

Top and b mass effects in Higgs production at LHC

Vittorio Del Duca

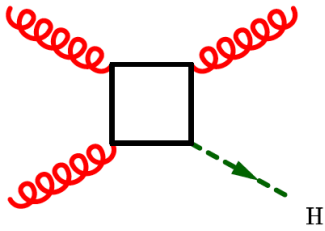
INFN LNF

in collaboration with

R. Bonciani, H. Frellesvig, M. Hidding, V. Hirschi,
F. Moriello, G. Salvatori, G. Somogyi, F. Tramontano

LNF 7 February 2024

Higgs p_T distribution at LHC

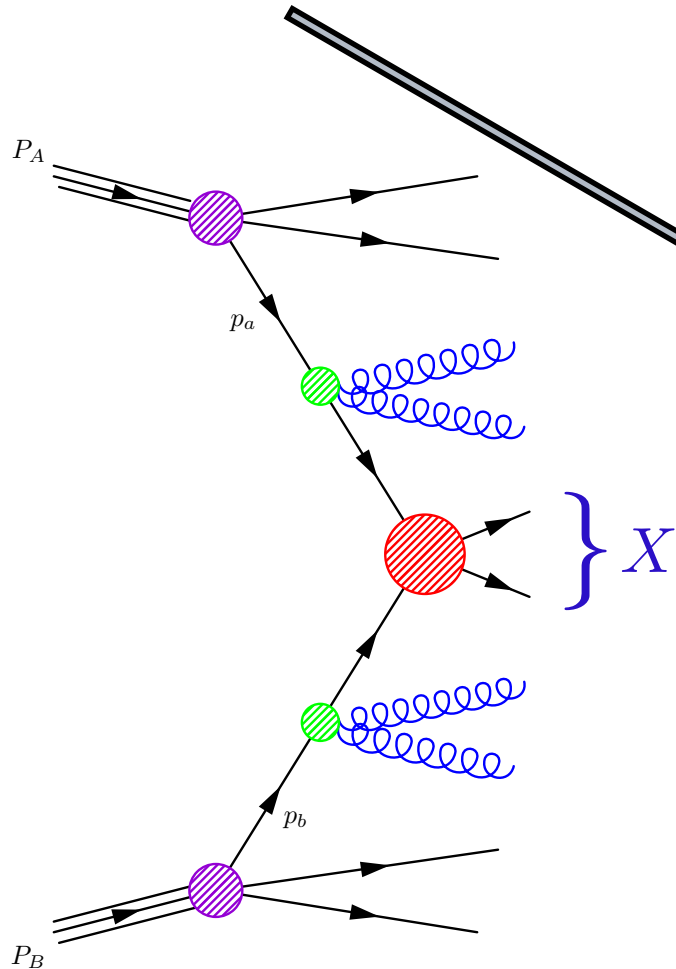


- high- p_T tail of the Higgs p_T distribution is sensitive to the structure of the loop-mediated Higgs-gluon coupling
New Physics particles circulating in the loop would modify it
- QCD NLO corrections to the top- and b -quark mass effects on the Higgs p_T distribution, in the on-shell and $\overline{\text{MS}}$ mass renormalisation schemes

Parton model

extracted from data
evolved through DGLAP

computed in QCD



factorising short- and long-range interactions

$$\sigma_X = \sum_{a,b} \int_0^1 dx_1 dx_2 f_{a/A}(x_1, \mu_F^2) f_{b/B}(x_2, \mu_F^2) \times \hat{\sigma}_{ab \rightarrow X} \left(x_1, x_2, \{p_i^\mu\}; \alpha_S(\mu_R^2), \alpha(\mu_F^2), \frac{Q^2}{\mu_R^2}, \frac{Q^2}{\mu_F^2} \right)$$

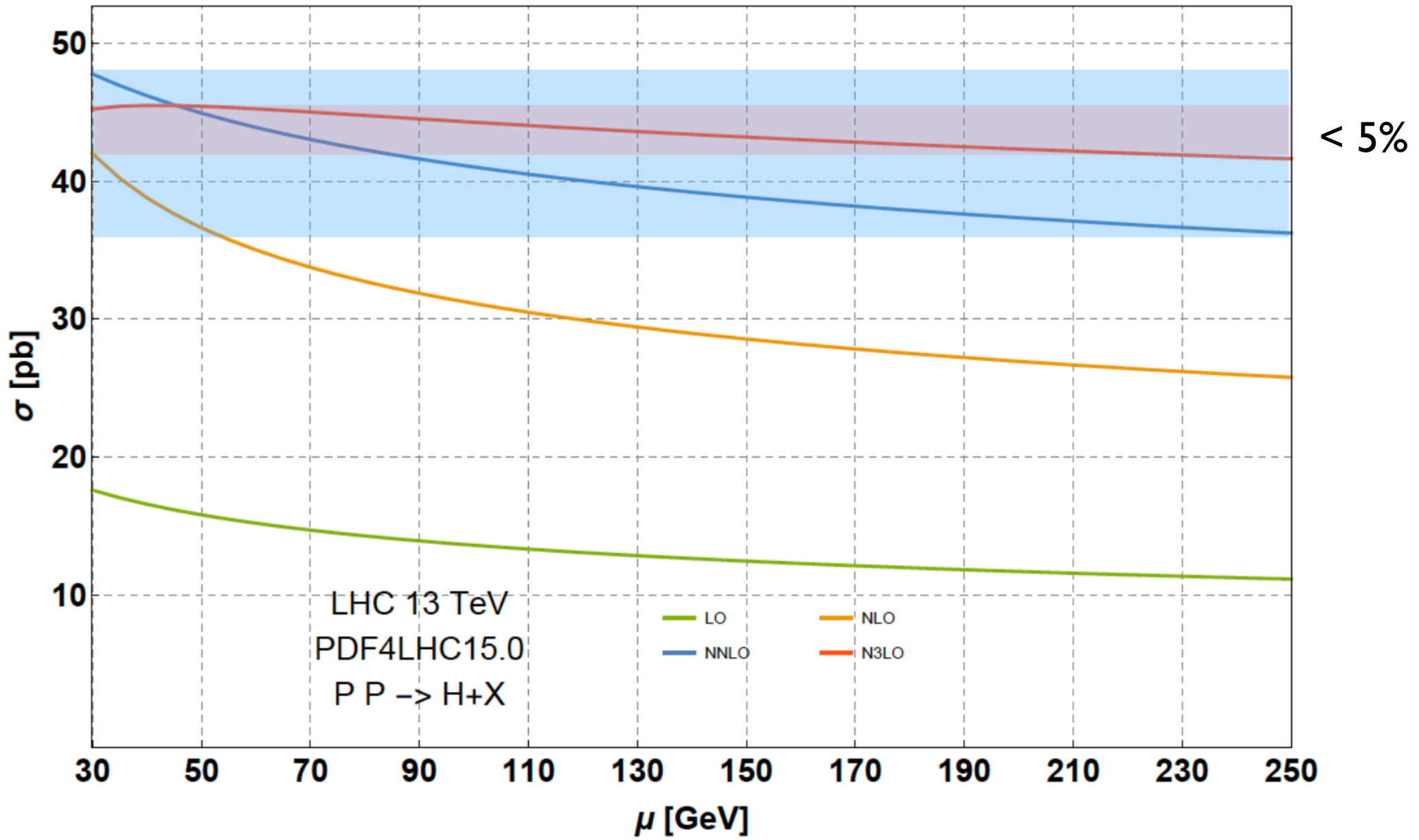
$X = W, Z, H, Q\bar{Q}, \text{high-}E_T \text{jets}, \dots$

$\hat{\sigma}$ is known as a fixed-order expansion in α_S

$$\hat{\sigma} = C \alpha_S^n (1 + c_1 \alpha_S + c_2 \alpha_S^2 + \dots)$$

$c_1 = \text{NLO}$ $c_2 = \text{NNLO}$

the computed cross section depends on unphysical scales: μ_R and μ_F



from F. Maltoni's talk at GGI tea breaks 2021

- the crucial ingredient of a parton cross section is the amplitude

$$\hat{\sigma} \sim \int dP_{PS} |\mathcal{M}|^2$$

- amplitudes are on-shell and gauge-invariant objects
- amplitudes exhibit unexpected symmetries

Parke-Taylor formula for MHV n -gluon amplitudes

$$A_4^{tree}(1^+, 2^+, \dots, i^-, \dots, j^-, \dots, n^+) = \frac{\langle ij \rangle^4}{\langle 12 \rangle \langle 23 \rangle \dots \langle (n-1)n \rangle \langle n1 \rangle}$$

# external gluons	# Feynman diagrams
4	4
6	220
8	34,300
10	10,521,900

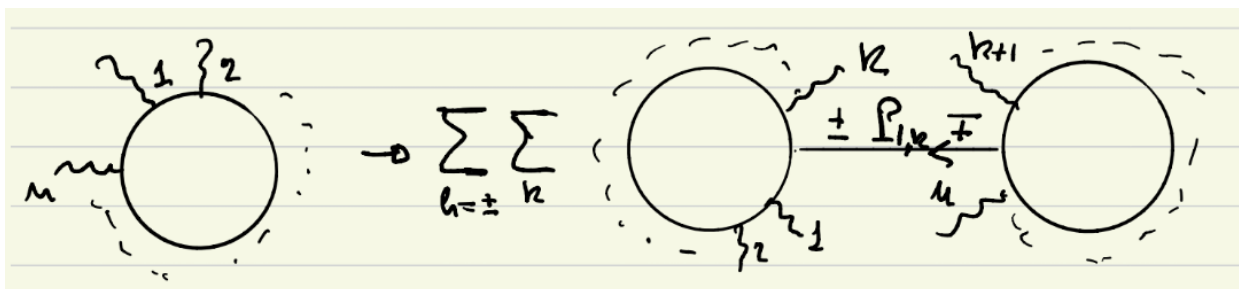
of Feynman diagrams grows factorially with # of gluons



Tree amplitudes



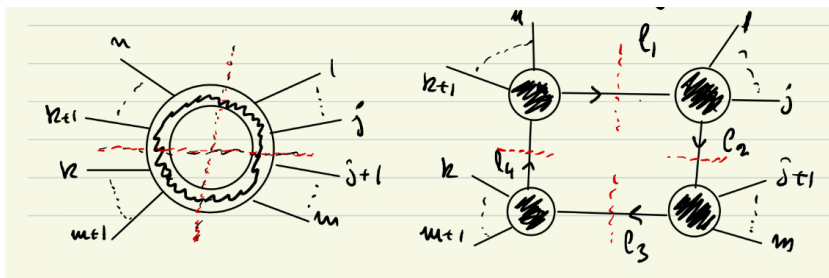
Britto Cachazo Feng Witten (BCFW) on-shell recursion relations



