

“Higgs Impostors at the LHC”

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If the Vacuum is a substance

Shake it

Its vibrations are QUANTA

The Higgs

Τὸ Κενόν

LHC = MSV

Run the
machine

Find something
looking like a H



A visualization of particle tracks, likely from a detector, showing a central point with many lines radiating outwards. The lines are colored in shades of yellow, orange, and green, suggesting different particle types or energies. The tracks are dense and chaotic, radiating from a central point.

What the
Higgs
is this?

Find a “Higgs” Candidate Particle

$$\sigma[\text{Prod}] \times \text{BR}(s) \sim \text{STANDARD}$$

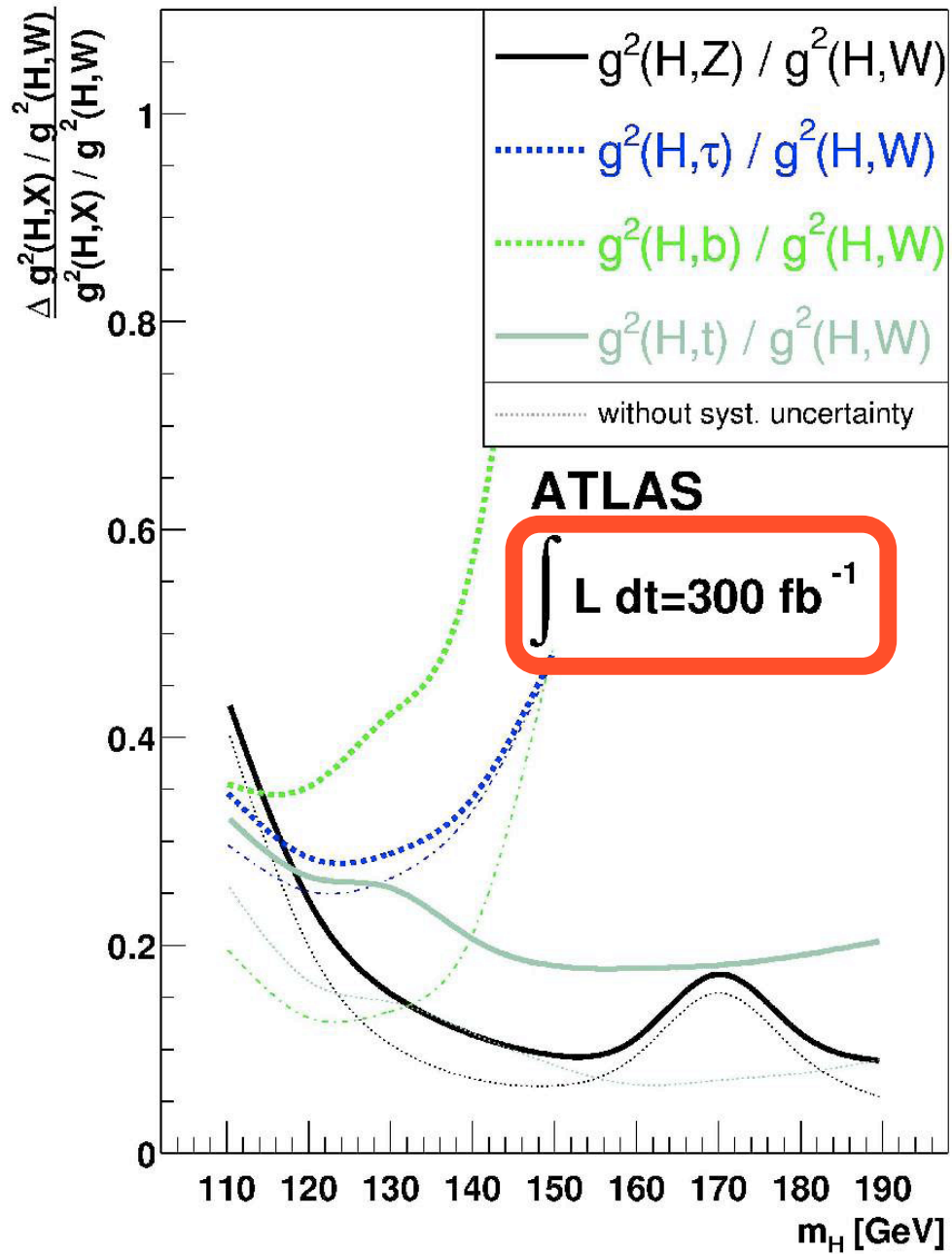
Is it *the Higgs*
or an Impostor?

Very L-dt
demanding

What is its J, P, C ???

What is not its J, P, C ???

Is it Pure J^{PC} ? Mixed? Compo
- site?



Duhrssen, ATL-
PHYS-2003-030

$$\sqrt{s} = 14 \text{ TeV}$$

Motivation ?

— The **currently-available** data-analysis “**protocols**”,
are not demonstrably the best one could use

+ Surely experimentalists are
planning to do much better

∴ **It pays TO DO IT RIGHT ... NOW!!**

+ **Some room for improvement :-)**

To be realistic:

A

Competition



The contest:

- **Team 1 is doing things “thoroughly” from Starters**
- **Team 2 is applying “shortcut” analysis methods**

*Teams may or may not
belong to the same experiment*

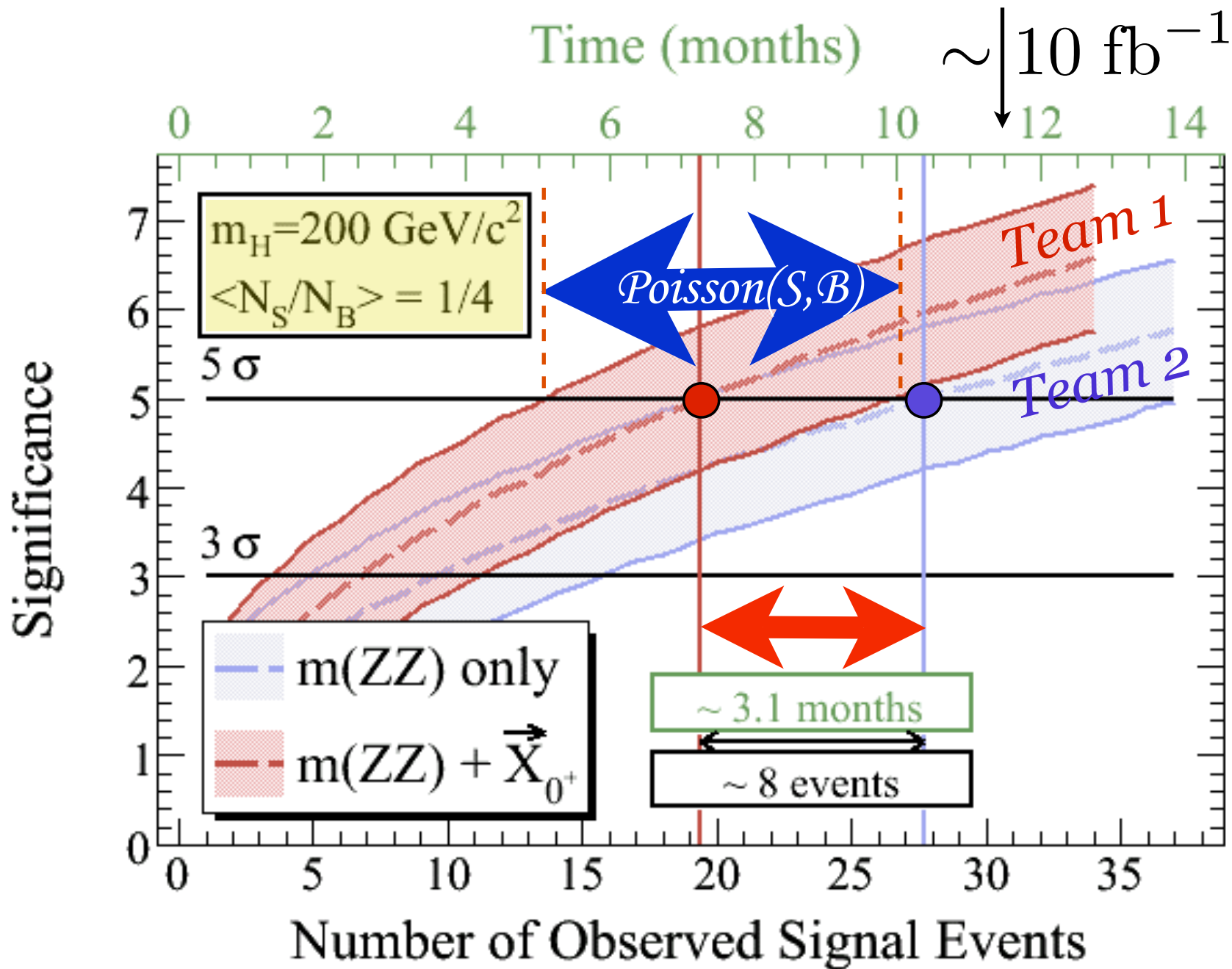
0^+ *Discovery-time Plots*

● $\sqrt{s} = 10 \text{ TeV}$; @!!!&*** ?

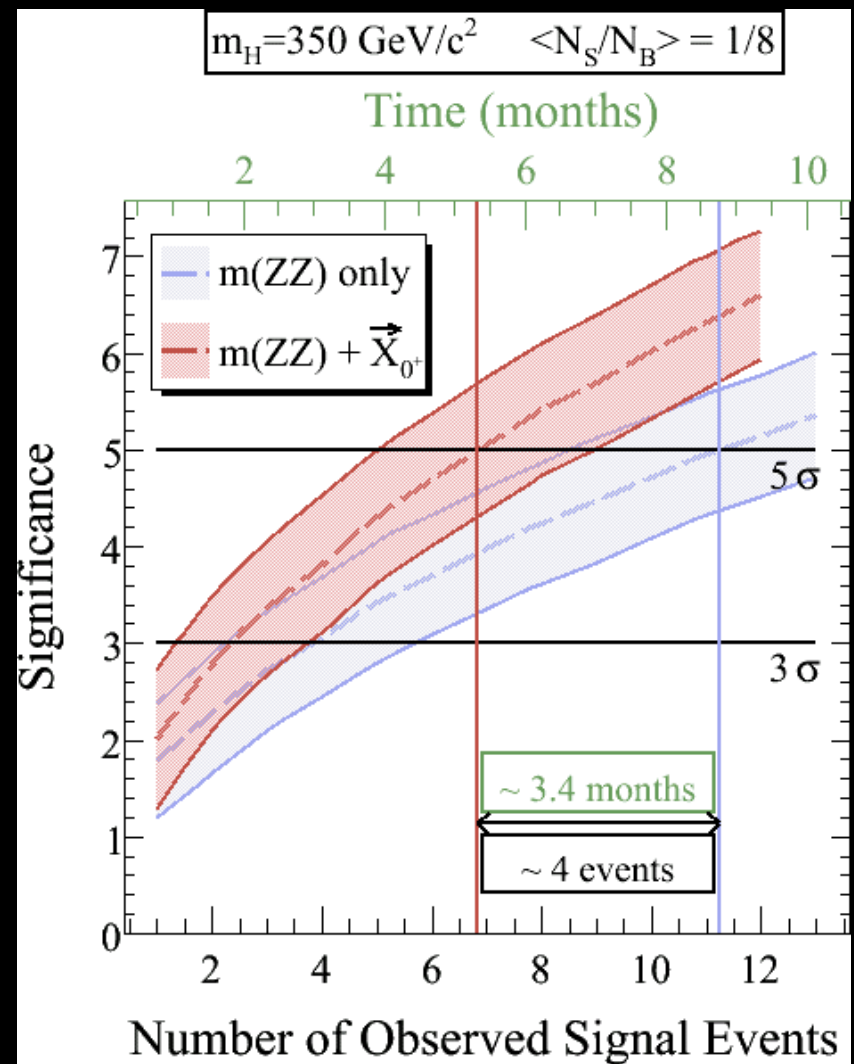
● $L = 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$

● *Snowmass factor of 3 (LHC start)*

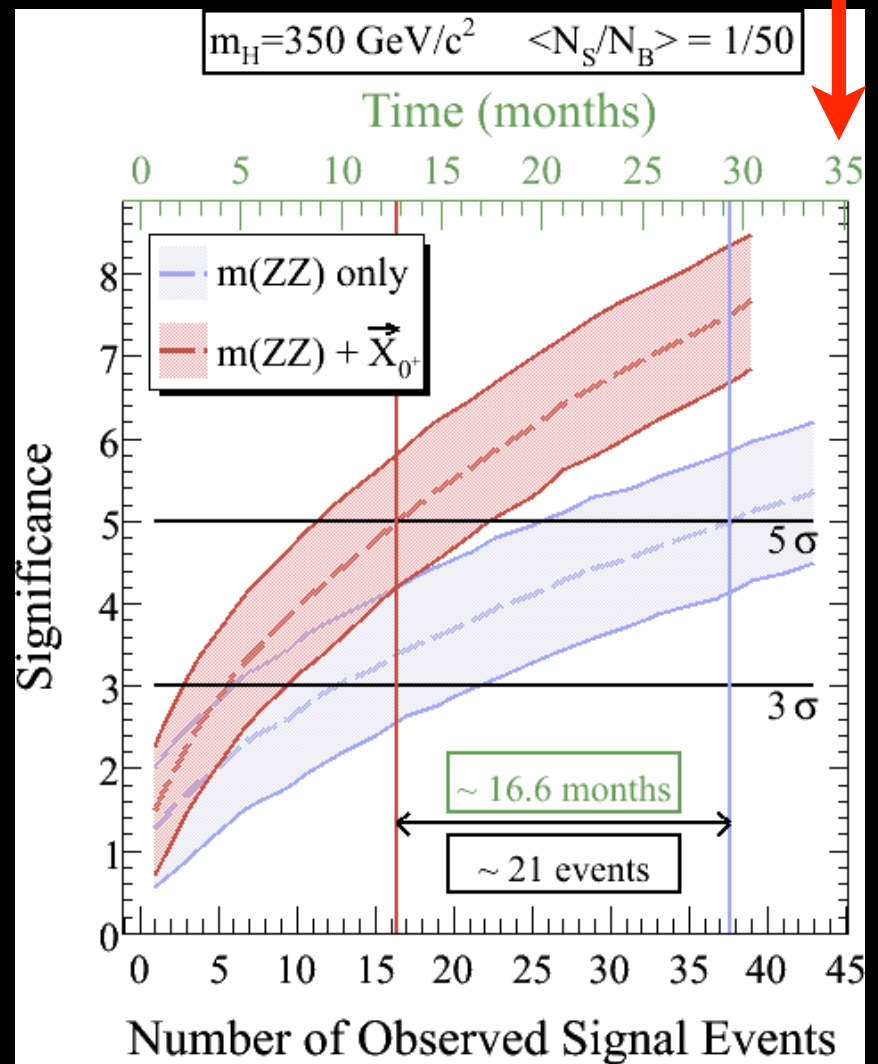
● **Background: Currently estimated**



$\sim 30 \text{ fb}^{-1}$



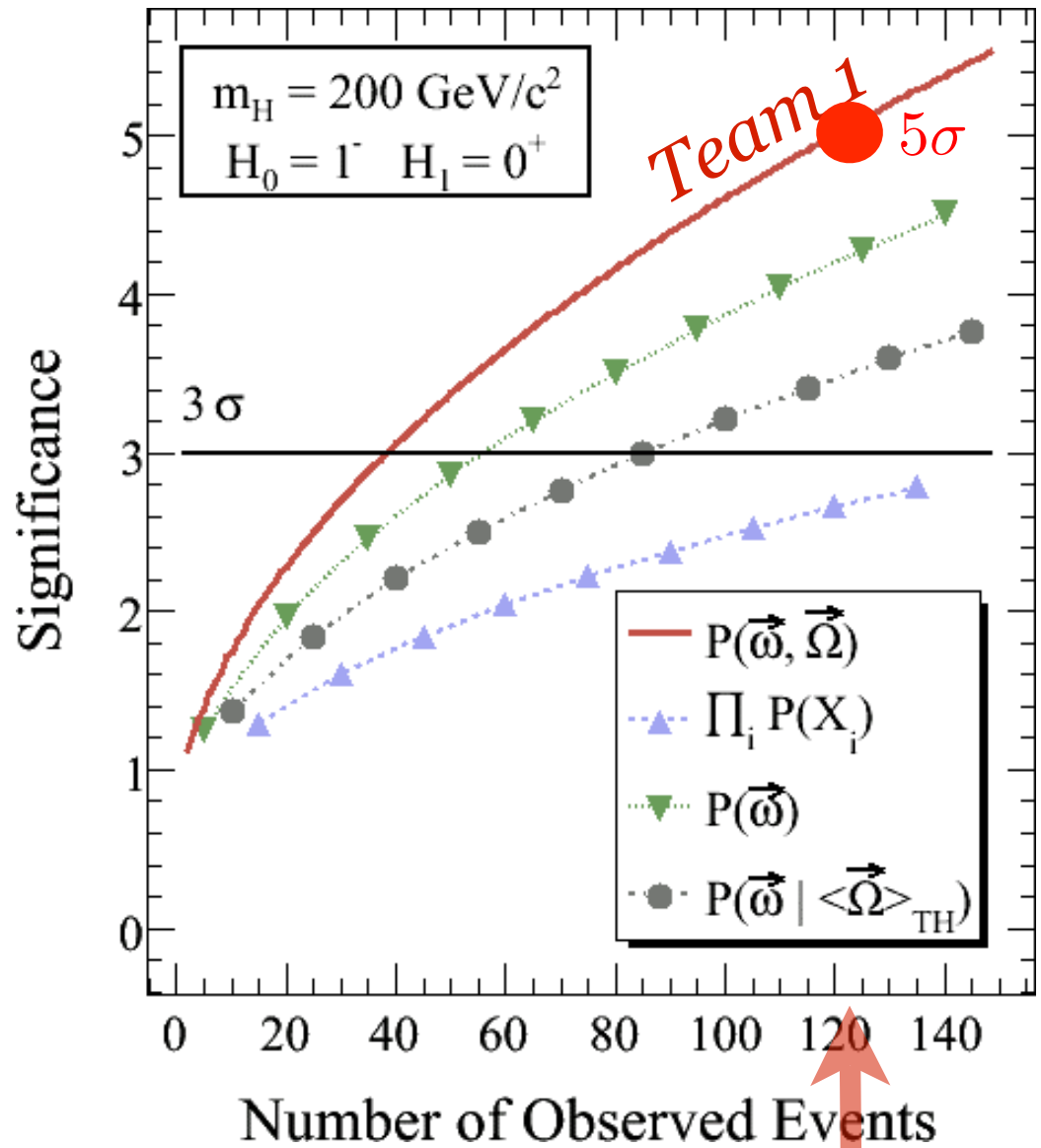
Nominal BackGround



~ 6 times more BG

While gathering **significance faster, Team 1 is checking agreement with $J^P = 0^+$**

