

# NNLO QCD calculations at future colliders

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# *Outline*

- ➊ Introduction
- ➋ Isolation criteria (IC)
- ➌ IC comparison ( $\gamma\gamma$  NLO)
- ➍ Les Houches accord (“tight” isolation accord)
- ➎ ATLAS and CMS results
- ➏ qT Resummation  $\gamma\gamma$  (ATLAS)
- ➐ Summary

## Introduction

- $p\bar{p} \rightarrow F / F: \{\gamma + \text{jet}, \gamma\gamma, \gamma\gamma + \text{jet}, \gamma\gamma + (\text{n}) \text{jets}, V\gamma, W\gamma\gamma, \dots\}$
- $\sigma = \alpha_s^a \sigma^{\text{LO}} + \alpha_s^{a+1} \sigma^{\text{NLO}} + \alpha_s^{a+2} \sigma^{\text{NNLO}} + \dots / a = 0, 1, 2, \dots$

## Why processes with photons in the final state are important?

- Clean experimental signature
- These are channels that we can use to check the validity of perturbative Quantum Chromodynamics (pQCD)
  -  Soft gluon logarithmic resummation techniques
- Irreducible backgrounds for Higgs Boson searches and studies
- Backgrounds for BSM searches
- PDFs extractions
- Test of self-couplings ( $V\gamma$ ) as predicted by the non-Abelian  $SU(2)_L \times U(1)_Y$  (SM)
- S/B discrimination improvements
- Anomalous couplings

# **Why processes with photons in the final state are important?**

{  **$\gamma + \text{jet}$** ,  **$\gamma\gamma$** ,  **$\gamma\gamma + \text{jet}$** ,  **$\gamma\gamma + (\text{n}) \text{ jets}$** ,  **$V\gamma$** ,  **$W\gamma\gamma, \dots$**  }

• This talk is devoted to the study of parton level (FO) integrators and the comparison of their results with the LHC data

• In particular →  **$\gamma\gamma$**

• What can we learn from these final states regarding the future colliders?

## + ) Isolation:

Marco Delmastro private communication (2015)

\*) Comparison smooth-standard cone

\*) Size of the cone  $R = \{0.7; 0.4; 0.2; 0.1\}$

→ **New requirements at Run II LHC.** A game between pile-up and how the cross section is sensitive to  $\text{Log}(R)$

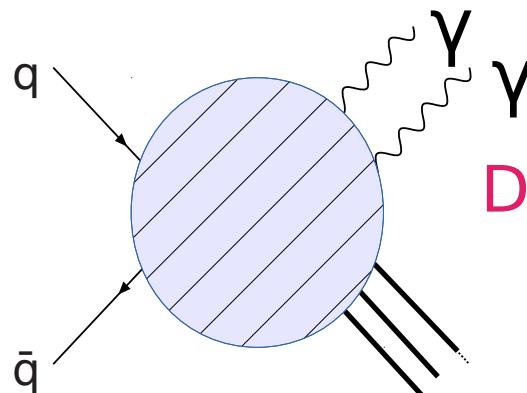
## + ) Origin of the discrepancies Theory/Data

\*) Isolation, EW corrections, missing higher order QCD correction terms. The NNLO will be enough to describe the Data in the next years?

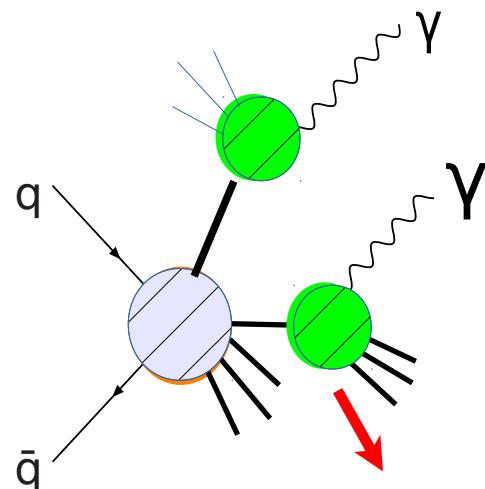
All these processes are connected by the presence of at least one-photon in the final state. Therefore all of them have a common feature: their origin arises in the photon production mechanisms

# Photon production

When we deal with the production of photons we have to consider two production mechanisms:



**Direct component:** photon is directly produced through the hard interaction



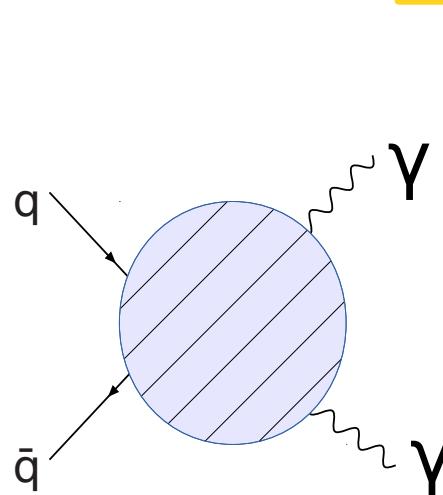
**Fragmentation component:** photon is produced from non-perturbative fragmentation of a hard parton (analogously to a hadron)

Calculations of cross sections with photons have additional singularities in the presence of QCD radiation. (i.e. When we go beyond LO)

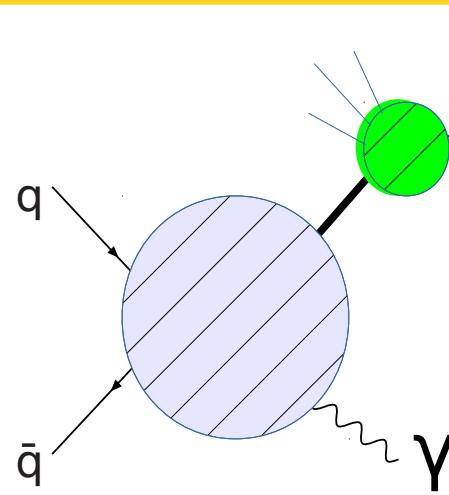
Fragmentation function:  
to be fitted from data

# Photon production

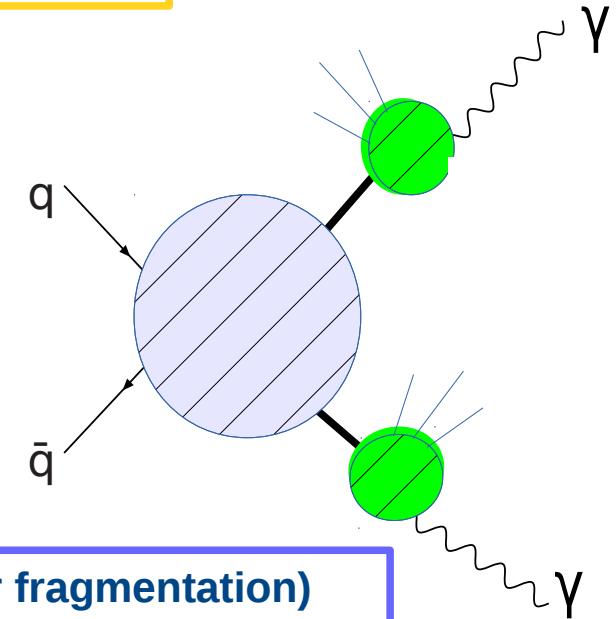
Two mechanisms for photon production



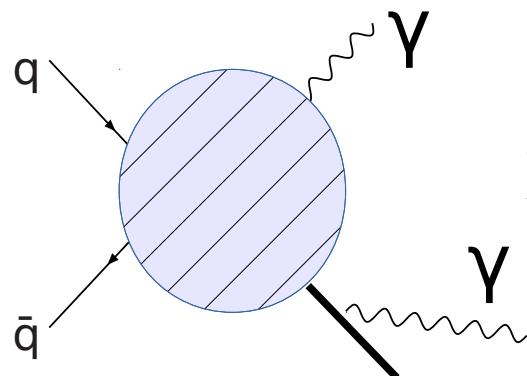
Direct (point-like)



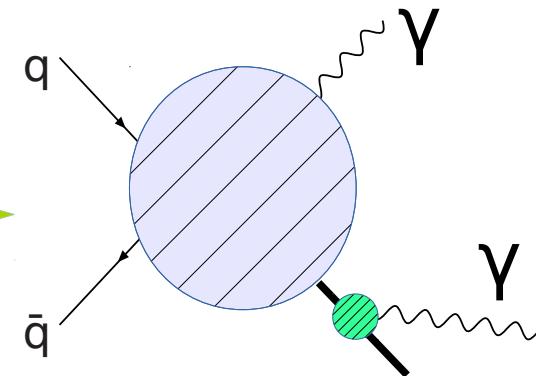
Direct and double resolved (collinear fragmentation)



In general the separation between them is not-physical (beyond LO)



Collinear divergence



Cancelled by fragmentation

# Photon production

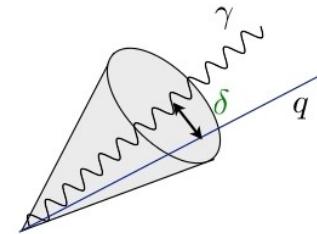
- Experimentally photons must be isolated
- Isolation reduces fragmentation component

Large Corrections

## Isolation criteria

- Standard (cone)** Baer, Ohnemus, Owens (1990). Aurenche, Baier, Fontannaz (1990)

$$\sum_{\delta < R_0} E_T^{had} \leq \epsilon_\gamma p_T^\gamma$$



$$\sum_{\delta < R_0} E_T^{had} \leq E_T^{max}$$

- Smooth (Frixione)** S. Frixione (1998)

$$\chi(\delta) = \left( \frac{1 - \cos(\delta)}{1 - \cos(R_0)} \right)^n \leq 1$$

$$\sum_{\delta < R_0} E_T^{had} \leq E_T^{max} \chi(\delta)$$

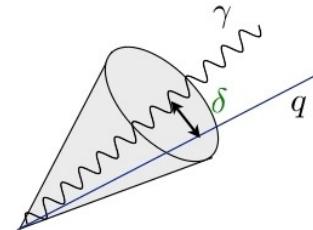
- Democratic** Glover, Morgan(1994). Gehrmann-De Ridder, Gehrmann, Glover (1997)

final state particles are clustered into jets, treating photons and hadrons equally. The obtained object is called a photon or a photon jet, if the energy fraction  $Z = E_\gamma / (E_\gamma + E_{had})$  of an observed photon inside the jet is larger than an experimentally defined value  $Z_{cut}$ .

# Photon production

- Experimentally photons must be isolated
- Isolation reduces fragmentation component
- Experimentalist may choose:

$$\sum_{\delta < R_0} E_T^{had} \leq \epsilon_\gamma p_T^\gamma$$



$$\sum_{\delta < R_0} E_T^{had} \leq E_T^{max}$$

Large Corrections

**Using conventional isolation, only the sum of the direct and fragmentation contributions is meaningful.**

**But there is a way to isolate and make physical the direct cross section (Infrared safe)**

## Smooth cone Isolation

Soft emission allowed arbitrarily close to the photon

$$\chi(\delta) = \left( \frac{1 - \cos(\delta)}{1 - \cos(R_0)} \right)^n \leq 1$$



- no quark-photon collinear divergences
- no fragmentation component (only direct)
- direct well defined by itself

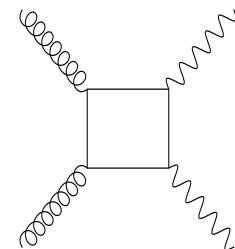
$$\sum_{\delta < R_0} E_T^{had} \leq E_T^{max} \chi(\delta)$$

# **Available theoretical (FO) tools for $\gamma\gamma$ production**

## **DIPHOX**

T. Binoth, J.Ph. Guillet, E. Pilon and M. Werlen

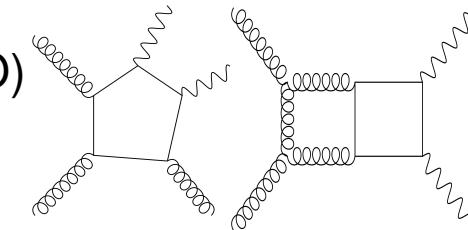
Full NLO for direct and fragmentation + Box contribution (one piece of NNLO)



## **gamma2MC**

Zvi Bern, Lance Dixon, and Carl Schmidt

Full NLO (direct only) + Box, + partial correction to Box contribution ( $N^3LO$ )



## **MCFM**

John M. Campbell, R.Keith Ellis, Ciaran Williams

Full NLO for direct, but only LO for fragmentation + partial correction to Box contribution ( $N^3LO$ )

## **Resbos**

C. Balázs, E. L. Berger, P. Nadolsky, and C.-P. Yuan

NLL  $q_T$  resummation for direct (with regulator for collinear singularities)

## **2 $\gamma$ NNLO**

Catani, LC, de Florian, Ferrera, Grazzini

Full NNLO for direct + partial correction to Box contribution ( $N^3LO$ )

## **2 $\gamma$ Res**

LC, Coradeschi, de Florian

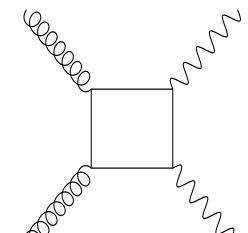
Incorporates the  $q_T$  resummation at NNLL+NNLO

# **Available theoretical (FO) tools for $\gamma\gamma$ production**

## **DIPHOX**

T. Binoth, J.Ph. Guillet, E. Pilon and M. Werlen

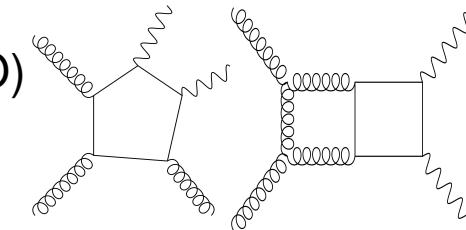
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Full NLO (direct only) + Box, + partial correction to Box contribution ( $N^3LO$ )



## **MCFM**

John M. Campbell, R.Keith Ellis, Ciaran Williams

Full NLO for direct, but only LO for fragmentation + partial correction to Box contribution ( $N^3LO$ )

The user can use these codes to predict the  $q_T$  ( $\gamma\gamma + \text{jet}$ ) spectrum, but at one perturbative order less than the total Xsection

## **Resbos**

C. Balázs, E. L. Berger, P. Nadolsky, and C.-P. Yuan

NLL  $q_T$  resummation for direct (with regulator for collinear singularities)

## **2 $\gamma$ NNLO**

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Full NNLO for direct + partial correction to Box contribution ( $N^3LO$ )

## **2 $\gamma$ Res**

LC, Coradeschi, de Florian

Incorporates the  $q_T$  resummation at NNLL+NNLO

# **Available theoretical (FO) tools for:**

## **$\gamma + (n < 4) \text{ jet}$**

T. Gehrmann , N. Greiner , G. Heinrich (2013) ;Z. Bern, L.J. Dixon, F. Febres Cordero, S. Hoeche, H. Ita, D.A. Kosower, N. A. Lo Presti, D. Maitre (2013); S. Badger, A. Guffanti, V. Yundin (2013)

## **$\gamma + \text{jet}$**

### **JetPHOX** Aurenche, Catani, Fontannaz, Binoth, Guillet, Pilon, Werlen

Full NLO for direct and fragmentation

### **MCFM** John M. Campbell, R.Keith Ellis, Ciaran Williams

Full NLO for direct, but only LO for fragmentation

## **$V\gamma \text{ production}$**

### **MCFM** John M. Campbell, R.Keith Ellis, Ciaran Williams

Full NLO for direct, but only LO for fragmentation

### **NNLO** Grazzini, Kallweit, Rathlev, Torre

Full NNLO for direct

## **$VV\gamma, W\gamma\gamma, VV\gamma\gamma, Z\gamma\gamma, \dots \text{ production}$**

### **MCFM** Ellis, Campbell, C. Williams , T. Dennen

Full NLO for direct, but only LO for fragmentation

# **Available theoretical (FO) tools for:**

**$\gamma + (n < 4) \text{ jet}$**

T. Gehrmann , N. Greiner , G. Heinrich (2013) ;Z. Bern, L.J. Dixon, F. Febres Cordero, S. Hoeche, H. Ita, D.A. Kosower, N. A. Lo Presti, D. Maitre (2013); S. Badger, A. Guffanti, V. Yundin (2013)

**$\gamma + \text{jet}$**

**JetPHOX** Aurenche, Catani, Fontannaz, Bineth, Guillet, Pilon, Werlen

Full NLO for direct and fragmentation

**MCFM** John M. Campbell, R.Keith Ellis, Ciaran Williams

Full NLO for direct, but only LO for fragmentation

## **$V\gamma$ production**

**MCFM** John M. Campbell, R.Keith Ellis, Ciaran Williams

Full NLO for direct, but only LO for fragmentation

**NNLO** Grazzini, Kallweit, Rathlev, Torre

Full NNLO for direct

## **$VV\gamma, W\gamma\gamma, VV\gamma\gamma, Z\gamma\gamma, \dots$ production**

**MCFM** Ellis, Campbell, C. Williams , T. Dennen

Full NLO for direct, but only LO for fragmentation

The list is not  
exhaustive!!!!

## **VBFNLO**

Full NLO for direct

JG. Bozzi, F. Campanario, M. Rauch, H. Rzehak, D. Zeppenfeld

## ***Available theoretical (FO) tools for:***

**{ $\gamma + \text{jet}$  ,  $\gamma\gamma$  ,  $\gamma\gamma + \text{jet}$  ,  $\gamma\gamma + (\text{n}) \text{ jets}$  ,  $V\gamma$  ,  $W\gamma\gamma, \dots$  }**

**NNLO**

**+ ) Only direct  $\rightarrow$  smooth cone**

**NLO**

**+ ) Only direct  $\rightarrow$  smooth cone**

**+ ) Direct + Fragmentation**

*IC comparison (NLO)*  
*Standard vs Smooth*  
 *$\gamma\gamma$  production*

# *IC comparison (NLO)*

## *Standard vs Smooth*

### *$\gamma\gamma$ production*

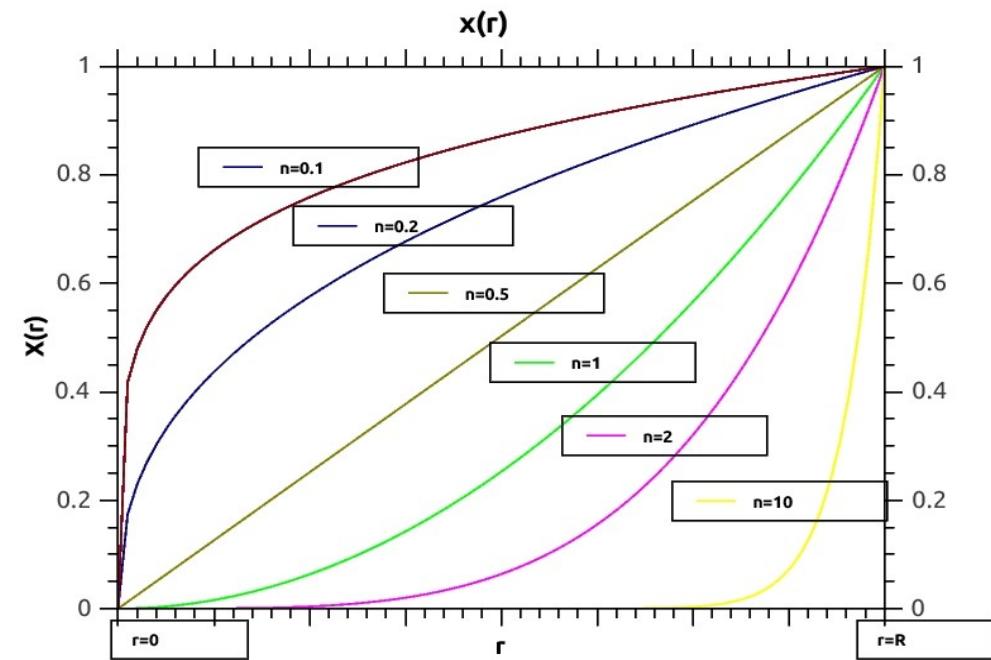
*Full NLO  
fragmentation  
contributions*

DIPHOX

*Would be nice  
the same study  
with  $\gamma+jet$*

JetPHOX

# IC comparison ( $\gamma\gamma$ at NLO)



$$\chi(\delta) = \left( \frac{1 - \cos(\delta)}{1 - \cos(R_0)} \right)^n \leq 1$$

**Standard**

$$E_T^{had}(\delta) \leq E_{T\max}^{had}$$

**Smooth**

$$E_T^{had}(\delta) \leq E_{T\max}^{had} \chi(\delta)$$



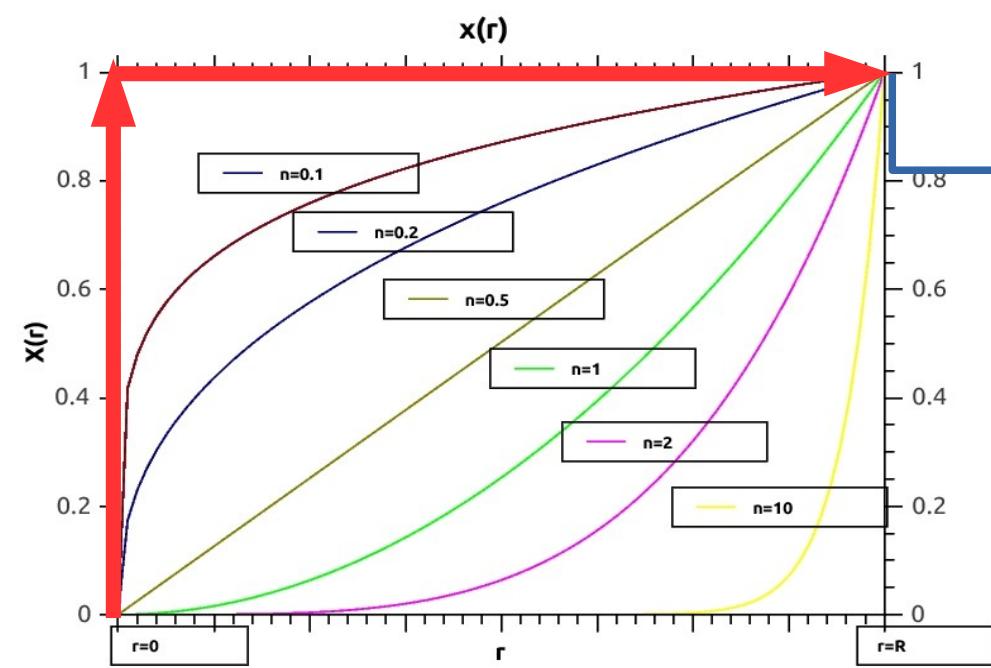
No quark-photon collinear divergences



No fragmentation contribution (only direct)



Direct contribution well defined



$$\chi(\delta) = \left( \frac{1 - \cos(\delta)}{1 - \cos(R_0)} \right)^n \leq 1$$

**Standard**

$$E_T^{had}(\delta) \leq E_{T\max}^{had}$$

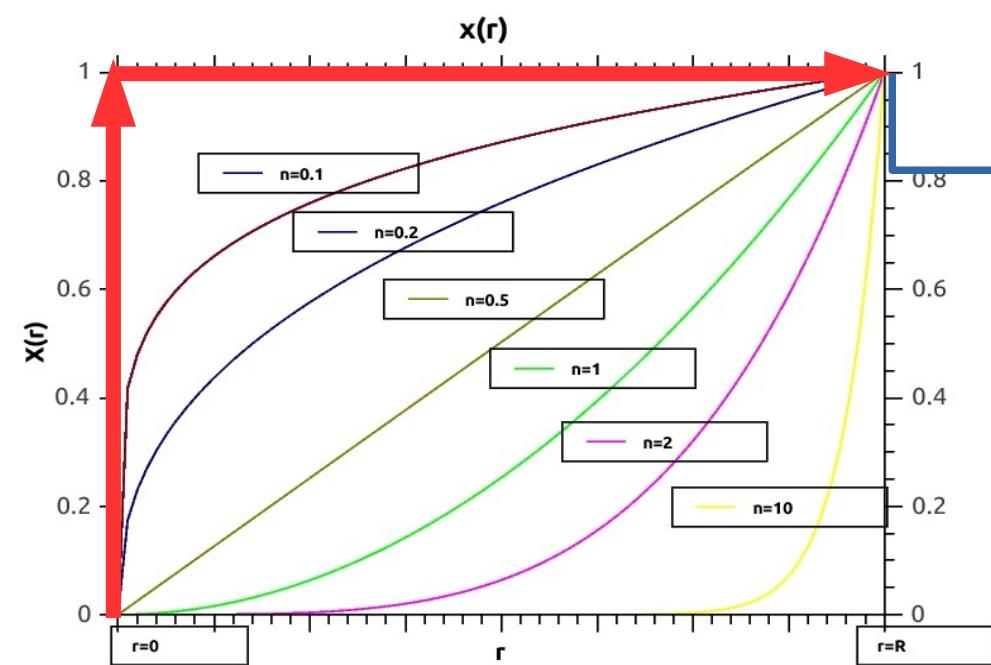
**Smooth**

$$E_T^{had}(\delta) \leq E_{T\max}^{had} \chi(\delta)$$

**No quark-photon collinear divergences**

**No fragmentation contribution (only direct)**

**Direct contribution well defined**



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$$E_T^{had}(\delta) \leq E_{T\max}^{had}$$

**Smooth**

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No quark-photon collinear divergences



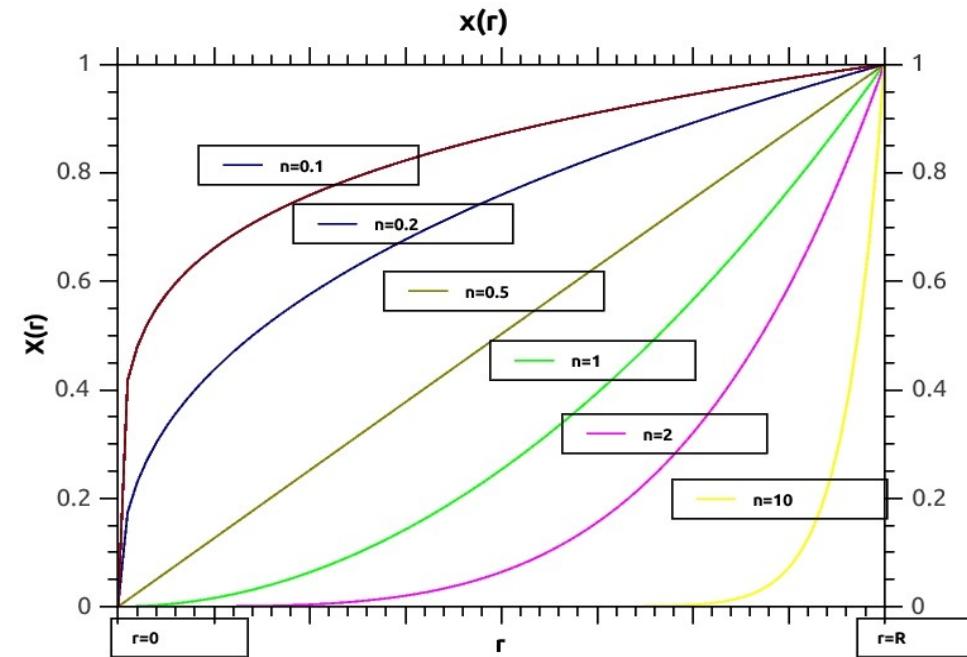
No fragmentation contribution (only direct)



Direct contribution well defined

- The smooth cone isolation criterion is more restrictive than the standard one
- $\sigma_{Frix}\{R, E_T \max\} \leq \sigma_{Stand}\{R, E_T \max\}$

(both theoretically and experimentally)



$$\chi(\delta) = \left( \frac{1 - \cos(\delta)}{1 - \cos(R_0)} \right)^n \leq 1$$

**Standard**

$$E_T^{had}(\delta) \leq E_{T\max}^{had}$$

**Smooth**

$$E_T^{had}(\delta) \leq E_{T\max}^{had} \chi(\delta)$$



No quark-photon collinear divergences



No fragmentation contribution (only direct)



Direct contribution well defined

In real life... how much are different?

NLO comparison

(Standard vs. Smooth)

Ro=0.4 n=1

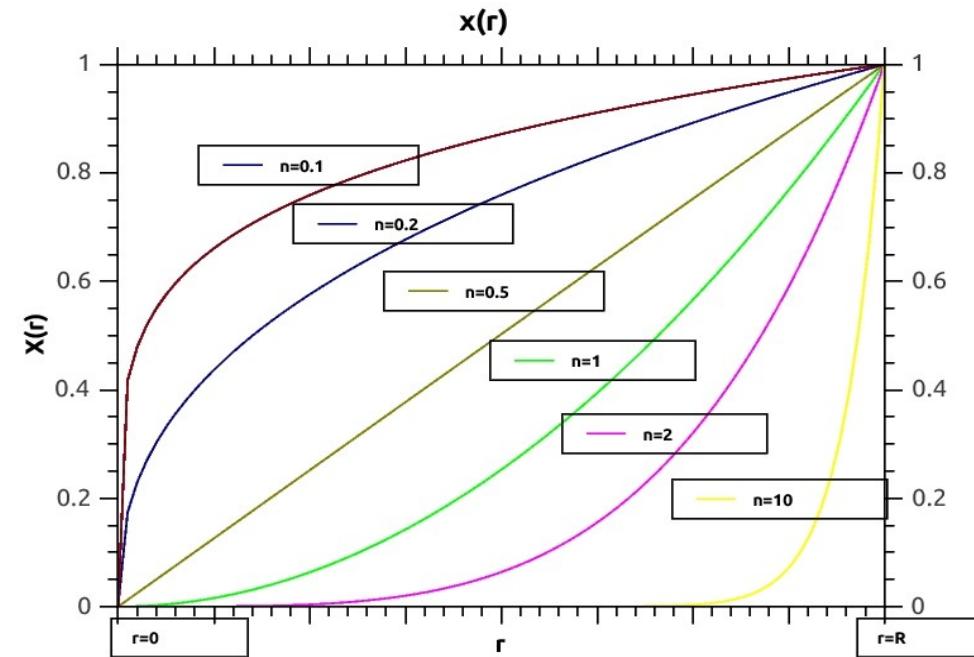


DIPHOX → (Direct + Fragmentation)[NLO]

$E_{T\max}^{had}$	standard/smooth
2 GeV	< 1%
3 GeV	< 1%
4 GeV	1%
5 GeV	3%
0.05 $p_T$	< 1%
0.5 $p_T$	11%

T. Binoth, J. Guillet, E. Pilon, and M. Werlen (1999)

NLO	MCFM	J. M. Campbell, R. K. Ellis, and C. Williams (2011)
	gamma2MC	Bern, Dixon and Schmidt (2011)
	Resbos	Balazs, Berger, Nadolsky, C.P Yuan (2007)
NNLO	2yNNLO	S. Catani, LC, D. de Florian, G. Ferrera, and M. Grazzini (2011)
	2yRes	LC, Coradeschi, de Florian (2015)
NNLL+ NNLO		



$$\chi(\delta) = \left( \frac{1 - \cos(\delta)}{1 - \cos(R_0)} \right)^n \leq 1$$

**Standard**

$$E_T^{had}(\delta) \leq E_{T\max}^{had}$$

**Smooth**

$$E_T^{had}(\delta) \leq E_{T\max}^{had} \chi(\delta)$$



No quark-photon collinear divergences



No fragmentation contribution (only direct)



Direct contribution well defined

In real life... how much are different?

