

# First ADS analysis of $B^- \rightarrow D^0 K^-$ decays in hadron collisions

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# Motivation: CKM $\gamma$ angle measurement



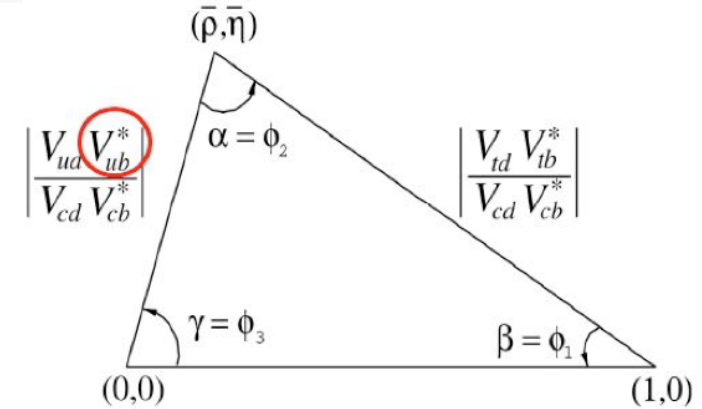
CKM matrix

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + O(\lambda^4)$$

CP violation if  $\eta \neq 0$

$A\lambda^3(\rho - i\eta)$

$b \rightarrow u$  transition  
B meson system





# CKM $\gamma$ angle through $B \rightarrow DK$ decays



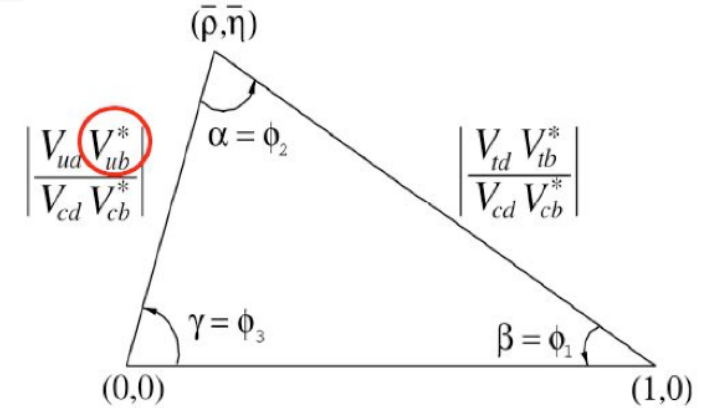
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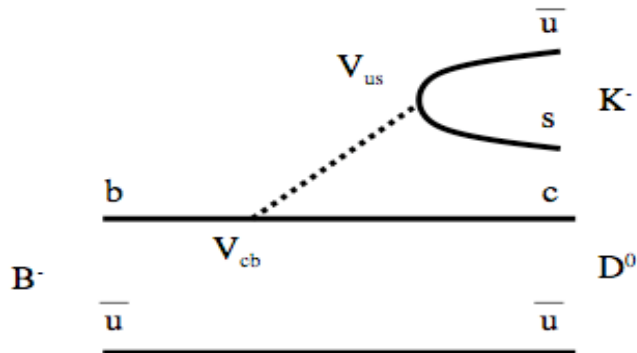


Use of  $B \rightarrow DK$  decays is the cleanest way to measure  $\gamma$ :

- tree-level amplitude only
- tiny theoretical uncertainties

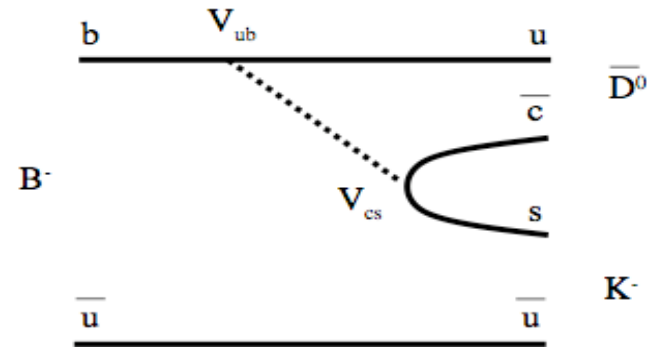
$\gamma$  can be extracted exploiting the **interference** between the processes

$b \rightarrow c \bar{u}s$  ( $B^- \rightarrow D^0 K^-$ ) and  $b \rightarrow u \bar{c}s$  ( $B^- \rightarrow \bar{D}^0 K^-$ ), when  $D^0$  and  $\bar{D}^0$  decay into the **same final state**



Favored  $b \rightarrow c$  transition

$$A_1 \sim V_{cb} V_{us}^* \sim \lambda^3$$

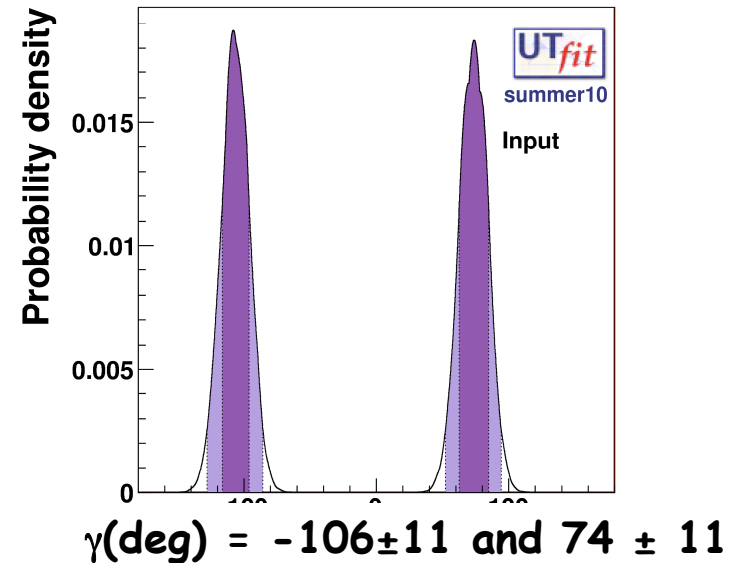
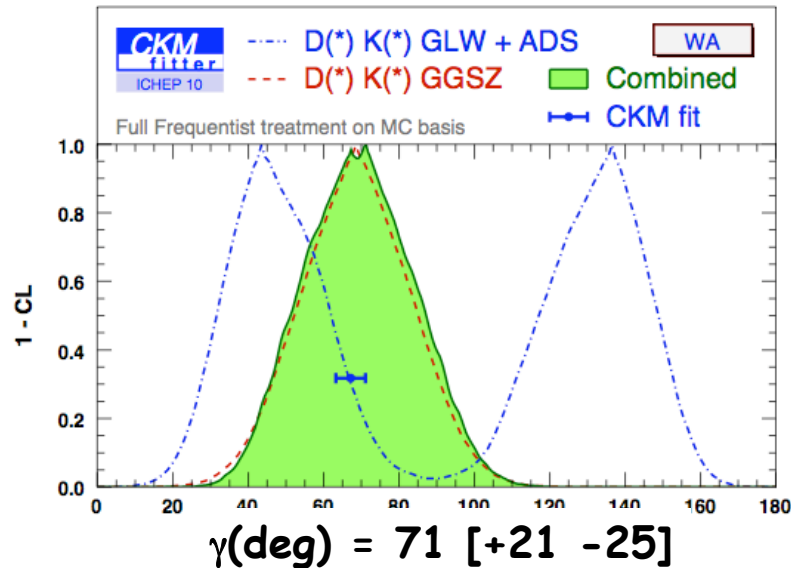


Color suppressed  $b \rightarrow u$  transition 3

$$A_2 \sim V_{ub} V_{cs}^* \sim \lambda^3 r_B e^{-i\delta_B} e^{-i\gamma}$$



# Current situation of $\gamma$ using $B^- \rightarrow D^0 K^-$



$\gamma$  is the least well-known angle of the CKM triangle nowadays

- **GGSZ (Giri-Grossmann-Soffer-Zupan) method** ([PRL78,3257, PRD68,054018])

that uses the  $B^\pm \rightarrow D K^\pm$  decays with the  $D^0$  and  $\bar{D}^0$  reconstructed into three-body final state. For example the  $D^0 \rightarrow K_s^0 \pi^+ \pi^-$

- **GLW (Gronau-London-Wyler) method** ([PLB253,483 PLB265,172])

that uses the  $B^\pm \rightarrow D K^\pm$  decays with  $D_{CP}$  decay modes.  $D_{CP^+} \rightarrow \pi^+ \pi^-, K^+ K^-$  and  $D_{CP^-} \rightarrow K_s^0 \pi^0, K_s^0 \omega, K_s^0 \phi$ .

- **ADS (Atwood-Dunietz-Soni) method** ([PRL78,3257;PRD63,036005])

that uses the  $B^\pm \rightarrow D K^\pm$  decays with D reconstructed in the doubly Cabibbo suppressed

$D_{DCS}^0 \rightarrow K^+ \pi^-$





# ADS method



# ADS Observables



Direct  $CP$  violation in  $B \rightarrow D_{DCS}K$  modes

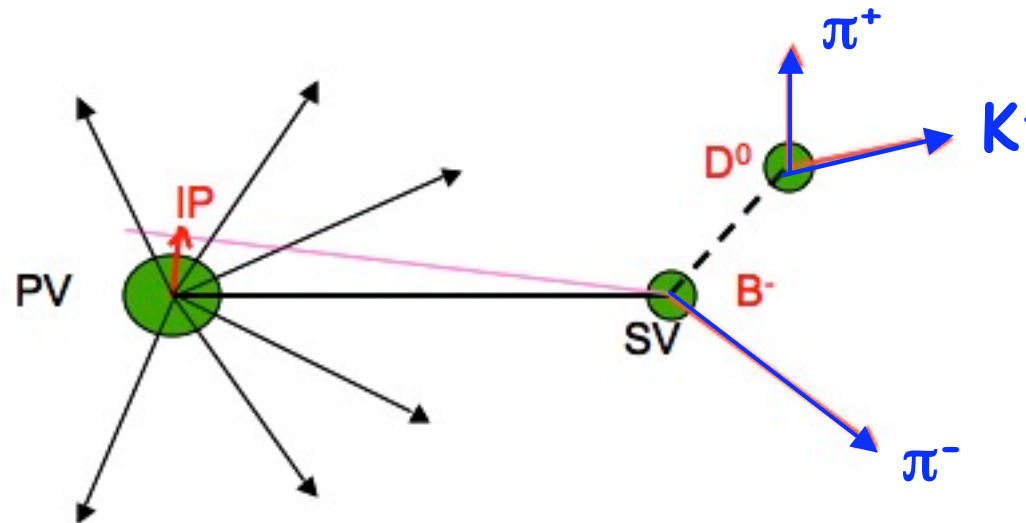
- expected large  $CP$  asymmetry
- decay suppressed by a factor of  $\sim 10^{-3}$  wrt favored
- results have to be combined with other methods to obtain  $\gamma$  measurement

