

La Thuile, 28 February 2011

The Early Days of QCD
(as seen from Rome)

Guido Altarelli
Roma Tre/CERN

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In honour of Mario Greco

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The Early Days of QCD
(as seen from Rome)

In honour of Mario Greco

or

QCD in Rome in the Seventies

Guido Altarelli
Roma Tre/CERN

I have a half-century-long friendship with Mario

We met when students at the University of Rome
in the early '60's

Then I went to Florence and then to the USA

When back in Rome in '70 we came in close contact,
also with our families

At present we are both at Roma Tre and our offices are
a few meters away





Da sinistra: Mario Greco, Yogi Srivastava e Guido Altarelli nel 1979 all'Accademia dei Lincei, Roma.



One can say that the application of QCD starts with the Nobel winner papers by **Gross & Wilczek** and by **Politzer** in **1973**

Ultraviolet Behavior of Non-Abelian Gauge Theories*

David J. Gross† and Frank Wilczek

Joseph Henry Laboratories, Princeton University, Princeton, New Jersey 08540

(Received 27 April 1973)

It is shown that a wide class of non-Abelian gauge theories have, up to calculable logarithmic corrections, free-field-theory asymptotic behavior. It is suggested that Bjorken scaling may be obtained from strong-interaction dynamics based on non-Abelian gauge symmetry.

Reliable Perturbative Results for Strong Interactions?*

H. David Politzer

Jefferson Physical Laboratories, Harvard University, Cambridge, Massachusetts 02138

(Received 3 May 1973)

An explicit calculation shows perturbation theory to be arbitrarily good for the deep Euclidean Green's functions of any Yang-Mills theory and of many Yang-Mills theories with fermions. Under the hypothesis that spontaneous symmetry breakdown is of dynamical origin, these symmetric Green's functions are the asymptotic forms of the physically significant spontaneously broken solution, whose coupling could be strong.



Sure enough there has been a pre-history with very important works

Parton
model

Bjorken
Paschos
Feynman
.....

Ren. Group.

Gell-Mann-Low
Callan-
Symanzik
.....

Quarks

Gell-Mann
Zweig
Greenberg
.....

QCD
field theory

Fritzsch-
Gell-Mann-
Leutwyler
.....

Short
distance

Wilson
Brandt-
Preparata
.....

Asymptotic
freedom

't Hooft
.....

but the systematic application of QCD to physics started in ~'73

In '73 three groups were active in Rome at:
Roma 1 "La Sapienza", Istituto Superiore di Sanita' and
Laboratori Nazionali di Frascati
(Roma 2 "Tor Vergata" was born in '82 and Roma Tre in '92)

Roma 1

Altarelli
Cabibbo
Petronzio
.....

Sanita'

Maiani
.....

Frascati

Greco
Pancheri
Parisi
Srivastava
.....

The QCD related activities had already started before
Gross&Wilczek and Politzer



With Symanzik, Giorgio Parisi was very influential on the study of physical implications of anomalous dimensions

LETTERE AL NUOVO CIMENTO

VOL. 7, N. 2

12 Maggio 1973

Deep Inelastic Scattering in a Field Theory with Computable Large-Momenta Behaviour.

G. PARISI

Laboratori Nazionali di Frascati del CNEN - Frascati

(ricevuto il 7 Febbraio 1972)

In this paper he studied structure functions in $\lambda\phi^4$ with $\lambda < 0$, a theory discussed by Symanzik as a field theory model for Bjorken scaling

This paper was cited by Gross & Wilczek and by D. Gross, Asymptotic Freedom and QCD - a Historical perspective, Nucl. Phys. B (Proc. Suppl) 135(2004)193

Here limits on logarithmic scaling violations are derived from the existing data

Volume 43B, number 3

PHYSICS LETTERS

5 February 1973

EXPERIMENTAL LIMITS ON THE VALUES OF ANOMALOUS DIMENSIONS

G. PARISI

Laboratori Nazionali del C.N.E.N., Frascati, Italia

Received 31 October 1972

We show how to use the data on deep inelastic $e-p$ scattering to put bounds on the values of the anomalous dimensions of the operators involved in the Wilson expansion of the product of two currents near the lightcone. Anomalous dimensions of the order of unity are found not to be in contradiction with present experimental evidence.

This paper was cited by Politzer



In '73 in our group we were studying hard processes in the parton model (with scaling)

Deep inelastic processes in ladder models.

Guido Altarelli, L. Maiani (Rome U.). 1973.

Published in Nucl.Phys. B51 (1973) 509-534

a $\lambda\phi^3$
field theory
model
for scaling

Deep-inelastic one-particle inclusive processes in the parton model.

Guido Altarelli (Rome U.), L. Maiani (Rome, ISS). 1973.

Published in Nucl.Phys. B56 (1973) 477-492

The Nucleon as a bound state of three quarks and deep inelastic phenomena.

Guido Altarelli (Rome U.), N. Cabibbo (CERN & Rome U. & INFN, Rome), L. Maiani (Rome, ISS & INFN, Rome), R. Petronzio (Rome U.). Aug 1973.

Published in Nucl.Phys. B69 (1974) 531-536

the nucleon is described in terms of constituent quarks, each of them with a parton structure. This idea is still viable.



