

Noise lower limit for Cluster Counting front-end electronics

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Update on detection efficiency of cluster counting algorithms using Garfield simulated data sets

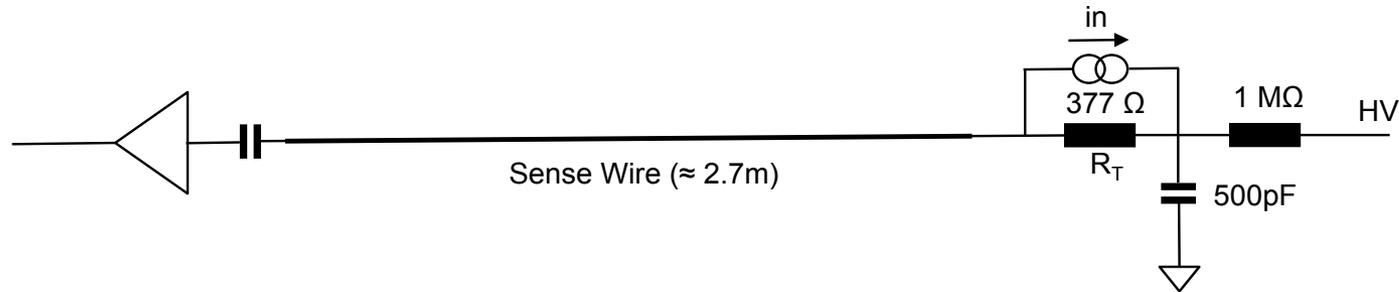
- *Lower limit for front-end noise in Cluster Counting scenario*
- *Efficiency estimation of Cluster Counting algorithms based on GARFIELD simulation*
- *Possible implementation of on-detector/off-detector interconnections*
- *Power supply requirements estimation*

Noise lower limit for Cluster Counting front-end electronics

Cluster Counting technique can improve particles identification in SuperB DCH

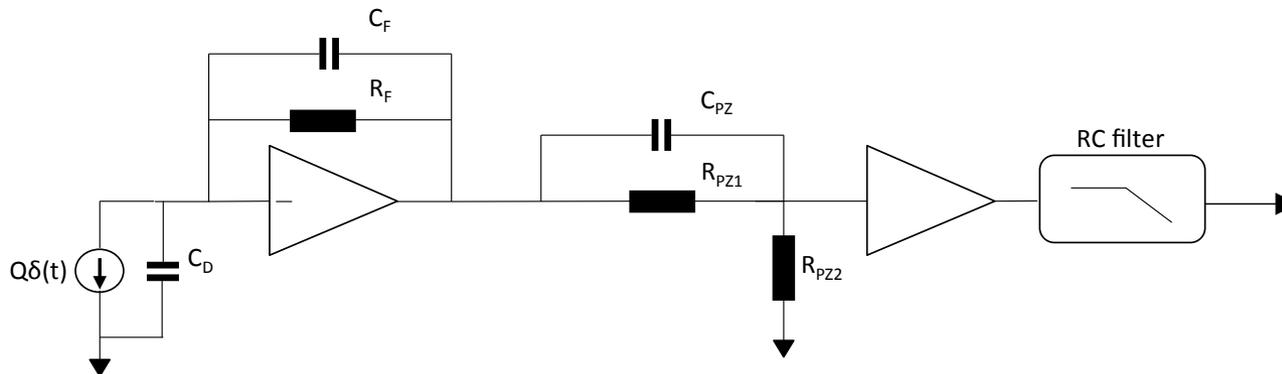
- *The technique is based on primary ionization cluster detection and requires:*
 - *Slow drift velocity gas mixtures (es 90% He – 10% Iso)*
 - *Quite high gas gain ($> 10^5$)*
 - *Fast amplifiers*
 - *Fast sampling devices ($> 1\text{GSPS}$)*
 - *Correct termination of the sense wire (to avoid signal reflection)*
- *Assuming the chamber sense wire as a lossless transmission line and discarding external noise pick-up the main noise sources are the termination resistor and the preamplifier intrinsic noise*
- *At the moment there is no a definitive decision about the readout chain , nevertheless termination resistor noise contribution can be evaluated by means of the Equivalent Noise Charge (ENC) contribution of a typical readout chain.*

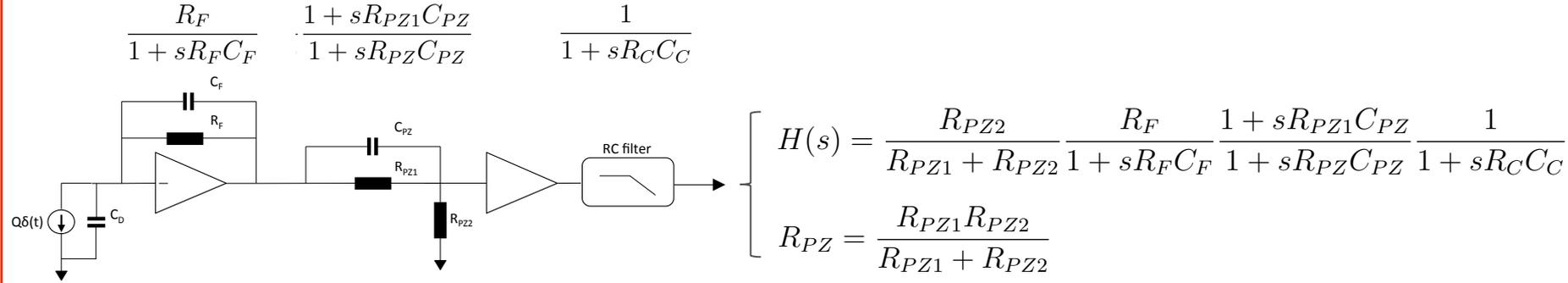
Termination resistor ENC contribution evaluation



ENC = input signal magnitude that generates a preamplifier output signal equal to the output rms noise

- *Termination resistor noise contribution can be evaluated both in frequency domain (direct transfer function calculation) and in time domain (using system weighting function)*
- *Generic front-end chain made of preamplifier, pole-zero cancellation network and filter has been used*





Assuming $R_FC_F = R_{PZ1}C_{PZ} \rightarrow H(s) = \frac{R_{PZ2}R_F}{R_{PZ1} + R_{PZ2}} \frac{1}{1 + sR_{PZ}C_{PZ}} \frac{1}{1 + sR_C C_C}$

Choosing low-pass filter time constant $R_{PZ}C_{PZ} = R_C C_C = \tau \rightarrow H(s) = \alpha\tau \cdot \frac{1}{(1 + s\tau)^2}$

Where $\alpha\tau = \frac{R_{PZ2}R_F}{R_{PZ1} + R_{PZ2}} = \frac{R_{PZ2}R_{PZ1}}{R_{PZ1} + R_{PZ2}} \frac{1}{R_{PZ1}} R_F \frac{C_{PZ}}{C_{PZ}} = \frac{R_F}{R_{PZ}C_{PZ}} \tau$

$s=i\omega \rightarrow T(j\omega) = \alpha\tau \cdot \frac{1}{(1 + j\omega\tau)^2}$

RMS output noise voltage due to termination resistor (noiseless preamplifier) $\rightarrow V_n^2(rms) = i_n^2 \alpha^2 \tau^2 \int_0^\infty |T(j\omega)|^2 df \left[i_n = \sqrt{\frac{4KT}{R_T}} \right]$

Changing the integration variable $\rightarrow z = \omega\tau = 2\pi f\tau$ and extending the integration range to $-\infty$

$$V_n^2(\text{rms}) = i_n^2 \alpha^2 \tau^2 \frac{1}{4\pi\tau} \int_{-\infty}^{\infty} \frac{dz}{(1+z^2)^2} \rightarrow \frac{\pi}{2}$$

RMS output noise voltage due to termination resistor $\rightarrow V_n^2(\text{rms}) = \frac{4KT}{R_T} \frac{1}{4\pi\tau} \tau^2 \alpha^2 \frac{\pi}{2} = \frac{4KT}{R_T} \frac{1}{8} \tau \alpha^2$

