

Shell evolution in neutron-rich Al isotopes around N=20 shell closure

Chiara Nociforo
GSI, Darmstadt

- Evolution of neutron shell structure
 - magic numbers ($N = 16, 20$), shell gaps
- GSI- FRS results on one-neutron removal reactions
 - $^{32-34}\text{Al}$ momentum distribution analysis

Magic numbers and shell gaps

To what extent the shell model is still valid in nuclei with large proton-neutron asymmetry ?

For light nuclei far off stability

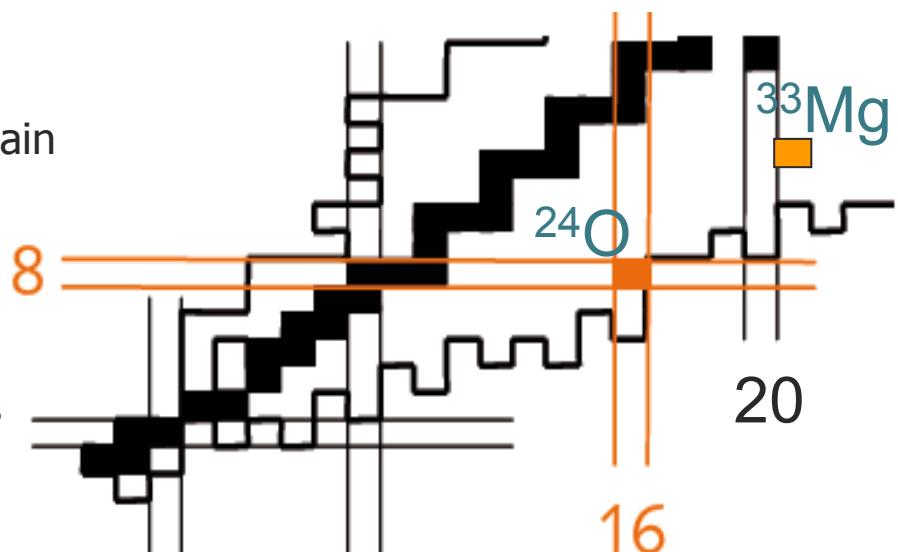
- new magic numbers
→ **N=16** new shell gaps in O isotopic chain

R. Kanungo, et al., PRL 102 (2009) 152501

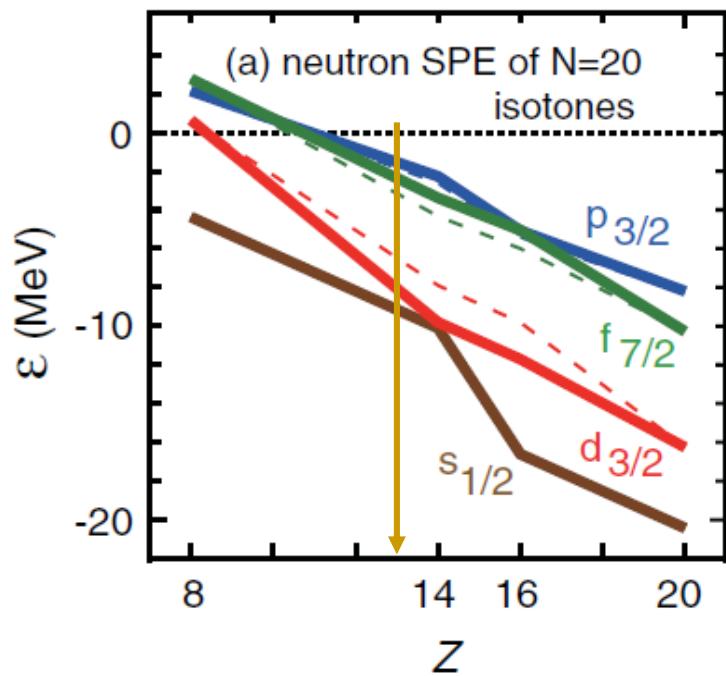
- change in shell ordering
→ **N=20** disappearance for Mg isotopes

(*Island of Inversion*)