In '72 Mario evaluated the hadronic contribution to a_μ from e^+e^- cross sections

HADRONIC CONTRIBUTIONS TO THE MUON
ANOMALOUS MAGNETIC MOMENT

A. BRAMÒN*, E. ETIM** and M. GRECO
Laboratori Nazionali del CNEN, Frascati, Italy

Received 9 March 1972

The hadronic contribution to the muon anomalous magnetic moment is calculated using recent results from colliding beam experiments; a value of $(68 \pm 9) \times 10^{-9}$ is obtained.

they found: $a_\mu = 68 \pm 9 \cdot 10^{-9}$

Davier et al '10 (ArXiv:1010.4180): $a_\mu = 69.23 \pm 0.42 \cdot 10^{-9}$



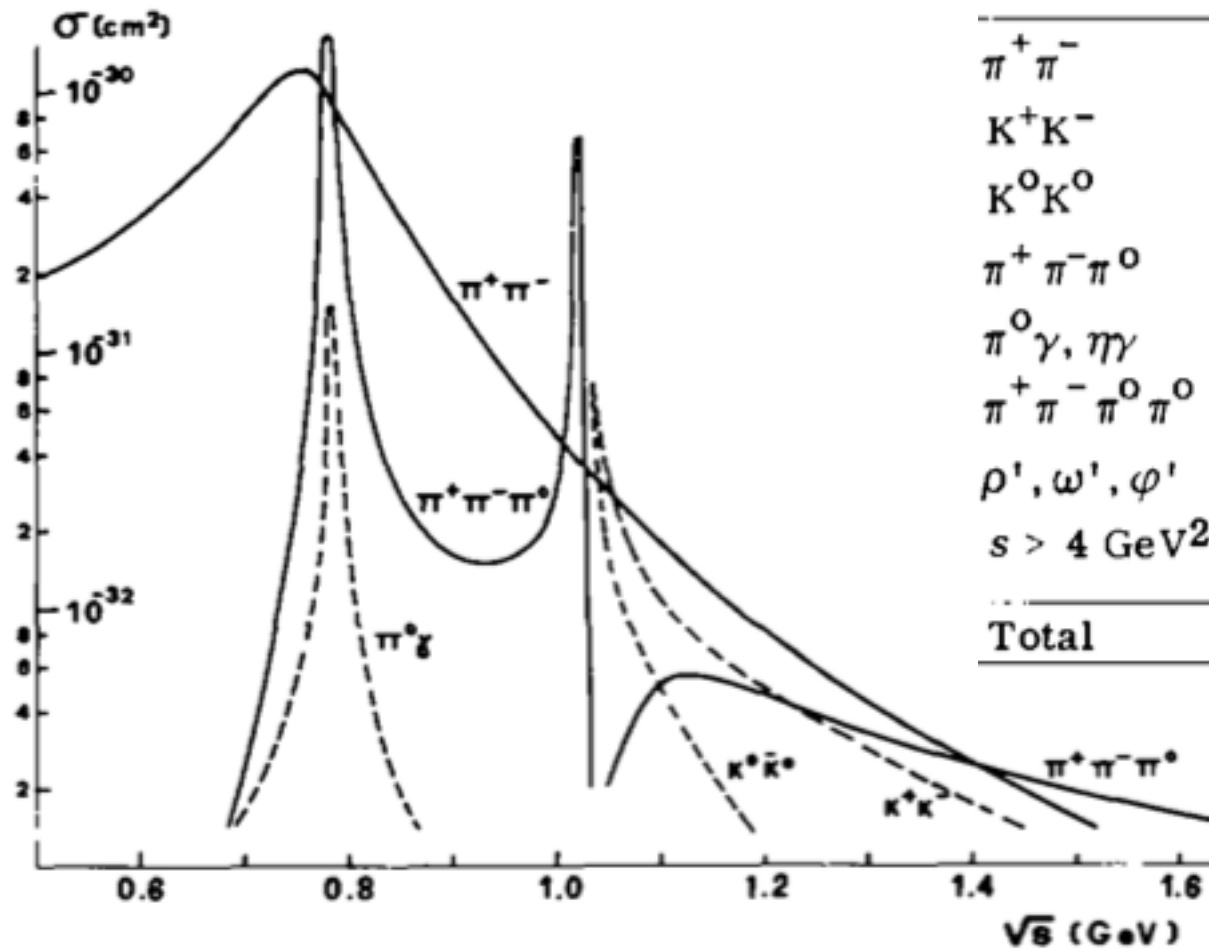


Table 1

f	$a_{\mu}(f) \times 10^9$
$\pi^+ \pi^-$	49.4 ± 5.7
$K^+ K^-$	2.2 ± 0.2
$K^0 \bar{K}^0$	1.5 ± 0.2
$\pi^+ \pi^- \pi^0$	6.5 ± 0.9
$\pi^0 \gamma, \eta \gamma$	0.5 ± 0.1
$\pi^+ \pi^- \pi^0 \pi^0$	0.9 ± 0.2
ρ', ω', ϕ'	5.3 ± 1.5
$s > 4 \text{ GeV}^2$	~ 1.5
Total	68 ± 9

Note: with errors in quadrature it would be $a_{\mu} = 68 \pm 6 \cdot 10^{-9}$

see next talk by Bramon



At that time Mario was interested in hard processes and was advocating a model based on extended vector boson dominance

Nuclear Physics B63 (1973) 398–412. North-Holland Publishing Company

DEEP-INELASTIC PROCESSES

M. GRECO*

CERN, Geneva and Laboratori Nazionali del CNEN, Frascati, Italy

Received 12 February 1973

$e+e^-$ annihilation, DIS, Drell-Yan were studied in this paper

Couplings vs mass of vector bosons chosen to get scaling

It was a competitive model for some time cited 171

But predicted no jets in $e+e^-$, and no suppressed σ_L/σ_T

in DIS, so it was later abandoned



After Gross&Wilczek and Politzer we immediately turned to study the implications of QCD

Volume 52B, number 3

PHYSICS LETTERS

14 October 1974

**OCTET ENHANCEMENT OF NON-LEPTONIC WEAK INTERACTIONS
IN ASYMPTOTICALLY FREE GAUGE THEORIES**

G. ALTARELLI

Istituto di Fisica dell'Università di Roma, Rome, Italy

L. MAIANI

*Lab. di Fisica, Istituto Superiore di Sanità, Rome, Italy
and Ist. Naz. di Fisica Nucleare, Sezione Sanità, Rome, Italy*

Received 22 June 1974

cited 863

Octet enhancement of weak non leptonic amplitudes is found to occur in asymptotically free gauge theories of strong interactions, combined with unified weak and e.m. interactions. The order of magnitude of the enhancement factor for different models is discussed.

