

and



# THE NEW MESONS: DIRECT & INDIRECT SEARCH

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Work done mainly with AD Polosa and F Piccinini

SuperB Meeting - Elba May 30, 2011



- Standard Charmonium/Bottomonium and Charmonium/Bottomonium-like resonances (XYZ mesons).
- Exotic mesons: molecules, tetraquarks, hybrids, hadrocharmonium.

## Direct searches.

- Indirect searches.
  - Inclusive production of J/ $\psi$  in B decays: state of the art and update.
    - Two body modes (color singlet).
    - Non resonant multi body modes (color octet) NRQCD.
    - Contribution from XYZ mesons.



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    - Two body modes (color singlet).
- SUPER FLAVOUR FACTORIES HIGHER STATISTICS IS NEEDED. Non resonant multi body modes (color octet) NRQCD.
  - Contribution from XYZ mesons.

## Predictions for cc<sup>\*</sup> states

:: Godfrey, Isgur, Phys. Rev. D 32, 189–231 (1985) ::













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# Data for bb<sup>\*</sup> states



## Unexpected

:: Belle, Phys.Rev.Lett. 100 (2008) 1120014 :: :: Belle, arXiv:1105.4583 ::



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# The road to $Z_{b}^{+}(10610) \& Z_{b}^{+}(10650)$ : $\Upsilon(5S)$

Belle, Phys. Rev. Lett. 100, 112001 (2008)

### Anomalous production of $\Upsilon(nS) \pi^+\pi^-$ (n=1,2,3) @ the $\Upsilon(5S)$ resonance (e<sup>+</sup>e<sup>-</sup> collisions at $\sqrt{s} \approx 10.87$ GeV).

TABLE II. The total width  $\Gamma_{\text{total}}$ , and the partial width  $\Gamma_{e^+e^-}$ ,  $\Gamma_{\Upsilon(1S)\pi^+\pi^-}$ . Most values are from Refs. [3,4,11].

Process	$\Gamma_{ m total}$	$\Gamma_{e^+e^-}$	$\Gamma_{\Upsilon(1S)\pi^+\pi^-}$
$\Upsilon(2S) \rightarrow \Upsilon(1S) \pi^+ \pi^-$	0.032 MeV	0.612 keV	0.0060 MeV
$\Upsilon(3S) \rightarrow \Upsilon(1S)\pi^+\pi^-$	0.020 MeV	0.443 keV	0.0009 MeV
$\Upsilon(4S) \rightarrow \Upsilon(1S)\pi^+\pi^-$	20.5 MeV	0.272 keV	<u>0.0019 MeV</u>
$\Upsilon(10860) \to \Upsilon(1S)\pi^+\pi^-$	110 MeV	0.31 keV	0.59 MeV



 $\gg$  Exotic - tetraquark state Y<sub>b</sub> = [cq][c\*q\*] A.Ali, C. Hambrock, and M.Aslam, Phys.Rev.Lett. 104, 162001 (2010)

Standard - rescattering  $\Upsilon(5S) \rightarrow BB\pi\pi \rightarrow \Upsilon(nS)\pi\pi$ Simonov JETP Lett 87,147(2008)

# The road to $Z_{b}^{+}(10610) \& Z_{b}^{+}(10650)$ : h<sub>c</sub>

R. E. Mitchell (2011), 1102.3424.

Similar in all respects to the Y(4260) resonance in the charm sector.

The (S=0, L=1) charmonium state  $h_c$  has been discovered by CLEO-c in a scan around  $\sqrt{s} \approx 4.26$  GeV.



This is the motivation for the Belle search of  $h_b$  at the  $\Upsilon(5S)$  peak.

# The road to $Z_{b}^{+}(10610) \& Z_{b}^{+}(10650)$ : h<sub>b</sub>

Belle, arXiv:1103.3419





 $M(\pi^{+}\pi^{-})$ , (GeV/c<sup>2</sup>)

 $M(\Upsilon(3S)\pi)_{\min}$ , (GeV/c<sup>2</sup>)

 $M(\Upsilon(3S)\pi)_{max}$ , (GeV/c<sup>2</sup>)

# $Z_{b}^{+}(10610) \& Z_{b}^{+}(10650)$

[From A. Bondar FPCP2011]



# Are they exotic hadrons?

- - Many exotic candidates have been identified among the so-called XYZ particles.
- Exotic means non qq<sup>\*</sup> or qqq structures ... what else?
  - Strongly interacting clusters of hadrons: molecules [Voloshin; Tornqvist; Close; Braaten; Swanson...]



- Tetraquark mesons, Pentaquarks, ... [Maiani,Piccinini,Polosa,Riquer ...]
- Hybrids [Close, Kou&Pene, ...]
- Hadrocharmonium [Voloshin]







Bound states of mesons or baryons.

We will focus on meson-meson molecules. Main features:

- short range interactions between mesons  $\rightarrow$  L=0 states
- > typical binding energy 50 MeV for light mesons resonances, 10 MeV for heavy mesons resonances ( $R \sim I$  fm and  $E=I/(2\mu R^2)$ )

large branching fractions to final states containing the constituent mesons

How do we model the interaction?

