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YANG-MILLS THERMODYNAMICS

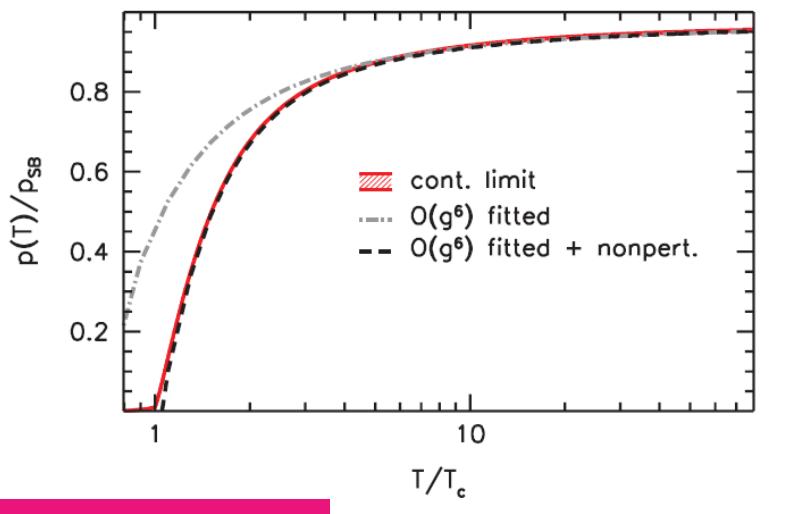
Quasiparticles and Z(3) lines condensates

In this talk:

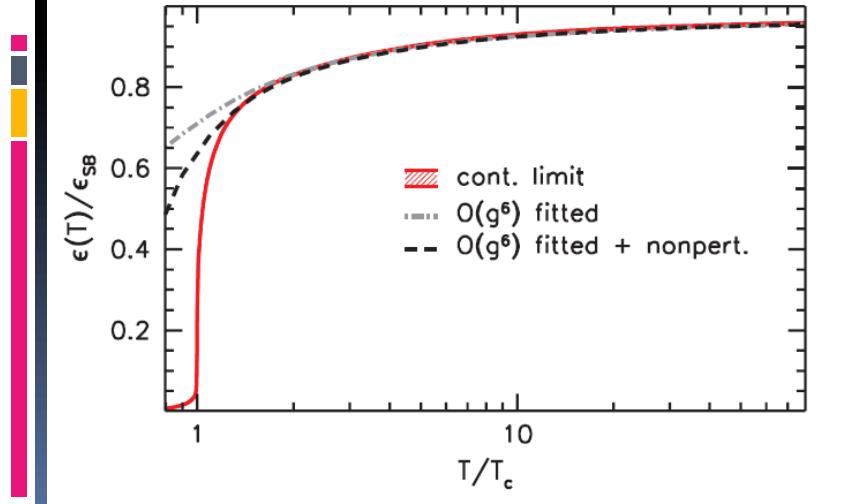
- Salient features of $SU(3)$ Yang-Mills thermodynamics
- Quasiparticles picture of plasmas
- $Z(3)$ lines condensate picture of plasmas
- Merging the two pictures
- Conclusions and Outlook

Yang-Mills Data

Pressure



Energy density



Hot SU(3) pure Yang-Mills theory

First order phase transition, from hadron phase to deconfinement phase.

Critical temperature: $T_c = 270$ MeV

Latent heat (energy density jump):
about 9×10^9 MeV 4

Non-perturbative regime

Similar results obtained in:

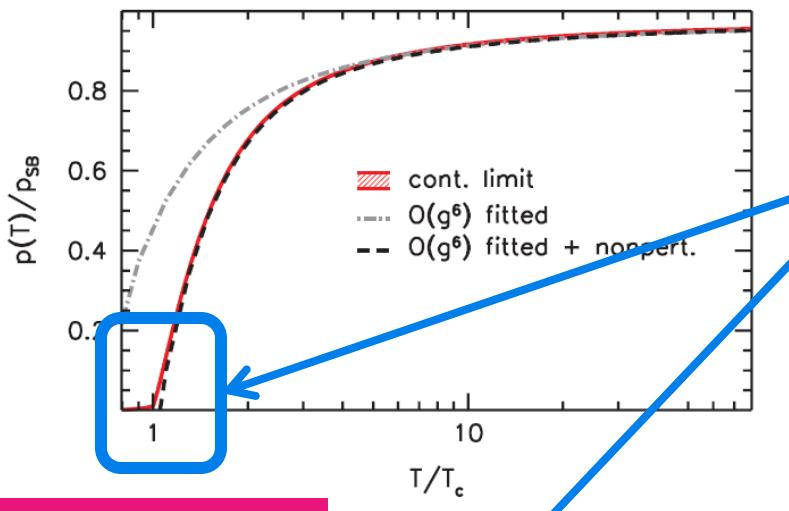
G. Boyd *et al.*, Nucl.Phys. B469 (1996)

S. Datta and S. Gupta, Phys. Rev. D82 (2010)

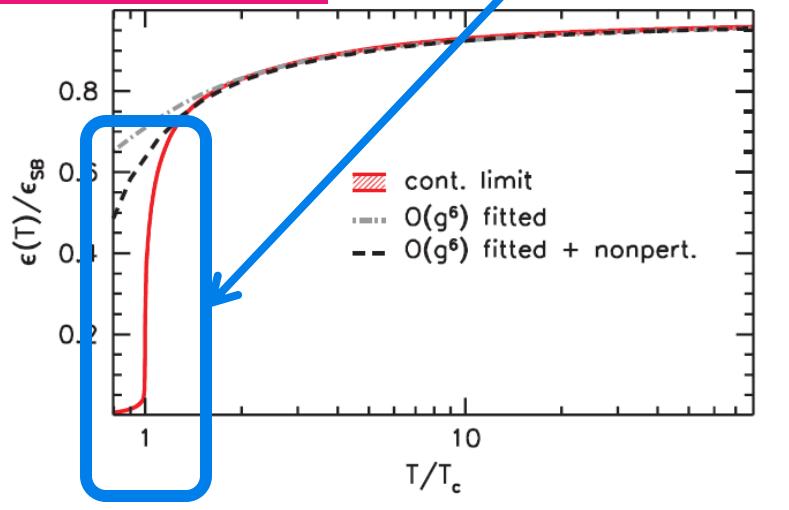
G. Endrodi *et al.*, arXiv:1104.0013

Yang-Mills Data

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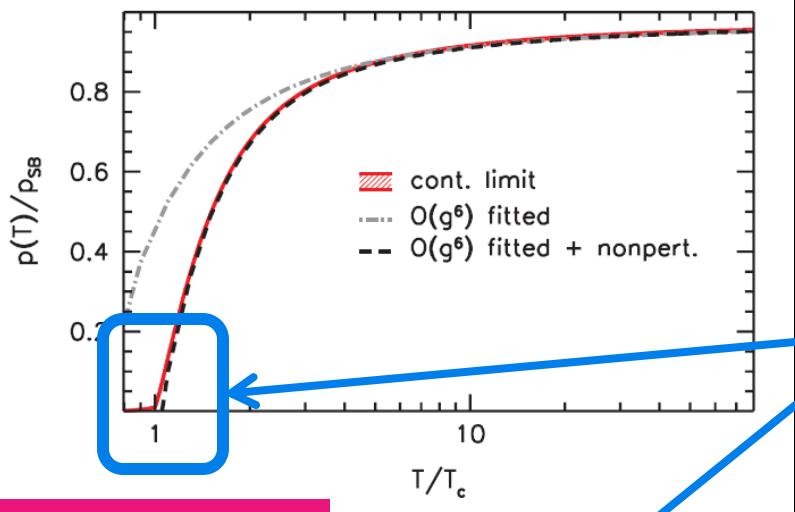
First order phase transition, from hadron phase to deconfinement phase.

Hadron (*Confinement*) Phase:
Glueballs + Hagedorn Spectrum
(WUB collaboration , arXiv:1204.6184
H. B. Meyer, Phys. Rev. D80 (2009))

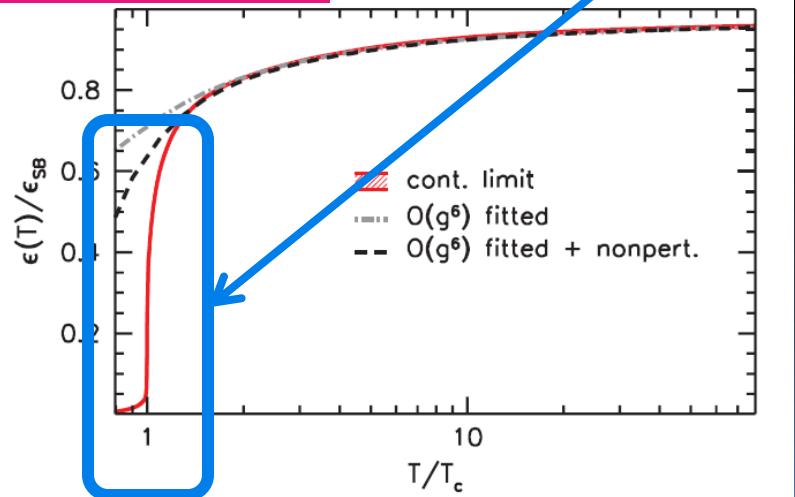
Deconfinement Phase:
Gluon Quasiparticles
 $Z(3)$ Lines Condensate

Yang-Mills Data

Pressure



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Hot SU(3) pure Yang-Mills theory

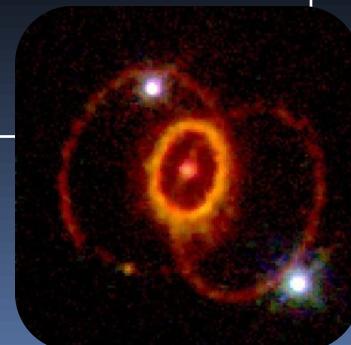
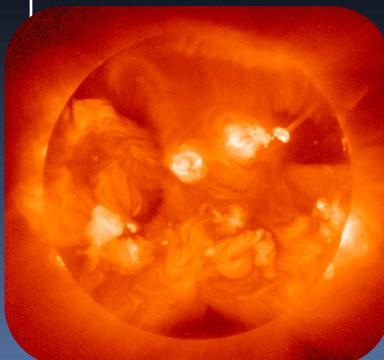
First order phase transition, from hadron phase to deconfinement phase.