With a few extra lines of code, Team 1 is checking whether the “object” is an **impostor, e.g.:**

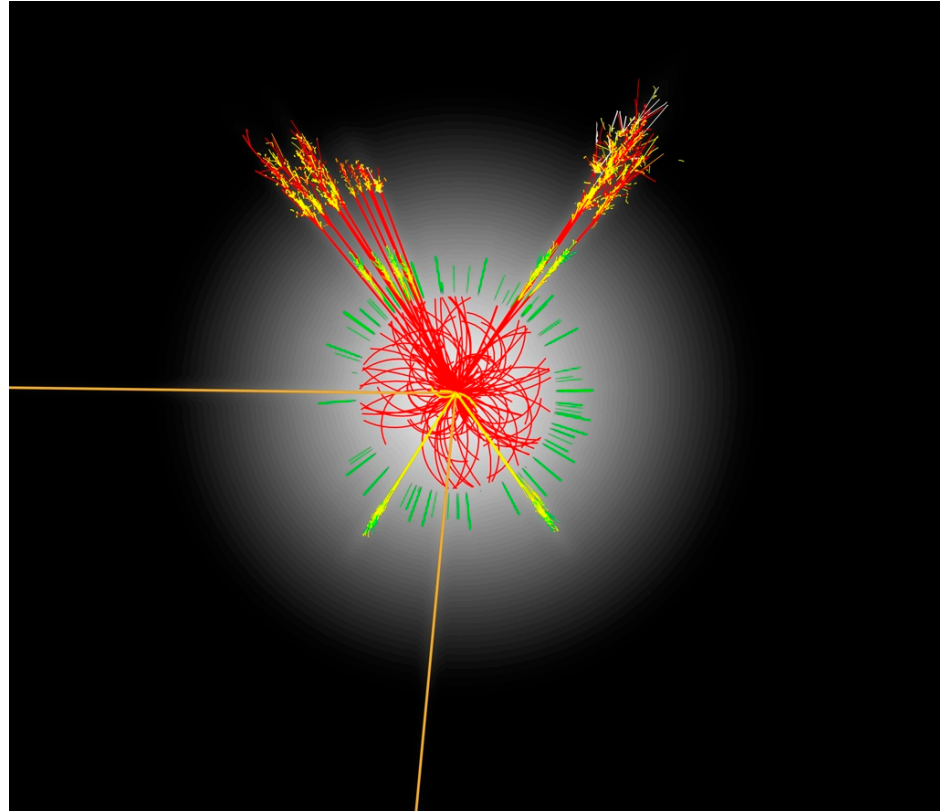


$\sim 40 \text{ fb}^{-1}$

**Back
to
all
this
in
detail**

We ARE
“translating”
to #-standard
deviations,
but NOT assuming
that anything is
Gaussian

*Whaaat
am I
talking
about ?*



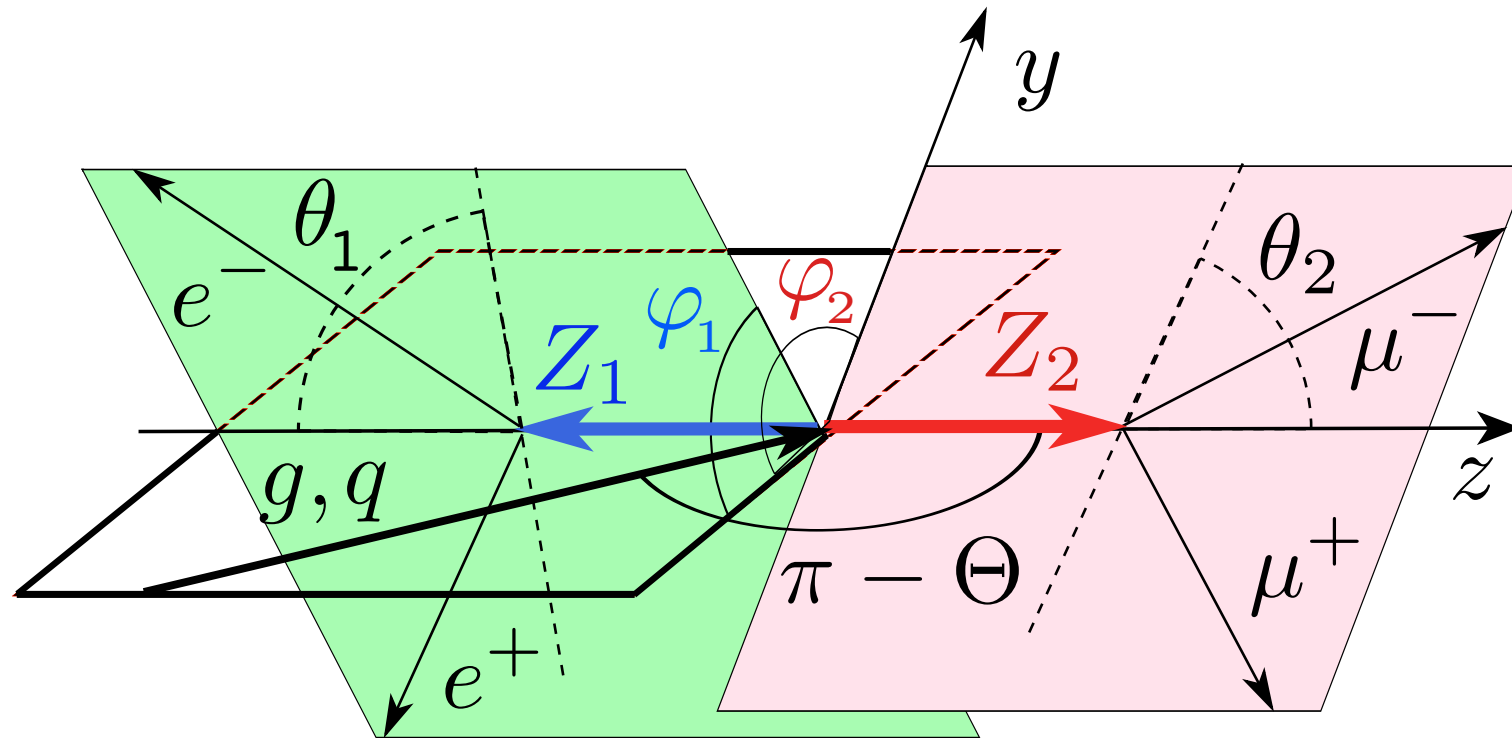
H or $HI \rightarrow ZZ$ or ZZ^*

$Z, Z^{(*)} \rightarrow \mu^+ \mu^-$

$(e^+e^-$

exercise)

H (HI) Rest System (undo η and p_T boosts)



$$M^* \text{ in } H(HI) \rightarrow ZZ^*$$

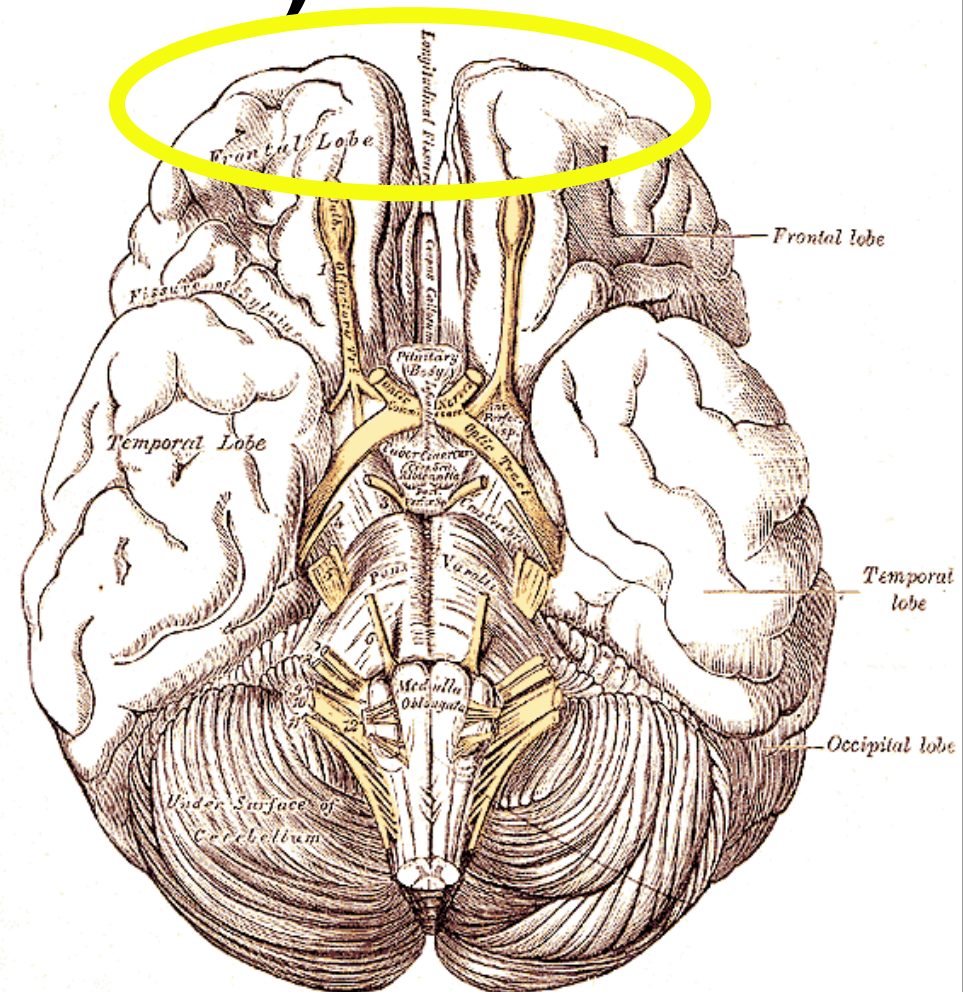
$$\vec{\omega} \equiv \{\cos \theta_1, \cos \theta_2, \varphi \equiv \varphi_2 - \varphi_1\} \quad \text{Z-pair decays}$$

$$\vec{\Omega} \equiv \{\cos \Theta, \Phi \equiv \varphi_2\} \quad \begin{array}{l} \text{Z-pair} \\ \text{production} \end{array} \quad \begin{array}{l} \text{6 "handles" !!!} \\ \text{6 dimensions !??} \end{array}$$

Neural Networks (NNWs)

NNWs that
know:

- What they are doing
- How
- Why



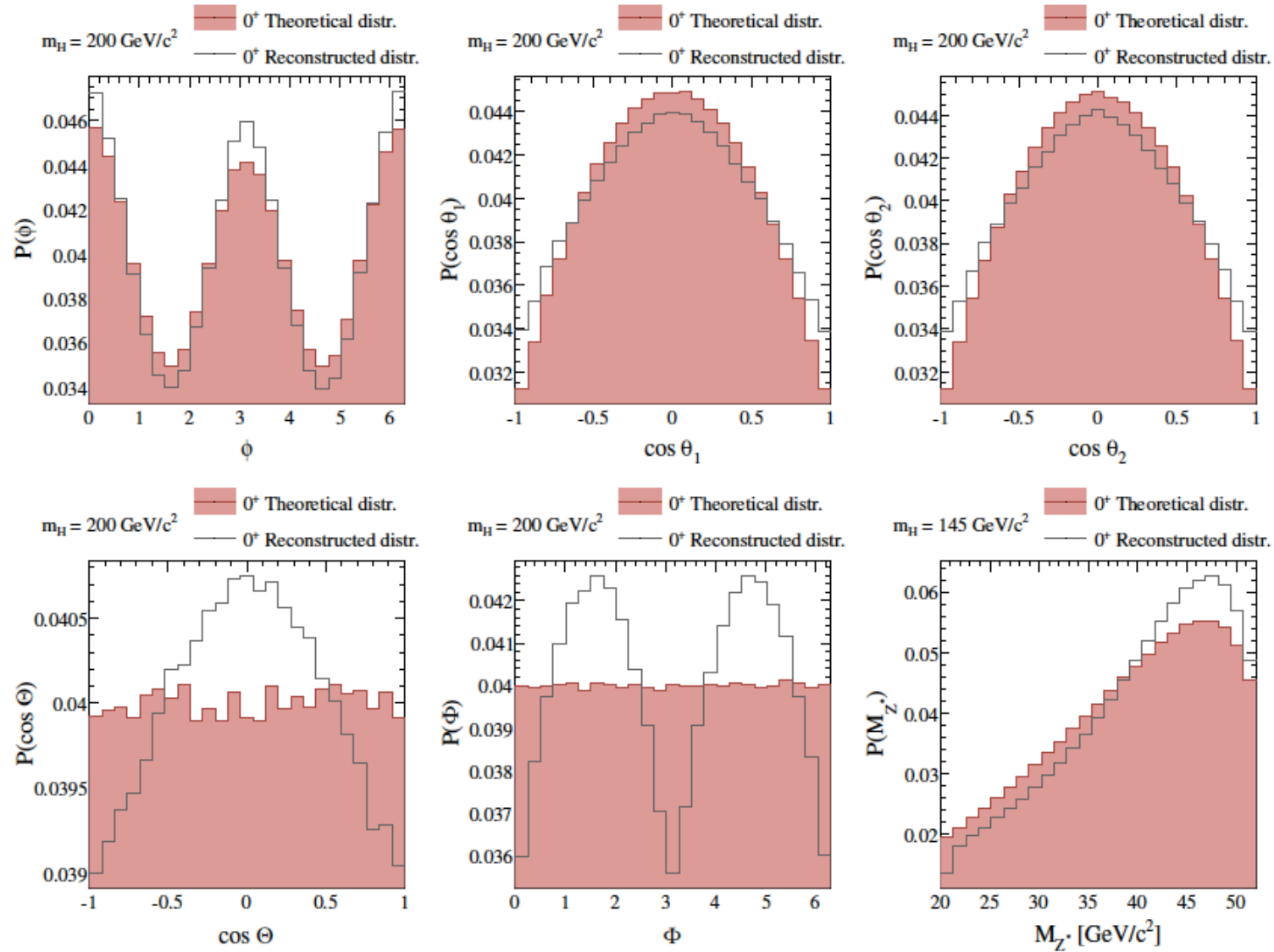



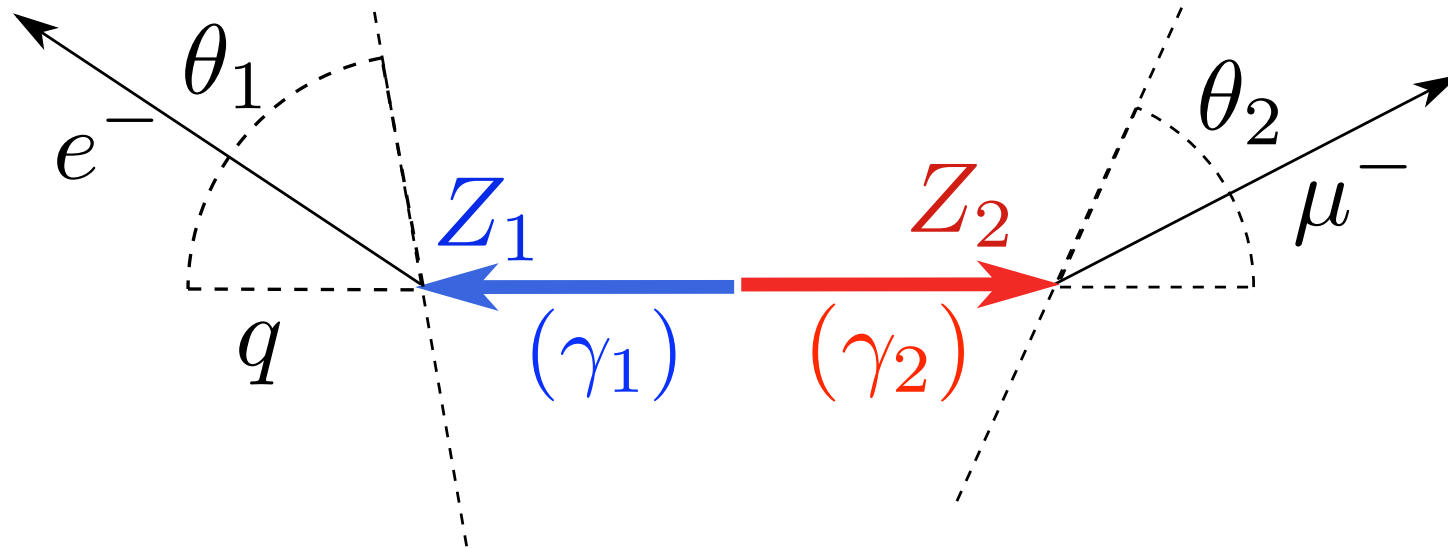
FIG. 24: Kinematic distributions for the variables \vec{X} used in this analysis for a SM Higgs with mass $200 \text{ GeV}/c^2$. The filled histograms who the one dimensional projected distributions of each of these variables as described by the analytic matrix element squared PDF's. The unfilled histograms (black lines) show the same one dimensional projections for reconstructed events (muon kinematics are smeared) for events that have passed the signal event selection (introducing acceptance effects). All distributions are normalized to have an integral of 1.