Long distance



Short distance



gluon exchange



Tetraquark: a diquark-antidiquark bound state

#### Diquark: bound state of two quarks

 $\Rightarrow$  not neutral in color, needs to be bound to an antidiquark

$$\begin{bmatrix} [qq'] \in 3_C \otimes 3_C = \bar{3}_C \oplus 6_C \\ [\bar{q}\bar{q}'] \in \bar{3}_C \otimes \bar{3}_C = 3_C \oplus 6_C \end{bmatrix}$$

$$3_C \otimes \bar{3}_C = 1_C \oplus 8_C$$

Tetraquarks can be classified with:

 $\gg$  **S** total spin of the diquark-antidiquark system S=S<sub>1</sub> $\oplus$ S<sub>2</sub>=(0,1) $\oplus$ (0,1) = 0,1,2

L orbital excitation between the diquark and the antidiquark

$$\mathbf{J} = \mathbf{L} \oplus \mathbf{S}, \ \mathbf{P} = (-1)^{\mathbf{L}}, \ \mathbf{C} = (-1)^{\mathbf{L}+\mathbf{S}}$$

# OutlineSpectrumExoticsDirect SearchesINdirect Searches: $B \rightarrow J/\psi + AII$ Diquarks

Why a diquark should be bound? One Gluon Exchange:

$$Q_C \propto \sum_{a} T_A^a T_B^a = \frac{1}{2} \sum_{a} \left( T_{A \otimes B}^{a2} - T_A^{a2} - T_B^{a2} \right) \implies Q_c \propto \frac{1}{2} \left( C(A \otimes B) - C(A) - C(B) \right)$$
$$\frac{\overline{R} \quad 1_c \quad \overline{3}_c \quad 6_c \quad 8_c}{C(R) \quad 0 \quad 4/3 \quad 10/3 \quad 3}$$

Ordinary Meson



$$A = 3_c, \quad B = \bar{3}_c$$
$$A \otimes B = 1_c \Rightarrow Q_c \propto -4/3$$









> One can obtain a color singlet combining  $\overline{q} q g$ 



- In a constituent gluons model the gluon has a fixed orbital angular momentum with respect to the qq<sup>\*</sup> pair. The hybrid state is characterized by  $l_g \quad l_{q\bar{q}} \quad s_{q\bar{q}}$
- In a flux tube model instead one can describe the decay of an hybrid meson



#### Spectrum

Exotics

# Hadrocharmonium (I)



Slides by Mikhail Voloshin - QWG 2010

https://indico.fnal.gov/getFile.py/access?contribId=51&sessionId=16&resId=0&materialId=slides&confld=3347

Y(4.26), Y(4.32 - 4.36), Y(4.66)

• Y(4260): Confirmed by Belle, CLEO, CLEO-c. Also seen in  $B \to \pi^+ \pi^- J/\psi K$ .  $Y(4260) \rightarrow \pi^+\pi^- J/\psi$ :  $M = 4264^{+10}_{-12} \text{ MeV}, \Gamma = 83^{+20}_{-17} \text{ MeV}$ Other decay modes seen:  $\pi^0 \pi^0 J/\psi$ ,  $K^+ K^- J/\psi$ .  $\frac{\Gamma(Y \to K^+ K^- J/\psi)}{\Gamma(Y \to \pi^+ \pi^- J/\psi)} \approx 0.15$ No decays with  $D\overline{D}$  in the final state were seen. In particular:  $\frac{\Gamma(Y \to D\bar{D})}{\Gamma(Y \to \pi^+ \pi^- J/\psi)} \lesssim 1.0, \qquad \frac{\Gamma(Y \to D\bar{D} + pions)}{\Gamma(Y \to \pi^+ \pi^- J/\psi)} \lesssim 1.0$ Impossible to explain if Y(4260) is a pure charmonium state! Compare e.g. with  $\Gamma(\psi(3770) \rightarrow D\bar{D})/\Gamma(\psi(3770) \rightarrow \pi^+\pi^- J/\psi) \approx 400$ • Y(4.32 - 4.36): "Broad structure" in (ISR)  $e^+e^- \rightarrow \pi^+\pi^-\psi'$  (not  $J/\psi!$ ) BaBar:  $M = 4324 \pm 24 \text{ MeV}, \Gamma = 172 \pm 33 \text{ MeV}$  Belle:  $M = 4361 \pm 9 \pm 9 \text{ MeV},$  $\Gamma = 74 \pm 15 \pm 10 \,\mathrm{MeV}$  and additionally: • Y(4.66)Peak in  $\pi^+\pi^-\psi'$  at  $M = 4664 \pm 11 \pm 5$  MeV,  $\Gamma = 48 \pm 15 \pm 3$  MeV.

# Hadrocharmonium (2)

Slides by Mikhail Voloshin - QWG 2010

https://indico.fnal.gov/getFile.py/access?contribId=51&sessionId=16&resId=0&materialId=slides&confld=3347

• If you ask me...