$H(s)$ Laplace antitransform $\rightarrow \mathcal{L}^{-1}\left(\alpha\tau \frac{1}{\tau^2} \frac{1}{(1/\tau + s)^2}\right) = \alpha \frac{t}{\tau} e^{-t/\tau}$

To evaluate system ENC the square root of rms output voltage must be normalized to the peak output voltage generated by a unit test pulse $\delta(t)$ $\rightarrow V_{\text{peak}} = \alpha \cdot \frac{1}{e}$

Assuming a peaking time ≈ 3 ns the ENC due to 377 Ω termination resistor is

$$ENC = e \cdot \sqrt{\frac{kT}{R_T} \frac{1}{2}} \cdot \tau \simeq 0.35 \text{ fC} \simeq 2200 \text{ erms}$$

Termination resistor ENC contribution evaluation – time domain calculation (I)

System output noise variance can be estimated starting with noise spectral density and system time response as shown by Radeka* thanks to the Parseval's theorem

$$\text{Parseval's theorem} \rightarrow \int_{-\infty}^{\infty} h^2(t) dt = \frac{1}{2\pi} \int_{-\infty}^{\infty} |H(j\omega)|^2 d\omega = 2 \int_0^{\infty} |H(2\pi jf)|^2 df$$

$$\sigma^2 = \frac{1}{2} W_0 \int_{-\infty}^{\infty} h^2(t) dt$$

$W_0 =$ input white noise (thermal noise due to resistor connected to the sense wire $\sqrt{\frac{4KT}{R_T}}$)

$h(t) =$ system impulse response ($\mathcal{L}^{-1}(\alpha\tau \frac{1}{\tau^2 (1/\tau + s)^2}) = \alpha \frac{t}{\tau} e^{-t/\tau}$)

$$\text{Evaluating the system impulse response for } t \geq 0 \rightarrow \sigma^2 = \frac{1}{2} W_0 \int_0^{\infty} \alpha^2 \left(\frac{t}{\tau}\right)^2 e^{-2\frac{t}{\tau}} dt = \frac{1}{2} \frac{4KT}{R_T} \frac{\alpha^2 \tau}{4}$$

$$\text{Normalizing to the peak voltage} \rightarrow ENC^2 = \frac{1}{2} \frac{4kT}{R_T} \frac{e^2}{4} \tau = \frac{1}{2} \frac{kT}{R_T} e^2 \tau \quad \text{As shown shown before}$$

ENC decrease for small peaking times but

* Low Noise Techniques in Detector - Radeka - Ann. Rev. Nud. Parl. Sci. 1988. 38: 217-77

More generally there are 2 basic noise sources: input noise current (i_n) and input noise voltage (v_n)

$$\text{Time domain} \quad \longrightarrow \quad ENC^2 = i_n^2 \tau_S F_i + C^2 v_n^2 \frac{F_v}{\tau_S}$$

F_i, F_v = form factors (shape of the pulse)

τ_S = peaking time

i_n, v_n = noise input current and voltage

C = total input capacitance (detector + preamp + stray)

$$\text{Termination resistor = noise current source} \quad \longrightarrow \quad ENC_P^2 = i_n^2 \tau_S F_i$$

F_i = dimensionless parameter function of the CR = nRC filter order $\longrightarrow F_i = \frac{1}{2T_S} \int_{-\infty}^{\infty} |W(t)|^2 dt$

F_i (time invariant filters) = normalized system input response

T_S = system shaping factor

General solution for CR-nRC unipolar shaping factor can be found in literature

Es : Blum - Riegler - Rolandi Particle Detection with drift Chamber

$$\begin{aligned} F_i &= \frac{1}{2} \left(\frac{e}{2n} \right)^{2n} (2n - 1)! \\ F_v &= \frac{1}{2} \left(\frac{e}{2n} \right)^{2n} n^2 (2n - 2)! \end{aligned}$$

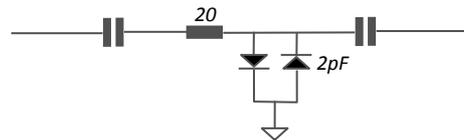
$$ENC_n^2 = i_n^2 \tau_S F_i + v_n^2 F_v \frac{C_T^2}{\tau_S}$$

C_T is the sum of capacitance at the preamplifier input

$$F_i = \frac{1}{2} \left(\frac{e}{2n} \right)^{2n} (2n - 1)!$$

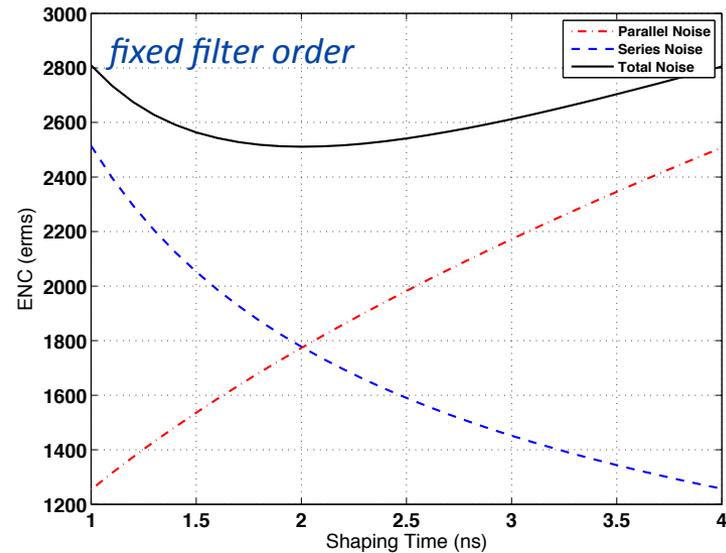
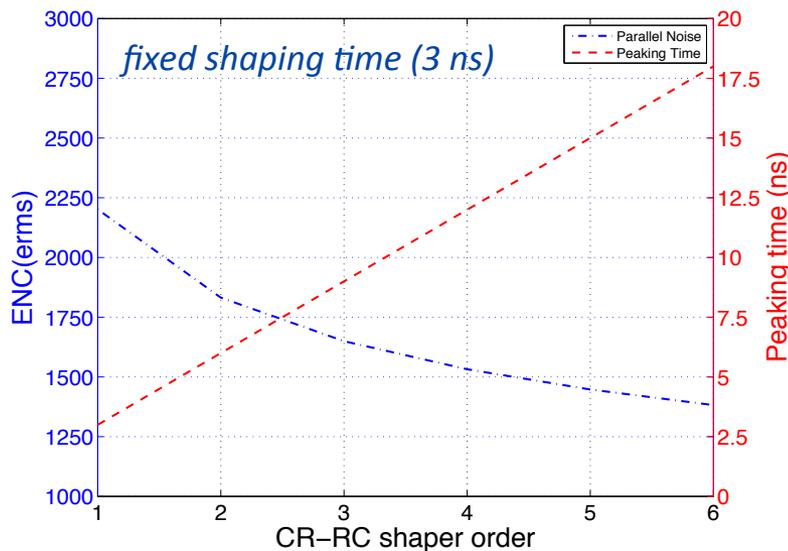
$$F_v = \frac{1}{2} \left(\frac{e}{2n} \right)^{2n} n^2 (2n - 2)!$$

To simplify calculation only preamplifier protection circuit against discharges will be considered



+ 21 pF (wire parasitic capacitance) and $v_n^2 = 4KTR$

noiseless preamplifier



- Wire termination resistor is one of the main noise sources of the system (≈ 2200 *erms* @ 3ns peaking time)
- An equal amount of noise can be estimated for a high bandwidth preamplifier thus the *system total amount of noise is about 3100 erms ≈ 0.5 fC*
ES: LNF proto2 gain ≈ 8 mV/fC (@ 250 MH BW) \rightarrow Noise ≈ 4 mV rms (≈ 26 mV pp)
- Single electron cluster charge collected on the wire @ nominal gas gain = 10^5

$$10^5 \times 0.5 \times 0.25 \times 1.6 \times 10^{-19} \approx 2 \text{ fC} \rightarrow 1 \text{ fC}$$

charge division due to
termination resistor

charge collected
percentage
(approximation)

