

**BSM effects in B physics:
Where do we stand?**

Diego Guadagnoli
CNRS, LAPTh Annecy

This talk assignment before Dec. 20, 2022



D. Guadagnoli, La Thuile, 5-11 March, 2023

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Before any anomaly

Why new physics in B decays

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- $b \rightarrow s$ transitions are the FCNCs closest to 3rd gen. physics

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[Isidori-Nir-Perez, 1002.0900]

Operator	Bounds on Λ in TeV ($c_{ij} = 1$)		Bounds on c_{ij} ($\Lambda = 1$ TeV)		Observables
	Re	Im	Re	Im	
$(\bar{s}_L \gamma^\mu d_L)^2$	9.8×10^2	1.6×10^4	9.0×10^{-7}	3.4×10^{-9}	$\Delta m_K; \epsilon_K$
$(\bar{s}_R d_L)(\bar{s}_L d_R)$	1.8×10^4	3.2×10^5	6.9×10^{-9}	2.6×10^{-11}	$\Delta m_K; \epsilon_K$
$(\bar{c}_L \gamma^\mu u_L)^2$	1.2×10^3	2.9×10^3	5.6×10^{-7}	1.0×10^{-7}	$\Delta m_D; q/p , \phi_D$
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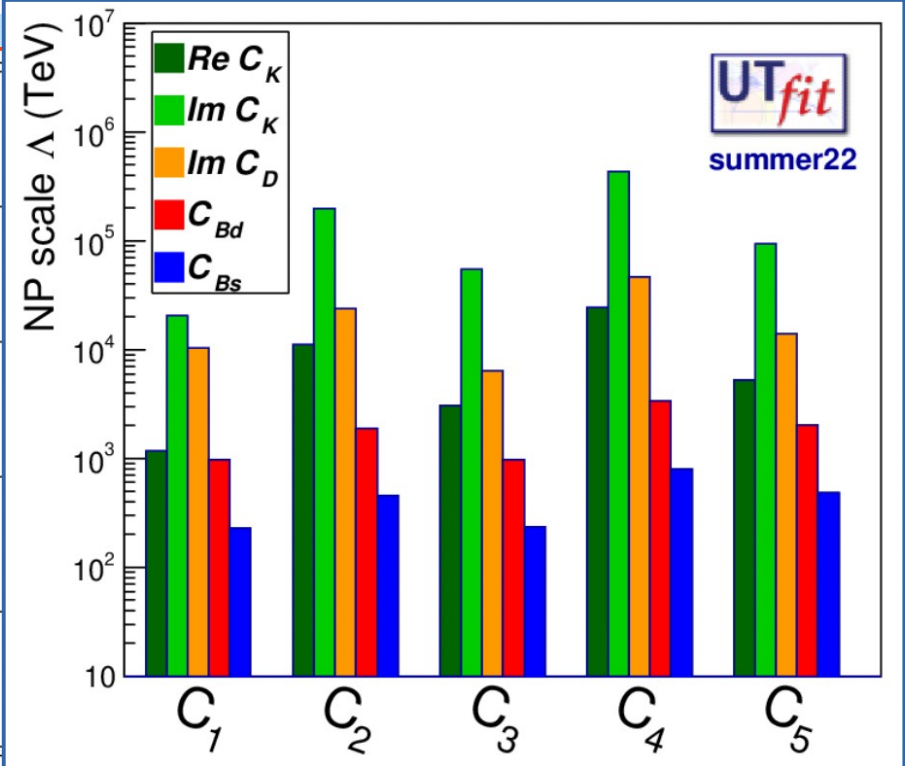
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- And if flavour is after all not just a puzzle, then flavour observables are all the more important **[Davighi-Isidori, 2303.two-days-ago]**

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- And if flavour is after all not just a puzzle, then flavour observables are all the more important [Davighi-Isidori, 2303.two-days-ago]
- In either case, if focus is on the highest scales attainable, flavour observables remain among the deepest probes

Anomalies (?)

