

W Mass and Width Measurements at the Tevatron



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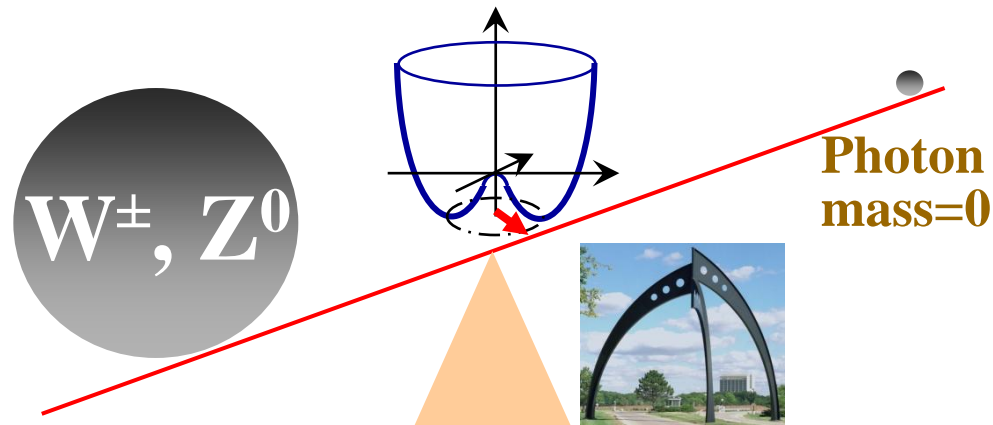
on behalf of the CDF and DØ Collaborations

XXIV Rencontres de Physique de la Vallée d'Aoste,
La Thuille, Italy, March 4, 2010



Electroweak Symmetry Breaking

- W (and Z) bosons are interesting objects to study: mass, width, production and decay properties
- Even more interesting to find out how exactly these objects came to be



- What is the mechanism by which W and Z bosons acquired their mass ?
- Precise measurements of $M(W)$ tell us about Electroweak Symmetry Breaking ₂

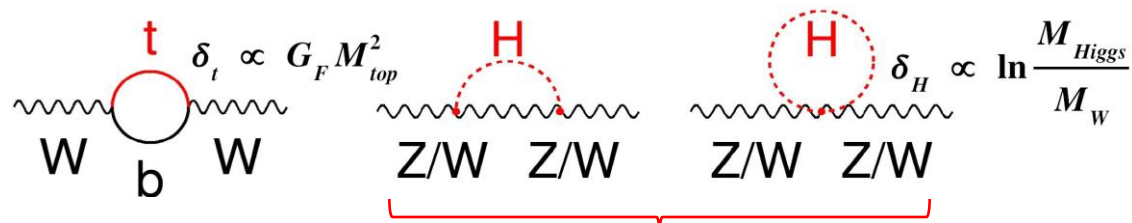
M(W) Motivation

- W boson mass is an important Standard Model parameter related to G_F , α_{EM} , and M_Z via

$$M_W^2 = \frac{\text{tree level } \pi\alpha_{EM}(0)}{\sqrt{2}G_F (1 - M_W^2/M_Z^2)(1 - \Delta r)}$$

- Δr term represents (large!) higher-order corrections to M_W

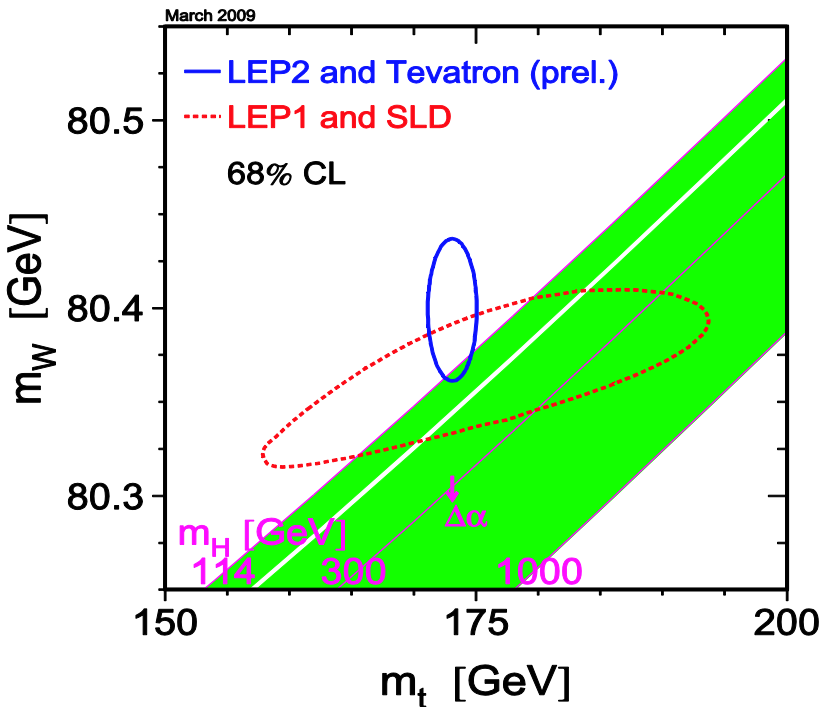
$$\Delta r = \alpha_{EM}(0 \rightarrow M_Z) \text{ Running of } \alpha_{EM} + \text{Radiative Corrections}$$



Sensitivity to Higgs Mass

Constraining Standard Model

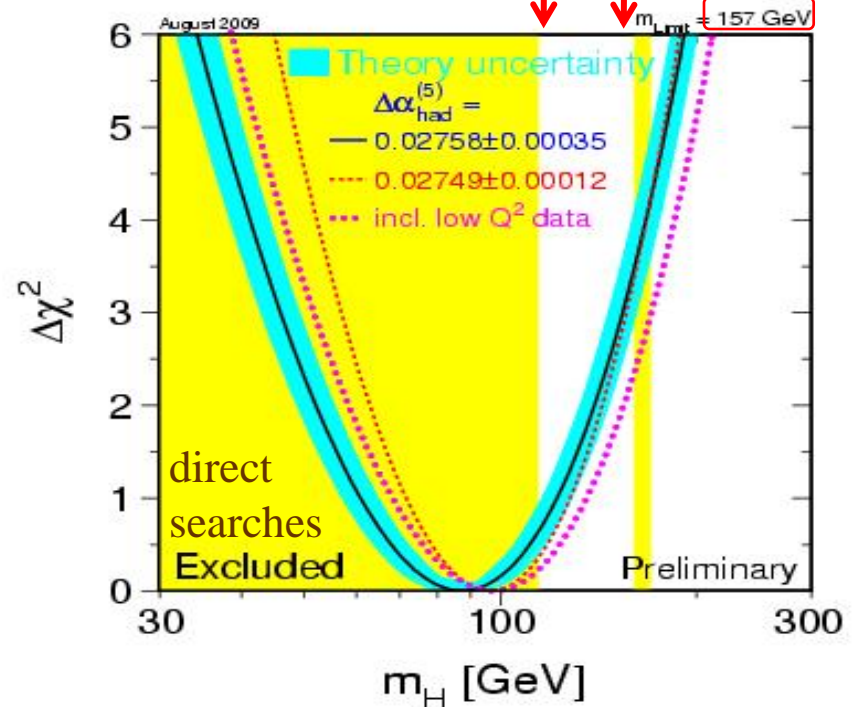
- Precision measurements provide sensitivity to new physics at much higher energy scales than the mass of the particles on which the measurements are performed
- Measurements of the M_W and M_{top} constrain the mass of the Higgs boson



Higgs limit from EW fits

may be possible with
 full Tevatron dataset

Current
 157 GeV @95%CL

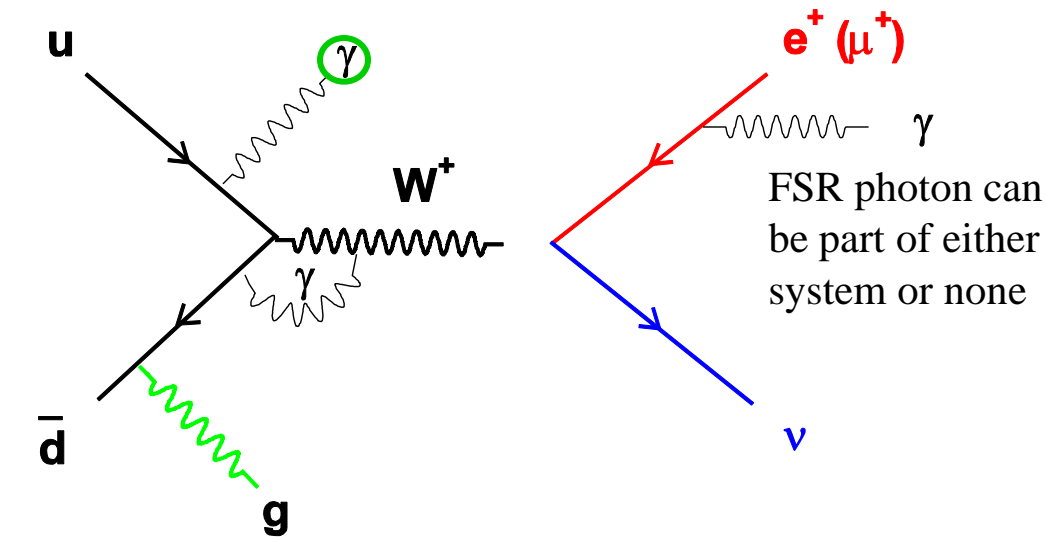


W Boson Mass and Top Quark Mass

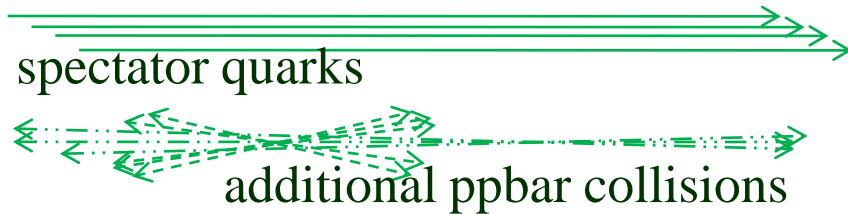
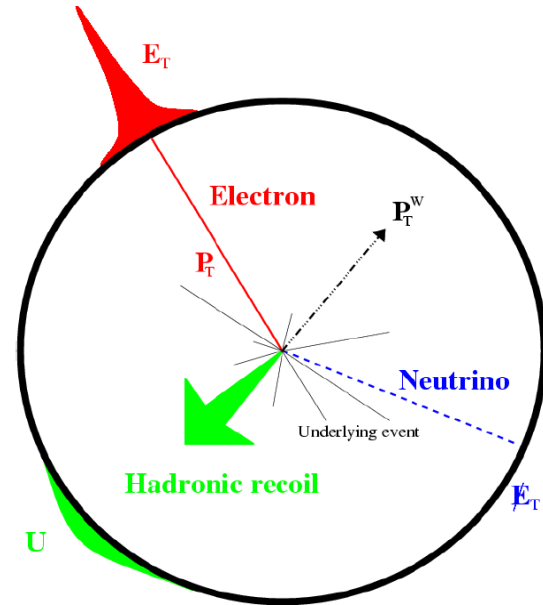
- Higgs boson mass is sensitive to $M(W)$ and $M(\text{top})$
- For equal contribution to the Higgs mass uncertainty need: $\Delta M_W \approx 0.006 \Delta M_{\text{top}}$
- Current Tevatron average $\Delta M_{\text{top}} = 1.3 \text{ GeV}$
- \Rightarrow Would need: $\Delta M_W = 8 \text{ MeV}$ (currently have: $\Delta M_W = 23 \text{ MeV}$)

W → ev Event: Theory and Analysis View

hard component = recoil against W



FSR photon can be part of either system or none



$$\vec{E}_T = -\vec{P}_T^e - \vec{P}_T^{recoil}$$

Analysis: describe W → ev event in terms of **recoil** and **electron** systems

to achieve

$$\Delta M_W / M_W \approx 0.5 \times 10^{-3}$$

Required detector electron $\sim 0.3 \times 10^{-3}$
response precision: hadronic recoil $\sim 1\%$

Measuring $M(W)$

- Cannot reconstruct $M(W)$ directly (missing neutrino p_z)
- Extract it from observables that are sensitive to $M(W)$