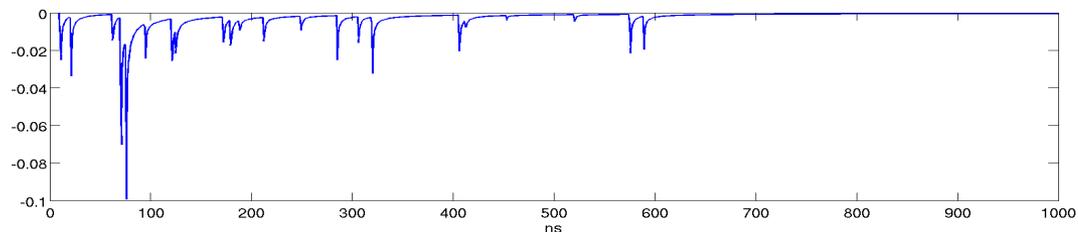
gas gain
fluctuation
(upper limit)

DCH operated @ 10^5 nominal gas gain corresponds to a SNR ≈ 2

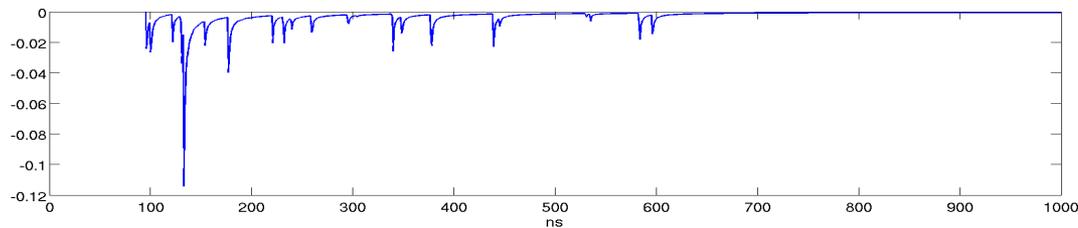
*Update on detection efficiency of cluster
counting algorithms using Garfield simulated
data sets*

Remind from Dec 2011 WS: step 1: Garfield Outputs Waveforms samples

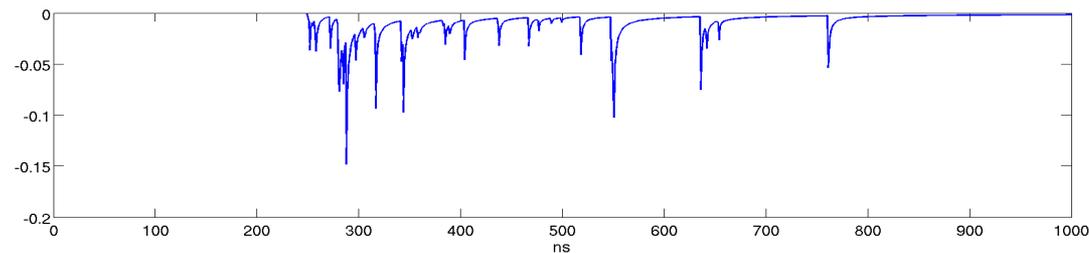
Garfield output (Gas gain 3×10^5 – preamp gain $\approx 8 \text{ mV/fC}$)



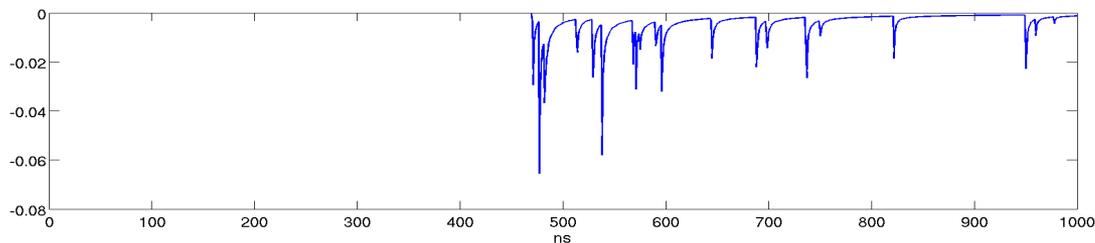
Impact parameter = 0 mm



Impact parameter = 2.5 mm

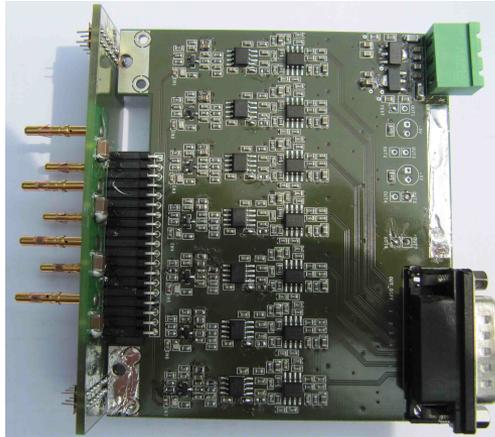


Impact parameter = 5.0 mm



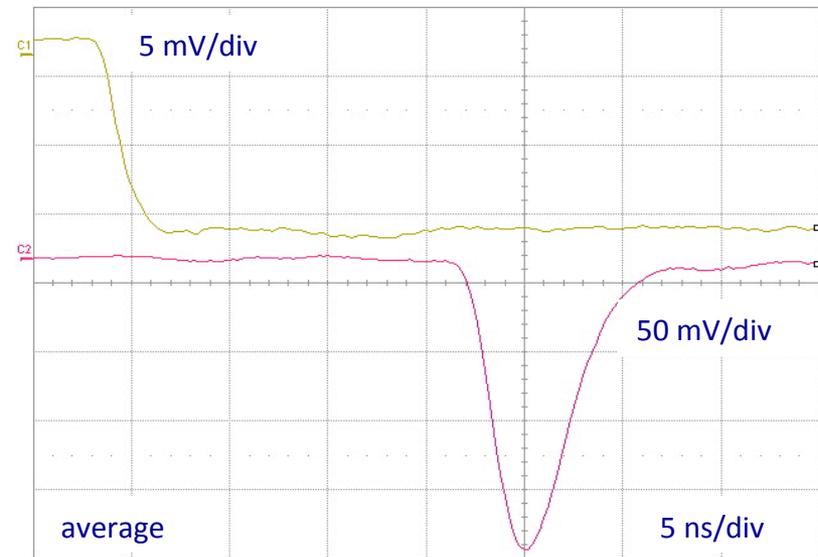
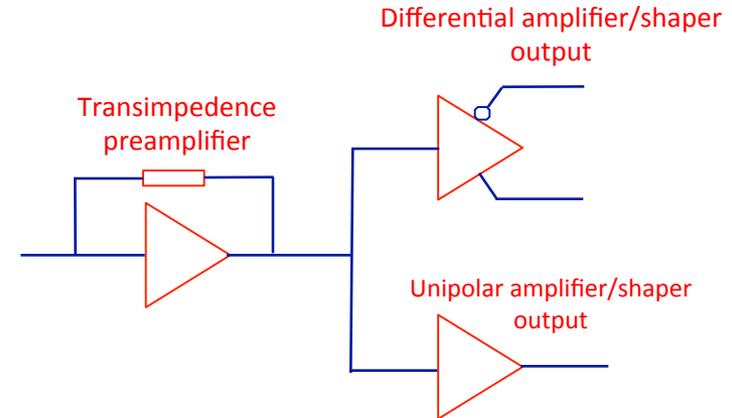
Impact parameter = 7.5 mm

Preamplifier Board



Preamplifier main features

- Number of channels : 7
- $Z_{in} \approx 60 \Omega$
- Gain $\approx 8.8 \text{ mV/fC}$ ($C_D = 0 \text{ pF}$)
- Linearity $< 1\%$ (1-100 fC)
- Noise $\approx 3000 \text{ erms @ 250 MHz BW}$ ($C_D = 24 \text{ pF}$)
- Rise time $\approx 2.4 \text{ ns}$ ($C_D = 24 \text{ pF}$)
- Fall time $\approx 2.4 \text{ ns}$ ($C_D = 24 \text{ pF}$)
- Unipolar & Differential outputs ($50 \Omega - 110 \Omega$)
- Test input
- Supply Voltage : + 7V (310 mA) - 7V (190 mA)
- Power Dissipation : 490 mW/ch