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- expected large CP asymmetry
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We need to reconstruct two final states:

### 1) Cabibbo favored

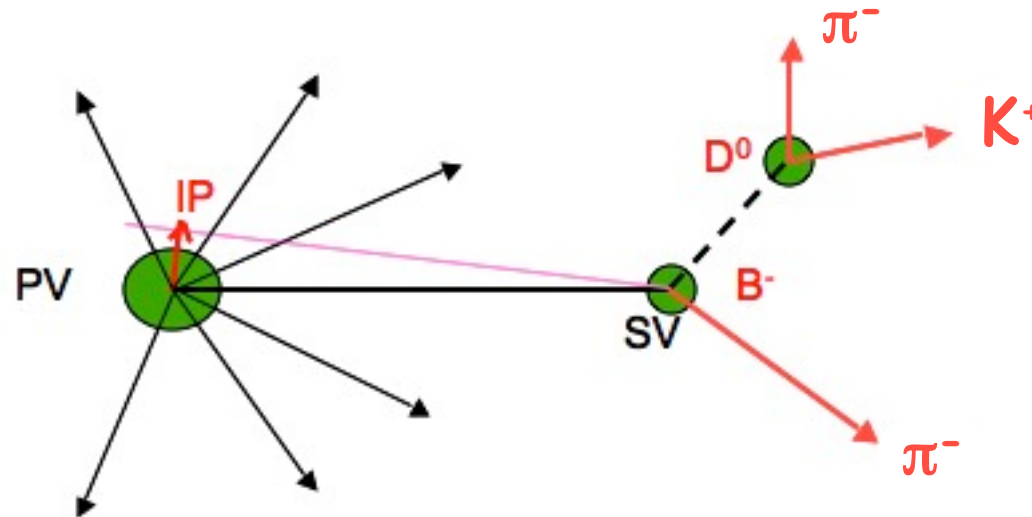


## Direct CP violation in $B \rightarrow D_{DCS}K$ modes

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- decay suppressed by a factor of  $\sim 10^{-3}$  wrt favored
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We need to reconstruct two final states:

**2) Doubly Cabibbo suppressed**





# ADS Observables



## Direct CP violation in $B \rightarrow D_{DCS}K$ modes

- expected large CP asymmetry
- decay suppressed by a factor of  $\sim 10^{-3}$  wrt favored
- results have to be combined with other methods to obtain  $\gamma$  measurement

### Observables

$$R_{ADS}(h) = \frac{N(B^- \rightarrow D_{DCS}^0 h^-) + N(B^+ \rightarrow D_{DCS}^0 h^+)}{N(B^- \rightarrow D_{CF}^0 h^-) + N(B^+ \rightarrow D_{CF}^0 h^+)}$$

$$\mathcal{A}_{ADS}(h) = \frac{N(B^- \rightarrow D_{DCS}^0 h^-) - N(B^+ \rightarrow D_{DCS}^0 h^+)}{N(B^- \rightarrow D_{DCS}^0 h^-) + N(B^+ \rightarrow D_{DCS}^0 h^+)}$$

$h = K$  or  $\pi$

From theory:

$$R_{ADS}(K) = r_D^2 + r_B^2 + 2r_B r_D \cos(\delta_B + \delta_D) \cos\gamma$$

$$\mathcal{A}_{ADS}(K) = 2r_B r_D \sin(\delta_B + \delta_D) \sin\gamma / R_{ADS}(K)$$



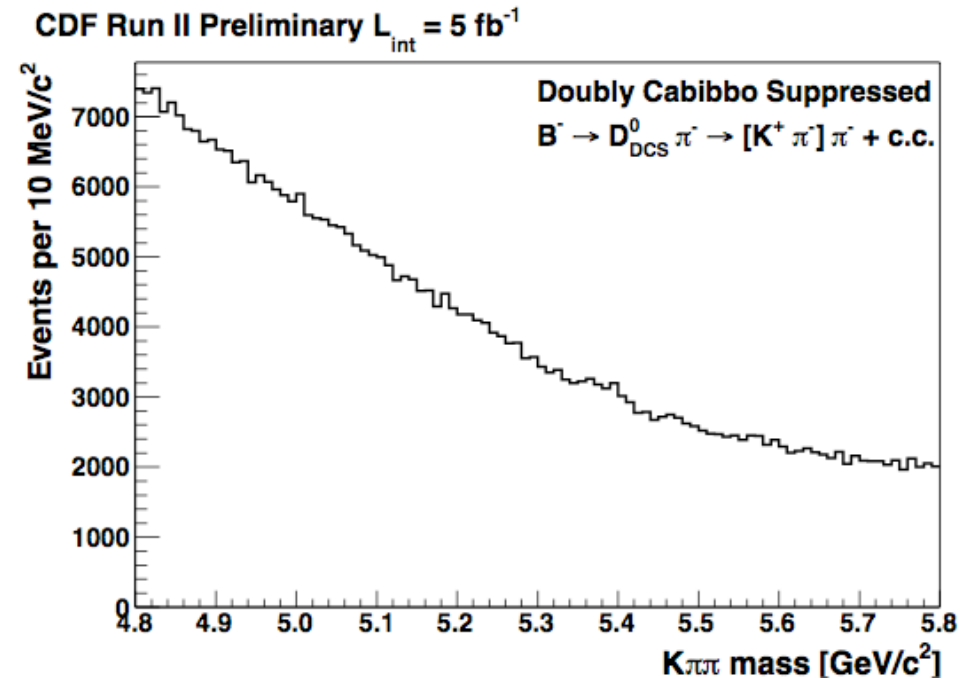
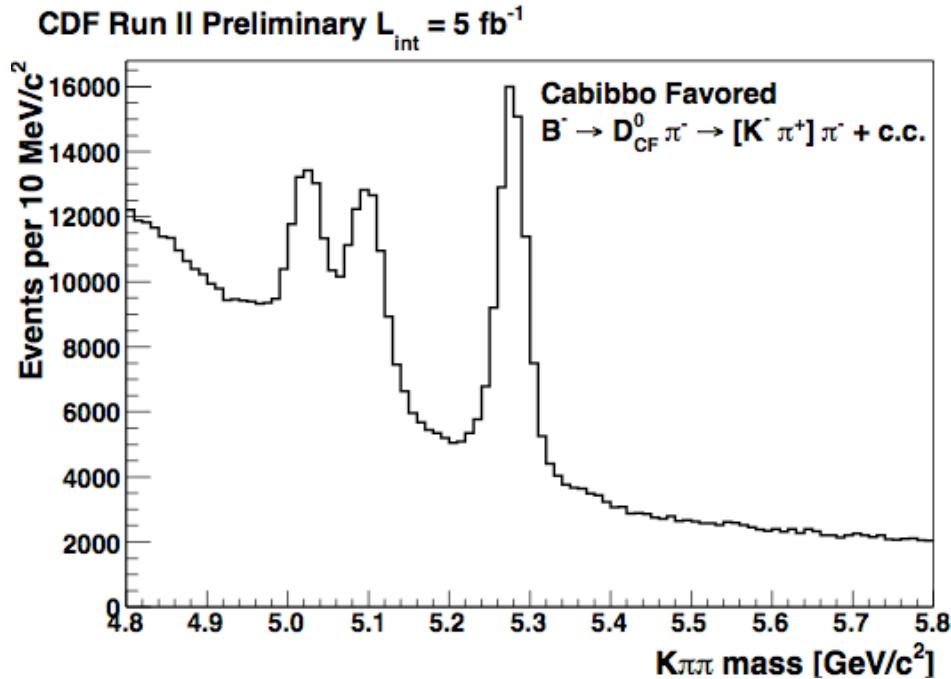
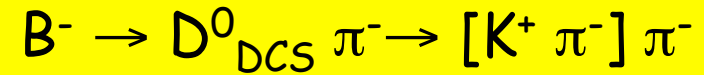
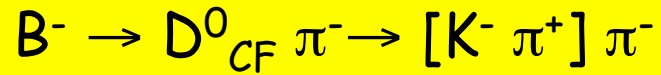


# ADS method at CDF

First measurement of  $A_{ADS}$  and  $R_{ADS}$   
at a hadron collider



# CF and DCS samples ( $L = 5\text{fb}^{-1}$ )



Cuts optimization



Crucial step toward the DCS modes

- We directly used the CF sample (not MC) selecting the signal (S) in  $\pm 2\sigma$  of  $B \rightarrow D\pi$  peak and the background (B) in [5.4,5.8] range

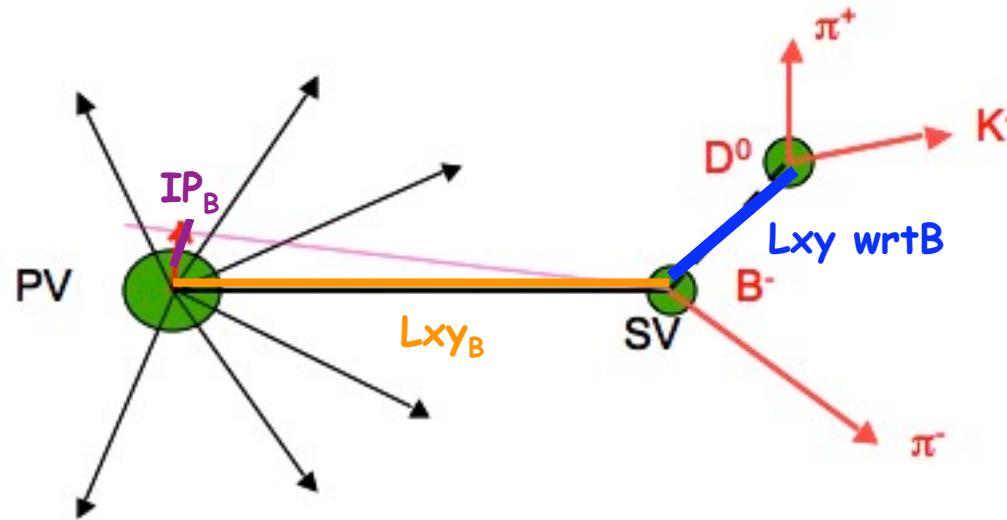
- We maximized the quantity  $\frac{S}{1.5 + \sqrt{B}}$

(arXiv:0808063v2)

## $D^0$ candidate

Cuts on:

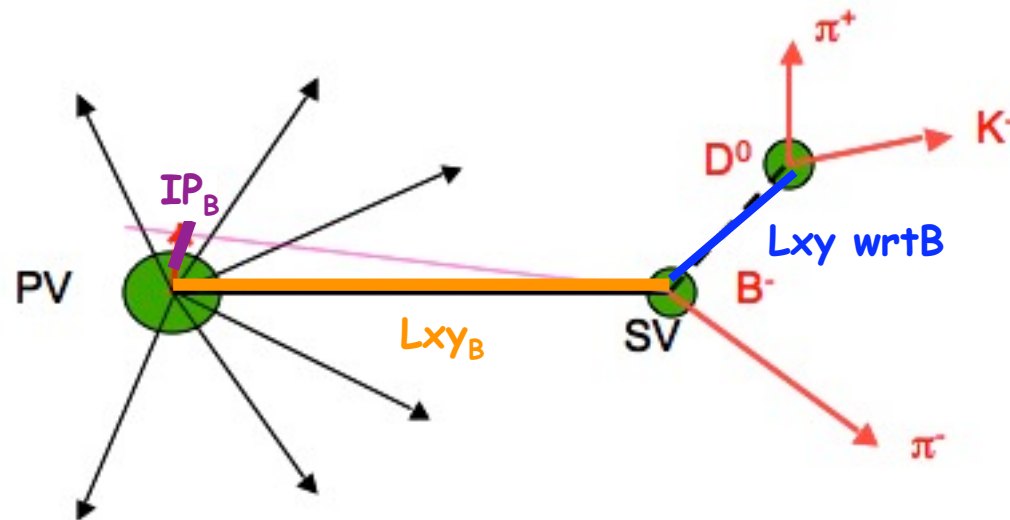
- the invariant mass
- angular distribution
- the **decay length wrt B** to remove  $B \rightarrow 3$  body decays
- **particle identification** of tracks from  $D^0$  to remove  $D^0 \rightarrow \pi\pi$  events



B candidate

Cuts on:

- decay length wrt primary vertex
- impact parameter
- angle between momentum and decay length



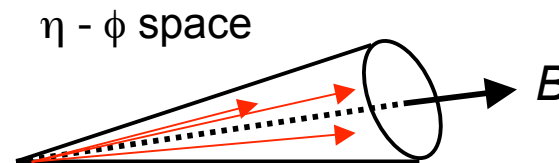
## B candidate

Cuts on:

- decay length wrt primary vertex
- impact parameter
- angle between momentum and decay length

• **isolation**

$$I(B) = \frac{p_T(B)}{p_T(B) + \sum_i p_T(i)}$$



- **3D vertex quality**, obtained with the 3D silicon-tracking, to:
  - resolve multiple vertices along the beam direction
  - reject fake tracks.

Backg. reduces x2, small inefficiency on signal (<10%).





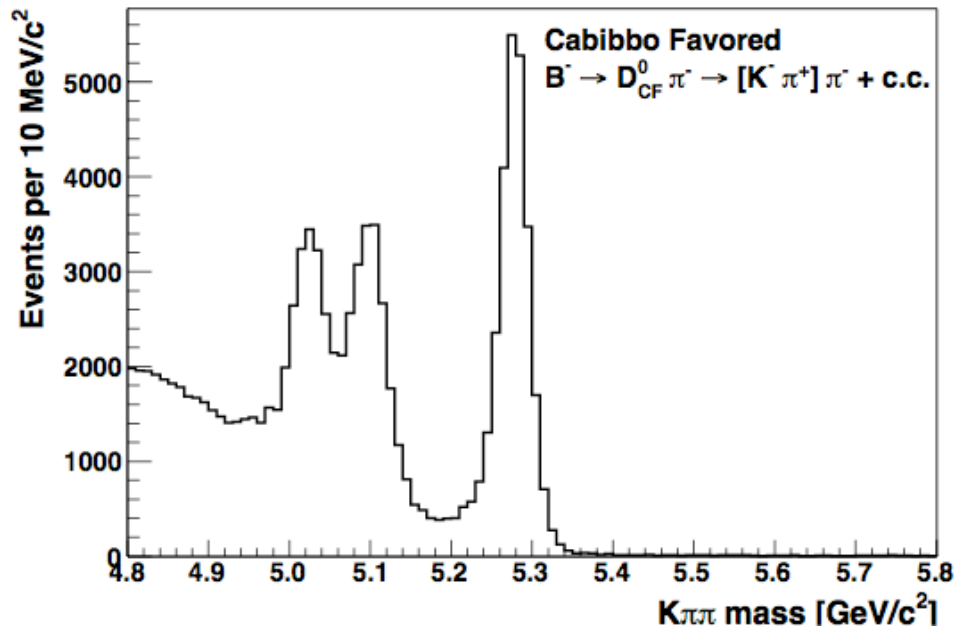
# CF and DCS after cut optimization



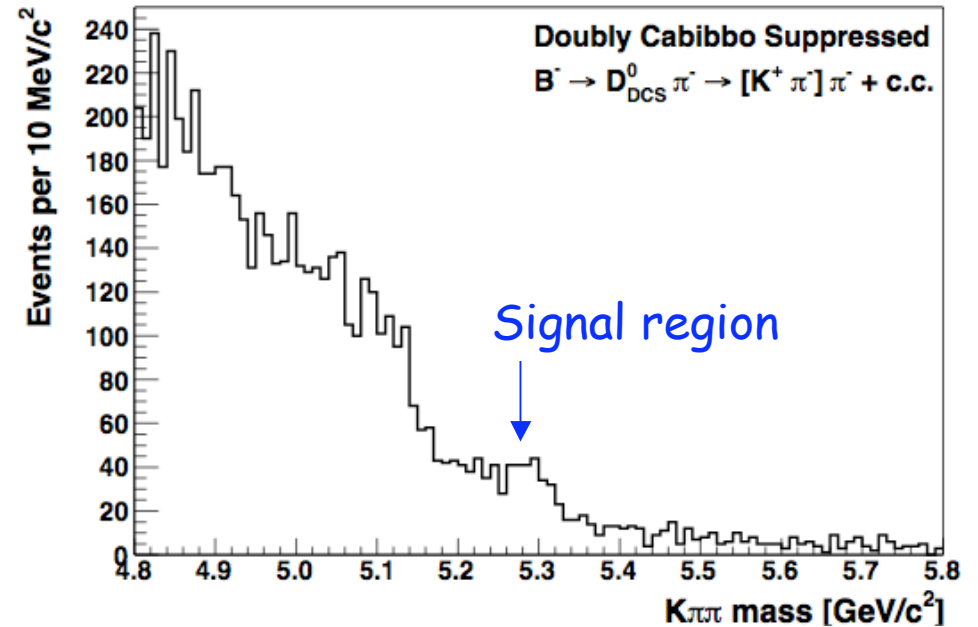
$$B^- \rightarrow D_{CF}^0 \pi^- \rightarrow [K^- \pi^+] \pi^-$$

$$B^- \rightarrow D_{DCS}^0 \pi^- \rightarrow [K^+ \pi^-] \pi^-$$

CDF Run II Preliminary  $L_{int} = 5 \text{ fb}^{-1}$



CDF Run II Preliminary  $L_{int} = 5 \text{ fb}^{-1}$



## Fit procedure

Use of an *unbinned maximum likelihood fit* (combined on CF and DCS modes) to separate signals contribution using:

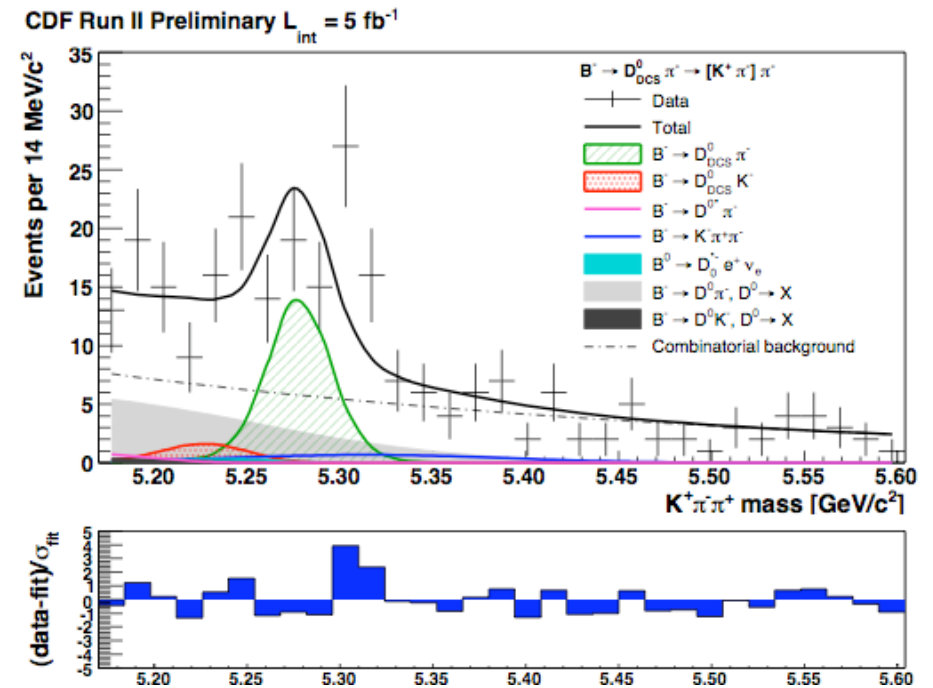
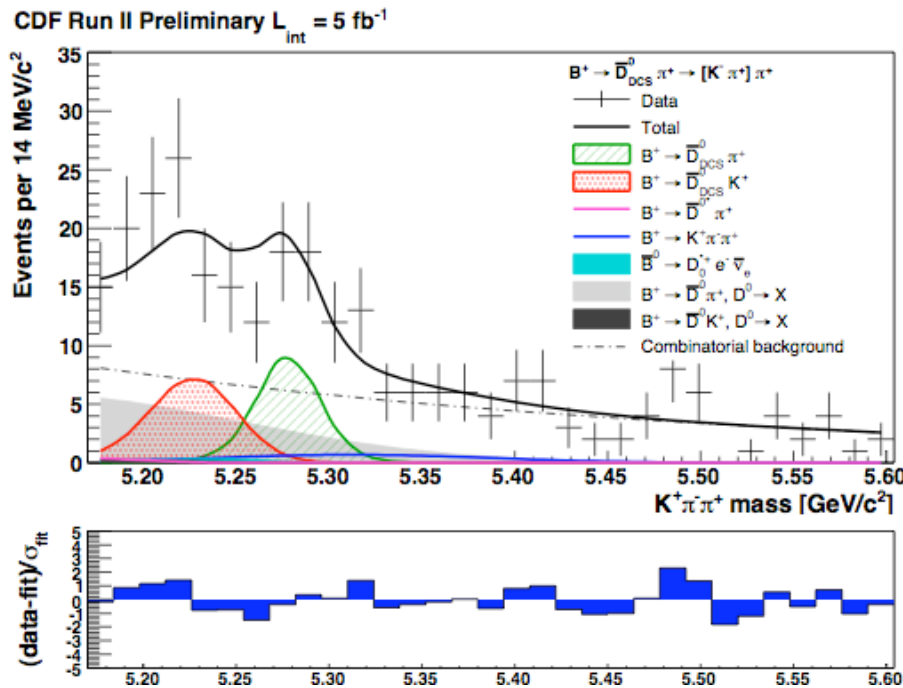
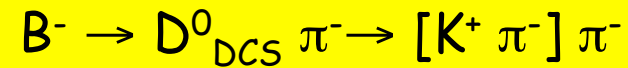
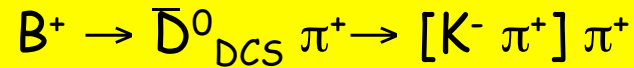
- mass information
- particle identification (dE/dx with K- $\pi$  separation:  $1.5 \sigma$  for  $p > 2 \text{ GeV}/c$ )



# Results: DCS reconstruction



First reconstruction of DCS signals at a hadron collider.