This is an important paper (together with the work by M. K. Gaillard and B. W. Lee, Phys. Rev. Lett. 33(1974)108)
Cited by D. Gross, Asymptotic Freedom and QCD - a Historical
⊕ perspective, Nucl. Phys. B (Proc. Suppl) 135(2004)193

It was the first calculation of QCD corrections to the coefficients of the Wilson expansion in the product of two weak currents

TUM-HEP-343/99

[hep-ph/9901409](#)

January 1999

A quote from A. J. Buras

**Operator Product Expansion, Renormalization Group
and
Weak Decays ***

Andrzej J. Buras

am convinced that OPE will play an important role in the next 10 years in the field of weak decays as it played already in almost 25 years since the pioneering applications of this very powerful method by Gaillard and Lee [5] and Altarelli and Maiani [6].



Application to charm decay

ENHANCEMENT OF NON-LEPTONIC DECAYS OF CHARMED PARTICLES

G. ALTARELLI

*Laboratoire de Physique Théorique de l'Ecole Normale Supérieure, Paris, France**
Istituto di Fisica dell'Università, Roma, Italy

N. CABIBBO

Istituto di Fisica dell'Università, Roma, Italy
CERN, Genève, Switzerland

L. MAIANI

*Laboratoire de Physique Théorique de l'Ecole Normale Supérieure, Paris, France**
Laboratori di Fisica, Istituto Superiore di Sanità, Roma, Italy

Received 14 October 1974

before charm was discovered!!



Mario Greco graduated with a thesis on $e^+e^- \rightarrow e^+e^-\gamma\gamma$
with B. De Tollis

Then, in Frascati, working with Touschek (and Pancheri,
Srivastava, Etim), Mario became an expert in QED
radiative corrections and the resummation of soft photons

Here are two papers on the QED corrections near the J/Ψ

Radiative Effects for Resonances with Applications to Colliding Beam Processes.

Mario Greco, G. Pancheri-Srivastava, Y. Srivastava (Frascati). LNF-75/9-P. Feb 1975. 12 pp.
Published in *Phys.Lett.* B56 (1975) 367

Radiative Corrections for Colliding Beam Resonances.

Mario Greco, G. Pancheri-Srivastava, Y. Srivastava (Frascati). LNF-75/23-P. May 1975. 42 pp.
Published in *Nucl.Phys.* B101 (1975) 234

With the advent of QCD Mario naturally turned into resumming
soft gluons (see later)

EXPONENTIAL HADRONIC SPECTRUM AND QUARK LIBERATION

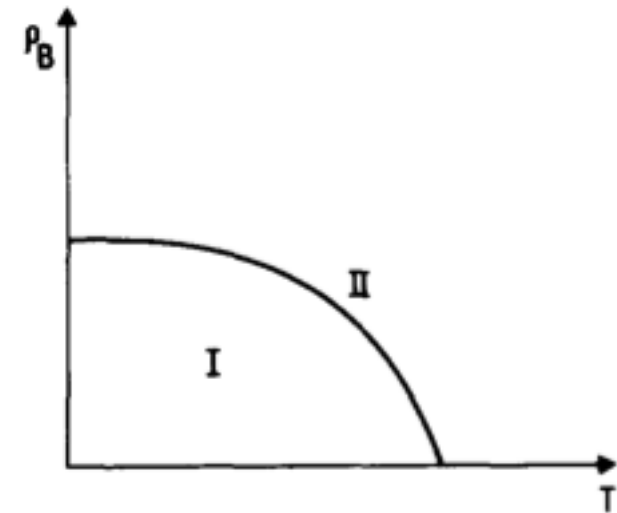
N. CABIBBO

*Istituto di Fisica, Università di Roma,
Istituto Nazionale di Fisica Nucleare, Sezione di Roma, Italy*

G. PARISI

Istituto Nazionale di Fisica Nucleare, Frascati, Italy

Received 9 June 1975



One of the first papers where quark deconfinement is discussed

It is shown that an exponentially growing hadronic spectrum (a' la Hagedorn) could be associated to a 2nd order phase transition into the quark-gluon plasma



CHARMED QUARKS AND ASYMPTOTIC FREEDOM IN NEUTRINO SCATTERING

G. ALTARELLI, R. PETRONZIO

Istituto di Fisica, Roma, Italy

Istituto Nazionale di Fisica Nucleare, Sezione di Roma, Italy

and

G. PARISI

Istituto Nazionale di Fisica Nucleare, Frascati, Italy

Received 24 March 1976

Asymptotic freedom and charm production are both important ingredients for a theoretical analysis of neutrino cross sections. We study in detail the Q^2 dependence of integrated quantities like cross sections, y -distributions and $\langle x \rangle$ values. Deviations from scaling are quite substantial in the present energy range.

This paper contributed to downgrading the “ y -anomaly”
from a signal of new physics (right-handed charged currents)
⊕ down to a charm threshold + QCD-logs effect

