

# Prospects for double Higgs production

Giuliano Panico

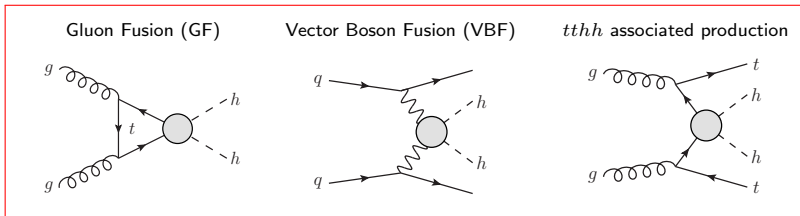
IFAE, Barcelona

**'LFC15'**

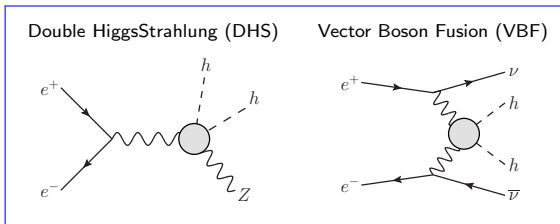
**Trento – 9 September 2015**

# Processes for double Higgs production

*pp* colliders (HL-LHC, FCC-hh)



$e^+e^-$  colliders (ILC, FCC-ee, CLIC)



# The Effective Field Theory approach

- ❖ EFT is a perfect framework for **low-energy machines with high precision** ( $e^+e^-$ , HL-LHC)

Can not access directly  
the new states



Probe their **tail effects**  
with precision measurements

- ❖ Primary goal of **high-energy machines** (FCC-hh) is to directly produce new states

EFT can only be used near threshold, well below the new resonances

- ▶ useful to obtain a model-independent parametrization of the contributions of the new states in terms of few local operators

# The Effective Field Theory approach

- ❖ New-physics effects in Higgs production typically grow with energy

on-shell single production  $\frac{\delta c}{c} \sim \frac{g_*^2}{g_{\text{SM}}^2} \frac{m_h^2}{m_*^2}$

$m_*$  scale of NP

$2 \rightarrow 2$  processes  $\frac{\delta \mathcal{A}}{\mathcal{A}} \sim \frac{g_*^2}{g_{\text{SM}}^2} \frac{E^2}{m_*^2}$

$g_*$  coupling of new states

- useful to extend the analysis to higher energies and to use differential distributions to increase the sensitivity

range of validity:  $m_h \ll E \ll m_*$

# The effective Lagrangian for a Higgs doublet

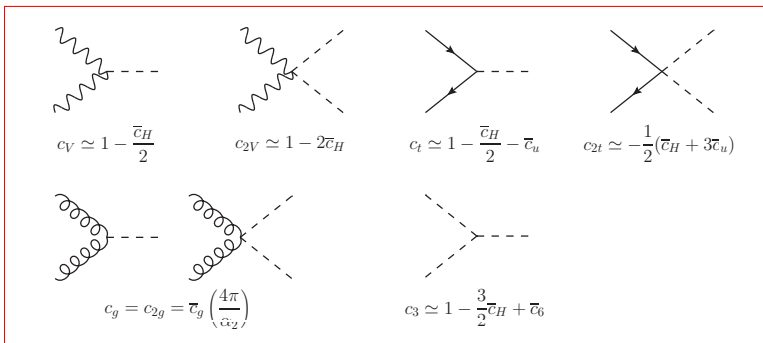
## Assumptions:

- Higgs is an  $SU(2)_L$  doublet
- derivative expansion
- expansion in Higgs powers

$$\mathcal{L} = \mathcal{L}_{SM} + \Delta\mathcal{L}_6 + \Delta\mathcal{L}_8 + \dots$$

[Buchmuller and Wyler; ...  
Giudice et al.; Grzadkowski et al.]

