

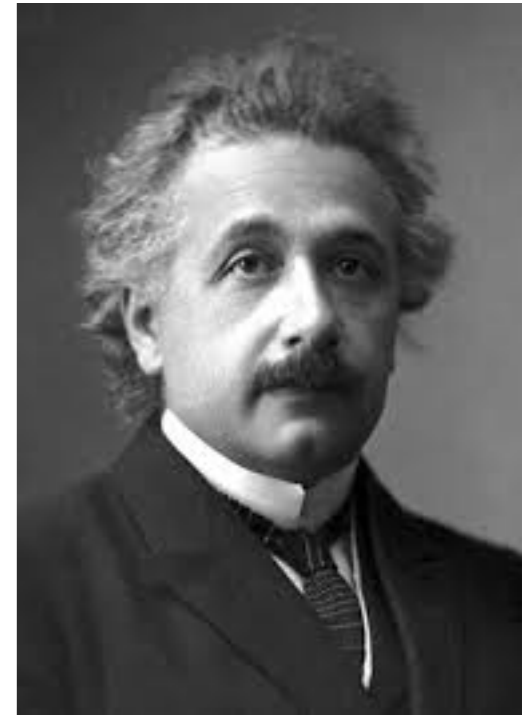
# Natural SUSY, string landscape and implications for LHC searches



Howard Baer  
University of Oklahoma

INFN Frascati talk  
April 8, 2024

twin pillars of guidance:  
naturalness & simplicity



“The appearance of fine-tuning in a scientific theory is like a cry of distress from nature, complaining that something needs to be better explained”

S. Weinberg

“Everything should be made as simple as possible, but not simpler”

A. Einstein

We have seen from LHC: the Standard Model rules  
at  $E \sim 100\text{--}200$  GeV!

nonetheless, it is hardly the end of story since  
the SM is beset by several finetuning problems:

- Gauge hierarchy: how can weak scale be so much smaller than GUT/Planck scale?
- Strong CP problem (QCD): why is QCD theta parameter so small  $< \sim 10^{-10}$
- Cosmological constant:  $\rho_{vac} \sim (0.003 \text{ eV})^4 \ll m_P^4$

The SM is beset by several finetuning problems:  
**most plausible solutions to date**

- Gauge hierarchy: how can weak scale be so much smaller than GUT/Planck scale? **SUSY**
- Strong CP problem (QCD): why is QCD theta parameter so small  $\sim 10^{-10}$  **axion**
- Cosmological constant:  $\rho_{vac} \sim (0.003 \text{ eV})^4 \ll m_P^4$

**anthropic vacua selection from multiverse/string vacua**

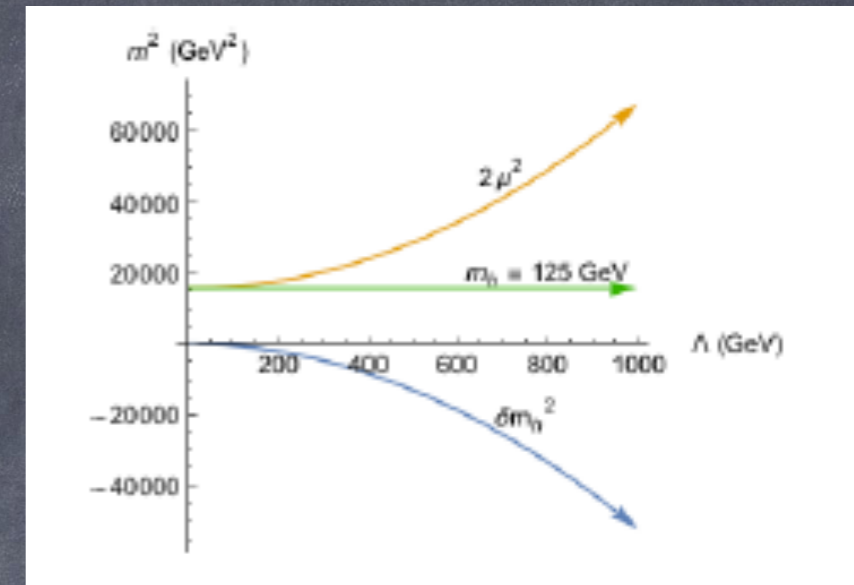
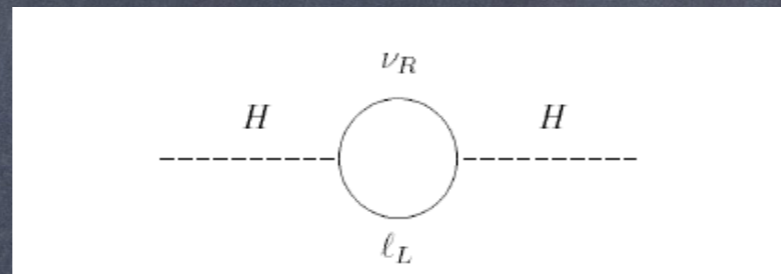
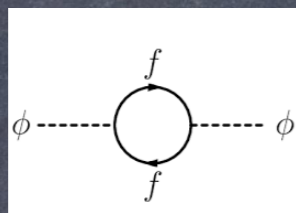
Each of these solutions affects  
phenomenology in a profound way

# Hierarchy of scales problem in the SM

Biggest conundrum of SM: why is Higgs mass so small?

1. There is a lowest order mass term

2. Quantum corrections diverge quadratically with energy scale of new physics



$$m_{H_{SM}}^2 = 2\mu^2 + \delta m_{H_{SM}}^2$$

$$\delta m_{H_{SM}}^2 \simeq \frac{3}{4\pi^2} \left( -\lambda_t^2 + \frac{g^2}{4} + \frac{g^2}{8 \cos^2 \theta_W} + \lambda \right) \Lambda^2$$

3. To avoid the pathology of fine-tuning, SM must be valid only to  $\Lambda \sim 1 \text{ TeV}$

4. Need theory which is free of quadratic divergences to extend e.g. to GUT/Planck scale

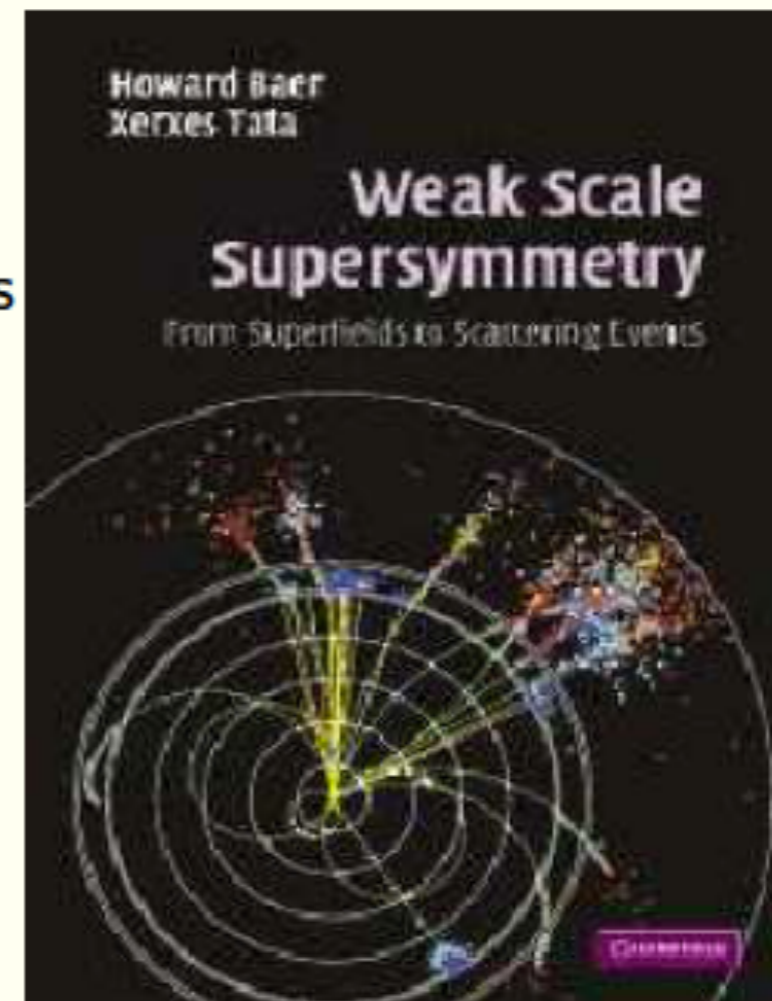
# Supersymmetry: all quadratic divergences cancel!

## Weak Scale Supersymmetry

HB and X. Tata

Spring, 2006; Cambridge University Press

- ★ Part 1: superfields/Lagrangians
  - 4-component spinor notation for exp'ts
  - master Lagrangian for SUSY gauge theories
- ★ Part 2: models/implications
  - MSSM, SUGRA, GMSB, AMSB, ...
- ★ Part 3: SUSY at colliders
  - production/decay/event generation
  - collider signatures
  - $R$ -parity violation



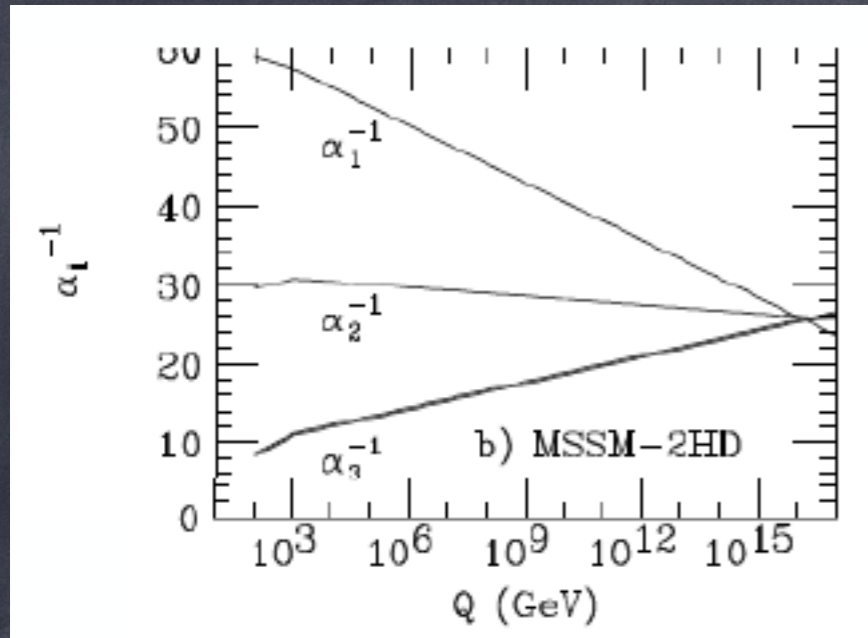
## Minimal Supersymmetric Standard Model (MSSM)

- ★ Adopt gauge symmetry of Standard Model:  $SU(3)_C \times SU(2)_L \times U(1)_Y$ 
  - gauge boson plus spin  $\frac{1}{2}$  gaugino  $\in$  gauge superfield
- ★ SM fermions  $\in$  chiral scalar superfields:  $\Rightarrow$  scalar partner for each SM fermion helicity state
  - electron  $\Leftrightarrow \tilde{e}_L$  and  $\tilde{e}_R$
- ★ *two* Higgs doublets to cancel triangle anomalies:  $H_u$  and  $H_d$
- ★ add all admissible soft SUSY breaking terms
- ★ resultant Lagrangian has 124 parameters!
- ★ Lagrangian yields mass eigenstates, mixings, Feynman rules for scattering and decay processes
- ★ predictive model!

## Physical states of MSSM:

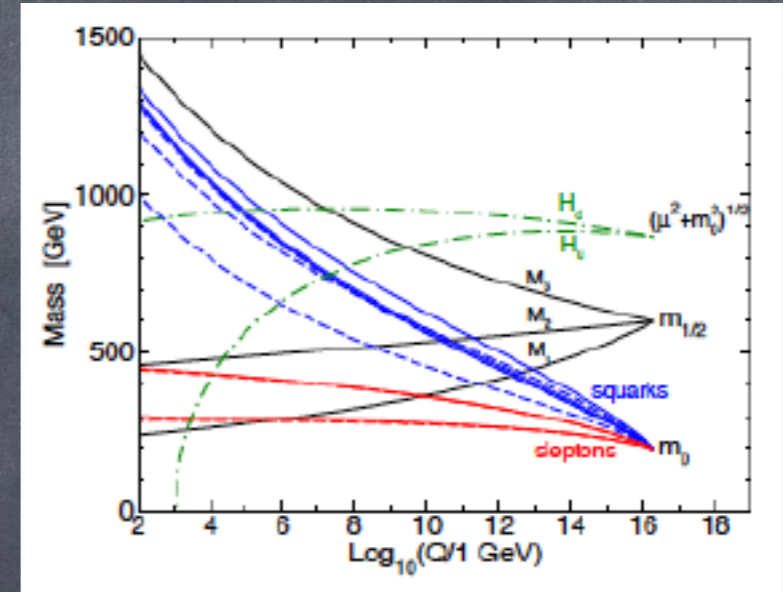
- ★ usual SM gauge bosons, quarks and leptons
- ★ gluino:  $\tilde{g}$
- ★ bino, wino, neutral higgsinos  $\Rightarrow$  neutralinos:  $\tilde{Z}_1, \tilde{Z}_2, \tilde{Z}_3, \tilde{Z}_4$
- ★ charged wino, higgsino  $\Rightarrow$  charginos:  $\tilde{W}_1^\pm, \tilde{W}_2^\pm$
- ★ squarks:  $\tilde{u}_L, \tilde{u}_R, \tilde{d}_L, \tilde{d}_R, \dots, \tilde{t}_1, \tilde{t}_2$
- ★ sleptons:  $\tilde{e}_L, \tilde{e}_R, \tilde{\nu}_e, \dots, \tilde{\tau}_1, \tilde{\tau}_2, \tilde{\nu}_\tau$
- ★ Higgs sector enlarged:  $h, H, A, H^\pm$
- ★ a plethora of new states to be found at LHC/ILC?!

# The MSSM is supported by virtual quantum effects!

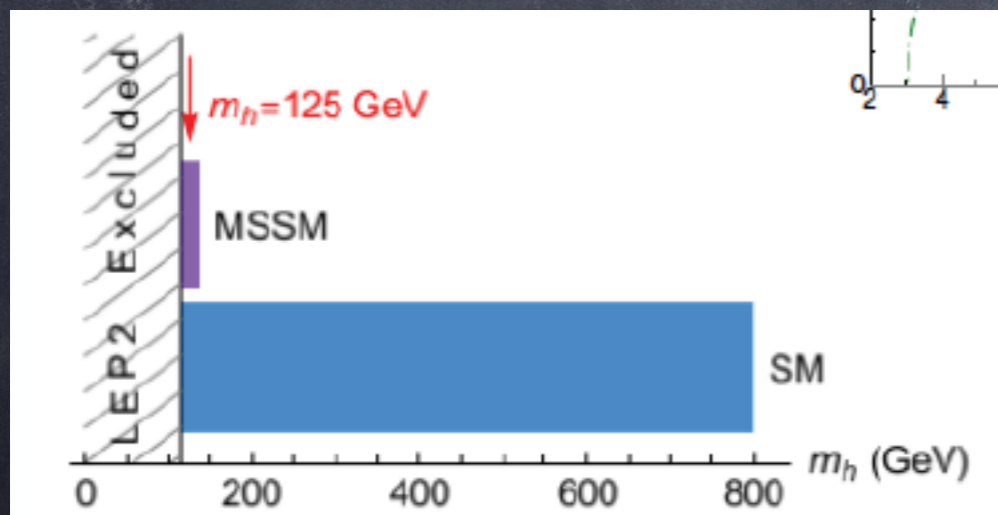


Unification of gauge couplings

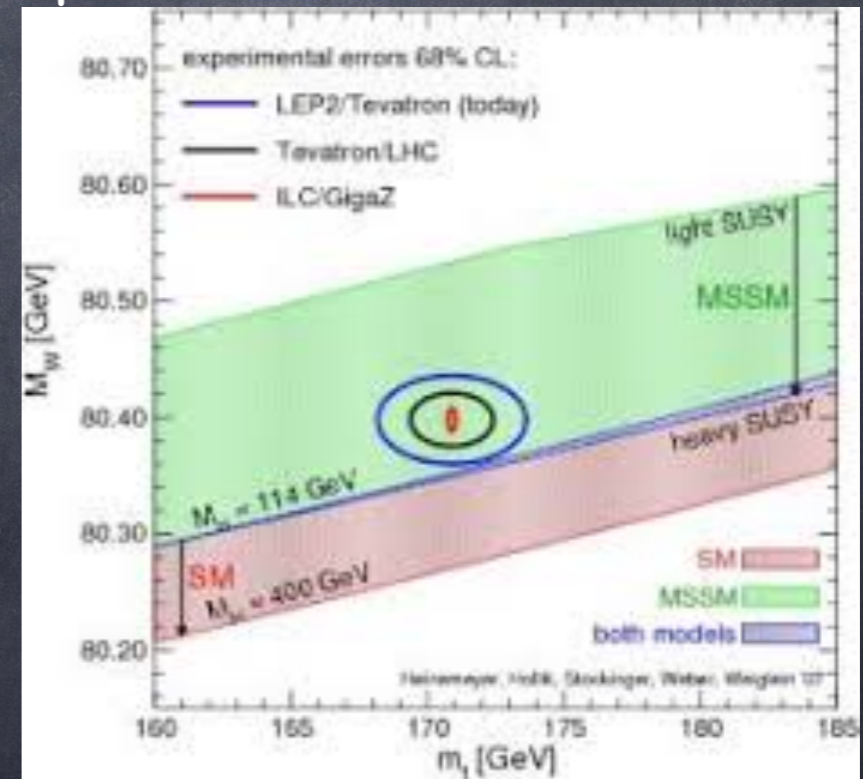
$m(t) \sim 150-200$  GeV  
required for radiative EWSB



$m(h)$  just right



precision electroweak fits

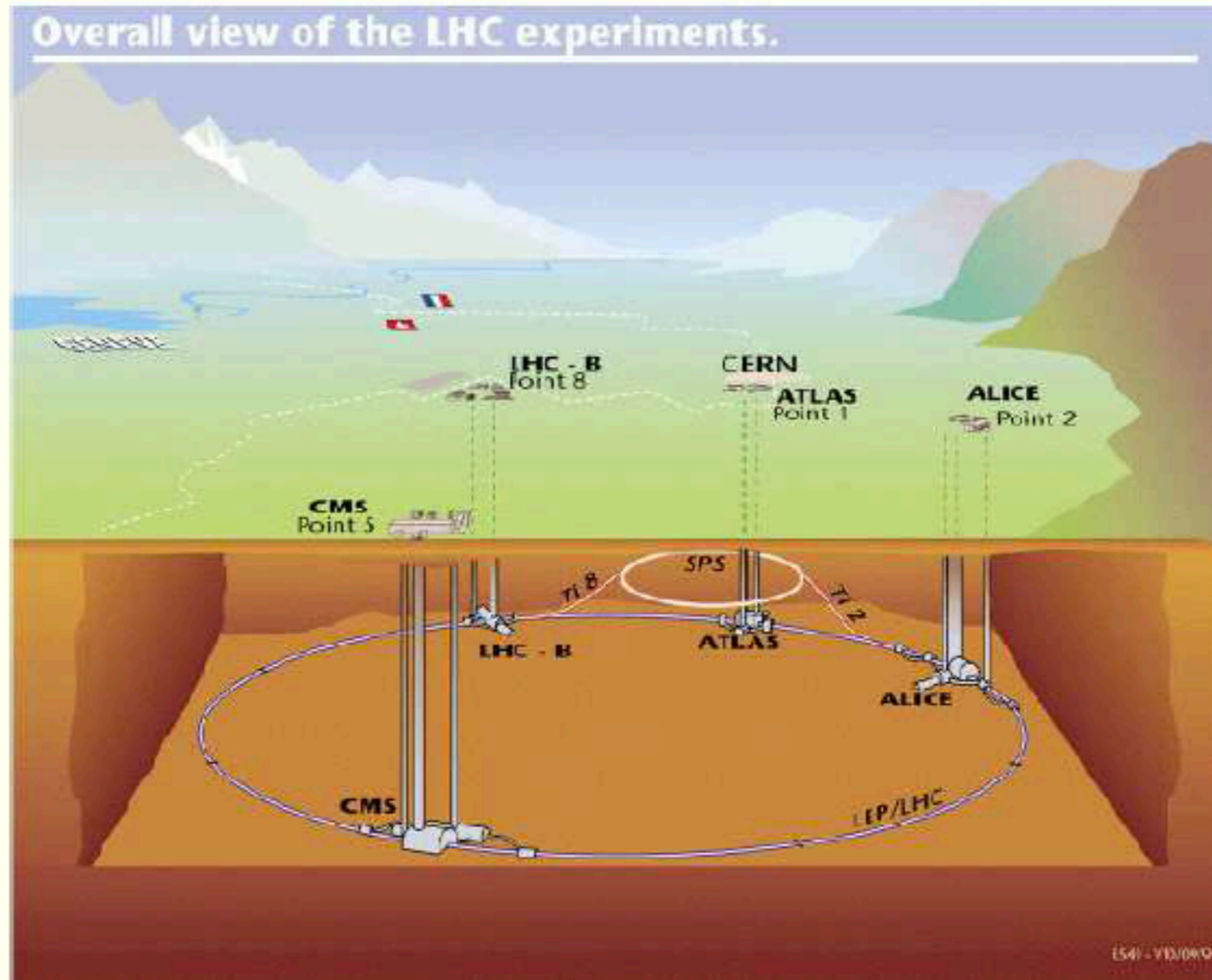


Radiative corrections have proven to be a reliable guide to new physics



# Direct search for superpartners at LHC

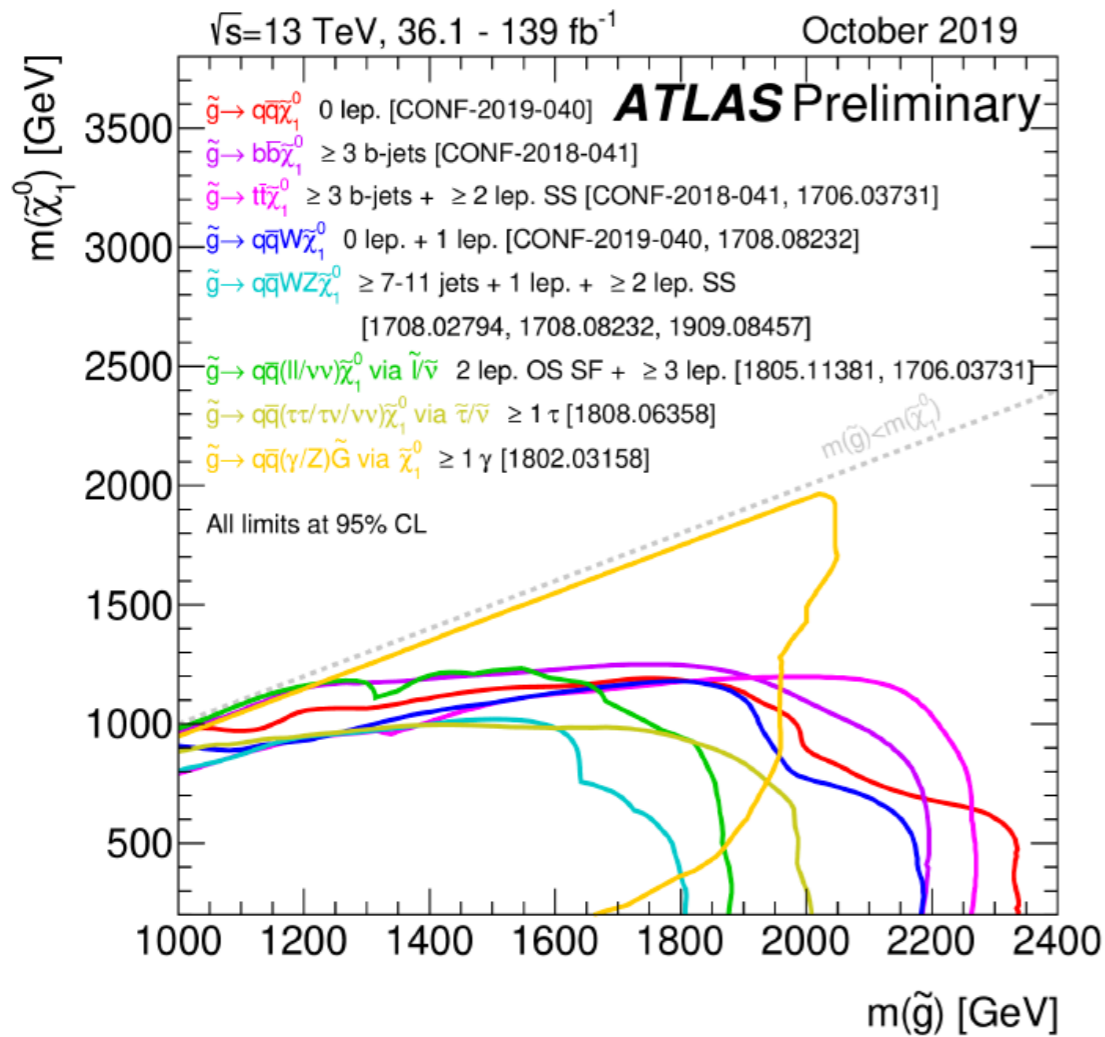
Layout of the LHC: two main detectors: Atlas and CMS



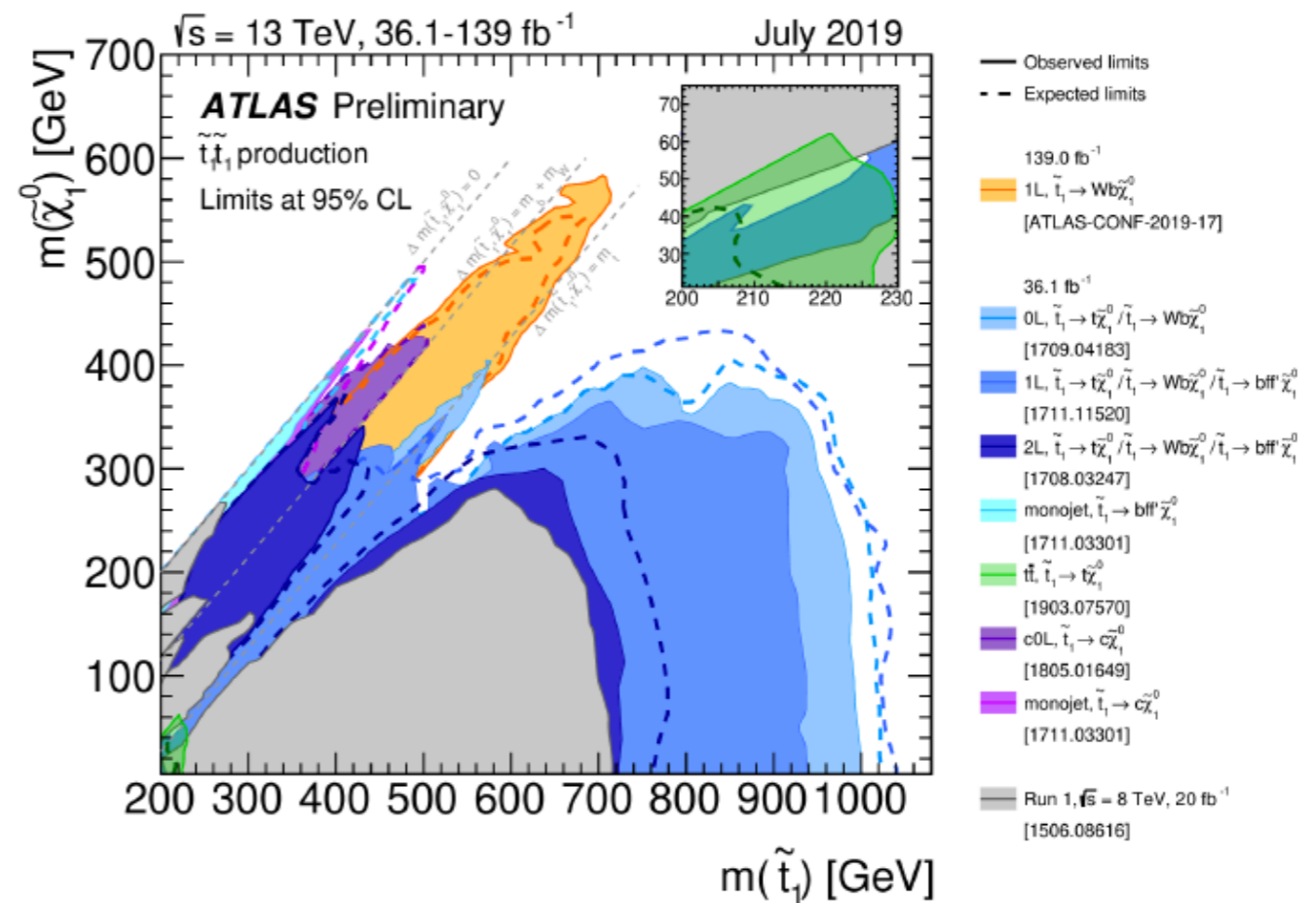
Nowadays: almost always within simplified models