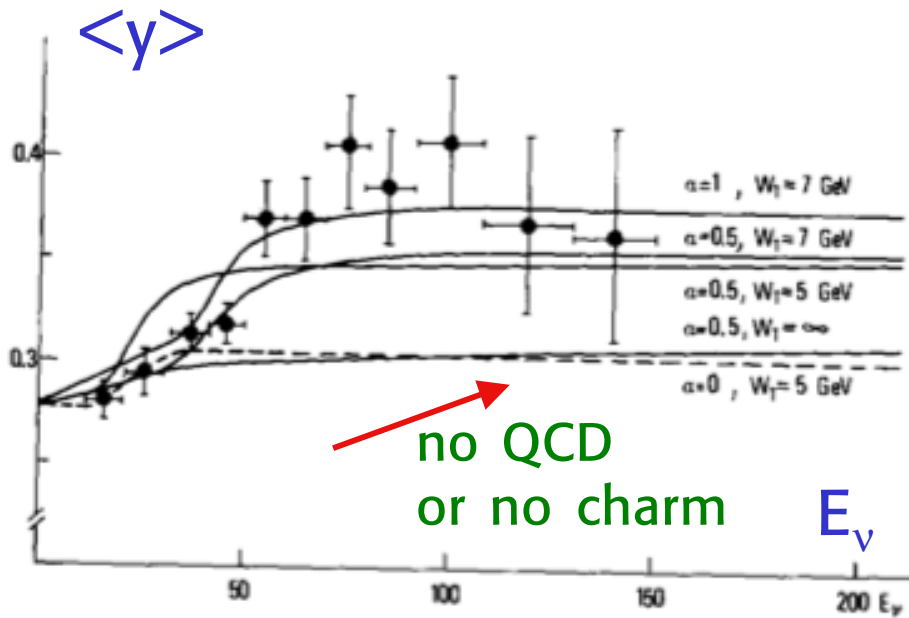
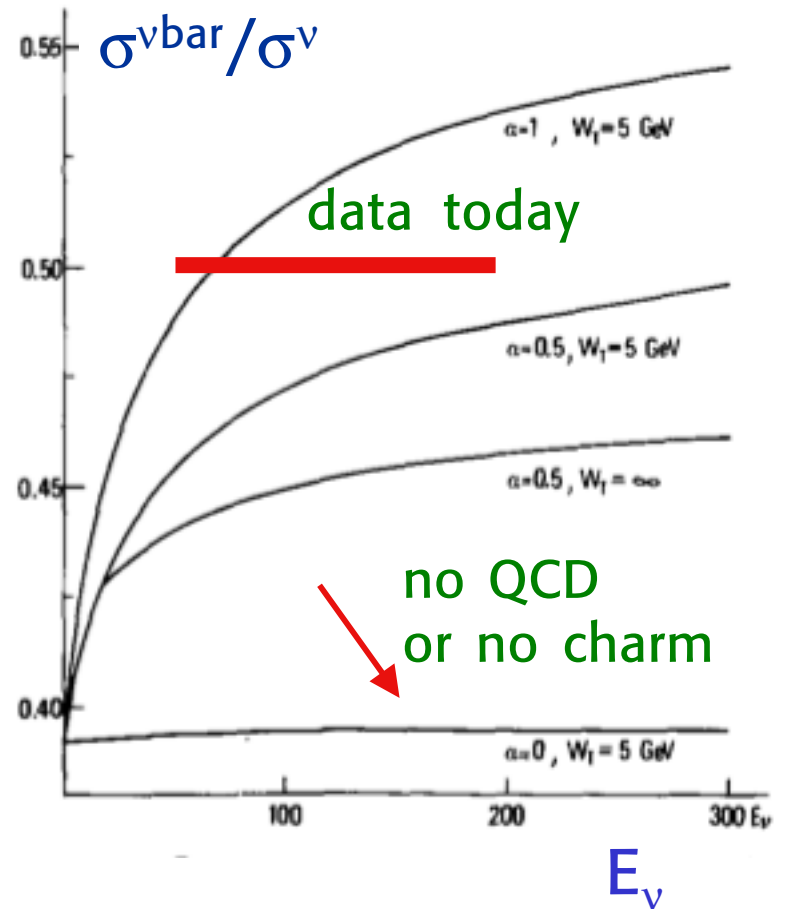


Fig. 3. Average value of y for antineutrinos for different values of $\alpha \equiv \alpha_s(\mu^2)$ and W_T , the effective invariant mass for charm threshold. $\alpha = 0$ corresponds to Q^2 independent parton distributions. $W_T \rightarrow \infty$ corresponds to neglecting effects from charm production. Both effects seem to be needed to reproduce the data. $\alpha = 0.5$ is the value suggested in the text, while $\alpha = 1$ is reported for comparison.



ASYMPTOTIC FREEDOM IN PARTON LANGUAGE

G. ALTARELLI *

*Laboratoire de Physique Théorique de l'École Normale Supérieure ** , Paris, France*

G. PARISI ***

Institut des Hautes Etudes Scientifiques, Bures-sur-Yvette, France

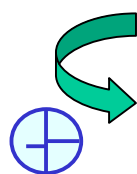
Received 12 April 1977

cited 4080

$$\frac{dq^i(x,t)}{dt} = \frac{\alpha(t)}{2\pi} \int_x^1 \frac{dy}{y} \left[\sum_j^{2f} q^j(y,t) P_{q^i q^j} \left(\frac{x}{y} \right) + G(y,t) P_{q^i G} \left(\frac{x}{y} \right) \right] \quad (22)$$

$t = \ln Q^2 / \mu^2$

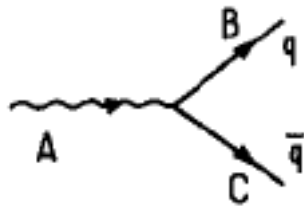
$$\frac{dG(x,t)}{dt} = \frac{\alpha(t)}{2\pi} \int_x^1 \frac{dy}{y} \left[\sum_j^{2f} q^j(y,t) P_{G q^j} \left(\frac{x}{y} \right) + G(y,t) P_{GG} \left(\frac{x}{y} \right) \right] \quad (23)$$



The QCD evolution equations hand-written by me on the '77 preprint (scanned by KEK)

In our paper, formulated in parton language, with running coupling, the splitting functions are derived directly from the QCD vertices, making clear they are the same for all processes (factorisation)

$$P_{BA}(z) = \frac{1}{2} z(1-z) \overline{\sum}_{\text{spins}} \frac{|V_{A \rightarrow B+C}|^2}{p_{\perp}^2} \quad (z < 1)$$



$$\overline{\sum}_{\text{pol}} |V_{q \rightarrow G+q}|^2 = \frac{2p_{\perp}^2}{z(1-z)} \frac{1 + (1-z)^2}{z} C_2(\mathbf{R})$$

$$P_{Gq}(z) = C_2(\mathbf{R}) \frac{1 + (1-z)^2}{z}$$

$$P_{qq}(z) = C_2(\mathbf{R}) \frac{1+z^2}{1-z} \quad (z < 1)$$

$$P_{qq}(z) = C_2(\mathbf{R}) \left[\frac{1+z^2}{(1-z)_+} + \frac{3}{2} \delta(z-1) \right]$$

The polarized splitting functions were also derived by us (not considered by DGL) in agreement with Ahmed&Ross and Sasaki (operator method)



The evolution equations are now often called DGLAP

DEEP INELASTIC ep SCATTERING IN PERTURBATION THEORY

V. N. GRIBOV and L. N. LIPATOV

Leningrad Institute for Nuclear Physics, USSR Academy of Sciences

Submitted October 18, 1971

Yad. Fiz. 15, 781–807 (April, 1972)

before G&W and P!