$$\Delta\mathcal{L}_6 \supset \frac{\bar{c}_H}{2v^2} [\partial_\mu (H^\dagger H)]^2 + \frac{\bar{c}_u}{v^2} y_u H^\dagger H \bar{q}_L H^c u_R - \frac{\bar{c}_6}{v^2} \frac{m_h^2}{2v^2} (H^\dagger H)^3 + \frac{\bar{c}_g}{m_w^2} g_s^2 H^\dagger H G_{\mu\nu} G^{\mu\nu}$$



# The effective Lagrangian for a Higgs doublet

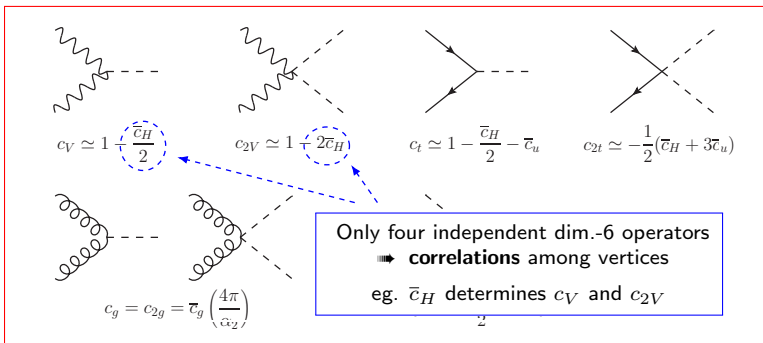
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# The effective Lagrangian for a Higgs doublet

The effective vertices correspond to the interactions in the unitary gauge

$$\mathcal{L} \supset \left( m_W^2 W_\mu^2 + \frac{m_Z^2}{2} Z_\mu^2 \right) \left( 1 + 2c_V \frac{h}{v} + c_{2V} \frac{h^2}{v^2} \right) - m_t \bar{t}t \left( 1 + c_t \frac{h}{v} + c_{2t} \frac{h^2}{2v^2} \right) \\ - c_3 \frac{m_h^2}{2v} h^3 + \frac{g_s^2}{4\pi^2} \left( c_g \frac{h}{v} + c_{2g} \frac{h^2}{2v^2} \right) G_{\mu\nu}^a G^{a\mu\nu}$$

This parametrization is more general than the previous one

- ▶ valid for a generic Higgs (even not part of a doublet)
- ▶ resums the expansion in Higgs powers (if Higgs is a doublet)

# Double Higgs at Hadron Colliders

## Literature (for FCC<sub>100</sub>):

Baglio, Djouadi, Groeber, Muellheitner, Quevillon, Spira, JHEP 1304 (2013) 151

Yao, arXiv:1308.6302 (Snowmass Summer Study 2013)

Barr, Dolan, Englert, De Lima, Spannowsky, JHEP 1502 (2015) 016

Azatov, Contino, G.P, Son, Phys.Rev. D92 (2015) 3

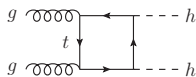
<b>Benchmark Scenarios:</b>	<b>LHC<sub>14</sub></b>	$\sqrt{s} = 14 \text{ TeV}, L = 300 \text{ fb}^{-1}$
	<b>HL-LHC</b>	$\sqrt{s} = 14 \text{ TeV}, L = 3 \text{ ab}^{-1}$
	<b>FCC<sub>100</sub></b>	$\sqrt{s} = 100 \text{ TeV}, L = 3 \text{ ab}^{-1}$



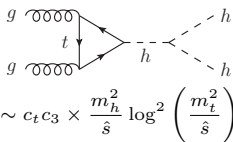
# Double Higgs production via Gluon Fusion

results from Azatov, Contino, G.P., Son, Phys.Rev. D92 (2015) 3

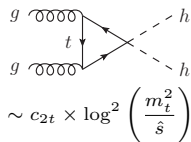
# Double Higgs production via gluon fusion