NP before Dec. 20

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 - an exact symmetry of the SM gauge sector
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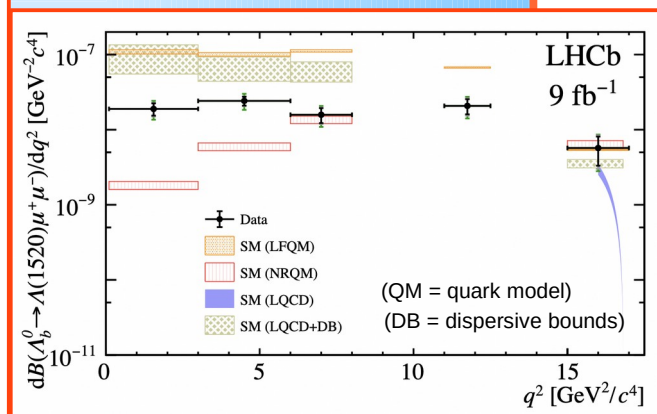
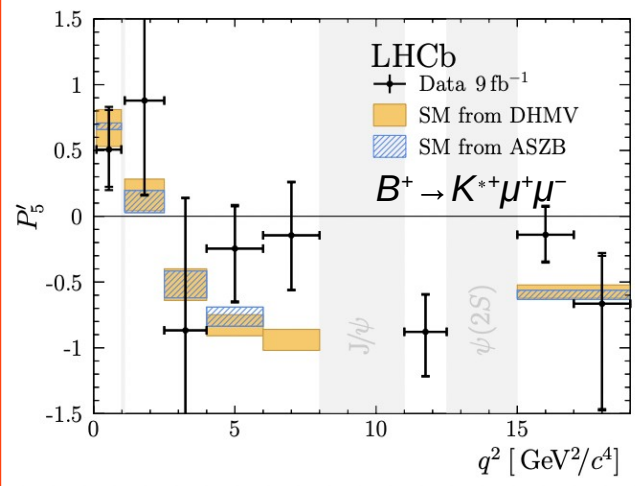
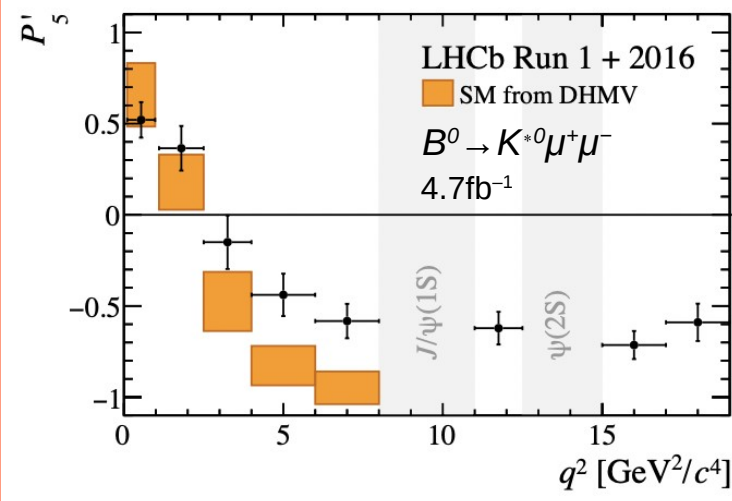
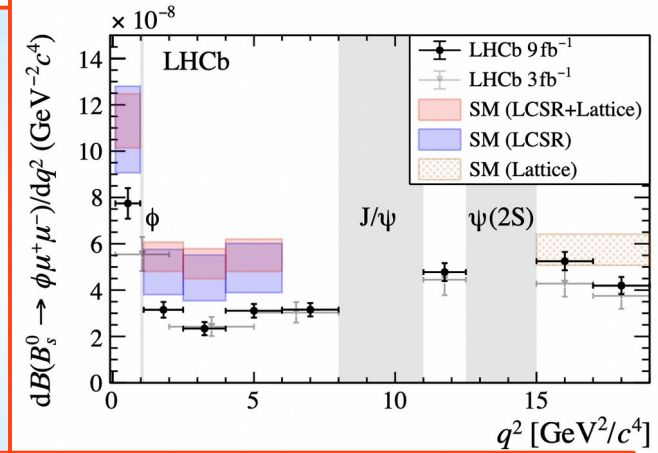
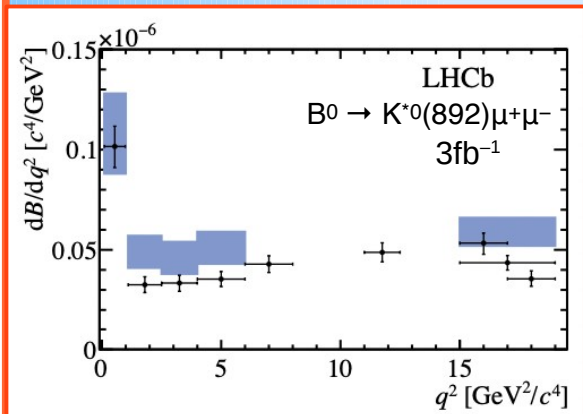
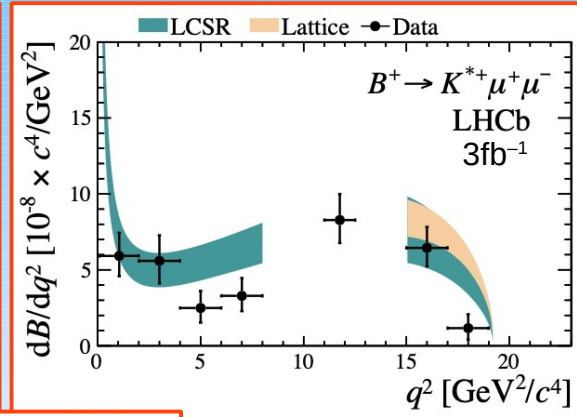
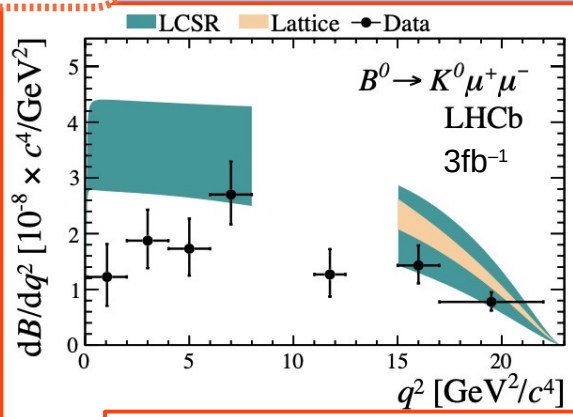
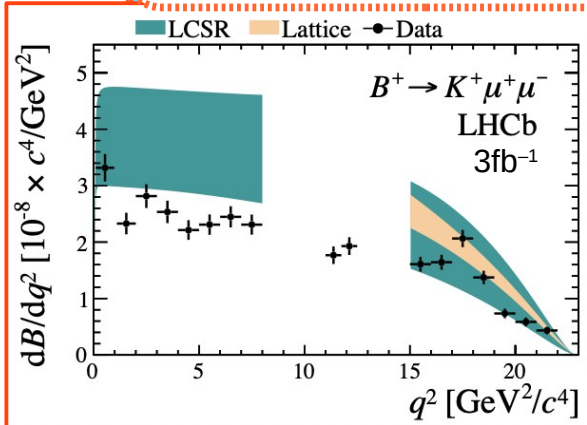
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- The NP hinted at by this “seed” was somewhat unexpected, a gross violation of:
 - an exact symmetry of the SM gauge sector
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- But it was supported by a number of (less TH-clean) measurements
 - that in isolation displayed only mild disagreements
 - but in aggregate suggested a coherent picture

NP after Dec. 20

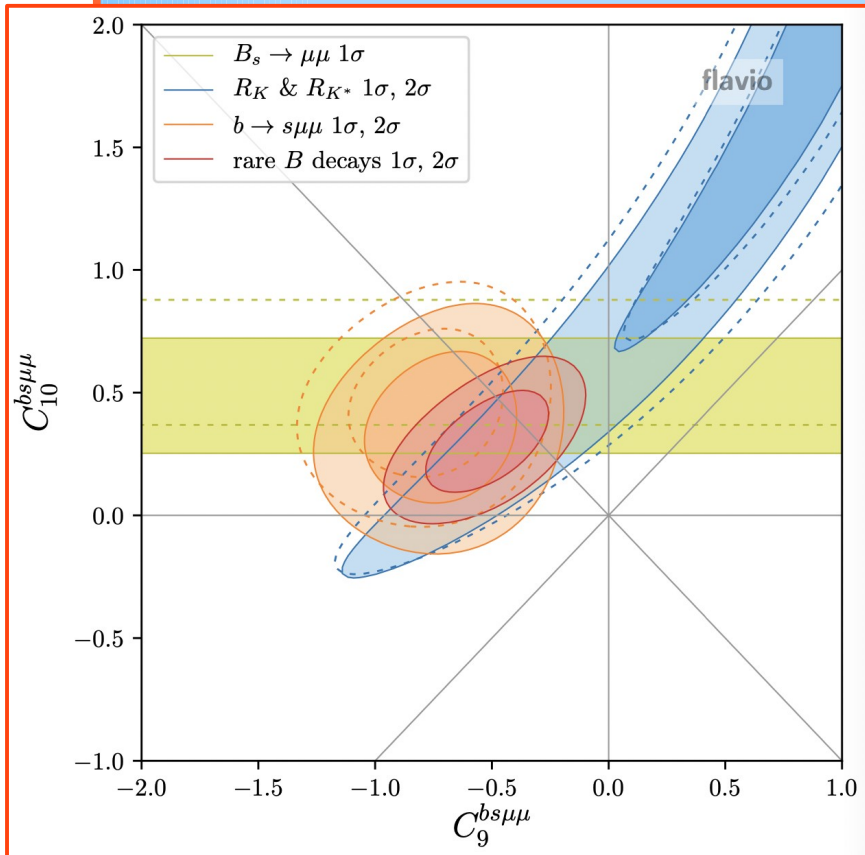
- The more (TH-)solid NP hints have disappeared – overnight.
- The remaining discrepancies (in $b \rightarrow s$ BRs and angular obs. & in $RD^{(*)}$) are debatable