To me Y(4260), Y(4.32 - 4.36), Y(4.66), Z(4430) all look like 'a charmonium stuck in a light hadron'. At least this can explain why dominantly a specific charmonium state e.g.  $J/\psi$  or  $\psi'$  appears in the decay. Here's what I mean:

Van der Waals interaction of charmonium with light hadronic matter



Chromo-polarizability:  $\alpha_{AB}$ . Chromo-electric field  $\vec{E}^a$ .  $|\alpha_{\psi'J/\psi}| \approx 2 \, GeV^{-3}$  is known from  $\psi' \to \pi \pi \, J/\psi$ . Schwartz inequality:  $\alpha_{J/\psi} \alpha_{\psi'} \ge \alpha_{\psi'J/\psi}^2$ , so that either  $\alpha_{J/\psi}$  or  $\alpha_{\psi'}$  or both should be bigger than  $2 \, GeV^{-3}$ .

## Direct Searches

:: Drenska et al., Riv.Nuovo Cim. 033 (2010) 633-712 ::



Many final states have not been even searched for: one should: look in existing data from B-factories

B decays	JPC	J/ψππ	J/ψω	J/ψγ	J/ψφ	J/ψη	ψ(2S)ππ	ψ(2S)ω	ψ(2S)γ	χεγ	рр	лл	лслс	DD	DD*	D*D*	Ds(*)Ds(*)	γγ
X(3872)	1++ [2-																	
	+]	s	S*	S	N/A	N/S	N/A	N/A	S	N/S	M/F	M/F	N/A	N/A	s	N/A	N/A	N/S
X,Y (3940)	0-+	M/F	s	N/S	N/A	N/A	N/A	N/A	M/F	N/A	M/F	M/F	N/A	M/F	N/S	N/A	N	N
Z(3940)	2++	M/F	S?^	N/S	N/A	N/A	N/A	N/A	M/F	N/A	M/F	M/F	N/A	M/F	M/F	N/A	N	N
Y(4140)	JP+	M/F	M/F	N	s	N/A	N	N/A	N	N/A	M/F	M/F	N/A	M/F	N	N	N	N
X(4160)	0P+	M/F	M/F^	N	M/F	N/A	N	N/A	N	N/A	M/F	M/F	N/A	M/F	N	N	N	N
Y(4260)	1	s	N/A	N/A	N/A	M/F	N	N/A	N/A	N	M/F	M/F	N/A	N	N	N	N	N/A
X(4350)	JP+	M/F	M/F^	N	M/F	N/A	N	N	N	N/A	M/F	M/F	N/A	N	N	N	N	N
Y(4350)	1	M/F	N/A	N/A	N/A	M/F	N	N/A	N/A	N	M/F	M/F	N/A	N	N	N	N	N/A
Y(4660)	1	N	N/A	N/A	N/A	M/F	N	N/A	N/A	N	M/F	M/F	M/F^^	N	N	N	N	N/A
	_																	
			10.01		_	_												

ISR	JPC	]/ψππ	ψ(2S)ππ	J/ψη	χ <sub>e</sub> γ	рр	лл	ΛርΛር	DD	DD*	D*D*	Ds(*)Ds(*)
Y(4260)	1	s	N/S	N/S	N/S	N/S	M/F	N/A	N/S	N/S	N/S	N
Y(4350)	1	N/S	S	M/F	M/F	M/F	M/F	N/A	M/F	M/F	M/F	N
Y(4660)	1	N/S	S	M/F	M/F	M/F	M/F	S	M/F	M/F	M/F	N

legenda
S: seen
M/F: missing fit
N/S: not seen
N: not searched
N/A: not applicable N/F: not feasible

"Nonetheless in the present generation of experiments statistics is extremely low and we will not be able to have a convincing picture until the results of ultra-high intensity machines, LHC and the Super Flavour Factories will be available".







Exotic mesons can be intermediate states in a number of processes.

 $\triangleright$  Can they explain the low momentum excess of  $\psi$  in inclusive B decays ?





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- In e<sup>+</sup>e<sup>-</sup> collisions at  $\sqrt{s} \sim m_{\Upsilon(4S)}$  with 20.3 fb<sup>-1</sup> they measure: B  $\rightarrow J/\psi$  + All.
- In B  $\rightarrow$  J/ $\psi$  + All there is a feed-down from  $\chi_{c1,2} \rightarrow$  J/ $\psi \gamma$  and  $\psi(2S) \rightarrow$  J/ $\psi \pi^+ \pi^-$ .





Subtracting the feed-down from  $\chi_{c1,2} \rightarrow J/\psi \gamma$  and  $\psi(2S) \rightarrow J/\psi \pi^+ \pi^-$ , they obtain the p<sup>\*</sup> decay distribution of J/ $\psi$  produced directly in B decays.





- Subtracting the feed-down from  $\chi_{c1,2} \rightarrow J/\psi \gamma$  and  $\psi(2S) \rightarrow J/\psi \pi^+ \pi^-$ , they obtain the p<sup>\*</sup> decay distribution of J/ $\psi$  produced directly in B decays.
- Theoretical predictions reveal an excess at low  $p_{\psi}$ .