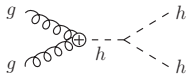
$$\sim c_t^2 \times \text{const.}$$



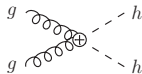
$$\sim c_t c_3 \times \frac{m_h^2}{\hat{s}} \log^2 \left( \frac{m_t^2}{\hat{s}} \right)$$



$$\sim c_{2t} \times \log^2 \left( \frac{m_t^2}{\hat{s}} \right)$$



$$\sim c_g c_3 \frac{\alpha_s}{4\pi} \times \text{const.}$$



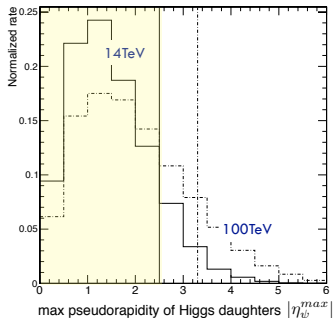
$$\sim c_{2g} \frac{\alpha_s}{4\pi} \frac{\hat{s}}{v^2}$$

- ❖ Different behaviour at high energy  $\sqrt{\hat{s}} = m_{hh} \gg 2m_h$
- ❖ Dependence on Higgs trilinear suppressed at high energy
  - ▶ events at threshold more sensitive to Higgs trilinear, events at large  $m_{hh}$  more important to determine the other operators

# Kinematics of the signal

Two **main differences** between 14 TeV and 100 TeV:

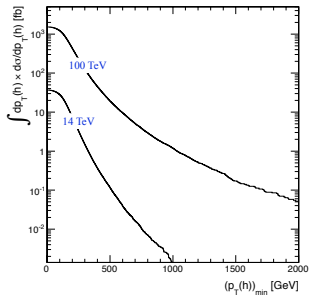
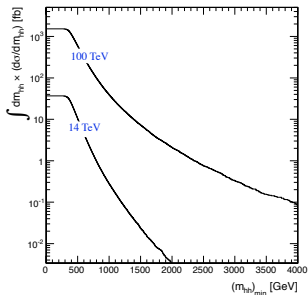
1. **Larger boost** of the  $hh$  system  $\Rightarrow$  higher fraction of decay products outside the detector region



- ▶ Fraction of events with  $|\eta| > 2.5$ : 13% at LHC  $\Rightarrow$  30% at 100 TeV
- ▶ Need to extend to  $|\eta| \leq 3.3$  to keep same fraction of events

# Kinematics of the signal

## 2. Larger invariant mass of the $hh$ system



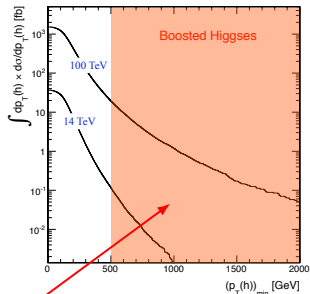
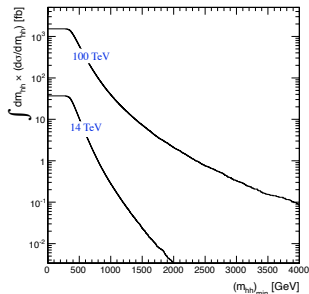
Highest accessible  $m_{hh}$  and  $p_T$  estimated by requiring at least 5 events beyond the threshold

channel	$b\bar{b}b\bar{b}$ (33.3%)	$b\bar{b}WW^*$ (24.9%)	$b\bar{b}\tau^+\tau^-$ (7.35%)	$b\bar{b}\gamma\gamma$ (0.264%)
Cross section	> 0.05 fb	> 0.067 fb	> 0.227 fb	> 6.31 fb
$m_{hh}$ [GeV]	< 1340(4290)	< 1280 (4170)	< 1039 (3235)	< 558 (1552)
$p_T$ [GeV]	< 575(2000)	< 575 (2000)	< 550 (1890)	< 210 (664)

[We use  $L = 3/\text{ab}$  and assume 10% efficiency. Numbers in parenthesis for a 100 TeV collider]