Critical temperature: $T_c = 270$ MeV
(about 3×10^{12} Kelvin)

For comparison:

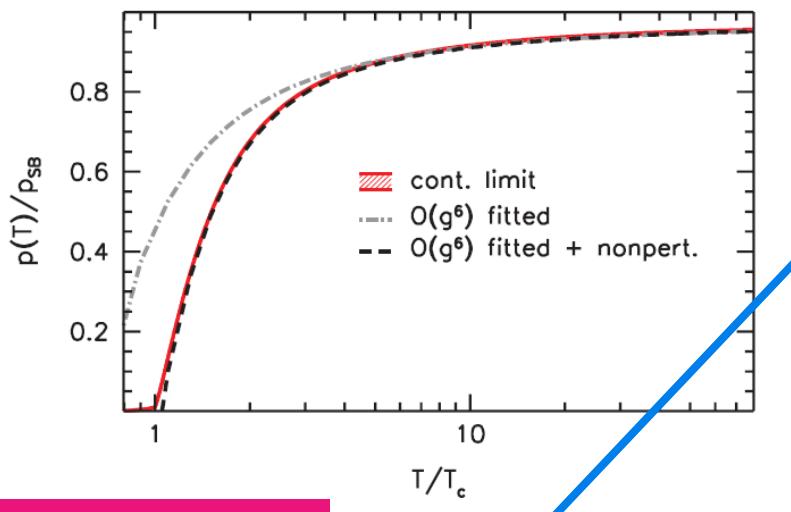
Sun core temperature: about 10^7 Kelvin

Supernova core: about 5×10^{11} Kelvin
(from NASA website)

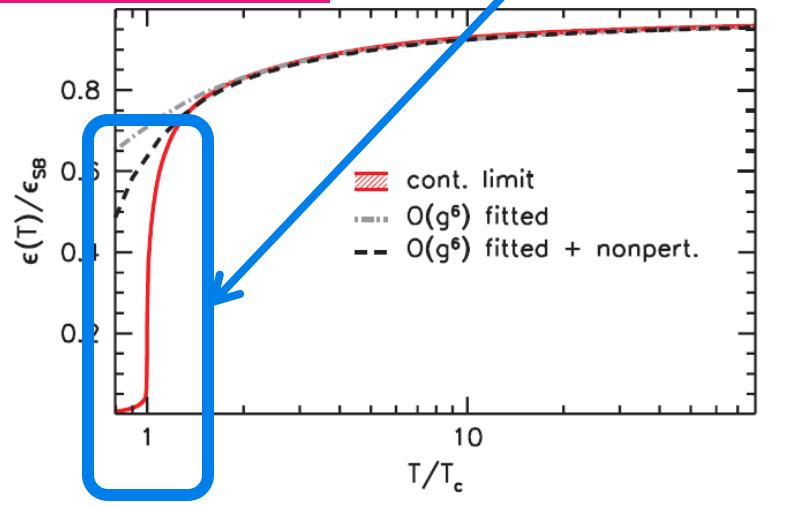


Yang-Mills Data

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Energy density



Hot SU(3) pure Yang-Mills theory

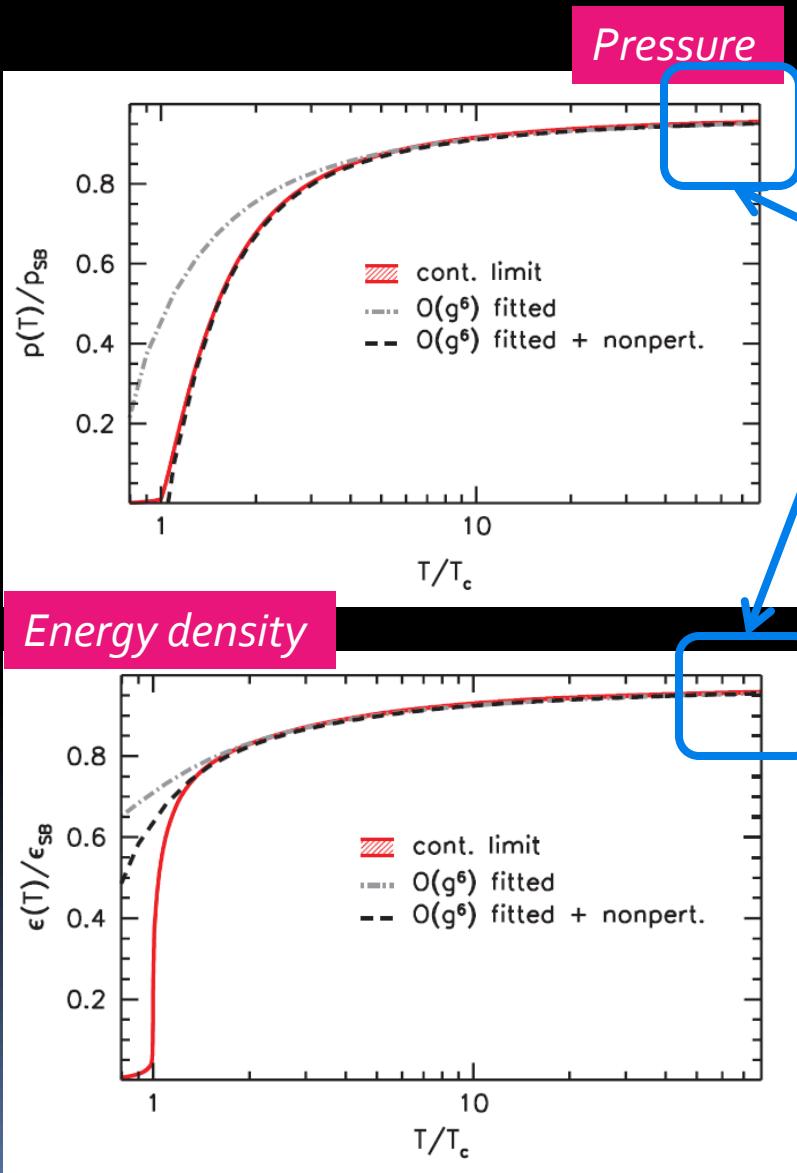
Latent heat (energy density jump):
about 9×10^9 MeV 4

About 10^{26} times larger than boiling water:

SU(3): about 10^{29} J/cm 3
Boiling water: about 10^3 J/cm 3



Yang-Mills Data



Hot SU(3) pure Yang-Mills theory

"Non-perturbative" regime

Data below Stefan-Boltzmann limit
(gas made of free massless particles)

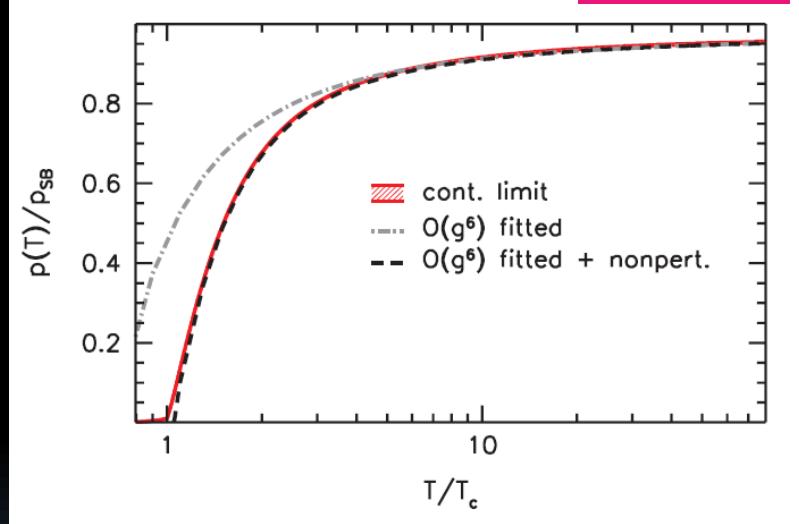
$$P = v_b \frac{\pi^2 T^4}{90} \quad \epsilon = v_b \frac{\pi^2 T^4}{30}$$

(for example, at $T=100 T_c$, $p/p_{SB} = 0.95$)

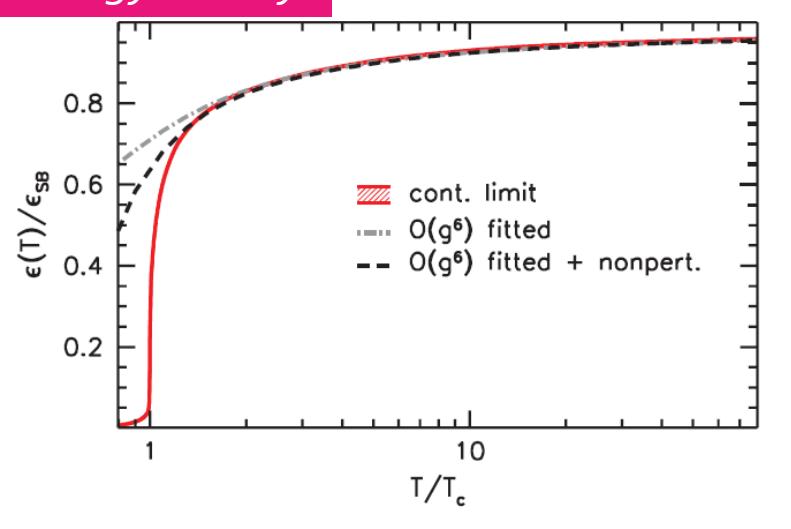
Yang-Mills Thermodynamics

Scope: understand Lattice data about thermodynamics, in terms of the relevant degrees of freedom.