- To OPTIMIZE  J, P, C properties of the object and its couplings with an absolute MINIMUM of extra assumptions

“Pessimise”:

- WHATEVER the object happens to be:
- Not to use relative BRs (more than one H !)
- Assume η and p_T distributions \sim Standard (actually, roughly expected)

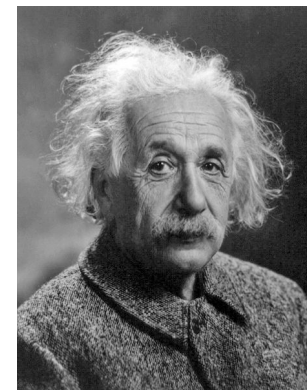
*Why is this
so deeeeeeply
interesting?*



$$P(\cos \theta_1, \cos \theta_2)$$

$$\hat{P}(\cos \theta_1) \neq P(\cos \theta_1, \cos \bar{\theta}_2)$$

Spooky Action at a distance



What used to be
paradoxes (*EPR*)

first became the
paradigms of QM

and are now procedures
for FASTER- { SEARCH
and CHARACTERIZATION }

● $\mathcal{L}\text{-inv} =$

$X g_{\mu\nu}$ **Standard**

Spin 0

$H(k)$

$Z^\mu(p_1)$

$Z^\nu(p_2)$

$$+(P + iQ)\epsilon_{\mu\nu\alpha\beta} \frac{p_1^\alpha p_2^\beta}{M_Z^2}$$

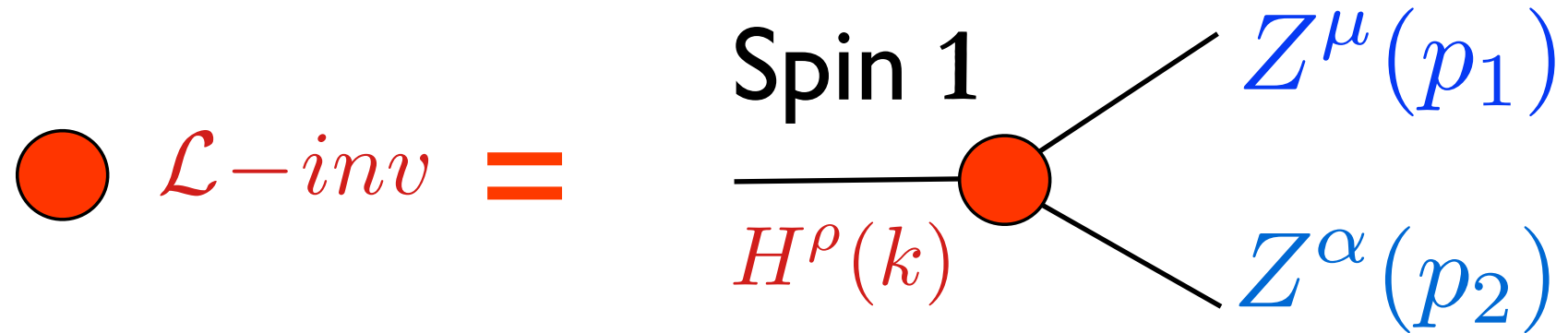
Pseudoscalar

$$-(Y + iZ) \frac{k_\mu k_\nu}{M_Z^2}$$

Derivative (Composite)

$$L = \frac{1}{\Lambda} H (A_1 \vec{W}_{\mu\alpha} \cdot \vec{W}^{\mu\alpha} + A_2 B_{\mu\alpha} B^{\mu\alpha})$$

$$+ \frac{1}{\Lambda} H i \epsilon^{\mu\alpha\sigma\tau} (A_3 \vec{W}_{\mu\alpha} \vec{W}_{\sigma\tau} + A_4 B_{\mu\alpha} B_{\sigma\tau})$$

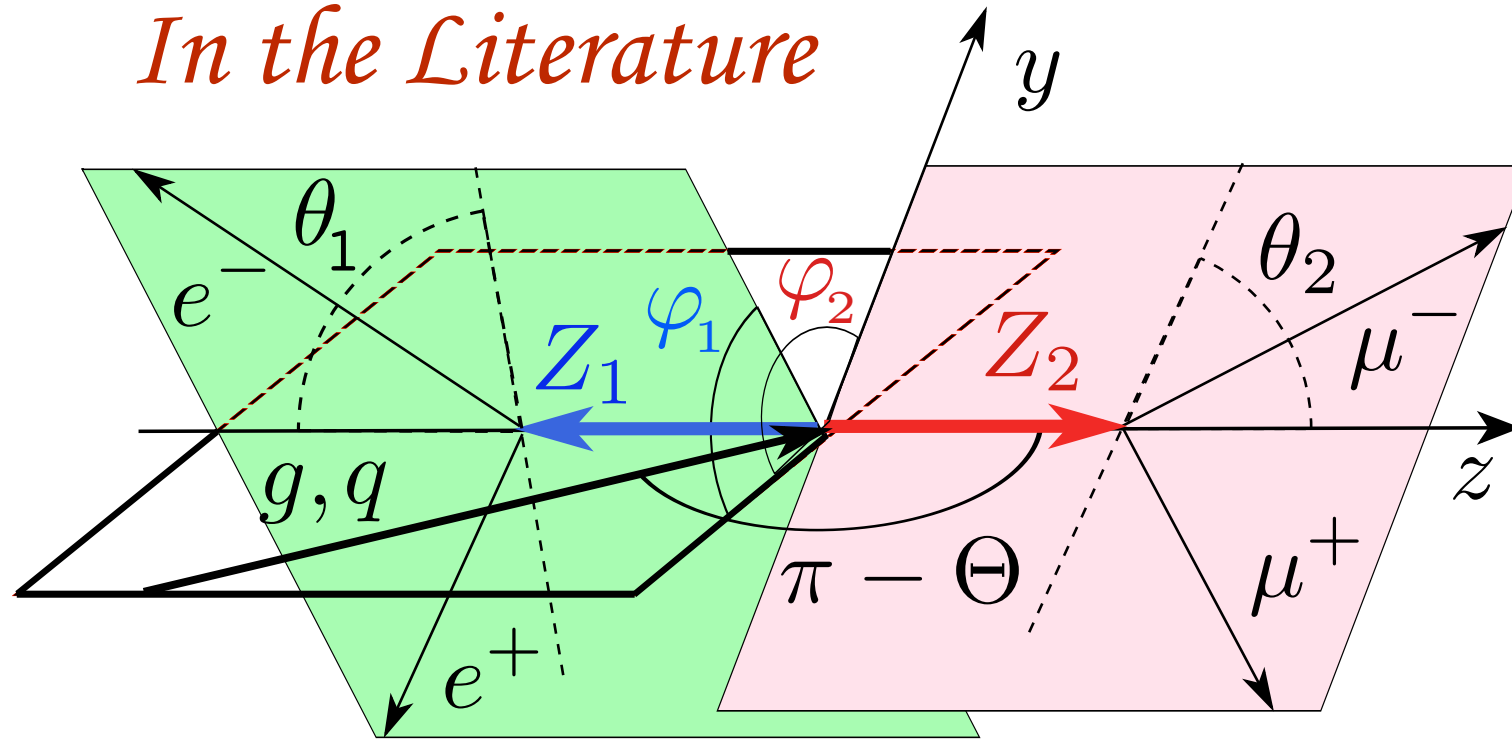


$$X (g^{\rho\mu} p_1^\alpha + g^{\rho\alpha} p_2^\mu) \quad \mathbf{Vector}$$

$$+ (P + iQ) \epsilon^{\rho\mu\alpha} (p_1 - p_2) \quad \mathbf{Axial}$$

$$\begin{aligned}
 L &= \frac{1}{\Lambda^2} (\partial^\mu H^\alpha + \partial^\alpha H^\mu) (A_1 \vec{W}_\mu^\lambda \cdot \vec{W}_{\alpha\lambda} + A_2 B_\mu^\lambda B_{\alpha\lambda}) \\
 &+ \frac{1}{\Lambda^2} \epsilon^{\mu\nu\alpha\rho} [A_3 (\vec{W}_\mu^\lambda \overleftrightarrow{D}_\alpha \vec{W}_{\nu\lambda}) H_\rho + A_4 (B_\mu^\lambda \overleftrightarrow{\partial}_\alpha B_{\nu\lambda}) H_\rho]
 \end{aligned}$$

In the Literature



$$\vec{\omega} \equiv \{\cos \theta_1, \cos \theta_2, \varphi \equiv \varphi_2 - \varphi_1\}$$

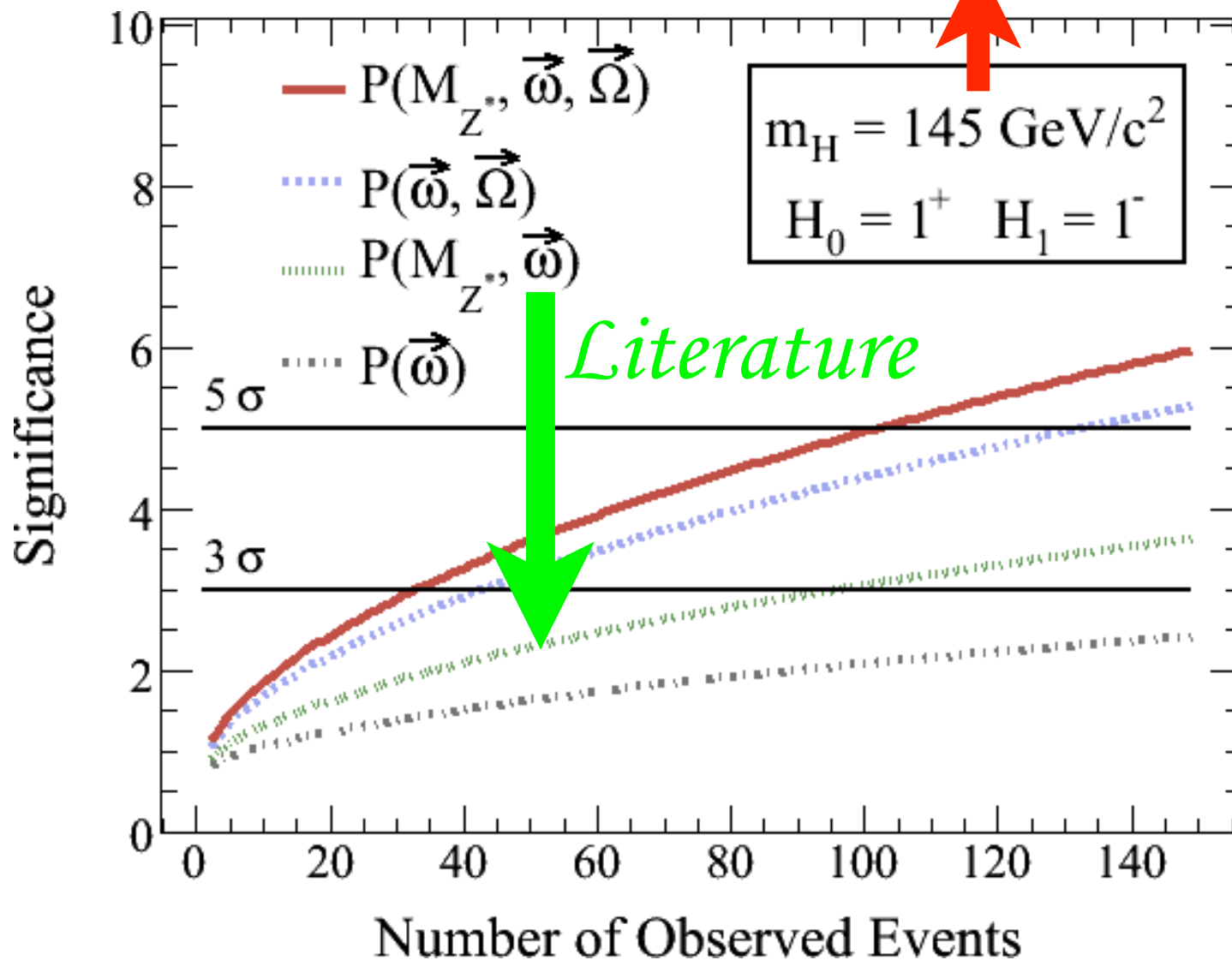
Lepton-
angles: Kept

$$\vec{\Omega} \equiv \{\cos \Theta, \Phi \equiv \varphi_2\} \quad (\text{Z-pair})\text{-angles: Averaged}$$

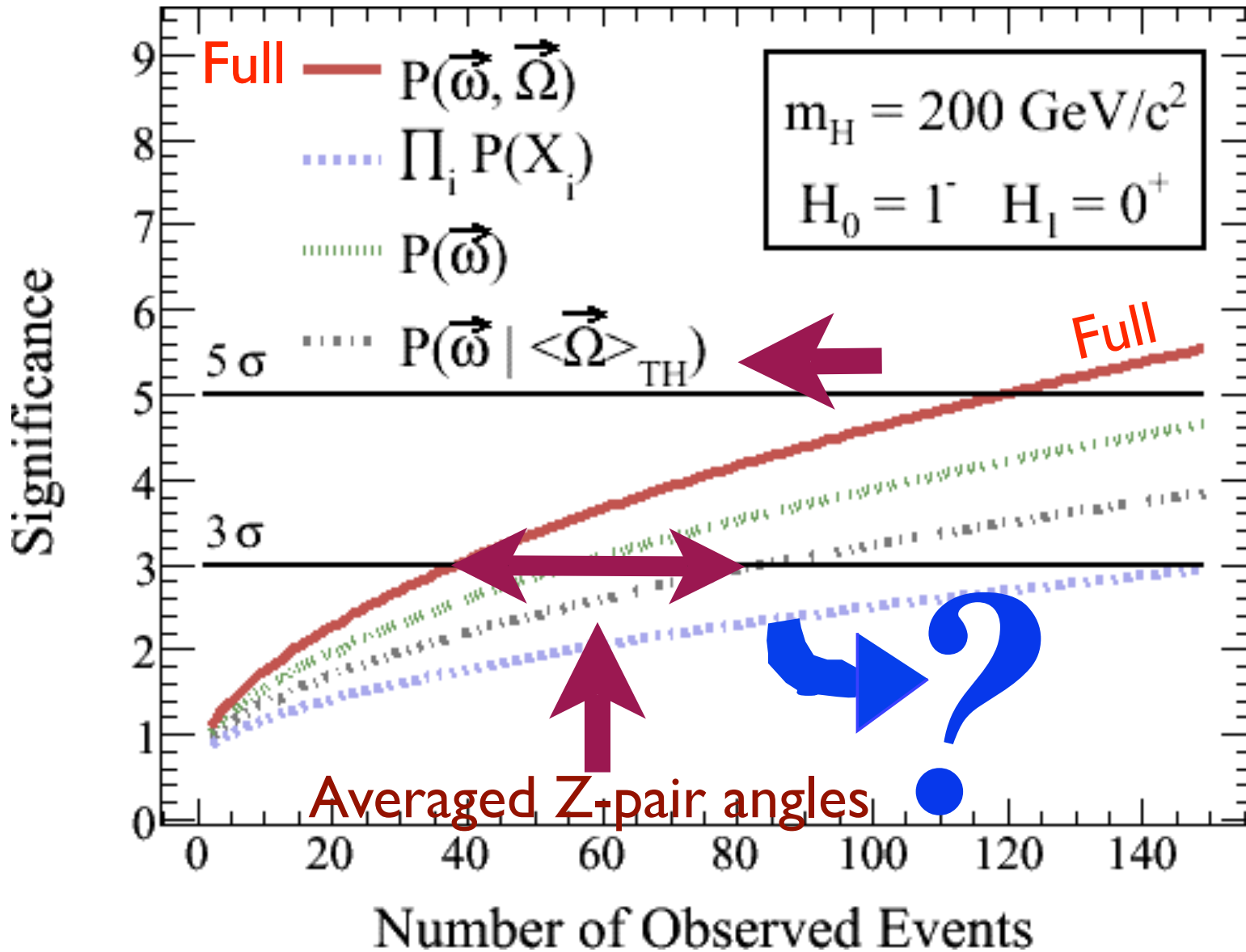
Deletes polarization-memory for spin > 0
Good only for uniform 4π acceptance

Median significance curves

$H \rightarrow ZZ^*$



DIS-Favouring VECTOR interpretation of SCALAR signal



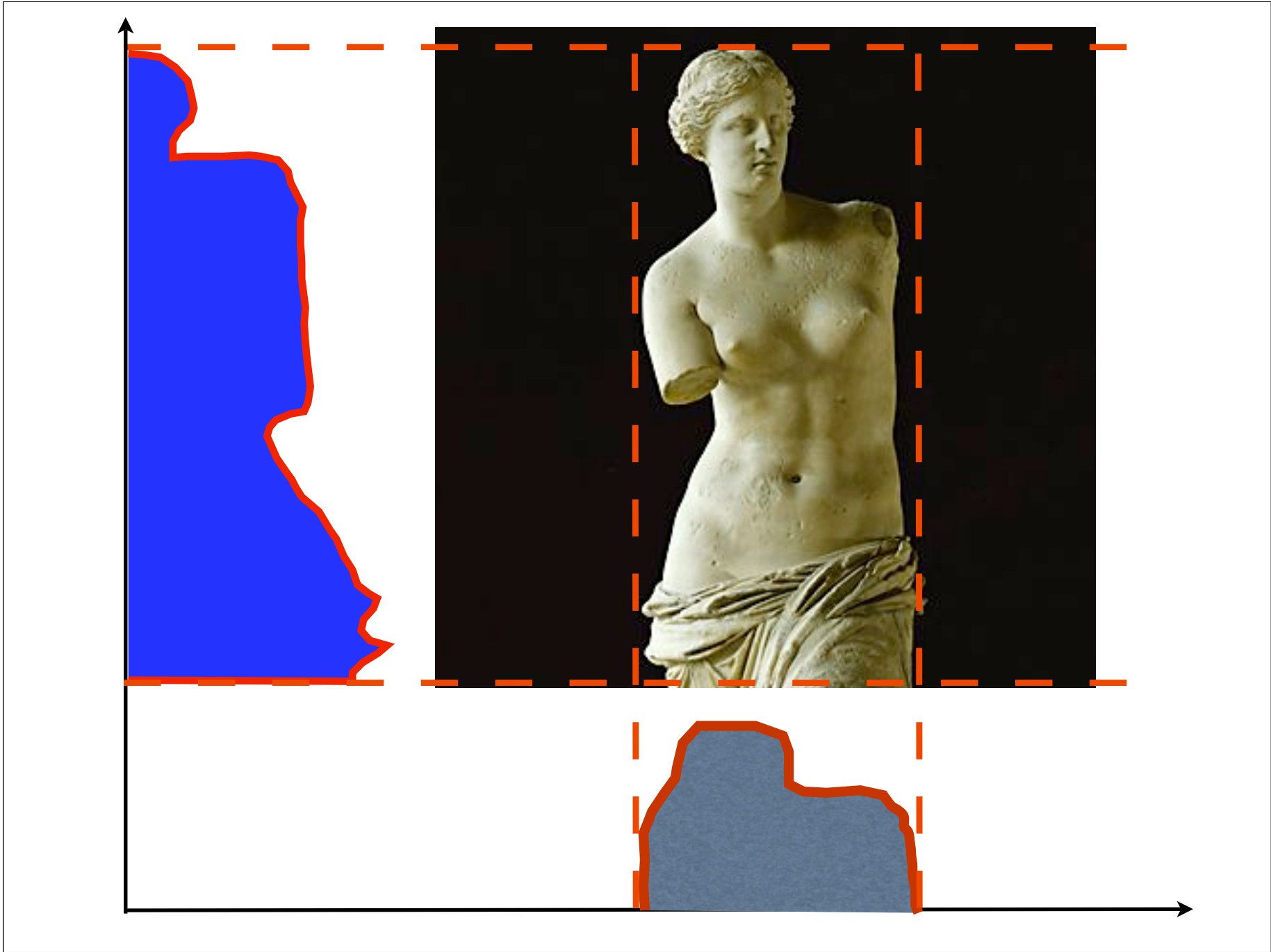
To handle multi-dimensional PDFs and their likelihoods, occasionally suggested to:

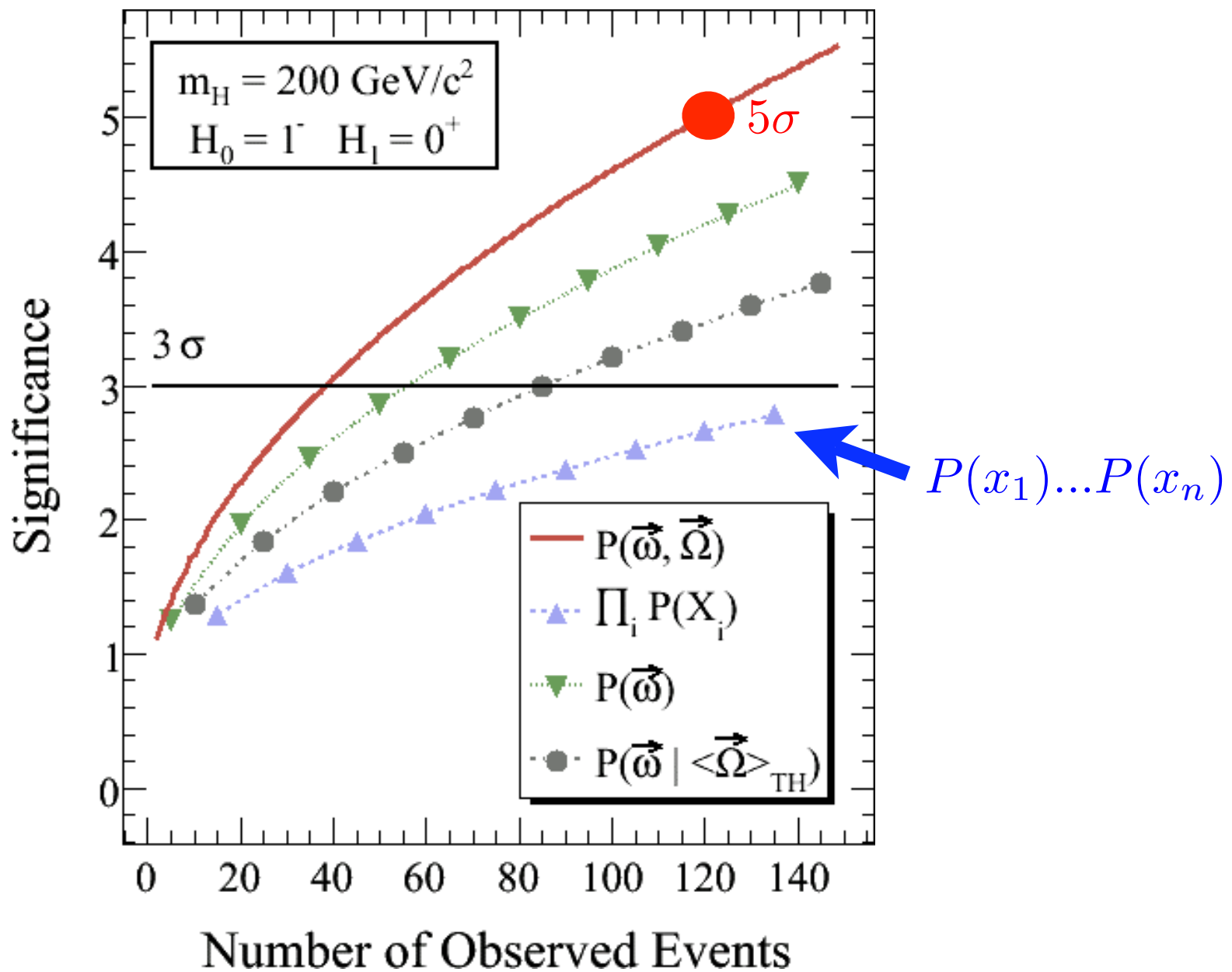
$$P(x_1, \dots, x_n)$$

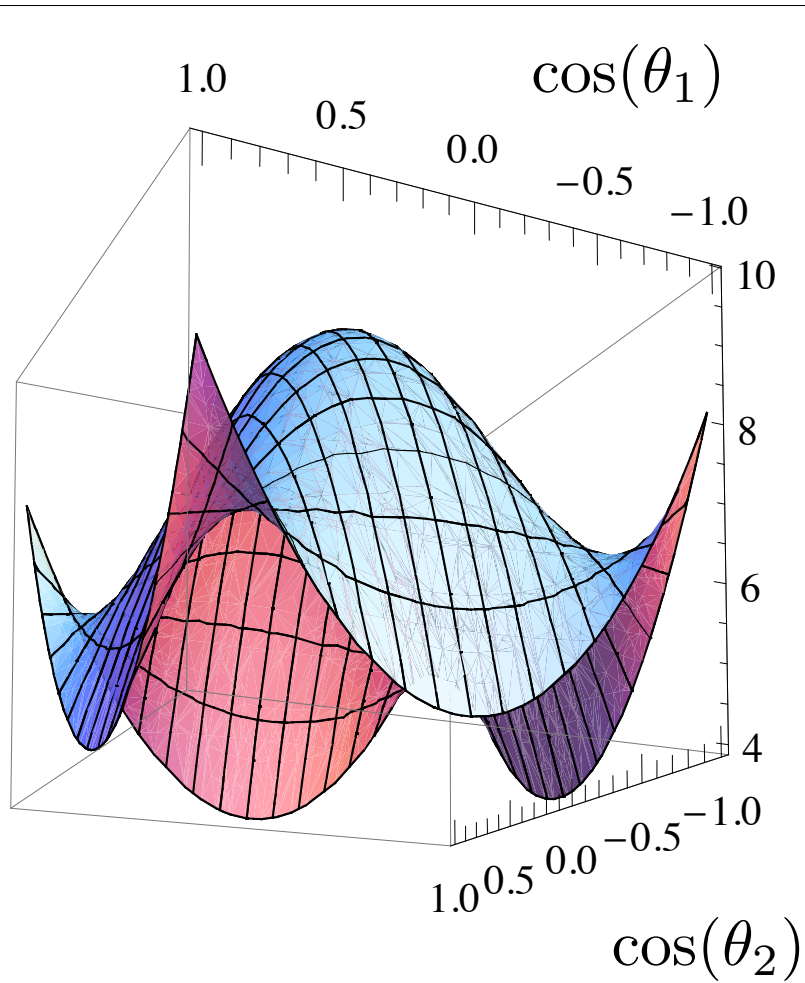
$$P(x_1) = \int P dx_2 \dots dx_n$$

$$\ddots$$
$$P(x_n) = \int P dx_1 \dots dx_{n-1}$$

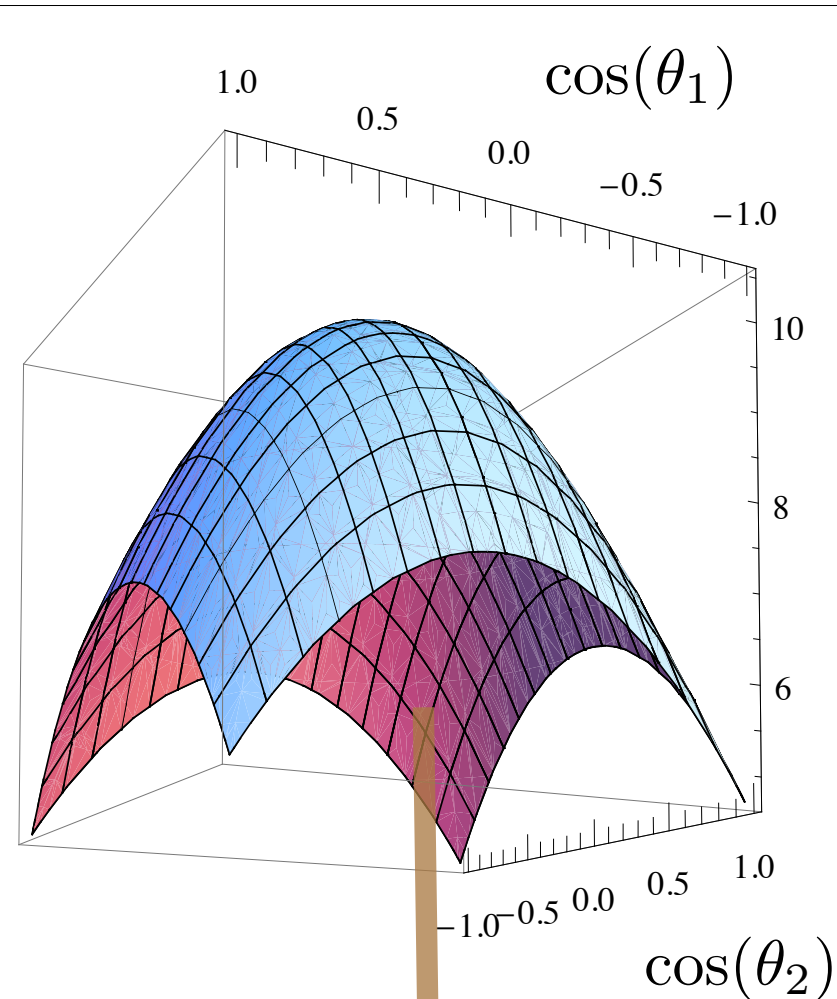
$$P(x_1, \dots, x_n) \rightarrow P(x_1) \dots P(x_n)$$







$$P[\cos(\theta_1), \cos(\theta_2)]$$



$$P[\cos(\theta_1)] * P[\cos(\theta_2)]$$

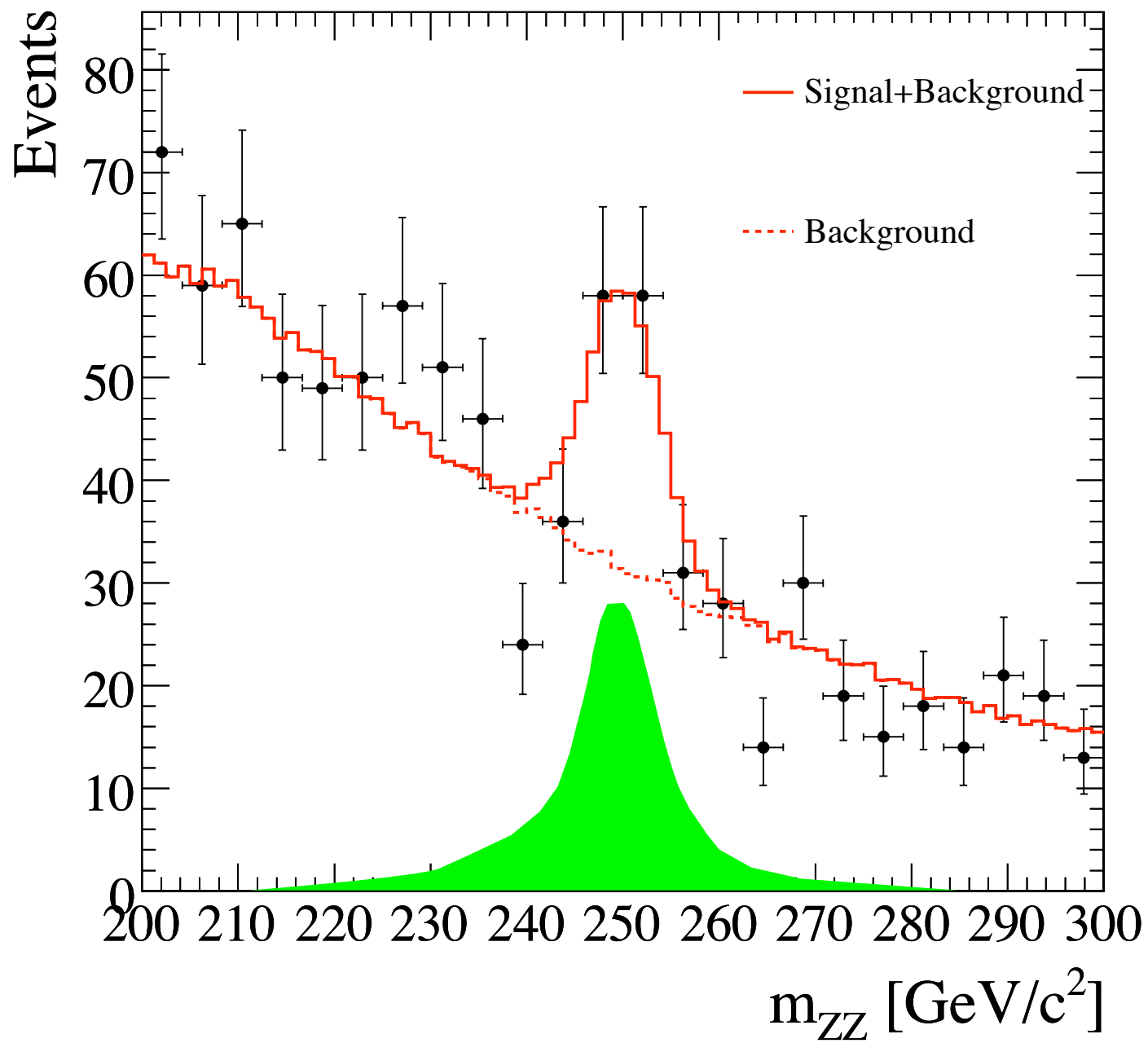
A goodness-of-fit test would eventually “disprove” the right theory



Data Analysis

and

Statistics



MC
Truth

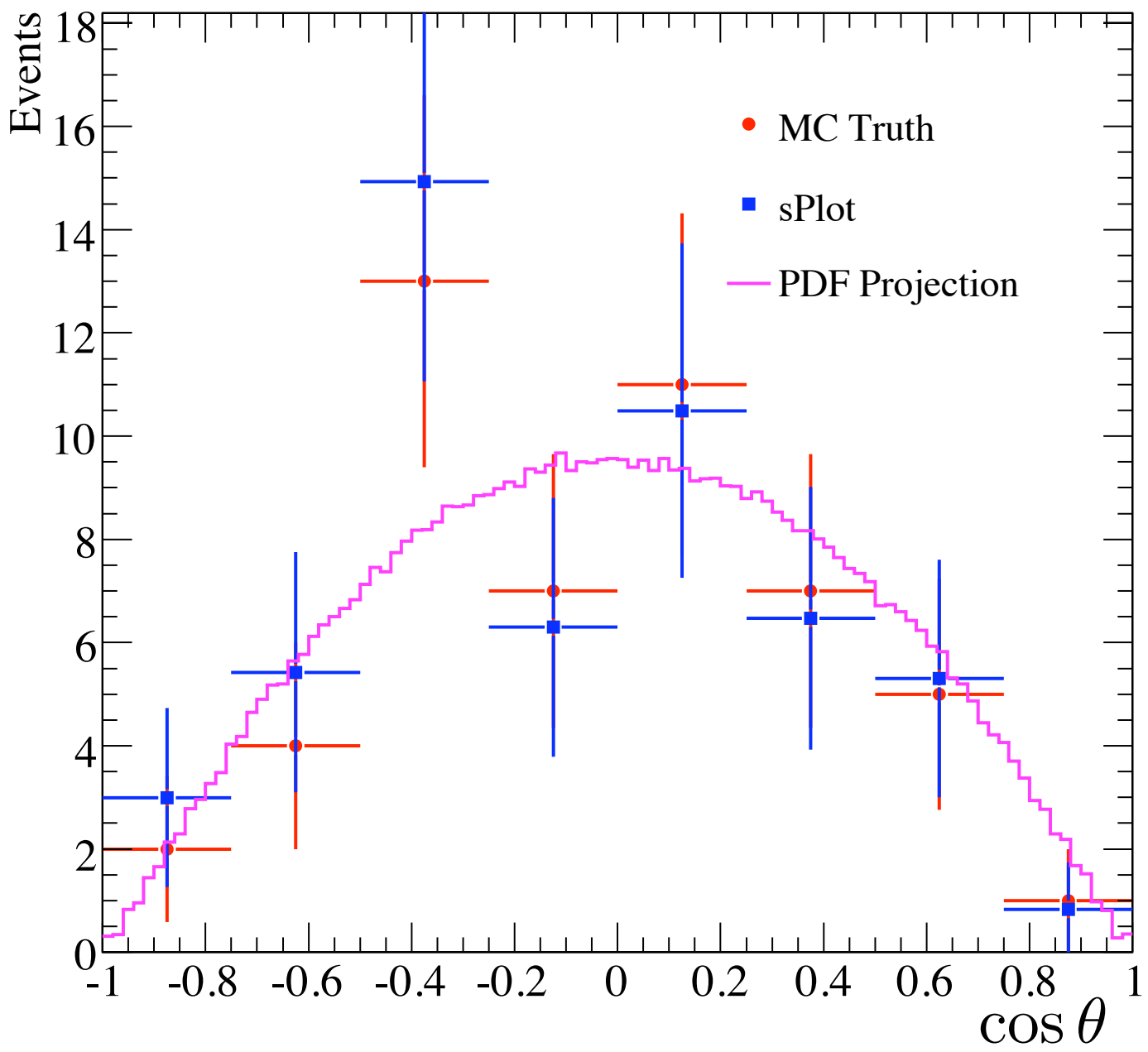
SIGNAL

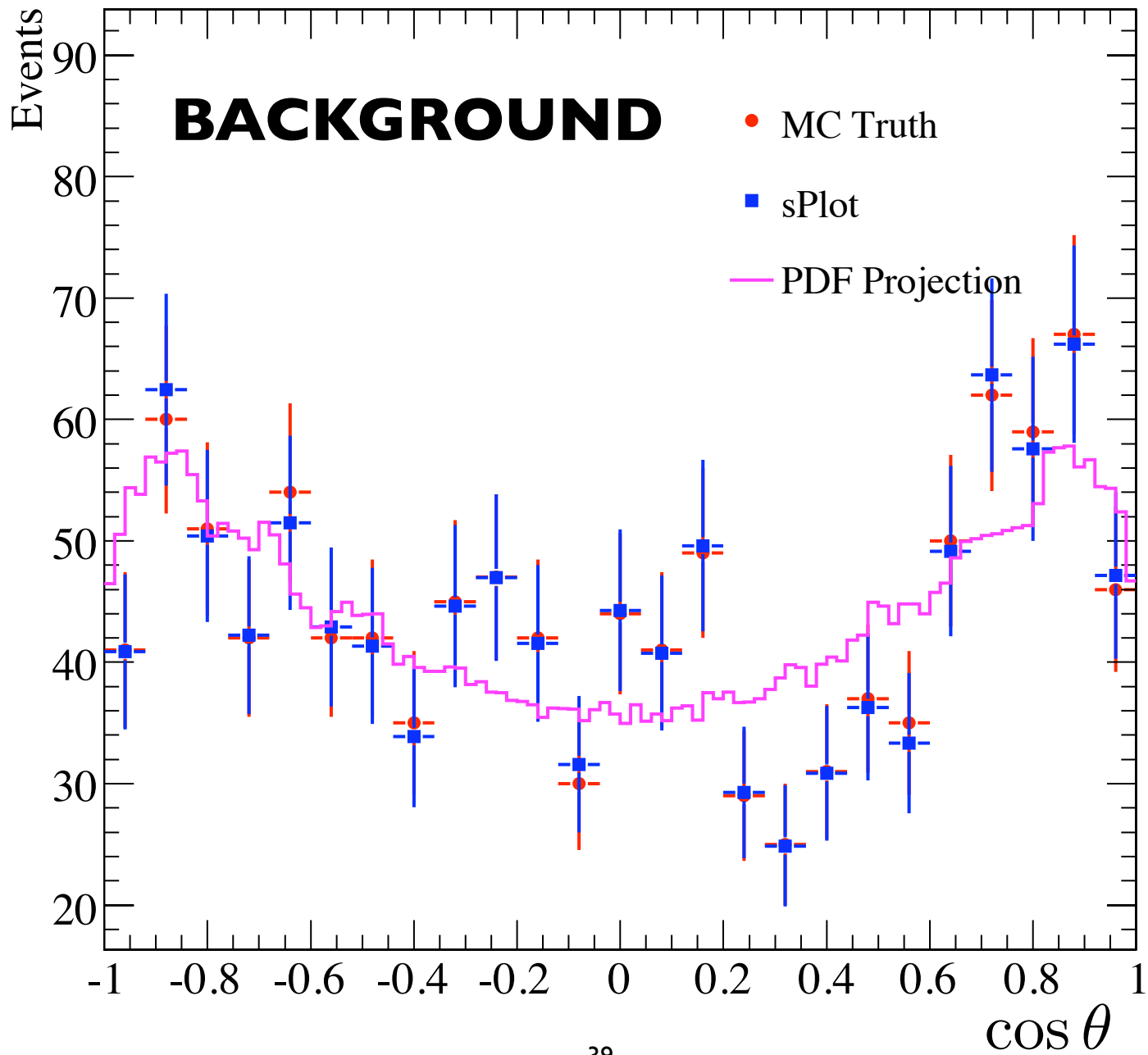
$\cos \theta =$

$\cos \theta_1$

or

$\cos \theta_2$





s-Separates signal and background

In our case with use of Maximum-Likelihood fit to the $M(ZZ)$ or $M(ZZ^)$ distribution $\Rightarrow N_s, N_b$*

