Quark fragmentation in the cold nuclear medium

using kaons and nuclei to discover the mechanisms of hadronization

Will Brooks U. Santa María, Valparaíso, Chile

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 - correlated photons, multiplicity correlations, and more

Connections











• production time τ_p - propagating quark



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• formation time ${}^{h}\tau_{f}$ - dipole grows to hadron

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Partonic multiple scattering: medium-stimulated gluon emission, broadened p_T

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prehadron forms *outside* the medium; or....

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Hadron forms inside the medium; then also have prehadron/hadron interaction

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Amplitudes for hadronization inside and outside the medium can interfere

Drell-Yan in Cold Nuclear Medium

e.g., 800 GeV protons - no in-medium hadronization, but do have p_T broadening

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Relativistic Heavy Ion Collisions - parton propagation in a hot dense medium

Comparison of Parton Propagation in Three Processes



Accardi, Arleo, Brooks, d'Enterria, Muccifora, Riv.Nuovo Cim.032:439-553,2010 [arXiv:0907.3534] Majumder, van Leuween, arXiv:1002.2206

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 $\nu(1-z_h)$ dE | au_p drvacuum

Energy conservation, time dialation

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 $u(1-z_h)$ dE | τ_p dxvacuum

Energy conservation, time dialation

String model

$$\frac{dE}{dx}\Big|_{vacuum} \approx \kappa \approx 1 \quad GeV / fm$$

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 $\tau_p = \frac{\nu(1-z_h)}{\frac{dE}{dx}|_{vacuum}}$

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BACK-OF-ENVELOPE - ${}^{h}\tau_{f}$

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Given hadron of size R_h , can build color field of hadron in its rest frame in time no less than $t_0 \sim R_h/c$. In lab frame this is time dialated:

 $t_f \ge \frac{E}{m} R_h$

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 $t_f \ge \frac{E}{m} R_h$

If take, e.g., the pion mass, radius 0.66 fm, E = 4 GeV, then $\tau_f \sim 20 \text{ fm/c}$.

BACK OF ENVELOPE, but using Quantum mechanics - ${}^{h}\tau_{f}$

Given propagating pre-hadron with energy E in the lab frame, the time it takes to resolve the final hadron mass is given by the difference between the masses of the nearest two states into which it can evolve (e.g., ground state and first radial excited state), boosted to the lab frame.

$$\tau_f = \frac{2E}{m_1^2 - m_2^2}$$

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Pion of 4 GeV, m_1 =0.14 GeV, m_2 = 1.3 GeV, E = 4 GeV, then $\tau_f \sim 1 \text{ fm/c.}$ (*Much less than previous page!* [and Kaons?])

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Pion of 4 GeV, m_1 =0.14 GeV, m_2 = 1.3 GeV, E = 4 GeV, then $\tau_f \sim 1 \text{ fm/c}$. (Much less than previous page! [and Kaons?]) p.s., note connection to the quark model and hadron structure!
Comparison of p_T broadening data - Drell-Yan and DIS









The transverse momentum broadening experienced by a quark is *diluted* by the time it is part of a hadron



 $p_T(pion) \approx z \ k_T(quark)$

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Hermes p_T broadening data

World's first comparison between pion and K⁺ p_T broadening





$$R_{M}^{h}(z,\nu,p_{T}^{2},Q^{2},\phi) = \frac{\left\{\frac{N_{h}^{DIS}(z,\nu,p_{T}^{2},Q^{2},\phi)}{N_{e}^{DIS}(\nu,Q^{2})}\right\}_{A}}{\left\{\frac{N_{h}^{DIS}(z,\nu,p_{T}^{2},Q^{2},\phi)}{N_{e}^{DIS}(\nu,Q^{2})}\right\}_{D}}$$
Hadronic multiplicity ratio



