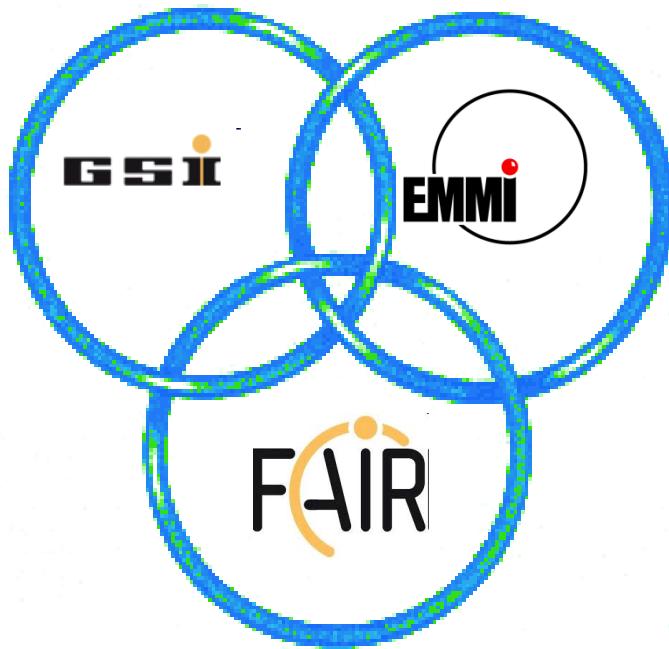


**DREB 2012**  
**Direct Reactions with Exotic Beams**  
**26-29 March 2012**

**Angular-momentum content of  
momentum profile  
in a neutron knockout from  $^{14}\text{Be}$ .**



L. V. Chulkov  
LAND-ALADIN collaboration



This talk is devoted to a novel experimental method using momentum profile of  $^{13}\text{Be}$  in a neutron knockout from  $^{14}\text{Be}$  for studies the  $^{13}\text{Be}$  structure.

Puzzling structures of neutron-rich berylliums require

## Introduction

$^{12}\text{Be}$  is well bound and is a good core for  $^{13}\text{Be}$

$$S_n = 3.7 \text{ MeV}$$

$$S_{2n} = 3.2 \text{ MeV}$$

$\frac{1}{2}^+$  state  $^{13}\text{Be} = {}^{12}\text{Be} \otimes (1s_{1/2})$



# Situation is complex: neutron-rich berylliums are essentially the few-body systems.

$^{12}\text{Be}$   $0^+$  ground state

F.C.Barker, J.Phys.G 2(1976)L45

T=2 states of A=12 nuclei.

Disappearance of N=8 magicity  
1976

$$^{12}\text{Be}(\text{g.s.}) = \alpha \left[ {}^{10}\text{Be} \otimes (1s_{1/2})^2 \right] + \beta \left[ {}^{10}\text{Be} \otimes (0p_{1/2})^2 \right] + \gamma \left[ {}^{10}\text{Be} \otimes (0d_{5/2})^2 \right]$$

$^{13}\text{Be}$   $1/2^+$  state

$$^{13}\text{Be}(1/2^+) = \zeta \left[ {}^{10}\text{Be} \otimes (0p_{1/2})^2 \otimes (1s_{1/2}) \right] + \eta \left[ {}^{10}\text{Be} \otimes (0d_{5/2})^2 \otimes (1s_{1/2}) \right]$$

	$\alpha^2$	$\beta^2$	$\gamma^2$	S
H.Fortune +, Phys.Rev. C 74(2006)024301	0.53	0.32	0.15	$\leq 0.47$
C.Romero +, Phys.Rev. C 77(2008)054313	0.67-0.76	0.13-0.19	0.10-0.13	$\leq 0.32$
F.Barker, J.Phys. G 36(2009) 038001	0.35	0.31	0.34	$\leq 0.69$
A.Navin +, Phys.Rev.Lett., 85(2000)266	0.38*	0.32*	0.30	$\leq 0.62$

Few-body system → s-wave resonance can exist.

$$S = (\beta\zeta + \gamma\eta)^2$$

(\*) numerical data are taken from F.Barker J.Phys. G 36(2009)038001.

# **s-wave resonances**

## **illustrated by the $\frac{1}{2}^+$ state in ${}^9\text{Be}$**

The description of this unbound level is a long-standing problem. Despite the sizable amount of data, there still exist considerable uncertainties of the resonance parameters.

O.Burda et al., Phys.Rev. C 82, 015808 (2010)  
F.Barker, Phys.Rev. C 68, 054602 (2003)  
Aust. J. Phys. 53, 247 (2000).  
V.Efros et al., Eur.Phys.J. A 4, 33 (1999)  
E.Garrido et al., Phys.Rev.Lett. B 684, 132 (2010)