Yield ( $B \rightarrow D_{DCS} K$ ) =  $34 \pm 14$  ( $5 \text{ fb}^{-1}$ )  
 Yield ( $B \rightarrow D_{DCS} \pi$ ) =  $73 \pm 16$  ( $5 \text{ fb}^{-1}$ )

Significance for all DCS signals ( $D_{DCS} \pi + D_{DCS} K$ )  $> 5 \sigma$



# Results: the observables



First measurement of  
 $A_{ADS}$  and  $R_{ADS}$  at a  
hadron collider.

$$R_{ADS}(\pi) = 0.0041 \pm 0.0008(stat) \pm 0.0004(syst)$$

$$A_{ADS}(\pi) = 0.22 \pm 0.18(stat) \pm 0.06(syst)$$

$$R_{ADS}(K) = 0.0225 \pm 0.0084(stat) \pm 0.0079(syst)$$

$$A_{ADS}(K) = -0.63 \pm 0.40(stat) \pm 0.23(syst)$$

(CDF public note 10309)



# Results: the observables



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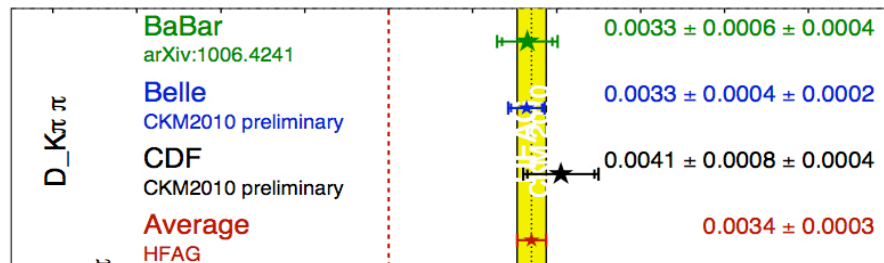
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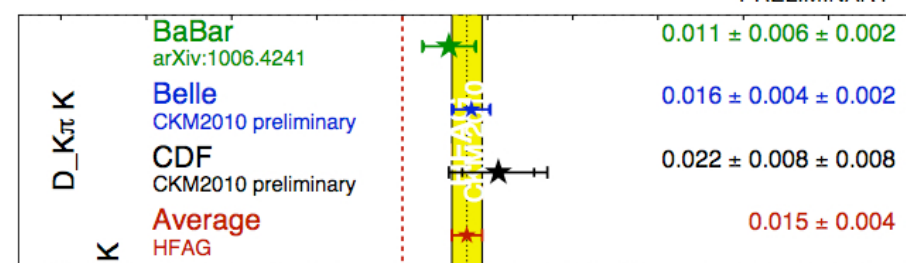
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The results are in agreement and compatible with B-factories

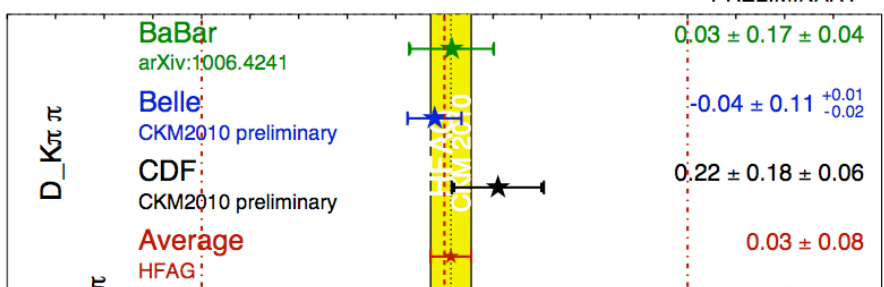
## $B \rightarrow D\pi$ $R_{ADS}$ Averages



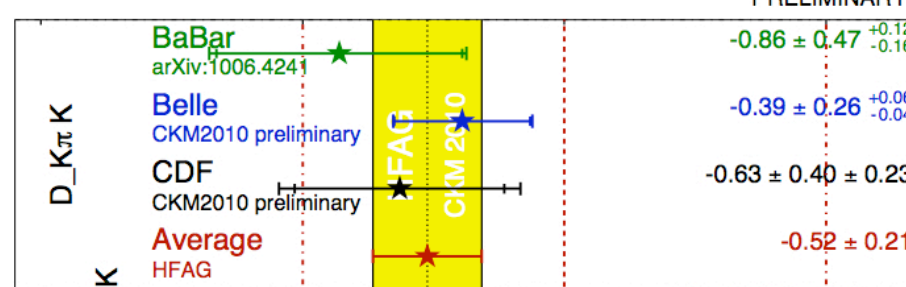
## $B \rightarrow DK$ $R_{ADS}$ Averages



## $B \rightarrow D\pi$ $A_{ADS}$ Averages



## $B \rightarrow DK$ $A_{ADS}$ Averages





# ADS update to $7\text{fb}^{-1}$



- Work in progress to update the ADS analysis up to  $7\text{fb}^{-1}$
- We already find **evidence of signals**:
  - $B \rightarrow DK$  ( $3.2\sigma$  including systematics)
  - $B \rightarrow D\pi$  ( $3.6\sigma$ )
- Exclusion of a value of  $A_{\text{ADS}}(K)$  equal to zero at a level of 95% ( $2\sigma$ ).
- Ongoing: finalization of the results.







# CDF program on $\gamma$



The ADS measurement belongs to a *broader program of CDF for measuring  $\gamma$  from trees.*

Recently published the **GLW** measurement using  $1 \text{ fb}^{-1}$  of data  
(*Phys.Rev.D81:031105,2010*)

## The GLW method

- Direct CP violation in  $B \rightarrow D_{CP} K$  modes  
( $D_{CP+} \rightarrow \pi^+ \pi^-, K^+ K^-$  and  $D_{CP-} \rightarrow K_s^0 \pi^0, K_s^0 \omega, K_s^0 \phi.$ )
- very clean method
- small asymmetry, sensitivity to  $\gamma$  proportional to  $r_B$

## The observables

$$R_{CP\pm} = \frac{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}{[\Gamma(B^- \rightarrow D^0 K^-) + \Gamma(B^+ \rightarrow D^0 K^+)]/2}$$

$$A_{CP\pm} = \frac{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) - \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}$$

From theory:

$$R_{CP\pm} = 1 + r_B^2 \pm 2r_B \cos\delta_B \cos\gamma$$

$$A_{CP\pm} = 2r_B \sin\delta_B \sin\gamma / R_{CP\pm}$$

**3 independent equations**

$$(A_{CP+} R_{CP+} = -A_{CP-} R_{CP-})_{20}$$

and **3 unknowns** ( $r_B, \gamma, \delta_B$ )



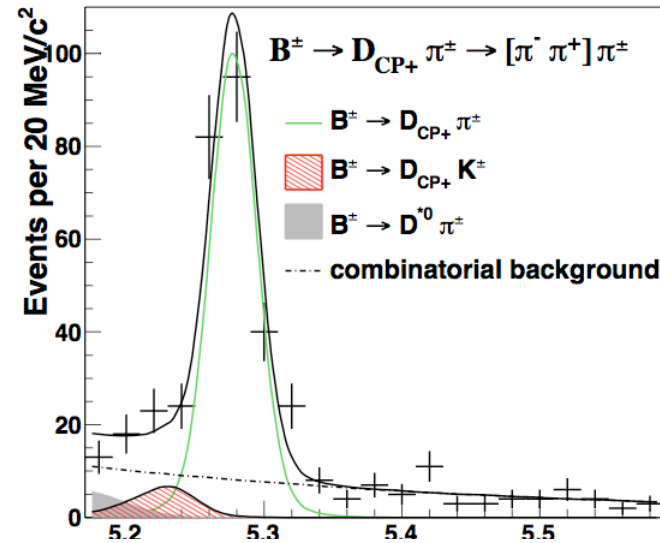
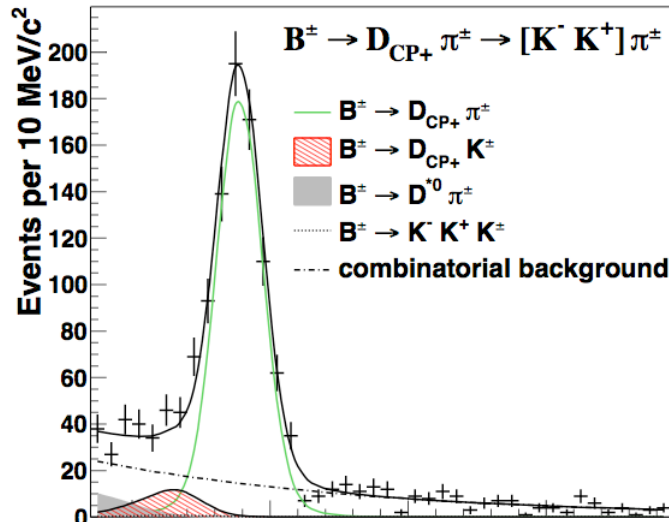
# CP+ modes results



D mode  $B^+ \rightarrow D\pi^+$   $B^- \rightarrow D\pi^-$   $B^+ \rightarrow DK^+$   $B^- \rightarrow DK^-$

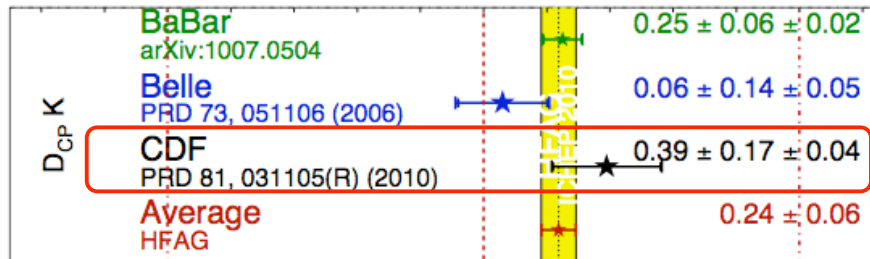
$K^-\pi^+$	$3769 \pm 68$	$3763 \pm 68$	$250 \pm 26$	$266 \pm 27$
$K^+K^-$	$381 \pm 25$	$399 \pm 26$	$22 \pm 8$	$49 \pm 11$
$\pi^+\pi^-$	$101 \pm 13$	$117 \pm 14$	$6 \pm 6$	$14 \pm 6$