R. Kanungo, et al., PLB 685 (2010) 253



N=20 gap evolution



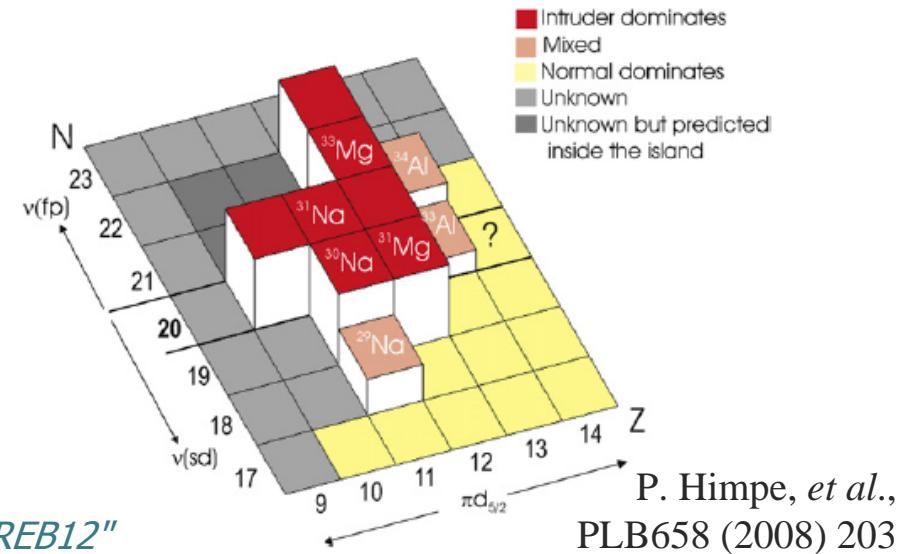
$Z=8 \rightarrow Z=20$, adding *sd* protons
 \rightarrow wide N=20 gap

T. Otsuka *et al.*, PRL 104 (2010) 012501

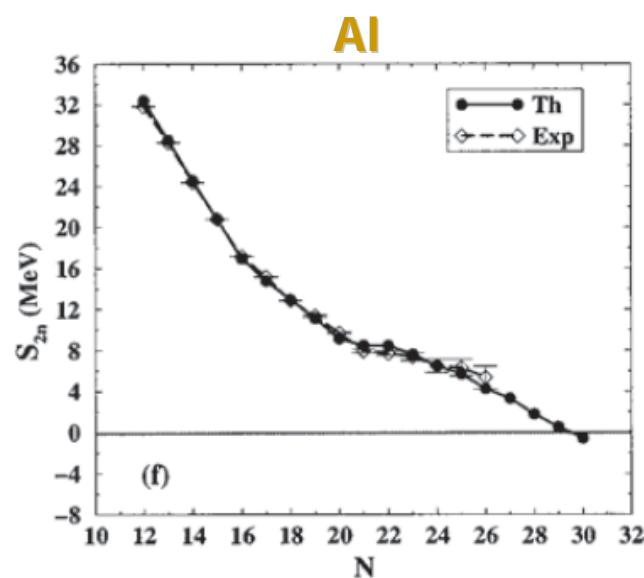
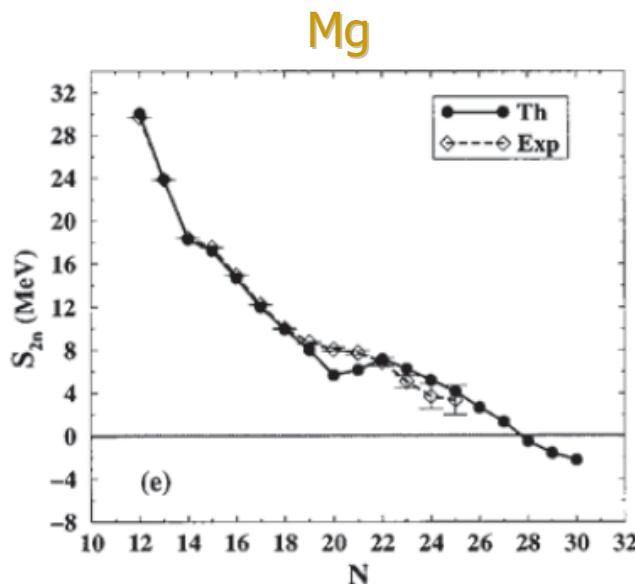
C. Nociforo - "DREB12"

Direct measurements of the weakness of the N=20 shell closure are difficult at lower Z

The n-rich Al isotopes are easier to access experimentally and are located in a *transition* region between the spherical shell of Si nuclei and the deformed Mg isotopes.