One-loop amplitudes

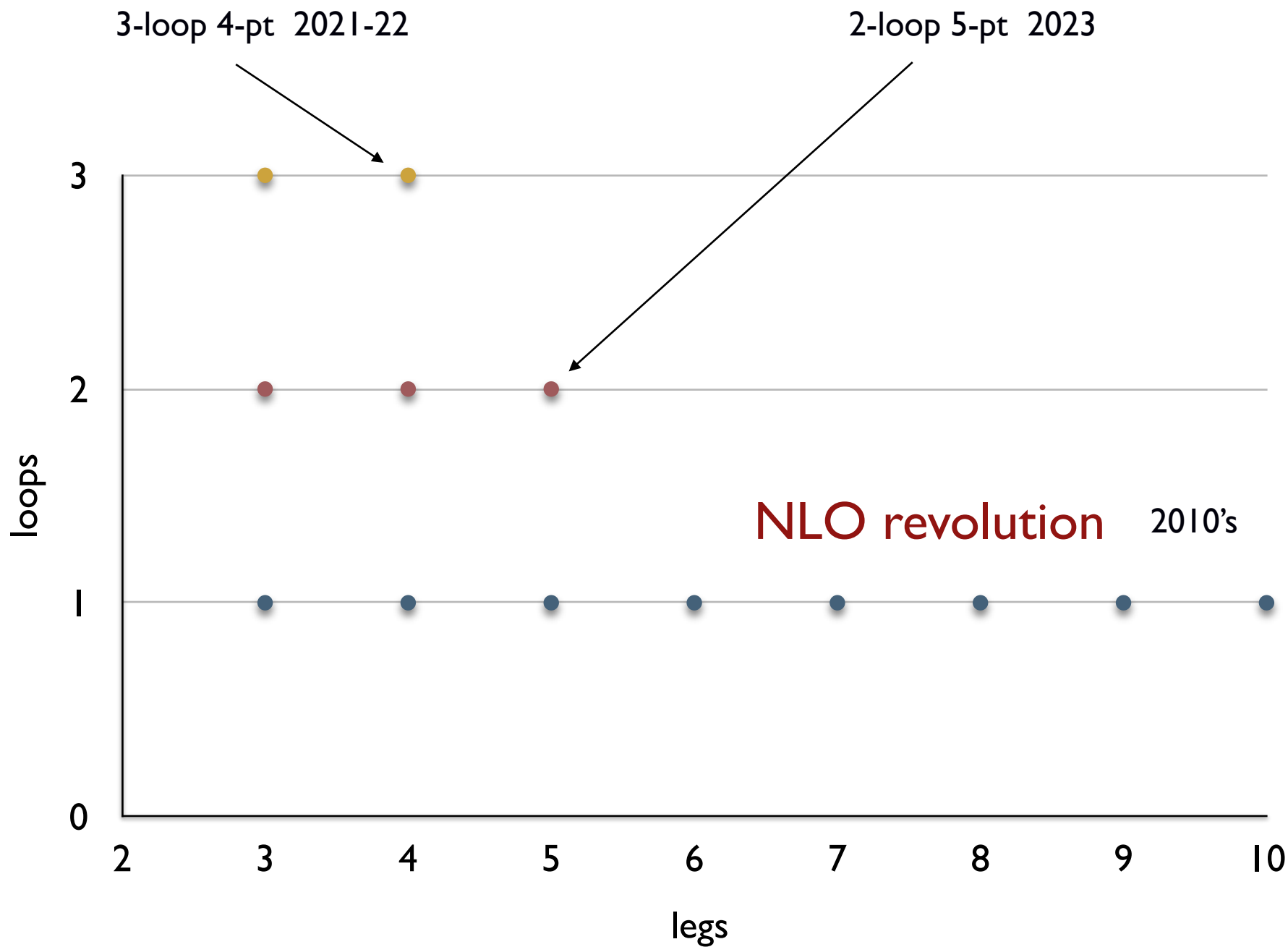


generalised unitarity



Galileo Galilei Medal 2023

“for the development of powerful methods for high-order perturbative calculations in quantum field theory”



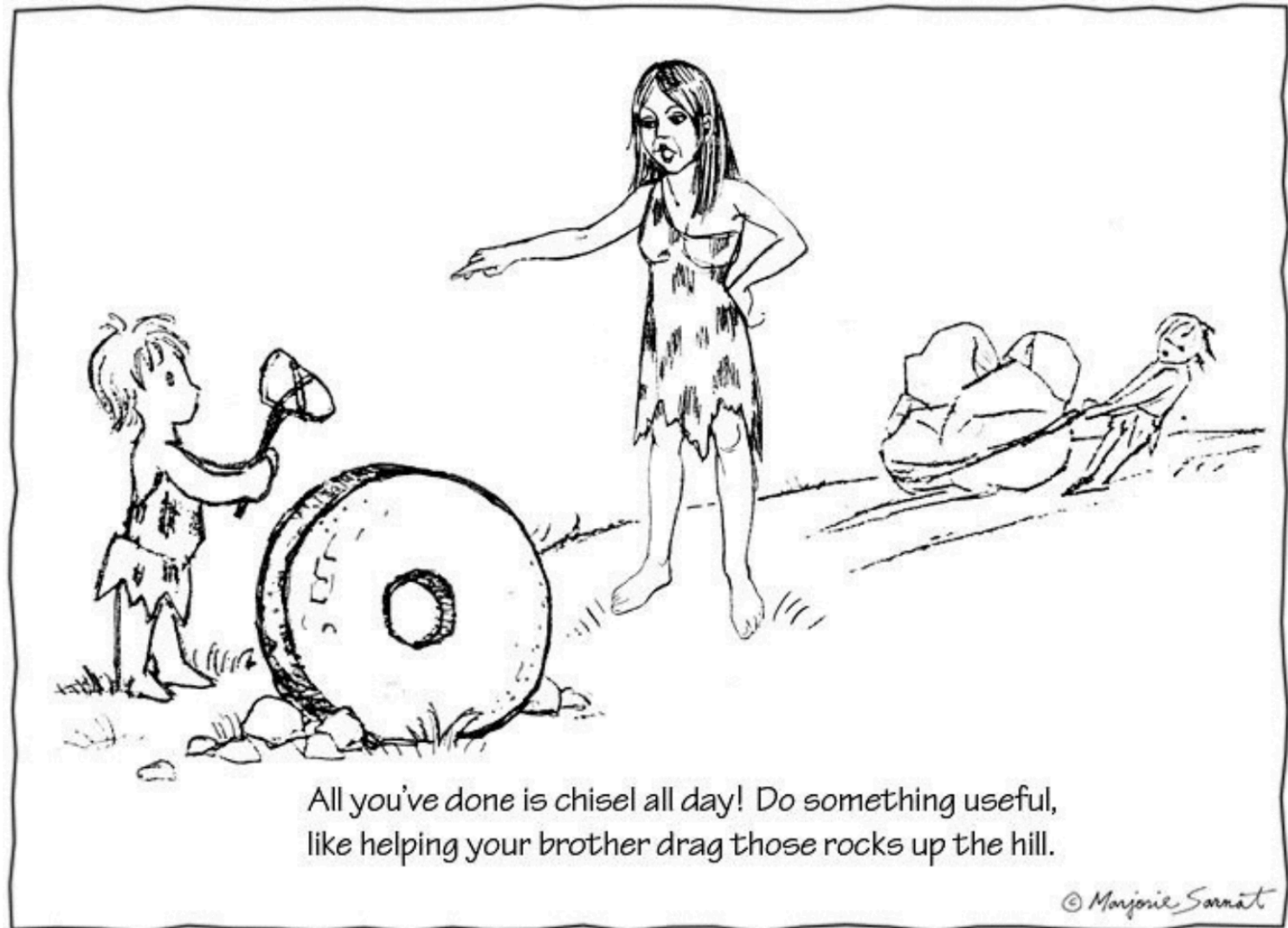
Tree level: computed without Feynman diagrams

One loop: computed without Feynman diagrams

Two loops: oh no! Feynman diagrams again ...

although many modern techniques (tensor decomposition, integration by parts identities, method of differential equations) have been devised to compute multiloop Feynman integrals

Do we need a completely different approach?



All you've done is chisel all day! Do something useful, like helping your brother drag those rocks up the hill.

from G. Heinrich's talk at LNF in May 2019

... but through multiloop amplitude studies,
beautiful mathematical structures were uncovered...

Polylogarithms



classical polylogarithms

$$\text{Li}_m(z) = \int_0^z dt \frac{\text{Li}_{m-1}(t)}{t} = \sum_{n=1}^{\infty} \frac{z^n}{n^m}$$

$$\text{Li}_1(z) = \sum_{n=1}^{\infty} \frac{z^n}{n} = -\ln(1-z)$$

Euler 1768
Spence 1809



multiple polylogarithms

$$G(a, \vec{w}; z) = \int_0^z \frac{dt}{t-a} G(\vec{w}; t), \quad G(a; z) = \ln\left(1 - \frac{z}{a}\right) \quad a, \vec{w} \in \mathbb{C}$$

Goncharov 1998

classical polylogarithms are multiple polylogarithms with specific roots

$$G(\vec{0}_n; x) = \frac{1}{n!} \ln^n x \quad G(\vec{a}_n; x) = \frac{1}{n!} \ln^n \left(1 - \frac{x}{a}\right) \quad G(\vec{0}_{n-1}, a; x) = -\text{Li}_n\left(\frac{x}{a}\right)$$



multiple polylogarithms are endowed with a rich algebraic structure

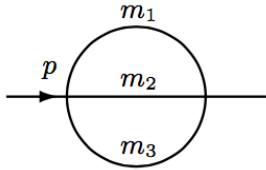
Hopf Algebra  functional identities among polylogarithms



multiple polylogarithms are iterated integrals on the Riemann sphere

Elliptic iterated integrals

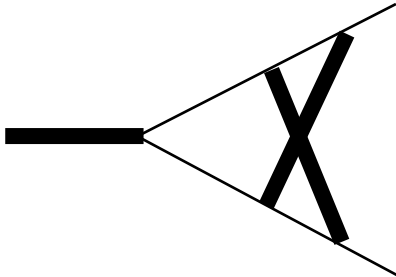
2-loop sunrise graph



Sabry 1962: ...; Broadhurst 1989; ...; Bloch Vanhove 2013; ...
Brödel Duhr Dulat Penante Tancredi 2017-2019

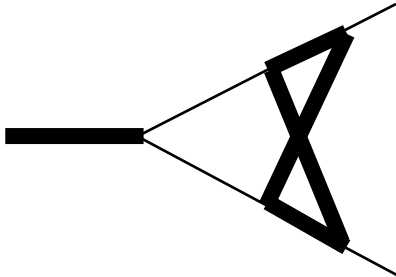
2-loop 3-pt functions

electroweak form factor



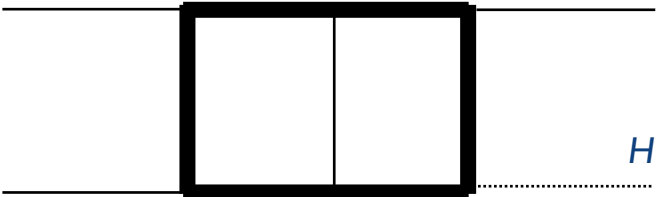
Aglietti Bonciani Grassi Remiddi 2007

t - t bar



von Manteuffel Tancredi 2017

2-loop 4-pt function for Higgs + 1 jet

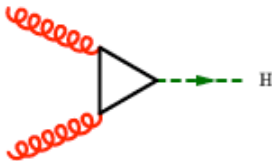


Bonciani VDD Frellesvig Henn Moriello Smirnov 2016

first instance of elliptic iterated integrals
in a genuine 4-pt topology

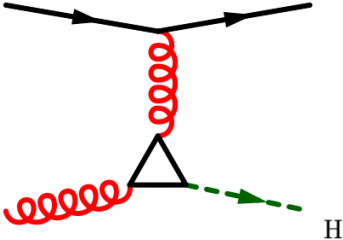
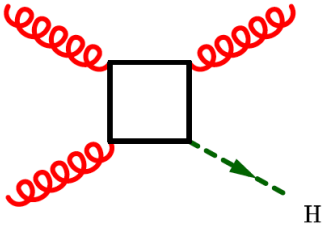
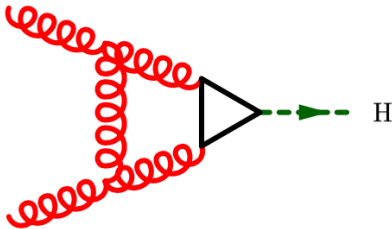
Higgs production at LHC