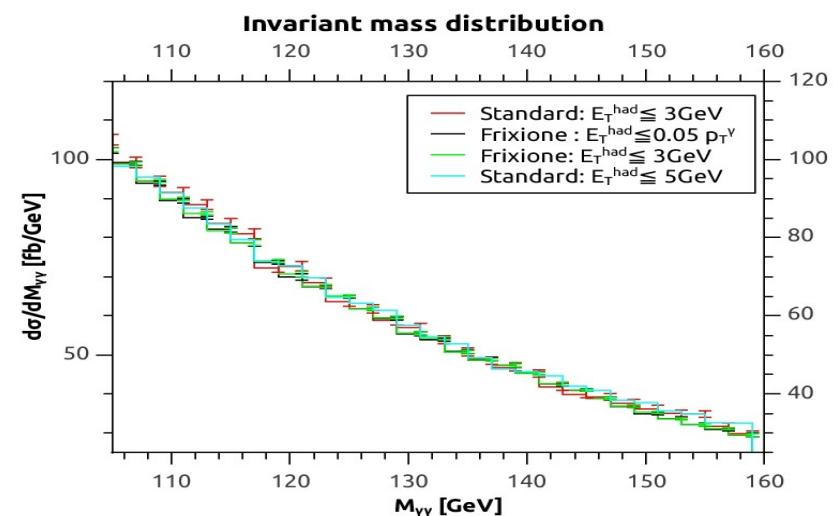
NLO comparison

(Standard vs. Smooth)

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0.5 $p_T$	11%



$$\left(\frac{\delta}{\delta_0}\right)^n \leq 1$$

$$d(\delta) \leq E_{T max}^{had}$$

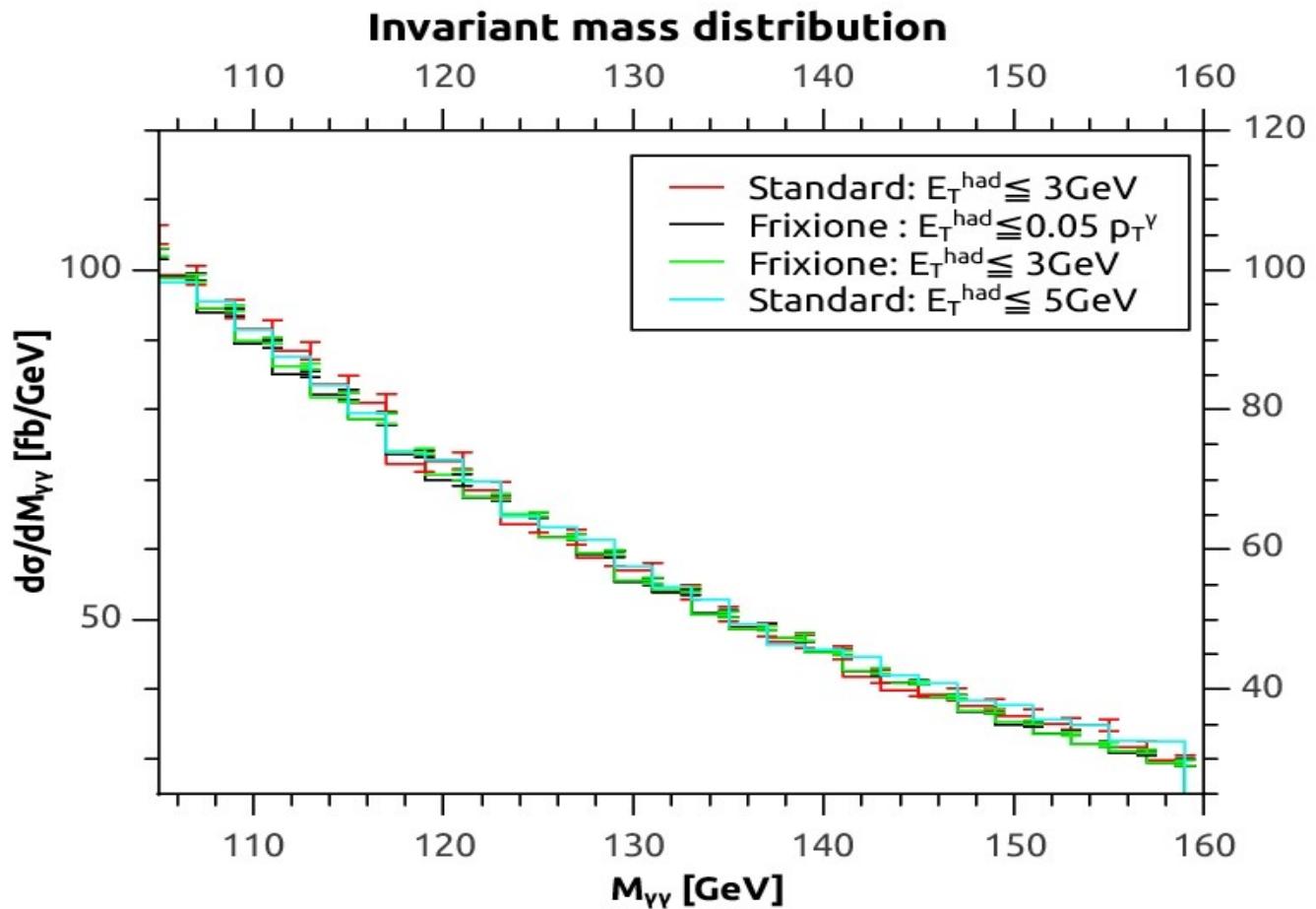
$$t(\delta) \leq E_{T max}^{had} \chi(\delta)$$

linear divergences

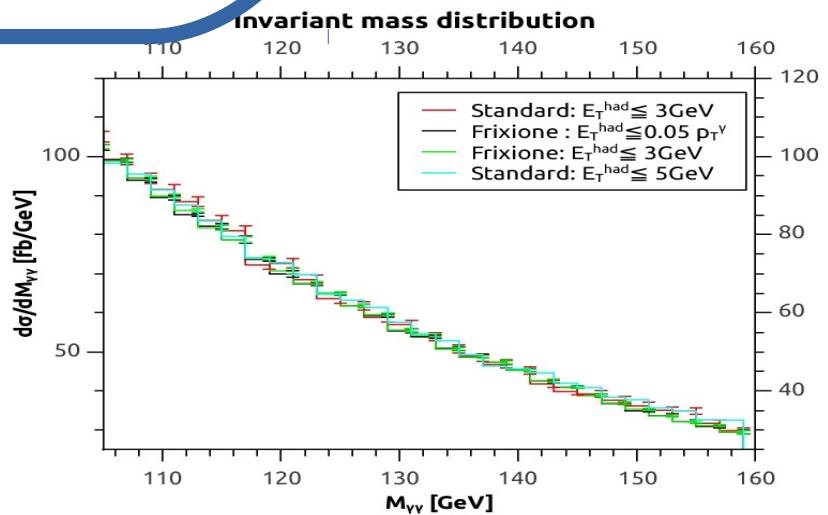
contribution (only direct)

well defined

Direct + Fragmentation



$E_T^{\text{had}}$	standard/smooth
2 GeV	< 1%
3 GeV	< 1%
4 GeV	1%
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0.05 $p_T$	< 1%
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$$\left(\frac{\delta}{\delta_0}\right)^n \leq 1$$

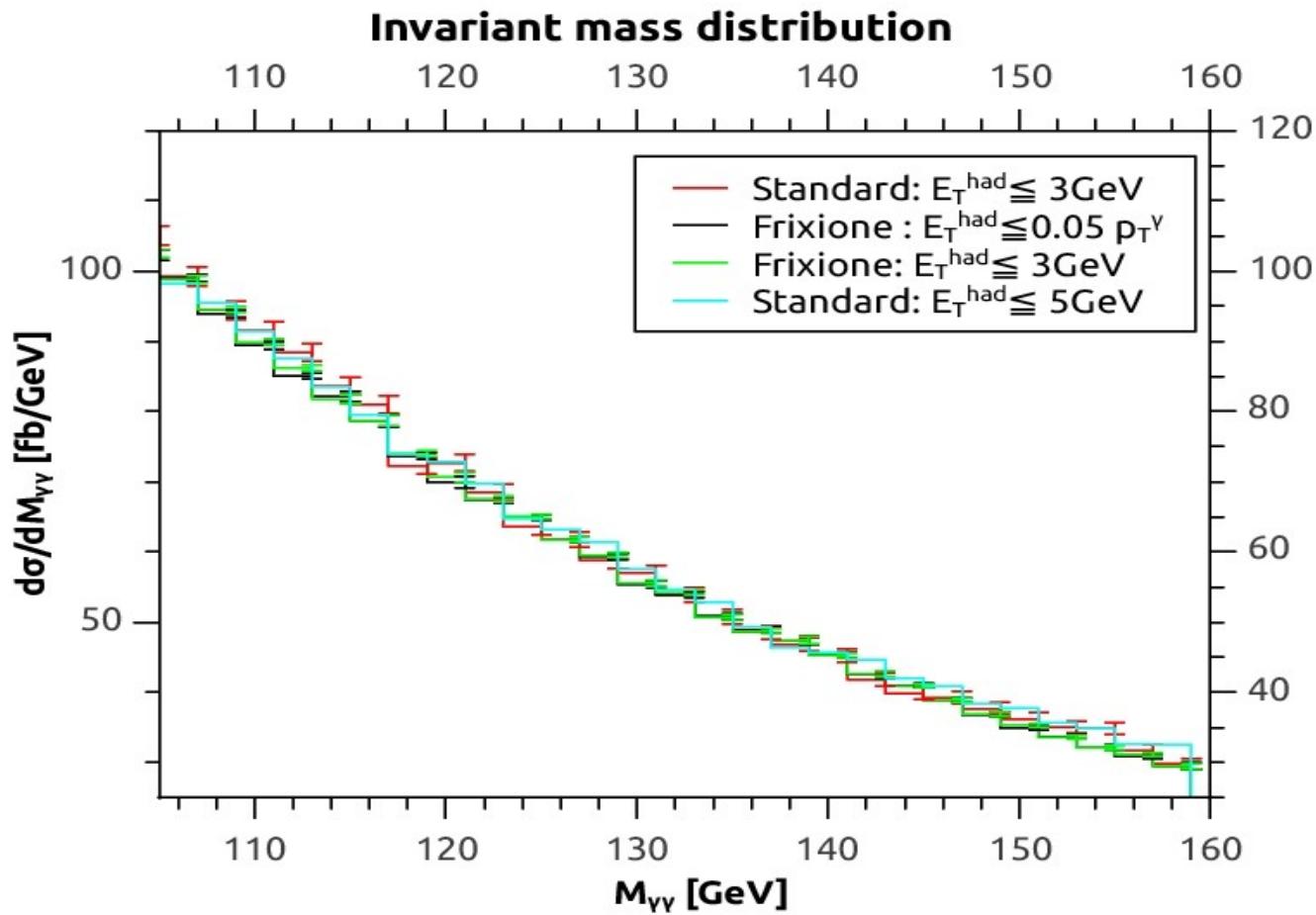
$$d(\delta) \leq E_{T max}^{had}$$

$$t(\delta) \leq E_{T max}^{had} \chi(\delta)$$

**linear divergences**

**contribution (only direct)**

**well defined**



But the effects of the fragmentation could appear strongly in kinematical regions far away from the back-to-back configuration....

# *Isolation criteria comparison*

[Les Houches 2013: Physics at TeV Colliders: Standard Model Working Group Report ]

**For the next slides:** [For all the cases we use the same set of isolation parameters]

Xsection [NLO] = **Direct [NLO] + Frag [NLO]** (Isolation Criterion: Standard, Democratic, Frixione, etc.)

Xsection [NLO] = Direct [NLO] **Frag [NLO]** (Isolation Criterion: Frixione)

Xsection [NLO] = Direct [NLO] + **Frag [LO]** (Isolation Criterion: Standard, Democratic, Frixione, etc.)

The calculation of fragmentation contributions is very difficult:

We can find calculations in which the fragmentation component is considered at one perturbative level less than the direct component.

Diphoton production  $\sqrt{s} = 8 \text{ TeV}$  CTEQ6M  $\mu_F = \mu_R = M_{\gamma\gamma}$

$$p_T^{\gamma \text{ hard}} \geq 40 \text{ GeV}$$

$$p_T^{\gamma \text{ soft}} \geq 30 \text{ GeV}$$

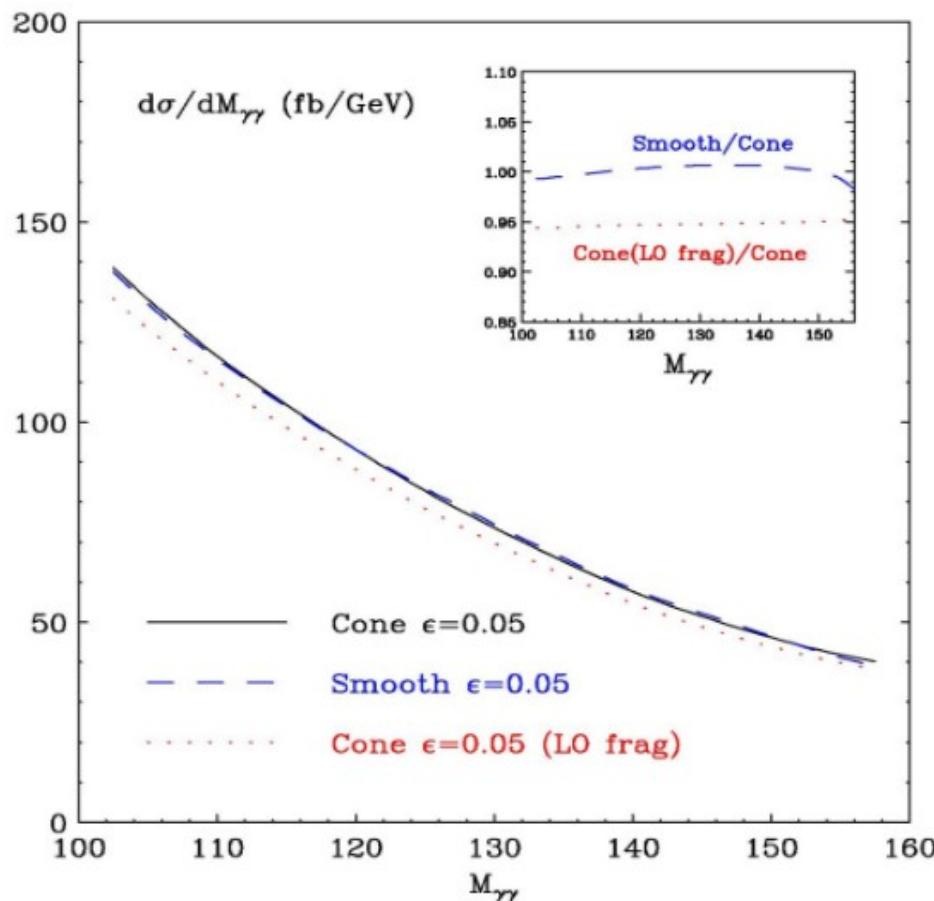
$$100 \text{ GeV} \leq M_{\gamma\gamma} \leq 160 \text{ GeV}$$

$$|\eta^\gamma| \leq 2.5$$

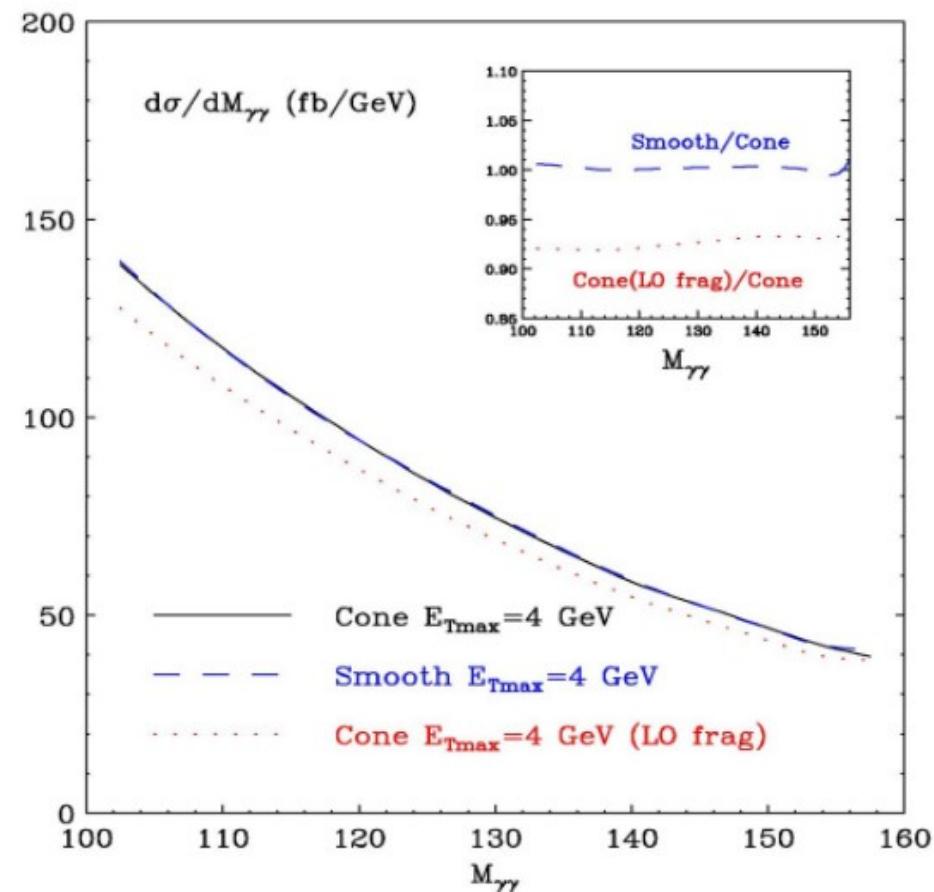
$$R_{\gamma\gamma} \geq 0.45$$

full NLO Cone (DIPHOX) vs Cone with LO fragmentation vs NLO Smooth

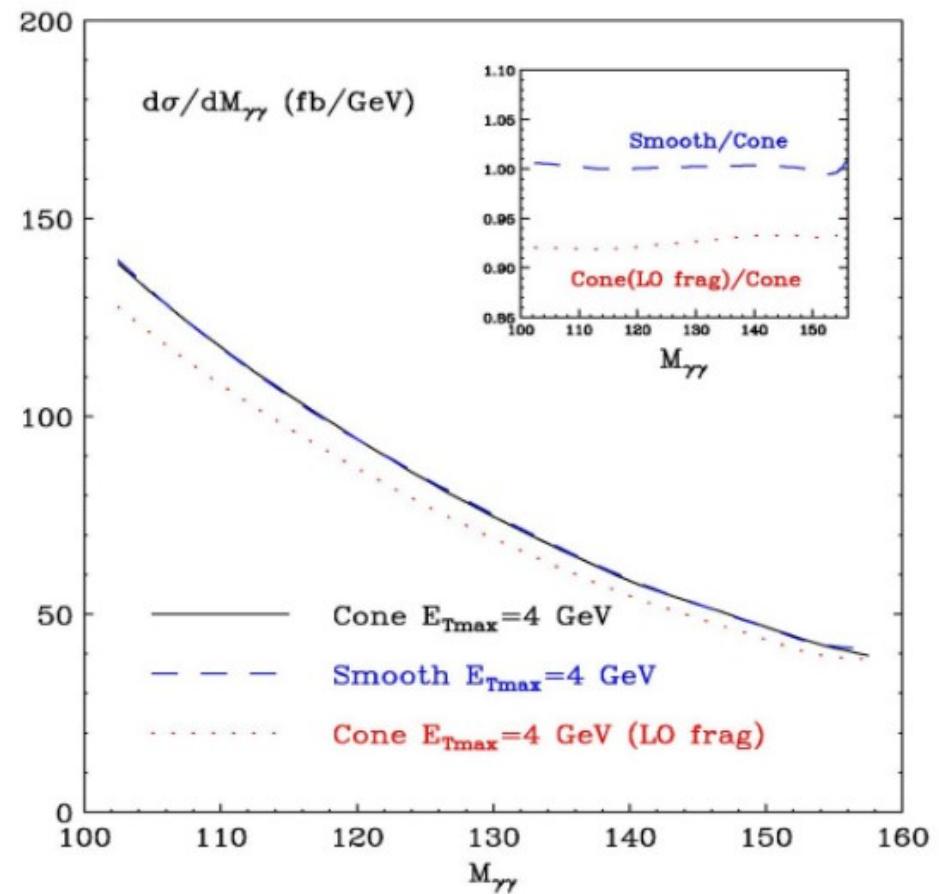
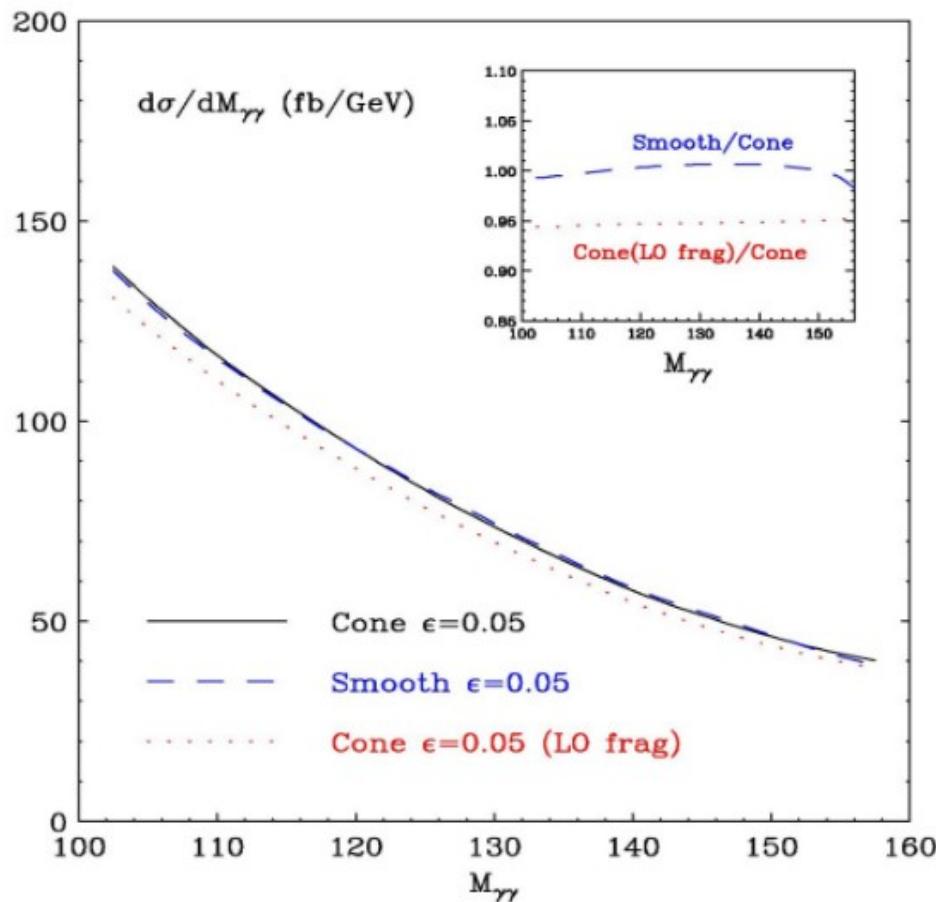
$$E_{T \max}^{\text{had}} = \epsilon p_T^\gamma \quad \epsilon = 0.05$$



$$E_{T \max}^{\text{had}} = 4 \text{ GeV}$$



Be carefull to make conclusions here  
 It is not true that the smooth approach gives a larger Xsection  
 See the Full NLO result with Fragmentation



Diphoton production  $\sqrt{s} = 8 \text{ TeV}$  CTEQ6M  $\mu_F = \mu_R = M_{\gamma\gamma}$

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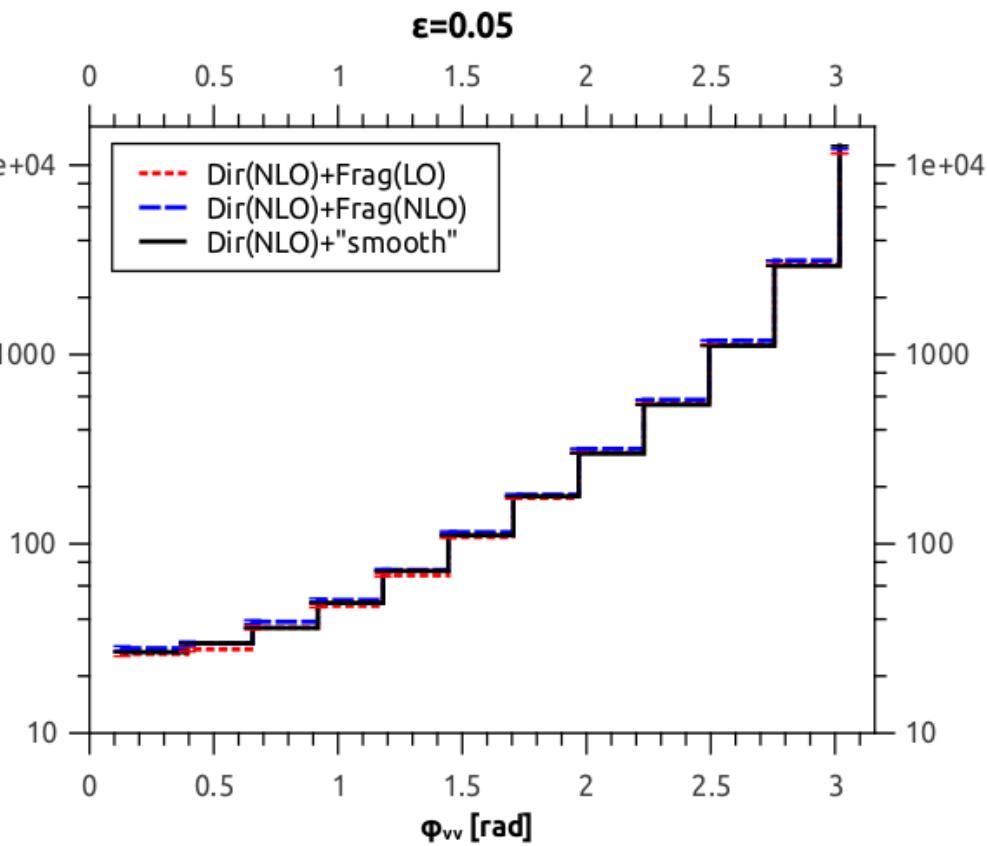
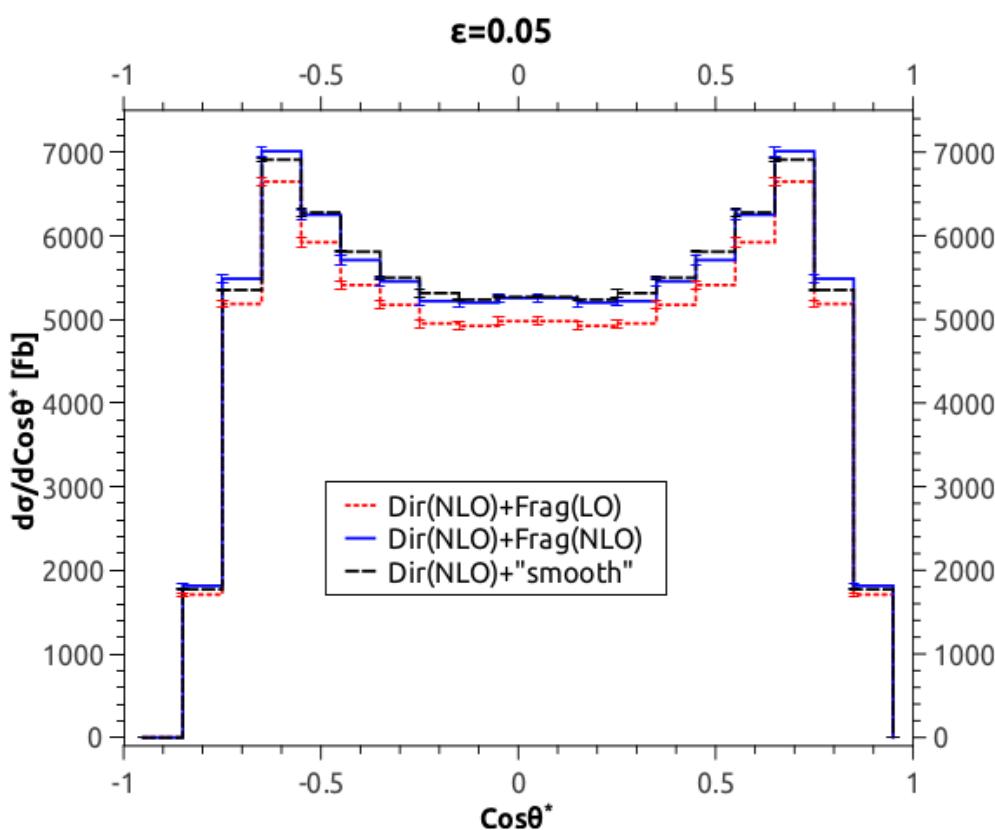
$$|\eta^\gamma| \leq 2.5$$

$$R_{\gamma\gamma} \geq 0.45$$

full NLO Cone (DIPHOX) vs Cone with LO fragmentation vs NLO Smooth

$$E_{T \max}^{had} = \epsilon p_T^\gamma \quad \epsilon = 0.05$$

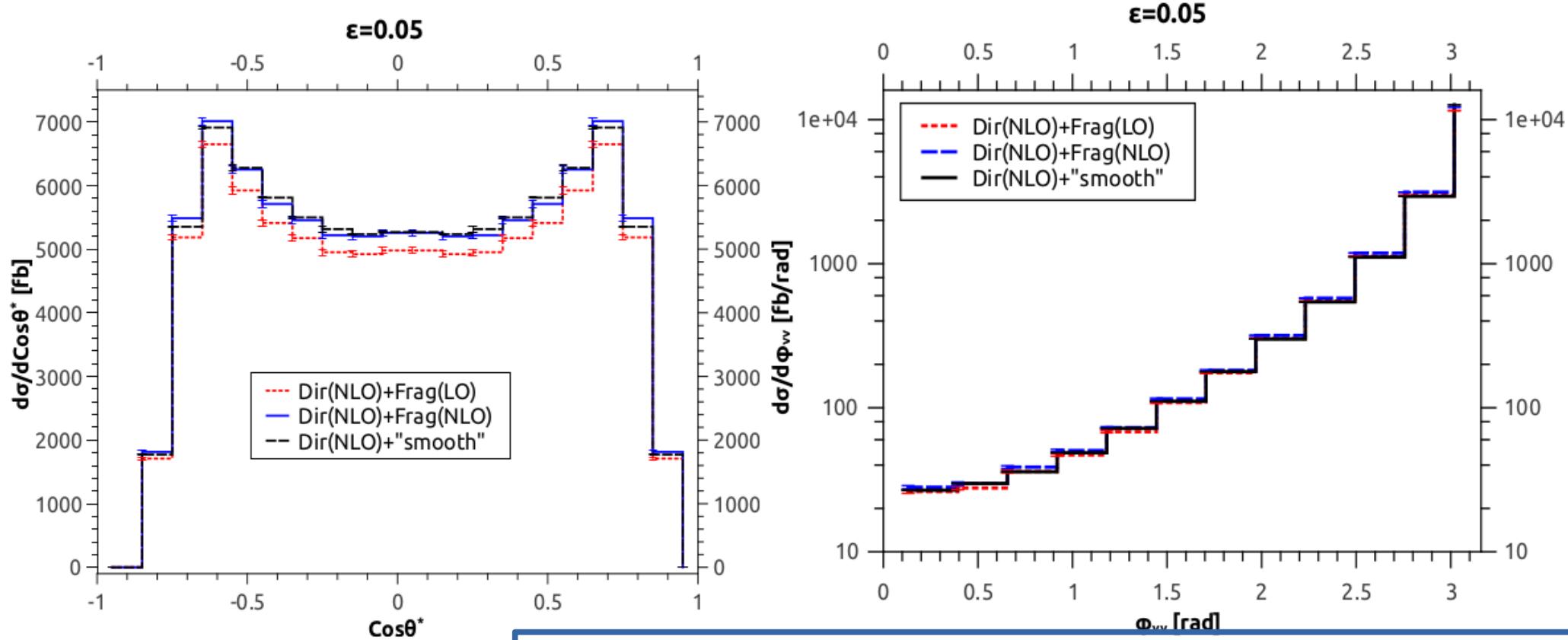
$$E_{T \max}^{had} = 4 \text{ GeV}$$



## Same Features for all distributions

Smooth cone @NLO ~ Cone @ NLO 1-2 %

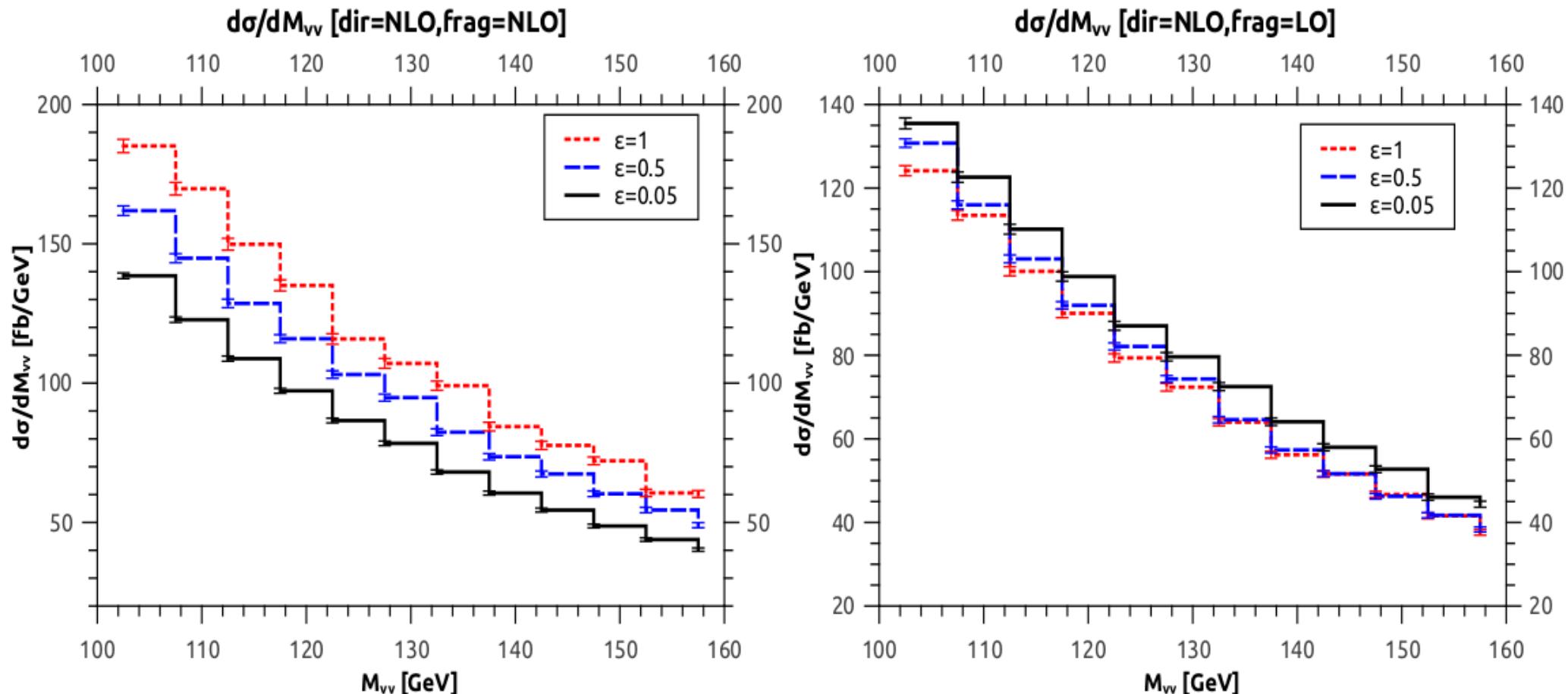
Cone + LO fragmentation component worse than 5%



Be carefull to make conclusions here  
It is not true that the smooth approach gives a larger Xsection  
See the Full NLO result with Fragmentation

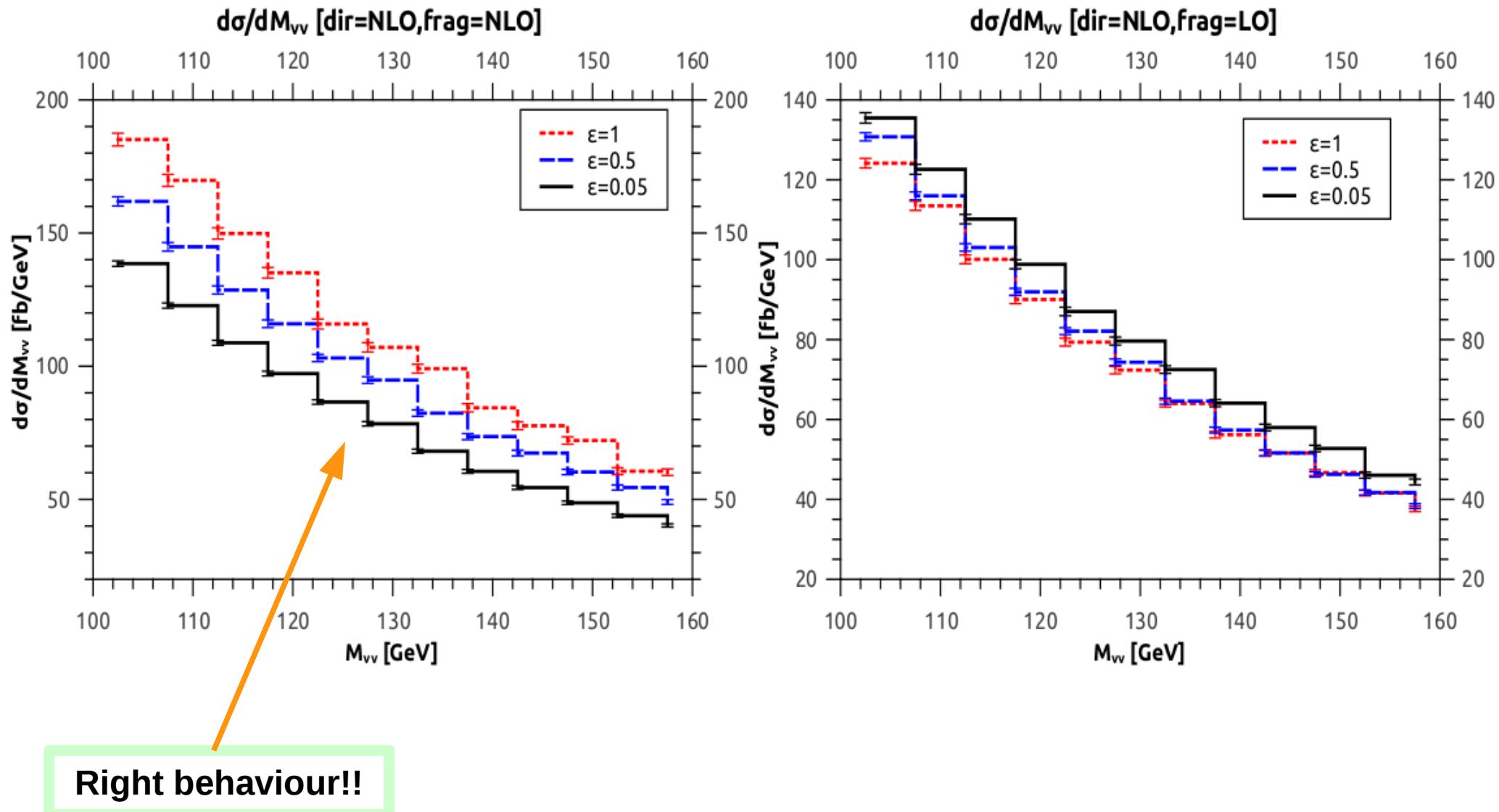
In some cases, using LO fragmentation component can make things look very strange...

## Standard cone isolation → DIPHOX



In some cases, using LO fragmentation component can make things look very strange...

## Standard cone isolation → DIPHOX



# **Les Houches accord 2013**

[Les Houches 2013: Physics at TeV Colliders: Standard Model Working Group Report ]

## “LH tight photon isolation accord”

- EXP: use (tight) Cone isolation      solid and well understood
- TH: use smooth cone with same  $R$  and  $E_{T\max}$       accurate, better than using cone with LO fragmentation  
Estimate TH isolation uncertainties  
using different profiles in smooth cone

While the definition of "tight enough" might slightly depend on the particular observable (that can always be checked by a lowest order calculation), our analysis shows that at the LHC isolation parameters as  $E_T^{max} \leq 5$  GeV (or  $\epsilon < 0.1$ ),  $R \sim 0.4$  and  $R_{\gamma\gamma} \sim 0.4$  are safe enough to proceed.

This procedure would allow to extend available NLO calculations to one order higher (NNLO) for a number of observables, since the direct component is always much simpler to evaluate than the fragmentation part, which identically vanishes under the smooth cone isolation.