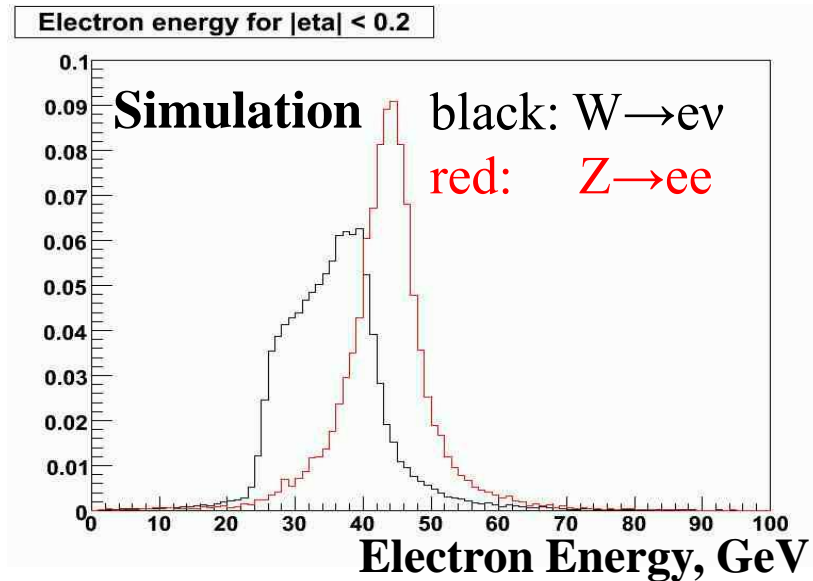
$$M_T = \sqrt{2p_T^e p_T^\nu (1 - \cos \phi_{e\nu})} \quad p_T^e \quad p_T^\nu \left(\mathbf{E}_T = \left| \vec{p}_T^e + \vec{p}_T^{recoil} \right| \right)$$

- due to complicated detector effects analytical computation impossible
- determine $M(W)$ via template fit (need Fast Monte Carlo model of detector effects)
- The observables are transverse, not Lorentz-invariant: sensitive to transverse motion of W boson
 - need good model of W boson production

Electron Energy Calibration (DØ)

- $M(W)$ precision is controlled by electron energy scale precision
- Understanding electron showers in the calorimeter is very important
- Knowing the amount of un-instrumented material is the key
- Use $Z \rightarrow ee$ data sample for calibration to precisely measured $M(Z)$ by LEP
- Need proper description of energy dependence as well
- Achieved via
 - dedicated version of GEANT simulation
 - calibration of longitudinal shower profile
 - accurate tuning of material model

**measurement of W/Z mass ratio
⇒ many systematic effects cancel**



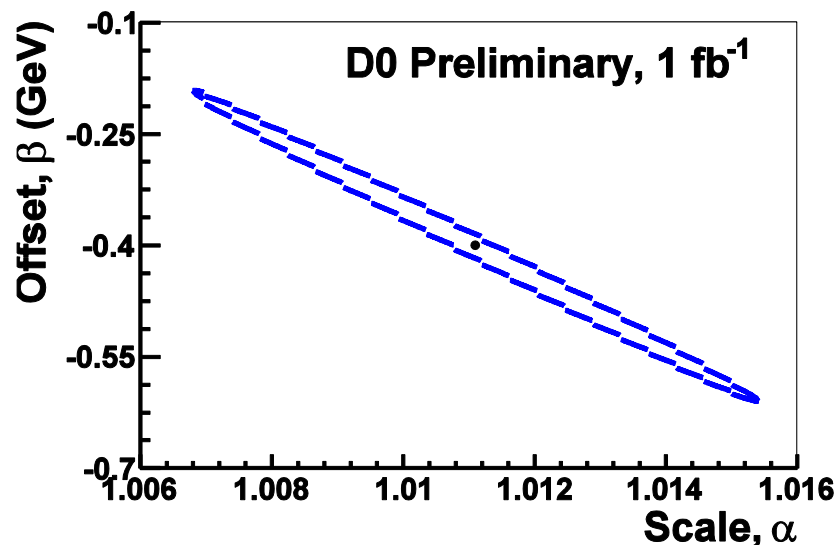
Final M(W) Calibration (DØ)

- Linear response model : $E_{\text{measured}}(e) = \alpha \times E_{\text{true}}(e) + \beta$
 $\alpha \rightarrow \text{scale}$ $\beta \rightarrow \text{offset}$
- Use $Z \rightarrow ee$ electrons to constrain α and β (precision limited by statistics)
- Calibrate to $M_Z (\pm 2 \text{ MeV from LEP})$
- Two observables to fit the data
 - $Z \rightarrow ee$ invariant mass
 - f_Z variable “scans” the response as a function of energy

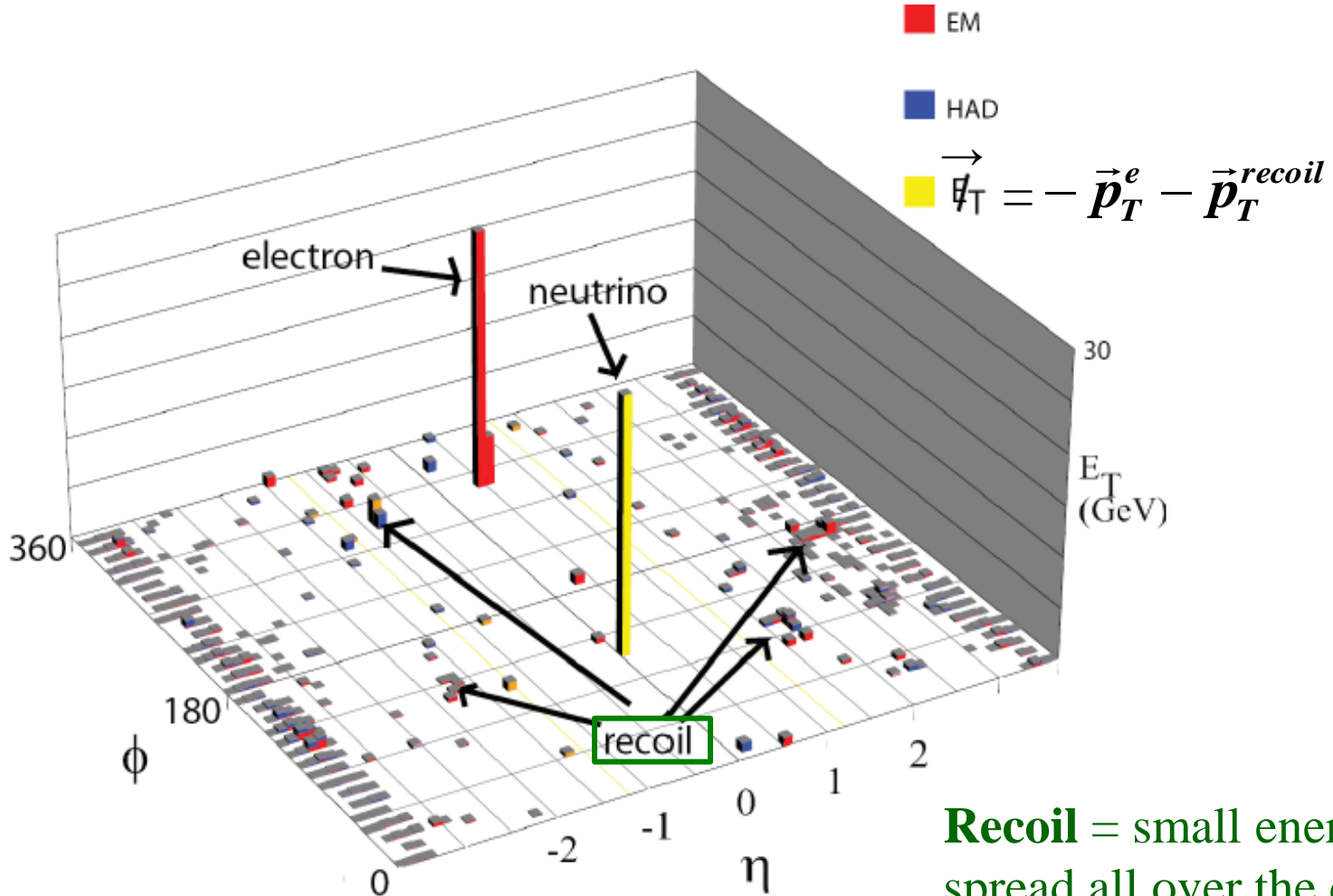
$$f_Z = (E(e1)+E(e2))(1-\cos(\gamma_{ee}))/m_Z$$

$$\begin{aligned} \alpha &= 1.0111 \pm 0.0043 \\ \beta &= -0.404 \pm 0.209 \text{ GeV} \\ \text{correlation} &= -0.997 \end{aligned}$$

\Rightarrow dominant systematic error,
100 % correlated between
three observables



Event Display of DØ $W \rightarrow e\nu$ Candidate Event



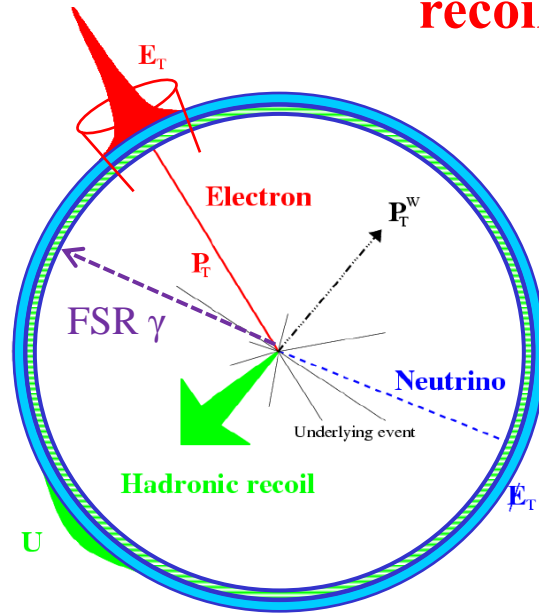
Recoil = small energy deposits spread all over the detector
 \Rightarrow sensitivity to small effects, challenges for modeling

Recoil Model (DØ)

Recoil in Fast MC: $\vec{u}_T = \vec{u}_T^{\text{Hard}} + \vec{u}_T^{\text{Soft}} + \vec{u}_T^{\text{Elec}} + \vec{u}_T^{\text{FSR}}$

FSR photon outside
electron cone
full MC derived model

$$\vec{u}_T^{\text{FSR}} = \sum_{\gamma} \vec{p}_T(\gamma)$$



recoil energy “lost” in electron cone(s)
estimate from $W \rightarrow e\nu$ data

$$\vec{u}_T^{\text{Elec}} = - \sum \Delta u_{\parallel} \cdot \hat{p}_T(e)$$

not correlated with
the vector boson,
two sub-components:
-- spectator partons
-- additional interactions

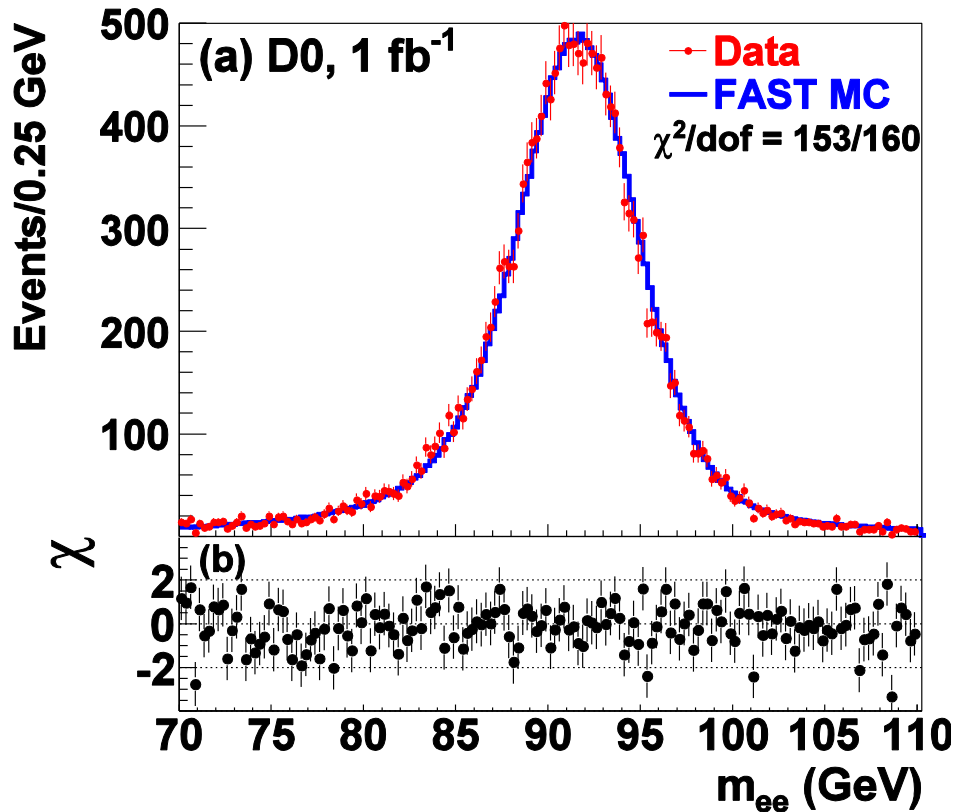
balances \mathbf{P}_T of the vector boson:

$Z \rightarrow \nu\nu$ full MC model $q_T \rightarrow (\Delta q_T, \Delta\phi)$

$$\vec{u}_T^{\text{Hard}} = \vec{f}(\vec{q}_T)$$

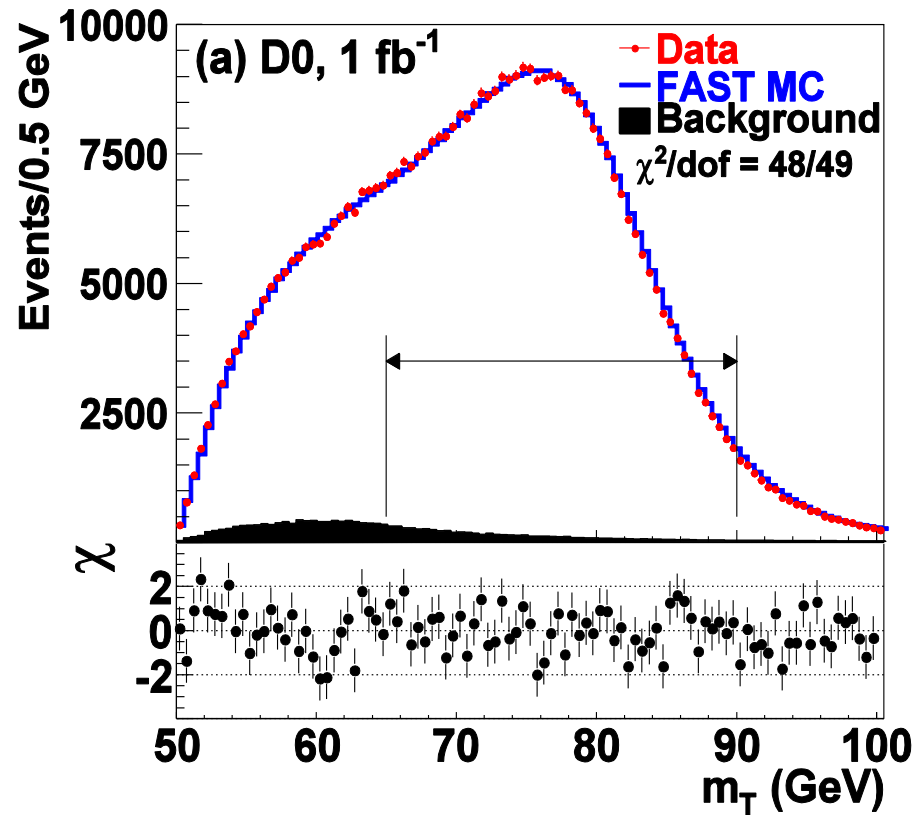
$$\vec{u}_T^{\text{Soft}} = \alpha_{\text{MB}} \cdot \vec{E}_T^{\text{MB}} + \alpha_{\text{ZB}} \cdot \vec{E}_T^{\text{ZB}}$$

Mass fits: $M(Z)$, $M_T(W)$



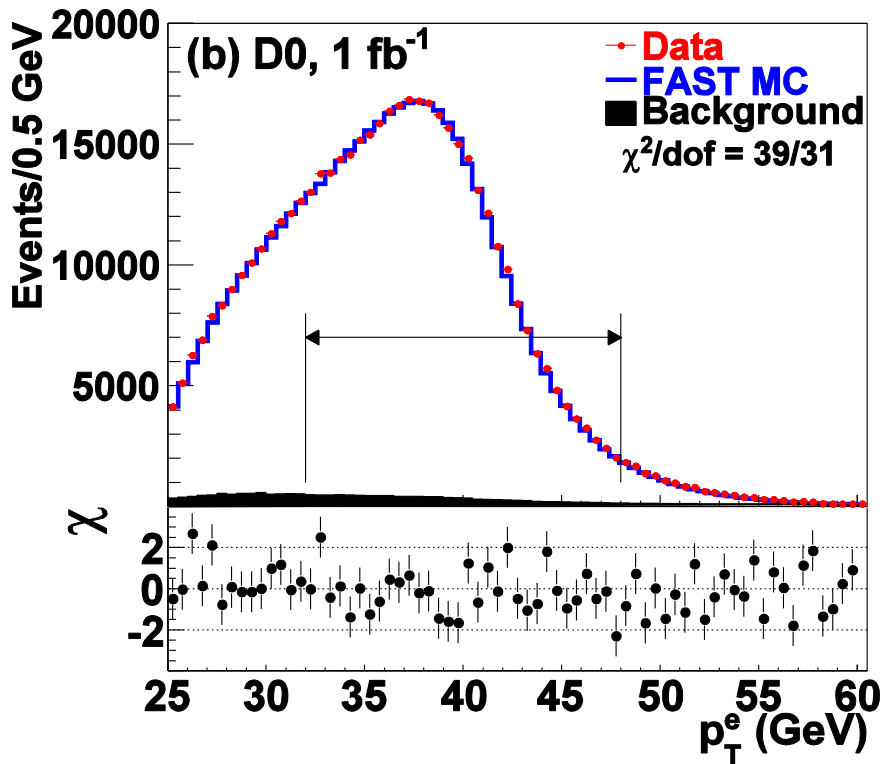
$$m(Z) = 91.185 \pm 0.033 \text{ GeV (stat)}$$

remember that Z mass value from LEP was
input to electron energy scale calibration,
PDG: $M(Z) = 91.1876 \pm 0.0021 \text{ GeV}$

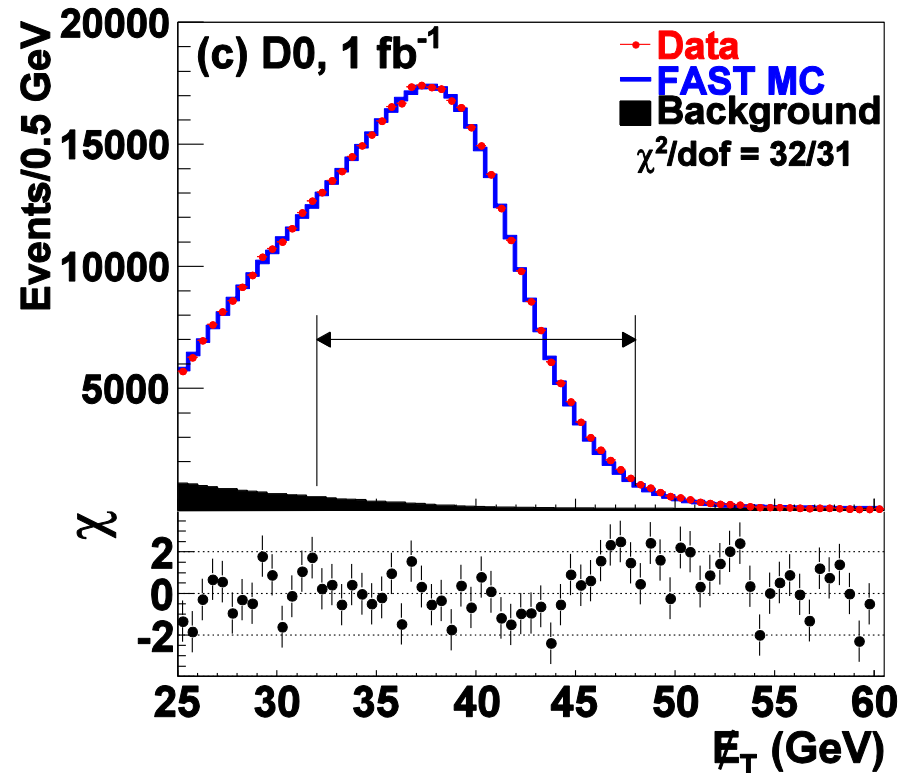


$$m(W) = 80.401 \pm 0.023 \text{ GeV (stat)}$$

Mass fits: $P_T(e)$, MET



$$m(W) = 80.400 \pm 0.027 \text{ GeV (stat)}$$



$$m(W) = 80.402 \pm 0.023 \text{ GeV (stat)}$$

M(W) Uncertainties, MeV (DØ)

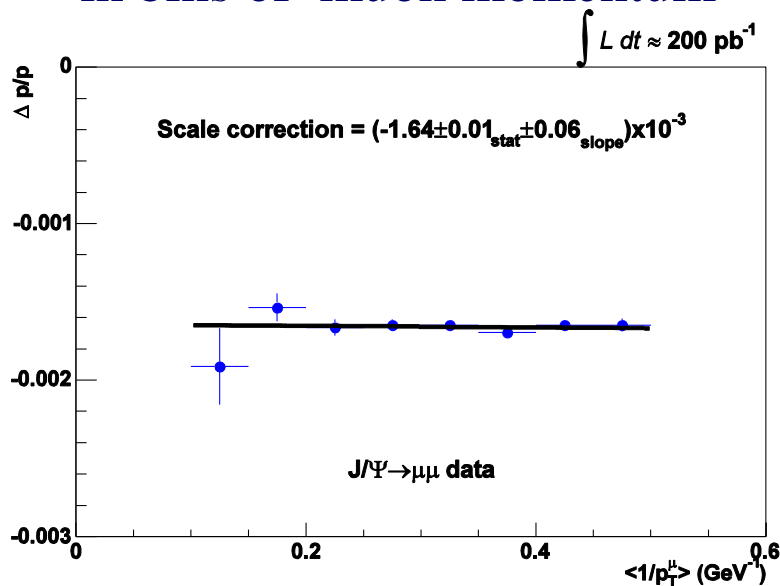
Source	m_T	p_T^e	\cancel{E}_T
Statistical	23	27	23
Systematic - Experimental			
Electron energy response	34	34	34
Electron energy resolution	2	2	3
Electron energy non-linearity	4	6	7
Electron energy loss differences	4	4	4
Recoil model	6	12	20
Efficiencies	5	6	5
Backgrounds	2	5	4
Experimental Subtotal	35	37	41
Systematic – W production and decay model			
PDF	10	11	11
QED	7	7	9
Boson pT	2	5	2
W model subtotal	12	17	17
Systematic -- Total	37	40	44

in the near future
 expect reduction of
 experimental errors
 and increased
 importance of
 theoretical errors

Lepton Energy Calibration (CDF)

precise tracker calibration

measure J/ψ mass
in bins of muon momentum

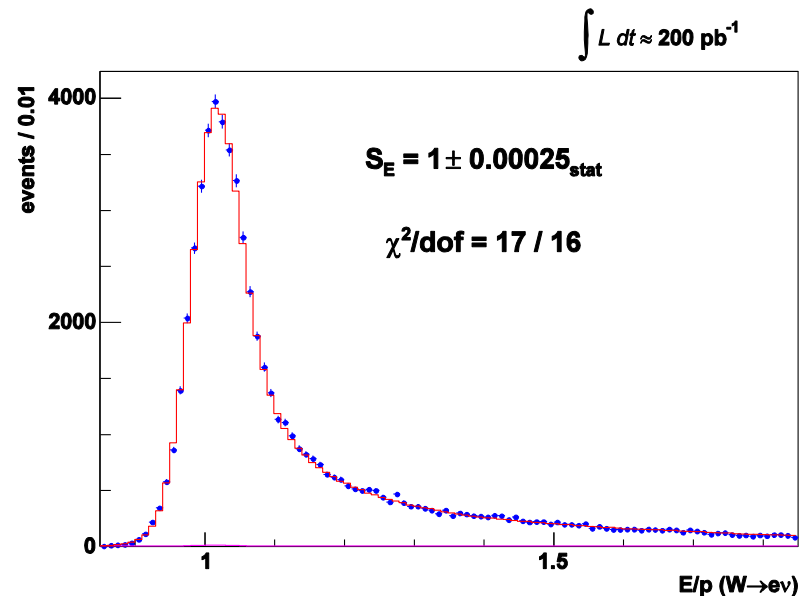


adjust energy loss model

0.02% calibration precision
main uncertainties:

- QED corrections
- magnetic field non-uniformity

transferred to calorimeter
using E/p in $W \rightarrow e\nu$ sample



M(W) Uncertainties (CDF)

L = 200 pb⁻¹

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L = 200 pb⁻¹

m _T Uncertainty [MeV]	Electrons	Muons	Common	Electrons	Muons	Common	Electrons	Muons	Common
Lepton Scale	30	17	17	30	17	17	30	17	17
Lepton Resolution	9	3	0	9	3	0	9	5	0
Recoil Scale	9	9	9	17	17	17	15	15	15
Recoil Resolution	7	7	7	3	3	3	30	30	30
u Efficiency	3	1	0	5	6	0	16	13	0
Lepton Removal	8	5	5	0	0	0	16	10	10
Backgrounds	8	9	0	9	19	0	7	11	0
p _T (W)	3	3	3	9	9	9	5	5	5
PDF	11	11	11	20	20	20	13	13	13
QED	11	12	11	13	13	13	9	10	9
Total Systematic	39	27	26	45	40	35	54	46	42
Statistical	48	54	0	58	66	0	57	66	0
Total	62	60	26	73	77	35	79	80	42

M_T(W)

P_T(e,μ)

MET

Individual measurements dominated by **statistical uncertainties**

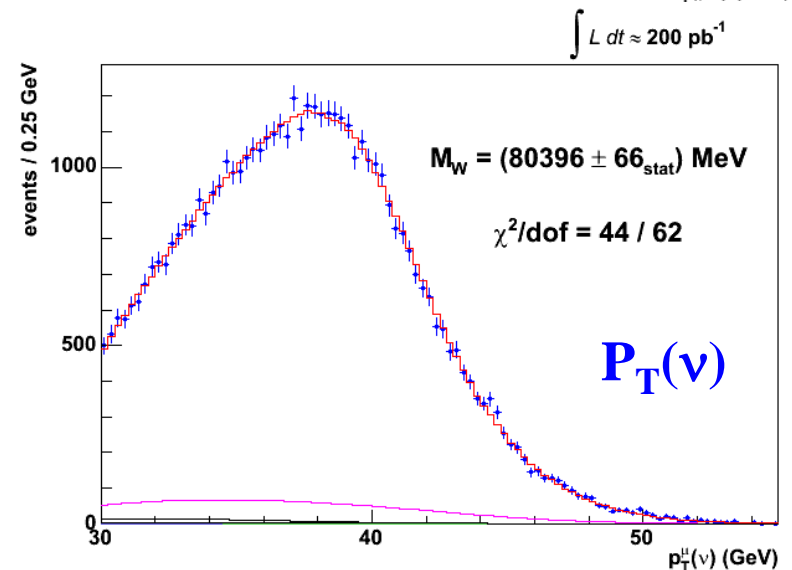
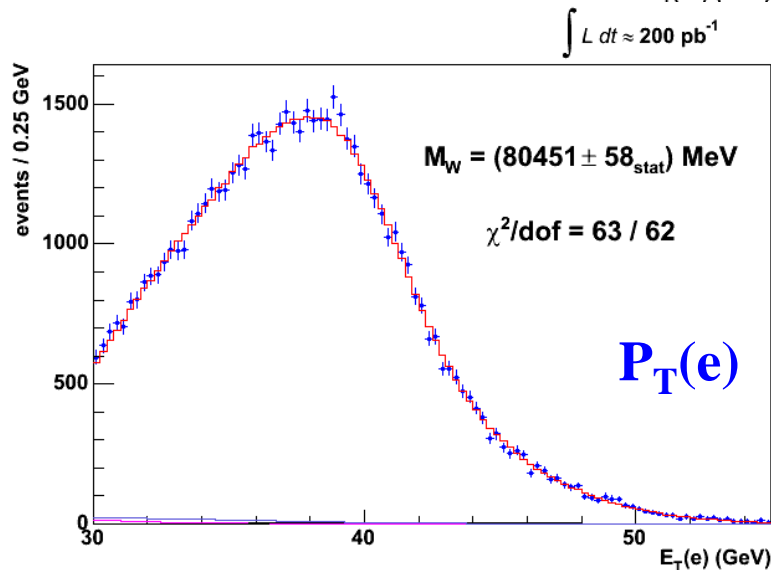
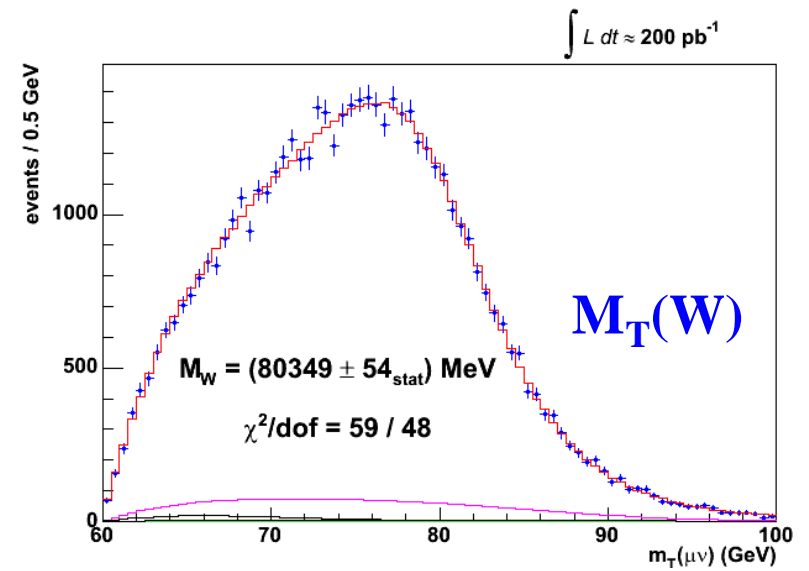
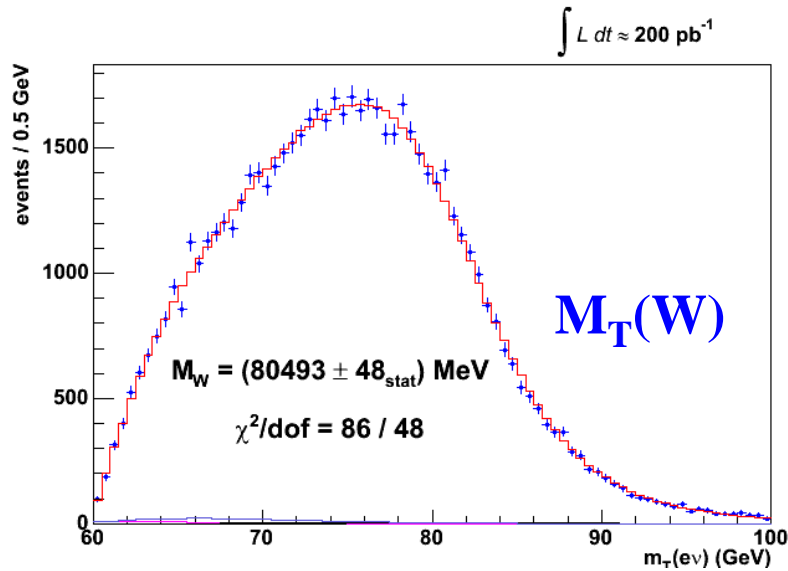
Largest **systematic uncertainties** (M_T example)

Experiment: Lepton Scale
Theory: PDF and QED

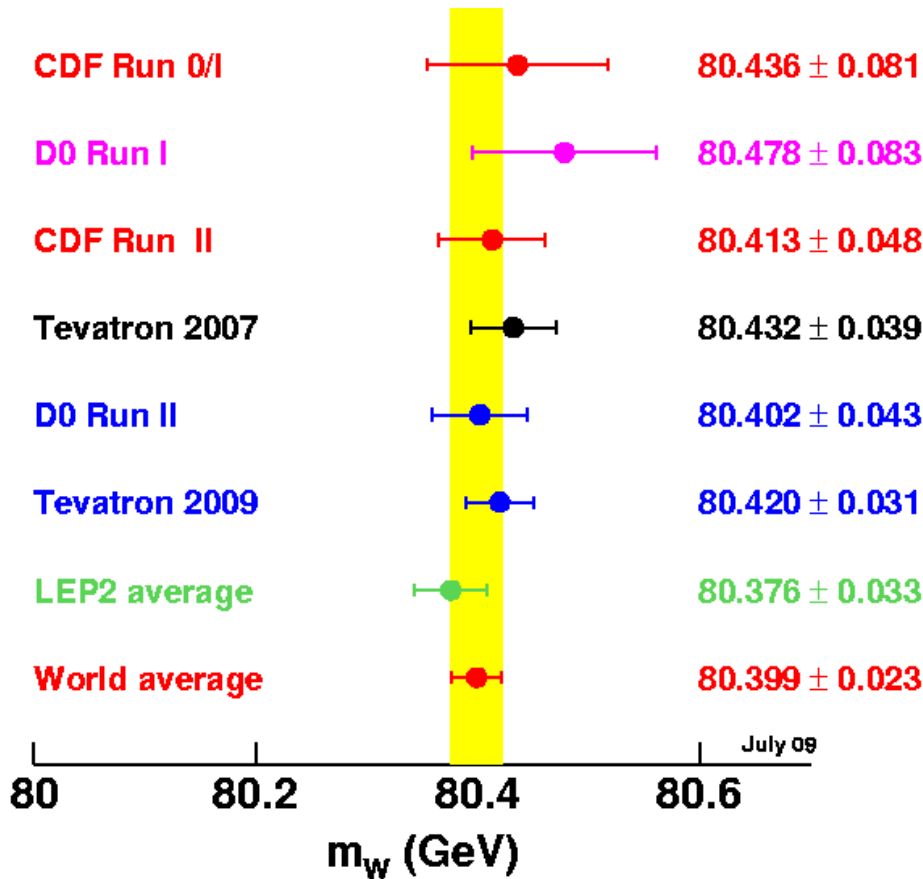
CDF M(W) Analysis

Electron Channel

Muon Channel



Results



DØ RunII 1fb⁻¹ PRL 103, 141801 (2009)

80.401 ± 0.021(stat.) ± 0.038(syst.) GeV

80.401 ± 0.043 GeV

this new result is the

single most precise measurement

of the W boson mass to date

total Tevatron uncertainty

of 31 MeV is now smaller

than that of 33 MeV from LEP2

World average is now

80.399 ± 0.023 GeV

CDF RunII 0.2 fb⁻¹ PRL 99, 151801 (2007)

PRD 77, 112001 (2008)

80.413 ± 0.034 (stat.) ± 0.034 (syst.) GeV

80.413 ± 0.048 GeV

Tevatron ElectroWeak Working Group

<http://tevewwg.fnal.gov>

Combination performed with B.L.U.E. method

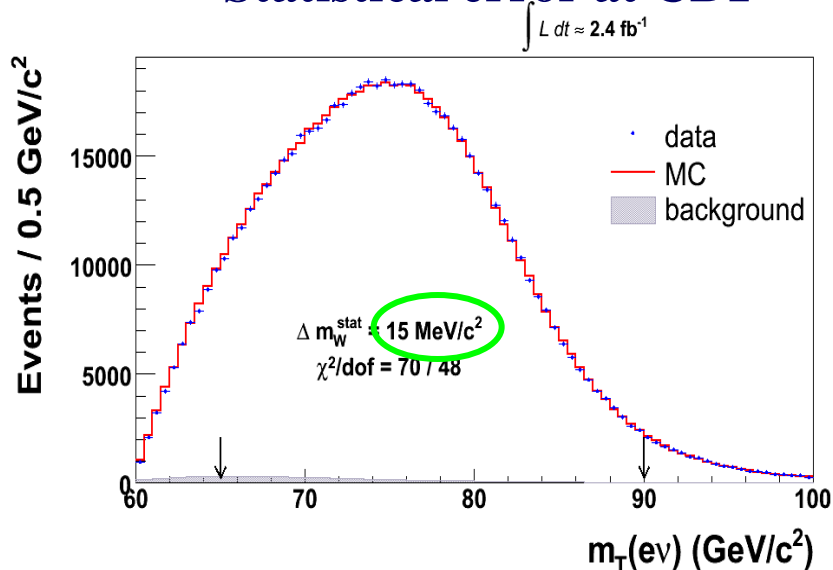
L. Lyons et al, NIM in Phys. Res. A **500**, 391 (2003)