## **S-wave resonance or virtual state?**

$a = -27.6 \text{ fm}$ ;  $r_0 = 8.8 \text{ fm} \rightarrow$  Efros +

**$E_s = -27 \text{ keV}$**

$E_r = 19 \text{ keV}$ ,  $\Gamma = 217 \text{ keV} \rightarrow$  Kuechler +

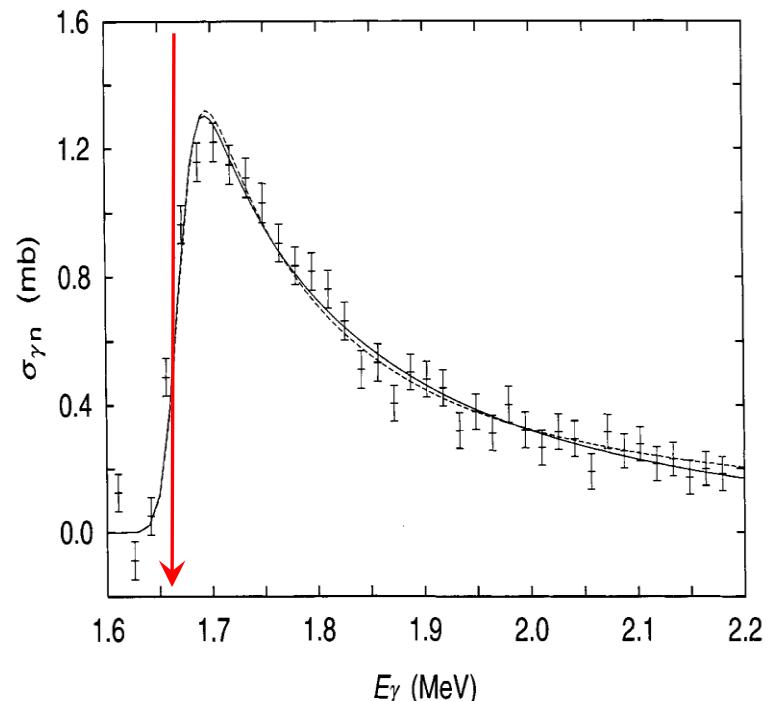
**$E_s = -0.62 \text{ keV}$**

$E_r = 67.6 \text{ keV}$ ,  $\Gamma = 280 \text{ keV} \rightarrow$  Barker

**$E_s = -23 \text{ keV}$**

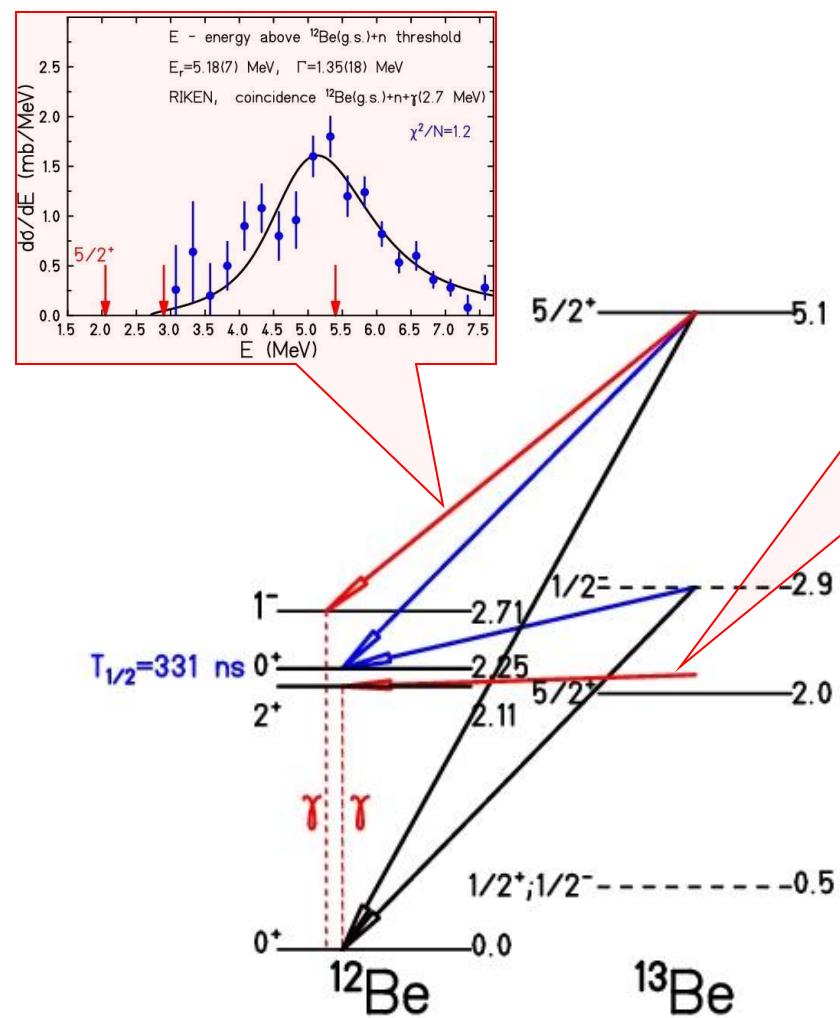
$E_r = 83(6) \text{ keV}$ ,  $\Gamma = 274(10) \text{ keV} \rightarrow$  Burda +

**$E_s = -30 - i 77 \text{ keV}$**

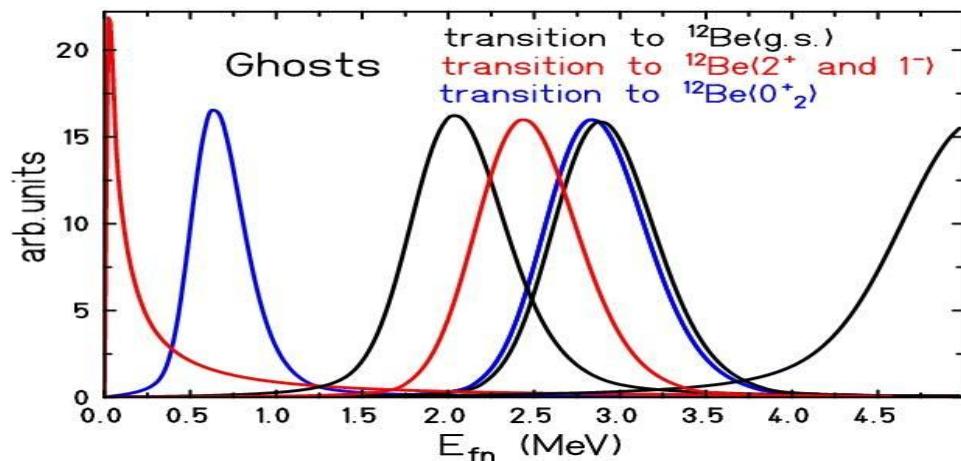
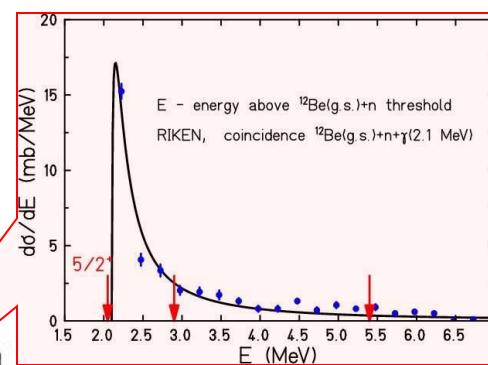


${}^9\text{Be}(\gamma, n){}^8\text{Be}$  cross section as a function of  $E_\gamma$ ,  
Kuechler et al., Z. Phys. A 326, 447 (1987).

# Situation is complex: ghosts in the $^{12}\text{Be}+\text{n}$ relative-energy spectrum



Y.Kondo et al., Phys.Lett. B 690, 245 (2010)  
Coincidence with 2.7 Mev  $\gamma$  and 2.1 MeV  $\gamma$



# $^{13}\text{Be}$ puzzle

## Virtual state as a dominant

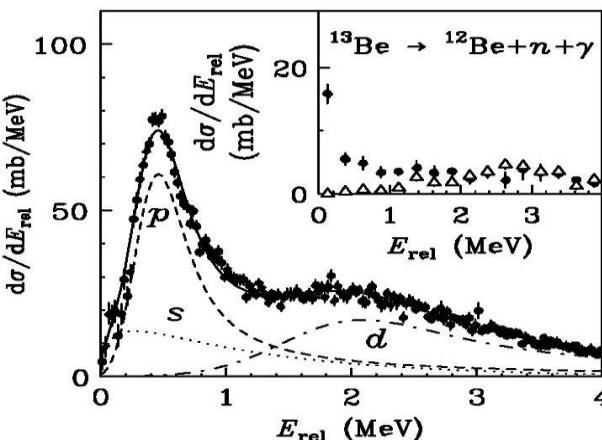
$a_s = -3.2(1.0)$  fm (antibound state)

$E_r = 0.41(8)$  MeV,  $\Gamma = 0.4(5)$  MeV

$E_r = 3.04$  MeV,  $\Gamma = 0.4$  MeV

$E_r = 2.0$  MeV,  $\Gamma = 0.3$  MeV

H.Simon et al., Nucl.Phys. A791, 267 (2007)



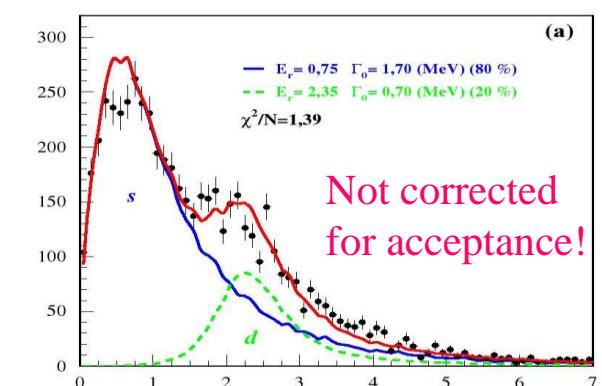
## Narrow p-wave resonance

$a_s = -3.4(6)$  fm (antibound state)

$E_r = 0.51(1)$  MeV,  $\Gamma = 0.45(3)$  MeV

$E_r = 2.39(5)$  MeV,  $\Gamma = 2.4(2)$  MeV       $\Gamma = 2.5 \Gamma_{\text{sp}}$  !