# *Les Houches accord 2013*

[Les Houches 2013: Physics at TeV Colliders: Standard Model Working Group Report ]

## “LH tight photon isolation accord”

- EXP: use (tight) Cone isolation      solid and well understood
- TH: use smooth cone with same  $R$  and  $E_{T\max}$       accurate, better than using cone with LO fragmentation  
Estimate TH isolation uncertainties  
using different profiles in smooth cone

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Estimate TH isolation uncertainties  
using different profiles in smooth cone

Considering that NNLO corrections are of the order of 50% for diphoton cross sections and a few 100% for some distributions in extreme kinematical configurations, it is far better accepting a few % error arising from the isolation (less than the size of the expected NNNLO corrections and within any estimate of TH uncertainties!) than neglecting those huge QCD effects towards some “more pure implementation” of the isolation prescription.

Recently, some calculations use the smooth cone isolation criteria to arrive at the highest level of accuracy:

V $\gamma$  production [NNLO]    M. Grazzini, S. Kallweit, D. Rathlev, A. Torre (2013), (2015)

$\gamma\gamma + 2\text{Jets}$  [NLO]    T. Gehrmann , N. Greiner , G. Heinrich (2013) ;Z. Bern, L.J. Dixon, F. Febres Cordero, S. Hoeche, H. Ita, D.A. Kosower, N. A. Lo Presti, D. Maitre (2013)

$\gamma\gamma + (\text{up to}) 3\text{Jets}$  [NLO]    S. Badger, A. Guffanti, V. Yundin (2013)

# *Les Houches accord 2013*

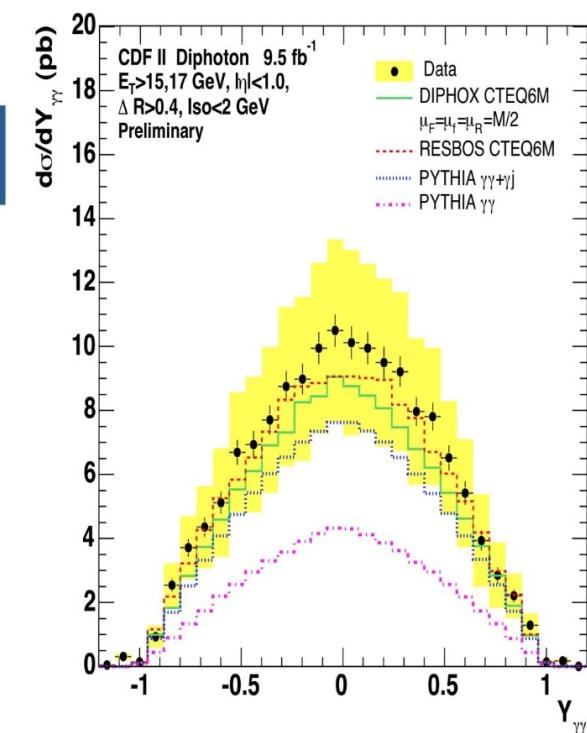
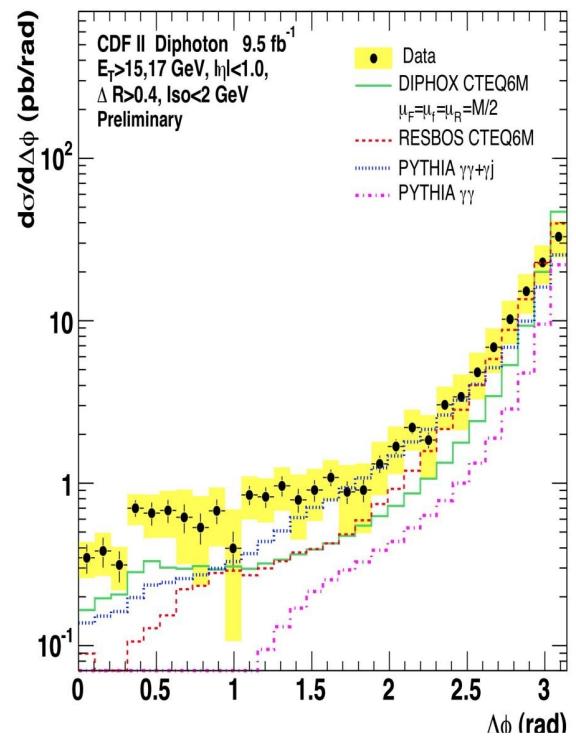
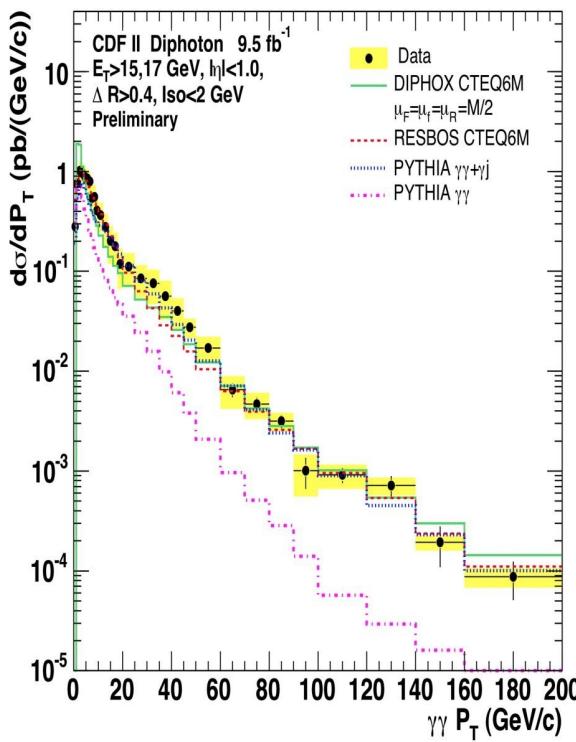
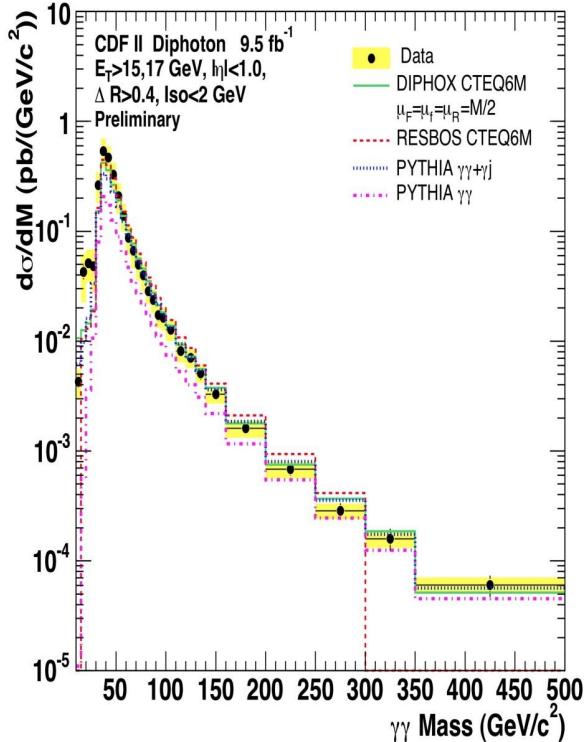


Generalization to other processes containing  
photons in the final state



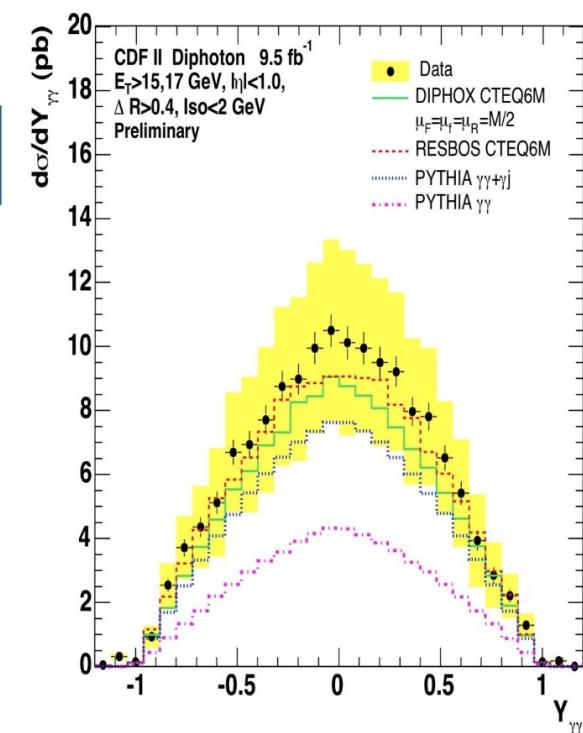
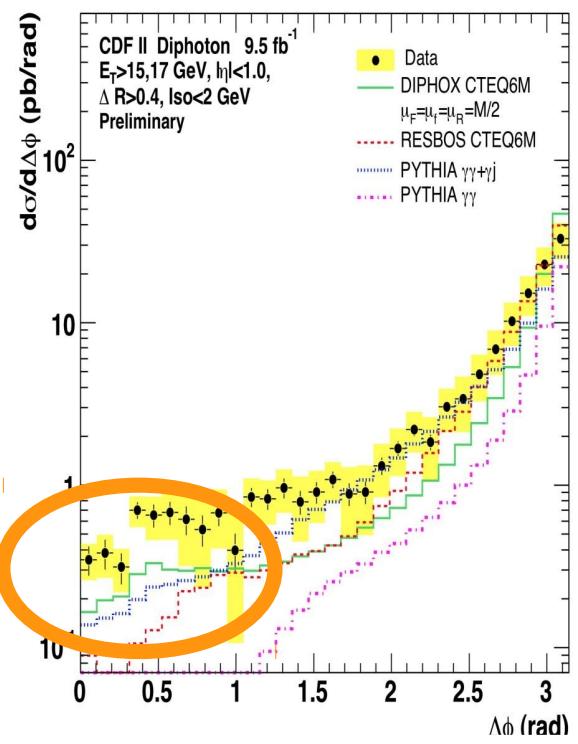
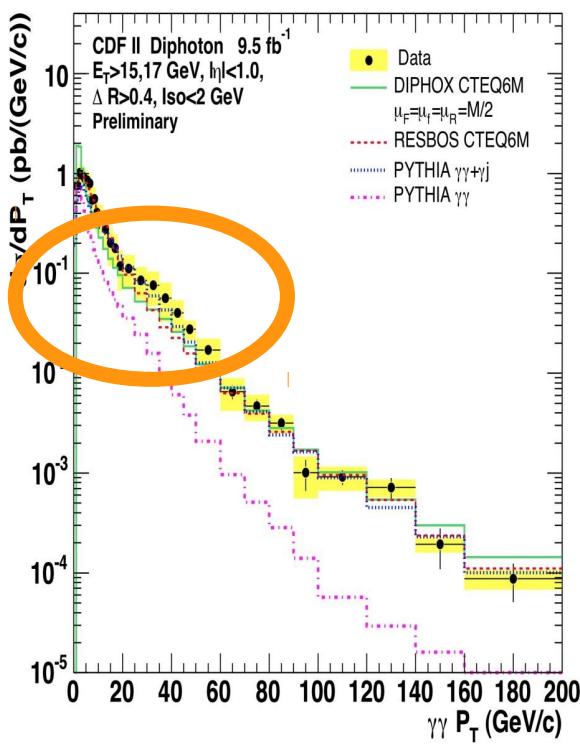
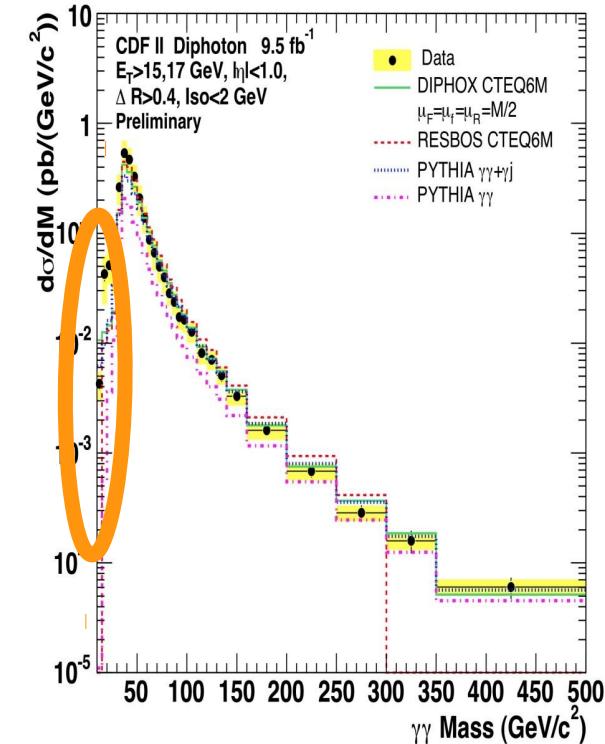
# *Les Houches accord 2015*

## ***Results and comparison with data***



## Differential cross sections: CDF

Phys. Rev. D84 (2011) 052006

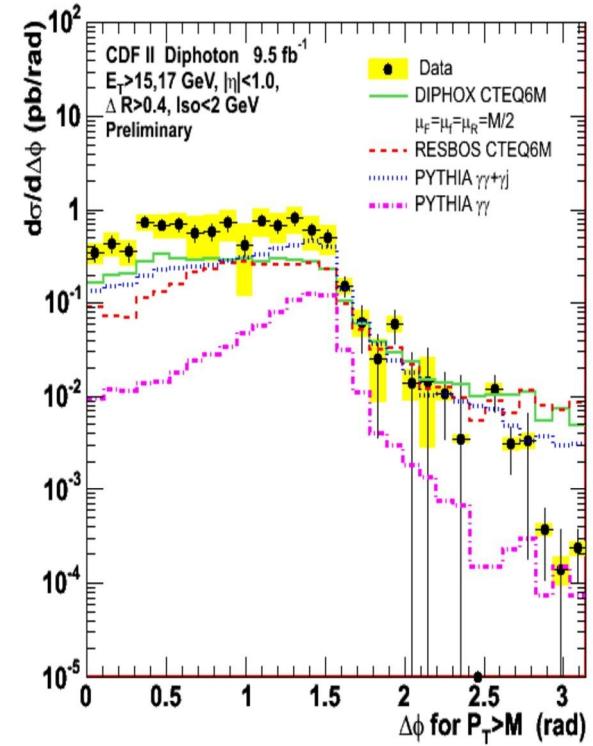
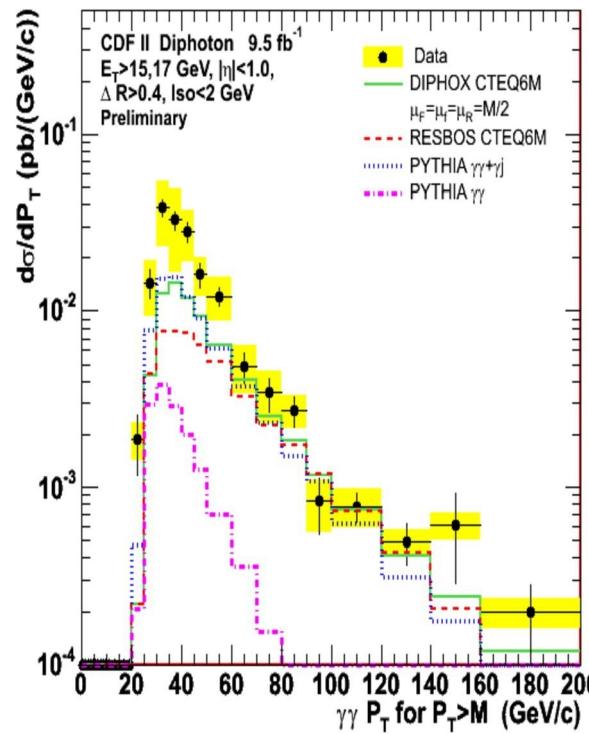
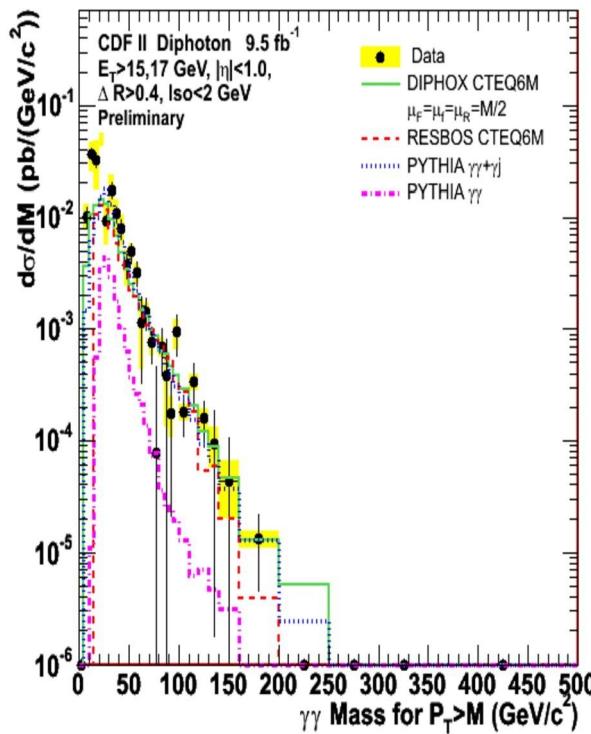


## Differential cross sections: CDF

Phys. Rev. D84 (2011) 052006

# Differential cross sections for $P_T(\gamma\gamma) > M_{\gamma\gamma}$ : CDF

Phys. Rev. D84 (2011) 052006



- Low statistics
- Excess of data over theory for  $M_{\gamma\gamma} < 30$  GeV/c<sup>2</sup>

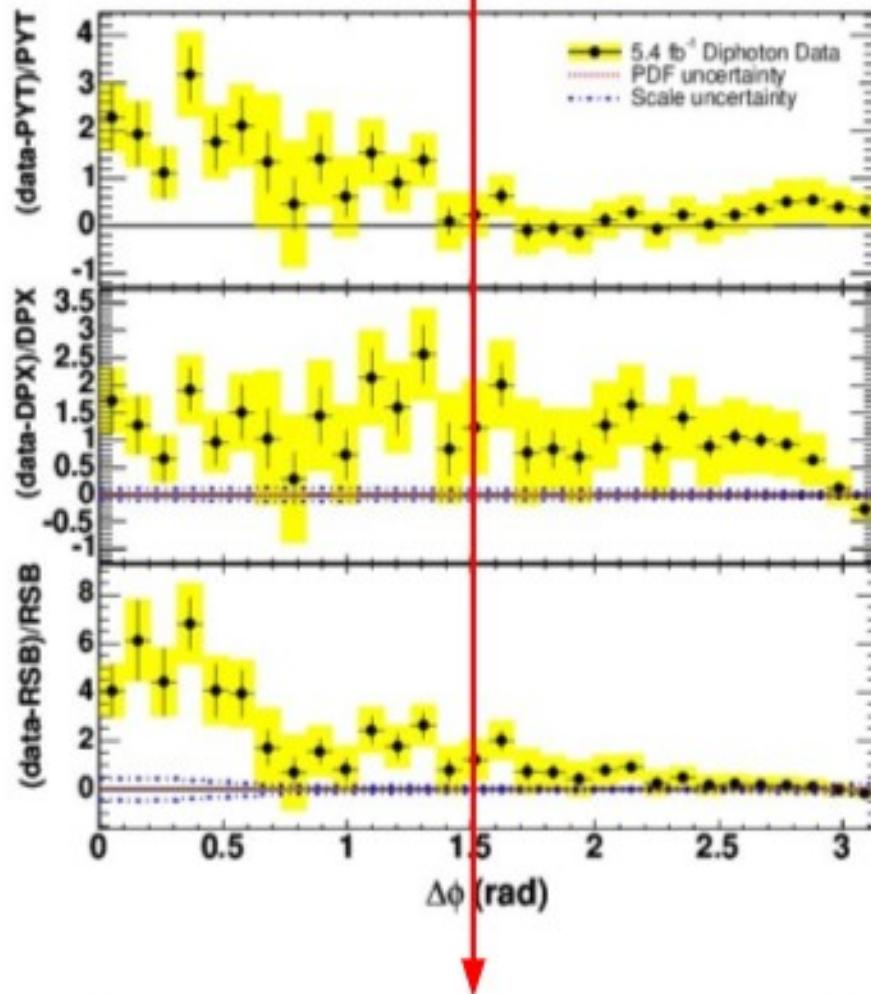
Costas Vellidis, Paris  
Photon workshop (2012)

- Low statistics
- No events below  $P_T(\gamma\gamma) = 20$  GeV/c
- Excess of data over theory for  $P_T(\gamma\gamma) = 20 - 50$  GeV/c (the “Guillet shoulder”)

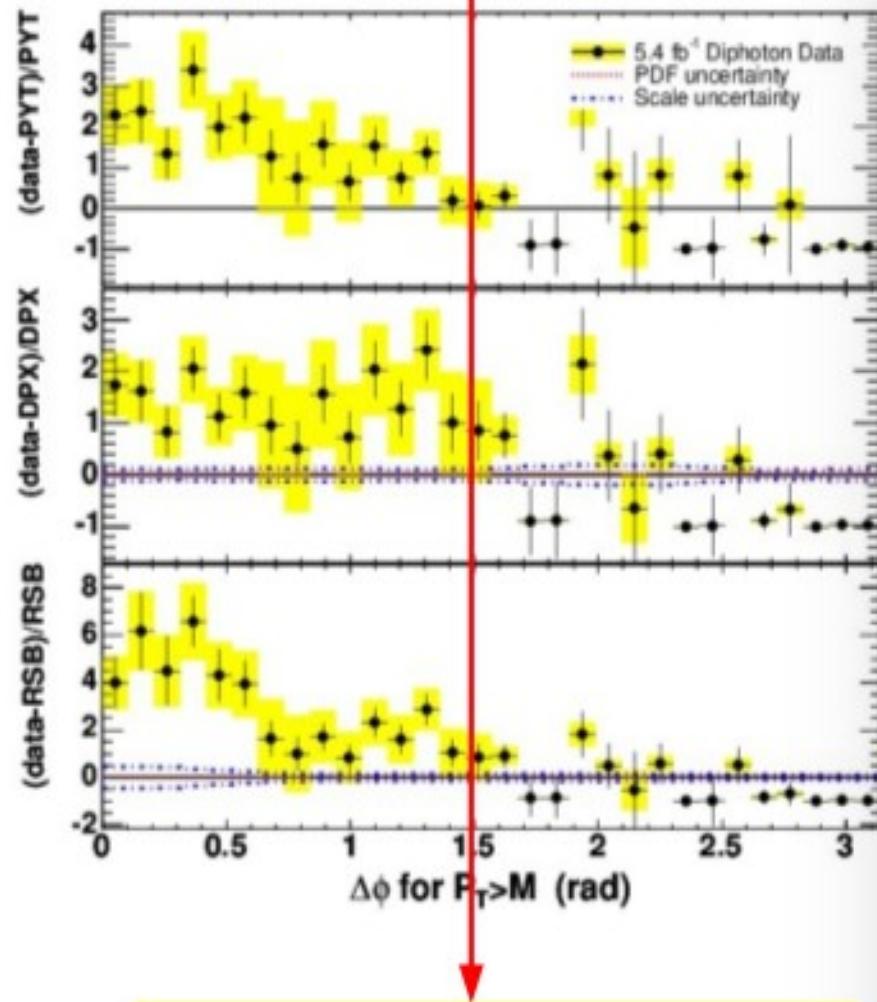
- Low statistics
- Data spectrum harder than predicted for  $\Delta\phi < 1.5$  rad
- Spectrum suppressed for  $\Delta\phi_{\gamma\gamma} > 1.5$  rad

$P_T(\gamma\gamma) > M_{\gamma\gamma} \rightarrow$  Kills born-like contributions

# $\text{Pt}(\gamma\gamma) > M_{\gamma\gamma} \rightarrow$ Kills born-like contributions

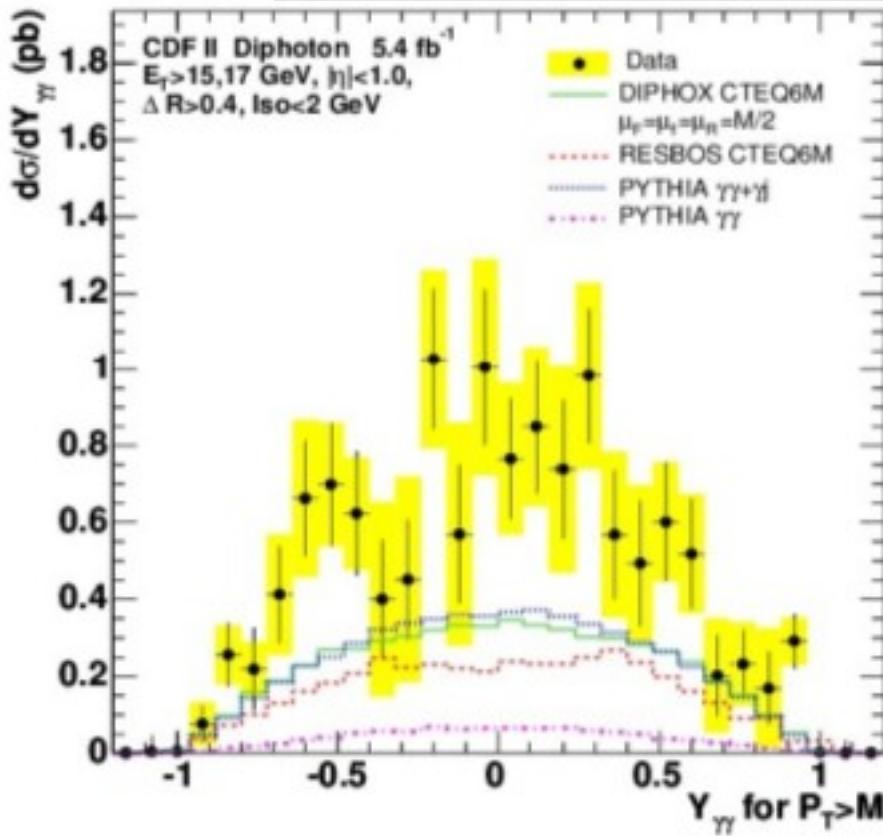


Full Xsection (NLO)

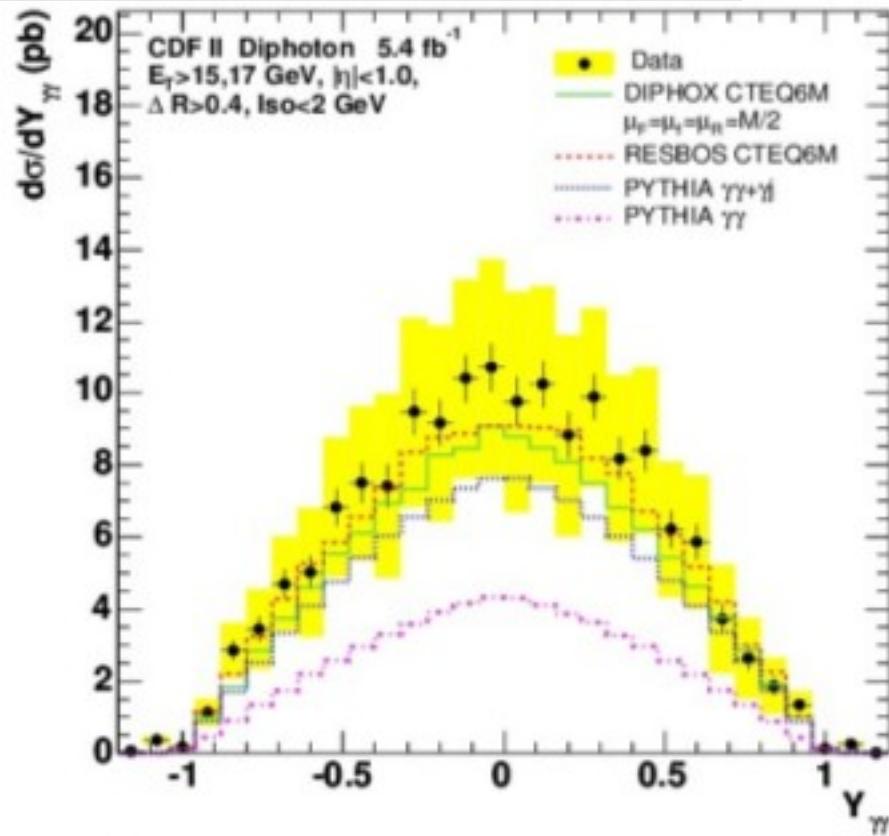


Only real corrections (NLO)

# $Pt(\gamma\gamma) > M_{\gamma\gamma} \rightarrow$ Kills born-like contributions



Only real corrections (NLO)

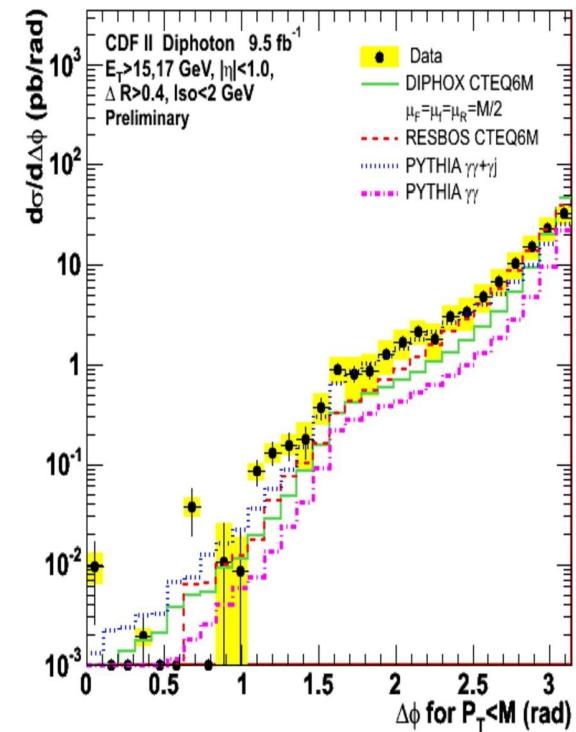
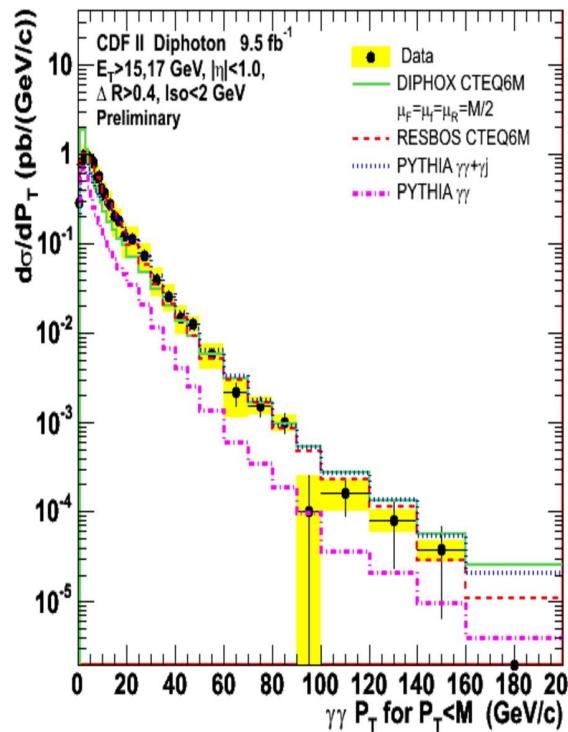
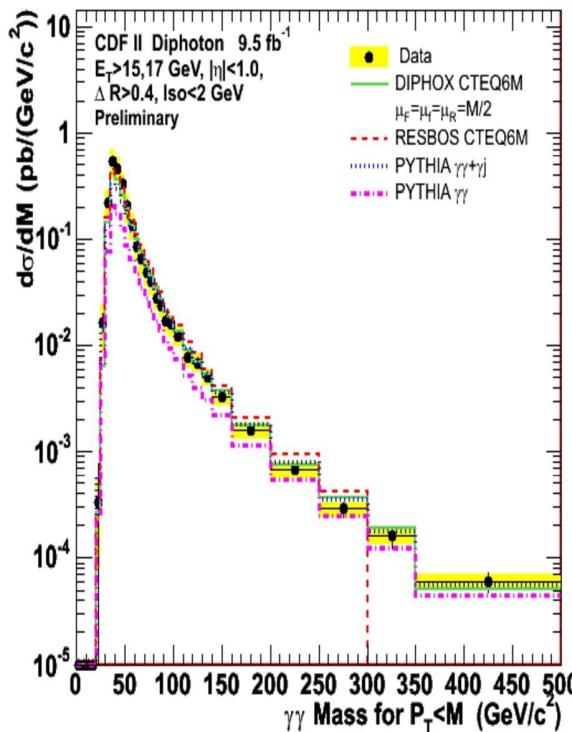


Full Xsection (NLO)

$Pt(\gamma\gamma) > M_{\gamma\gamma} \rightarrow \text{NLO} \sim \text{"LO"}$

# Differential cross sections for $P_T(\gamma\gamma) < M_{\gamma\gamma}$ : CDF

Phys. Rev. D84 (2011) 052006



- Good agreement between data and theory
- No events for  $M_{\gamma\gamma} < 30$  GeV/c<sup>2</sup>

Costas Vellidis, Paris  
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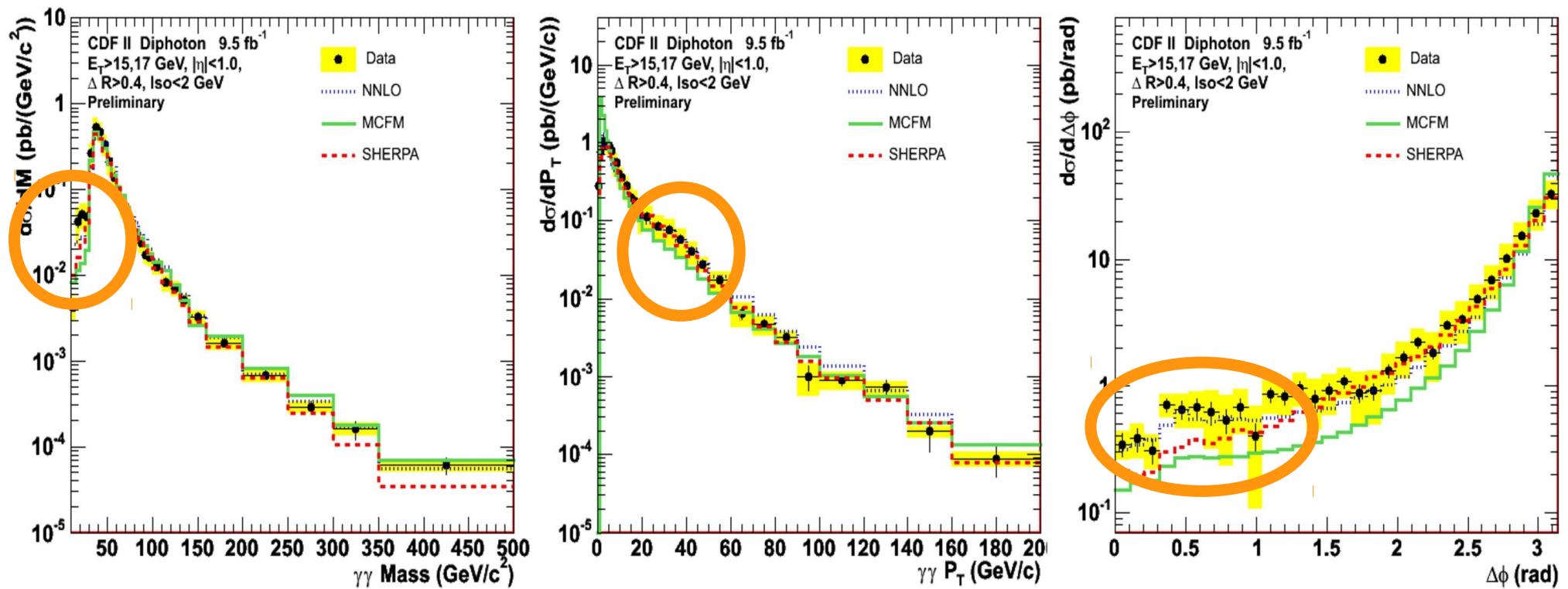
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$P_T(\gamma\gamma) < M_{\gamma\gamma} \rightarrow$  Kills real radiation  
“Only survive” the born-like contributions

