

Testing gravity with atom interferometry

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Firenze, Italy

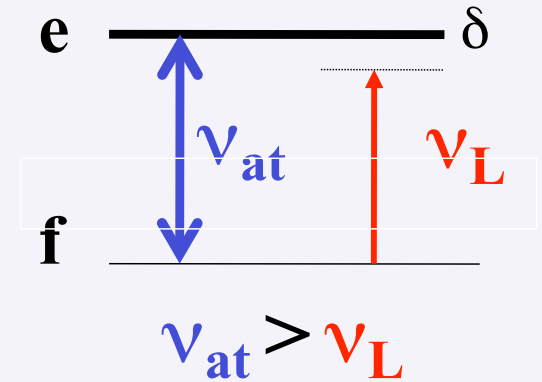
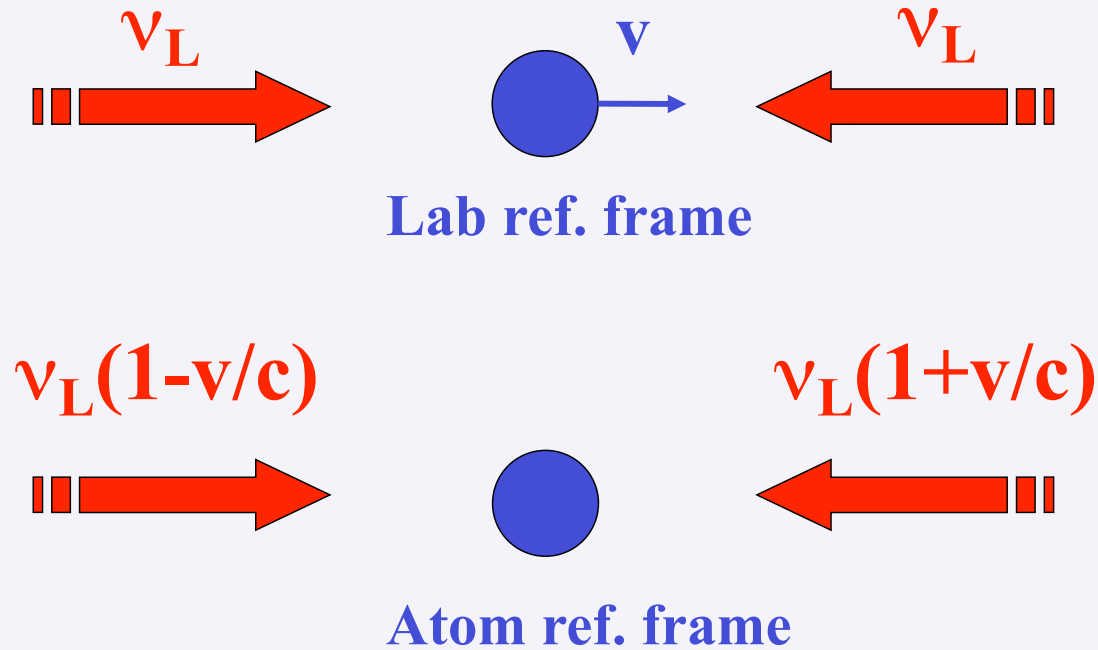
<http://coldatoms.lens.unifi.it/>

Outline

- *Laser cooling and manipulation of atoms*
- *Future optical clocks with trapped atoms*
- *Cold atom interferometry*
- *Fundamental physics experiments and applications on Earth and in space*

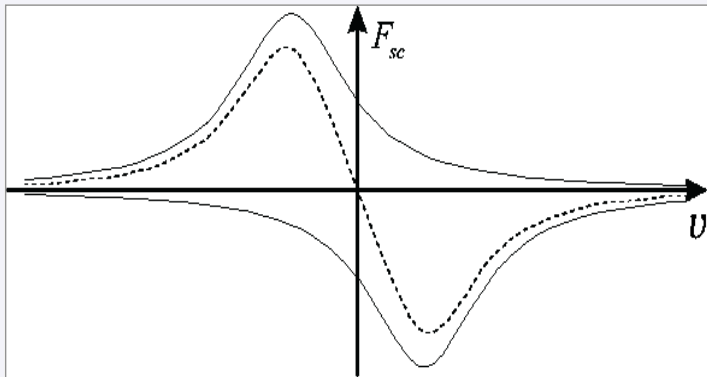
Laser cooling and manipulation of atoms

Optical molasses



$(I/I_0 \ll 1)$

$$F(\nu) \approx \frac{h\nu_L}{c} \times \frac{1}{2\pi} \times \left[\frac{I/I_0}{1 + I/I_0 + \frac{4}{\Gamma^2} (\delta - \frac{\nu_L}{c} \nu)^2} - \frac{I/I_0}{1 + I/I_0 + \frac{4}{\Gamma^2} (\delta + \frac{\nu_L}{c} \nu)^2} \right]$$



$$F(\nu) \approx \frac{h}{4\pi^2} \frac{\omega_L^2 8\delta}{c^2 \Gamma} \frac{I/I_0}{[1 + (\frac{2\delta}{\Gamma})^2]^2} \nu = -\alpha \nu$$

Idea: T.W. Hänsch, A. Schawlow, 1975

Exp. demonstration: S. Chu et al., 1985

Laser cooling: atomic temperatures

Atomic Temperature : $k_B T = M v_{\text{rms}}^2$

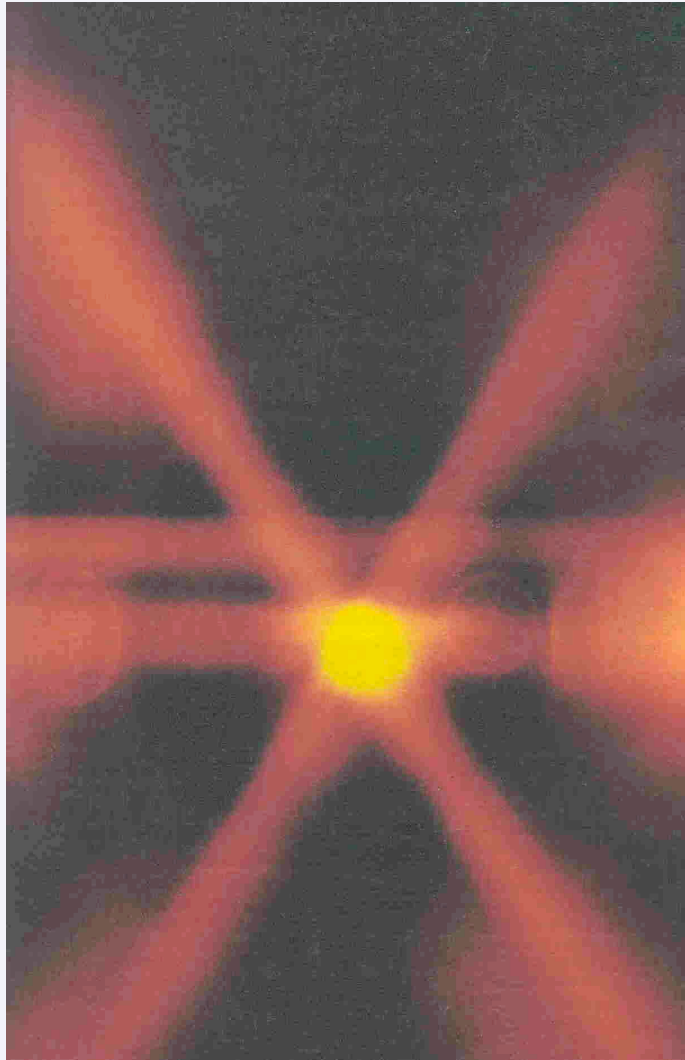
Minimum temperature for Doppler cooling: $k_B T_D = \frac{h\Gamma}{2}$

Single photon recoil temperature: $k_B T_r = \frac{1}{M} \left(\frac{h\nu_L}{c} \right)^2$

Examples:

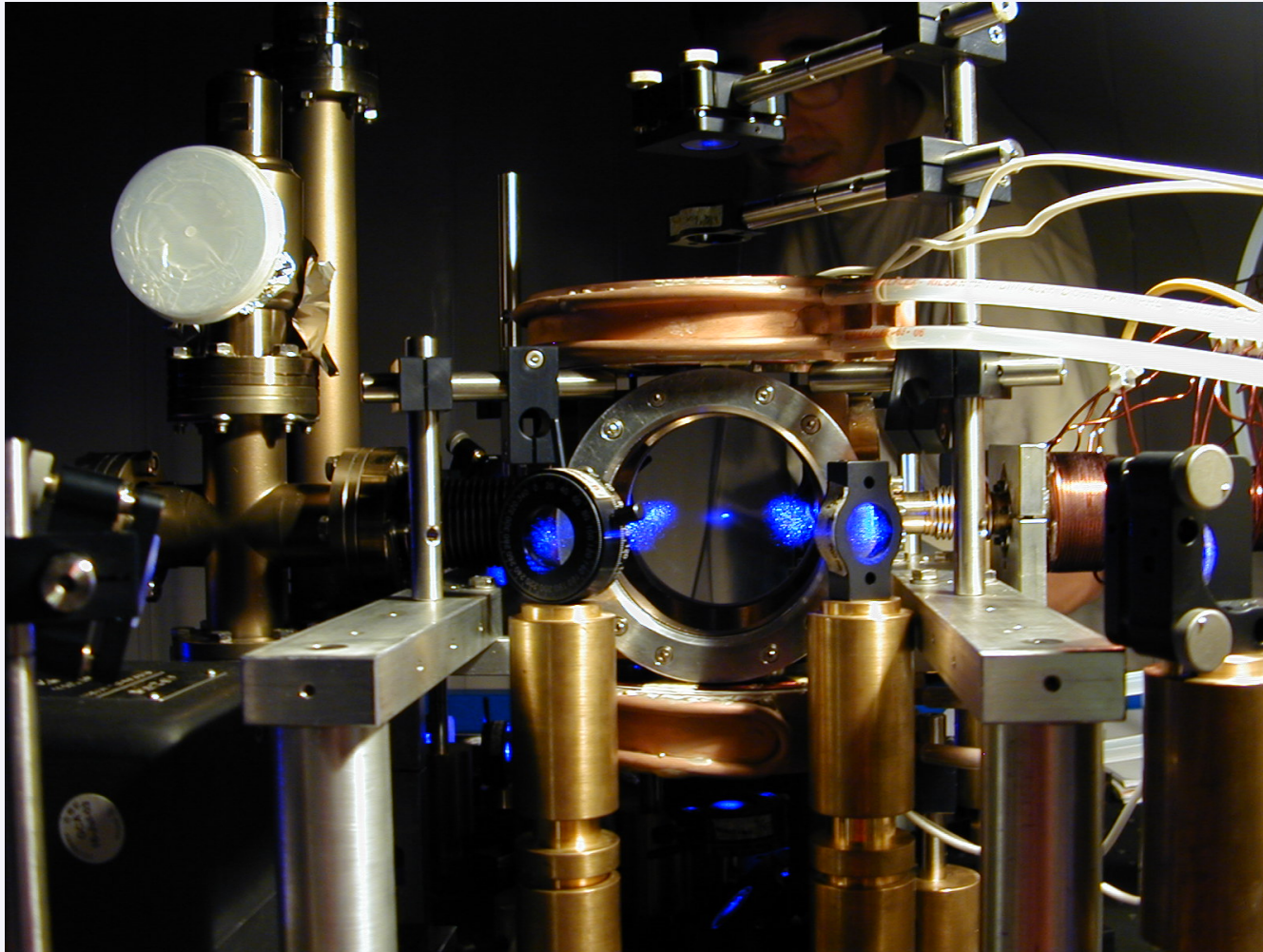
	T_D	T_r
Na	240 μK	2.4 μK
Rb	120 μK	360 nK
Cs	120 μK	200 nK
Sr (intercombination transition)	180 nK	460 nK

3D molasses



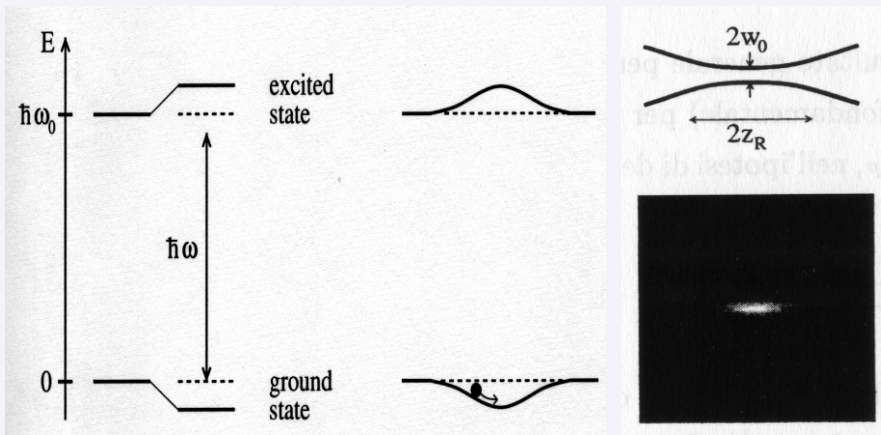
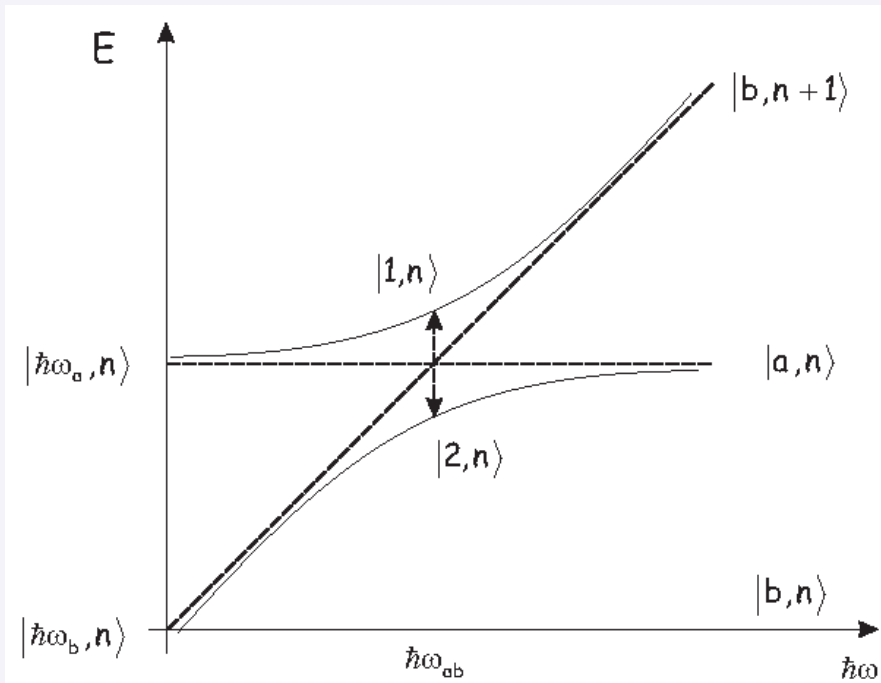
Na molasses

Sr MOT picture



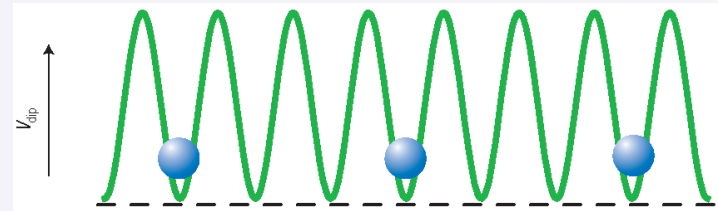
LENS, Firenze

Light shifts and optical traps

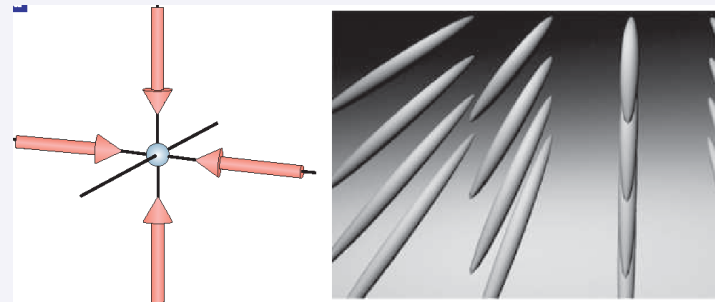


$$V_{\text{dip}}(\mathbf{r}) = -\mathbf{d} \cdot \mathbf{E}(\mathbf{r}) \propto \alpha(\omega_L) |\mathbf{E}(\mathbf{r})|^2$$

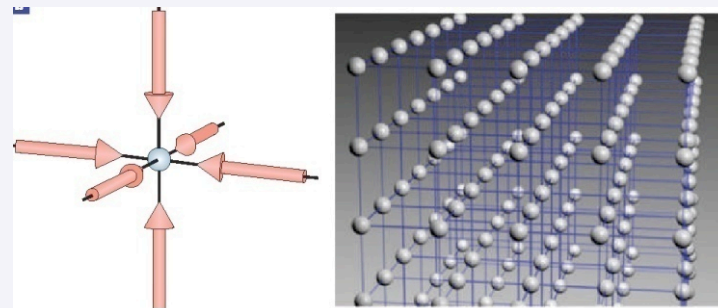
optical lattices



1D optical lattice \Rightarrow array of 2D disk-like trapping potentials



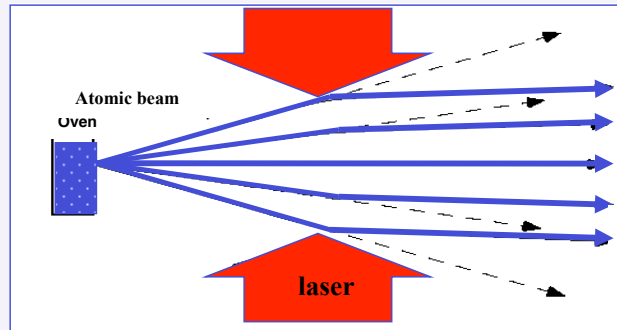
2 D optical lattice \Rightarrow array of 1D potential tubes



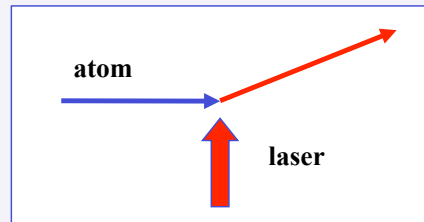
3 D optical lattice \Rightarrow 3D simple cubic array of h.o. potentials

Atom optics

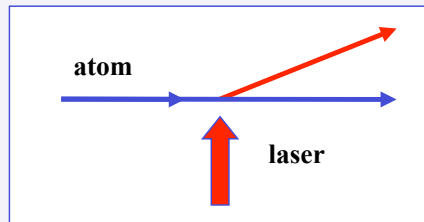
lenses



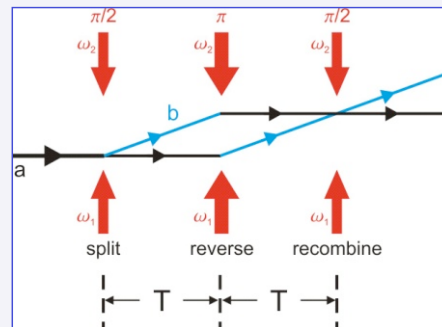
mirrors



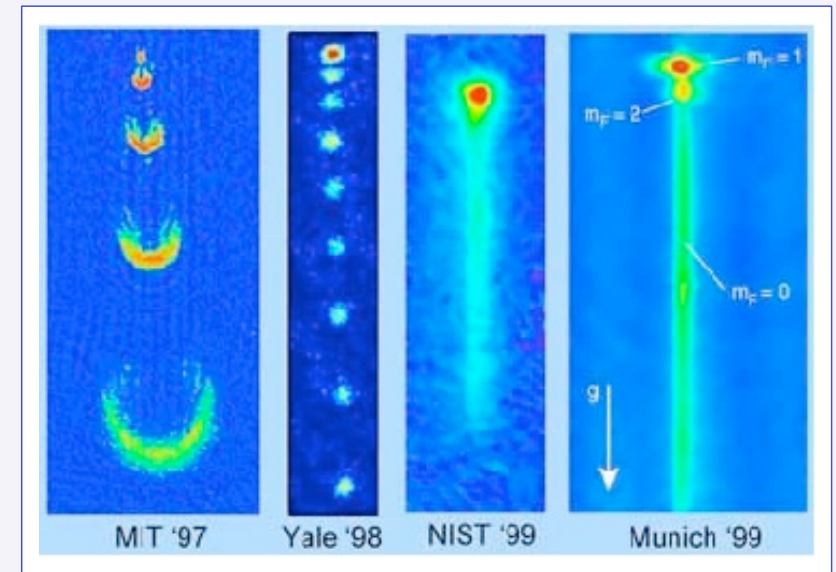
beam-splitters



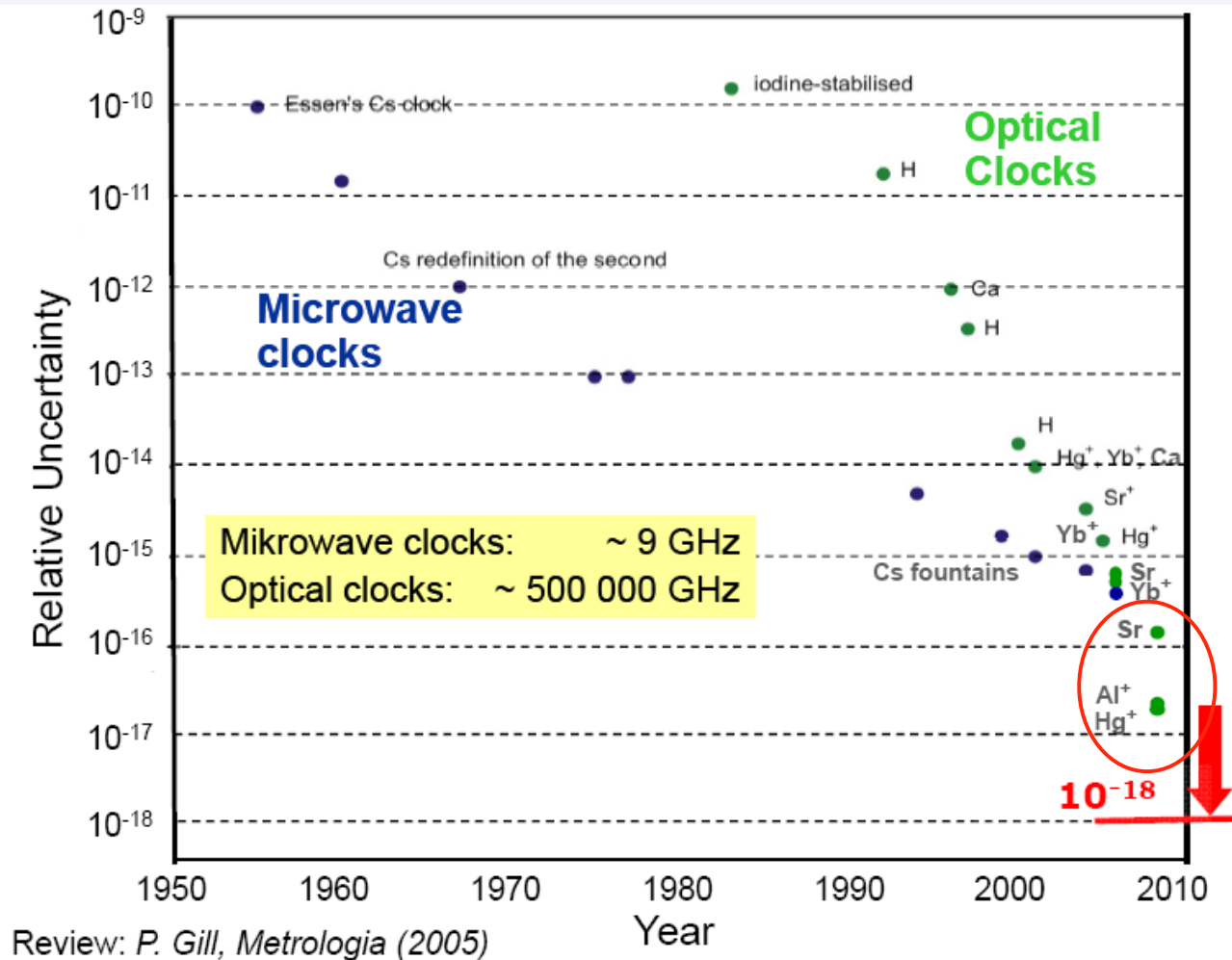
interferometers



atom laser



Optical vs microwave clocks



- Al⁺, Hg⁺ single ion clocks

T. Rosenband *et al.*,
Science **319**, 1808 (2008)

- Sr optical lattice clock

G. K. Campbell *et al.*,
Science **324**: 360 (2009)

clock **stability**

$$\sigma_y(\tau) \approx 10^{-15} \tau^{-1/2}$$

clock **accuracy**

$$\delta\nu / \nu < 10^{-17}$$

Optical clocks: Towards 10^{-18}

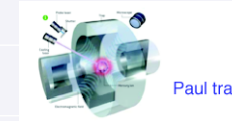
- Narrow optical transitions

$$\delta\nu_0 \sim 1\text{-}100 \text{ Hz}, \nu_0 \sim 10^{14}\text{-}10^{15} \text{ Hz}$$

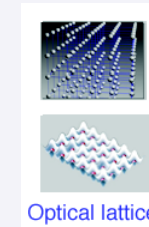
$$\sigma_y \approx \frac{\text{Noise}}{\pi Q \cdot \text{Signal}} \approx \frac{\Delta\nu}{\nu_0} \frac{1}{\sqrt{N_{\text{atom}}}} \sqrt{\frac{T_{\text{cycle}}}{2\tau_{\text{average}}}} \frac{1}{C_{\text{fringe}}}$$