If the cc\* pair is produced in color singlet configuration one has a two body docty:  $\mathbf{R} \rightarrow 1/11$  (c)





PHYSICAL REVIEW D 83, 032005 (2011)

Study of the  $K^+\pi^+\pi^-$  final state in  $B^+ \to J/\psi K^+\pi^+\pi^-$  and  $B^+ \to \psi' K^+\pi^+\pi^-$ 

Submode Decay fraction  $J_1$ Nonresonant  $K^+\pi^+\pi^ 0.152 \pm 0.013 \pm 0.028$  $K_1(1270) \to K^*(892)\pi$  $0.232 \pm 0.017 \pm 0.058$  $B^+ \to \mathcal{K}_i J/\psi \to \mathcal{R}_i J/\psi \to J/\psi K^+ \pi^+ \pi^ K_1(1270) \rightarrow K\rho$  $0.383 \pm 0.016 \pm 0.036$ 1+  $K_1(1270) \rightarrow K\omega$  $0.0045 \pm 0.0017 \pm 0.0014$  $K_1(1270) \rightarrow K_0^*(1430)\pi$  $0.0157 \pm 0.0052 \pm 0.0049$  $\mathcal{B}(B^+ \to \mathcal{K}_i J/\psi \to \mathcal{R}_i J/\psi \to J/\psi K^+ \pi^+ \pi^-) = \mathcal{B}_{tot} \mathbf{f}_i^{\mathbf{j}}$  $K_1(1400) \to K^*(892)\pi$  $0.223 \pm 0.026 \pm 0.036$  $K^*(1410) \to K^*(892)\pi$ 1- $0.047 \pm 0.016 \pm 0.015$ 600  $K_{2}^{*}(1430) \rightarrow K^{*}(892)\pi$  $0.088 \pm 0.011 \pm 0.011$ Entries / 25.0 MeV/c<sup>2</sup> 500 E  $K_2^*(1430) \rightarrow K\rho$ 0.0233 (fixed) Signal Region 400  $2^{+}$  $K_2^*(1430) \rightarrow K\omega$ 0.00036 (fixed)  $0.0739 \pm 0.0073 \pm 0.0095$  $K_2^*(1980) \to K^*(892)\pi$ 300  $0.0613 \pm 0.0058 \pm 0.0059$  $K_2^*(1980) \rightarrow K\rho$ 200 **Sideband Region**  $K(1600) \rightarrow K^*(892)\pi$  $0.0187 \pm 0.0058 \pm 0.0050$ 100  $K(1600) \rightarrow K\rho$  $0.0424 \pm 0.0062 \pm 0.0110$ 0 0.8 1.2 2 2.2 2.4 1.4 1.6 1.8  $K_2(1770) \to K^*(892)\pi$  $0.0164 \pm 0.0055 \pm 0.0061$  $2^{-}$ M'(Kππ) (GeV/c<sup>2</sup>)  $K_2(1770) \rightarrow K_2^*(1430)\pi$  $0.0100 \pm 0.0028 \pm 0.0020$  $K_2(1770) \rightarrow Kf_2(1270)$  $0.0124 \pm 0.0033 \pm 0.0022$  $K_2(1770) \rightarrow Kf_0(980)$  $0.0034 \pm 0.0017 \pm 0.0011$ 

(The Belle Collaboration)

TABLE V. Fitted parameters of the signal function for  $B^+ \rightarrow J/\psi K^+ \pi^+ \pi^-$ , along with the corresponding decay fractions.



From the fractions we compute the two body branching ratios

$\mathcal{K}_j$	$m_{\mathcal{K}_j} \; (\text{GeV})$	$\Gamma_{\mathcal{K}_j}$ (GeV)	$\mathcal{B}(B^+ \to \mathcal{K}_j J/\psi) \times 10^5$	
K	0.494	—	$95.0\pm3.6$	*
$K^*$	0.892	0.050	$137.0\pm7.8$	*
$K_1(1270)$	1.270	0.090	$144.0\pm29.3$	
$K_1(1400)$	1.403	0.174	$25.1 \pm 5.7$	
$K^*(1410)$	1.414	0.232	$> 5.1 \pm 2.4$ and $< 11.8 \pm 5.7$	
$K_2^*(1430)$	1.430	0.100	$40.2\pm24.0$	
$K_2(1600)$	1.605	0.115	$> 8.4 \pm 2.9$	
$K_2(1770)$	1.773	0.186	$> 4.4 \pm 1.5$	
$K_2(1980)$	1.973	0.373	$> 15.2 \pm 2.5$	

\* <u>http://hfag.phys.ntu.edu.tw/b2charm/index.html</u>



Two body contributions accounts for the high  $p_{\psi}$  region: we found good agreement for  $p_{\psi} > 1.2$  GeV.





# Color Octet Contribution

Two main parameters to model the color octet contribution: ∧<sub>QCD</sub>∈[200,450]MeV :the characteristic energy-momentum scale of the soft gluons; p<sub>F</sub> ∈[300,450]MeV : Fermi momentum of the b-quark inside the B-meson.