The parton model and perturbation theory

L. N. Lipatov

Leningrad Institute of Nuclear Physics, USSR Academy of Sciences

(Submitted November 5, 1973)

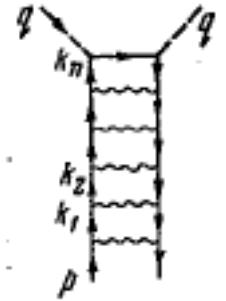
Yad. Fiz. 20, 181–198 (July 1974)



These papers refer to an **abelian** vector theory and also to a pseudoscalar theory

$$H_{\text{int}} = g \bar{\psi} \gamma_{\mu} \psi V_{\mu}$$

They ask the right question and extract the relevant terms from the dominant class of diagrams



But from their presentation it is very difficult to extract the useful results (for the vector theory).

$$\frac{dD_i^j(x)}{d\lambda} = -D_i^j(x) w_j(g_{\lambda}^2) \frac{1}{\lambda} + \sum_{j'} \int_x dx' D_i^{j'}(x') w_{j' \rightarrow j}(x', x) \frac{1}{\lambda},$$

$$D_i^j(x) |_{\lambda=m^2} = \delta(x-1) \delta_{ij},$$

$$w_{N \rightarrow N}(x_j', x_N) = w_{\bar{N} \rightarrow \bar{N}}(x', x_N) = \frac{g_{\lambda}^2}{16\pi^2} 2 \frac{1}{(x')^2} \frac{x'^2 + x_N^2}{x' - x_N}$$

$$w_{N \rightarrow M}(x', x_M) = w_{\bar{N} \rightarrow M}(x', x_M) = \frac{g_{\lambda}^2}{16\pi^2} 2 \frac{1}{(x')^2} \frac{x'^2 + (x' - x_M)^2}{x_M}$$



Calculation of structure functions of deep-inelastic scattering and e^+e^- annihilation by perturbation theory in quantum chromodynamics

Yu. L. Dokshitzer

Leningrad Institute of Nuclear Physics, USSR Academy of Sciences
 (Submitted April 20, 1977)
 Zh. Eksp. Teor. Fiz. 73, 1216-1240 (October 1977)

Exactly contemporary to us

More explicit than G&L

$$\begin{aligned} &\equiv V_F^F(x) = 2 \frac{1+x^2}{1-x}, \\ &\equiv V_F^G(x) = 2 \frac{1+(1-x)^2}{x}, \\ &\equiv V_G^F(x) = 2[x^2+(1-x)^2], \\ &\equiv V_G^G(x) = 4x(1-x) \left[1 + \frac{1}{x^2} + \frac{1}{(1-x)^2} \right] \end{aligned}$$

The limit $x \rightarrow 1$ is not made explicit

He knew G&L who are quoted in the refs.:

¹V. N. Gribov and L. N. Lipatov, *Yad. Fiz.* **15**, 781, 1218 (1972) [*Sov. J. Nucl. Phys.* **15**, 438, 675 (1972)].

²L. N. Lipatov, *Yad. Fiz.* **20**, 181 (1974) [*Sov. J. Nucl. Phys.* **20**, 94 (1975)].

non abelian



This is the D. result “equivalent” to the evolution equations

$$W_q(\omega_k, \xi_k; \xi) = \frac{e_q^2}{d_F(\xi)} \delta\left(1 - \frac{1}{\omega_k}\right) + \int_{\xi_k}^{\xi} d\xi' \int_0^1 \frac{dx}{x} \Phi_{F^F}(x).$$

$$W_q(x\omega_k, \xi'; \xi) + \int_{\xi_k}^{\xi} d\xi' \frac{d_G(\xi')}{d_F(\xi')} \int_0^1 \frac{dx}{x} \Phi_{F^G}(x) \tilde{W}(x\omega_k, \xi'; \xi),$$

$$\tilde{W}(\omega_k, \xi_k; \xi) = \int_{\xi_k}^{\xi} d\xi' \int_0^1 \frac{dx}{x} \Phi_G(x) \tilde{W}(x\omega_k, \xi'; \xi).$$

$$+ \int_{\xi_k}^{\xi} d\xi' \frac{d_F(\xi')}{d_G(\xi')} \int_0^1 \frac{dx}{x} \Phi_G(x) \sum_{q, \bar{q}=1}^{n_f} [W_q(x\omega_k, \xi'; \xi) + W_{\bar{q}}].$$

$$\sigma^q = \frac{1}{16\pi^2} \int_{\mu^2}^{Q^2} \frac{dk^2}{k^2} \tilde{g}^2(k^2)$$