- Candidate atoms

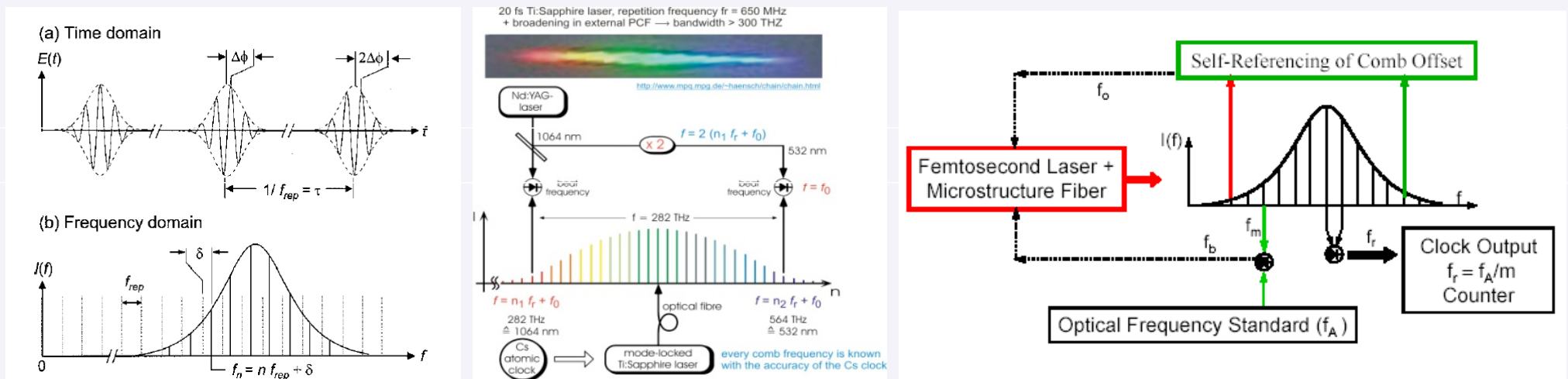
Trapped ions: $\text{Hg}^+, \text{In}^+, \text{Sr}^+, \text{Yb}^+, \dots$



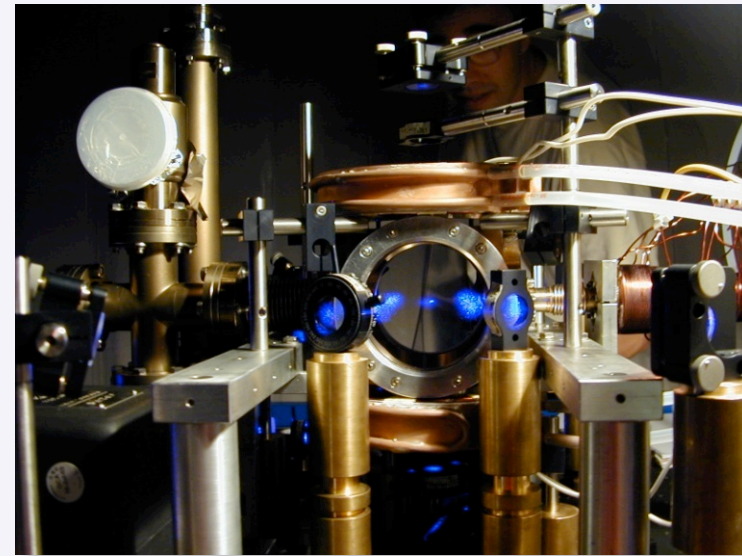
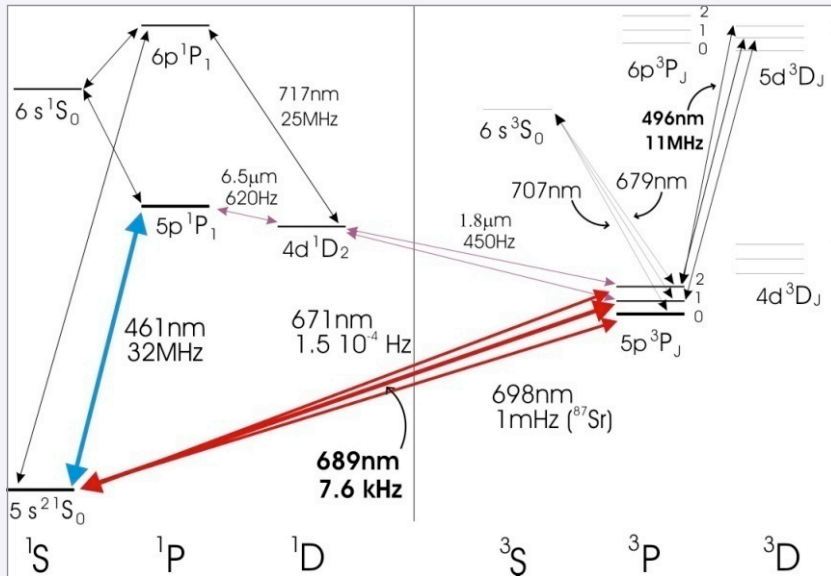
Cold neutral atoms: $\text{H}, \text{Ca}, \text{Sr}, \text{Yb}, \dots$
(Fermions?)



- Direct optical- μ wave connection by optical frequency comb



Ultracold Sr – The experiment in Firenze



- Optical clocks using visible intercombination lines

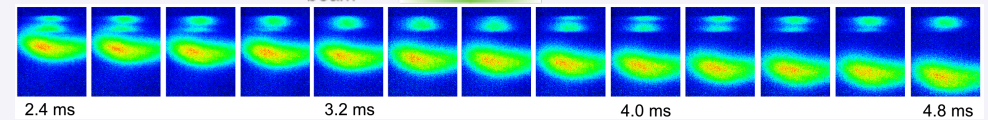
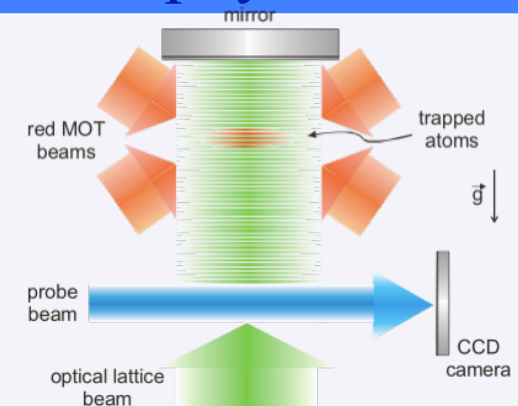
- New atomic sensors for fundamental physics tests

Optical clocks using visible intercombination lines

- $^1S_0 - ^3P_1$ (7.5 kHz)
- $^1S_0 - ^3P_0$ (1 mHz, ^{87}Sr)
- $^1S_0 - ^3P_2$ (0.15 mHz)
- Optical trapping in Lamb-Dicke regime with negligible change of clock frequency
- Comparison with different ultra-stable clocks



G. Ferrari, P. Cancio, R. Drullinger, G. Giusfredi, N. Poli, M. Prevedelli, C. Toninelli, G.M. Tino, *Precision Frequency Measurement of Visible Intercombination Lines of Strontium*, Phys. Rev. Lett. 91, 243002 (2003)



G. Ferrari, N. Poli, F. Sorrentino, and G. M. Tino, Long-lived Bloch oscillations with bosonic Sr atoms and application to gravity measurement at micrometer scale, Phys. Rev. Lett. 97, 060402 (2006)

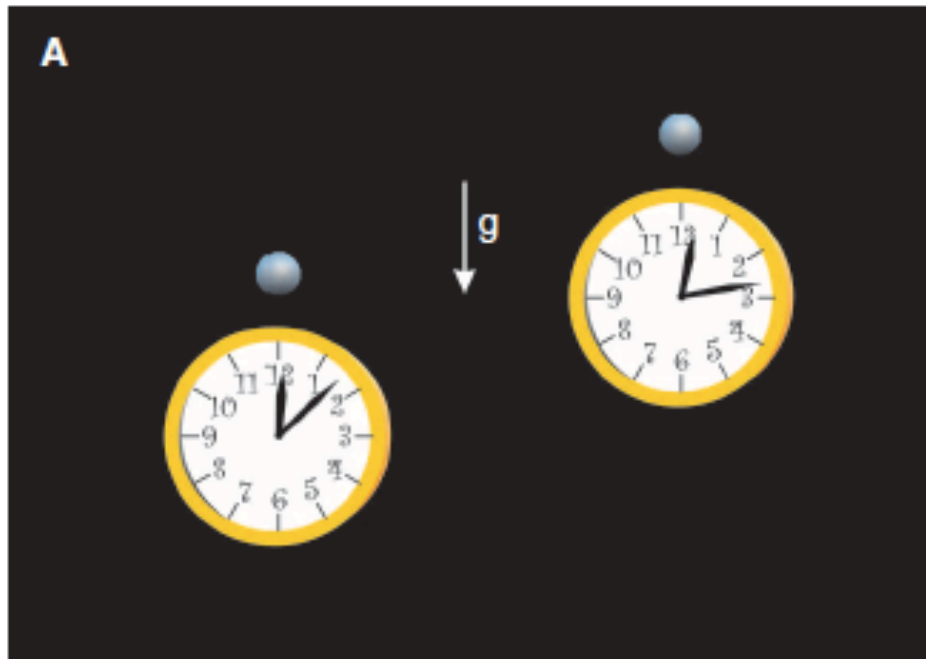
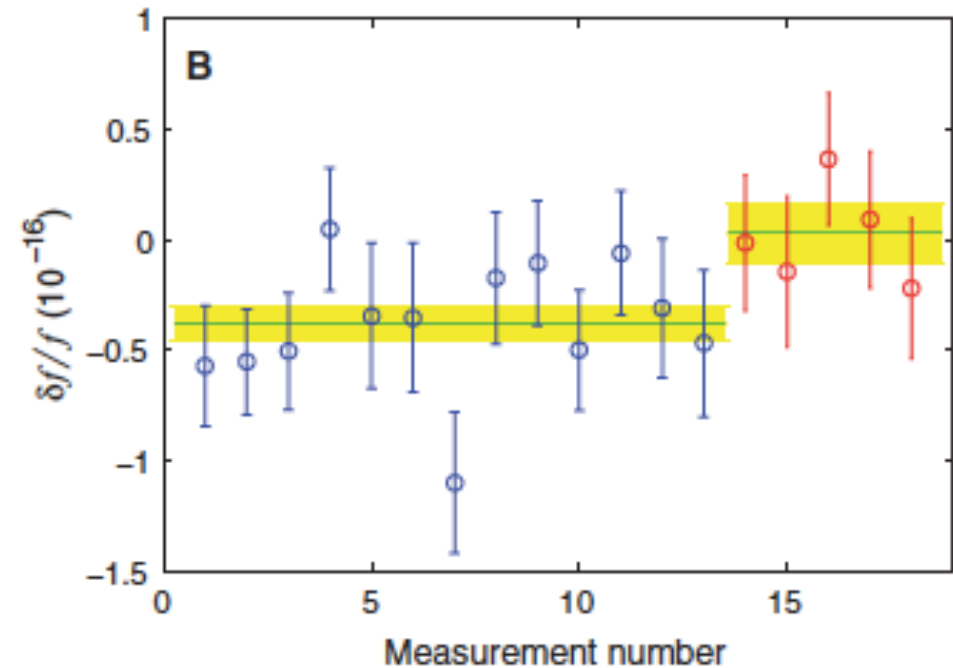


Fig. 3. Gravitational time dilation at the scale of daily life. **(A)** As one of the clocks is raised, its rate increases when compared to the clock rate at deeper gravitational potential. **(B)** The fractional difference in frequency between two Al^+ optical clocks at different heights. The Al-Mg clock was initially 17 cm lower in height than the Al-Be clock, and subsequently, starting at data point 14, elevated by 33 cm. The net relative shift due to the increase in

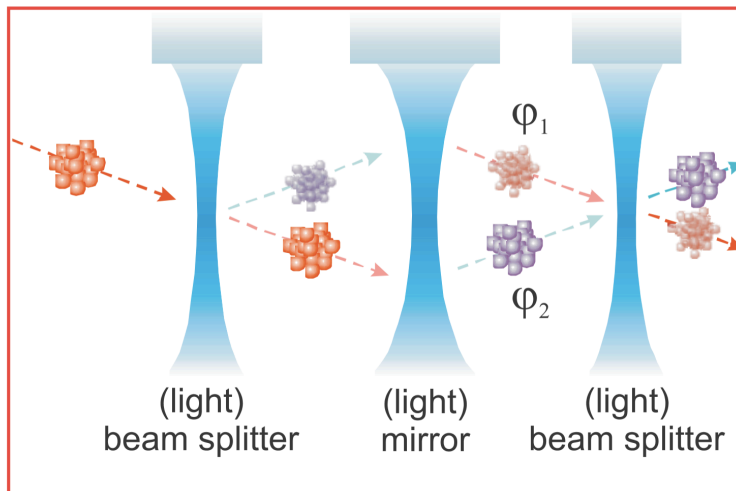


height is measured to be $(4.1 \pm 1.6) \times 10^{-17}$. The vertical error bars represent statistical uncertainties (reduced $\chi^2 = 0.87$). Green lines and yellow shaded bands indicate, respectively, the averages and statistical uncertainties for the first 13 data points (blue symbols) and the remaining 5 data points (red symbols). Each data point represents about 8000 s of clock-comparison data.

Atom Interferometry

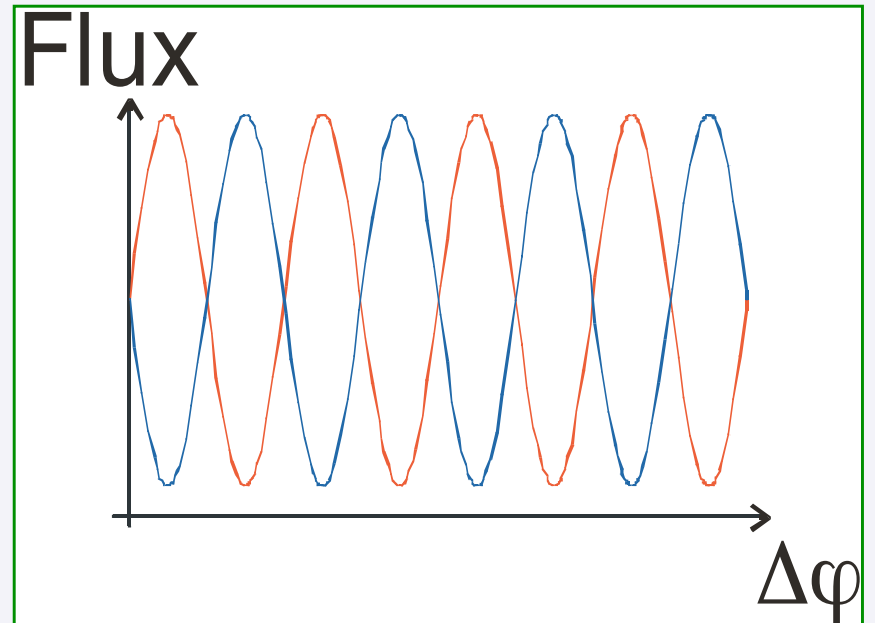
Atom interferometry

Atom interferometer



Phase difference

$$\Delta\varphi = \varphi_1 - \varphi_2$$



atomic flux at **exit** port **1**
at **exit** port **2**

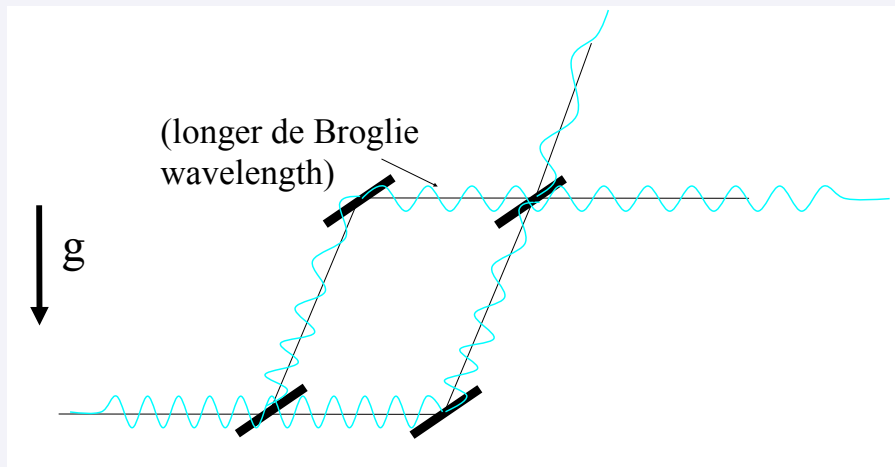
Atom interferometer force sensors

The quantum mechanical wave-like properties of atoms can be used to sense inertial forces.

$$\lambda_{DB} = \frac{h}{Mv}$$

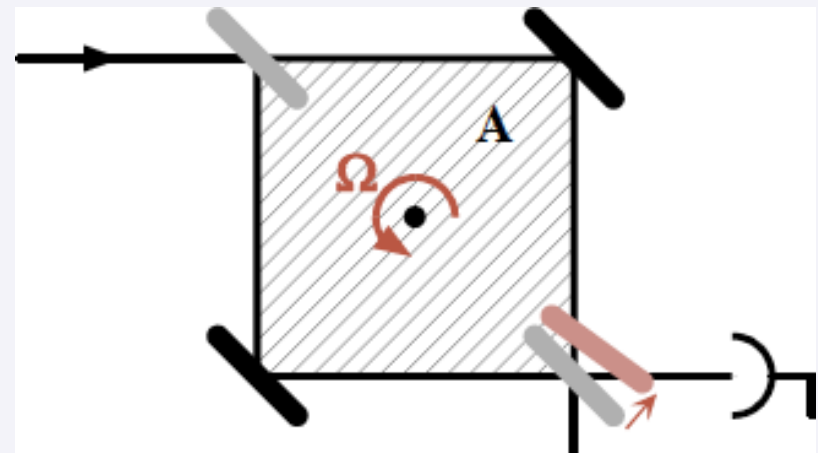
Gravity/Accelerations

As atom climbs gravitational potential, velocity decreases and wavelength increases



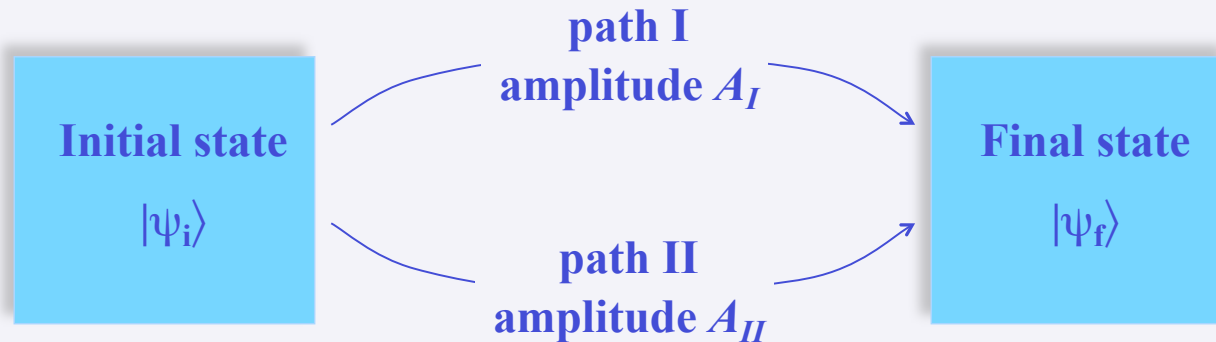
Rotations

Rotations induce path length differences by shifting the positions of beam splitting optics



From M. Kasevich

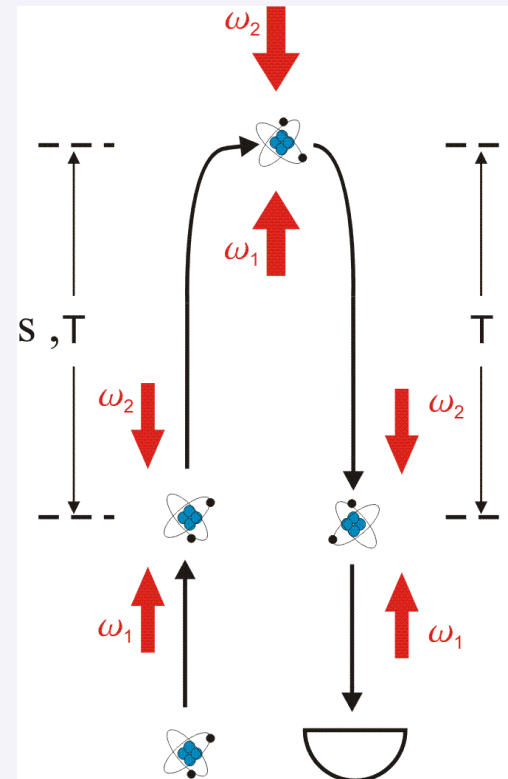
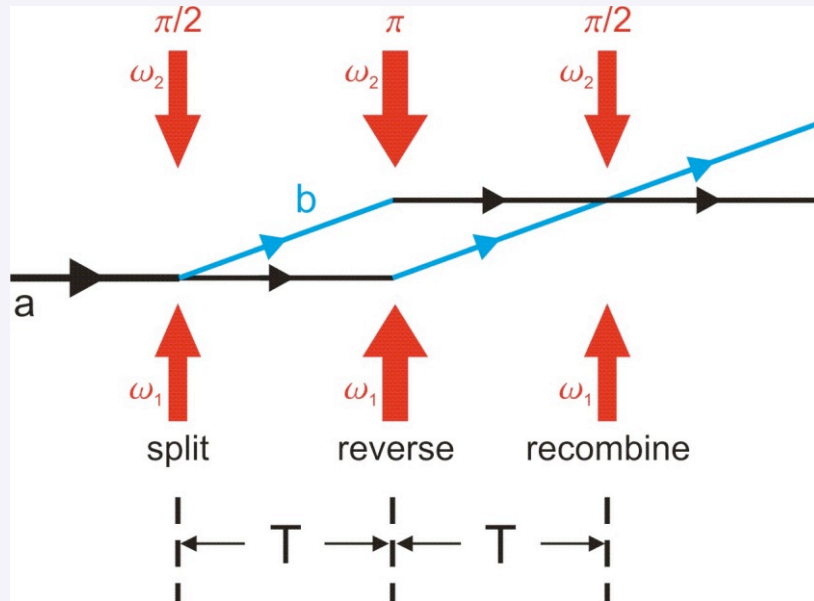
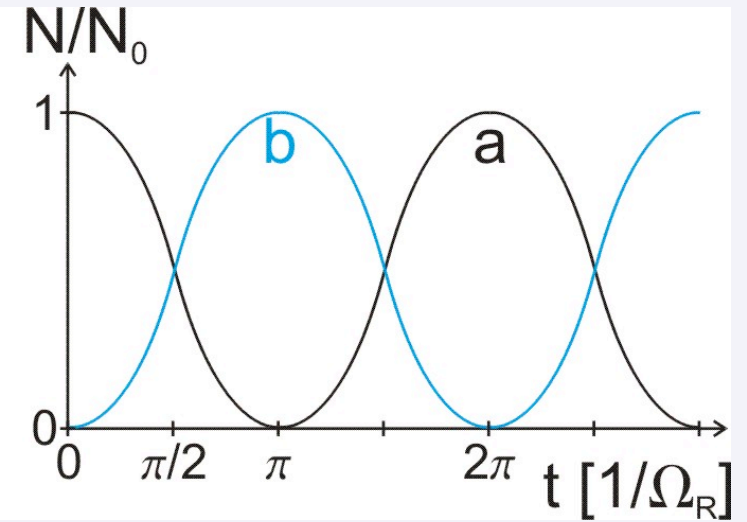
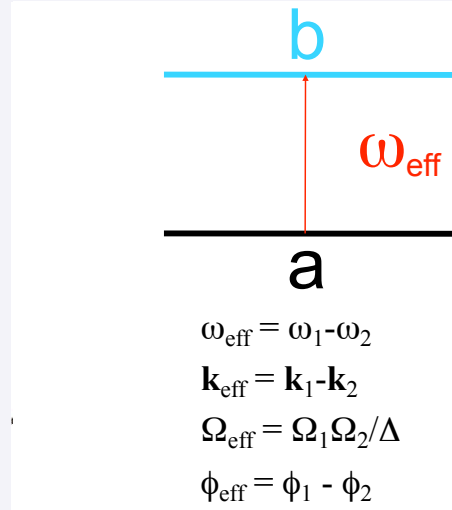
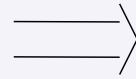
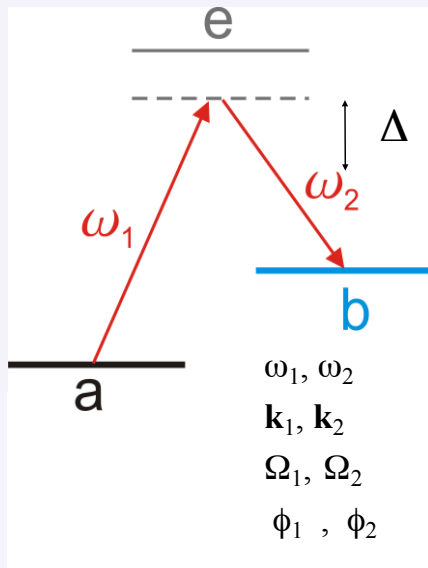
Quantum interference



Interference of transition amplitudes

$$\mathbf{P}(|\psi_i\rangle \Rightarrow |\psi_f\rangle) = |A_I + A_{II}|^2 = |A_I|^2 + |A_{II}|^2 + 2 \operatorname{Re}(A_I A_{II}^*)$$

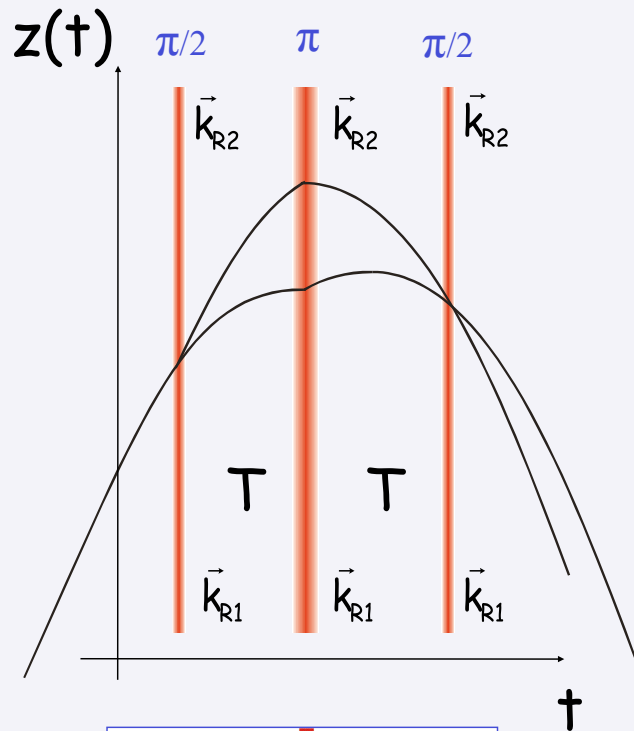
Raman pulse interferometer



M. Kasevich, S. Chu, *Appl. Phys. B* **54**, 321 (1992)

A. Peters, K.Y. Chung and S. Chu, *Nature* **400**, 849 (1999)

Raman interferometry in an atomic fountain



Phase difference between the paths:

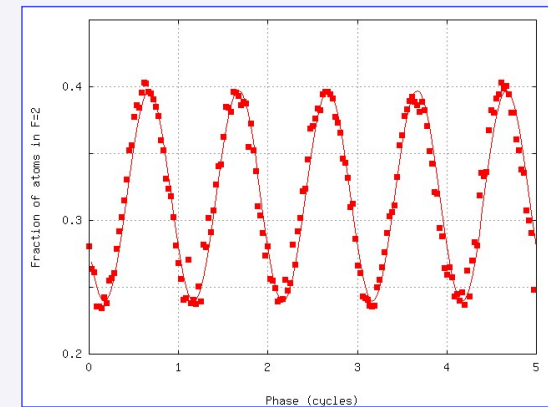
$$\Delta\Phi = k_e[z(0) - 2z(T) + z(2T)] + \Phi_e \quad k_e = k_1 - k_2, \quad \omega_e = c k_e$$

with $z(t) = -g t^2/2 + v_0 t + z_0$ & $\Phi_e = 0 \Rightarrow \Delta\Phi = k_e g T^2$

$$g = \Delta\Phi / k_e T^2$$

Final population:

$$N_a = N/2 (1 + \cos[\Delta\Phi])$$

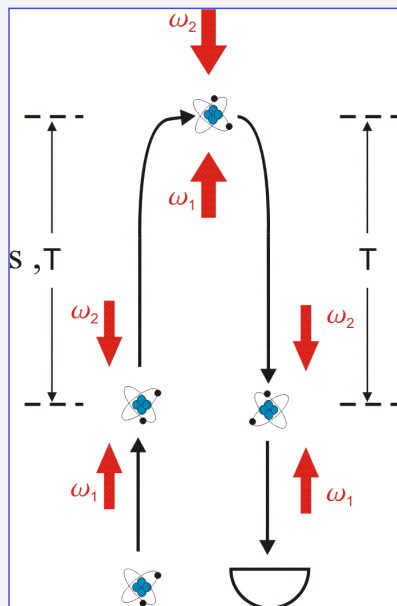


Interference fringes – Firenze 2006

$$T = 150 \text{ ms} \Rightarrow 2\pi = 10^{-6} g$$

$$S/N = 1000$$

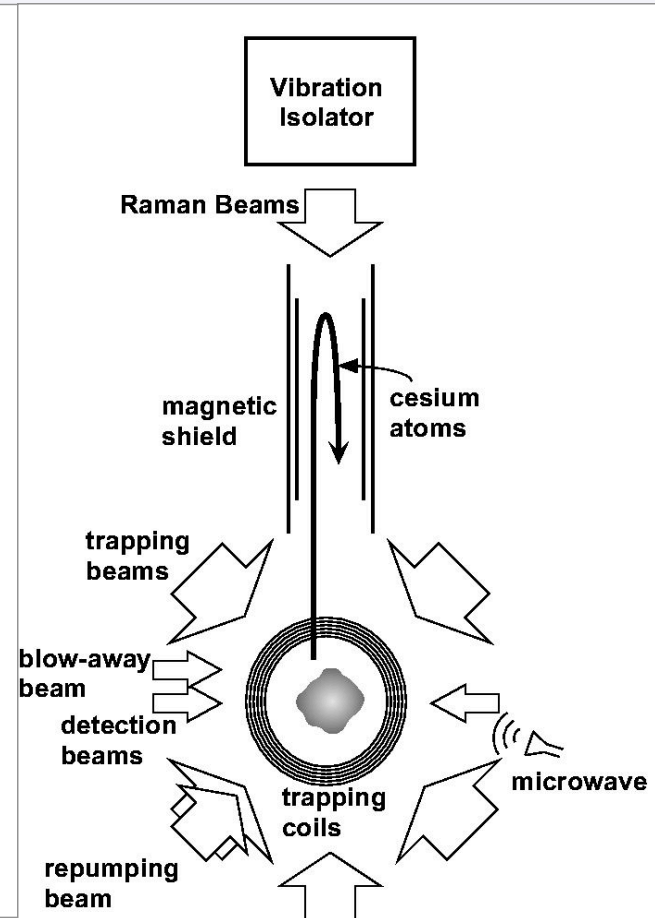
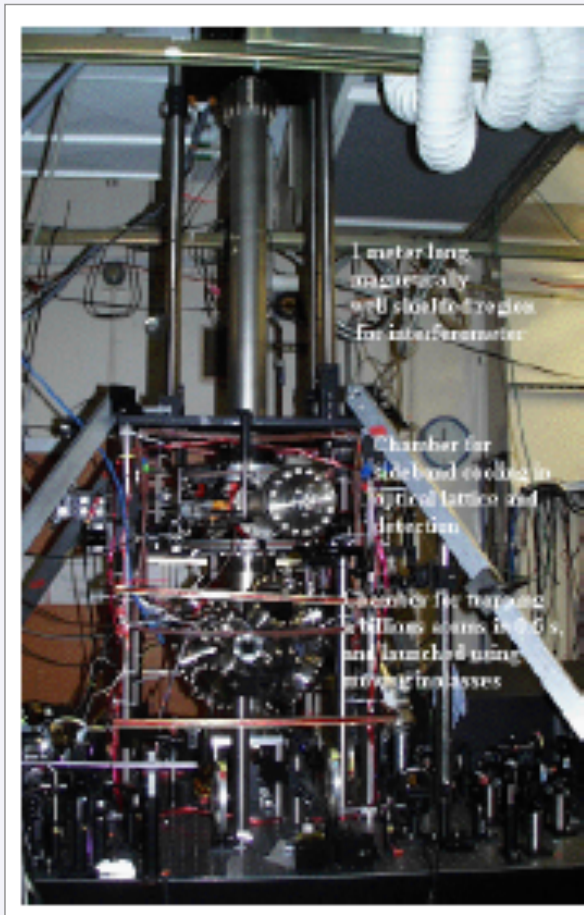
$$\Rightarrow \text{Sensitivity } 10^{-9} \text{ g/shot}$$



M. Kasevich, S. Chu, *Appl. Phys. B* **54**, 321 (1992)

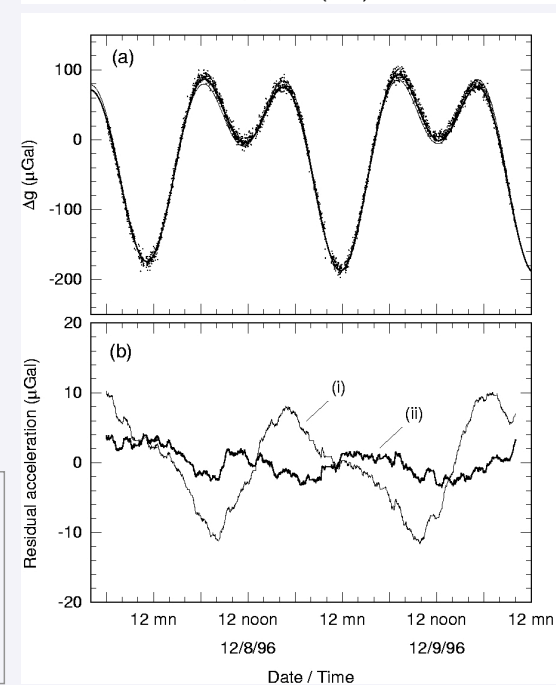
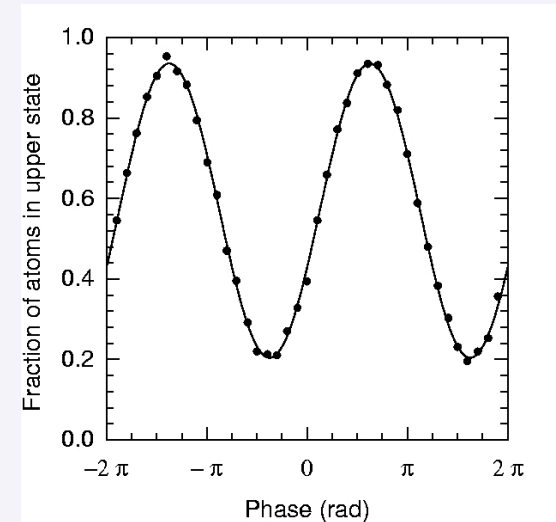
A. Peters, K.Y. Chung and S. Chu, *Nature* **400**, 849 (1999)

Stanford atom gravimeter

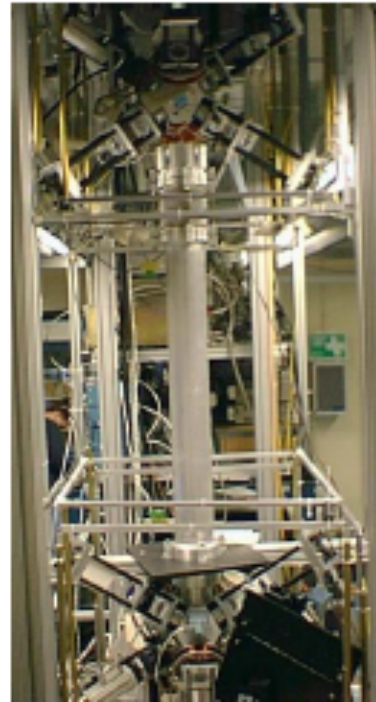


Resolution: 3×10^{-9} g after 1 minute

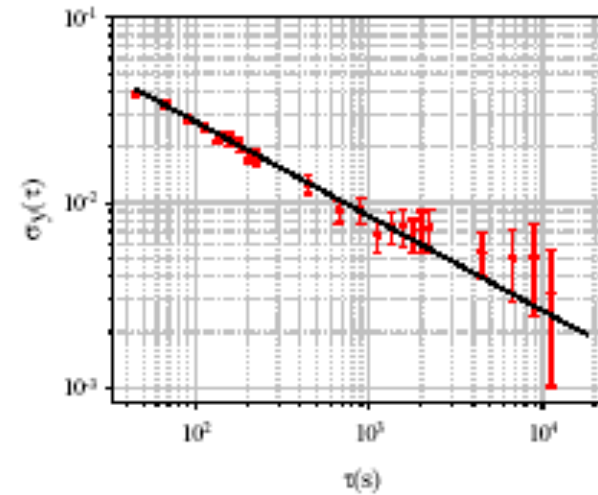
Absolute accuracy: $\Delta g/g < 3 \times 10^{-9}$



Stanford/Yale gravity gradiometer



1.4 m



Demonstrated differential acceleration sensitivity:

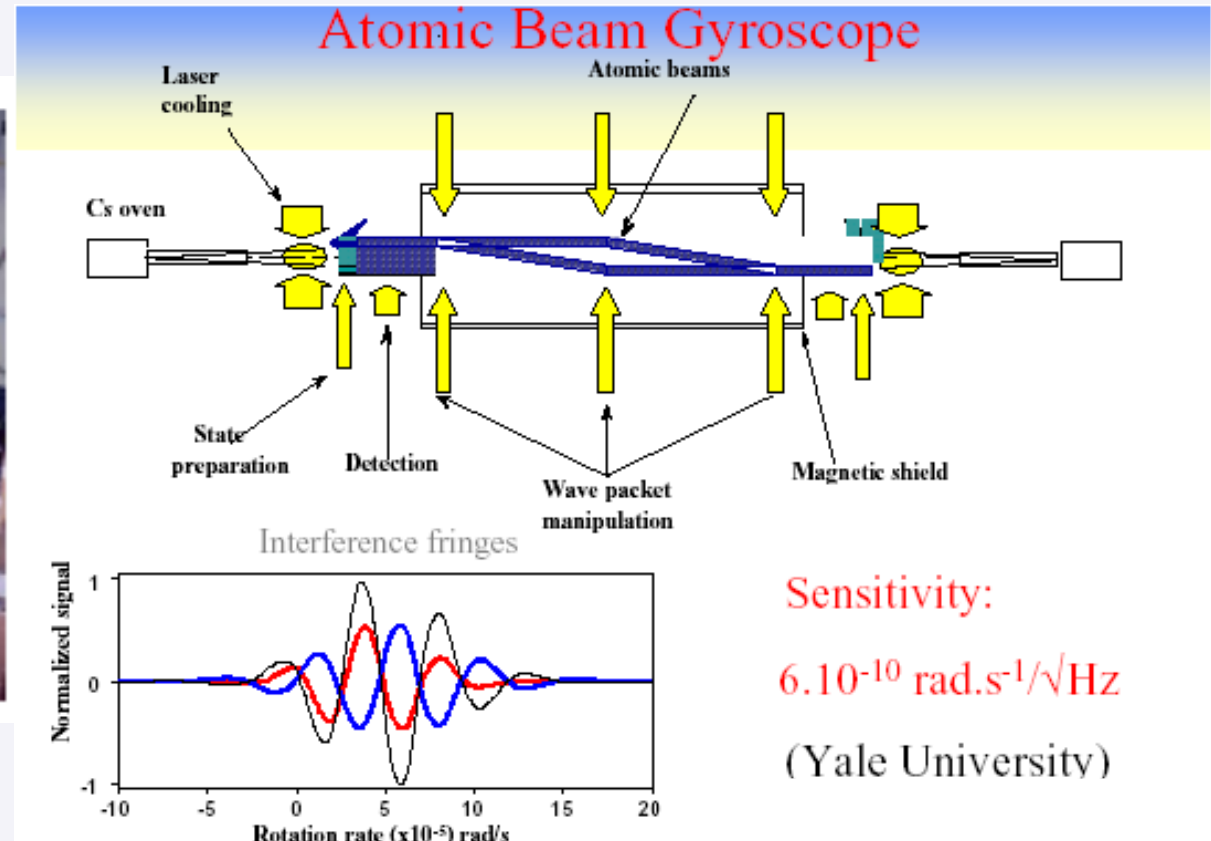
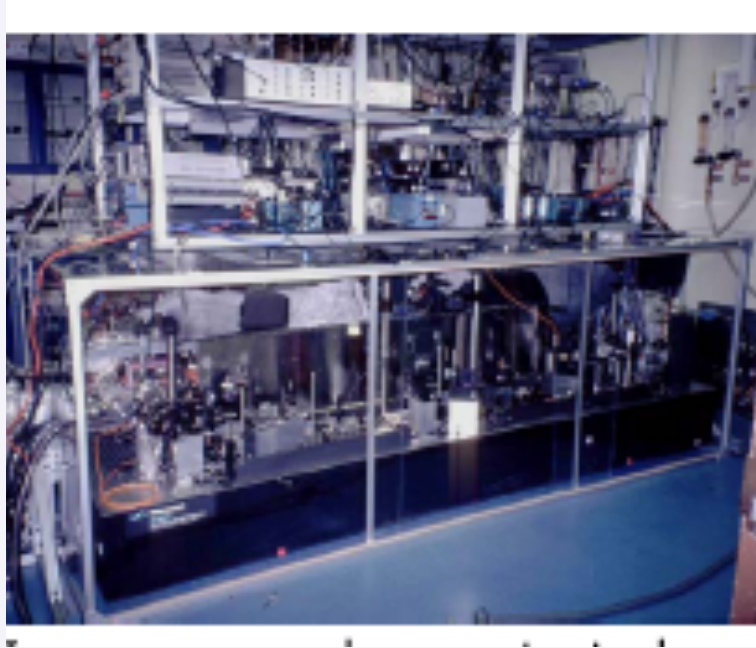
$$4 \times 10^{-9} \text{ g/Hz}^{1/2}$$

($2.8 \times 10^{-9} \text{ g/Hz}^{1/2}$ per accelerometer)

from M.A. Kasevich

Distinguish gravity induced accelerations from those due to platform motion with differential acceleration measurements.

Stanford/Yale gyroscope



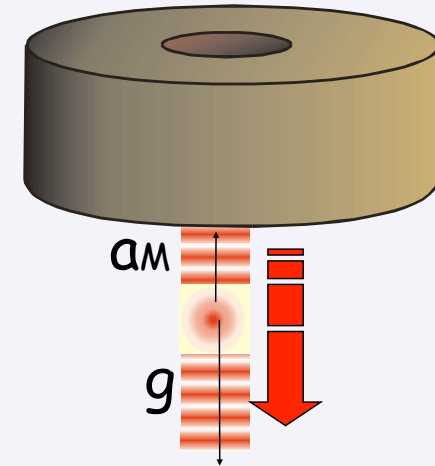
T.L. Gustavson, A. Landragin and M.A. Kasevich, *Class. Quantum Grav.* **17**, 2385 (2000)

MAGIA

(*MISURA ACCURATA di G MEDIANTE INTERFEROMETRIA ATOMICA*)

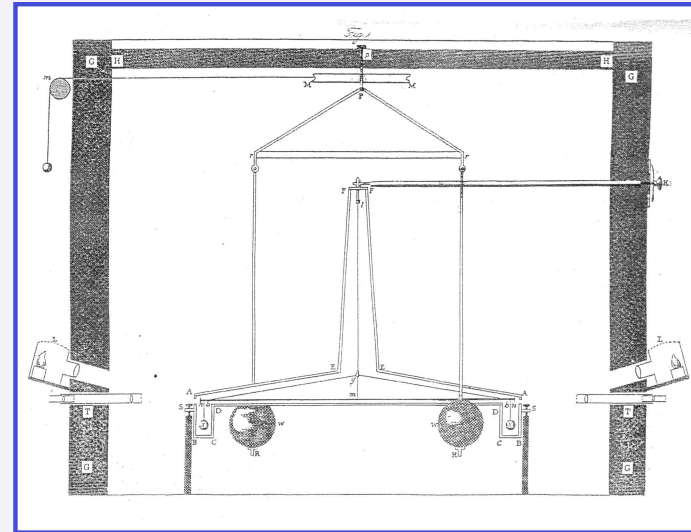
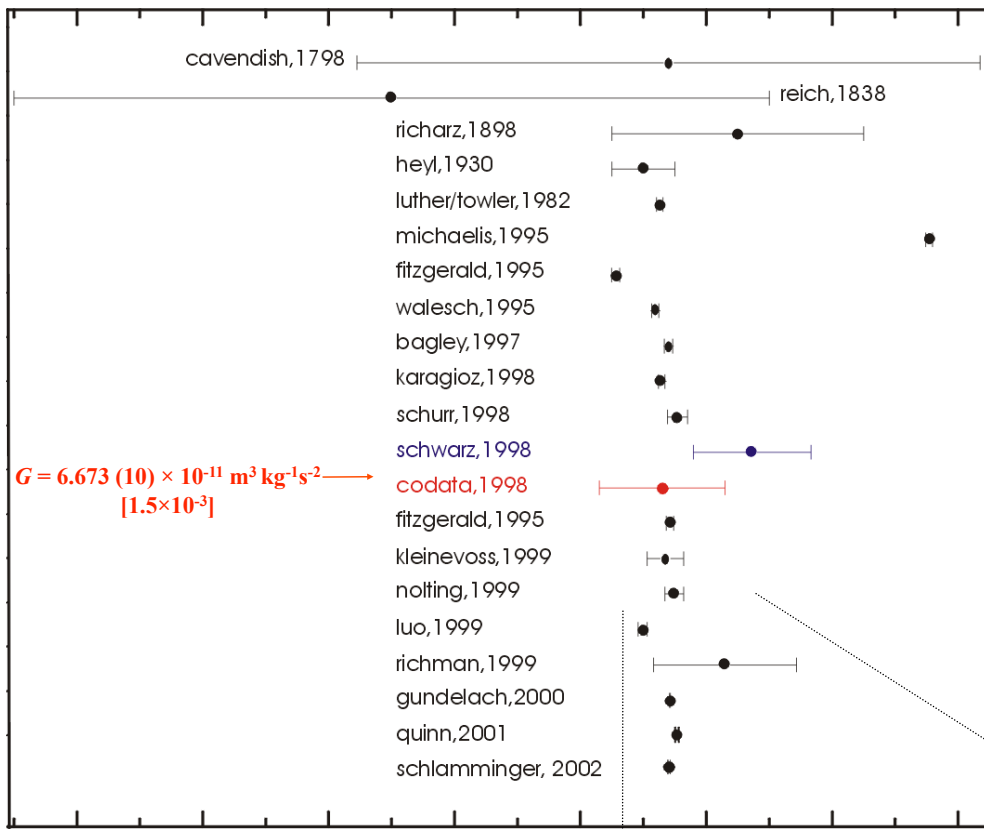


- Measure g by atom interferometry
- Add source masses
- Measure change of g

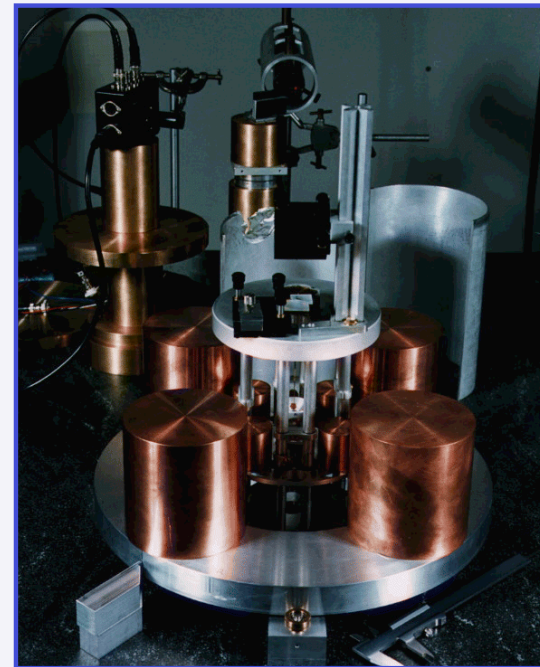


- *Precision measurement of G*
- *Test of Newtonian law at micrometric distances*

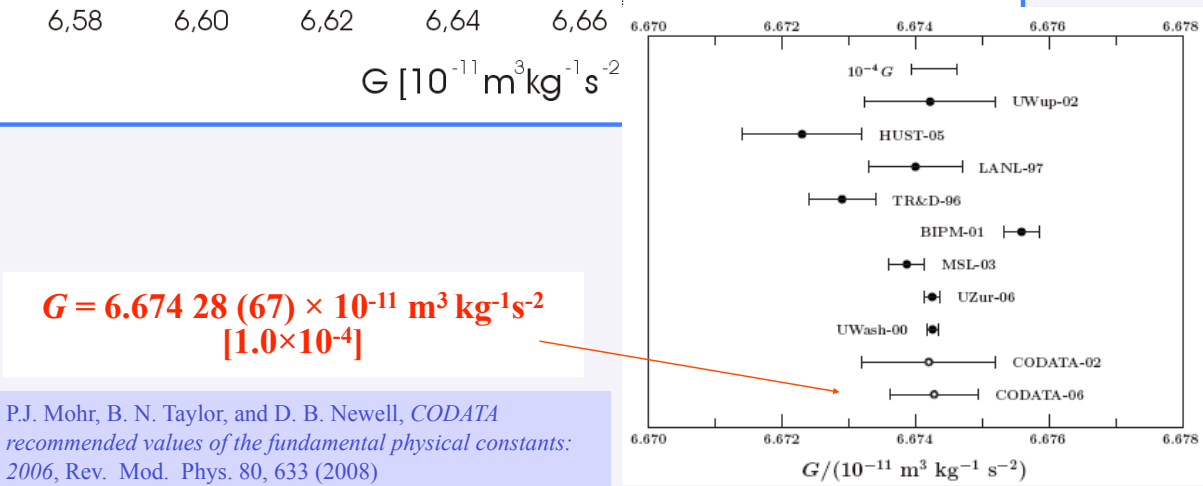
Measurements of the Newtonian gravitational constant G



Cavendish
1798



Quinn
2001

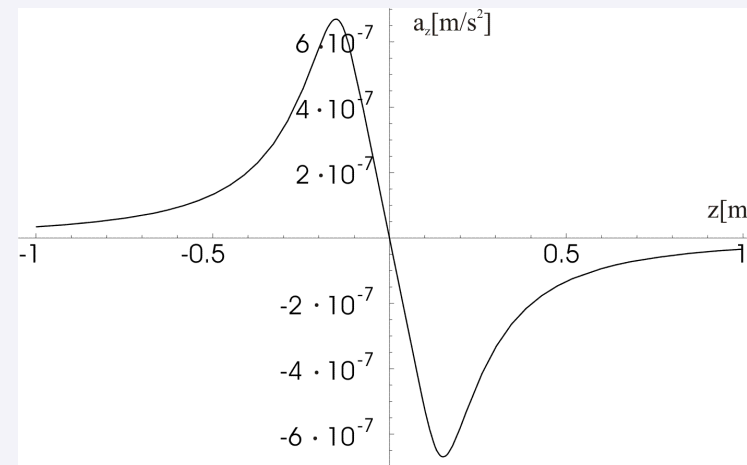
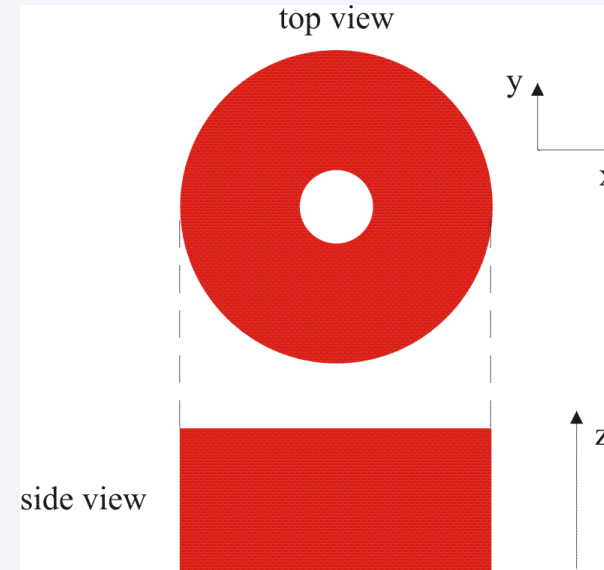
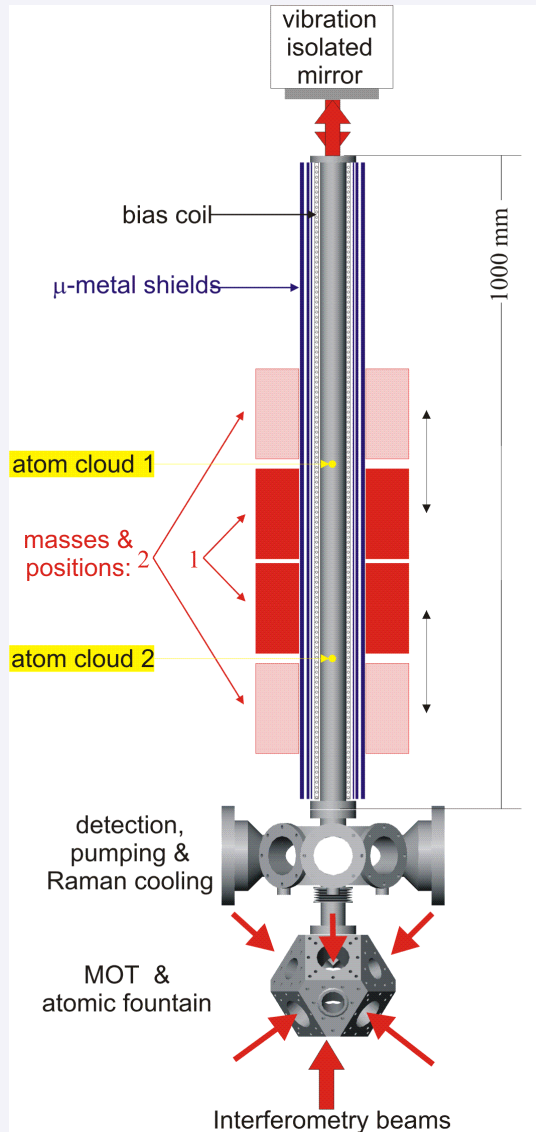


P.J. Mohr, B. N. Taylor, and D. B. Newell, *CODATA recommended values of the fundamental physical constants: 2006*, Rev. Mod. Phys. 80, 633 (2008)

Why atoms?