# Kinematics of the signal

## 2. Larger invariant mass of the $hh$ system



H  
be

**Jet substructure techniques crucial at 100 TeV**

least 5 events

$$\Delta R \sim \frac{2m_h}{p_T(h)} \lesssim 0.5 \quad \text{for} \quad p_T(h) \gtrsim 500 \text{ GeV}$$

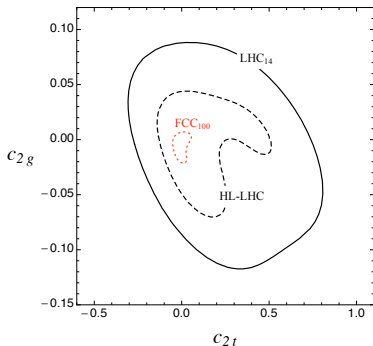
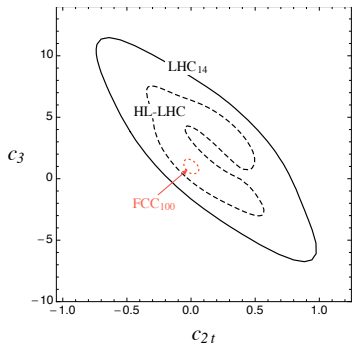
)  $b\bar{b}\gamma\gamma$  (0.264%)

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# Higgs couplings from the $b\bar{b}\gamma\gamma$ channel

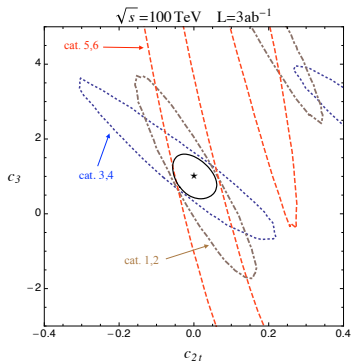
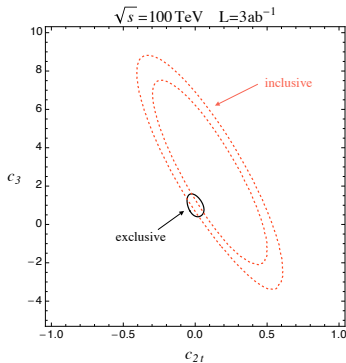
The non-linear Higgs couplings  $c_3$ ,  $c_{2t}$ ,  $c_{2g}$  can only be directly accessed in double-Higgs production



- ▶ Higgs trilinear can only be extracted at FCC (at LHC only  $\mathcal{O}(1)$  determination possible)
- ▶ good precision on  $c_{2t}$  and  $c_{2g}$

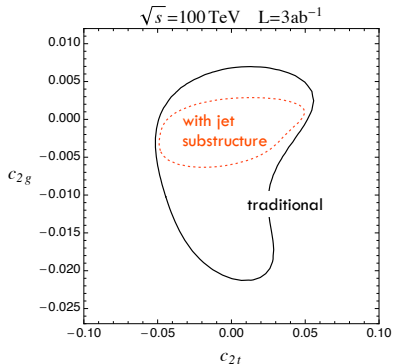
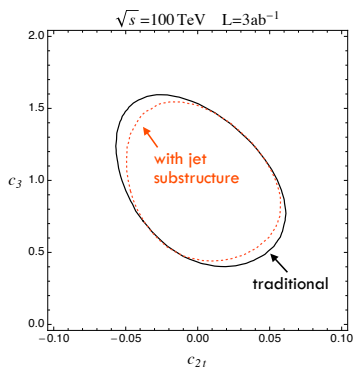
# Exclusive vs inclusive analysis

❖ **Exclusive analysis** is crucial at FCC<sub>100</sub>!



category	1	2	3	4	5	6
$m_{hh}$ [GeV]	250–400	400–550	550–700	700–850	850–1000	1000–