Yield ( $B \rightarrow D_{CP+}K$ )  $\sim 90$  ( $1 \text{ fb}^{-1}$ )



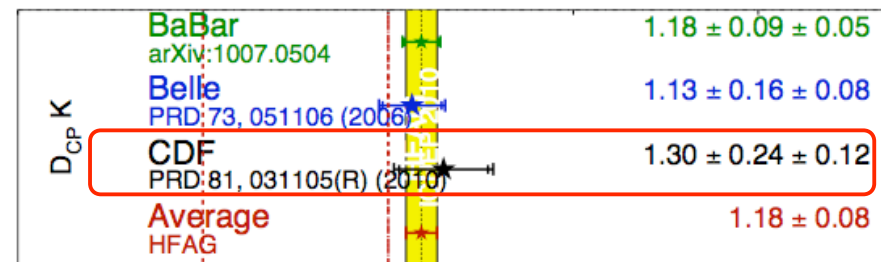
## $B \rightarrow DK$ $A_{CP+}$ Averages

**HFAG**  
ICHEP 2010  
PRELIMINARY



## $B \rightarrow DK$ $R_{CP+}$ Averages

**HFAG**  
ICHEP 2010  
PRELIMINARY





# Conclusions



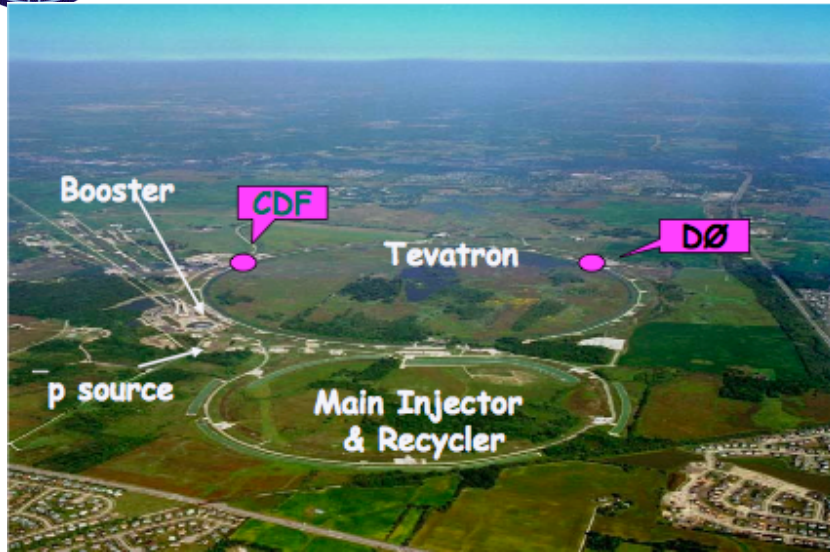
- CDF performed:
  - first measurement of  $A_{ADS}$  and  $R_{ADS}$  at a hadron collider using  $5 \text{ fb}^{-1}$ .
    - Significance of DCS signals ( $D_{DCS} \pi + D_{DCS} K$ )  $> 5\sigma$
  - update up to  $7 \text{ fb}^{-1}$ .
    - Evidence of  $D_{DCS} \pi$  and  $D_{DCS} K$
    - $A_{ADS}(K)$  at  $2\sigma$  different from zero
  - first measurement of  $A_{CP+}$  and  $R_{CP+}$  at a hadron collider using  $1 \text{ fb}^{-1}$ .
- Not only demonstrated the capability of hadron collider with B to charm decays, but we even get competitive results with B-factories



# BACK-UP

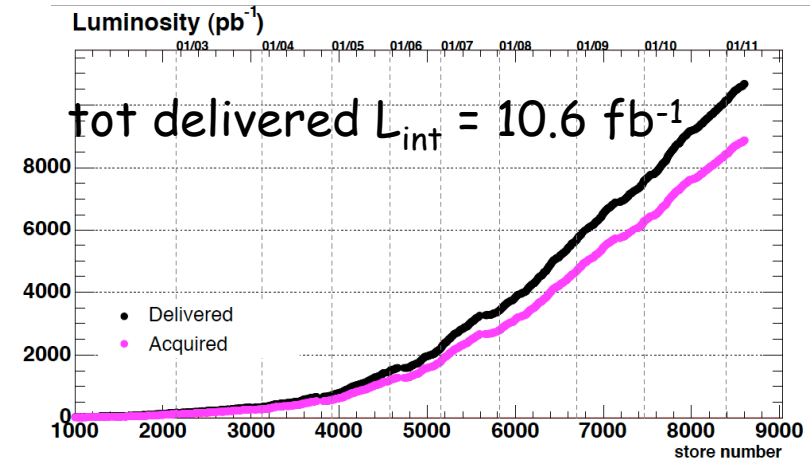


# The Tevatron



Good performances on Run II:

- peak  $L_{inst} = 3.5-4 \cdot 10^{32} \text{cm}^{-2}\text{s}^{-1}$
- delivering  $2.5 \text{fb}^{-1}/\text{year}$



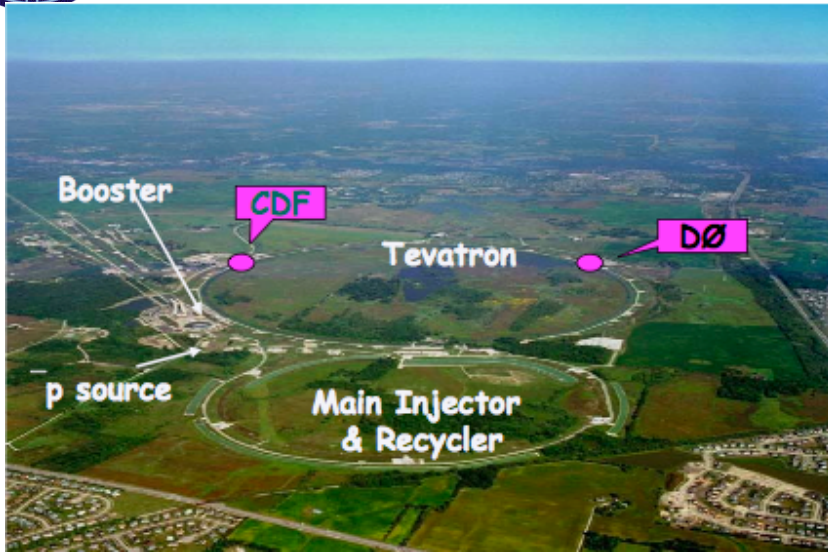
Tevatron is great for rare B decay searches:

- **Large  $b$  production cross section**  
(x1000 times larger than  $e^+e^-$  B factories)
- **All B species** are produced ( $B^0, B^+, B_s, \Lambda_b \dots$ )



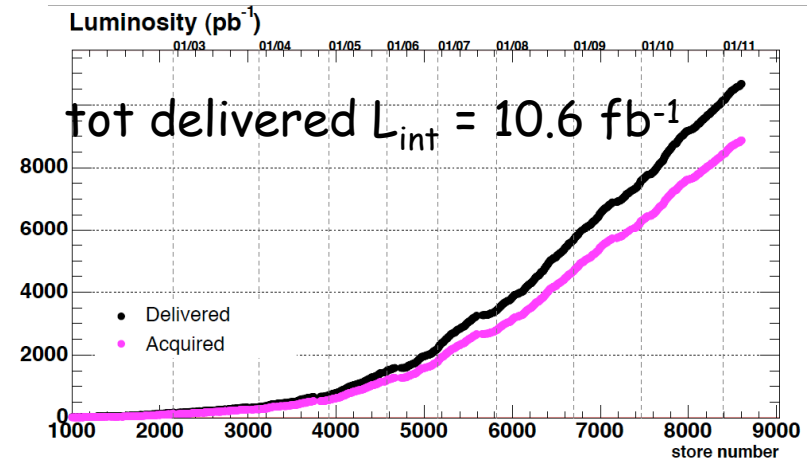


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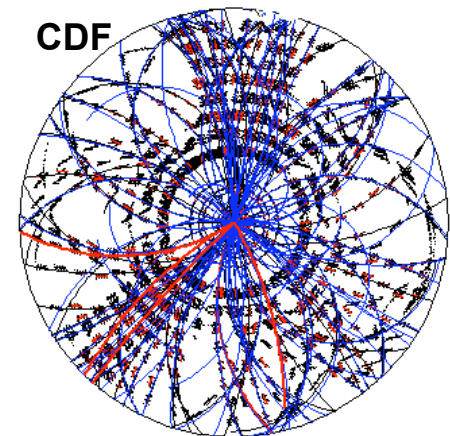
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(x1000 times larger than  $e^+e^-$  B factories)
- **All B species** are produced ( $B^0, B^+, B_s, \Lambda_b \dots$ )

**But:**

- The **total inelastic x-section** is a factor  $10^3$  larger than  $\sigma(b\bar{b})$
- The **BRs** of rare b-hadron decays are  $O(10^{-6})$  or lower

Interesting events must be extracted from a high track multiplicity environment



**Detectors need to have:**

- Very good tracking and vertex resolution and highly selective trigger



# The CDF II detector



## TRACKING system:

- **DRIFT CHAMBER**

96 layers ( $|\eta| < 1$ )

→  $1.5\sigma$   $\pi/K$  separation by  $dE/dx$

- **SILICON TRACKER**

7 layers (1.5-22cm from beam pipe)