A. Valassi, NIM in Phys. Res. A **500**, 391 (2003)

Current M(W) Effort at the Tevatron

- More data are being analyzed at CDF and DØ
- Main new challenges
 - “busier” events (recorded at higher instantaneous luminosities)
 - need for more careful treatment of systematic effects that used to be swamped by statistical fluctuations
- With the data currently analyzed dominant errors are reduced by a factor of 2-3 compared to published analyses

Statistical error at CDF



Electron scale error at DØ

$M_T(W)$	$34.0 \pm 0.9 \text{ MeV}$
$PT(e)$	$33.5 \pm 0.5 \text{ MeV}$
MET	$33.6 \pm 0.7 \text{ MeV}$



$M_T(W)$	$15.3 \pm 0.4 \text{ MeV}$
$PT(e)$	$16.2 \pm 0.2 \text{ MeV}$
MET	$16.6 \pm 0.2 \text{ MeV}$

M(W) Prospects with all Tevatron Data

- Electroweak fits favor light Higgs
- Currently
 - most probable Higgs mass value = 87 GeV
 - excluded above 157 GeV @95% CL

- Under the following example scenario

$$\Delta M_W : 23 \text{ MeV} \rightarrow 15 \text{ MeV}$$

central values (M_W, M_{top}) do not move

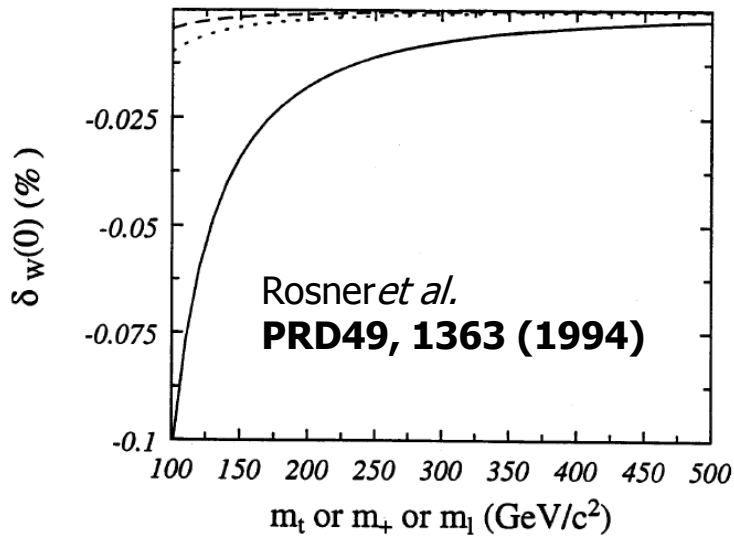
$$\Delta M_{\text{top}} : 1.3 \text{ GeV} \rightarrow 1 \text{ GeV}$$

- Higgs:
 - most probable value = 71 GeV
 - excluded above 117 GeV @95% CL (114.4 from current direct searches)

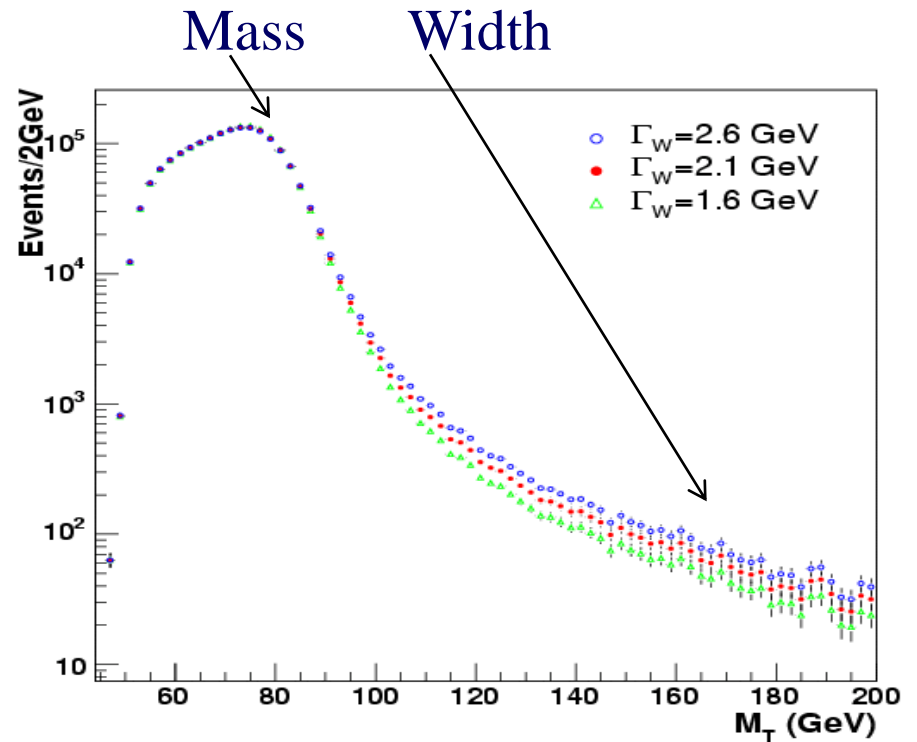
can be achieved at
the Tevatron with
the full dataset !!!

$\Gamma(W)$

Due to insensitivity to “oblique” corrections, expected to agree with SM prediction almost regardless of new physics



Exploit high tail of $M_T(W)$ distribution

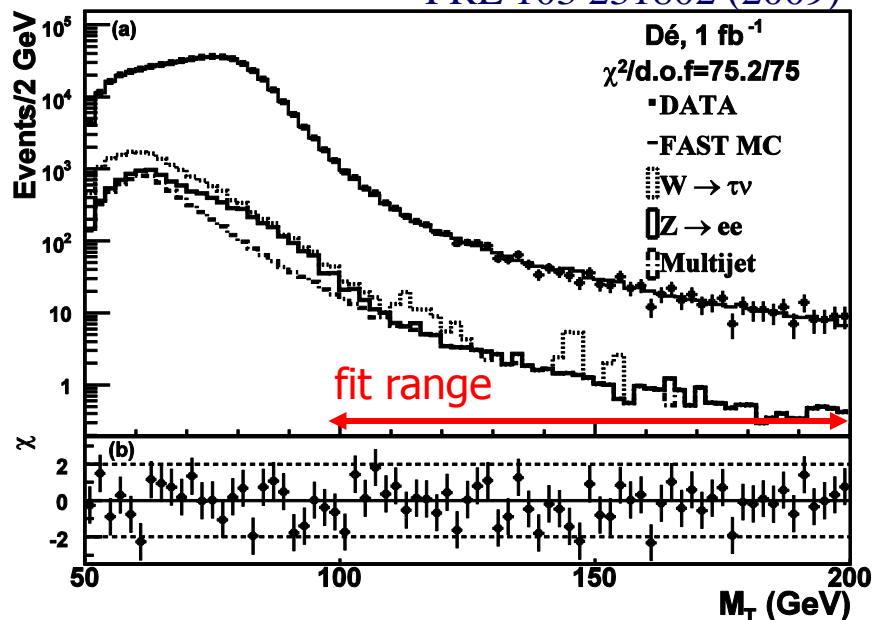


Width, to LO, is proportional to the fraction of events at high M_T

$\Gamma(W)$ Results

$D\emptyset \Gamma_W = 2.028 \pm 0.038$ (stat) ± 0.061 (syst) GeV = 2.028 ± 0.072 GeV

PRL 103 231802 (2009)



Source	$\Delta\Gamma_W$ (MeV)
Electron energy scale	33
Electron resolution model	10
Recoil model	41
Electron efficiencies	19
Backgrounds	6
PDF	20
Electroweak radiative corrections	7
Boson p_T	1
M_W	5
Total Systematic	61

CDF RunII 350 pb⁻¹ 2.032 \pm 0.073 GeV

PRL 100 071801 (2008)

Tevatron combined value without DØ Run II:

$\Gamma_W = 2.050 \pm 0.058$ GeV

Expect ~ 10 MeV improvement from including it

Standard Model prediction
and LEP result

(SM $\Gamma_W = 2.093 \pm 0.002$ GeV)

(LEP $\Gamma_W = 2.196 \pm 0.083$ GeV)

Summary

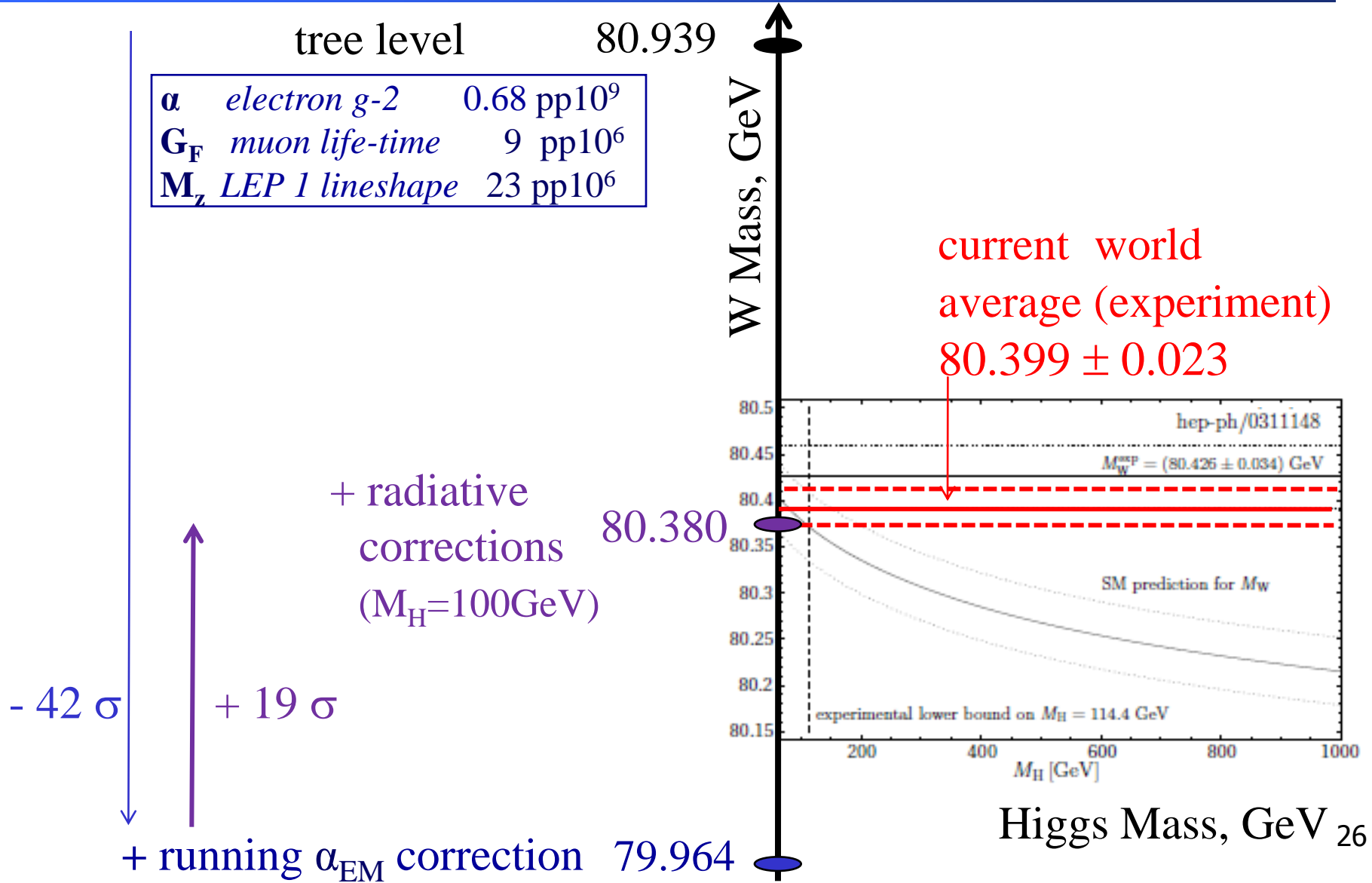
- W Mass measurement is crucial for constraining the Standard Model
- DØ recently published the most precise measurements of the W boson mass and width from a single experiment
- Comparable results published earlier by CDF
- Considering $M(W)$ prospects and its physics implications with the full Tevatron dataset as well as direct Higgs searches
→ we are in exciting time and place !
- More data are being analyzed, expecting significant improvements in precision soon
- Stay tuned for new results