1.8 pF injecting capacitance

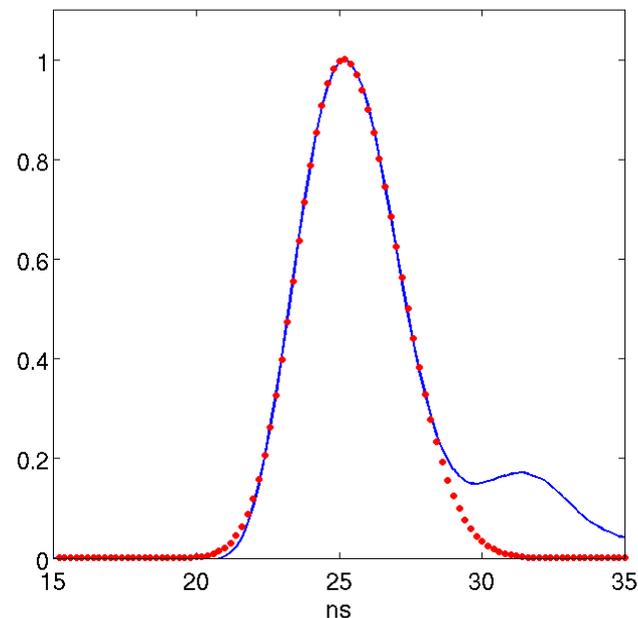


- Preamplifier board has been connected to the chamber and pulsed through a 1.8 pF internal capacitor.
- Output pulse has been fitted to find out the preamplifier impulse response.

Fitting function:

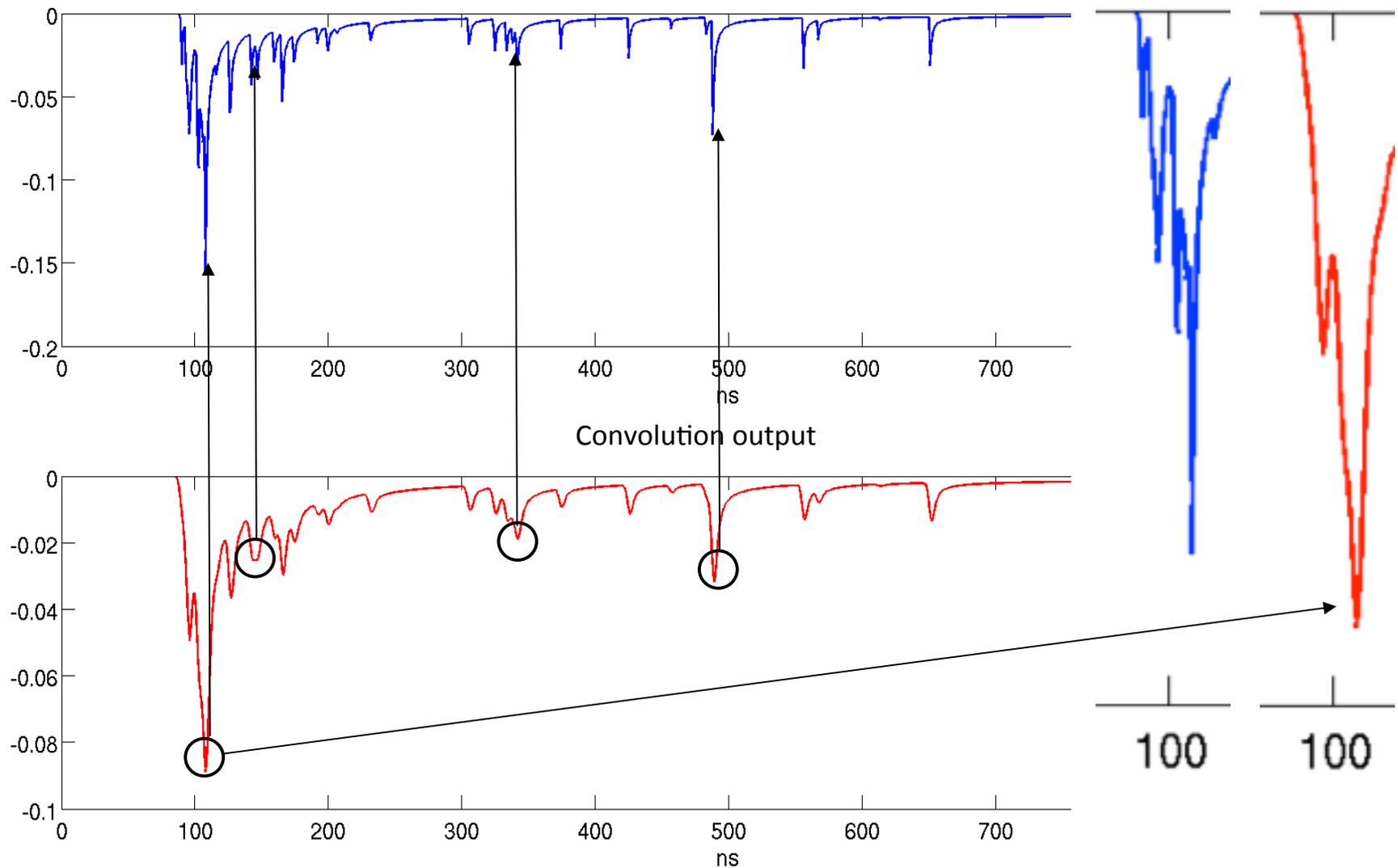
$$h(t) = a_1 e^{-\left(\frac{t-b_1}{c_1}\right)^2} + a_2 e^{-\left(\frac{t-b_2}{c_2}\right)^2}$$

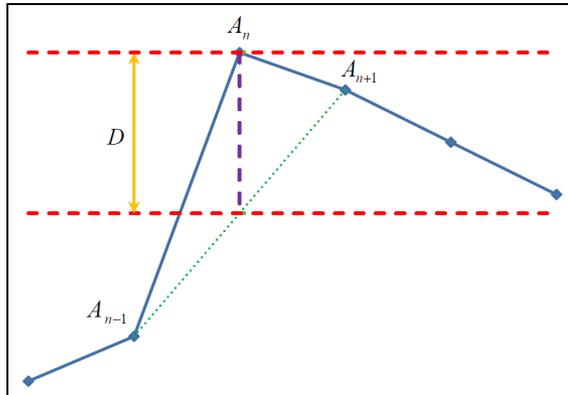
a_1	0.479
b_1	24.367
c_1	1.797
a_2	0.691
b_2	25.983
c_2	2.305



Remind from Dec 2011 WS: Preamplifier response convolution example

Garfield output (Gas gain 3×10^5 – preamp gain $\approx 8 \text{ mV/fC}$)



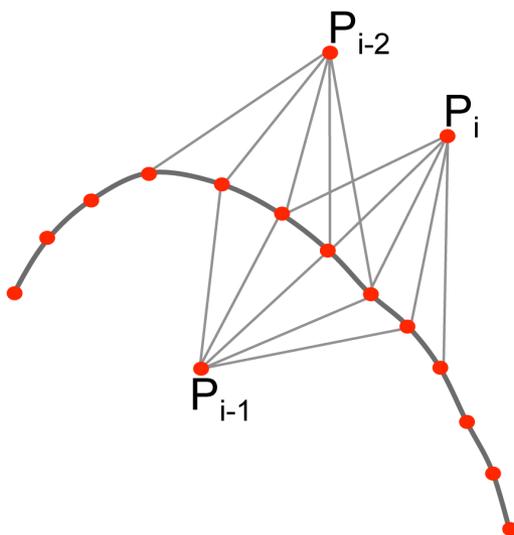


Peak Detecting algorithm

$$D = A_n - \left(\frac{A_{n-1} + A_{n+1}}{2} \right) \geq 3\sigma_d \quad \text{Peak Found Condition}$$