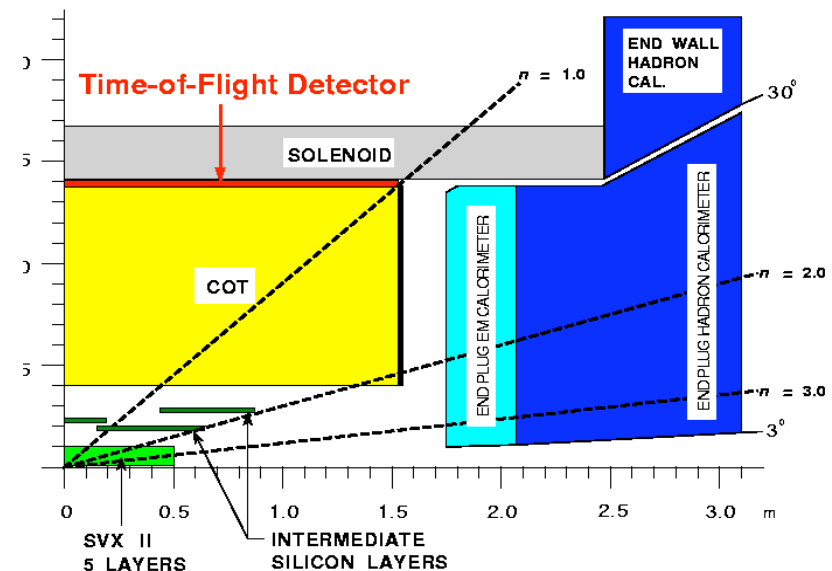
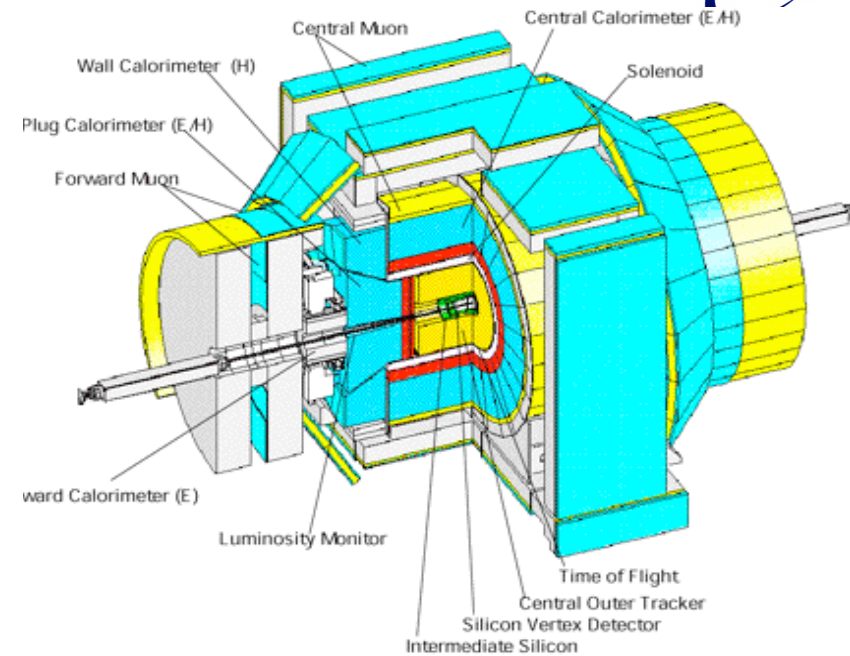
→ I.P. resolution  $35 \mu\text{m}$  at  $2 \text{ GeV}$

→  $\sigma(p_T)/p_T^2 \sim 0.015\%$  ( $c/\text{GeV}$ )

## TRACKING TRIGGER system:

- **Chamber track processor at L1,**  
2D tracks in COT,  $p_T > 1.5 \text{ GeV}$

- **Silicon Vertex Trigger at L2,**  
2D tracks  $p_T > 2 \text{ GeV}$ ,  
Impact Parameter measurement (trigger  
on events containing long lived particles)





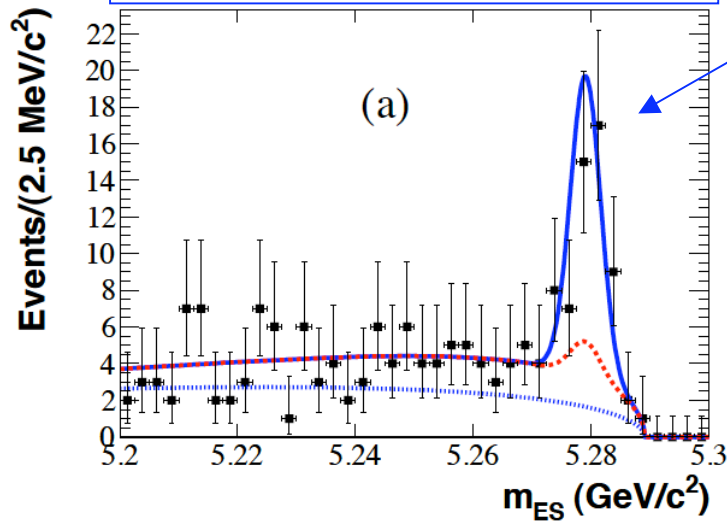
# B → DK at b-factories



## BaBar ADS result (467M BB)

(arXiv:1006.4241, accepted by Phys. Rev. D (September 2010))

B → D<sub>DCS</sub>π reconstruction



~ 80 B → D<sub>DCS</sub>π events

$$\mathcal{R}_{D\pi} = (3.3 \pm 0.6 \pm 0.4) \times 10^{-3}$$

$$\mathcal{A}_{D\pi} = 0.03 \pm 0.17 \pm 0.04$$

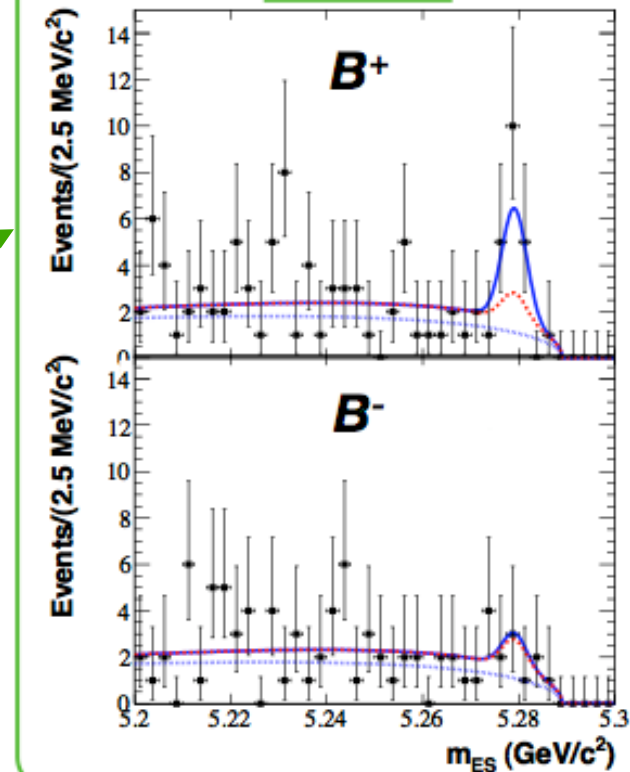
B → D<sub>DCS</sub>K reconstruction

$$\mathcal{R}_{DK} = (1.1 \pm 0.6 \pm 0.2) \times 10^{-2}$$

$$\mathcal{A}_{DK} = -0.86 \pm 0.47 \begin{matrix} +0.12 \\ -0.16 \end{matrix}$$

~ 20 B → D<sub>DCS</sub>K events,  
with a significance of ~2σ

B → DK



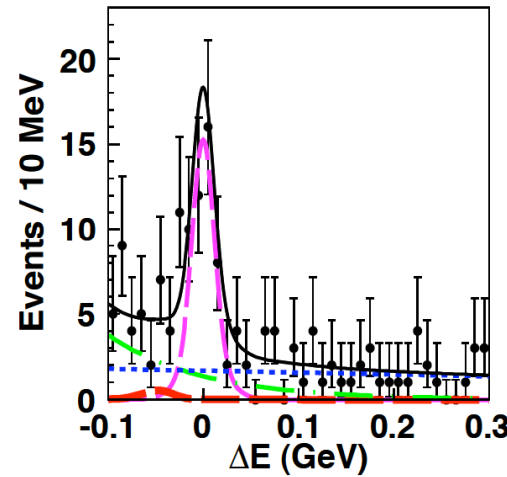
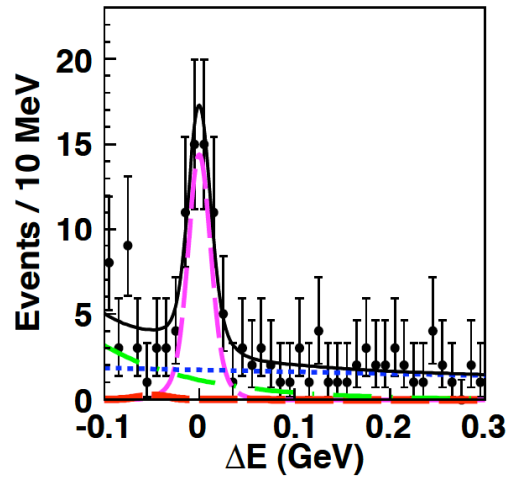


# B → DK at b-factories



## Belle ADS result (772M B $\bar{B}$ )

(arXiv:1103.5951v1, submitted to PRL (March 2011))



B → D<sub>DCS</sub>π reconstruction

~ 165 B → D<sub>DCS</sub>π events

$$\mathcal{R}_{D\pi} = [3.28_{-0.36}^{+0.38}(\text{stat})_{-0.18}^{+0.12}(\text{syst})] \times 10^{-3}$$

$$\mathcal{A}_{D\pi} = -0.04 \pm 0.11(\text{stat})_{-0.01}^{+0.02}(\text{syst})$$

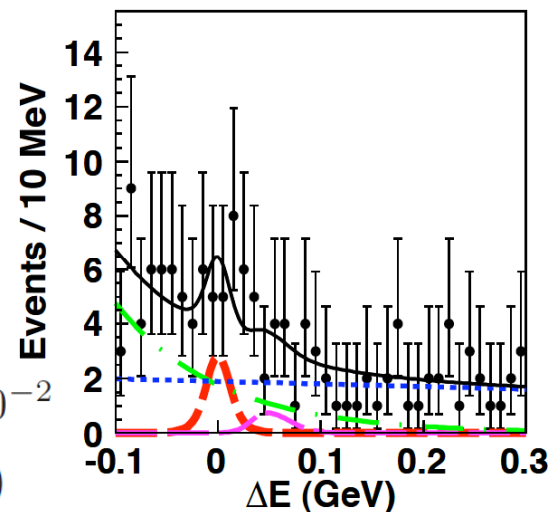
B → D<sub>DCS</sub>K reconstruction

~ 56 B → D<sub>DCS</sub>K events,  
Evidence of B → D<sub>DCS</sub>K,  
with a significance of 4.1σ

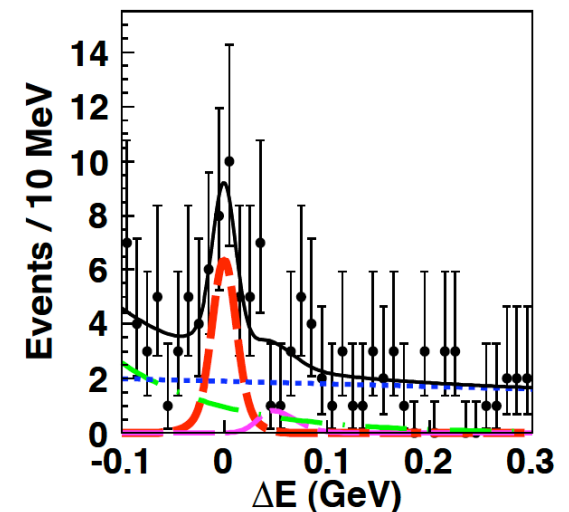
$$\mathcal{R}_{DK} = [1.63_{-0.41}^{+0.44}(\text{stat})_{-0.13}^{+0.07}(\text{syst})] \times 10^{-2}$$

$$\mathcal{A}_{DK} = -0.39_{-0.28}^{+0.26}(\text{stat})_{-0.03}^{+0.04}(\text{syst})$$