Pressure



Energy density



Microscopic/Phenomenological description of Lattice data is interesting for (at least) two reasons:

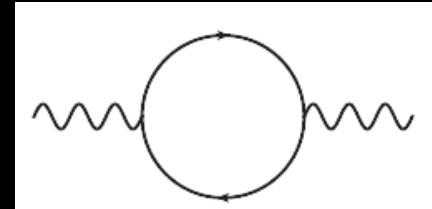
- 1.) Better theoretical understanding of hot and deconfined Yang-Mills system.
- 2.) Applications to heavy ion collision simulations.

Collective excitations in a QCD plasma

Retarded gluon propagator at finite temperature:

$$D_{\mu\nu}^R = \frac{i}{Q^2 - G} P_{\mu\nu}^T + \frac{i}{Q^2 - F} P_{\mu\nu}^L - i \frac{\xi}{Q^2} \frac{Q_\mu Q_\nu}{Q^2}$$

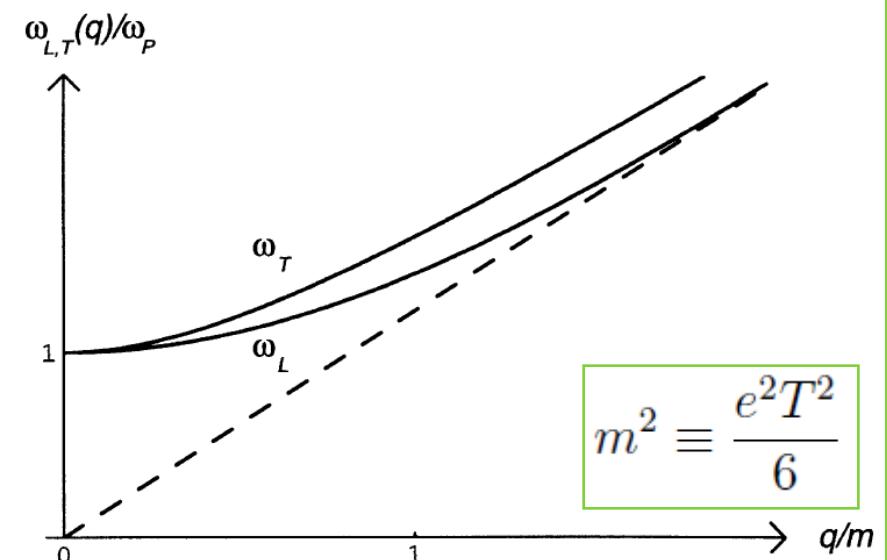
G = Transverse self-energy
F = Longitudinal self-energy



Poles of transverse and longitudinal parts of the gluon propagator give the *dispersion laws* for the transverse and longitudinal *damped travelling waves* in the plasma.

$$\omega_T^2(\mathbf{q}) = \mathbf{q}^2 + \text{Re}G(q_0 = \omega_T(\mathbf{q}), \mathbf{q})$$

$$\omega_L^2(\mathbf{q}) = \mathbf{q}^2 + \text{Re}F(q_0 = \omega_L(\mathbf{q}), \mathbf{q})$$



H. Arthur Weldon, Phys. Rev. D26 (1982)

See also:

Le Bellac textbook

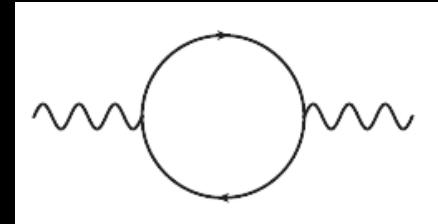
$$m^2 \equiv \frac{e^2 T^2}{6}$$

Collective excitations in a QCD plasma

Retarded gluon propagator at finite temperature:

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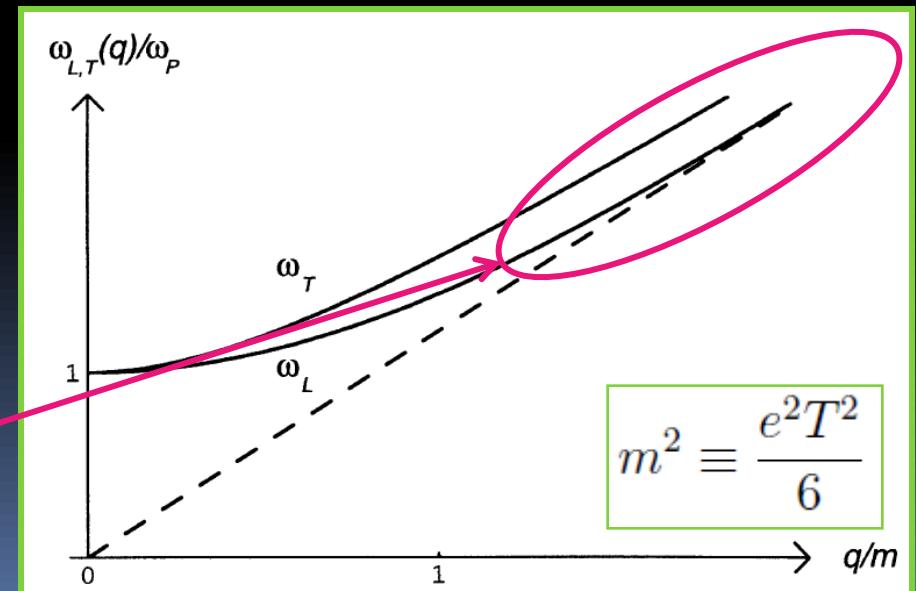
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$$\omega_L^2(\mathbf{q}) = \mathbf{q}^2 + \text{Re}F(q_0 = \omega_L(\mathbf{q}), \mathbf{q})$$

Transverse (Gluons)

Longitudinal (Plasmon)

$|q| \gg m :$
 $\omega_T^2 \approx \mathbf{q}^2 + m^2$
 $\omega_L^2 \approx \mathbf{q}^2$



Collective excitations in a QCD plasma

$$\omega_T^2(\mathbf{q}) = \mathbf{q}^2 + \text{Re}G(q_0 = \omega_T(\mathbf{q}), \mathbf{q})$$

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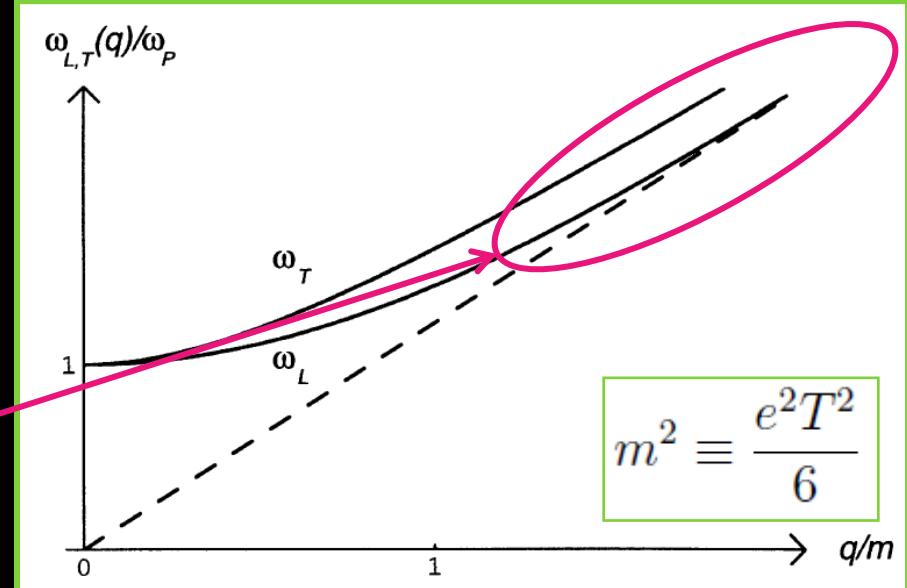
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Transverse (Gluons)

Longitudinal (Plasmon)

$$\omega_L^2 \approx \mathbf{q}^2$$



$$D_{pole} \approx \frac{Z(q_0, \mathbf{q})}{q_0^2 - \mathbf{q}^2 - m^2}$$

$|\mathbf{q}| \gg m :$

$$Z_T \approx \frac{1}{2|\mathbf{q}|}$$

$$Z_L \approx \frac{2|\mathbf{q}|}{m^2} \exp\left(-\frac{\mathbf{q}^2 + m^2}{m^2}\right)$$

Large momentum *longitudinal* mode does NOT propagate .