$b \rightarrow s$ discrepant data



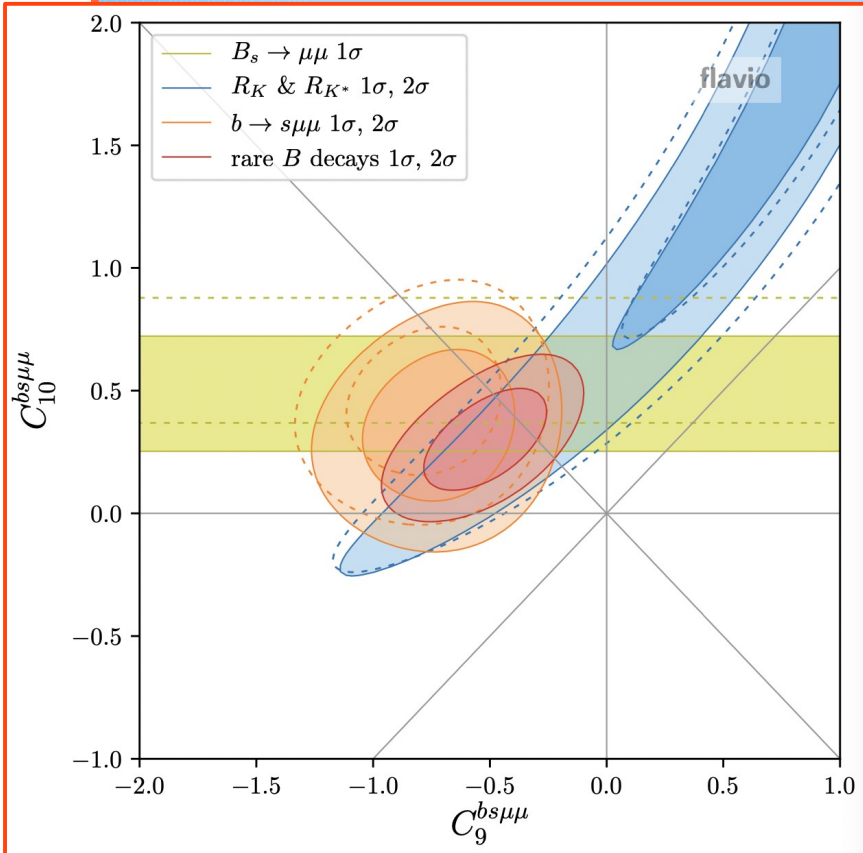
WET bounds

[Altmannshofer, Stangl, 2103.13370]

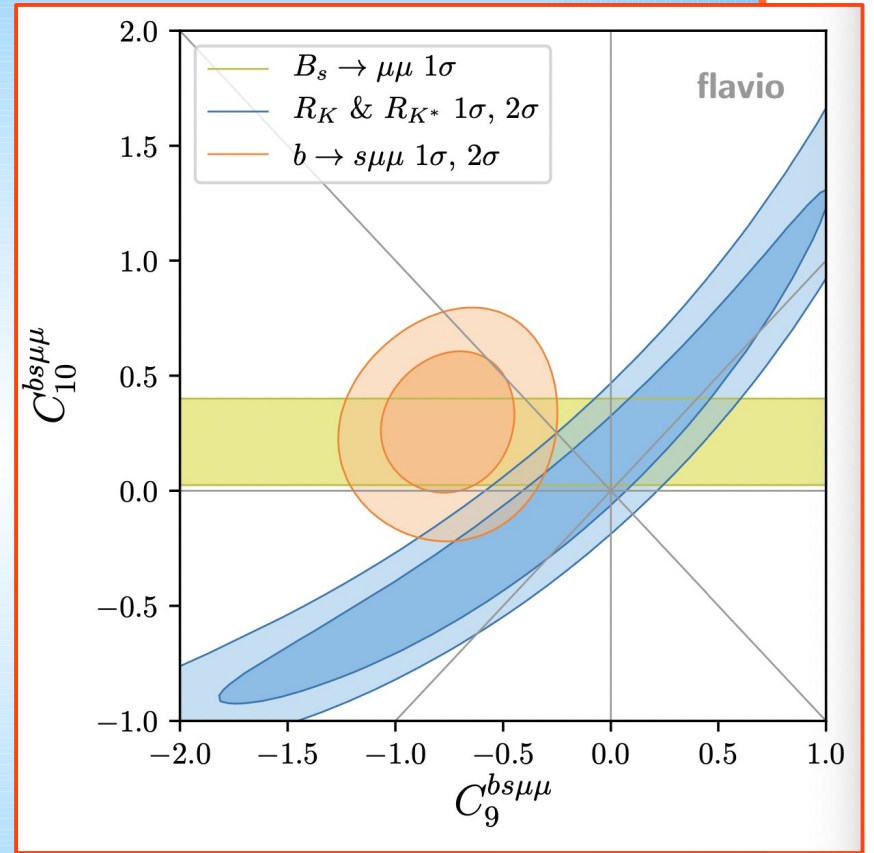


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[Greljo et al., 2212.10497]



Tension between LFU ratios (blue) and $b \rightarrow s \mu^+ \mu^-$ data (orange)

WET bounds

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Tension solvable with LFU NP, in either the C_9 or the $C_9 = -C_{10}$ direction