$A_{n-1}, A_n, A_{n+1} \rightarrow$ consecutive samples
 $\sigma_d \rightarrow$ rms noise (rms)

Proposed by Luigi Cappelli
 on behalf of CLUTIM Group



Slope Detection Algorithm

$$P_i = A_i - \frac{\sum_{n=1}^4 A_{i-n}}{4}$$

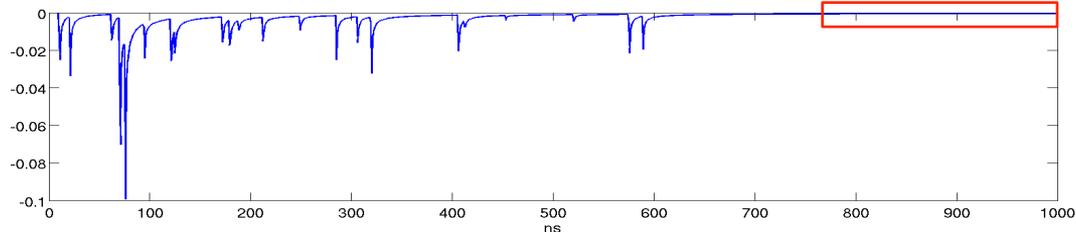
$$C_1 = P_i - P_{i-1} \quad C_2 = P_{i-1} - P_{i-2} \quad C_3 = P_i - P_{i-2}$$

$$(C_1 < -Thr) \text{ AND } (C_2 < -Thr) \text{ AND } (C_3 < -3Thr)$$

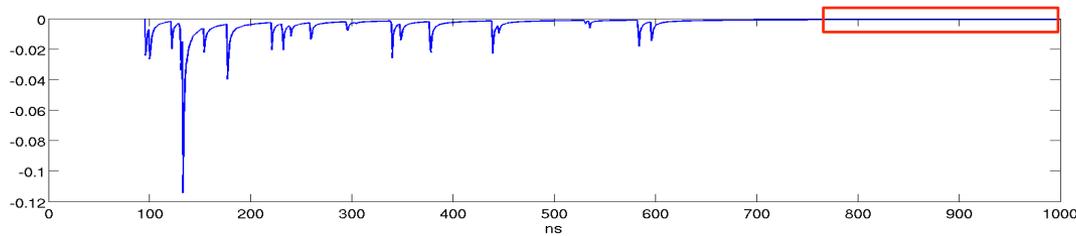
$A_i \rightarrow$ Data samples $Thr \rightarrow$ Threshold

Dead time asserted to avoid extra counting

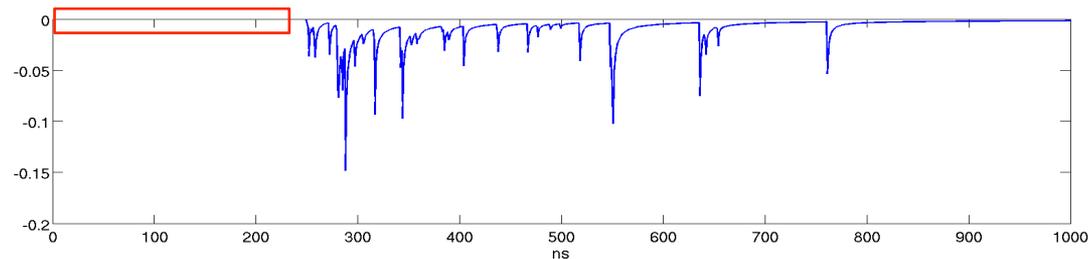
Noise RMS evaluated off-signal



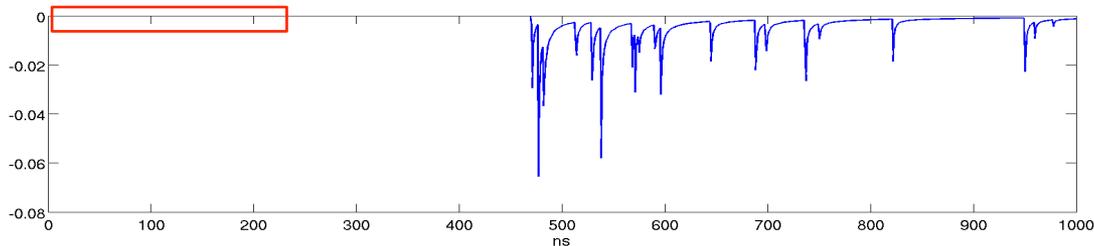
Impact parameter = 0 mm



Impact parameter = 2.5 mm



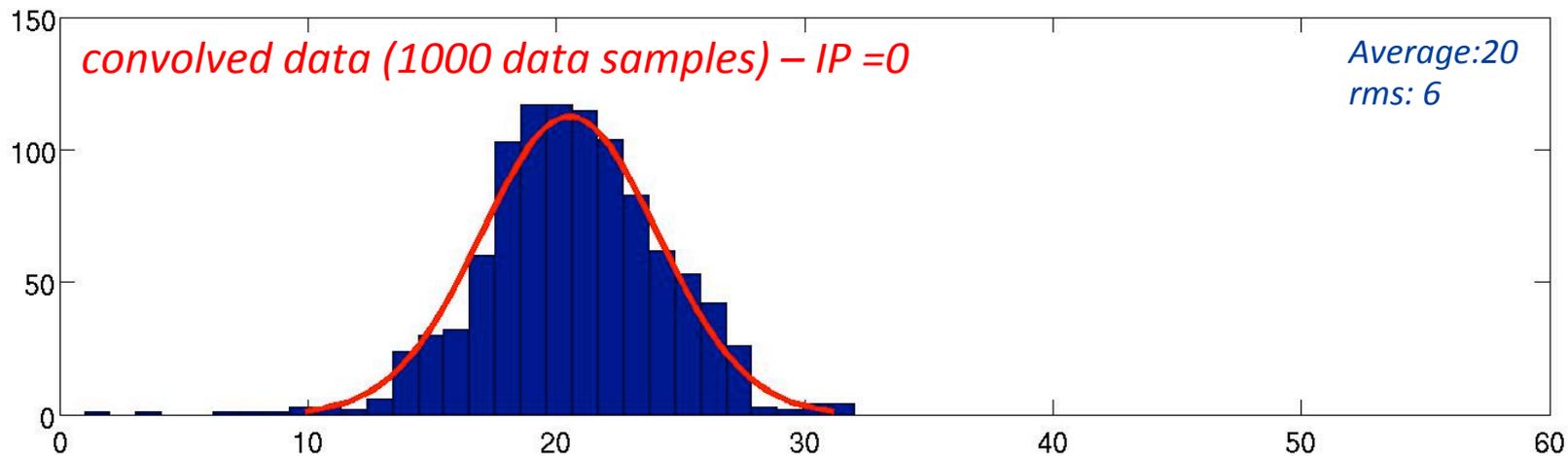
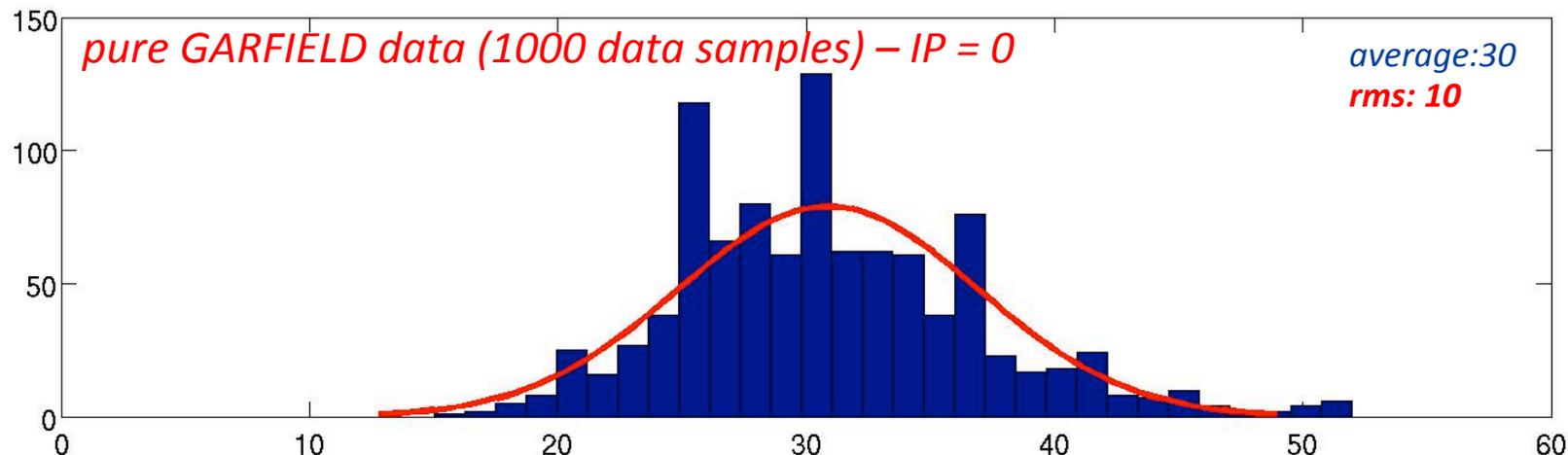
Impact parameter = 5.0 mm