# But where are the sparticles?

none seen so far at LHC

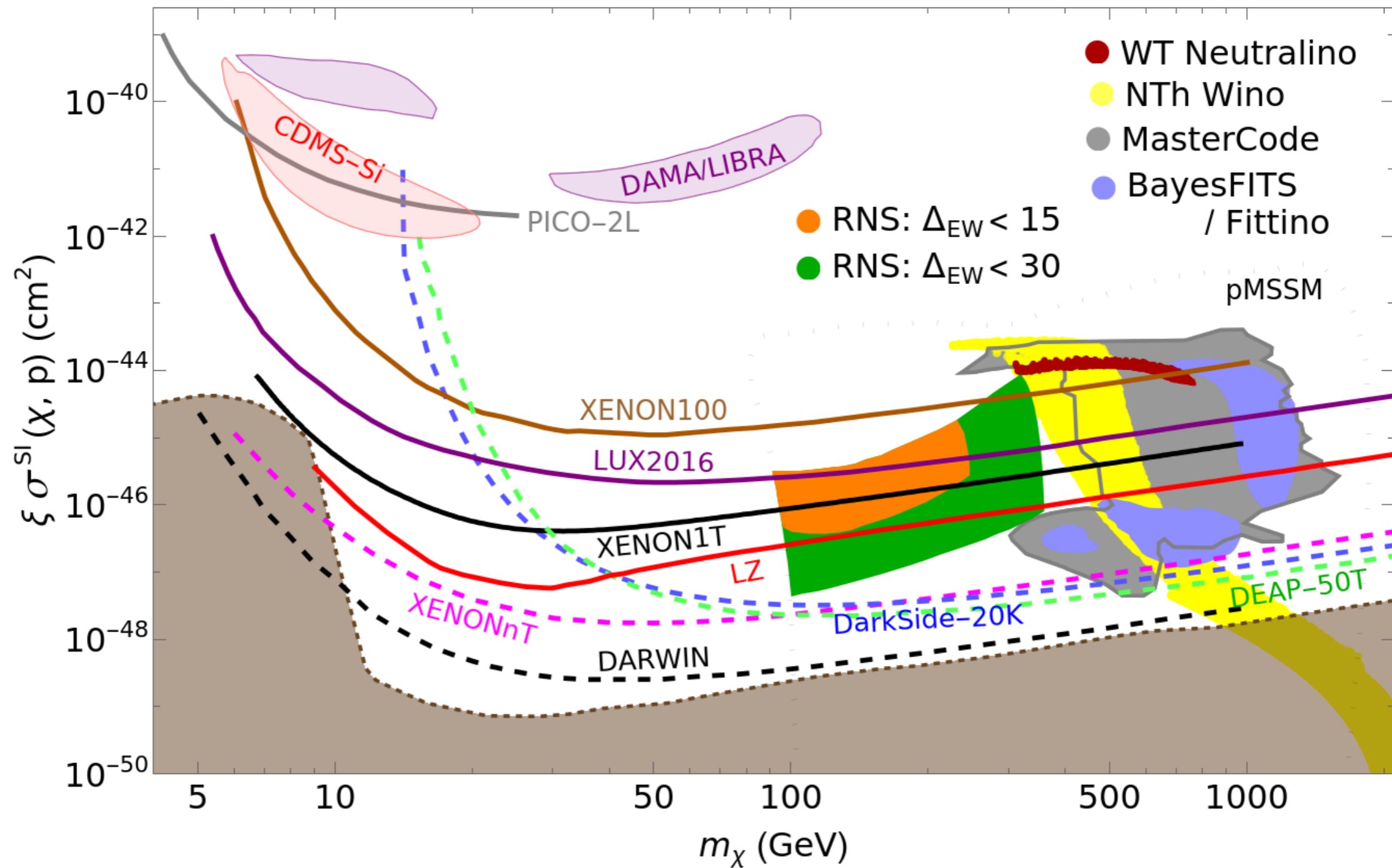


$$m_{\tilde{g}} > 2.25 \text{ TeV}$$



$$m_{\tilde{t}_1} > 1.1 \text{ TeV}$$

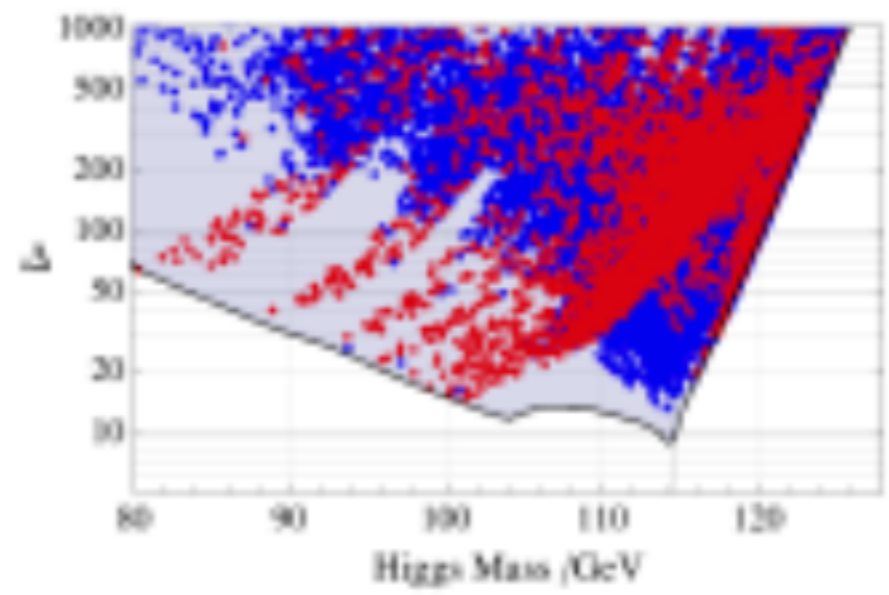
# Where are the WIMPs?



latest DD bounds from LZ2022: still no signal

These bounds appear in sharp conflict with EW “naturalness”

	mass
gluino	400 GeV
uR	400 GeV
eR	350 GeV
chargino	100 GeV
neutralino	50 GeV



Cassel, Ghilencea, Ross, 2009

$\Delta \rightarrow 1000$   
 as  $m_h \rightarrow 125$  GeV  
 0.1% tuning!?

Barbieri-Giudice 10% bounds, 1987

Pardon this slide but I grew up in Wisconsin in the 1960s;  
Vince Lombardi, legendary football coach



“...settling the ultimate fate of naturalness is perhaps the most profound theoretical question of our time”



Arkani-Hamed et al.,  
arXiv:1511.06495

“Given the magnitude of the stakes involved,  
it is vital to get a clear verdict  
on naturalness from experiment”

This should be matched by theoretical scrutiny  
of what we mean by naturalness

# SUSY solves Big Hierarchy ('t Hooft natural): but LHC => Little Hierarchy $m(\text{weak}) \sim 100 \text{ GeV} \ll m(\text{soft}) \sim \text{TeV}?$

- It is (**mistakenly**) believed that weak scale SUSY is no longer natural due to strong LHC constraints on sparticle masses ( $m(\text{gluino}) > 2.2 \text{ TeV}$ ) and the rather large value of  $m(h) \sim 125 \text{ GeV}$
- 1. BG naturalness measure overestimates finetuning by factors of 10–1000 due to adopting various soft terms as independent when in realistic SUGRA models these are in fact **\*dependent\***: soft terms computed as multiples of gravitino mass  $m_{3/2}$
- 2. Higgs mass finetuning measure breaks soft terms into **\*dependent\*** contributions which each vary as they are tuned: violates finetuning rule, leading again to overestimates by orders of magnitude 10–1000
- 3. EW finetuning measure: mandatory and model independent: **if you run spectra codes, this is where finetuning actually occurs!**

PHYSICAL REVIEW D 88, 095013 (2013)

**How conventional measures overestimate electroweak fine-tuning in supersymmetric theory**

Howard Baer,<sup>1,\*</sup> Vernon Barger,<sup>2,†</sup> and Dan Mickelson<sup>1,‡</sup>

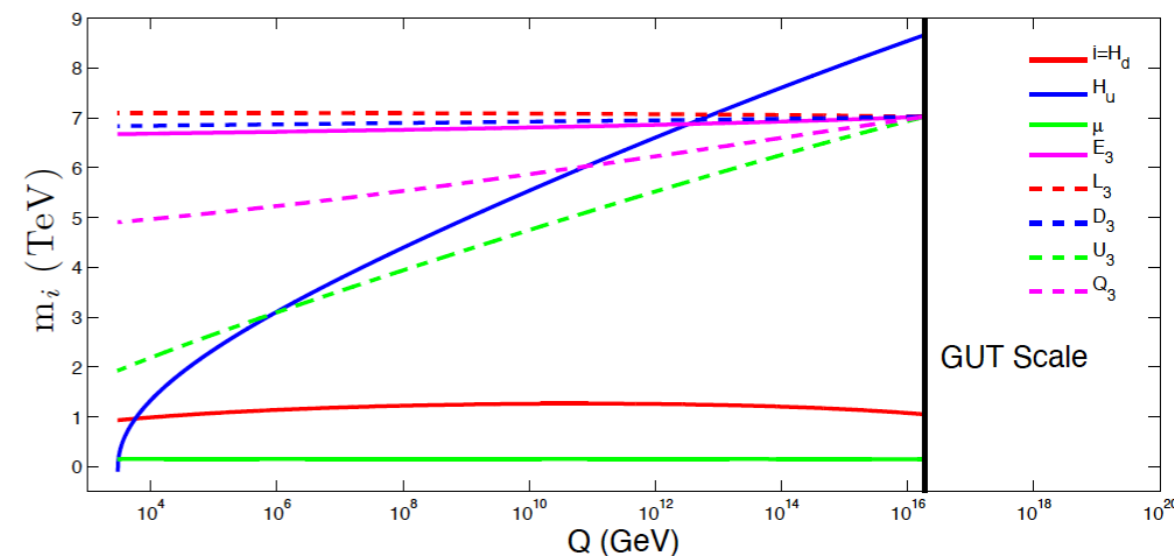
practical naturalness: all **\*independent\*** contributions to an observable should be comparable to or less than the observable

[This is the way naturalness has been successfully applied by e.g. Gaillard and Lee to predict the value of  $m(\text{charm})$  shortly before it was discovered]

$$\frac{m_Z^2}{2} = \frac{m_{H_d}^2 + \Sigma_d^d - (m_{H_u}^2 + \Sigma_u^u) \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2$$

$$\simeq -m_{H_u}^2 - \Sigma_u^u(\tilde{t}_{1,2}) - \mu^2.$$

$$\Delta_{EW} = \max|\text{term on RHS}| / (m_Z^2/2)$$

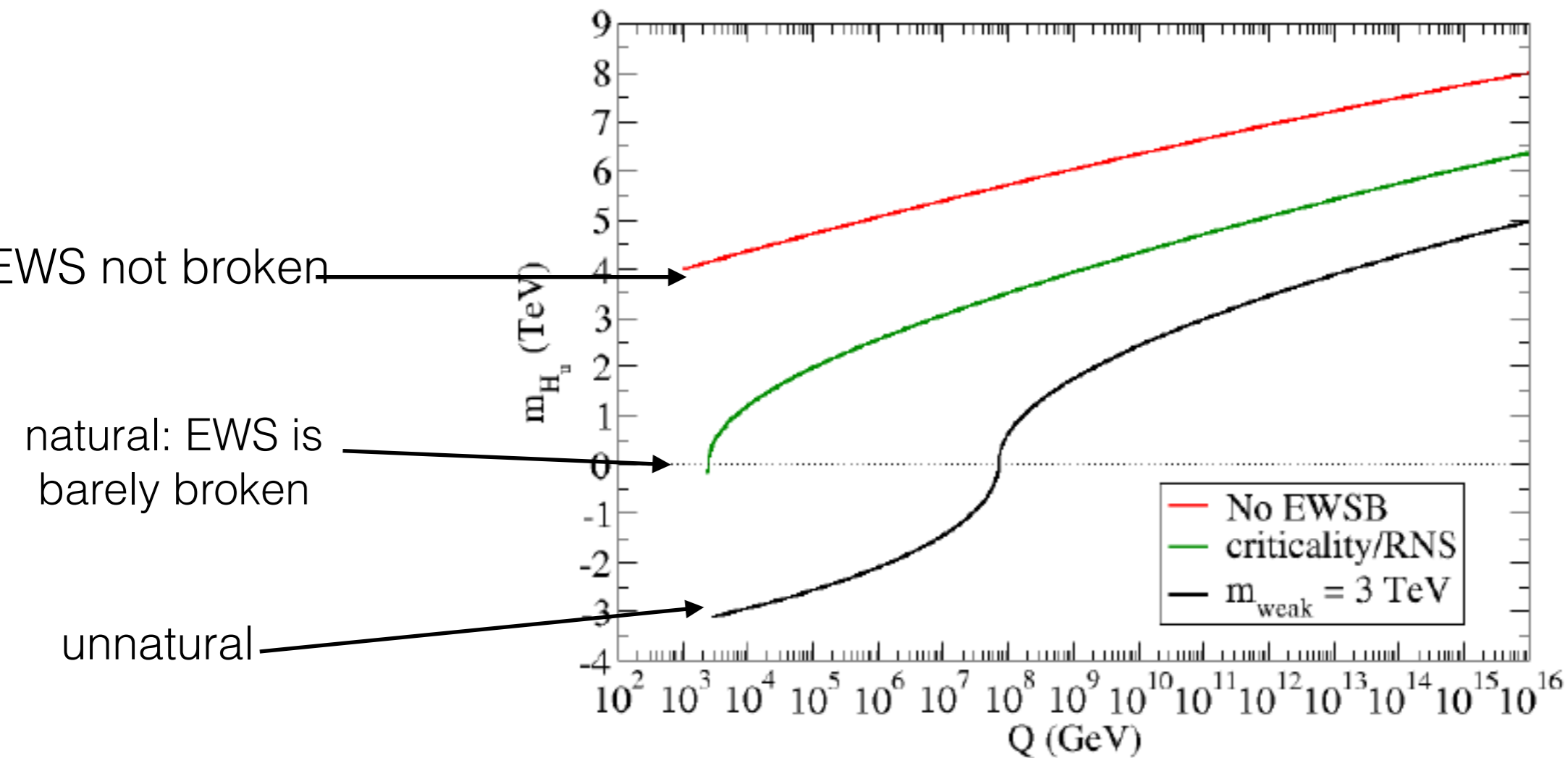


1.  $\mu \sim m(Z) \sim 100\text{--}300$  GeV: **LSP is higgsino-like!**
2.  $m(H_u) \sim m(Z) \sim 100\text{--}300$  GeV can be radiatively driven to small (natural) values
3. top squarks loop suppressed: range up to 3 TeV
4. gluinos enter at 2-loops: can range up to 6 TeV

**SUSY with radiatively-driven naturalness is natural!** review: [arXiv:2002.03013](https://arxiv.org/abs/2002.03013)

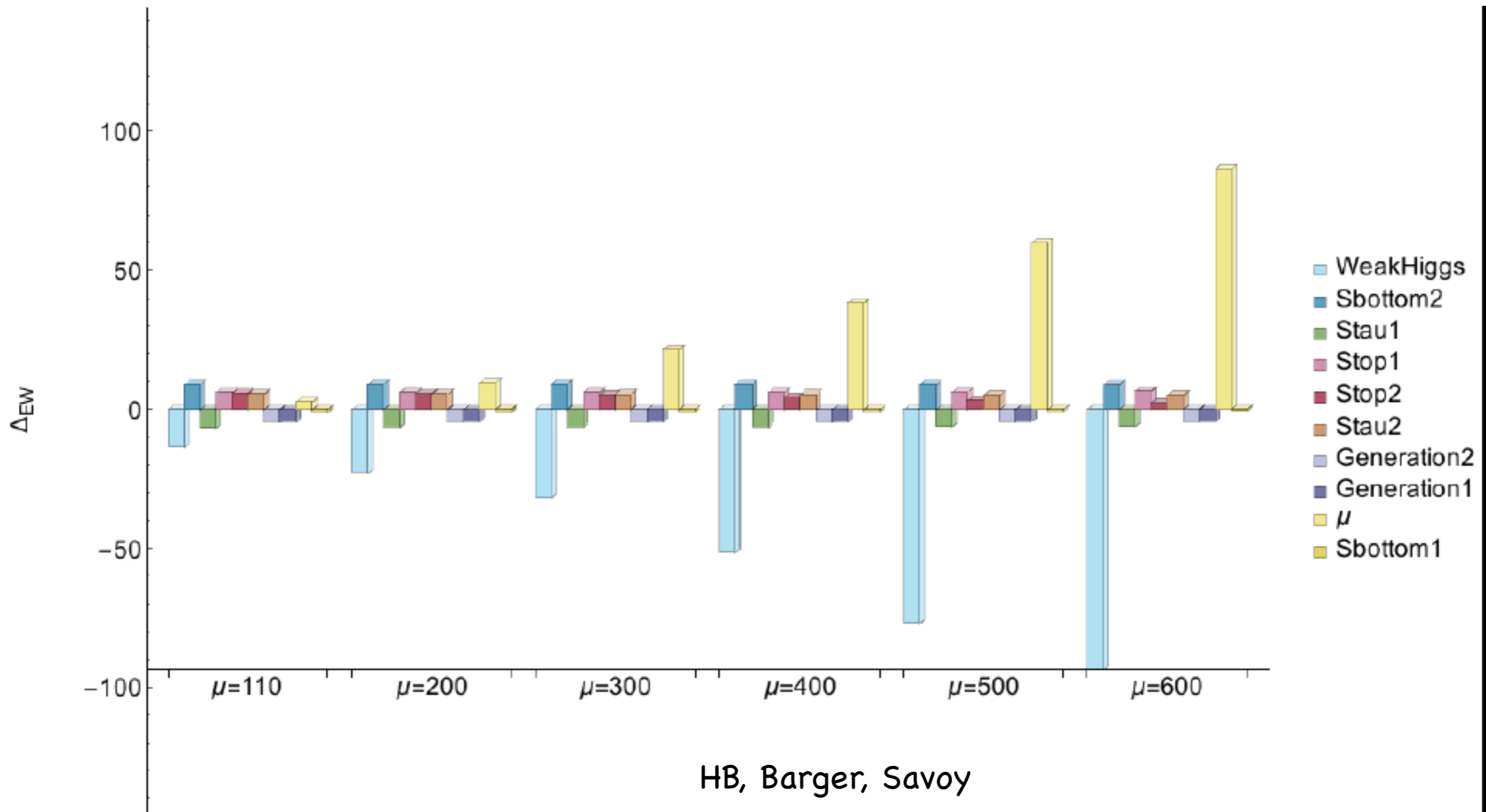


radiative corrections drive  $m_{H_u}^2$  from unnatural GUT scale values to naturalness at weak scale:  
radiatively-driven naturalness



Evolution of the soft SUSY breaking mass squared term  $sign(m_{H_u}^2)\sqrt{|m_{H_u}^2|}$  vs.  $Q$

# How much is too much fine-tuning?

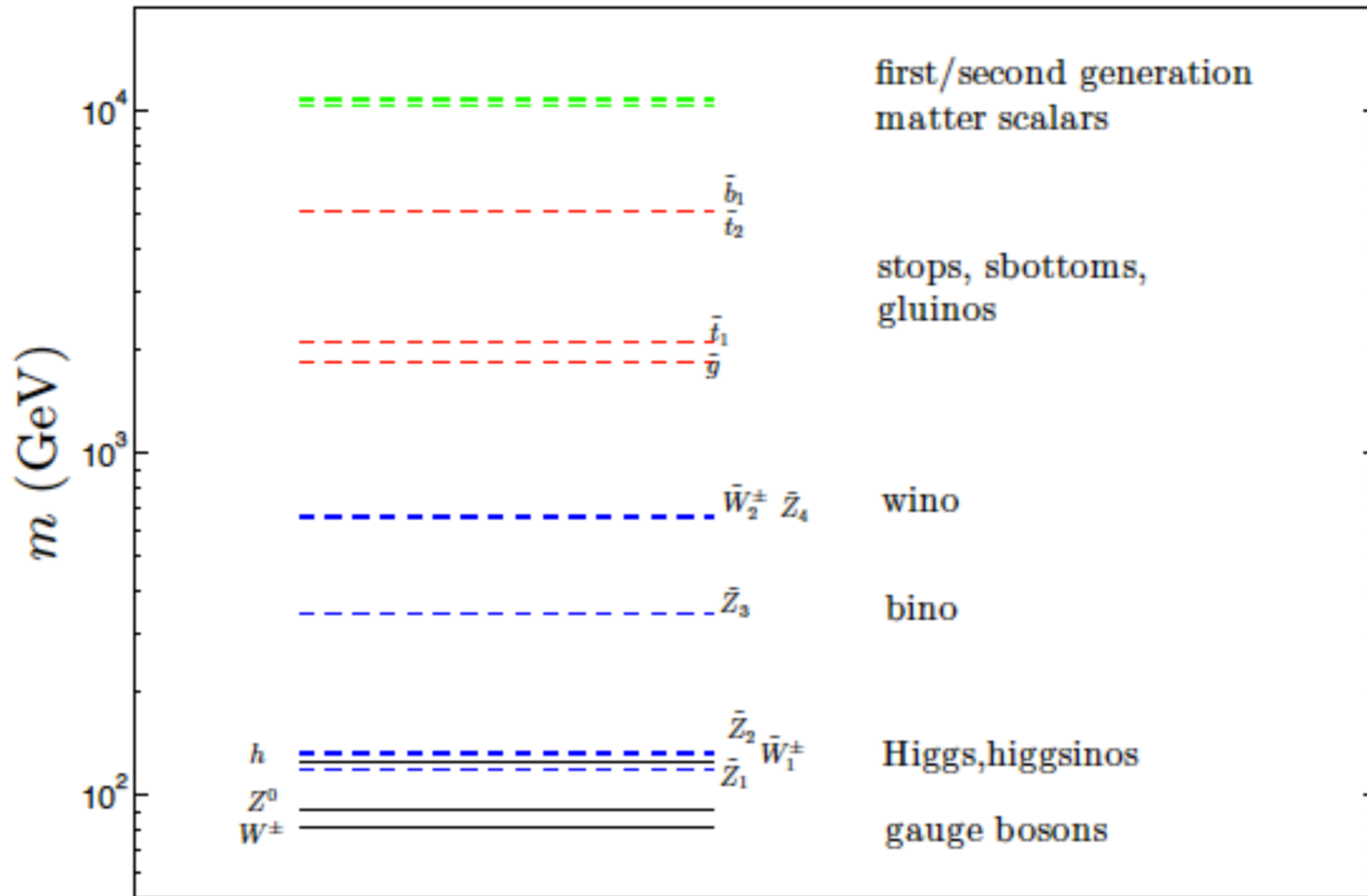


Visually, large fine-tuning has already developed by  $\mu \sim 350$  or  $\Delta_{EW} \sim 30$

bounds from naturalness (3%)	BG/DG	Delta_EW
mu	350 GeV	350 GeV
gluino	400-600 GeV	6 TeV
t1	450 GeV	3 TeV
sq/sl	550-700 GeV	10-30 TeV

h(125) and LHC limits are perfectly compatible with 3-10% naturalness: **no crisis!**

# Typical spectrum for low $\Delta_{EW}$ models



There is a Little Hierarchy, but it is **no problem**

$$\mu \ll m_{3/2}$$

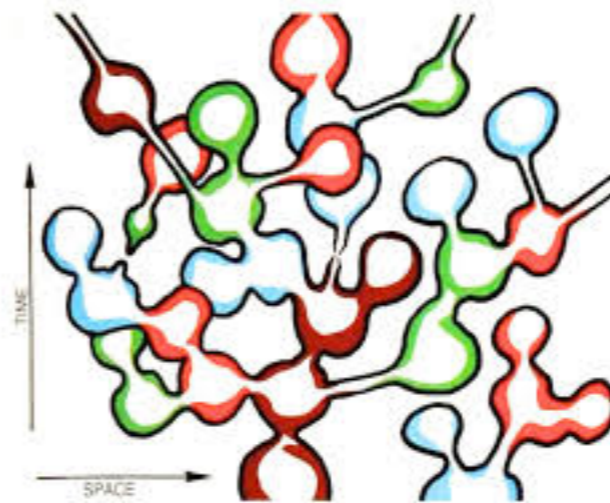
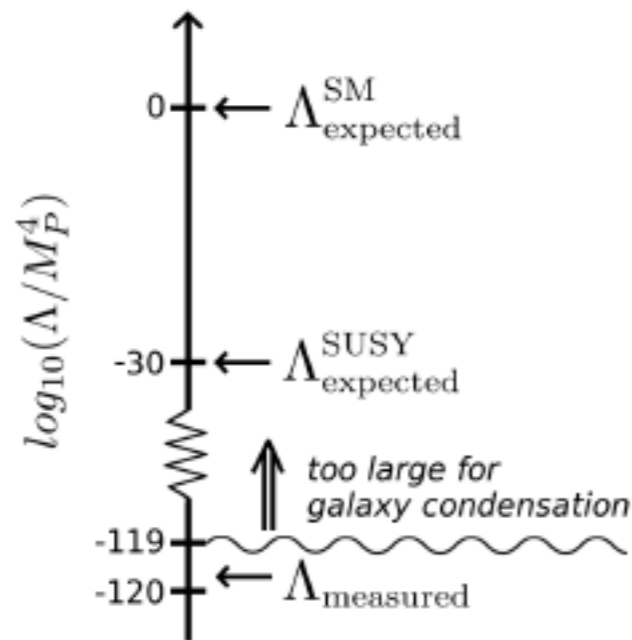
higgsinos likely the lightest superparticles!

Takeaway lesson:  
policy decisions for future accelerators  
should not be based on  
faulty naturalness estimates!

Take note: European strategy report  
and US Snowmass/P5 reports!