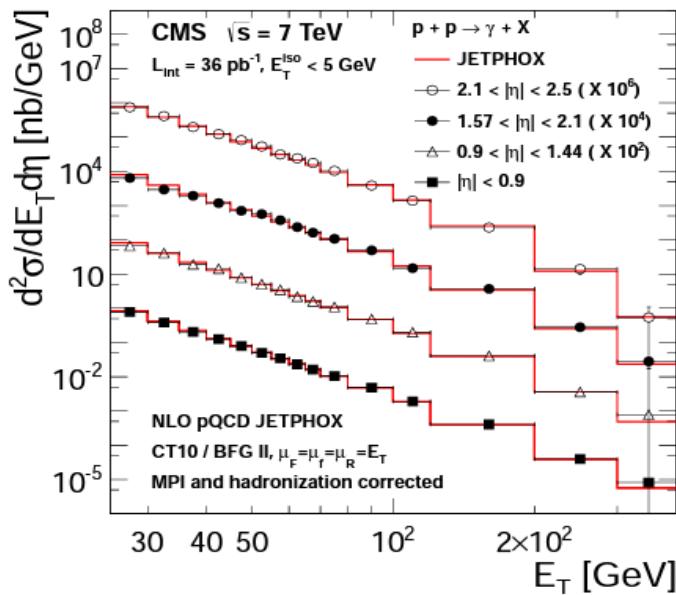
# Differential cross sections

Phys. Rev. Lett. 110 (2013) 10, 101801



Good agreement between the NNLO distributions and the data

# $\gamma + jet \rightarrow ATLAS \text{ and CMS}$

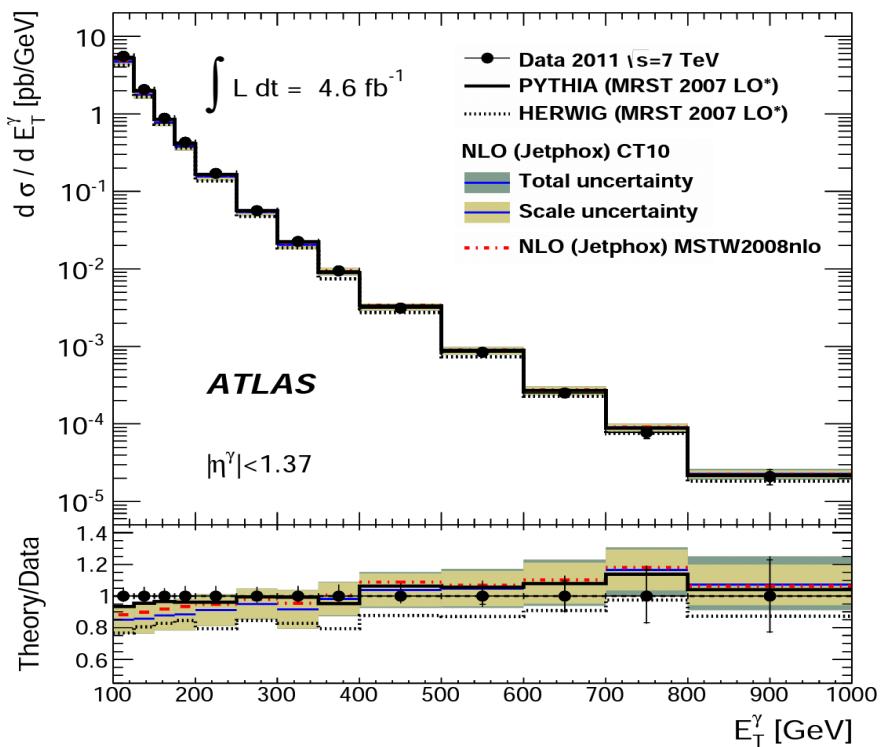


At low ET the predictions tend to be higher than the measured cross section

In some kinematic regimes the Xsection is sensible at PDFs variations

The Xsection has the potential to provide additional constraints on the proton PDFs

Results in good agreement with data



Phys.Rev. D89 (2014) 052004

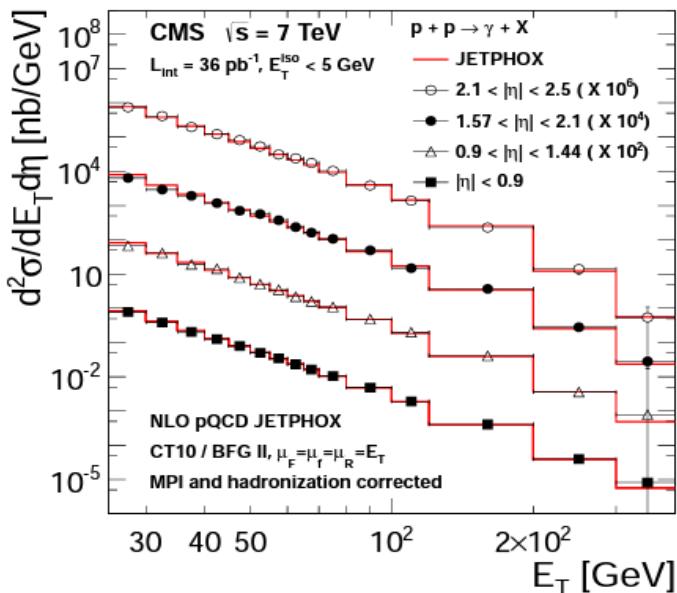
At low ET the data tends to be higher than the NLO predictions

Phys.Rev. D84 (2011) 052011

Phys.Rev.Lett. 106 (2011) 082001

Exp. Details in Ruggero's talk

# $\gamma + jet \rightarrow ATLAS \text{ and CMS}$

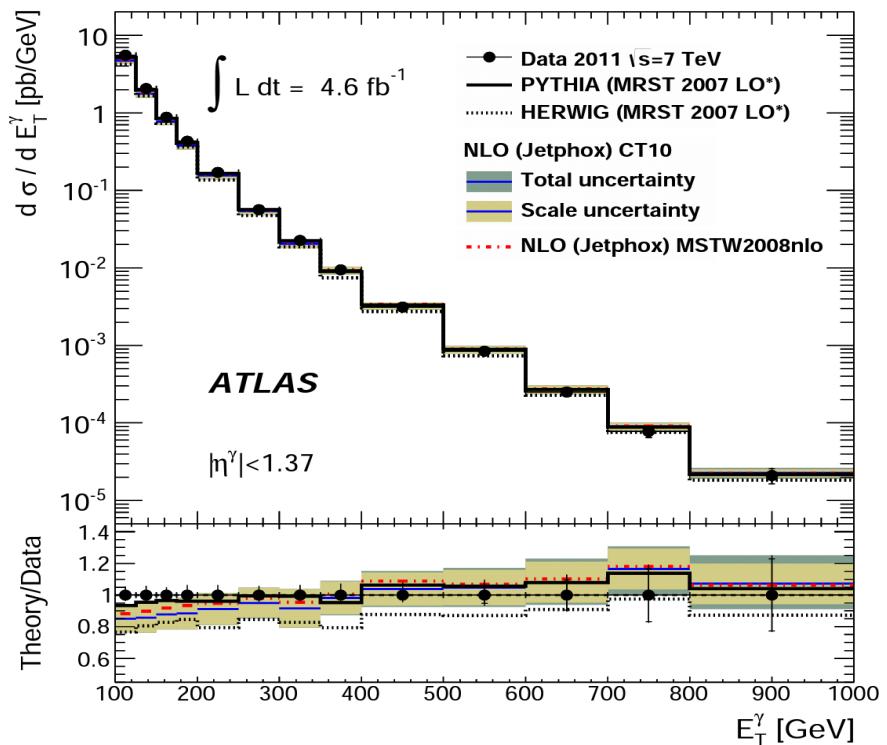


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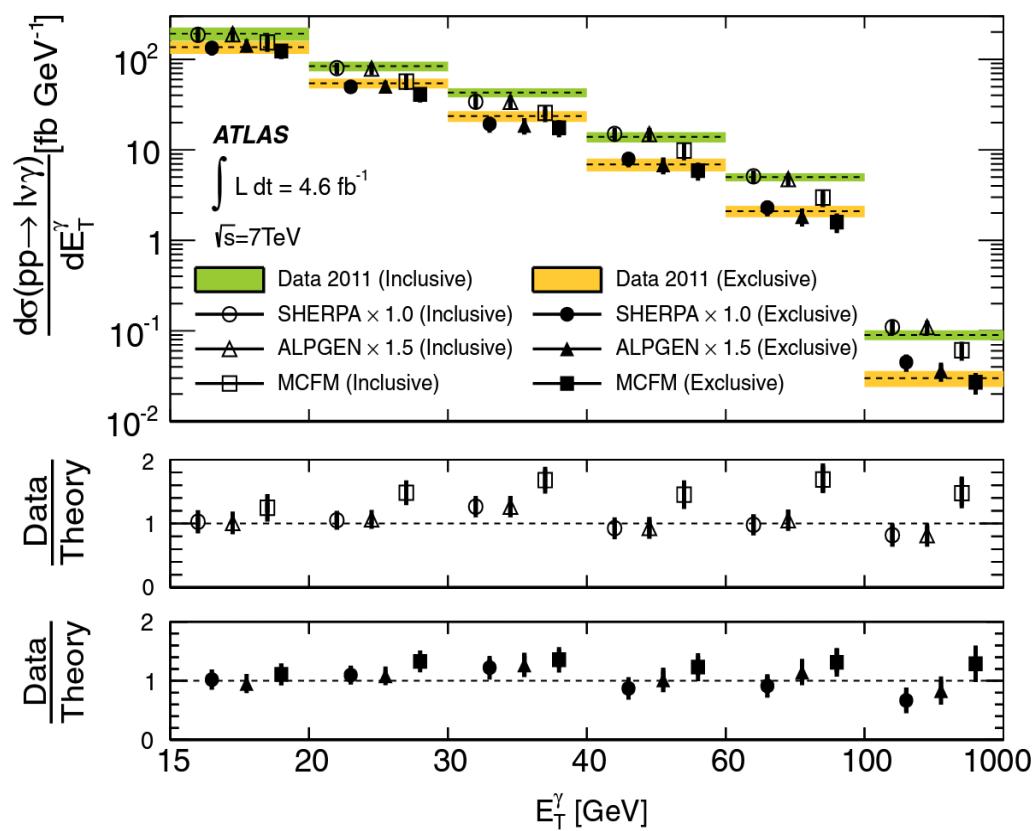


Phys. Rev. D89 (2014) 052004

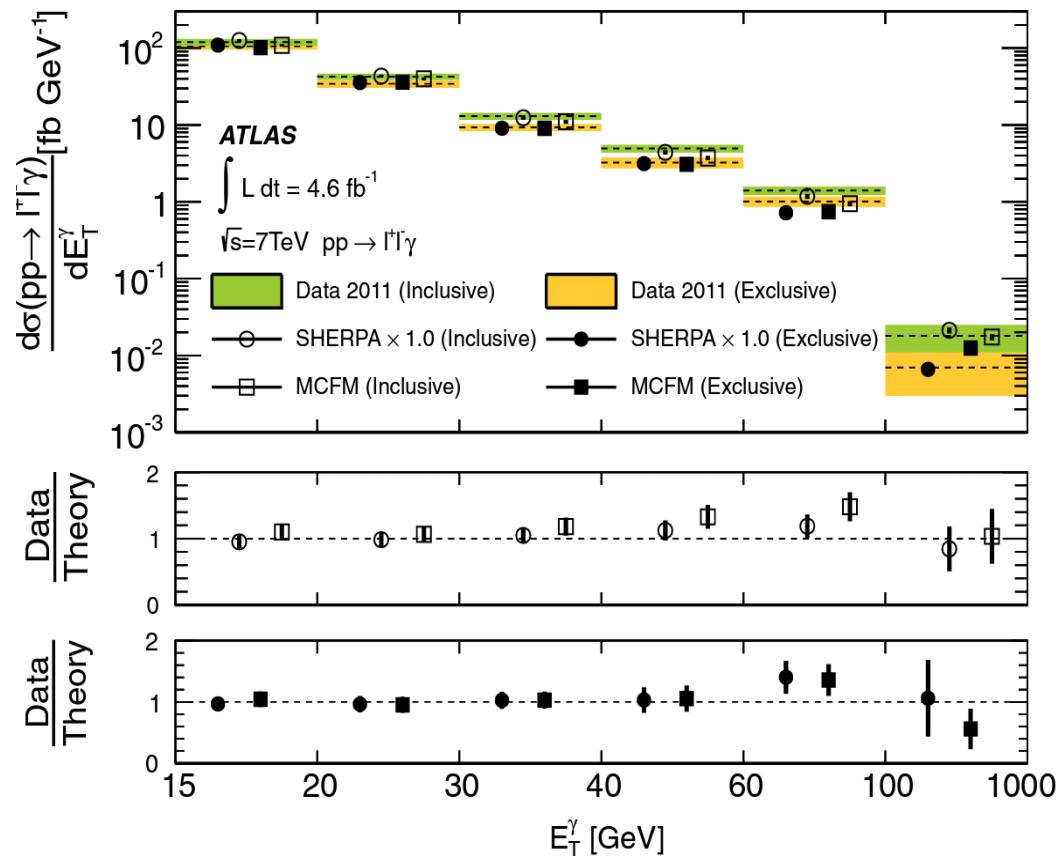
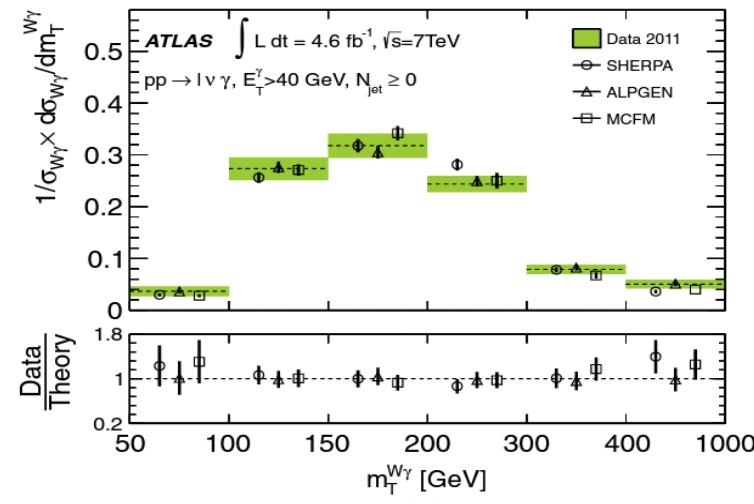
At low ET the data tends to be higher than the NLO predictions

ATLAS and CMS use different values for Etmax  
 $\text{ETmax(Atlas)} > \text{ETmax(CMS)}$

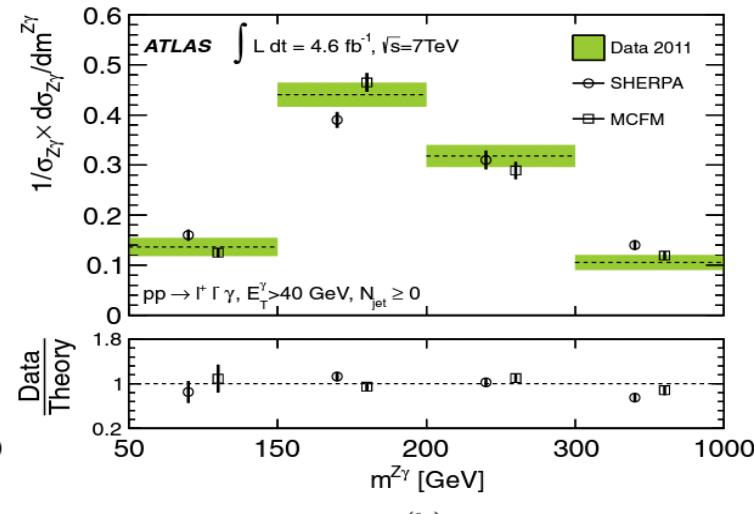
# V $\gamma$ production



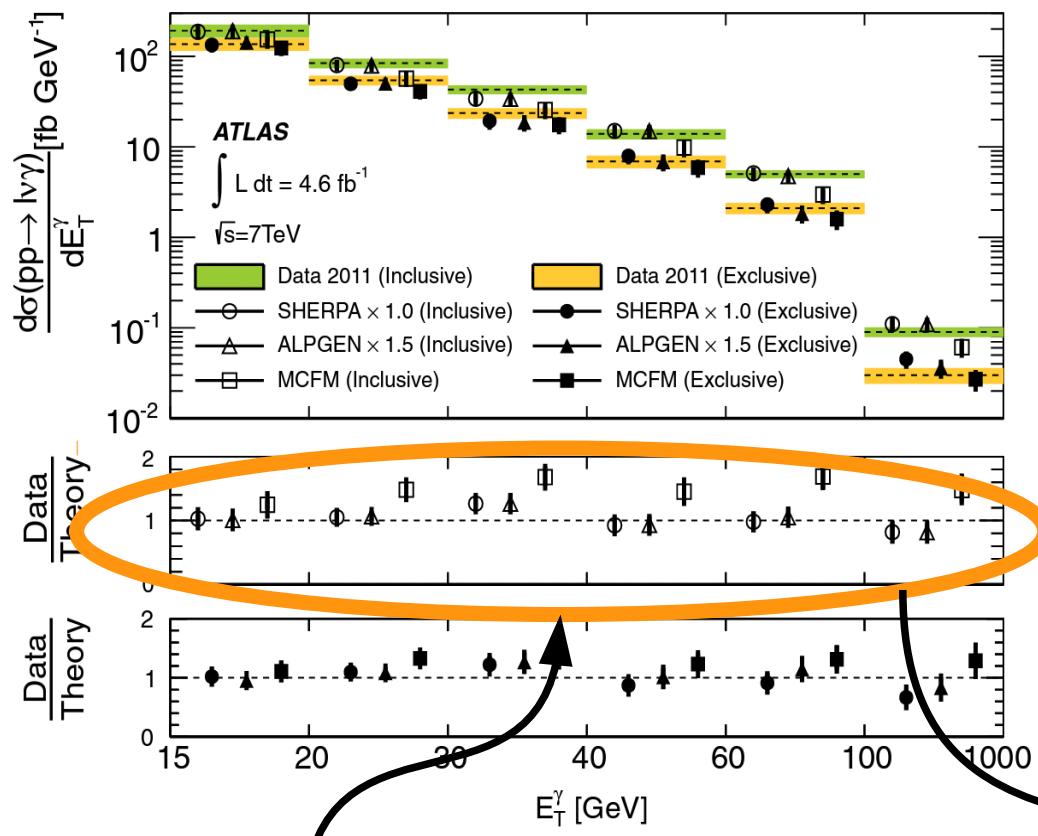
Results in  
good  
agreement  
with data



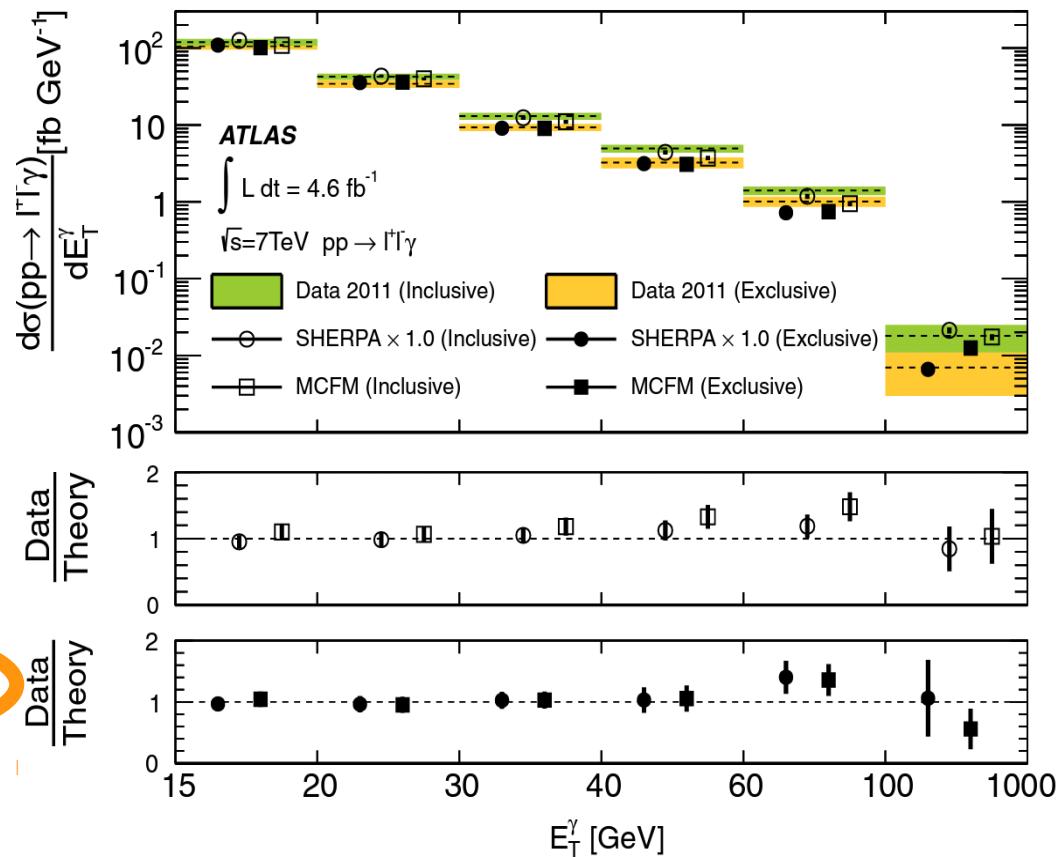
Phys.Rev. D87 (2013) 112003



# $V\gamma$ production



NLO predictions do not include multiple q/g emissions

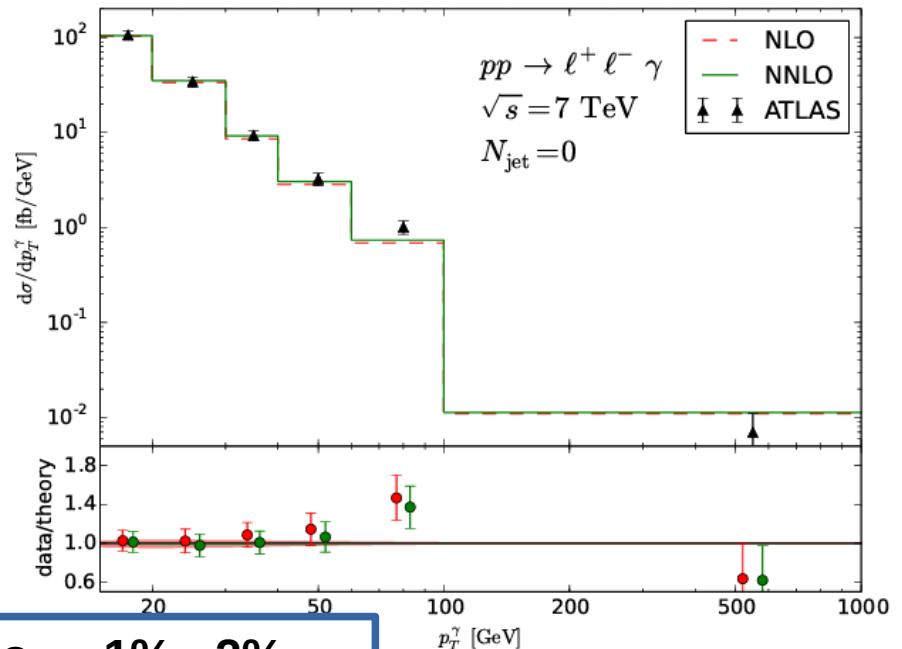
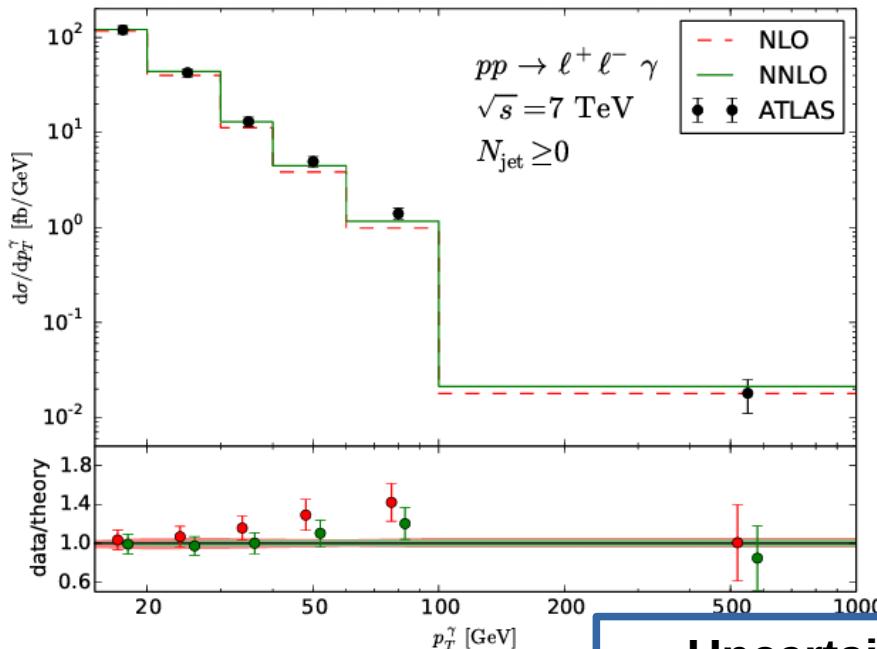
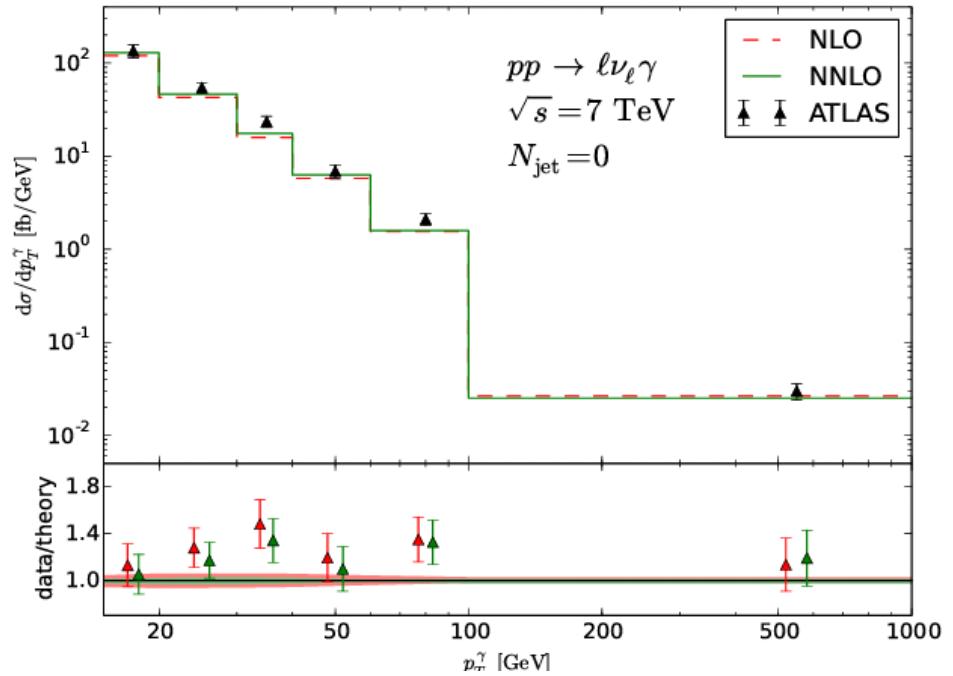
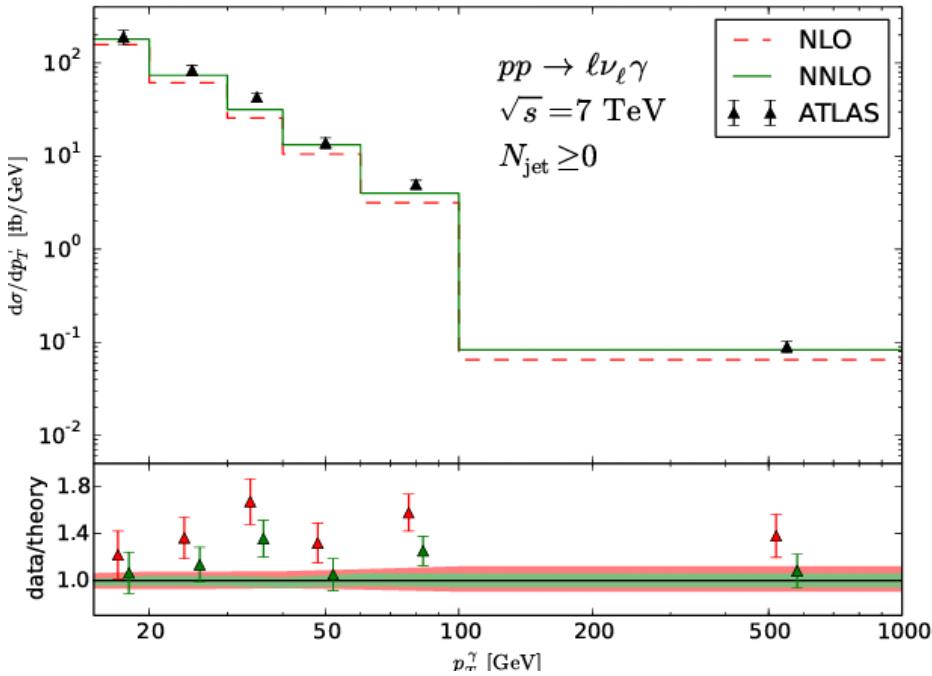


Phys.Rev. D87 (2013) 112003

This constitutes a motivation to go at NNLO in which we have up to 2-jets in the final state

# $\ell\gamma$ production NNLO

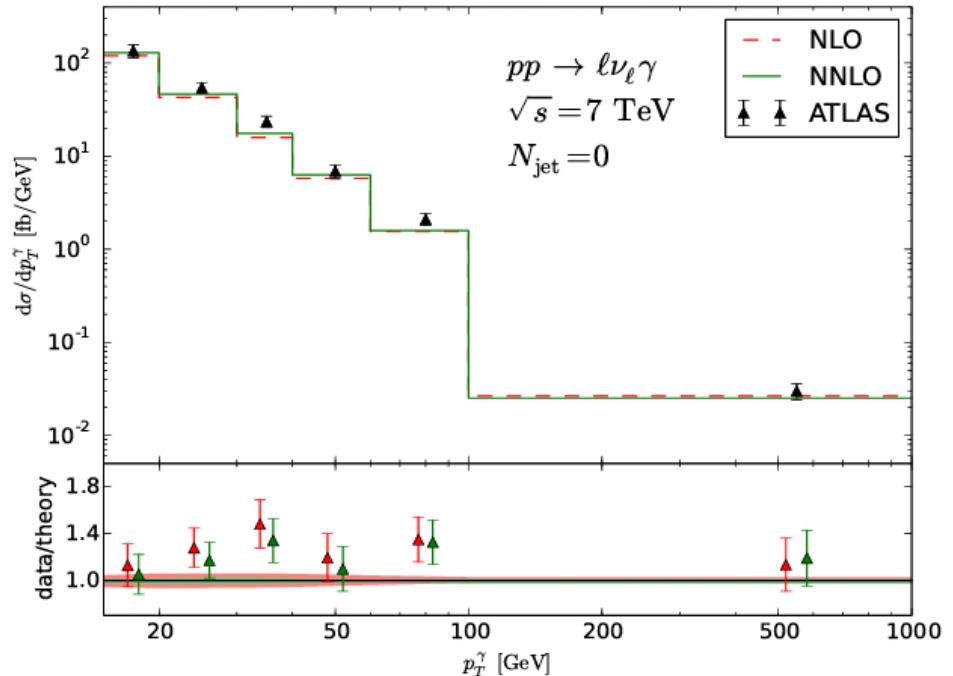
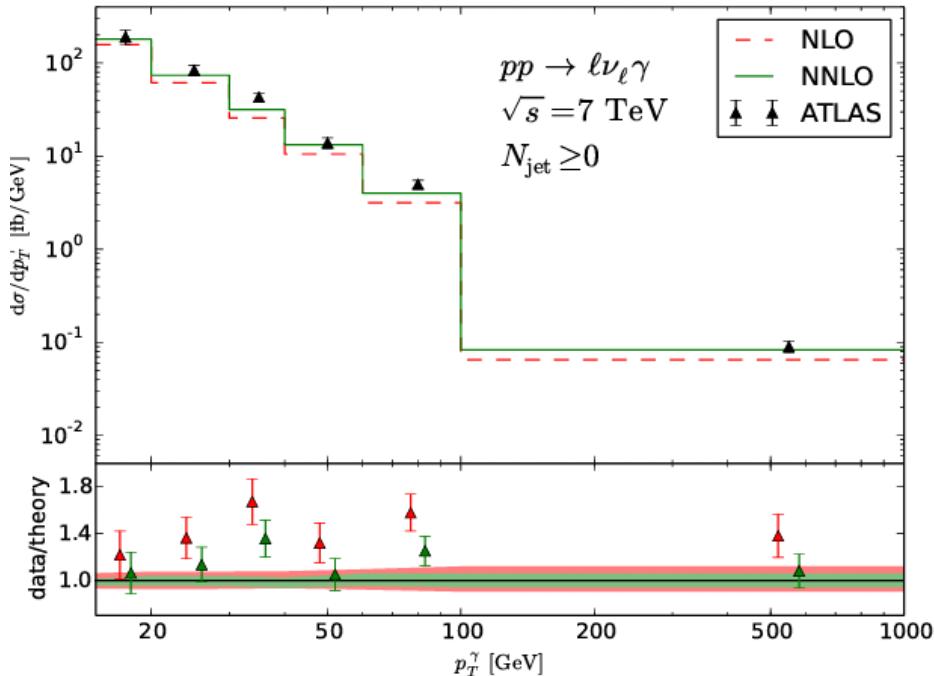
Grazzini, Kallweit, Rathlev, Torre



Uncertainties → 1% - 2%

# $V\gamma$ production NNLO

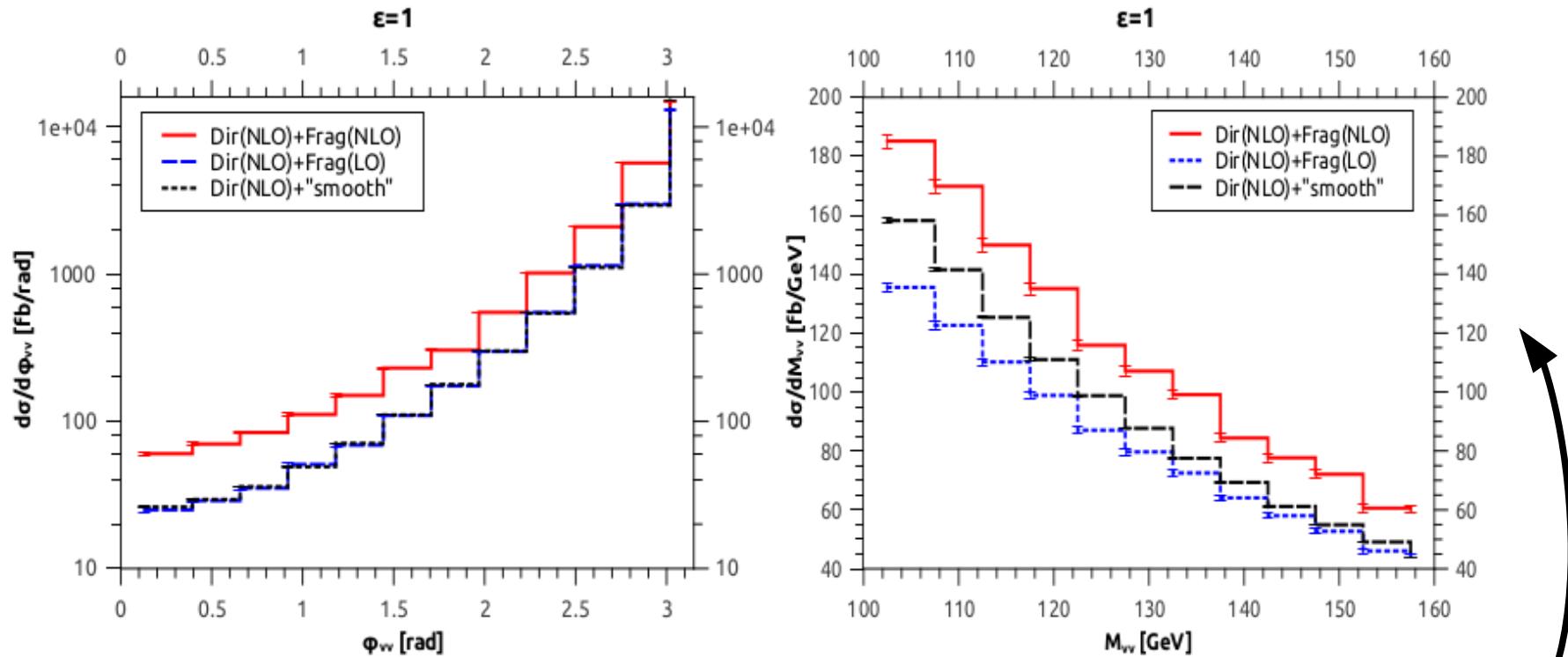
Grazzini, Kallweit, Rathlev, Torre



In the exclusive case, the excess of the measured fiducial cross sections over the theoretical prediction is reduced from  $1.6\sigma$  to  $1.2\sigma$  when going from NLO to NNLO

In the inclusive case, the excess of the data over the theoretical prediction is reduced from  $2\sigma$  to below  $1\sigma$  when going from NLO to NNLO

# What we learnt from $\gamma\gamma$



Fragmentation could be very relevant!!!!