# Improvement from jet substructure

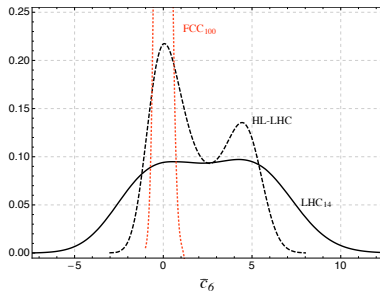
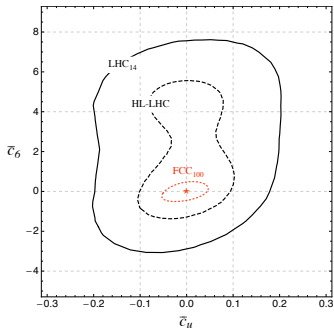


Jet substructure efficiently improves the sensitivity to boosted events

- important to extract  $c_{2g}$  (effects in the tail of the distribution)
- not crucial to determine  $c_3$  and  $c_{2t}$  (effects close to threshold)



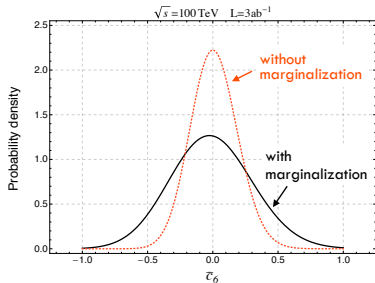
# Constraining the dim.-6 operators: $\bar{c}_u$ and $\bar{c}_6$



68% probability intervals on  $\bar{c}_6$

LHC <sub>14</sub>	HL-LHC	FCC <sub>100</sub>
$[-1.2, 6.1]$	$[-1.0, 1.8] \cup [3.5, 5.1]$	$[-0.33, 0.29]$

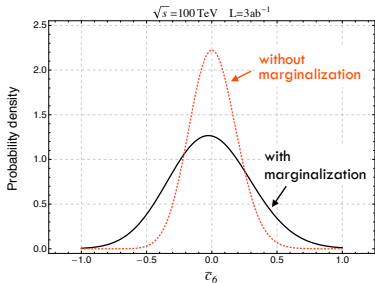
# The statistical treatment



**Marginalization** has a significant impact on the precision on  $\bar{c}_6$

	with marginalization	without marginalization
precision at FCC <sub>100</sub>	$[-0.33, 0.29]$	$[-0.18, 0.18]$

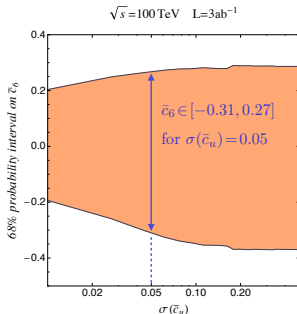
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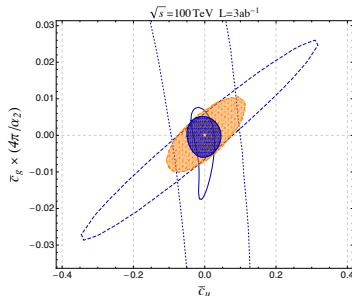
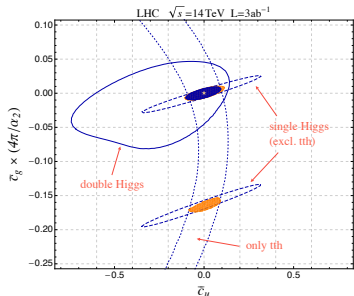
e.g. uncertainty on  $\bar{c}_u$   
increases uncertainty on  $\bar{c}_6$

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# Constraining the dim.-6 operators: $\bar{c}_u$ and $\bar{c}_g$



- double Higgs can resolve the degeneracy in  $c_g$
- at FCC<sub>100</sub> it can be competitive with  $t\bar{t}h$  for the determination of the top Yukawa  $\bar{c}_u$  (if precision from single Higgs similar to the LHC one)

Orange region: single Higgs incl.  $t\bar{t}h$

Blue region: single + double Higgs

# Double Higgs production via Vector Boson Fusion

results from Contino, Rojo, work in progress (courtesy of R. Contino)