# How does this all relate to string landscape?

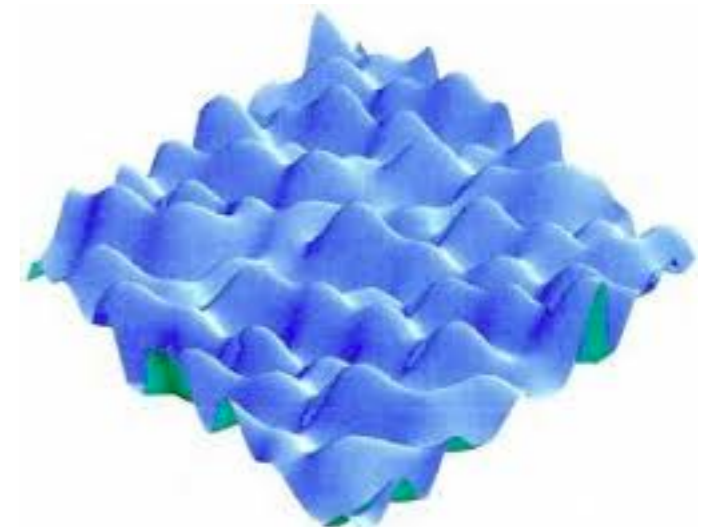
It is sometimes invoked that maybe we should abandon naturalness: after all, isn't the cosmological constant (CC) fine-tuned?



eternally inflating  
multiverse

In the landscape with  $10^{500}$  vacua with different CCs, then the tiny value of the CC may not be surprising since larger values would lead to runaway pocket universes where galaxies wouldn't condense—anthropics: no observers in such universes (Weinberg)

The CC is as natural as possible subject to the condition that it leads to galaxy condensation



Bousso &  
Polchinski

For some recent review material, see M. Douglas,  
The String Theory Landscape, 2018, Universe 5 (2019) 7, 176

Apply similar reasoning to origin of weak scale  
(which arises from SUSY breaking in SUSY models):

Statistical analysis of SUSY breaking scale in IIB theory:

M. Douglas, hep-th/0405279

start with  $10^{500}$  string vacua states

- string theory landscape contains vast ensemble of  $N=1, d=4$  SUGRA EFTs at high scales
- the EFTs contain the SM as weak scale EFT
- the EFTs contain visible sector +potentially large hidden sector
- visible sector contains MSSM plus extra gauge singlets (e.g. a PQ sector, RN neutrinos,...)
- SUGRA is broken spontaneously in hidden sector via superHiggs mechanism via either F- or D- terms or in general a combination

In fertile patch of vacua with MSSM as weak scale effective theory  
but with no preferred SUSY breaking scale...

$$dP/d\mathcal{O} \sim f_{prior} \cdot f_{selection}$$

What is  $f_{prior}$  for SUSY breaking scale?

In string theory, usually multiple ( $\sim 10$ ) hidden sectors  
containing a variety of F- and D- breaking fields

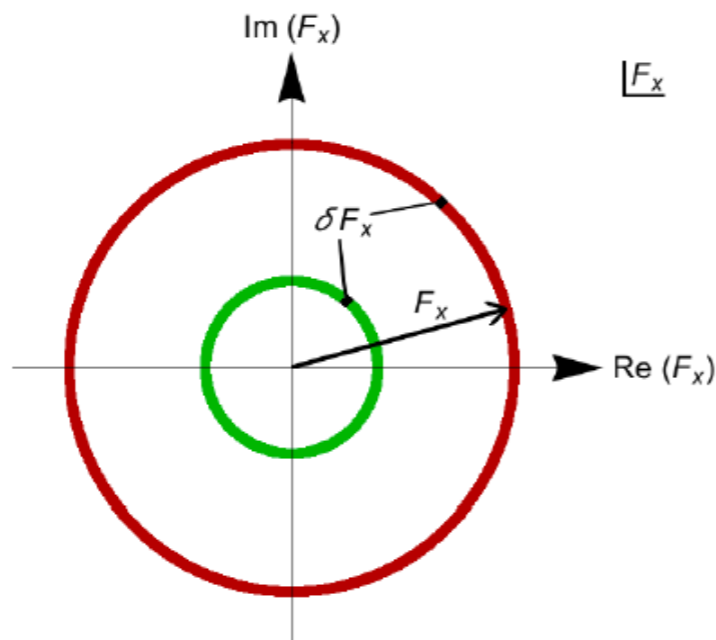
For comparable  $\langle F_i \rangle$  and  $\langle D_j \rangle$  values, then expect

$$f_{prior} \sim m_{soft}^{2n_F + n_D - 1}$$

Douglas ansatz

arXiv:0405279

Under single F-term  
SUSY breaking,  
expect **linearly increasing**  
**statistical selection**  
**of soft terms**



For uniform values of SUSY breaking fields,  
expect landscape to **prefer**  
**high scale of SUSY breaking!**

Figure 1: Annuli of the complex  $F_X$  plane giving rise to linearly increasing selection of soft SUSY breaking terms.

$$m_{hidden}^4 = \sum_i F_i F_i^\dagger + D_\alpha D_\alpha$$

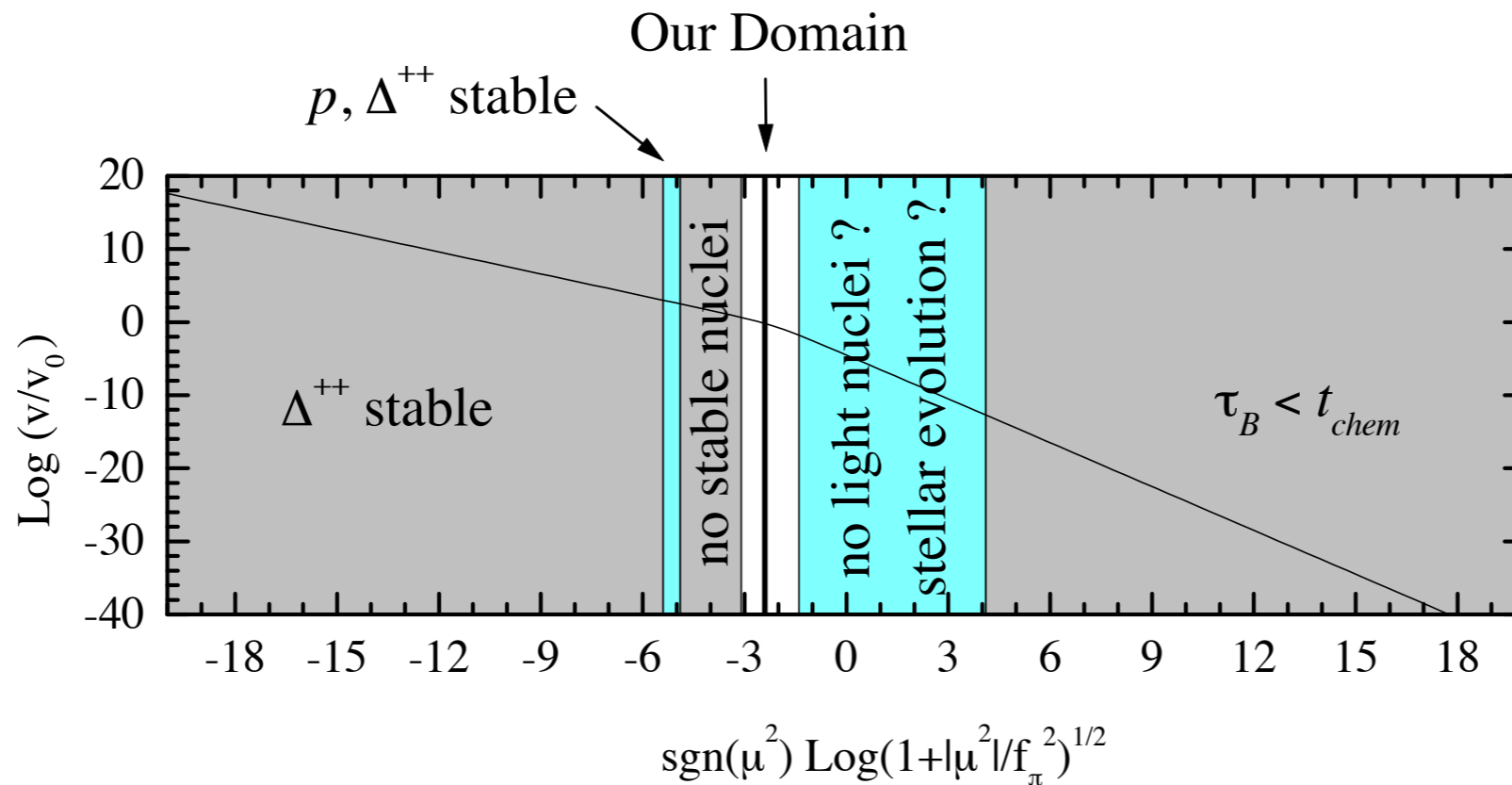


# What about $f_{\text{selection}}$ ?

Agrawal, Barr, Donoghue, Seckel result (1998):

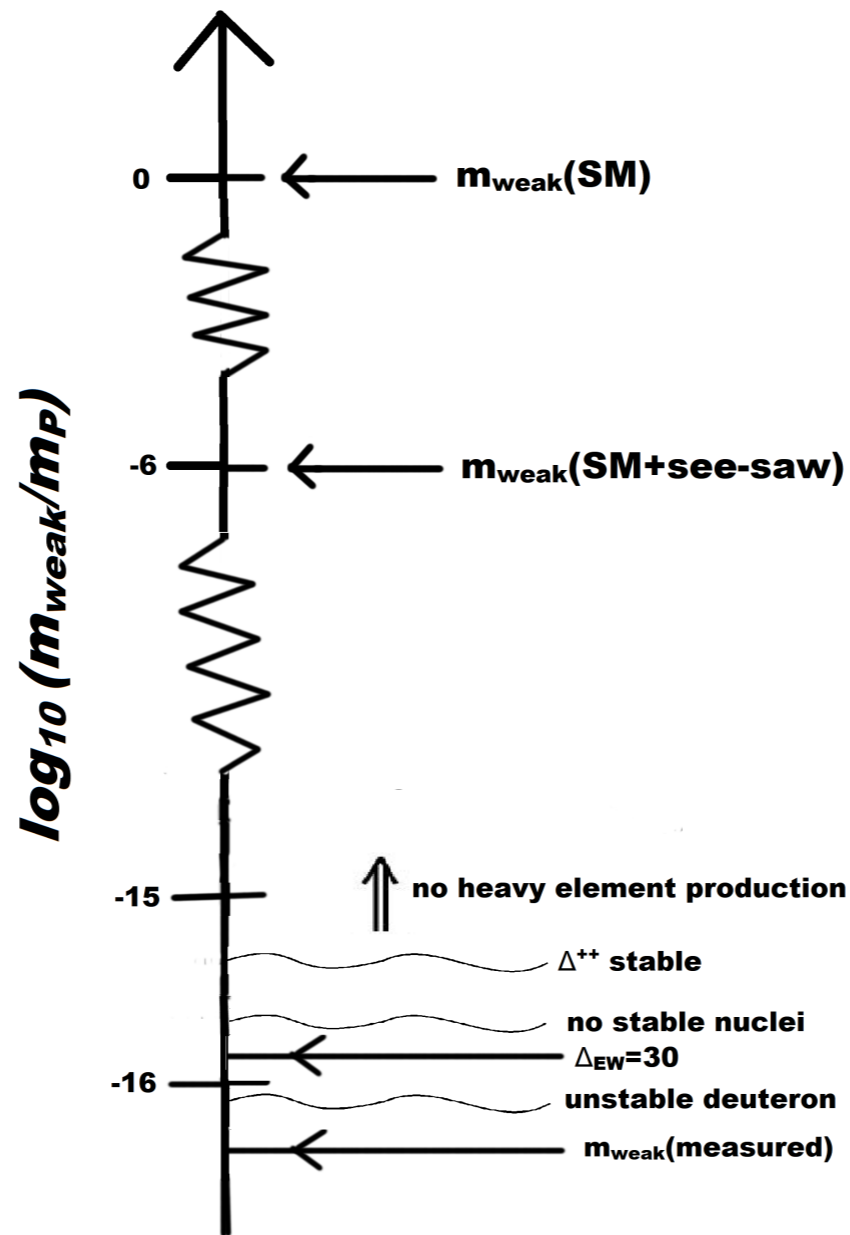
pocket-universe value of weak scale  
cannot deviate by more than  
factor 2-5 from its measured value

lest disasters occur in nuclear physics: no nuclei, no atoms  
(violates atomic principle)

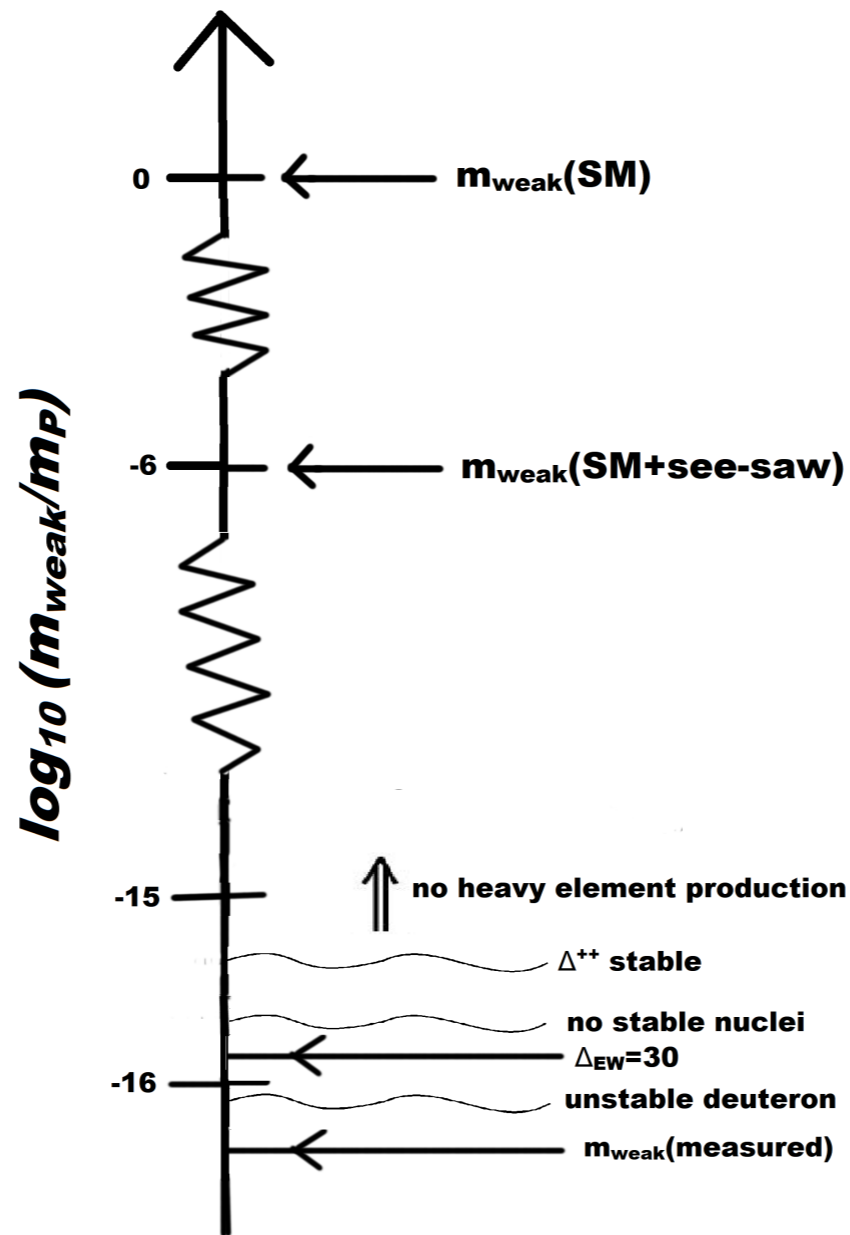


$m(\text{weak})$  must lie within ABDS window to have atoms/chemistry:  
 $\sim 50 \text{ GeV} < m(\text{weak}) < \sim 350 \text{ GeV}$

ABDS window  $\Leftrightarrow$  DEW  $< \sim 30$

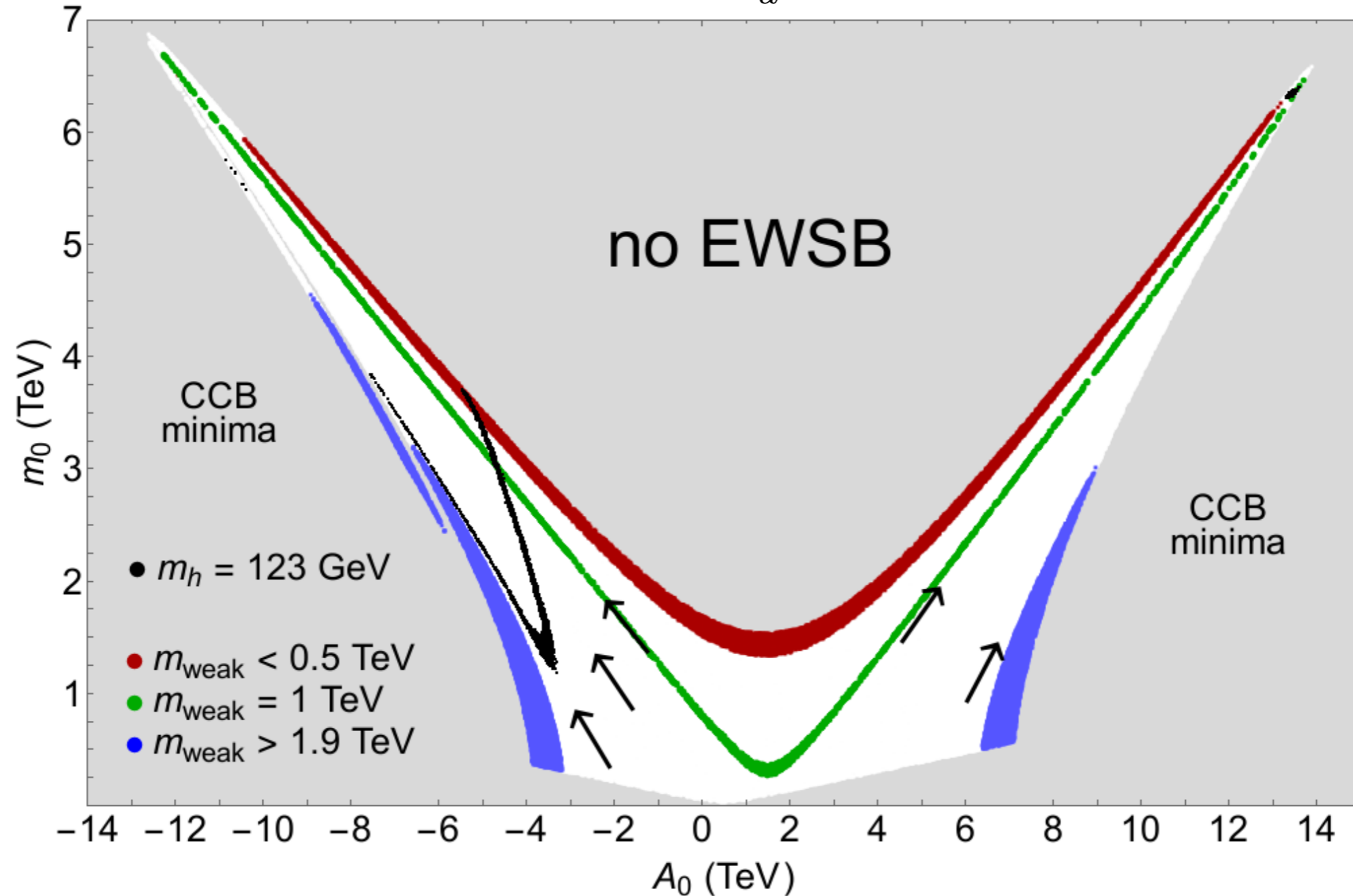


**Veto** pocket universes with CCB minima or minima leading to weak scale a (conservative) factor four greater than our value  $m(W,Z,h) \sim 100 \text{ GeV}$



Veto pocket universes with CCB minima or noEWSB or minima leading to weak scale a (conservative) factor four greater than our value  $m(W,Z,h) \sim 100 \text{ GeV}$

$$m_{H_u} = 1.3m_0$$



statistical draw to large soft terms balanced by anthropic draw toward red ( $m(\text{weak}) \sim 100 \text{ GeV}$ ): then  $m(\text{Higgs}) \sim 125 \text{ GeV}$  and natural SUSY spectrum!

Recent work: place on more quantitative footing:  
scan soft SUSY breaking parameters in NUHM3 model  
as  $m(\text{soft})^n$  along with  $f(\text{EWFT})$  penalty

We scan according to  $m_{\text{soft}}^n$  over:

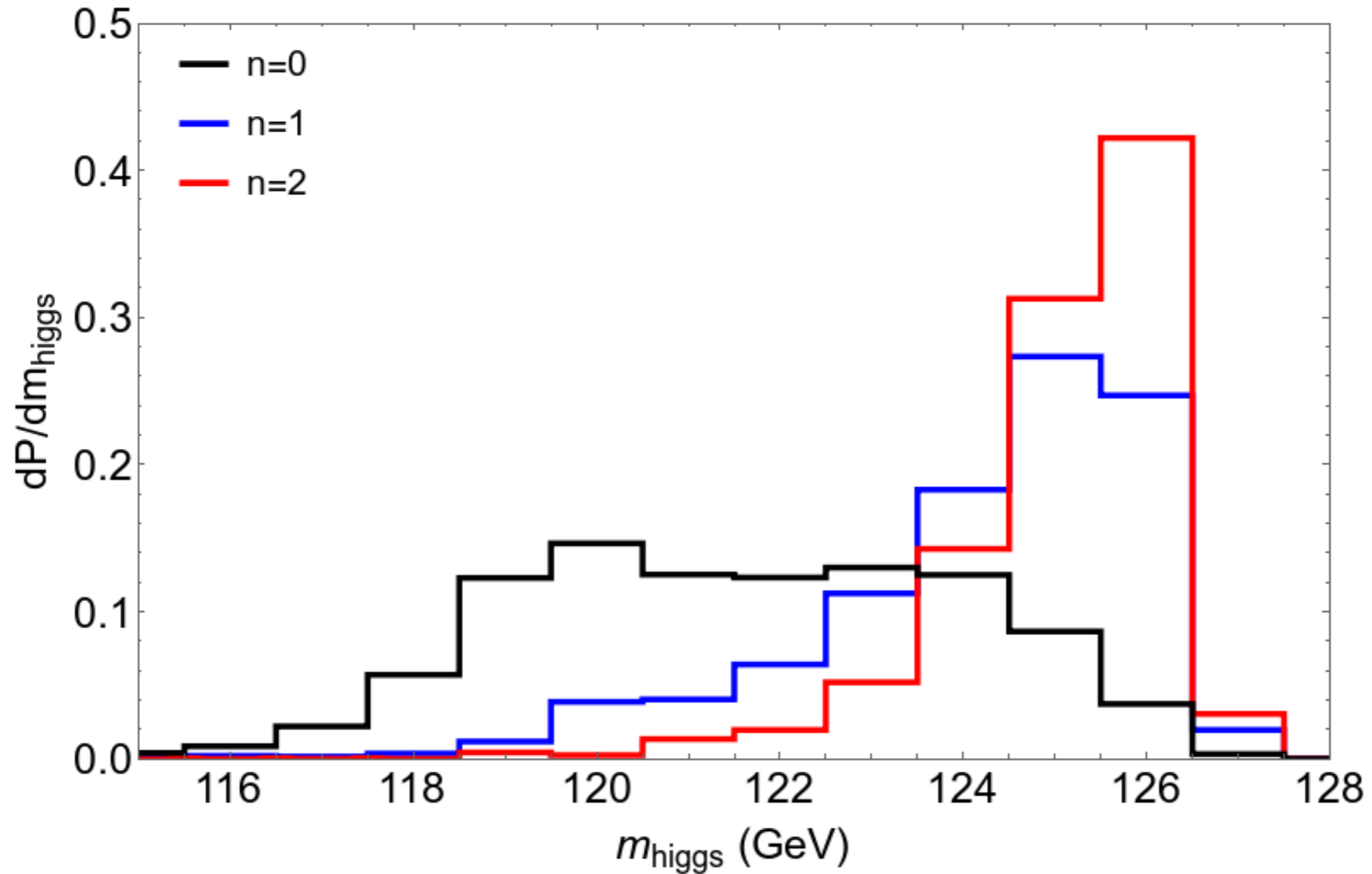
- $m_0(1, 2) : 0.1 - 40 \text{ TeV},$
- $m_0(3) : 0.1 - 20 \text{ TeV},$
- $m_{1/2} : 0.5 - 10 \text{ TeV},$
- $A_0 : 0 - -60 \text{ TeV},$
- $m_A : 0.3 - 10 \text{ TeV},$
- $\tan \beta : 3 - 60 \quad (\text{flat})$

$\mu=150 \text{ GeV}$  (fixed)

(then rescale to  $m_Z=91.2 \text{ GeV}$  to compare apples with apples)

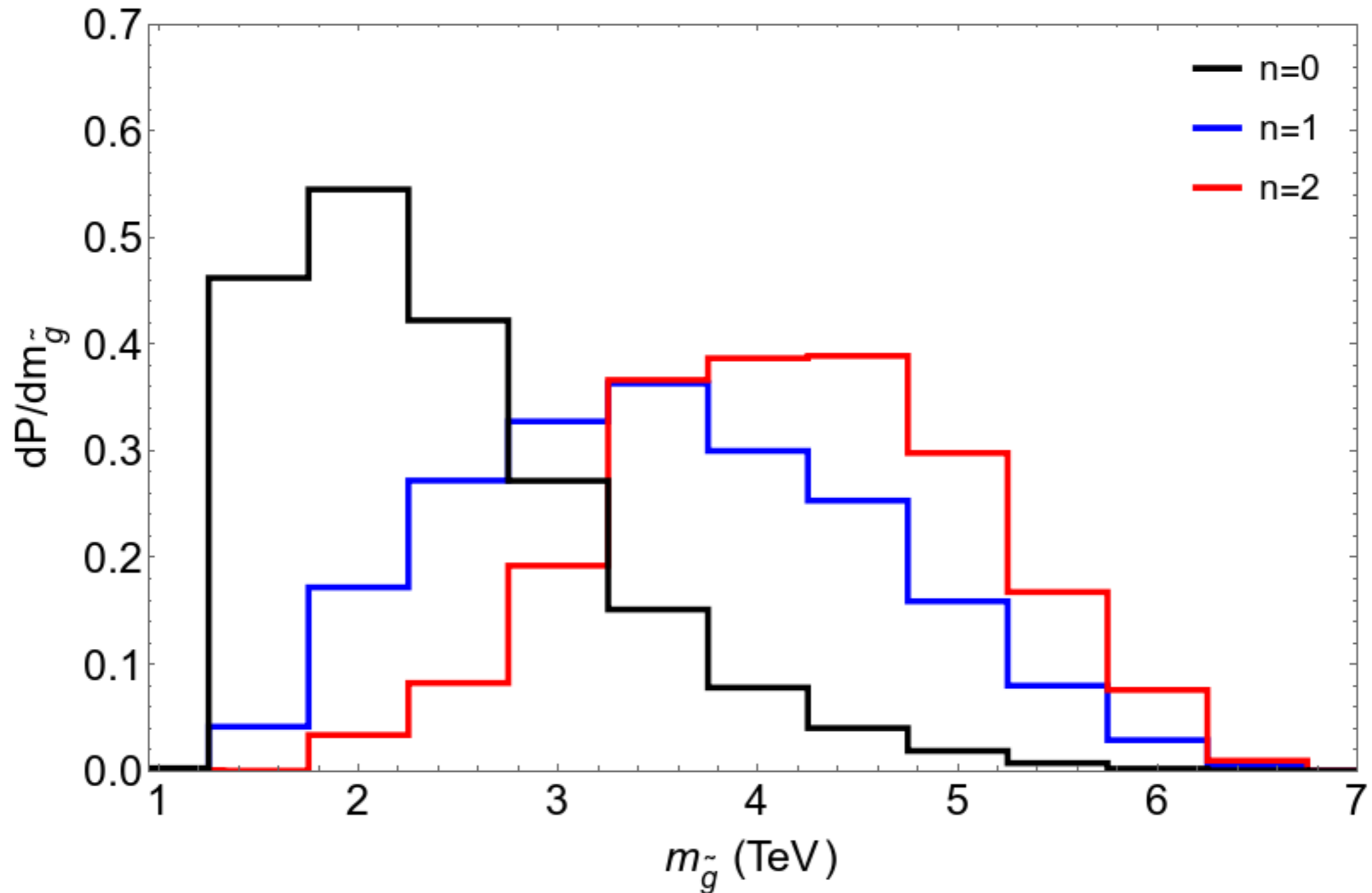
Making the picture more quantitative:

$$dN_{vac}[m_{hidden}^2, m_{weak}, \Lambda] = f_{SUSY}(m_{hidden}^2) \cdot f_{EWFT} \cdot f_{cc} dm_{hidden}^2$$