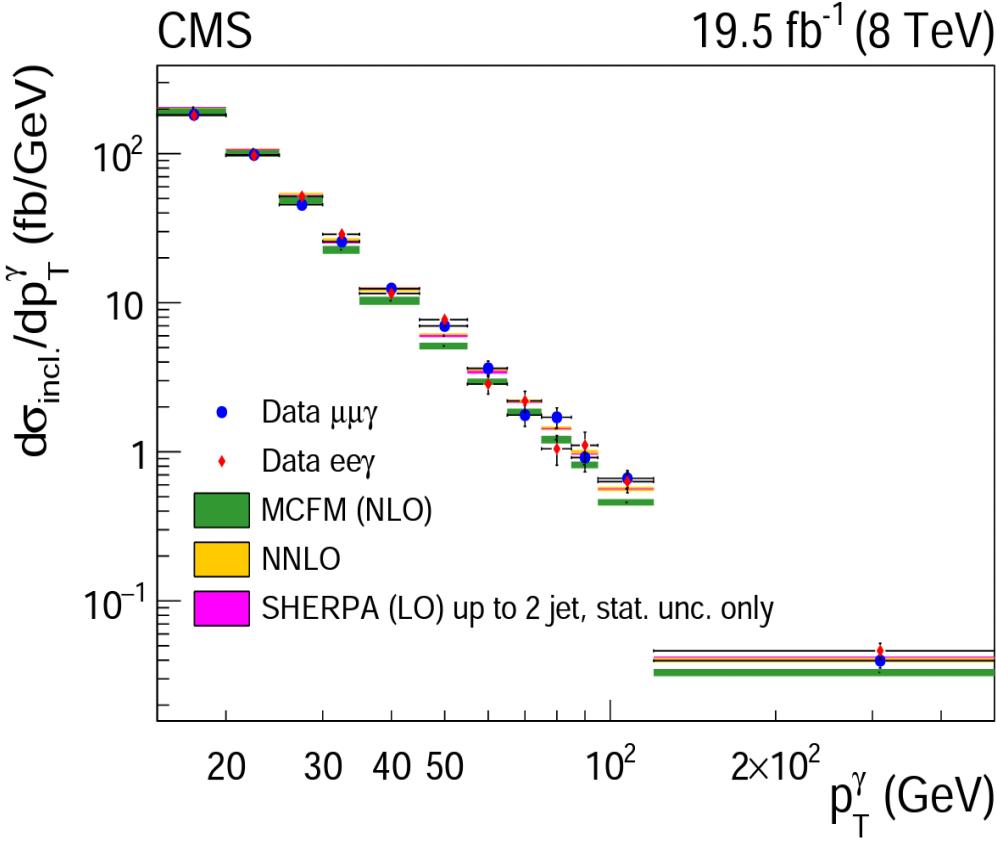
$$E_T \max \sim 20 \text{ GeV}$$

$\gamma\gamma ATLAS$

$$E_T < \epsilon_\gamma p_T^\gamma , \quad \epsilon_\gamma = 0.5$$

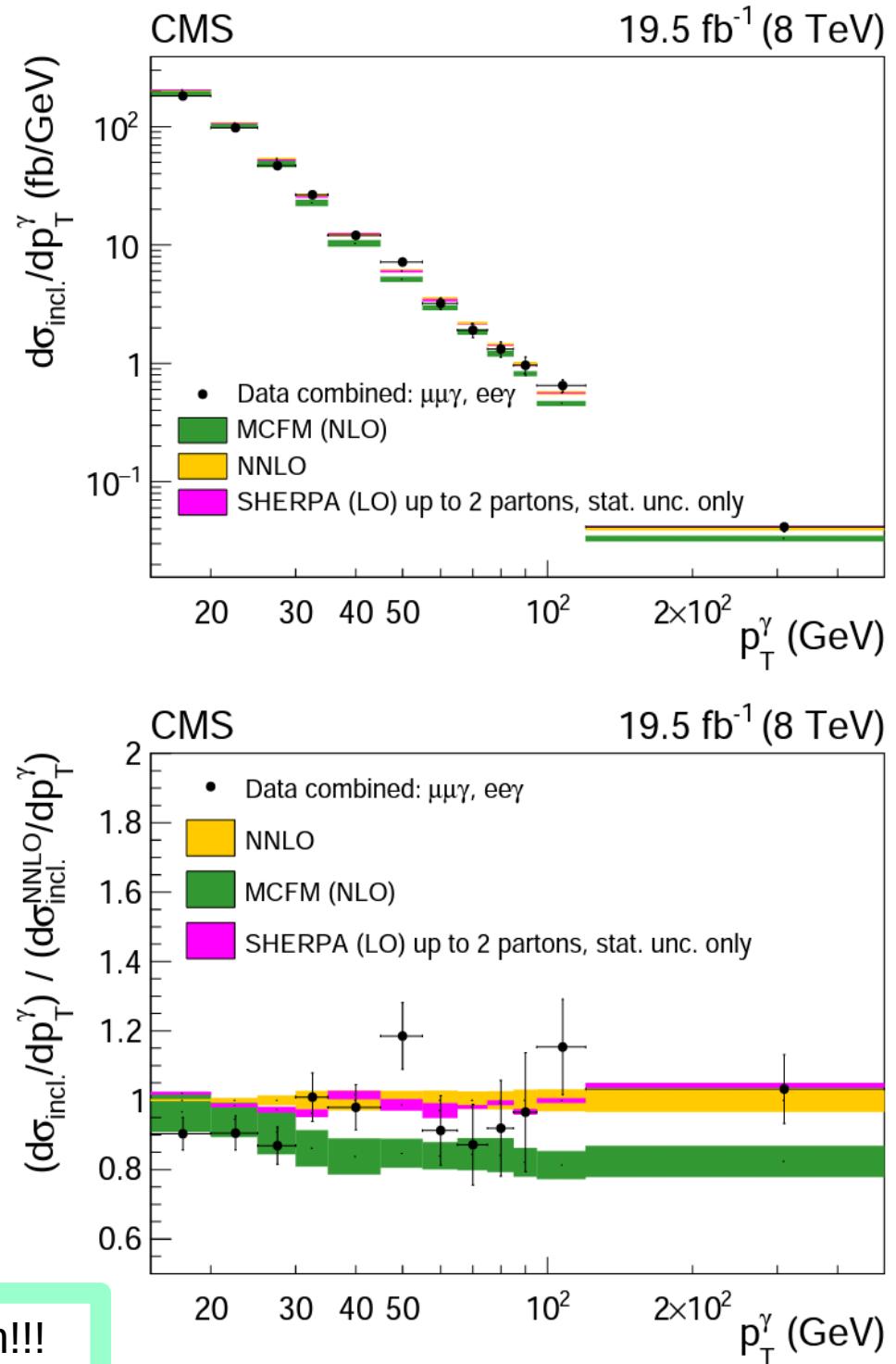
# Z $\gamma$ production

JHEP04 (2015) 164



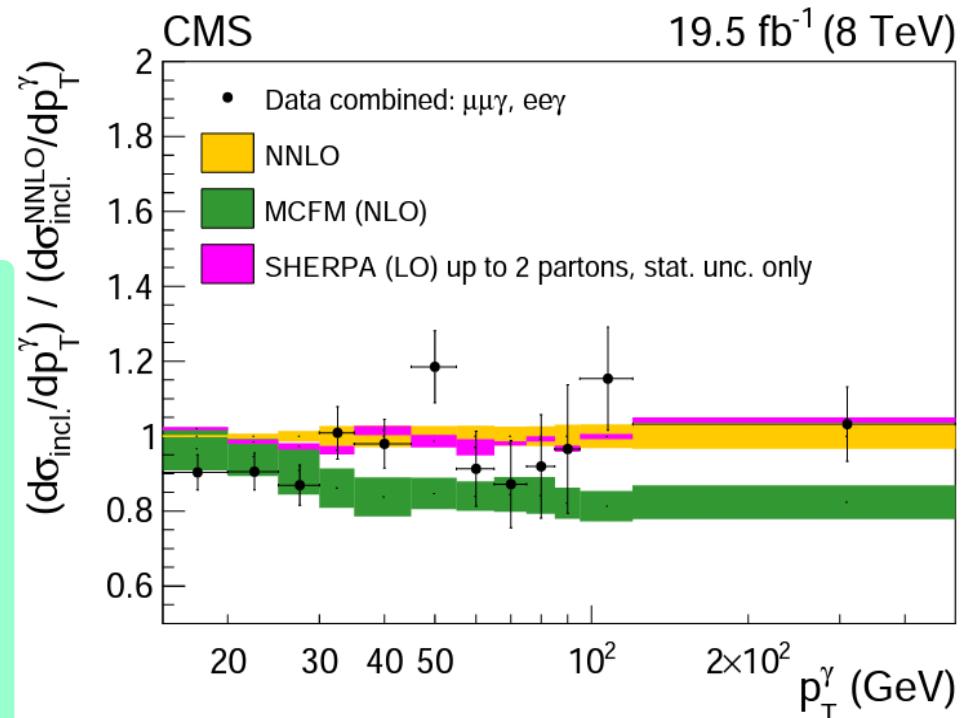
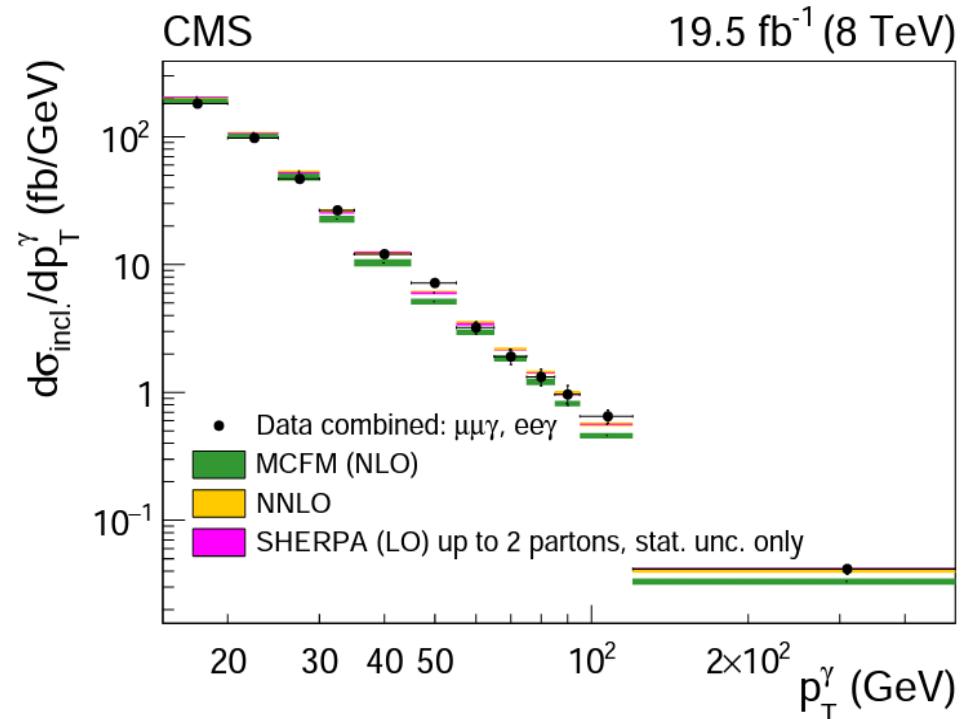
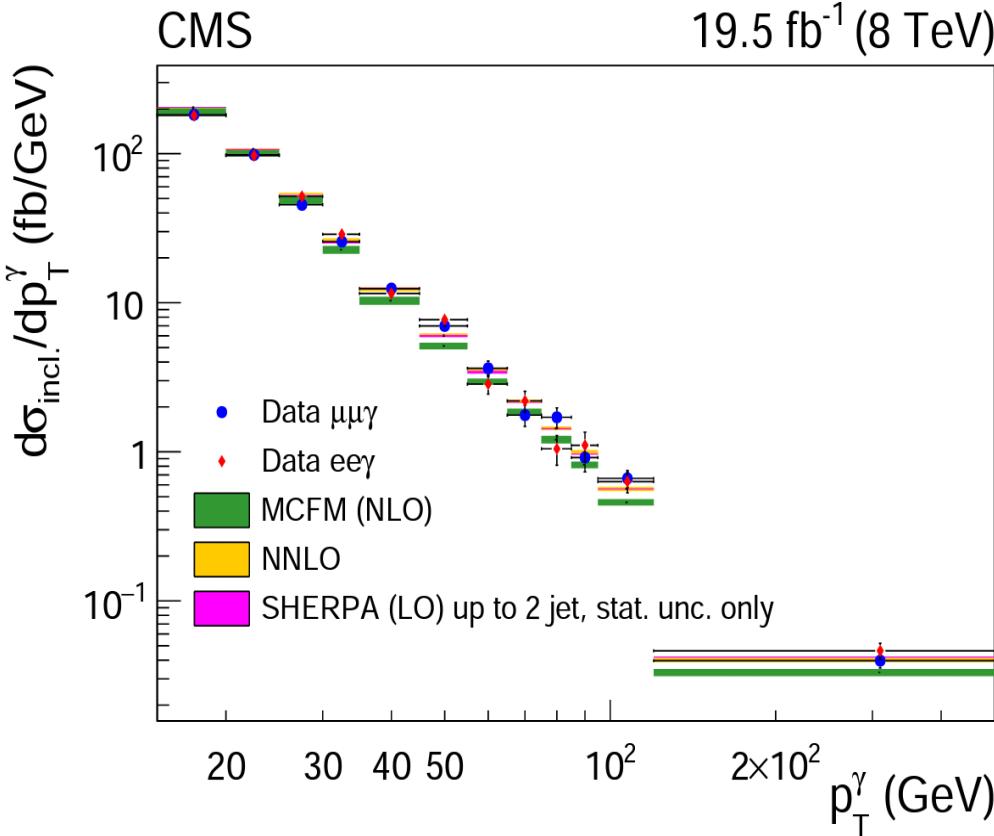
$I_{gen} < 5$  GeV

to exclude photons to jet fragmentation!!!



# Z $\gamma$ production

JHEP04 (2015) 164



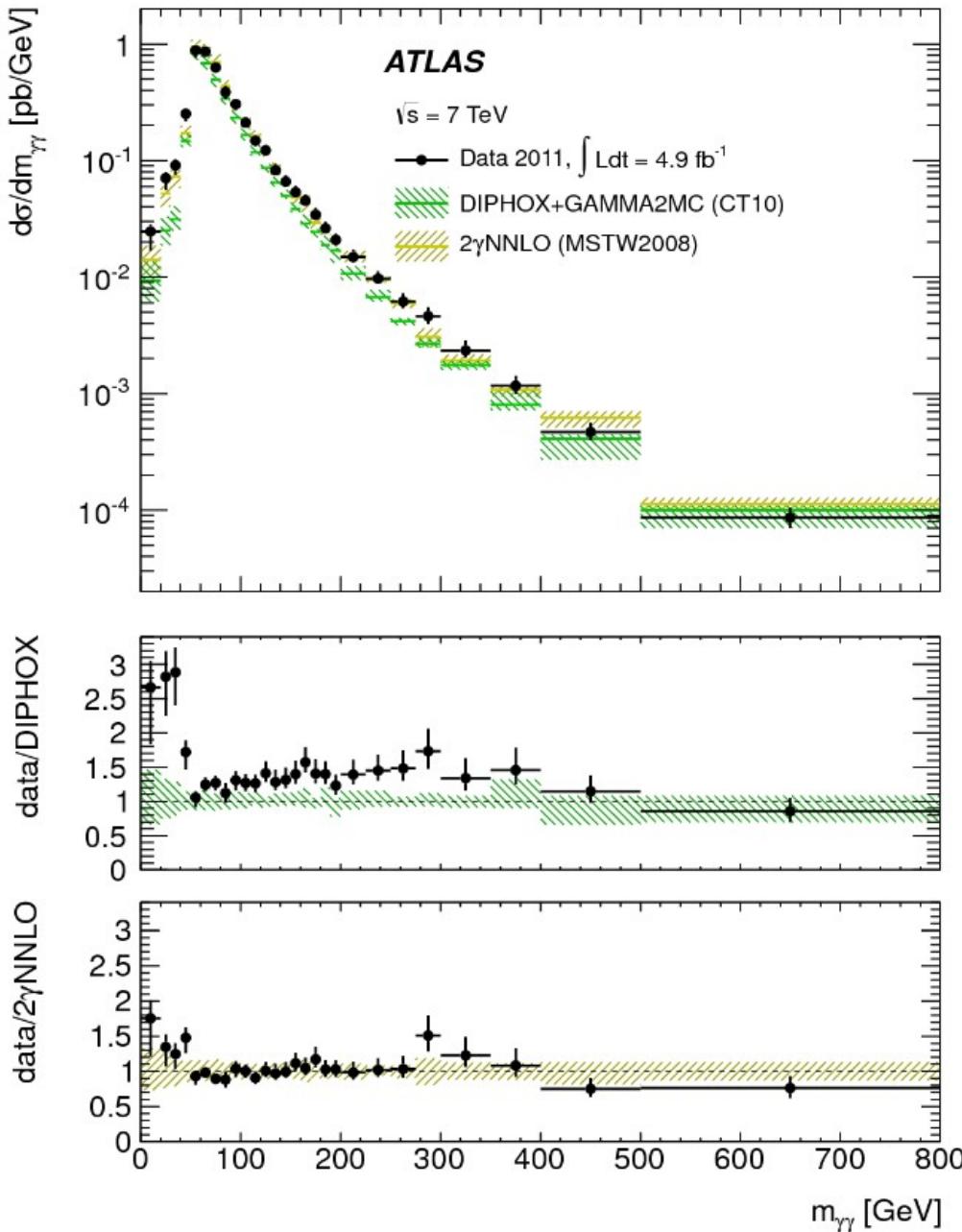
- + Are important the EW contributions?
- + The isolation issues are under control?
- + If the last two items are under control : can we repeat the study of CDF in order to identify the origin of the discrepancies? (missing higher order correction terms → Real radiation)

# **ATLAS results $\gamma\gamma$**

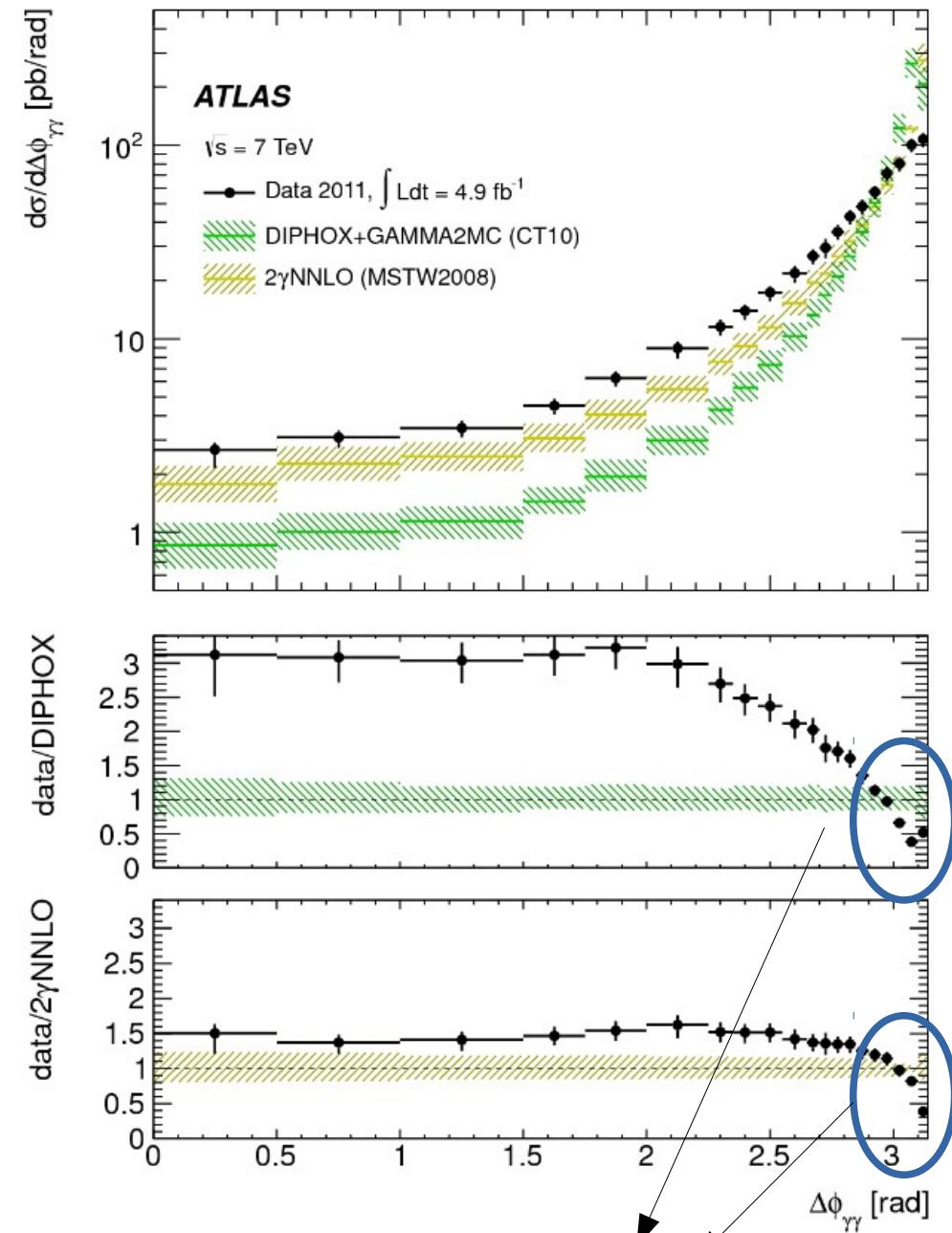
$p_T^{\text{harder}} \geq 25 \text{ GeV}, \quad p_T^{\text{softer}} \geq 22 \text{ GeV},$   
 $|y_\gamma| < 1.37 \vee 1.52 < |y_\gamma| \leq 2.37,$   
 $E_T \max = 4 \text{ GeV}, \quad n = 1, \quad R = 0.4,$   
 $R_{\gamma\gamma} = 0.4$

# ATLAS results $\gamma\gamma$

arXiv:1211.1913 [hep-ex].

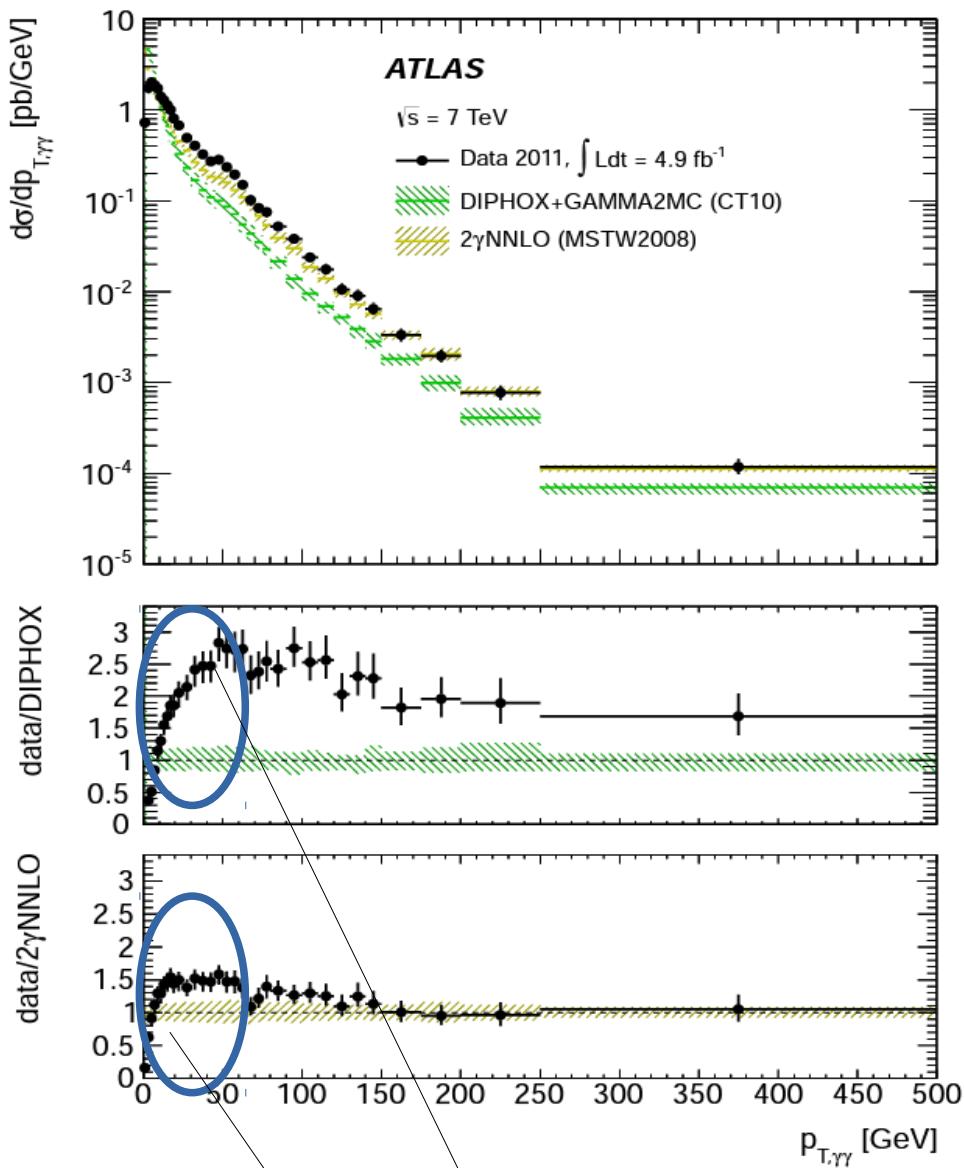


Uncertainties  $\rightarrow 6\% - 8\%$



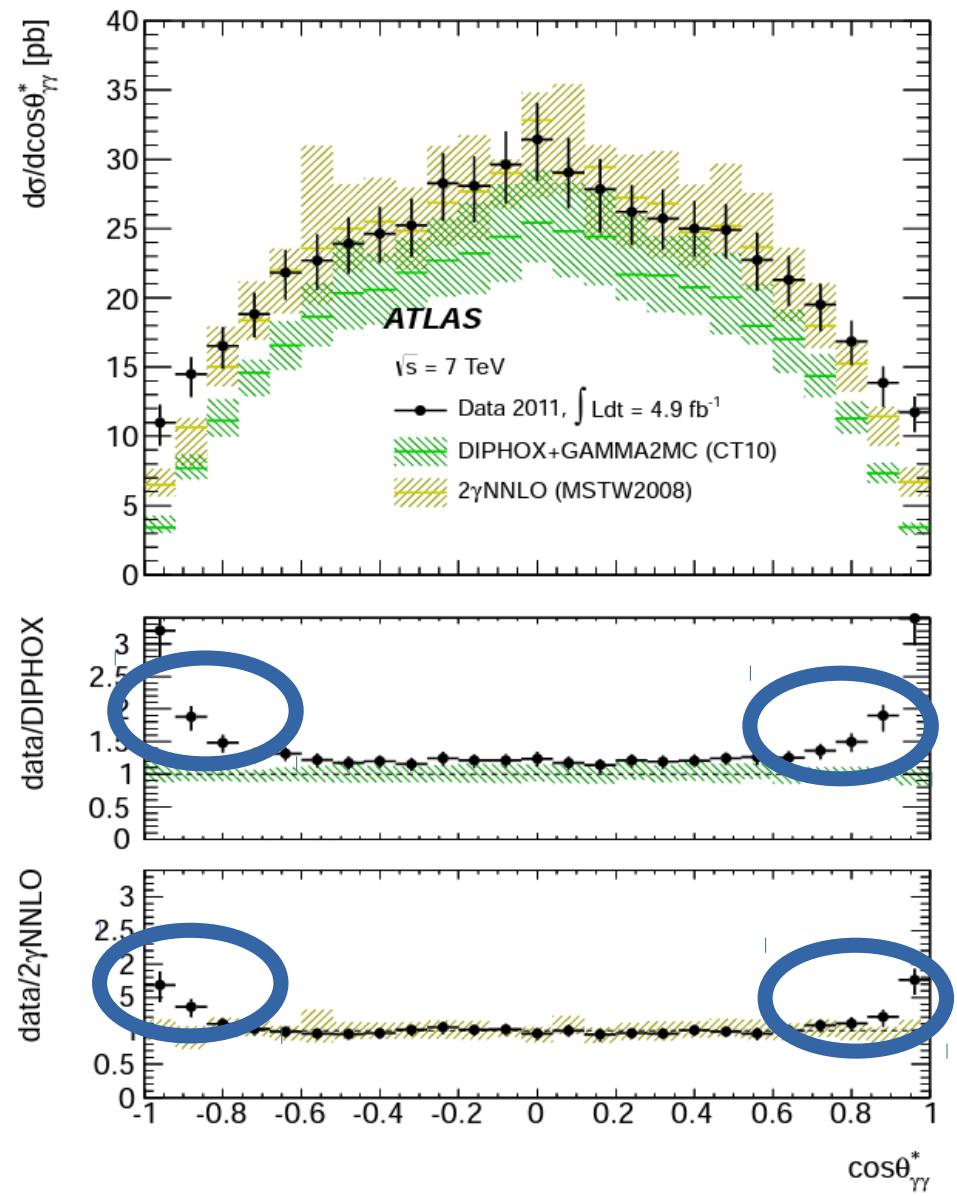
Fixed order tools

# ATLAS results $\gamma\gamma$



Fixed order tools

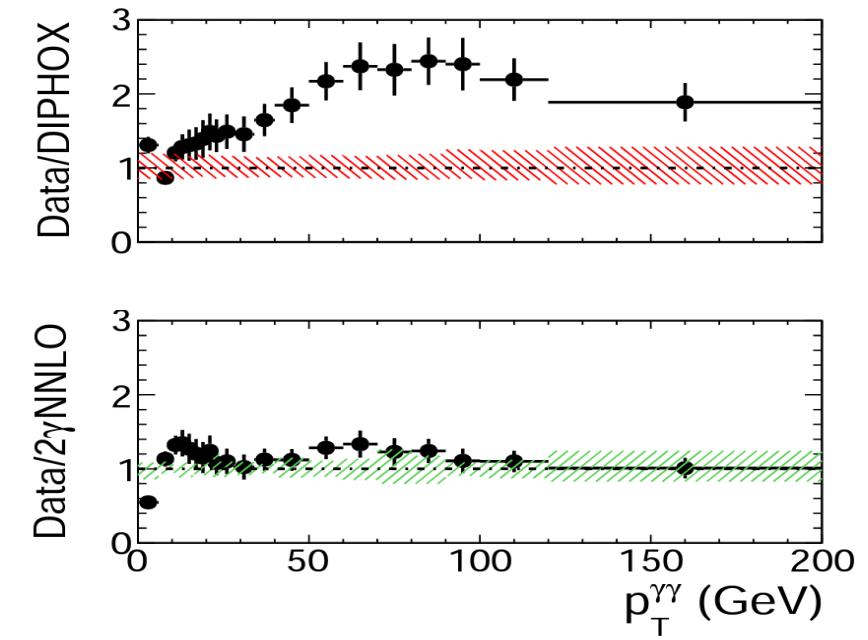
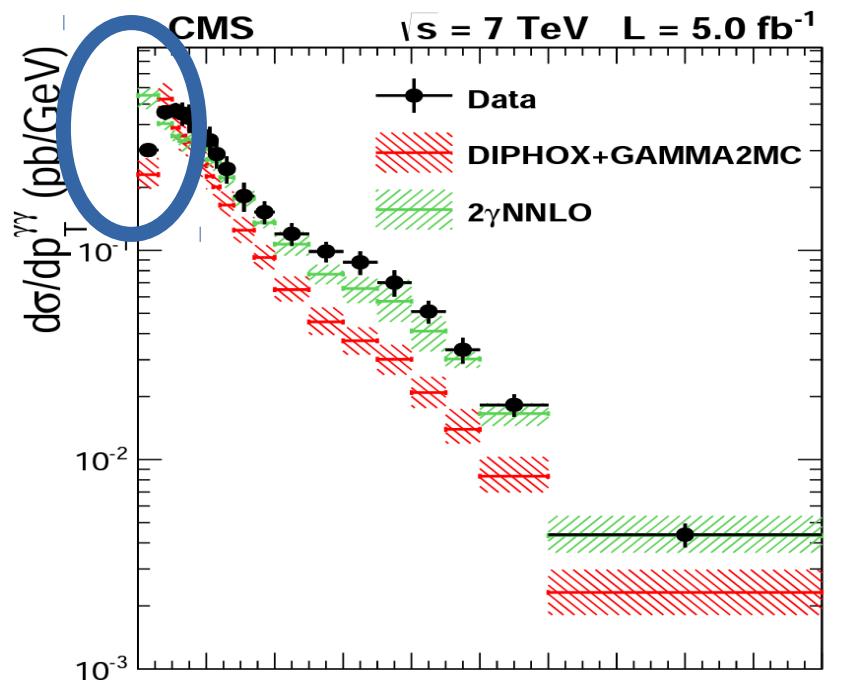
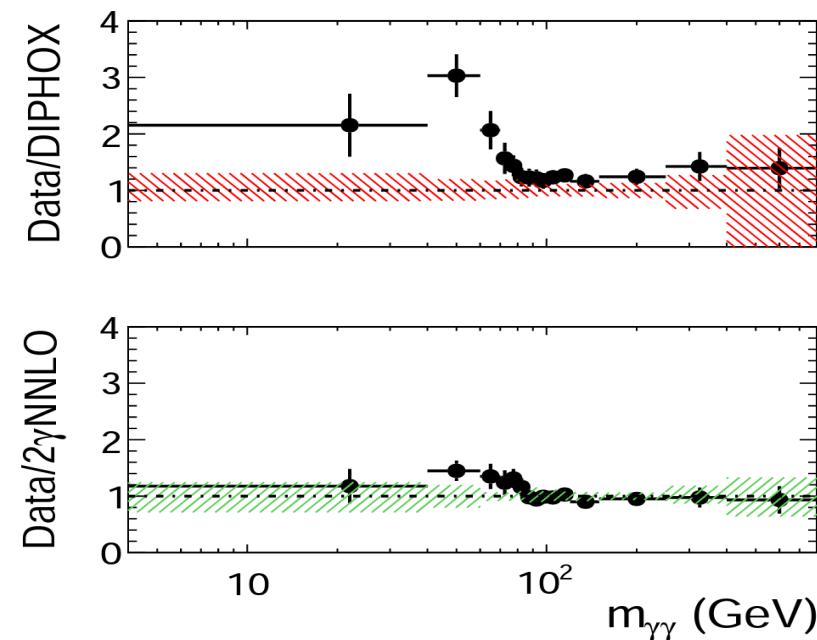
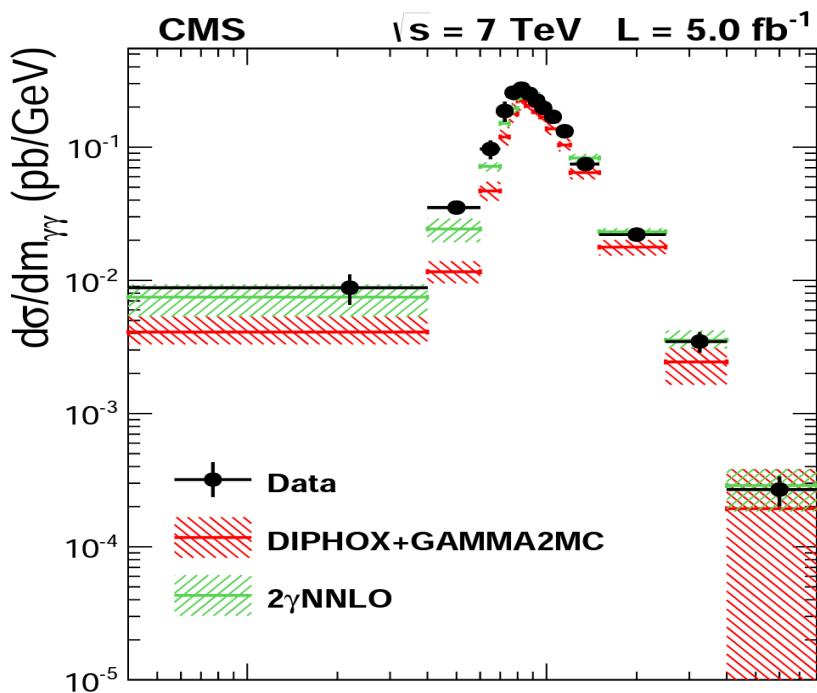
Uncertainties  $\rightarrow 6\% - 8\%$  due to the opening of the gg channel which is “effectively” LO at NNLO