Y.Kondo et al., Phys.Lett. B 690, 245 (2010)



## Broad s-wave resonance.

$E_r = 0.7(2)$  MeV,  $\Gamma = 1.7(2)$  MeV

$E_r = 2.4(2)$  MeV,  $\Gamma = 0.6(3)$  MeV

G.Randisi, PhD Thesis 2012,  
see also J.L.Lecouey, Few-Body Systems  
34, 21 (2004).

Three recent experiments resulted to similar spectra but also to vastly different interpretations

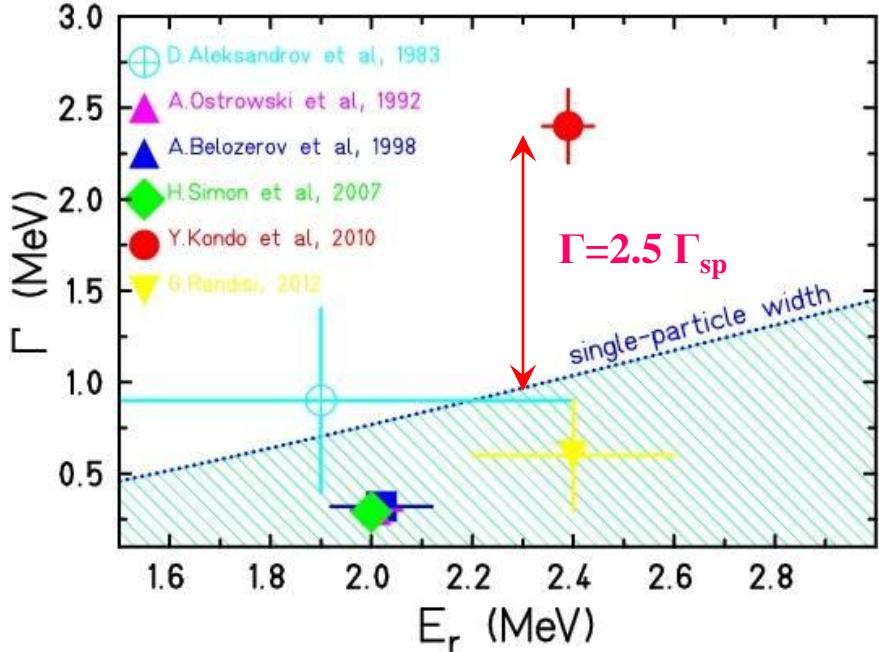
# Reaction Dependence of Nuclear Decay Widths

Various reactions have been used to study the reaction dependence of a resonance decay width. The resonance widths are self-consistent and indicate little if any reaction dependence.

D.Overway et al., Nucl.Phys. A366, 299 (1981)

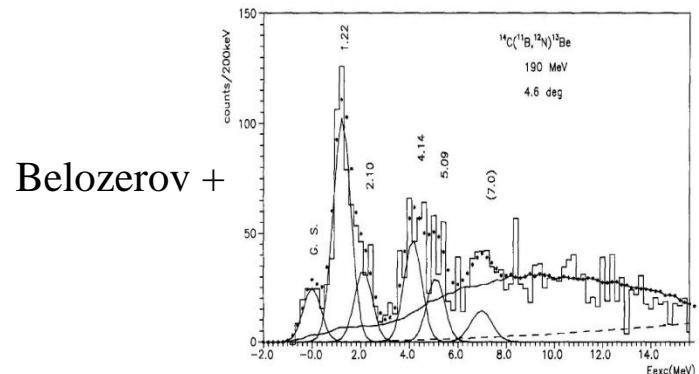
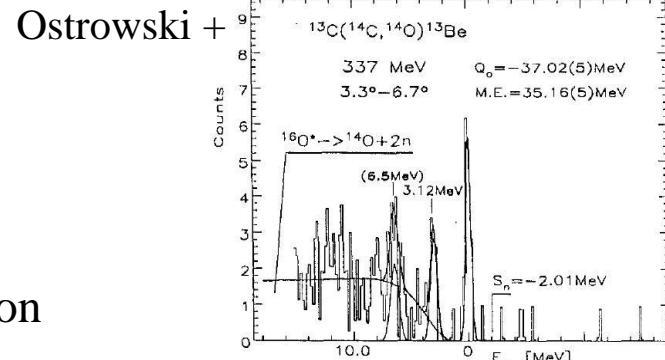
N.Arena et al., Il Nuovo Cimento, A106, 1007(1993)

**5/2<sup>+</sup> state in  $^{13}\text{Be}$**

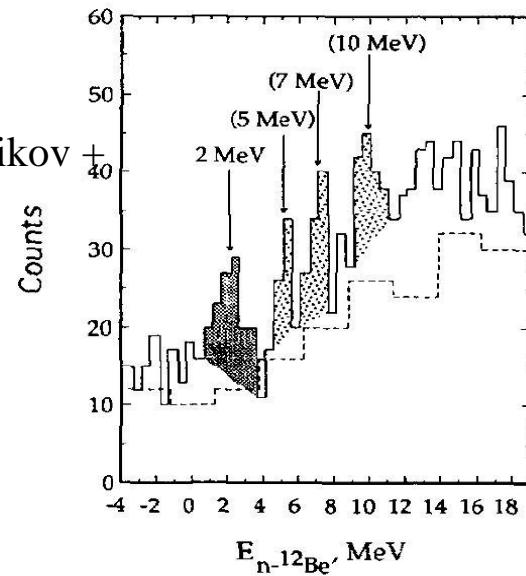


Reference for  $\Gamma_{\text{sp}}$ :