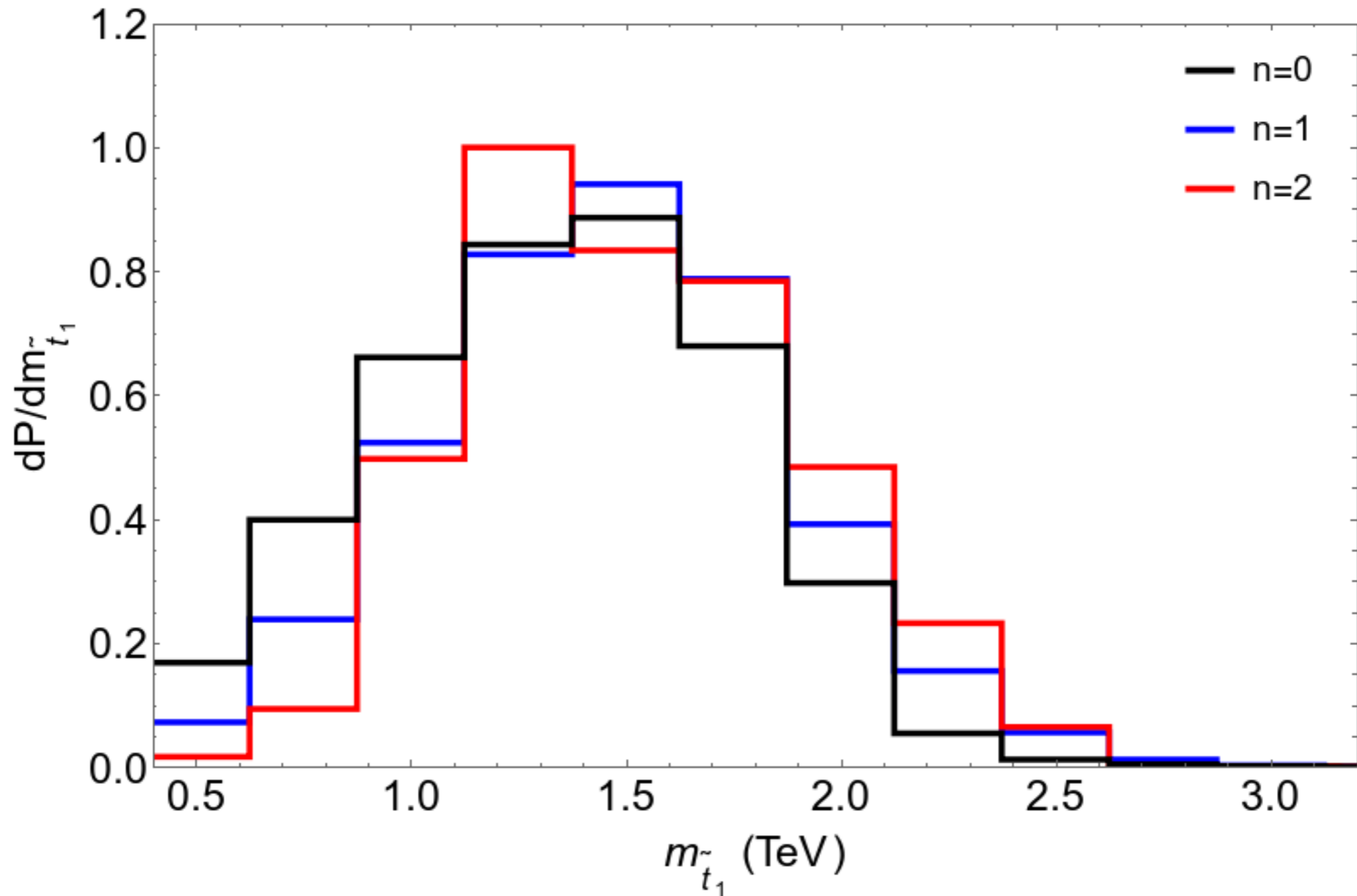
$m(h) \sim 125$  most favored for  $n=1,2$

What is corresponding distribution for gluino mass?



gluino typically beyond LHC 14 reach  
(need higher energy hadron collider)

and top-squark mass  $m(t_1)$ ?

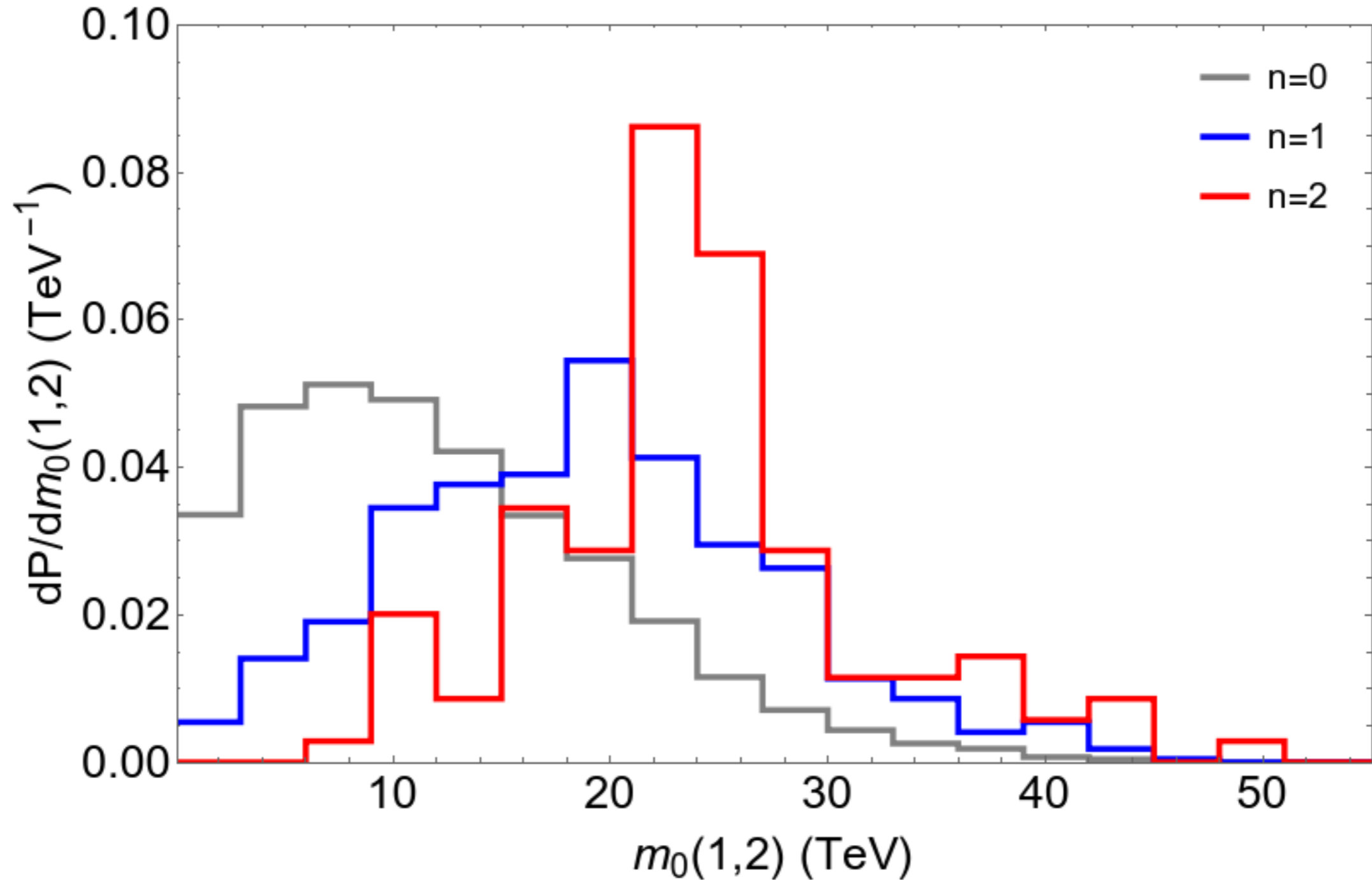


$m(t_1)$  typically beyond present LHC reach



first/second generation sfermions pulled to 10–40 TeV:  
landscape mixed decoupling/quasi-degeneracy sol'n  
to SUSY flavor/CP problems

HB, Barger, Sengupta, arXiv:1910.00090



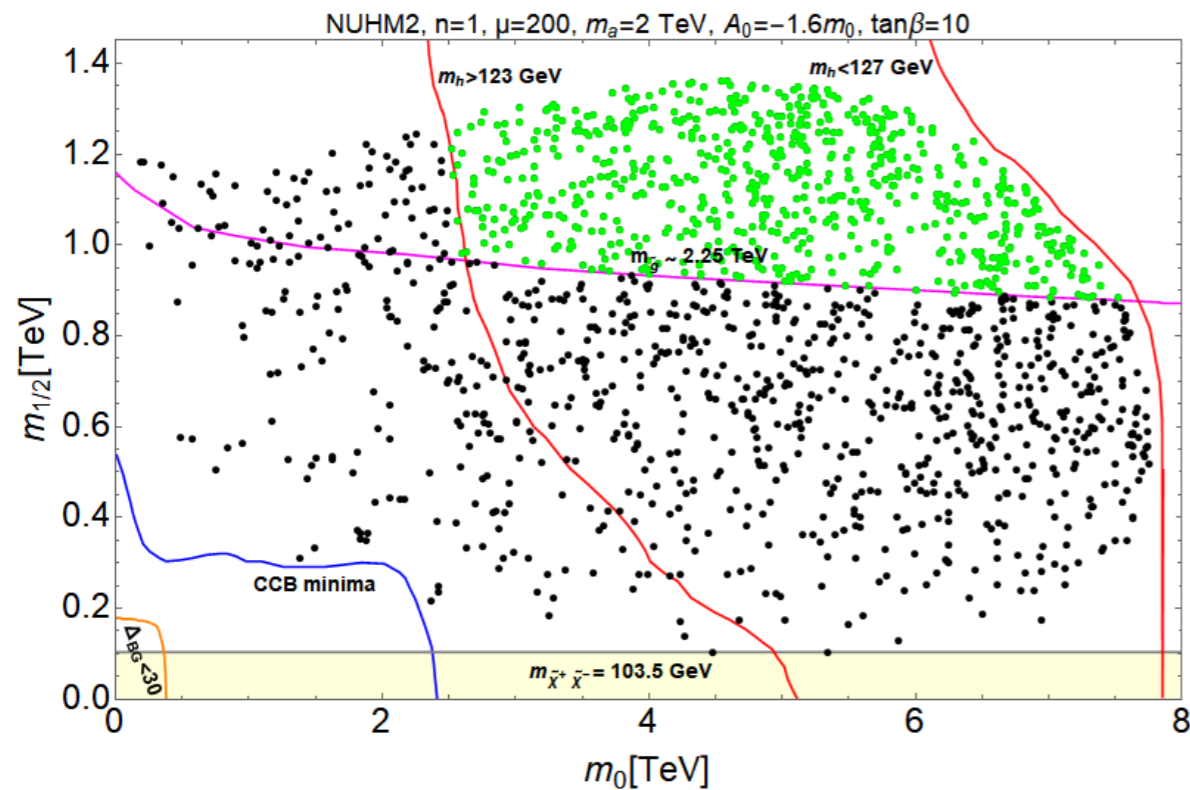
**Stringy naturalness:** higher density of points are more stringy natural!

conventional natural: favor low  $m_0$ ,  $m_h$

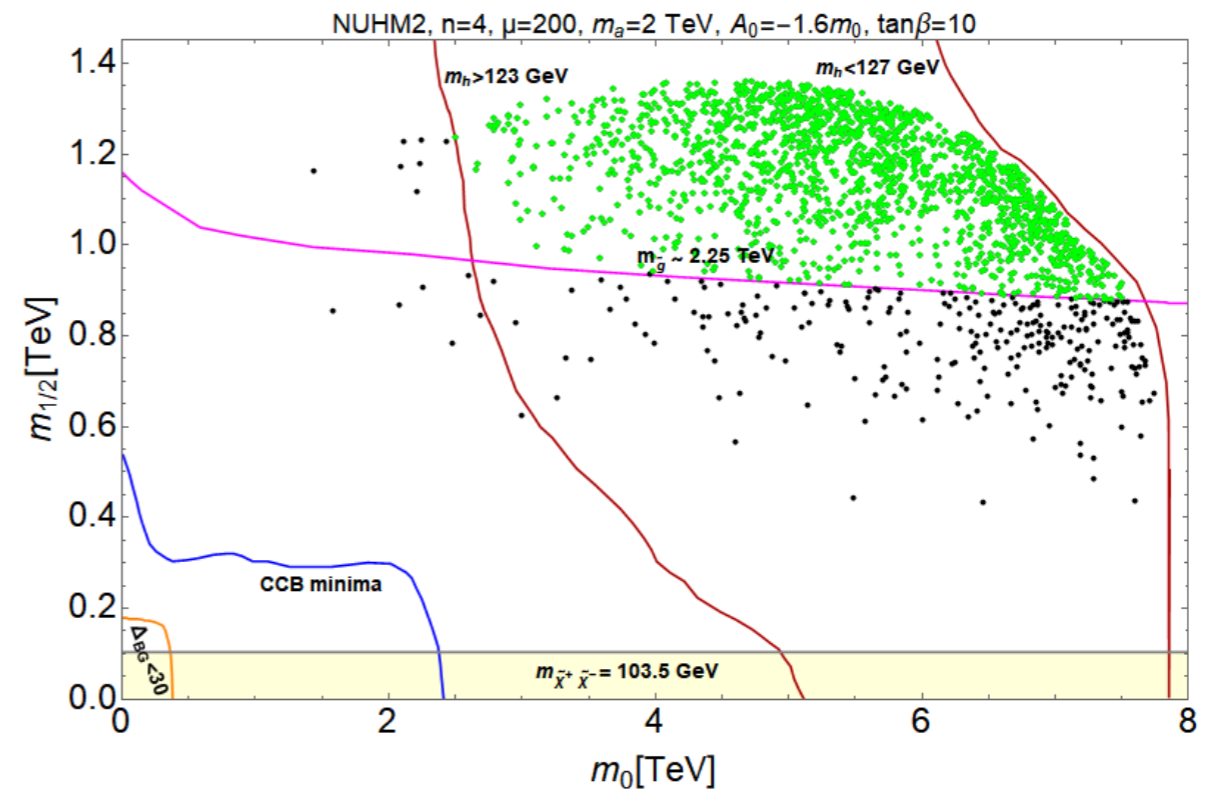
**stringy naturalness:** favor high  $m_0$ ,  $m_h$  so long as  $m(\text{weak}) \sim 100 \text{ GeV}$

HB, Barger, Salam, arXiv:1906.07741

Living dangerously: Arkani-Hamed, Dimopoulos, Kachru, hep-ph/0501082



$m(\text{soft})^1$

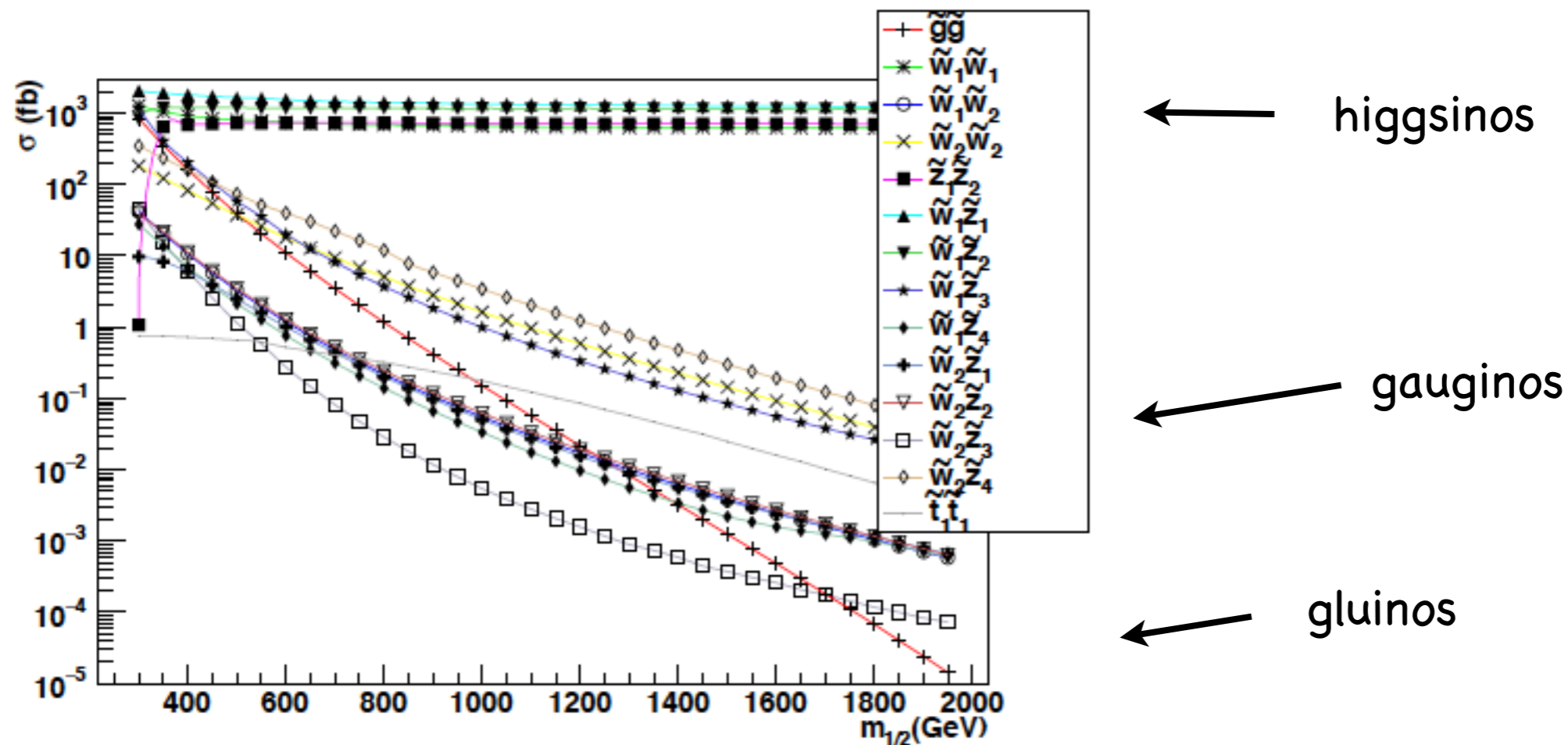


$m(\text{soft})^4$

**Under stringy naturalness, a 3 TeV gluino is more natural than a 300 GeV gluino!**

Prospects for discovering  
landscape/natural SUSY  
at LHC and ILC

# Sparticle prod'n along Radiative Natural SUSY model-line at LHC14:



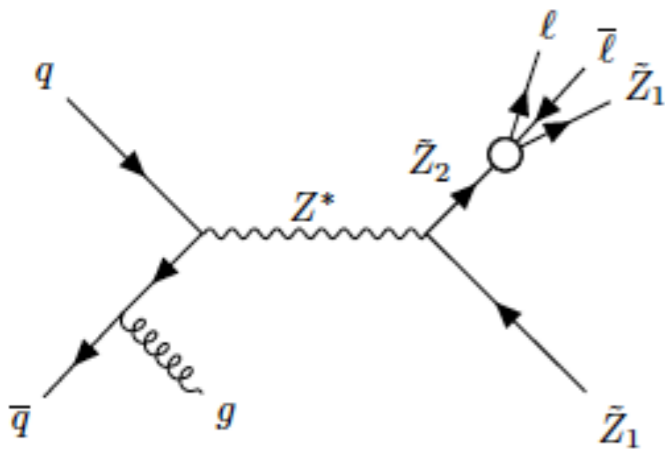
higgsino pair production dominant—but only soft visible energy release from higgsino decays

largest visible cross section: **wino pairs**

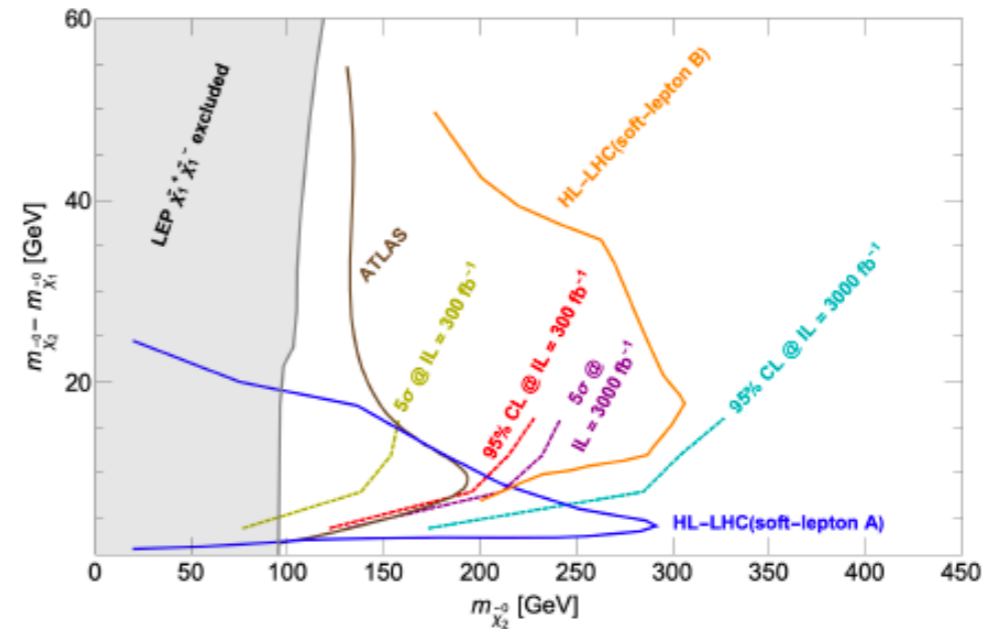
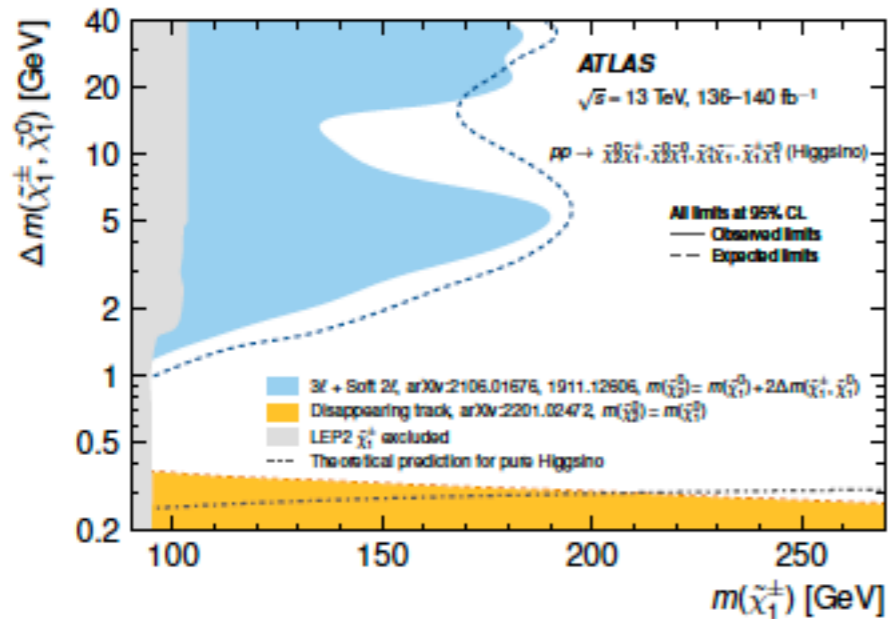
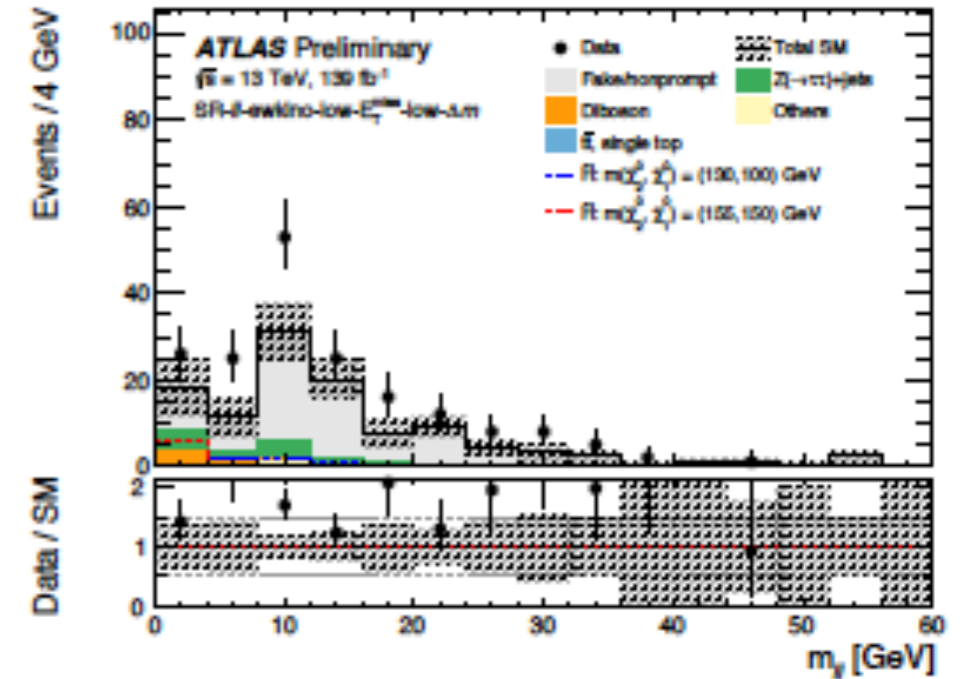
gluino pairs sharply dropping