$$C_9^{bsee} = C_9^{\text{univ.}}$$

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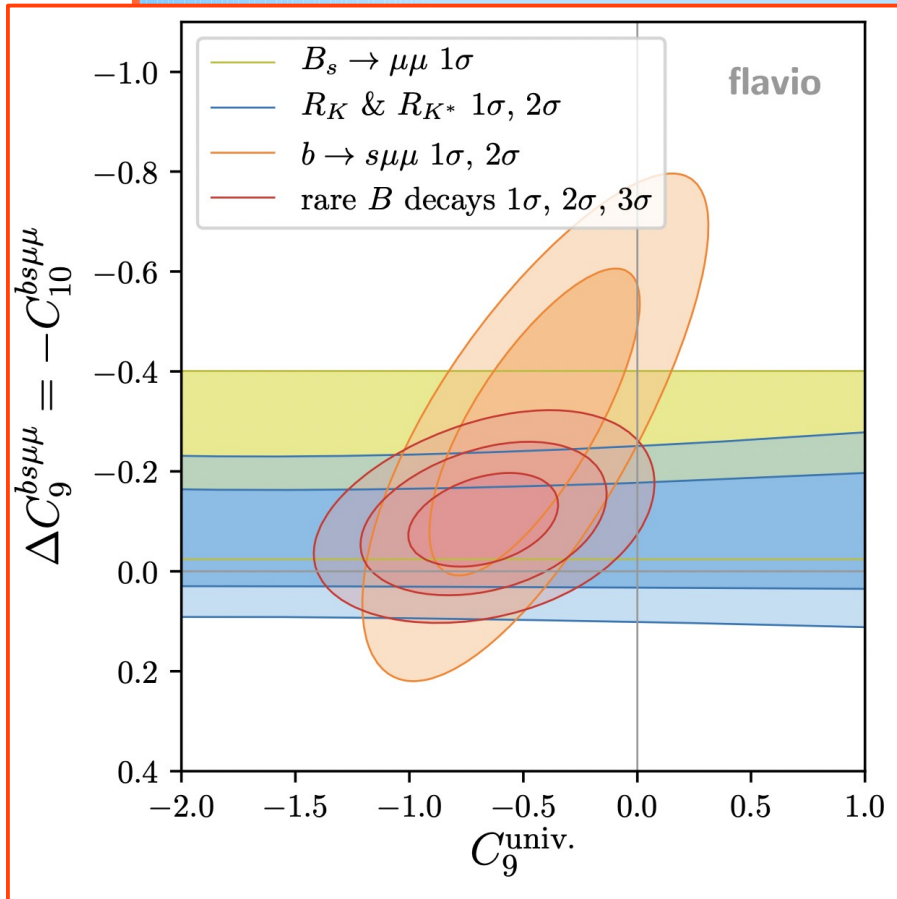
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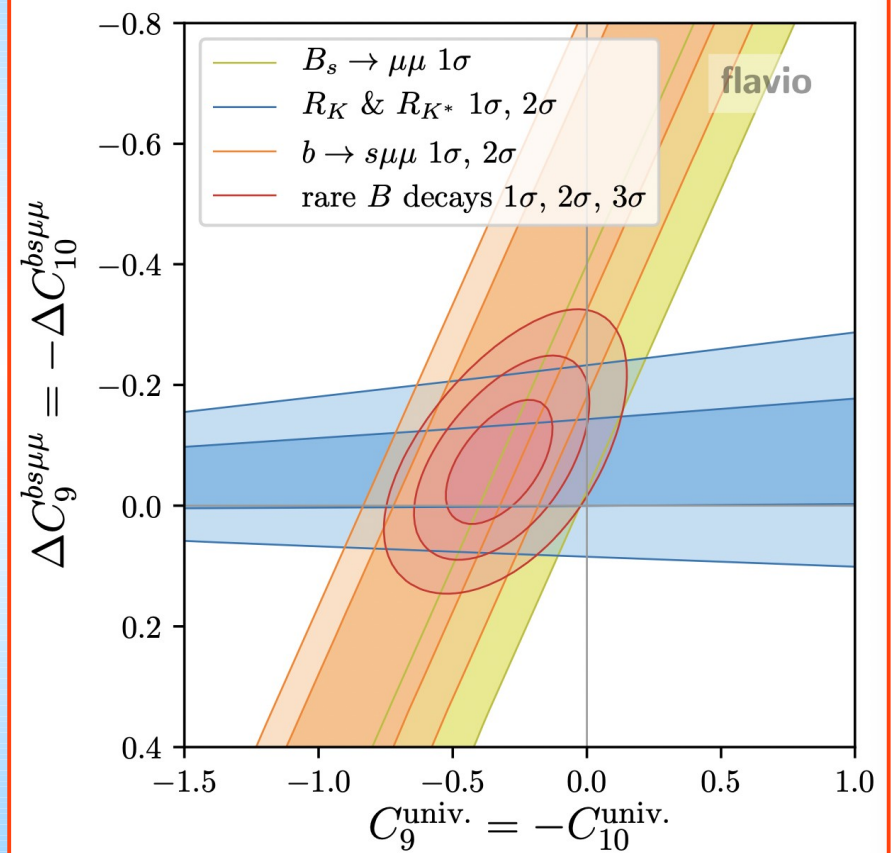
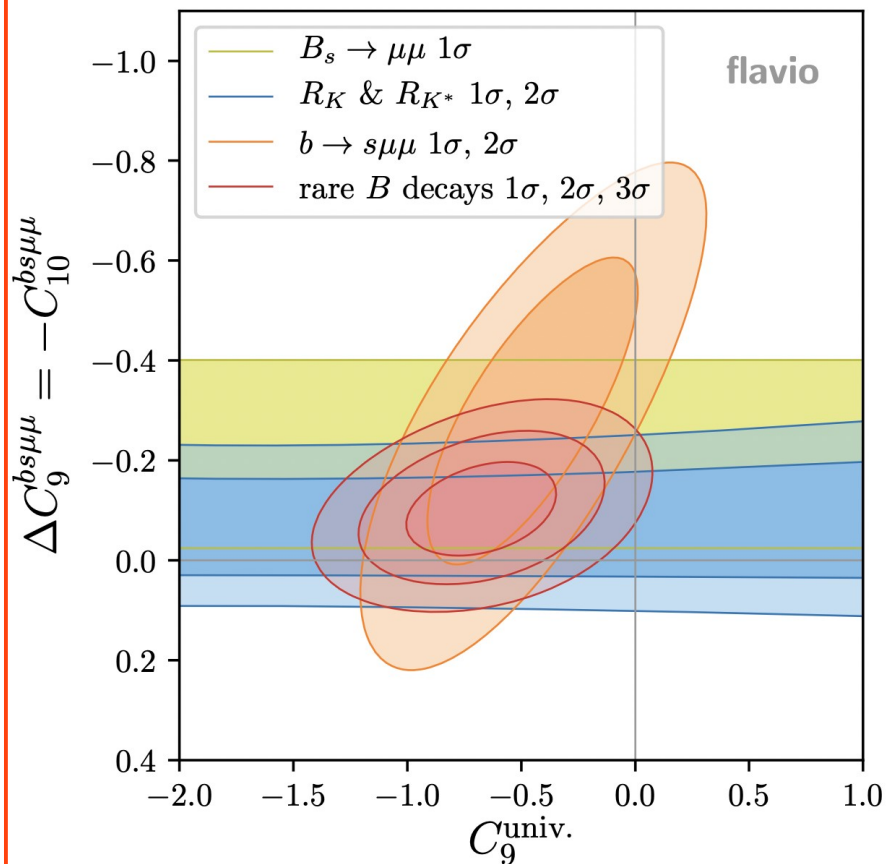
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- Purely muonic shift consistent with 0
- Univ. contrib. $O(13\%)$ for C_9 -only, or half as much for C_L

Connection with $b \rightarrow c$?