Two-neutron separation energy S_{2n}



E. Caurier, *et al.*, PRC58 (1998) 2033

Al: Exp S_{2n} do not show anomalies and are perfectly reproduced by shell model calculations involving the full sd proton shell ($Z = 8$) and the pf neutron shell ($N = 20$) as valence space

Al isotopic chain (A=32-36)

- β -decay and g-factor measurements available up to A=34

magnetic moments measurements of $^{33,34}\text{Al}$ show large discrepancies with shell model predictions

→ non-negligible presence of intruder configurations

$\sim 25\%$ in ^{33}Al and 60% in ^{34}Al , at least

(P. Himpe, *et al.*,
PLB643 (2006) 257,
PLB658 (2008) 203)

- polarization effects due in even-mass Al (N=21-23) to the unpaired $1d_{5/2}$ proton

pf shell

N = 20

$1d_{5/2}$ -ooooox

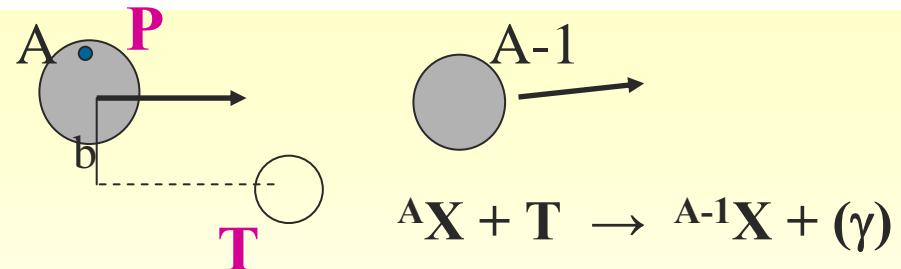
p

n

1n removal reactions test the neutron single particle structure

[¹ⁿ removal reactions at relativistic energies]

At high energy



structure & reaction mechanism can be much easily disentangle

calculations: Glauber theory $\longrightarrow |\psi\rangle = \text{core} + \text{neutron},$
eikonal approx.

$$\frac{d\sigma}{dp_{||}} = \int d\mathbf{r}_t \left| \frac{1}{\sqrt{2\pi}} \int \varphi_0(\mathbf{r}_t, z) e^{ip_z z} \right|^2 \int d\mathbf{b} D(\mathbf{b}, \mathbf{r}_t)$$

Sensitivity of the $p_{||}$ distribution to single particle states:

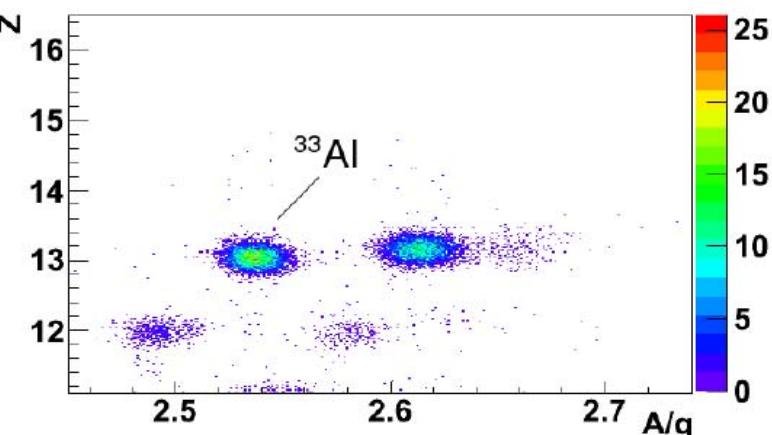
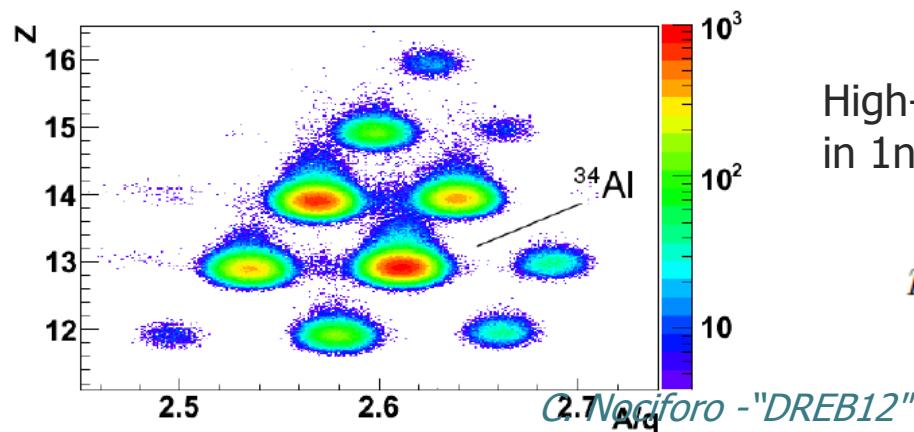
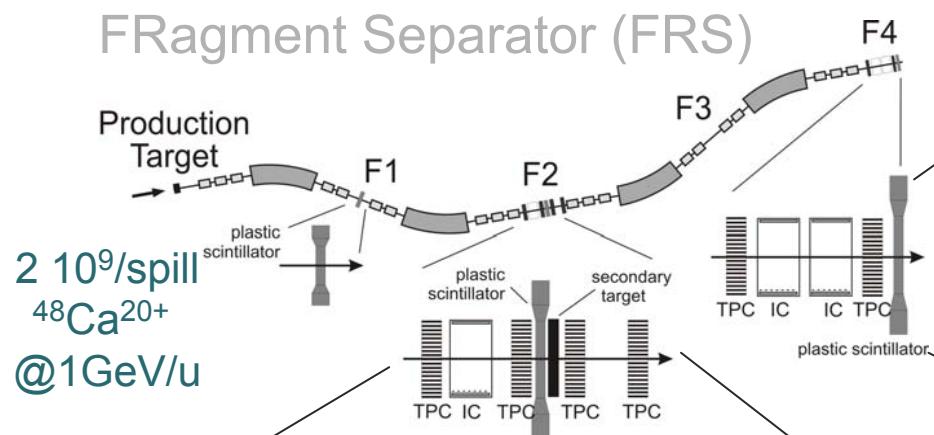
- Shape of $d\sigma/dp_{||}$ of the residual nucleus $\longrightarrow I_n$ of the removed nucleon
- Cross section σ_{-1n} \longrightarrow spectroscopic factors

C. Nociforo - "DREB12" $\sigma_{-1n} = \sum_l S_l \sigma^{sp}(\psi_{nlj} \otimes Al(I_c^\pi))$

Experimental technique

Relativistic energy RIBs advantages:

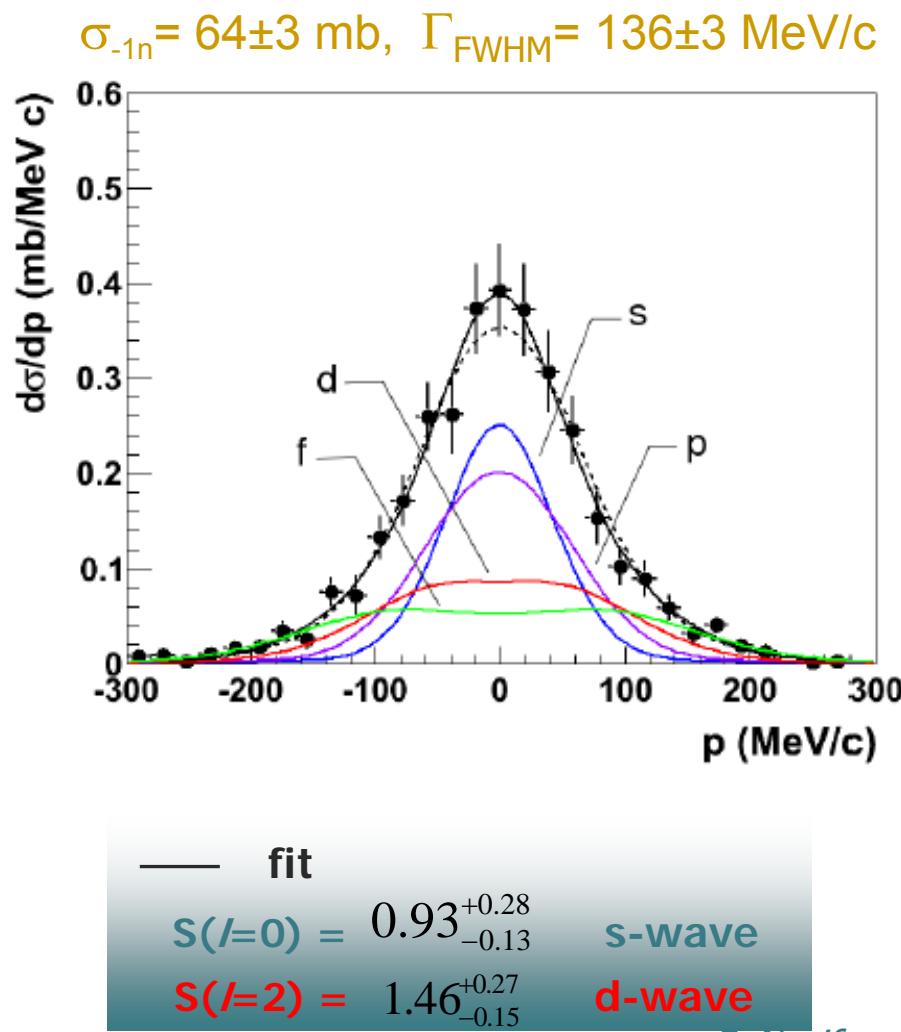
- thick target
- small forward scattering angles