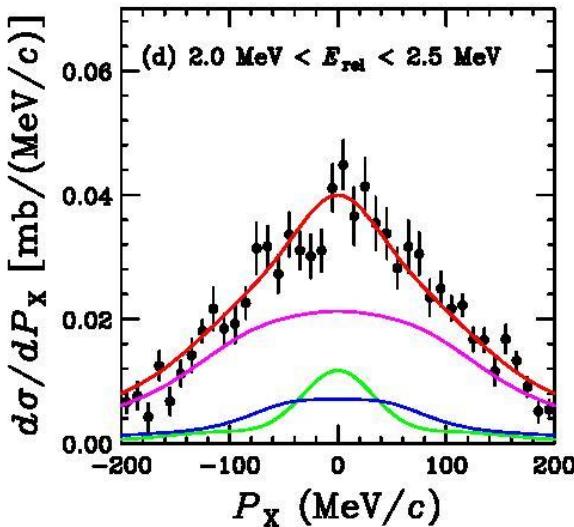
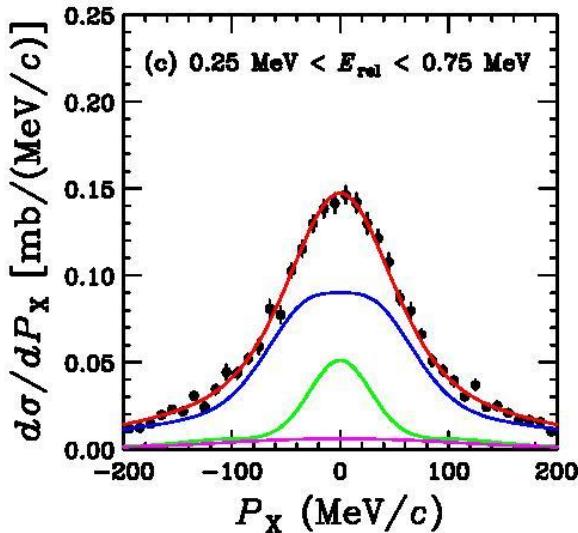
A.Bohr & B.R.Mottelson, Nuclear structure, 1998, v.1, p.441, Eq.3f-51



Korsheninnikov

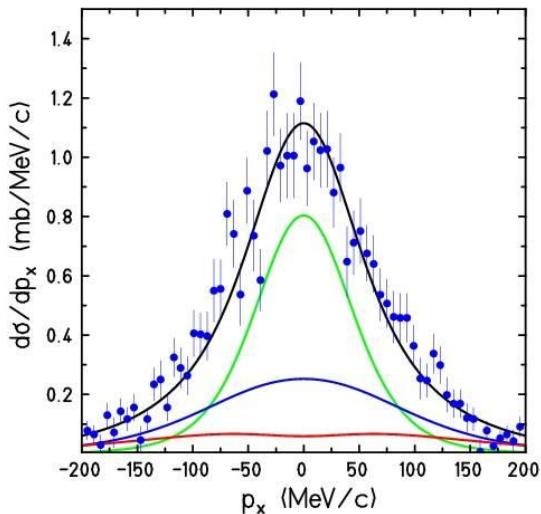


# Shapes of momentum distributions cannot remove ambiguity



Yosuke Kondo  
Doctoral Dissertation  
2007  
 $^1\text{H}(^{14}\text{Be}, ^{12}\text{Be}+\text{n})$ ,  $E=69 \text{ MeV/u}$

s- p- d-



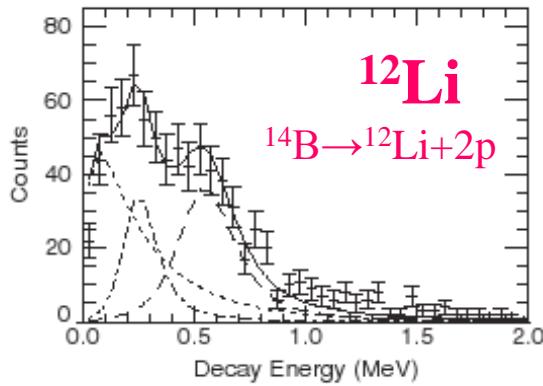
H.Simon et al., Nucl.Phys. A791, 267 (2007)  
 $\text{C}(^{14}\text{Be}, ^{12}\text{Be}+\text{n})$ ,  $E=287 \text{ MeV/u}$

**Our aim is in finding  
free from contradiction  
interpretation of existing experimental data on  
 $^{13}\text{Be}$**

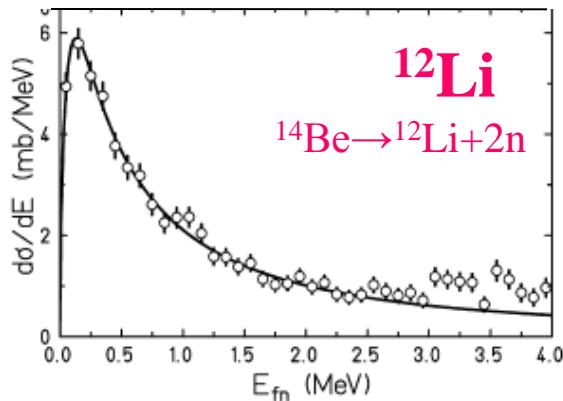
**New observable – momentum profile-  
width of  $^{12}\text{Be} + \text{n}$  momentum distribution  
as a function of  $^{12}\text{Be} + \text{n}$  relative energy  
in a neutron knockout from  $^{14}\text{Be}$ .**

# Step aside....

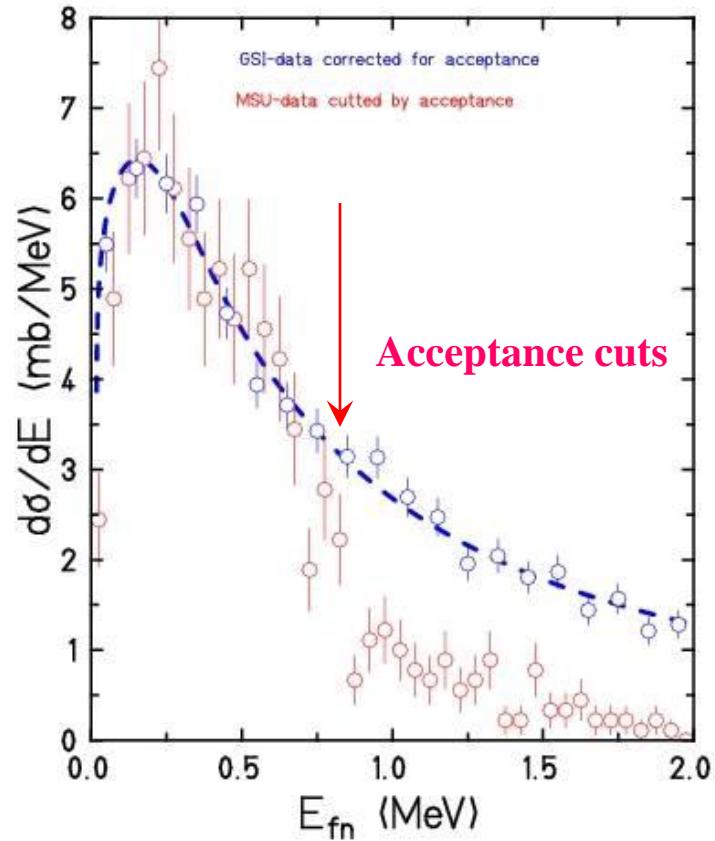
Our aim is in finding free from contradiction interpretation of existing experimental data



The ground state (dotted) and two  $d$  states (dot-dashed and dashed).



The spectrum is fitted with a single virtual  $s$ -state.