Thermodynamics is dominated by **transverse modes**.

Transverse Quasiparticles and Thermodynamics

Idea: Extend the high temperature, transverse quasiparticle picture of the plasma down to deconfinement temperature.

$$p \propto T \int \frac{d^3q}{(2\pi)^3} \log(1 - e^{-\beta\omega})$$
$$\omega = \sqrt{\mathbf{q}^2 + m^2},$$
$$m(T) = \frac{A}{(t - \delta)^c} + Bt, \quad t \equiv \frac{T}{T_c}$$

Perfect, massive gas of transverse QPs

Dispersion relation

(nonperturbative) Thermal mass

M. I. Gorenstein and S. N. Yang, **Phys. Rev. D52** (1995)

A. Peshier et al., **Phys. Rev. D54** (1996)

P. Levai and U. W. Heinz, **Phys. Rev. C57** (2001)

M. Bluhm et al., **Phys. Lett. B709** (2012)

P. N. Meisinger et al., **Phys. Lett. B585** (2004)

P. Castorina et al., **Eur. Phys. J. C71** (2011)

S. Plumari et al., **Phys. Rev. D84** (2011)

P. Castorina and M. Mannarelli, **Phys. Lett. B644** (2007)

Transverse Quasiparticles and Thermodynamics

$$p \propto T \int \frac{d^3q}{(2\pi)^3} \log(1 - e^{-\beta\omega})$$

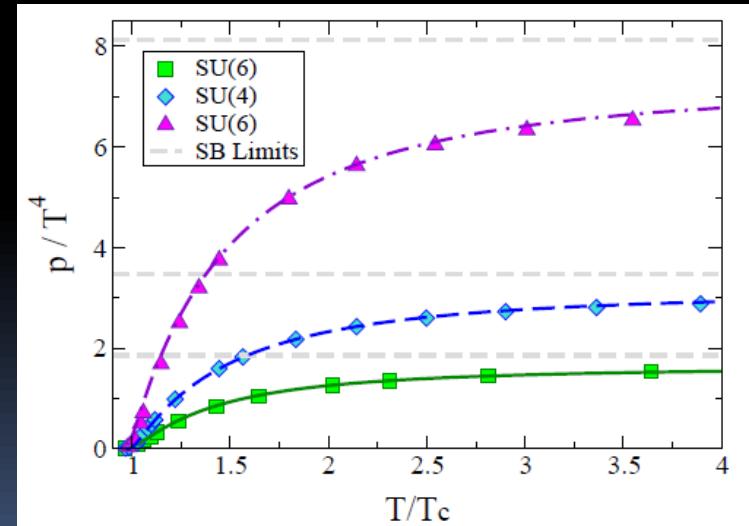
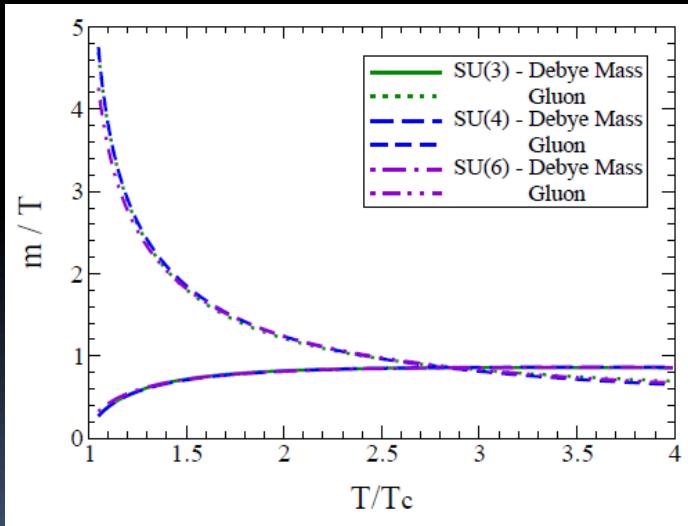
Perfect, massive gas of transverse QPs

$$\omega = \sqrt{\mathbf{q}^2 + m^2},$$

Dispersion relation

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(nonperturbative) Thermal mass



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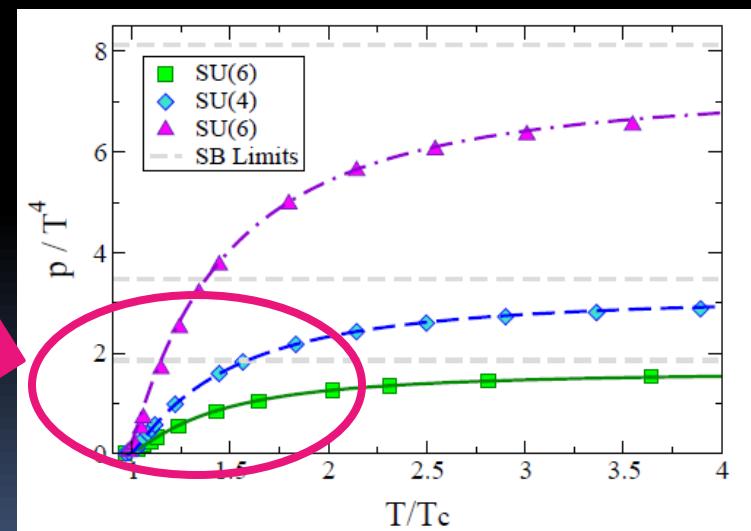
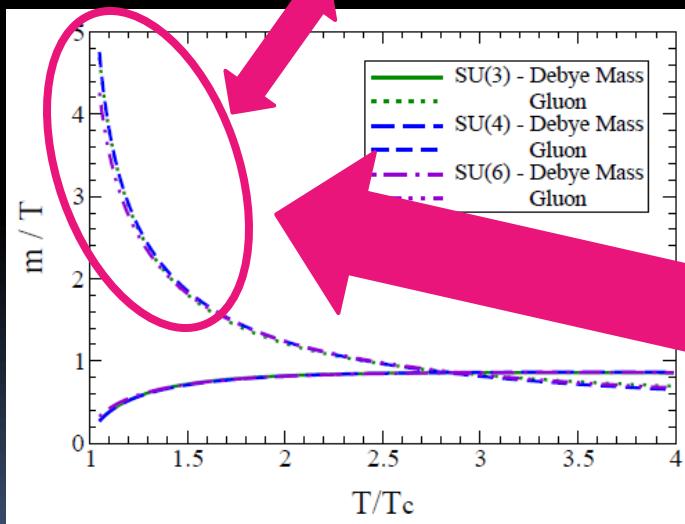
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$$\omega = \sqrt{q^2 + m^2},$$

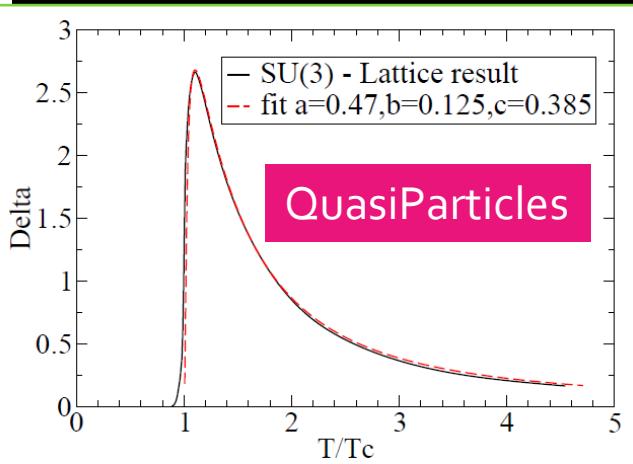
Dispersion relation

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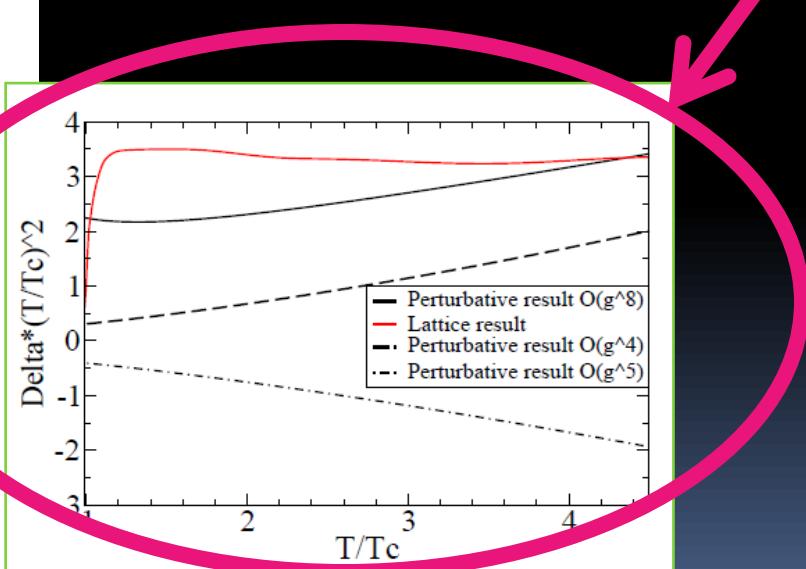
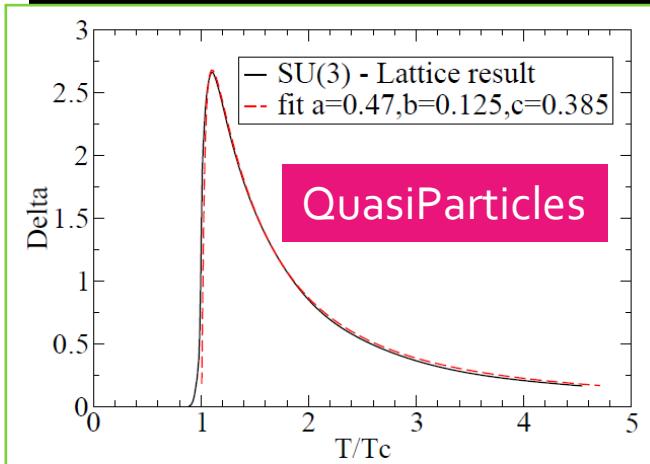