- Extremely small size
- Well known and reproducible properties
- Quantum systems
- Precision gravity measurement by atom interferometry
- Potential immunity from stray fields effects
- Different states, isotopes,...

MAGIA: atom gravimeter + source mass



500 kg tungsten mass

Sensitivity 10^{-9} g/shot

Peak mass acceleration $a_G \approx 10^{-7}$ g

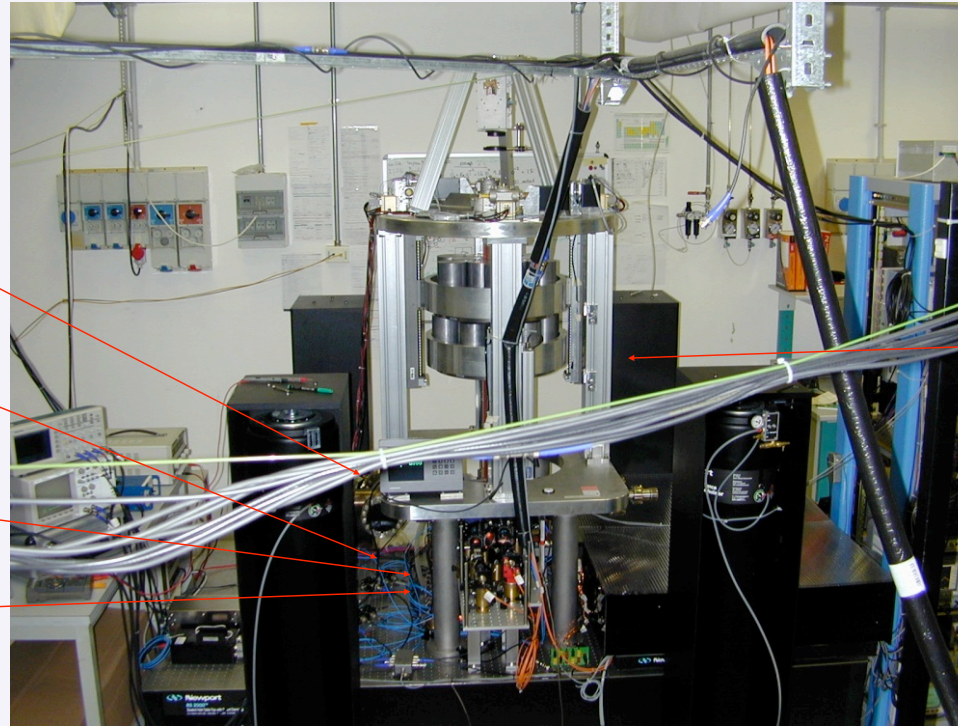
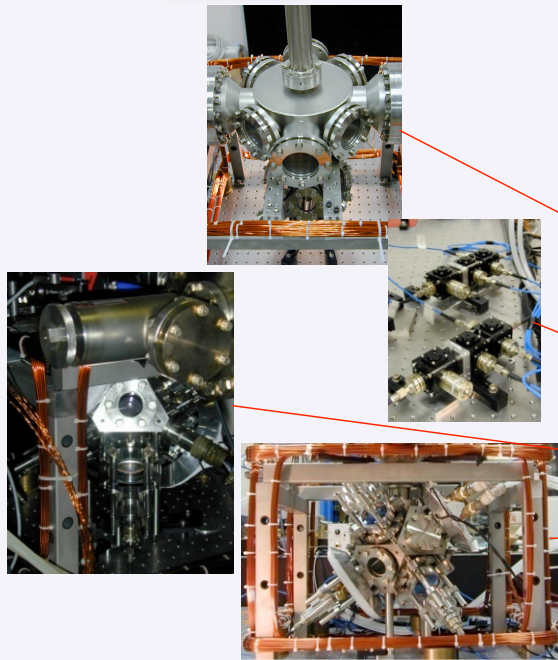
one shot $\Rightarrow \Delta G/G \approx 10^{-2}$

10000 shots $\Rightarrow \Delta G/G \approx 10^{-4}$



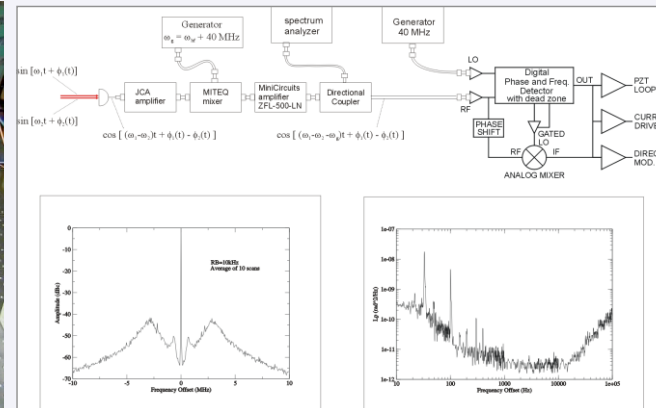
Atom gravity-gradiometer apparatus

Source masses and support



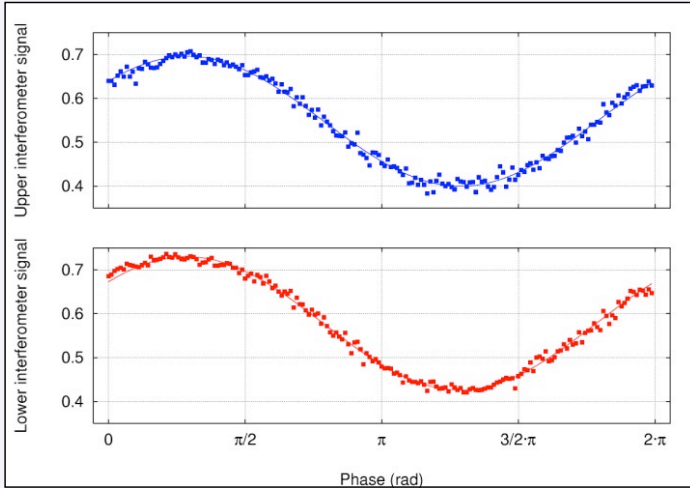
G. Lamporesi, A. Bertoldi, A. Cecchetti, B. Dulach, M. Fattori, A. Malengo, S. Pettoruso, M. Prevedelli, G.M. Tino, *Source Masses and Positioning System for an Accurate Measurement of G*, Rev. Scient. Instr. 78, 075109 (2007)

Laser and optical system



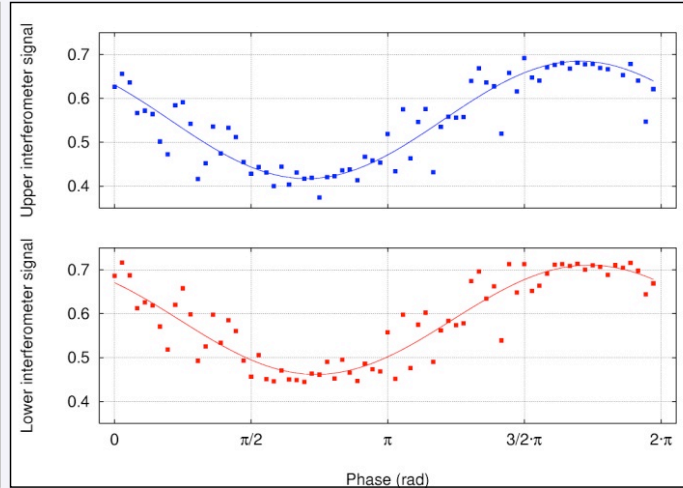
L. Cacciapuoti, M. de Angelis, M. Fattori, G. Lamporesi, T. Petelski, M. Prevedelli, J. Stuhler, G.M. Tino, *Analog+digital phase and frequency detector for phase locking of diode lasers*, Rev. Scient. Instr. 76, 053111 (2005)

Gradiometer



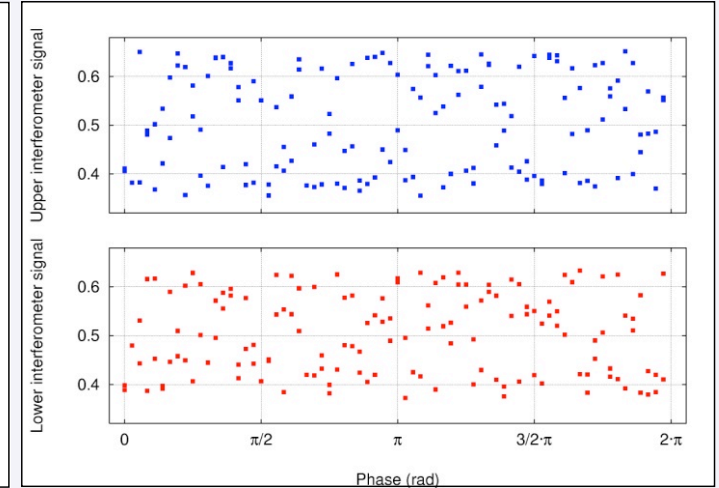
T=5 ms

$$\begin{aligned} \varphi(g) &= 4.0 \cdot 10^3 \text{ rad} \\ \varphi(\nabla g) &= 0.4 \text{ mrad} \\ \text{res} &= 220 \text{ mrad}/\sqrt{\text{Hz}} \\ &= 5.5 \cdot 10^{-5} \text{ g}/\sqrt{\text{Hz}} \\ &= 2.3 \cdot 10^{-5} \text{ g/shot} \end{aligned}$$



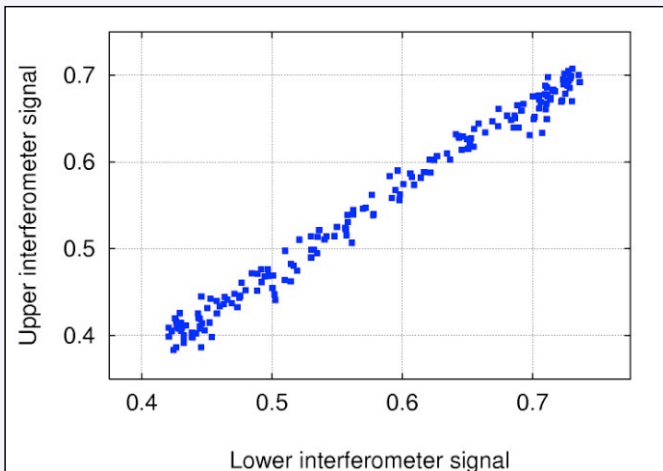
T=50 ms

$$\begin{aligned} \varphi(g) &= 4.0 \cdot 10^5 \text{ rad} \\ \varphi(\nabla g) &= 40 \text{ mrad} \\ \text{res} &= 1.0 \text{ rad}/\sqrt{\text{Hz}} \\ &= 2.5 \cdot 10^{-6} \text{ g}/\sqrt{\text{Hz}} \\ &= 1.0 \cdot 10^{-6} \text{ g/shot} \end{aligned}$$



T=150 ms

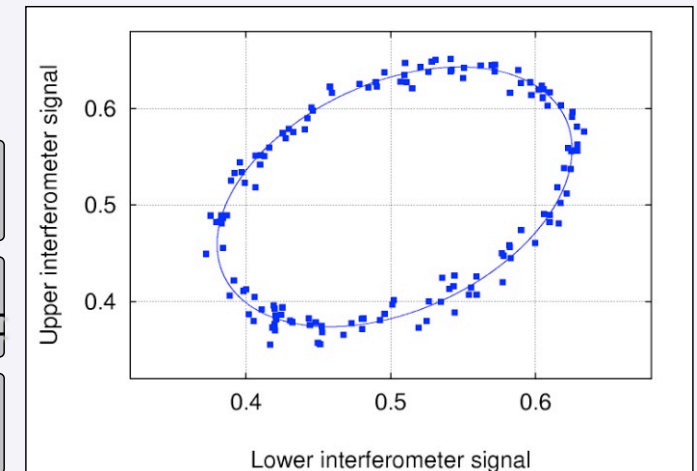
$$\begin{aligned} \varphi(g) &= 3.6 \cdot 10^6 \text{ rad} \\ \varphi(\nabla g) &= 380 \text{ mrad} \\ \text{res} &= 290 \text{ mrad}/\sqrt{\text{Hz}} \\ &= 7.6 \cdot 10^{-8} \text{ g}/\sqrt{\text{Hz}} \\ &= 3.2 \cdot 10^{-8} \text{ g/shot} \end{aligned}$$



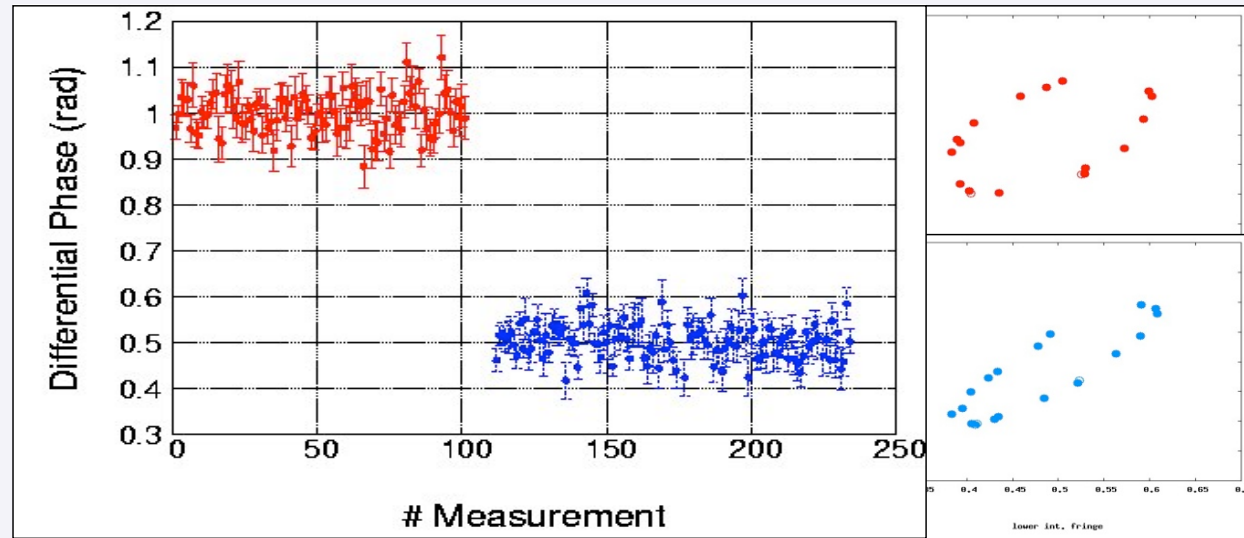
$$\Delta\varphi_{\text{grad}} = k_R \Delta g T^2$$

$$\Delta\varphi_{\text{rot}} = -2\Omega \Delta v_{\text{EW}} k_R T^2 \cos\theta_{\text{lat}}$$

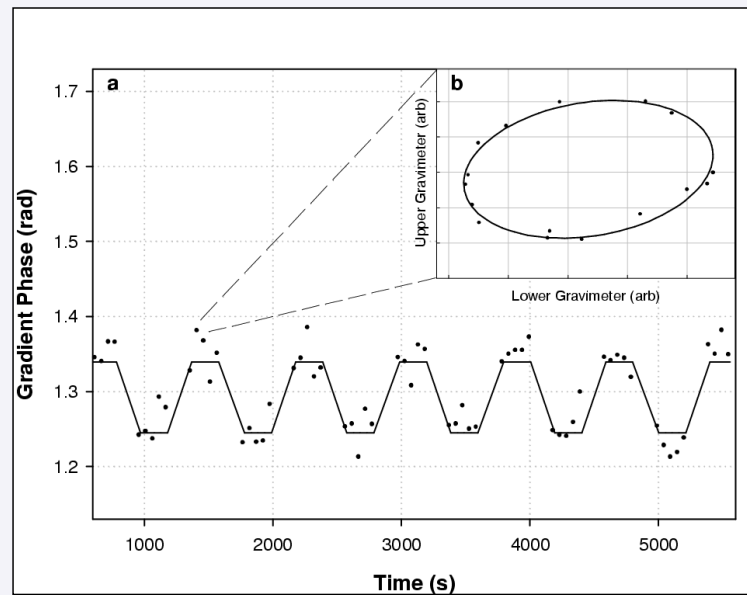
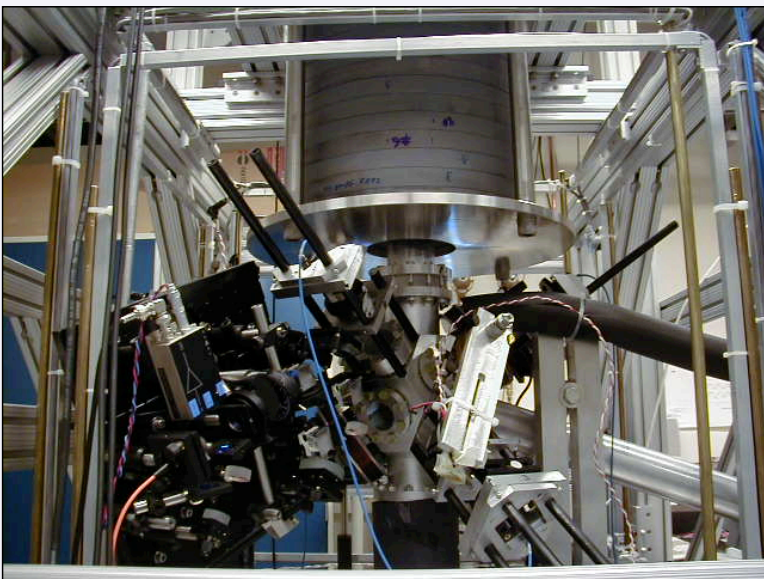
$$\Delta\varphi_B = 2\pi a_{\text{II}} B^2 \Delta t$$



Ellipse fitting method: G.T. Foster et al., *Opt. Lett.* 27, 951 (2002)



A. Bertoldi G.Lamporesi , L. Cacciapuoti, M. deAngelis, M.Fattori, T.Petelski, A. Peters, M. Prevedelli, J. Stuhler, G.M. Tino, *Atom interferometry gravity-gradiometer for the determination of the Newtonian gravitational constant G* , Eur. Phys. J. D 40, 271 (2006)



J. B. Fixler, G. T. Foster, J. M. McGuirk and M. A. Kasevich, *Atom Interferometer Measurement of the Newtonian Constant of Gravity*, Science 315, 74 (2007)

Source masses and support

INERMET 180K (95% W, 3.5% Ni, 1.5% Cu)

Hot isostatic pressing (1200 °C, 1500 atm)

Density= 18 g cm⁻³

Resistivity= 12 x 10⁻⁸ Ωm

Thermal expansion = 5 x 10⁻⁶ K⁻¹

Surface roughness = 3 μm

24 cylinders

External radius = 5 cm

Height = 15 cm

Cylinder mass = 20 kg

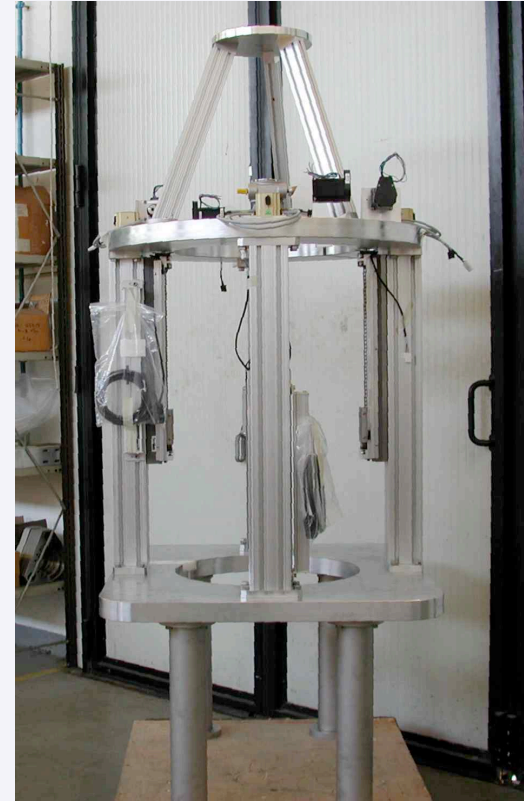
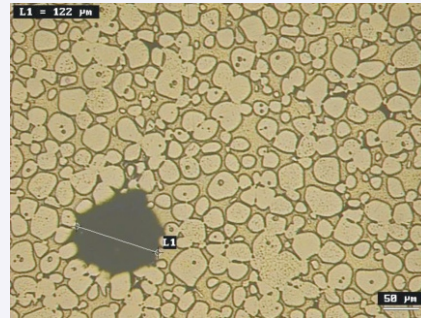
Total mass ~ 500 kg



Hot Isostatic Pressing at 1200 C°
and 1500 atm

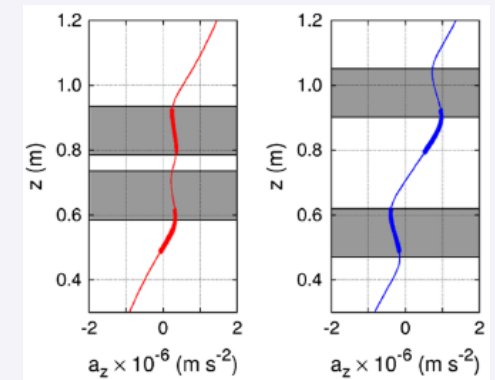
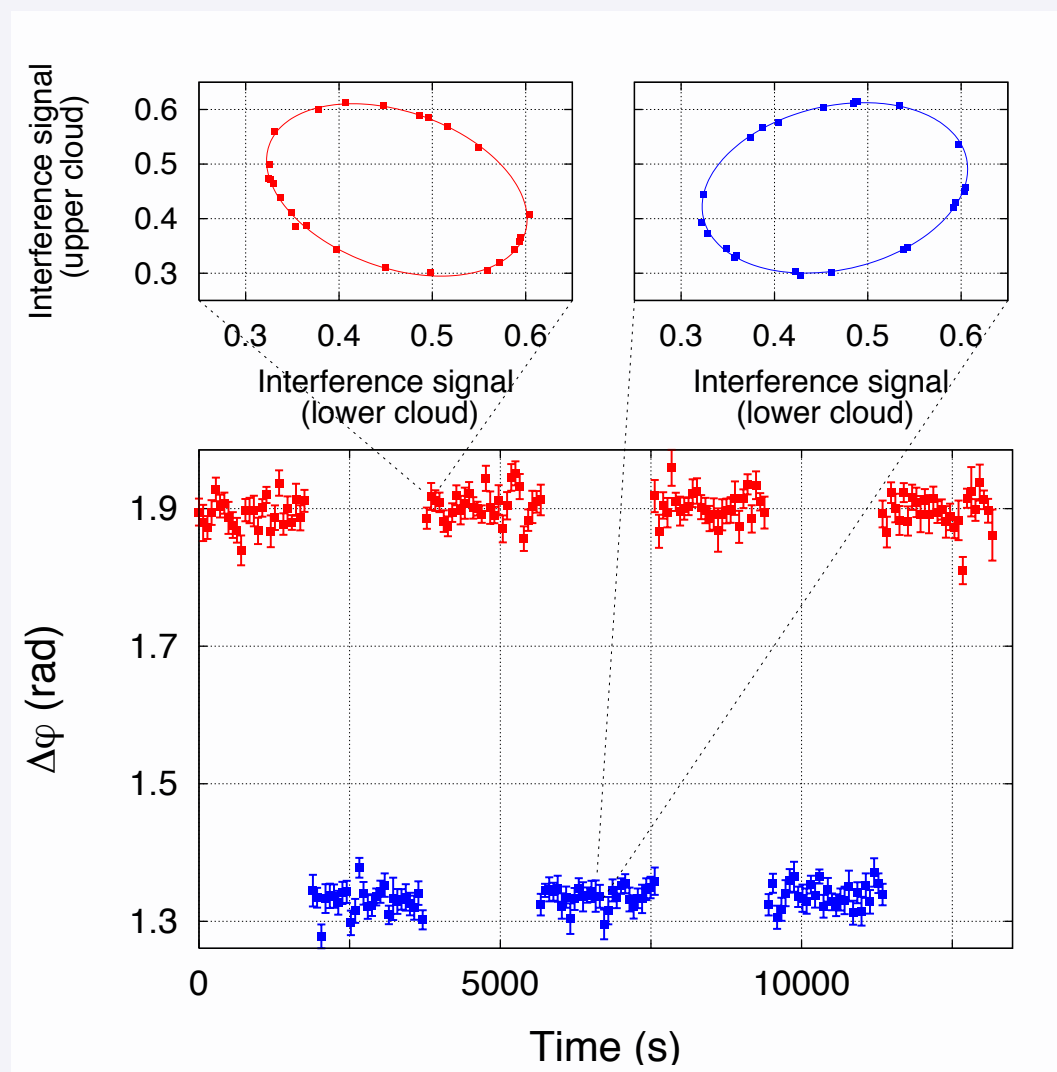
Ultrasonic and destructive test of
homogeneity of probe cylinders
to 10⁻⁴