C.C.Hall +, Phys.Rev. C 81, 021302 (2010)  
Yu.Aksyutina +, Phys.Lett. B 666, 430 (2008)

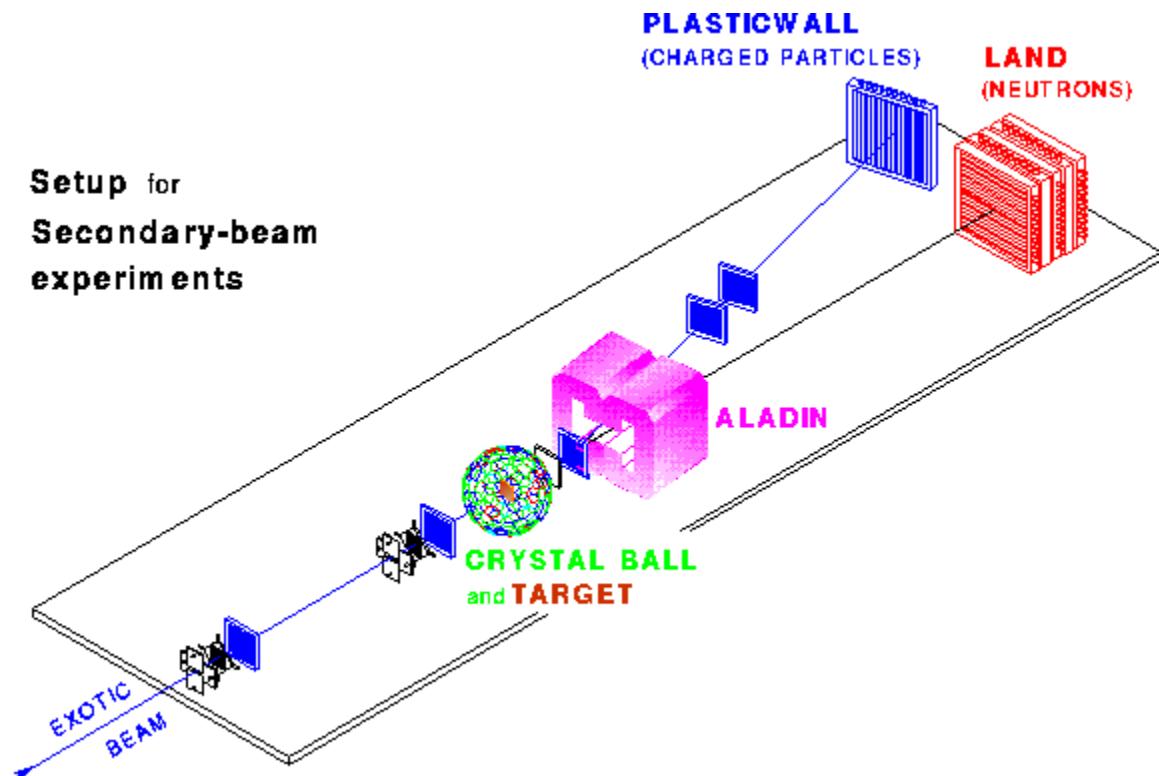
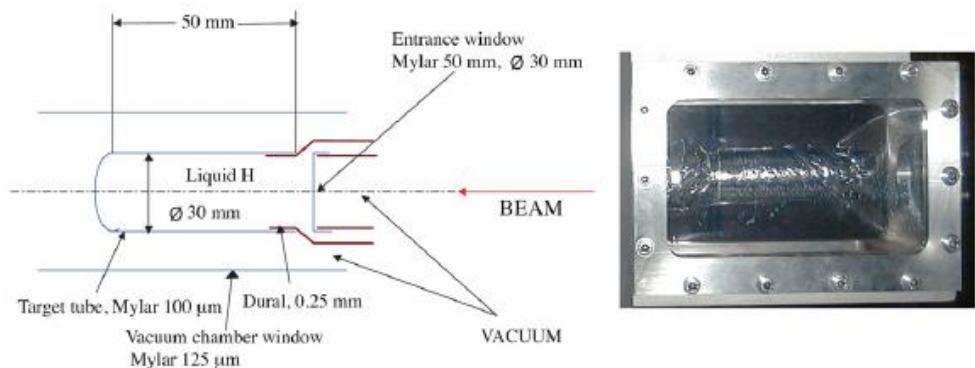
# Experimental set up