QPs vs “Perturbative”

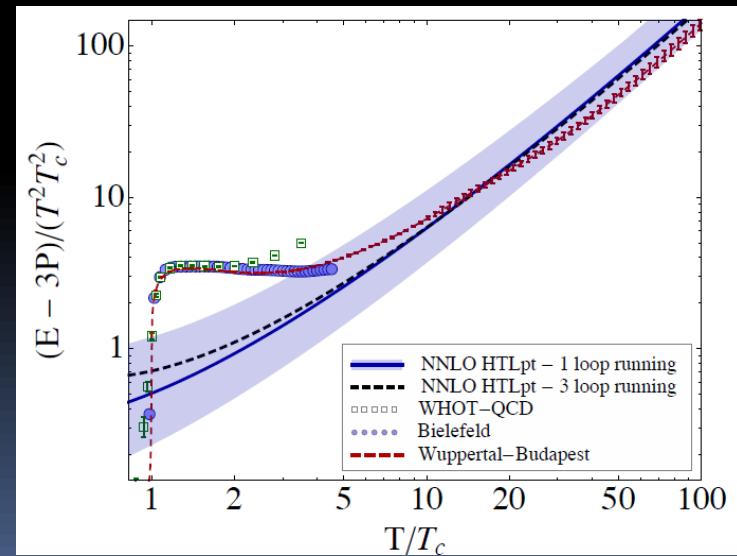


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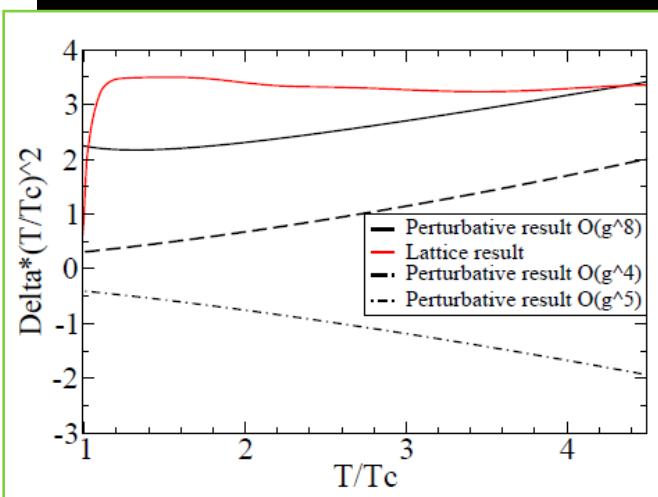
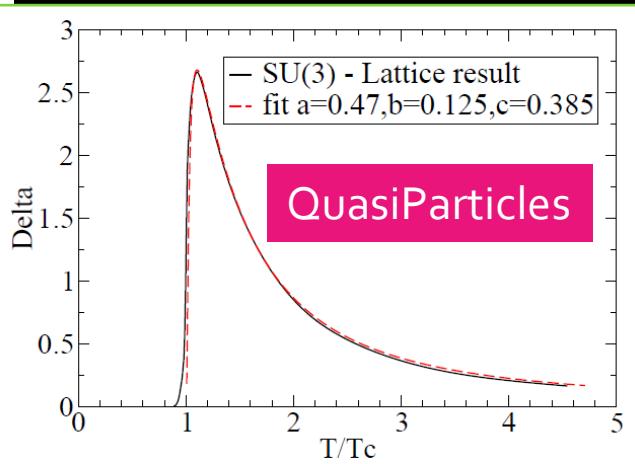
QPs vs “Perturbative”



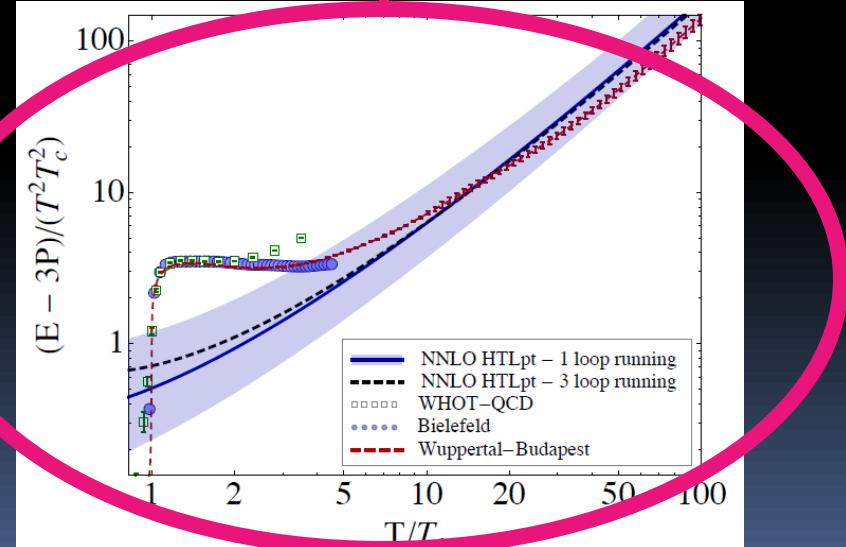
Perturbative Computation



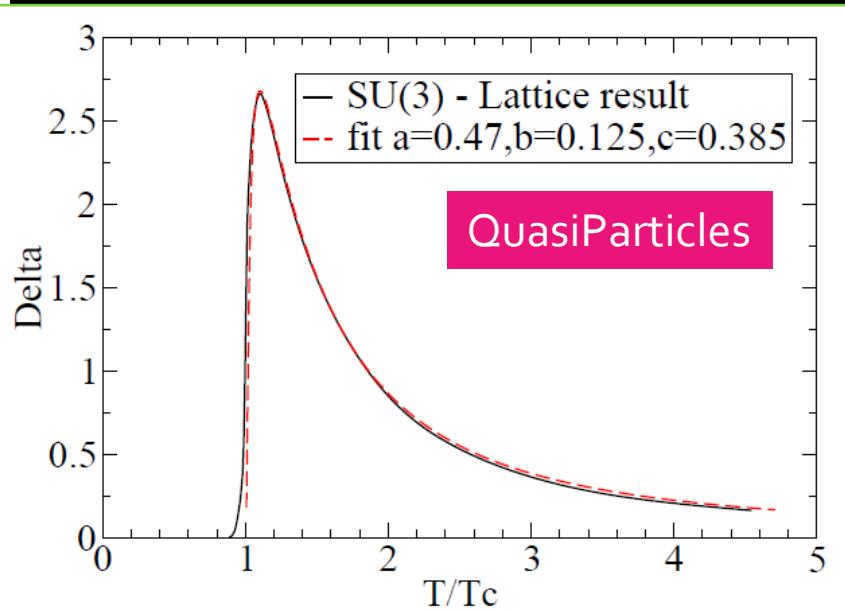
QPs vs “Perturbative”



Hard Thermal Loop



QPs vs “Perturbative”



Advantage of QPs:
 Offer a *simple interpretation* of the
non-perturbative gluon plasma,
 where perturbative methods do not work.

Alternative description: *Holographic QCD*.
 See for example:

- U. Gursoy *et al.*, JHEP 0905:033 (2009)
- P. Colangelo *et al.*, Phys. Rev. D80 (2009)
- F. Bigazzi *et al.*, Comm. Theor. Phys. 57 (2012)
- E. Megias *et al.*, Phys. Rev. D83 (2011)
- O. Andreev, Phys. Rev. D76 (2007)
- F. Xu and M. Huang, arXiv:1111.5152 [hep-ph]

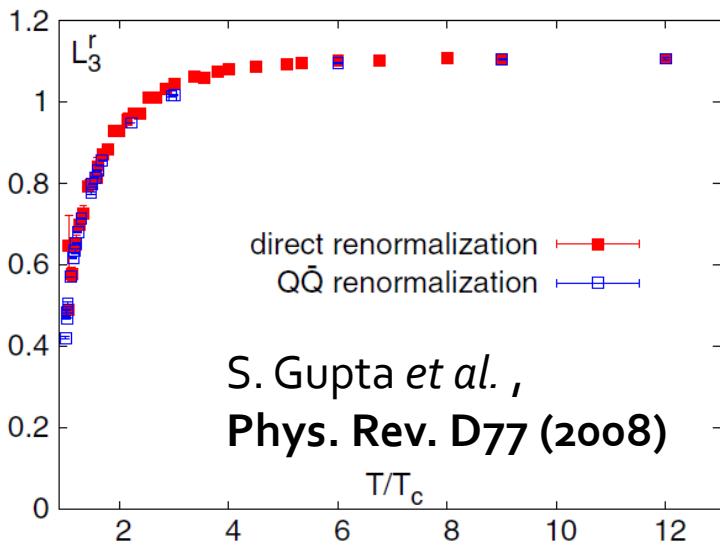
Polyakov loop

Consider the following order parameter for the confinement-deconfinement phase transition:

$$\ell_F(\mathbf{x}) = \frac{1}{N_c} \text{Tr} L_F(\mathbf{x})$$

$$L_{\mathcal{R}}(\mathbf{x}) = \mathcal{P} \exp \left[i \int_0^{1/T} d\tau \ A_4^a(\mathbf{x}, \tau) T_{a, \mathcal{R}} \right]$$

Confinement phase corresponds to vanishing Polyakov loop expectation value.