Impact parameter = 7.5 mm

Remind from Dec 2011 WS – step 6: preamplifier convolution effect

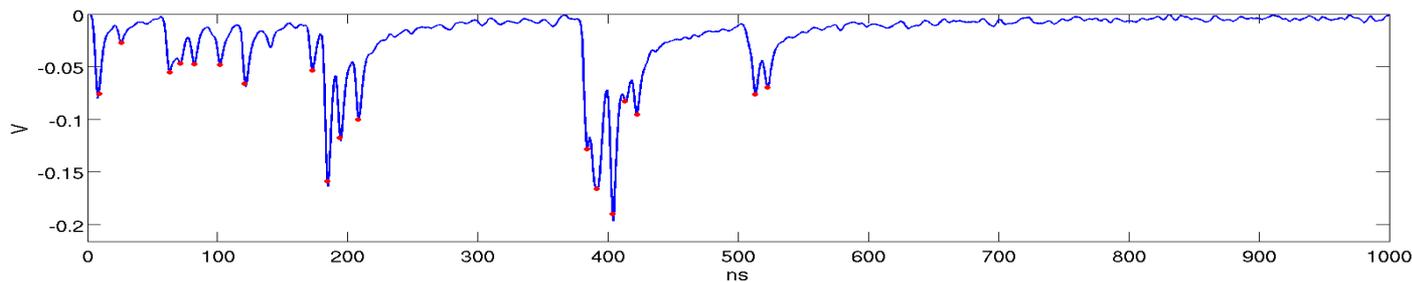
About 30% loss efficiency due to preamplifier response convolution
(peak finding method)



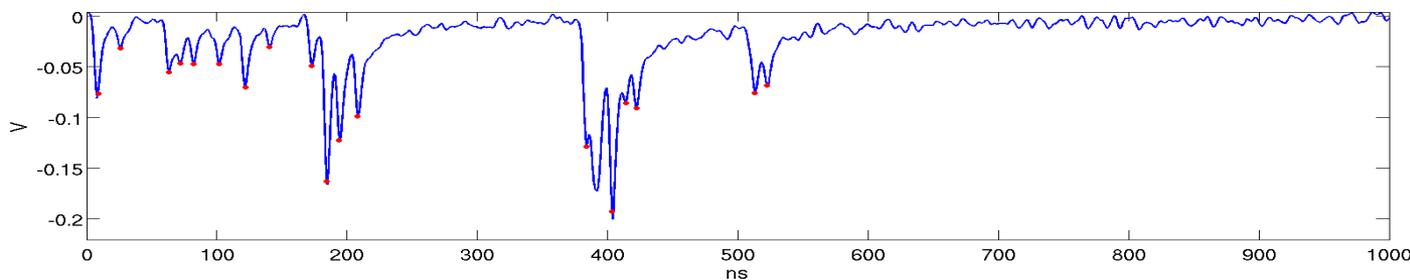
The same result is obtained adding only noise to the pure GARFIELD data

Remind from Dec 2011 WS – step 7: Adding noise and convolution

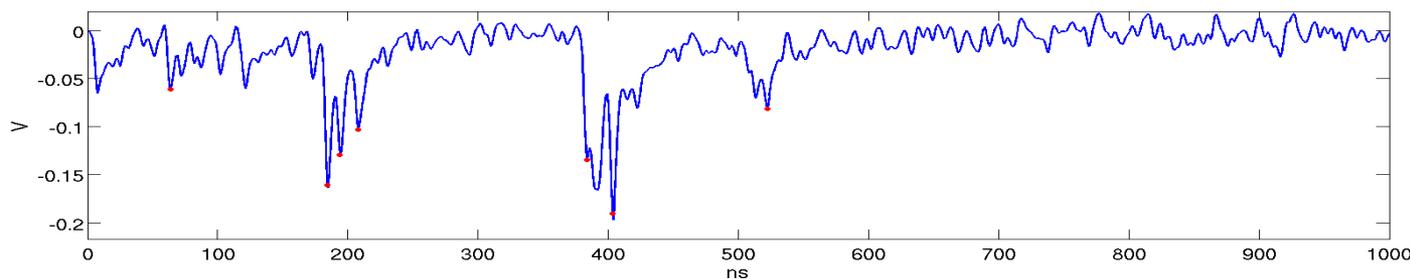
SNR evaluated considering single electron cluster average amplitude (~10mV)