$p_T^{\text{harder}} \geq 40 \text{ GeV}, \ p_T^{\text{softer}} \geq 25 \text{ GeV},$   
 $|y_\gamma| < 1.44 \ \vee \ 1.57 < |y_\gamma| \leq 2.5,$   
 $E_T \max = 5 \text{ GeV}, \ n = 0.05, \ R = 0.4,$   
 $R_{\gamma\gamma} = 0.45$

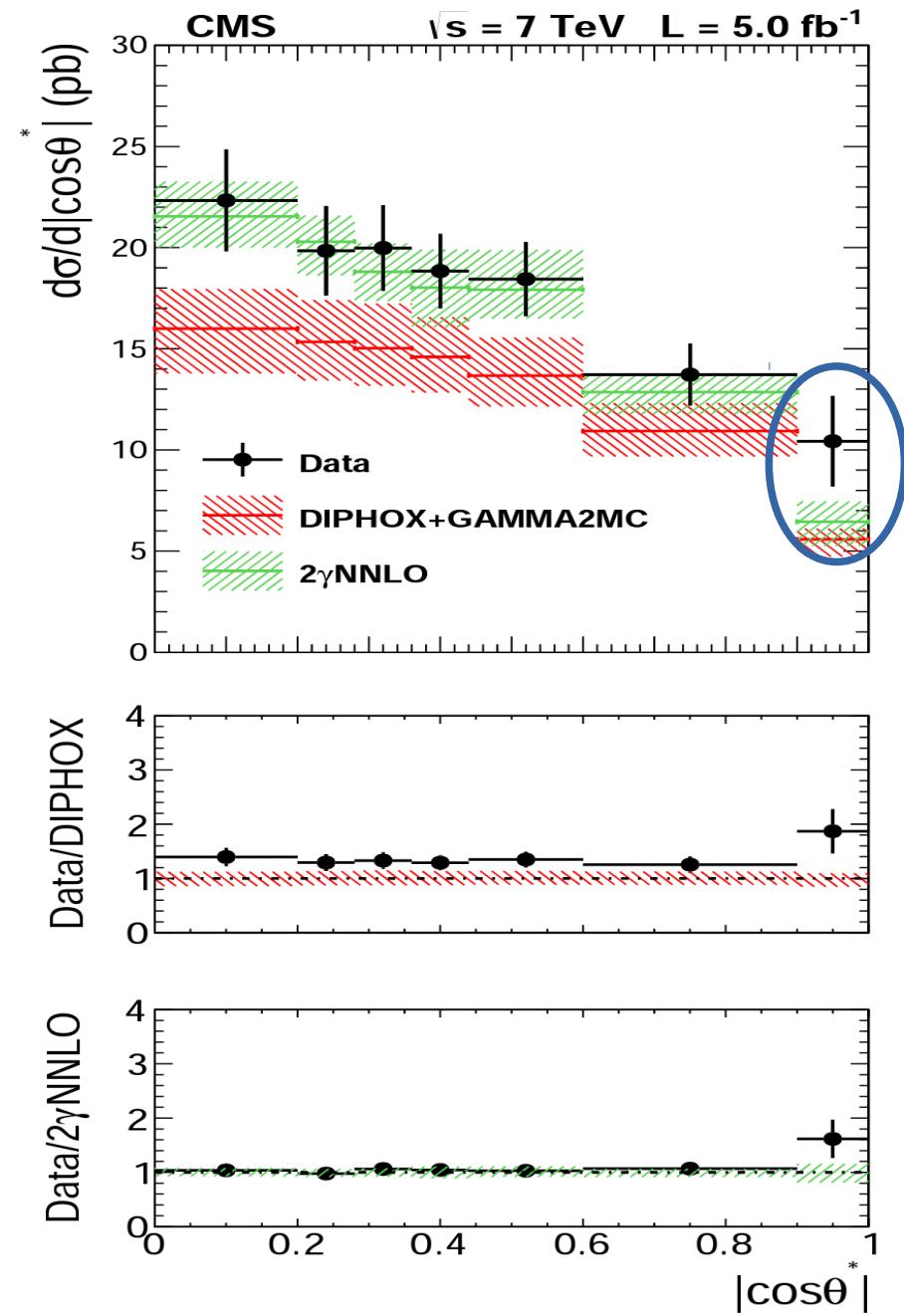
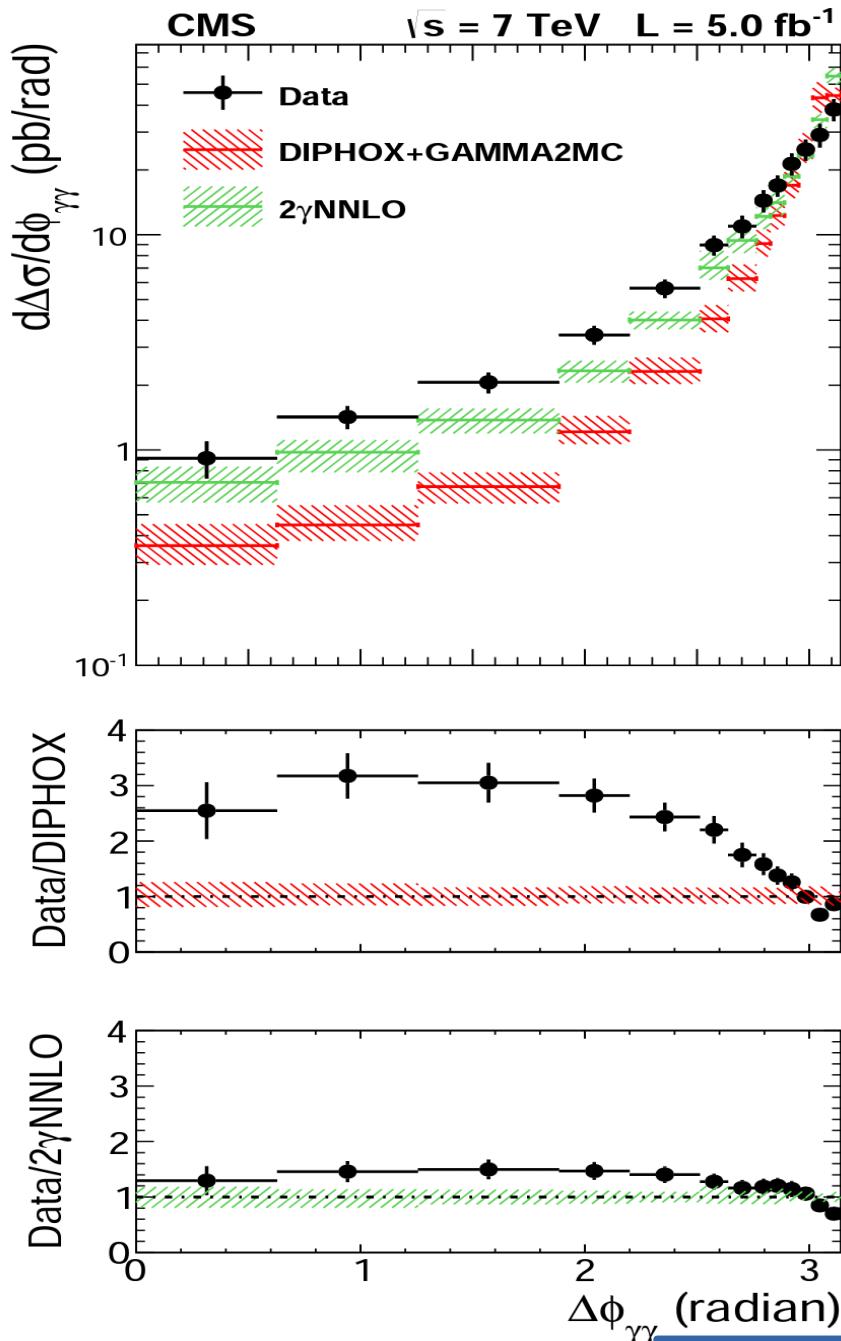
# CMS results $\gamma\gamma$

arXiv:1405.7225



# CMS results $\gamma\gamma$

arXiv:1405.7225

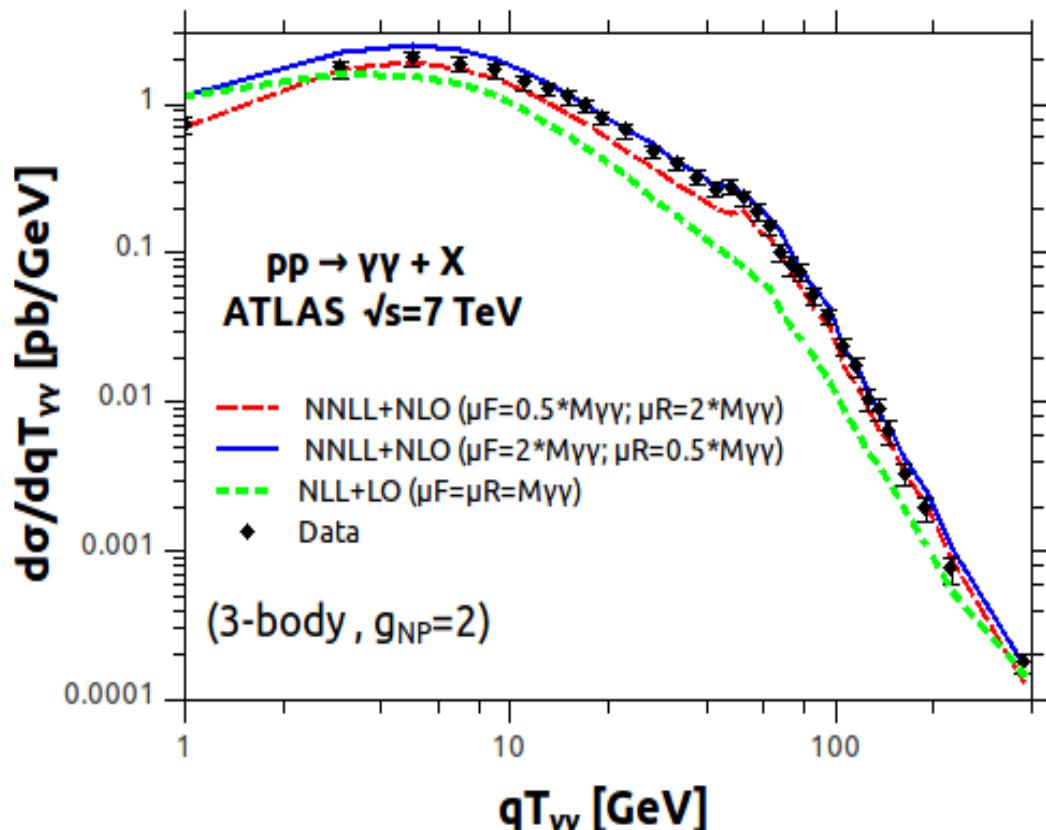
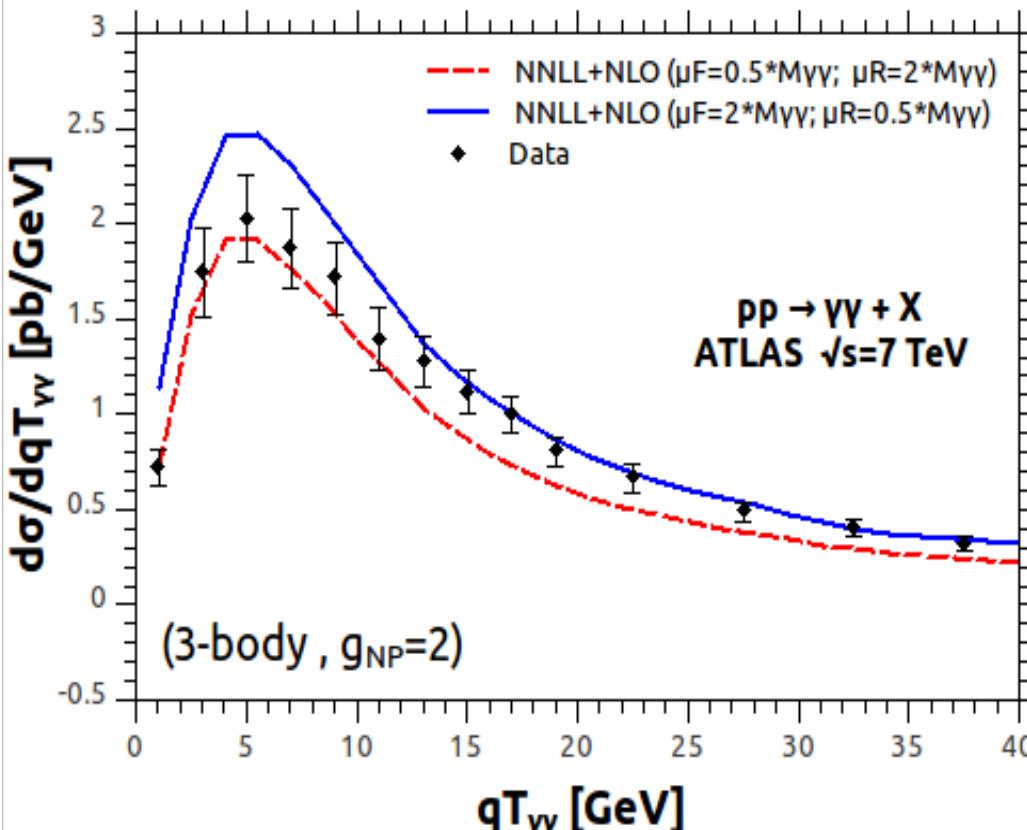


Uncertainties  $\rightarrow 6\% - 8\%$

# Resummation → ATLAS $\gamma\gamma$

LC, Coradeschi, de Florian

First results!



$$S_{NP}^a = \exp(-C_a g_{NP} b^2)$$

$a = F$  for  $q\bar{q}$  and  $a = A$  for  $gg$

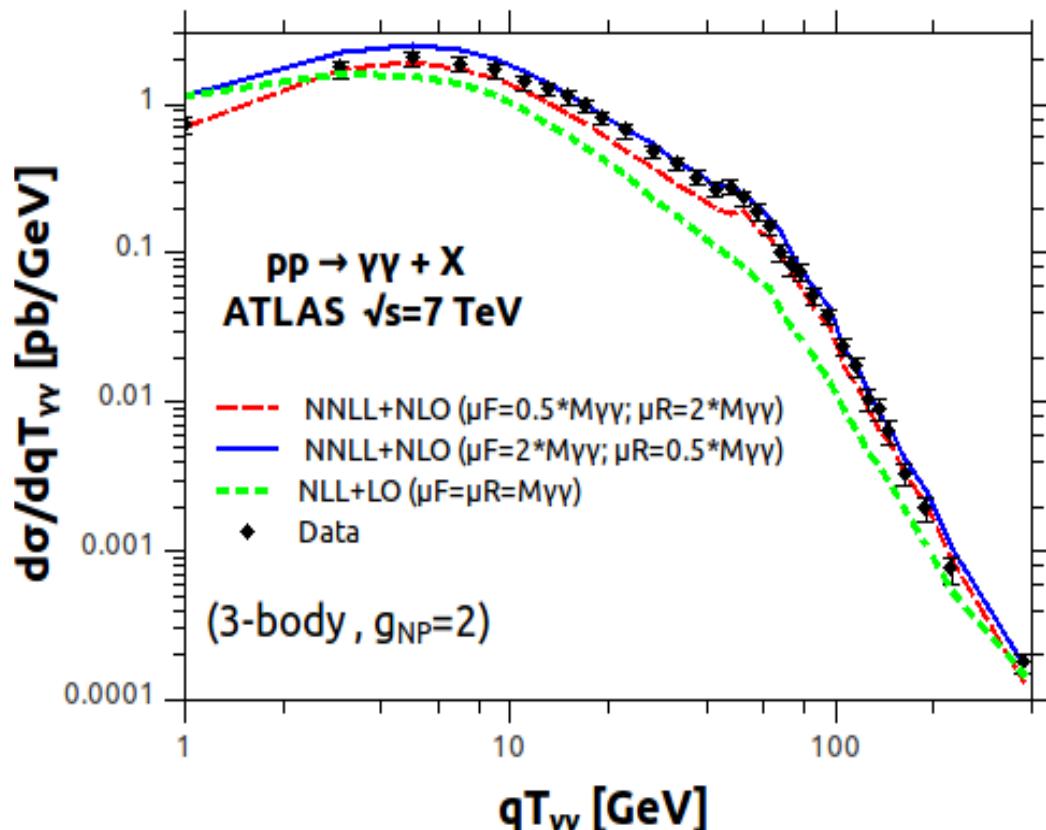
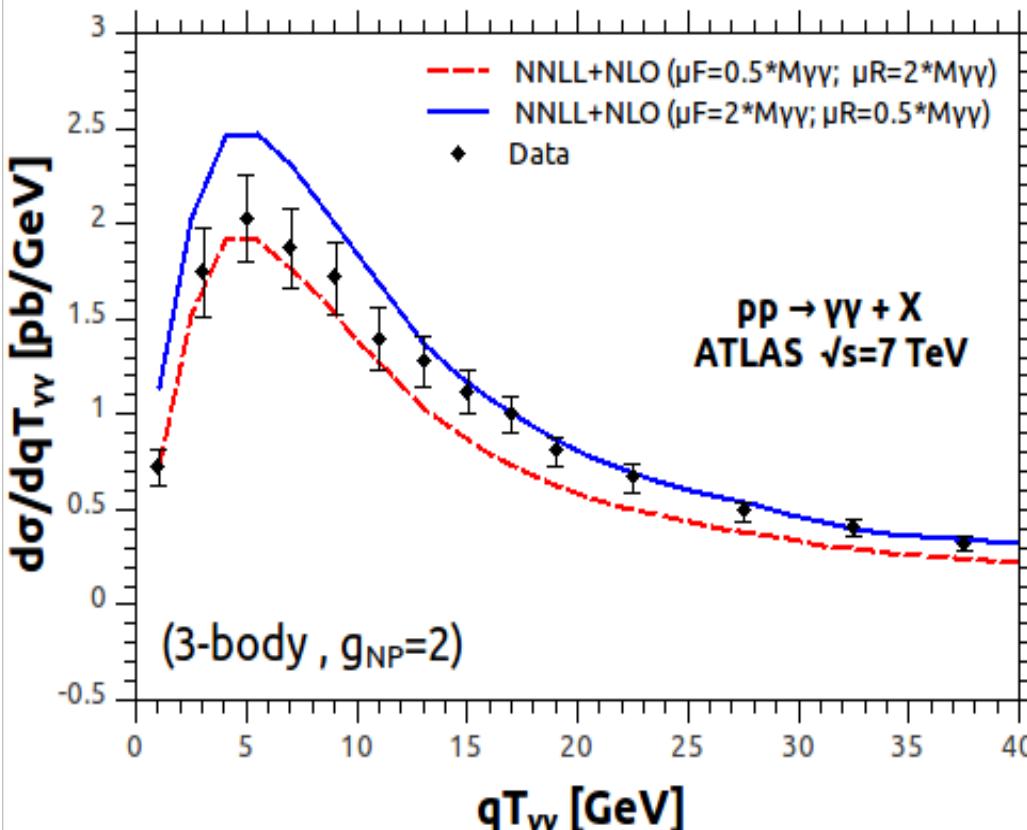
$$C_F = (N_c^2 - 1)/(2N_c) \quad \text{and} \quad C_A = N_c$$

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 $|y_\gamma| < 1.37 \vee 1.52 < |y_\gamma| \leq 2.37,$   
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# Resummation → ATLAS $\gamma\gamma$

LC, Coradeschi, de Florian

First results!



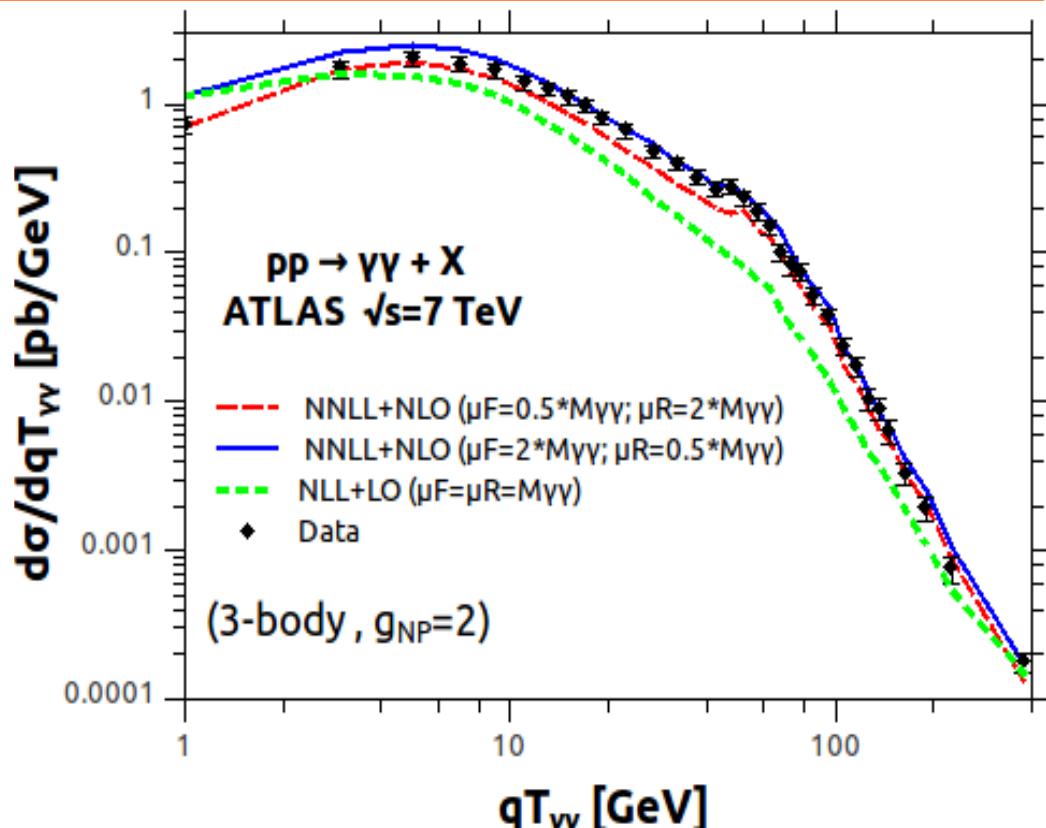
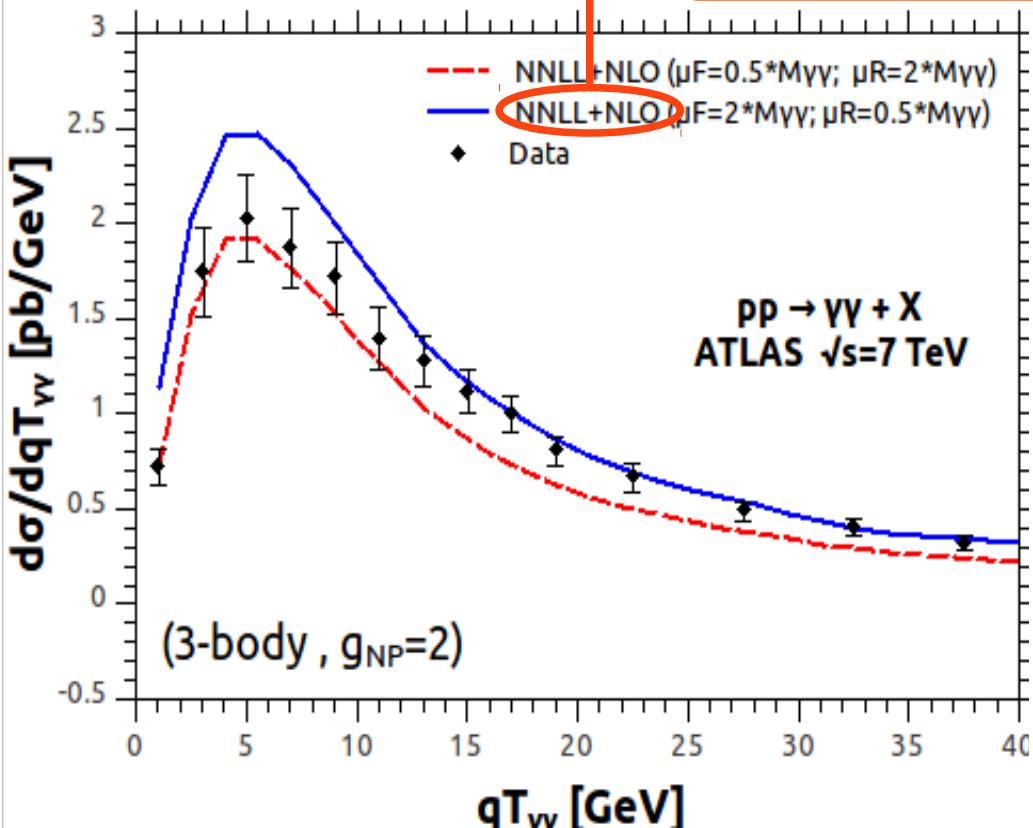
qT resummation “spreads” the uncertainties of the gg channel over the whole qT range

$p_T^{\text{harder}} \geq 25$  GeV,  $p_T^{\text{softer}} \geq 22$  GeV,  
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 $E_T \text{ max} = 4$  GeV,  $n = 1$ ,  $R = 0.4$ ,  
 $R_{\gamma\gamma} = 0.4$

# Resummation → ATLAS $\gamma\gamma$

LC, Coradeschi, de Florian

- + ) NLO here means:  $\gamma\gamma + \text{jet}$  at NLO
- + )  $\gamma\gamma + \text{jet}$  at NLO is a part of  $\gamma\gamma$  production at NNLO



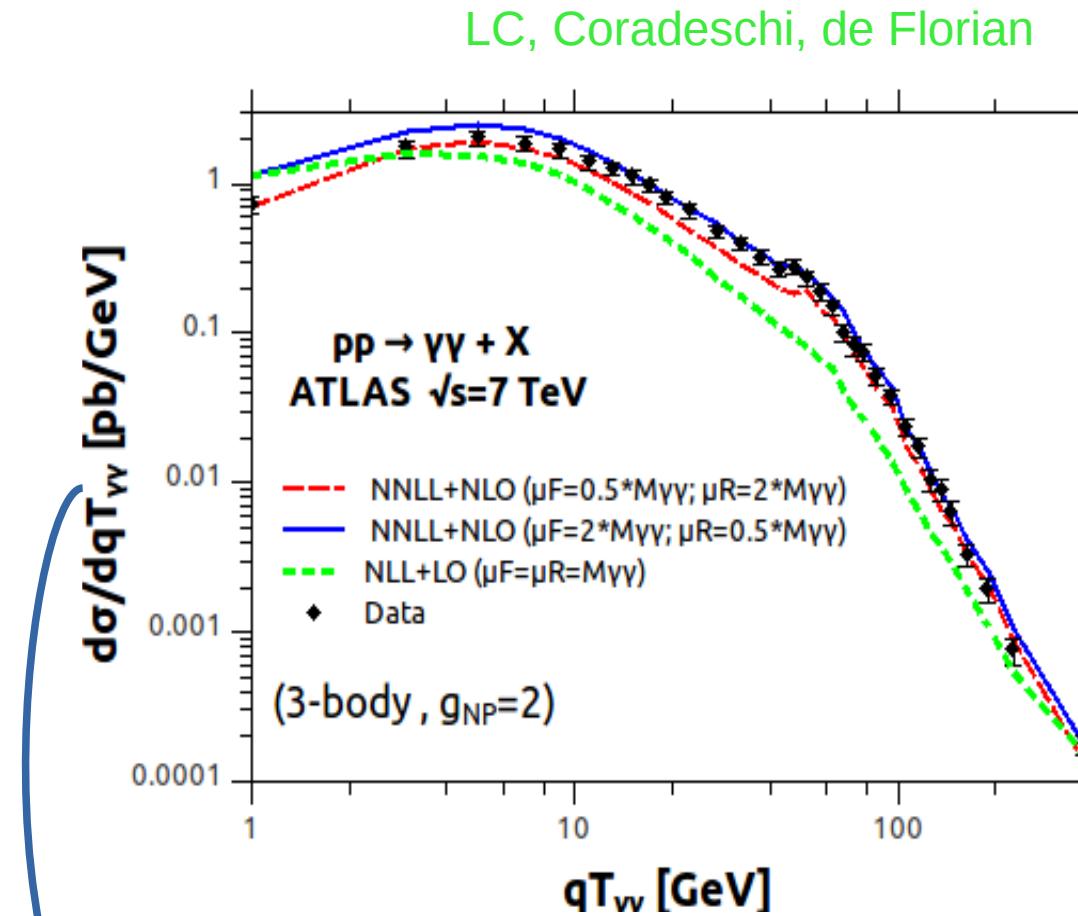
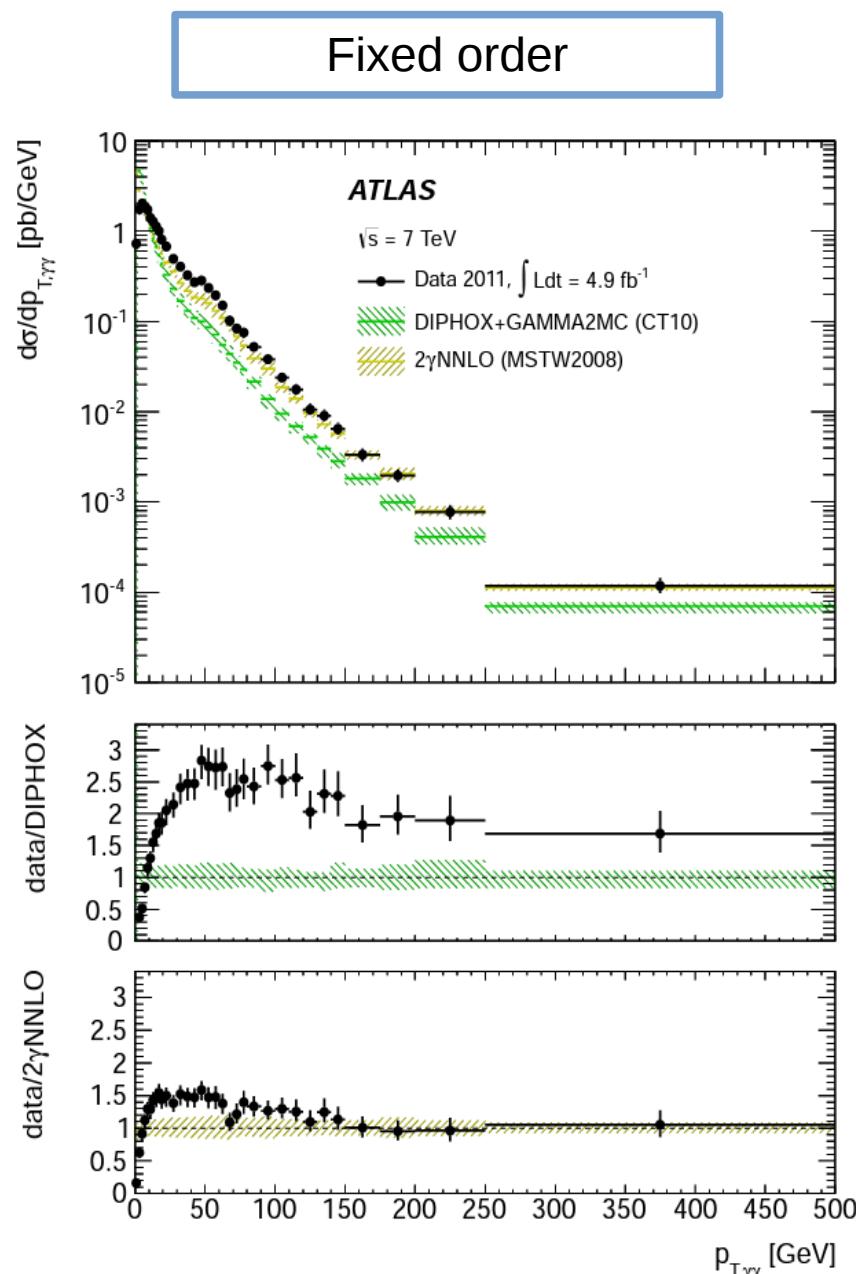
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$$C_F = (N_c^2 - 1)/(2N_c) \quad \text{and} \quad C_A = N_c$$

$p_T^{\text{harder}} \geq 25 \text{ GeV}, \quad p_T^{\text{softer}} \geq 22 \text{ GeV},$   
 $|y_\gamma| < 1.37 \vee 1.52 < |y_\gamma| \leq 2.37,$   
 $E_T \max = 4 \text{ GeV}, \quad n = 1, \quad R = 0.4,$   
 $R_{\gamma\gamma} = 0.4$

# Resummation → ATLAS $\gamma\gamma$

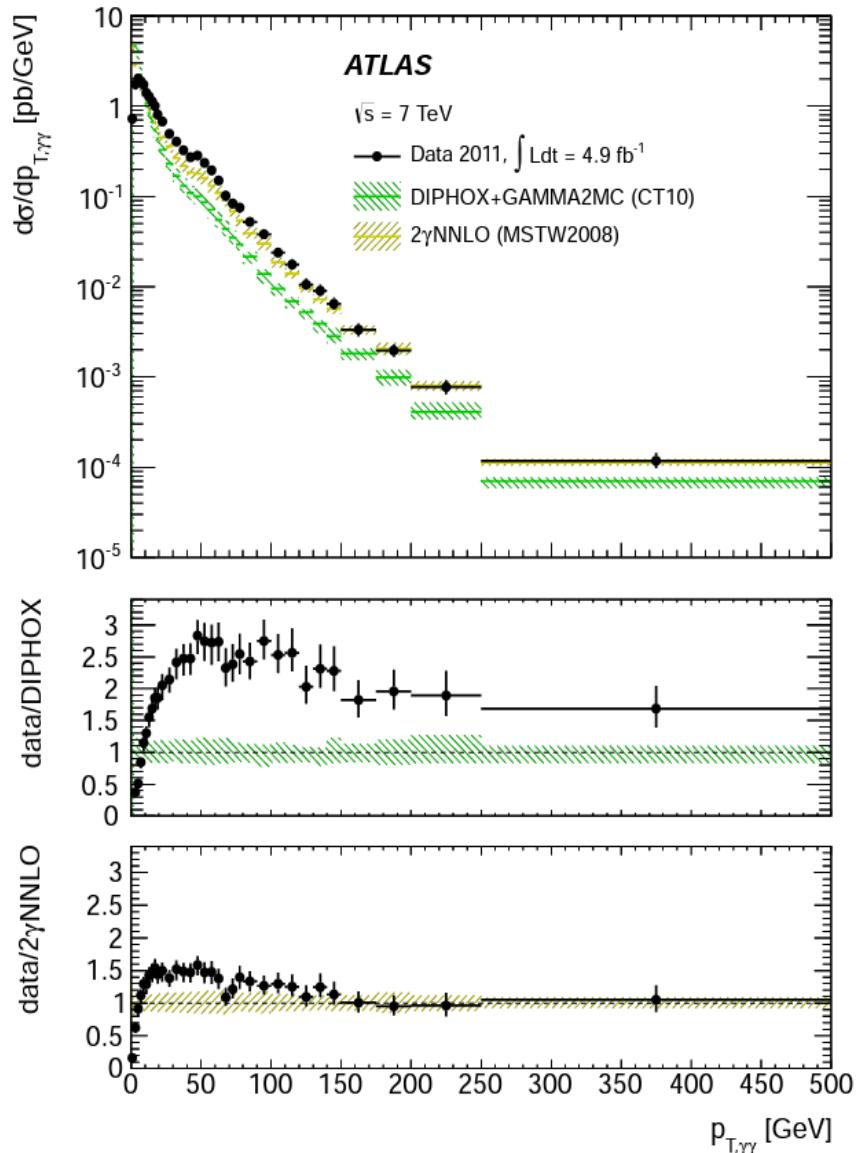


qT resummation “spreads” the uncertainties of the gg channel over the whole qT range

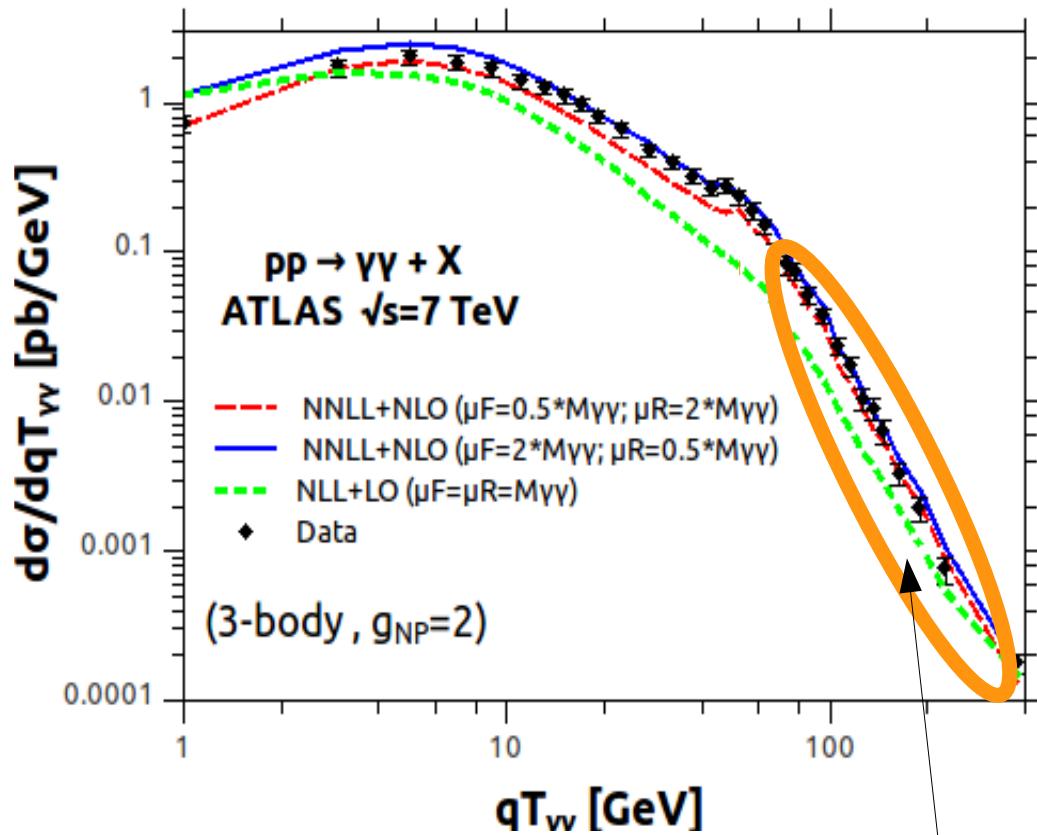
With respect to the fixed-order calculation, the present implementation provides a better description of the data and recovers the correct physical behaviour in the small qT region, with the spectrum going to zero.