DK<sup>-</sup>



DK<sup>+</sup>



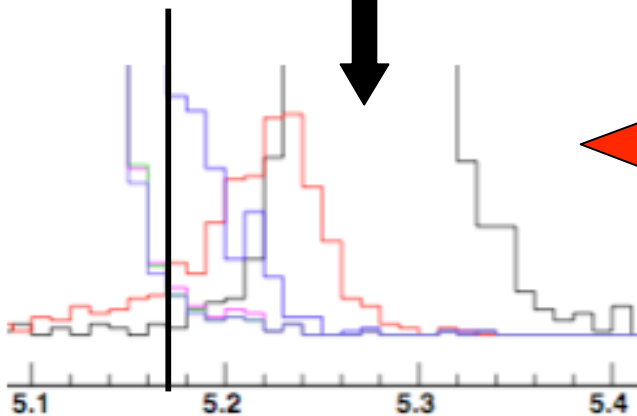
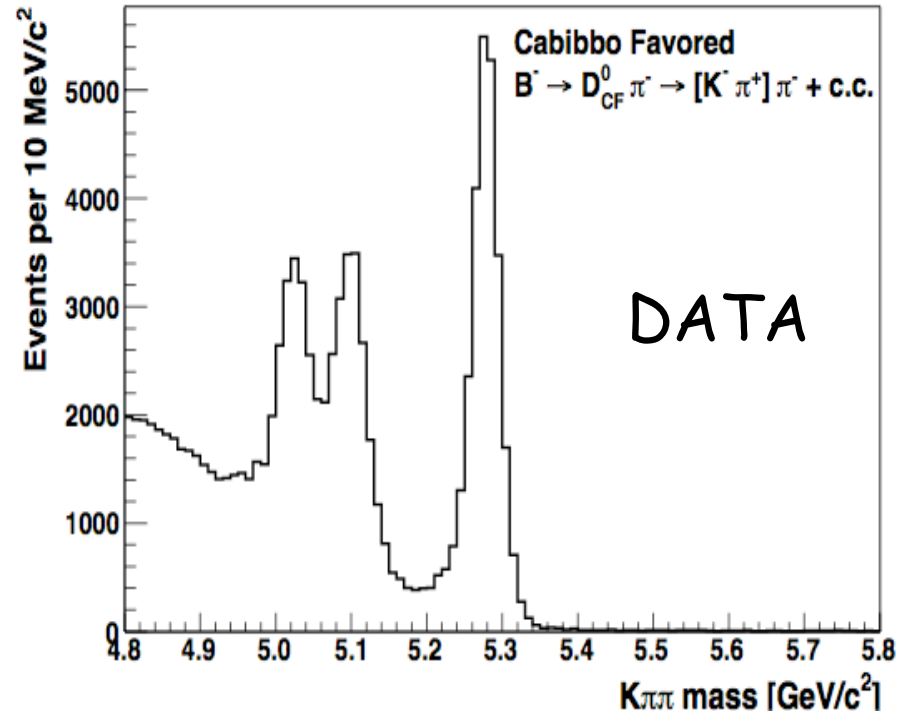
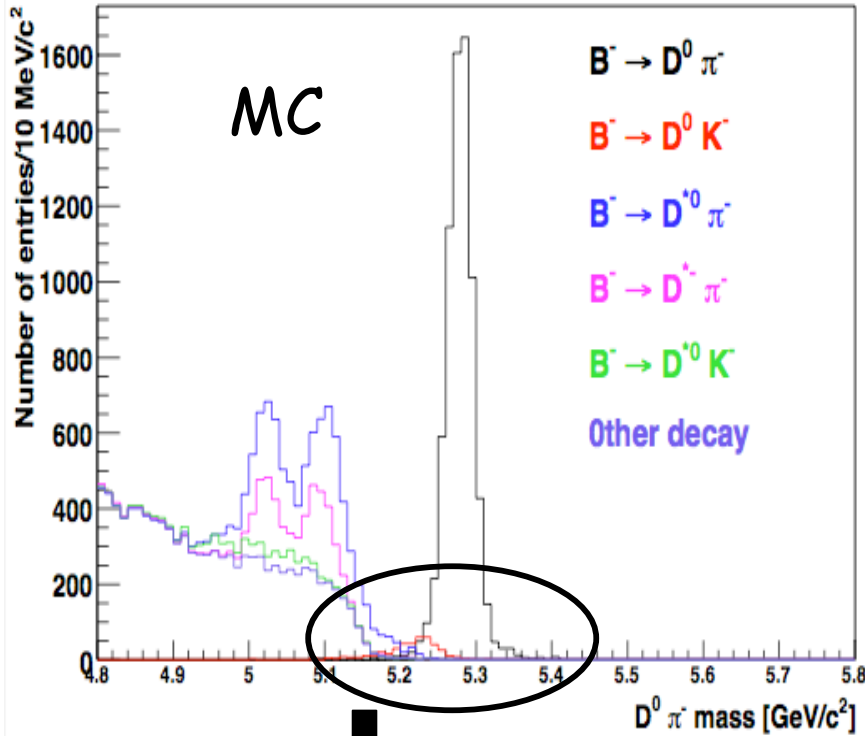


# Separating DK from other modes



CDF Run II MC

$$B^- \rightarrow D_{CF}^0 \pi^- \rightarrow [K^- \pi^+] \pi^- \quad y L_{int} = 5 \text{ fb}^{-1}$$



To reject most of the physical backgrounds, narrow fit windows [5.17, 6.5]

The only significant physics backgrounds are  $B^- \rightarrow D^0 \pi^-$  and  $B^- \rightarrow D^{*0} \pi^-$





# Fit procedure



Use of an **unbinned maximum likelihood fit** (combined on CF and DCS modes) to separate signals contribution.

$$\mathcal{L} = \prod_k^{N_{events}} [f_{sig} \mathcal{F}_{sig} + (1 - f_{sig}) \cdot \mathcal{F}_{back}]$$

$\mathcal{F}_{sig}$  = sum of  $B^- \rightarrow D^0 \pi^-$ ,  $B^- \rightarrow D^{*0} \pi^-$  and  $B^- \rightarrow D^0 K^-$  likelihood

$\mathcal{F}_{back}$  = sum of combinatorial and physics background likelihood

We used:

- mass information
- particle identification (dE/dx with K- $\pi$  separation:  $1.5 \sigma$  for  $p > 2 \text{ GeV}/c$ )

Common parameters between CF and DCS:

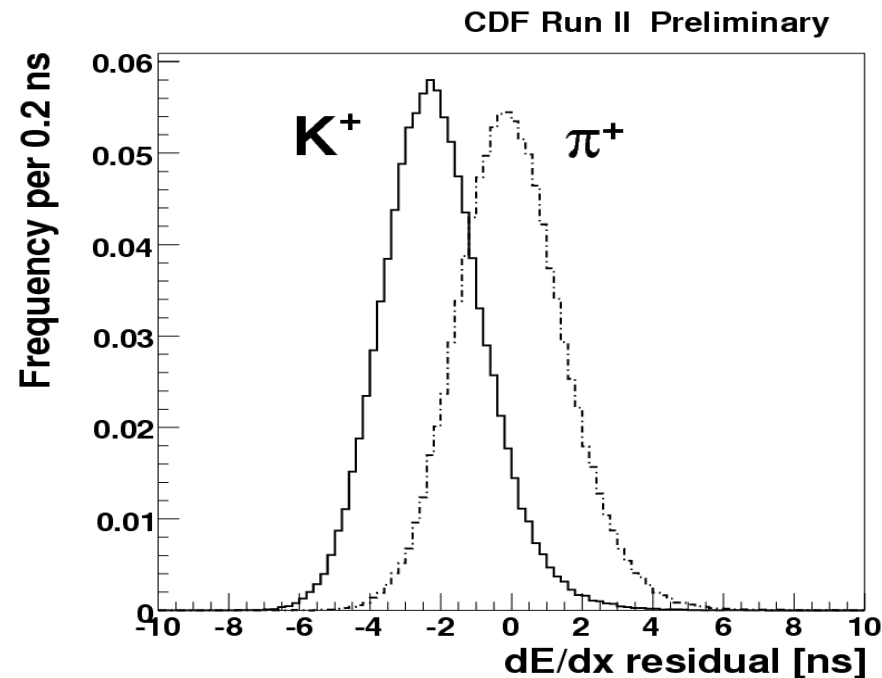
- ratio between  $N(B^- \rightarrow D^{*0} \pi^-) / N(B^- \rightarrow D^0 \pi^-)$
- combinatorial background pdf