To result in what we need:

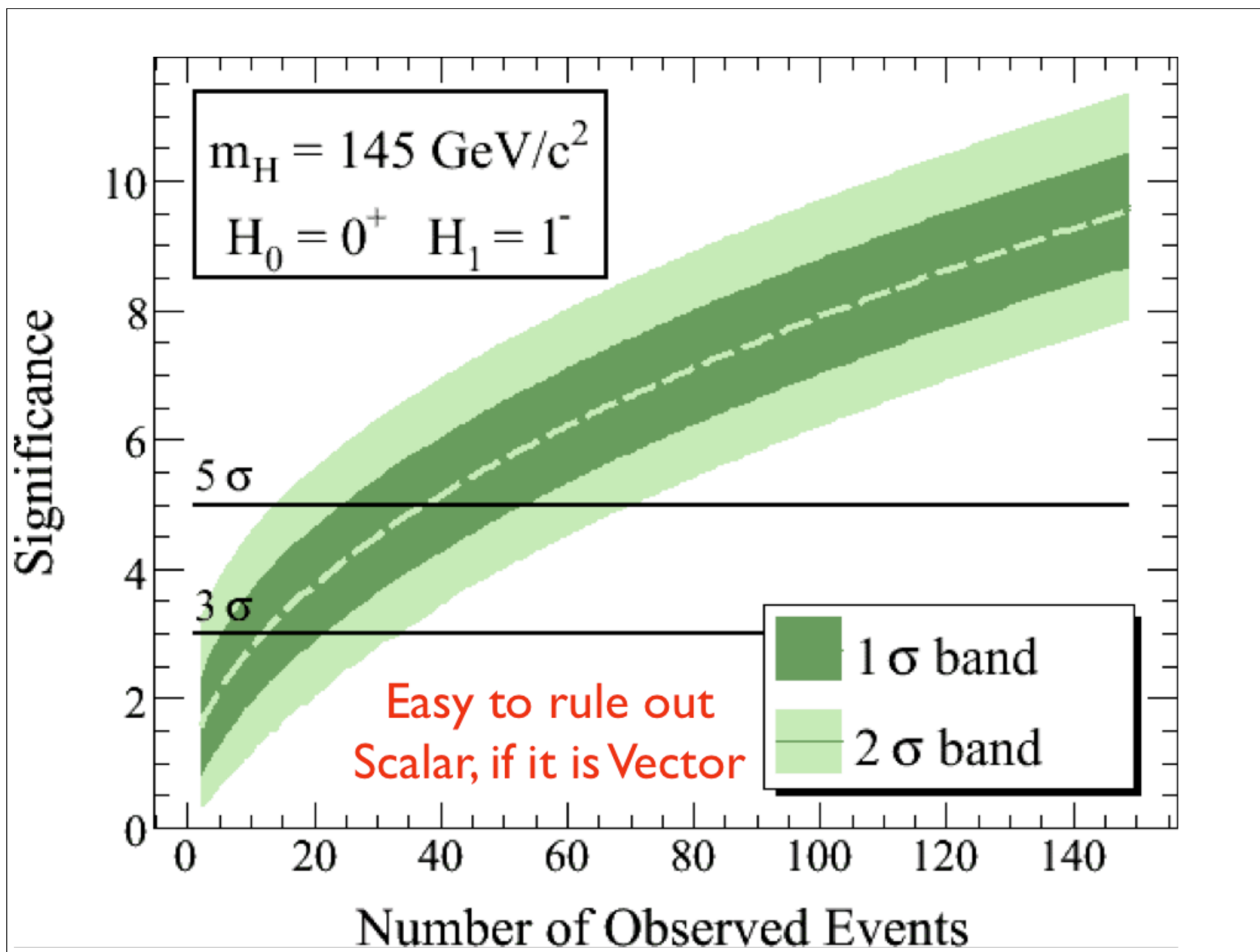
a signal-only 5-d (or 6-d) “potato”:

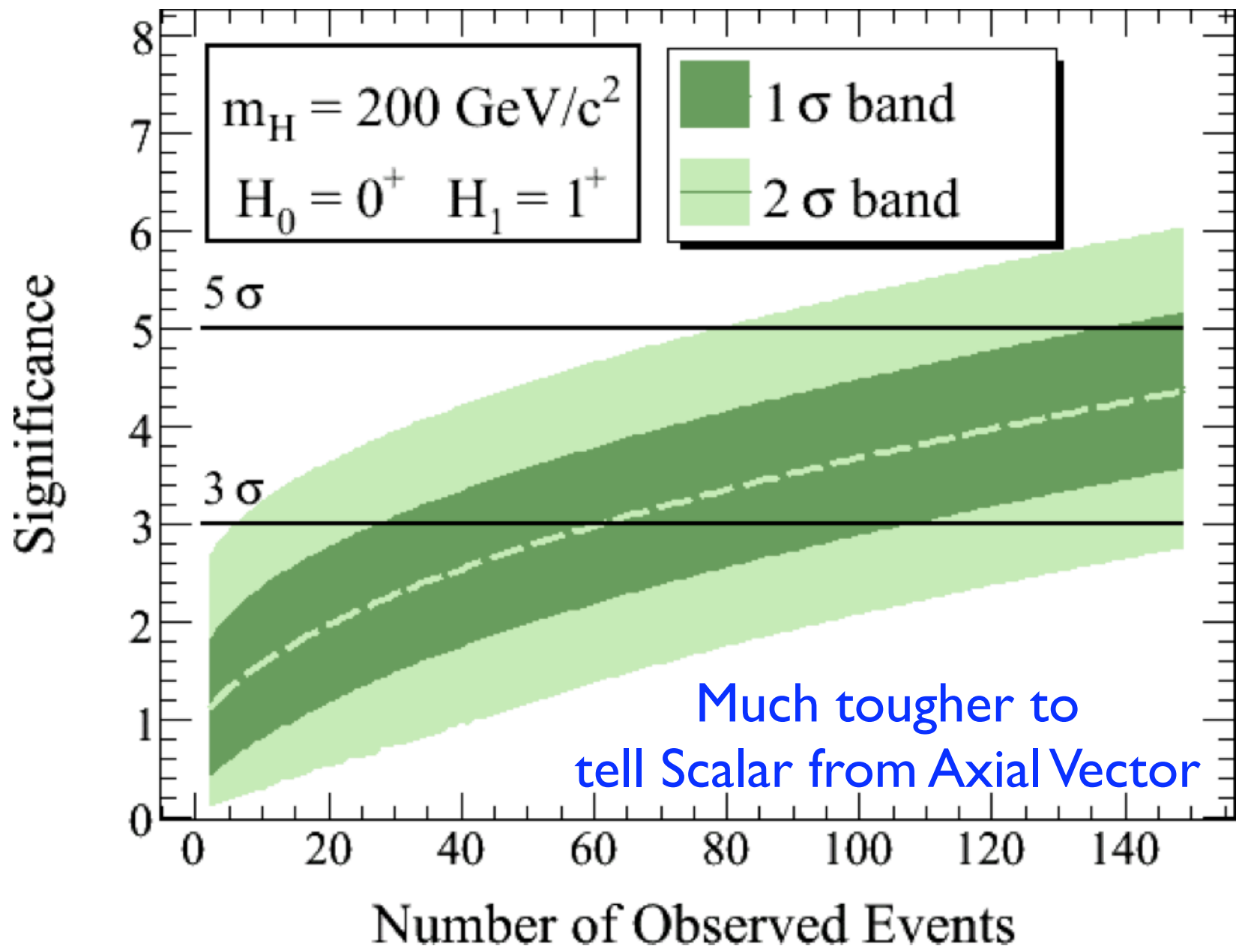
The distribution of events in all 5 angles (+ M^* in $H \Rightarrow ZZ^*$).

IDEAL FOR TESTING WHAT
THE SIGNAL IS... AND IS NOT

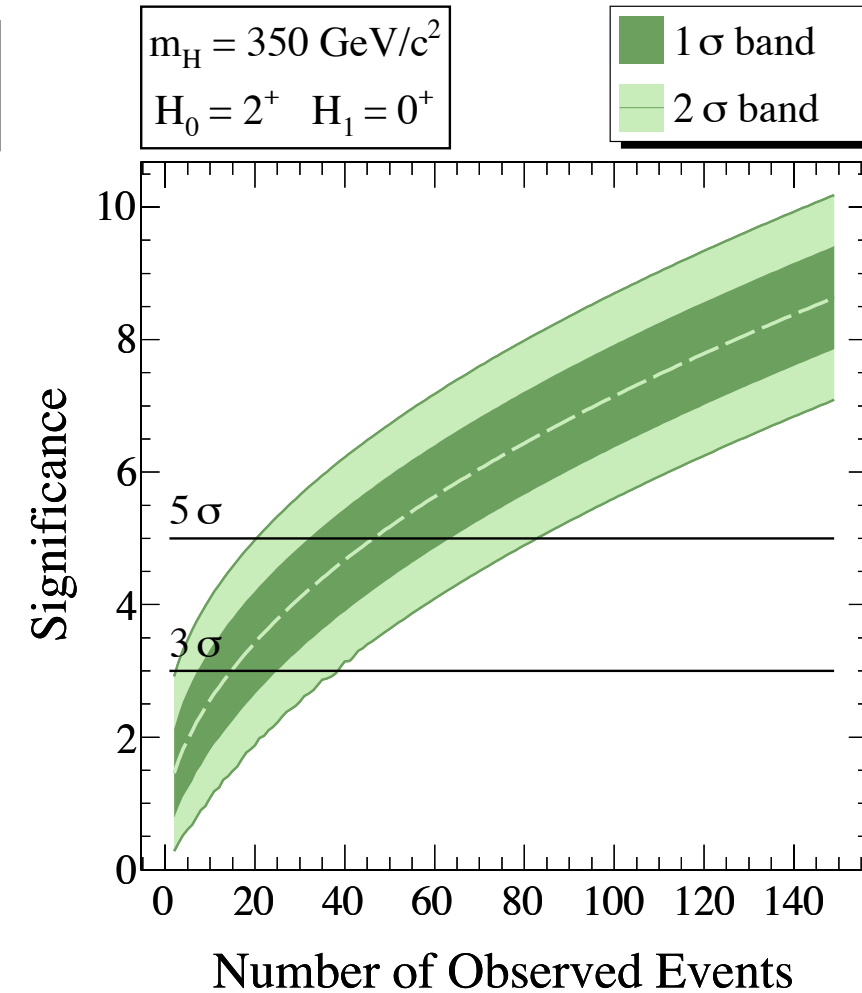
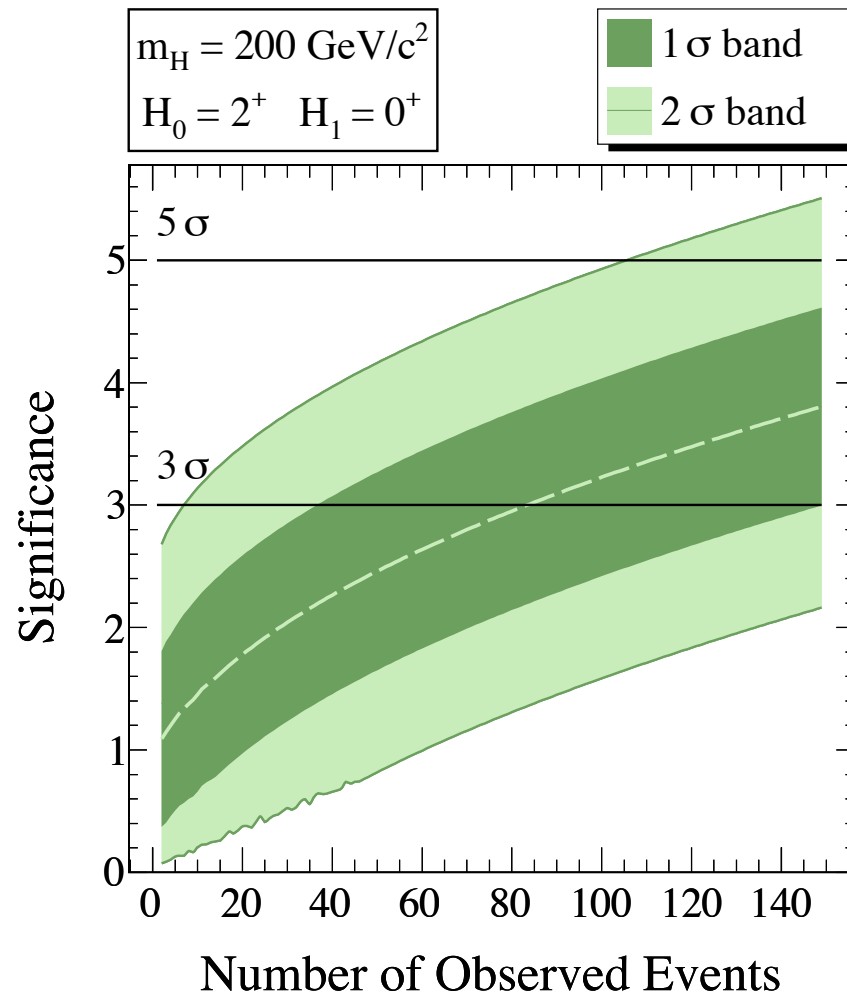
Neyman-Pearson test

No statistics schpiel
Translate into
HEP Language
Convert actual
probabilities to
Gaussian-equivalent
Standard Deviations





Higgs vs Kaluza-Klein (Heavy Graviton)



HZZ "Mixed-(P,C,T)" couplings



“Mixed” hypotheses

e.g.: Standard coupling + Opposite-parity coupling

$$\cos \xi L[0^+, ZZ] + \sin \xi L[0^-, ZZ]$$

Conventional likelihood approach, as in

$$N_S S[M(ZZ)] + N_B B[M(ZZ)]$$

Not certifiably optimal, but the alternatives are not significantly different

$\bullet \mathcal{L} - inv =$
 $X g_{\mu\nu}$ **Standard**
 $-(Y + iZ) \frac{k_\mu k_\nu}{M_Z^2}$

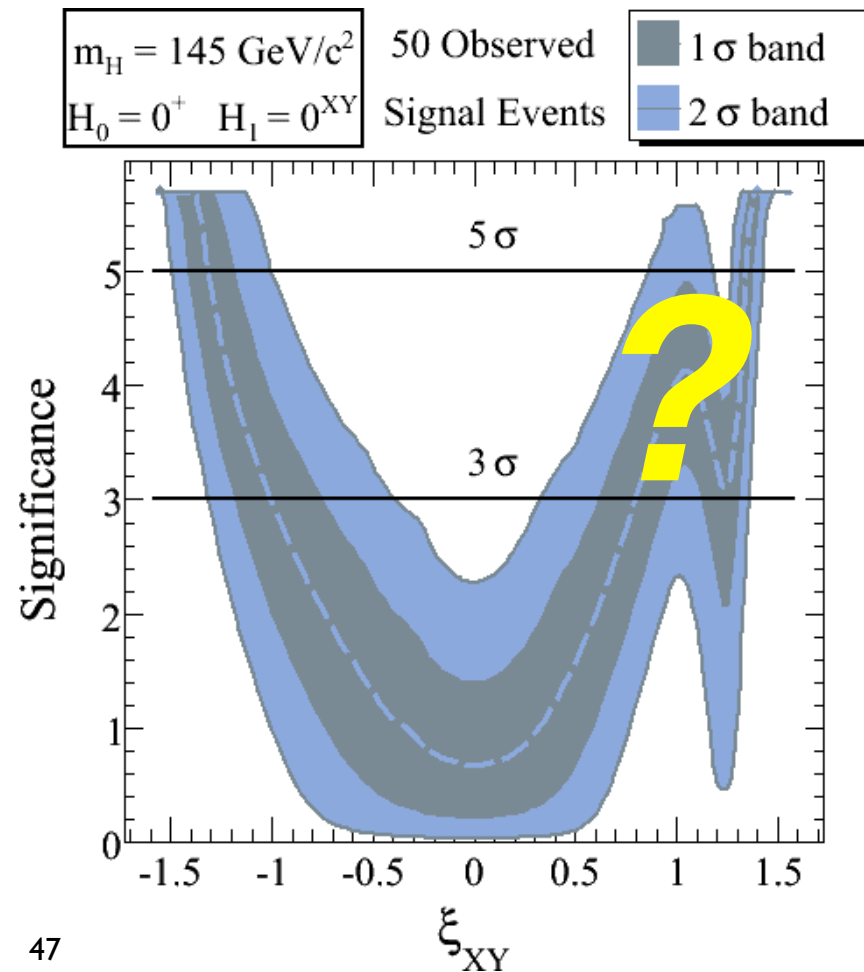
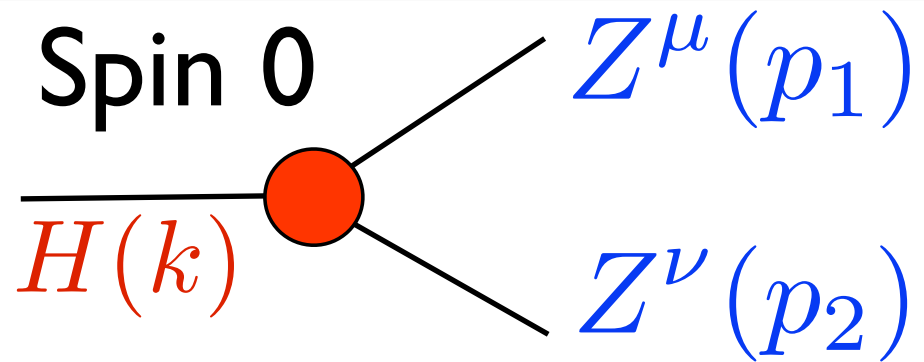
XZ: CP-odd, P-even