$^{8}\text{He}$  240 MeV/u

$^{11}\text{Li}$  280 MeV/u

$^{14}\text{Be}$  304 MeV/u

Liquid hydrogen target

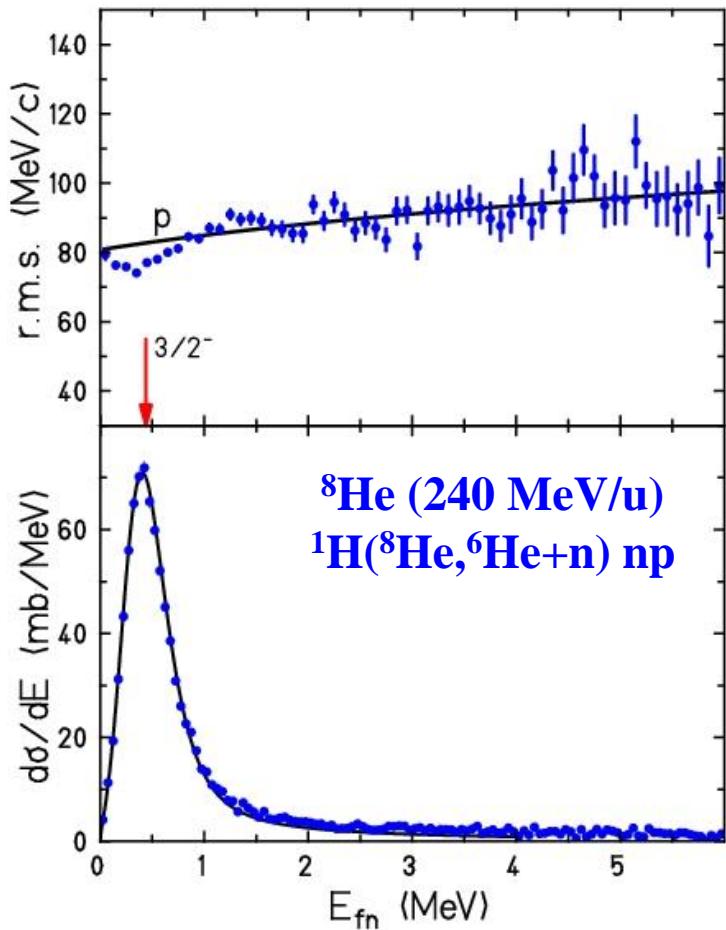


Setup for  
Secondary-beam  
experiments

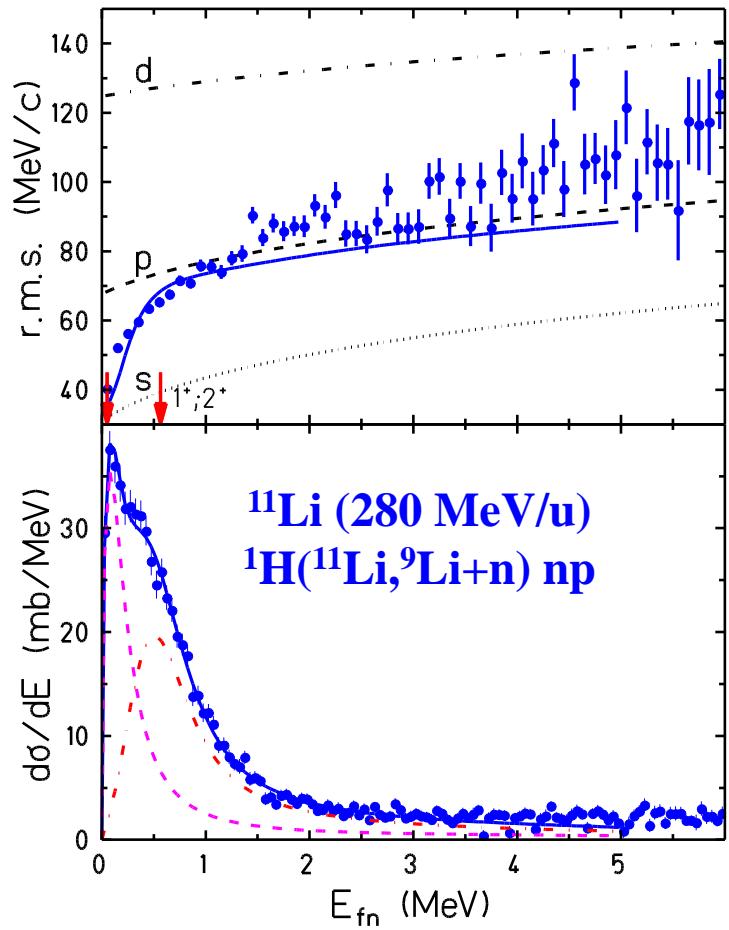
# Momentum width as a function of *fragment-n* relative energy

## Momentum Profile: $^7\text{He}$ & $^{10}\text{Li}$

$$P(E_{fn}) = \sqrt{\left\langle (p_f^x + p_n^x)^2 \right\rangle - \left\langle (p_f^x + p_n^x) \right\rangle^2}$$

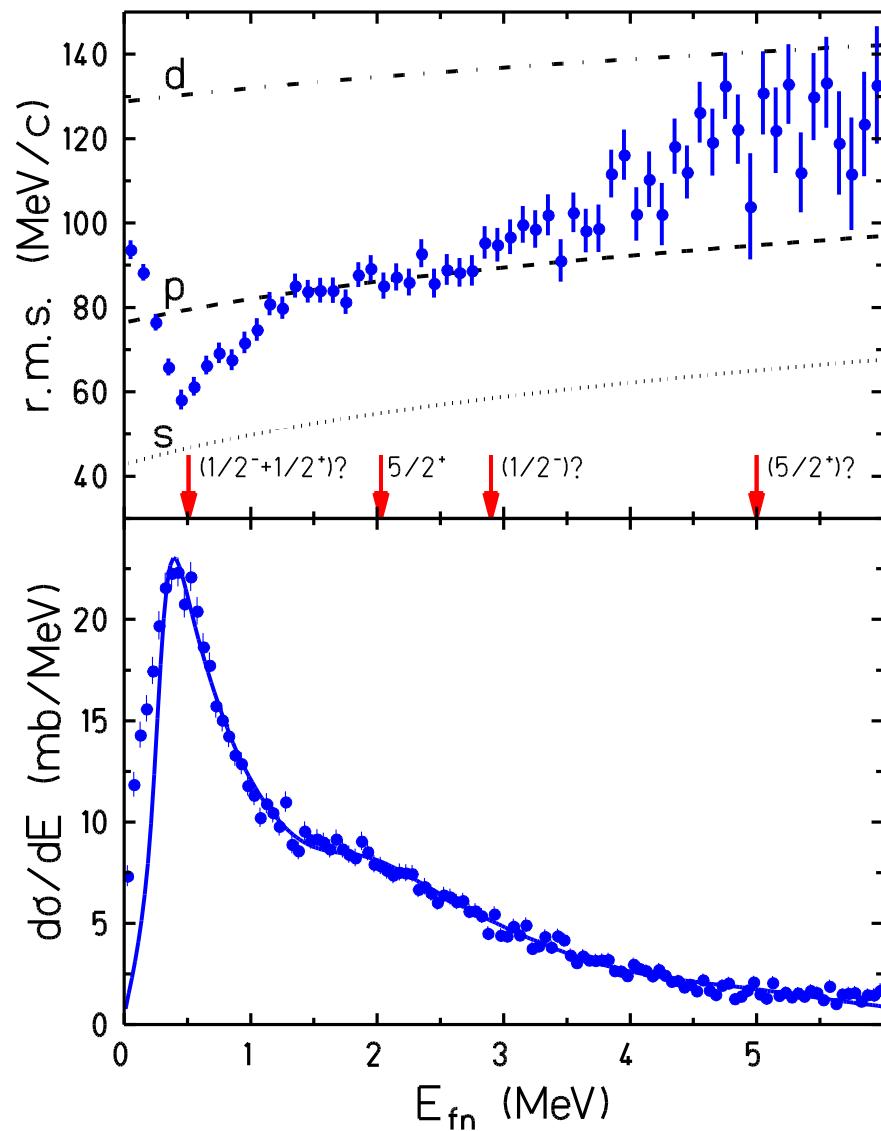


P.G. Hansen, PRL 77 (1996) 1016  
 M. Smedberg, Thesis Chalmers University of Technology



# Momentum Profile: $^{13}\text{Be} \rightarrow ^{12}\text{Be(g.s.)} + \text{n}$

$$P(E_{fn}) = \sqrt{\left\langle (p_f^x + p_n^x)^2 \right\rangle - \left\langle (p_f^x + p_n^x) \right\rangle^2}$$