Year	$E \; ({\rm GeV})$	Target	Identified hadrons
1997	27.6	D, N	h^{\pm}, π^{\pm}
1999	27.6	D, Kr	$h^{\pm}, \pi^{\pm}, \pi^0, K^{\pm}, p, \overline{p}$
2000	27.6	D, He, Ne	$\pi^{\pm}, \pi^0, K^{\pm}, p, \overline{p}$
2000	12.0	D, N, Kr	h^{\pm}, π^{\pm}
2004	27.6	D, Kr, Xe	$\pi^{\pm}, K^{\pm}, \pi^0, p, \overline{p}$
2005	27.6	D, Kr, Xe	$\pi^{\pm}, K^{\pm}, \pi^0, p, \overline{p}$

Hermes nuclear target program

















- Three-parameter model:
 - scale factor (proportional to transport coefficient)
 - production time (distributed exponentially)
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- Three-parameter model:
 - scale factor (proportional to transport coefficient)
 - production time (distributed exponentially)
 - effective absorption cross section
- Simultaneous fit of pT broadening and multiplicity ratio in the same 3-fold kinematic bin in Q², ∨, and z
- Realistic nuclear densities



- Path begins at point with probability proportional to density
- Part of path is quark, part of path is (pre-)hadron

Results from combined fit 3 parameter geometric model various bins in Q², v, and z



 $\begin{array}{c} \text{Scale factor} \\ \propto \hat{q} \end{array}$

Production length lp

Effective absorption cross section σ



JLab/CLAS 3-D preliminary data



Four out of ~50 plots! ²² K⁰, π ⁻, π ⁰, η , Λ underway

Consistent with features of data

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• Dependence of transport coefficient on z

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• Effective cross section moderately larger than hadronic - energy loss mechanism visible (?)

New Multiplicity Studies

Requiring multiple pions allows studies of highermultiplicity states - feasible because of high luminosities

10X higher luminosities for CLAS12!

Broadening vs. pi+ multiplicity



1-piplus(typ)

2-piplus

3-piplus

JLab/CLAS 5 GeV data



Higher multiplicity may correlate with more in-medium interactions, in analogy with 'centrality' in RHI



At I2 GeV, more reach to explore multiplicity dependence



What is the importance of kaons in these studies?

- Provide important continuity between CLASI2 measurements and HERMES measurements
- Can compare K⁰ to charged kaons, in pT broadening and multiplicity ratios
- Kaons have smaller cross section than pions absorption scenario: multiplicity ratio should be larger for kaons - energy loss scenario: opposite trend (based on shapes of fragmentation functions for kaon and pion).
- Will reduce backgrounds on all channels where strangeness is involved, such as lambda baryons or phi mesons.
- ~3 orders of magnitude more integrated luminosity than Hermes, so one can study the details of the K⁺ K⁻ comparison as a function of several kinematic variables simultaneously.

Landscape of kaon hadronization



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The CLAS12 Experiment in the 12 GeV Era

Dependency of observables (and thus derived quantities, such as production time, formation times, transport coefficient, in-medium cross section, etc.) on mass, flavor, and number of valence quarks

The CLAS12 Experiment in the 12 GeV Era

hadron	сτ	mass	flavor content	limiting error (60 PAC days)
π^0	25 nm	0.13	uudd	5.7% (sys)
$\pi^{\scriptscriptstyle +}$, $\pi^{\scriptscriptstyle -}$	7.8 m	0.14	ud, du	3.2% (sys)
η	170 pm	0.55	uuddss	6.2% (sys)
ω	23 fm	0.78	uuddss	6.7% (sys)
η'	0.98 pm	0.96	uuddss	8.5% (sys)
ϕ	44 fm	1.0	uuddss	5.0% (stat)*
fl	8 fm	1.3	uuddss	-
<i>K</i> ⁰	27 mm	0.50	ds	4.7% (sys)
<i>K</i> +, <i>K</i> -	3.7 m	0.49	us, us	4.4% (sys)
р	stable	0.94	ud	3.2% (sys)
\bar{p}	stable	0.94	ud	5.9% (stat)**
Λ	79 mm	1.1	uds	4.1% (sys)
A(1520)	13 fm	1.5	uds	8.8% (sys)
Σ^+	24 mm	1.2	us	6.6% (sys)
Σ^{-}	44 mm	1.2	ds	7.9% (sys)
Σ^0	22 pm	1.2	uds	6.9% (sys)
Ξ^0	87 mm	1.3	us	16% (stat)*
Ξ^{\cdot}	49 mm	1.3	ds	7.8% (stat)*