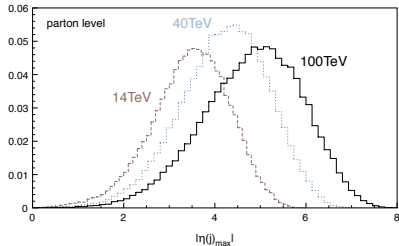
# Double Higgs production via vector boson fusion

$$\begin{array}{c} \text{Diagram 1: } \text{Wavy line} \text{ and } \text{Dashed line} \text{ cross} \\ \text{Diagram 2: } \text{Dashed line} \text{ and } \text{Wavy line} \text{ cross} \end{array} + \sim \frac{\hat{s}}{v^2} (c_V^2 - c_{2V})$$
$$\begin{array}{c} \text{Diagram 3: } \text{Wavy line} \text{ and } \text{Dashed line} \text{ meet at a vertex} \\ \text{Diagram 4: } \text{Dashed line} \text{ and } \text{Wavy line} \text{ meet at a vertex} \end{array} \sim \frac{m_h^2}{v^2} c_3 c_V$$

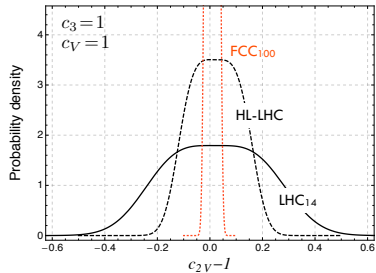
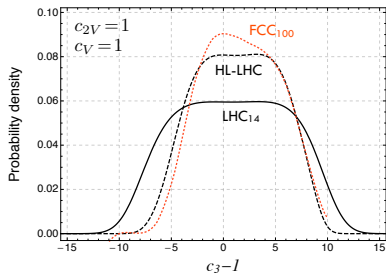
- ▶ Sensitivity on  $c_3$  mainly from events at threshold
- ▶ Events with large  $m_{hh}$  more important to extract  $c_{2V}$

Study of double Higgs in VBF at 100 TeV requires a detector in the very forward region

$\sim 67\%$  of signal events has  $|\eta(j)_{max}| > 4.5$



# Higgs couplings from the $hh \rightarrow 4b$ channel



Huge background, sensitive only if deviations much larger than the SM

- Poor precision on Higgs trilinear (not competitive with gluon fusion)
- FCC<sub>100</sub> can provide good bounds on  $\Delta c_{2V} \equiv c_{2V} - 1$

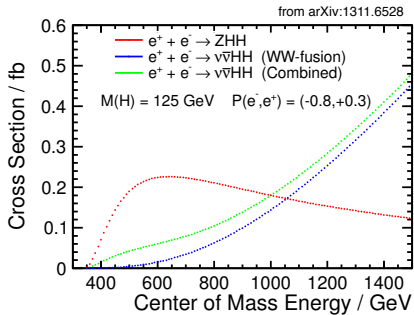
68% probability intervals on $\Delta c_{2V}$	LHC <sub>14</sub>	HL-LHC	FCC <sub>100</sub>
	$[-0.18, 0.22]$	$[-0.08, 0.12]$	$[-0.01, 0.03]$

# Double Higgs at $e^+e^-$ Colliders

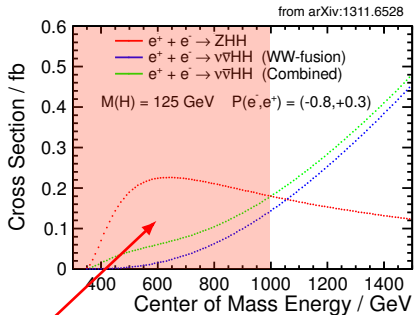
taken from R. Contino, talk at HPPC2015 (Mainz)