XY: P-even, CP-even

$\xi \equiv \arctan \frac{Y}{X}$


$R(H) \sim M^{-1} (\leftrightarrow \pi)$

e.g.: observable for some(large) values of ξ



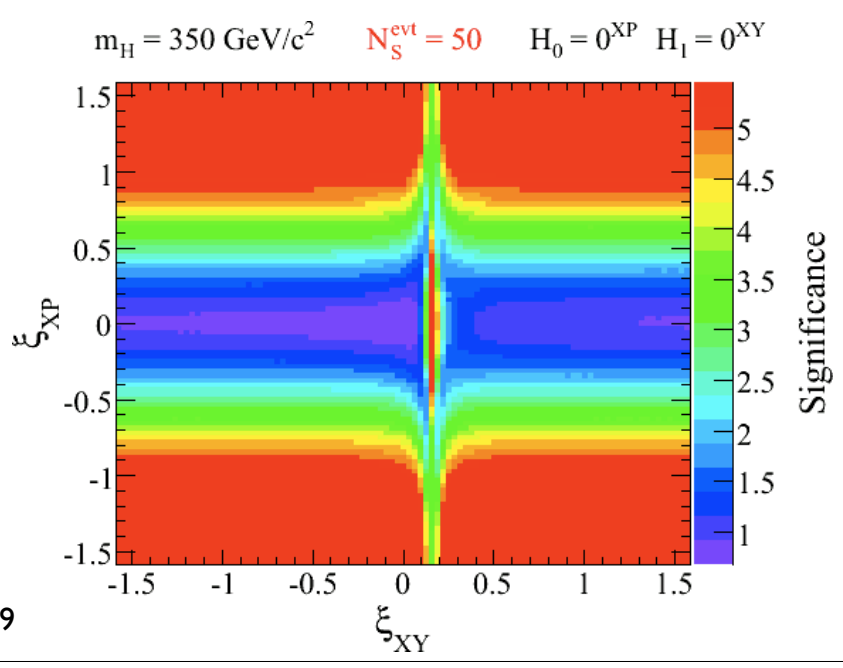
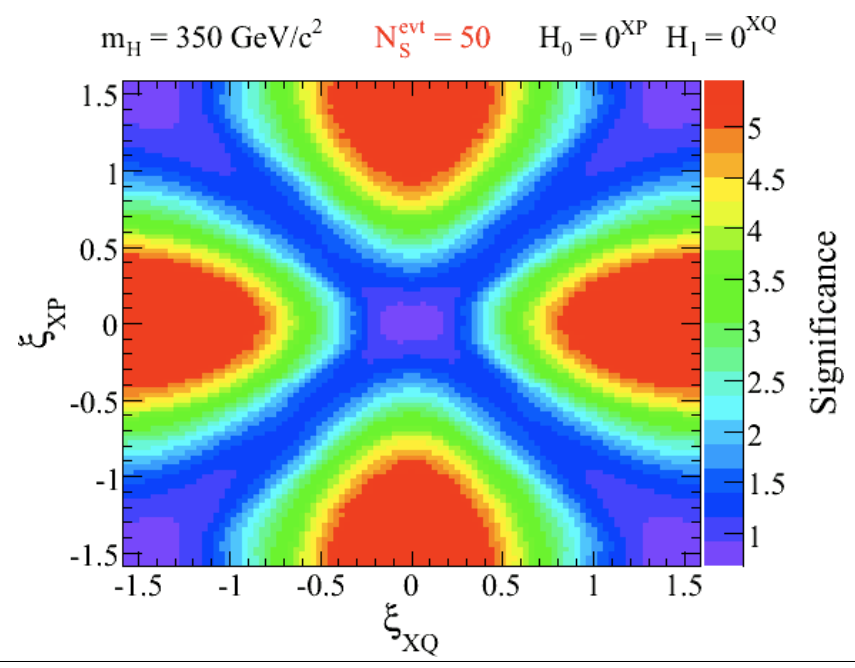
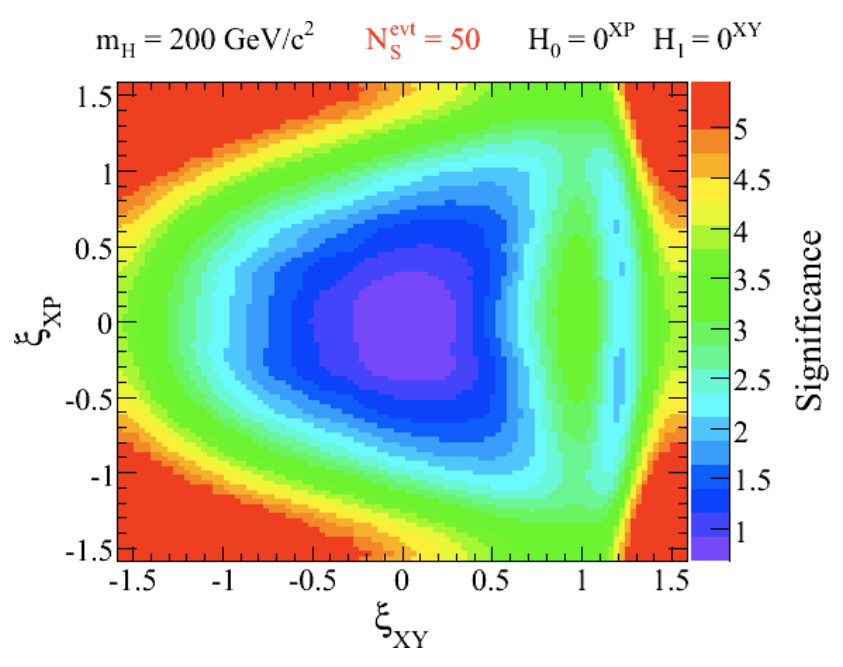
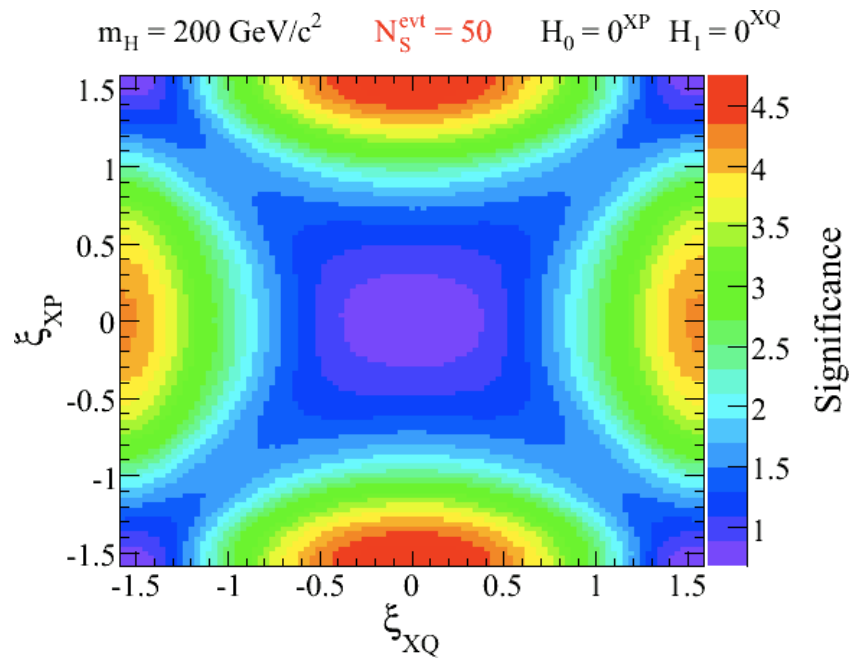


**A few examples of ...
Dozens of *[fair]* questions
and their *[careful]* answers**



**Some examples of ...
NEXT-TO-LEADING
questions and their answers**

**e.g.: The Higgs-impostor has zero spin, but is
non-standard. What is its best description ???**





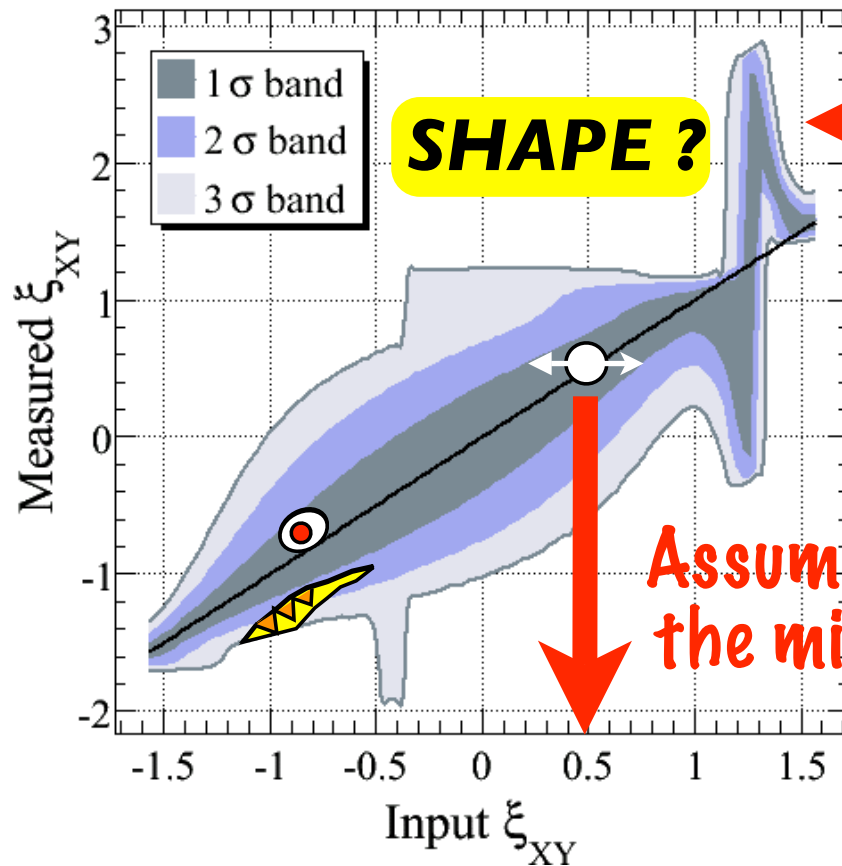
Fairly difficult to tell apart
different “mixed” $J = 0$ HIs

Fairly easy to tell apart any
(mixed) $J = 0$ HI from any
(mixed) $J = 1$ HI

NNLQ (Next to Next to Leading Questions)

e.g.: A “composite Higgs” of $M \sim 145$ GeV

50 observed signal events



1σ Measured

Assumed value of the mixing angle

A problem of
some
very large
organisations

$$\cos(\xi) g_{\mu\nu} - \sin(\xi) k_{\mu} k_{\nu} / M_Z^2$$

Two terms with the same Quantum Numbers

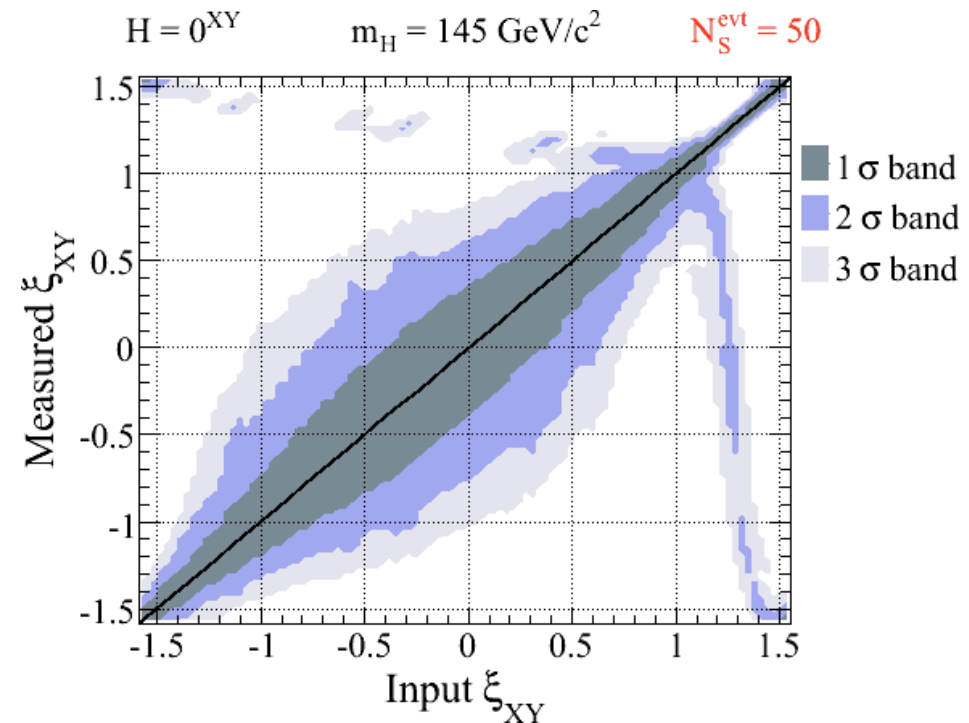
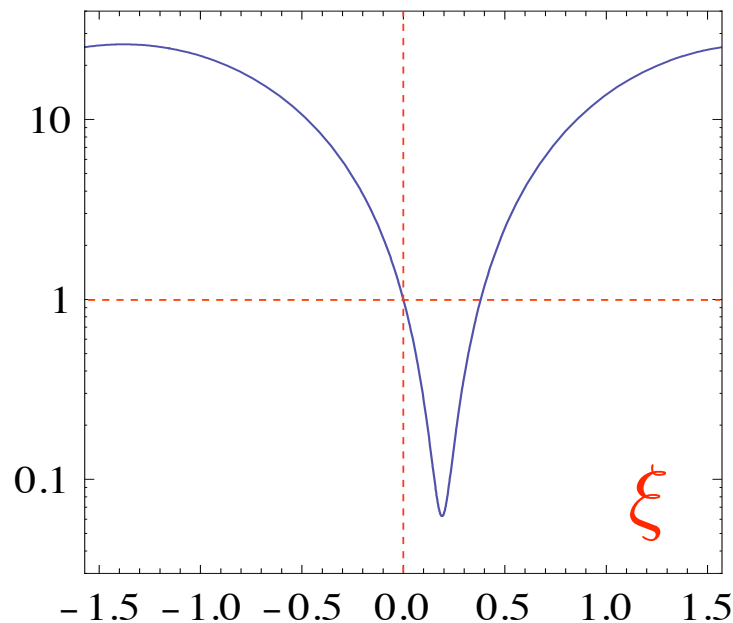


Analogous angular distributions

Very destructive interferences

Feldman-Cousins belt construction

$$\frac{|\mathbf{M}(\xi)|^2}{|\mathbf{M}(0)|^2}$$



For given

Detector performance

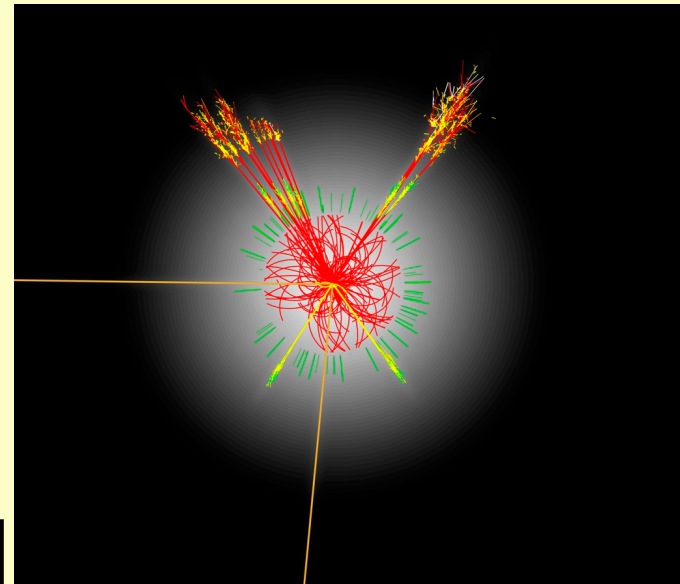
Integrated Luminosity

No extra SF

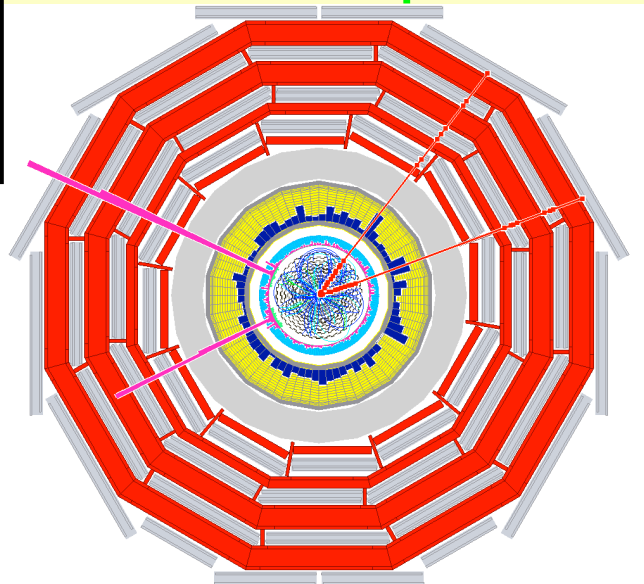
It pays to have **ab-initio (!)**
an **ANALYSIS** combining
DISCOVERY & SCRUTINY