BACKUP SLIDES

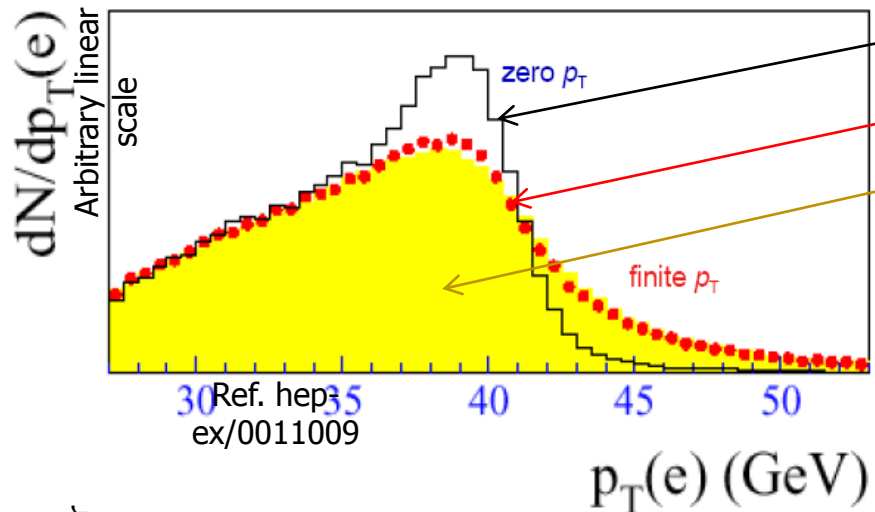
Main Differences between CDF and DØ M(W) Analyses

	CDF	DØ
Luminosity	0.2 fb ⁻¹	1.0 fb ⁻¹
Events	63964 W→eν 51128 W→μν	499830 W→eν
W Decay Channels	electron, muon	electron
Lepton Energy Scale	tracker	Z→ee calorimeter data
Interpretation	absolute M(W)	M(W)/M(Z) ratio
MC Closure Test		full analysis performed first on Monte Carlo
Beyond M(W)	M(W ⁺) and M(W ⁻) comparison (intriguing!)	

Effect of Corrections on M(W)



What Affects Observable Shapes

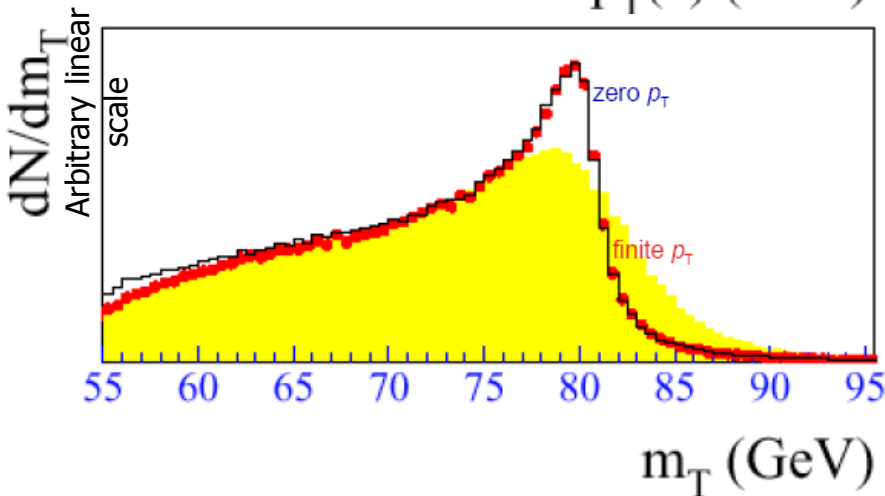


$P_T(W)=0$, no detector effects

$P_T(W)$ included

detector effects added

$p_T(e)$ most affected by $p_T(W)$



$$M_T = \sqrt{2E_T^l E_T (1 - \cos \Delta\phi)}$$

M_T most affected by measurement of missing transverse momentum

For W/Z production and decay both CDF and DØ use **ResBos** (Balazs, Yuan; Phys Rev D56, 5558,1997);
 For photons CDF:**WGRAD** (Baur, Keller, Wackerth PRD59, 013002 (1998)),
 DØ: **Photos** (Barbiero, Was, Comp Phys Com 79, 291 (1994))

M(W) Measurement Strategy

Generator-Level $W \rightarrow e\nu$ Input

Fast Monte Carlo Detector Model

electron

recoil

background modeling

repeat with many M(W) hypotheses

modeled M_T, P_T^e, MET

FIT

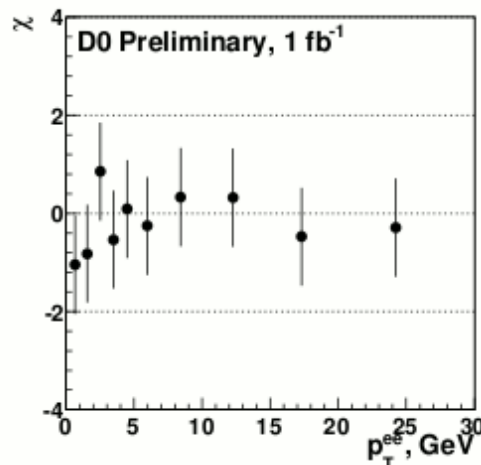
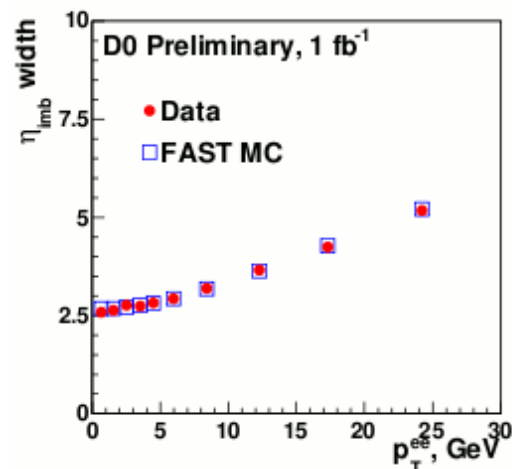
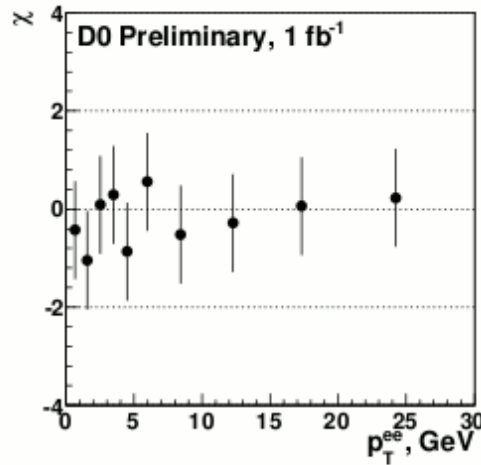
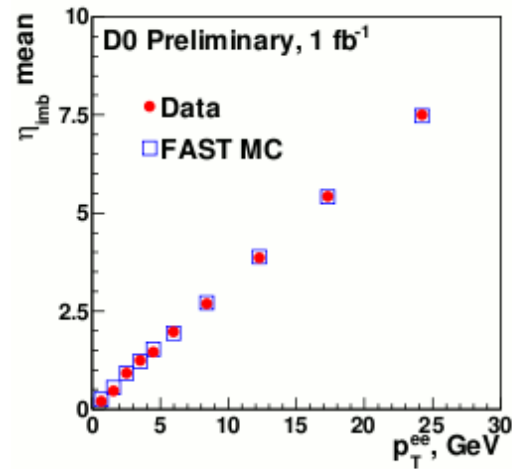
understand,
calibrate
detector



- blinded measured M(W) value
- evaluate uncertainty
- collaboration approval
- un-blinding \Rightarrow result

Recoil Calibration

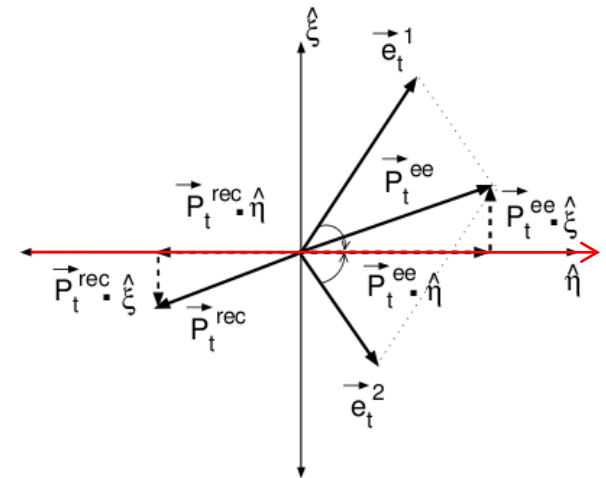
Final adjustment of free parameters in the recoil model is done *in situ* using balancing in $Z \rightarrow ee$ events and the standard **UA2 observables**:



in the transverse plane, use a coordinate system defined by the bisector of the two electron momenta.

$$\eta\text{-imbalance} : (\vec{P}_t^{ee} + \vec{P}_t^{\text{rec}}) \cdot \hat{\eta}$$

$$\xi\text{-imbalance} : (\vec{P}_t^{ee} + \vec{P}_t^{\text{rec}}) \cdot \hat{\xi}$$

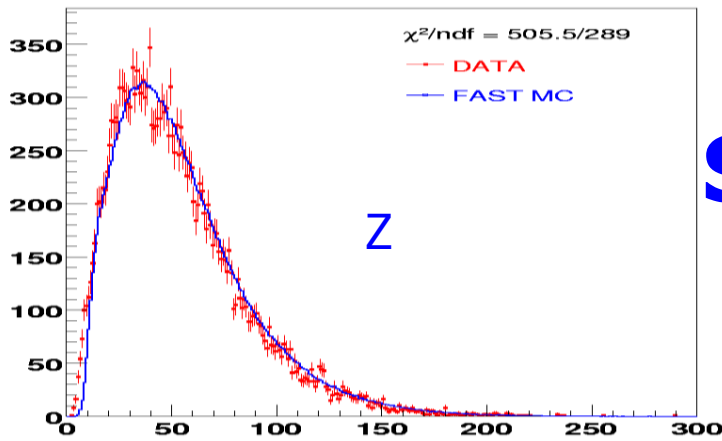


Stages of Electron Energy Calibration

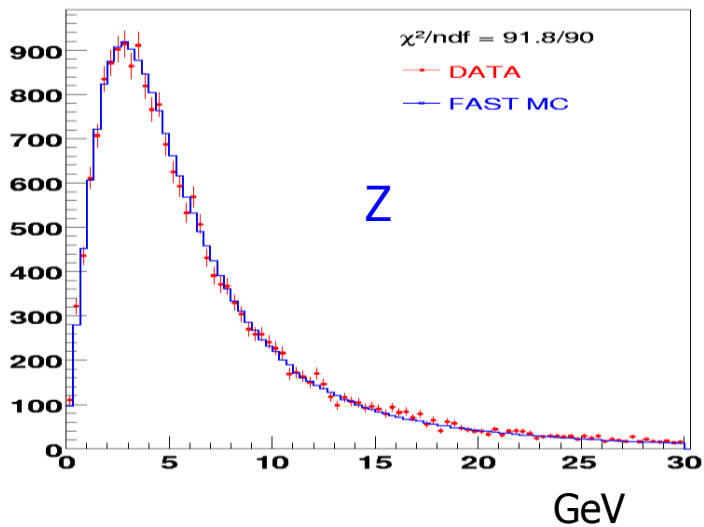
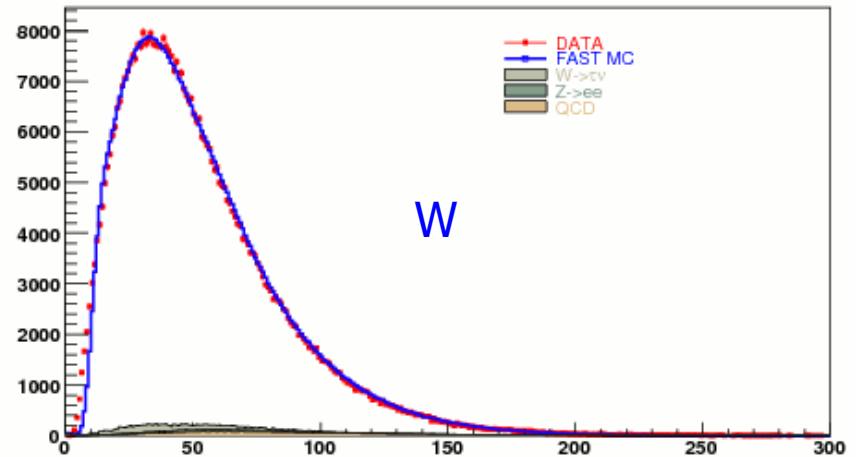
- Cell-level
 - pulser calibration (*ADC* \rightarrow *collected charge*)
 - sampling fractions (*collected charge* \rightarrow *total deposited energy*)
- Cluster – level
 - energy loss corrections
 - inter- ϕ calibration
 - η equalization and absolute scale
 - layer inter-calibration
- Final M_W calibration