- In proton collisions, the Higgs boson is produced mostly via gluon fusion
The gluons do not couple directly to the Higgs boson
For matter, the coupling is mediated by a heavy quark loop
The largest contribution comes from the top-quark loop
The production mode is (roughly) proportional to the top Yukawa coupling y_t^2



- QCD NLO corrections are known for top-, b - and charm-quark loops
(in principle for any heavy quark mass)

Djouadi Graudenz Spira Zerwas 1991-1995



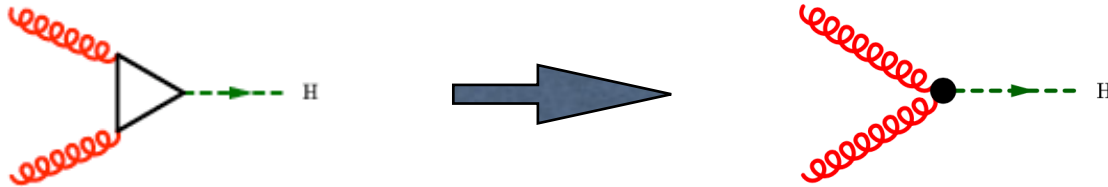
- QCD NLO corrections are about 100% larger than leading order
- QCD NNLO corrections are known for top- and b -quark loops

Czakon Harlander Klappert Niggetiedt 2021 (top)
Czakon Eschment Niggetiedt Poncelet Schellenberger 2023 (top + b)

Higgs Effective Field Theory



$$m_H \ll 2m_t$$



all amplitudes are reduced by one loop

$$R_{LO} = \frac{\sigma_{ex:t}^{LO}}{\sigma_{EFT}^{LO}} = 1.063$$

rescaled HEFT (rHEFT) tuned to reproduce the exact (only top) LO σ



in HEFT **QCD** corrections have been computed at **N³LO**

Anastasiou Duhr Dulat Herzog Mistlberger 2015
Mistlberger 2018

(in terms of MPLs and elliptic integrals)



the **N³LO** computation raised the central value by 3%
and featured a 3% scale variation

Higgs production



including quark-mass effects and QCD-EW interference the cross section is

$$\sigma = 48.58 \text{ pb}^{+2.22 \text{ pb} (+4.56\%)}_{-3.27 \text{ pb} (-6.72\%)} \text{ (theory)} \pm 1.56 \text{ pb} (3.20\%) \text{ (PDF} + \alpha_s)$$



The breakdown of the cross section

48.58 pb =	16.00 pb	(+32.9%)	(LO, rEFT)
	+ 20.84 pb	(+42.9%)	(NLO, rEFT)
	- 2.05 pb	(-4.2%)	((<i>t, b, c</i>), exact NLO)
	+ 9.56 pb	(+19.7%)	(NNLO, rEFT)
	+ 0.34 pb	(+0.2%)	(NNLO, $1/m_t$)
	+ 2.40 pb	(+4.9%)	(EW, QCD-EW)
	+ 1.49 pb	(+3.1%)	(N ³ LO, rEFT)

Higgs production

Handbook 4 of LHC Higgs Cross Sections 2016

- 6 sources of uncertainties due to:
 - higher orders
 - truncation of the threshold expansion
 - PDFs
 - NLO corrections to QCD-EW interference
 - quark mass effects (2: top mass and top-b interference) at NNLO

$\delta(\text{scale})$	$\delta(\text{trunc})$	$\delta(\text{PDF-TH})$	$\delta(\text{EW})$	$\delta(t, b, c)$	$\delta(1/m_t)$
+0.10 pb -1.15 pb	± 0.18 pb	± 0.56 pb	± 0.49 pb	± 0.40 pb	± 0.49 pb
+0.21% -2.37%	$\pm 0.37\%$	$\pm 1.16\%$	$\pm 1\%$	$\pm 0.83\%$	$\pm 1\%$

$$\delta(\text{trunc}) = 0.11 \text{ pb} \quad \text{Mistlberger 2018}$$

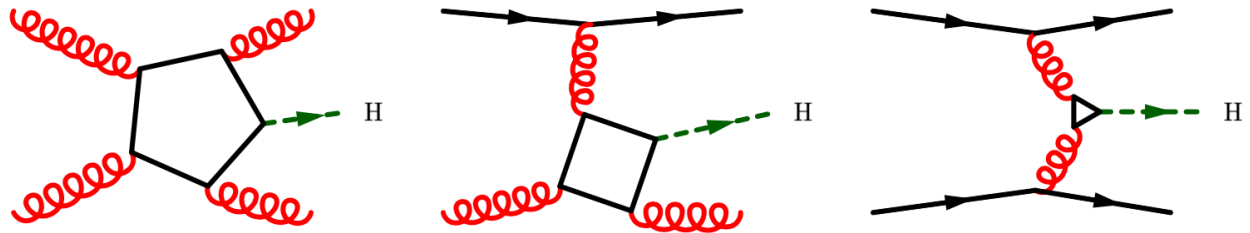
$$\delta(1/m_t) = -0.26\% \quad \text{Czakon Harlander Klappert Niggetiedt 2021}$$

$$\delta(t, b) = -4.6\% \quad \text{Czakon Eschment Niggetiedt Poncelet Schellenberger 2023}$$

QCD NNLO corrections

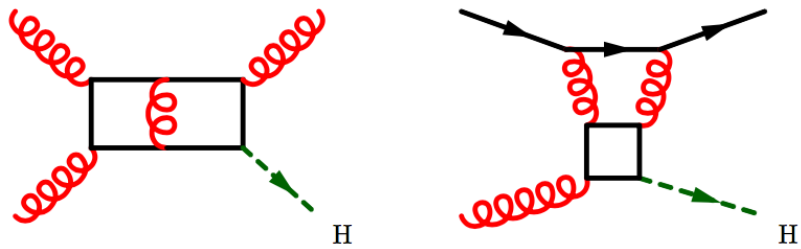
Higgs + 4-parton amplitudes at one loop

VDD Kilgore Oleari Schmidt Zeppenfeld 2001
 Budge Campbell De Laurentis K. Ellis Seth 2020



OpenLoops

Higgs + 3-parton amplitudes at two loops

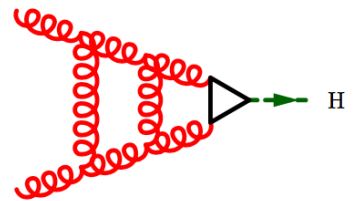


top loop: Jones Kerner Luisoni 2018
 Czakon Harlander Klappert Niggetiedt 2021

Bonciani VDD Frellesvig Moriello Hidding
 Hirschi Salvatori Somogyi Tramontano 2022



gg → Higgs amplitudes at three loops



one scale: one & two top loops
 top loop + light-quark loop

two scales: top loop + b-quark loop

Czakon Niggetiedt 2020
 Harlander Prausa Usovitsch 2019

Niggetiedt Usovitsch 2023

Top and b -quark mass corrections at NNLO

Czakon Harlander Klappert Niggetiedt 2021 (top)

Czakon Eschment Niggetiedt Poncelet Schellenberger 2023 (top + b)

Order	σ_{HEFT} [pb]	$(\sigma_t - \sigma_{\text{HEFT}})$ [pb]	$\sigma_{t-b\text{-interference}}$ [pb]	$\sigma_{t-b\text{-interference}}/\sigma_{\text{HEFT}}$ [%]
$\sqrt{s} = 8 \text{ TeV}$				
$\mathcal{O}(\alpha_s^2)$	+7.39	–	–0.895	
LO	$7.39^{+1.98}_{-1.40}$	–	$-0.895^{+0.17}_{-0.24}$	–12
$\mathcal{O}(\alpha_s^3)$	+9.14	–0.0873	–0.269(2)	
NLO	$16.53^{+3.63}_{-2.73}$	$-0.0873^{+0.030}_{-0.052}$	$-1.16^{+0.10}_{-0.08}$	$-7.0^{+1.0}_{-0.8}$
$\mathcal{O}(\alpha_s^4)$	+4.19	+0.0523(2)	+0.167(3)	
NNLO	$20.72^{+1.84}_{-2.06}$	$-0.350(2)^{+0.048}_{-0.013}$	$-0.998(4)^{+0.12}_{-0.05}$	$-4.8^{+0.9}_{-0.8}$
$\sqrt{s} = 13 \text{ TeV}$				
$\mathcal{O}(\alpha_s^2)$	+16.30	–	–1.975	
LO	$16.30^{+4.36}_{-3.10}$	–	$-1.98^{+0.37}_{-0.53}$	–12
$\mathcal{O}(\alpha_s^3)$	+21.14	–0.3029(2)	–0.447(4)	
NLO	$37.44^{+8.42}_{-6.29}$	$-0.3029(2)^{+0.10}_{-0.17}$	$-2.42^{+0.19}_{-0.12}$	$-6.5^{+0.9}_{-0.8}$
$\mathcal{O}(\alpha_s^4)$	+9.72	+0.147(1)	+0.434(8)	
NNLO	$47.16^{+4.21}_{-4.77}$	$-0.158(1)^{+0.13}_{-0.03}$	$-1.99(1)^{+0.30}_{-0.15}$	$-4.2^{+0.9}_{-0.8}$

	σ_t	σ_{t+b}	$\frac{\sigma_{t+b}}{\sigma_t} - 1$	$\frac{\sigma_{t+b}}{\sigma_{\text{HEFT}}} - 1$
$\mathcal{O}(\alpha_s^3)$	20.84 pb	20.39 pb	– 2.14 %	– 3.55 %
$\mathcal{O}(\alpha_s^2 + \alpha_s^3)$	37.14 pb	34.71 pb	– 6.5 %	– 7.3 %
$\mathcal{O}(\alpha_s^4)$	9.87 pb	10.30 pb	+ 4.3 %	+ 6.0 %
$\mathcal{O}(\alpha_s^2 + \alpha_s^3 + \alpha_s^4)$	47.00 pb	45.01 pb	– 4.2 %	– 4.6 %

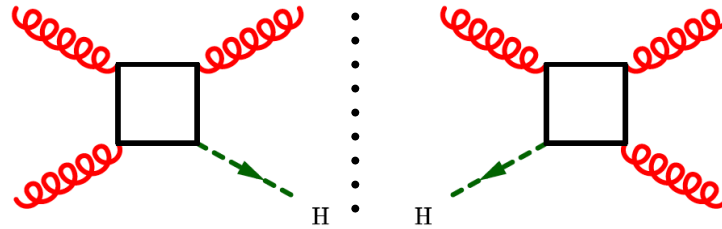
- top- b interference has a larger effect than top-quark corrections
- top- b interference as large at $O(\alpha_s^4)$ as it is at $O(\alpha_s^3)$, but with opposite sign (and larger than expected from NLO scale uncertainties)
- for top-quark mass, used $m_t^2/m_H^2 = 23/12$ (on-shell scheme)

The main obstacle when calculating the total cross section with full top-mass dependence are the two-loop single-emission amplitudes.