# Natural SUSY: only higgsinos need lie close to weak scale

Soft dilepton+jet+MET signature from higgsino pair production



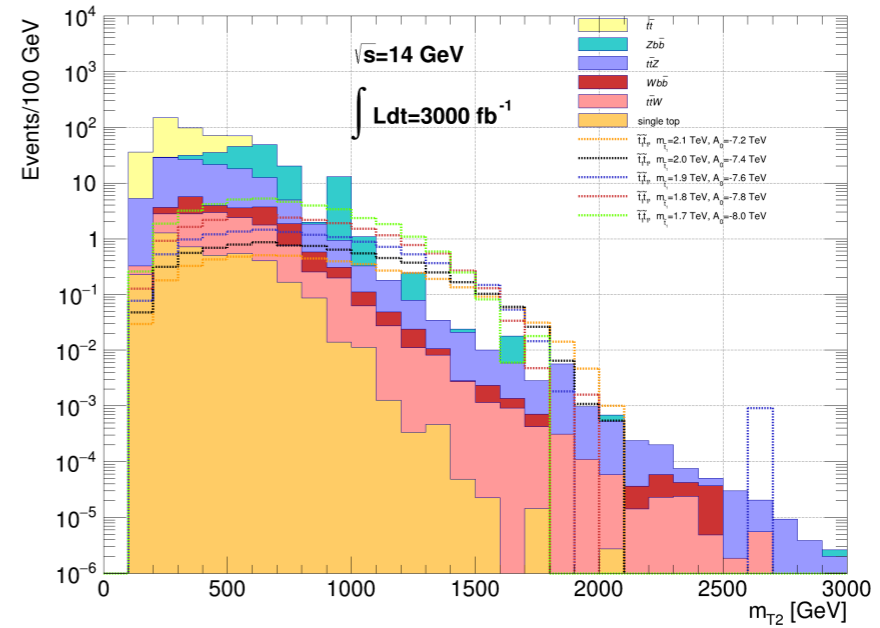
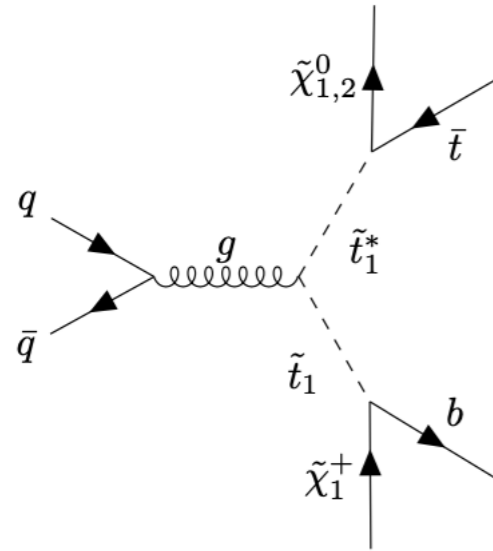
- HB, Barger, Huang, 1107.5581;
- Z. Han, Kribs, Martin, Menon, 1401.1235;
- HB, Mustafayev, Tata; 1409.7058;
- C. Han, Kim, Munir, Park, 1502.03734;
- HB, Barger, Savoy, Tata, 1604.07438;
- HB, Barger, Salam, Sengupta, Tata, 2007.09252;
- HB, Barger, Sengupta, Tata, 2109.14030



It appears that HL-LHC can see much (but not all) of natural SUSY p-space; signal in this channel should **emerge slowly** as more integrated luminosity accrues

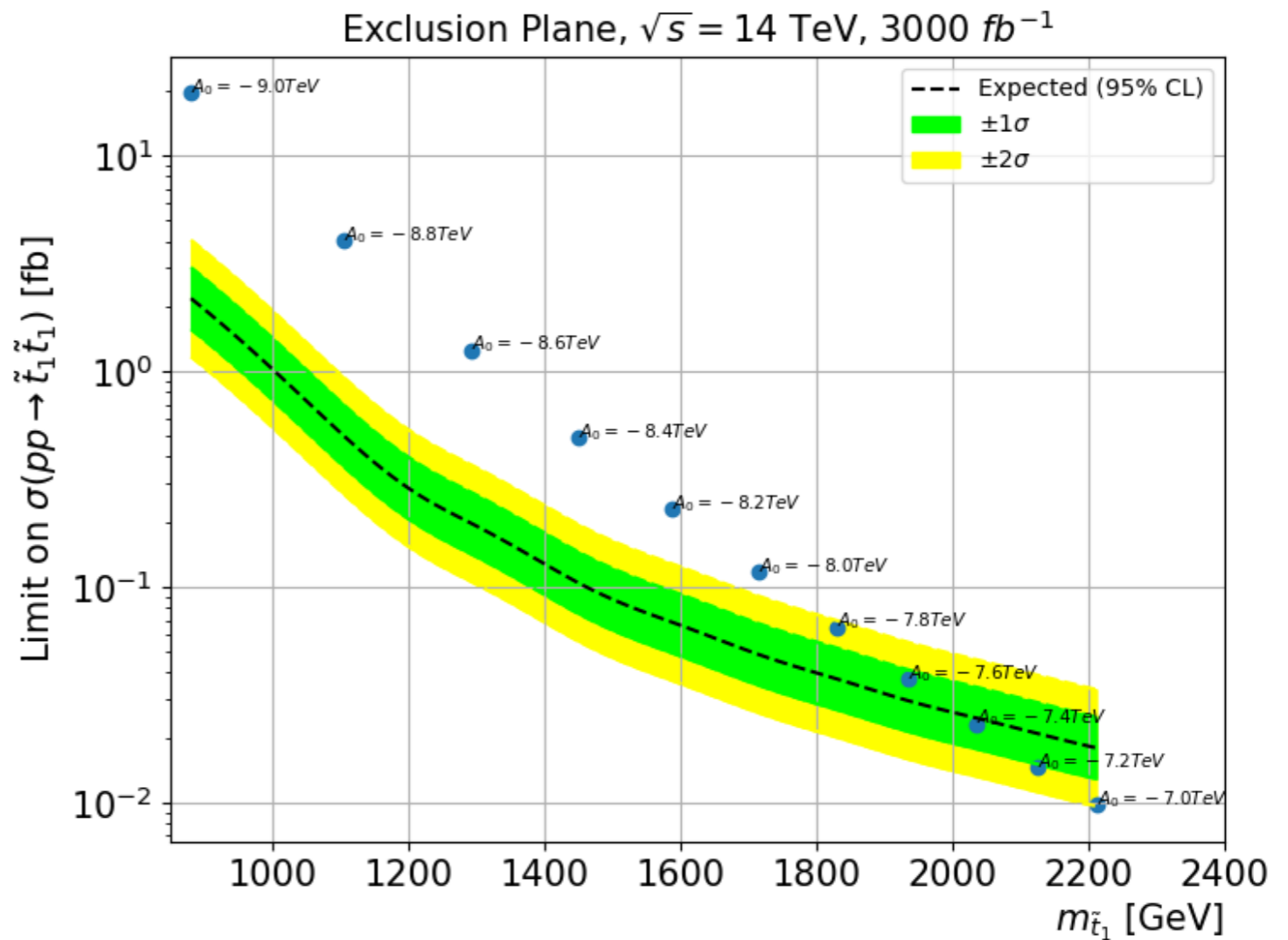
**ATLAS/CMS: 2-sigma excess from Run 2!**

# top-squark pair production:

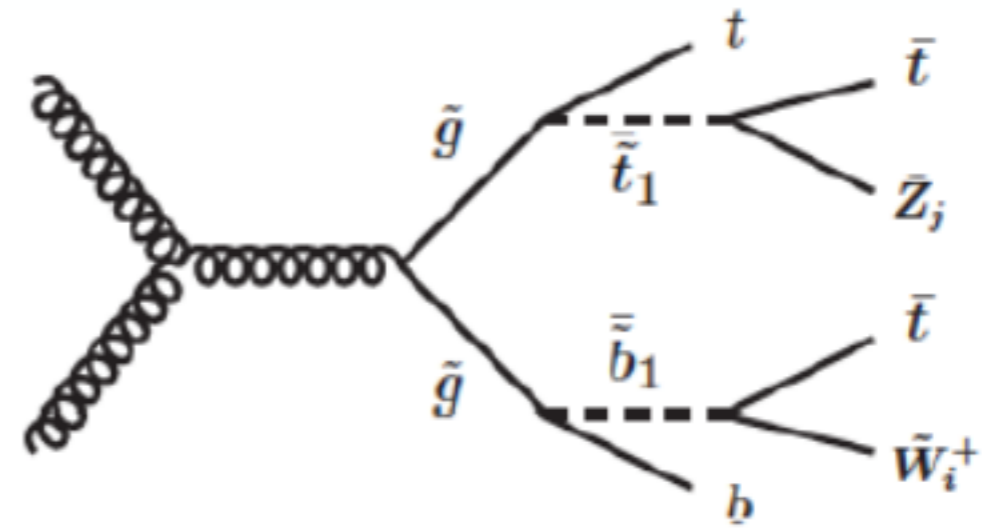


HL-LHC can see  
 $m(t_1) \sim 1.7-2$  TeV  
 @5sigma/ 95% CL

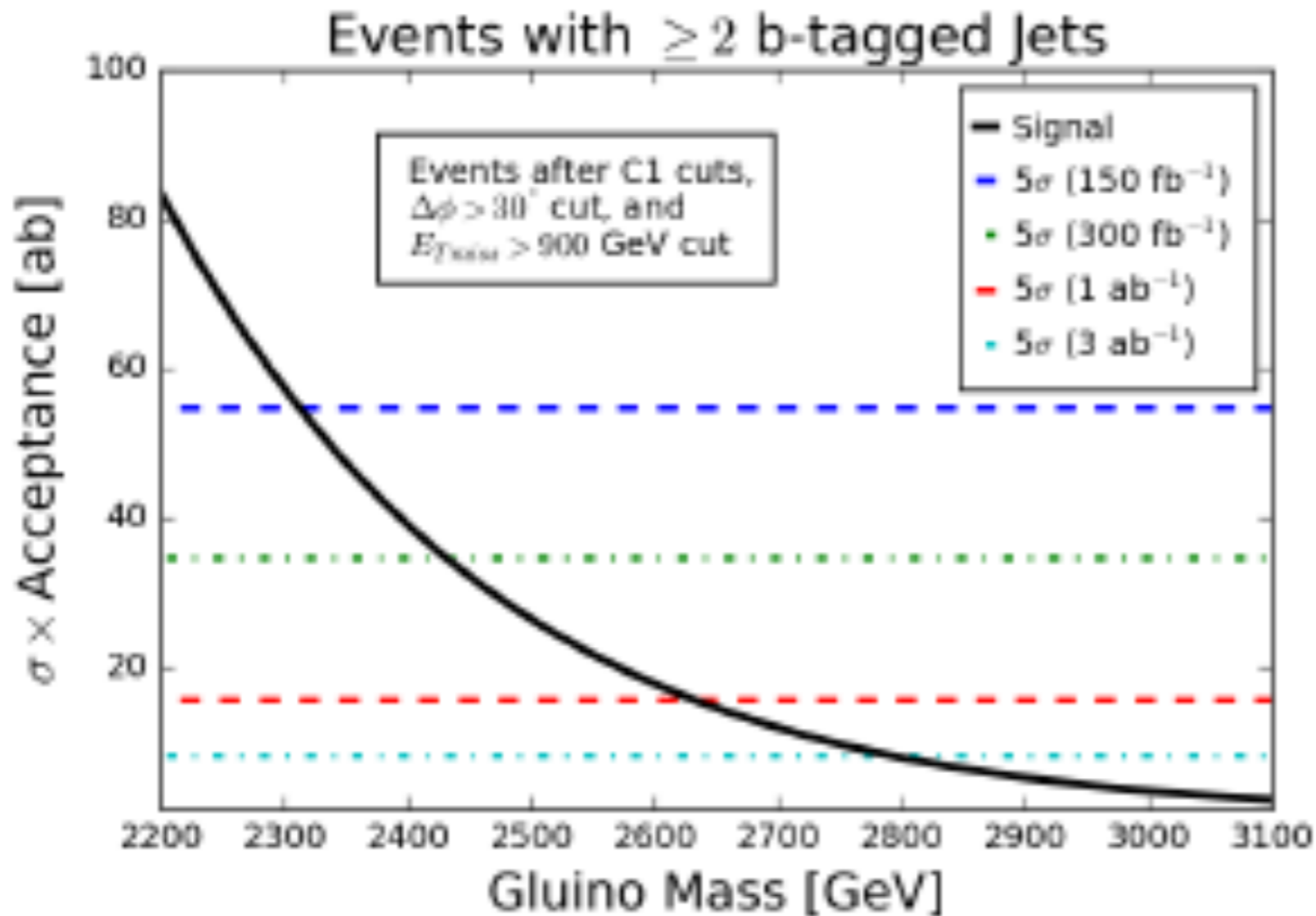
HB, Barger,  
 Dutta, Sengupta, Zhang



# gluino pair cascade decay signatures



LHC14

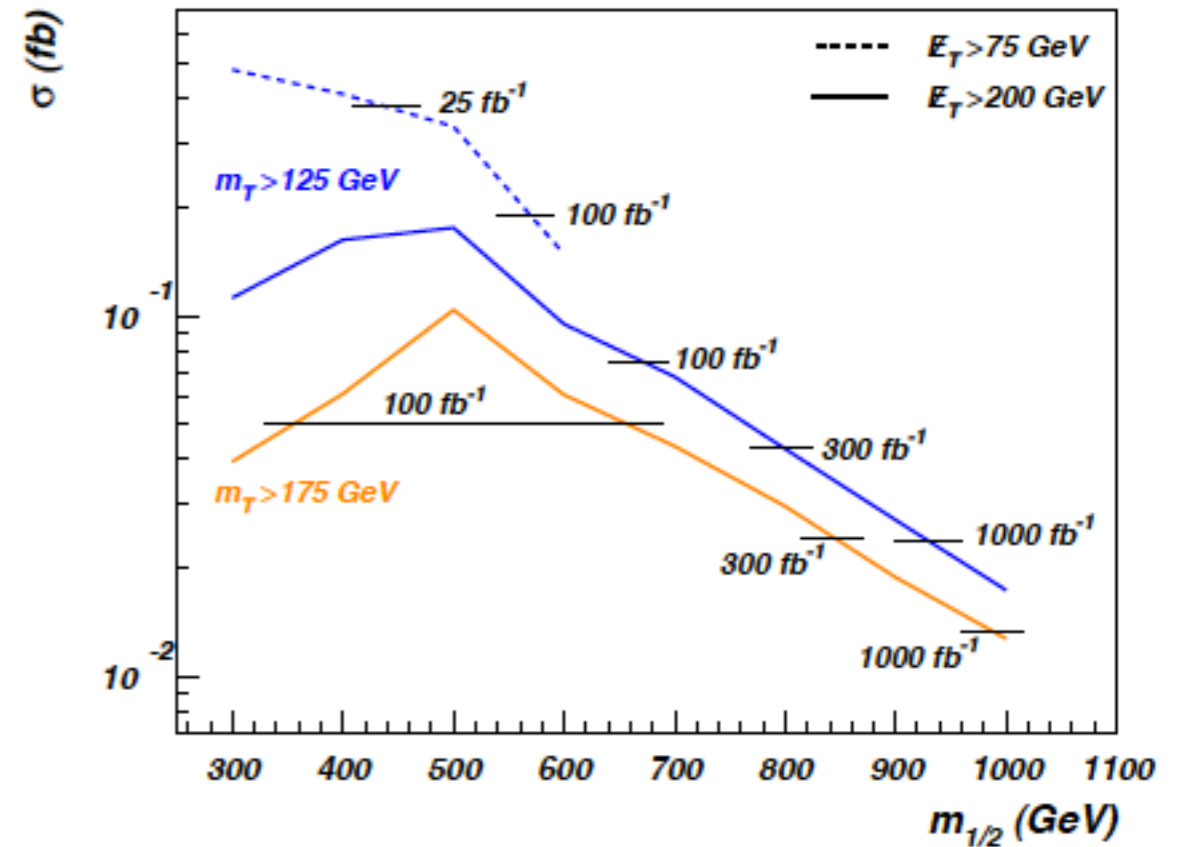
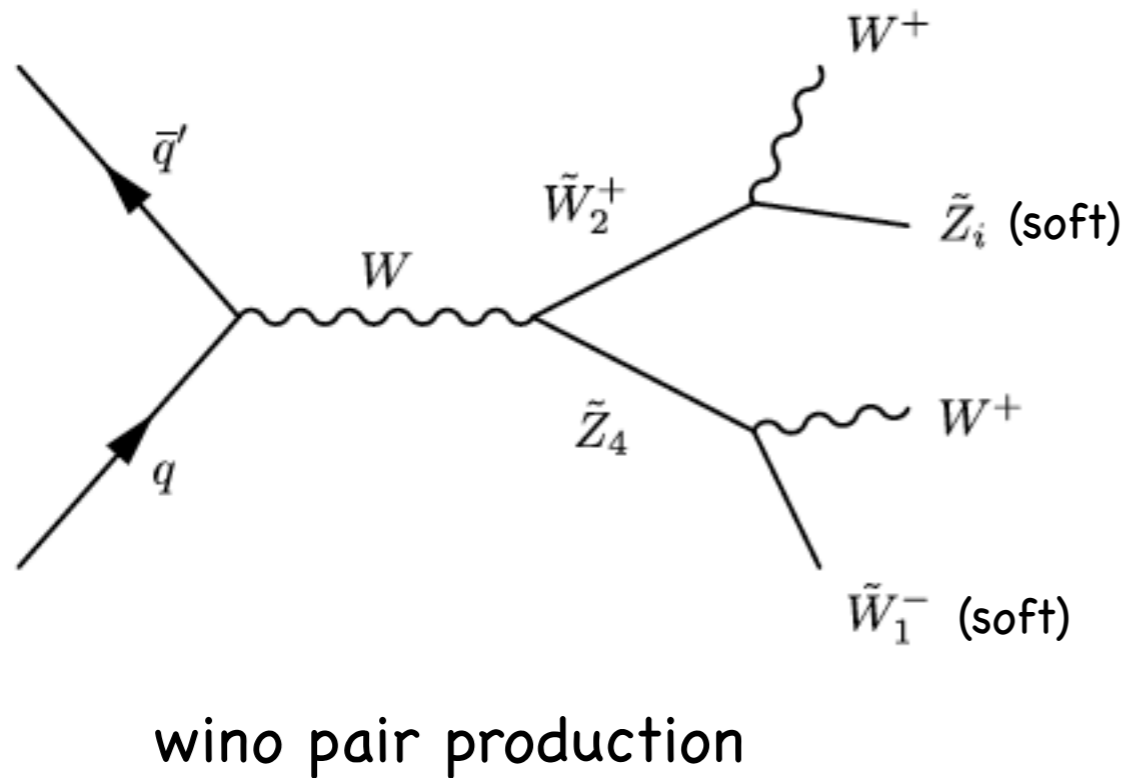


HB, Barger, Gainer, Huang, Savoy, Sengupta, Tata

HL-LHC to probe  $m(\text{gl}) \sim 2.8 \text{ TeV}$

FCC-hh(100) to probe  $m(\text{gl}) \sim 10 \text{ TeV}$

**Distinctive** new same-sign diboson (SSdB)  
signature from SUSY models with light higgsinos!



This channel offers added reach of LHC14 for natSUSY; it is also indicative of wino-pair prod'n followed by decay to higgsinos

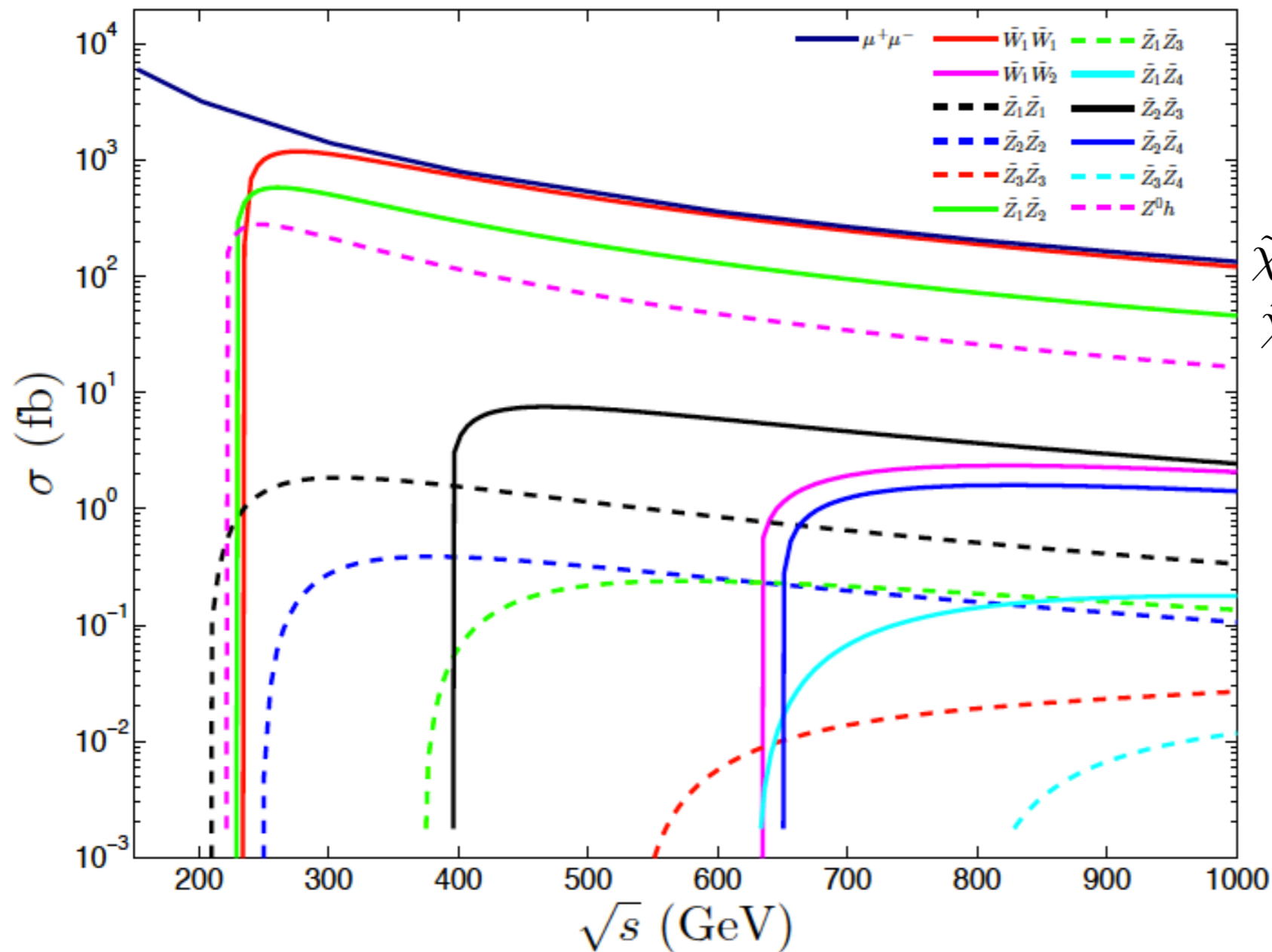
**So far: no distinct ATLAS/CMS analysis**



# Smoking gun signature: light higgsinos at ILC:

ILC is Higgs/higgsino factory!

ILC1:  $m_0 = 7025$  GeV,  $m_{1/2} = 568.3$  GeV,  $A_0 = -11426.6$  GeV,  $\tan\beta = 10$ ,  $\mu = 115$  GeV,  $m_A = 1000$  GeV



$$\sigma(\text{higgsino}) \gg \sigma(Zh)$$

$\tilde{\chi}_1^+ \tilde{\chi}_1^-$   
 $\tilde{\chi}_1^0 \tilde{\chi}_2^0$

3-15 GeV higgsino mass  
 gaps no problem  
 in clean ILC environment

HB, Barger, Mickelson, Mustafayev, Tata  
 arXiv:1404.7510

$$e^+e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow (\ell\nu_\ell \tilde{\chi}_1^0) + (q\bar{q}' \tilde{\chi}_1^0)$$

measure  $m(jj) < m_{\tilde{\chi}_1^\pm} - m_{\tilde{\chi}_1^0}$  and  $E(jj)$

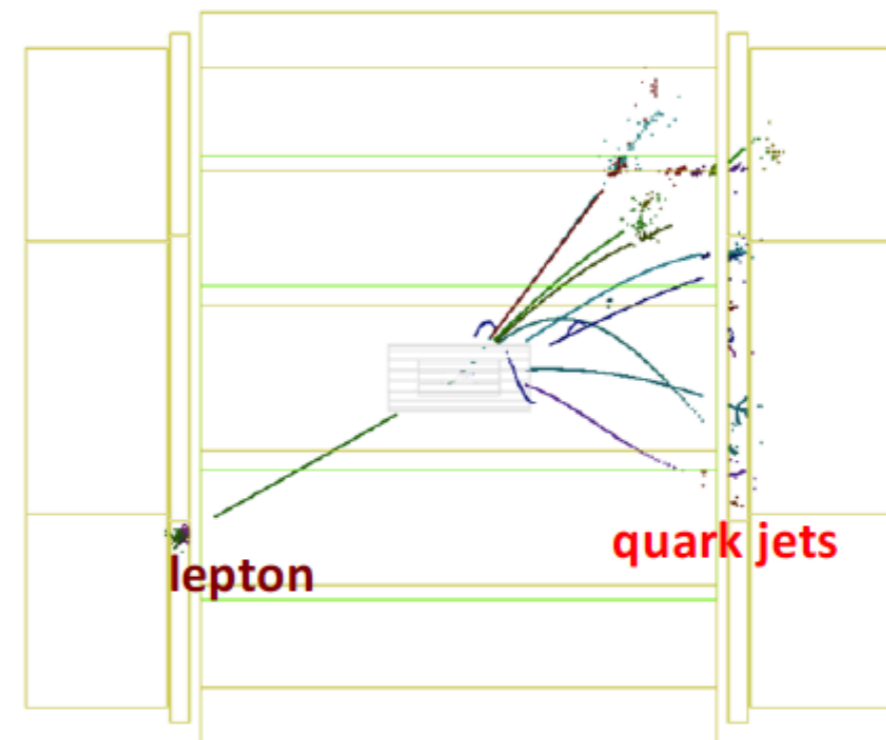
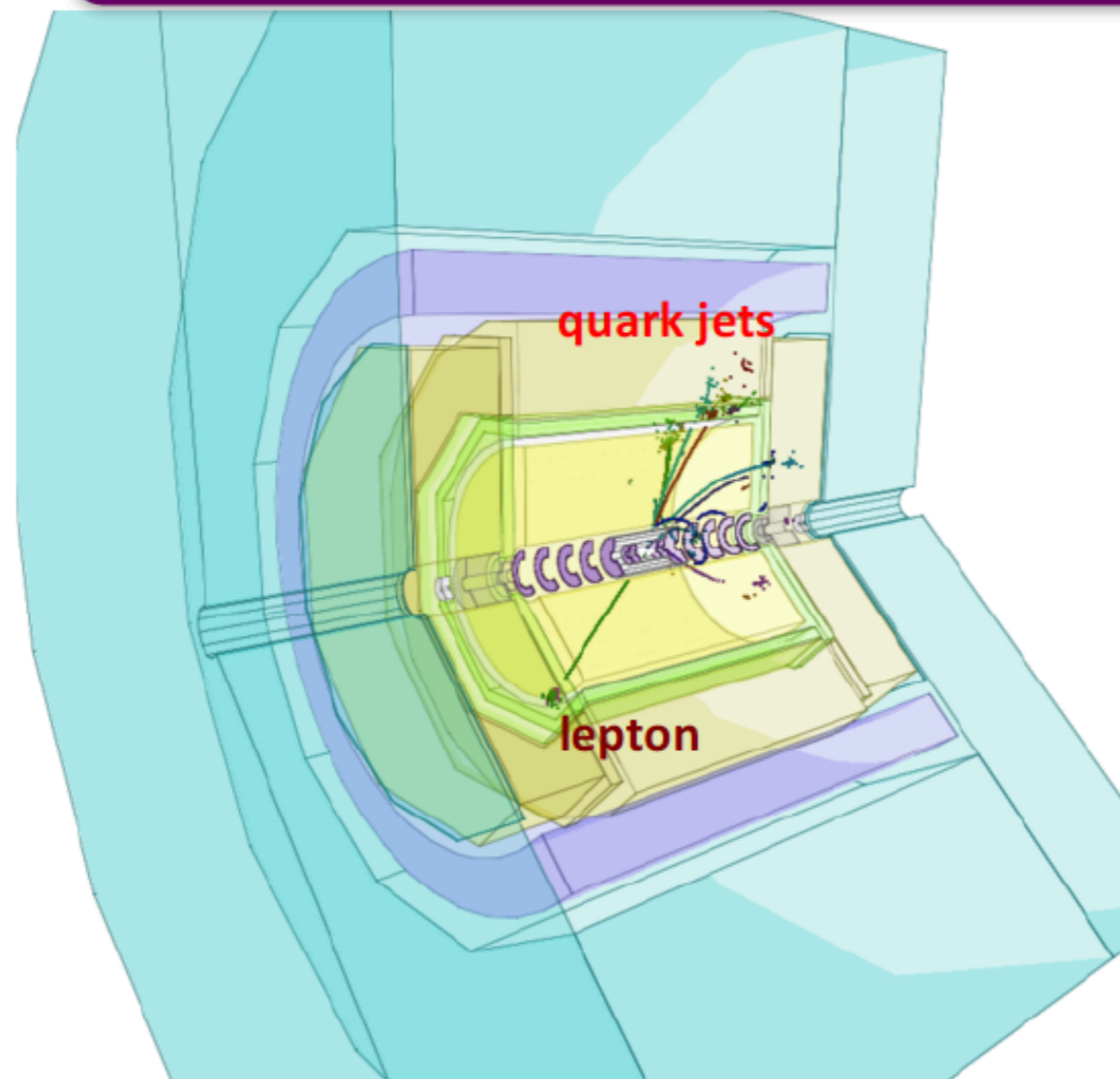
soft visible particles since small higgsino mass gaps