$Z \rightarrow e e$ and $W \rightarrow e \nu$

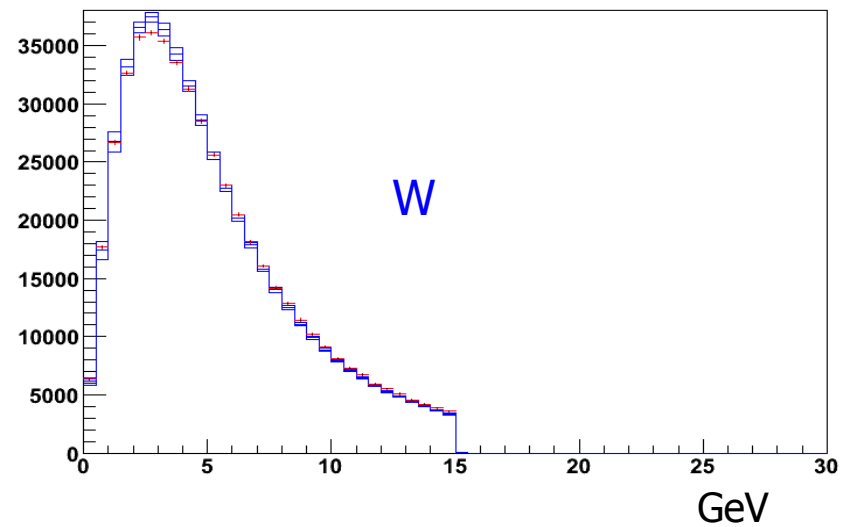
Data in red
MC in blue



SET



UT



GENERATOR-LEVEL INPUT 4-Vectors:

Electron

FSR Photon(s)

W boson

recoil modeling

electron modeling

merge electron
and photon(s)

PHOTON-RELATED MEASUREMENTS

Probability to Reach the Calorimeter
Photon Energy Response

position
in $D\phi$

BEAM SHAPE MEASUREMENT

smear

ELECTRON-RELATED MODELS

Electron Energy Response
Electron Energy Resolution
Electron Direction Resolution

efficiency
corrections

(non-electron) ENERGY CORRECTION

ELECTRON EFFICIENCY MEASUREMENTS

Trigger
EM ID
Tracking
“ U_{\parallel} Efficiency”, “Scalar ET Efficiency”

analysis cuts

OUTPUT: Modeled distributions of $M(W)$ observables

there is a “two-way”
dependence between
recoil model
and
electron model

Electron Energy Resolution

Electron energy resolution is driven by two components:

sampling fluctuations and constant term

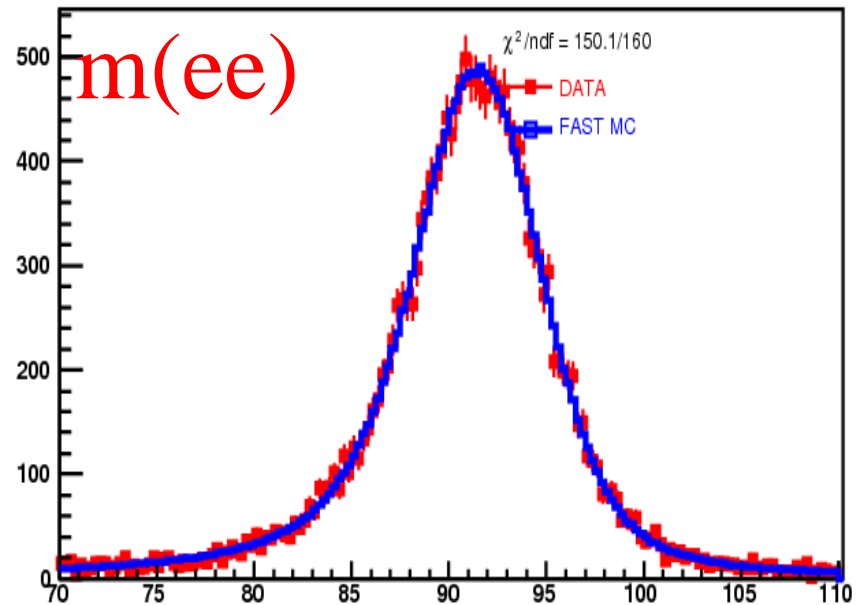
$$\frac{\sigma_{EM}}{E} = \sqrt{C_{EM}^2 + \frac{S_{EM}^2}{E} + \frac{N_{EM}^2}{E^2}}$$

Sampling fluctuations are driven by sampling fraction of CAL modules (well known from simulation and test-beam) and by un-instrumented material. Amount of material has been quantified with good precision.

Constant term is extracted from $Z \rightarrow ee$ data (fit to observed width of the Z peak).

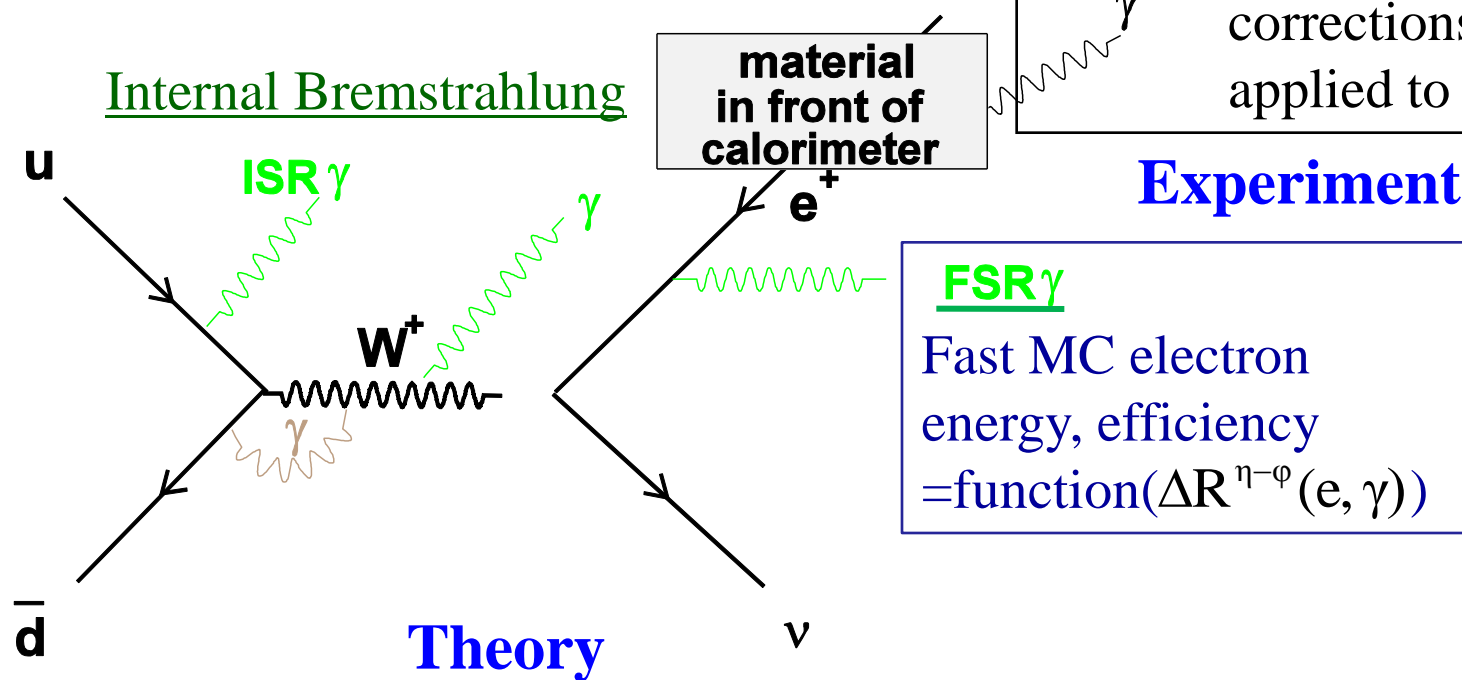
Result: $C = (2.05 \pm 0.10) \%$
in excellent agreement
with Run II design goal (2%)

ZCandMass_CCCC_Trks



Photons

Tool	Process	QCD	EW
RESBOS	W, Z	NLO	-
WGRAD	W	LO	complete $\mathcal{O}(\alpha)$, Matrix Element, ≤ 1 photon
ZGRAD	Z	LO	complete $\mathcal{O}(\alpha)$, Matrix Element, ≤ 1 photon
PHOTOS			QED FSR, ≤ 2 photons



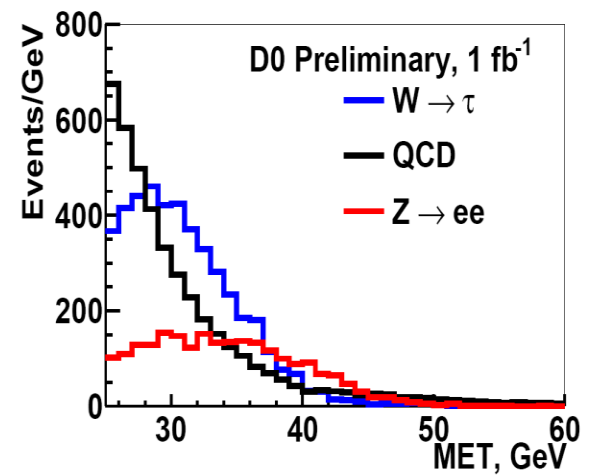
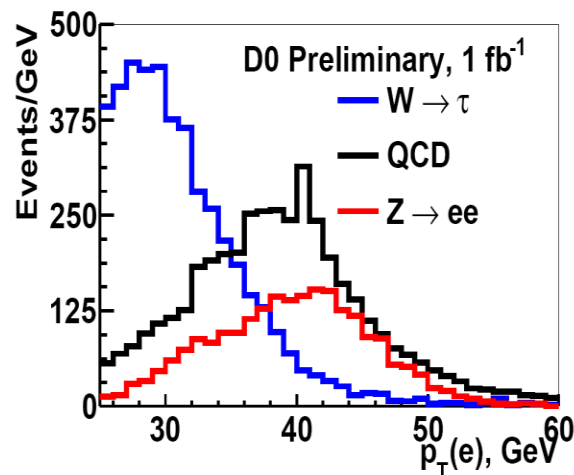
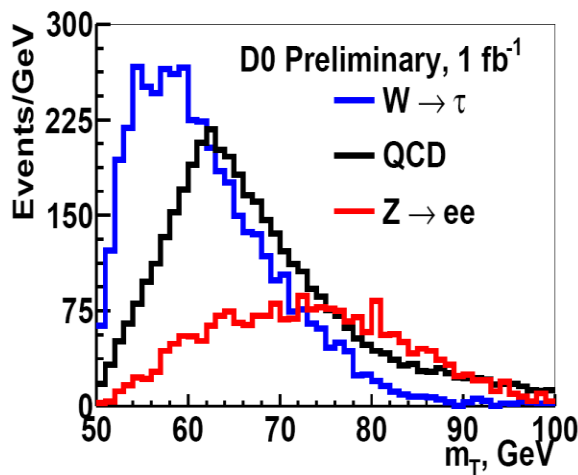
Leading EW effects: 1st and 2nd FSR photons -- modeled with PHOTOS.