## Which XYZ contribute to $B \rightarrow J/\psi + AII$ ?



# $B \rightarrow \mathscr{K} \mathscr{N} \rightarrow \mathscr{K} J/\psi + \text{light hadrons}$

#### ▷ $B \rightarrow K(500)$ $% \rightarrow K(500)$ J/ψ + light hadrons branching ratios are known:

$\mathcal{X}_j$	$m_{\mathcal{X}_j} (\text{GeV})$	$\Gamma_{\mathcal{X}_j}$ (GeV)	Final State	$\mathcal{B}(B \to K \mathcal{X}_j \to K J/\psi + \text{light hadrons}) \times 10^5$
X(3872) 3.87	3 872	0.003	$J/\psi \ \rho \to J/\psi \ \pi^+\pi^-$	$0.72 \pm 0.22$ [A]
$\left  \frac{1}{2} \left( \frac{3012}{2} \right) \right $	0.012	0.000	$J/\psi\;\omega$	$0.6 \pm 0.3 \; [B]$
Y(3940)	3.940	0.087	$J/\psi\;\omega$	$3.70 \pm 1.14$ [C]
Y(4140)	4.140	0.012	$J/\psi \; \phi$	$0.9 \pm 0.4 \; [D]$
Y(4260)	4.260	0.095	$J/\psi f_0 \to J/\psi \pi^+\pi^-$	$2.00 \pm 0.73$ [C]

[A] B. Aubert et al. (BABAR), Phys. Rev. **D77**, 111101 (2008), 0803.2838.

[B] P. del Amo Sanchez et al. (BABAR), Phys. Rev. **D82**, 011101 (2010), 1005.5190.

[C] http://hfag.phys.ntu.edu.tw/b2charm/index.html.

[D] K. Yi and f. t. C. collaboration, PoS EPS-HEP **2009**, 2009:085,2009 (2009), 0910.3163.

#### For heavy kaons $\mathscr{K}$ we deduce the coupling B- $\mathscr{K}$ from the B-K(500) $\mathscr{X}$ one:

$$\begin{array}{ll} \underline{\operatorname{Spin}} & \mathbf{0} \ \mathbf{\mathscr{K}} & \langle \mathcal{X}(\epsilon, p) \mathcal{K}(q) | B(P) \rangle = \underbrace{g} \epsilon \cdot q \\ \\ \underline{\operatorname{Spin}} & \mathbf{1} \ \mathbf{\mathscr{K}} & \langle \mathcal{X}(\epsilon, p) \mathcal{K}(\eta, q) | B(P) \rangle = \underbrace{g} \epsilon \cdot \eta \end{array}$$

$$g' = \Lambda \; g$$
  $\Lambda$  some mass scale

#### We assume

 $\Lambda = m_{K(J=1)}$ taking all  $\Re$  to be Spin 1 states.

We simulate the decay  $B \rightarrow \mathscr{K} X \rightarrow \mathscr{K} J/\psi$  + light hadrons taking into account the partial decay wave.

We fit the sum of all the contributions to data using as a free parameter the overall normalization of the color octet component.





The best fit in the allowed region for the two parameters ( $\Lambda_{QCD}$ ,  $p_F$ ) is obtained choosing:  $\Lambda_{QCD} = 500 \text{ MeV}$  and  $p_F = 500 \text{ MeV}$ .





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If the branching ratio due to XYZ turns out to be larger than the one measured (more XYZ states!) the best fit could be obtained with more reasonable parameters for the color octet component.



## Conclusions

- Almost ten years of studies have uncovered a completely new spectroscopy .
- A unifying picture is still lacking :
  - Data
    - la strong interplay between theory and experiments is needed
    - higher statistics is needed
  - ▶<u>Theory</u>

Indirect searches may represent a complementary strategy.

SUPER B OFFERS US THIS POSSIBILITY



Unexpected (2)

:: Heavy Quarkonium Working Group, Eur.Phys.J. C71 (2011) 1534 ::



# Data for bb<sup>\*</sup> states







## Unexpected

:: Belle, Phys.Rev.Lett. 100 (2008) 1120014 :: :: Belle, arXiv:1105.4583 ::



# $B \rightarrow J/\psi + AII$

:: BaBar, Phys. Rev. D67,032002 ::

In e<sup>+</sup>e<sup>-</sup> collisions at  $\sqrt{s} \sim m_{\Upsilon(4S)}$  with 20.3 fb<sup>-1</sup> they measure: B  $\rightarrow J/\psi + AII, B \rightarrow \psi(2S) + AII, B \rightarrow \chi_{c1,2} + AII.$ 

$$\begin{split} & \bigvee J/\psi \rightarrow e^+e^-, \mu^+\mu^- \\ & \psi(2S) \rightarrow e^+e^-, \mu^+\mu^- \text{ and } J/\psi \ \pi^+\pi^- \\ & \chi_{c1,2} \rightarrow J/\psi \ \gamma \end{split}$$

$$\Im (J/\psi \rightarrow e^+e^-) = 5.94\%$$

$$\Im (J/\psi \rightarrow \mu^+\mu^-) = 5.93\%$$

 $\Im (\chi_{c1} \rightarrow J/\psi \gamma) = 34.1\%$   $\Im (\chi_{c2} \rightarrow J/\psi \gamma) = 19.4\%$ 

TABLE II. Summary of B branching fractions (percent) to charmonium mesons with statistical and systematic uncertainties. The direct branching fraction is also listed, where appropriate. The last column contains the world average values [15].