High temperature phase of the pure gauge theory is like the low temperature phase of a spin model, where the Polyakov loop takes the role of magnetization.



Condensate of Z(3) lines.

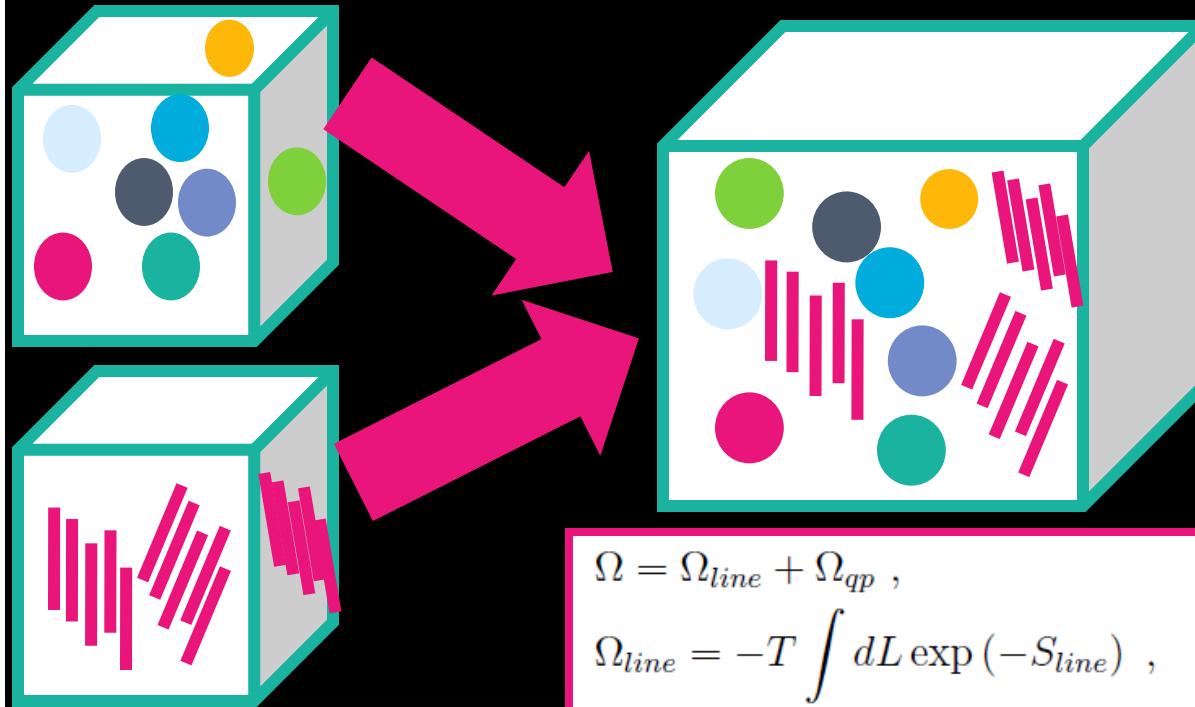
R. Pisarski, Phys. Rev. D62 (2000)
A. Dumitru *et al.*, Phys. Rev. D70 (2004)
R. Pisarski and V. Skokov, arXiv:1206.1329

Similar results on the Lattice obtained in:

M. Panero *et al.*, JHEP 1205 (2012)

O. Kaczmarek *et al.*, Phys. Lett. B543 (2002)

Z(3) condensates and QPs



Unified view:
*Transverse quasiparticles
 propagating in a
 $Z(3)$ lines condensate.*

$$\Omega = \Omega_{line} + \Omega_{qp} ,$$

$$\Omega_{line} = -T \int dL \exp(-S_{line}) , \quad S_{line} \propto \int dx dy \ell_F(\mathbf{x}) \ell_F^*(\mathbf{x} + \mathbf{y}) ,$$

$$\Omega_{qp} = 2T \int \frac{d}{(2\pi)^3} \text{Tr} \log \left[1 - L_A \exp \left(-\beta \sqrt{\mathbf{q}^2 + m^2} \right) \right] .$$

S_{line} inspired by:

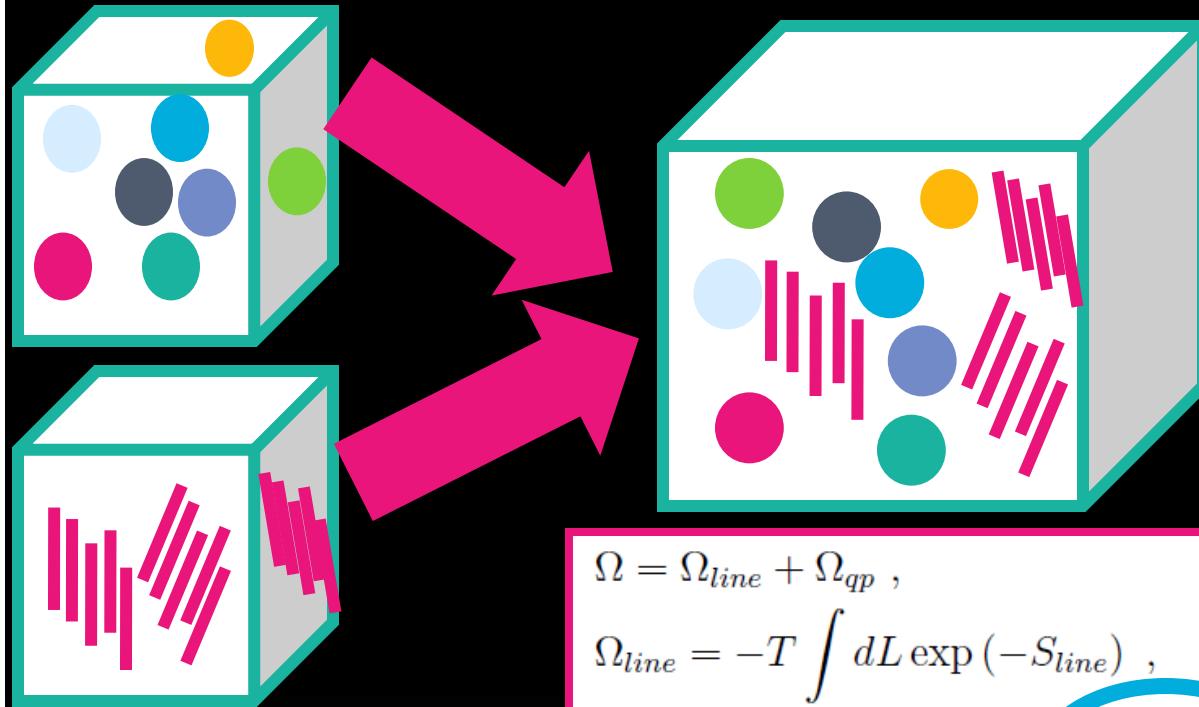
H. Abuki and K. Fukushima, Phys.Lett. B676 (2009)

T. Zhang et al., JHEP 1006 (2010) 064

Ω_{qp} inspired by:

P. Meisinger et al., Phys.Lett. B676 (2009)

Z(3) condensates and QPs



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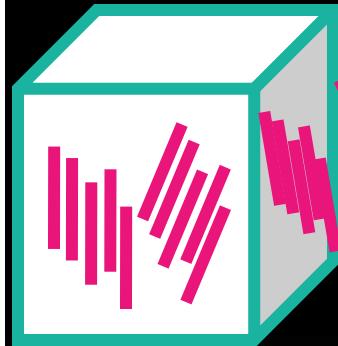
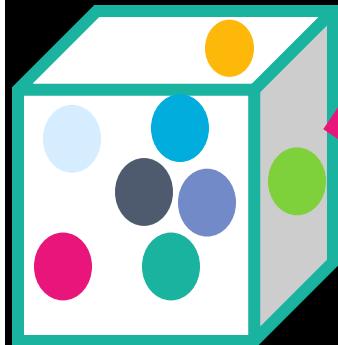
Ω_{qp} inspired by:

P. Meisinger et al., Phys.Lett. B676 (2009)

Coupling

N. Weiss,
 Phys.Rev. D24 (1981) 475

Z(3) condensates and QPs



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4 free parameters:

2 in the pure matrix model potential

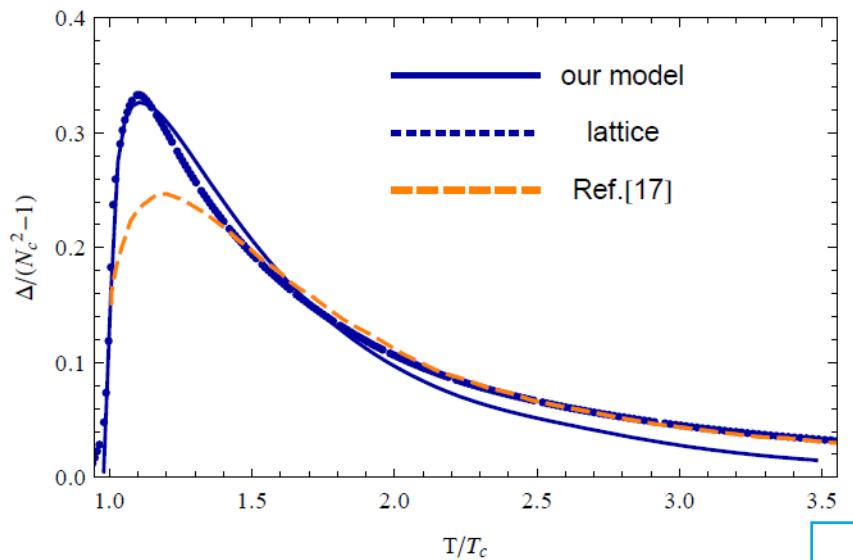
2 in the gluon quasiparticle mass

They are fixed by a best fit of pressure computed on the Lattice

Coupling

Results

Interaction Measure



The indigo line corresponds to the mass which offers the *best fit to* Lattice data for pressure.

