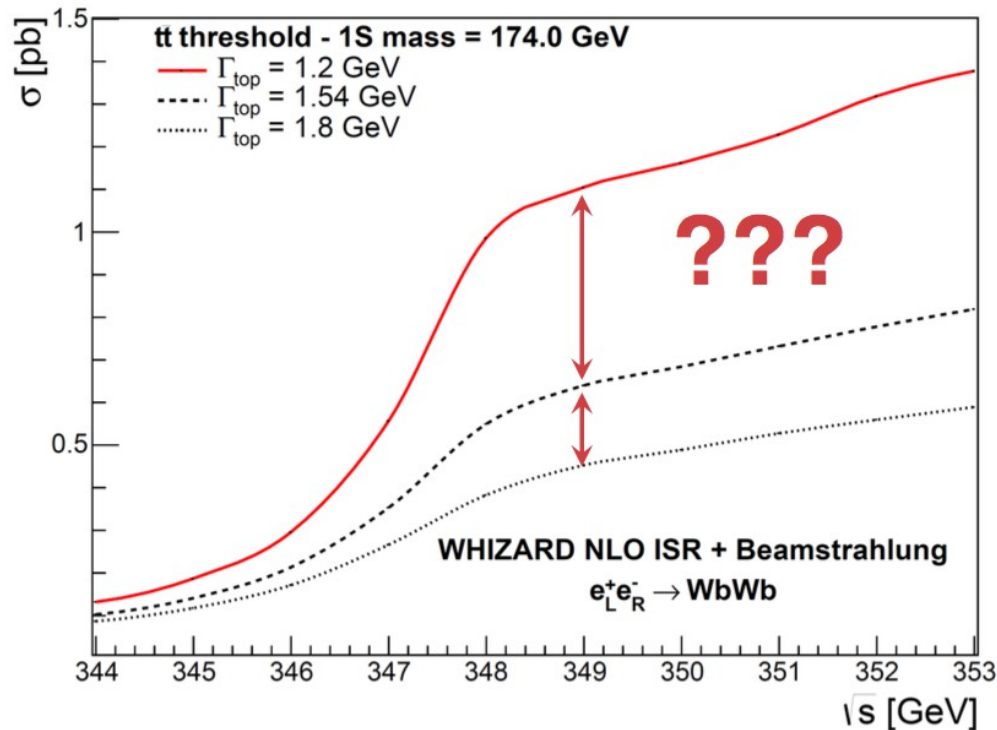
Dimension 6 effective operators  
 (~equivalent role to anomalous form factors)  
 have been implemented in WHIZARD...

Allow to map the dependence on  $\sqrt{s}$  of the  
 impact of new physics on given  
 observable

May help to explore the sensitivity of  
 new/additional observables



## Study with WHIZARD generator



- “Erratic” behaviour of theory prediction when using  $\Gamma_t$  as free parameter
- Using  $V_{tb}$  as free parameter leads to more benign behaviour

Experimentally observable final state requires proper definition of theory parameters