Oscillation of cylinders on air
cushion reveal radial
inhomogeneities



In collaboration with IMG C, Torino

In collaboration with LNF, Frascati



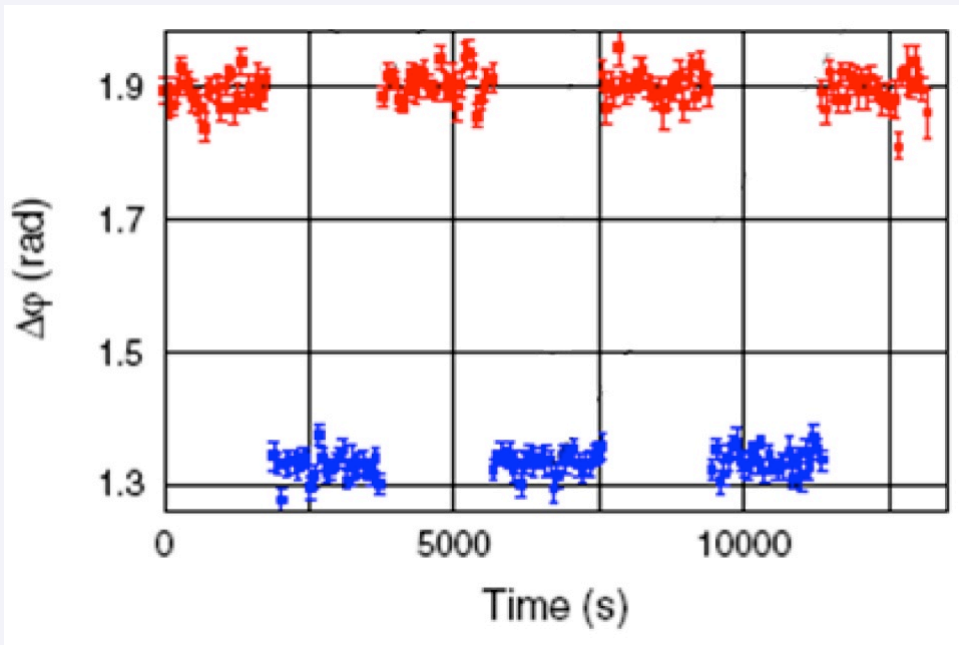
Results from MAGIA
 $G = 6.667 (11) (3) \text{ m}^3 \text{ kg}^{-1} \text{ s}^{-2}$

G. Lamporesi, A. Bertoldi, L. Cacciapuoti, M. Prevedelli, G. M. Tino
Determination of the Newtonian Gravitational Constant Using Atom Interferometry
Phys. Rev. Lett. 100, 050801 (2008)

MAGIA



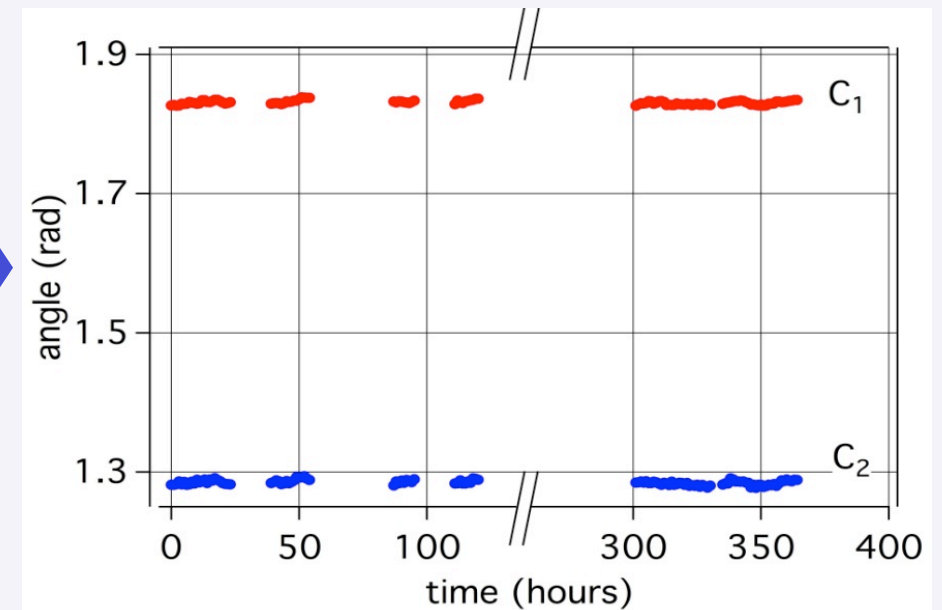
2008



Statistical uncertainty: 1.6×10^{-3}

G. Lamporesi, A. Bertoldi, L. Cacciapuoti, M. Prevedelli,
G. M. Tino, *Phys. Rev. Lett.* **100**, 050801 (2008)

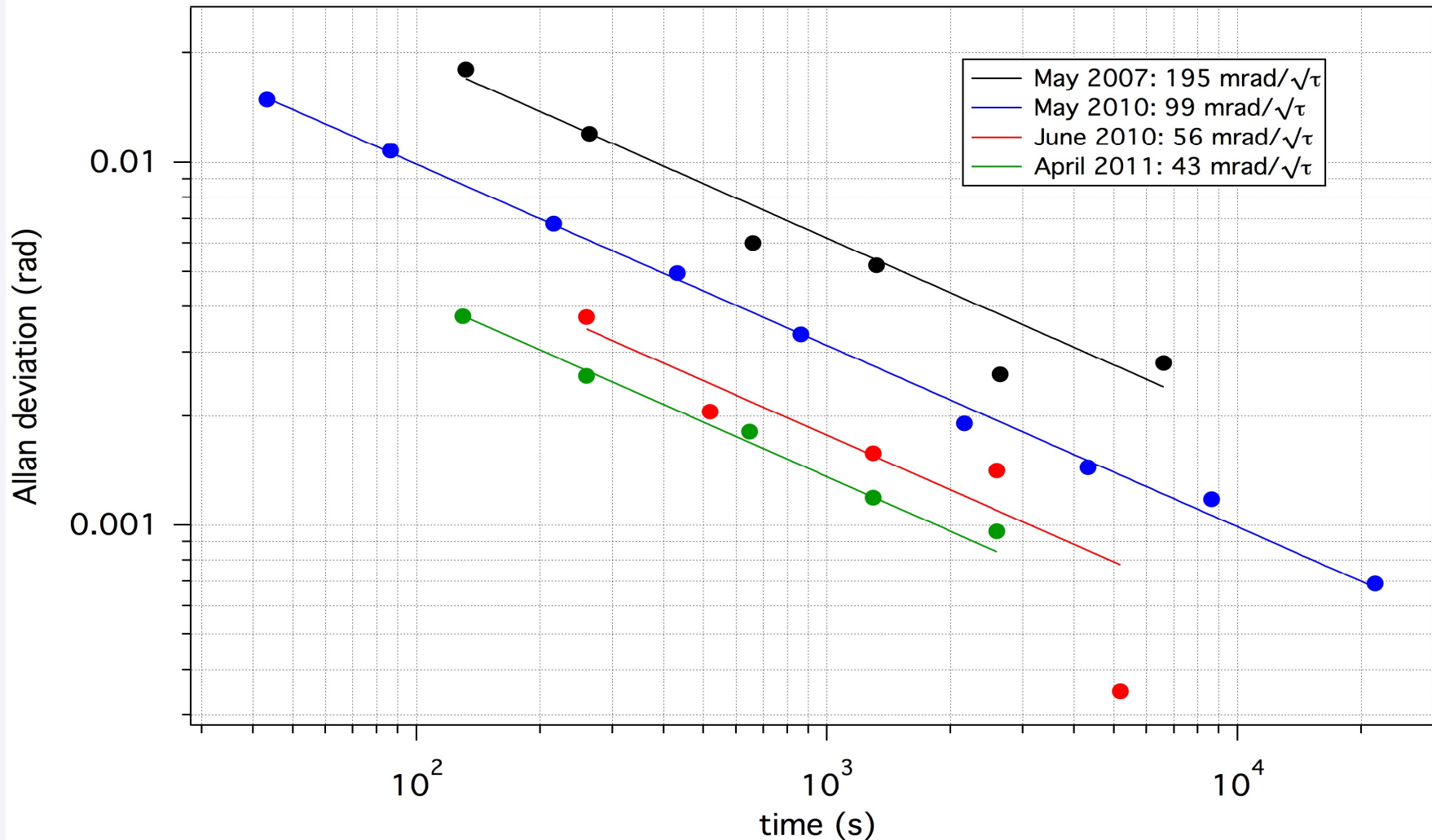
2010



Statistical uncertainty: 4×10^{-4}

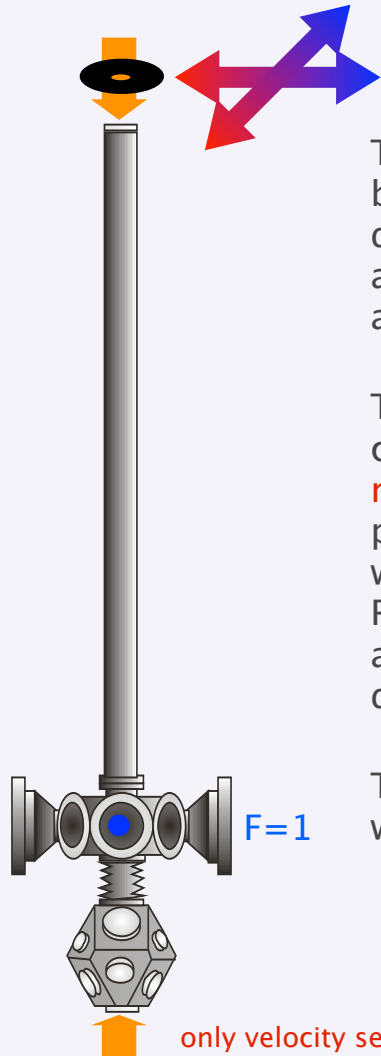
F. Sorrentino, Y.H. Lien, G. Rosi, L. Cacciapuoti,
M. Prevedelli, G.M. Tino, *New J. Phys.* **12**, 095009 (2010)

Upgrade of detection system



larger number of atoms and higher repetition rate (2D-MOT);
 more powerful Raman laser sources;
 minimized the stray light at detection photodiodes;
 improved the contrast with triple-pulse velocity selection;
 improved electronics for photodiodes readout: detection close to QPN

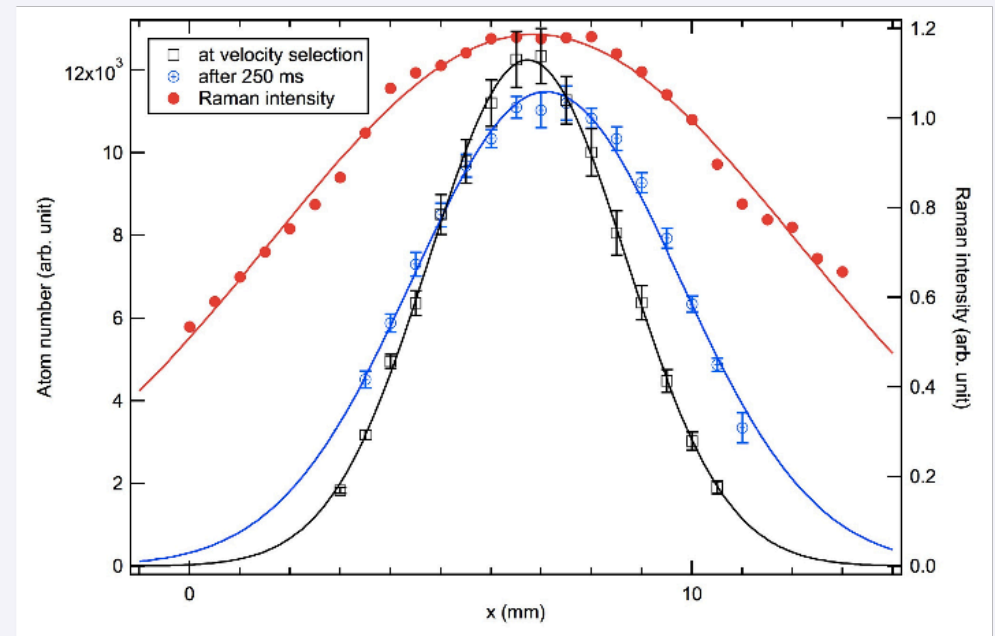
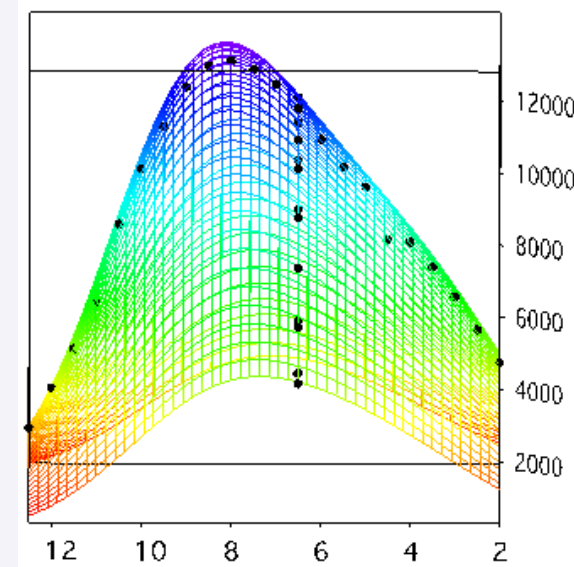
Atomic Cloud Trajectory



The atomic distribution is measured by scanning a horizontally movable diaphragm on the Raman beam path and detecting the $F=1$ population after velocity selection.

The **horizontal position** of atomic cloud can be determined with **sub mm precision** by fitting 2D population signal with a function which is a convolution of a gaussian Raman intensity profile and an asymmetric 2D gaussian for atomic distribution.

The **vertical position** is determined with **sub mm precision** by TOF signal.





Systematics

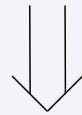
SOURCE	Uncertainty	$\Delta G/G (10^{-4})$	Status
Cylinders radial positioning	10 μm	0.5	Done
Cylinder shape	10 μm	$\ll 1$	Done
Cylinder mass	10 mg	$\ll 1$	Done
Density radial homogeneity	2×10^{-3}	0.01	Done
Density vertical homogeneity	0.5×10^{-3}	0.25	Done
Support platform mass	60 g	0.8	To be improved
Cloud-Masses vertical distance	100 μm	0.02	Done
Cloud-Masses horiz. distance	100 μm	N/A	Partially done
Atomic horiz. distribution	100 μm	N/A	Partially done
Launch direction C/F	N/A	N/A	Not detectable
Raman mirror tilt C/F	0.1 μrad	0.3	Done

- MonteCarlo simulation of the experiment to implement correctly the clouds dynamic
- Launch direction changes induced by source mass below 0.1 mrad
 - Too small to be detected with cloud scanning method
 - Possible effect on $\Delta\Phi$ by Coriolis force ($\sim 3\text{-}4$ mrad)
- Possible solutions:
 - Improve sensitivity on trasversal position measurements
 - Compensate Coriolis effect (rotating Raman mirror)



MAGIA – Relevant numbers

- time separation between pulses $T=150$ ms
- 10^6 atoms
- shot noise limited detection
- launch accuracy: 1 mm e $\Delta v \sim 5$ mm/s
- knowledge of the masses dimensions and relative positions: 10 μm
- 10000 measurements



$$\Delta G/G \approx 10^{-4}$$

Experiments on gravity at small spatial scale



Motivation

- **Physics beyond the standard model**

Extra space-time dimensions

Deviations from $1/r^2$ law

Hierarchy problem: why is gravity so weak?

N. Arkani-Hamed, S. Dimopoulos, G. Dvali, Phys. Lett. B 429, 263 (1998)

N. Arkani-Hamed, S. Dimopoulos, G. Dvali, Phys. Rev. D 59, 086004 (1999)

New boson-exchange forces

Radion – low-mass spin-0 fields with gravitational-strength couplings

Moduli – massive scalar particles producing gravitylike forces

Dilaton – Light scalar in string theory, coupling to nucleons

Axion – pseudoscalar particles explaining smallness of CP violation in QCD for strong nuclear force

Multi-particle exchange forces

S. Dimopoulos and G. F. Giudice, Phys. Lett. B 379, 105 (1996)

I. Antoniadis, S. Dimopoulos, and G. Dvali, Nuc. Phys. B 516, 70 (1998)

T.R. Taylor, G. Veneziano, Phys. Lett. B 213, 450 (1988)

D. B. Kaplan, M. B. Wise, J. High Energy Phys. 8, 37 (2000)

Moody and Wilczek, Phys. Rev. D 30, 130 (1984)

R. Barbieri, A. Romanino, A. Strumia, Phys. Lett. B 387, 310 (1996)

L.J. Rosenberg, K.A. van Bibber, Phys. Rep. 325, 1 (2000)

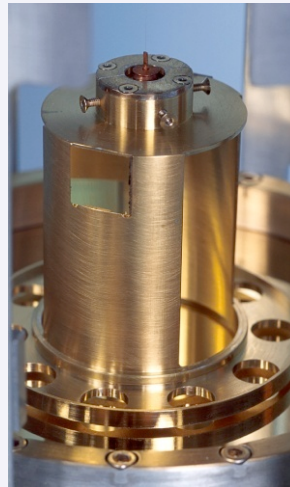
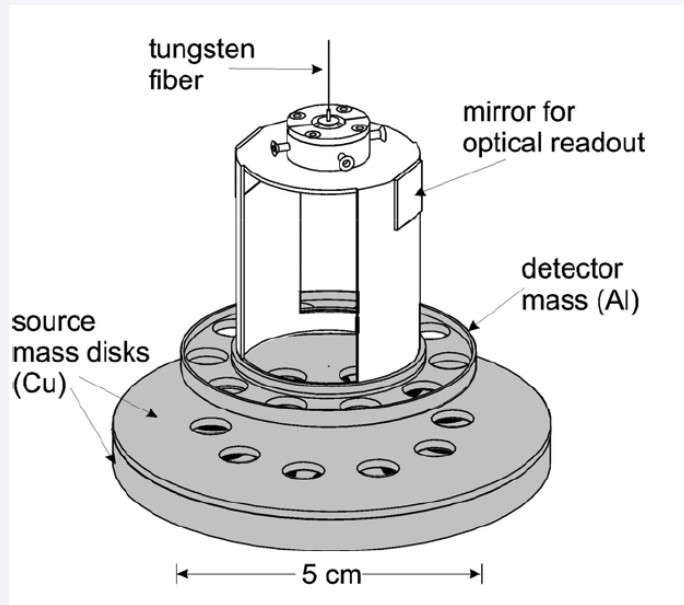
- **Small observed size of Einstein cosmological constant**

S.R. Beane, Gen. Rel. Grav. 29, 945 (1997)

R. Sundrum, Phys. Rev. D 69, 044014 (2004)

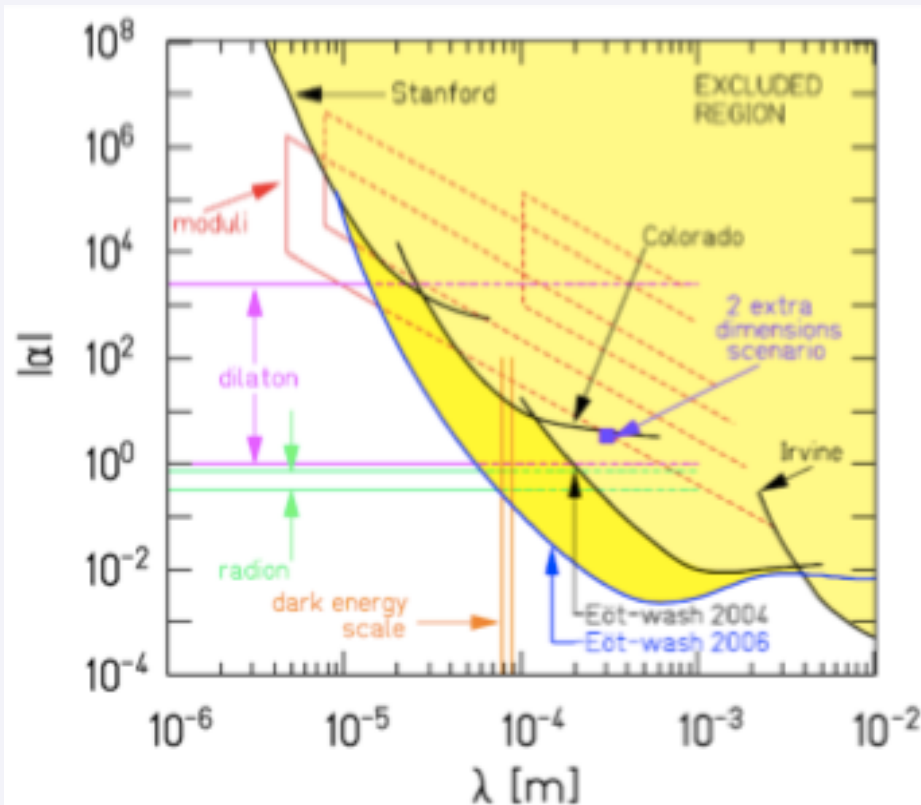
- **Experimental challenge**

Torsion balance - Washington experiment



- **Test bodies: “missing masses” of holes bored into plates**
- **Torsion pendulum**
7075 aluminum, gold coated
disk height = 2 mm
10 cylindrical holes evenly spaced about the azimuth
- **Attractor**
high-purity copper disk
top surface coated with gold
10 cylindrical holes evenly spaced about the azimuth
uniformly rotating
- **Electrostatic shield**
tightly stretched 20- μ m-thick BeCu foil

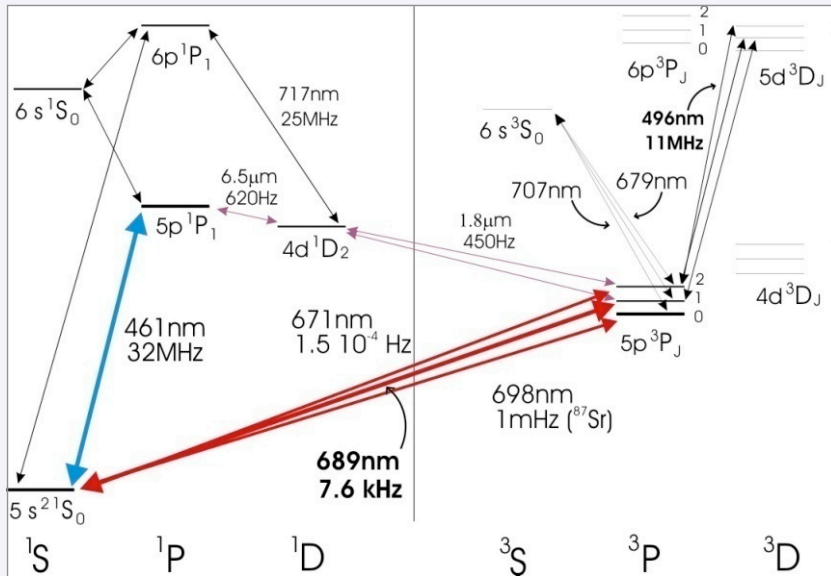
- **Distance from top of attractor to bottom of pendulum**
from 9.53 mm to 55 μ m



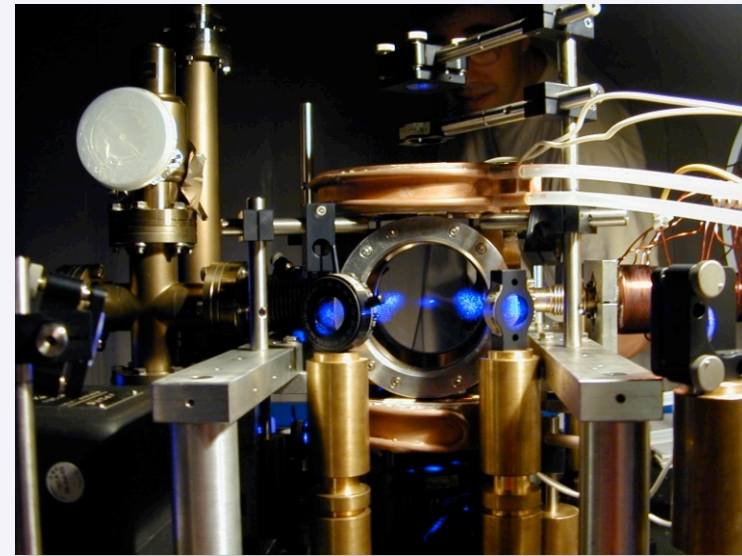
C. D. Hoyle, D. J. Kapner, B. R. Heckel, E. G. Adelberger, J. H. Gundlach, U. Schmidt, H. E. Swanson, *Submillimeter tests of the gravitational inverse-square law*, PRD 70, 042004 (2004)

D. J. Kapner, T. S. Cook, E. G. Adelberger, J.H. Gundlach, B. R. Heckel, C. D. Hoyle, H. E. Swanson, *Tests of the Gravitational Inverse-Square Law below the Dark-Energy Length Scale*, PRL 98, 021101 (2007)