Czakon Harlander Klappert Niggetiedt 2021

Higgs p_T distribution at LHC

leading order



K. Ellis Hinchliffe Soldate van der Bij 1988

high- p_T tail of the Higgs p_T distribution is sensitive to the structure of the loop-mediated Higgs-gluon coupling
New Physics particles circulating in the loop would modify it

in high- p_T regime, clean signature of decay products ($H \rightarrow \gamma\gamma$)

QCD NLO corrections

for the top-quark, with on-shell scheme

Jones Kerner Luisoni 2018

Chen Huss Jones Kerner Lang Lindert Zhang 2021

for the top-quark, with on-shell and $\overline{\text{MS}}$ schemes

for top- and b -quarks (for any heavy quark mass), with $\overline{\text{MS}}$ scheme

Bonciani VDD Frellesvig Moriello Hidding Hirschi Salvatori Somogyi Tramontano 2022

HEFT $m_H \ll 2m_t$ and $p_T \ll m_t$

Baur Glover 1990

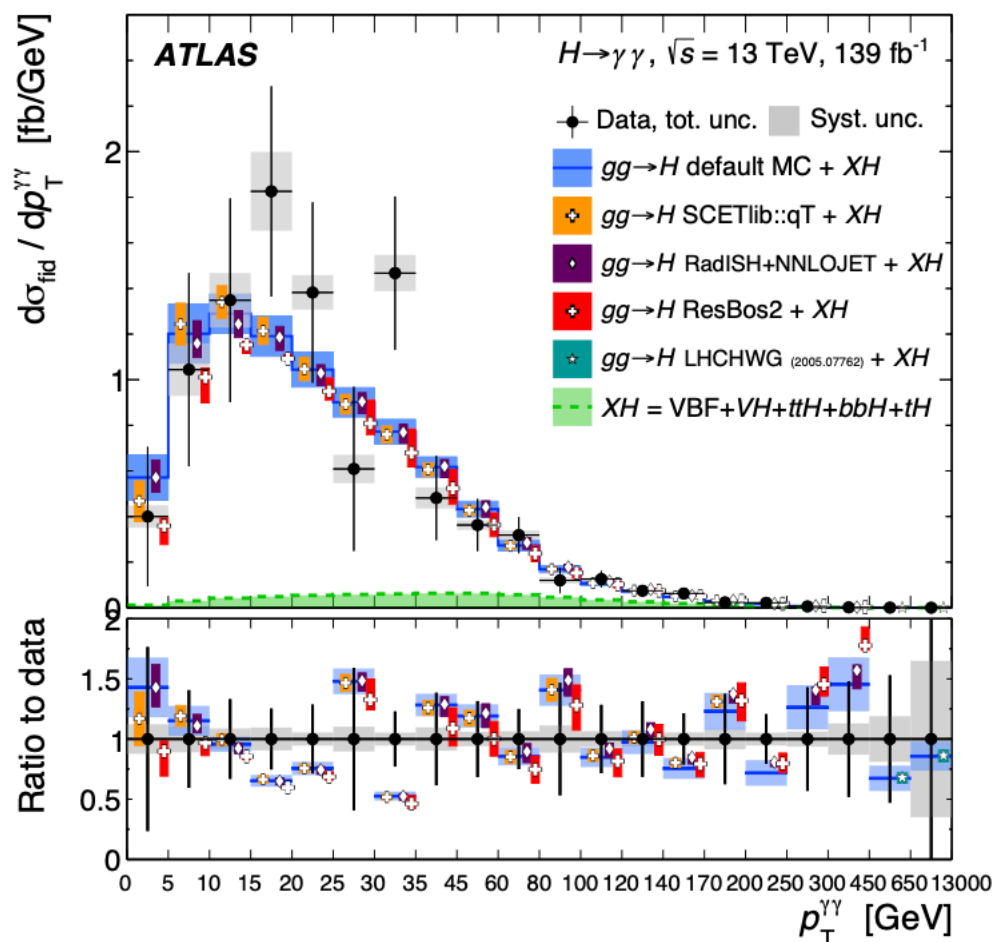
QCD corrections are known at NNLO in HEFT, and yield a 15% increase wrt NLO

Boughezal Caola Melnikov Petriello Schulze 2015

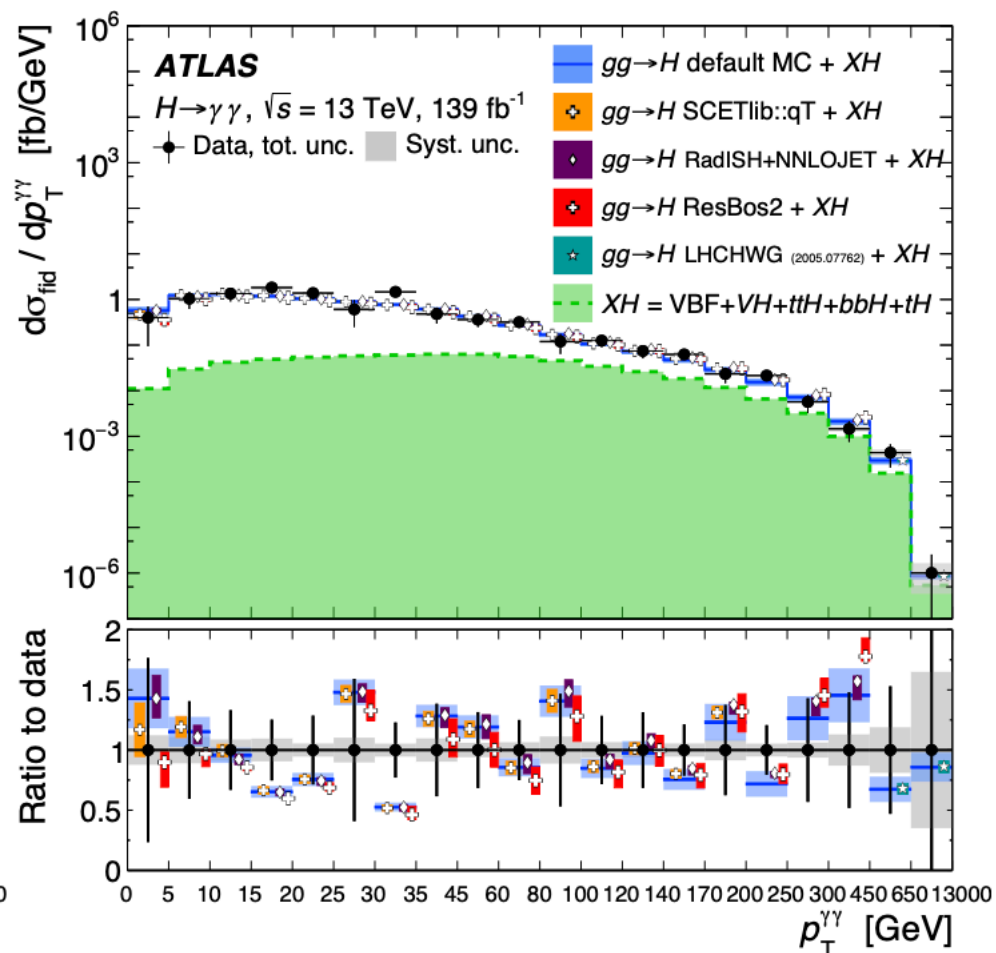
Boughezal Focke Giele Liu Petriello 2015

Chen Cruz-Martinez Gehrman Glover Jaquier 2016

Higgs p_T distribution at LHC



(a)



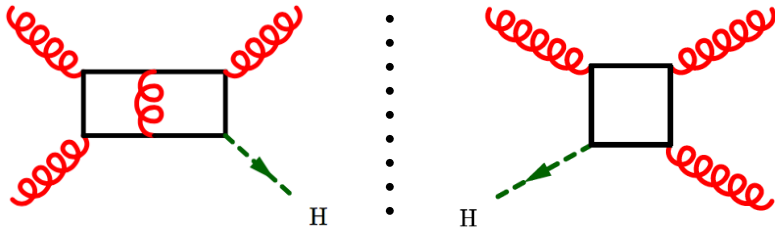
(b)

Figure 8: Particle-level fiducial differential cross-sections times branching ratio for the diphoton variable $p_T^{\gamma\gamma}$ in (a) linear and (b) logarithmic scale. The measured cross-sections are compared with several predictions changing the

Higgs p_T distribution at NLO



virtual corrections



top-quark loop

Jones Kerner Luisoni 2018

Czakon Harlander Klappert Niggetiedt 2021

top- and b -quark (any heavy quark) loop

Bonciani VDD Frellesvig Henn Moriello V. Smirnov 2016

all above + Hidding Maestri Salvatori 2019

Bonciani VDD Frellesvig Moriello Hidding Hirschi Salvatori Somogyi Tramontano 2022

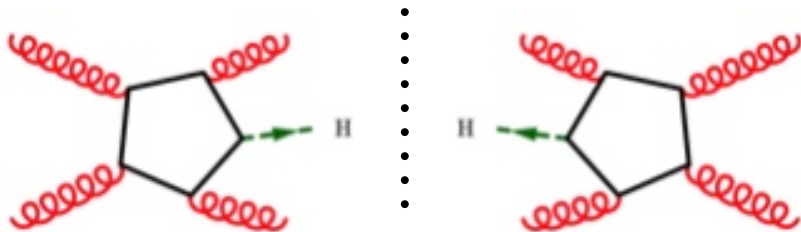
multi-scale problem with complicated analytic structure
elliptic iterated integrals appear



in the loop

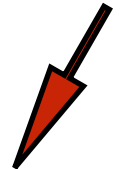


real corrections

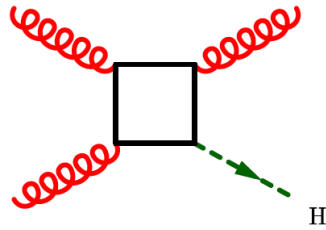


VDD Kilgore Oleari Schmidt Zeppenfeld 2001

Budge Campbell De Laurentis K. Ellis Seth 2020



one-loop amplitudes for Higgs + 3-partons



leading order: up to $\mathcal{O}(\epsilon^2)$

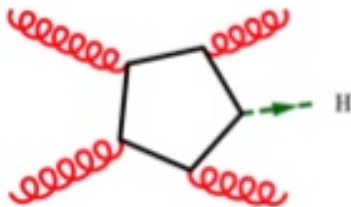
analytic: up to $\mathcal{O}(\epsilon^0)$

numeric: up to $\mathcal{O}(\epsilon^2)$

K. Ellis Hinchliffe Soldate van der Bij 1988

(numeric) derivative for mass renormalisation

one-loop amplitudes for Higgs + 4-partons



NLO real corrections: up to $\mathcal{O}(\epsilon^0)$

analytic: unitarity-cut methods (taken from MCFM-9.1)

Budge Campbell De Laurentis K. Ellis Seth 2020

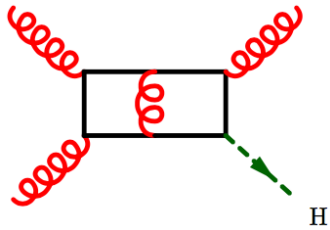
numeric: GoSam & MG5_aMC

run time

analytic: few ms/pt

numeric: $\mathcal{O}(100)$ times slower than analytic

two-loop amplitudes for Higgs + 3-partons



NLO virtual corrections

amplitude \rightarrow form factors \rightarrow scalar integrals \rightarrow Master Integrals
IBP