Meson	Value	Stat	Sys	World Average
$J/\psi$	1.057	±0.012	±0.040	$1.15 \pm 0.06$
$J/\psi$ direct	0.740	±0.023	±0.043	$0.80 \pm 0.08$
$\chi_{c1}$	0.367	$\pm 0.035$	$\pm 0.044$	$0.36 \pm 0.05$
$\chi_{c1}$ direct	0.341	$\pm 0.035$	$\pm 0.042$	$0.33 \pm 0.05$
$\chi_{c2}$	0.210	$\pm 0.045$	±0.031	$0.07 \pm 0.04$
$\chi_{c2}$ direct	0.190	$\pm 0.045$	±0.029	-
$\psi(2S)$	0.297	±0.020	±0.020	$0.35 \pm 0.05$



Direct contribution 9 10 9 10 9 7.5 10 5 9 7.5 10 5 9 2.5 10 5 9 2.5 10 5 10 5 10 5 10 5 10 5 10 5 10 5 10 5 10 5 10 5 10 5 10 5 10 5 10 5 10 5 10 5 10 5 10 5 10 5 10 5 10 5 10 5 10 5 10 5 1 1.5 $2 p^* (GeV/c)$   $\gg$  535 x 10 <sup>6</sup> BB<sup>\*</sup> events (492 fb<sup>-1</sup>) from e<sup>+</sup>e<sup>-</sup> collisions at  $\sqrt{s} \sim m_{\Upsilon(4S)}$ 

The PDF is  $p(\underline{x},\underline{a})$ , with  $\underline{x}=M^2(K\pi\pi),M^2(K\pi),M^2(\pi\pi)$  and  $\underline{a}=$  fit parameters

$$p(\vec{x};\vec{a}) = \begin{pmatrix} p_B(\vec{x}) \\ f p_B(\vec{x})d^3x \end{pmatrix} + \begin{pmatrix} p_S(\vec{x};\vec{a}) \\ f p_S(\vec{x};\vec{a})d^3x \end{pmatrix}$$
Signal
$$p_S(\vec{x};\vec{a}) = \varepsilon(\vec{x})\phi(\vec{x})s(\vec{x};\vec{a})$$
Background modelled
from sideband region
$$= |a_{nr}A_{nr}(\vec{x})|^2 + \sum_{J_1} \left| \sum_{J_2} a_{J_1J_2}A_{J_1J_2}(\vec{x}) \right|^2$$



The  $K^+\pi^+\pi^-$  final state is modelled as a non resonant signal plus a superposition of initial state resonances  $R_{L}$ The latter are assumed to decay through intermediate state resonances R<sub>2</sub>

 $R_1 \rightarrow a R_2$  and  $R_2 \rightarrow bc$ 

Signal

$$p_{S}(\vec{x}; \vec{a}) = \varepsilon(\vec{x})\phi(\vec{x})s(\vec{x}; \vec{a})$$

$$s(\vec{x}; \vec{a}) \equiv s(\vec{x}; a_{k})$$

$$= a_{nr}A_{nr}(\vec{x})|^{2} + \sum_{J_{1}} \left|\sum_{J_{2}}a_{J_{1}J_{2}}A_{J_{1}J_{2}}(\vec{x})\right|^{2}$$
complex coefficients



Since the components of the signal function are not individually normalized, a decay fraction is calculated as

$$f_k = \frac{\int \phi(\vec{x}) |a_k A_k(\vec{x})|^2 d^3 x}{\int \phi(\vec{x}) s(\vec{x}; \vec{a}) d^3 x}$$



Belle measures

$$\mathcal{B}(B^+ \to \mathcal{K}_j J/\psi \to R_i J/\psi \to J/\psi K^+ \pi^+ \pi^-) = \mathcal{B}_{\text{tot}} f_i^j$$

where the intermediate resonant states are

 $\mathcal{R}_i = K\rho, \ K\omega, \ K^*\pi, \ K_0^*(1430)\pi, \ K_2^*(1430)\pi \text{ and } Kf_{0,2}$ 

To extract two body branching ratios one needs to take into account isospin multiplicity

 $\mathcal{B}(B^+ \to \mathcal{K}_j J/\psi \to R_i J/\psi \to J/\psi \ K^+ \pi^+ \pi^-) = \mathcal{I}_i \times \mathcal{B}(B^+ \to \mathcal{K}_j J/\psi) \times \mathcal{B}(\mathcal{K}_j \to R_i) \times \mathcal{B}(R_i \to K\pi\pi)$ 

where the isospin factors are

$$\mathcal{I}(K\rho) = 1/3, \ \mathcal{I}(K^*\pi) = \mathcal{I}(K_0^*(1430)\pi) = 4/9, \ \mathcal{I}(K\omega) = 1, \ \mathcal{I}(Kf_0) = \mathcal{I}(Kf_2) = 2/3$$

so that

$$\mathcal{B}(B^+ \to \mathcal{K}_j J/\psi) = \frac{\mathcal{B}(B^+ \to \mathcal{K}_j J/\psi \to R_i J/\psi \to J/\psi \ K^+ \pi^+ \pi^-)}{\mathcal{I}_i \times \mathcal{B}(\mathcal{K}_j \to R_i) \times \mathcal{B}(R_i \to K\pi\pi)} = \frac{\mathcal{B}_{\text{tot}} f_i^j}{\mathcal{I}_i \times \mathcal{B}(\mathcal{K}_j \to R_i) \times \mathcal{B}(R_i \to K\pi\pi)}$$



Interference effects among different heavy kaons  $\mathscr{K}_j$  have been neglected, so that one needs to rescale the two body branching ratios by some factor.