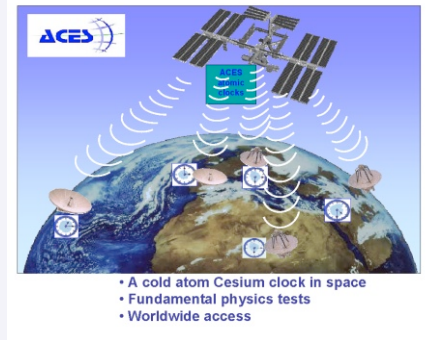
Ultracold Sr – The experiment in Firenze



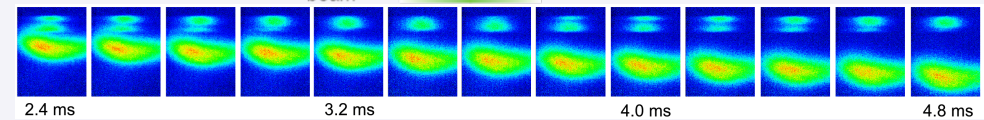
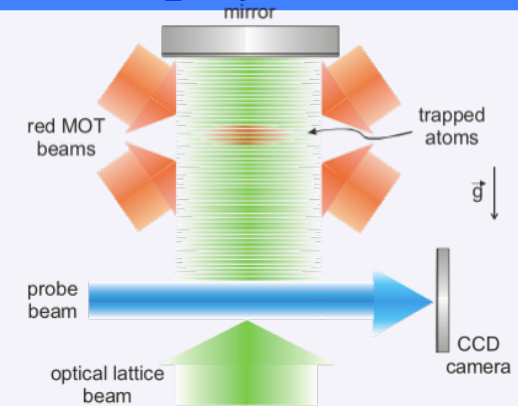
- Optical clocks using visible intercombination lines



- New atomic sensors for fundamental physics tests

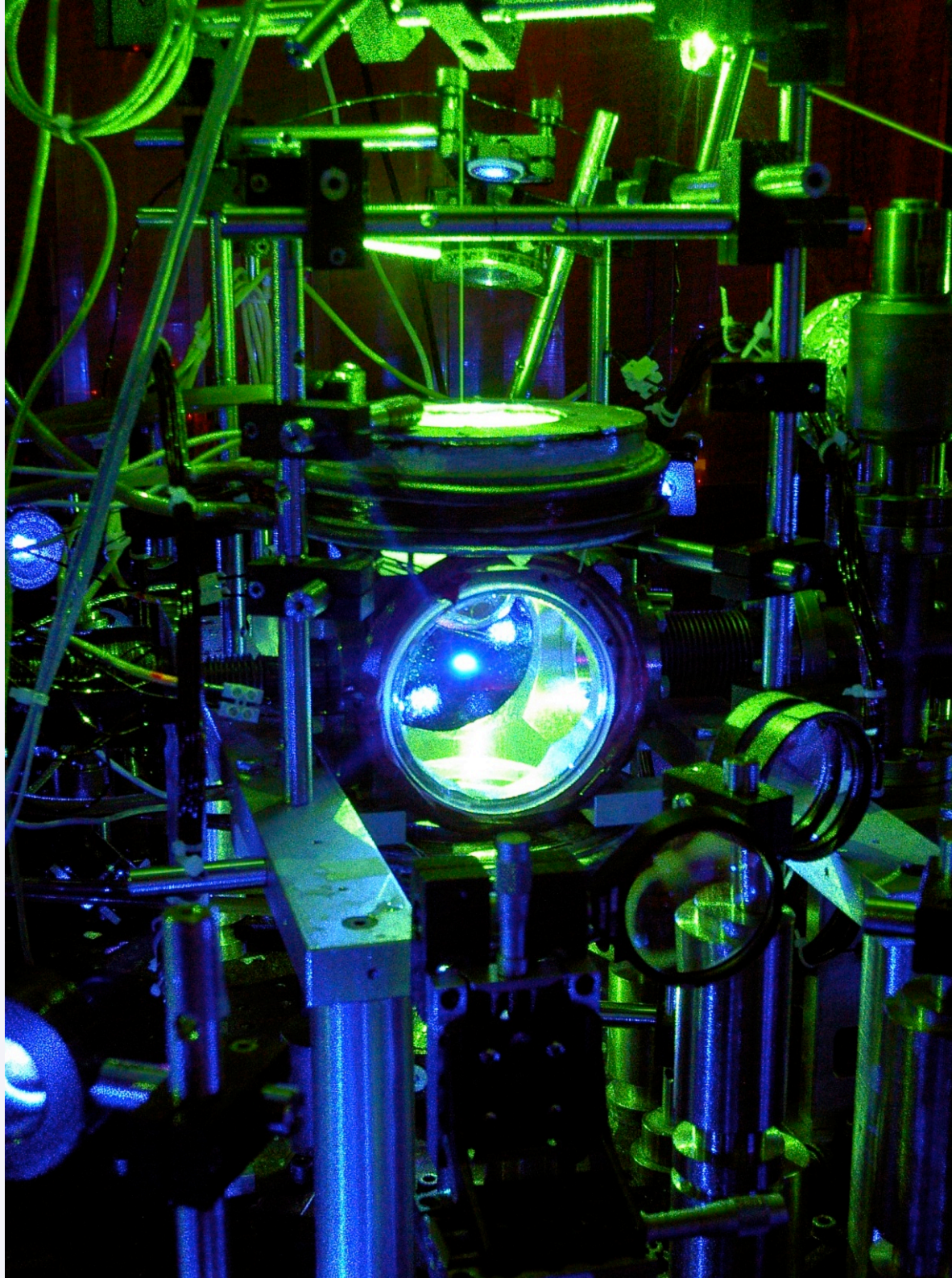


- A cold atom Cesium clock in space
- Fundamental physics tests
- Worldwide access

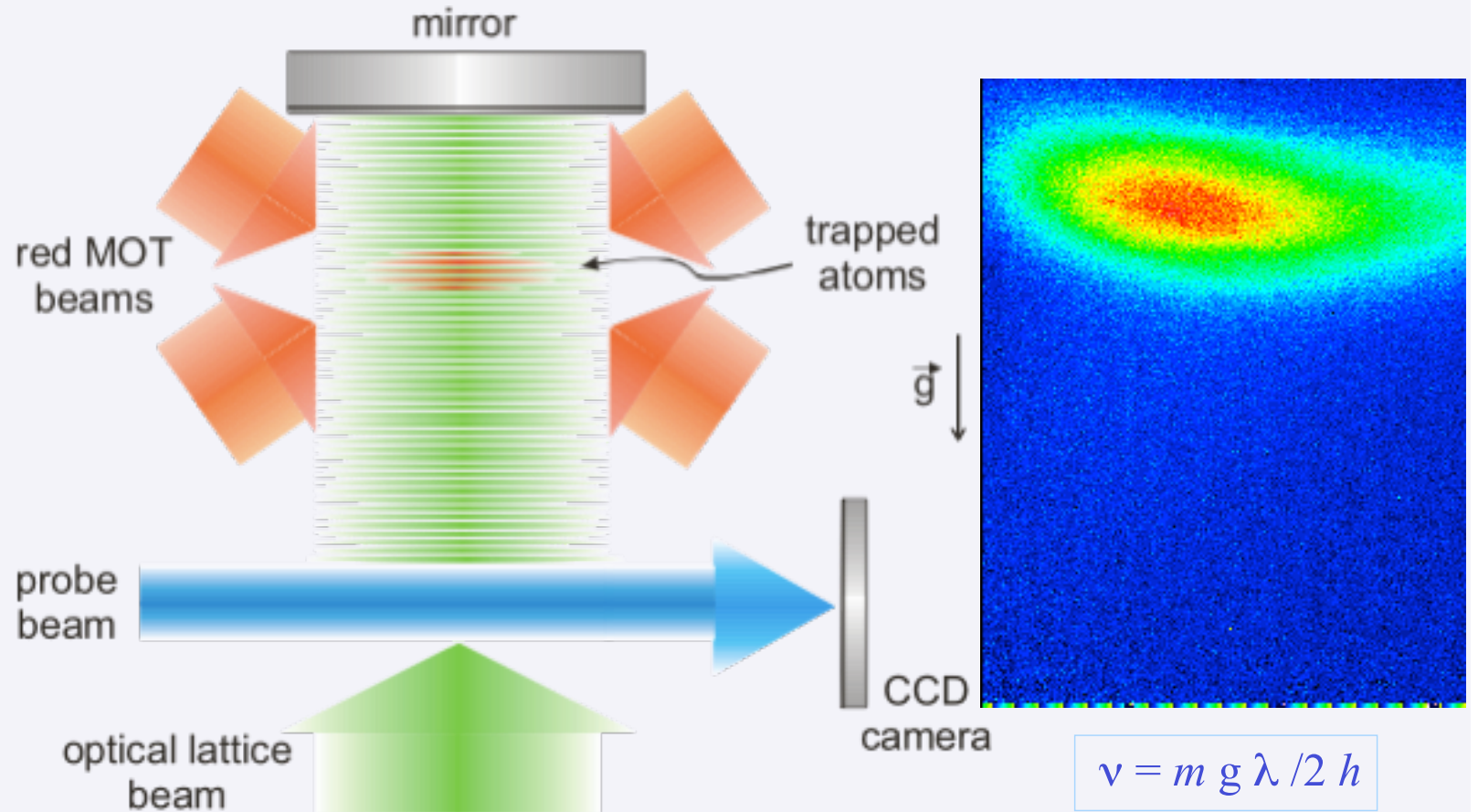


G. Ferrari, N. Poli, F. Sorrentino, and G. M. Tino, *Long-lived Bloch oscillations with bosonic Sr atoms and application to gravity measurement at micrometer scale*, Phys. Rev. Lett. 97, 060402 (2006)

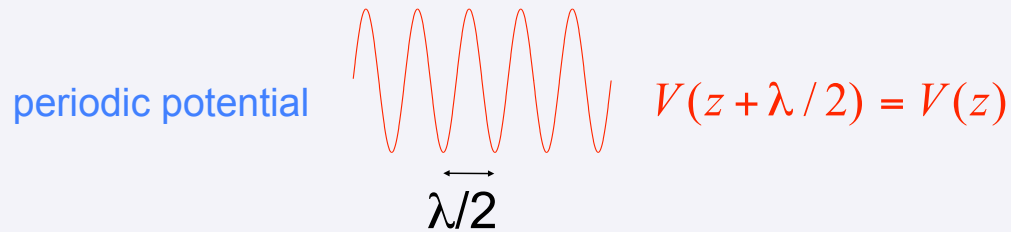
G. Ferrari, P. Cancio, R. Drullinger, G. Giusfredi, N. Poli, M. Prevedelli, C. Toninelli, G.M. Tino, *Precision Frequency Measurement of Visible Intercombination Lines of Strontium*, Phys. Rev. Lett. 91, 243002 (2003)



Precision gravity measurement at μm scale with Bloch oscillations of Sr atoms in an optical lattice



Particle in a periodic potential: Bloch oscillations

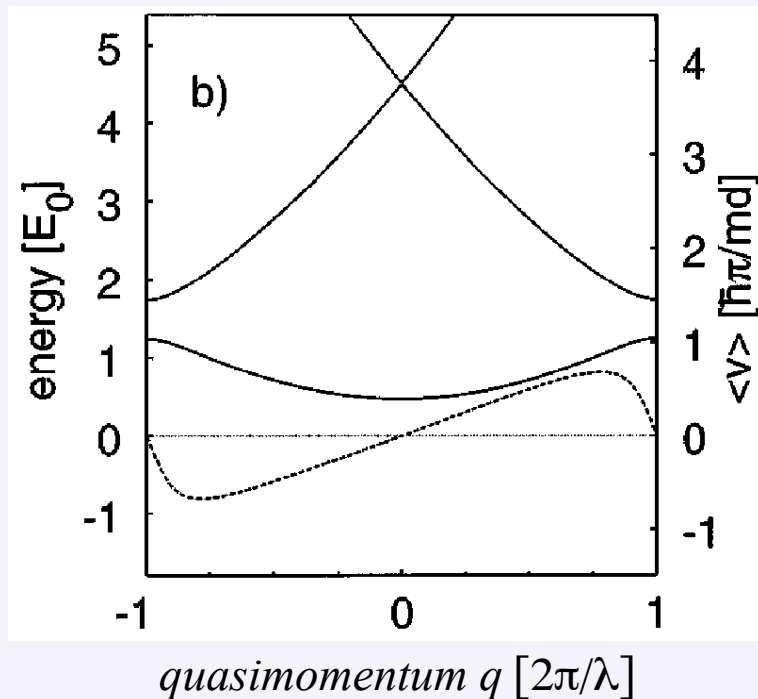


$$\Psi(z) = e^{i \frac{q}{\hbar} z} u(z)$$

$$u(z + \lambda/2) = u(z)$$

Bloch's theorem

$$\Psi(z + \lambda/2) = e^{i \frac{q}{\hbar} \frac{\lambda}{2}} \Psi(z)$$



$$\langle v \rangle_n(q(t)) = \frac{1}{\hbar} \frac{dE_n(R(q(t)))}{dq}$$

with a constant external force F

$$q(t) = q(0) + Ft/\hbar$$

↓
Bloch oscillations

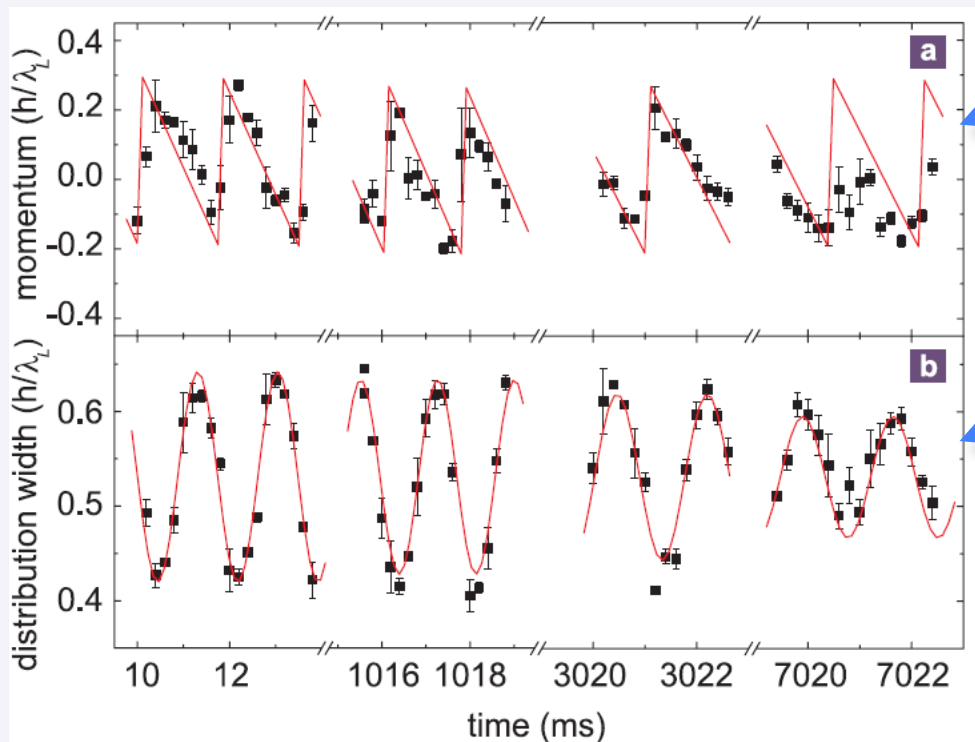
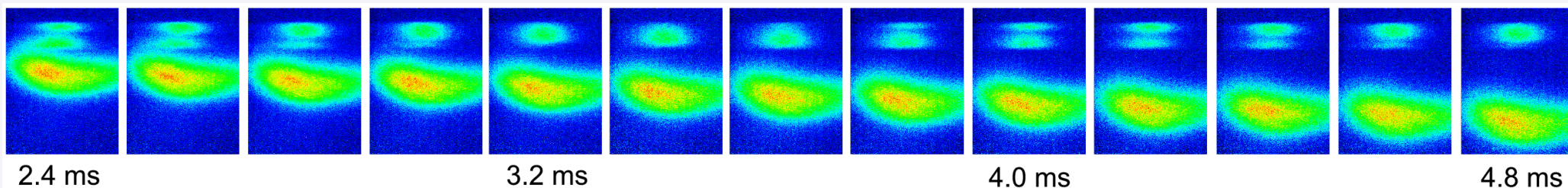
Quantum theory for electrons in crystal lattices: **F. Bloch**, *Z. Phys.* **52**, 555 (1929)

Never observed in natural crystals (evidence in artificial superlattices)

Direct observation with Cs atoms: **M. Ben Dahan, E. Peik, J. Reichel, Y. Castin, C. Salomon**, *PRL* **76**, 4508 (1996)



Persistent Bloch oscillations



average vertical momentum of the lower peak

width of the atomic momentum distribution

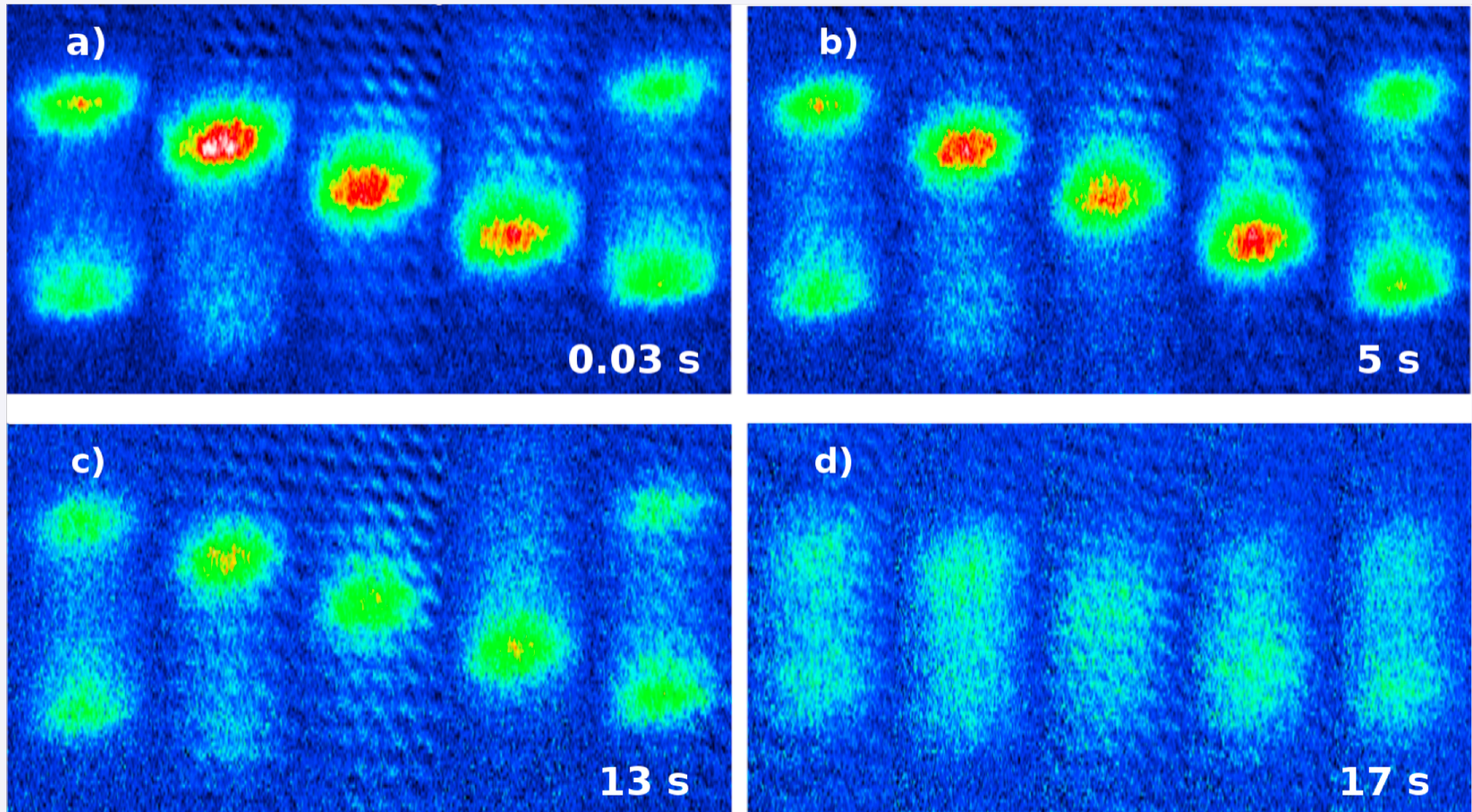
Bloch frequency $\nu_B = 574.568(3)$ Hz

damping time $\tau = 12$ s

8000 photon recoils in 7s

$g_{\text{meas}} = 9.80012(5)$ ms⁻²

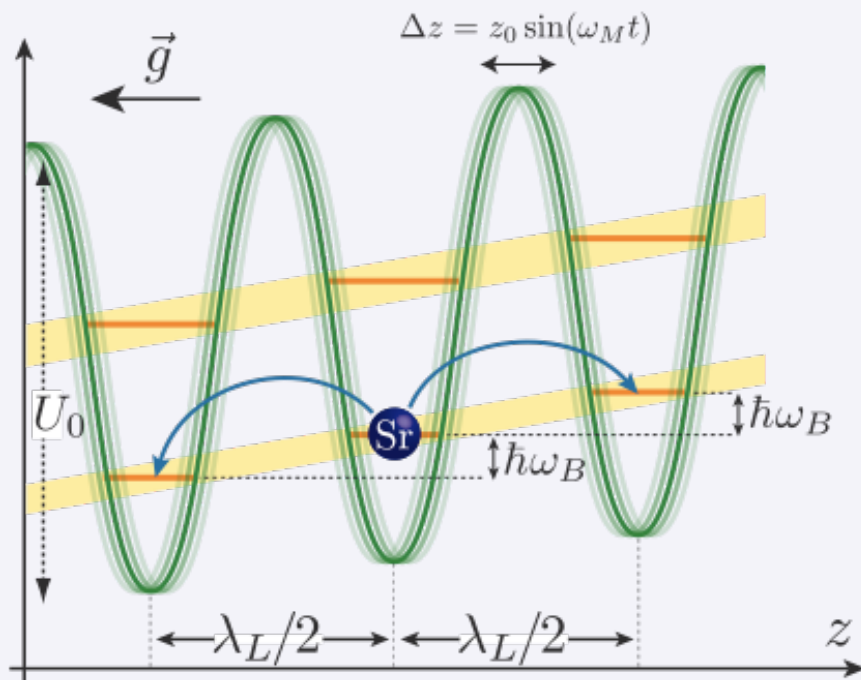
G. Ferrari, N. Poli, F. Sorrentino, G. M. Tino, *Long-Lived Bloch Oscillations with Bosonic Sr Atoms and Application to Gravity Measurement at the Micrometer Scale*, *Phys. Rev. Lett.* **97**, 060402 (2006)



N. Poli, F.Y. Wang, M.G. Tarallo, A. Alberti, M. Prevedelli, G.M. Tino,
Phys. Rev. Lett. 106, 038501 (2011)

Modulation of optical lattices

Phase modulation

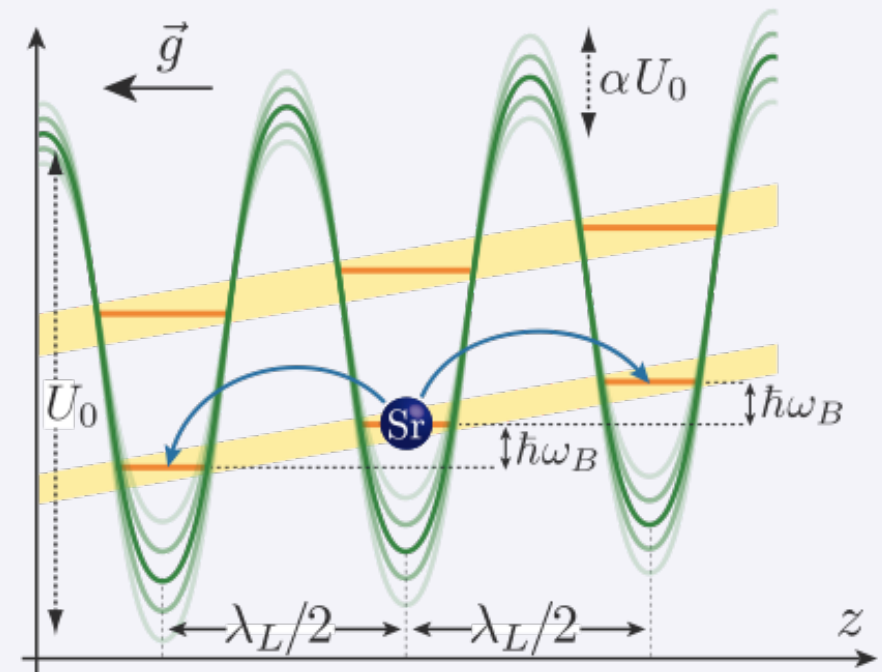


$$\mathcal{H}_0 = \frac{p^2}{2m} - \frac{U_0}{2} \cos \{2k_L [z - z_0 \sin(\omega_M t)]\} + mgz$$

V.V. Ivanov, A. Alberti, M. Schioppo, G. Ferrari, M. Artoni, M. L. Chiofalo, G. M. Tino, *Coherent Delocalization of Atomic Wave Packets in Driven Lattice Potentials*,

Phys. Rev. Lett. **100**, 043602 (2008)