# Resummation → ATLAS $\gamma\gamma$

Fixed order



LC, Coradeschi, de Florian

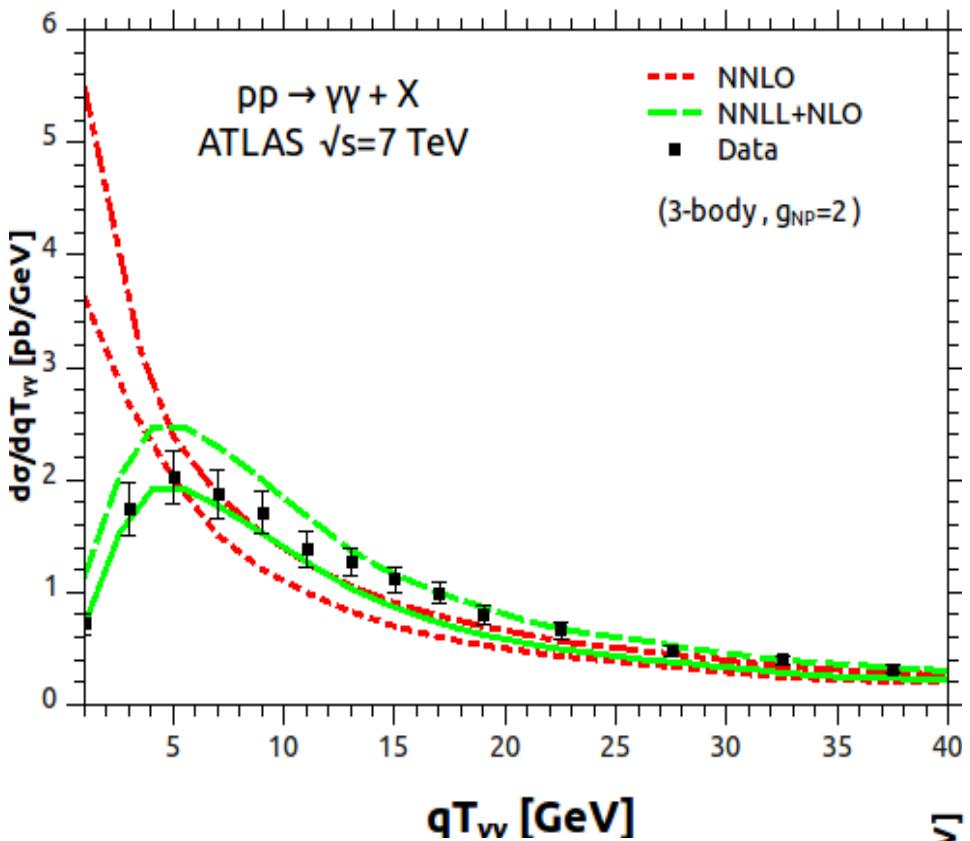


qT resummation “spreads” the uncertainties of the gg channel over the whole qT range

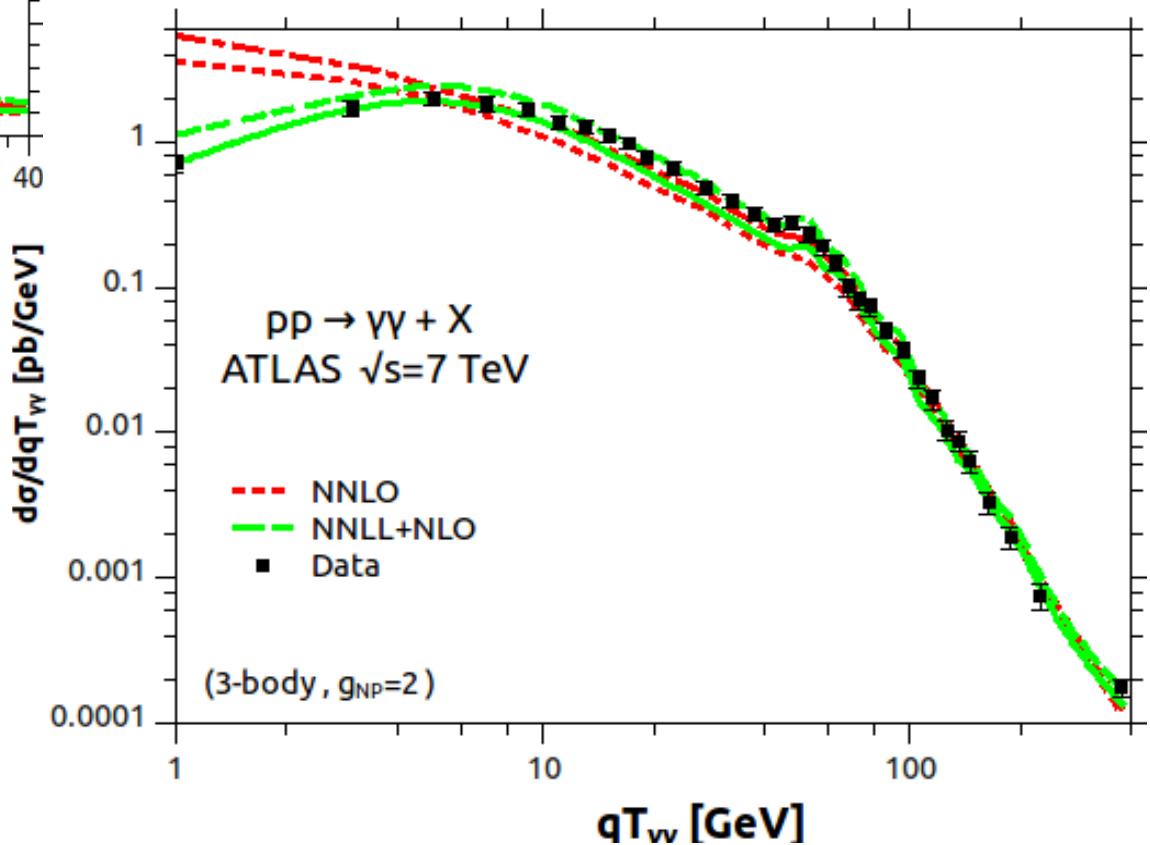
The size of the bands is proportional to the luminosity of the PDF of the gluon

# Resummation → ATLAS $\gamma\gamma$

LC, Coradeschi, de Florian



Good agreement between theory and experiment over the whole qT range.

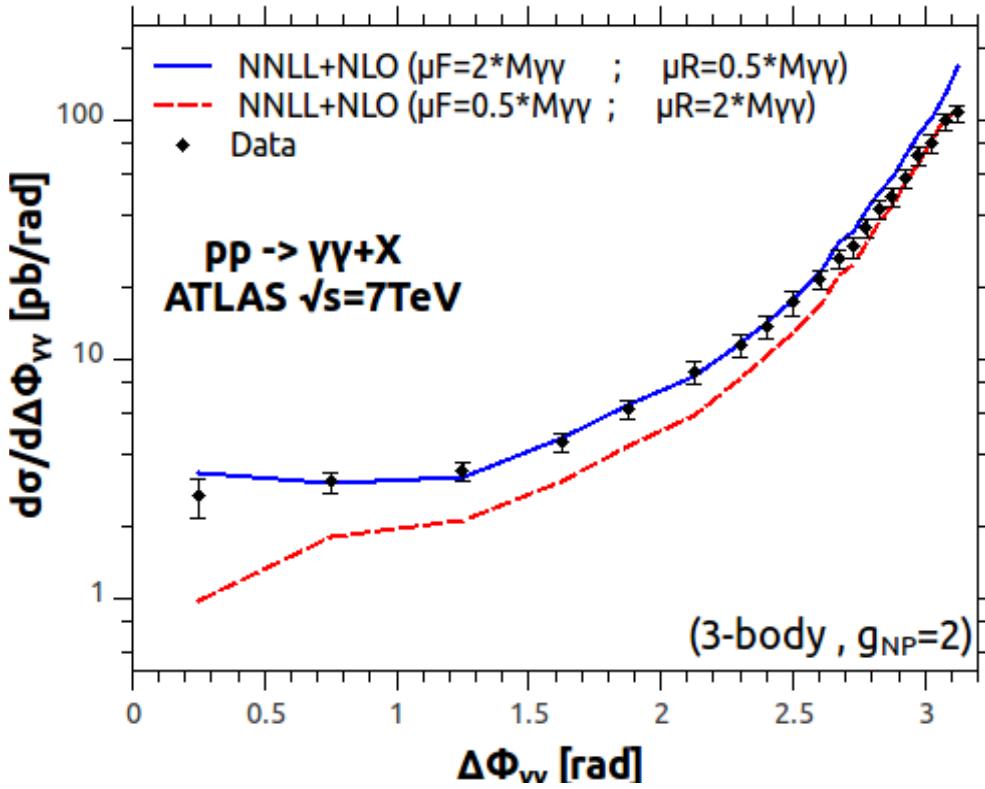


With respect to the fixed-order calculation, the present implementation provides a better description of the data and recovers the correct physical behaviour in the small qT region, with the spectrum going to zero.

# Resummation → ATLAS $\gamma\gamma$

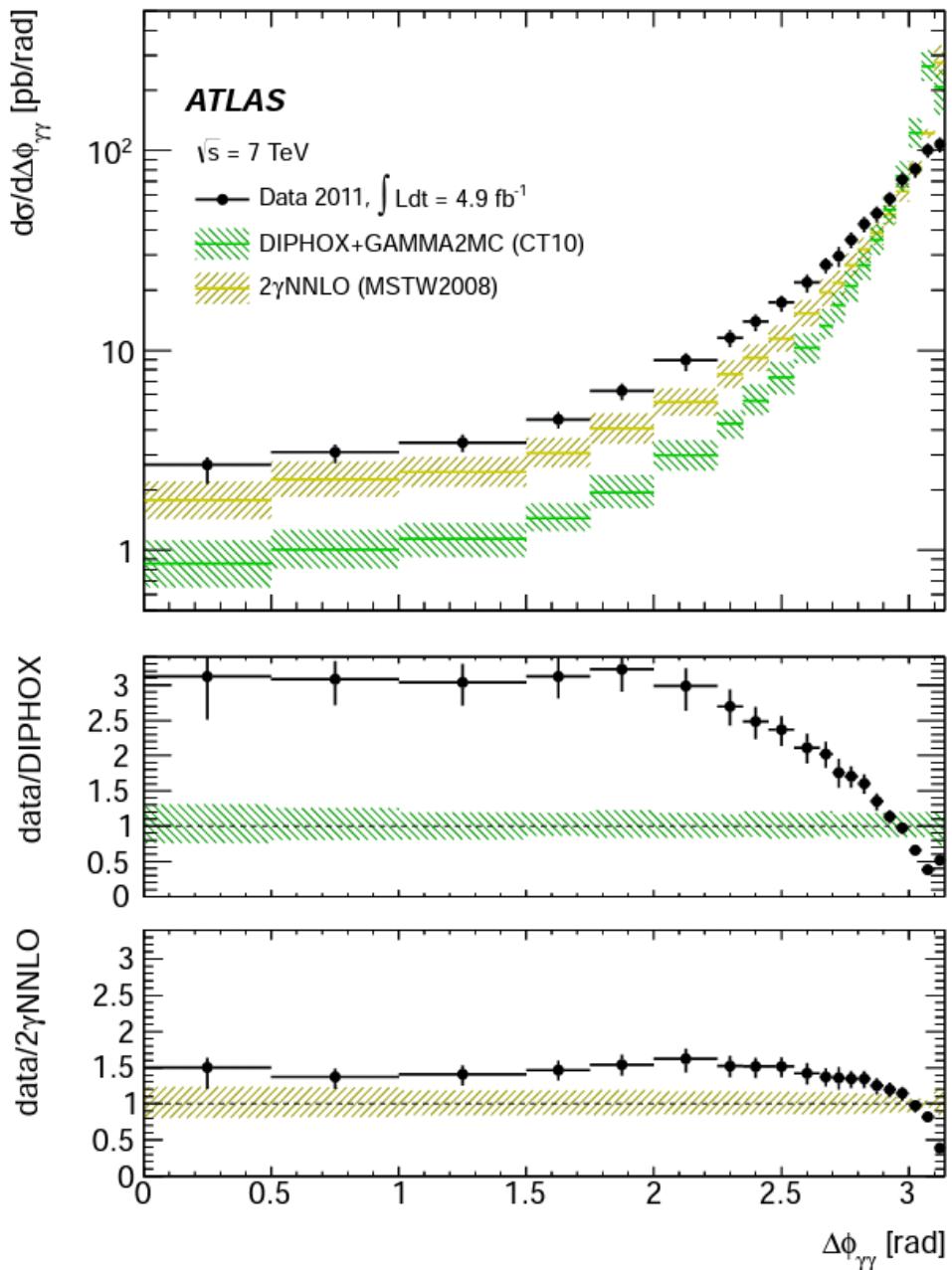
LC, Coradeschi, de Florian

First results!



The same set-up also allows the calculation of more exclusive observable distributions

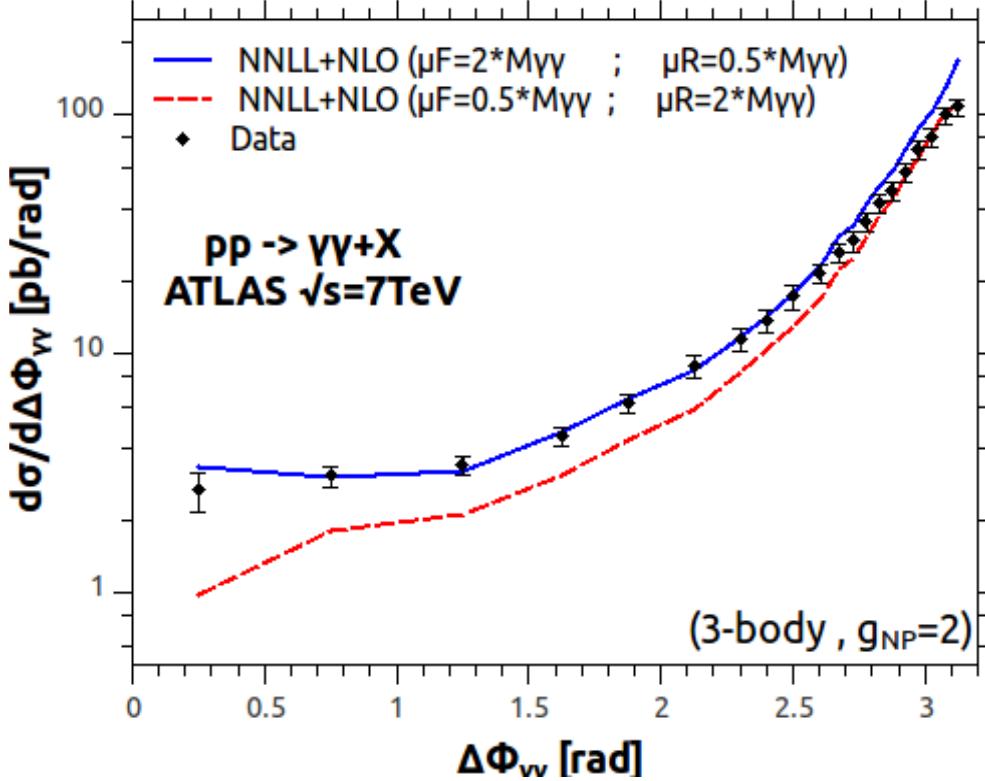
Uncertainties → 6% - 8%



# Resummation → ATLAS $\gamma\gamma$

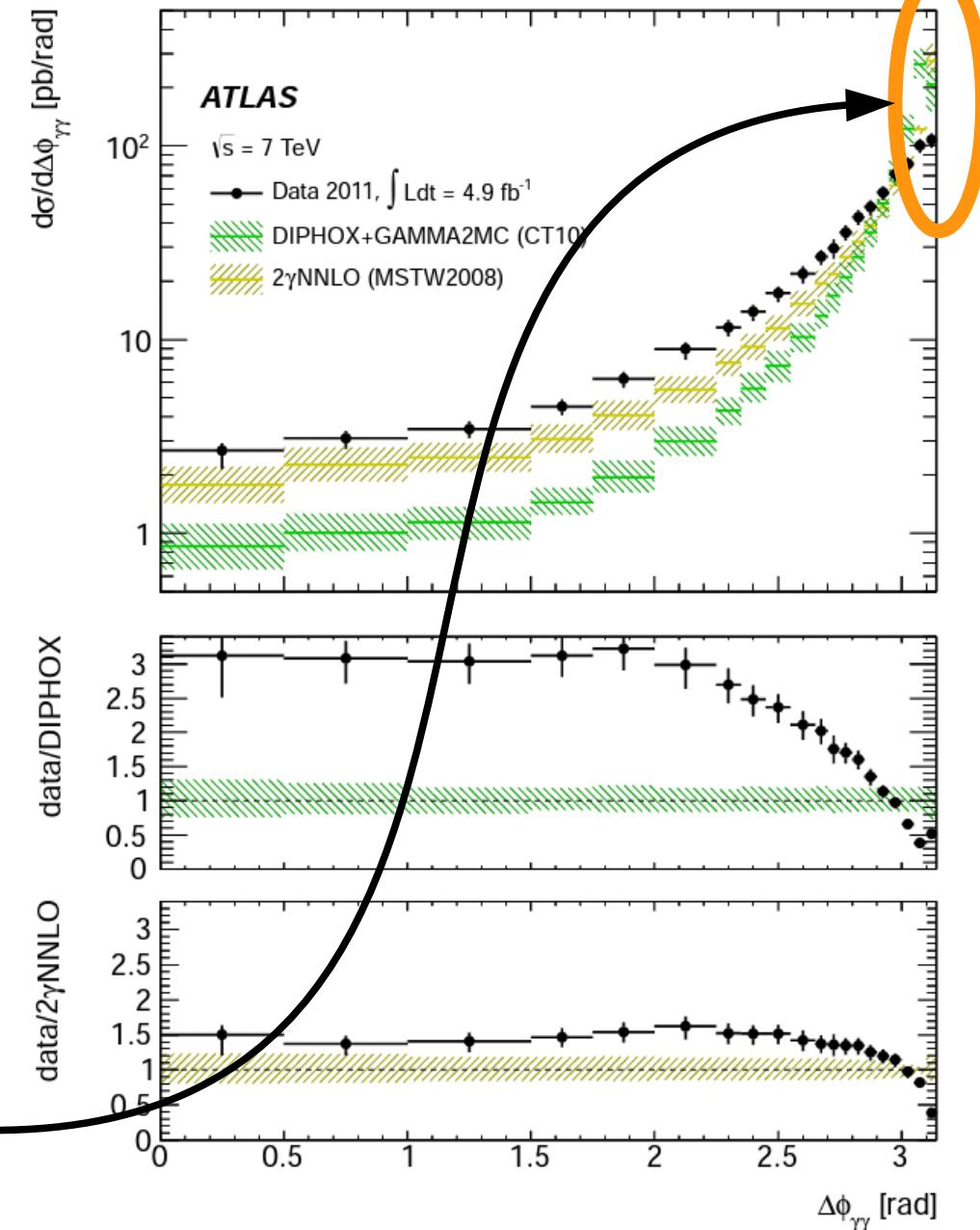
LC, Coradeschi, de Florian

First results!

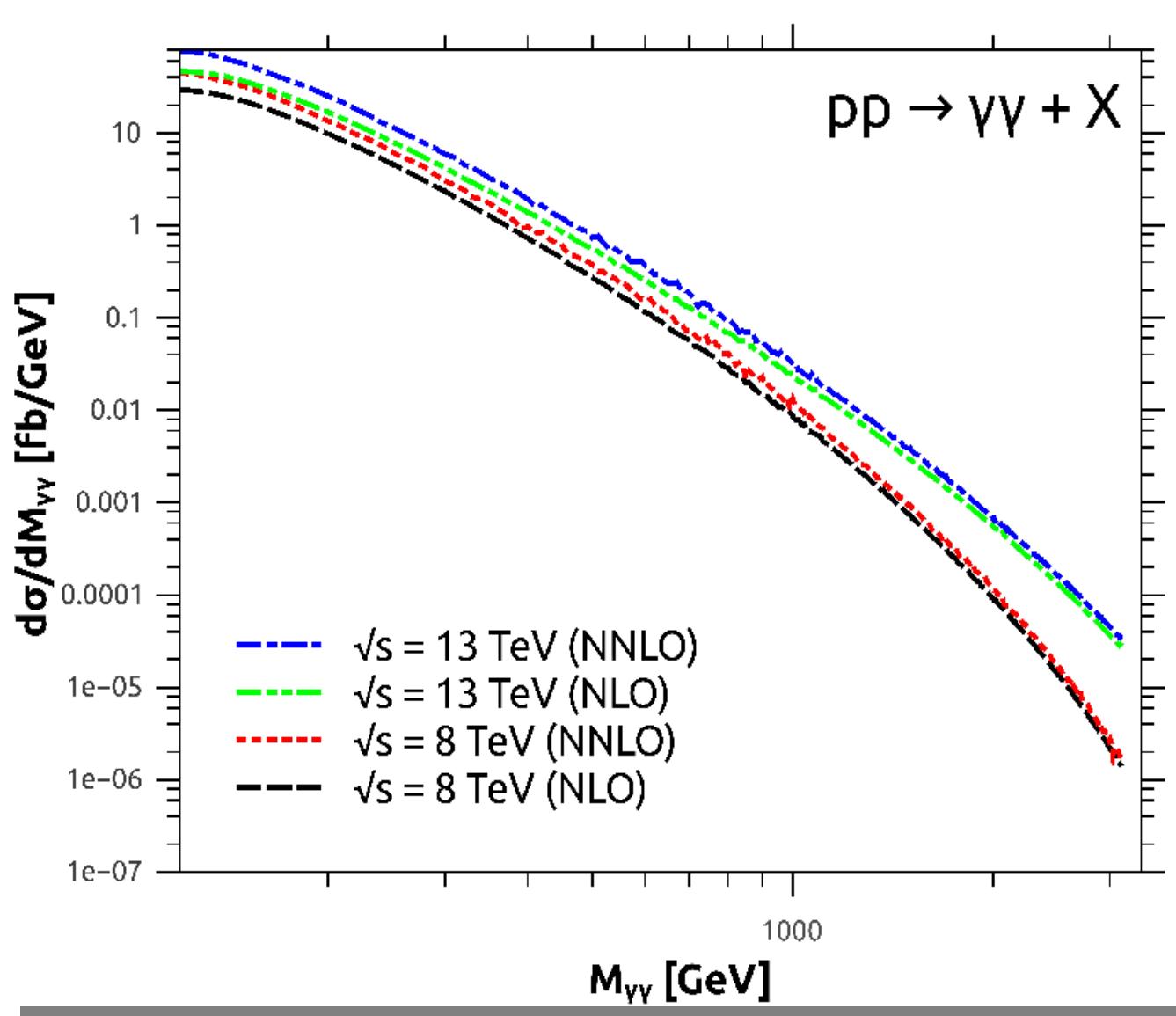


Uncertainties → 6% - 8% due to the opening of the gg channel which is “effectively” LO at NNLO

qT resummation “spreads” the uncertainties of the gg channel over the whole  $\Delta\phi$  range



# *LHC Run II → 13 TeV*

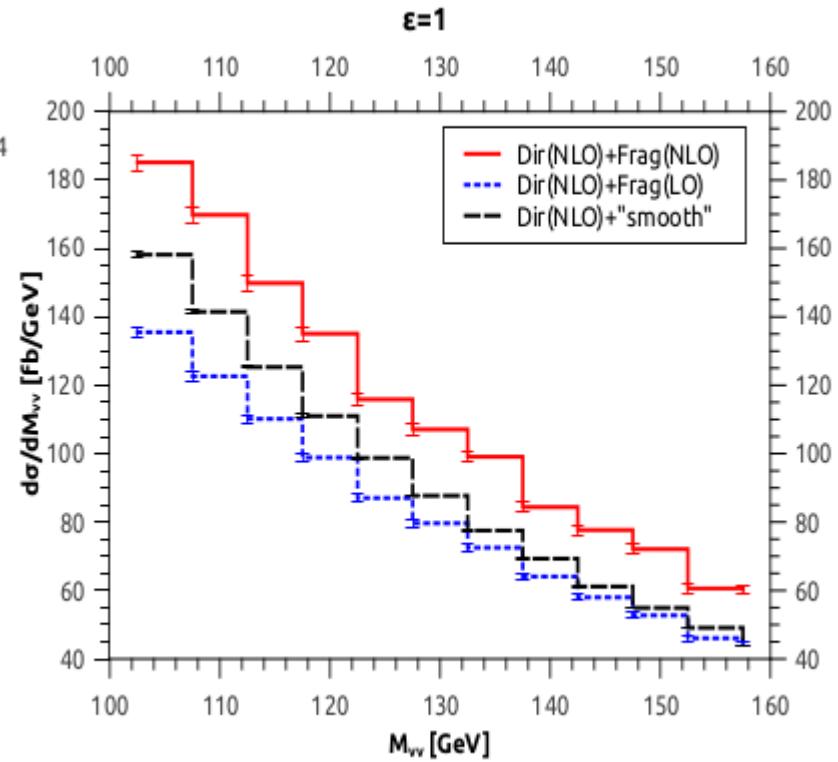
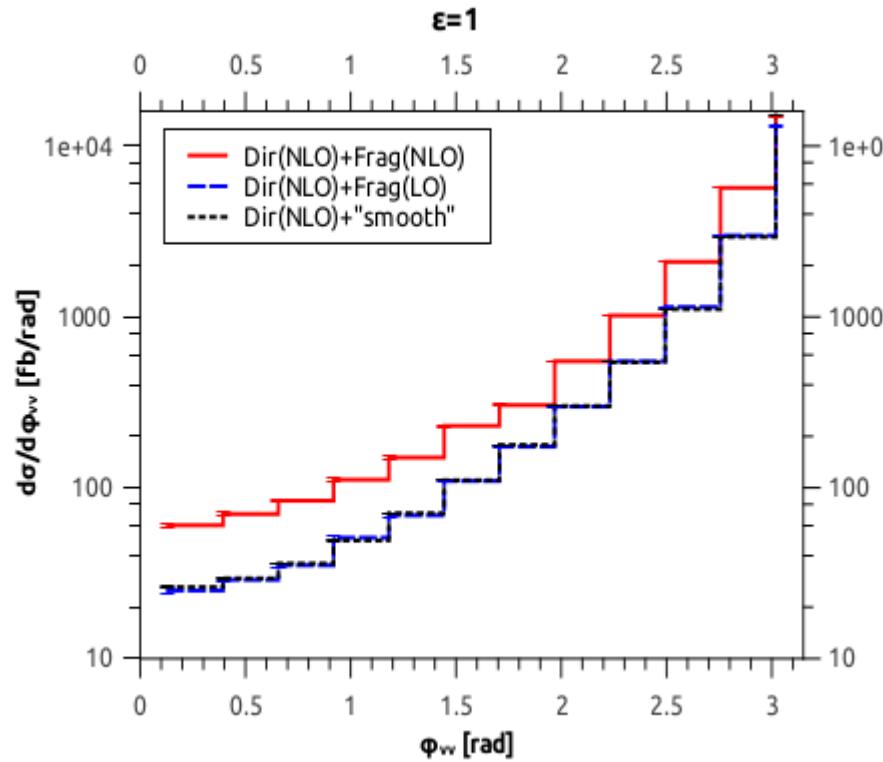


# **Summary**

- Cross section with “smooth” isolation is a lower bound for cross section with standard isolation.
- Other calculations use the “smooth” isolation to reach the highest level of accuracy:  $\gamma\gamma$  production,  $\gamma\gamma + (n)$  Jets, etc.
- We have to be aware, that inconsistent results could appear, if we use the fragmentation component at one perturbative level less than the direct component.
- Pragmatic accord (LH 2013): it is far better accepting a few % error arising from the isolation, than neglecting those huge QCD effects towards some, "more pure implementation" of the isolation prescription.
- Good agreement between theory and data for  $\gamma+\text{jet}$  production
- Good agreement between theory and data for  $\gamma\gamma$  production with a few exceptions
- First results of diphoton production at NNLL+NNLO show an improved agreement (respect NNLO) with the LHC data over the whole  $qT$  range.

***Thank you!!!***

# *Backup slides*



In cases, using LO fragmentation component can make things look very strange...

Standard cone isolation → DIPHOX

CMS [ 7 TeV ]

	Code	$\sum E_T^{had} \leq$	$\sigma_{total}^{NLO}$ (fb)	$\sigma_{dir}^{NLO}$ (fb)	$\sigma_{onef}^{NLO}$ (fb)	$\sigma_{twof}^{NLO}$ (fb)	Isolation
a	DIPHOX	2 GeV	3746	3504	239	2.6	Standard
b	DIPHOX	3 GeV	3776	3396	374	6	Standard
c	DIPHOX	4 GeV	3796	3296	488	12	Standard
d	DIPHOX	5 GeV	3825	3201	607	17	Standard
e	DIPHOX	$0.05 p_T^\gamma$	3770	3446	320	4	Standard
f	DIPHOX	$0.5 p_T^\gamma$	4474	2144	2104	226	Standard
g	DIPHOX	<i>incl</i>	6584	1186	3930	1468	none
h	$2\gamma$ NNLO	$0.05 p_T^\gamma \chi(r)$	3768	3768	0	0	Smooth
i	$2\gamma$ NNLO	$0.5 p_T^\gamma \chi(r)$	4074	4074	0	0	Smooth
j	$2\gamma$ NNLO	$2 \text{ GeV } \chi(r)$	3743	3743	0	0	Smooth
k	$2\gamma$ NNLO	$3 \text{ GeV } \chi(r)$	3776	3776	0	0	Smooth
l	$2\gamma$ NNLO	$4 \text{ GeV } \chi(r)$	3795	3795	0	0	Smooth
m	$2\gamma$ NNLO	$5 \text{ GeV } \chi(r)$	3814	3814	0	0	Smooth

In cases, using LO fragmentation component can make things look very strange...