Main effect of Polyakov loops:
QP mass does no longer diverge
at the deconfinement temperature.

Relevant for HICs simulations

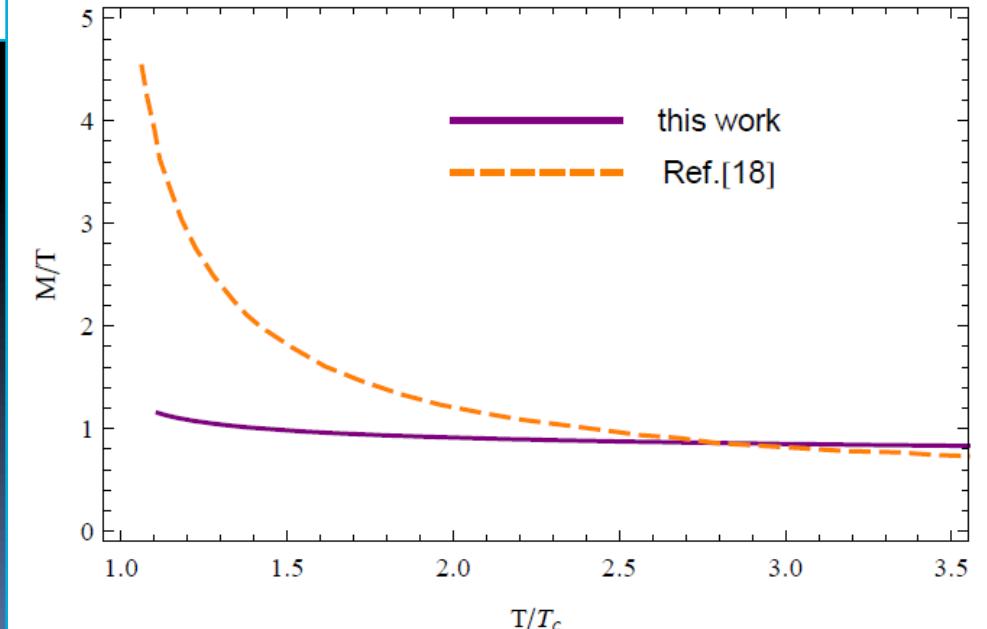
Lattice data from:

WUB collaboration , arXiv:1204.6184 [hep-lat]

[17] P. Meisinger et al., Phys.Lett. B676 (2009)

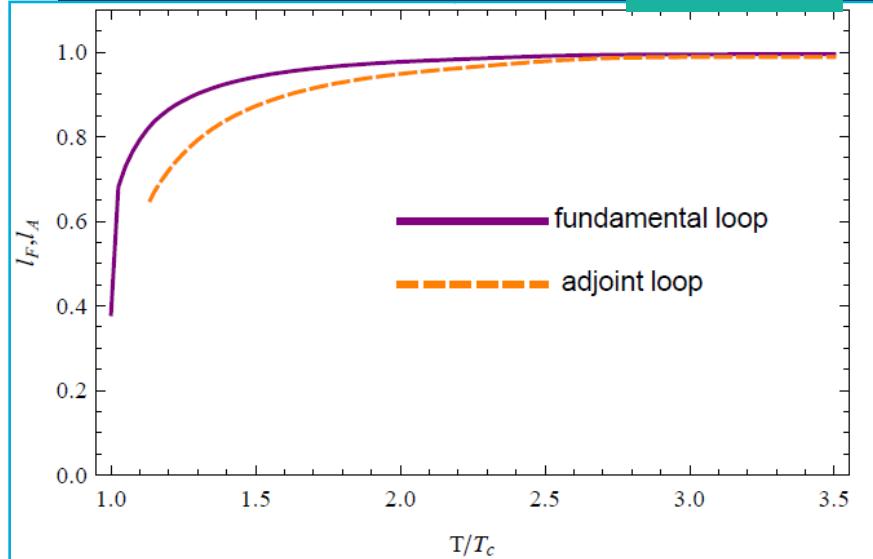
[18] P. Castorina et al., Eur. Phys. J. C71 (2011)

Quasiparticle Mass



Results

Polyakov Loops



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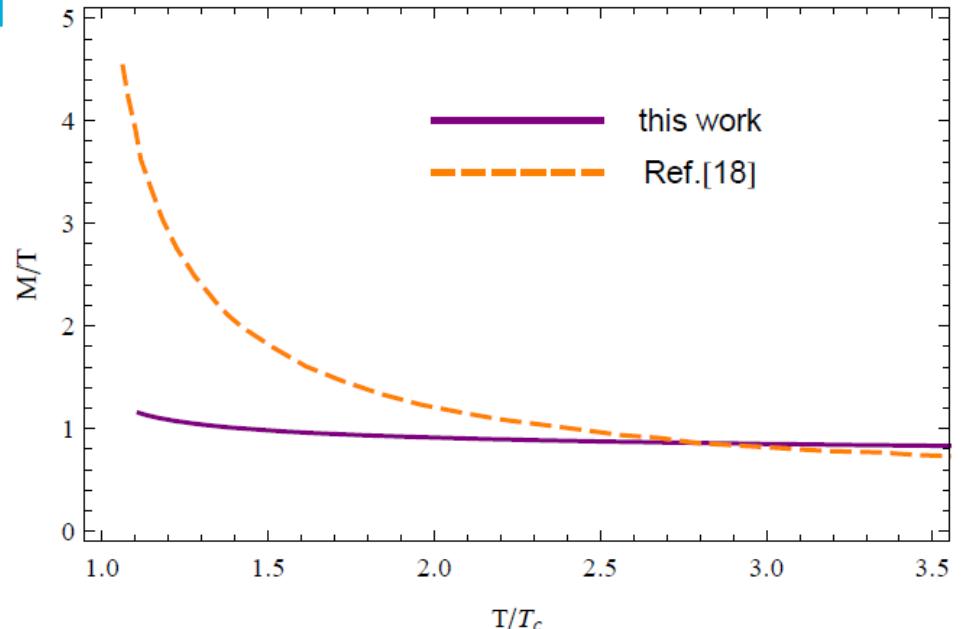
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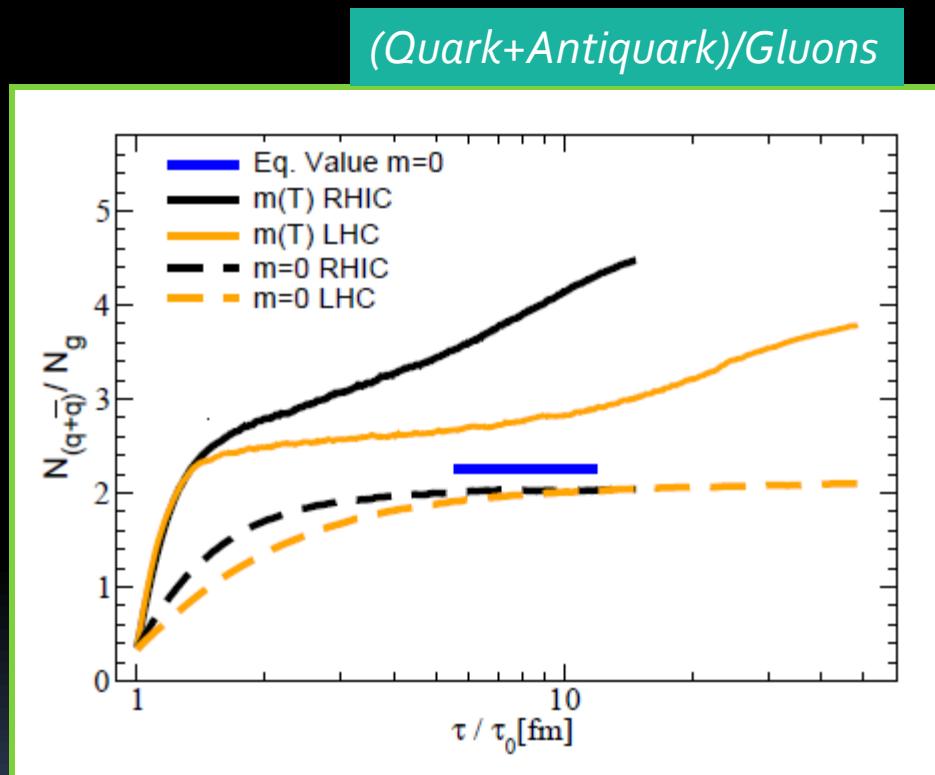
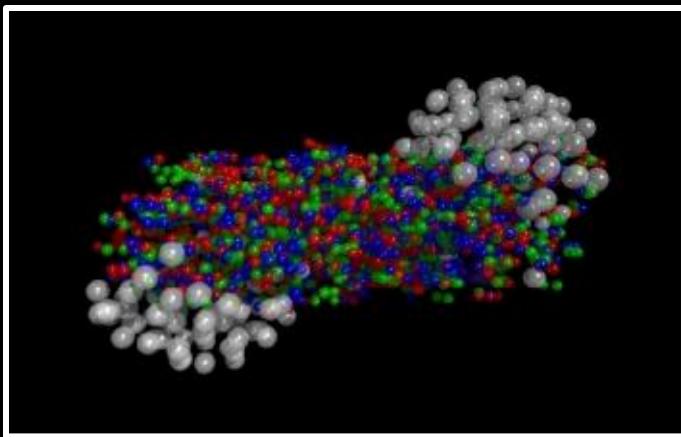
[18] P. Castorina et al., Eur. Phys. J. C71 (2011)