Amplitude modulation

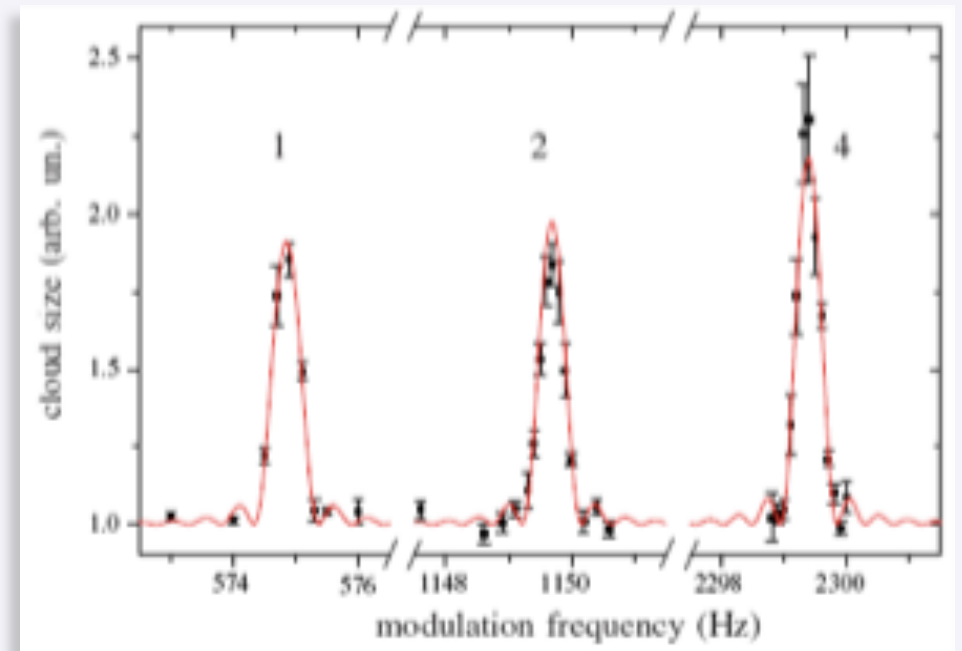
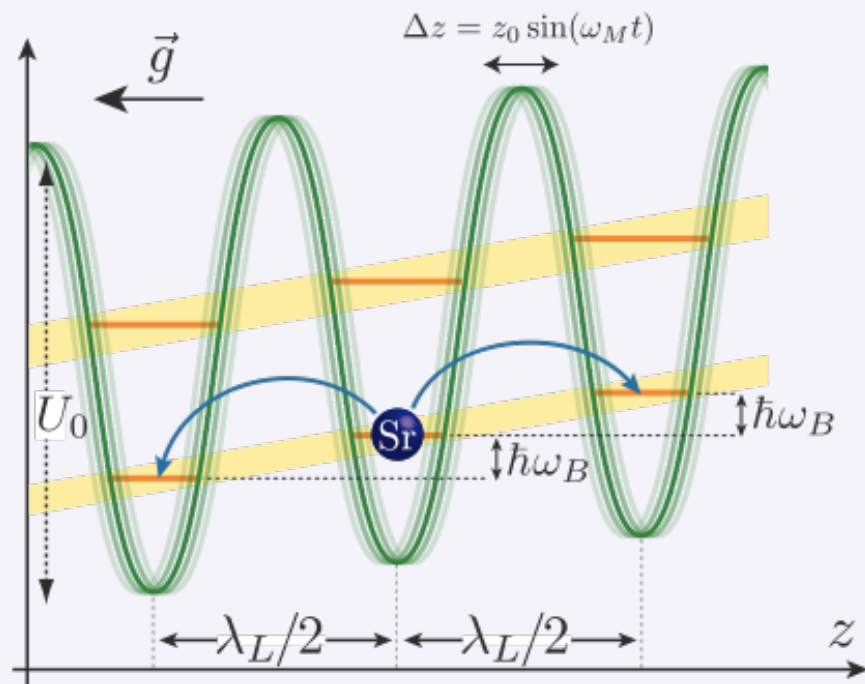


$$\mathcal{H}_0 = \frac{p^2}{2m} - \frac{U_0}{2} \cos(2k_L z) [1 + \alpha \sin(\omega_M t)] + mgz$$

A. Alberti, G. Ferrari, V.V. Ivanov, M. L. Chiofalo, G. M. Tino, *Atomic wave packets in amplitude-modulated vertical optical lattices*

New Journal of Physics **12**, 065037 (2010)

Coherent Delocalization of Atomic Wave Packets in Driven Lattice Potentials



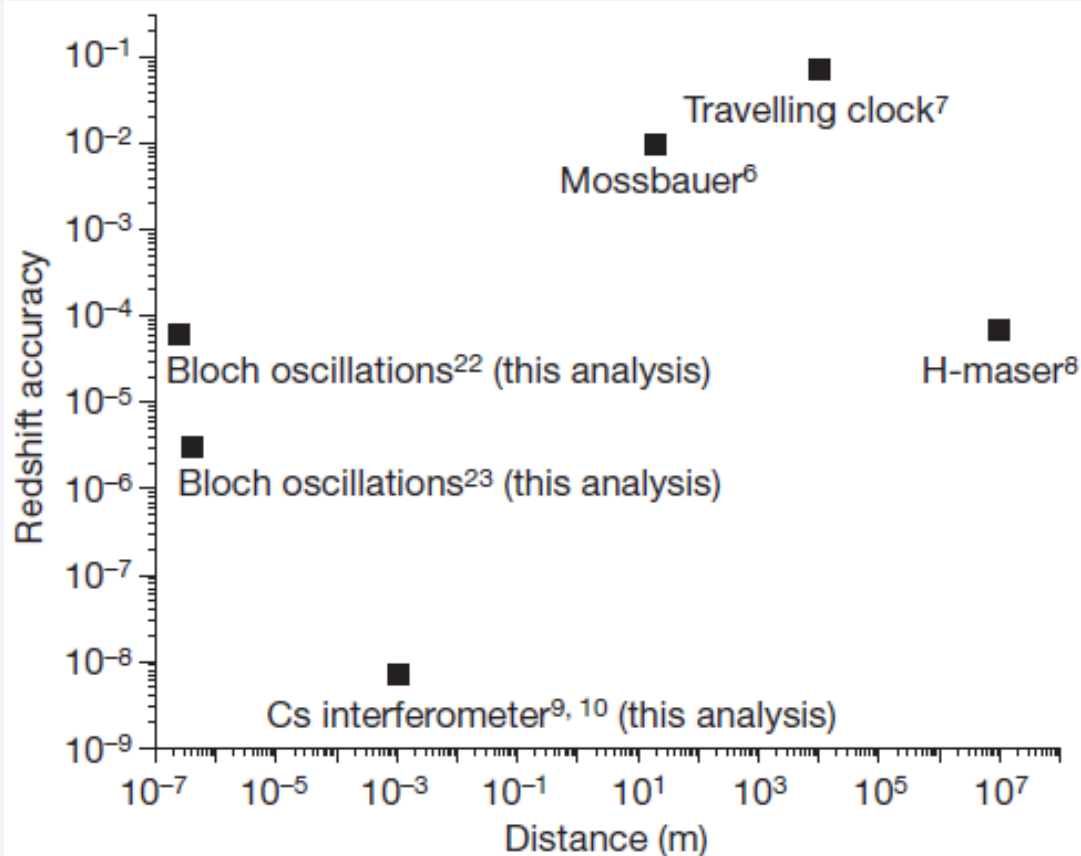
$$\nu_B = (574.8459 \pm 0.0015) \text{ Hz},$$
$$g = (9.805301 \pm 0.000026) \text{ m/s}^2$$

V.V. Ivanov, A. Alberti, M. Schioppo, G. Ferrari, M. Artoni, M. L. Chiofalo, G. M. Tino,
Coherent Delocalization of Atomic Wave Packets in Driven Lattice Potentials,
Phys. Rev. Lett. 100, 043602 (2008)

LETTERS

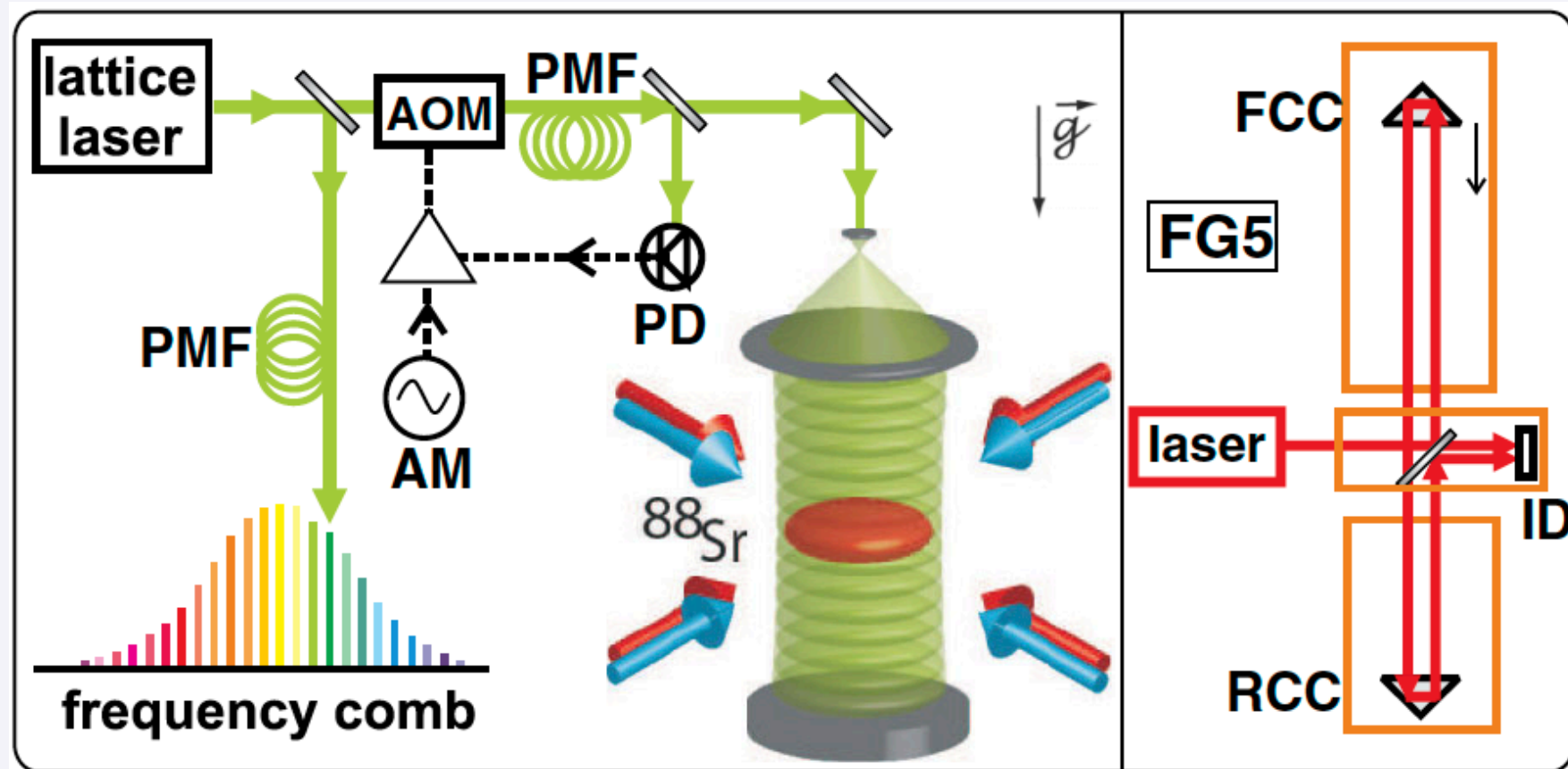
A precision measurement of the gravitational redshift by the interference of matter waves

Holger Müller^{1,2}, Achim Peters³ & Steven Chu^{1,2,4}



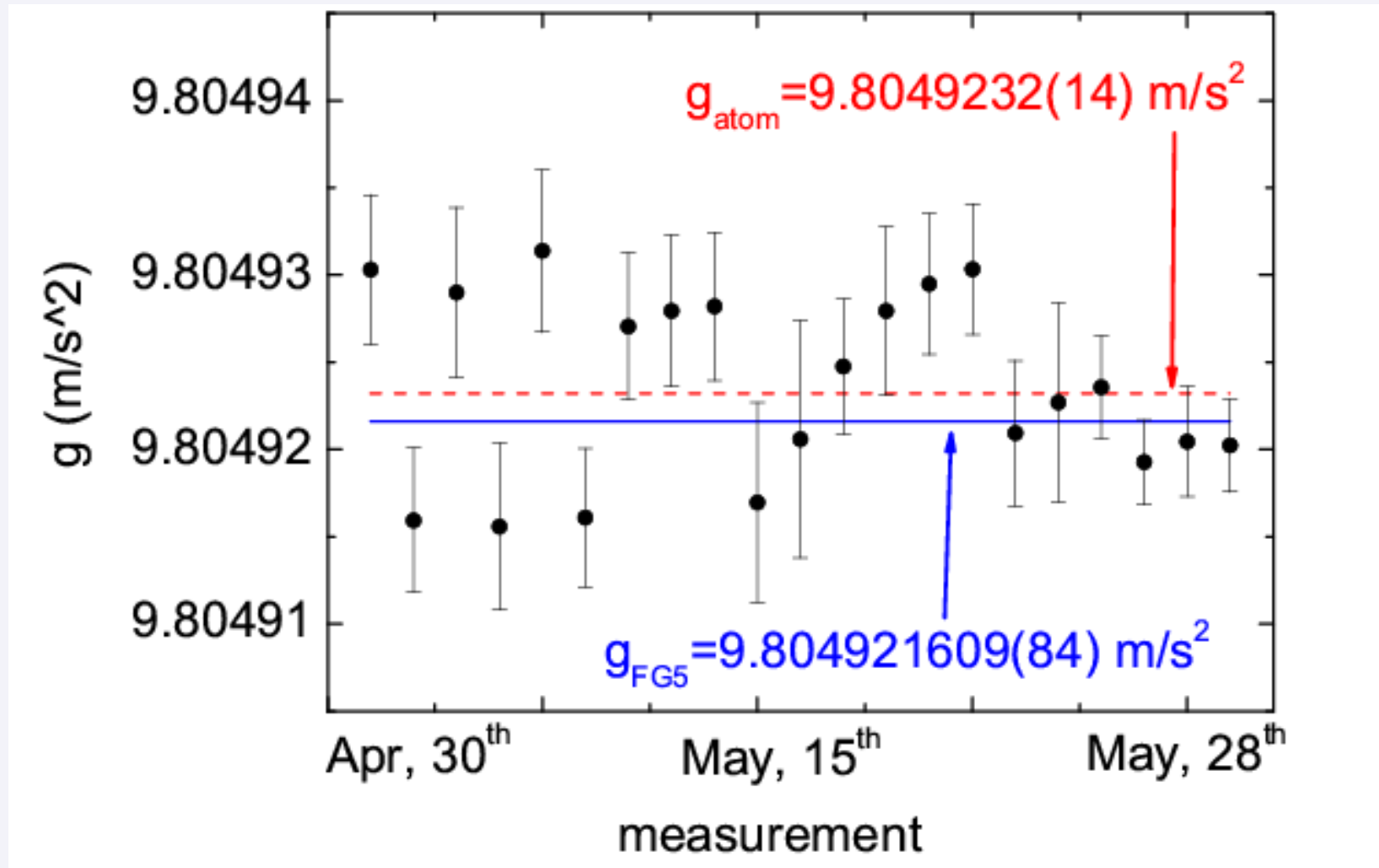
6. Pound, R. V. & Snider, J. L. Effect of gravity on gamma radiation. *Phys. Rev.* **140**, B788–B803 (1965).
7. Hafele, J. C. & Keating, R. E. Around-the-world atomic clocks: observed relativistic time gains. *Science* **177**, 168–170 (1972).
8. Vessot, R. F. C. *et al.* Test of relativistic gravitation with a space-borne hydrogen maser. *Phys. Rev. Lett.* **45**, 2081–2084 (1980).
9. Peters, A., Chung, K. Y. & Chu, S. A measurement of gravitational acceleration by dropping atoms. *Nature* **400**, 849–852 (1999).
10. Peters, A., Chung, K.-Y. & Chu, S. High-precision gravity measurements using atom interferometry. *Metrologia* **38**, 25–61 (2001).
22. Ivanov, V. V. *et al.* Coherent delocalization of atomic wave packets in driven lattice potentials. *Phys. Rev. Lett.* **100**, 043602 (2008).
23. Cladé, P. *et al.* A promising method for the measurement of the local acceleration of gravity using Bloch oscillations of ultracold atoms in a vertical standing wave. *Europhys. Lett.* **71**, 730–736 (2005).

Precision measurement of gravity with cold atoms in an optical lattice and comparison with a classical gravimeter



N. Poli, F.Y. Wang, M.G. Tarallo, A. Alberti, M. Prevedelli, G.M. Tino,
Phys. Rev. Lett. 106, 038501 (2011)

Precision measurement of gravity with cold atoms in an optical lattice and comparison with a classical gravimeter

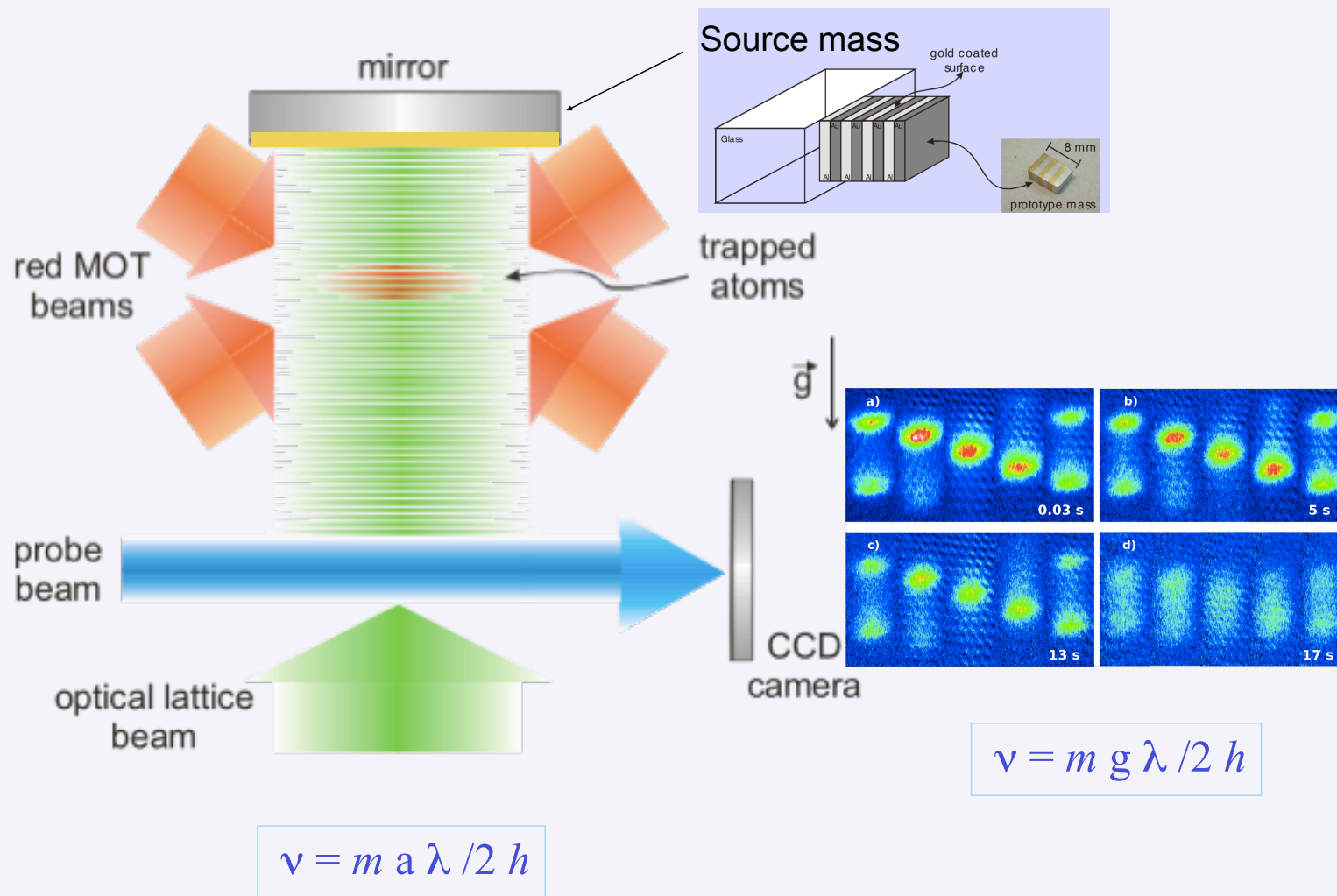


140 ppb relative uncertainty

N. Poli, F.Y. Wang, M.G. Tarallo, A. Alberti, M. Prevedelli, G.M. Tino,
Phys. Rev. Lett. **106**, 038501 (2011)

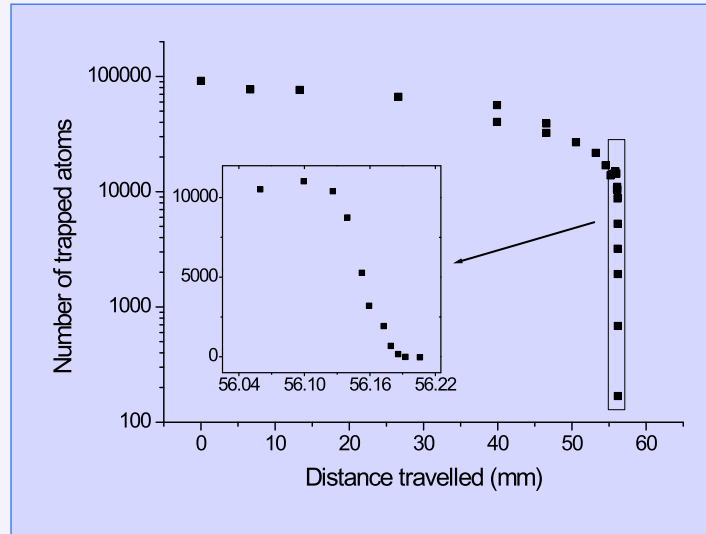
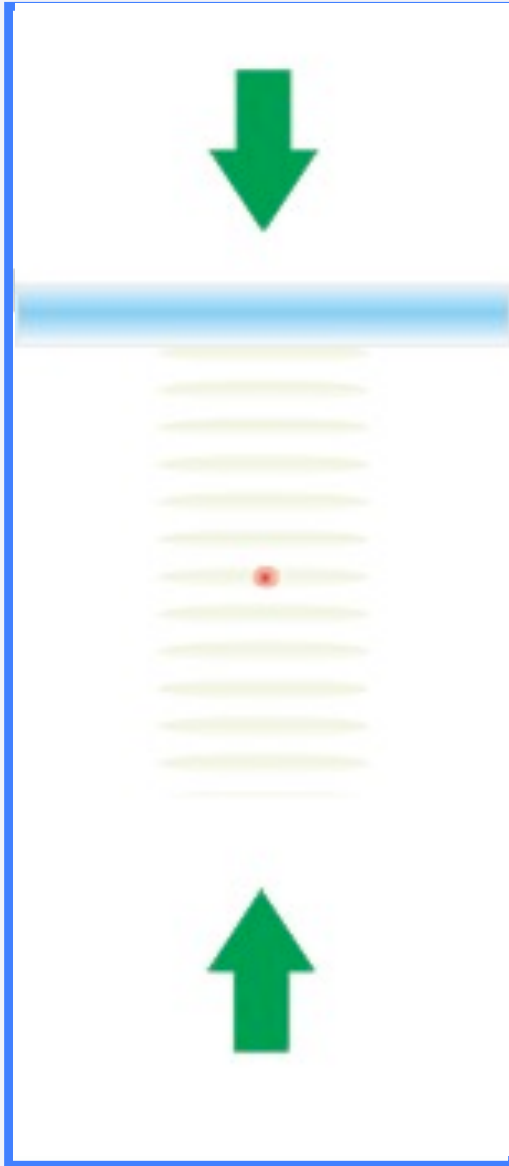


Scheme for the measurement of small distance forces



Objective: $\lambda = 1-10 \mu m$, $\alpha = 10^3-10^4$

Atom elevator

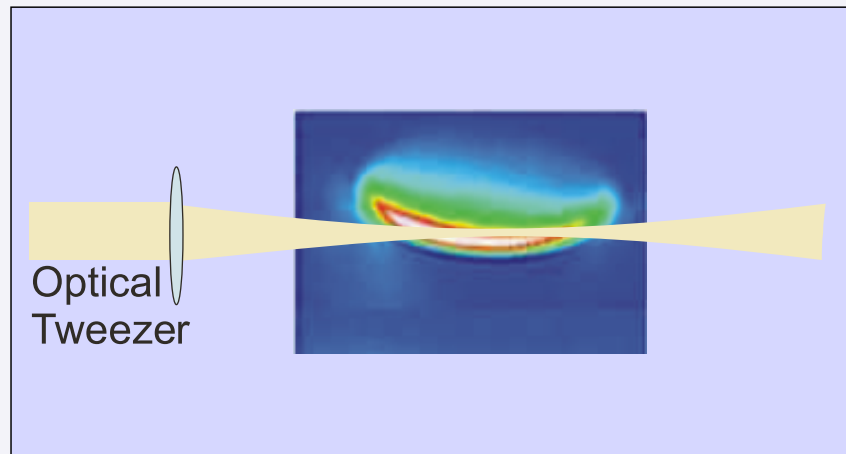


Vertical size of the atomic sample: $15\ \mu\text{m}$

Atom elevator:

upward acceleration ($1.35\ \text{g}$) for $10\ \text{ms}$
uniform velocity ($133\ \text{mm/s}$) for variable time
downward acceleration ($-1.35\ \text{g}$) for $10\ \text{ms}$
rest for $470\ \text{ms}$
reverse motion back to the starting point