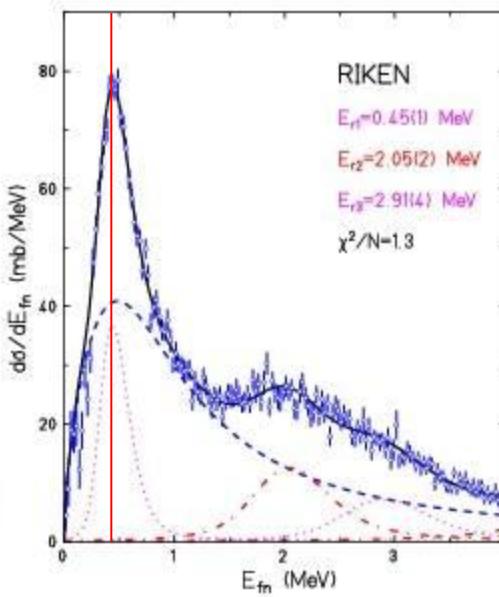
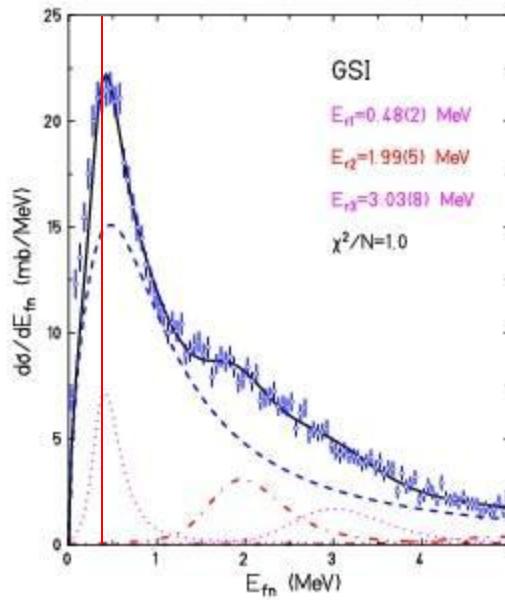
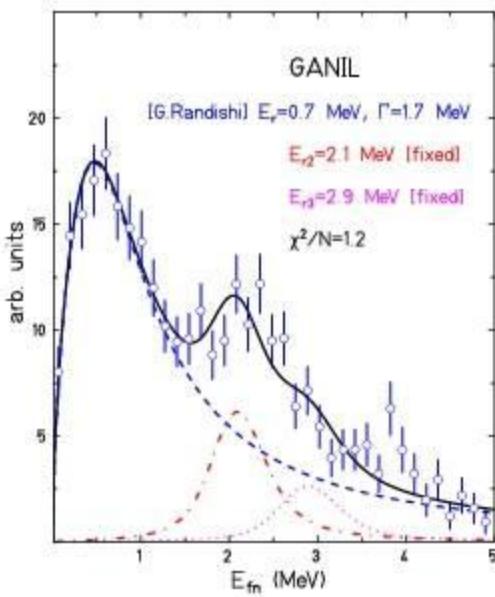


$^{14}\text{Be}$  (304 MeV/u)  
 $^1\text{H}(^{14}\text{Be}, ^{12}\text{Be} + \text{n})$  np

# Breit-Wigner $\ell=0$ resonance

$$\delta_0 = \tan^{-1} \left( \frac{\frac{1}{2} \Gamma_0}{E_r - E} \right)$$

$$\frac{d\sigma}{dE} \sim \frac{1}{k} (\sin \delta_0)^2 = 2\gamma^2 \left( \frac{\Gamma_0}{(E_r - E)^2 + \frac{\Gamma_0^2}{4}} \right)$$

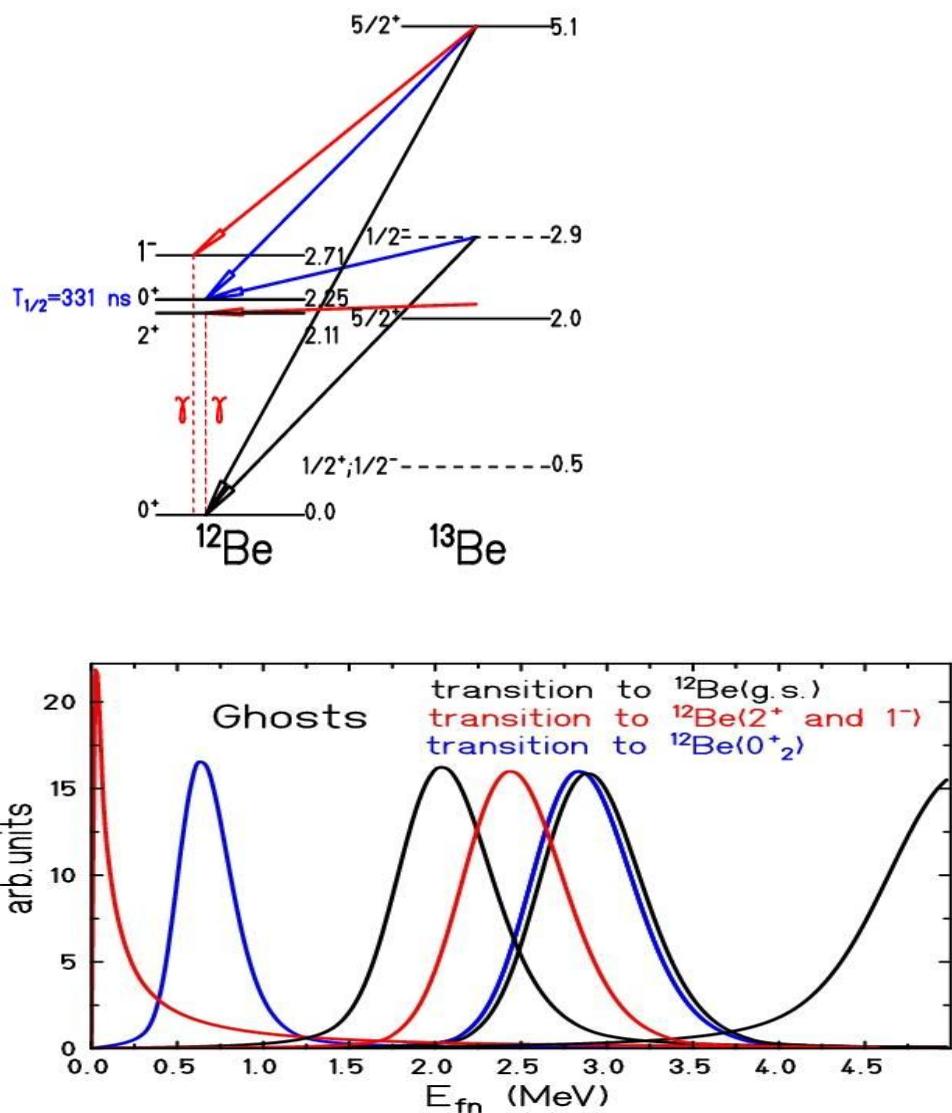
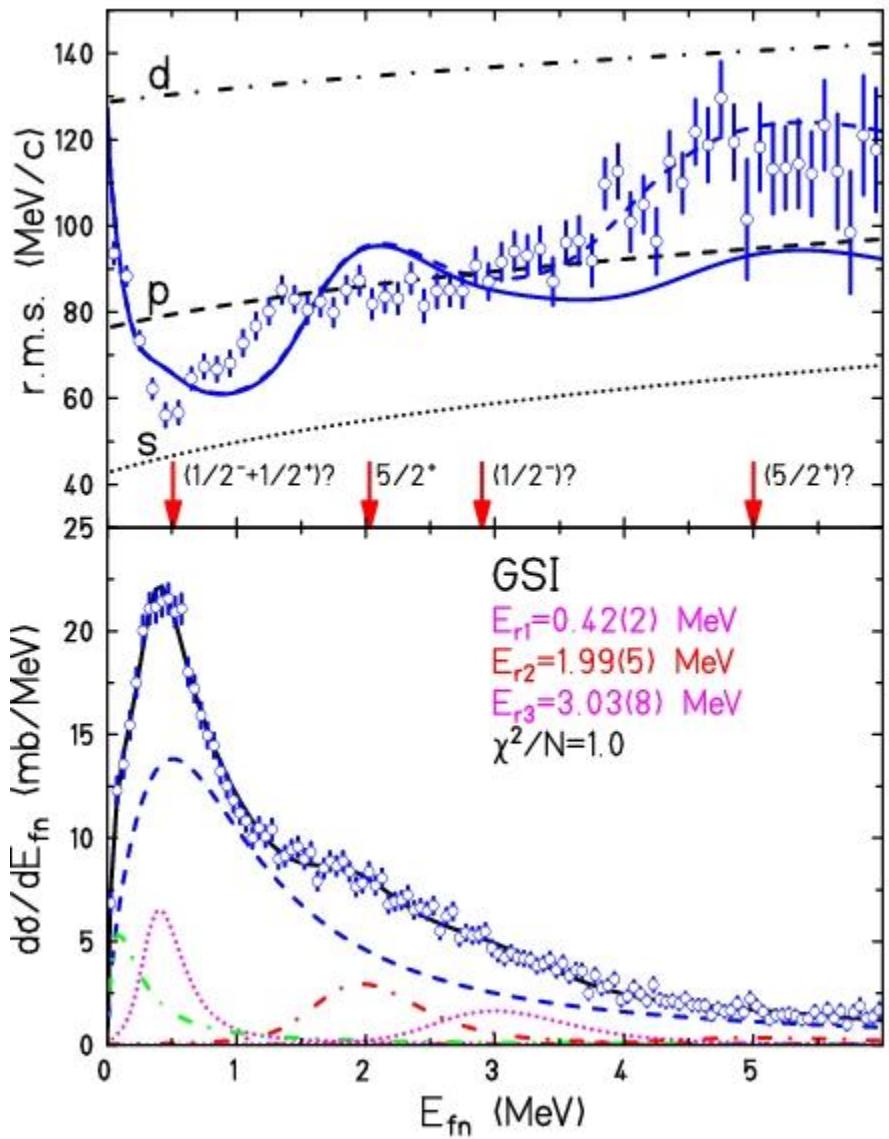