$$\mathcal{B}(B^+ \to \mathcal{K}_j J/\psi \to \mathcal{R}_i J/\psi \to J/\psi \ K^+ \pi^+ \pi^-) = \mathcal{B}_{\text{tot}} \tilde{f}_i^j$$
$$\tilde{f}_i^j = C \times \left(1 - \frac{\Gamma_j}{m_j}\right) f_i^j \qquad \mathcal{B}_{\text{tot}} = (71.6 \pm 1 \pm 6) \times 10^{-5}$$

$\mathcal{K}_j$	$m_{\mathcal{K}_j}$ (GeV)	$\Gamma_{\mathcal{K}_j}$ (GeV)	$\mathcal{B}(B^+ \to \mathcal{K}_j J/\psi) \times 10^5$	
K	0.494	_	$95.0 \pm 3.6$	*
$K^*$	0.892	0.050	$137.0\pm7.8$	*
$K_1(1270)$	1.270	0.090	$144.0\pm29.3$	
$K_1(1400)$	1.403	0.174	$25.1 \pm 5.7$	
$K^{*}(1410)$	1.414	0.232	$> 5.1 \pm 2.4$ and $< 11.8 \pm 5.7$	
$K_2^*(1430)$	1.430	0.100	$40.2\pm24.0$	
$K_2(1600)$	1.605	0.115	$> 8.4 \pm 2.9$	
$K_2(1770)$	1.773	0.186	$> 4.4 \pm 1.5$	
$K_2(1980)$	1.973	0.373	$> 15.2 \pm 2.5$	

\* <u>http://hfag.phys.ntu.edu.tw/b2charm/index.html</u>

# $B \rightarrow \mathscr{K} \mathscr{X} \rightarrow \mathscr{K} J/\psi + \text{light hadrons}$

#### ▷ $B \rightarrow K(500)$ $% \rightarrow K(500)$ J/ψ + light hadrons branching ratios are known:

$\mathcal{X}_j$	$m_{\mathcal{X}_j} (\text{GeV})$	$\Gamma_{\mathcal{X}_j}$ (GeV)	Final State	$\mathcal{B}(B \to K\mathcal{X}_j \to KJ/\psi + \text{light hadrons}) \times 10^5$
X(3872)	3.872	0.003	$J/\psi \ \rho \to J/\psi \ \pi^+\pi^-$	$0.72 \pm 0.22$ [A]
			$J/\psi\;\omega$	$0.6 \pm 0.3 \; [B]$
Y(3940)	3.940	0.087	$J/\psi\;\omega$	$3.70 \pm 1.14$ [C]
Y(4140)	4.140	0.012	$J/\psi ~\phi$	$0.9 \pm 0.4 \; [D]$
Y(4260)	4.260	0.095	$J/\psi f_0 \to J/\psi \pi^+\pi^-$	$2.00 \pm 0.73$ [C]

[A] B. Aubert et al. (BABAR), Phys. Rev. **D77**, 111101 (2008), 0803.2838.

[B] P. del Amo Sanchez et al. (BABAR), Phys. Rev. **D82**, 011101 (2010), 1005.5190.

[C] http://hfag.phys.ntu.edu.tw/b2charm/index.html.

[D] K. Yi and f. t. C. collaboration, PoS EPS-HEP **2009**, 2009:085,2009 (2009), 0910.3163.

#### For heavy kaons $\mathscr{K}$ we deduce the coupling B- $\mathscr{K} \mathscr{X}$ from the B-K(500) $\mathscr{X}$ one:

$$\underbrace{\operatorname{Spin 0}}_{\mathsf{Spin 1}} \mathscr{K} \quad \langle \mathcal{X}(\epsilon, p) \mathcal{K}(q) | B(P) \rangle = \underbrace{g}_{\epsilon} \cdot q$$

$$\underbrace{\operatorname{Spin 1}}_{\epsilon} \mathscr{K} \quad \langle \mathcal{X}(\epsilon, p) \mathcal{K}(\eta, q) | B(P) \rangle = \underbrace{g}_{\epsilon} \cdot \eta$$

$$g' = \Lambda \; g$$
   
  $\Lambda$  some mass scale

From  $\mathcal{B}(B \to K^*X(3872)) \times \mathcal{B}(X(3872) \to J/\psi \pi^+\pi^-) < 0.34 \times 10^{-5}$ we deduce  $\Lambda > 600 \text{ MeV} \approx m_{K^*}$  and thus we assume  $\Lambda = m_{K1}$ , taking all  $\mathcal{A}$  to be Spin I states.

# Color Octet Contribution

:: Beneke, Schuler, Wolf, Phys.Rev. D62 (2000) 034004 ::



- At leading order in the non-relativistic expansion the  $cc^*$  pair has to be produced in a color singlet  ${}^3S_1$  state.
- At relative order  $v^4 \approx I/I5$  in the non-relativistic expansion, J/ $\psi$  can also be produced through cc<sup>\*</sup> in  ${}^{1}S_{0}{}^{(8)}$ ,  ${}^{3}P_{J}{}^{(8)}$ ,  ${}^{3}S_{I}{}^{(8)}$  color octet states
- The short-distance structure of the  $\Delta B=1$  weak effective Hamiltonian favors the production of color octet  $cc^*$  pairs in the b $\rightarrow cc^*q$  transition