SNR=10



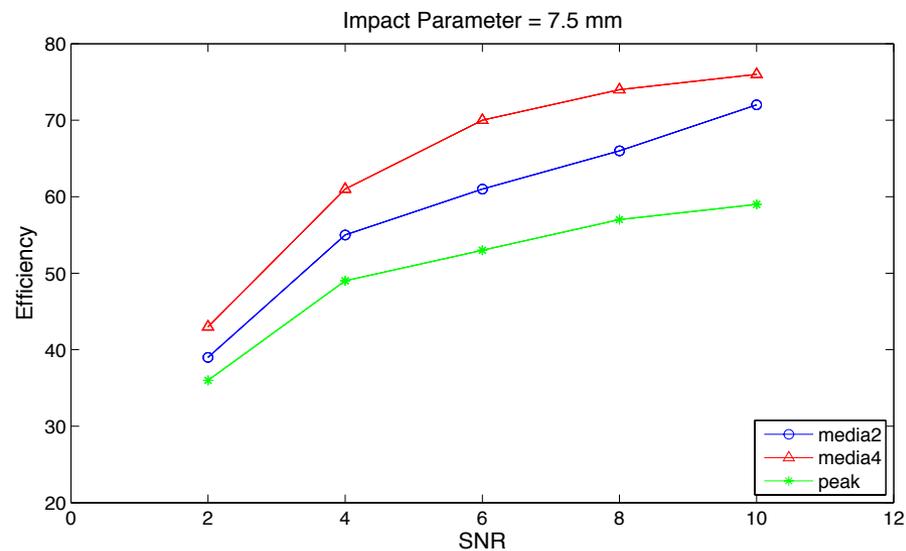
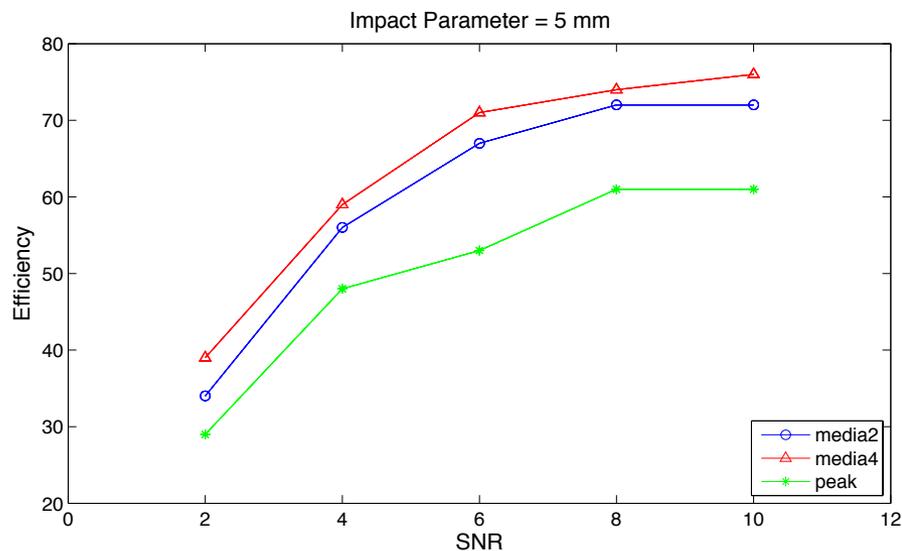
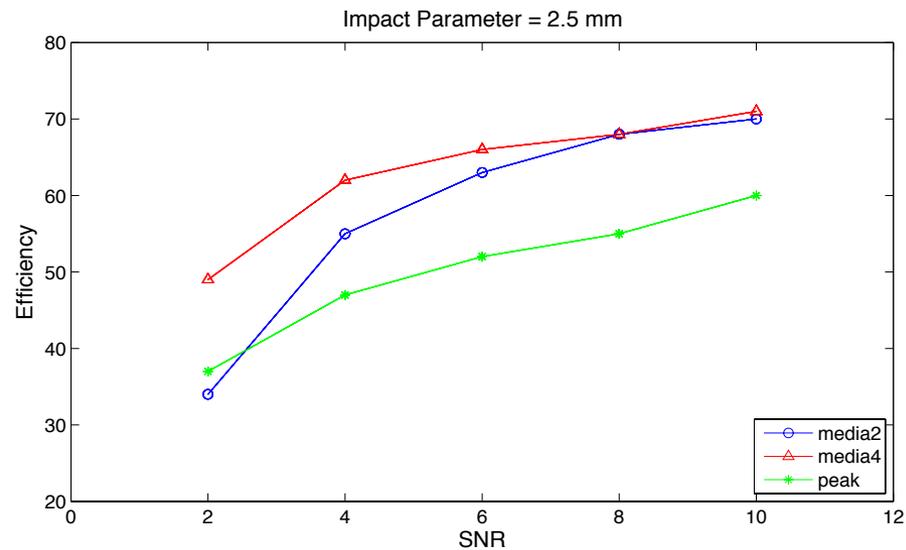
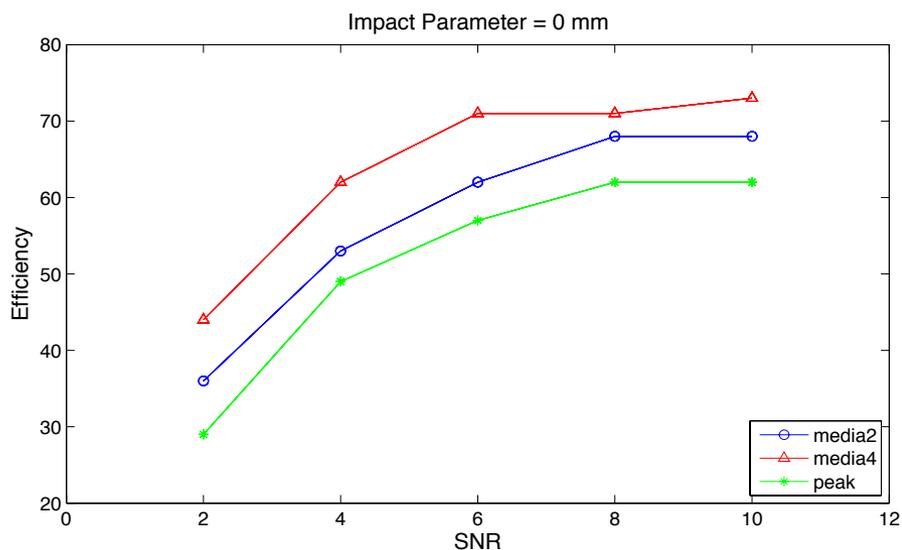
SNR=6



SNR=2

SNR=Signal Amplitude/Noise RMS

Cluster detecting algorithms comparison – Threshold @ 2.5σ



- *Operating region around SNR = 8 can be inferred*
- *External noise pickup reduces efficiency because higher thresholds must be required*

A cluster counting feasibility study using two algorithms that can be implemented in a FPGA has been carried out.

The analysis have been performed using data sets based on GARFIELD simulations at different impact parameters.

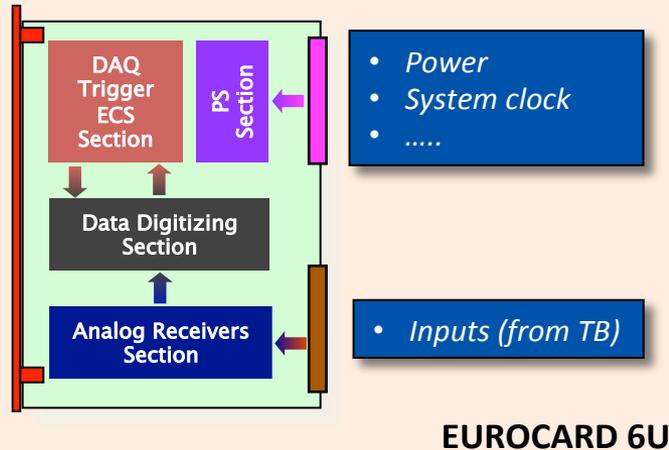
Results show that preamplifier response convolution causes a loss of about 28% in detected clusters for different impact parameters.

The addition of Gaussian noise with different SRN increases the counting inefficiency from 40% (SNR=10) to about 70% (SNR=2) for the peak finding algorithm. Slope detection method is less sensitive to noise, anyway chamber must be operated with high gas gain to guarantee a $SNR \geq 8$ (taking into account of external picked-up noise)

Peak detecting algorithm can be easily implemented in a FPGA, but is more sensitive to noise

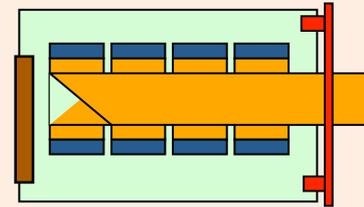
On/Off detector electronics interconnections (I)

Data Conversion Board

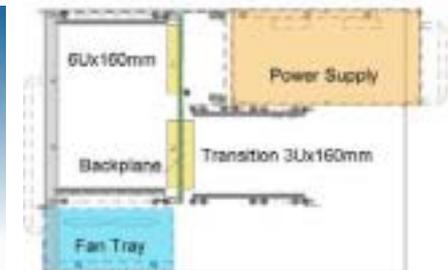


TB I/O signals

- Input Signals (from on-detector)
- On-Detector PS
- Test Pulse (to o-detector)