High-resolution momentum ($\Delta p/p \sim 1.5 \cdot 10^{-4}$)
in 1n removal channel

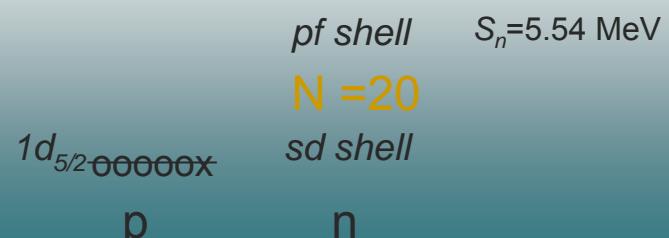
$$p_{lab} = B\rho \cdot q \cdot \left(1 + \frac{x_{F4} - C \cdot x_{F2}}{D_{F2-F4}} \right)$$

$[$ $^{33}\text{Al} \rightarrow n + ^{32}\text{Al}$ at 922 MeV/u $]$



$^{33}\text{Al}_{\text{g.s.}}(5/2^+)$: shell model calc. ([USDB](#))

$C^2S = 1.40 (l=0) \leftarrow 15\text{-}40\% \text{ higher}$
 $C^2S = 3.61 (l=2)$



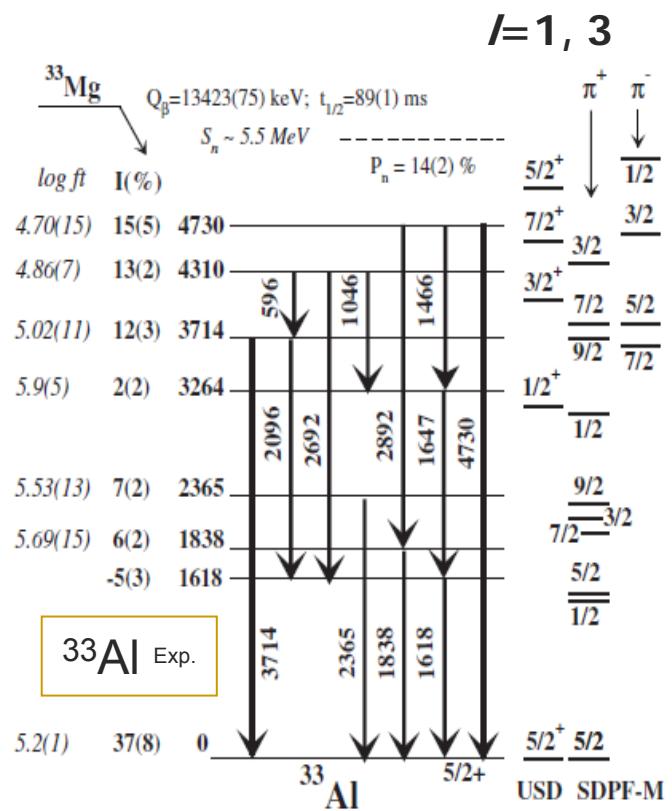
Adding $l=1, 3$
(p- and f-waves) } with negative parity core state ($E(4^-) = 1.2 \text{ MeV}$)

does not change the results of the fit

--- fit assuming $S(l=0) = 0$
 $S(l=1) < 1.63$, 60% upper limit
intruder configurations