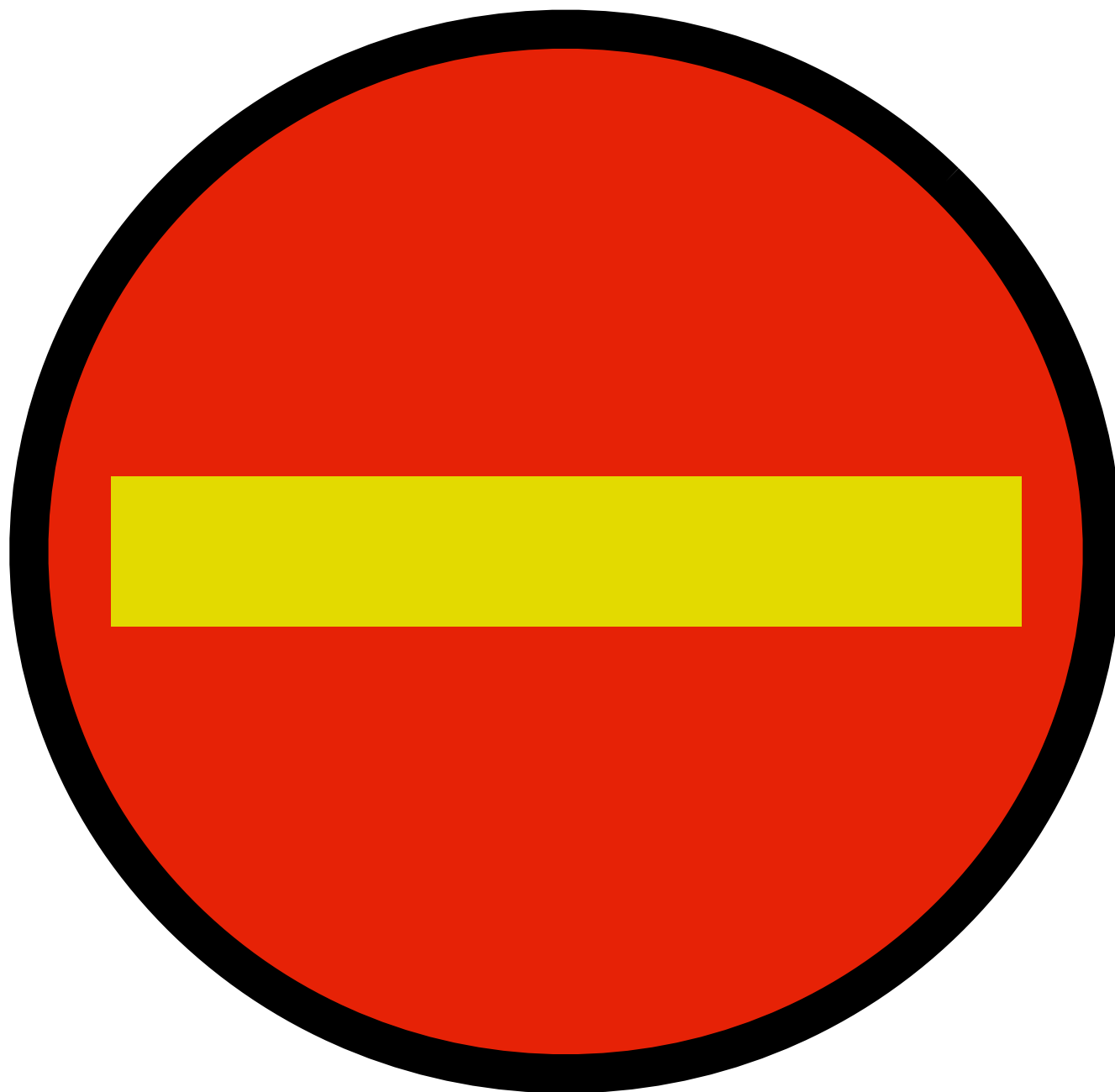
**Arguably true as well for many
other physics items, which... ..**

Readily come to mind ...



Proved by way
of example





$$\varphi_H(x)$$

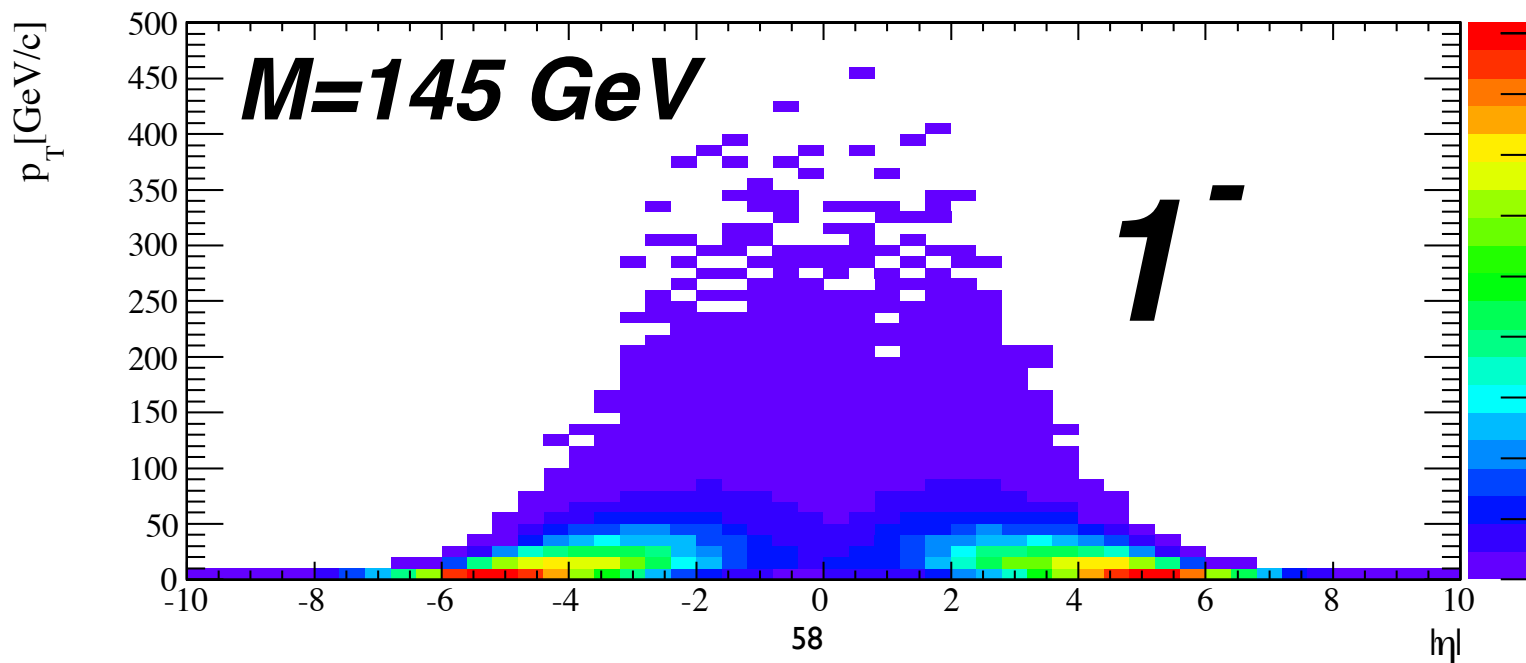
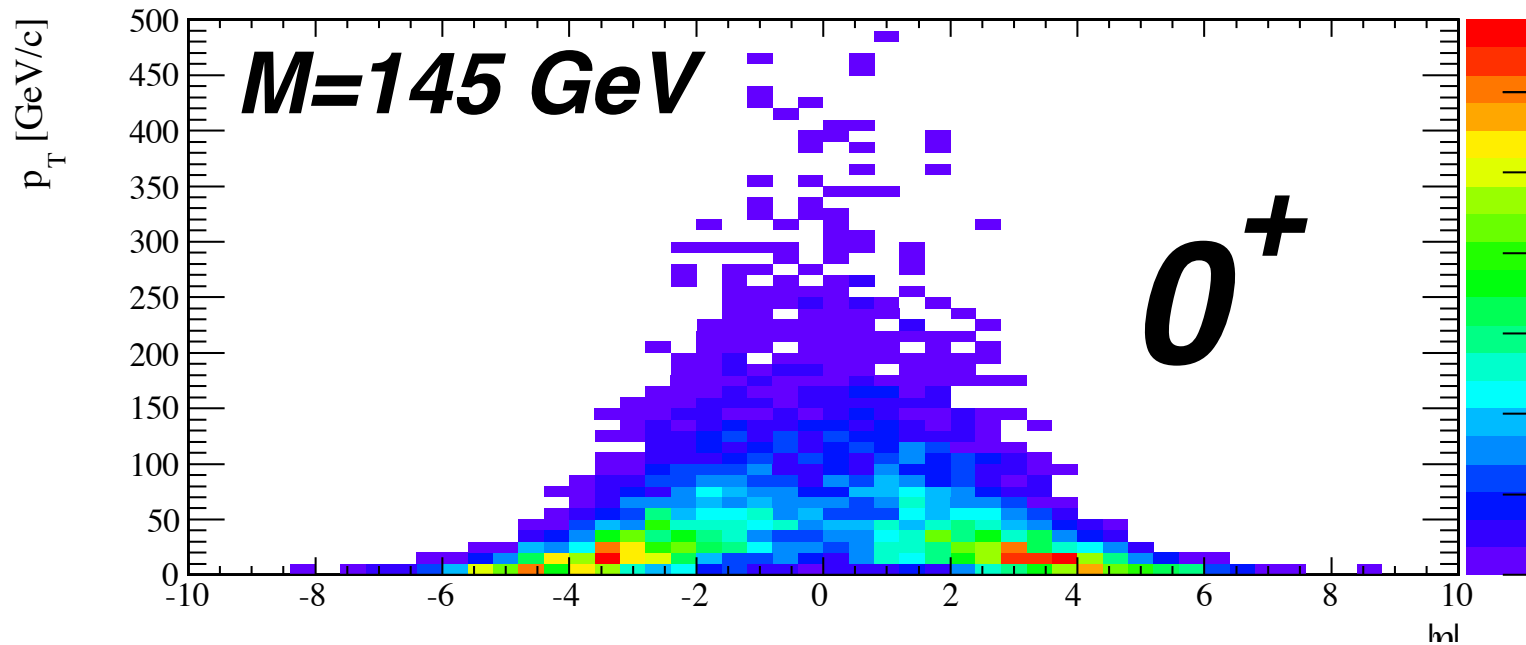
at minimum of

$$V(\varphi_H)$$

WARNING

Not a **WORD** of
what I am saying is

TRULY **NOVEL**



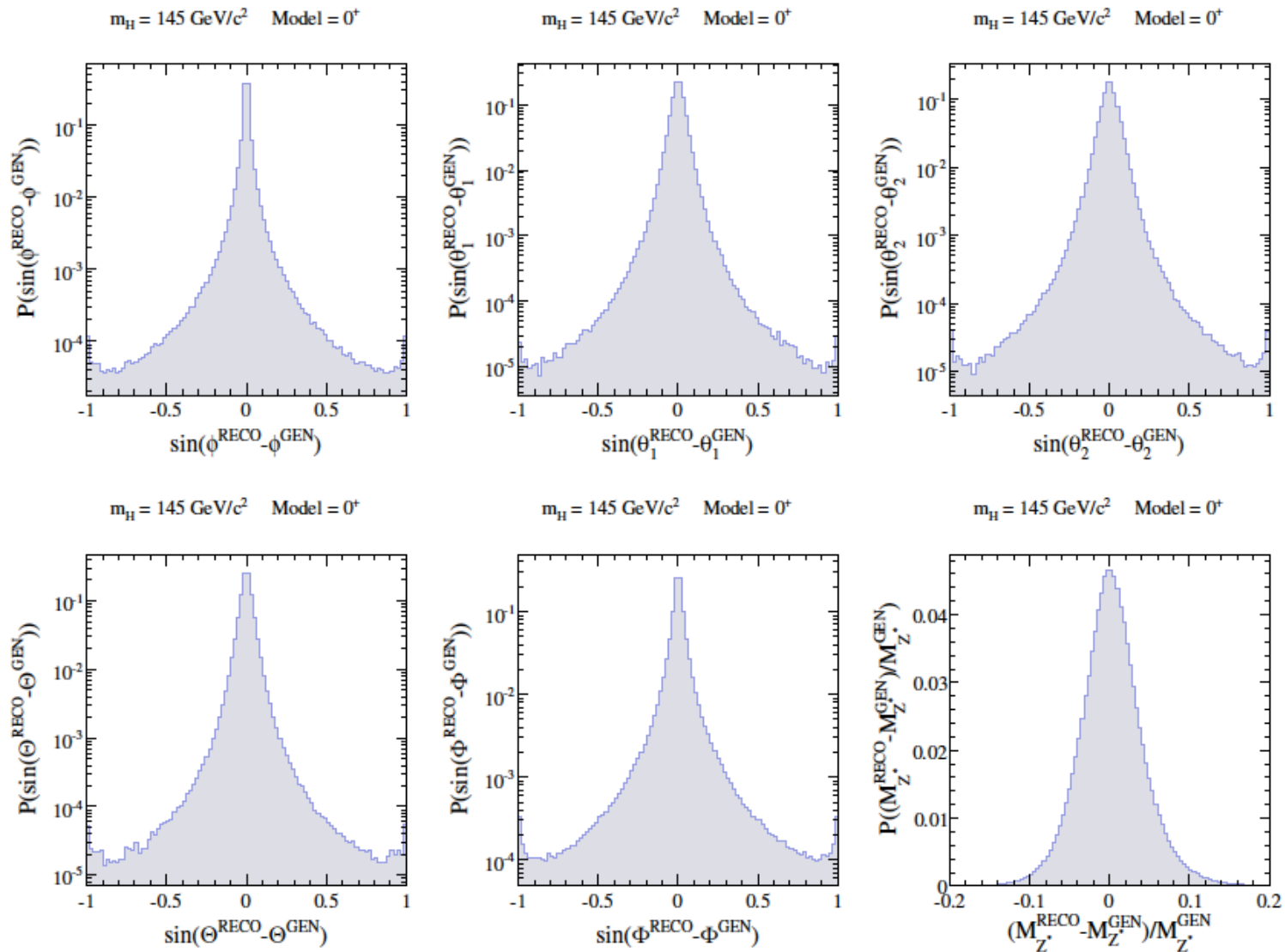


FIG. 25: Distributions indicating the reconstruction resolution for each of the variables \vec{X} for a SM Higgs with mass $145 \text{ GeV}/c^2$. Only events which pass the signal selection are included. All distributions are normalized to have an integral of 1.

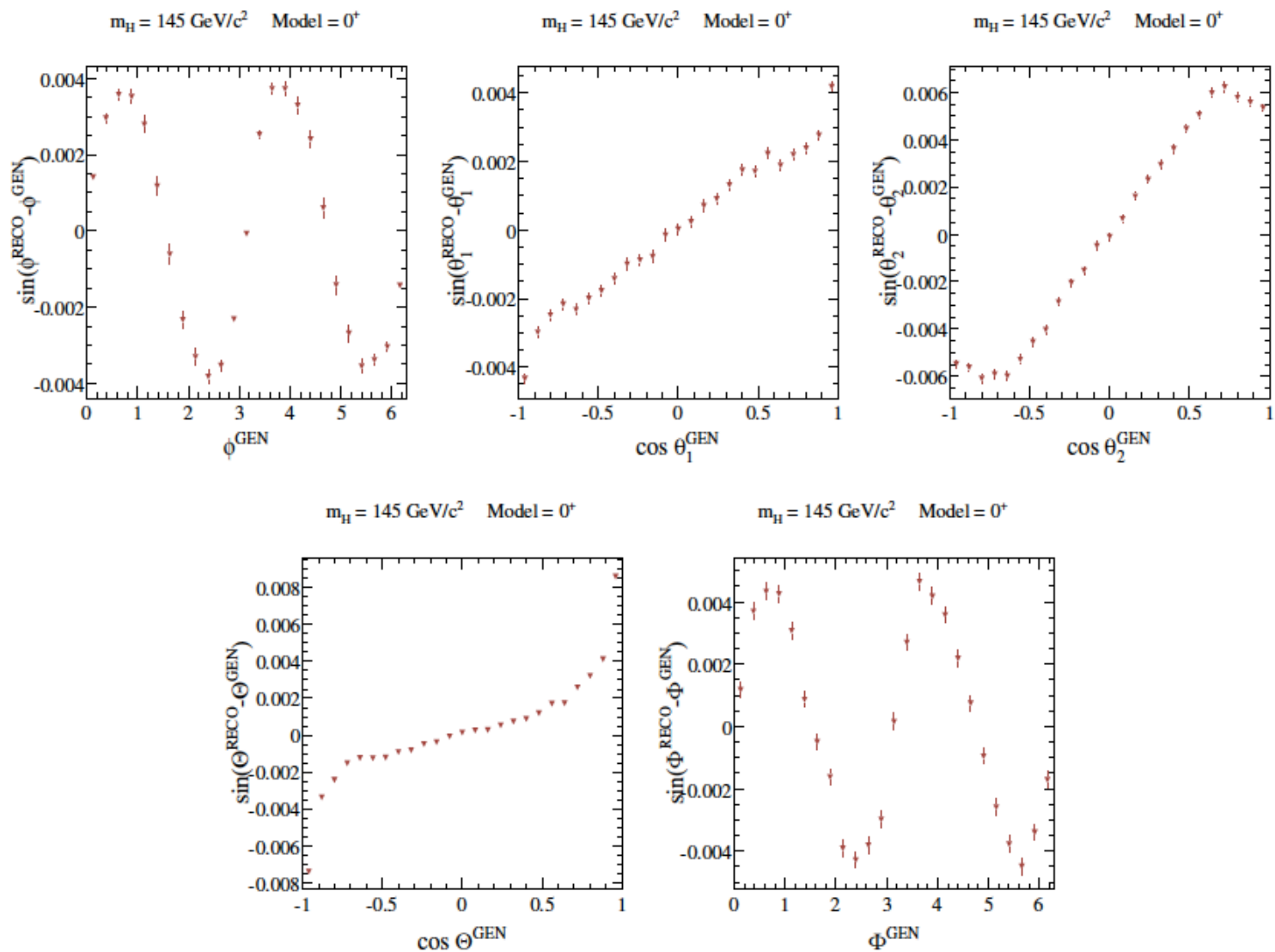


FIG. 26: Distributions showing systematic biases for reconstructed variables \vec{X} for a SM Higgs with mass $145 \text{ GeV}/c^2$. Only events which pass the signal selection are included. All biases are at negligible levels in the context of the numerical representations of the multidimensional PDFs used in this analysis.