## How do these signals look in the detector? (2)

$\sqrt{s} = 500 \text{ GeV}$

Chargino pair production with semileptonic decay

$$e^+e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 qq' \ell \nu$$



$$e^+e^- \rightarrow \tilde{\chi}_1^0\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 + (\ell^+\ell^-\tilde{\chi}_1^0)$$

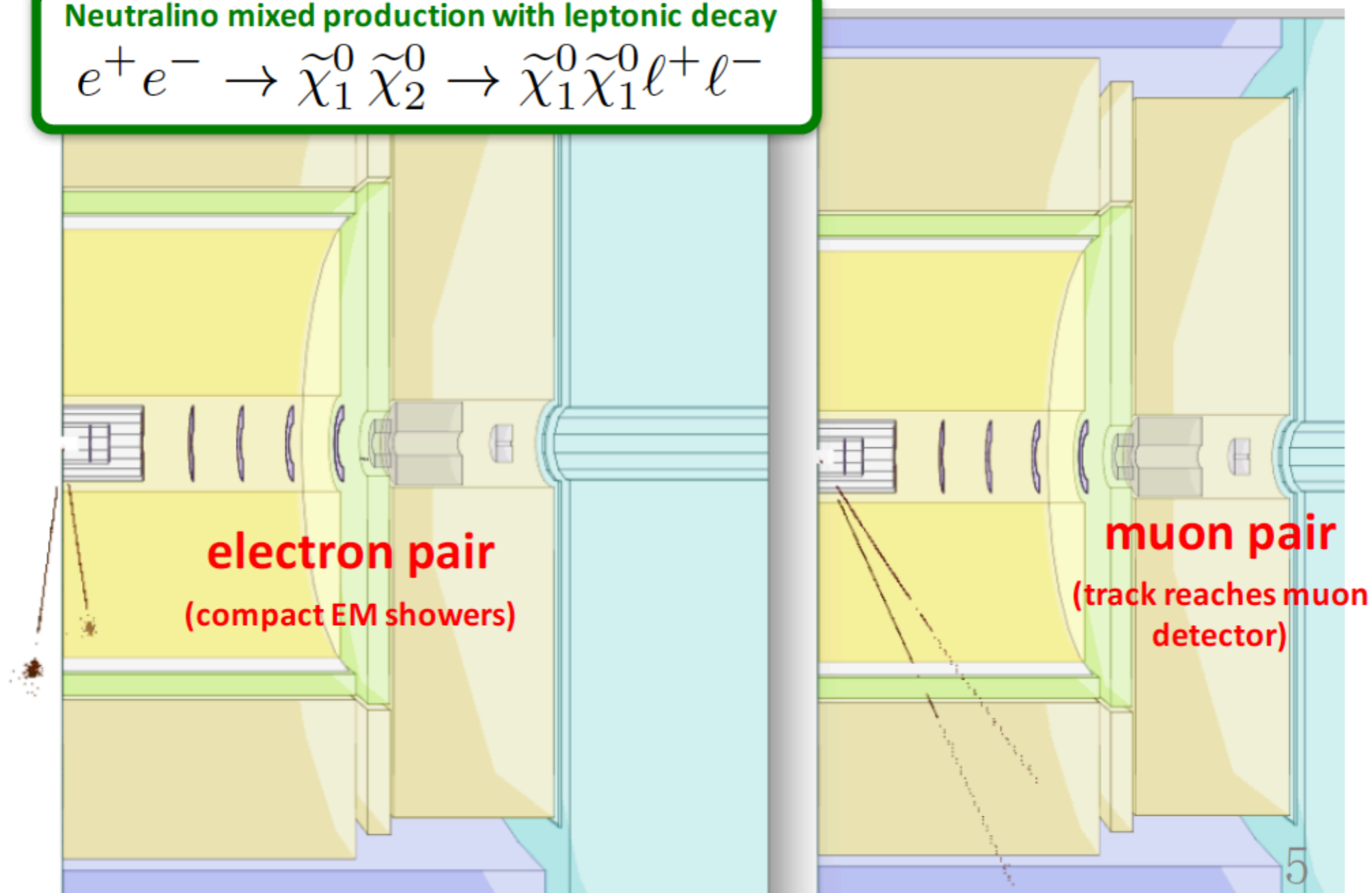
measure  $m(\ell^+\ell^-) < m_{\tilde{\chi}_2^0} - m_{\tilde{\chi}_1^0}$  and  $E(\ell^+\ell^-)$

## How do these signals look in the detector? (1)

$\sqrt{s} = 500 \text{ GeV}$

Neutralino mixed production with leptonic decay

$$e^+e^- \rightarrow \tilde{\chi}_1^0\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0\tilde{\chi}_1^0\ell^+\ell^-$$

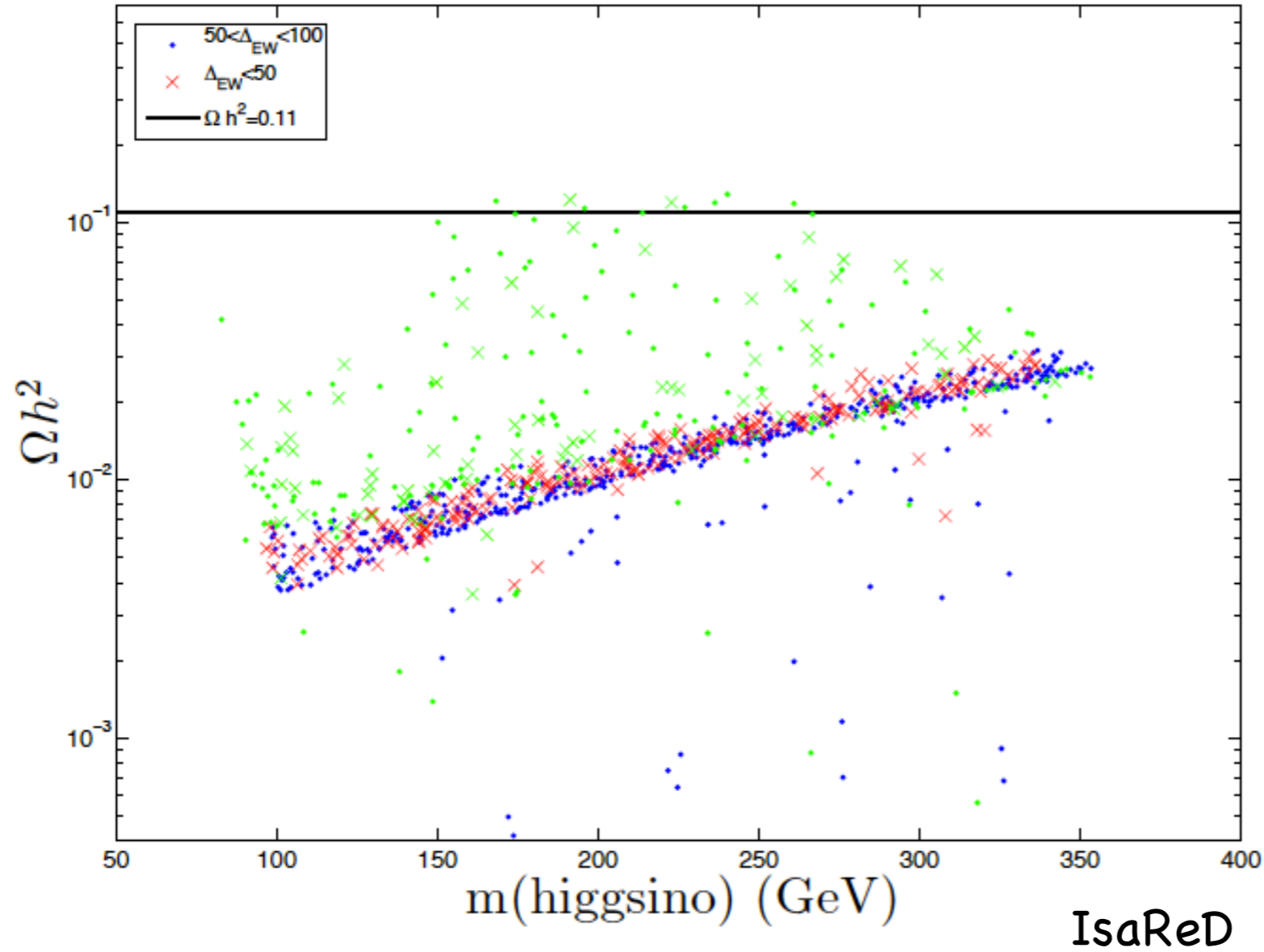


# For further reading:

- The string theory landscape, Bousso & Polchinski, Sci. Am. 291 (2004) 60–69
- Midi-review: Status of weak scale supersymmetry after LHC Run 2 and ton-scale noble liquid WIMP searches, HB, Barger, Salam, Sengupta, Sinha, arXiv: 2002.03013

Dark matter from SUSY  
with radiatively-driven naturalness

Mainly higgsino-like WIMPs thermally underproduce DM



green: excluded;  
red/blue: allowed

HB, Barger, Mickelson

Factor of 10-15 too low

But so far we have addressed only **Part 1**  
of fine-tuning problem:

In QCD sector, the term  $\frac{\bar{\theta}}{32\pi^2} F_{A\mu\nu} \tilde{F}_A^{\mu\nu}$  must occur

But neutron EDM says it is not there: strong CP problem

(frequently ignored by SUSY types)

Best solution after 35 years:  
PQWW/KSVZ/DFSZ **invisible axion**

In SUSY, axion accompanied by axino and saxion

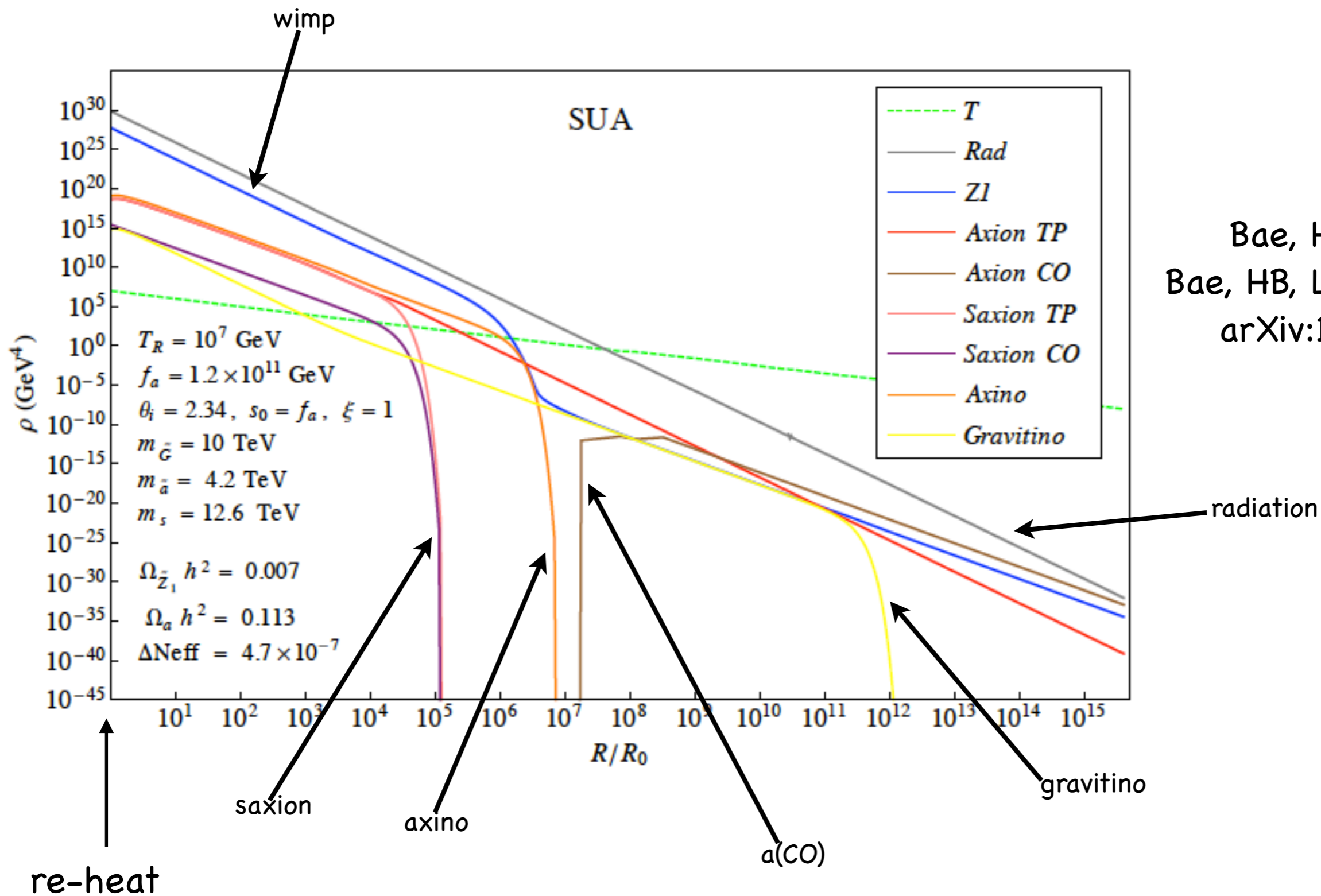
Changes DM calculus:  
expect mixed WIMP/axion DM (**2 particles**)

## mixed axion-neutralino production in early universe: 2 CDM particles

- neutralinos: thermally produced (TP) or NTP via  $\tilde{a}$ ,  $s$  or  $\tilde{G}$  decays
  - re-annihilation at  $T_D^{s,\tilde{a}}$
- axions: TP, NTP via  $s \rightarrow aa$ , bose coherent motion (BCM)
- saxions: TP or via BCM
  - $s \rightarrow gg$ : entropy dilution
  - $s \rightarrow SUSY$ : augment neutralinos
  - $s \rightarrow aa$ : dark radiation ( $\Delta N_{eff} < 1.6$ )
- axinos: TP
  - $\tilde{a} \rightarrow SUSY$  augments neutralinos
- gravitinos: TP, decay to SUSY



# DM production in SUSY DFSZ: solve eight coupled Boltzmann equations

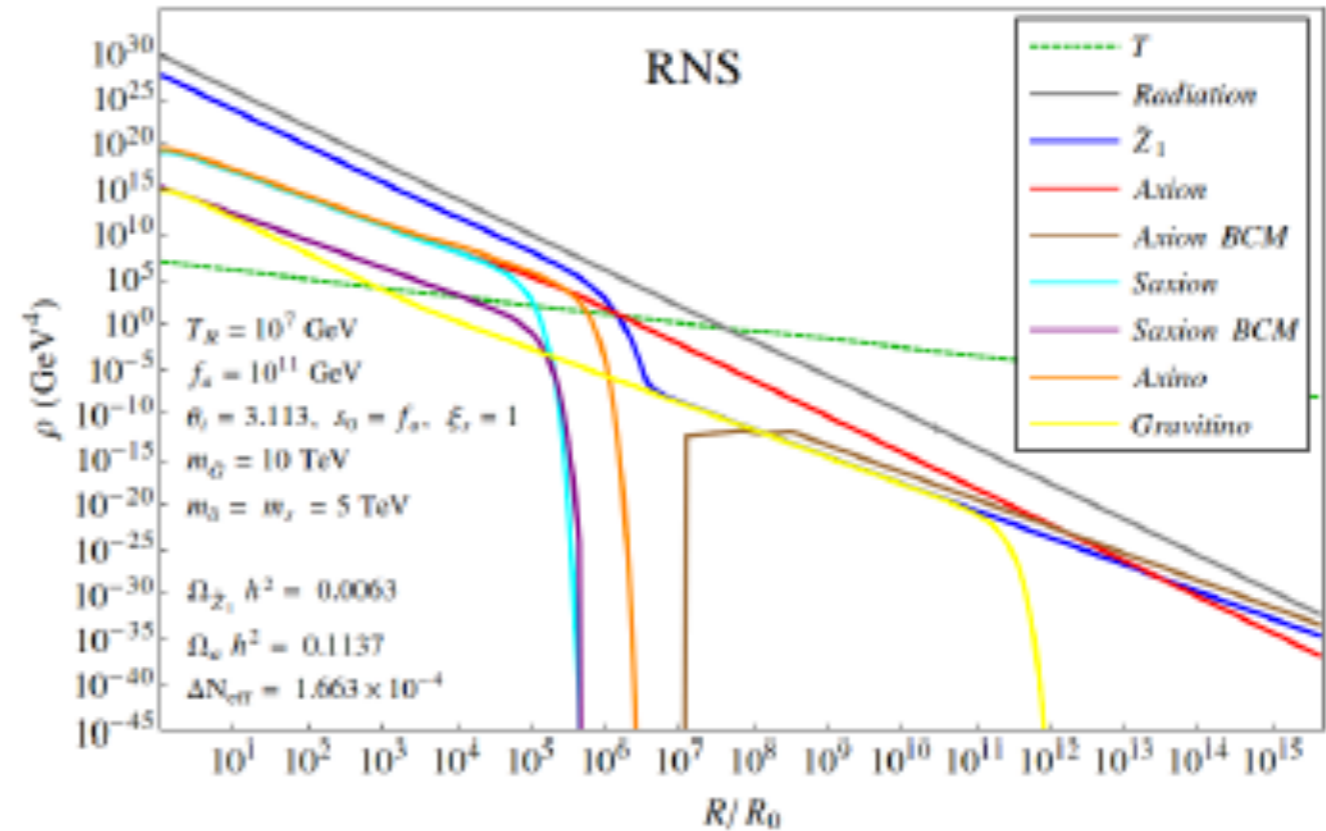
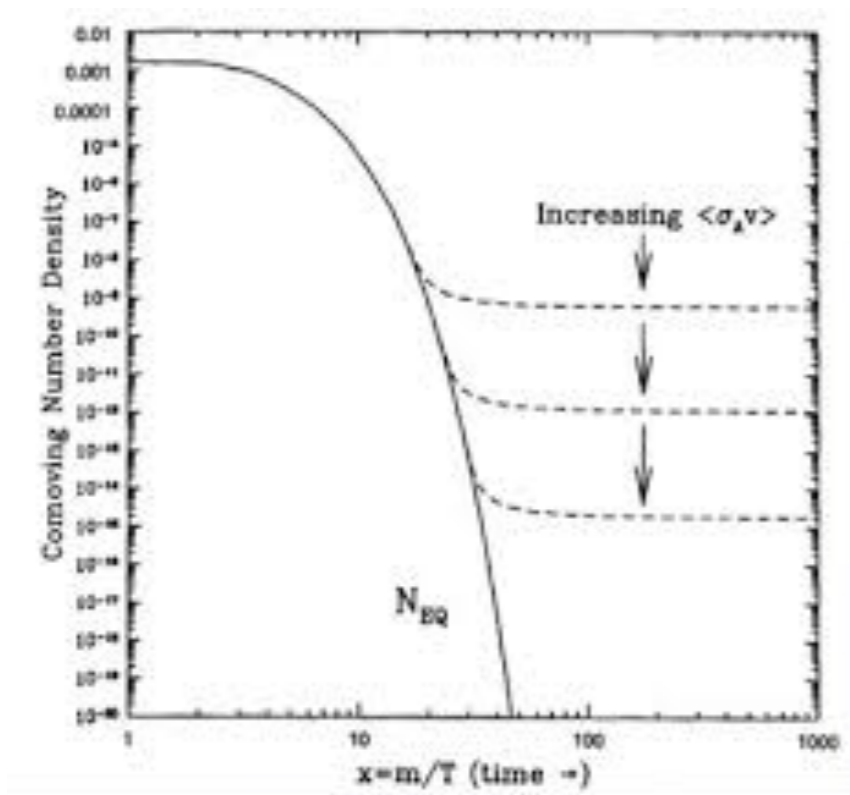