$^{34}\text{Al} \rightarrow n + ^{33}\text{Al}$ at 880 MeV/u

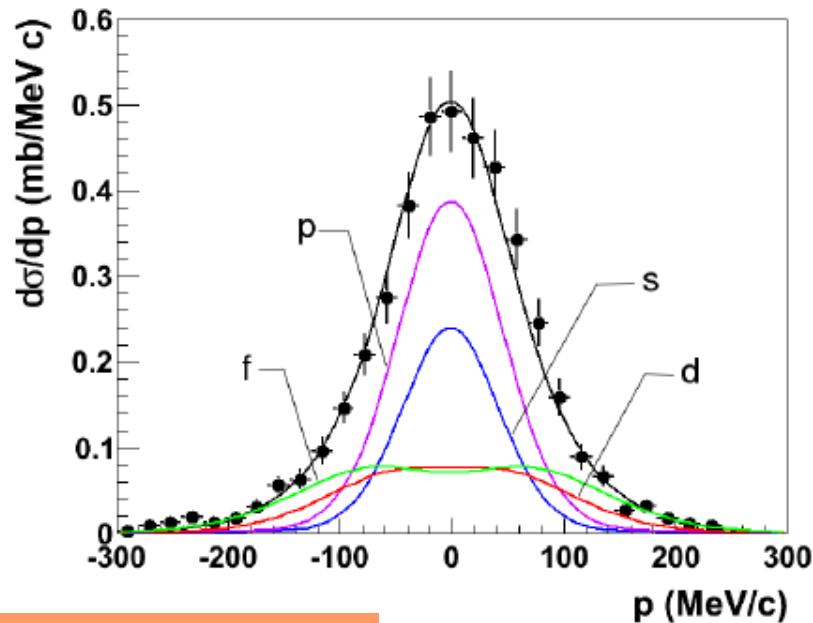
$^{34}\text{Al}_{\text{g.s.}}(4^-)$



$I=0, 2$
with
negative
parity
core states

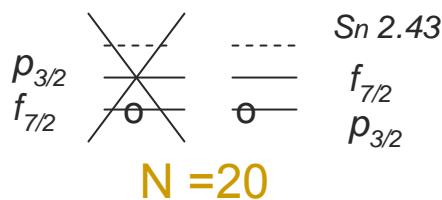
2p_{3/2} occupancy: 20-60%

$$\sigma_{-1n} = 81 \pm 4 \text{ mb}, \Gamma_{\text{FWHM}} = 134 \pm 3 \text{ MeV/c}$$



fit

$$\begin{aligned} S(I=0) &< 1.45 \\ S(I=1) &= 0.97^{+0.10}_{-0.45} \\ S(I=2) &= 1.40^{+0.63}_{-0.58} \\ S(I=3) &< 0.6 \end{aligned}$$



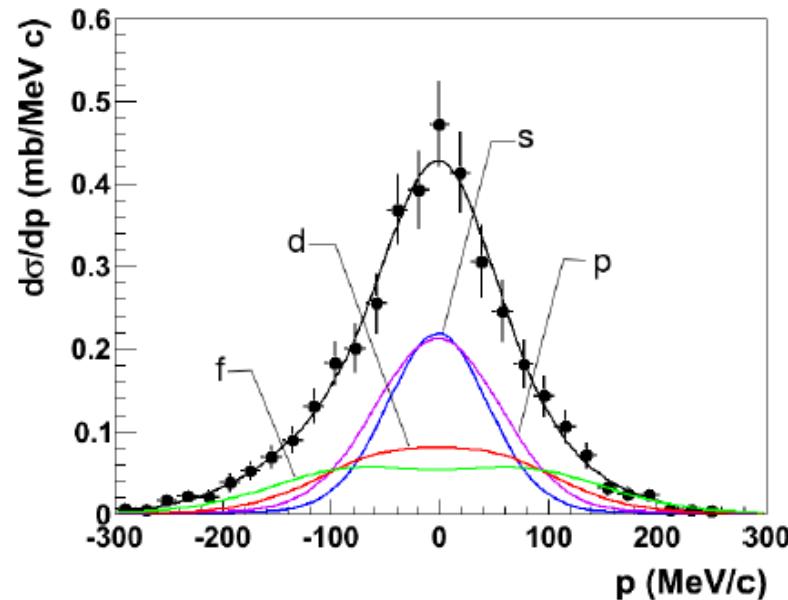
^{34}Al
C. Nociforo - "DREB12"