Note: $d_G/d_F \tilde{W}$ is what we call the gluon density in terms of partons

**TRANSVERSE MOMENTUM OF JETS IN ELECTROPRODUCTION
FROM QUANTUM CHROMODYNAMICS**

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Istituto di Fisica dell'Università, Roma, and Istituto Nazionale di Fisica Nucleare, Sezione di Roma, Italy

and

G. MARTINELLI

Istituto Nazionale di Fisica Nucleare, Laboratori Nazionali di Frascati, Italy

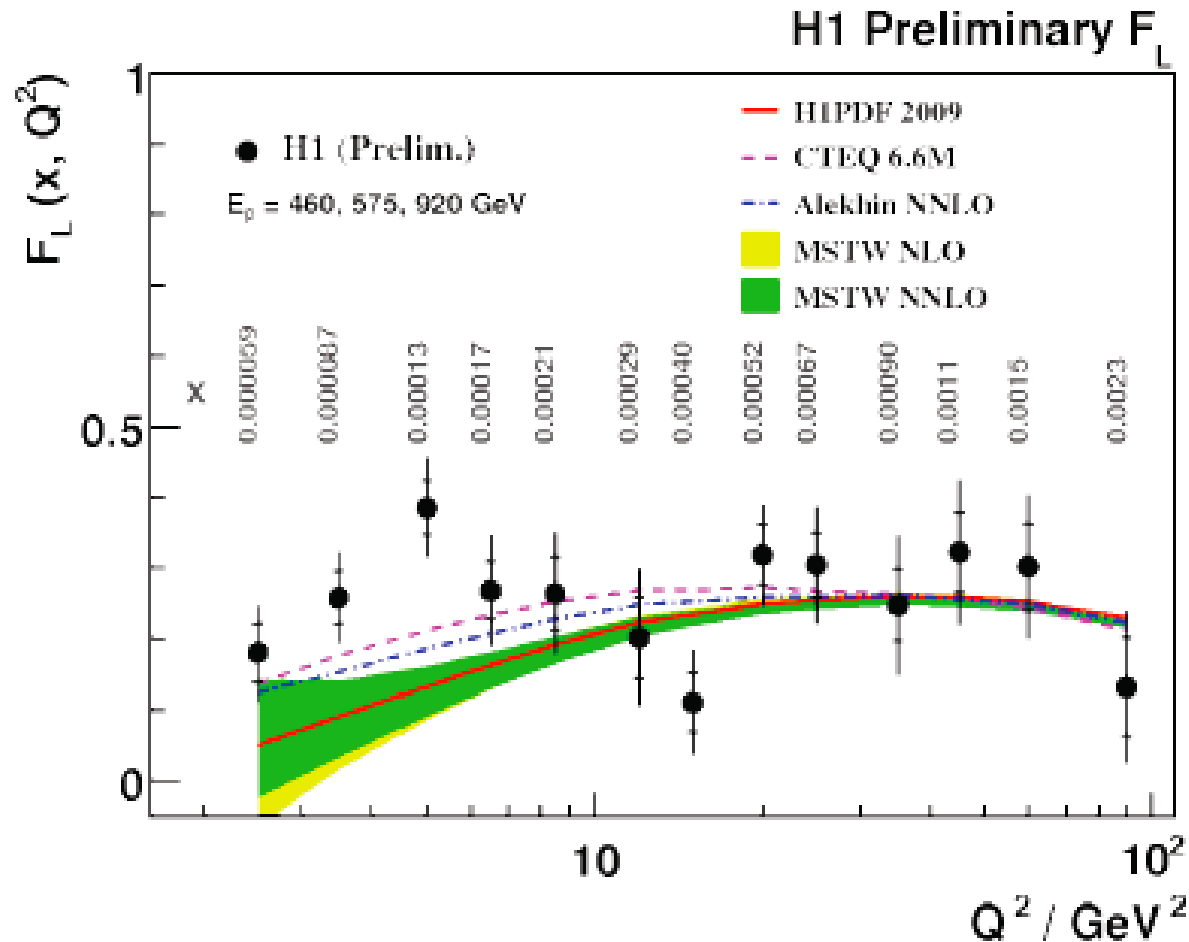
Received 26 January 1978

Among $o(\alpha_s)$ effects this formula for the longitudinal structure function was derived

$$F_L(x, Q^2) = \frac{\alpha_s(Q^2)}{2\pi} x^2 \int_x^1 \frac{dy}{y^3} \left[\frac{8}{3} F_2(y, Q^2) + \frac{40}{9} yg(y, Q^2) \left(1 - \frac{x}{y}\right) \right]_{n_f=4}$$



It took ~40 years to get meaningful data on the longitudinal structure function!!



$$F_L(x, Q^2) = \frac{\alpha_s(Q^2)}{2\pi} x^2 \int_x^1 \frac{dy}{y^3} \left[\frac{8}{3} F_2(y, Q^2) + \frac{40}{9} y g(y, Q^2) \left(1 - \frac{x}{y}\right) \right]_{n_f=4}$$



We said that in Frascati, working with Touschek (and Pancheri, Srivastava, Etim), Mario became an expert in QED radiative corrections and the resummation of soft photons

With the advent of QCD Mario naturally turned into resumming soft gluons

In a series of papers with Curci and Srivastava he applied those techniques to

- jets a la Serman Weinberg
- resummation near the end point of phase space

$x \rightarrow 1$ in DIS, $\tau \rightarrow 1$ in Drell-Yan

⊕ [Unfortunately Giuseppe Curci is no more with us]

Here the QED formalism of coherent states is applied to QCD

Volume 77B, number 3

PHYSICS LETTERS

14 August 1978

COHERENT STATE APPROACH TO THE INFRA-RED BEHAVIOUR OF NON-ABELIAN GAUGE THEORIES

M. GRECO, F. PALUMBO, G. PANCHERI-SRIVASTAVA¹ and Y. SRIVASTAVA¹
INFN, Laboratori Nazionali di Frascati, Rome, Italy

Received 31 January 1978

Volume 79B, number 4,5

PHYSICS LETTERS

4 December 1978

MASS SINGULARITIES AND COHERENT STATES IN GAUGE THEORIES

G. CURCI
CERN, Geneva, Switzerland

and

M. GRECO
Laboratori Nazionali dell'INFN, Frascati, Italy

Received 18 July 1978



QCD JETS FROM COHERENT STATES

G. CURCI

CERN, Geneva, Switzerland

M. GRECO and Y. SRIVASTAVA **

INFN, Laboratori Nazionali di Frascati, Frascati, Italy

cited 118

Received 27 February 1979

$e^+e^- \rightarrow q\bar{q}$:

$$d\sigma_{\text{super}} = d\sigma_0 \exp \left\{ -\frac{1}{\pi^2} \int_{\Delta\omega/E}^1 dx \mathcal{P}_{gq}(x) \int_{k_{1T}}^{k_{2T}} \frac{d^2k_T}{k_T^2} \bar{\alpha}(k_T) \right\},$$

where the gluon distribution due to the quarks is [11]

$$\mathcal{P}_{gq}(x) = C_F \left\{ \frac{1 + (1-x)^2}{x} \right\},$$

Probability that a fraction ε of total energy $2E$ is outside
 a cone of semi-aperture δ (Sterman-Weinberg '77 resummed)