Bae, HB, Chun;  
Bae, HB, Lessa, Serce;  
arXiv:1406.4138

usual picture

=>

mixed axion/WIMP



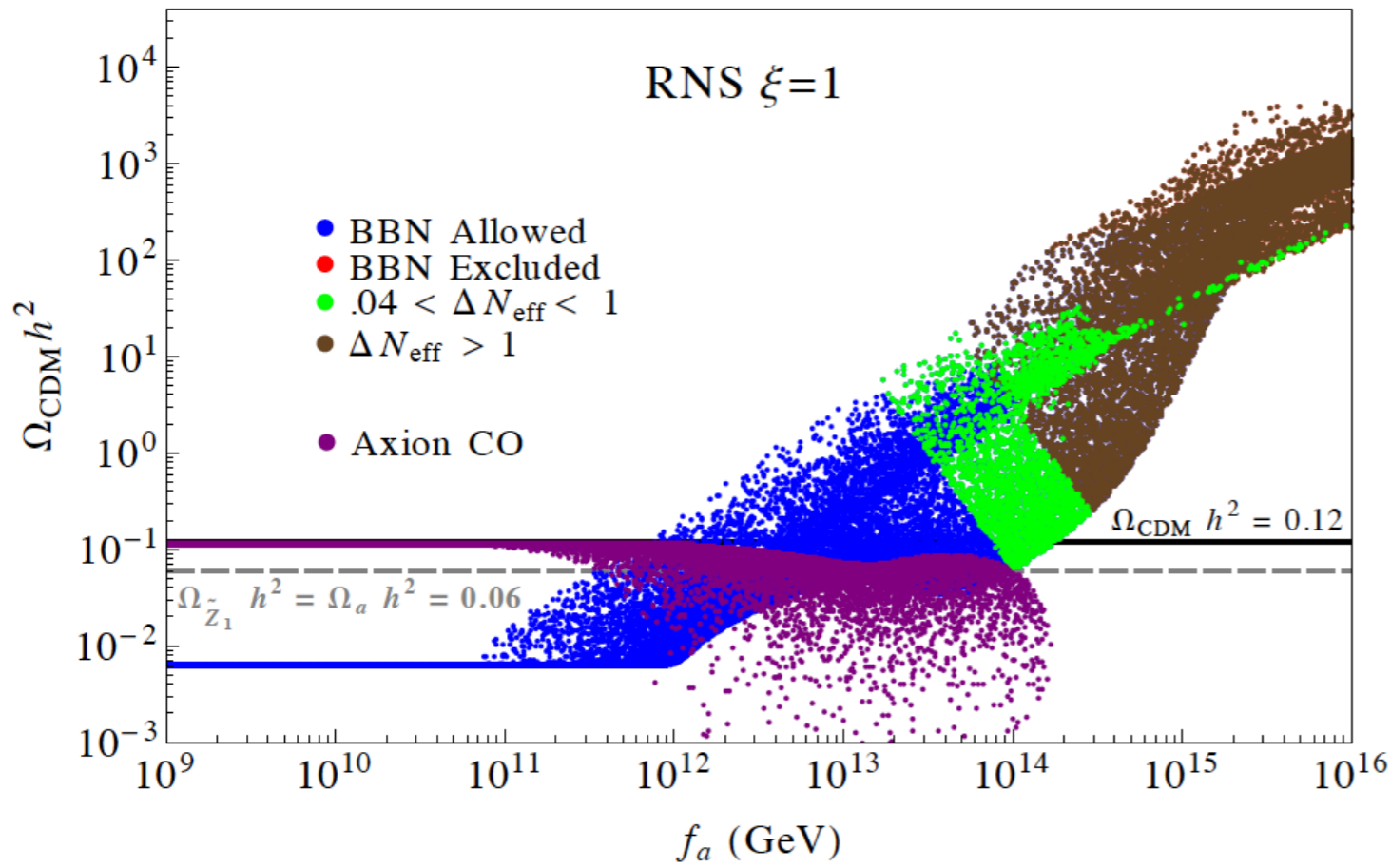
KJ Bae, HB, Lessa, Serce

much of parameter space is axion-dominated  
with 10-15% WIMPs



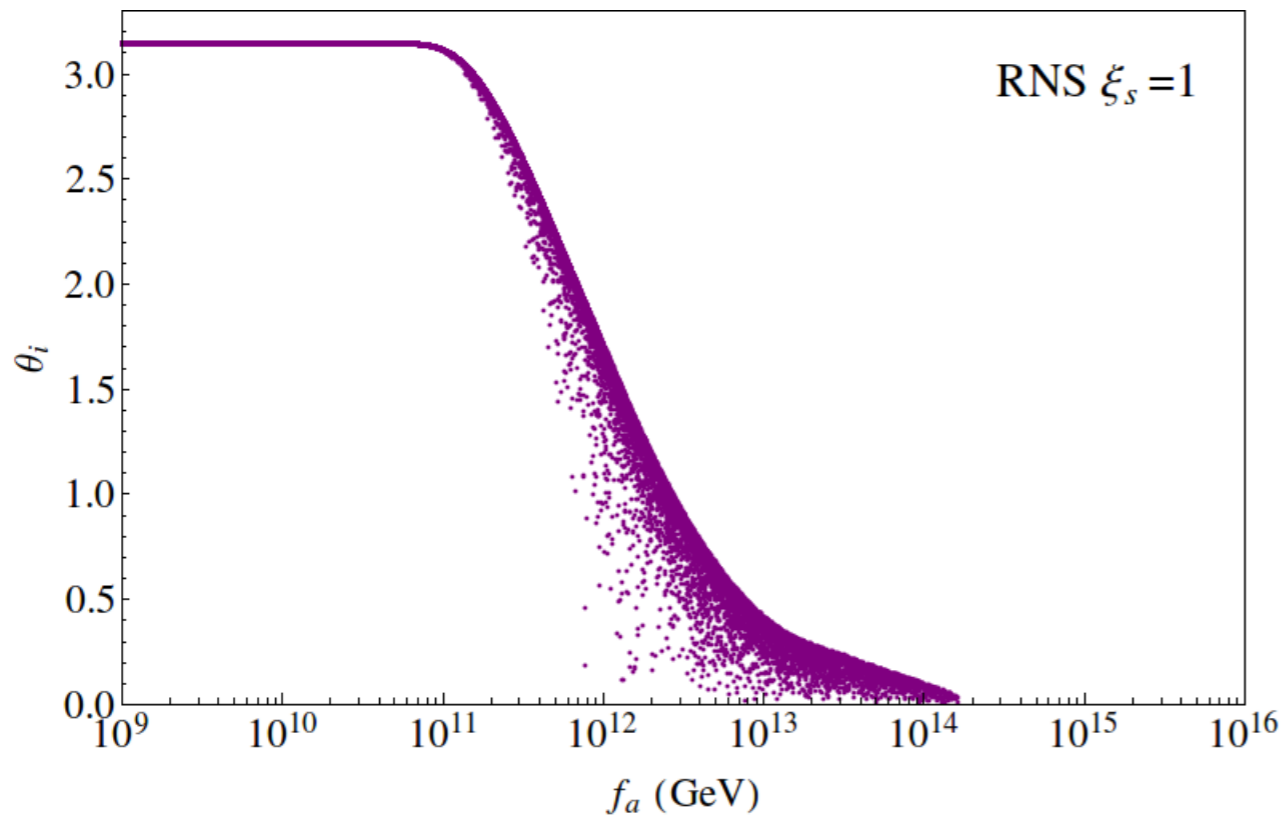
$\Rightarrow$





higgsino abundance

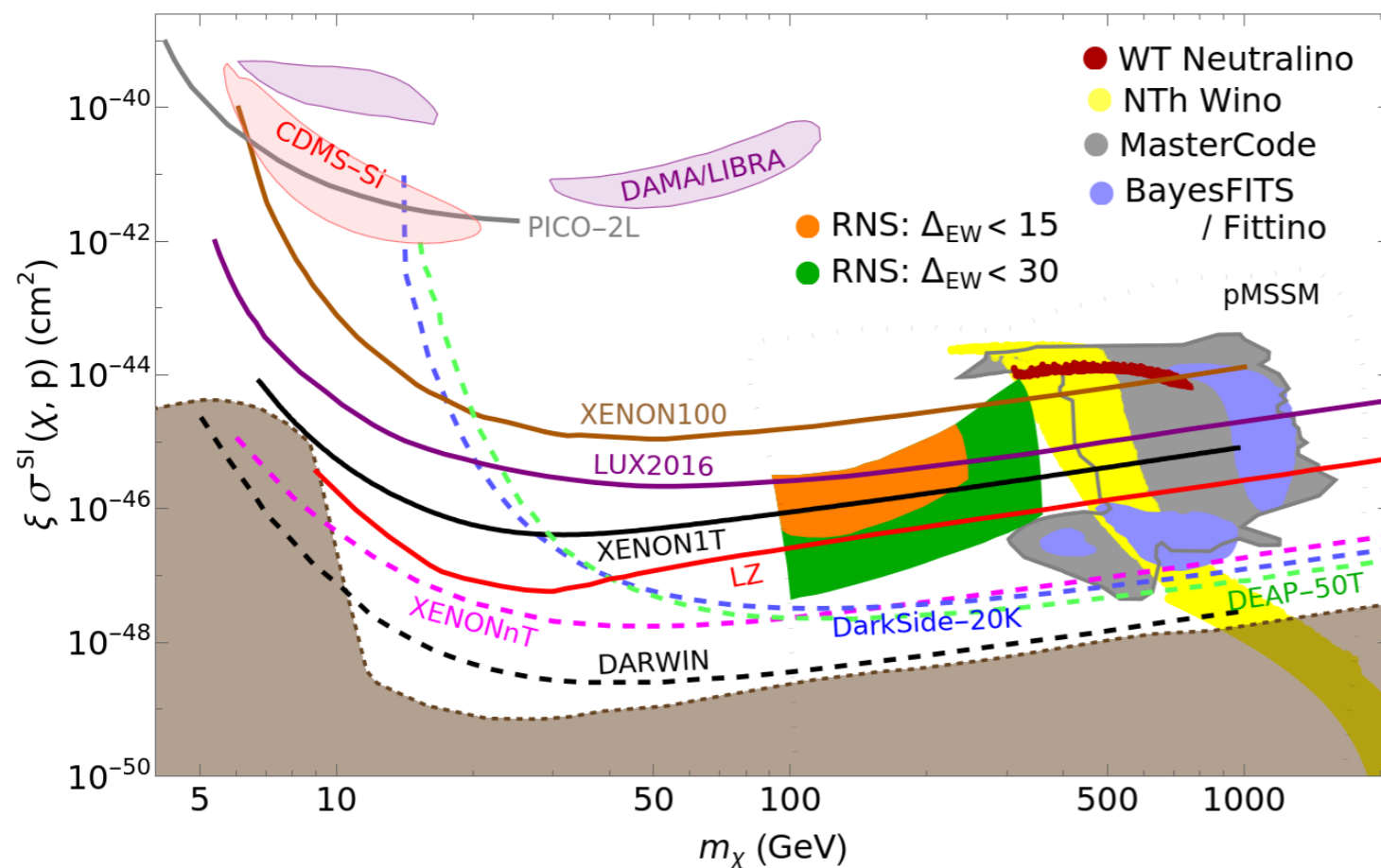
axion abundance



mainly axion CDM  
for  $f_a < \sim 10^{12}$  GeV;  
for higher  $f_a$ , then get increasing  
wimp  
abundance

# Direct higgsino detection rescaled

for minimal local abundance  $\xi \equiv \Omega_{\chi}^{TP} h^2 / 0.12$



Bae, HB, Barger, Savoy, Serce

$$\mathcal{L} \ni -X_{11}^h \bar{\tilde{Z}}_1 \tilde{Z}_1 h$$

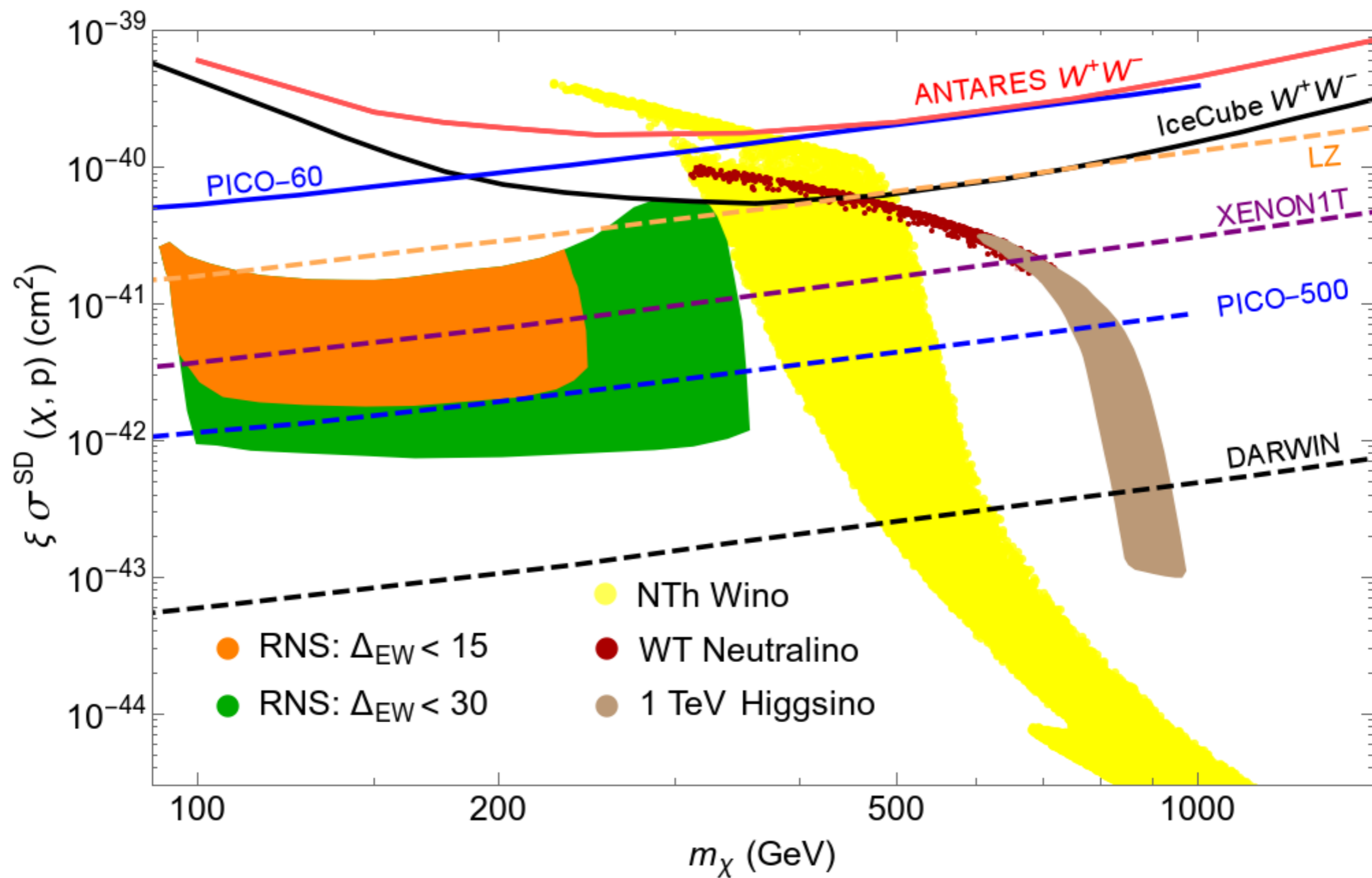
$$X_{11}^h = -\frac{1}{2} (v_2^{(1)} \sin \alpha - v_1^{(1)} \cos \alpha) (g v_3^{(1)} - g' v_4^{(1)})$$

includes latest  
LZ2022 results!

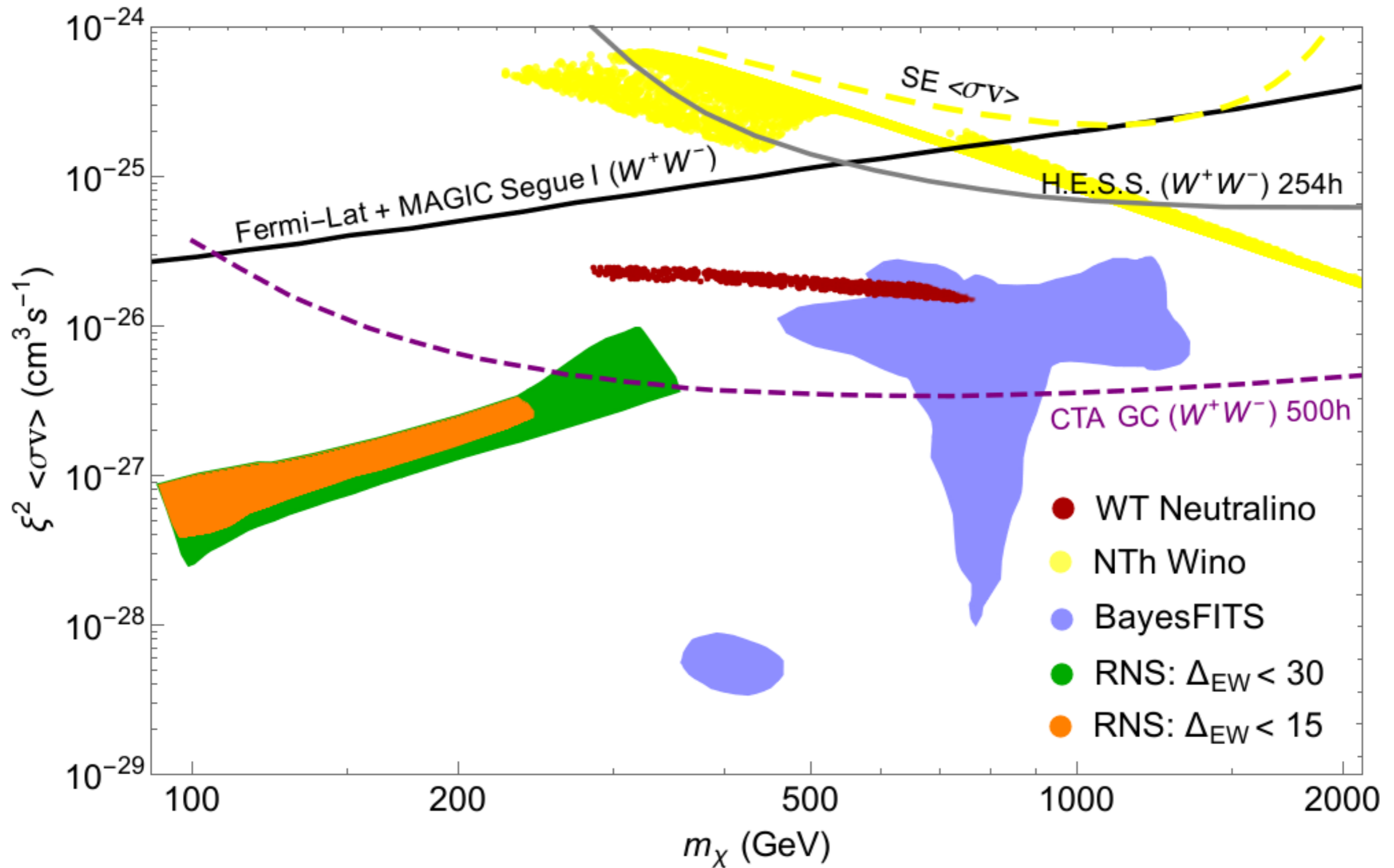
natural SUSY

Can test completely with multi-ton scale detector  
or equivalent (subject to minor caveats)

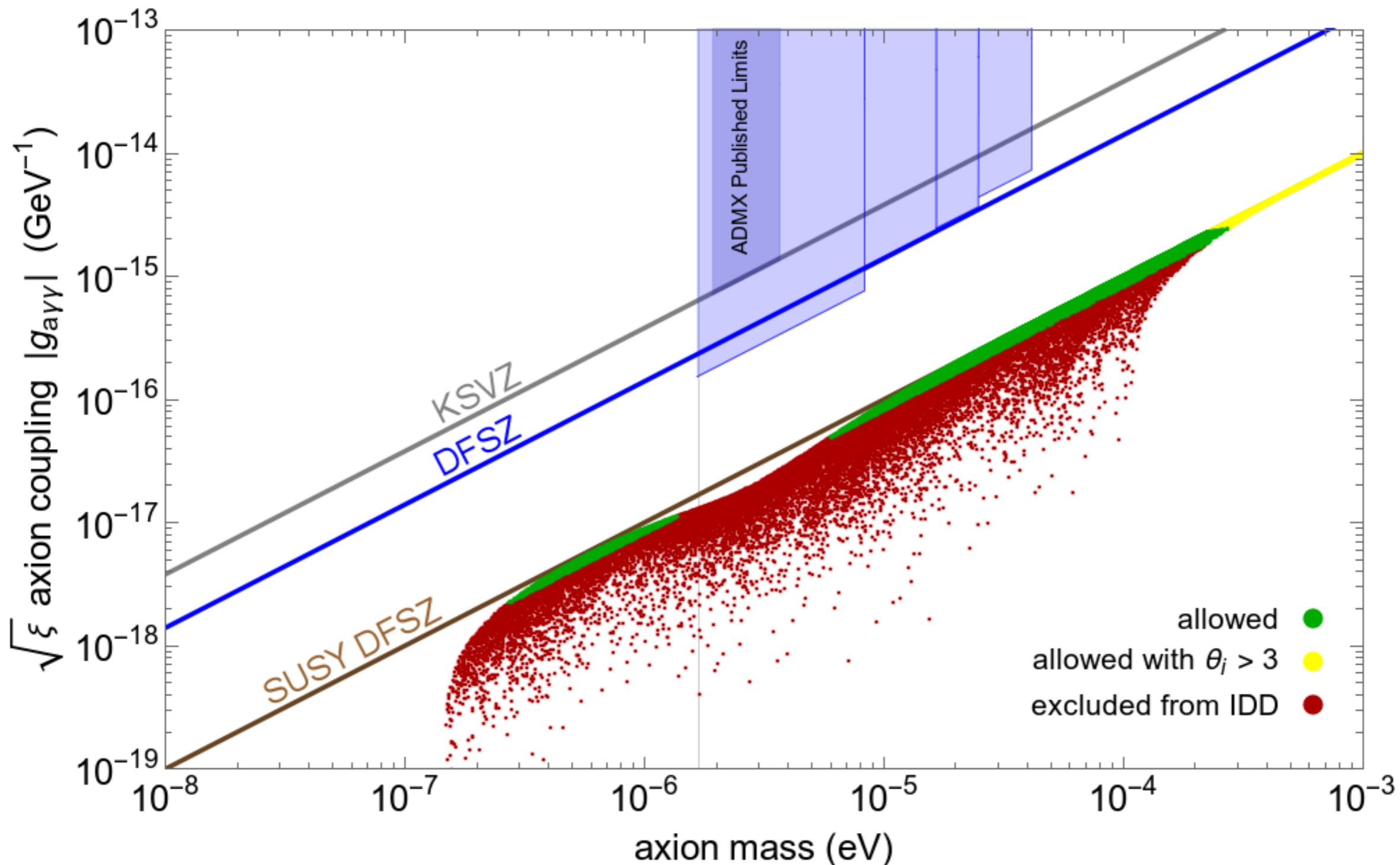
# Prospects for SD WIMP searches:



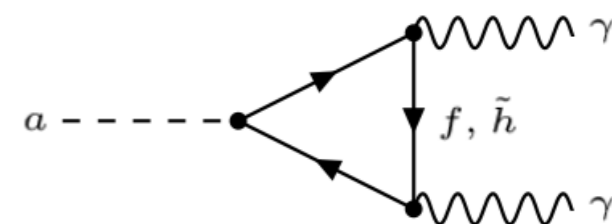
# Prospects for IDD WIMP searches:



suppressed by square of diminished WIMP abundance



SUSY DFSZ axion: large range in  $m(a)$  but coupling reduced  
 may need to probe broader and deeper!





# SUSY solution to axion quality problem!

Gravity safe, electroweak natural axionic solution to strong CP and SUSY  $\mu$  problems

HB, Barger, Sengupta, arXiv:1810.03713

1. Global symmetries fundamentally incompatible with gravity completion
2. Expect global symmetry to emerge as accidental (approximate) symmetry from some more fundamental gravity-safe (e.g. gauge or R-) symmetry
3. Discrete R-symmetries (intrinsically supersymmetric) and arise from compactification of extra dimensions in string theory

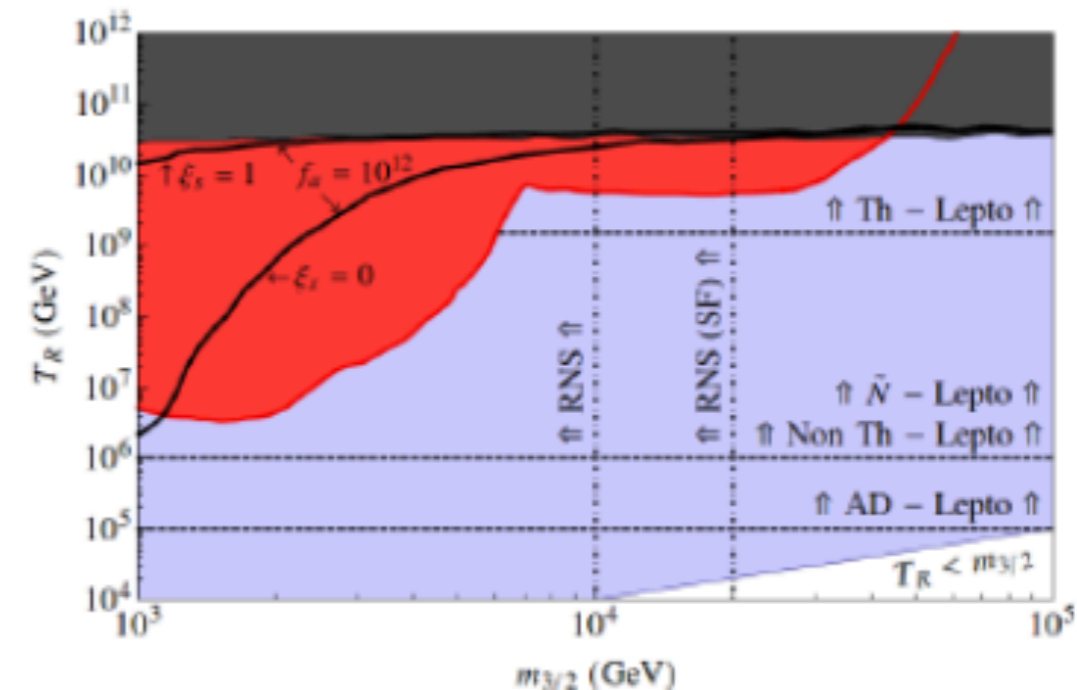
A model which works: Z(24) R symmetry (see also Lee et al.)

$$W \ni f_u Q H_u U^c + f_d Q H_d D^c + f_\ell L H_d E^c + f_\nu L H_u N^c + M_N N^c N^c / 2 + \lambda_\mu X^2 H_u H_d / m_P + f X^3 Y / m_P + \lambda_3 X^p Y^q / m_P^{p+q-3}$$

- Lowest dimension PQ breaking operator contributing to scalar PQ potential  $\sim 1/m_P^8$ : enough suppression so that PQ is gravity-safe
- Also forbids/suppresses RPV/p-decay operators
- $\mu \sim \lambda_\mu f_a^2 / m_P$

# Baryogenesis scenarios for radiative natural SUSY

- thermal leptogenesis
- non-thermal (inflaton decay)
- oscillating sneutrino
- Affleck-Dine (AD)



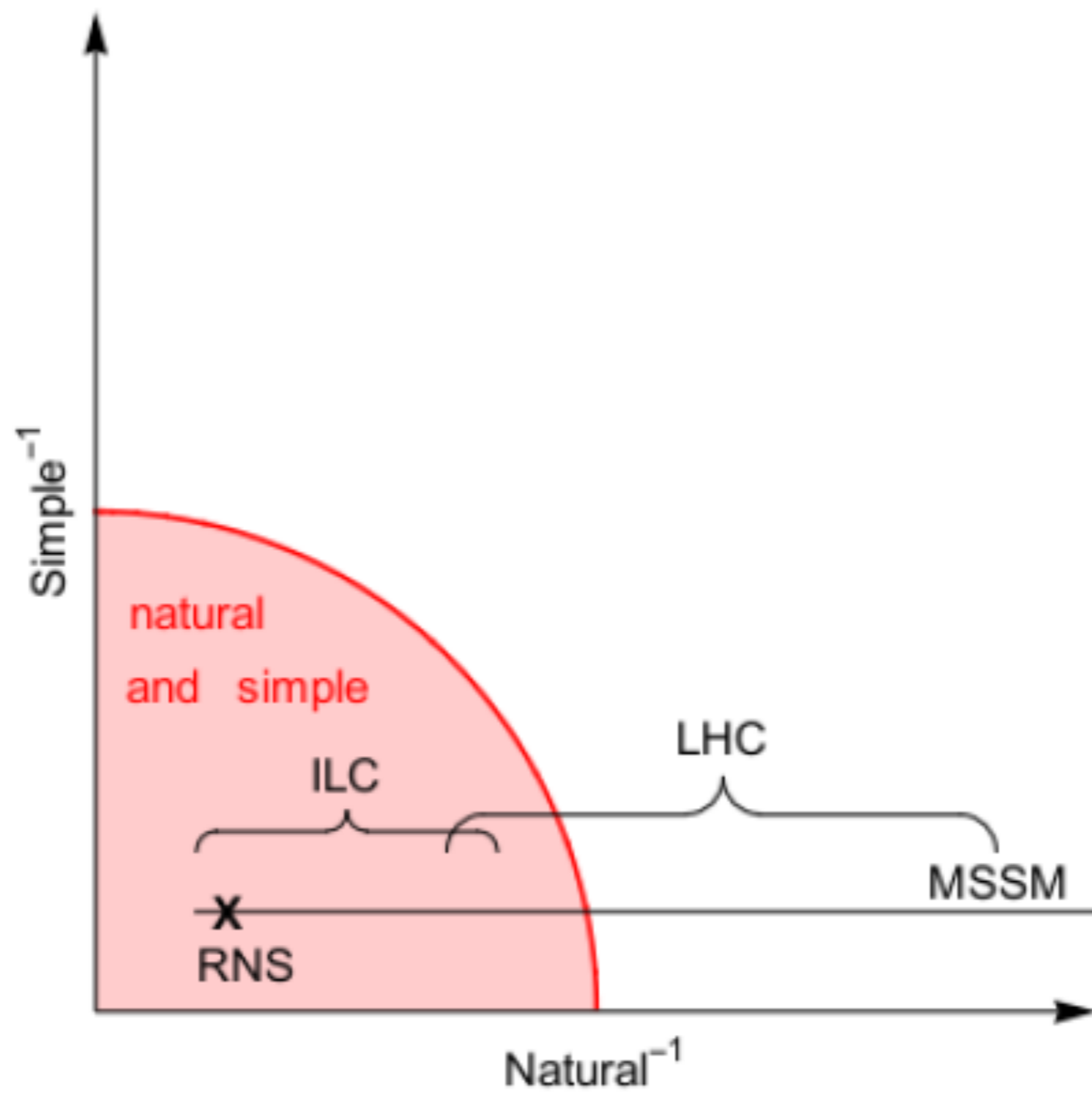
gravitino problem plus  
axino/saxion problem:  
still plenty room

$$f_a = 10^{11}, 10^{12} \text{ GeV}$$

Bae, HB, Serce, Zhang, arXiv:1510.00724

# Conclusions:

- Time to set aside old notions of naturalness:
- Plenty of natural parameter space under model independent measure DEW
- $\mu \sim 100\text{--}350$  GeV: **light higgsinos!**
- other sparticle contributions to  $m(\text{weak})$  are loop suppressed- masses can be TeV-  
>multi-TeV
- stringy naturalness: **what the string landscape prefers**
- draw to large soft terms provided  $m(\text{weak}) \sim (2\text{--}5) * 100$  GeV
- predicts LHC sees  $m_h \sim 125$  GeV but as yet no sign of sparticles
- LHC best bet: higgsino pair production/soft dileptons: **small excess ATLAS/CMS**
- under stringy naturalness, a 3 TeV gluino more natural than 300 GeV gluino
- landscape  $\rightarrow$  non-universal 1st/2nd gen. scalars at 20-40 TeV: natural but gives quasi-degeneracy/decoupling sol'n to SUSY flavor, CP and cosmological moduli problems
- dark matter: a mix of axions+higgsino-like WIMPs (typically mainly axions)
- SUSY solves axion quality problem via  $Z(24)^R$  symmetry