V. Tripathi *et al.*, PRL 101 (2008) 142504

$[35\text{Al} \rightarrow n + ^{34}\text{Al} \text{ at } 916 \text{ MeV/u}]$

$^{35}\text{Al}_{\text{g.s.}}(5/2^+)$

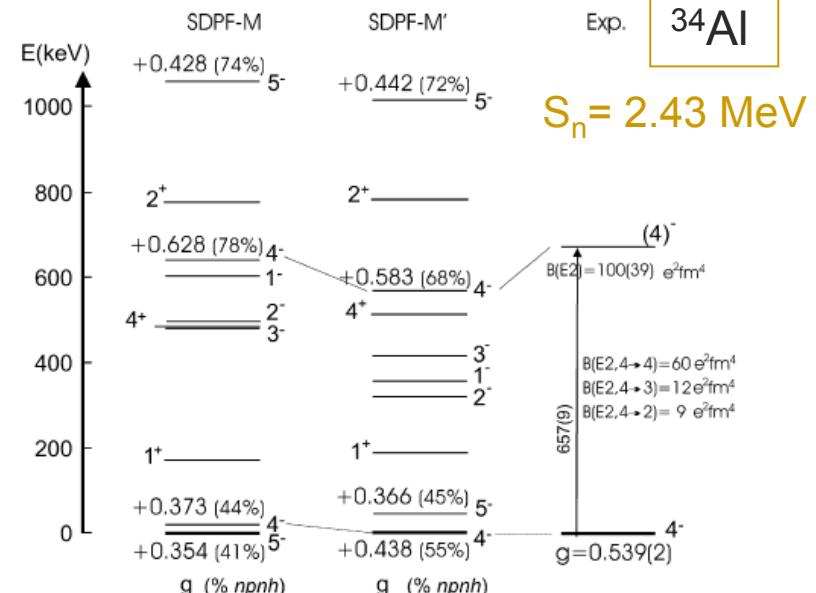
$$\sigma_{-1n} = 75 \pm 4 \text{ mb}, \Gamma_{\text{FWHM}} = 145 \pm 3 \text{ MeV/c}$$



--- fit $S(l=0) = 0.89^{+0.58}_{-0.89}$ $S(l=1) = 0.63^{+0.14}_{-0.28}$ $S(l=2) = 0.59^{+1.15}_{-0.59}$ $S(l=3) = 1.06^{+0.31}_{-0.39}$
--

$\text{----- } S_n 5.27$ $\textcircled{o} f_{7/2}$ $\textcircled{o} p_{3/2}$ $N = 20$
--