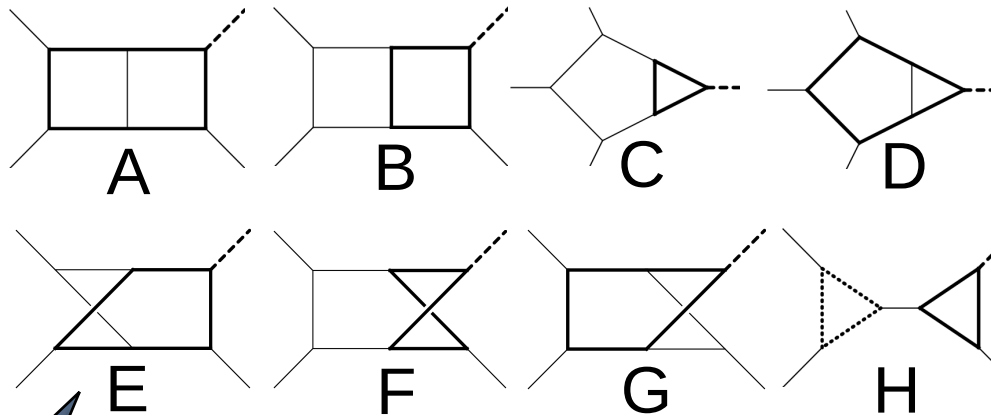
run time: 5 — 60 min/pt

FIRE-KIRA

4 scales, $s, t, m_H, m_t \rightarrow$ 3 external parameters
7 seven-propagator integral families

Bonciani VDD Frellesvig Henn Moriello Smirnov 2016 (A, B, C, D)
Bonciani VDD Frellesvig Henn Hidding Maestri Moriello Salvatori Smirnov 2019 (F)
Frellesvig Hidding Maestri Moriello Salvatori 2019 (G)
Bonciani VDD Frellesvig Moriello Hidding Hirschi Salvatori Somogyi Tramontano 2022 (H)

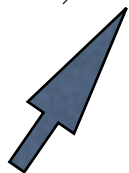
elliptic



MIs
A: 72
B: 5
C: 45
D: 17
F: 73
G: 84
H: 12

= 0

colour conservation



elliptic



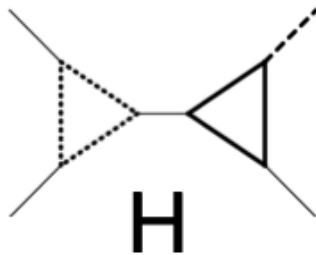
two masses



two-loop amplitudes for Higgs + 3-partons: Renormalisation

Bonciani VDD Frellesvig Moriello Hidding Hirschi Salvatori Somogyi Tramontano 2022

- coupling constant: 5-flavour running in $\overline{\text{MS}}$
- renormalisation:
 - top Yukawa coupling and top mass in OS scheme (massless b)
 - top Yukawa coupling and top mass in $\overline{\text{MS}}$ scheme (massless b)
 - top and b Yukawa couplings and masses in $\overline{\text{MS}}$ scheme



massive b in Higgs- b loop
massless b in b loop

alternative:

massive b everywhere,

but requires 4-flavour running and including $gg \rightarrow Hbb$

two-loop amplitudes for Higgs + 3-partons: validation checks

IR poles

$$\mathcal{M}_{ij,IR}^{(2)} \propto I_{ij}^{(1)}(\{p\}, \epsilon) \mathcal{M}_{ij}^{(1)}$$

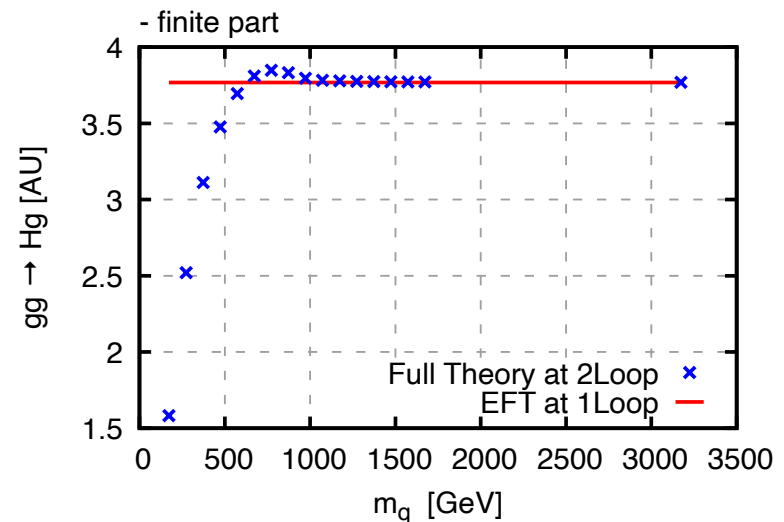
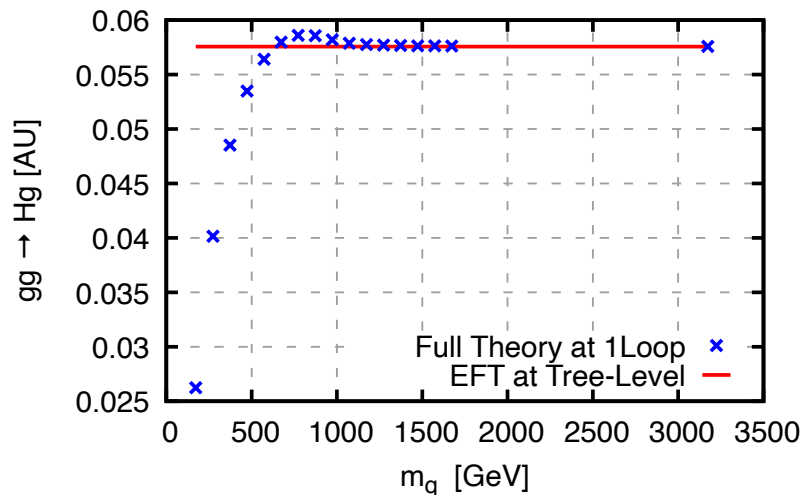
with insertion operators

$$I_{gg}^{(1)}(\{p\}, \epsilon) = -\frac{\alpha_S}{\pi} \frac{(4\pi)^\epsilon}{\Gamma(1-\epsilon)} \left(\frac{N_c}{\epsilon^2} + \frac{\beta_0}{\epsilon} \right) \left[\left(\frac{\mu^2}{-s} \right)^\epsilon + \left(\frac{\mu^2}{-t} \right)^\epsilon + \left(\frac{\mu^2}{-u} \right)^\epsilon \right]$$

$$I_{q\bar{q}}^{(1)}(\{p\}, \epsilon) = -\frac{\alpha_S}{2\pi} \frac{(4\pi)^\epsilon}{\Gamma(1-\epsilon)} \left\{ -\left(\frac{N_c}{\epsilon^2} + \frac{3N_c}{4\epsilon} + \frac{\beta_0}{2\epsilon} \right) \left[\left(\frac{\mu^2}{-t} \right)^\epsilon + \left(\frac{\mu^2}{-u} \right)^\epsilon \right] + \frac{1}{N_c} \left(\frac{1}{\epsilon^2} + \frac{3}{2\epsilon} \right) \left(\frac{\mu^2}{-s} \right)^\epsilon \right\}$$

agreement with HEFT limit

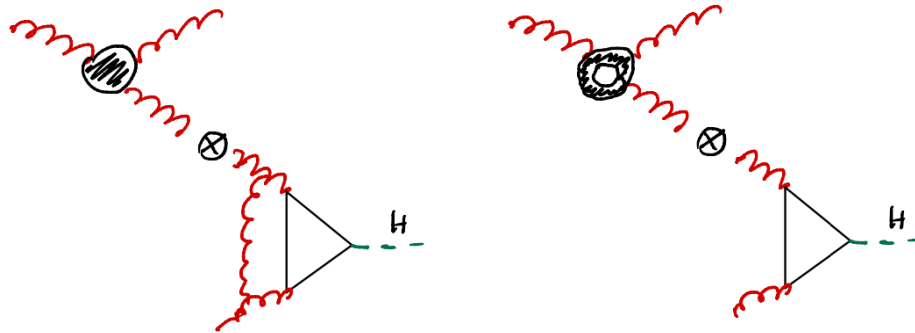
$$\mathcal{M} = \mathcal{M}_{HEFT} + \mathcal{O}\left(\frac{1}{M_t}\right)$$



two-loop amplitudes for Higgs + 3-partons: validation checks

soft and collinear limits

(these are checks on real-virtual parts of NNLO cross section, however they are feasible on our two-loop amplitudes)



Aglietti Bonciani Degrassi Vicini 2006

Bern Dixon Dunbar Kosower 1994
Bern Kilgore Schmidt VDD 1998-99
Kosower Uwer 1999

one-loop 2-parton splitting functions

one-loop 1-soft-gluon factor

Bern Kilgore Schmidt VDD 1998-99
Catani Grazzini 2000

checked also “two-loop photon correction”

Higgs p_T distribution at NLO: checks with previous results



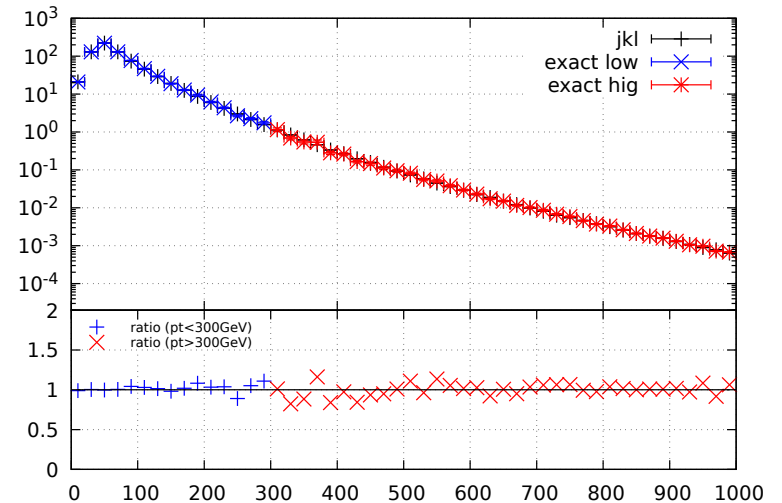
inclusive p_T distribution ($p_{T,j} > 30$ GeV)
with OS mass renormalisation

our result

$$\sigma_{NLO} = 14.37 \pm 0.05 \text{ pb}$$

Chen Huss Jones Kerner Lang Lindert Zhang 2021
(Jones Kerner Luisoni 2018-2021)

$$\sigma_{NLO} = 14.15 \pm 0.07 \text{ pb}$$



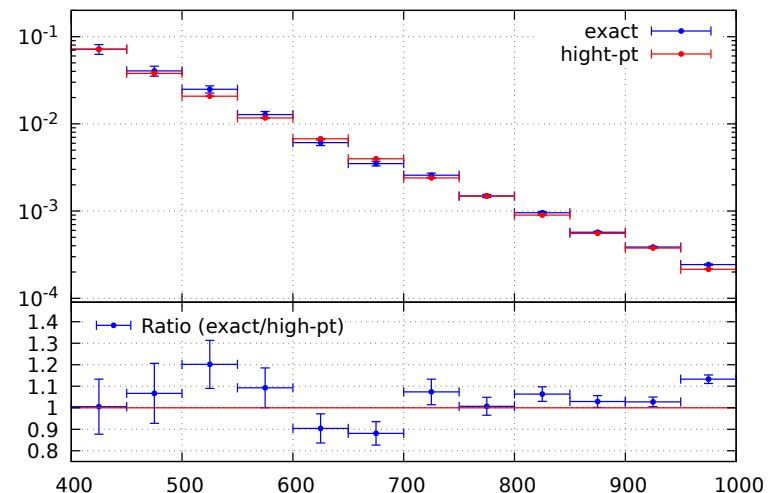
high p_T tail of distribution

checked with approximate high- p_T distribution

Lindert Melnikov Kudashkin Wever 2018

based on approximate high- p_T two-loop amplitudes

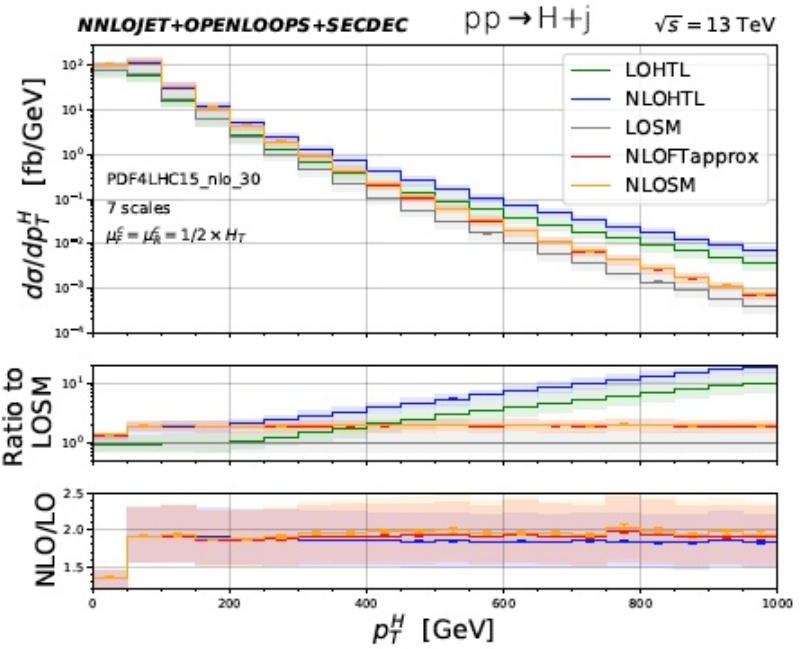
Melnikov Kudashkin Wever 2018



Higgs p_T distribution at LHC



QCD NLO corrections for the top-quark (on-shell mass renormalisation)