- $C_9^{\text{univ.}}$ of the correct size can be generated through RGE effects
[Bobeth-Haisch, 2011] [Crivellin *et al.*, 2018] [Aebischer *et al.*, 2019]

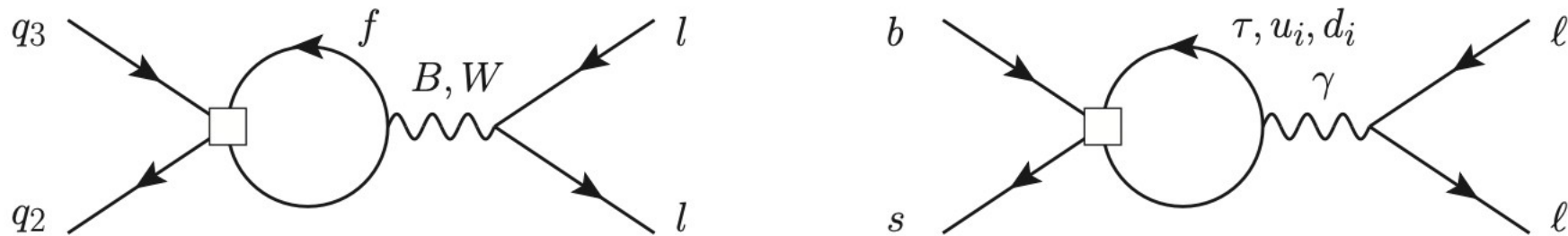


Figure 3: Diagrams inducing a contribution to C_9 through RG running above (left panel) and below (right panel) the EW scale. A sizeable contribution to C_9 is obtained when $f = u_{1,2}, d_{1,2,3}$ or l_3 , see text for details.

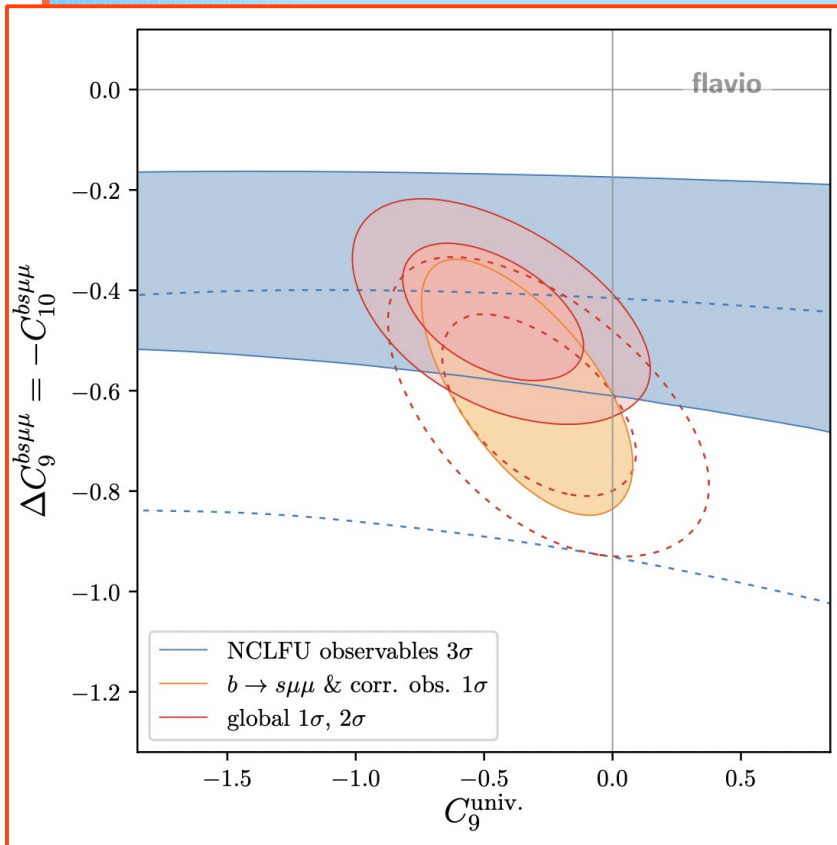
Connection with $b \rightarrow c$ after Dec. 20?

Exercise not yet done quantitatively AFAIK. But it will probably work:

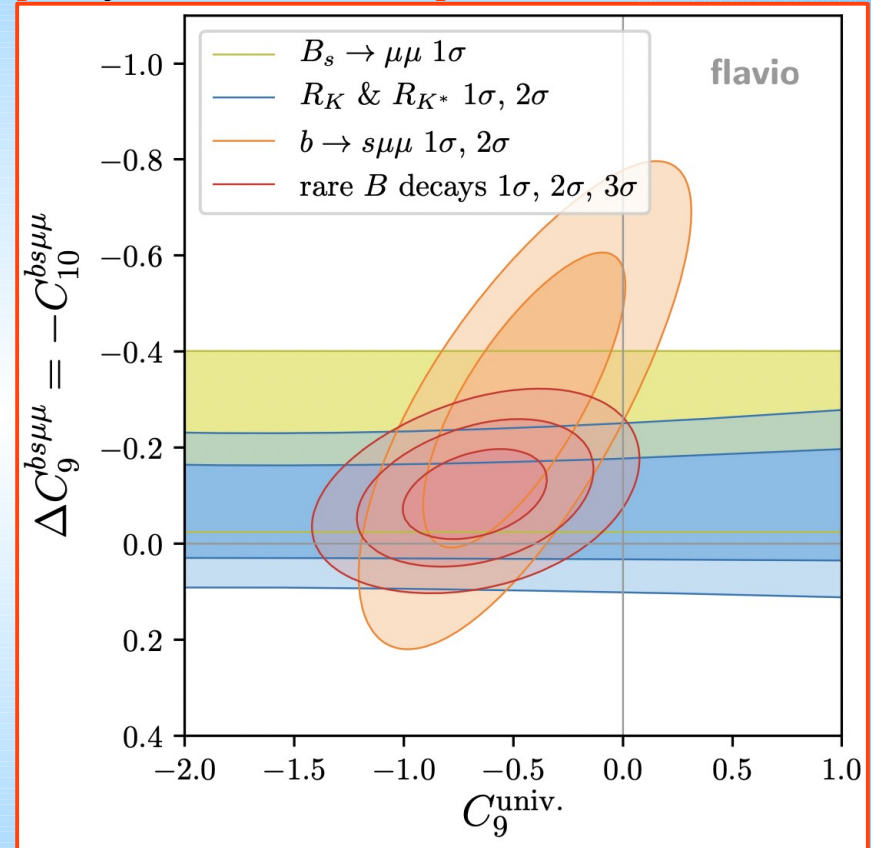
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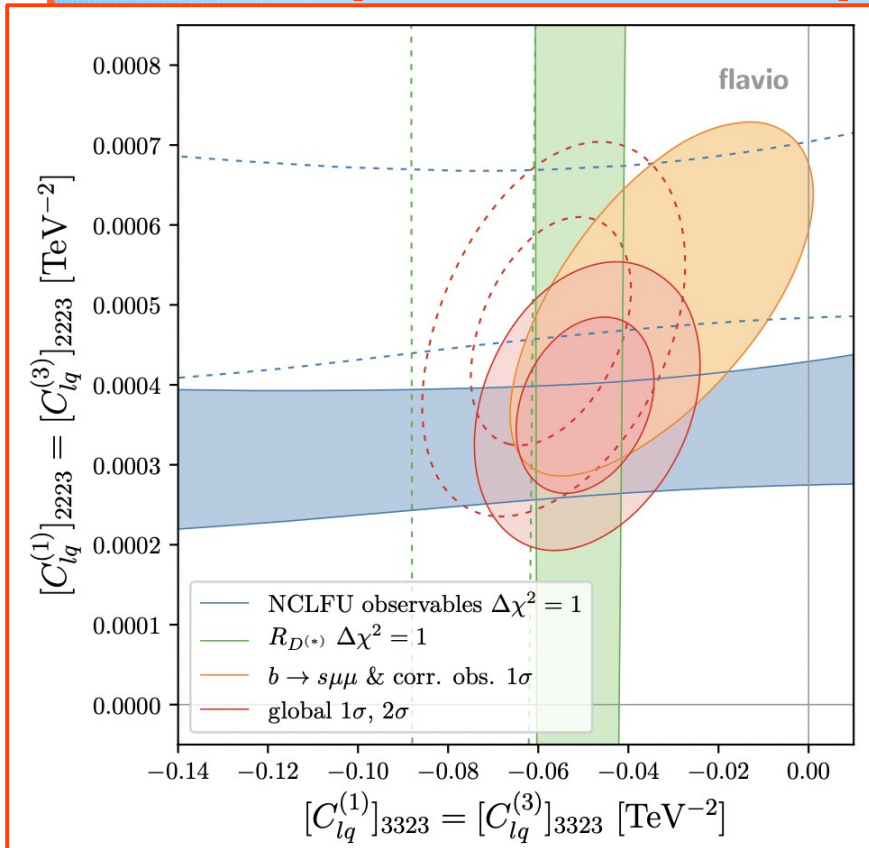