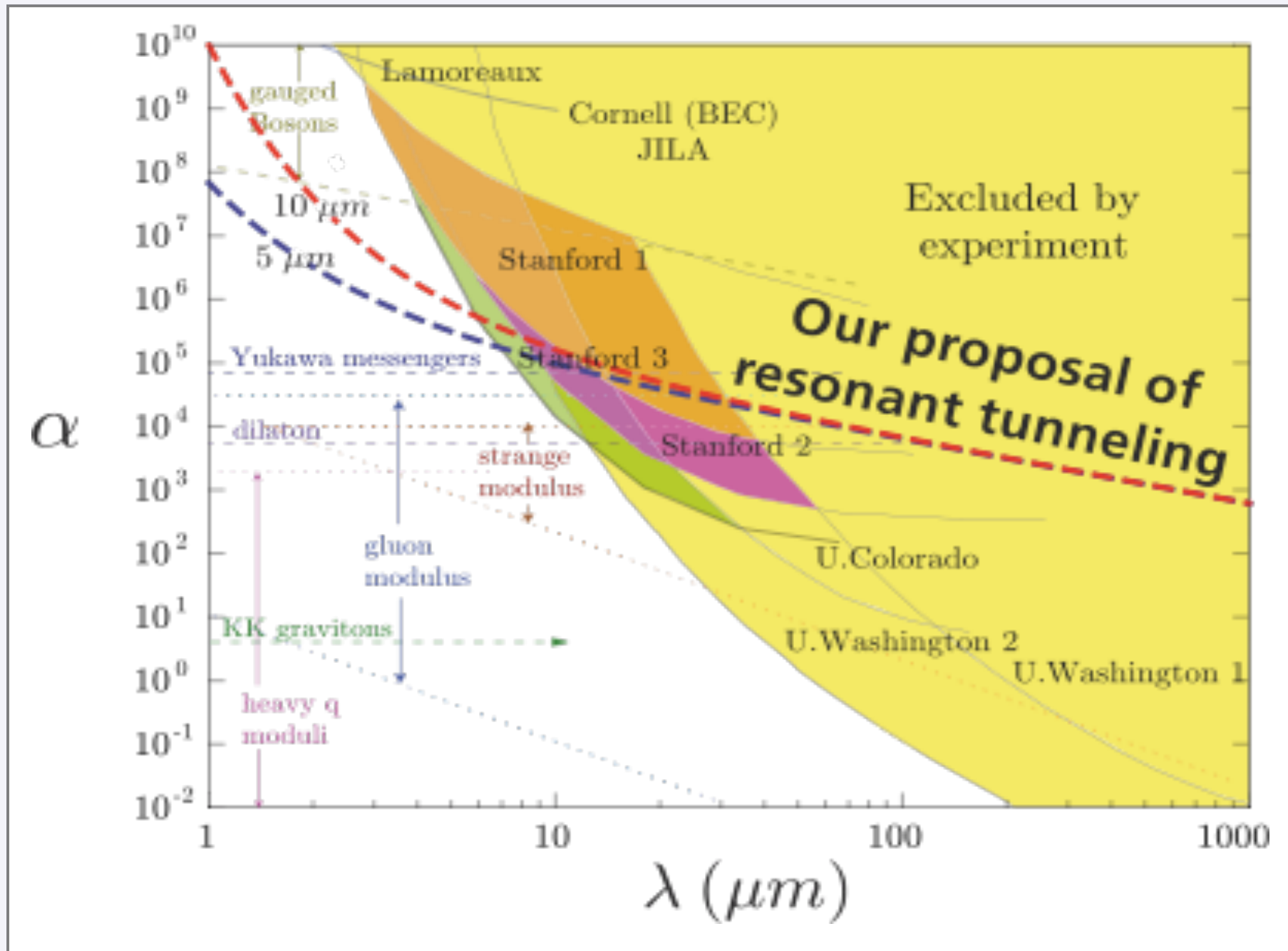
Vertical position fluctuations: $3\ \mu\text{m rms}$



• Vertical size reduced to $4\ \mu\text{m}$
with an optical tweezer

F. Sorrentino, A. Alberti, G. Ferrari, V. V. Ivanov, N. Poli, M. Schioppo, and G. M. Tino, *Quantum sensor for atom-surface interactions below $10\ \mu\text{m}$* , **Phys. Rev. A** **79**, 013409 (2009)

Accessible region with atomic probes

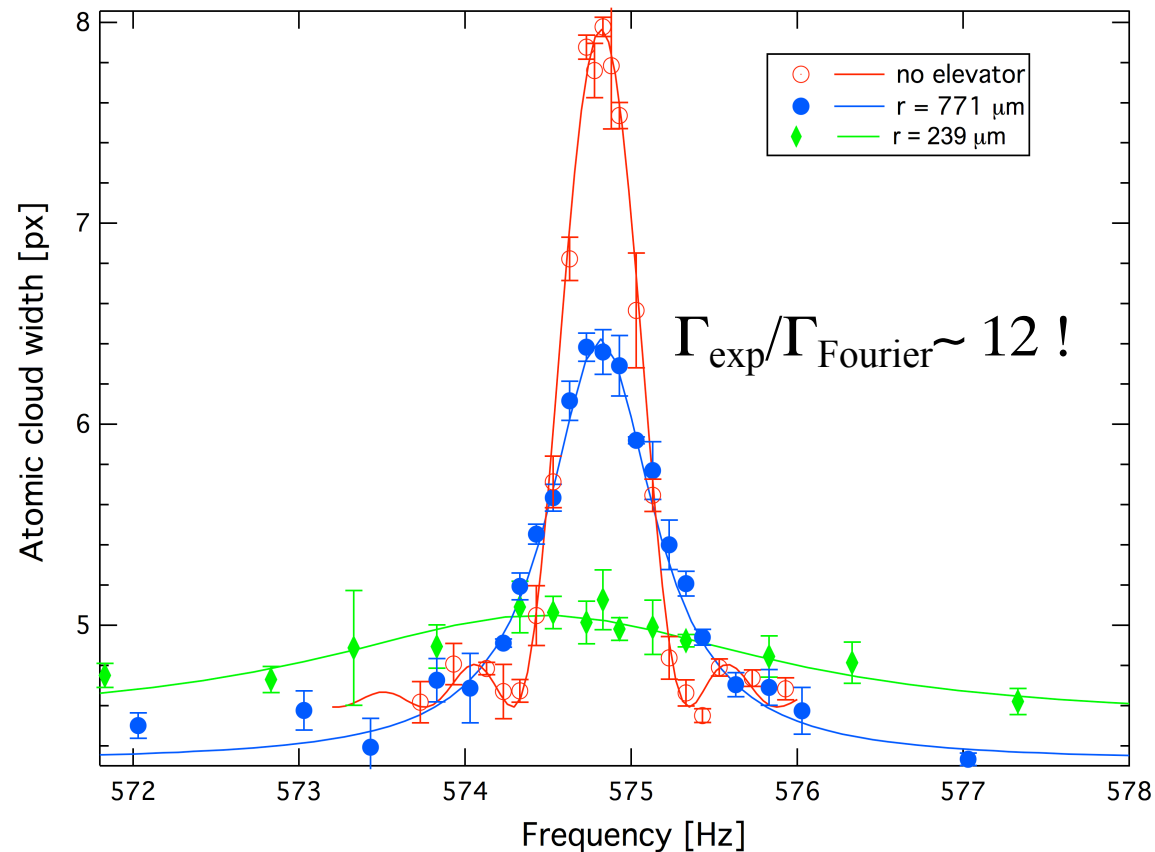
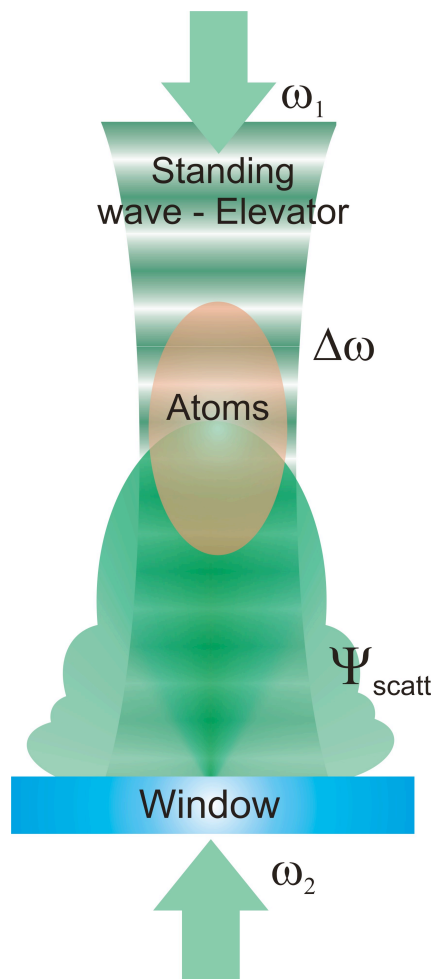


Short-distance measurements

- **Optical elevator** to bring atoms close to a sample surface: trying to measure Casimir-Polder force

⇒ AM measurement close to the surface (preliminary)

Getting closer:



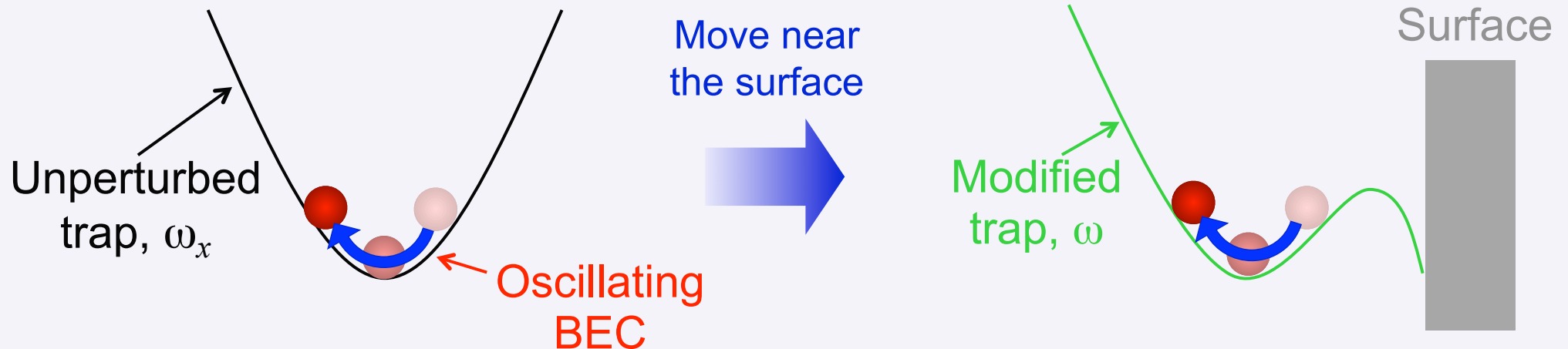
Measuring atom-surface forces

Use trapped BEC as a mechanical oscillator

Measure changes in dipole oscillation frequency

Negative curvature
attractive potential

Trap frequency decrease



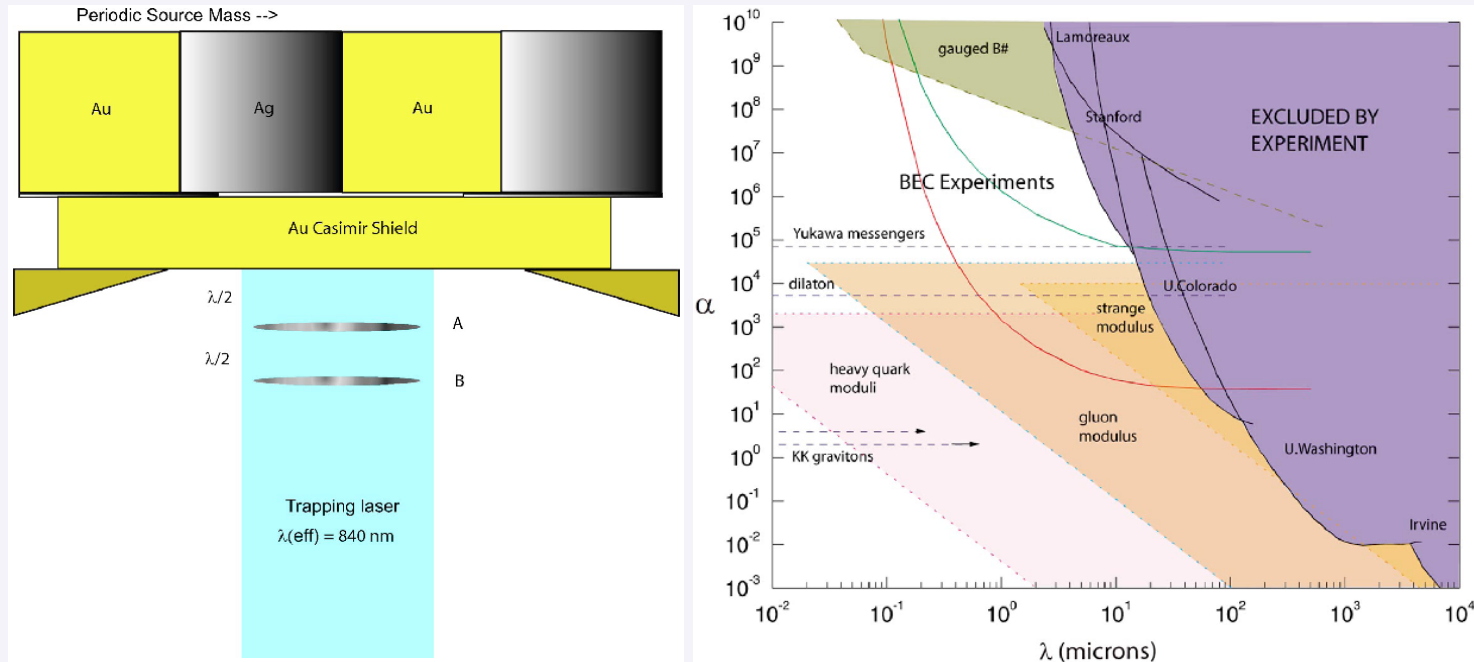
Express trap frequency changes as normalized frequency shifts:

From E.A. Cornell, San Feliu Conference, 2005

D. M. Harber, J. M. Obrecht, J. M. McGuirk, E. A. Cornell, *Measurement of the Casimir-Polder force through center-of-mass oscillations of a Bose-Einstein condensate*, PRA 72, 033610 (2005)

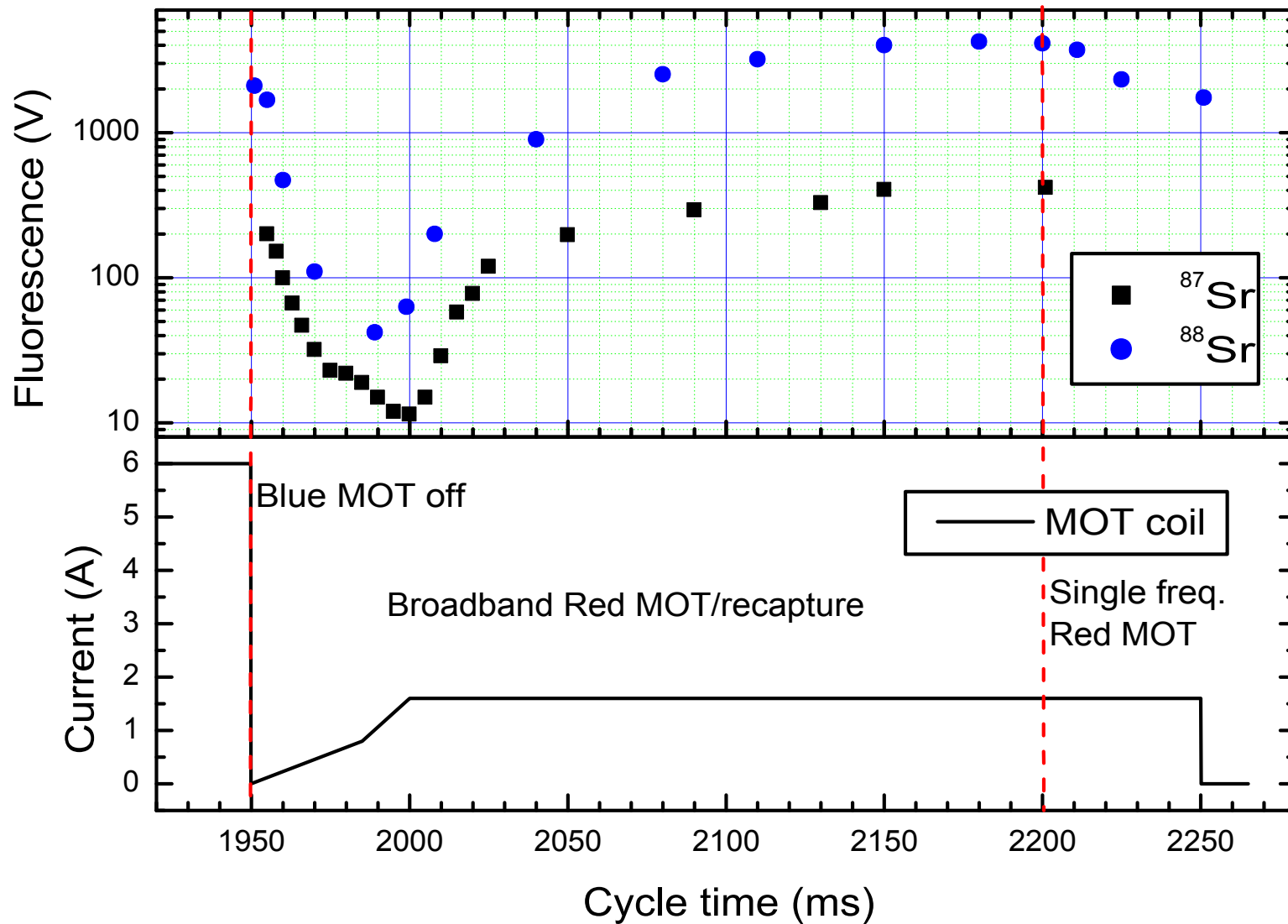
$$\frac{\omega_x - \omega}{\omega_x} \approx - \frac{1}{2\omega_x^2 m} \frac{d^2U}{dx^2}$$

Other proposals



- S. Dimopoulos, A. A. Geraci, *Probing submicron forces by interferometry of Bose-Einstein condensed atoms*, Phys. Rev. D 68, 124021 (2003)
- I. Carusotto et al., *Sensitive measurement of forces at micron scale using Bloch oscillations of ultracold atoms*, Phys. Rev. Lett. 95, 093202 (2005)
- Peter Wolf, et al., *From Optical Lattice Clocks to the Measurement of Forces in the Casimir Regime*, Phys. Rev. A 75, 063608 (2007)

Simultaneous trapping of ^{88}Sr and ^{87}Sr



STE-QUEST

Space-Time Explorer and Quantum Test of the Equivalence Principle

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STE-QUEST

<http://sci.esa.int/ste-quest>

Applications of new quantum sensors based on atom interferometry

- Measurement of fundamental constants $\begin{matrix} \nearrow G \\ \searrow \alpha \end{matrix}$ 
- New definition of kg 
- Test of equivalence principle 
- Measurement of the gravitational redshift 
- Tests of quantum gravity 
- Short-distances forces measurement 
- Search for electron-proton charge inequality 
- New detectors for gravitational waves ? 
- Development of transportable atom interferometers $\begin{matrix} \longrightarrow \text{geophysics} \\ \searrow \text{space} \end{matrix}$ 
- 
- 

Test of quantum gravity

PRL **103**, 171302 (2009)

PHYSICAL REVIEW LETTERS

week ending
23 OCTOBER 2009

Constraining the Energy-Momentum Dispersion Relation with Planck-Scale Sensitivity Using Cold Atoms

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(Received 22 June 2009; published 21 October 2009)

We use the results of ultraprecise cold-atom-recoil experiments to constrain the form of the energy-momentum dispersion relation, a structure that is expected to be modified in several quantum-gravity approaches. Our strategy of analysis applies to the nonrelativistic (small speeds) limit of the dispersion relation, and is therefore complementary to an analogous ongoing effort of investigation of the dispersion relation in the ultrarelativistic regime using observations in astrophysics. For the leading correction in the nonrelativistic limit the exceptional sensitivity of cold-atom-recoil experiments remarkably allows us to set a limit within a single order of magnitude of the desired Planck-scale level, thereby providing the first example of Planck-scale sensitivity in the study of the dispersion relation in controlled laboratory experiments.

$$E = \sqrt{p^2 + m^2} + \Delta_{QG}(p, m, M_P)$$

$$E \simeq m + \frac{p^2}{2m} + \frac{1}{2M_P} \left(\xi_1 m p + \xi_2 p^2 + \xi_3 \frac{p^3}{m} \right)$$

$$|\xi_1| \sim 1 \text{ to } |\xi_1| \sim 10^3$$

$$-6.0 < \xi_1 < 2.4$$

$$|\xi_2| \lesssim 10^9$$

Gravitational wave detection

Can we use atom interferometers in searching for gravitational waves?

- C.J. Bordé, *University of Paris N.*
- G. Tino, *University of Firenze*
- F. Vetrano, *University of Urbino*

F.Vetrano - Aspen Winter Conference, FEB 2004

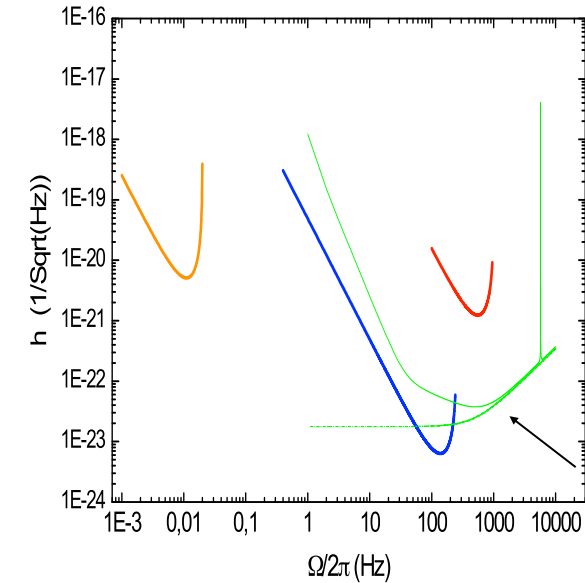
Build the

The sensitivity (2)

$v_L = 10^6$ m/s; $\dot{N} = 10^{18}$ atoms(H)/s;
 $T = 10^{-3}$ s; $L = 10^3$ m; $v_T = 10$ m/s

$v_L = 10^7$ m/s; $L = 10^5$ m
 $T = 10^{-2}$ s

$v_L = 10$ m/s; $v_T = 5$ m/s; $L = 50$ m;
 $\dot{N} = 10^{18}$ atoms(Cs)/s



Virgo

F.Vetrano - Aspen Winter Conference, FEB 2004

- C. Bordé, G. M. Tino, F. Vetrano, "Can we use atom interferometers in searching for gravitational waves?", 2004 Aspen Winter College on Gravitational Waves. Available online at: http://www.ligo.caltech.edu/LIGO_web/Aspen2004/pdf/vetrano.pdf
- R.Y. Chiao, A. D. Speliotopoulos, "Towards MIGO, the matter-wave interferometric gravitational-wave observatory, and the intersection of quantum mechanics with general relativity", *Journal of Modern Optics* (2004), 51(6-7), 861-899
- A. Roura, D.R. Brill, B. L. Hu, C.W. Misner, W.D. Phillips, "Gravitational wave detectors based on matter wave interferometers (MIGO) are no better than laser interferometers (LIGO)", *Physical Review D: Particles and Fields* (2006), 73(8), 084018/1-084018/14
- G.M. Tino, F. Vetrano, "Is it possible to detect gravitational waves with atom interferometers?", *Class. Quantum Grav.* 24, 2167 (2007)
- S. Dimopoulos, P.W. Graham, J.M. Hogan, M. A. Kasevich, S. Rajendran, "Atomic gravitational wave interferometric sensor", *Phys. Rev. D* 78, 122002 (2008)



October 14, 2008

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Gravitational Waves Detection with Atom Interferometry

Conference

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Organizers:

Guglielmo M. Tino, University of Firenze, Italy Flavio Vetrano, University of Urbino, Italy

Period: from 23-02-2009 to 24-02-2009

Deadline: 15-01-2009

Note: The number of participants is limited to 50 The participation fee for the Workshop is 150 Euros including registration, coffee-breaks, lunches and the social dinner. The fee should be paid cash on arrival at the registration desk

Abstract

The possibility of using atom interferometers to detect gravitational waves is attracting increasing interest as an alternative to other detectors. Several papers were published discussing theoretical and experimental aspects. Although the results show that dedicated technological developments are still needed to achieve the required sensitivity values which are beyond those presently available, newschemes for atom interferometers, beam splitters and high flux coherent atomic sources could lead to an increase in sensitivity and make atom interferometers competitive with other gravitational wave detectors. The Workshop on "Gravitational Waves Detection with Atom Interferometry" will bring together scientists interested in theoretical and experimental aspects to discuss different points of view and possible experimental implementations in Earth laboratories.

Special issue on
Gravitational Waves Detection with Atom Interferometry
 G.M. Tino, F. Vetrano, C. Laemmerzahl Editors,
 General Relativity and Gravitation **43**, 1901 (2011)



SOCIETÀ ITALIANA DI FISICA



International School of Physics "Enrico Fermi" Summer Course 2013 - *"Atom Interferometry"* *Varenna, 14 - 20 July 2013*

Directors: G. M. Tino (Università di Firenze), M. A. Kasevich (Stanford University)



G. Tino team members

Nicola Poli Researcher, Università di Firenze
Fiodor Sorrentino Post-doc, LENS
Quentin Bodart Post-doc, Università di Firenze/ESA
Yu-Hung Lien Post-doc, Università di Firenze/ICTP
Marco Schioppo Post-doc, LENS
Marco Tarallo Post-doc, LENS
Gabriele Rosi Post-doc, Università di Firenze
Denis Sutyryn PhD student, Università di Pisa
Tommaso Mazzoni Diploma student, Università di Firenze

Luigi Cacciapuoti Long term guest, ESA-Noordwijk
Marella de Angelis Long term guest, CNR
Marco Prevedelli Long term guest, Università di Bologna
Elisa Tonelli Secretary

Previous members and visitors

Andrea Alberti, PhD student
Andrea Bertoldi, Post-doc
Sergei Chepurov, Institute of Laser Physics, Novosibirsk, visitor
Robert Drullinger, NIST, Long term guest
Marco Fattori, PhD student
Gabriele Ferrari, Researcher, INFN/CNR
Antonio Giorgini, PhD and Post-doc
Vladyslav Ivanov, Post-doc
Marion Jacquey, Post-doc
Giacomo Lamporesi, PhD student
Chris Oates, NIST, visitor
Torsten Petelski, PhD student
Juergen Stuhler, Post-doc
Fu-Yuan Wang, Post-doc, Università di Firenze/ICTP

Support and funding

- ✓ Istituto Nazionale di Fisica Nucleare (INFN)
- ✓ European Commission (EC)
- ✓ ENI
- ✓ Ministero dell'Istruzione, dell'Università e della Ricerca (MIUR)
- ✓ European Laboratory for Non-linear Spectroscopy (LENS)
- ✓ Ente Cassa di Risparmio di Firenze (CRF)
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- ✓ Istituto Nazionale Geofisica e Vulcanologia (INGV)

<http://coldatoms.lens.unifi.it/>