## #2: Higgs mass or large-log fine-tuning

 $\Delta_{HS}$ 

It is tempting to pick out one-by-one quantum fluctuations **but** must combine log divergences before taking any limit

$$m_h^2 \simeq \mu^2 + m_{H_u}^2 + \delta m_{H_u}^2|_{rad}$$

$$\frac{dm_{H_u}^2}{dt} = \frac{1}{8\pi^2} \left( -\frac{3}{5}g_1^2 M_1^2 - 3g_2^2 M_2^2 + \frac{3}{10}g_1^2 S + 3f_t^2 X_t \right) \quad X_t = m_{Q_3}^2 + m_{U_3}^2 + m_{H_u}^2 + A_t^2$$

neglect gauge pieces, S,  $m_{H_u}$  and running;  
then we can integrate from  $m(SUSY)$  to  $\Lambda$

$$\delta m_{H_u}^2 \sim -\frac{3f_t^2}{8\pi^2} (m_{Q_3}^2 + m_{U_3}^2 + A_t^2) \ln(\Lambda/m_{SUSY})$$

$$\Delta_{HS} \sim \delta m_h^2 / (m_h^2/2) < 10$$

$$m_{\tilde{t}_{1,2}, \tilde{b}_1} < 500 \text{ GeV}$$

$$m_{\tilde{g}} < 1.5 \text{ TeV}$$

**old natural SUSY**

then

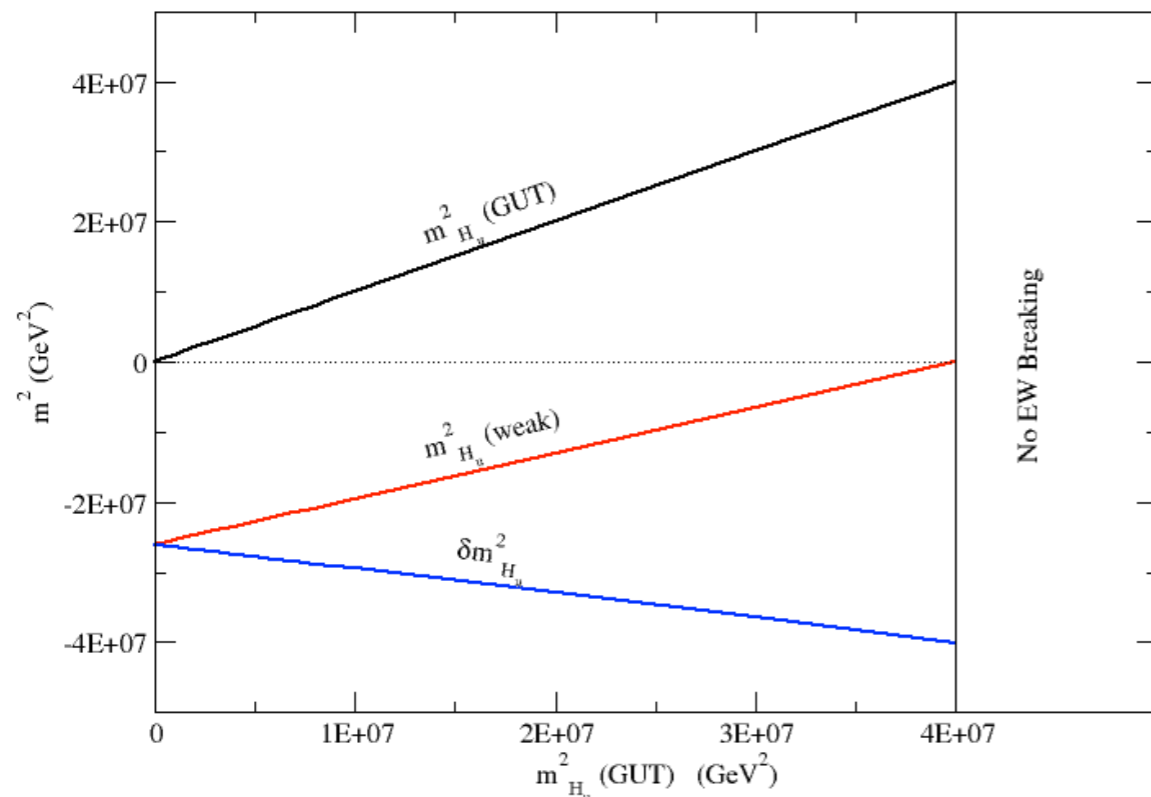
$A_t$  can't be too big

What's wrong with this argument?

In zeal for simplicity, have made several simplifications: most **egregious** is that one sets  $m(H_u)^2=0$  at beginning to simplify

$m_{H_u}^2(\Lambda)$  and  $\delta m_{H_u}^2$  are *not* independent!

**violates prime directive!**



The larger  $m_{H_u}^2(\Lambda)$  becomes, then the larger becomes the cancelling correction!

HB, Barger, Savoy

To fix: combine dependent terms:

$$m_h^2 \simeq \mu^2 + (m_{H_u}^2(\Lambda) + \delta m_{H_u}^2) \text{ where now both } \mu^2 \text{ and } (m_{H_u}^2(\Lambda) + \delta m_{H_u}^2) \text{ are } \sim m_Z^2$$

After re-grouping:

$$\Delta_{HS} \simeq \Delta_{EW}$$

Instead of: the radiative correction  $\delta m_{H_u}^2 \sim m_Z^2$   
we now have: the radiatively-corrected  $m_{H_u}^2 \sim m_Z^2$

Recommendation: put this horse out to pasture

$$\delta m_{H_u}^2 \sim -\frac{3f_t^2}{8\pi^2} (m_{Q_3}^2 + m_{U_3}^2 + A_t^2) \ln(\Lambda/m_{SUSY})$$

R.I.P.

sub-TeV 3rd generation squarks **not** required for naturalness



### #3. What about EENZ/BG measure?

$$\Delta_{BG} = \max_i \left| \frac{\partial \log m_Z^2}{\partial \log p_i} \right| = \max_i \left| \frac{p_i}{m_Z^2} \frac{\partial m_Z^2}{\partial p_i} \right|$$

$p_i$  are the theory parameters

applied to pMSSM, then  $\Delta_{BG} \simeq \Delta_{EW}$

apply to high (e.g. GUT) scale parameters

$$\begin{aligned} m_Z^2 \simeq & -2.18\mu^2 + 3.84M_3^2 + 0.32M_3M_2 + 0.047M_1M_3 - 0.42M_2^2 \\ & + 0.011M_2M_1 - 0.012M_1^2 - 0.65M_3A_t - 0.15M_2A_t \\ & - 0.025M_1A_t + 0.22A_t^2 + 0.004M_3A_b \\ & - 1.27m_{H_u}^2 - 0.053m_{H_d}^2 \\ & + 0.73m_{Q_3}^2 + 0.57m_{U_3}^2 + 0.049m_{D_3}^2 - 0.052m_{L_3}^2 + 0.053m_{E_3}^2 \\ & + 0.051m_{Q_2}^2 - 0.11m_{U_2}^2 + 0.051m_{D_2}^2 - 0.052m_{L_2}^2 + 0.053m_{E_2}^2 \\ & + 0.051m_{Q_1}^2 - 0.11m_{U_1}^2 + 0.051m_{D_1}^2 - 0.052m_{L_1}^2 + 0.053m_{E_1}^2, \end{aligned}$$

applied to most parameters,

$\Delta_{BG}$  large, looks fine-tuned for e.g.  $m_{\tilde{t}_1} \sim 1$  TeV

$$\Delta_{BG}(Q_3) \simeq 0.73 \frac{1000^2}{91.2^2} \sim 100$$

### #3. What about EENZ/BG measure?

$$\Delta_{BG} = \max_i \left| \frac{\partial \log m_Z^2}{\partial \log p_i} \right| = \max_i \left| \frac{p_i}{m_Z^2} \frac{\partial m_Z^2}{\partial p_i} \right|$$

applied to pMSSM, then  $\Delta_{BG} \simeq \Delta_{EW}$

What if we apply to high (e.g. GUT) scale parameters ?

$$\begin{aligned} m_Z^2 \simeq & -2.18\mu^2 + 3.84M_3^2 + 0.32M_3M_2 + 0.047M_1M_3 - 0.42M_2^2 \\ & + 0.011M_2M_1 - 0.012M_1^2 - 0.65M_3A_t - 0.15M_2A_t \\ & - 0.025M_1A_t + 0.22A_t^2 + 0.004M_3A_b \\ & - 1.27m_{H_u}^2 - 0.053m_{H_d}^2 \\ & \hline & + 0.73m_{Q_3}^2 + 0.57m_{U_3}^2 + 0.049m_{D_3}^2 - 0.052m_{L_3}^2 + 0.053m_{E_3}^2 \\ & \hline & + 0.051m_{Q_2}^2 - 0.11m_{U_2}^2 + 0.051m_{D_2}^2 - 0.052m_{L_2}^2 + 0.053m_{E_2}^2 \\ & \hline & + 0.051m_{Q_1}^2 - 0.11m_{U_1}^2 + 0.051m_{D_1}^2 - 0.052m_{L_1}^2 + 0.053m_{E_1}^2, \end{aligned}$$

For correlated scalar masses  $\equiv m_0$ ,  
scalar contribution collapses:

what looks fine-tuned isn't: *focus point SUSY*  
multi-TeV scalars are *natural*

Feng, Matchev, Moroi

Even with FP, still  
fine-tuned on  $m(\text{gluino})$  :(

But wait! in more complete models,  
soft terms **not independent**

**violates prime directive!**

e.g. in SUGRA, for well-specified hidden sector,  
each soft term calculated as multiple of  $m_{3/2}$ ;  
soft terms must be combined!

e.g. dilaton-dominated SUSY breaking:  $m_0^2 = m_{3/2}^2$  with  $m_{1/2} = -A_0 = \sqrt{3}m_{3/2}$

in general:

$$m_{H_u}^2 = a_{H_u} \cdot m_{3/2}^2,$$

$$m_{Q_3}^2 = a_{Q_3} \cdot m_{3/2}^2,$$

$$A_t = a_{A_t} \cdot m_{3/2},$$

$$M_i = a_i \cdot m_{3/2},$$

....

since  $\mu$  hardly runs, then

$$\begin{aligned} m_Z^2 &\simeq -2\mu^2 + a \cdot m_{3/2}^2 \\ &\simeq -2\mu^2 - 2m_{H_u}^2 (weak) \end{aligned}$$

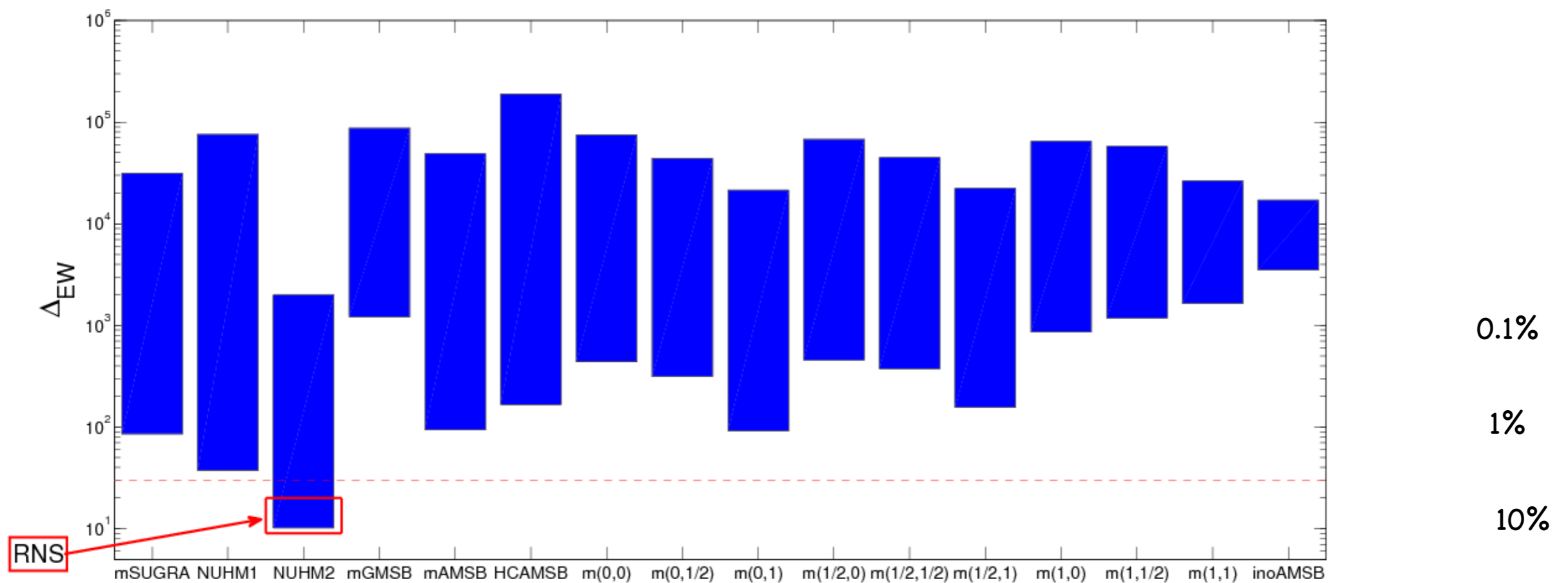
$$m_{H_u}^2 (weak) \sim -(100 - 200)^2 \text{ GeV}^2 \sim -a \cdot m_{3/2}^2/2$$

using  $\mu^2$  and  $m_{3/2}^2$  as fundamental,  
then  $\Delta_{BG} \simeq \Delta_{EW}$  even using high scale parameters!

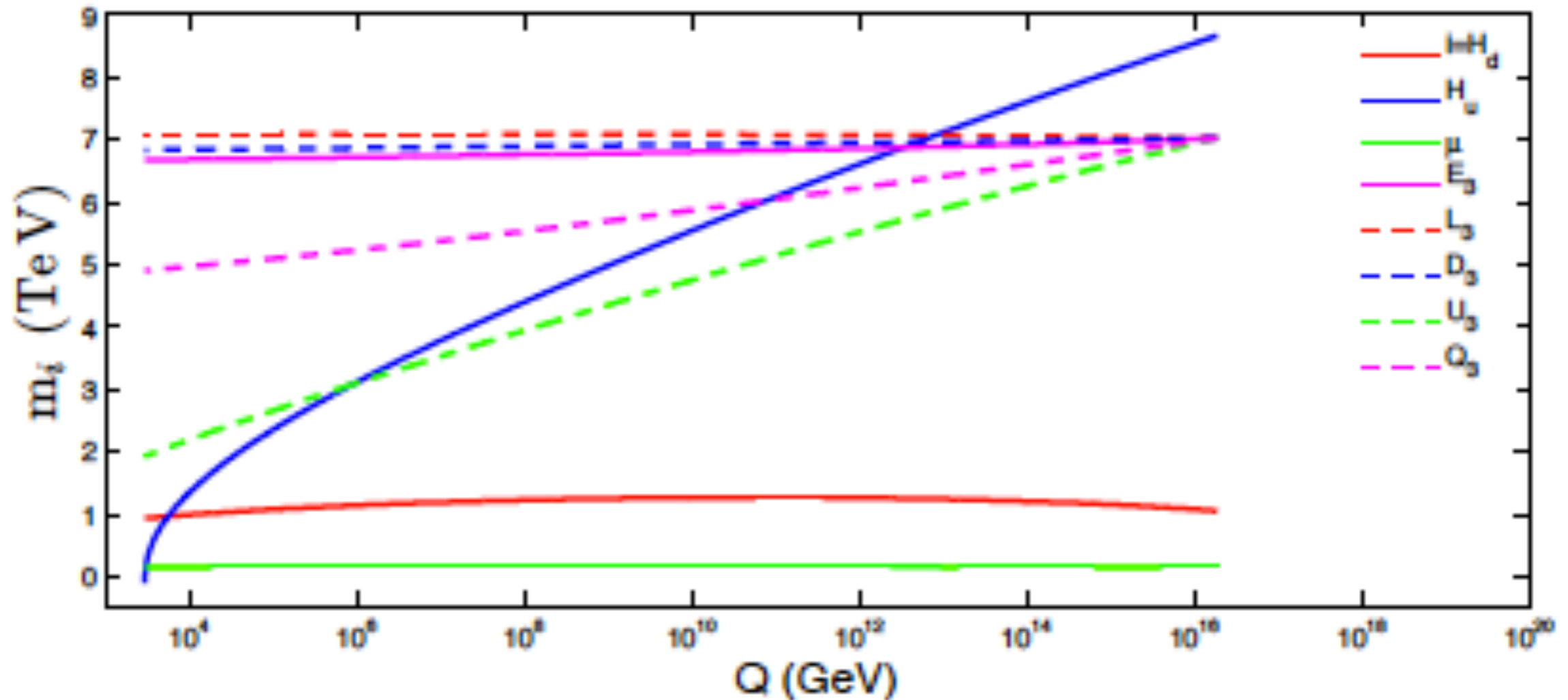
$\Delta_{EW}$  is highly selective:  
 most constrained models are ruled out  
 except NUHM2 and its generalizations:

J. Ellis, K. Olive and Y. Santoso, *Phys. Lett. B* 539 (2002) 107; J. Ellis, T. Falk, K. Olive and Y. Santoso, *Nucl. Phys. B* 652 (2003) 259; H. Baer, A. Mustafayev, S. Profumo, A. Belyaev and X. Tata, *J. High Energy Phys.* 0507 (2005) 065.

scan over p-space with  $m(h)=125.5\pm 2.5$  GeV:



Applied properly, all three measures agree:  
 naturalness is unambiguous and highly predictive!



## Radiatively-driven natural SUSY, or RNS:

(typically need  $m_{H_u} \sim 25\text{-}50\%$  higher than  $m_0$ )

H. Baer, V. Barger, P. Huang, A. Mustafayev and X. Tata, *Phys. Rev. Lett.* **109** (2012) 161802.

H. Baer, V. Barger, P. Huang, D. Mickelson, A. Mustafayev and X. Tata, *Phys. Rev. D* **87** (2013) 115028 [arXiv:1212.2655 [hep-ph]].

## Axion cosmology

★ Axion field eq'n of motion:  $\theta = a(x)/f_a$

$$- \ddot{\theta} + 3H(T)\dot{\theta} + \frac{1}{f_a^2} \frac{\partial V(\theta)}{\partial \theta} = 0$$

$$- V(\theta) = m_a^2(T) f_a^2 (1 - \cos \theta)$$

– Solution for  $T$  large,  $m_a(T) \sim 0$ :

$$\theta = \text{const.}$$

–  $m_a(T)$  turn-on  $\sim 1$  GeV

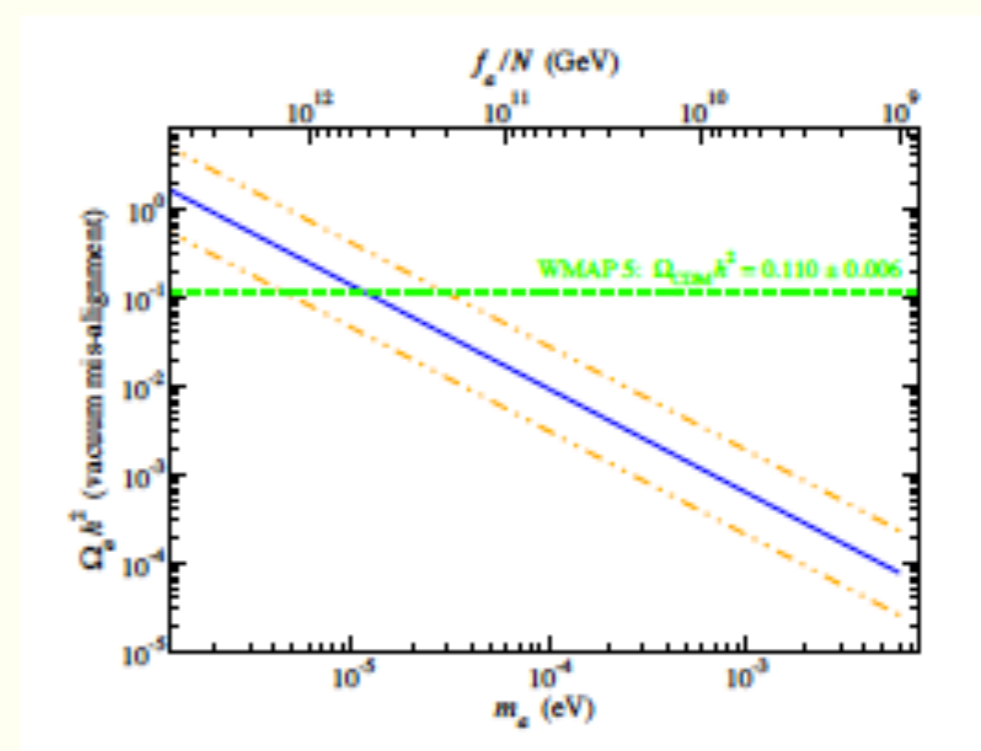
★  $a(x)$  oscillates,

creates axions with  $\vec{p} \sim 0$ :

production via vacuum mis-alignment

$$\star \Omega_a h^2 \sim \frac{1}{2} \left[ \frac{6 \times 10^{-6} \text{ eV}}{m_a} \right]^{7/6} \theta_i^2 h^2$$

★ astro bound: stellar cooling  $\Rightarrow f_a \gtrsim 10^9 \text{ GeV}$



## Why might $\mu \ll m(\text{soft})$ ?

SUSY  $\mu$  problem:  $\mu$  term is SUSY, not SUSY breaking:  
expect  $\mu \sim M(\text{Pl})$  but phenomenology requires  $\mu \sim m(\text{Z})$

- NMSSM:  $\mu \sim m(\text{soft})$ ; but beware singlets!
- Giudice–Masiero:  $\mu$  forbidden by some symmetry: generate via Higgs coupling to hidden sector:  $\mu \sim m(\text{soft})$
- **Kim–Nilles**: invoke SUSY version of DFSZ axion solution to strong CP:

KN: PQ symmetry forbids  $\mu$  term,  
but then it is generated via PQ breaking

$$\mu \sim \lambda_\mu f_a^2 / m_P$$

Little Hierarchy due to mismatch between  
PQ breaking and SUSY breaking scales?

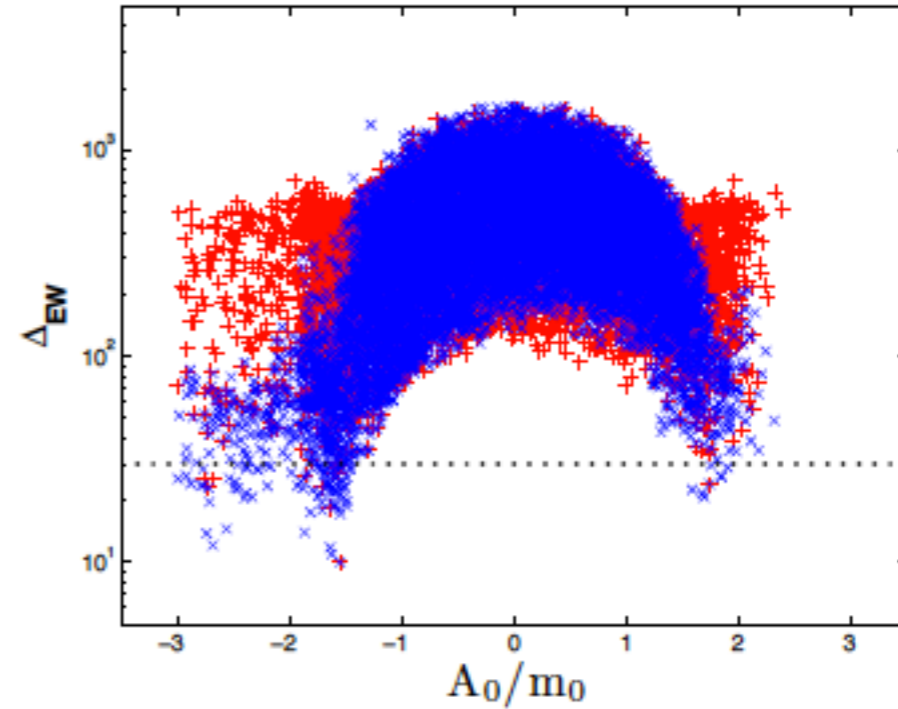
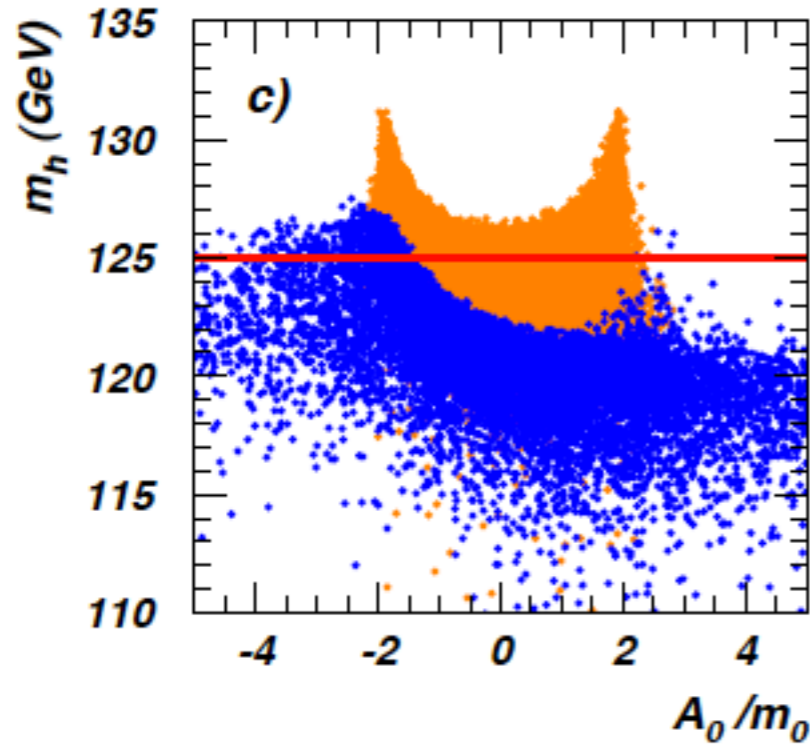
$$m(\text{soft}) \sim m_{3/2} \sim m_{\text{hidden}}^2 / m_P$$

$$f_a < m_{\text{hidden}} \Rightarrow \\ \mu \ll m(\text{soft})$$

Higgs mass  $m(h) \sim \mu$   
tells us where to look for axion!

$$m_a \sim 6.2 \mu\text{eV} \left( \frac{10^{12} \text{ GeV}}{f_a} \right)$$

Large value of  $A_t$  reduces  $\Sigma_u^u(\tilde{t}_{1,2})$  contributions to  $\Delta_{EW}$  while uplifting  $m_h$  to  $\sim 125$  GeV



$$\Sigma_u^u(\tilde{t}_{1,2}) = \frac{3}{16\pi^2} F(m_{\tilde{t}_{1,2}}^2) \left[ f_t^2 - g_Z^2 \mp \frac{f_t^2 A_t^2 - 8g_Z^2 (\frac{1}{4} - \frac{2}{3}x_W) \Delta_t}{m_{\tilde{t}_2}^2 - m_{\tilde{t}_1}^2} \right]$$

$$\Delta_t = (m_{\tilde{t}_L}^2 - m_{\tilde{t}_R}^2)/2 + M_Z^2 \cos 2\beta (\frac{1}{4} - \frac{2}{3}x_W)$$

$$F(m^2) = m^2 \left( \log \frac{m^2}{Q^2} - 1 \right) \quad Q^2 = m_{\tilde{t}_1} m_{\tilde{t}_2}$$