For details see arxiv: 1503.04247

Basic idea: Final state top polarisation contains information about factors

$$\begin{aligned}
 \mathcal{M}(e_L \bar{e}_R \rightarrow t_L \bar{t}_R)^{\gamma/Z} &= c_L^{\gamma/Z} [F_{1V}^{\gamma/Z} - \beta F_{1A}^{\gamma/Z} + F_{2V}^{\gamma/Z}] (1 + \cos \theta) e^{-i\phi} \\
 \mathcal{M}(e_L \bar{e}_R \rightarrow t_R \bar{t}_L)^{\gamma/Z} &= c_L^{\gamma/Z} [F_{1V}^{\gamma/Z} + \beta F_{1A}^{\gamma/Z} + F_{2V}^{\gamma/Z}] (1 - \cos \theta) e^{-i\phi} \\
 \mathcal{M}(e_L \bar{e}_R \rightarrow t_L \bar{t}_L)^{\gamma/Z} &= c_L^{\gamma/Z} \gamma^{-1} [F_{1V}^{\gamma/Z} + \gamma^2 (F_{2V}^{\gamma/Z} + \beta F_{2A}^{\gamma/Z})] \sin \theta e^{-i\phi} \\
 \mathcal{M}(e_L \bar{e}_R \rightarrow t_R \bar{t}_R)^{\gamma/Z} &= c_L^{\gamma/Z} \gamma^{-1} [F_{1V}^{\gamma/Z} + \gamma^2 (F_{2V}^{\gamma/Z} - \beta F_{2A}^{\gamma/Z})] \sin \theta e^{-i\phi} \\
 \mathcal{M}(e_R \bar{e}_L \rightarrow t_L \bar{t}_R)^{\gamma/Z} &= -c_R^{\gamma/Z} [F_{1V}^{\gamma/Z} - \beta F_{1A}^{\gamma/Z} + F_{2V}^{\gamma/Z}] (1 - \cos \theta) e^{i\phi} \\
 \mathcal{M}(e_R \bar{e}_L \rightarrow t_R \bar{t}_L)^{\gamma/Z} &= -c_R^{\gamma/Z} [F_{1V}^{\gamma/Z} + \beta F_{1A}^{\gamma/Z} + F_{2V}^{\gamma/Z}] (1 + \cos \theta) e^{i\phi} \\
 \mathcal{M}(e_R \bar{e}_L \rightarrow t_L \bar{t}_L)^{\gamma/Z} &= c_R^{\gamma/Z} \gamma^{-1} [F_{1V}^{\gamma/Z} + \gamma^2 (F_{2V}^{\gamma/Z} + \beta F_{2A}^{\gamma/Z})] \sin \theta e^{i\phi} \\
 \mathcal{M}(e_R \bar{e}_L \rightarrow t_R \bar{t}_R)^{\gamma/Z} &= c_R^{\gamma/Z} \gamma^{-1} [F_{1V}^{\gamma/Z} + \gamma^2 (F_{2V}^{\gamma/Z} - \beta F_{2A}^{\gamma/Z})] \sin \theta e^{i\phi}
 \end{aligned}$$

=> different sensitivities in different individual matrix elements:

$$\omega_i = \frac{\partial |\mathcal{M}|^2(\alpha)}{\partial \alpha_i} \Big|_{\alpha^0} \frac{1}{|\mathcal{M}|^2(\alpha^0)} \quad \text{For each } \alpha_i \text{ (=FF) there is one (measurable) } \omega_i$$

Using full matrix element information -> Full event reconstruction

$$d\text{Lips} \propto d \cos \theta_t \, d \cos \theta_b \, d\phi_b \, d \cos \theta_{\bar{b}} \, d\phi_{\bar{b}} \, d \cos \theta_{l+} \, d\phi_{l+} \, d \cos \theta_{l-} \, d\phi_{l-} \, dq_t^2 \, dq_{\bar{t}}^2 \, dq_W^2$$