The hard and soft part of the process can be factorized

$$(2\pi)^{3}2p_{R}^{0}\frac{d\sigma}{d^{3}p_{R}} \equiv \sum_{n} \int \frac{d^{4}l}{(2\pi)^{4}}\hat{\sigma}(c\bar{c}[n])(l)F_{n}(l)$$

$$F_{n}(l) = \int \frac{dk^{2}}{2\pi}\frac{d^{3}k}{(2\pi)^{3}2k^{0}}(2\pi)^{4}$$

$$F_{n}(l) = \int \frac{dk^{2}}{2\pi}\frac{d^{3}k}{(2\pi)^{3}2k^{0}}(2\pi)^{4}$$

$$\times \delta(p_{R}+k-P-l)\Phi_{n}(k;p_{R},P)$$
hard process cross section shape function

The distribution can be written as an integral over the energy and invariant mass of the soft radiated system:

$$(2\pi)^{3} 2p_{R}^{0} \frac{d\sigma}{d^{3}p_{R}}$$

$$= \sum_{n} \int_{0}^{\alpha\beta} \frac{dk^{2}}{2\pi} \int_{(\alpha^{2}+k^{2})/(2\alpha)}^{(\beta^{2}+k^{2})/(2\beta)} dk_{0} \times \text{flux}$$

$$\times \overline{H}_{n}(P_{in}, P, l, p_{X}) \frac{1}{4\pi(\beta-\alpha)} \Phi_{n}(k; p_{R}, P)$$

 $\gg$  The color octet configurations which contribute to  $B \rightarrow J/\psi$  + All are

$$n = {}^{1}S_{0}^{(8)}, {}^{3}P_{0}^{(8)}, {}^{3}S_{1}^{(8)}$$

The shape function is related to the NRQCD matrix elements as

$$\int \frac{d^4l}{(2\pi)^4} F_n(l) = \frac{1}{(2\pi)^3} \int_0^\infty dk^2 \int_{\sqrt{k^2}}^\infty dk_0$$
$$\times \sqrt{k_0^2 - k^2} \Phi_n(k; p_R, P)$$
$$= \langle \mathcal{O}_n^{J/\psi} \rangle,$$

An ansatz for the shape function is

$$\Phi_n(k; p_R, P) = a_n |k|^{b_n} \exp(-k_0^2 / \Lambda_n^2) k^2 \exp(-k^2 / \Lambda_n^2)$$

which is exact in the Coulombic limit. The exponential cutoff reflects the expectations that the typical energy and invariant mass of the radiated system is of order  $\Lambda_n \approx m_c v^2$ 

The decay distribution in the rest frame of the cc<sup>\*</sup> pair is

$$\frac{d\hat{\Gamma}}{d\hat{E}_{R}} = \frac{|\hat{p}_{R}|}{4\pi^{2}} \sum_{n} \int_{0}^{\alpha\beta} \frac{dk^{2}}{2\pi} \int_{(\alpha^{2}+k^{2})/(2\alpha)}^{(\beta^{2}+k^{2})/(2\beta)} dk_{0}$$
$$\times \frac{1}{2m_{b}} H_{n}(m_{b}, M_{c\bar{c}}(k)) \frac{M_{R}}{8\pi m_{b}|\hat{p}_{R}|} \Phi_{n}(k)$$

where

$$M_{c\bar{c}}^{2}(k) = (p+l)^{2} = (p_{R}+k)^{2} = M_{R}^{2} + 2M_{R}k_{0} + k^{2}$$

To normalize the shape function one uses

$$\langle \mathcal{O}_{8}^{J/\psi}({}^{3}S_{1}) \rangle = (0.5 - 1.0) \times 10^{-2} \text{ GeV}^{3}$$

$$M_{k}^{J/\psi}({}^{1}S_{0}^{(8)}, {}^{3}P_{0}^{(8)}) = \langle \mathcal{O}_{8}^{J/\psi}({}^{1}S_{0}) \rangle + \frac{k}{m_{c}^{2}} \langle \mathcal{O}_{8}^{J/\psi}({}^{3}P_{0}) \rangle \qquad M_{3.1}^{J/\psi}({}^{1}S_{0}^{(8)}, {}^{3}P_{0}^{(8)}) = (1.0 - 2.0) \times 10^{-2} \text{ GeV}^{3}$$



The b quark is moving inside the B meson at rest with a momentum p according to some distribution with a width of few hundred MeV. The cloud of gluons and light quarks is treated as spectator.

$$\Phi_{\rm ACM}(p) = \frac{4}{\sqrt{\pi p_F^3}} \exp(-p^2/p_F^2)$$

One needs thus to consider a floating b-mass

$$m_b^2(p) = M_B^2 + m_{sp}^2 - 2M_B\sqrt{m_{sp}^2 + p^2}$$

To obtain the distribution in the B rest frame

$$\frac{d\Gamma}{dE_R} = \int_{\max\{0,p_-\}}^{p_+} dp p^2 \Phi_{\text{ACM}}(p) \frac{m_b^2(p)}{2pE_b(p)} \times \int_{\hat{E}_R^{\min}(p)}^{\hat{E}_R^{\max}(p)} \frac{d\hat{E}_R}{\hat{E}_R} \frac{d\hat{\Gamma}}{d\hat{E}_R}.$$