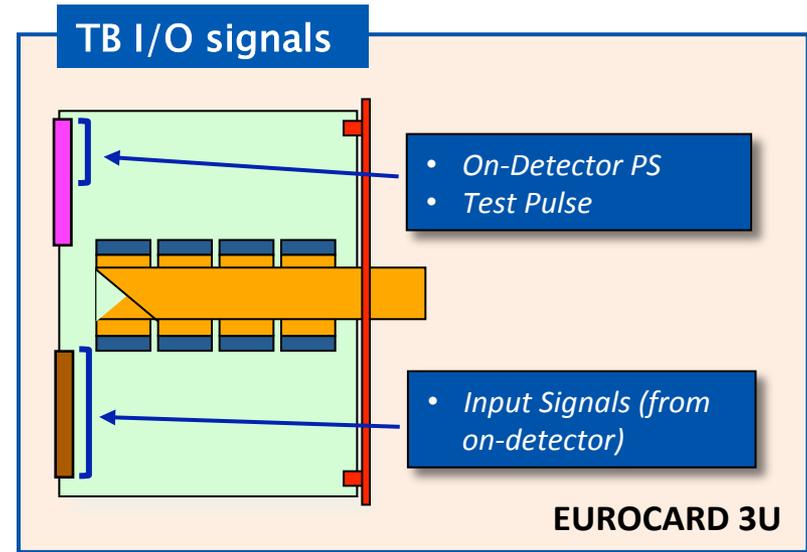
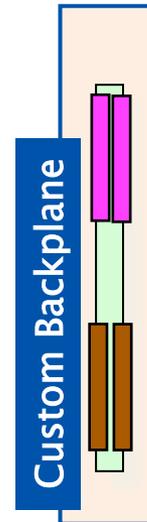
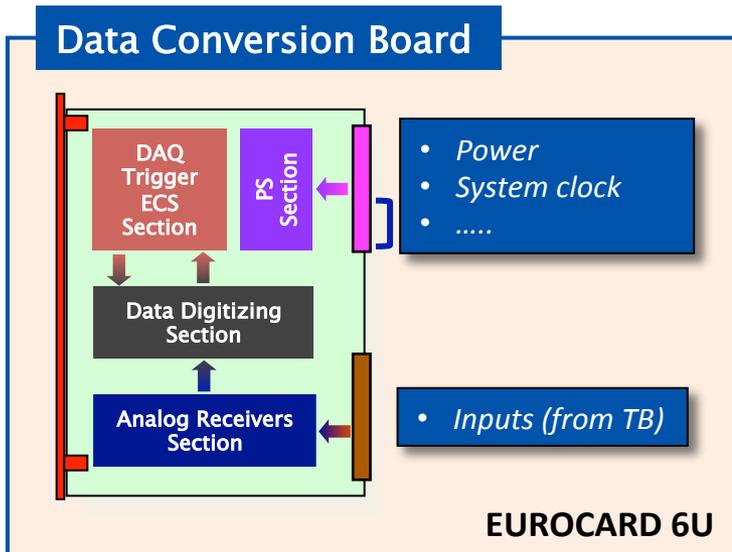
- Avoid on-detector cables running in front of crates
- Avoid disconnecting signal cables to change a readout board



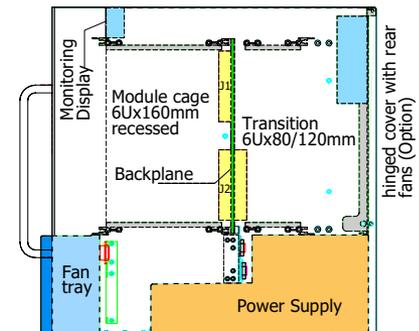
- 96 pin connectors (3 rows x 32 pins) can receive only 32 signals (twisted pairs or coax) (we need spare pins for on-detector PS and pulsing)
- NO controlled impedance (OK for charge measurements – Tested in KLOE experiment)

Crate Version	Backplane	+5V	+12V	-12V
VME 6021-611	VME/VME64	115A	23A	23A
VME 6021-613	VME/VME64	230A	23A	23A
VME 6021-614	VME/VME64	345A	23A	23A
VME 6021-620	VME/VME64	115A	46A	46A
VME 6021-621	VME/VME64	230A	46A	46A
VME 6021-622	VME/VME64	345A	46A	46A

On/Off detector electronics interconnections (II)

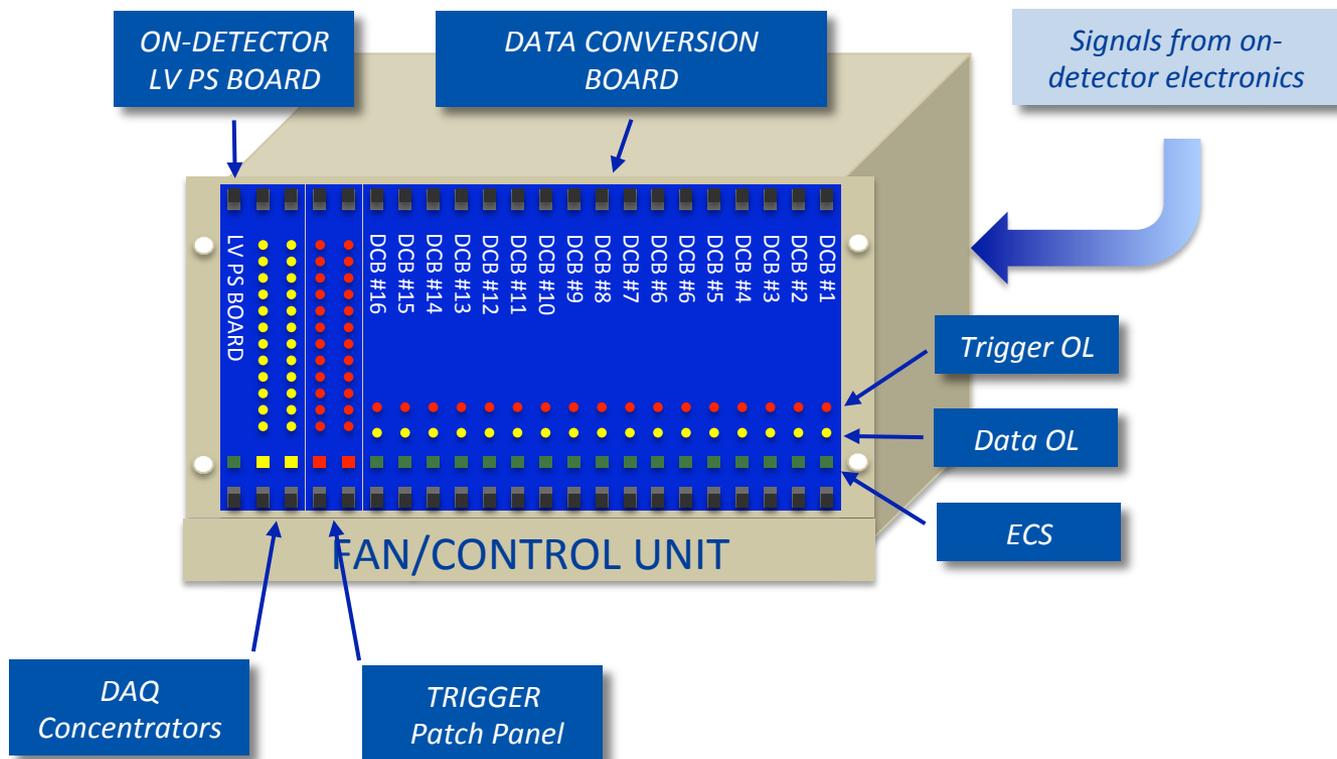


The solution allows to receive up to 64 signals (twisted pairs or coax) but use NON standard PS



Crate Version	Backplane	+5V	+12V	-12V
VME 4503-611	VME/VME64	115A	23A	23A
VME 4503-613	VME/VME64	230A	23A	23A
VME 4503-614	VME/VME64	345A (special)	23A	23A

On/Off detector electronics interconnections (III)



If can use standard VME crates (probably) we do not need external power supply

Power Supply Requirements

<i>Truncated Mean</i>	<i>Cluster Counting</i>
Single channel preamplifier	Single channel preamplifier
8 mA @ 4 V	30 mA @ 5 V

<i>Truncated Mean</i>		<i>Cluster Counting</i>	
<i>Channels/board</i>	<i>Number of Crates</i>	<i>Channels/board</i>	<i>Number of Crates</i>
64	10	16	40
32	20		

	<i>Truncated Mean (single crate)</i>		<i>Cluster Counting (single crate)</i>
	16x32 chs/board RO	16x64 chs/board RO	16x16 chs/board
<i>ON-DETECTOR</i>	512 channels	1024 channels	256 channels
	4.1 A @ 5 V	8.2 A @ 5 V	7.68 A @ 6V
<i>OFF-DETECTOR</i>	16 RO boards + 2 concentrators	16 RO boards + 2 concentrators	16 RO boards + 2 concentrators
	72 A @ 5 V 3.2 A @ 12 V 3.2 A @ 12 V	120 A @ 5 V 3.2 A @ 12 V 3.2 A @ 12 V	120 A @ 5 V 3.2 A @ 12 V 3.2 A @ 12 V