Jones Kerner Luisoni 2018
 Chen Huss Jones Kerner Lang Lindert Zhang 2021



$$\frac{d\sigma}{dp_T^2} \propto \frac{1}{p_T^2} \quad \text{in HEFT NLO corrections}$$

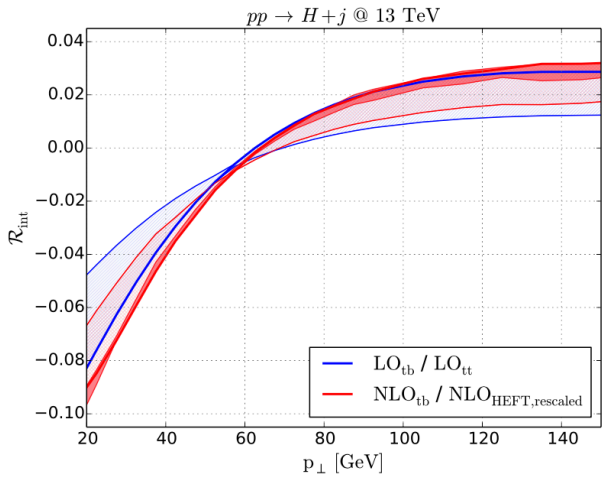
$$\frac{d\sigma}{dp_T^2} \propto \frac{1}{(p_T^2)^2} \quad \text{in top NLO corrections}$$

NLO/LO in HEFT and top loop agree to O(10%)



QCD NLO corrections to top-b interference, using top-quark loop in HEFT and b -quark loop in small m_b limit

Lindert Melnikov Tancredi Wever 2017



Higgs p_T distribution at NLO

- p_T distribution computed with CoLorFuLNLO dual subtraction Somogyi 2009
Prisco Tramontano 2020
 - evaluated on:
 - 3×10^4 pt for OS top (1.4×10^4 pt on basic grid, 1.6×10^4 pt on biased grid)
 - 9×10^4 pt for MSbar top
 - 1.8×10^5 pt for MSbar top and b
 - set-up
 - $\sqrt{s} = 13 \text{ TeV}$
 - $m_H = 125.25 \text{ GeV}$
 - $m_t^{\text{OS}} = 172.5 \text{ GeV}$
 - $m_t^{\overline{\text{MS}}}(m_t^{\overline{\text{MS}}}) = 163.4 \text{ GeV}$
 - $m_b^{\overline{\text{MS}}}(m_b^{\overline{\text{MS}}}) = 4.18 \text{ GeV}$
 - $G_F = 1.16639 \cdot 10^{-5} \text{ GeV}^{-2}$
 - NNPDF40_nlo_as_01180
- $p_{T,j_1} > 20 \text{ GeV}$
anti-kt algorithm with $R = 0.4$
7-pt scale variation about:
$$\mu_R^0 = \mu_F^0 = \frac{H_T}{2} = \frac{1}{2} \left(\sqrt{m_H^2 + p_T^2} + \sum_i |p_{T,i}| \right)$$

inclusive Higgs p_T distribution



QCD NLO corrections Bonciani VDD Frellesvig Moriello Hidding Hirschi Salvatori Somogyi Tramontano 2022

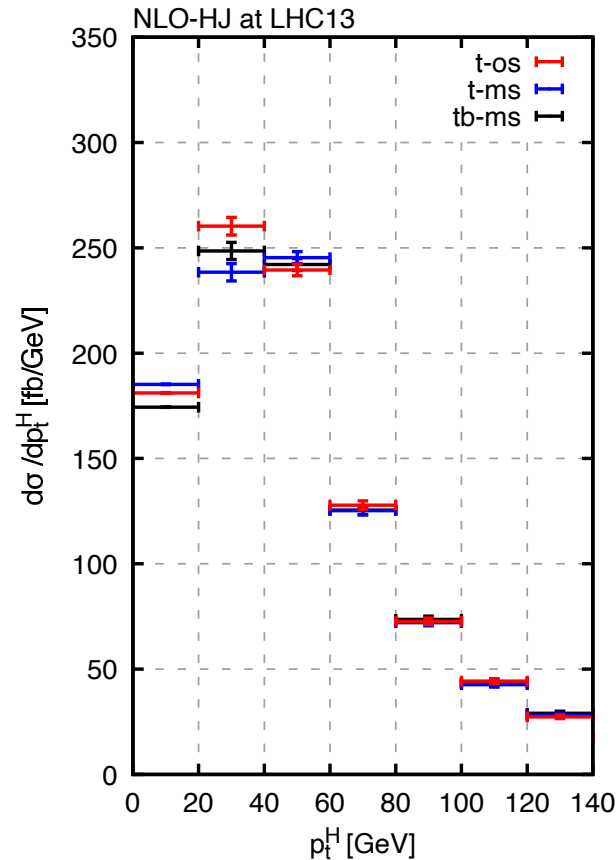
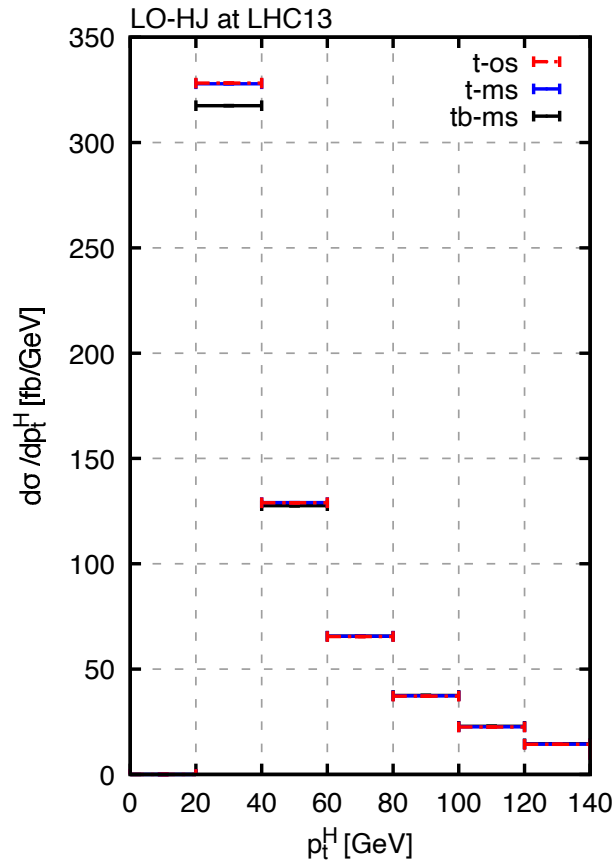
for the top-quark, with on-shell and $\overline{\text{MS}}$ schemes
for top- and b -quarks with $\overline{\text{MS}}$ scheme

renormalisation of internal masses	σ_{LO} [pb]	σ_{NLO} [pb]
top+bottom- $(\overline{\text{MS}})$	$12.318^{+4.711}_{-3.117}$	$19.89(8)^{+2.84}_{-3.19}$
top- $(\overline{\text{MS}})$	$12.538^{+4.822}_{-3.183}$	$19.90(8)^{+2.66}_{-2.85}$
top- (OS)	$12.551^{+4.933}_{-3.244}$	$20.22(8)^{+3.06}_{-3.09}$

- from LO to NLO large k factor and reduction of scale uncertainty
- top- b interference is a negative correction at $\mathcal{O}(\alpha_s^3)$ but positive at $\mathcal{O}(\alpha_s^4)$
- effect of top mass renormalisation utterly negligible at LO but 15 times bigger at NLO

$$\frac{\sigma_{t(\text{OS})}}{\sigma_{t(\overline{\text{MS}})}} - 1 = \begin{cases} 0.1\% \text{ at LO} \\ 1.6\% \text{ at NLO} \end{cases}$$