$k_{2T} = E$

$k_{1T} = E\delta$

2ε

LARGE INFRA-RED CORRECTIONS IN QCD PROCESSES

G. CURCI and M. GRECO¹*CERN, Geneva, Switzerland*

Received 29 November 1979

cited 157

Resummation near the phase space end point is an important issue in QCD

DIS near $x = 1$

$$q(x, Q^2) \simeq \frac{1}{2\pi} \int_{-\infty}^{\infty} db e^{ib(1-x)} \exp \left\{ C_F \int_0^1 \frac{dz}{1-z} \int_{\lambda^2}^{k_1^2 \max = Q^2(1-z)} \frac{dk_1^2}{k_1^2} \frac{\alpha(k_1)}{\pi} [e^{-ib(1-z)} - 1] \right\}$$

Drell-Yan near $\tau = z = 1$

$$\frac{d\sigma^{\text{DY}}}{dQ^2} = \frac{4\pi\alpha^2}{9SQ^2} \int \frac{dx_1}{x_1} \frac{dx_2}{x_2} \left[\sum_i e_i^2 q_i(x_1, Q^2) \bar{q}_i(x_2, Q^2) + (1 \leftrightarrow 2) \right] \tilde{f}(z, Q^2)$$

resummed π^2

$$\tilde{f}(z, Q^2) = \left\{ \frac{1}{2\pi} \int db e^{ib(1-z)} \exp \left[2C_F \int_0^1 \frac{dy}{1-y} \int_{Q^2(1-y)}^{Q^2(1-y)^2} \frac{dk_1^2}{k_1^2} \frac{\alpha(k_1)}{\pi} (e^{-ib(1-y)} - 1) \right] \right\} \exp \{ [\alpha(Q^2)/2\pi] C_F \pi^2 \} \quad (16)$$

Mario Greco
at a Moriond
meeting in '80

There he gave
the talk
"Soft gluon effects
in QCD processes".



The theory of Drell-Yan processes was much advanced in Rome

- Resummation

Large π^2 terms

Parisi '80

Logs of $(1-\tau)$

Curci, Greco '80

- NLO QCD corrections

Altarelli, K. Ellis, Martinelli '78, '79

The "K factor"

- Transverse momentum distribution

Perturbative

Altarelli, Parisi, Petronzio '78

K. Ellis, Martinelli, Petronzio '81, '83

Parisi, Petronzio '79

Sudakov double logs

(following and correcting

Dokshitzer, Dyakonov, Troyan'78)

Curci, Greco, Srivastava'79

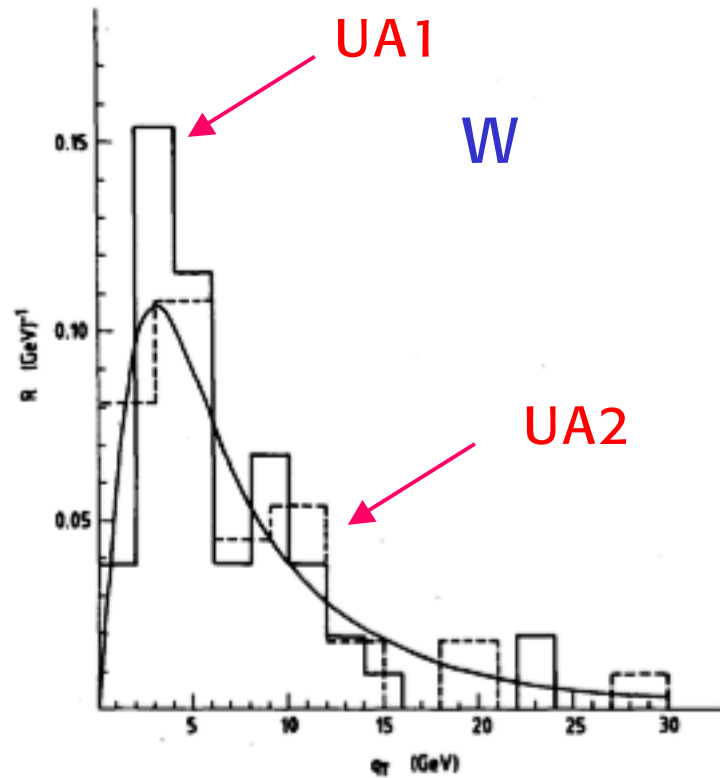
Matching of perturbative and Sudakov terms

Chiappetta, Greco '83, '84

Altarelli, K. Ellis, Greco, Martinelli '84



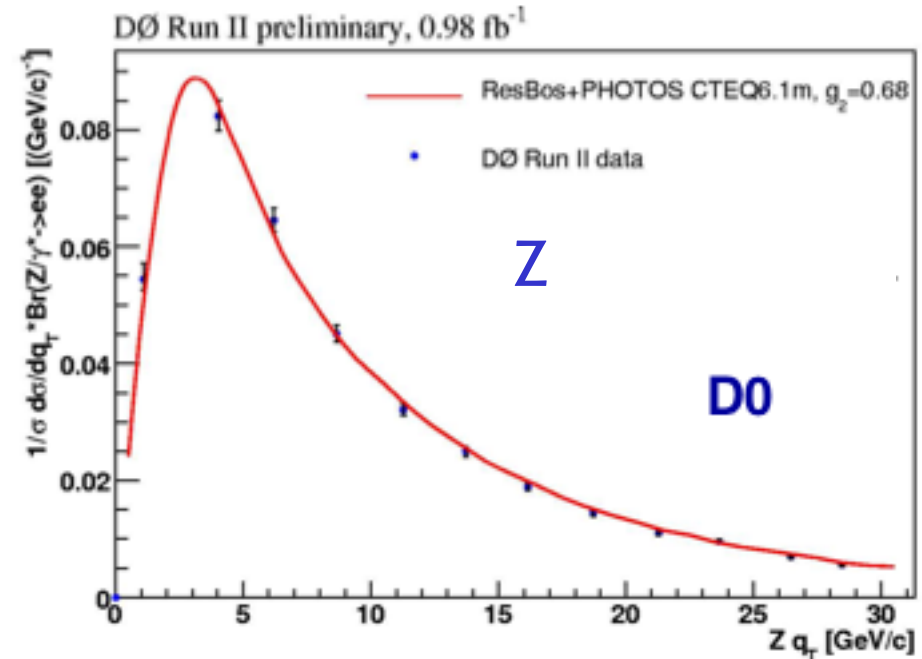
~27 years ago at CERN we computed the W and Z p_T distribution in QCD