Exp. method is not new

- (Para)-Positronium [$J^P = 0^-$] → *QM entangled*
- Helicity can be measured: Thomson scattering
- J.A. Wheeler (Ann .N.Y. Acad.Sci. 48 (1946) 219) got the theory wrong
- Sneyder, Pasternak & Hornbostel (P.R. 73 [1948] 440) and Pryce and Ward (Nat. 160 [1947] 435) got it right
- Bleuler & Bradt's experiment (P.R. 73 [1948] 1398) was not conclusive and Hanna's (Nature 162 [1948] 332) was wrong.
- C.S. Wu & Shaknov (P.R. 77 [1950] 136) did it right !!!

Hopefully history will not fully repeat

$$\bar{\eta} \equiv \frac{2c_v c_a}{c_v^2 + c_a^2} \quad Z \rightarrow l^+ l^- \quad c \equiv \cos \Theta, \quad s \equiv \sin \Theta$$

$$g_1 \equiv (c_v^2 + c_a^2)^2 (g_v^2 + g_a^2) \quad c_1 \equiv \cos \theta_1, \quad s_1 \equiv \sin \theta_1$$

$$g_{v,a} : q\bar{q} \rightarrow HI$$

$$c_2 \equiv \cos \theta_2, \quad s_2 \equiv \sin \theta_2$$

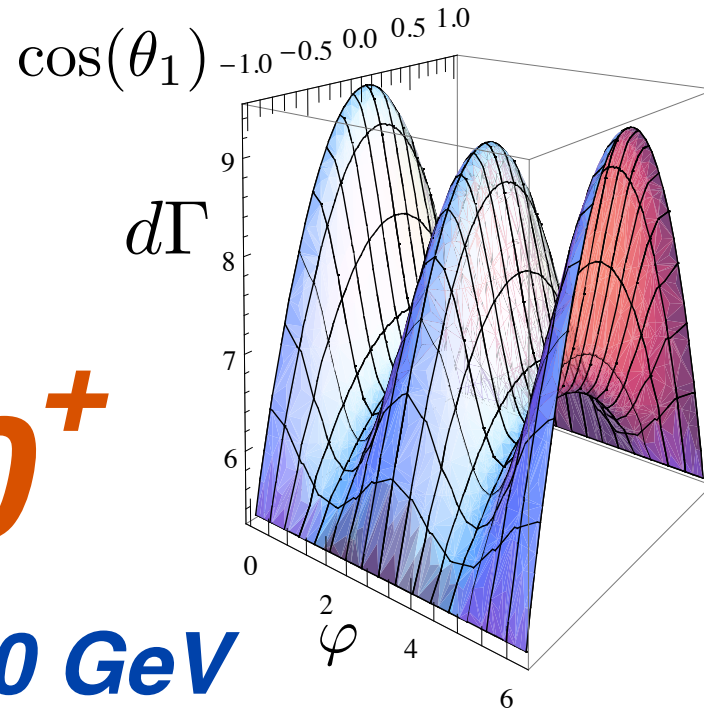
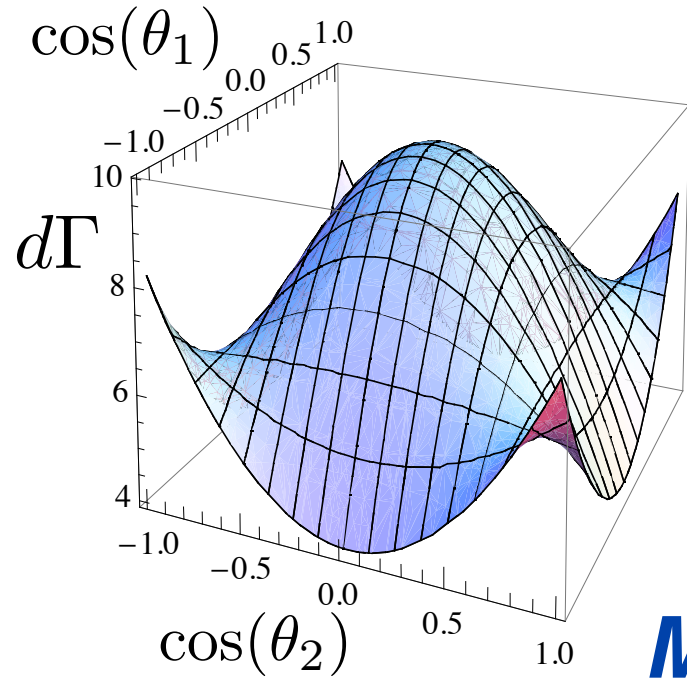
$$m_d^2 \equiv m_1^2 - m_2^2,$$

$$M_1^2 \equiv M^2 - 3m_1^2 - m_2^2, \quad M_2^2 \equiv M^2 - m_1^2 - 3m_2^2,$$

$$M_3^2 \equiv M^2 - 2(m_1^2 + m_2^2), \quad M_4^2 \equiv M^2 - (m_1^2 + m_2^2)$$

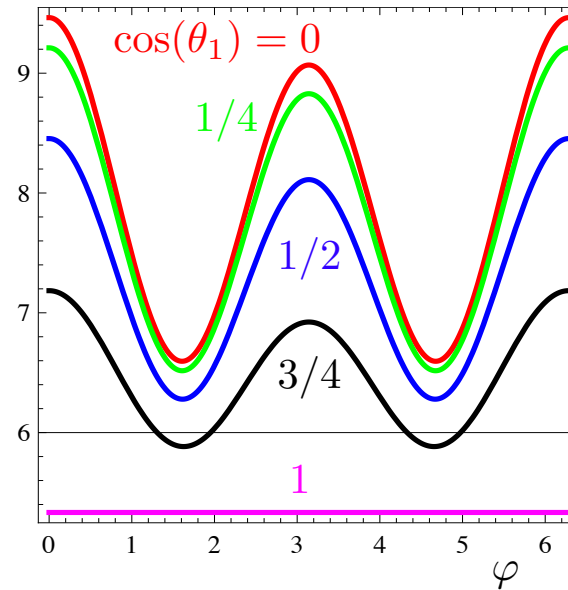
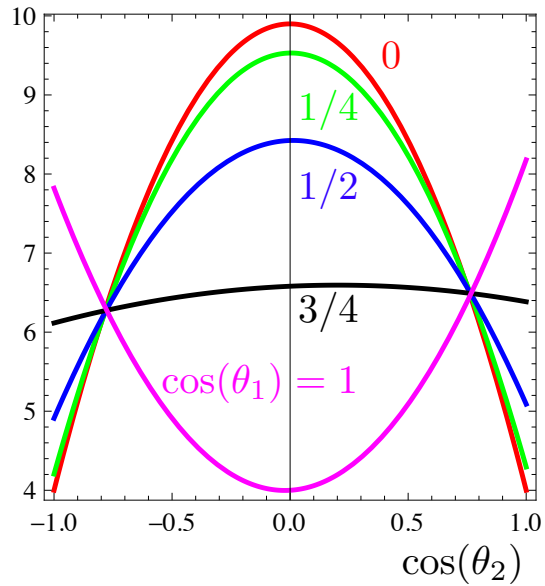
$$\frac{d\text{PDF}[\text{Pure } 1^+]}{dm^* d \cos \Theta d\Phi d \cos \theta_1 d \cos \theta_2 d\varphi} \propto PS(M, m_1, m_2 = m^*) \times$$

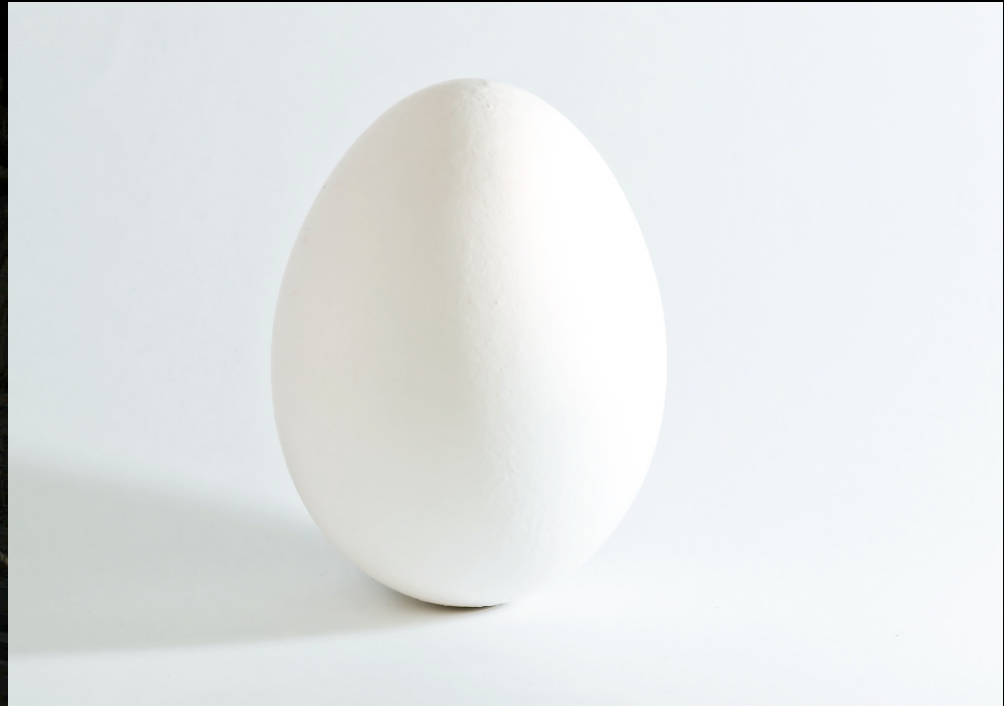
$$\begin{aligned} & P^2 g_1 \left[M^2 s^2 s_1^2 s_2^2 \left[M_2^4 m_1^2 \cos 2(\phi + \varphi) + M_1^4 m_2^2 \cos 2\phi \right] \right. \\ & \quad \left. + 8m_1^2 m_2^2 m_d^4 s^2 \left[(c_1^2 + c_2^2 + s_1^2 s_2^2 \sin^2 \varphi) + 2\bar{\eta}^2 c_1 c_2 \right] \right. \\ & \quad \left. + (1 + c^2) M^2 \left[2M_1^4 m_2^2 s_1^2 + 2M_2^4 m_1^2 s_2^2 - (M_2^4 m_1^2 + M_1^4 m_2^2) s_1^2 s_2^2 \right] \right. \\ & \quad \left. - 8M m_d^2 m_1 m_2 c s \left[M_2^2 m_1 s_2 (c_2 s_1^2 \sin(\phi + \varphi) \cos \varphi + c_1 (c_1 c_2 + \bar{\eta}^2) \sin \phi) \right. \right. \\ & \quad \left. \left. - M_1^2 m_2 s_1 (c_1 s_2^2 \sin \phi \cos \varphi + c_2 (c_1 c_2 + \bar{\eta}^2) \sin(\phi + \varphi)) \right] \right. \\ & \quad \left. + 2M^2 M_1^2 M_2^2 m_1 m_2 s_1 s_2 \left[(1 + c^2) (c_1 c_2 - \bar{\eta}^2) \cos \varphi - s^2 (c_1 c_2 + \bar{\eta}^2) \cos \varphi + 2\phi \right] \right] \end{aligned}$$



0^+

$M=200 \text{ GeV}$





$$F(x, y, z) = 0$$



$$z = P(x, y)$$



$$z = P(x) * P(y)$$

● $\mathcal{L}\text{-inv} =$

$X g_{\mu\nu}$ **Standard**

$$+(P + iQ)\epsilon_{\mu\nu\alpha\beta} \frac{p_1^\alpha p_2^\beta}{M_Z^2}$$

Pseudoscalar

$$-(Y + iZ) \frac{k_\mu k_\nu}{M_Z^2}$$

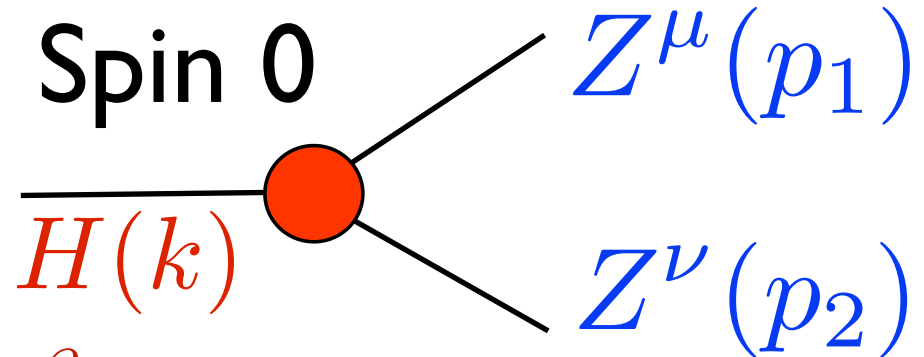
Derivative (Composite)

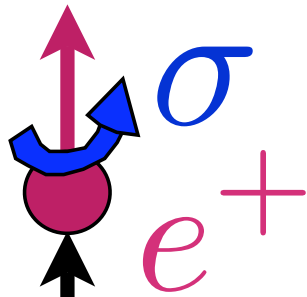
Some
Inteferences

XP is T-odd

XQ is C-odd

XY is C,CP-even





$$\text{Polarisation} = \frac{v}{c} \simeq 100\%$$

$$e^+ \leftrightarrow e_R^+$$

Demonstrated maximal parity violation in a purely leptonic decay

p

$$\mathcal{O}_P \equiv \vec{\sigma} \cdot \vec{p} \quad \text{P-odd}$$

$$\mathcal{O}_P \rightarrow -\mathcal{O}_P \quad \{ \vec{x} \rightarrow -\vec{x} \}$$

$$\langle \mathcal{O}_P \rangle \neq 0 \iff (\Gamma \propto A + B \mathcal{O}_P)$$



EXP: J. Duclos, J. Heintze, V. Soergel, ADR; Phys. Lett. 9, 62 (1964).

$$\mathcal{O}_T \equiv \vec{p}_{e^+} \cdot \vec{p}_{\mu^+} \times \vec{p}_{\mu^-} \propto \sin \theta_1 \sin \theta_2 \sin \varphi$$

$\mathcal{O}_T \rightarrow -\mathcal{O}_T \{t \rightarrow -t\}$ T-odd (& P-odd)

$\langle \mathcal{O}_T \rangle \neq 0$ You HAVE NOT proven
that T (\Leftrightarrow CP) is violated

At the LHC $H \Rightarrow$ ZZ statistics will
be In-Sufficient: You HAVE

Literature often wrong.

e.g. \mathcal{O}_T is T-even, C-odd

$$S \rightarrow S_{fi} \quad |S|^2 = 1 \quad S \equiv 1 + iT$$

$$T - T^\dagger = iT T^\dagger \equiv i\mathcal{A} \quad \sum_{\Gamma} |\Gamma\rangle\langle\Gamma| = 1$$

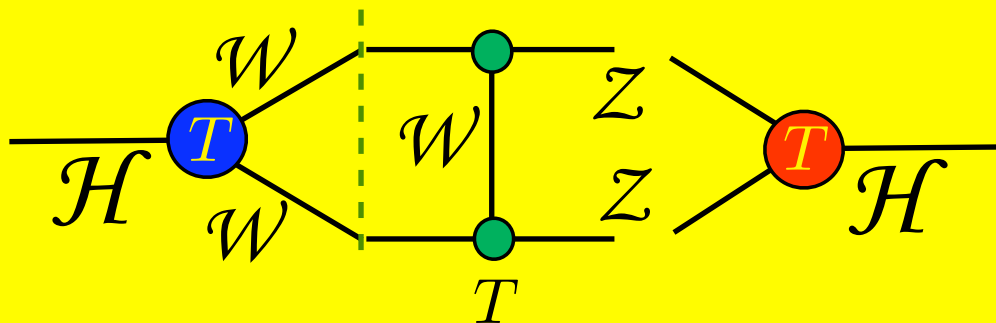
$$T_{fi} - T_{if}^* = i\mathcal{A}_{fi} \equiv \sum_{\Gamma} T_{f\Gamma} T_{i\Gamma}^*$$

$$|T_{fi}|^2 = |T_{if}|^2 + 2\text{Im}(\mathcal{A}T^*) - |\mathcal{A}|^2$$

Assume T (or CP) -inv $\sim: \{\vec{p} \rightarrow -\vec{p}, \vec{\sigma} \rightarrow -\vec{\sigma}\}$

$$|T_{fi}|^2 - |T_{\tilde{f}\tilde{i}}|^2 = \mathcal{O}(T^3) + \mathcal{O}(T^4)$$

\mathcal{O}_T



$$S \rightarrow S_{fi} \quad |S|^2 = 1 \quad S \equiv 1 + iT$$

$$T - T^\dagger = iT T^\dagger \equiv i\mathcal{A} \quad \sum_{\Gamma} |\Gamma\rangle\langle\Gamma| = 1$$

$$T_{fi} - T_{if}^* = i\mathcal{A}_{fi} \equiv \sum_{\Gamma} T_{f\Gamma} T_{i\Gamma}^*$$

$$|T_{fi}|^2 = |T_{if}|^2 + 2\text{Im}(\mathcal{A}T^*) - |\mathcal{A}|^2$$

Assume T (or CP) -inv $\sim: \{\vec{p} \rightarrow -\vec{p}, \vec{\sigma} \rightarrow -\vec{\sigma}\}$

$$|T_{fi}|^2 - |T_{\tilde{f}\tilde{i}}|^2 = \cancel{\mathcal{O}(T^3)} + \cancel{\mathcal{O}(T^4)}$$



$$\mathcal{O}_T \neq 0 \rightarrow$$

~~CP~~

sWeights and sPlots

P. E. Condon & P. L. Cowell, Phys. Rev. D 9 (1974) 2558

F.R. Le Diberder and M. Pivk, BABAR collab.

I can't believe it

Boy! t'is true !!!

So simple and obvious
Why didn't I think of it long
ago?

STATISTICALLY OPTIMAL FOR A NARROW $M(ZZ)$
and, WITH A BIT MORE EFFORT, FOR A WIDE ONE

$\bullet \mathcal{L}\text{-inv} =$
 $X g_{\mu\nu}$ **Standard**

$+(P + iQ)\epsilon_{\mu\nu\alpha\beta} \frac{p_1^\alpha p_2^\beta}{M_Z^2}$

Pseudoscalar

50 observed signal events

XP: CP-odd, P-even

XQ: P-odd, CP-even

$\xi \equiv \arctan \frac{Q}{X}$

Only large mixings may be disfavoured/Standard