Parton level analysis (with GRACE generator) using fully leptonic final state

Simultaneous extraction of 10 FF **including CP violating FFs**

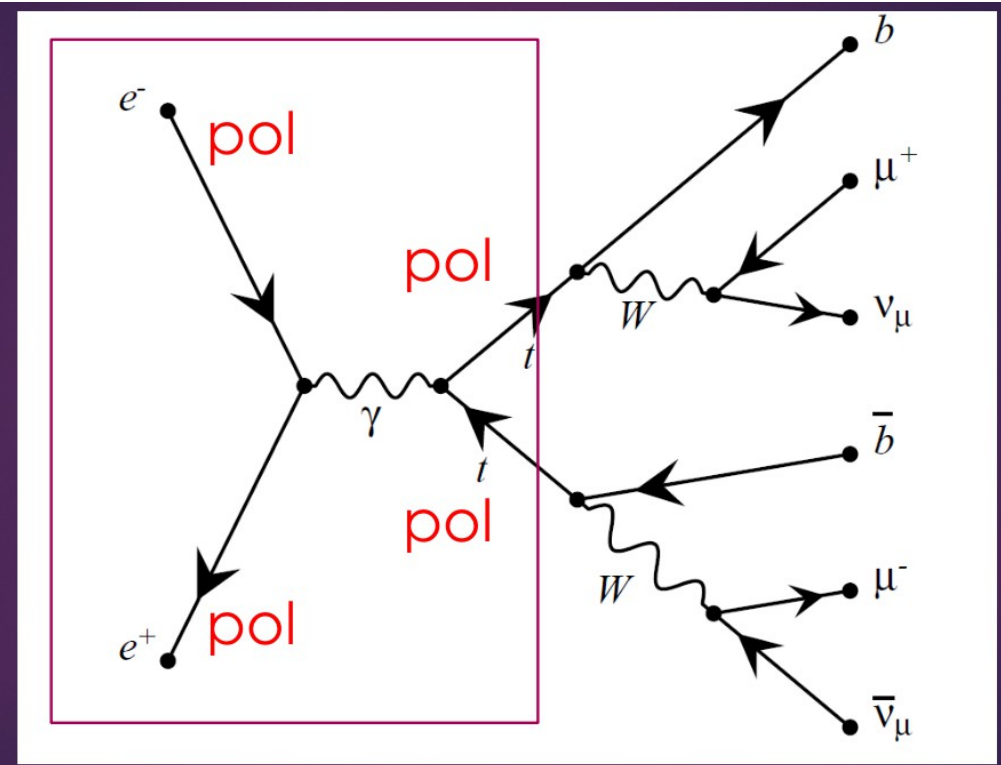
$\mathcal{R}e \delta \tilde{F}_{1V}^\gamma$	$\mathcal{R}e \delta \tilde{F}_{1V}^Z$	$\mathcal{R}e \delta \tilde{F}_{1A}^\gamma$	$\mathcal{R}e \delta \tilde{F}_{1A}^Z$	$\mathcal{R}e \delta \tilde{F}_{2V}^\gamma$	$\mathcal{R}e \delta \tilde{F}_{2V}^Z$	$\mathcal{R}e \delta \tilde{F}_{2A}^\gamma$	$\mathcal{R}e \delta \tilde{F}_{2A}^Z$	$\mathcal{I}m \delta \tilde{F}_{2A}^\gamma$	$\mathcal{I}m \delta \tilde{F}_{2A}^Z$
0.0037	-0.18	-0.09	+0.14	+0.62	-0.15	0	0	0	0
	0.0063	+0.14	-0.06	-0.13	+0.61	0	0	0	0
		0.0053	-0.15	-0.05	+0.09	0	0	0	0
			0.0083	+0.06	-0.04	0	0	0	0
				0.0105	-0.19	0	0	0	0
					0.0169	0	0	0	0
						0.0068	-0.15	0	0
							0.0118	0	0
								0.0069	-0.17
									0.0100

No particular improvement through beam polarisation

- No background, no smearing
- Needs experimental study – You?

Collaboration within French-Japanese TYL/FJPPL research programme

Elw. Corrections for polarised beams



Target:

- $e^+e^- \rightarrow t\bar{t} \rightarrow b\bar{b}f\bar{f}f\bar{f}$  @ ILC
- Full  $O(\alpha)$  electroweak corrections
- Beam polarization effects
- Finite width effects of top-quarks
- Matrix elements
- Event generation ?
- $O(\alpha^2)$  electroweak corrections ???

**Goal for accuracy < 1%**

Collaboration within French-Japanese TYL/FJPPL research programme

- **Luminosity:** Critical for cross section measurements  
Expected precision 0.1% @ 500 GeV
- **Beam polarisation:** Critical for asymmetry measurements  
Expected to be known to 0.1% for e- beam  
and 0.35% for e+ beam
- **Migrations/Ambiguities:** Critical for  $A_{FB}$ :  
PFLOW important for selection of 'clean events' but maybe subleading w.r.t. jet clustering  
**Control of b charge is most relevant topic !!!!**
- **Other effects:** b-tagging, passive material etc.  
LEP1 claims 0.2% error on  $R_b$  -> guiding line for LC

## Under discussion with theory groups:

- Consideration full 6f final state (Interference with single top and ZWW)
- Electroweak NLO predictions (Correction LO  $\rightarrow$  NLO  $\sim$  15%)
- Update and maintenance of event generators (WHIZARD, MADGRAPH etc.)