GA, K.Ellis, M. Greco, G.Martinelli '84

Here all relevant ingredients were assembled correctly.

⌚ Later only refinements



In agreement with perturbative QCD augmented by Collins-Soper-Sterman (CSS) resummation at low q_T

J. Collins, D. Soper, G. Sterman, Nucl. Phys. B250 (1985) 199.

ResBos describes data well up to ~ 30 GeV

F. Landry, R. Bock, P.Nadolsky, C.P. Yuan
Phys. Rev. D 67, 073016 (2003)

NNLO describes better above 30 GeV

K. Melnikov and F. Petriello Phys. Rev. D74 114017 (2006)

Yesterday the W&Z, today the Higgs!

Bozzi, Catani, De Florian, Grazzini'03-'08

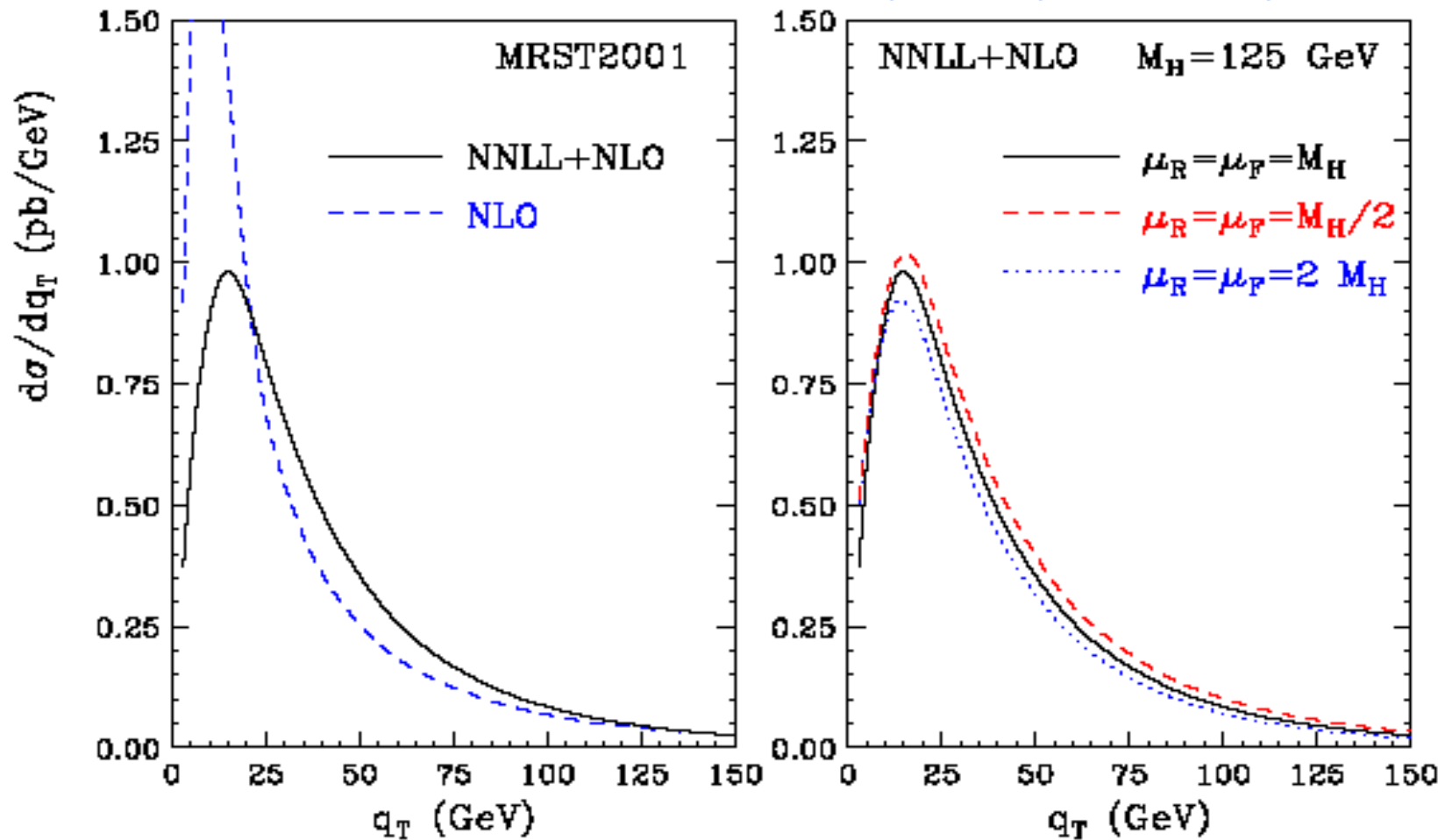


Figure 7. Resummed pQCD prediction for the Higgs transverse momentum distribution at the LHC, from Bozzi *et al.* [25](#)



I leave to the following speakers to describe other aspects of the scientific activity of Mario and also what he did later in QCD

I make to him my best wishes of a long and happy sequel of celebrations for 75, 80, 85,....100 anniversaries

And also I make to him my compliments for the co-foundation of these by now classical meetings in La Thuile

Thank you!