# Main production channels

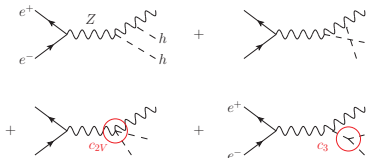


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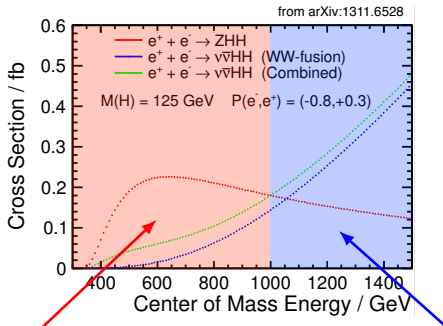


## Double Higgs-strahlung (DHS)

dominant below 1 TeV

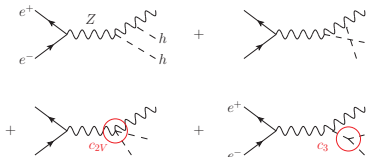


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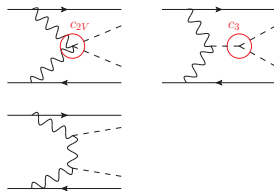
## Double Higgs-strahlung (DHS)

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## Vector Boson Fusion (VBF)

dominant above 1 TeV



# Expected precision on $c_3$ and $c_{2V}$

	COM Energy	Precision	Process	Reference
<b>ILC</b>	500 GeV [ $L = 500 \text{ fb}^{-1}$ ]	$\Delta c_3 \sim 104\%$	DHS	ILC TDR, Volume 2, arXiv:1306.6352
	1 TeV [ $L = 1 \text{ ab}^{-1}$ ]	$\Delta c_3 \sim 28\%$	VBF	ILC TDR, Volume 2, arXiv:1306.6352
		$\Delta c_{2V} \sim 20\%$	DHS	Contino et al., JHEP 1402 (2014) 006
<b>CLIC</b>	1.4 TeV [ $L = 1.5 \text{ ab}^{-1}$ ]	$\Delta c_3 \sim 24\%$	VBF	Roloff (CLICdp Coll.), talk at LCWS14
		$\Delta c_{2V} \sim 7\%$		
	3 TeV [ $L = 2 \text{ ab}^{-1}$ ]	$\Delta c_3 \sim 12\%$		
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Precision on  $c_{2V}$  worse than FCC100 (effects grow with energy)

# Conclusions

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- ❖ Double Higgs production is an essential channel to extract information on the non-linear Higgs couplings
  - Measure the Higgs trilinear coupling  $c_3$
  - Access new couplings to top and gluon:  $c_{2t}, c_{2g}, c_{2V}$
  
- ❖ Leptonic vs Hadronic colliders
  - $e^+e^-$  machines
    - ▶ can extract  $c_3$  and  $c_{2V}$ , but  $\sqrt{s} \gtrsim 1$  TeV is needed
  - $pp$  machines
    - ▶ better precision with energy-growing interactions  $c_{2t}, c_{2g}, c_{2V}$
    - ▶ good precision on Higgs trilinear thanks to high statistics



**Backup material**

# Sensitivity on the EFT coefficients

Precision on single-Higgs observables from ATLAS projection

[ATL-PHYS-PUB-2013-014]

	300 fb <sup>-1</sup>	3 ab <sup>-1</sup>
$\sigma(\bar{c}_H)$	7.9%	5.4%
$\sigma(\bar{c}_u)$	5.9% ( $w/t\bar{t}h$ )	5.4% ( $w/t\bar{t}h$ )
	20% ( $t\bar{t}h$ )	7.7% ( $t\bar{t}h$ )
$\sigma(\bar{c}_d)$	6.3%	4.4%

ATLAS Simulation Preliminary

$\sqrt{s} = 14$  TeV:  $\int \mathcal{L} dt = 300 \text{ fb}^{-1}$  ;  $\int \mathcal{L} dt = 3000 \text{ fb}^{-1}$