Effect of full EW corrections: compare W/ZGRAD in full EW mode with FSR-only mode

Quality of FSR model: compare PHOTOS with W/ZGRAD in FSR-only mode

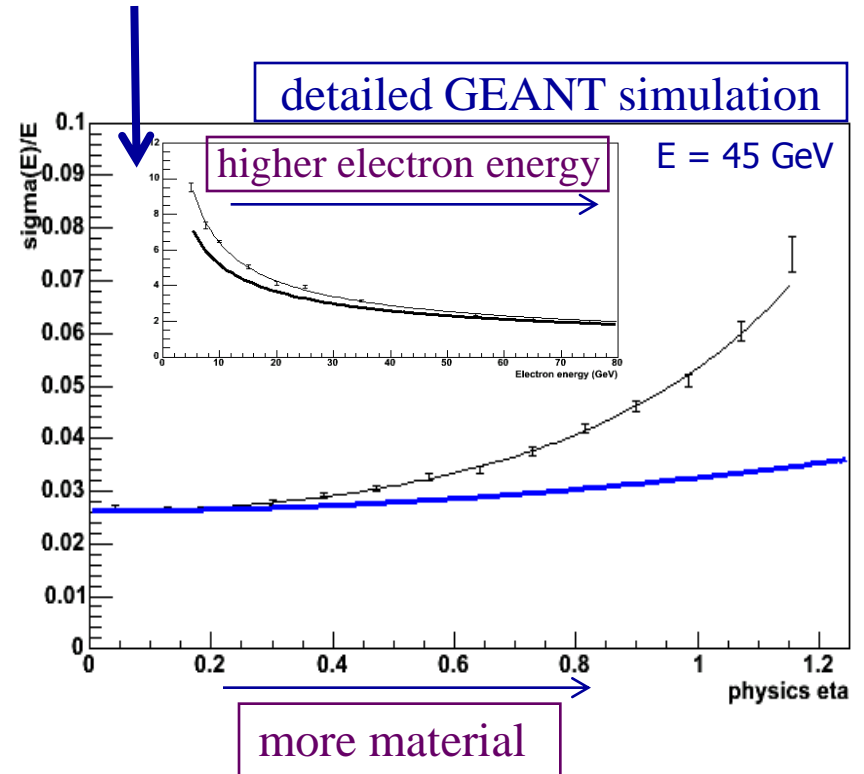
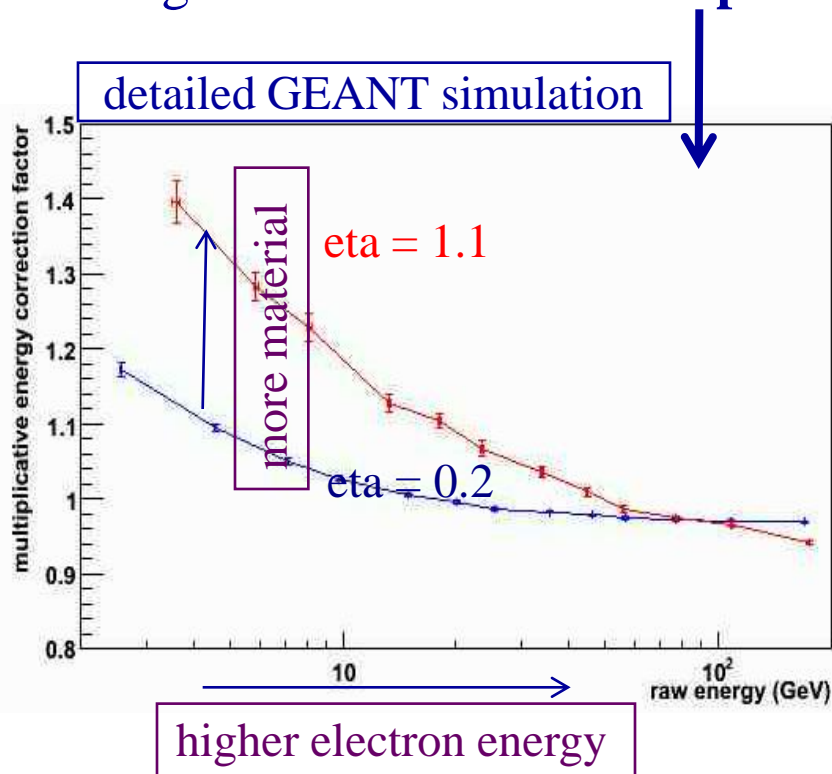
Backgrounds to $W \rightarrow ev$

- QCD (di-jet) (1.49 ± 0.3 %) : one jet fakes as an electron
 - determined from QCD data
- $Z \rightarrow ee$ (0.80 ± 0.01 %) : one electron lost in ICR (between central and end cap)
 - determined from $Z \rightarrow ee$ data
- $W \rightarrow \tau\nu$ (1.60 ± 0.02 %) : Taus decaying into $ev\nu$
 - determined from GEANT (full) MC
- **For all 3 observables: estimated backgrounds are added to Fast MC simulated signal**



Electron Response and Resolution

- Dead material in front of the calorimeter complicates shower sampling
- \Rightarrow Degradation of both the **response** and the **resolution**

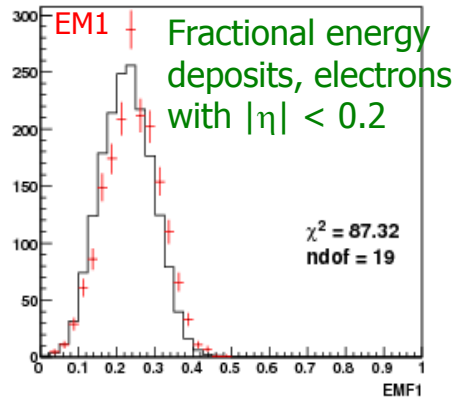


- The magnitude of the effect of the dead material depends on electron energy

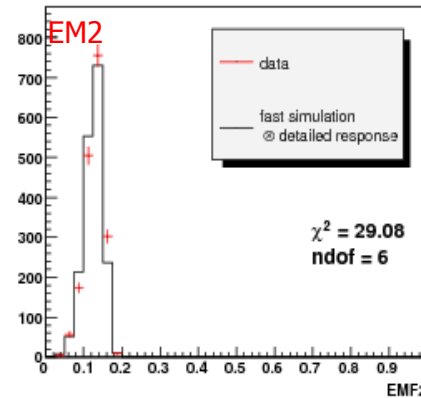
Before tuning of material model

Before tuning of material model:
distributions of fractional energy deposits
do not quite match between data and the simulation.

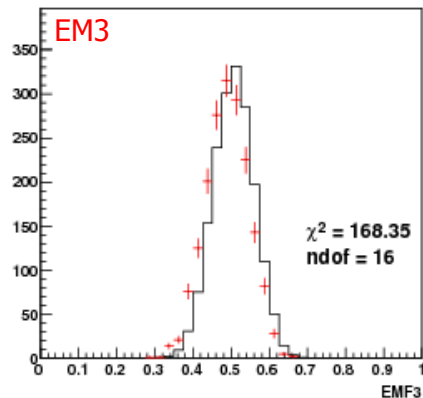
TOYEemf_1_10



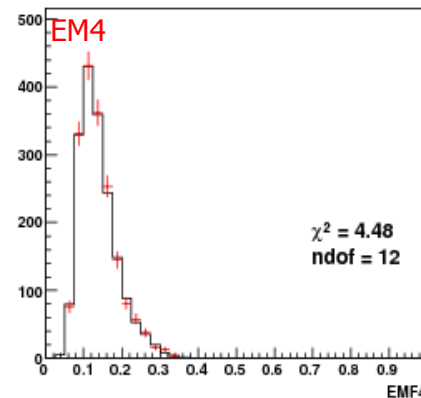
TOYEemf_2_10



TOYEemf_3_10

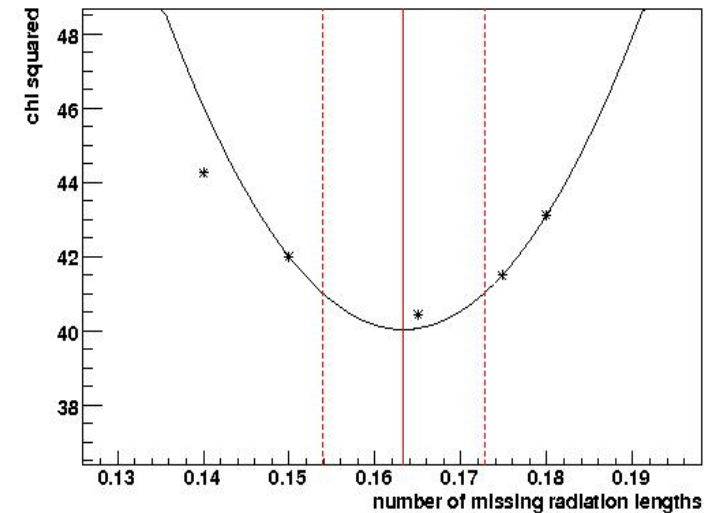


TOYEemf_4_10



FIT

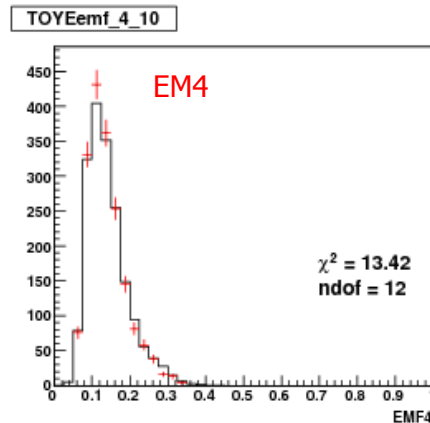
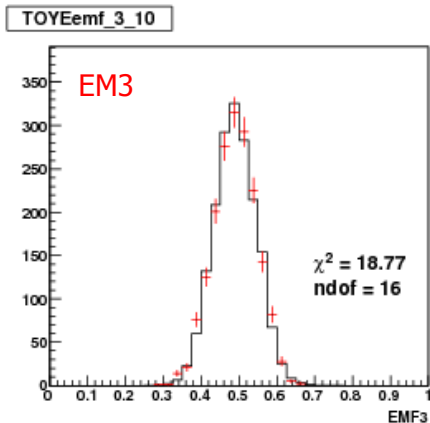
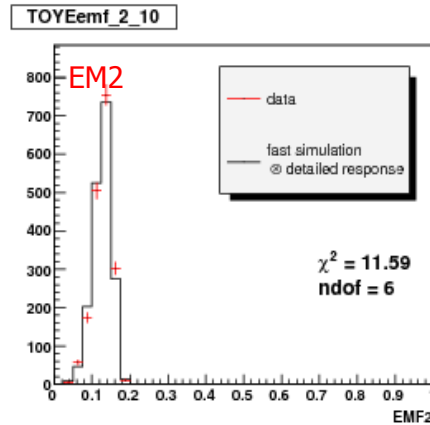
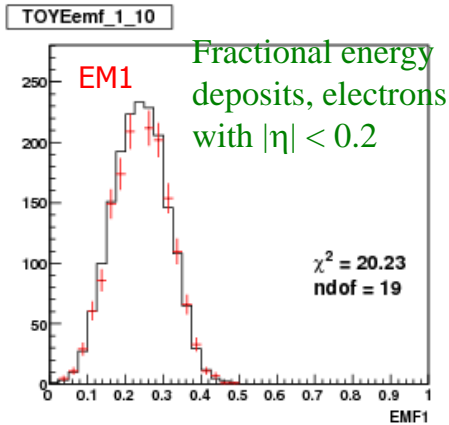
Fit for missing nX_0 from longitudinal profiles $\ln Z \rightarrow e e$



Amount of fudge material to
within less than $0.01X_0$!

After Tuning of Material Model

After tuning of material model:
distributions of fractional energy deposits
are very well described by the simulation.



As a cross-check:
Repeat fit for nX_0 ,
separately for each EM layer.
Good consistency is found.