## Standard cone isolation → DIPHOX

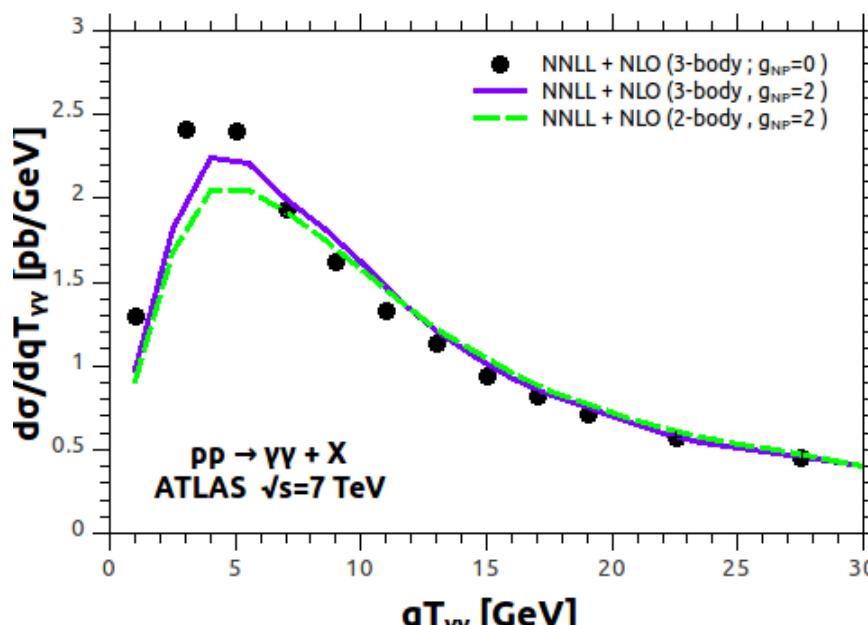
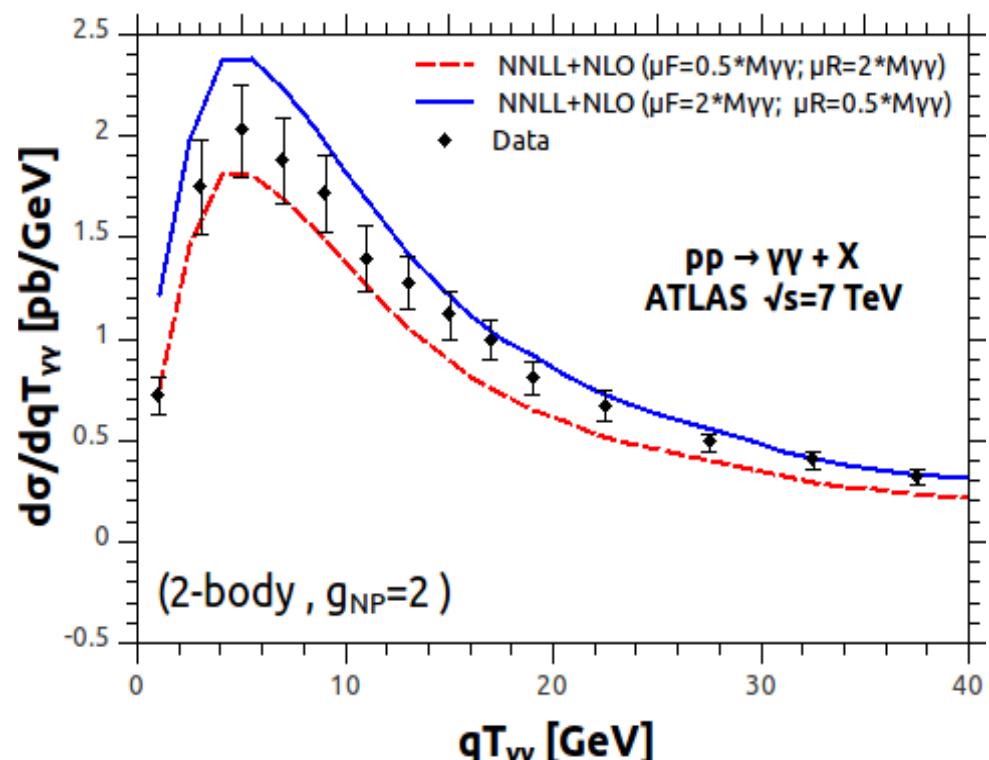
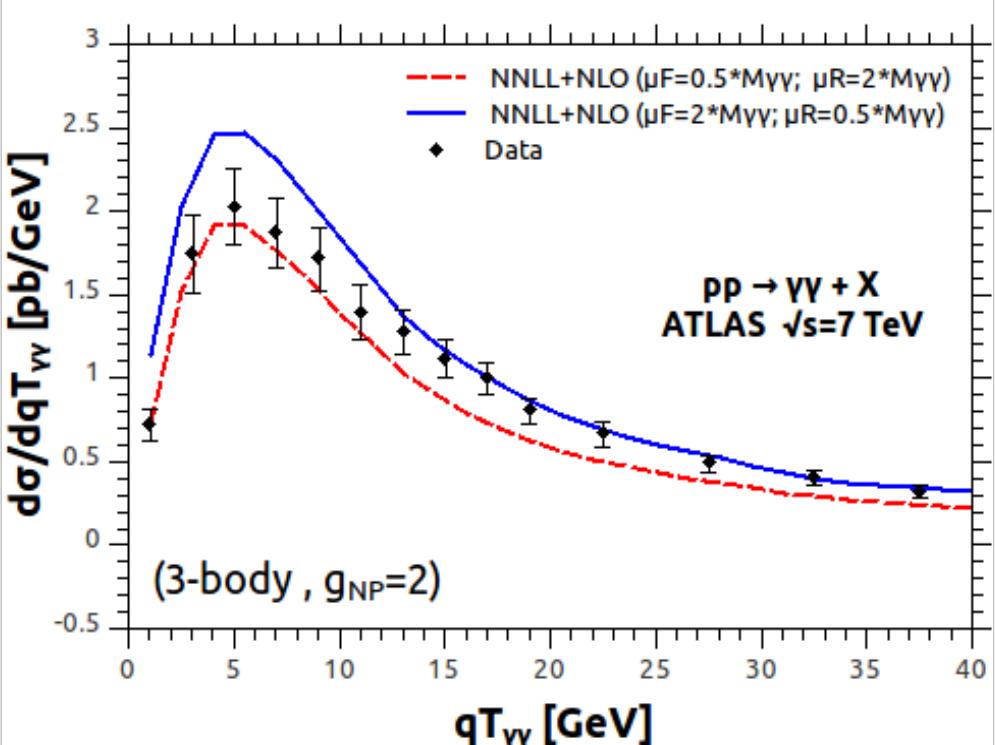
CMS [ 7 TeV ]

	Code	$\sum E_T^{had} \leq$	$\sigma_{total}^{NLO}(\text{fb})$	$\sigma_{dir}^{NLO}(\text{fb})$	$\sigma_{\text{frag}}^{NLO}(\text{fb})$	$\sigma_{\text{overf}}^{NLO}(\text{fb})$	Isolation
a	DIPHOX	2 GeV	3746	3504	239	2.6	Standard
b	DIPHOX	3 GeV	3776	3396	374	6	Standard
c	DIPHOX	4 GeV	3796	3296	488	12	Standard
d	DIPHOX	5 GeV	3825	3201	607	17	Standard
e	DIPHOX	$0.05 p_T^\gamma$	3770	3446	320	4	Standard
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g	DIPHOX	<i>incl</i>	6584	1186	3930	1468	none
h	$2\gamma\text{NNLO}$	$0.05 p_T^\gamma \chi(r)$	3768	3768	0	0	Smooth
i	$2\gamma\text{NNLO}$	$0.5 p_T^\gamma \chi(r)$	4074	4074	0	0	Smooth
j	$2\gamma\text{NNLO}$	$2 \text{ GeV } \chi(r)$	3743	3743	0	0	Smooth
k	$2\gamma\text{NNLO}$	$3 \text{ GeV } \chi(r)$	3776	3776	0	0	Smooth
l	$2\gamma\text{NNLO}$	$4 \text{ GeV } \chi(r)$	3795	3795	0	0	Smooth
m	$2\gamma\text{NNLO}$	$5 \text{ GeV } \chi(r)$	3814	3814	0	0	Smooth

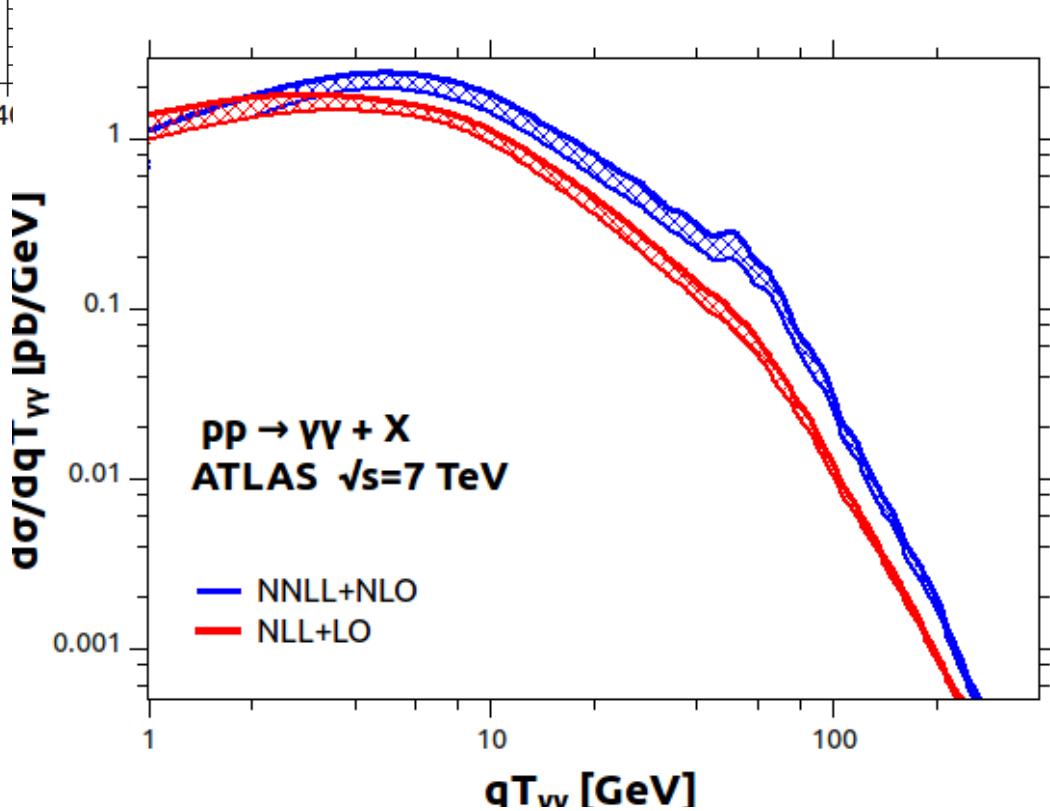
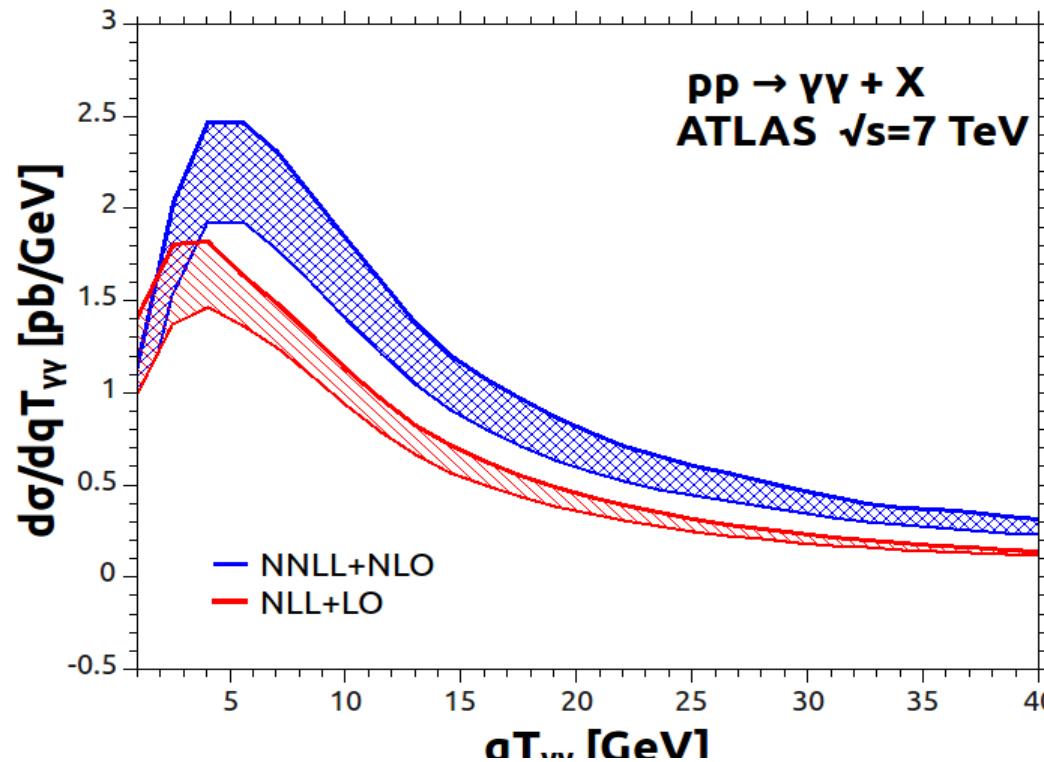
Tighter criteria

Direct component increasing

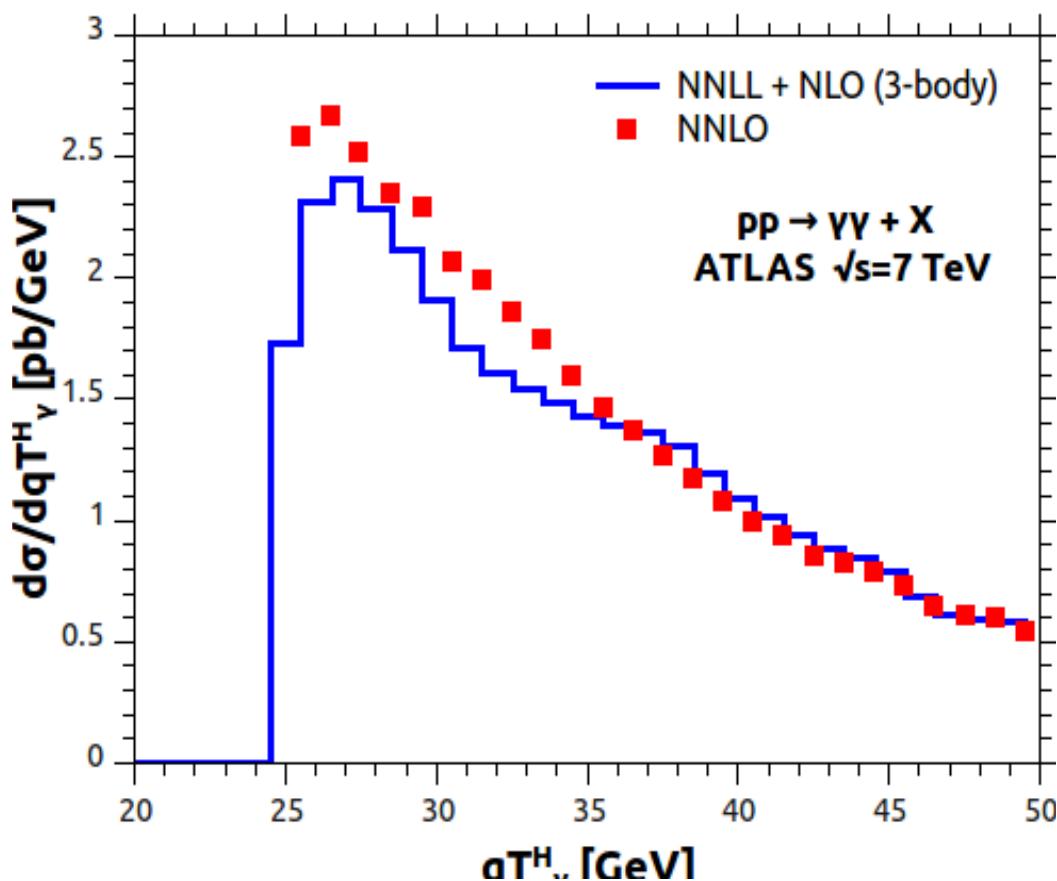
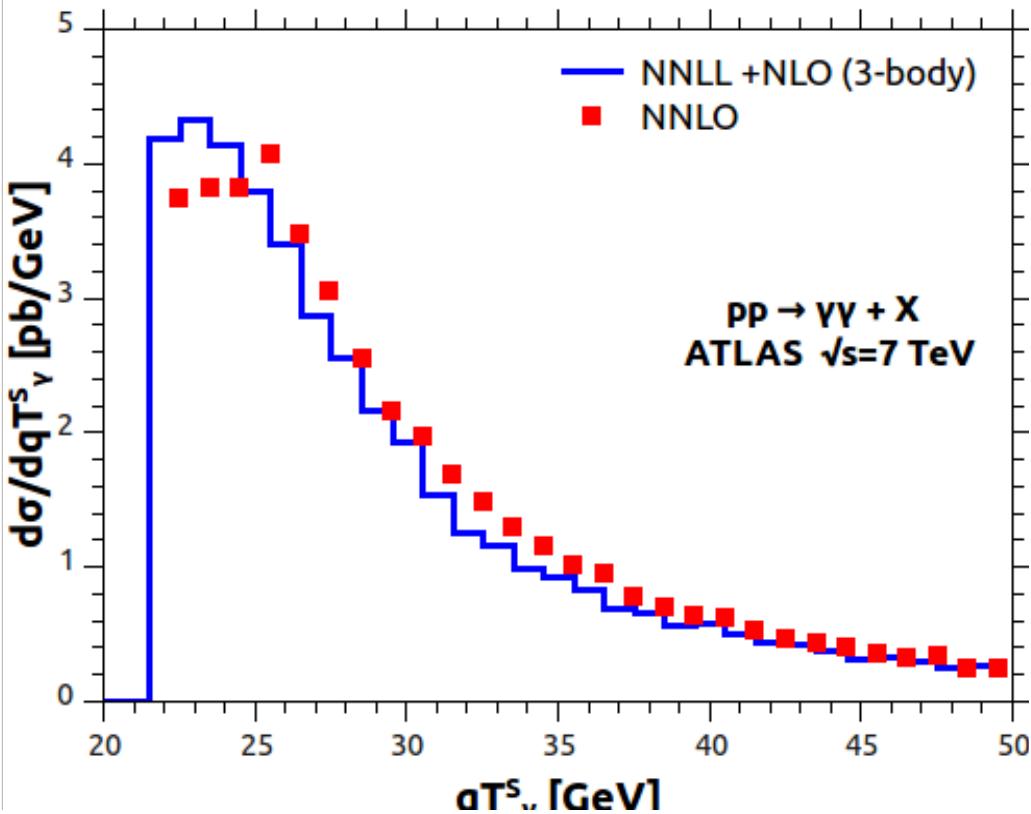
# Resummation



# Resummation

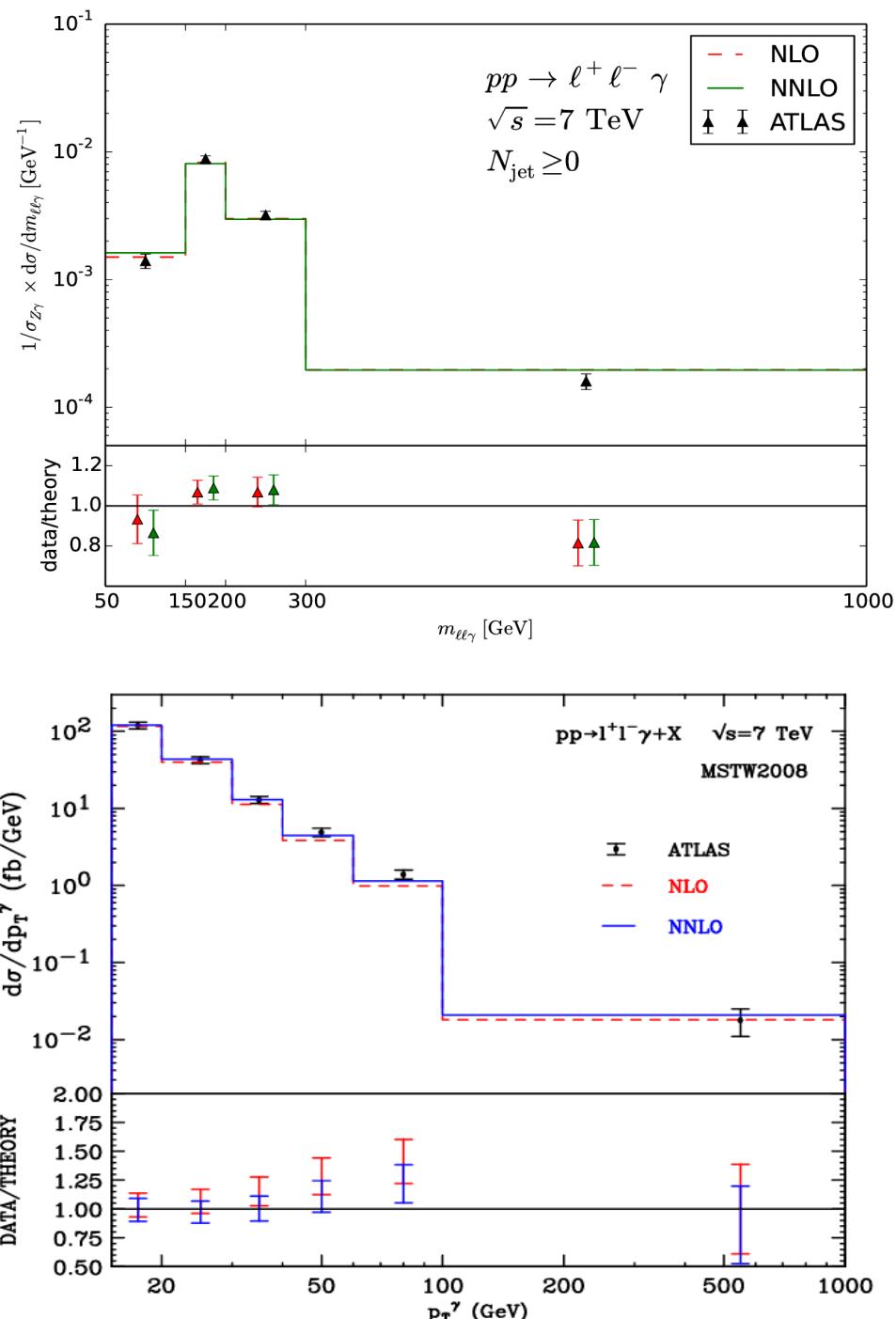
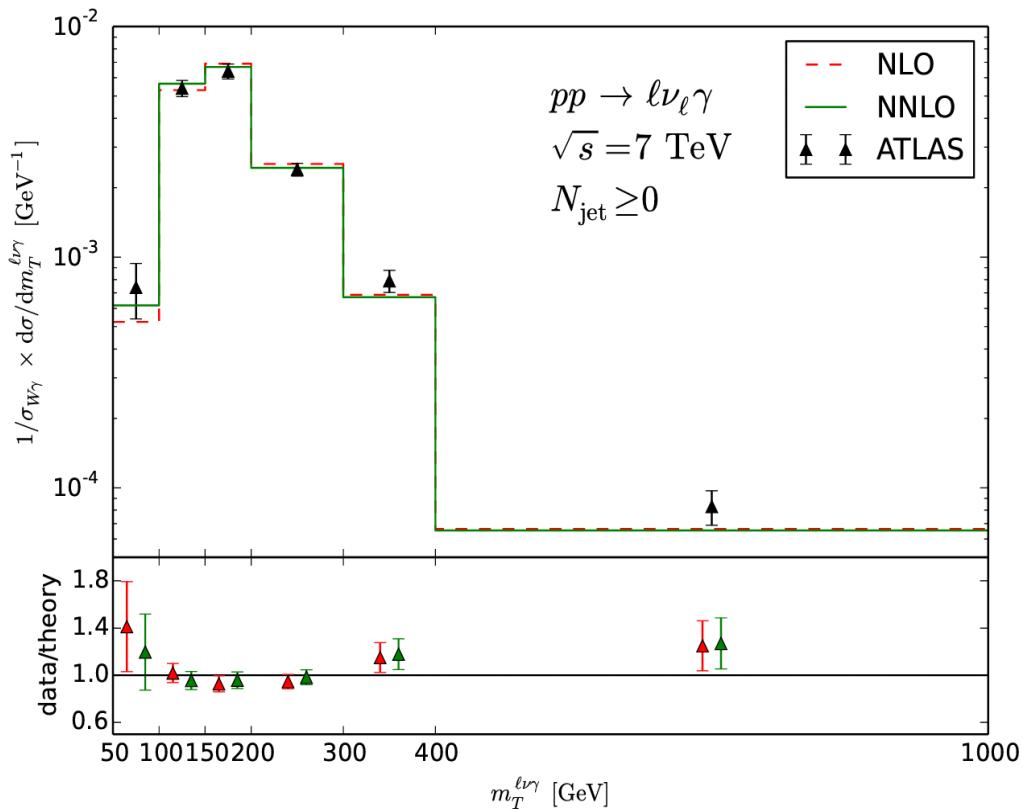


# Resummation



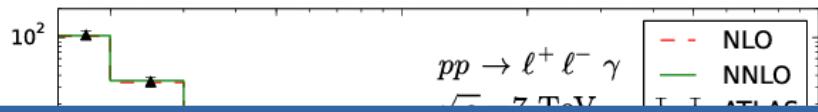
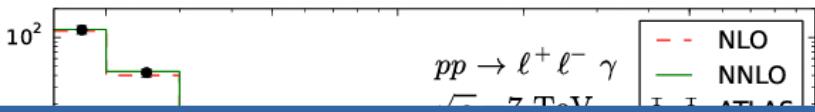
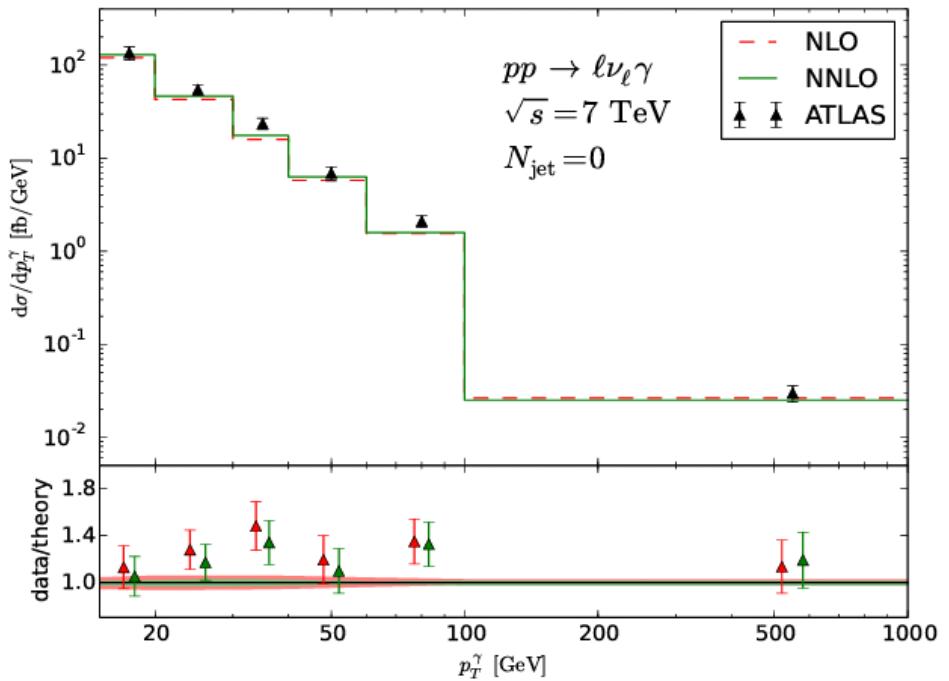
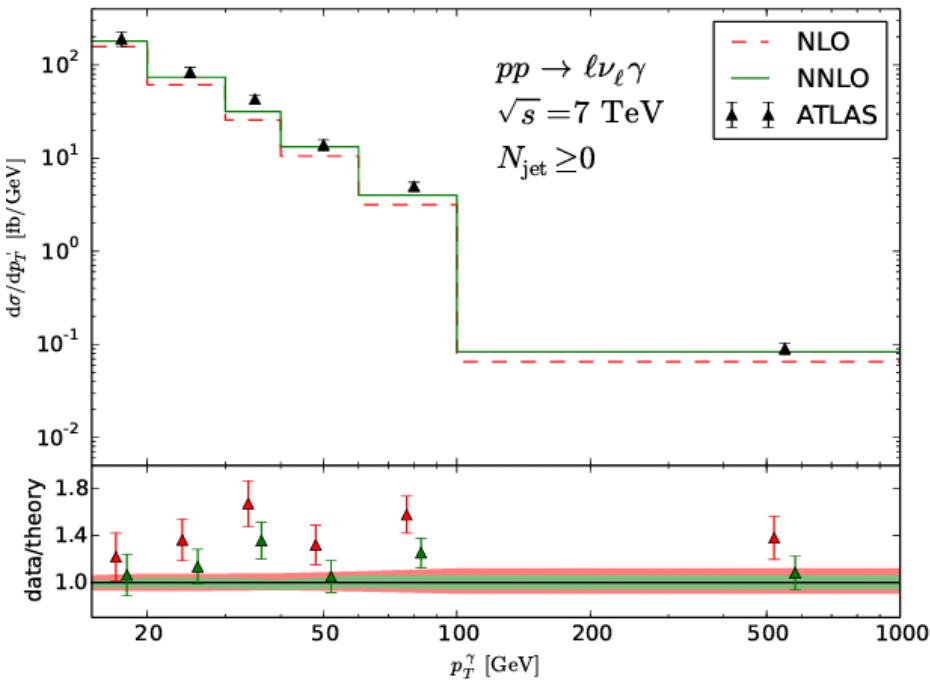
# V $\gamma$ production NNLO

Grazzini, Kallweit, Rathlev, Torre

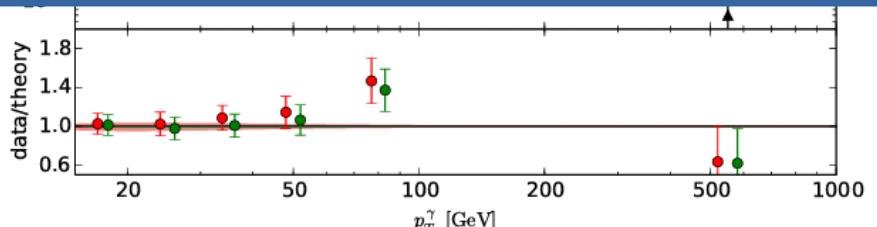
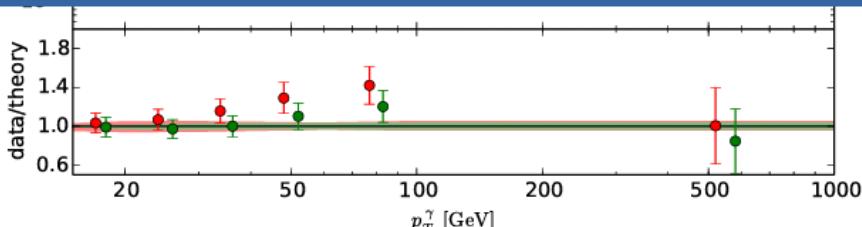


# *Vy production NNLO*

Grazzini, Kallweit, Rathlev, Torre

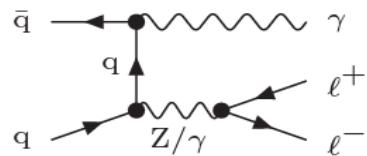


It is clear that the Wy process features much larger radiative effects with respect to the Zy processes. This should be contrasted to what happens in the case of inclusive W and Z boson production, where QCD radiative corrections are essentially identical. It is thus the emission of the additional photon that breaks the similarity between the charged current and the neutral current processes.

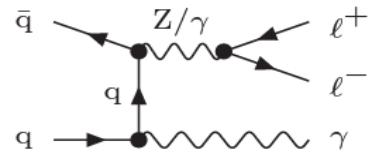


# $V\gamma$ production NNLO

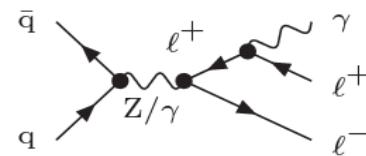
Grazzini, Kallweit, Rathlev, Torre



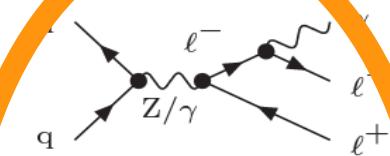
(a) Topology Ia



(b) Topology Ib

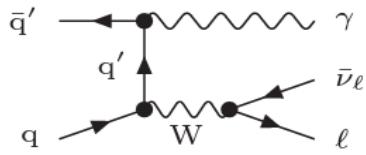


(c) Topology IIa

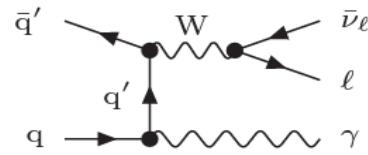


(d) Topology IIb

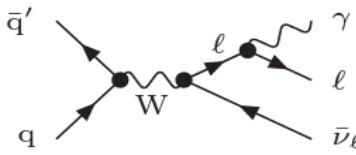
Figure 1: Feynman diagrams contributing to  $Z\gamma$  production at Born level.



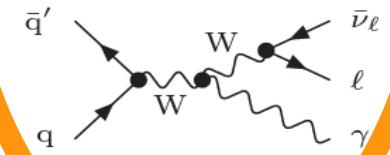
(a) Topology Ia



(b) Topology Ib



(c) Topology IIa



(d) Topology IIb

Figure 2: Feynman diagrams contributing to  $W\gamma$  production at Born level.

It is clear that the  $W\gamma$  process features much larger radiative effects with respect to the  $Z\gamma$  processes. This should be contrasted to what happens in the case of inclusive  $W$  and  $Z$  boson production, where QCD radiative corrections are essentially identical. It is thus the emission of the additional photon that breaks the similarity between the charged current and the neutral current processes.

# *Outline*

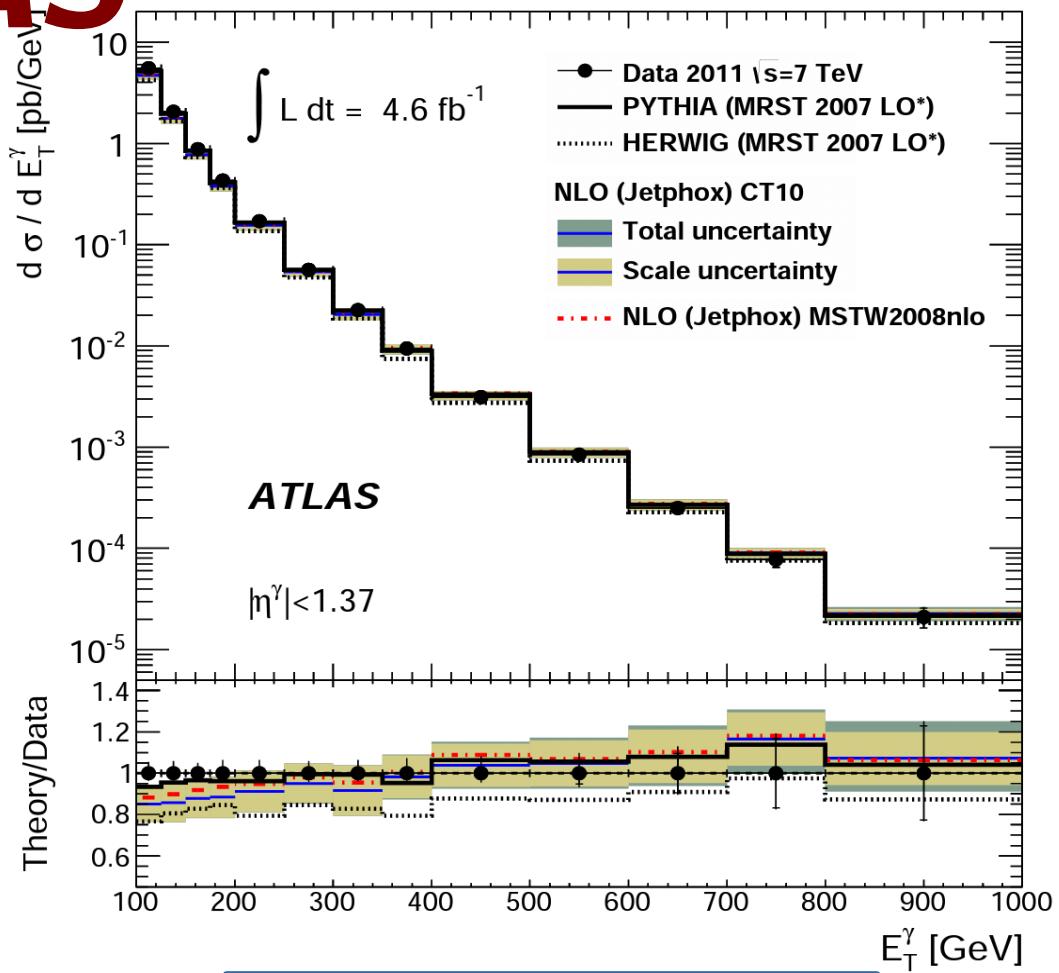
- ➊ Introduction → **Motivation**
- ➋ Isolation criteria (IC) → **Production mechanisms**
- ➌ Available FO tools
- ➍ IC comparison ( $\gamma\gamma$  NLO)
- ➎ Les Houches accord (“tight” isolation accord)
- ➏ ATLAS and CMS results
- ➐ qT Resummation  $\gamma\gamma$  (ATLAS)
- ➑ Summary

# $\gamma + jet$ ATLAS

Phys.Rev. D89 (2014) 052004

Results in good  
agreement with data

The data are also compared to MC predictions that include only direct photons from  $qg \rightarrow q\gamma$  and  $qq \rightarrow q\gamma$  processes calculated at LO QCD. These MC generators predict a cross section at low  $E_T^\gamma$  that is 20% lower than the data which includes all the higher-order fragmentation processes. This difference is reduced at high  $E_T^\gamma$ , where the contribution from photons originating from fragmentation becomes small. This shows that the higher order fragmentation processes contribute significantly to the shape of the predicted  $E_T^\gamma$  cross section.



In some kinematic regimes the Xsection is sensible at PDFs variations

The kinematic regions in which appear the discrepancies allow us to discriminate real radiation from fragmentation?