- $C_9^{univ.}$ has slightly increased in central value from pre- to post-Dec. 20

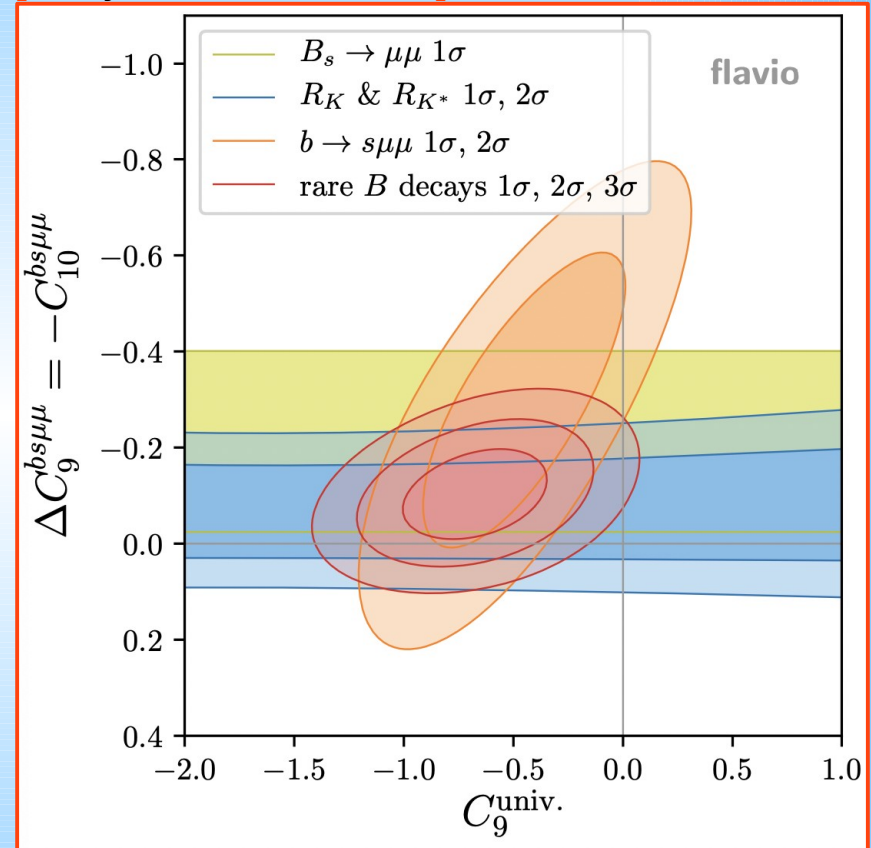
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- But $RD^{(*)}$ prefers the part of the yellow ellipse closer to zero (in the y-axis direction)

Connection with $b \rightarrow c$?

Beware: properly using LQCD + unitarity, $R(D^{(*)})$ significance $\sim 1.4\sigma$
[Martinelli, Simula, Vittorio, 2021]

Models

[Greljo et al., 2212.10497]

Post-Dec. 20 exercise:

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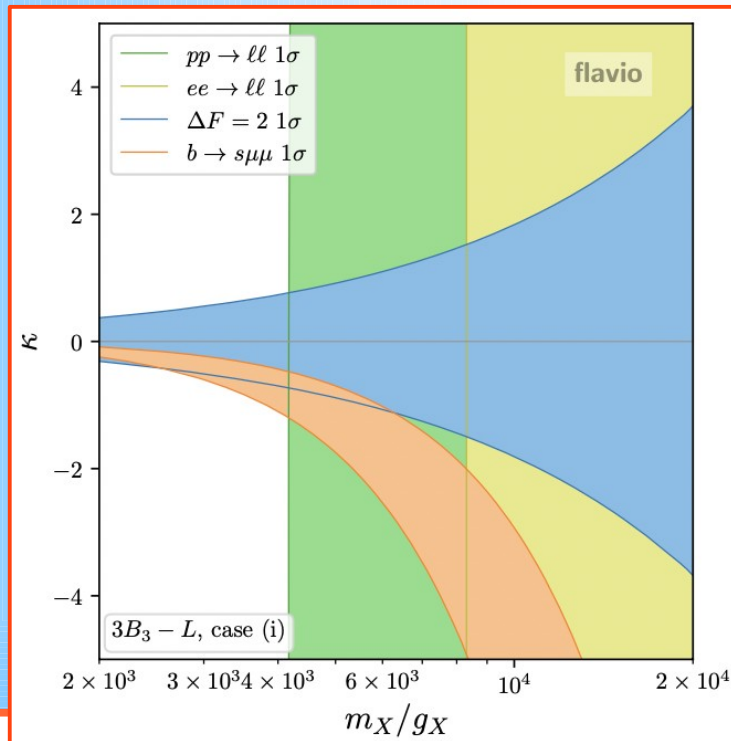
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Gauged U(1)'s