# Separation by Particle ID



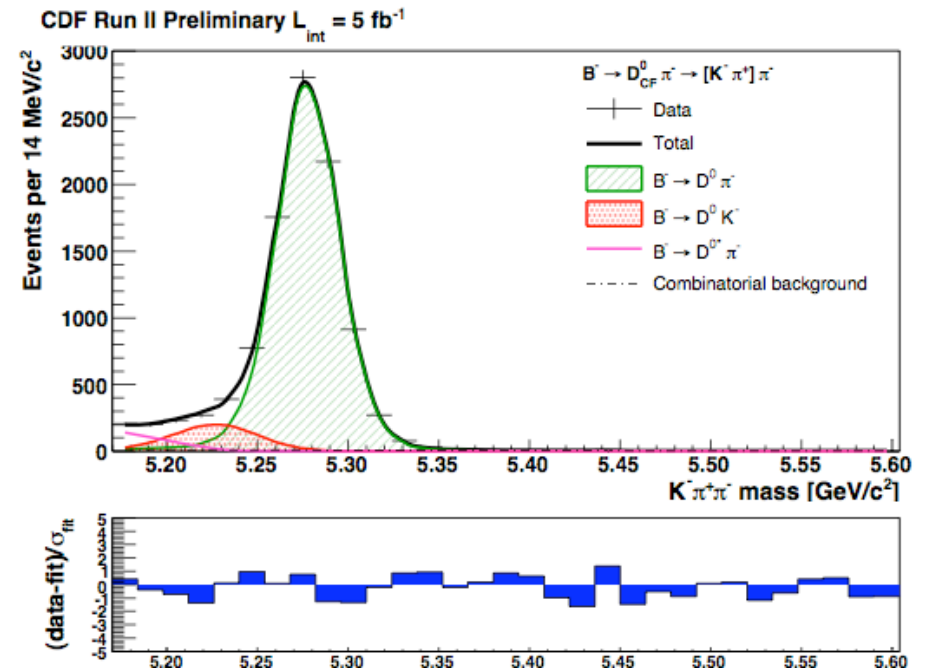
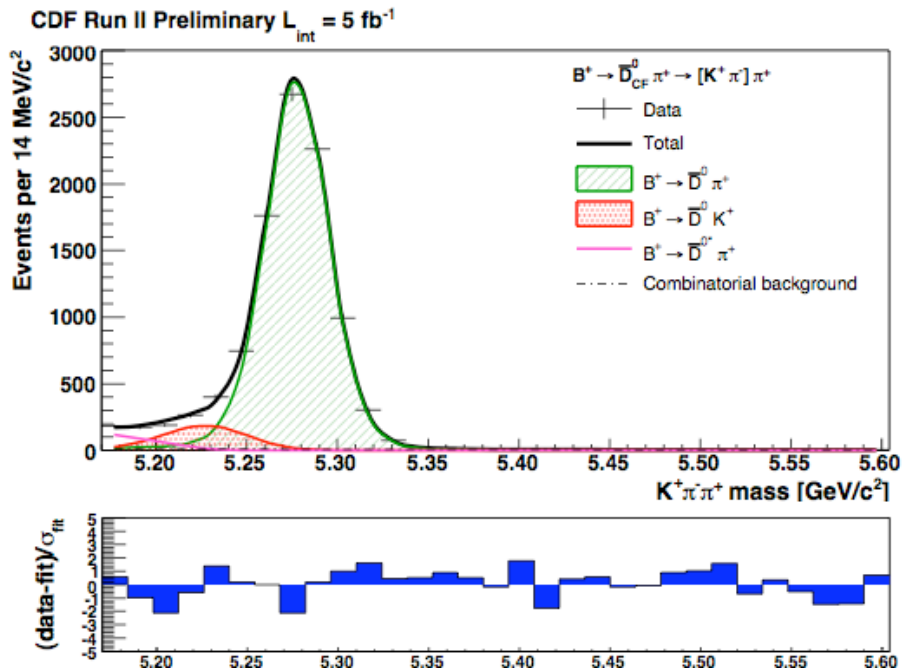
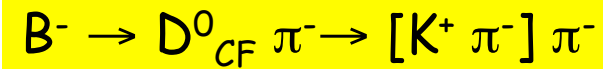
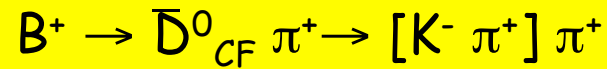
Implementation of a Likelihood FIT using **masses** and **particle identification** (dE/dx) information to determine the signal composition



**K -  $\pi$  separation:  $1.5 \sigma$  for  $p > 2 \text{ GeV}/c$**



# Results: CF reconstruction



Yield ( $B \rightarrow D_{CF} K$ ) =  $1513 \pm 68$  ( $5 \text{ fb}^{-1}$ )  
Yield ( $B \rightarrow D_{CF} \pi$ ) =  $17677 \pm 146$  ( $5 \text{ fb}^{-1}$ )





# Results: physics background



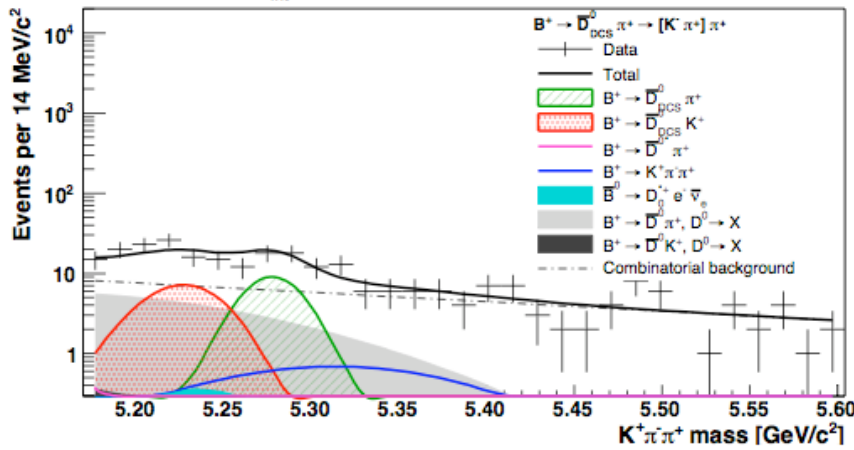
Physics background for DCS:

Decay	Yield
$B^- \rightarrow D^{0*} \pi^-, D^{0*} \rightarrow D^0 \gamma / \pi^0$	$3 \pm 3$
$B^- \rightarrow D^0 \pi^-, D^0 \rightarrow X$	$90 \pm 13$
$B^- \rightarrow D^0 K^-, D^0 \rightarrow X$	$4 \pm 3$
$B^- \rightarrow K^- \pi^+ \pi^-$	$18 \pm 4$
$B^0 \rightarrow D_0^{*-} e^+ \nu_e$	$4 \pm 3$

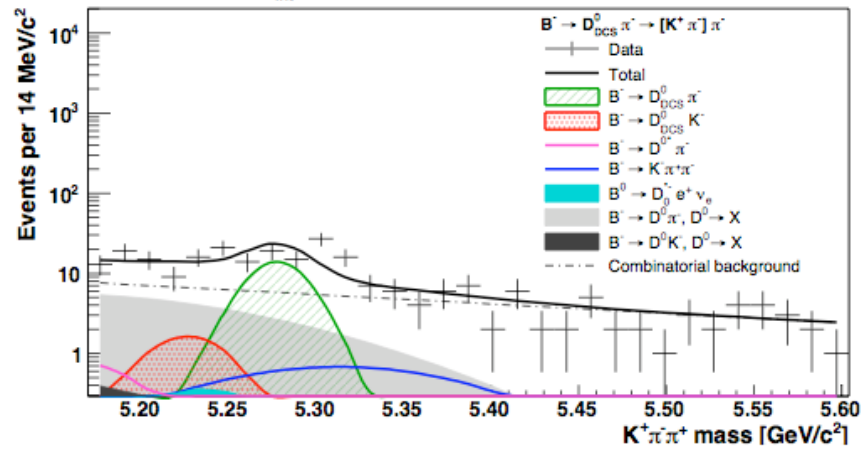
$$B^+ \rightarrow \bar{D}_{DCS}^0 \pi^+ \rightarrow [K^- \pi^+] \pi^+$$

$$B^- \rightarrow D_{DCS}^0 \pi^- \rightarrow [K^+ \pi^-] \pi^-$$

CDF Run II Preliminary  $L_{int} = 5 \text{ fb}^{-1}$



CDF Run II Preliminary  $L_{int} = 5 \text{ fb}^{-1}$





# ADS: Systematics



Source	$R_{ADS}(\pi)$	$R_{ADS}(K)$	$A_{ADS}(\pi)$	$A_{ADS}(K)$
dE/dx	0.0001	0.0050	0.0560	0.070
combinatorial background	0.0003	0.0037	0.0073	0.153
$B^- \rightarrow [X]_D \pi^-$ shape	0.0002	0.0025	0.0067	0.057
$B^- \rightarrow [X]_D K^-$ shape	-	0.0001	0.0003	0.003
$B^- \rightarrow K^- \pi^+ \pi^-$ shape	0.0001	0.0004	0.0049	0.009
$B^0 \rightarrow D_0^{*-} e^+ \nu_e$ shape	-	0.0003	0.0020	0.007
$B^- \rightarrow D^{*0} \pi^-$ shape	-	0.0005	0.0009	0.013
efficiency	-	0.0001	-	0.003
bias	0.0001	0.0042	0.0159	0.148
<b>Total</b>	<b>0.0004</b>	<b>0.0079</b>	<b>0.059</b>	<b>0.232</b>

- dE/dx we varied the shapes of the PID pdfs
- Combinatorial and physics background: we varied the shapes used in the fit
- efficiency of K+/K- reconstruction
- Fit bias: checked with pseudo-experiments MC



# ADS: Likelihood



$$\mathcal{L} = \mathcal{L}_{CF+} \cdot \mathcal{L}_{CF-} \cdot \mathcal{L}_{DCS+} \cdot \mathcal{L}_{DCS-}$$

$$\mathcal{L}_{CF+} = \prod_i^{N_{events}} \left[ (1 - b_{CF+}) \cdot \left( f_{\pi}^{CF+} \cdot pdf_{\pi}(M, ID) + \mathbf{c}^+ \cdot f_{\pi}^{CF+} \cdot pdf_{D^*}(M, ID) + \right. \right. \\ \left. \left. + \left( 1 - f_{\pi}^{CF+} - \mathbf{c}^+ \cdot f_{\pi}^{CF+} \right) \cdot pdf_K(M, ID) \right) + b_{CF+} \cdot pdf_{comb}(M, ID) \right]$$

$$\mathcal{L}_{DCS+} = \prod_i^{N_{events}} \left[ (1 - b_{DCS+}) \cdot \left( f_{\pi}^{DCS+} \cdot pdf_{\pi}(M, ID) + \mathbf{c}^+ \cdot f_{\pi}^{DCS+} \cdot pdf_{D^*}(M, ID) + \right. \right. \\ \left. \left. + \left( 1 - f_{\pi}^{DCS+} - \mathbf{c}^+ \cdot f_{\pi}^{DCS+} \right) \cdot pdf_K(M, ID) \right) + \right. \\ \left. + b_{DCS+} \cdot \left( f_{[X]\pi}^+ \cdot pdf_{[X]\pi}(M, ID) + f_{[X]K}^+ \cdot pdf_{[X]K} + f_{K\pi\pi}^+ \cdot pdf_{K\pi\pi}(M, ID) + \right. \right. \\ \left. \left. f_{B^0}^+ \cdot pdf_{B^0}(M, ID) + (1 - f_{[X]\pi}^+ - f_{[X]K}^+ - f_{K\pi\pi}^+ - f_{B^0}^+) \cdot pdf_{comb}(M, ID) \right) \right]$$

•  $pdf_i(M, ID) = pdf_i(M) * pdf_i(ID)$

*Analogous expressions for negative charges*

• **Fitted parameters**

- $b_{CF, DCS}$  = background fraction for CF and DCS
- $f_{\pi, CF, DCS}$  =  $B \rightarrow D^0 \pi$  fraction for CF and DCS signal
- $\mathbf{c}$  =  $f_{D^*} / f_{\pi}$  (equal for CF and DCS)
- $f_{[X]\pi}^+$  = fraction of  $B \rightarrow D^0 \pi$ ,  $D^0 \rightarrow X$  in DCS reconstruction (constrained from MC)
- $f_{[X]K}^+$  = fraction of  $B \rightarrow D^0 K$ ,  $D^0 \rightarrow X$  in DCS reconstruction (constrained from MC)
- $f_{K\pi\pi}^+$  = fraction of  $B \rightarrow K^- \pi^+ \pi^-$  in DCS reconstruction (constrained from MC)
- $f_{B^0}^+$  = fraction of  $B^0 \rightarrow D^{*-} e^+ \nu$  in DCS reconstruction (constrained from MC)