Dependency of observables (and thus derived quantities, such as production time, formation times, transport coefficient, in-medium cross section, etc.) on mass, flavor, and number of valence quarks

The CLASI2 Experiment in the I2 GeV Era

hadron	сτ	mass	flavor content	limiting error (60 PAC days)
π^0	25 nm	0.13	uudd	5.7% (sys)
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Dependency of observables (and thus derived quantities, such as production time, formation times, transport coefficient, in-medium cross section, etc.) on mass, flavor, and number of valence quarks

*in a bin in z from 0.7-0.8, integrated over all V, pT, ϕ_{Pq} , and Q²>5 GeV² **in a bin in z from 0.6-0.7, integrated over all V, pT, ϕ_{Pq} , and Q²>5 GeV²

The CLAS12 Experiment in the 12 GeV Era

hadron	сτ	mass	flavor content	limiting error (60 PAC days)	days) Dependency of observables (and thus derived quantities, such as productions)		
π^0	25 nm	0.13	uudd	5.7% (sys)	time, formation times, transport coefficient, in-medium cross section, etc.) on mass, flavor, and number of valence quarks		
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η	170 pm	0.55	uuddss	6.2% (sys)	0.7		
ω	23 fm	0.78	uuddss	6.7% (sys)			
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<i>K</i> +, <i>K</i> -	3.7 m	0.49	us, us	4.4% (sys)	$0.4 \ \pi^{-1}$ $0.4 \ anti-proton$		
р	stable	0.94	ud	3.2% (sys)			
\bar{p}	stable	0.94	ud	5.9% (stat)**	$\int_{-\infty}^{\infty} \pi^{0} = \frac{\pi^{0}}{1 - 1}$		
Λ	79 mm	1.1	uds	4.1% (sys)			
A(1520)	13 fm	1.5	uds	8.8% (sys)			
Σ^+	24 mm	1.2	us	6.6% (sys)	n-prime $n-1$		
Σ-	44 mm	1.2	ds	7.9% (sys)			
Σ^0	22 pm	1.2	uds	6.9% (sys)			
Ξ^0	87 mm	1.3	us	16% (stat)*	0 0.2 0.4 0.6 0.8 1 0 0.2 0.4 0.6 0.8 Zh Zh Zh		
Ξ-	49 mm	1.3	ds	7.8% (stat)*	CLAS12 Acceptance for Mesons CLAS12 Acceptance for Baryons		
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*in a bin in z from 0.7-0.8, integrated over all V, pT, ϕ_{Pq} , and Q²>5 GeV² **in a bin in z from 0.6-0.7, integrated over all V, pT, ϕ_{Pq} , and Q²>5 GeV²

Examples of Experimental Data and Theoretical Predictions



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Mechanisms of Hadronization

Examples of recent theory progress

- First fully quantum-mechanical calculation of in-medium hadronization
- Perturbative fragmentation via the KPPS-Berger model (KPPS, Phys. Lett.
 B662:117-122, 2008, arXiv:0706.3059v1 [hep-ph]
- Path-integral formulation of quantum mechanics (LCGF)
 - phases and interferences; all relevant timescales
 - includes the probability of prehadron production both inside and outside the medium

Inner/outer interference generates hadron 'attenuation': in-medium interactions affect overlap of dipole to pion wave function

B.Z. Kopeliovich, H.-J. Pirner, I.K. Potashnikova, Ivan Schmidt, A.V. Tarasov, O.O. Voskresenskaya, Phys. Rev. C78:055204,2008 arXiv:0809.4613v2 [hep-ph]

Conclusions

- Rich and exciting program of studies!
 - Hermes data the first with hadron-specific information
 - CLAS at 5 and 11 GeV
- Strangeness production a very important part of these studies of hadronization mechanisms and space-time QCD