- B – L direction + quark-flavour violation through VL heavy quarks
➡ challenged by $\Delta F = 2$ & $pp, ee \rightarrow \ell\ell$
- 3rd-(quark)-gen-philic variant: $3 B_3 - L$



➡ $pp \rightarrow \ell\ell$ gets less stringent,
but tension w/ $ee \rightarrow \ell\ell$ persists

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Scalar LQs

- Three “leptonic flavours” of $S \sim (\bar{\mathbf{3}}, \mathbf{3}, 1/3)$

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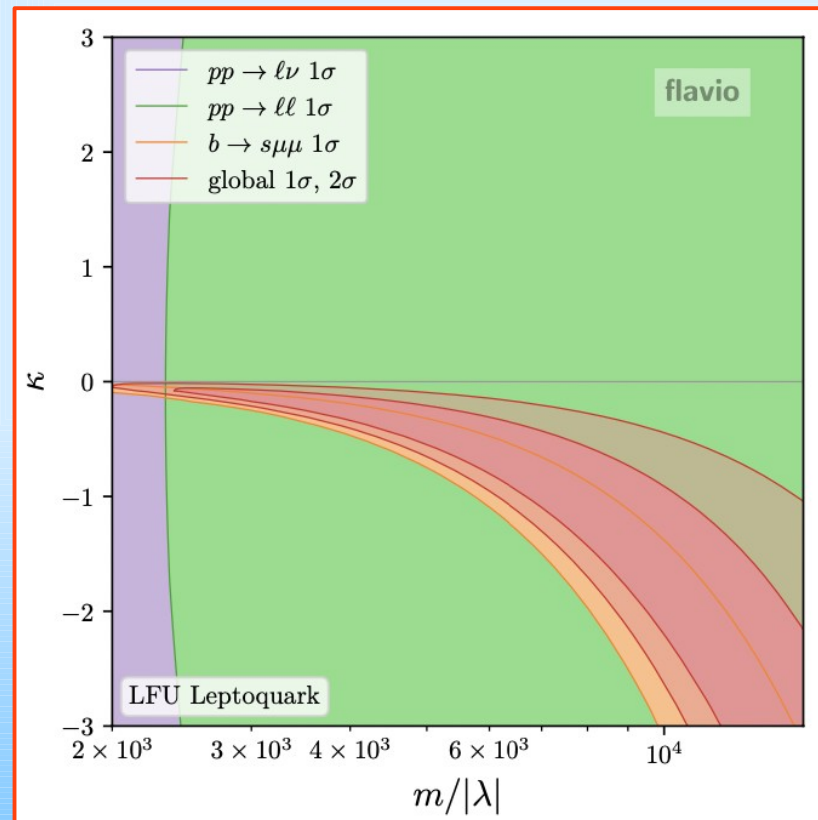
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Semilep at tree level, but $\Delta F = 2$ & $ee \rightarrow \ell\ell$ only at loop level



**Conclusive
remarks**

NP after Dec. 20

Main points

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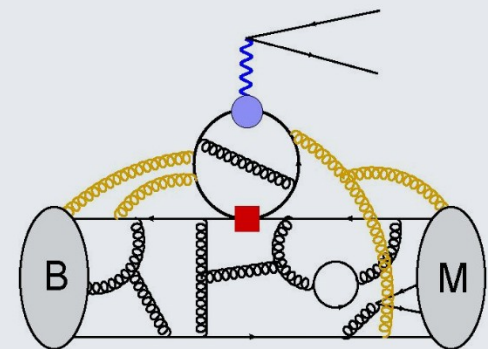
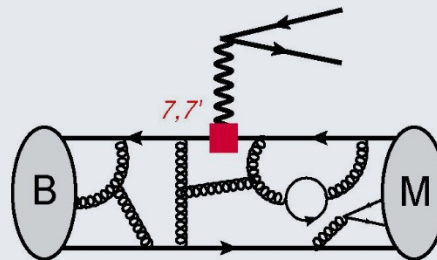
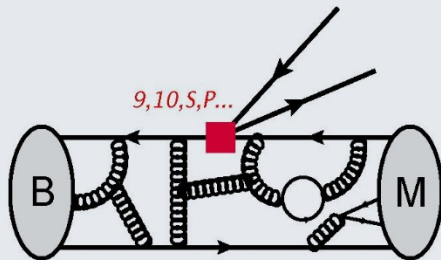
- ① The TH-cleaner bits (LUV observables; $B_s \rightarrow \mu^+\mu^-$) are gone
- ② Remaining hints suggest:
 - C_9^{NP} (or C_L^{NP}) at low q^2 , but not at high q^2 ?
 - C_9^{NP} (or C_L^{NP}) in di-muons, and also in di-electrons?

While waiting for updates of discrepant measurements, progress relies on a solid understanding of “non-local FFs” in $b \rightarrow s \ell^+\ell^-$ (because of ①)

Per aspera (= long-distance contributions) ad astra

Form factors in $b \rightarrow s\ell\ell$

$$\mathcal{H}(b \rightarrow s\ell\ell) = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_{i=1}^{10} C_i(\mu) \mathcal{O}_i(\mu)$$



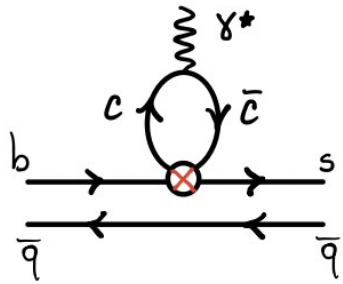
$$A_\lambda^{L,R}(B \rightarrow M_\lambda \ell\ell) = \mathcal{N}_\lambda \left\{ (C_9 \mp C_{10}) \mathcal{F}_\lambda(q^2) + \frac{2m_b M_B}{q^2} \left[C_7 \mathcal{F}_\lambda^T(q^2) - 16\pi^2 \frac{M_B}{m_b} \mathcal{H}_\lambda(q^2) \right] \right\}$$

$$\mathcal{H}_\mu(k, q) = i \int d^4x e^{iq \cdot x} \langle \bar{M}(k) | T \{ \mathcal{J}_\mu^{\text{em}}(x), C_i \mathcal{O}_i \} | \bar{B}(q+k) \rangle$$

Non-local form-factors

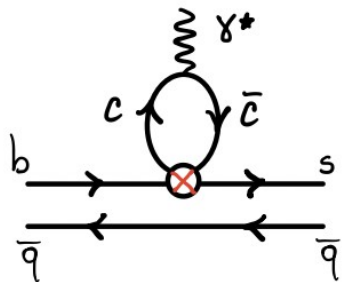
→ Main contributions: the “charm-loops” $\mathcal{O}_{2(1)}^c = (\bar{s}_L \gamma_\mu (T^a) c_L) (\bar{c}_L \gamma^\mu (T^a) b_L)$