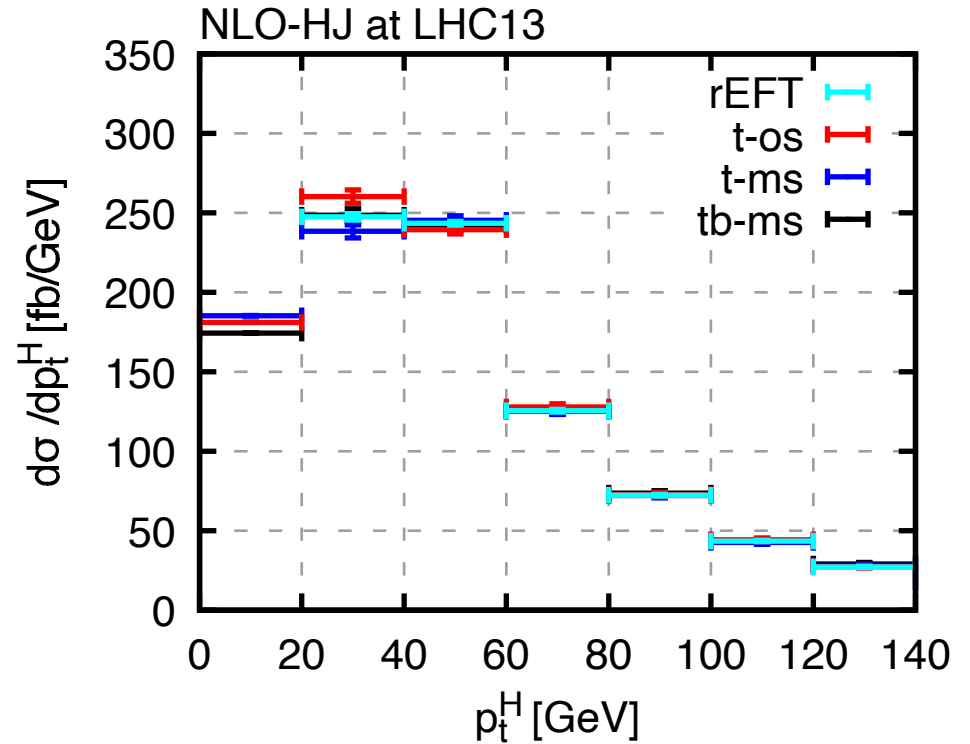
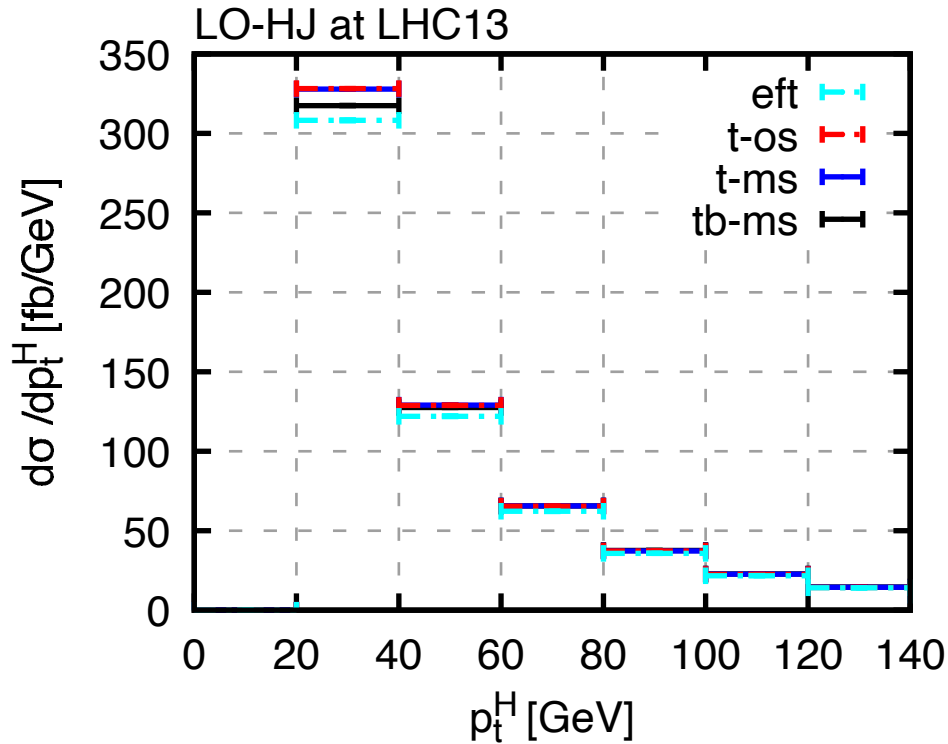
Higgs p_T distribution at low-intermediate p_T



20-40 GeV bin
 260^{+16}_{-83} fb/GeV
 249^{+21}_{-65} fb/GeV
 238^{+27}_{-98} fb/GeV

- at LO no events below 20 GeV since $p_{T,j} > 20$ GeV
- at LO no appreciable difference between $t(\text{OS})$ and $t(\text{MSbar})$
- at NLO sizeable shape distortion in the lowest bins
- scale uncertainty bands (not shown) are much larger than differences

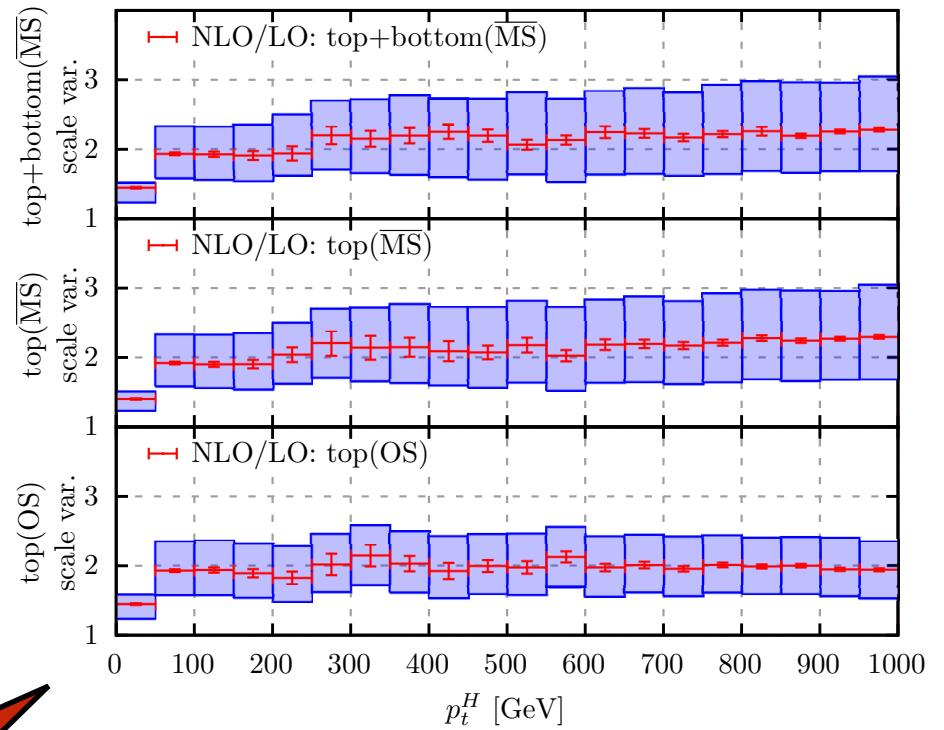
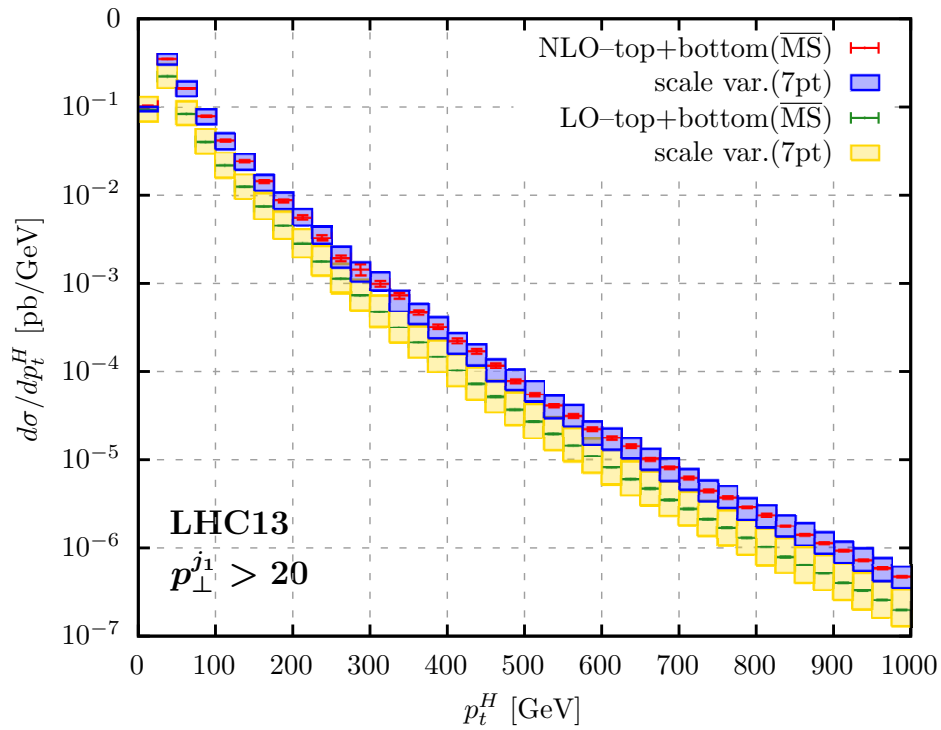
Higgs p_T distribution at low-intermediate p_T



at NLO agreement between exact and rHEFT in the low-middle p_T range

HEFT $m_H \ll 2m_t$ and $m_b \ll p_T \ll m_t$

Higgs p_T distribution at LHC

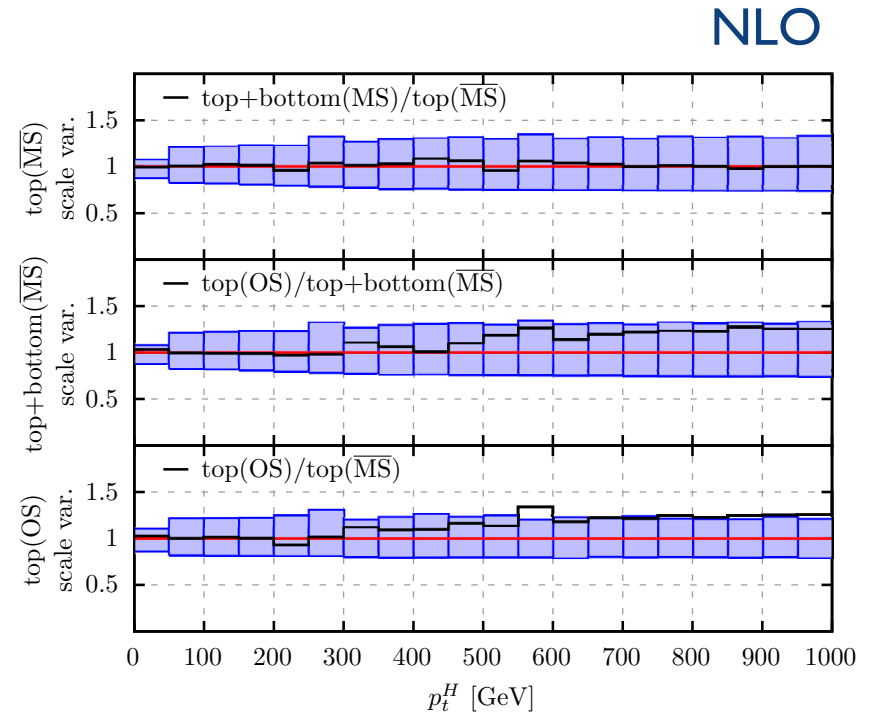
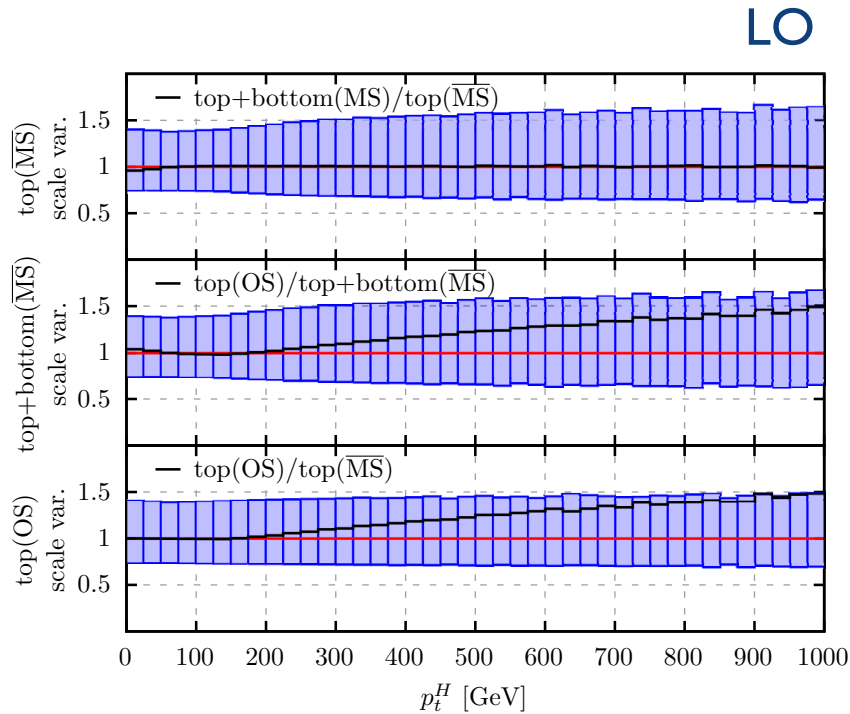


scale uncertainty bands = ratio of bands at **NLO** over central value at **LO**



k factor almost always larger than 2 for **MSbar**, and about 2 for **OS**

Ratios of Higgs p_T distributions



- from **LO** to **NLO**, reduction of scale uncertainty and of mass renormalisation scheme dependence
- except in the lowest bins, no appreciable difference between $t+b(\overline{\text{MS}})$ and $t(\overline{\text{MS}})$
 The b quark, and thus top- b interference, is negligible, except at low end of p_T range
- p_T distribution for $t(\overline{\text{MS}})$ falls off faster than same for $t(\text{OS})$ as p_T increases because μ_R increases with p_T and so $m_t^{\overline{\text{MS}}}(\mu_R)$ decreases
- mass renormalisation scheme difference between $t(\overline{\text{MS}})$ and $t(\text{OS})$ is same size as scale uncertainty at high end of p_T range, both at **LO** and **NLO**