Quasiparticle Mass



QPs and the Fireball

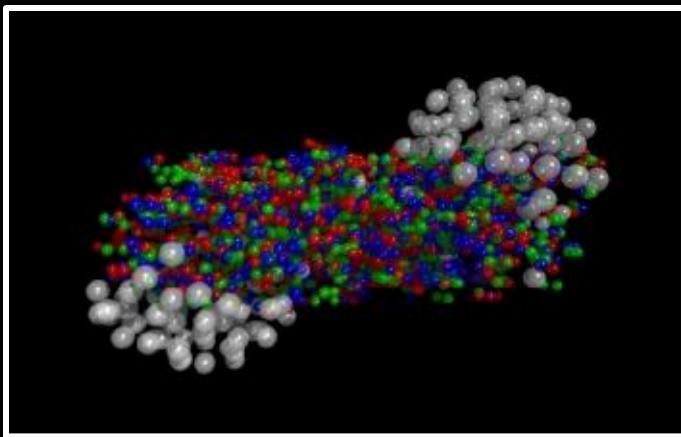
Quasiparticles have considerable application to the study of the chemical composition of the expanding fireball produced in a heavy ion collision .



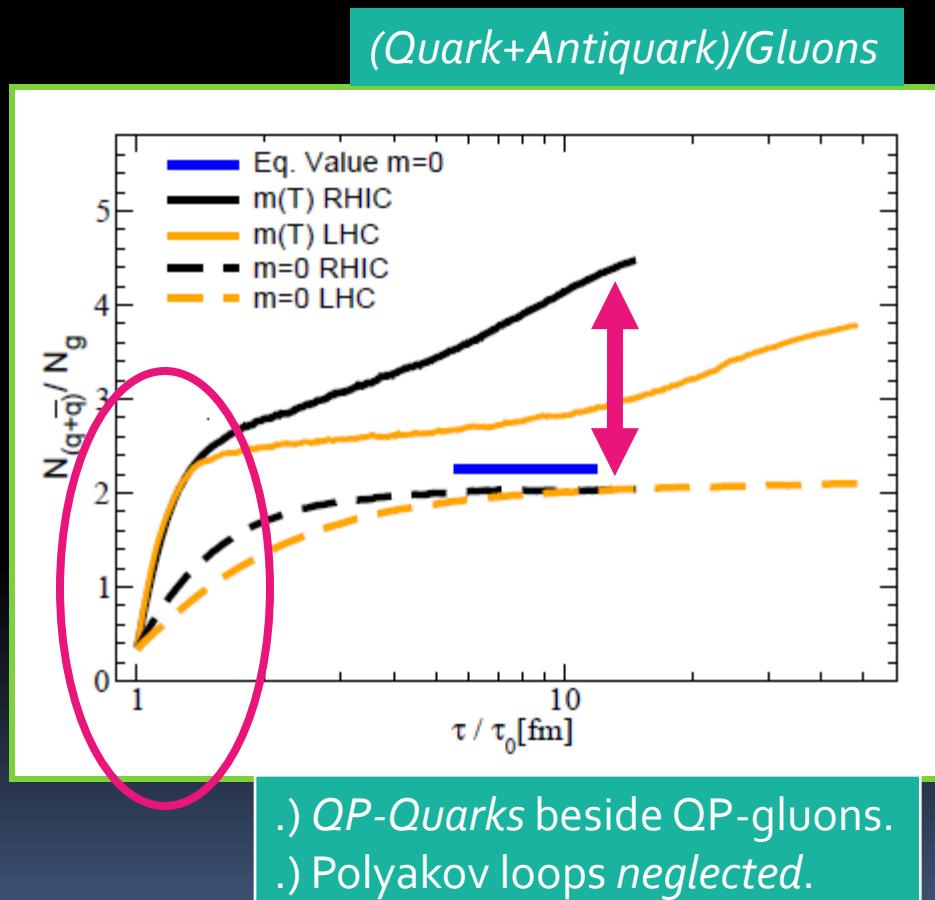
- .) QP-Quarks beside QP-gluons.
- .) Polyakov loops neglected.

QPs and the Fireball

Quasiparticles have considerable application to the study of the chemical composition of the expanding fireball produced in a heavy ion collision .



Quasiparticles have a strong effect on the ratio of fermions over gluons number:
Fermions are produced *faster*, and in a *larger amount* than in the case in which *massles particles* are considered.



Improvement of the results including the Polyakov loops is under investigation.

Conclusions and Outlook

- Yang-Mills Thermodynamics is well understood in terms of QPs and condensates of $Z(3)$ lines
- Results are relevant for HICs simulations: QP mass and Polyakov loops affect thermalization

- Introducing dynamical quarks (*wip*)
- Computation of transport coefficients
- Computation of susceptibilities
- QPs, $Z(3)$ lines and transport code

Acknowledgements

It is a pleasure of mine to acknowledge:

P. Alba, P. Castorina, S. Plumari, C. Ratti and V. Greco

for the fruitful collaboration. I also acknowledge discussions with:

M. Frasca and D. Zappalà.

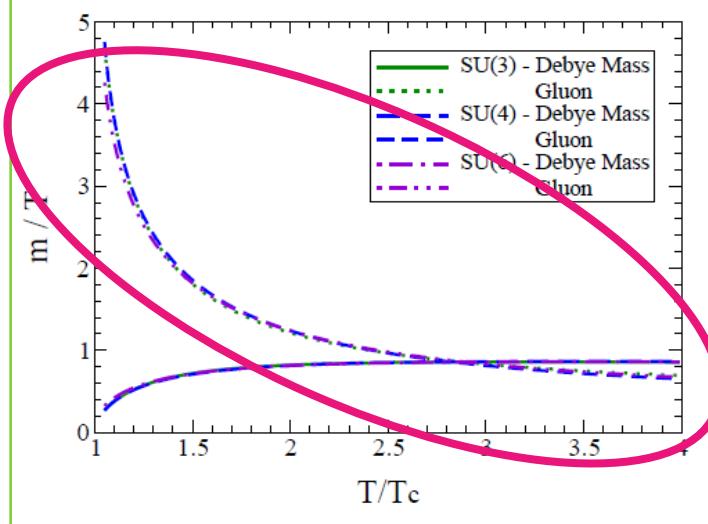


Chi ha paura muore ogni giorno. Chi non ha paura muore una sola volta.
(Who is afraid dies every day. Who is not afraid dies only once.)

P. Borsellino (19 Gennaio 1940 – 19 Luglio 1992)

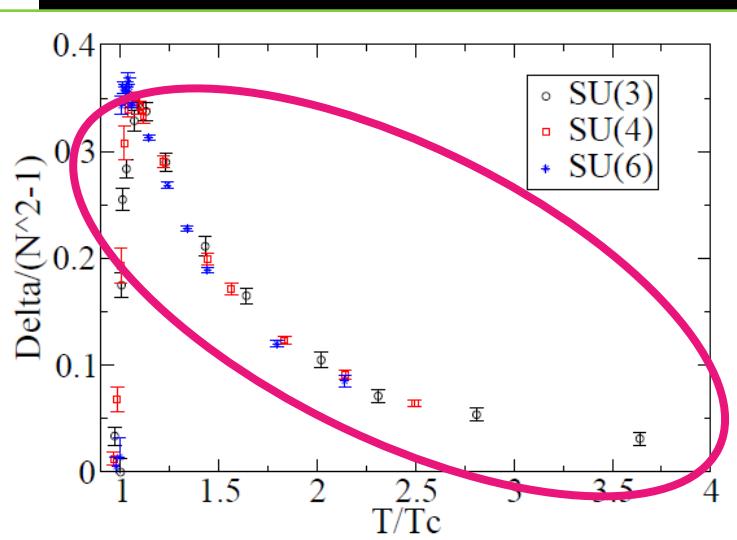
Transverse Quasiparticles and N_c^{2-1} scaling

P. Castorina *et al.*, Eur. Phys. J. C71 (2011)



Thermal mass turns out to be independent
on the number of colors. Noticing that:

$$\Delta(T) \approx \frac{N_c^2 - 1}{6\pi^2} \frac{m^2}{T^2} K_1(m/T) \left[\frac{m}{T} - \left(\frac{dm}{dT} \right) \right]$$



one has the simple interpretation of the N_c^{2-1}
scaling observed on the lattice.

N_c^{2-1} scaling

gluon mass independent on N_c

Lattice data from:
M. Panero, Phys. Rev. Lett. 103 (2009)