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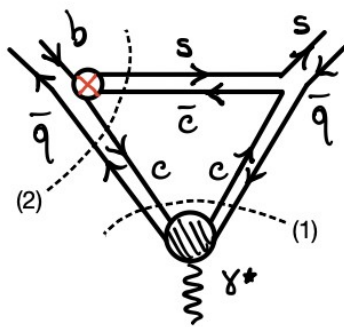


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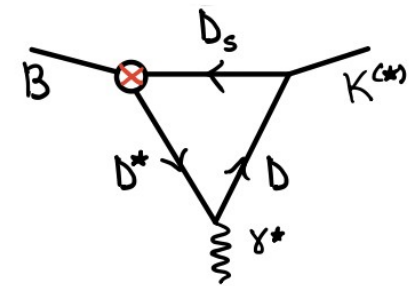
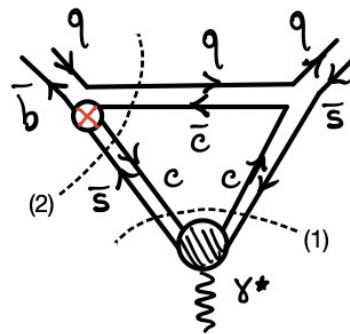
[Ciuchini et al., 2212.10516]



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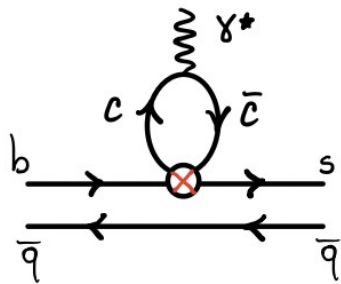
(b)



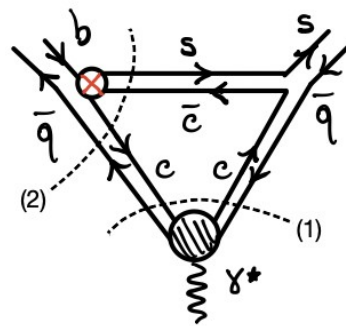
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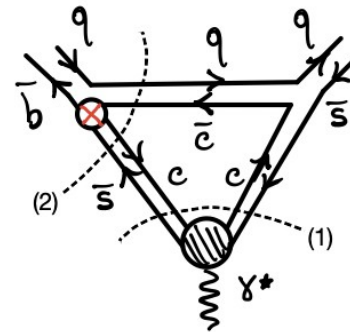
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(c)

What about contribs. (b)?

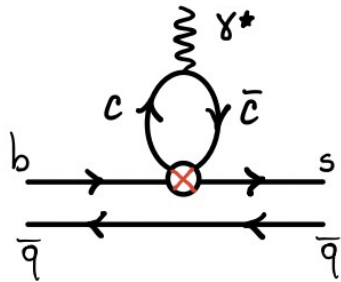
In principle, well-known to be there, e.g.

► On-shell cuts in the variable $(q+k)^2$ (the “forward” or “decay” channel) include branch cuts from intermediate states such as $B \rightarrow \bar{D}D_s \rightarrow K^*\ell^+\ell^-$. The physical point $(q+k)^2 = M_B^2$ lies on these cuts, which implies that the functions $\mathcal{H}_\lambda(q^2)$ are complex-valued for all values of q^2 . But this imaginary part is not associated with any singularity in the variable q^2 . Thus, one can write $\mathcal{H}_\lambda(q^2) = \mathcal{H}_\lambda^{(\text{re})}(q^2) + i\mathcal{H}_\lambda^{(\text{im})}(q^2)$, with $\mathcal{H}_\lambda^{(\text{re,im})}(q^2)$ satisfying the analytic properties of the previous point as functions of q^2 , and obeying the same dispersion relation.

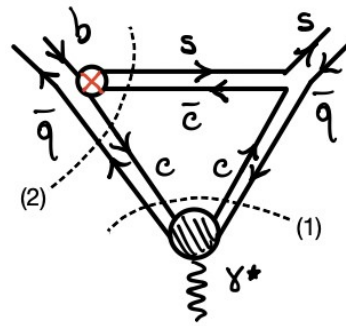
[Bobeth et al., 2017]

Per aspera (= long-distance contributions) ad astra

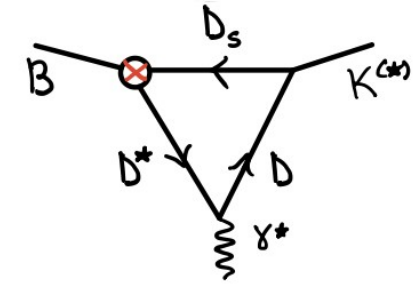
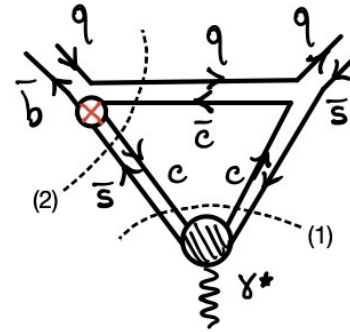
[Ciuchini et al., 2212.10516]



(a)



(b)



(c)

What about contribs. (b)?

In principle, well-known to be there, e.g.

► On-shell cuts in the variable $(q+k)^2$ (the “forward” or “decay” channel) include branch cuts from intermediate states such as $B \rightarrow \bar{D}D_s \rightarrow K^*\ell^+\ell^-$. The physical point $(q+k)^2 = M_B^2$ lies on these cuts, which implies that the functions $\mathcal{H}_\lambda(q^2)$ are complex-valued for all values of q^2 . But this imaginary part is not associated with any singularity in the variable q^2 . Thus, one can write $\mathcal{H}_\lambda(q^2) = \mathcal{H}_\lambda^{(\text{re})}(q^2) + i\mathcal{H}_\lambda^{(\text{im})}(q^2)$, with $\mathcal{H}_\lambda^{(\text{re,im})}(q^2)$ satisfying the analytic properties of the previous point as functions of q^2 , and obeying the same dispersion relation.

[Bobeth et al., 2017]

In practice, however...

to this kind of contributions, but the analytic structure of triangle diagrams is quite involved, depending on the values of external momenta and internal masses. A dispersion relation in q^2 of the kind used in refs. [43, 45–48], based on the cut denoted by (1) in Fig. 1 (b), could be written if the B invariant mass were below the threshold for the production of charmed intermediate states. However, when the B invariant mass raises above the threshold for cut (2), an additional singularity moves into the q^2 integration domain, requiring a nontrivial deformation of the path (see for example the detailed discussion in ref. [94]). Another possibility would be to get an

[Ciuchini et al., 2212.10516]