C. Nociforo - "DREB12"

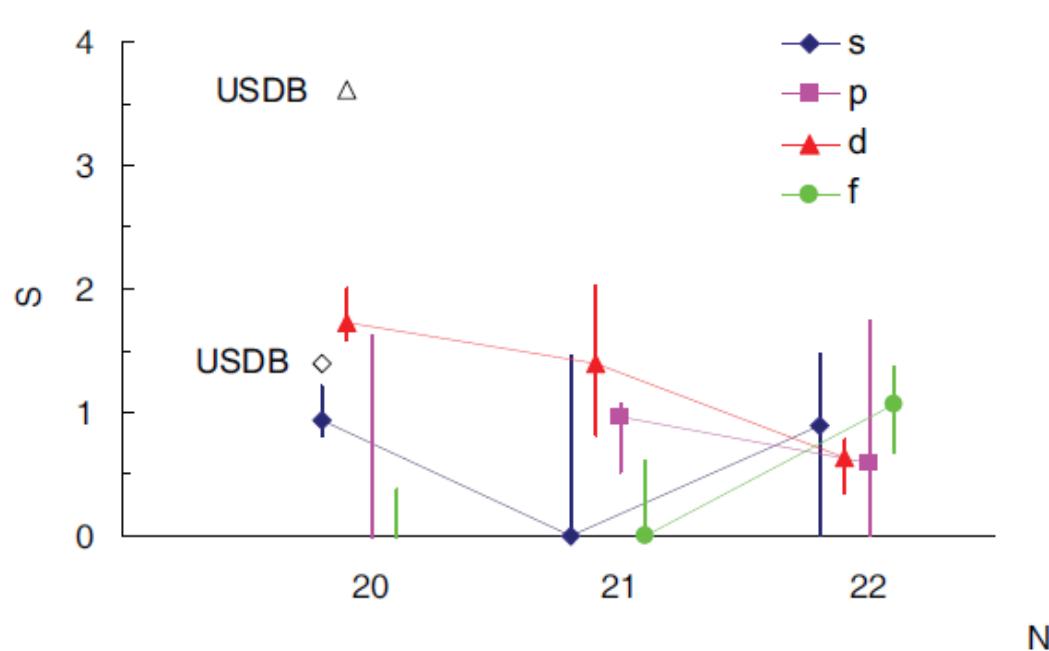


P. Himpe *et al.*, PLB 658 (2008) 203

2p_{3/2} and 1f_{7/2}
equally populated

Mixing in $^{33-35}\text{Al}$ g.s.

Evolution of single particle neutron occupancy



^{33}Al ^{34}Al ^{35}Al
Increasing p/f occupancy

Summary

The evolution of the single particle occupancy in the $^{33,34,35}\text{Al}_{\text{g.s.}}$ studied through precise measurements of p_{\parallel} and σ_{-1n} performed at relativistic energies ($\approx 900\text{MeV/u}$) and compared with shell model predictions

- p_{\parallel} does not exclude the presence of intruder states in ^{33}Al ($N=20$)
the inferred $2s_{1/2}$ neutron occupancy is 20-40% less than USDB predicted one
- 20-60% intruder $f=1$ occupancy found in ^{34}Al ($N=21$), in agreement with g factor measurement
lowering of the $2p_{3/2}$ level , similar to ^{33}Mg
- $1f_{7/2}$ occupancy increases adding neutrons, and correspondingly $1d_{3/2}$ one decreases.

List of collaborators

T. Aumann¹, D. Boutin², B. A. Brown⁴, D. Cortina-Gil⁵, B. Davids⁶, M. Diakaki⁷, F. Farinon^{1,2}, H. Geissel¹, R. Gernhäuser⁸, R. Janik⁹, B. Jonson¹⁰, R. Kanungo³, B. Kindler¹, R. Knöbel^{1,2}, R. Krücken⁸, N. Kurz, M. Lantz¹⁰, H. Lenske², Yu.A. Litvinov¹, K. Mahata¹, P. Maeirbeck⁸, A. Musumarra^{11,12}, T. Nilsson¹⁰, T. Otsuka¹³, C. Perro³, A. Prochazka^{1,2}, C. Scheidenberger^{1,2}, B. Sitar⁹, P. Strmen⁹, B. Sun², I. Szarka⁹, I. Tanihata¹⁴, H. Weick¹, M. Winkler¹

¹*GSI Helmholtzzentrum für Schwerionenforschung, Darmstadt, Germany*

²*Justus-Liebig University, Gießen, Germany*

³*Astronomy and Physics Department, Saint Mary's University, Halifax, Canada*

⁴*NSCL, Michigan State University, East Lansing, USA*

⁵*Universidad de Santiago de Compostela, Santiago de Compostela, Spain*

⁶*TRIUMF, Vancouver, Canada*

⁷*National Technical University, Athens, Greece*

⁸*Physik Department E12, Technische Universität München, Garching, Germany*

⁹*Faculty of Mathematics and Physics, Comenius University, Bratislava, Slovakia*

¹⁰*Fundamental Physics, Chalmers University of Technology, Göteborg, Sweden*

¹¹*Università di Catania, Catania, Italy*

¹²*INFN-Laboratori Nazionali del Sud, Catania, Italy*

¹³*Center for Nuclear Study, University of Tokyo, Saitama, Japan*

¹⁴*Research Center for Nuclear Physics, Osaka, Japan*