Conclusions

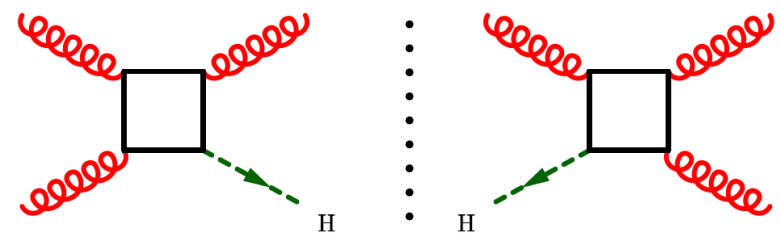
- we computed the Higgs p_T distribution at NLO in QCD including for the first time top and b quarks and the $\overline{\text{MS}}$ mass scheme
- computation has excellent numerical stability
- b quark, and thus top- b interference, is negligible, except at low end of p_T range, where it affects the shape of the distribution
- in the intermediate to high p_T range, use of top quark only is warranted, but sizeable dependence on mass renormalisation scheme
- p_T distribution can be improved:
mixed QCD-EW corrections (we already have $gg \rightarrow Hg$),
resummation,
top-charm interference, ...

Back-up slides

QCD NLO corrections



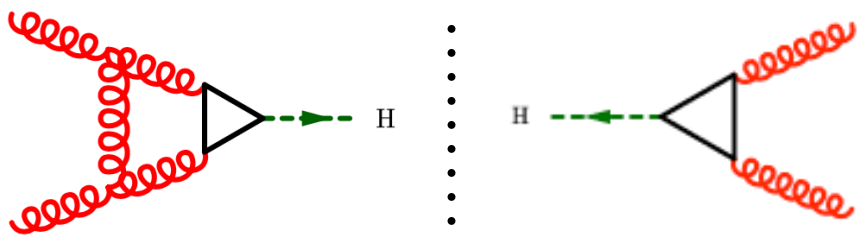
real radiation



K. Ellis Hinchliffe Soldate van der Bij 1988



virtual corrections



Djouadi Graudenz Spira Zerwas 1993
Anastasiou Beerli Bucherer Daleo Kunstz 2006
Aglietti Bonciani Degrassi Vicini 2006

} in terms of Harmonic Polylogarithms (HPL)

Differential Equations



Differential Equation method to solve the MIs

$$\partial_i f(x_n; \varepsilon) = A_i(x_n; \varepsilon) f(x_n; \varepsilon)$$

f : N-vector of MIs, A_i : NxN matrix, $i=1, \dots, n$ external parameters

but in some cases ε -independent form

$$\partial_i f(x_n; \varepsilon) = \varepsilon A_i(x_n) f(x_n; \varepsilon)$$

Henn 2013

solution in terms of iterated integrals



mass values are floating \rightarrow

DEs solved with 3 (top) or 4 (top and b) external parameters

DEs: Series Expansion Method

- Take two points (a_1, \dots, a_n) and (b_1, \dots, b_n) in the n -dim parameter space, and parametrise the contour $\gamma(t)$ that connects the two points

$$\gamma(t) : t \rightarrow \{x_1(t), \dots, x_n(t)\} \quad \vec{x}(0) = \vec{a}, \quad \vec{x}(1) = \vec{b}$$

and write the differential equation with respect to t .

Then find a solution about a point τ by series expanding the coefficient matrix A and then iteratively integrating it.

The procedure works for both polylogarithmic and elliptic sectors

Moriello 2019

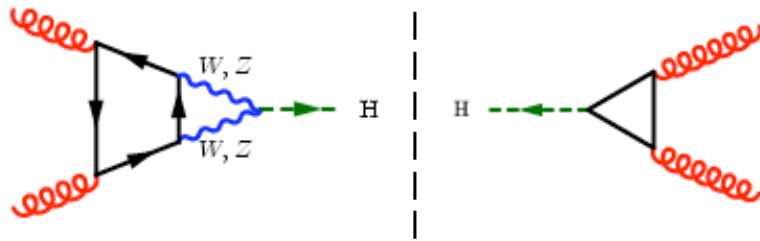
- numerical solution of DEs through [DiffExp](#):
Mathematica implementation of Moriello's series expansion method

Hidding 2021

- checked with AMFlow [Liu Ma Wang 2018](#)

QCD-EW interference

- The Higgs boson may (indirectly) couple to gluons also via the gauge coupling i.e. through a double (electroweak boson + quark) loop



Aglietti Bonciani Degrassi Vicini 2004
 (light fermion loop)
Degrassi Maltoni 2004
Actis Passarino Sturm Uccirati 2008
 (heavy fermion loop)

(in terms of MPLs)

(numerically
... elliptic integrals appear)

$O(\alpha_s^2 \alpha^2)$

- the top loop yields a 2% correction to the 5 light fermion loops

- gg-initiated QCD NLO corrections (light fermion loop)

computed in various approximations:

— $m_{W,Z} \rightarrow \infty$ limit

Anastasiou Boughezal Petriello 2009

— soft approximation

Bonetti Melnikov Tancredi 2018

— $m_{W,Z} \rightarrow 0$ limit

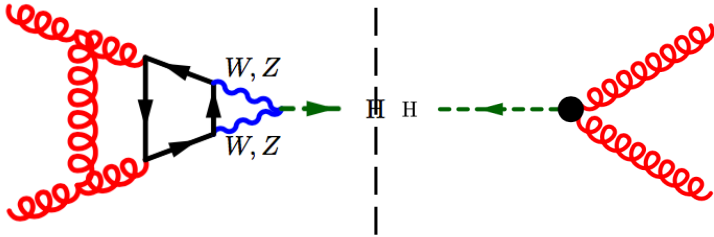
Anastasiou VDD Furlan Mistlberger Moriello Schweitzer Specchia 2018

and found to be about 5% wrt NLO (HEFT) cross section

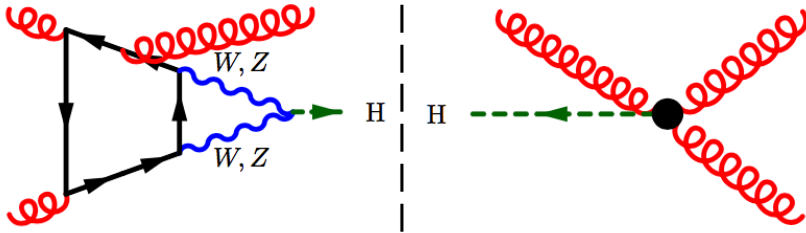
QCD-EW interference

🌐 gg-initiated QCD NLO corrections (light fermion loop): $O(\alpha_s^3 \alpha^2)$

Becchetti Bonciani VDD Hirschi Moriello Schweitzer 2020



Bonetti Melnikov Tancredi 2016



Becchetti Bonciani Casconi VDD Moriello 2018
 Bonetti Panzer V. Smirnov Tancredi 2020
 Becchetti Moriello Schweitzer 2021

IR local subtraction schemes

MadGraph MC@NLO

Frixione Kunszt Signer 1995
 Frederix Frixione Maltoni Stelzer 2009

COLORFUL

VDD Somogyi Trocsanyi 2006
 Somogyi 2009
 VDD Deutschmann Lionetti 2019

LO $\sigma_{gg \rightarrow H+X}^{(\alpha_s^2 \alpha^2)} = 0.68739_{-17.3\% -2.0\%}^{+23.4\% +2.0\%}$ pb

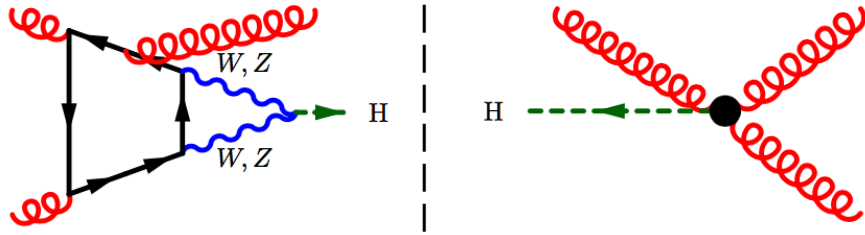
NLO $\sigma_{gg \rightarrow H+X}^{(\alpha_s^2 \alpha^2 + \alpha_s^3 \alpha^2)} = 1.467(2)_{-14.6\% -2.0\%}^{+18.7\% +2.0\%}$ pb

i.e. NLO 110% wrt LO

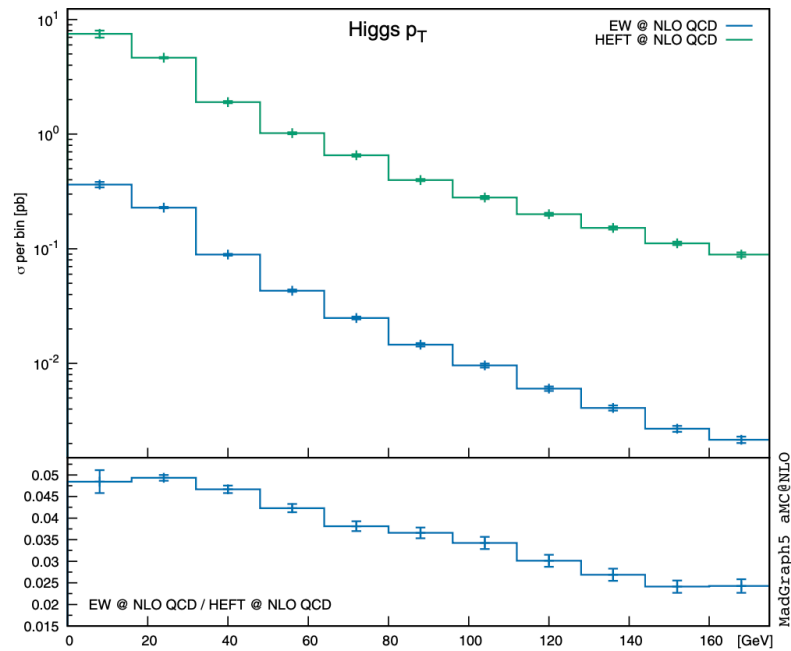
gg-initiated NLO corrections in HEFT $\sigma_{gg \rightarrow H+X}^{(\text{HEFT}, \alpha_s^2 \alpha + \alpha_s^3 \alpha)} = 30.484_{-15.3\% -1.9\%}^{+19.8\% +1.9\%}$ pb

thus our NLO result 4.8% wrt gg-initiated NLO HEFT

Higgs p_T distribution due to QCD-EW interference



Becchetti Bonciani VDD Hirschi Moriello Schweitzer 2020



gg-initiated QCD-EW p_T spectrum harder than HEFT