J.L.Lecouey,  
Few-Body  
Systems 34,  
21 (2004),  
corrected for  
acceptance

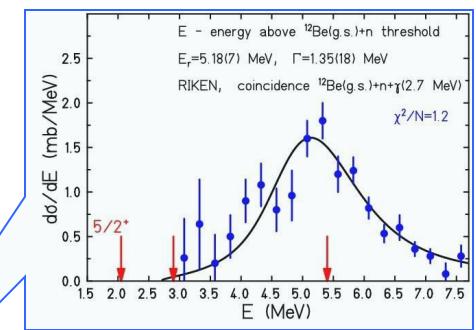
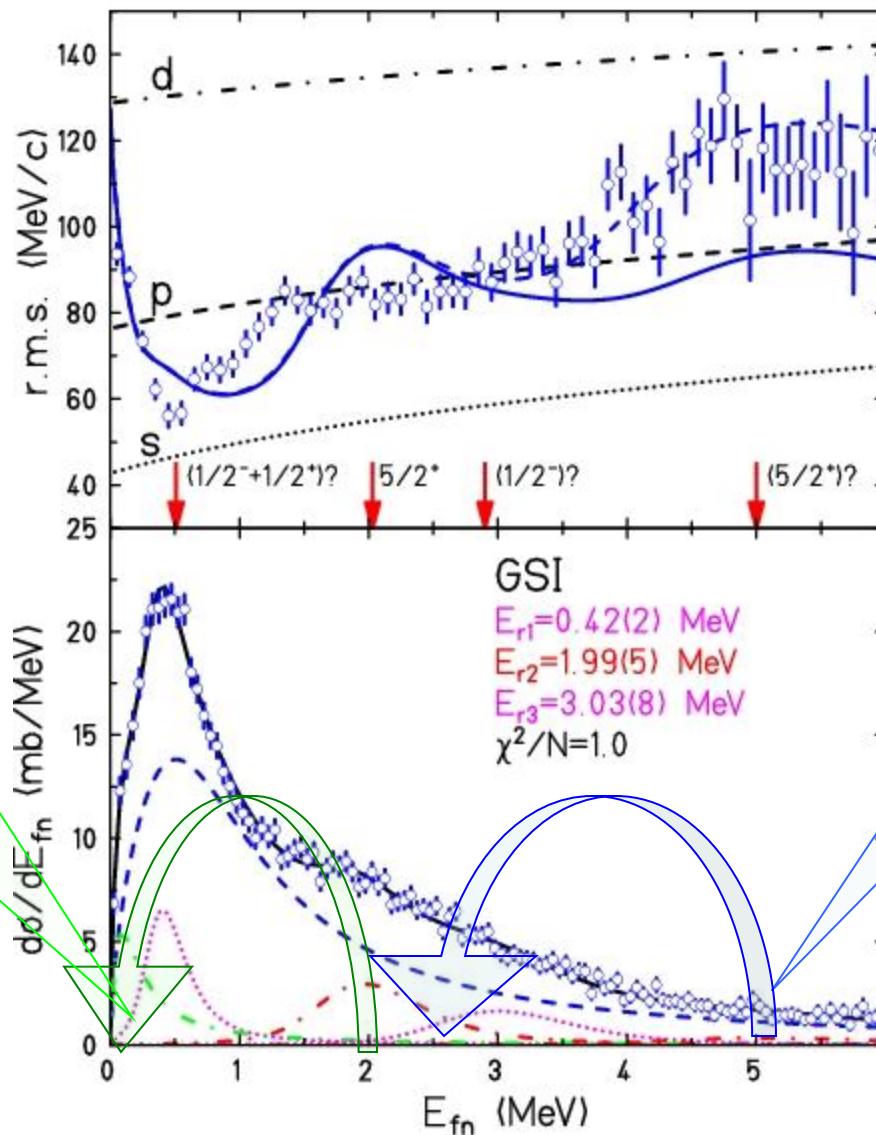
**Interference with potential scattering (background phase shift)**

$$\frac{d\sigma}{dE} \sim \frac{1}{k} (\sin(\delta_0 + \varphi_0))^2 = \frac{(\Gamma \cos(\varphi_0) + 2(E_r - E) \sin(\varphi_0))^2}{4k((E_r - E)^2 + \frac{\Gamma^2}{4})}$$

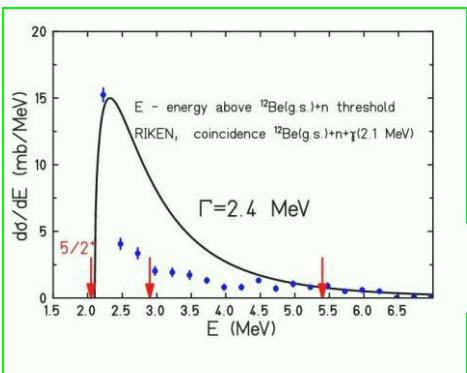
# Momentum Profile: $^{13}\text{Be} \rightarrow ^{12}\text{Be}(\text{g.s.}) + \text{n}$



# Momentum Profile: $^{13}\text{Be} \rightarrow ^{12}\text{Be}(\text{g.s.}) + \text{n}$



Y.Kondo et al., Phys.Lett. B  
690, 245 (2010)  
Coincidence with  
2.7 Mev  $\gamma$  and 2.1 MeV  $\gamma$



MCE



Thank you for your attention